



A Comparison of Radiometric Calibration Techniques for Lunar Impact

Rob Suggs, Ph.D. 105 Steve Ehlert, Ph.D.

NASA Marshall Space Flight Center Engineering Directorate/EV44 and Meteoroid Environment Office

Outline



- The Problem
- Photometric Calibration and Energy Calculation – Various Approaches
- Results of our approach
 - Crater "ground-truth"
 - Meteoroid Flux
- Suggested Refinements

The Problem



- Observations are made with unfiltered cameras to provide maximum sensitivity
- Magnitudes and luminous energies are available for standard stars only in filter passbands
- Determining the energy of the lunar impact flashes requires knowledge of the spectral distribution (color or temperature) of the standards and the impact flash

Magnitude determined by observing catalog stars $R = -2.5 \log_{10}(S) - k' X + T (B-V) + ZP$ $E_{lum} = f_{\lambda} \Delta \lambda f \pi d^2 t$ Joules Where $f_{\lambda} = 10^{-7} \times 10^{-(R+21.1+zp_R)/2.5}$ J cm⁻² s⁻¹ Å⁻¹ from Bessell et al. 1998

Suggs et al. 2014 and Rembold and Ryan 2015 use these expressions

Other researchers use variations of this

Sony HAD EX (Watec camera) response compared to Johnson-Cousins filters



NASA/MSFC/EV44/R.Suggs, S. Ehlert

Camera and Filter Responses with Sun, Vega, and Flash Blackbody



NASA/MSFC/EV44/R.Suggs, S. Ehlert

Effect of Ignoring Colors of Comparison Stars



Correction from HAD EX to R filter vs blackbody temperature R-EX replaces T(B-V)



Comparison of Various Methods



Ortiz published energy at earth for 9.3 magnitude. We multiplied by dist² and f=3 Yanagisawa is energy published for 9.4 magnitude flash Suggs and Rembold calibrated to R magnitudes, others are V magnitudes

Ground Truth – Suggs et al. 2014 March 17, 2013 Flash and Crater







17 Mar 2013 03:50:54.312 1.03 s $m_R = 3.0$ (saturation corrected) Virginid



Crater info

- Rim-to-rim diameter = 18 m
- Inner diameter = 15 m
- Depth ≈ 5 m

NASA/MSFC/EV44/R.Suggs, S. Ehlert

Transient crater diameter estimates



Assumptions: Virginid v_{gfoc}=25.7 km/s, θ_h = 56°; ρ_t = 1500 kg/m³ (regolith)

| Model | Lum eff. ղ | КЕ ×10 ⁹ (J) | Mass (kg) | $ ho_{p}$ (kg/m³) | D _{calc} (m) | D _{obs} (m) | % Err |
|---|---|----------------------------|---------------|-------------------|--------------------------|-------------------------|-------|
| Gault's crater scaling law (Gault 1974) | $5{	imes}10^{-4}$ (Bouley et al. 2012) | 14 [9.4,22] | 42 [28,66] | 1800 | 18.5 [16.5,21.1] | 15 | 23% |
| | | | | 3000 | 20.2 [18.0,23.0] | 15 | 35% |
| | 1.3 ×10 ⁻³ (Moser et al. 2011) | 5.4 [3.6,8.4] | 16 [11,26] | 1800 | 14.1 [12.5,16.0] | 15 | 6% |
| | | | | 3000 | 15.3 [13.6,17.4] | 15 | 2% |
| Holsapple's online calculator (Holsapple 1993) | 5×10 ⁻⁴ | 14 [9.4,22] | 42 [28,66] | 1800 | 12.2 [10.9,13.8] | 15 | 19% |
| | | | | 3000 | 12.5 [11.1,14.2] | 15 | 17% |
| | 1.3×10 ⁻³ | 5.4 [3.6,8.4] | 16 [11,26] | 1800 | 9.3 [8.3,10.5] | 15 | 38% |
| | | | | 3000 | 9.5 [8.5,10.8] | 15 | 37% |

Two example values of η from the literature yield large ranges for KE and mass. Consequently, model results are highly dependent on luminous efficiency η .

Assuming a velocity dependent $\eta = 1.3 \times 10^{-3}$, these model results are consistent with the observed crater diameters.

