

# Trajectory Design for a Cislunar CubeSat Leveraging Dynamical Systems Techniques: The Lunar IceCube Mission

AAS 17-286

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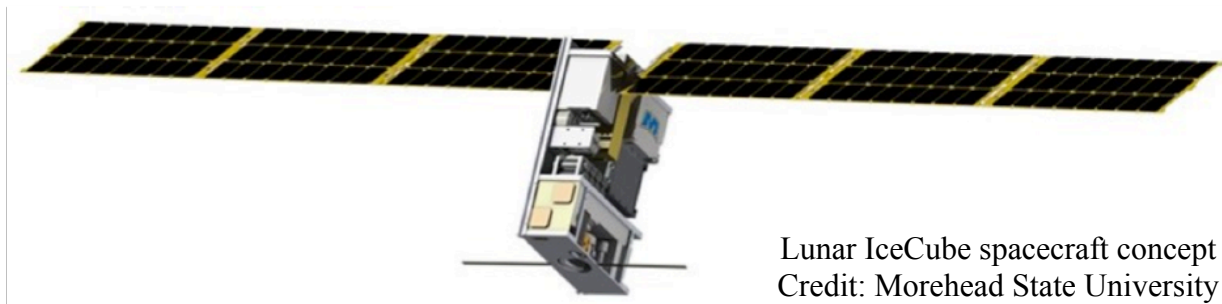
# Motivation

How to design complex path for CubeSat beyond LEO with limited propulsion and constrained deployment state?

- CubeSats: low-cost, rapidly-developed platform for exploration in cislunar space and beyond
- Deployment uncertainty and updates, limited propulsion create trajectory design challenges
- Leverage dynamical systems approach to construct framework for rapid and guided transfer design

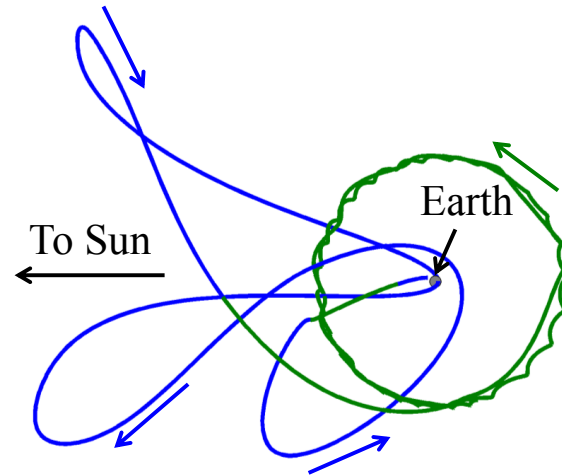
# Lunar IceCube

- 6U CubeSat led by Morehead State University
- Secondary payload on EM-1 (to launch in late 2018)
- Objective: observe water and lunar volatiles
- Lunar science orbit, highly inclined
- Busek Ion Thruster system,  $T = 0.9 \text{ mN}$ ,  $I_{sp} = 2500 \text{ s}$
- Initial spacecraft mass of 14 kg



Lunar IceCube spacecraft concept  
Credit: Morehead State University

# Trajectory Design Framework

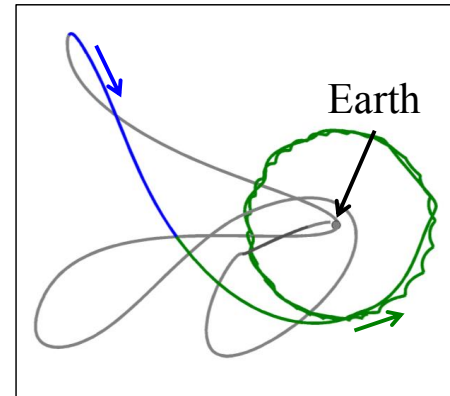
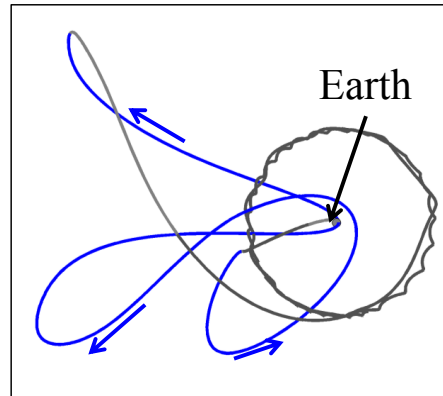
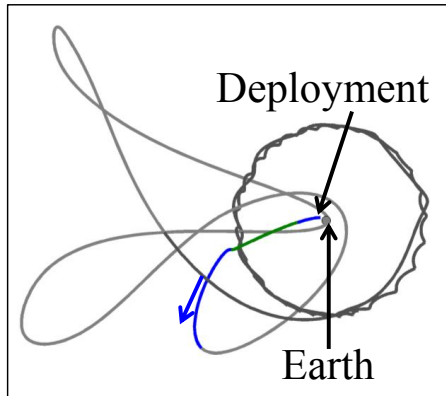


Transfer for original  
deployment state  
Credit: David Folta

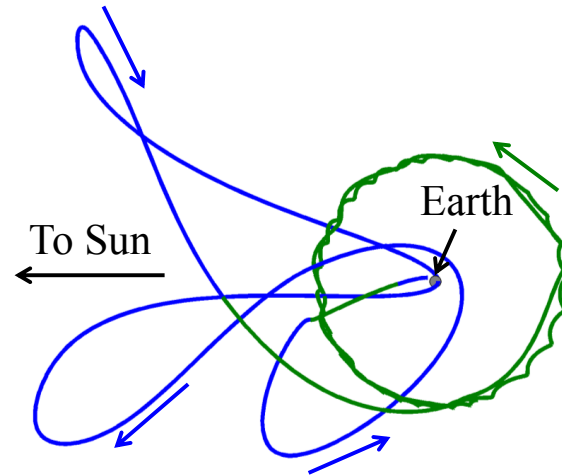
I: Earth Outbound

II: Phasing & Energy  
Adjustment

III: Lunar Approach  
& Capture



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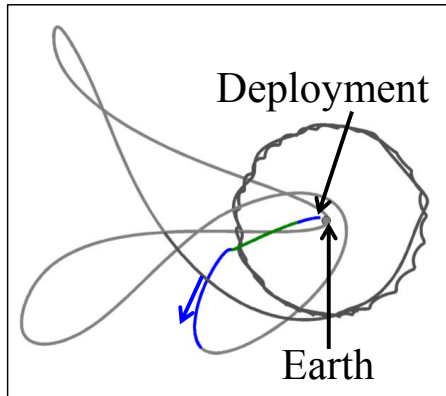


