

# Conjunction Assessment Risk Analysis

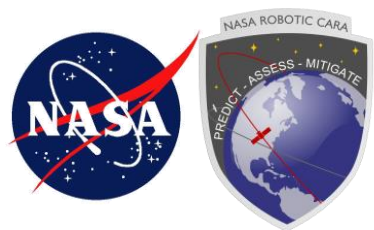


**Conjunction Assessment  
Late-Notice High-Interest  
Event Investigation:**

**Space Weather Aspects**

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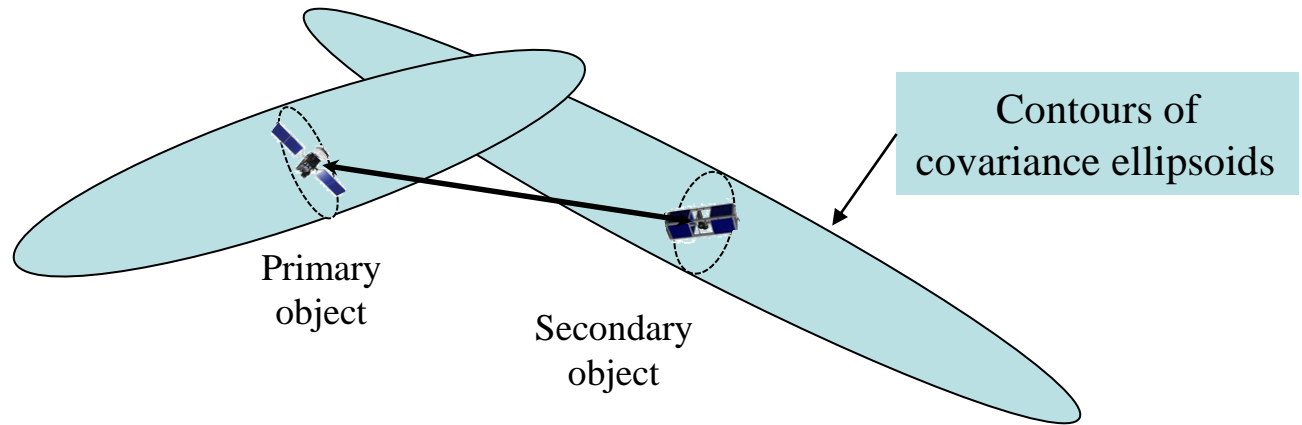
**TBD Sep 2016**



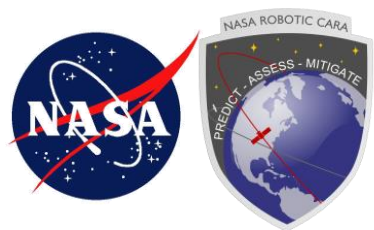
# Background: Conjunction Assessment

- **Conjunction Assessment Risk Analysis (CARA)**

- Evaluates collision risk between two satellites expected to come in close proximity of each other (by calculating probability of collision [Pc])
- Mitigates collision risk, if necessary

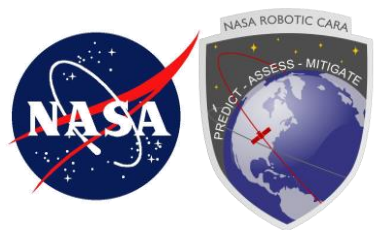


- **Conjunctions usually identified several days before close approach**
  - Risk usually follows more-or-less canonical development paradigm
- **However, sometimes risk increases or decreases quite suddenly**
  - More insight needed into the circumstances behind such cases



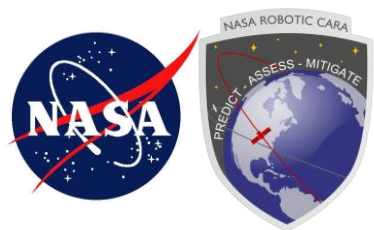
# Introduction

- **Tasked to analyze short notice events which are generally a result of unexpected, large state changes**
- **Looked at all reported conjunctions for *ca.* 700 km protected missions from May 2015 though Feb 2016**
- **Performed an analysis to determine whether there is any correlation between large state changes/late notice event identification and the following factors:**
  - Sparse tracking
  - High drag objects
  - Space weather
- **Examined specific late notice events identified by missions to try to identify root cause**



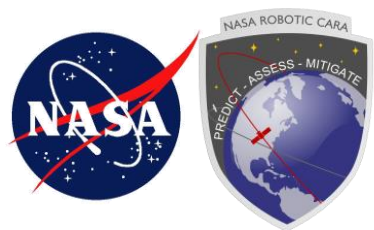
# Broad Investigation of Large State Changes

- **Late-notice events usually driven by large changes in primary (protected) object or secondary object state**
- **Main parameter to represent size of state change is component position difference divided by associated standard deviation ( $\epsilon/\sigma$ ) from covariance**
- **Investigation determined actual frequency of large state changes, in both individual and combined states**
  - Compared them to theoretically expected frequencies
- **Found that large changes ( $\epsilon/\sigma > 3$ ) in individual object states occur much more frequently than theory dictates**
  - Effect less pronounced in radial components and in events with  $P_c > 1e-5$
- **Found combined state matched much closer to theoretical expectation, especially for radial and cross-track**
  - In-track is expected to be the most vulnerable to modeling errors, so not surprising that non-compliance largest in this component



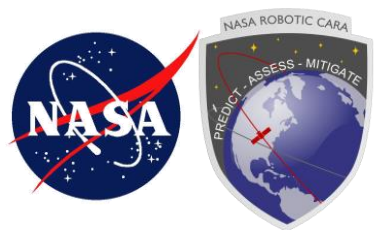
# Summary of “Other” Correlation Results

- **Pc correlation with large state changes in primary not very strong**
- **Large state changes in the secondary do correlate to large changes in Pc, but not all that strongly**
  - Value of Kendall’s Tau ranged from 0.37 to 0.6
- **Sparse tracking for secondary does not correlate with large state errors**
- **Higher EDR values for secondary do not correlate with larger state errors**

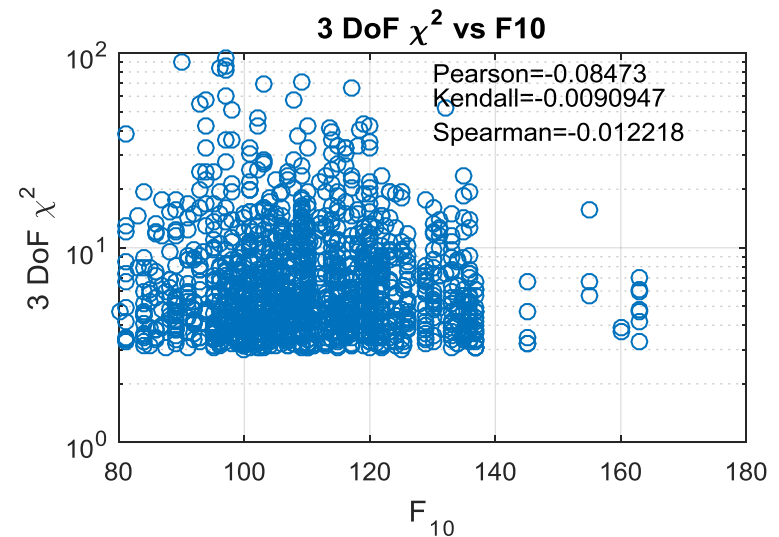
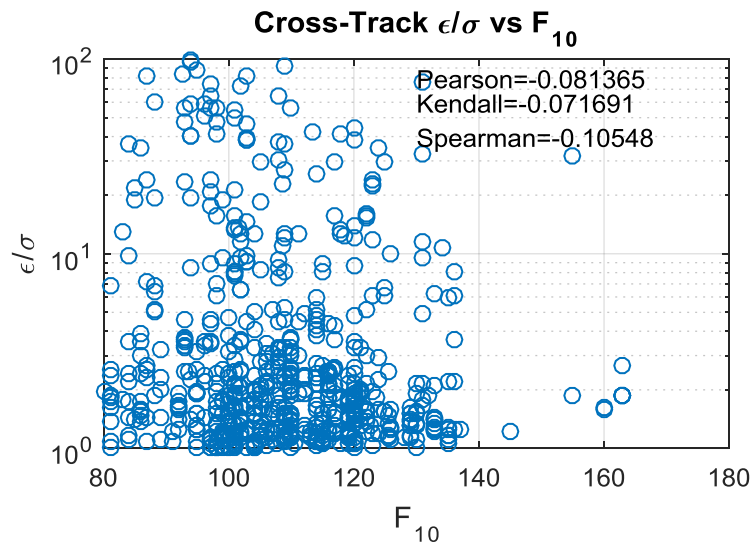
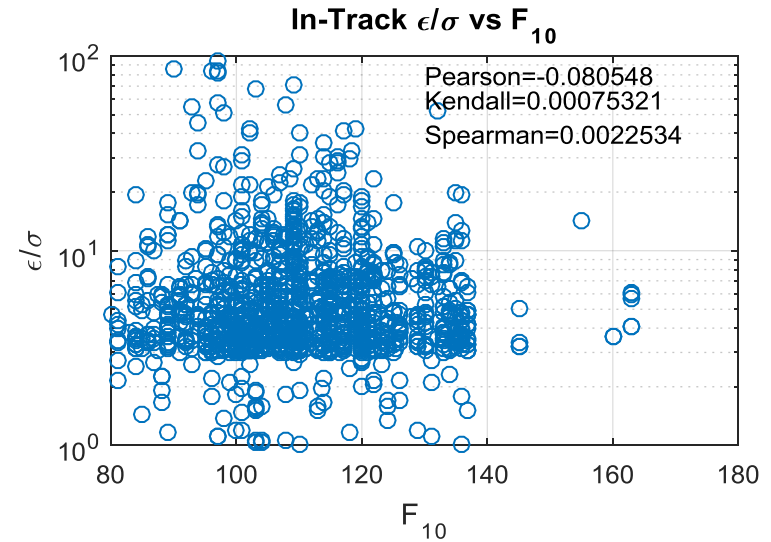
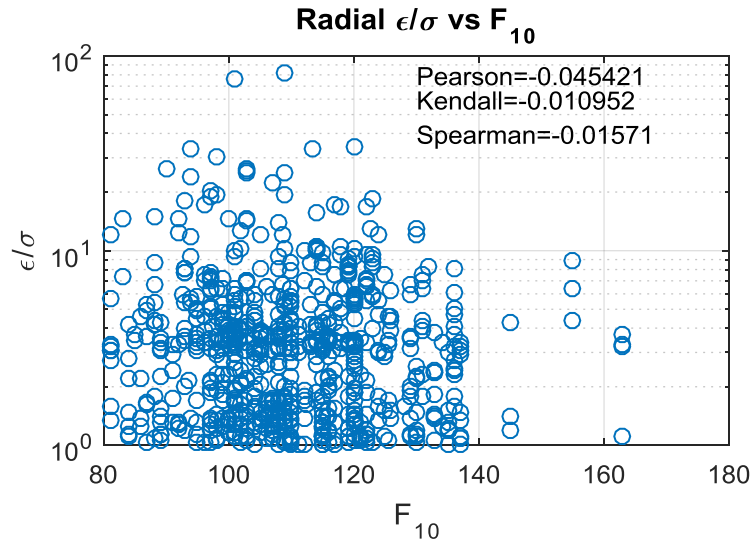


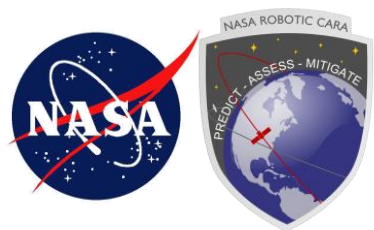
# Correlations with Solar Activity

- **Elevated levels of solar activity can produce an unstable atmosphere whose density is difficult to model**
  - More strongly true with geomagnetic storms ( $Dst$ ,  $a_p$ )
  - Can also be observed with EUV (F10, M10, S10, Y10, &c.)
- **Different possibilities for essence of the problem**
  - Higher solar activity *simpliciter*
  - Mismatch between predicted and realized solar activity
- **Will investigate the former with correlation studies**
  - Median F10 and  $a_p$  over prediction interval
  - Peak  $a_p$  over prediction interval
- **Will investigate the latter with case studies**



# Combined $\epsilon/\sigma$ vs Median $F_{10}$ : Any Component $\text{abs}(\epsilon/\sigma) > 3$





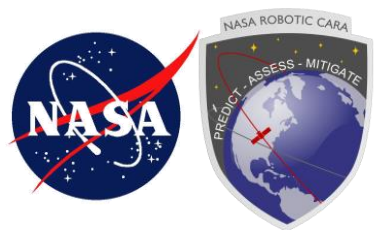
# Combined $\epsilon/\sigma$ vs Solar Indices: Tabular Summary

|                       | Radial | In-Track | Cx-Track | Chi-Sq |
|-----------------------|--------|----------|----------|--------|
| Median F10: Kendall   |        |          |          |        |
| All Data              | 0.008  | 0.01     | 0.006    | 0.02   |
| $\epsilon/\sigma > 3$ | 0.01   | 0.001    | 0.07     | 0.01   |
| $\epsilon/\sigma > 5$ | -0.03  | -0.05    | -0.09    | -0.05  |
| Median Ap: Kendall    |        |          |          |        |
| All Data              | 0.02   | -0.0001  | 0.02     | 0.02   |
| $\epsilon/\sigma > 3$ | -0.05  | -0.01    | 0.06     | -0.04  |
| $\epsilon/\sigma > 5$ | -0.003 | -0.003   | 0.03     | 0.01   |
| Peak Ap: Kendall      |        |          |          |        |
| All Data              | 0.03   | 0.009    | 0.03     | 0.04   |
| $\epsilon/\sigma > 3$ | -0.04  | -0.01    | 0.03     | -0.04  |
| $\epsilon/\sigma > 5$ | -0.04  | -0.01    | -0.02    | -0.04  |