 $D_{calc} = 8-18$ m transient crater $D_{calc} = 10-23$ m rim-to-rim $D_{obs} = 15$ m inner ('transient') $D_{obs} = 18$ m rim-to-rim

Other Considerations (1) Peak vs Time-Integrated Flash Energy

- Flashes can last for several video frames
- We use peak flash (1/60 sec video field) to avoid contaminating the energy calculation with regolith property and droplet cooling rates
 - Yanagisawa et al. 2002 and Bouley et al. 2012
 discuss light curve physics extensively

Other Considerations (2) Standard Photometric Calibration



- Flat fielding is important especially when focal reducers are used to increase field-of-view
 - Vingetting near the field edges can significantly affect magnitude measurements
- Dark signal is not significant at video exposure times
- Standard extinction corrections are necessary
 - Flash observations may be at higher airmasses than would ordinarily be used for astronomical photometry
- Atmospheric scintillation must be considered as an error source at video exposure times
- Non-linear camera response (gamma) must be corrected when used
 - Provides better dynamic range at low end of sensitivity
- Saturation correction may be necessary for brightest flashes



- Record flashes in standard filter passbands
 - V, R, I for example
 - Downside is reduced sensitivity, need larger aperture
- For existing unfiltered data use an approach similar to Ehlert 2016
 - Use a catalog of stellar spectra to define a CCD "filter" response
 - Downside spectral energy distribution of comparison star must be well-known
- Investigate use of Gaia spacecraft catalog (Jordi et al.), similar bandpass to HAD EX cameras
- Always designate luminous efficiency bandpass
 - $-\eta_{R}, \eta_{I}, \eta_{CCD}, etc.$

Summary



- Early lunar impact observers made approximations in photometric calibration which led to biases in energy estimations
 - Passband too wide
 - Assumed flash spectral distribution uniform across entire passband
- More accurate energy estimates can be made using color corrections between standard filters and camera response
 - Assume flash temperature/color
 - Account for colors of comparison stars
- Camera-defined "filter" can be derived using SynPhot or Gaia catalog observations (Jordi et al., 2010)
 - http://www.stsci.edu/institute/software_hardware/stsdas/synphot

References



Bessell, M.S., Castelli, F., Plez, B., 1998. Model atmospheres broad-band colors, bolometric corrections and temperature calibrations for O-M stars. Astron.m Astrophys. 333, 231-250.

Bouley, S., Baratoux, D., Vaubaillon, J., Mocquet, A., Le Feuvre, M., Colas, F., Benkhaldoun, Z., Daassou, A., Sabil, M., Lognonne, P., 2012. Power and duration of impact flashes on the Moon: Implication for the cause of radiation. Icarus, 218, 115-124.

Jordi, C., Gebran, M., Carrasco, J.M., de Bruijne, J., Voss, H., Fabricius, C., Knude, J., Vallenari, A., Kohley, R., Mora, A., 2010. Gaia broad band photometry. Astronomy and Astrophysics, 523, A48.

Moser, D.E., Suggs, R.M., Swift, W.R., Suggs, R.J., Cooke, W.J., Diekmann, A.M., Kohler, H.M., 2011., "Luminous Efficiency of Hypervelocity Meteoroid Impacts on the Moon Derived from the 2006 Geminids, 2007 Lyrids, and 2008 Taurids", Meteoroids 2010 Proceedings (NASA CP-2011-216469)

Nemtchinov, I.V., Shuvalov, V.V., Artemieva, N.A., Ivanov, B.A., Kosarev, I.B., Trubetskaya, I.A., 1998. Light impulse created by meteoroids impacting the Moon. Lunar Planet. Sci. XXIX. Abstract 1032.

Ortiz, J.L., Madiedo, J.M., Morales, N., Santos-Sanz, P., Aceituno, F.J., 2015. Lunar impact flashes from Geminids: analysis of luminous efficiencies and the flux of large meteoroids on Earth. MNRAS 454, 344-352.

Rembold. J.J., Ryan, E.V., 2015. Characterization and analysis of near-earth objects via lunar impact observations. Planetary and Space Science, 117, 119-126.

Suggs, R.M., Moser, D.E., Cooke, W.J., Suggs, R.J., 2014. The flux of kilogram-sized meteoroids from lunar impact monitoring. Icarus 238, 23-36.

Swift, W.R., Moser, D.E., Suggs, R.M., Cooke, W.J., 2011. An exponential luminous efficiency model for hypervelocity impact into regolith. In: Proceedings of the Meteoroids 2010 Conference, NASA CP-2011-216469, pp. 124-141.

Yanagisawa, M., Kisaichi, N., 2002.. Lightcurves of 1999 Leonid impact flashes on the moon. Icarus 159, 31-38.