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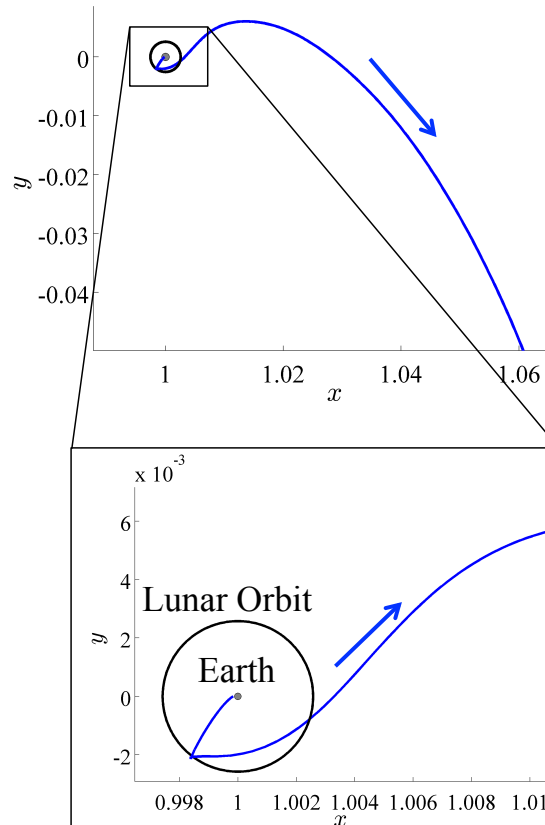


# Earth Outbound Segment

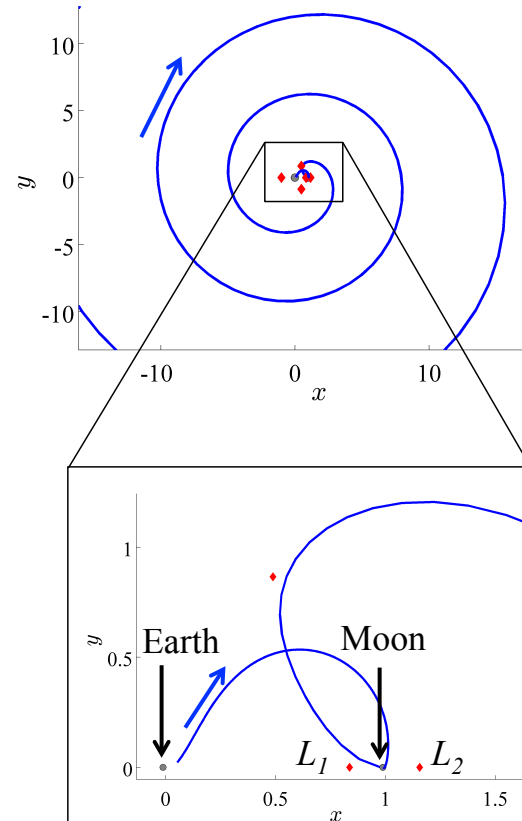
Naturally, trajectories would depart

Deployment:  
Oct 7, 2018

(a) Sun-Earth Rotating Frame



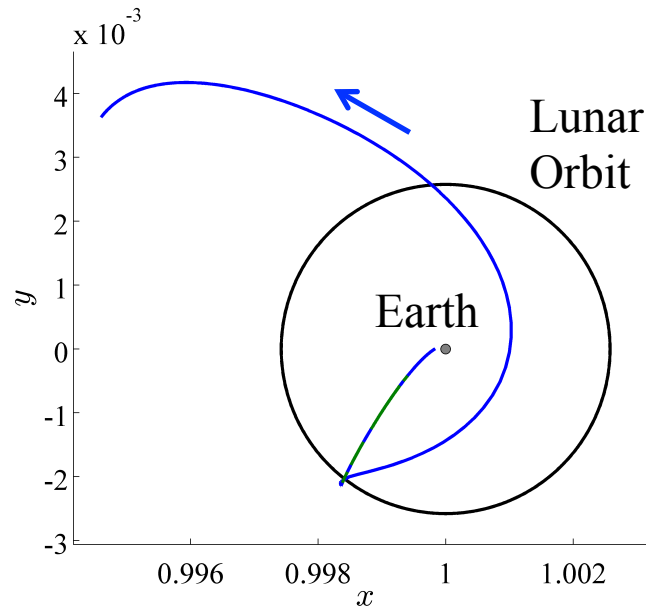
(b) Earth-Moon Rotating Frame



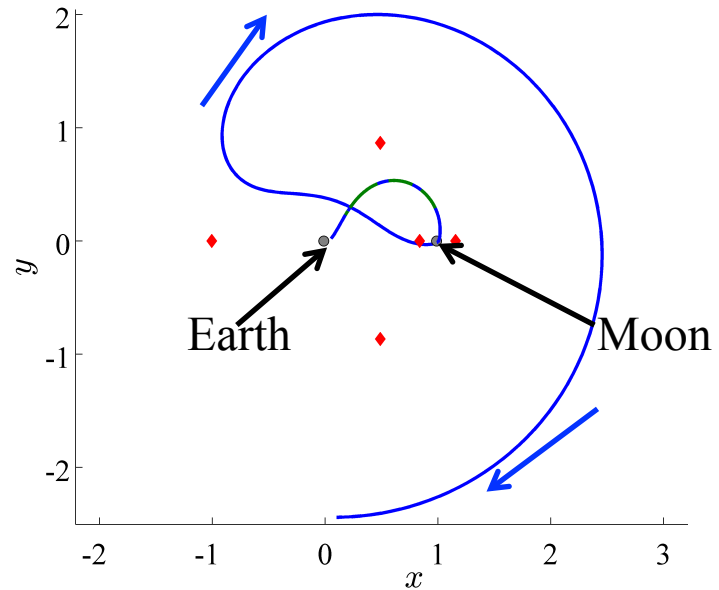
# Earth Outbound Segment

Low-thrust engine and lunar flyby prevents spacecraft from departing Earth vicinity