- Correlations are essentially nonexistent in all areas

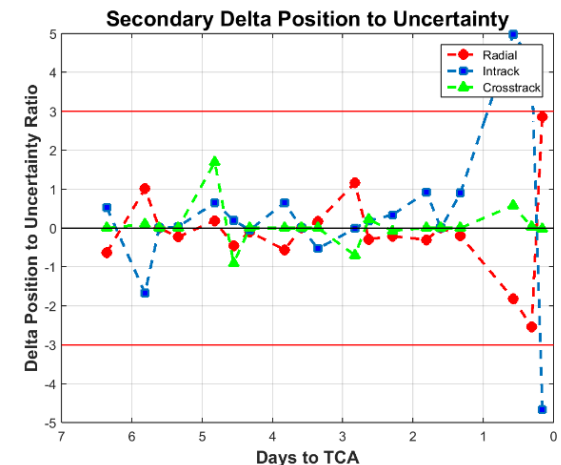
**Simple elevated levels of solar activity  
do not correlate with large changes in relative miss**

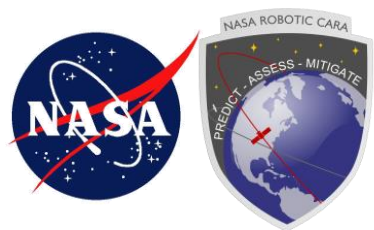




# Late-Notice HIE Case Studies

- **Examined four late-notice events that fell within data investigation period of current study**
  - 1 MAY 2015 to 1 FEB 2016
- **Events examined**
  - Terra vs 38192, TCA 24 JUN 201
  - Aura vs 89477; TCA 29 AUG 2015
  - Terra vs 37131; TCA 19 DEC 2015
  - GPM vs 28685; TCA 5 SEP 2015
    - Determined not to be space weather related
- **Will look at**
  - $\epsilon/\sigma$  vs time (same as  $\Delta$  position to uncertainty plots from daily/HIE report, like at right)
  - $P_c$  vs time (same as from daily/HIE report)
  - Dst and  $a_p$ ; prediction vs actual
    - Segmented by what is available in support of each update





# JSpOC Space Weather Information Files

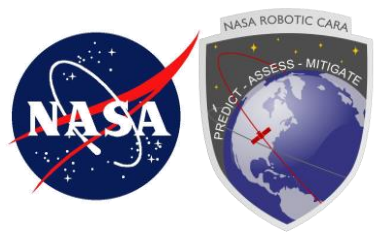
- **JSpOC uses JBH09**

- JB08 + HASDM
- Anemomilos DST prediction

- **Updated at JSpOC 3x per day**

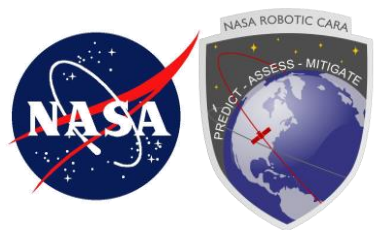
- **Model Input summary:**

- **S10, S54** are daily and 54-day S10.7 index for >200 km heating of O by solar chromosphere 28.4-30.4 nm emissions in  $\times 10^{-22}$  Watts per meter squared per Hertz
- **M10, M54** are daily and 54-day M10.7 index for 100-110 km heating of O<sub>2</sub> by solar photosphere 160 nm SRC emissions in  $\times 10^{-22}$  Watts per meter squared per Hertz
- **Y10, Y54** are daily and 54-day Y10.7 index for 85-90 km heating of N<sub>2</sub>, O<sub>2</sub>, H<sub>2</sub>O, NO by solar coronal 0.1-0.8 nm and Ly $\alpha$  121 nm emissions in  $\times 10^{-22}$  Watts per meter squared per Hertz
- **F10, F54** are daily and 54-day solar 10.7 cm radio flux in  $\times 10^{-22}$  Watts per meter squared per Hertz
- **a<sub>p</sub>** is the 3-hour planetary geomagnetic 2 nT index (00-21 UT)
- **Dst** is Disturbance Storm Time geomagnetic index in nT
- **DTC** is delta exospheric temperature correction in units of K

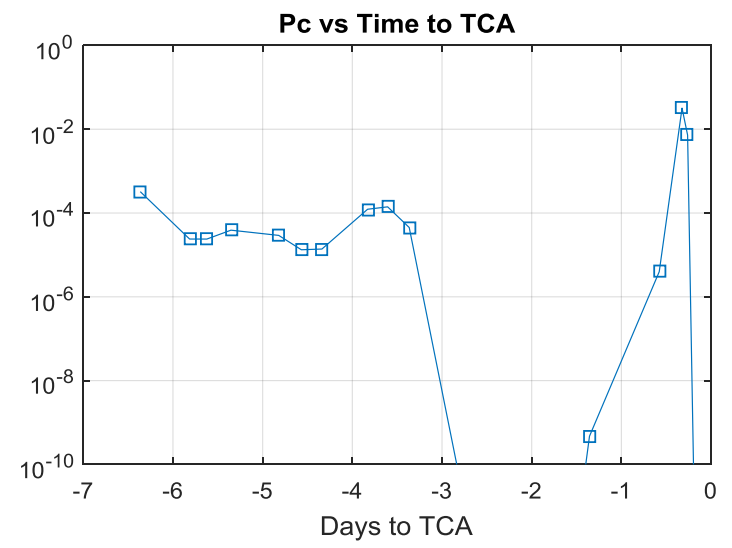
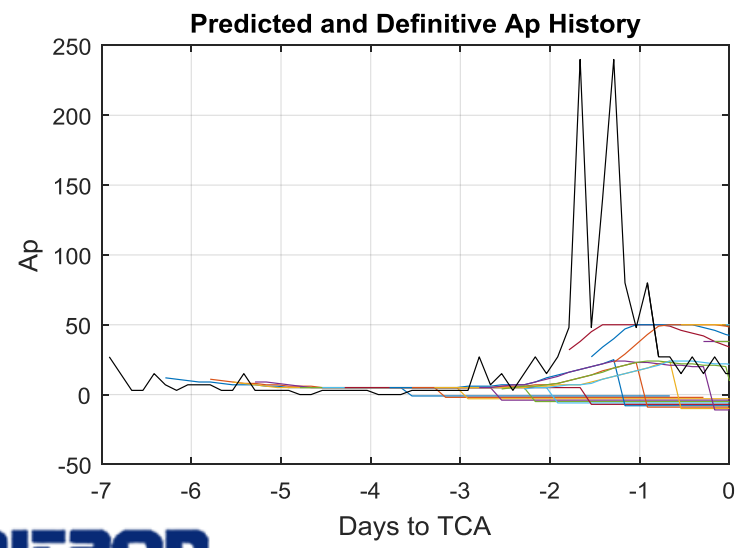
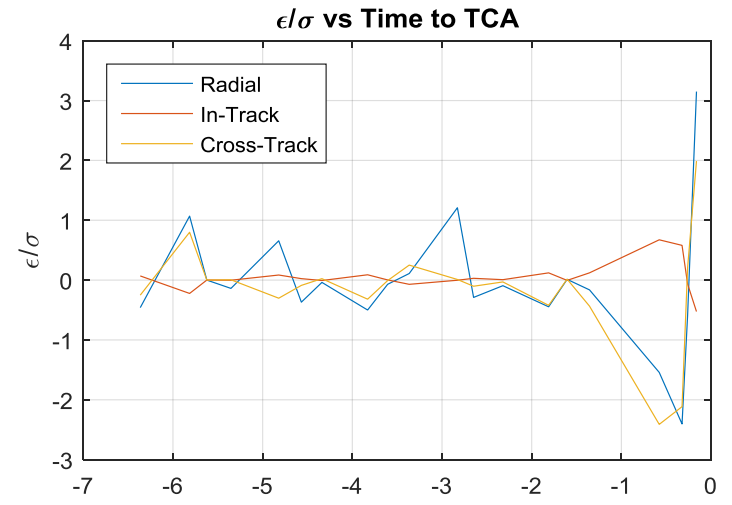
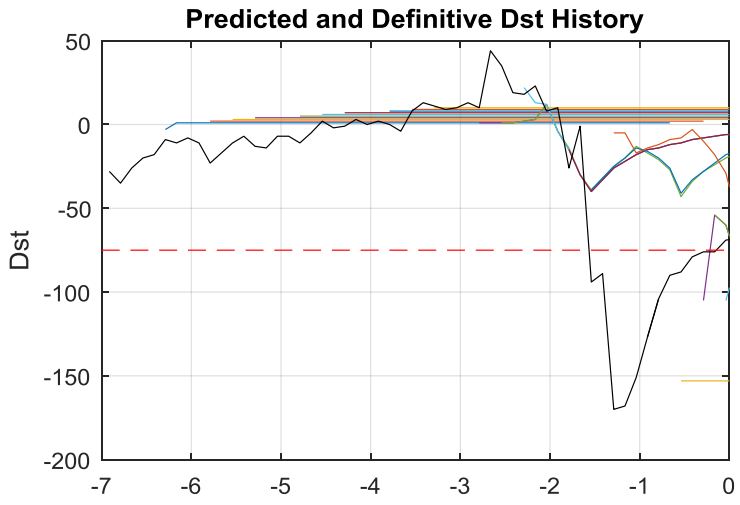


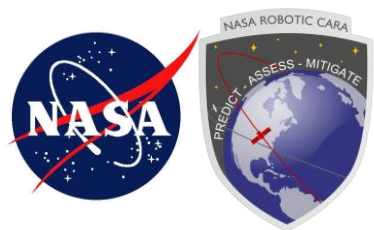
# Space Weather Evolution Charts

- **Upper left shows Dst; lower left shows  $a_p$**
- **Black line is “issued” (definitive) data**
- **Colored lines are predicted data**
  - Each line begins when a given OD update executed
  - Each line shows predicted values of the geomagnetic index of choice
    - When Dst lines move to small positive value, prediction stops (zeroes in file)
    - When  $a_p$  lines move to small negative value, prediction stops (ones in file)
- **Dst threshold for solar storm compensation engagement also shown**
- **Upper right shows  $\epsilon/\sigma$  for each component**
  - Miss distance vs combined covariance
- **Lower right shows Pc vs time**



# Case Study #1: Terra vs 38192, TCA 24 JUN 2015





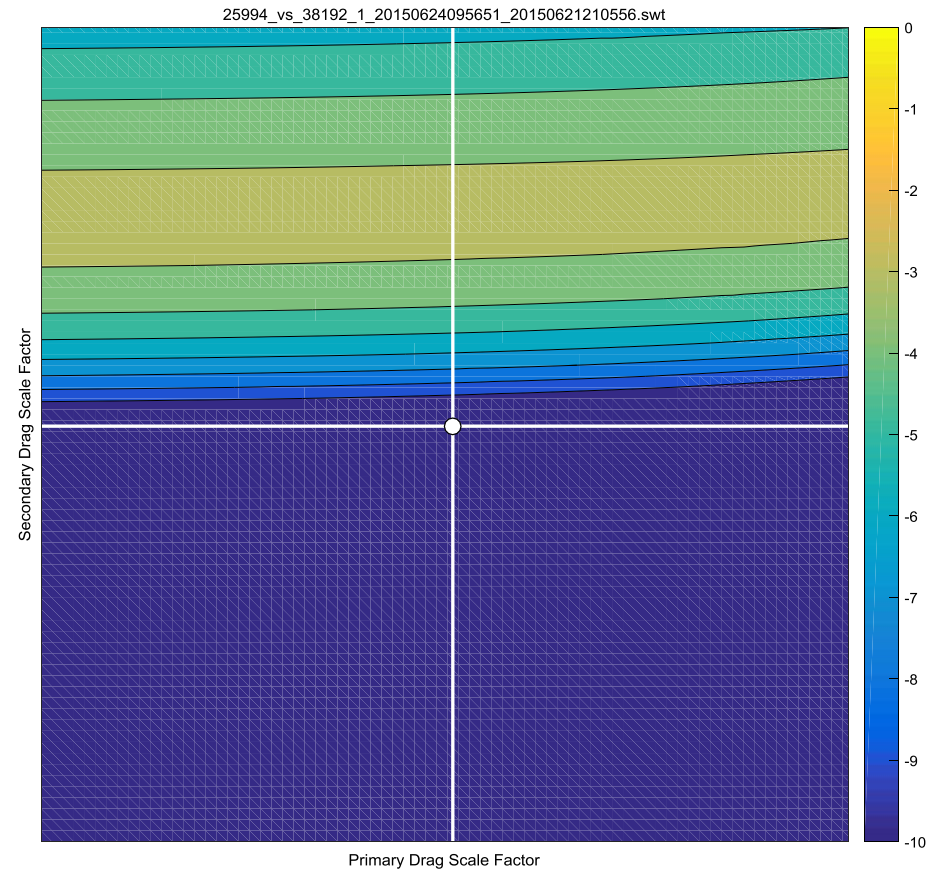
# Space Weather Trade-Space Result: 61 Hours to TCA