Backup



Impact Flux at Earth Compared with Other Measurements





After Brown et al. (2002)

with adjustments for gravitational focusing and surface area of Earth at 100km altitude



- Ortiz et al. assumes energy in the V filter uniformly distributed across almost entire CCD bandwidth
 - Ref. 2001 and later? not much detail
 - Shortcomings leads to overestimate of energy by a factor of 2?
 - Assumed passband is even greater than FWHM of camera response (500 nm vs 400 nm)
 - Flash blackbody curve drops off rapidly and isn't flat across the camera passband
 - Need calculation for this...

Historical Approaches (2)



- Yanagisawa et al. (2002, 2006, 2008)
 - Compare flash signal to comparison star
 - Assume blackbody spectrum for comparison
 - Integrate across camera passband (400-800nm) assuming flat response
 - Shortcomings statements in 2006 paper
 - "The spectral response of the cameras is not flat in the wavelength range between 400 and 800 nm... and the cameras have some sensitivity outside this range"
 - "The difference between the spectra for the flash and the comparison star will thus lead to some error in the calculated flux"
 - Estimated a factor of 2 error from these issues and lack of flat/dark corrections

Historical Approaches (3)



- Bouley et al., 2012, Icarus 218, 115-124.
 - $P = 183 \times 10^{-(m + 26.74)/2.5}$ sun power integrated in the visual domain (Pogson method)
 - Ed = P * t / 2 flash power and duration integrated over all frames assuming linear decrease
 - $E = Ed \pi f d^2 / \eta$
 - d = 384400 km, f = 2 (hemispherical emission)
 - η = 2 x 10 $^{\text{-3}}$ with range from 5 x 10 $^{\text{-4}}$ to 5 x 10 $^{\text{-3}}$
 - Used published magnitudes from Ortiz, Yanagisawa, Cooke (mixed bag of V and R magnitudes)
 - Shortcomings
 - "Visual domain" not defined relative to camera response
 - Stellar calibration filter passband not specified
 - Time-integrated flash vs. peak flash



- Suggs et al. 2014 (also Rembold and Ryan, 2015)
- Color correction using conventional astronomical photometric approach
 - Uses B-V colors of comparison stars to determine color correction term
 - Assumes blackbody temperature of flash from Nemtchinov modeling to correct to R filter (peak and FWHM)
 - We need good measurements of flash temperatures using measurements in independent filters (V-R, R-I, etc.)

10 Years of Observations

- The MSFC lunar impact monitoring program began in 2006 in support of environment definition for the Constellation Program
 - Needed a model/specification for impact ejecta risk
- Work continued by the Meteoroid Environment Office after Constellation cancellation
 - Lunar impact monitoring allows measurement of fluxes in a size range not easily observed (10s of grams to kilograms)
- A paper published in Icarus reported on the first 5 years of observations
 - Icarus: http://www.sciencedirect.com/science/article/pii/S0019103514002243
 - ArXiv: http://arxiv.org/abs/1404.6458

Observation Summary





394 impacts since 2005

Subset of 126 flashes on photometric nights to 2011 141 hrs evening - 81 flashes 126 hrs morning - 45 flashes Average: 2.1 hrs/flash evening/morning = 1.6:1



Photometric error ~0.2 mag

NASA/MSFC/EV44/R.Suggs, S. Ehlert

Filter and camera responses depend on color of object





Luminous Efficiency





From Moser et al. (2011)



Luminous efficiency $\eta = 1.5 \times 10^{-3} \exp(-9.3^2/v^2)$ v = impact speed in km/s**Kinetic Energy** $KE = E_{lum} / \eta$ Mass $M = 2 KE / v^2$

Calibration: Magnitude Equation



Parameters determined by observing stars with known magnitudes

 $R = -2.5 \log_{10}(S) - k' X + T (B-V) + ZP$

R = Johnson-Cousins R magnitude

k' = extinction coefficient

X = airmass (zenith = 1.0)

T =color response correction term

(B-V) = color index

Replace T(B-V) with R-EX for flash (next slide)

ZP = photometric zero point for the night

 $S = DN^{1/0.45}$ if camera gamma set to 0.45 which improves contrast near bottom of dynamic range

DN = pixel value 0 - 255

Luminous energy from impact peak magnitude



 $E_{lum} = f_{\lambda} \Delta \lambda f \pi d^2 t$ Joules $E_{lum} =$ luminous energy $\Delta \lambda$ = filter half power width, 1607 Ångstroms for R f = 2 for flashes near the lunar surface, 4 for free space d = distance from Earth to the Moon t = exposure time, 0.01667 for a NTSC field $f_{\lambda} = 10^{-7} \text{ x} 10^{(-R + 21.1 + zp_R)/2.5}$ J cm⁻² s⁻¹ Å⁻¹ R = the R magnitude $zp_R = 0.555$, photometric zero point for *R* from Bessell et al.