(a) Sun-Earth Rotating Frame



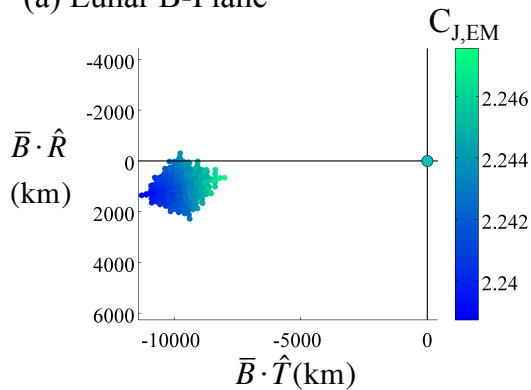
(b) Earth-Moon Rotating Frame



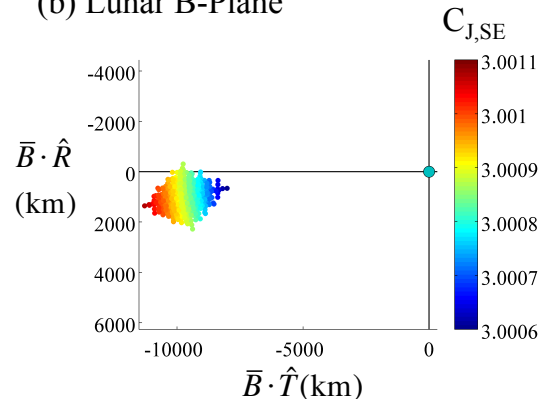
# Earth Outbound Segment

Pre-flyby thrust direction can be used to adjust flyby and apogee conditions

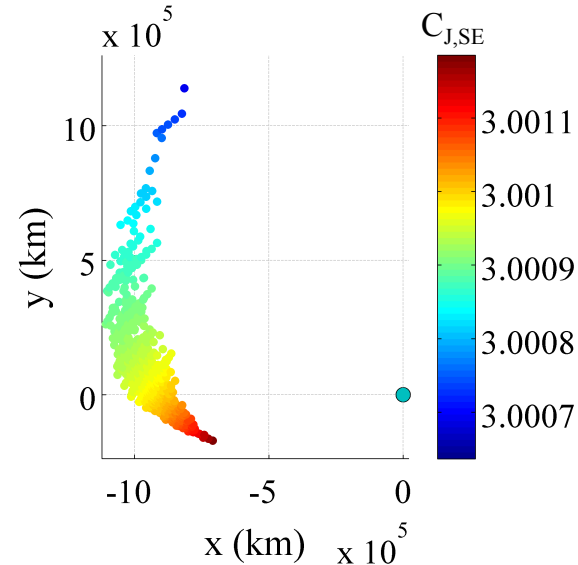
(a) Lunar B-Plane



(b) Lunar B-Plane

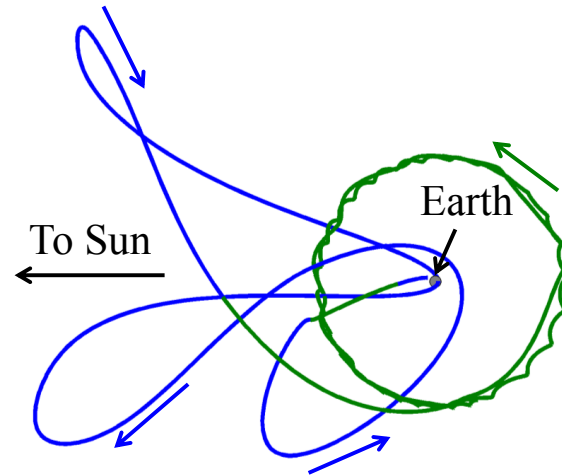


(c) Sun-Earth Rotating Frame



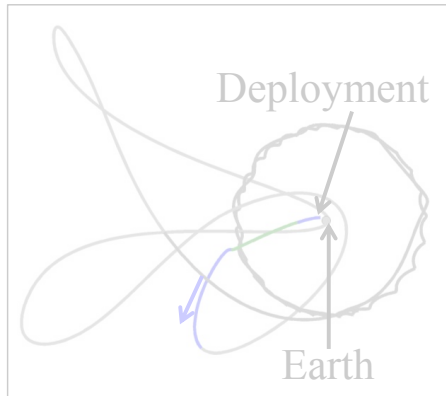


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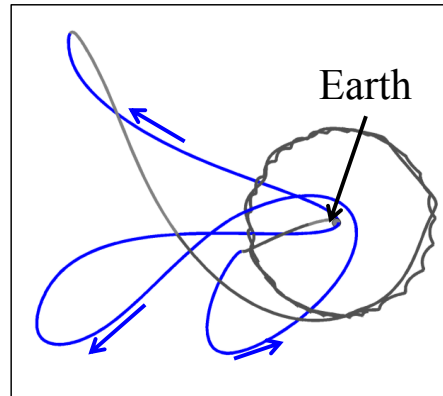


Transfer for original  
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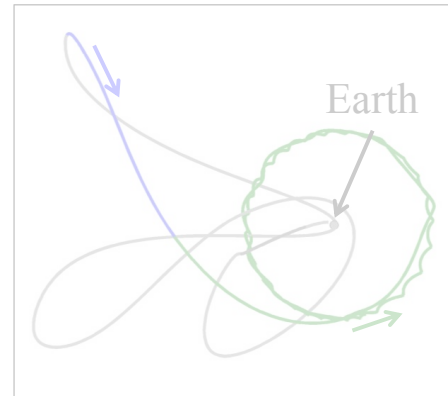
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II: Phasing & Energy Adjustment