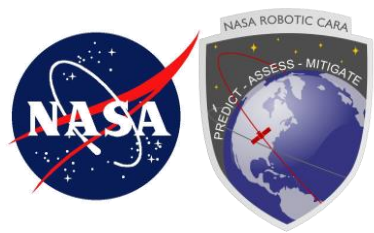
- **About half a day before spike in  $a_p$ /Dst begins**

- Some predicted increased Dst activity, but not of severity actually realized
- Predictions at very end of storm over-predict Dst
- Final prediction and shrinking covariance produces Pc drop off

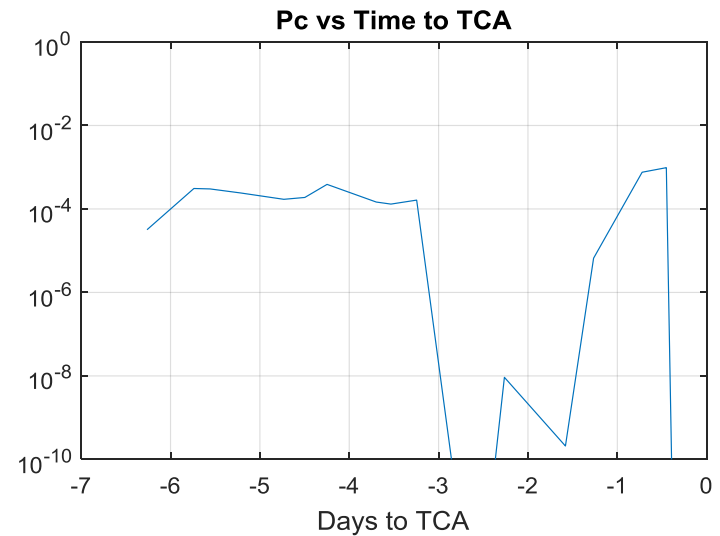
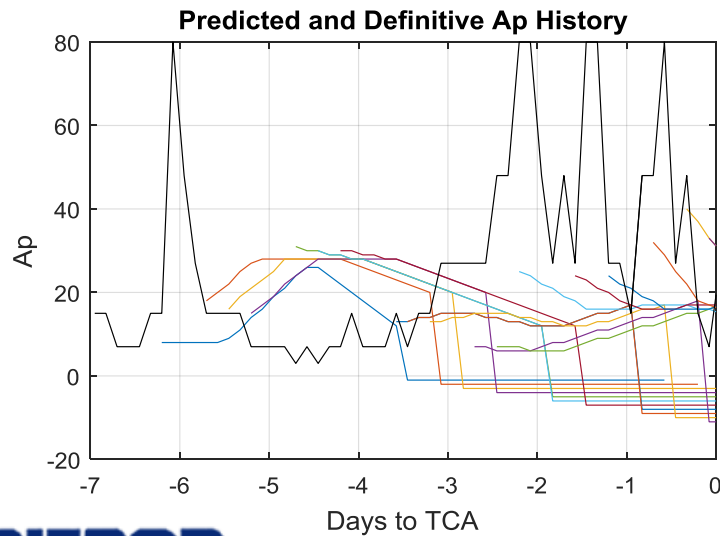
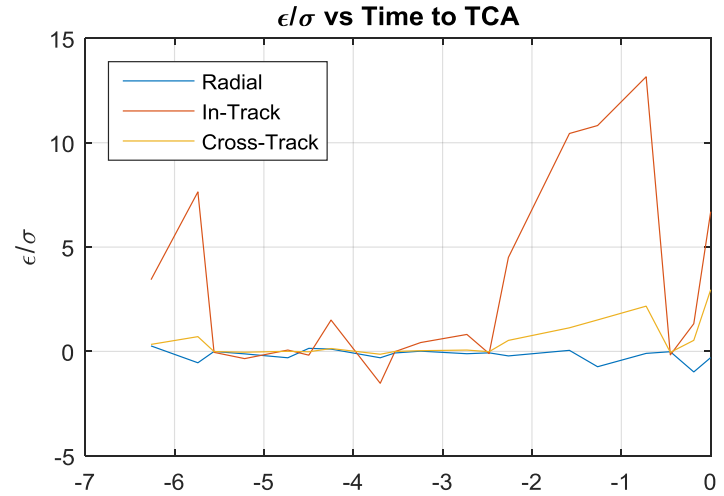
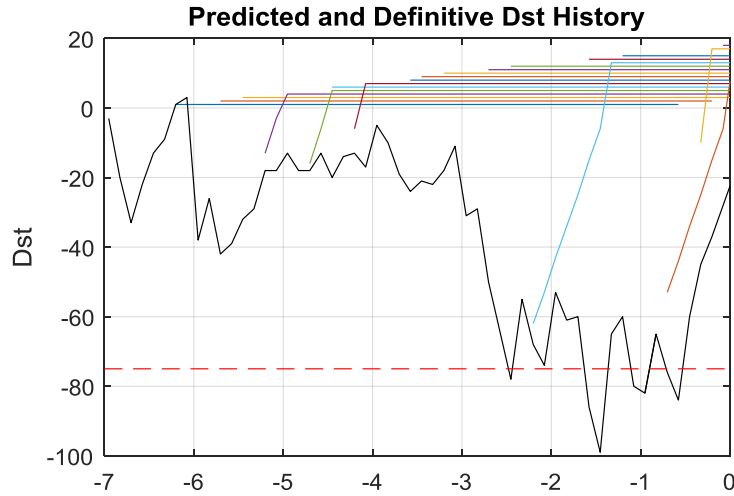
- **SWTS indicates conjunction vulnerable to large Pc changes due to density mis-modeling**

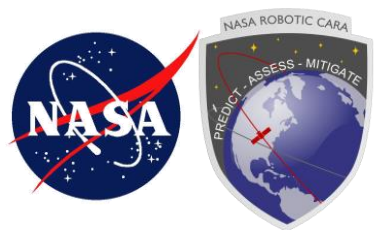
• **Bottom line: missed solar storm and subsequent prediction failures produced late changes**





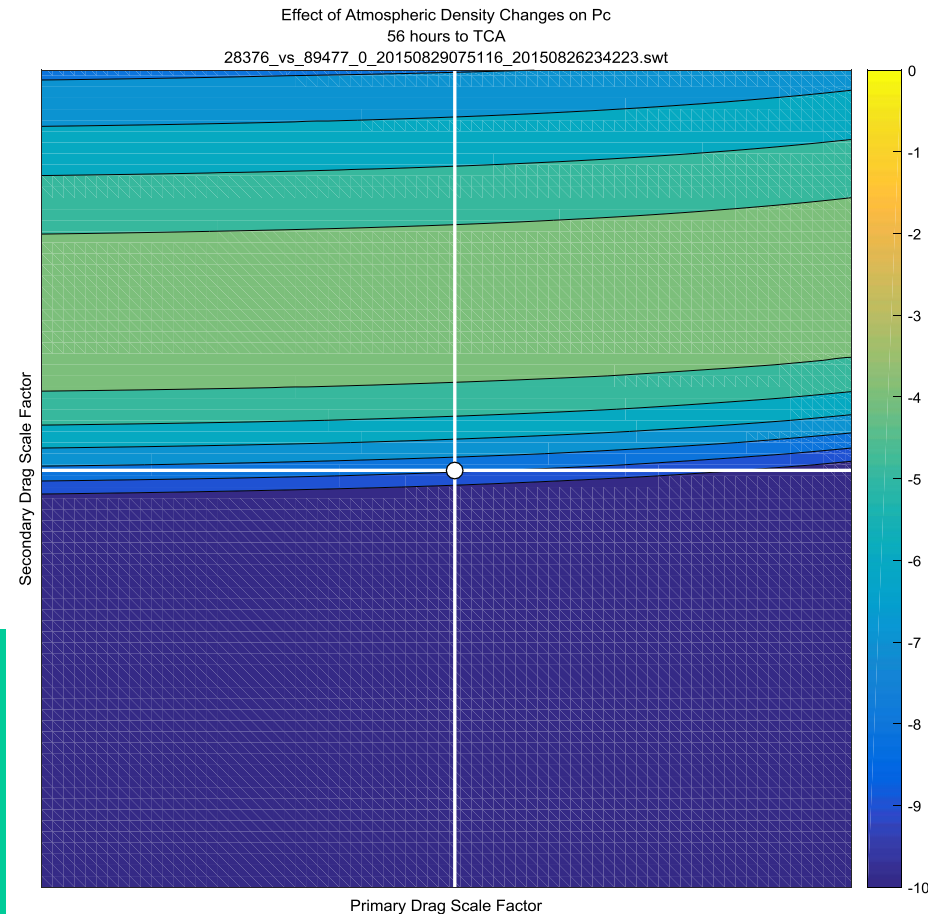
# Case Study #2: Aura vs 89477; TCA 29 AUG 2015

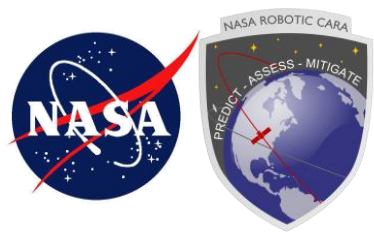




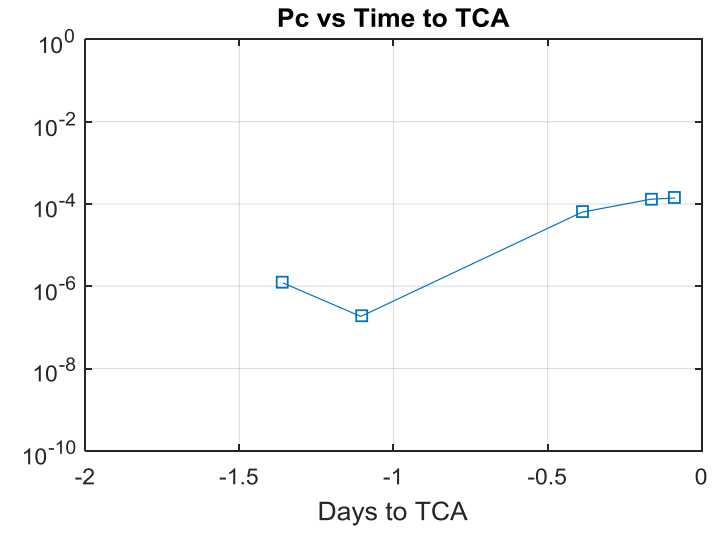
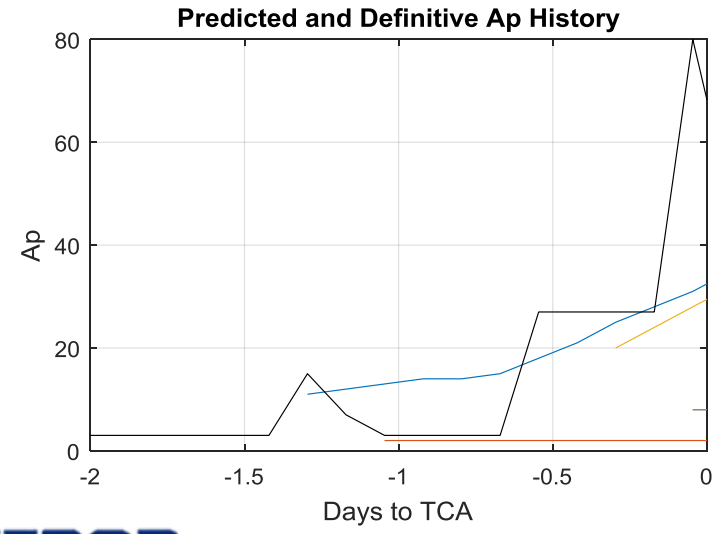
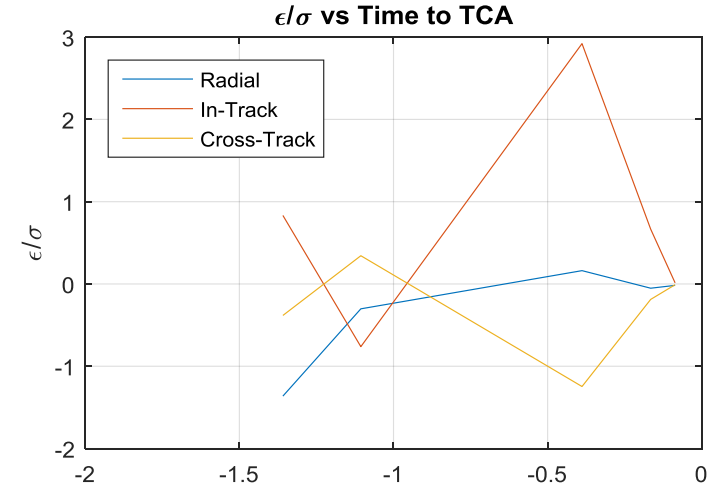
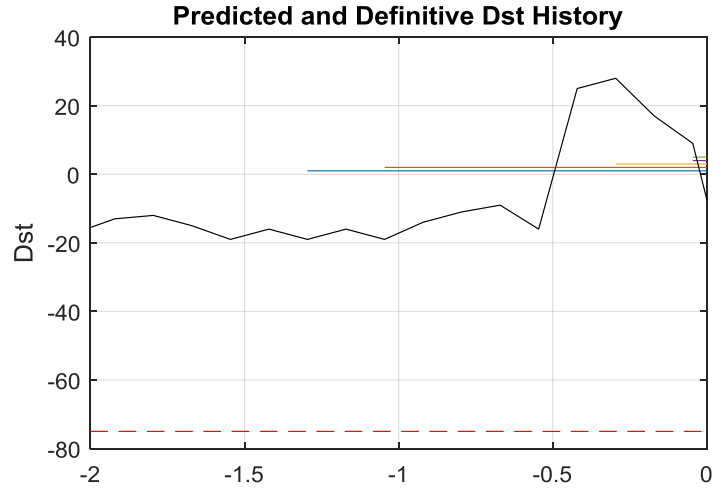
# Space Weather Trade-Space Result: Aura vs 89477; 56 Hours to TCA