(1998). This is not the same as *ZP* in magnitude equation)



Impact Energies



Red error bars - photometric uncertainty; Blue error bars - luminous efficiency uncertainty Squares indicate saturation

The flux to a limiting energy of 1.05×10^7 J is 1.03×10^{-7} km⁻² hr⁻¹

NASA/MSFC/EV44/R.Suggs, S. Ehlert

Shower Correlation



Peak R magnitude saturation correction







Meteoroid Masses



Red error bars - photometric uncertainty; Blue error bars - range of reasonable luminous efficiencies Squares indicate saturation

The flux to a limiting mass of 30 g is 6.14×10^{-10} m⁻² yr⁻¹

NASA/MSFC/EV44/R.Suggs, S. Ehlert

Bright flash on 17 March 2013





Impact crater found by LRO! Robinson et al. (2014)





<u>Features</u>

- Fresh, bright ejecta
- Circular crater
- Asymmetrical ray pattern

Crater info

- Rim-to-rim diameter = 18 m
- Inner diameter = 15 m
- Depth $\approx 5 \text{ m}$

Actual crater location

• 20.7135°N, 24.3302°W

Impact Constraints

- → Circular crater, impact angle constrained $\theta_h > 15^\circ$
- Ejecta gives no azimuth
 constraint (Robinson, personal comm.)

Comparison with Grün Flux



- For our completion limit of 30g we saw 71 impacts for a flux of
 6.14 x 10⁻¹⁰ m⁻² yr⁻¹
- The Grün et al. (1985) flux above a mass of 30g is 7.5 x10⁻¹⁰ m⁻² yr⁻¹

Favorable Virginid radiant geometry





Pink indicates the portion of the moon visible to the radiant. Impact angle ~56° from horizontal.

NASA/MSFC/EV44/R.Suggs, S. Ehlert

Mapping the impact location



LRO basemap





Nominal predicted crater position 20°.6644 N, 24°.1566 W

ArcMap was used to georeference the lunar impact following the geolocation workflow.

Refrac corr:

 $20^{\circ}.6842^{+0.2585}_{-0.2581}$ N, $24^{\circ}.2277^{+0.2881}_{-0.2887}$ W

NASA/MSFC/EV44/R.Suggs, S. Ehlert

Comparison of geolocation results to obs crater location





| Method | Longitude (° W) | Latitude | Angular distance | Surface distance |
|-------------------------------------|---------------------------------------|----------------|------------------|------------------|
| Rough workflow | 23.922 | 20.599 | 0.39875 | 12.096 |
| Refined workflow | 24.1566 | 20.6644 | 0.169665 | 5.1469 |
| Refined, with refraction correction | 24.2277 ^{+0.2881} -0.2887 | 20.6842+0.2585 | 0.100261 | 3.0415 |
| LRO observed | 24.3302 | 20.7135 | - | - |

NASA/MSFC/EV44/R.Suggs, S. Ehlert

Limiting Magnitude





Limiting Mass





4. Georeference flash image





6. Determine flash location

- Input flash location (\bar{x}_f', \bar{y}_f') to ArcMap's "Go to XY" tool
- Read & record selenographic coordinates (λ, φ) transformed by ArcMap
- Place marker at flash location, add point to database and shapefile







Mapping the impact location "Rough workflow"





ArcMap was used to georeference the lunar impact 3 times, at peak brightness and late impact.



Mapping the impact location



Results of several attempts with different features and frames



NASA/MSFC/EV44/R.Suggs, S. Einge location: $20.5820 \pm 0.10^{\circ}$ Mun $20.922 \pm 0.304^{\circ}$ W

Meteor Shower and Sporadic Source Radiants



Equipment



- Telescopes 14 inch (0.35m), have also used 0.5m and 0.25m
- Camera B&W video 1/2inch Sony HAD EX chip (Watec 902H2 Ultimate is the most sensitive we have found)
- Digitizer preferably delivering Sony CODEC .AVI files if using LunarScan (Sony GV-D800, many Sony digital 8 camcorders, Canopus ADVC-110)
 - This gives 720x480 pixels x8 bits
- Time encoder GPS (Kiwi or lota)
 - Initially used WWV on audio channel with reduced accuracy
- Windows PC with ~500Gb fast harddrive (to avoid dropped frames)
 - Firewire card for Sony or Canopus digitizers

Celestron 14

Finger Lakes focuser

Pyxis rotator Optec 0.3x - focal reducer

Watec 902H2 Ultimate