III: Lunar Approach & Capture



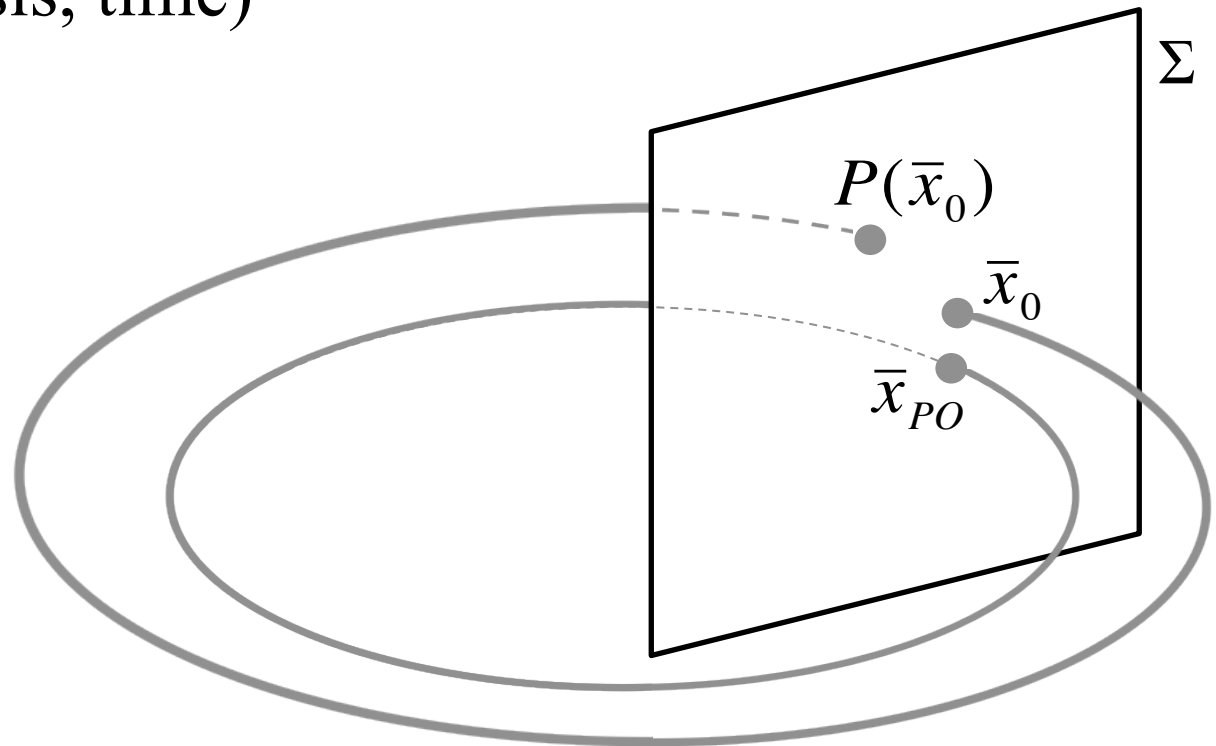
# Phasing and Energy Adjustment Segment

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- Identify connection between bounding segments
  - Leverage natural structures from Sun-Earth CR3BP
- Explore transfer arcs via apoapsis maps
  - Assume planar motion
  - Supports prediction of geometry, regions of existence
- Selected arc impacts TOF, communications feasibility

# Poincaré Mapping

Hyperplanes can take physical forms (e.g.  $y = 0$ ) or events (e.g. apsis, time)



Examples:

Koon, Lo, Marsden, Ross

Villac, Scheeres

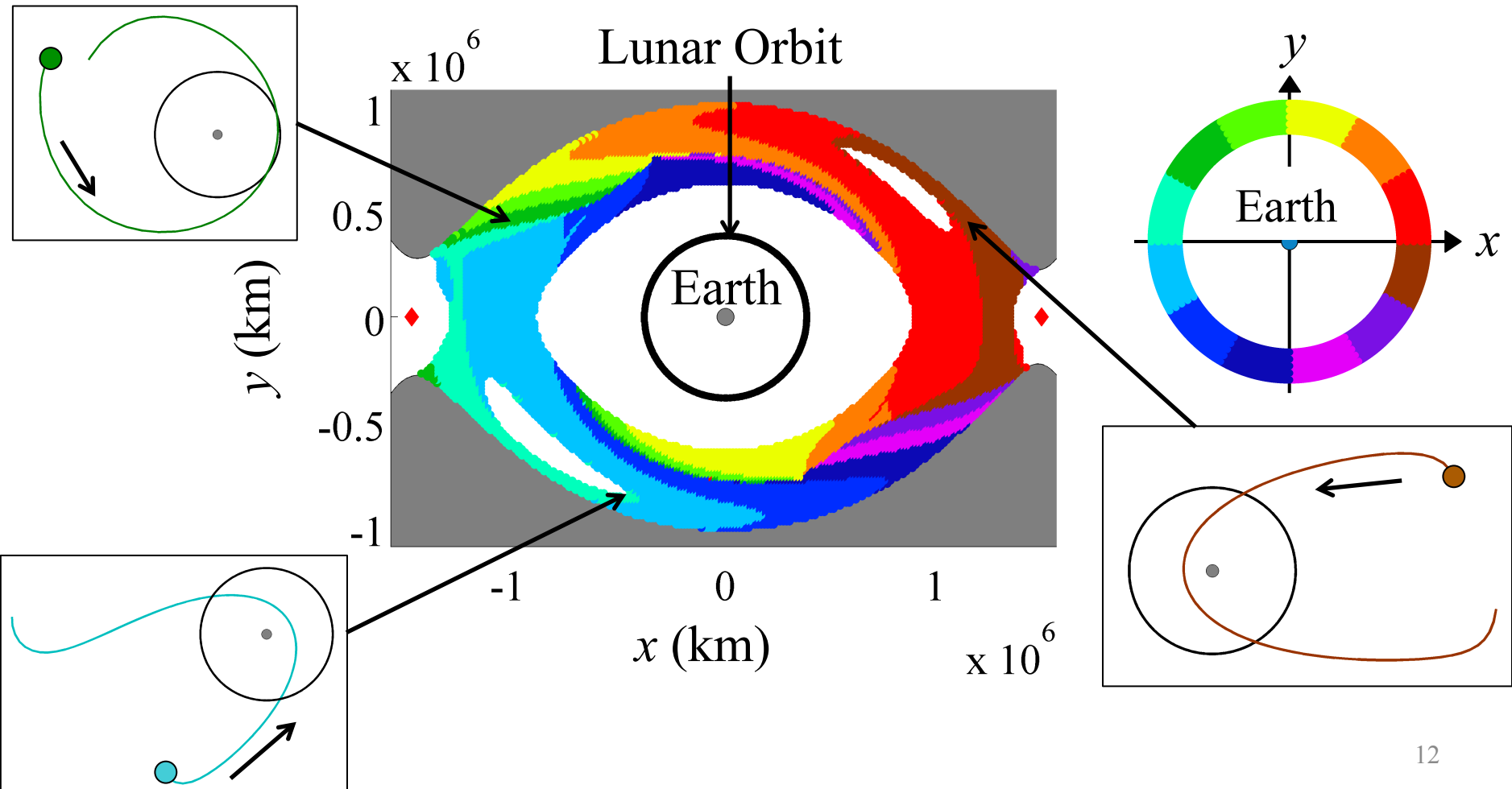
Paskowitz, Scheeres

Davis, Howell

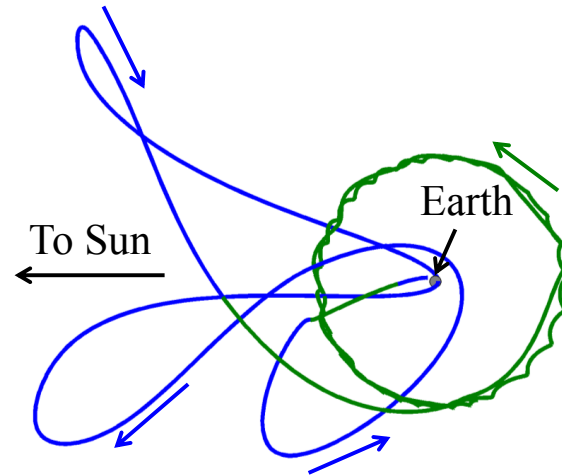
Haapala, Howell

# Apoapsis Map in Sun-Earth CR3BP, $C = 3.00088013$

Prograde initial conditions, encircle Earth once



# Trajectory Design Framework

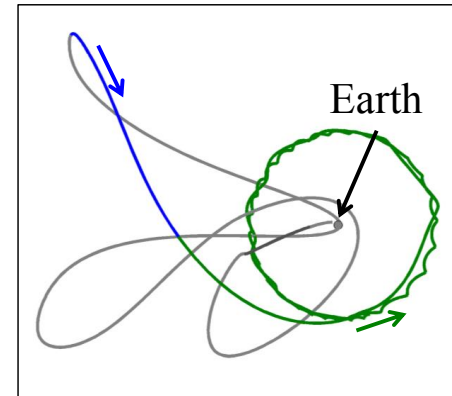
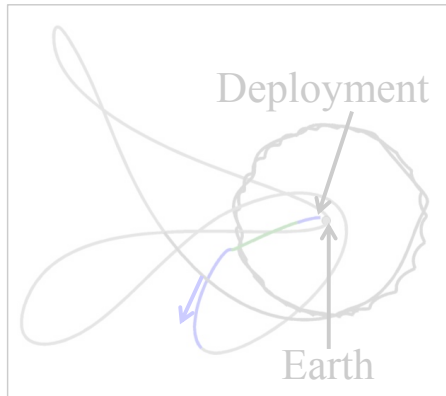


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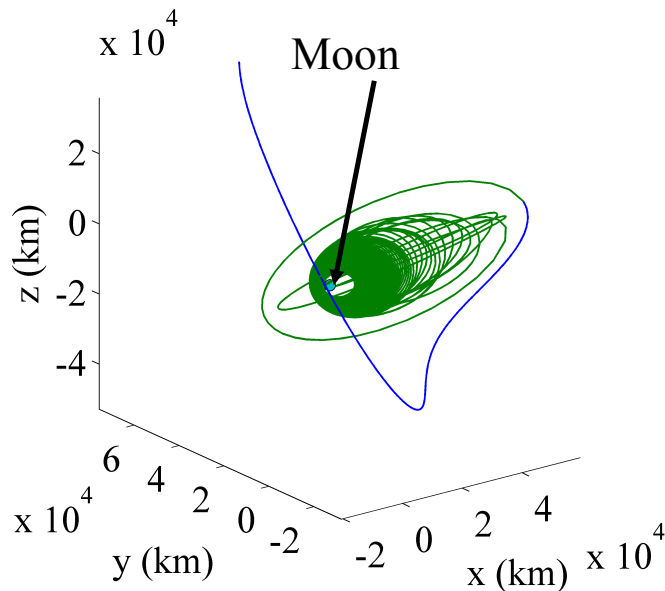
III: Lunar Approach  
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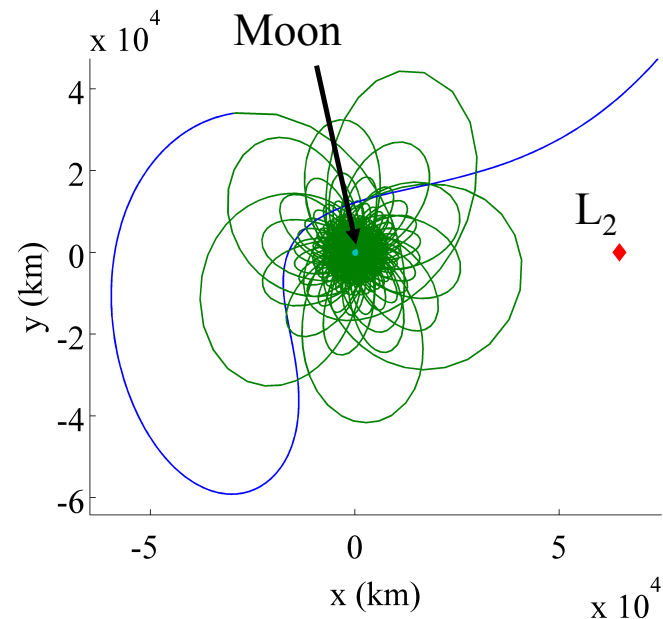
# Lunar Approach and Capture Segment