- **Run from update right as spike in  $a_p$ /Dst is beginning**
    - No predicted spike in relevant ASW space weather file
  - **Indicates that conjunction vulnerable to large Pc changes due to atmospheric mis-modeling**
- **Bottom line: space weather predictions missed significant solar storm**
  - Most likely cause of late-breaking change in Pc

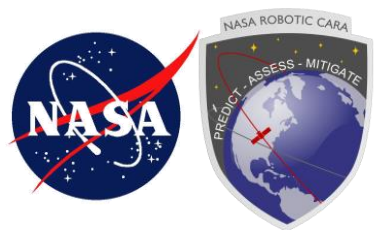




# Case Study #3: Terra vs 37131; TCA 19 DEC 2015



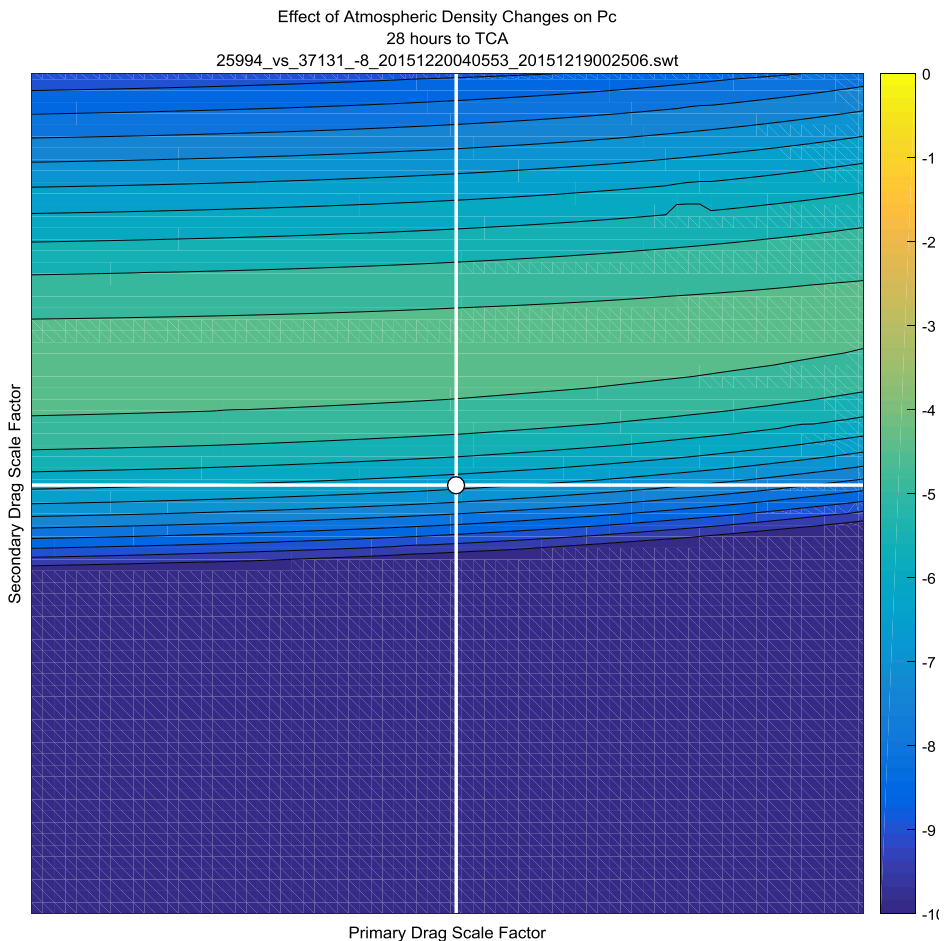


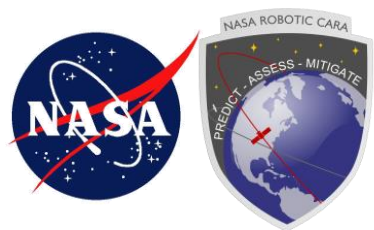


# Space Weather Trade-Space Result: Terra vs 37131; 28 Hours to TCA

- **Run from update before 2 OoM change in Pc observed**
  - Strange actual behavior in Dst
  - Modest unmodeled increase in Ap
- **SWTS indicates that conjunction vulnerable to Pc changes due to atmospheric mis-modeling**

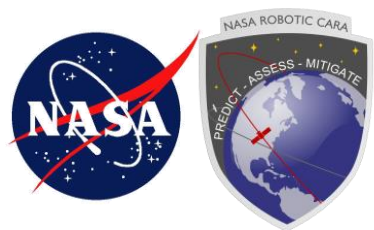
• **Bottom line: odd space weather behavior, and deviation from predication, probably responsible for modest increase in Pc**





# Late-Breaking HIEs: Overall Summary

- **Large state changes occur more often than theory would indicate**
- **Do not correlate at global level with any obvious causal condition**
  - Light tracking, hard-to-maintain orbits, or generally elevated solar activity
- **Case studies indicate two culprits**
  - Failure of JSpOC space weather predicted indices to predict solar storms
  - Edge cases for general screenings
- **Is there any good news?**
  - No, not really

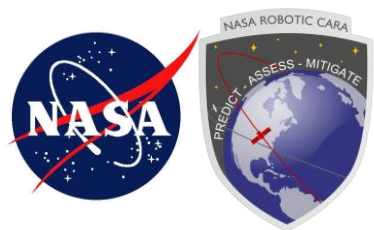


# Solar Storm Response – What are we doing?

- **CARA has begun receiving atmospheric model input data from JSpOC**
  - Gives CARA analysts insight into what is being modeled
  - CARA analysts can work with outside experts (SWRC) to evaluate reasonableness and likelihood of predicted space weather events
- **CARA analysts can use model input information and outside evaluation of predictions to provided more nuanced feedback as to when to expect increased uncertainty and variation due to space weather**
  - Additionally, as shown by this study, it is a great help for post-event analysis
- **Developing operational ConOps for how and when to apply space weather trade space with model insight**



# BACKUP SLIDES



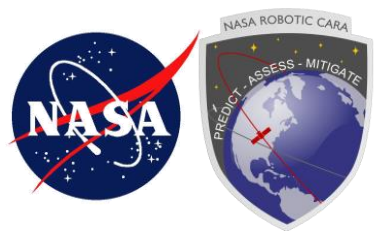
# JSpOC Space Weather Information Files: Data Currency

- **Three types of data in file**

- “Issued” – definitive values for the solar/geomagnetic index, subjected to full availability of feeder data and consistency tests
- “Nowcast” – initial observations of values, hand-scaled and not subject to consistency tests
  - Measurements stay in “nowcast” status for typically 24 hours
- “Predicted” – values are predicted
  - EUV predicted values from 54- and sometimes 108-day autoregression analyses of past data
  - Geomagnetic indices are predicted from observed solar activity earlier in the solar rotation (and thus expected to become georelevant at a given future time)

- **Data type timing**

- Issued/Nowcast data used in propagating states from epoch to current time
  - Scaled/debiased with HASDM results
- Predicted data used in propagating states from current time to TCA
- Accuracy of predicted data can influence propagated result substantially



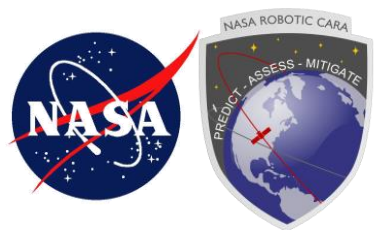
# Normal Deviates and Chi-squared Variables

- **Let  $q$  and  $r$  be vectors of values that conform to a Gaussian distribution**
  - These collection of values are called *normal deviates*
- **A normal deviate set can be transformed to a *standard normal deviate* by subtracting the mean and dividing by the standard deviation**
  - This produces the so-called Z-variables

$$Z_q = \frac{q - \mu_q}{\sigma_q}, \quad Z_r = \frac{q - \mu_r}{\sigma_r}$$

- **The sum of the squares of a series of standard normal deviates produces a chi-squared distribution, with the number of degrees of freedom equal to the number of series combined**

$$Z_q^2 + Z_r^2 = \chi_{2dof}^2$$



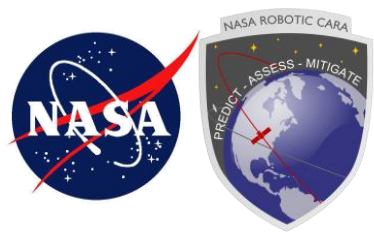
# Normal Deviates in State Estimation

- **In a state estimate, the errors in each component (u, v, and w here) are expected to follow a Gaussian distribution**
  - If all systematic errors have been solved for, only random error should remain
- **These errors can be standardized to the Z-formulation**
  - Mean presumed to be zero (OD should produce unbiased results), so no need for explicit subtraction of mean

$$Z_u = \frac{u}{\sigma_u}, \quad Z_v = \frac{v}{\sigma_v}, \quad Z_w = \frac{w}{\sigma_w}$$

- **Sum of squares of these standardized errors should follow a chi-squared distribution with three degrees of freedom**

$$Z_u^2 + Z_v^2 + Z_w^2 = \chi_{3dof}^2$$



# State Estimation Example Calculation

- **Let us presume we have a precision ephemeris, state estimate, and covariance about the state estimate**
  - For the present, further presume covariance aligns perfectly with uvw frame (no off-diagonal terms)
- **Error vector  $\varepsilon$  is position difference between state estimate and precision ephemeris, and covariance consists only of variances along the diagonal**
  - Inverse of covariance matrix is straightforward

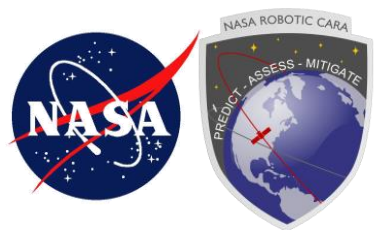
$$\varepsilon = \begin{bmatrix} \varepsilon_u \\ \varepsilon_v \\ \varepsilon_w \end{bmatrix}, \quad C = \begin{bmatrix} \sigma_u^2 & 0 & 0 \\ 0 & \sigma_v^2 & 0 \\ 0 & 0 & \sigma_w^2 \end{bmatrix}, \quad C^{-1} = \begin{bmatrix} 1/\sigma_u^2 & 0 & 0 \\ 0 & 1/\sigma_v^2 & 0 \\ 0 & 0 & 1/\sigma_w^2 \end{bmatrix}$$

- **Resultant simple formula for chi-squared variables**

$$\varepsilon C^{-1} \varepsilon^T = \frac{\varepsilon_u^2}{\sigma_u^2} + \frac{\varepsilon_v^2}{\sigma_v^2} + \frac{\varepsilon_w^2}{\sigma_w^2} = \chi_{3\text{dof}}^2$$

- **Extension to case with off-diagonal terms straightforward**

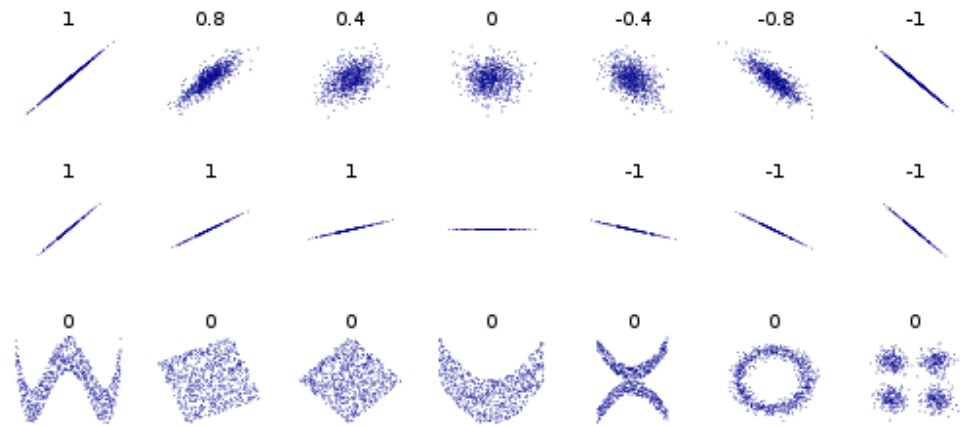




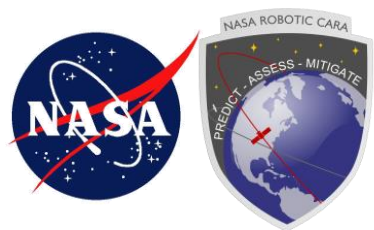
# Pearson Correlation Coefficient

- Evaluates the degree of a linear relationship between two variables
- Usually evaluated by the formula (s is sample standard deviation), with range of interesting and often not helpful outcomes

$$r = \frac{1}{n-1} \sum_{i=1}^n \left( \frac{x_i - \bar{x}}{s_x} \right) \left( \frac{y_i - \bar{y}}{s_y} \right)$$