Generate approach arcs through application of manifold computation techniques

(a) Moon-Centered Inertial J2000 Frame

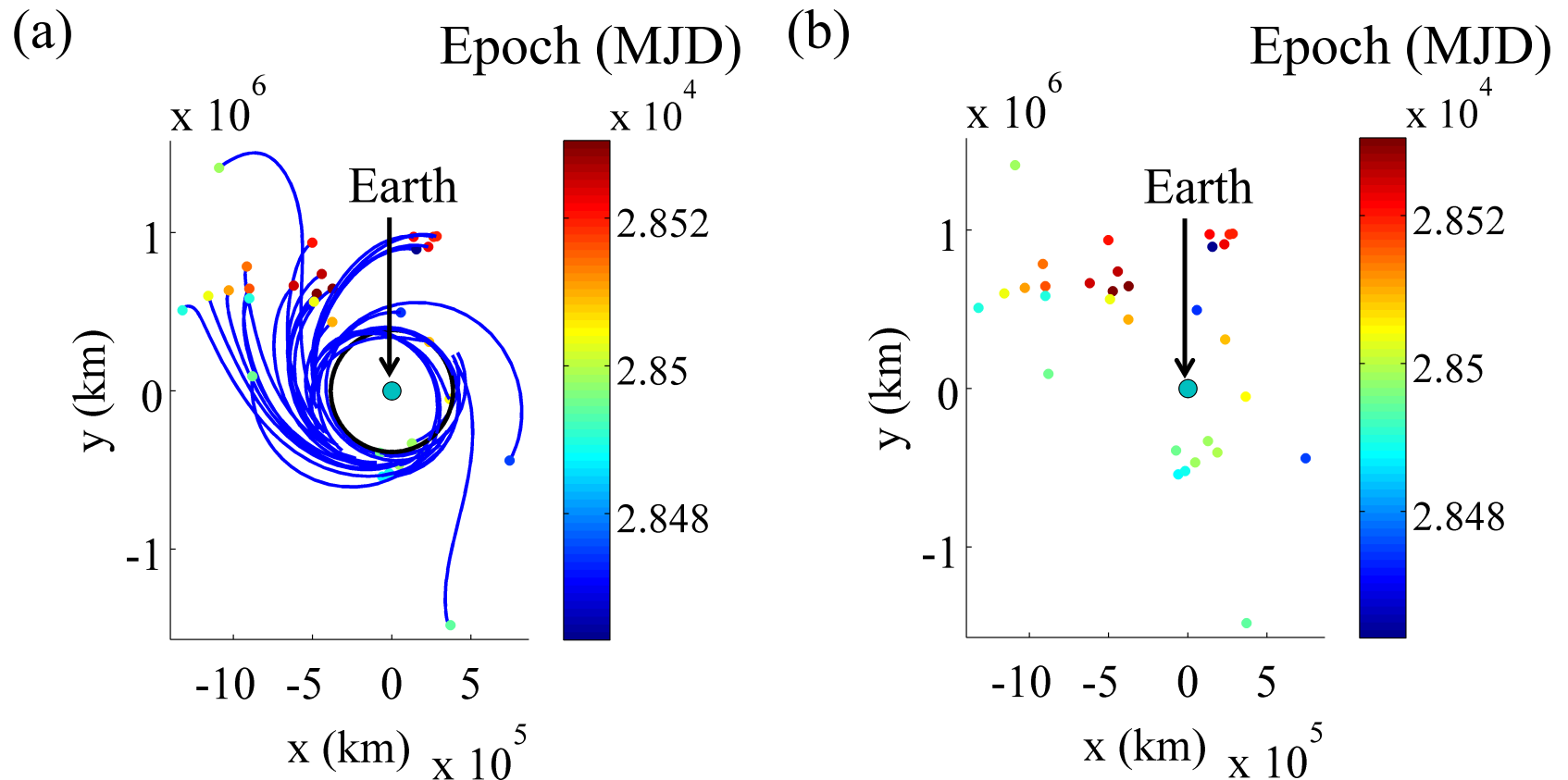


(b) Moon-Centered Earth-Moon Rotating Frame

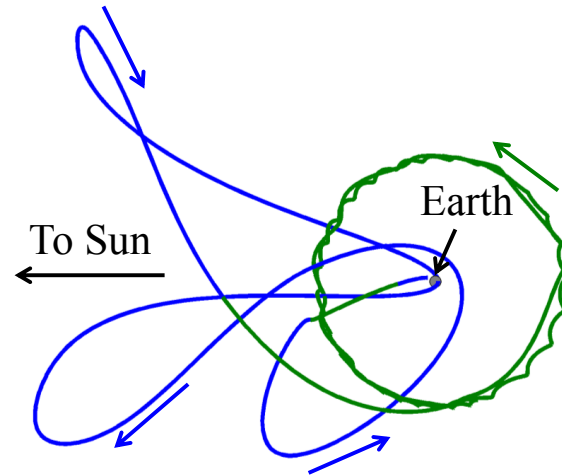


# Lunar Approach and Capture Segment

Visualize feasible approach arcs via mapping



# Trajectory Design Framework

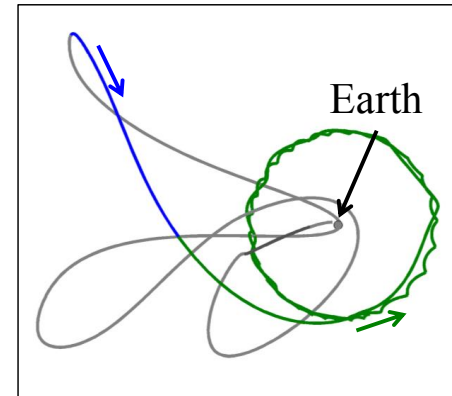
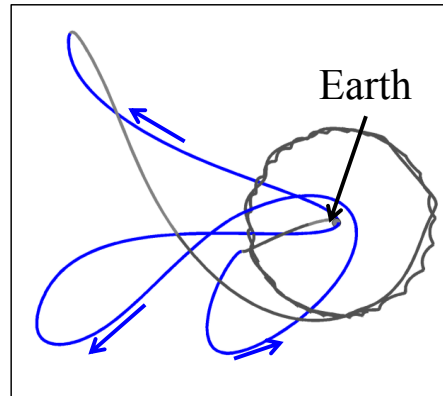
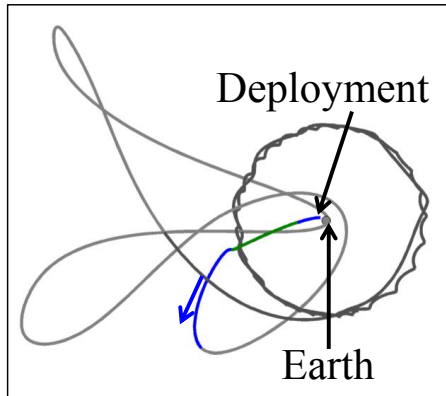


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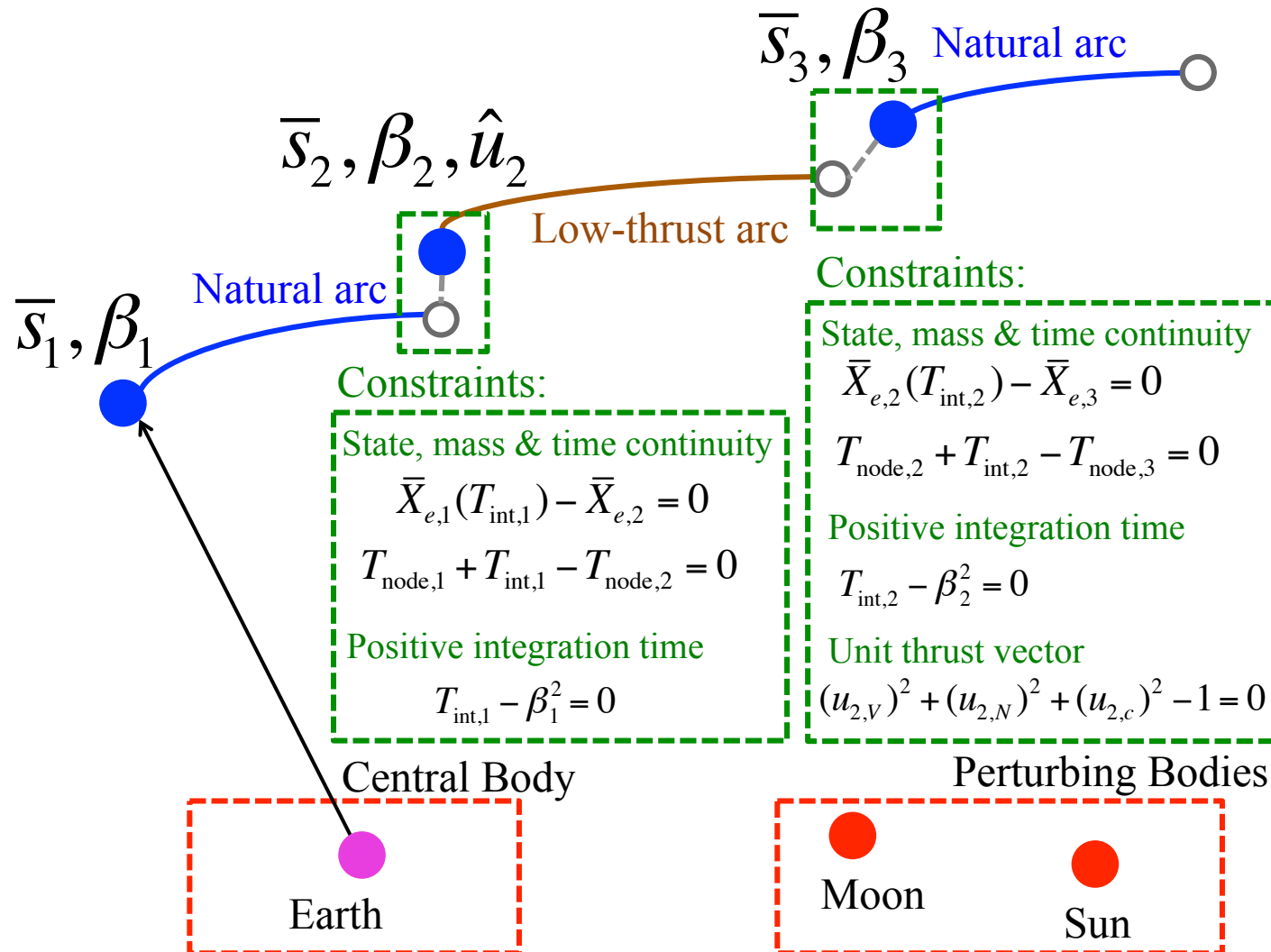
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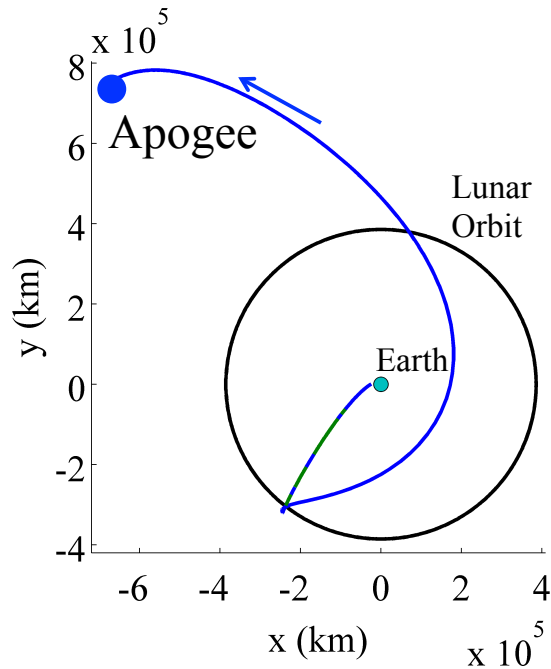