- Some interpretive guidance via relationship to  $r^2$  value from linear regression: square of Pearson = regression  $r^2$ 
  - Pearson value of 0.5 would equate to  $r^2$  of 0.25—not very impressive
- Really would like something that reveals even non-linear correlation



# Kendall's Tau

- **Rank correlation test**

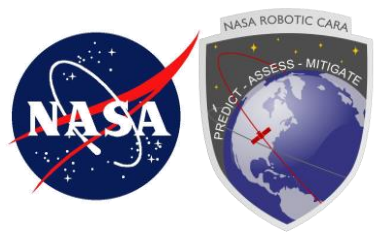
- With two vectors of data  $X$  and  $Y$ , compares  $(X_i, Y_i)$  to every other  $(X_j, Y_j)$
- Pair is concordant if, when  $X_i > X_j$ ,  $Y_i > Y_j$ ; discordant if the opposite
- Parameter is  $(\# \text{ concordant pairs} - \# \text{ discordant pairs}) / (\text{total pairs})$ 
  - So same range of values (-1 to 1) with same meaning

- **Much more robust test**

- Will find both linear and nonlinear correlation
- Computationally expensive [ $\sim O(n^2)$ ], but computers are doing the work

- **Tied situations create problems**

- In present analysis, arises when comparing continuous to discrete distribution
  - e.g.,  $\epsilon/\sigma$  to tracking levels (because tracking levels are counting numbers, so can have multiple  $\epsilon/\sigma$  values aligned with same tracking level)
- Even more computationally expensive modifications to adjust for ties
- Spot-checked these and saw no difference in computed result



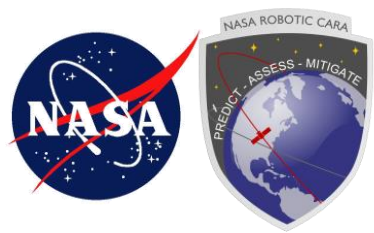
# Spearman's Rho

- **Test of monotonicity, computed by summing squares of differences in rank**
  - Mapped into same -1 to 1 range of values, with same interpretation
- **Computational formula**

$$\rho = 1 - \frac{6 \sum_{i=1}^n d_i^2}{n(n^2 - 1)}$$

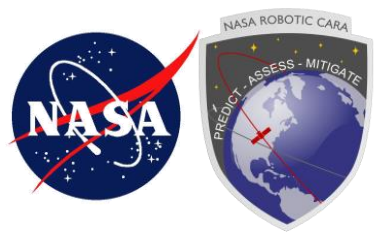
- **Computationally easier but more vulnerable to outlier data**
- **Usually larger than Kendall's tau**
- **Included here for consistency/contrast**

**Main factor to consult is Kendall's Tau**



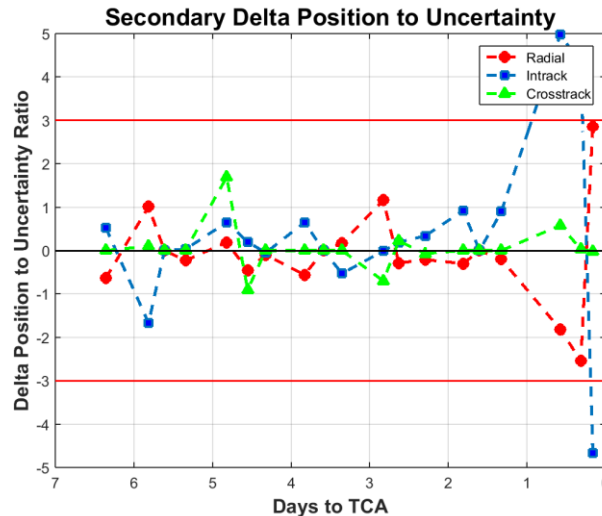
# Broad Investigation of Large State Changes

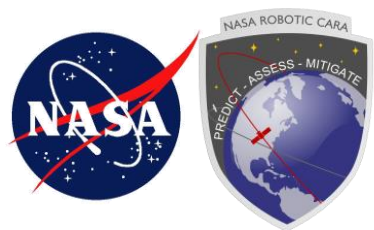
- **Determine actual frequency of large state changes, in both individual and combined states**
  - Compare to theoretically expected frequencies
- **Determine whether broadly correlated with potential/expected causes**
  - Low tracking
  - Harder-to-maintain orbits (larger energy dissipation rate)
  - General levels of solar activity (EUV and Joule atmospheric heating)



# Large State Changes: Parameterization (1 of 3)

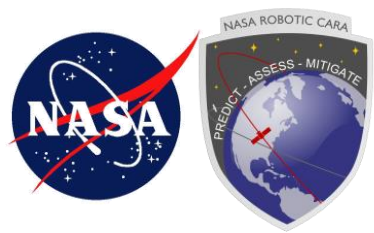
- **Main parameter to represent size of state change is component position difference divided by associated standard deviation ( $\epsilon/\sigma$ )**
  - Presumption of OD is that errors are normally distributed and unbiased
  - $\epsilon$  is difference in component position between subsequent state estimates
  - $\sigma$  is square root of associated variance from first state's covariance
  - Dividing  $\epsilon$  by  $\sigma$  creates standardized normal variable ( $\mu=0$  because unbiased)
  - Set of these should thus conform to standard normal distribution
- **Same method currently used in CARA daily and HIE reports**





# Large State Changes: Parameterization (2 of 3)

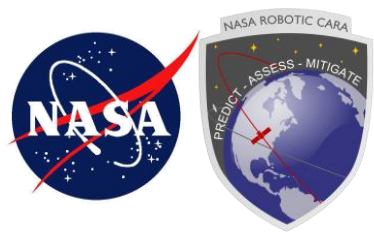
- **However . . . This is only true for the “diagonalized” situation, in which covariance axes and coordinate frame axes align**
  - Results meaningful only if ellipse closely aligns with coordinate axes
  - Once ellipse rotated, then component errors are correlated
    - Individual component error distributions no longer independent random variables
- **How often are covariance error ellipsoids naturally diagonalized?**
  - Not terrible assumption for individual satellites (primary, secondary)
  - More tenuous for combined situation (miss distance vs combined covariance)
- **Bottom line:  $\epsilon/\sigma$  statistics at the component level must be used with care**
  - When plotted against only positive axis, presume  $\epsilon/\sigma$  to be  $\text{abs}(\epsilon/\sigma)$



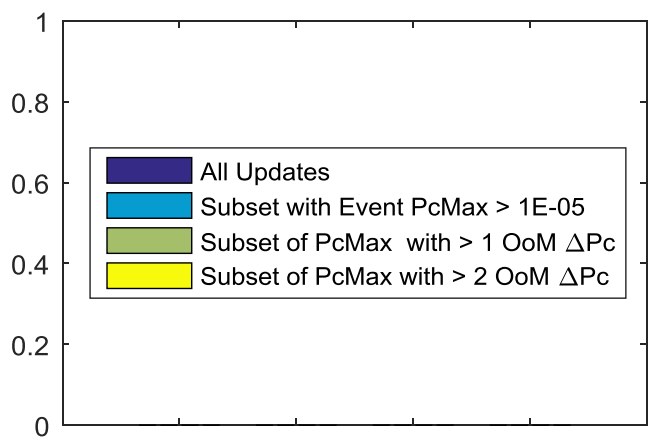
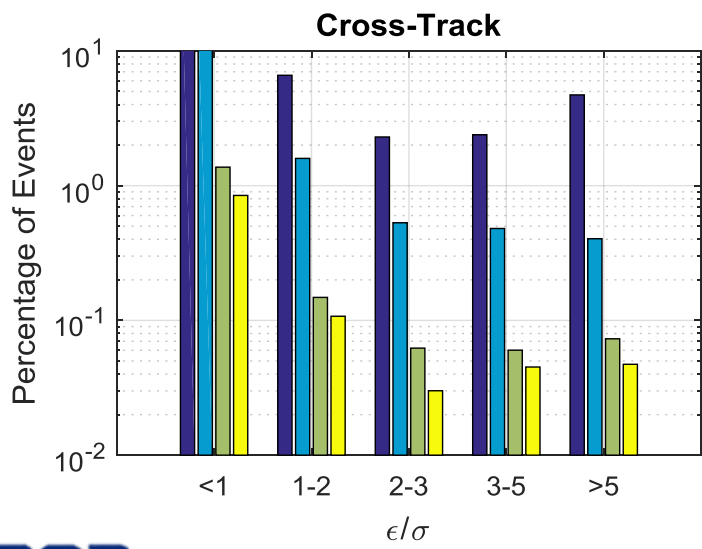
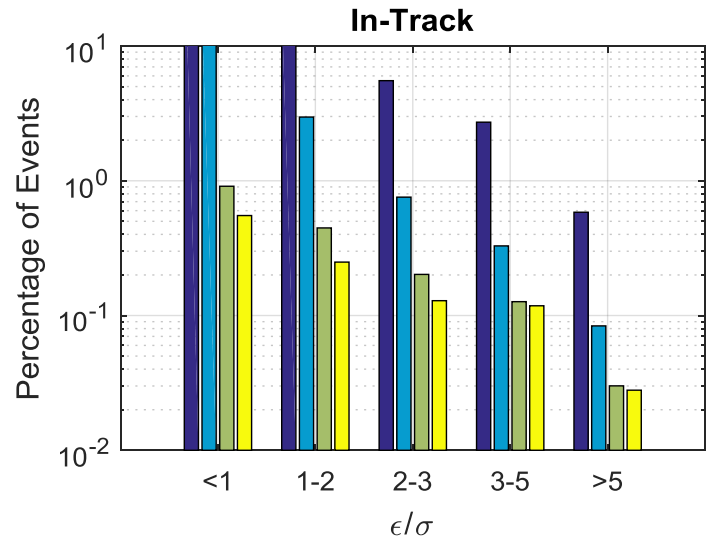
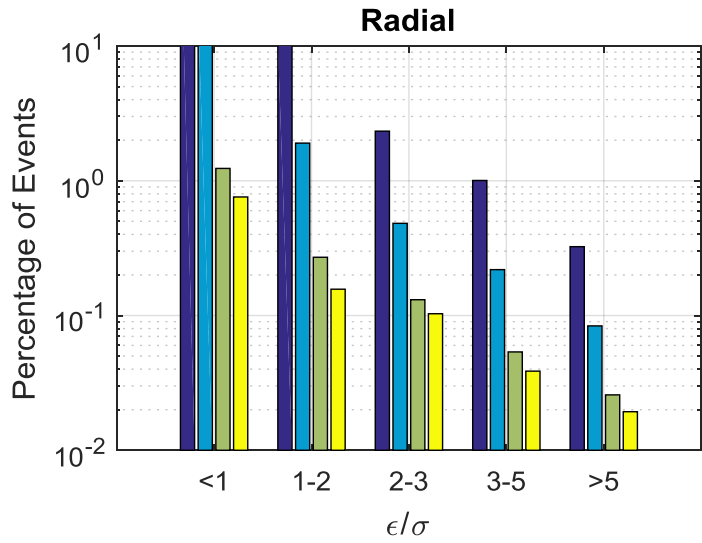
# Large State Changes: Parameterization (3 of 3)

- **Comparison alternative: Mahalanobis distance**

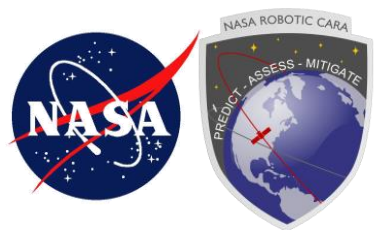
- If individual component errors normally distributed, then sum of squares of individual ratios ( $\epsilon^2/\sigma^2$ ) will constitute a 3-DoF  $\chi^2$  distribution
- Formulary  $\epsilon C^{-1} \epsilon^T$  properly considers all correlations and makes the calculation independent of coordinate system
- Approach less frequently encountered, so less intuition built up around result
- But will be supplied and examined along with Gaussian variables
- Can also examine 2-DoF situation for only radial and in-track
  - More information on this later



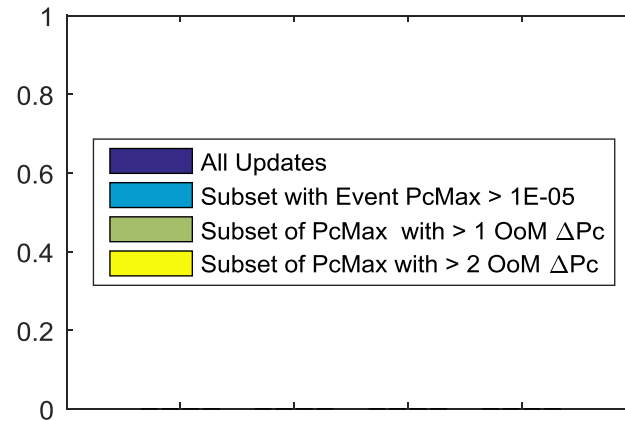
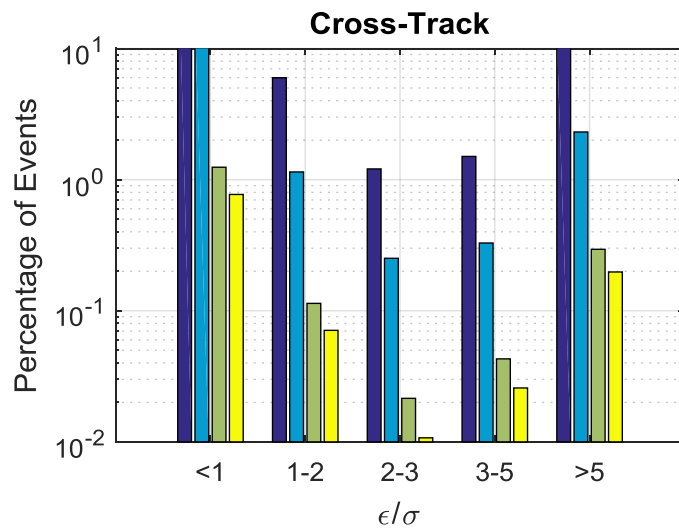
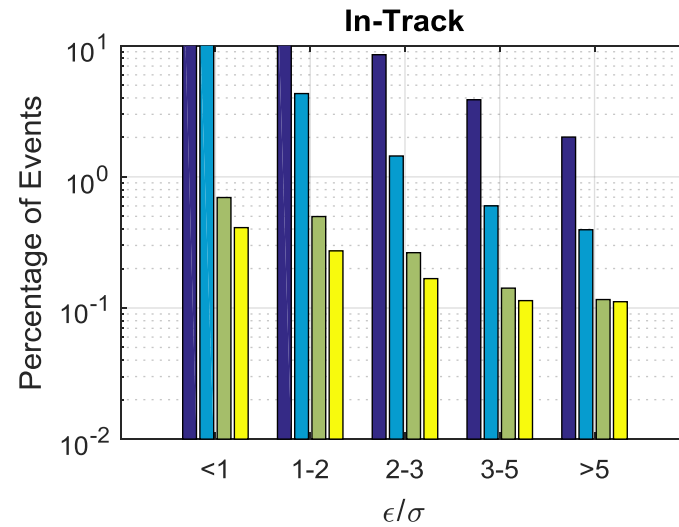
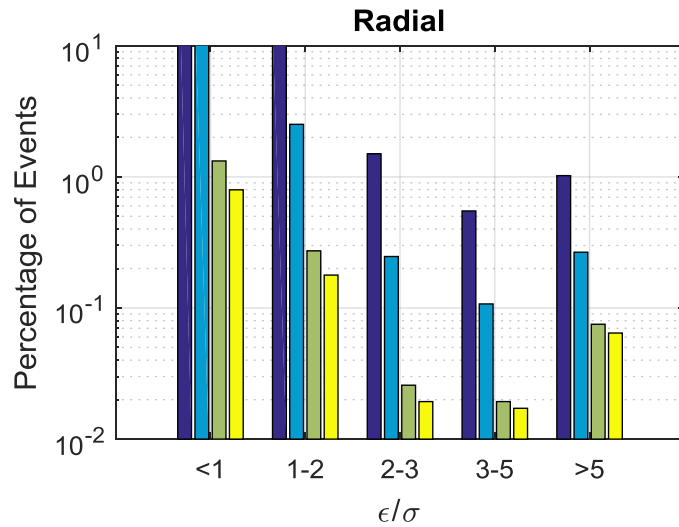
# Frequency of Large State Changes: Secondary Objects

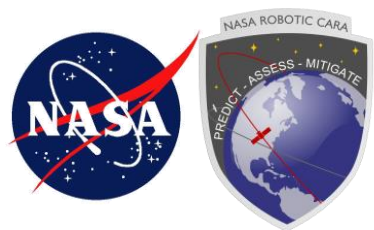






# Frequency of Large State Changes: Primary Objects





# Summary of Frequencies: Primary and Secondary Objects

- **Data summary**

- Table below reports situation for which  $\text{abs}(\epsilon/\sigma) > 3$

- **Commonly-known theoretical “percentages” for univariate Gaussian distribution consider two-tailed results**

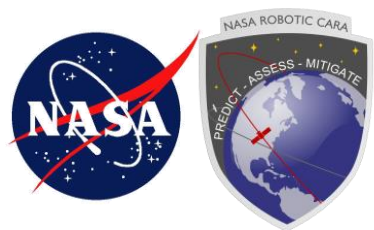
- 95.4% for 2- $\sigma$  distribution considers results from 2.3% to 97.7%
  - 99.7% for 3- $\sigma$  distribution considers results from 0.15% to 99.85%

- **Actual percentages for primaries surprisingly large**

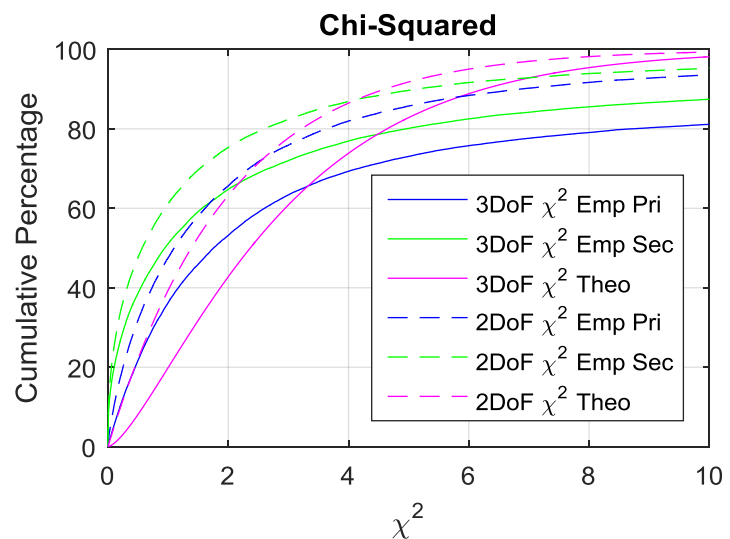
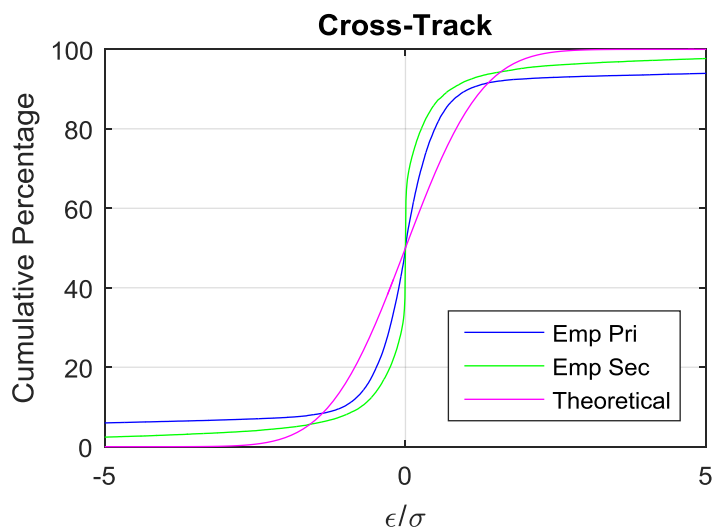
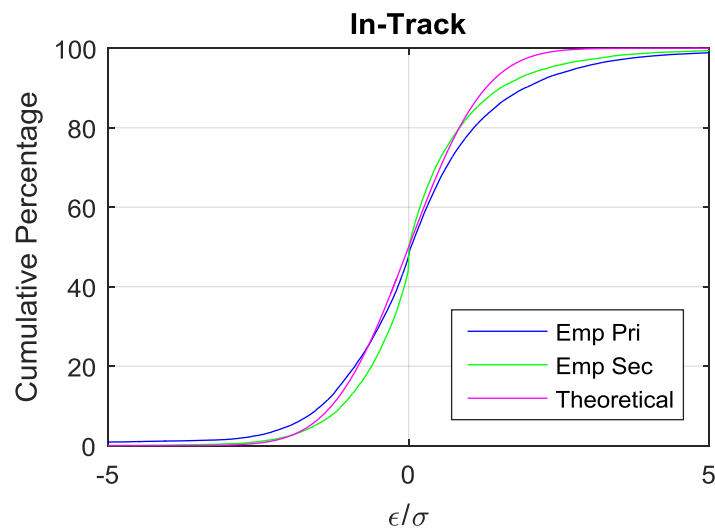
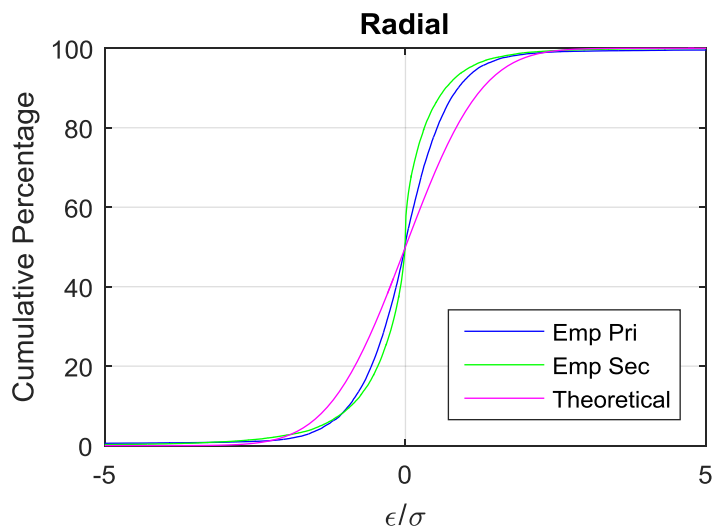
- Very similar for radial component; much larger differences with other two
  - Perhaps a little comfort in this, as radial generally most important component for CA

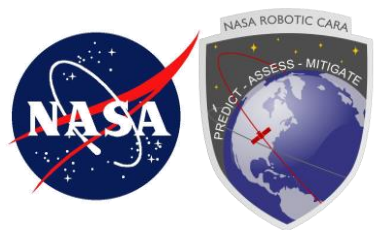
|             | Percent of Events in which $\text{abs}(\epsilon/\sigma)$ exceeds 3 |           |                     |           |                                  |           |                                  |           |
|-------------|--|-----------|---------------------|-----------|----------------------------------|-----------|----------------------------------|-----------|
|             | Overall  |           | Event $P_c > 1E-05$ |           | $> 1E-05$ & $\Delta P_c > 1$ OoM |           | $> 1E-05$ & $\Delta P_c > 2$ OoM |           |
|             | Primary  | Secondary | Primary             | Secondary | Primary                          | Secondary | Primary                          | Secondary |
| Radial      | 1.57   | 1.33      | 0.37                | 0.30      | 0.09                             | 0.08      | 0.08                             | 0.06      |
| In-Track    | 5.88   | 3.31      | 1.00                | 0.41      | 0.26                             | 0.16      | 0.23                             | 0.15      |
| Cross-Track | 13.53  | 7.10      | 2.64                | 0.88      | 0.34                             | 0.13      | 0.22                             | 0.09      |

**Overall, prevalence is greater than theory would predict. However, presence in events of significance notably reduced**



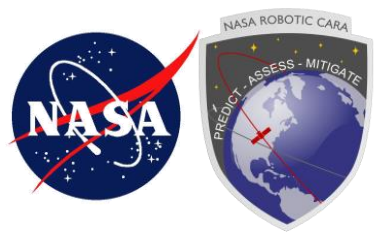
# Comparison of $\epsilon/\sigma$ to Theory: Primary and Secondary Objects





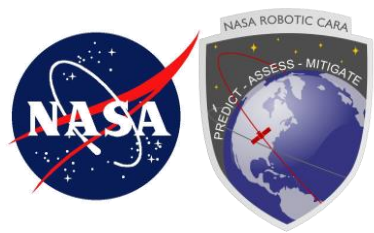
# Comparison of $\epsilon/\sigma$ to Theory: Interpretation

- **Radial behaves reasonably well—better than theory until more extreme part of tails reached**
  - Cannot see tail behavior very well in provided plots
- **In-track has non-theoretical distribution beyond about  $\epsilon/\sigma > 1$** 
  - As remarked previously, worse for secondaries than for primaries
- **Cross-track highly leptokurtic—peaked with very long tails**
  - Does not match a Gaussian distribution at all
- **In using chi-squared distribution, 2-DoF framework gives more sanguine situation**
  - Eliminates effect of large cross-track differences
  - Nonetheless, non-theory outliers dominate performance in the tails
- **None of these results sets match the theory particularly well**
- **Immediate conclusion difficult**
  - OD residuals suspected to be leptokurtic
  - Present trend could be extension of this