# Corrections Algorithm

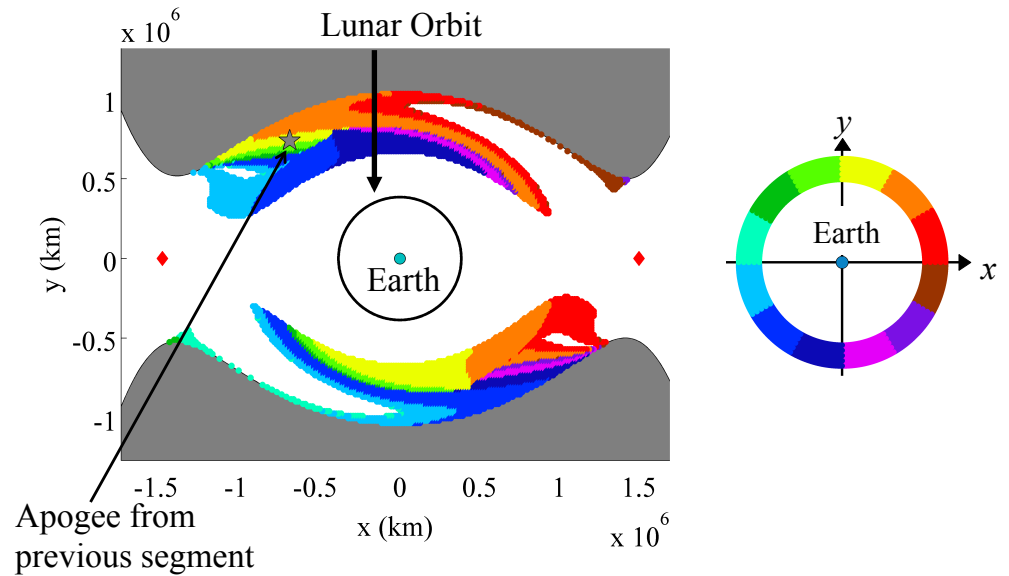


# Construction of Initial Guess Trajectory

1. Select Earth outbound arc  
Deployment: Oct 7, 2018

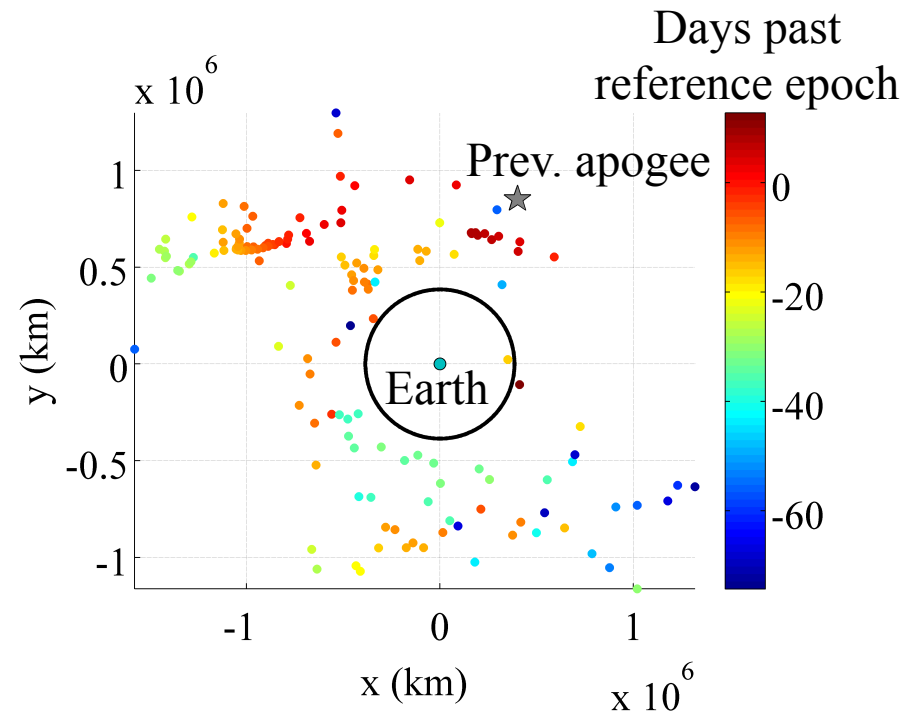
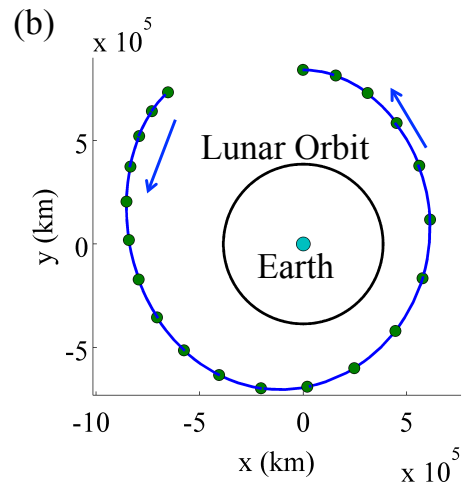
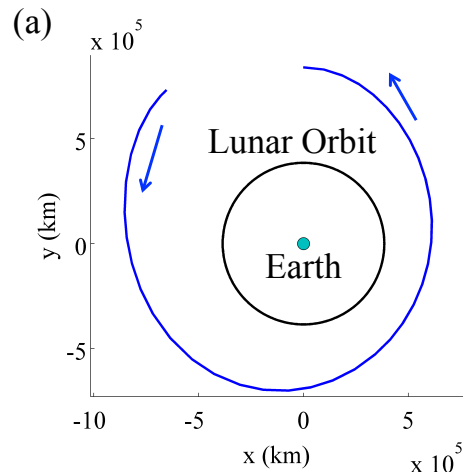