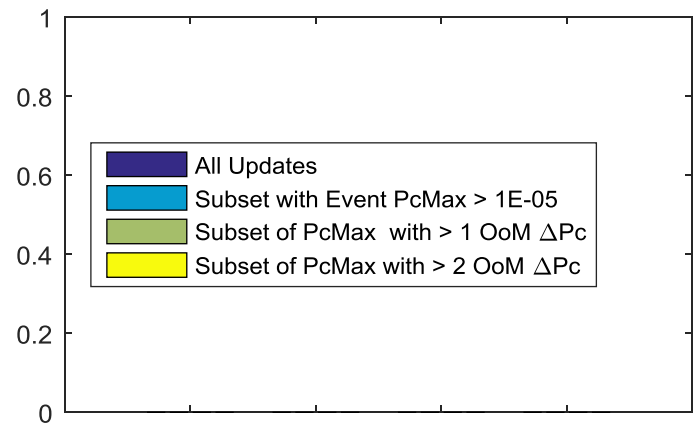
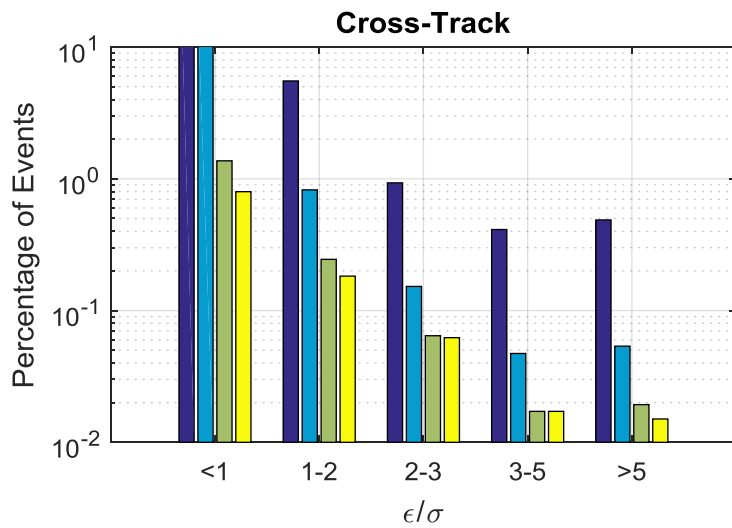
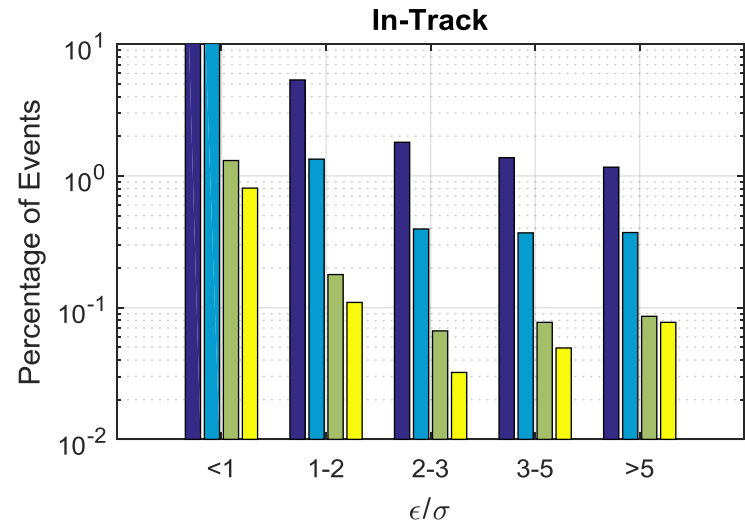
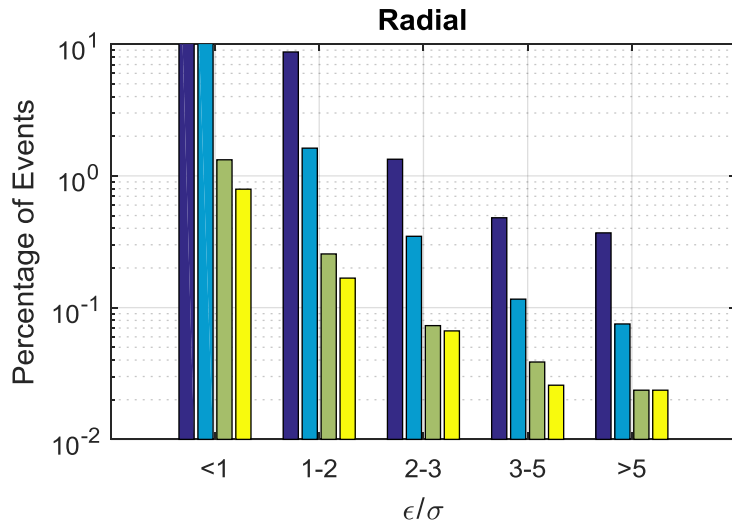


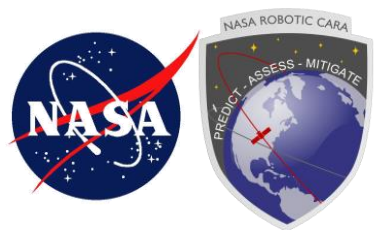
**Combined Situation**

# **STATE-CHANGE FREQUENCY AND COMPARISON TO THEORY**

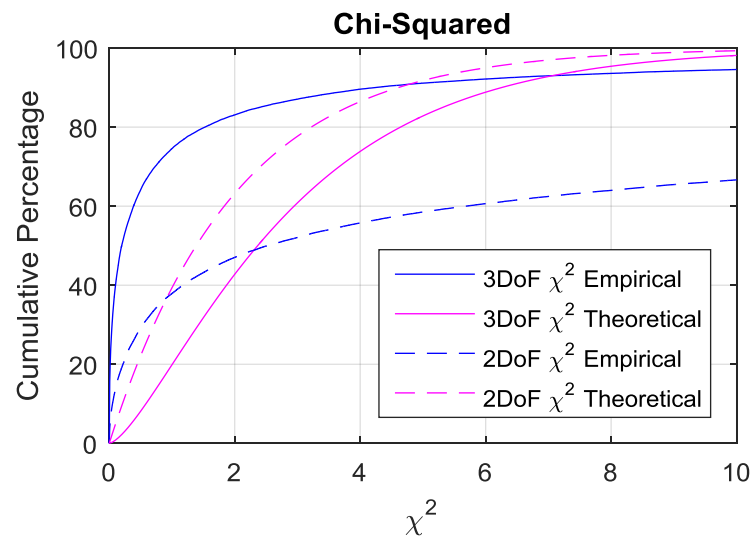
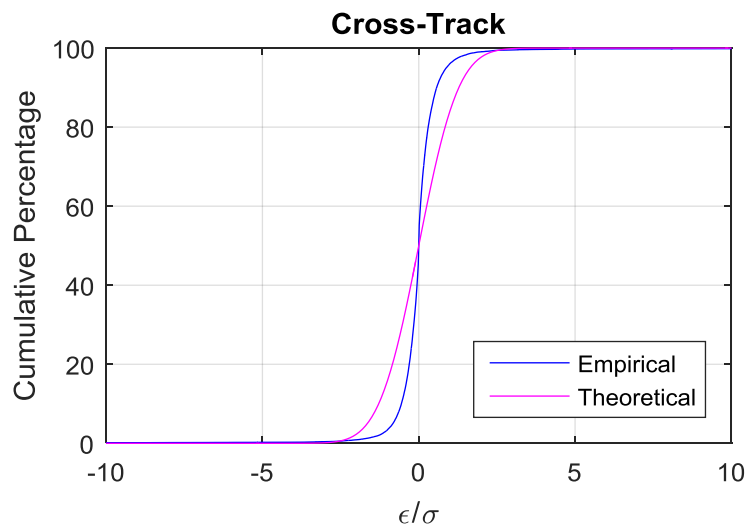
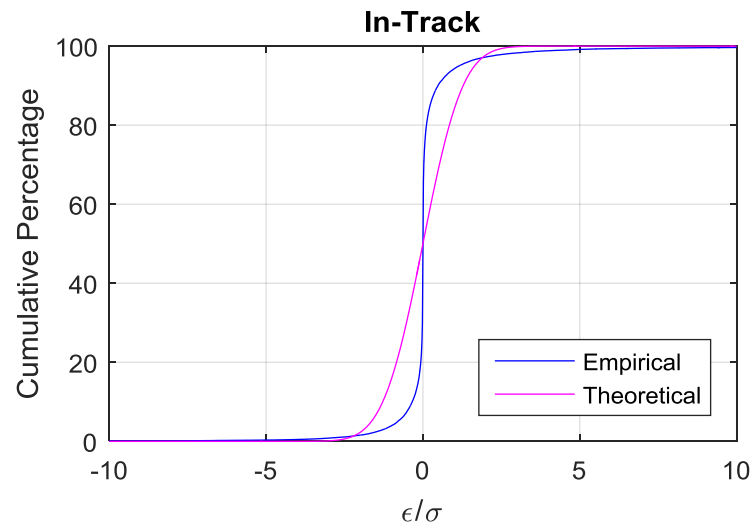
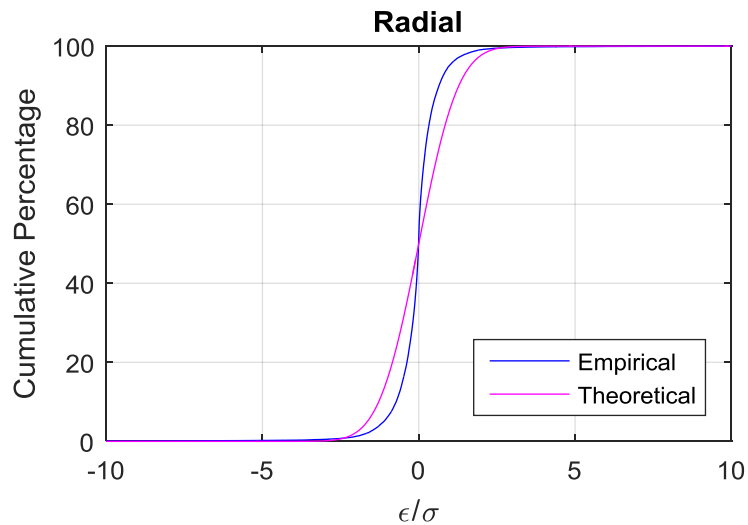


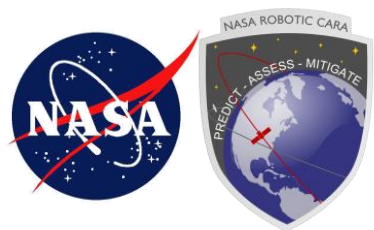
# Frequency of Large State Changes: Miss vs Combined Sigma





# Comparison of $\epsilon/\sigma$ to Theory: Miss Component vs Combined Sigma



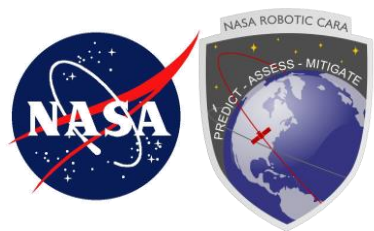


# Frequency of Large State Changes: Tabular Summary

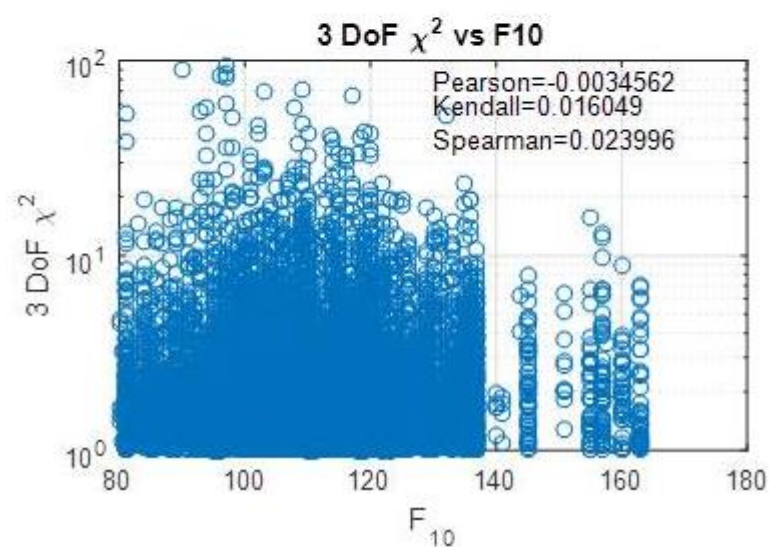
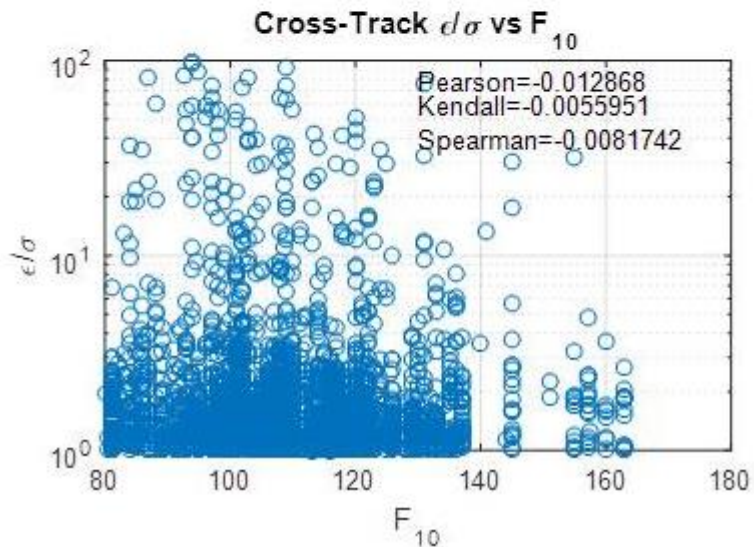
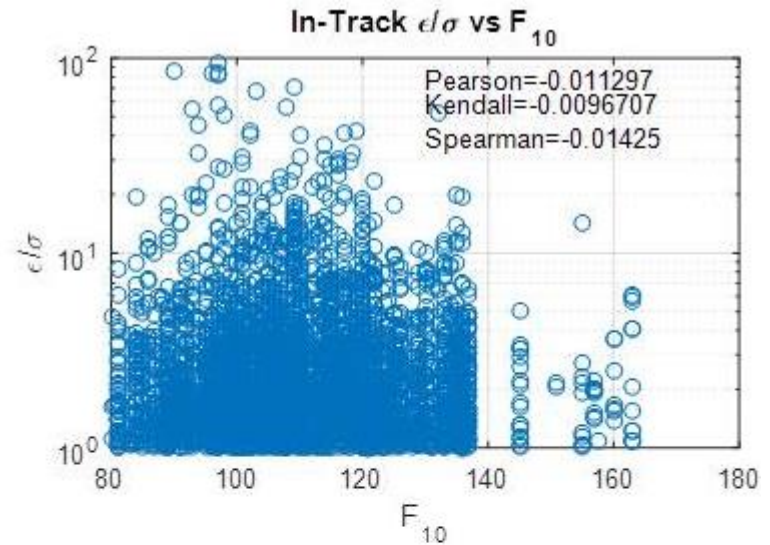
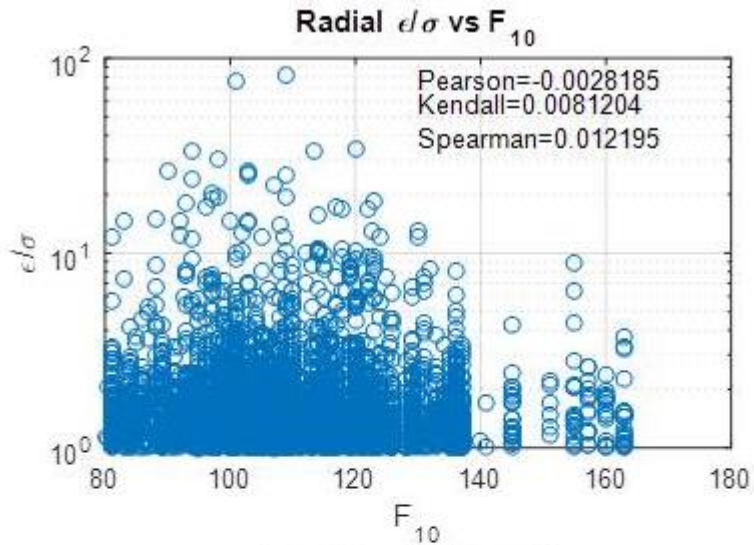
|             | Percent of Events in which $abs(\epsilon/\sigma)$ exceeds 3 |           |          |                     |           |          |                                  |           |          |                                  |           |          |
|-------------|---|-----------|----------|---------------------|-----------|----------|----------------------------------|-----------|----------|----------------------------------|-----------|----------|
|             | Overall   |           |          | Event $P_c > 1E-05$ |           |          | $> 1E-05$ & $\Delta P_c > 1$ OoM |           |          | $> 1E-05$ & $\Delta P_c > 2$ OoM |           |          |
|             | Primary   | Secondary | Combined | Primary             | Secondary | Combined | Primary                          | Secondary | Combined | Primary                          | Secondary | Combined |
| Radial      | 1.57  | 1.33      | 0.85     | 0.37                | 0.30      | 0.19     | 0.09                             | 0.08      | 0.06     | 0.08                             | 0.06      | 0.05     |
| In-Track    | 5.88  | 3.31      | 2.54     | 1.00                | 0.41      | 0.74     | 0.26                             | 0.16      | 0.16     | 0.23                             | 0.15      | 0.13     |
| Cross-Track | 13.53   | 7.10      | 0.90     | 2.64                | 0.88      | 0.10     | 0.34                             | 0.13      | 0.04     | 0.22                             | 0.09      | 0.03     |

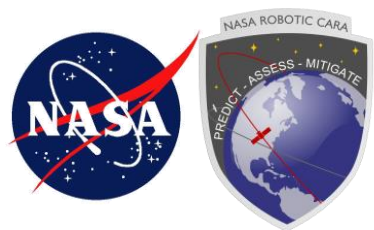
- **Values much closer to theoretical expectation, especially for radial and cross-track**
  - In-track is expected to be the most vulnerable to modeling errors, so not surprising that non-compliance largest in this component



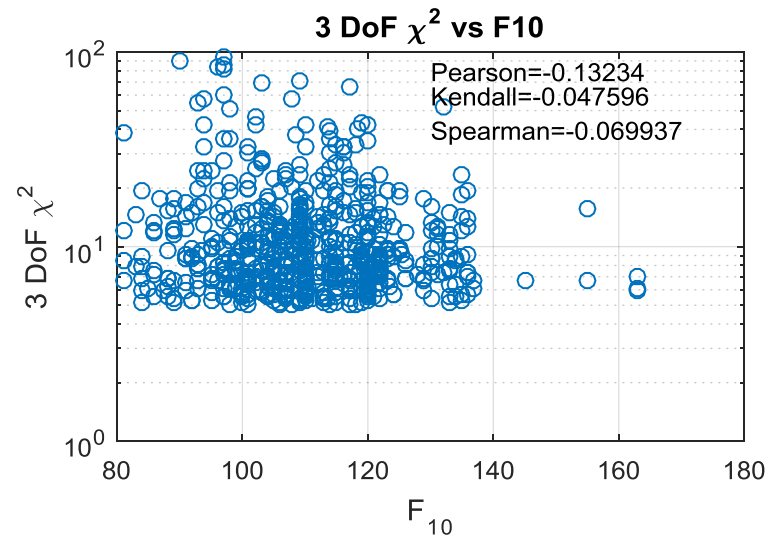
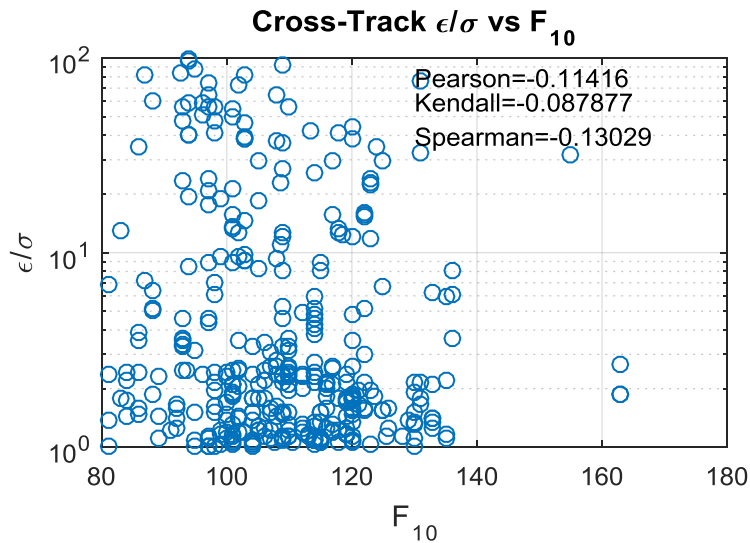
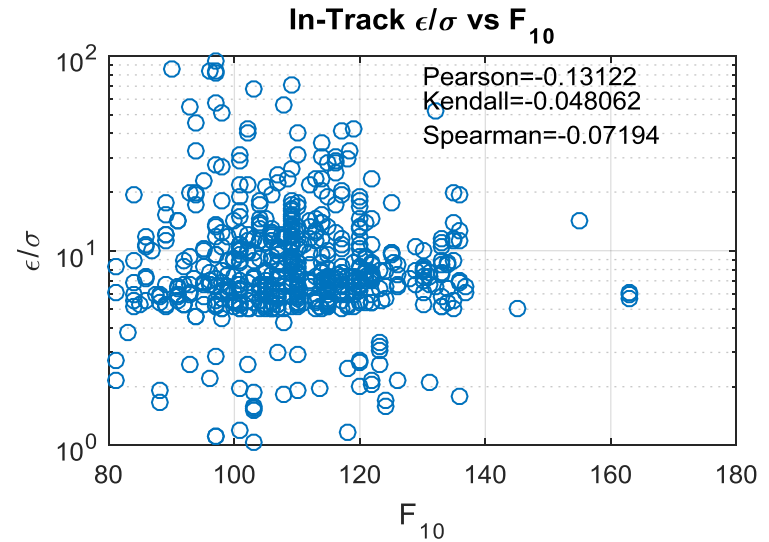
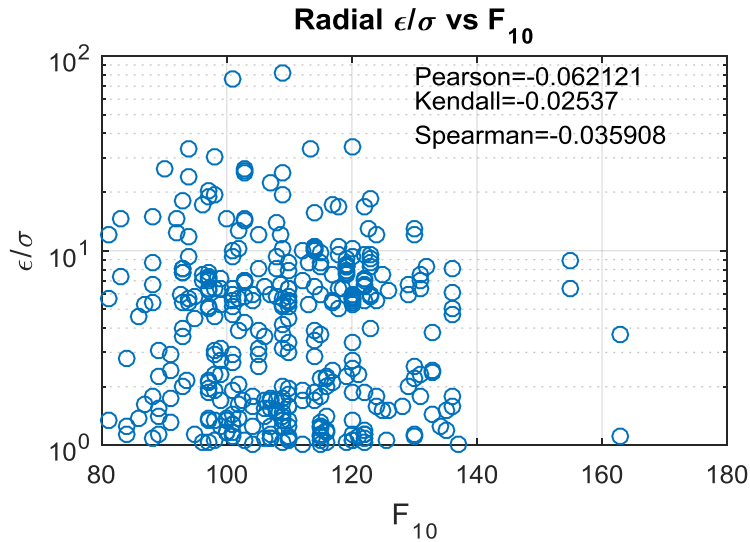


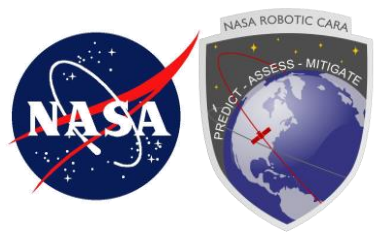
# Combined $\epsilon/\sigma$ vs Median $F_{10}$ : All Data





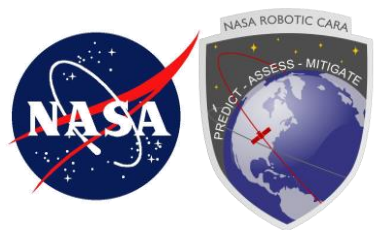
# Combined $\epsilon/\sigma$ vs Median $F_{10}$ : Any Component $\text{abs}(\epsilon/\sigma) > 5$





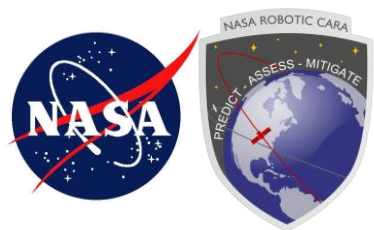
# Issues in Comparison to Theory

- **Commonly-known “percentages” for univariate Gaussian distribution consider two-tailed results**
  - 95.4% for 2- $\sigma$  distribution considers results from 2.3% to 97.7%
  - 99.7% for 3- $\sigma$  distribution considers results from 0.15% to 99.85%
- **Potential double-counting of large state changes**
  - Subsequent updates analyzed for large state change behavior
  - In a chain of updates, return to normalcy will appear as a second large change
  - Demarcation between one and two events not so easy to define (S = small state change; L = large state change)
    - S S L L S S – one or two events?
    - S S S L S S L S S – one or two events?
    - S S S S S S L – one or two events (would it have been counted as two if one more update had been available?)
  - For data-mining simplicity, all large changes counted, with the caveat that reported number might be twice as large as “actual” number



# Solar Storm Predictions: What are we Doing? (1 of 2)

- **CARA member of NASA LWS space weather expert panel**
  - Dr. Matt Hejduk as CA expert panel representative
  - Dr. Yihua Zheng as GSFC space physics representative, also representing mission interests
- **Purpose of panel to recommend NASA research investments to improve prediction and modeling**
  - Will issue formal report of recommendations by December, as well as accompanying journal article
  - Will attempt to focus at least part of recommendation to address JSpOC situation
- **Hope to leverage report to push state of the art at JSpOC**
  - However, from their perspective, a large investment was just made in atmospheric density prediction modeling; need to focus on other items



# Solar Storm Predictions: What are we Doing? (2 of 2)

- **Will investigate whether file update frequency can be accelerated**
  - Brief JSpOC on these results to show the problems that latencies create
    - See if there are mechanisms to improve efficiencies
  - Use SWTS function to determine whether such intervention is needed
    - Events that are not vulnerable to atmospheric density mismodeling would not require out-of-cycle updates
  - Would not have helped cases investigated here, as entire solar storms were missed
- **However, probably a fairly long time before there is much improvement with such scenarios**