2. Select nearby phasing and energy adjustment arc



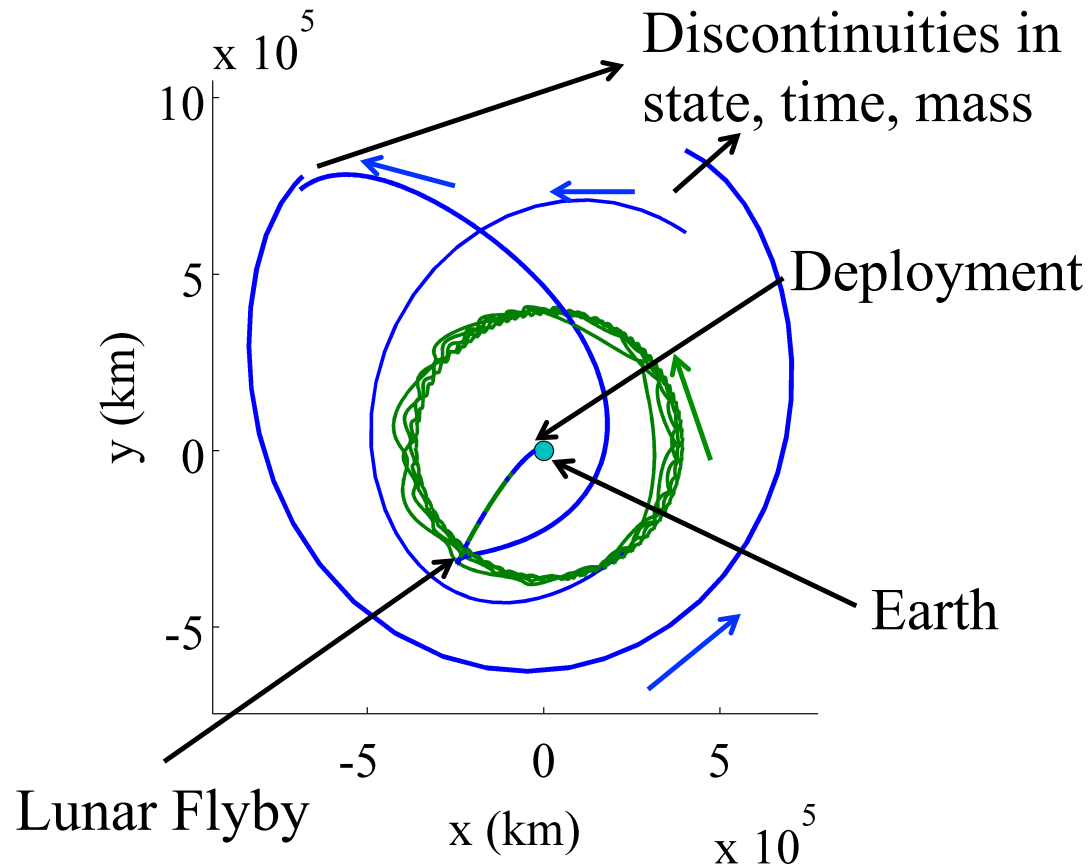
# Construction of Initial Guess Trajectory

3. Discretize initial guess from CR3BP      4. Select lunar capture arc nearby in  $(x,y)$  and epoch



# Construction of Initial Guess Trajectory

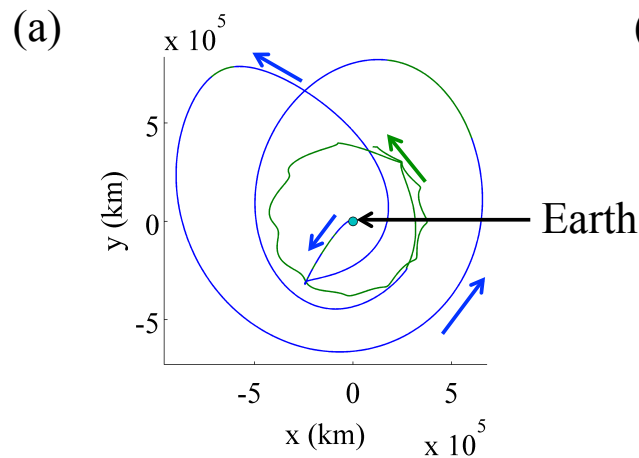
Assemble arcs, connect with short low-thrust arcs



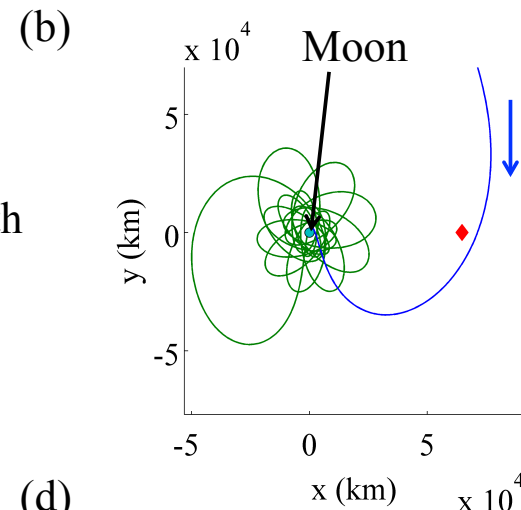
# Corrected Trajectory in Ephemeris

Dynamical model: Earth, Sun, Moon point masses; low-thrust

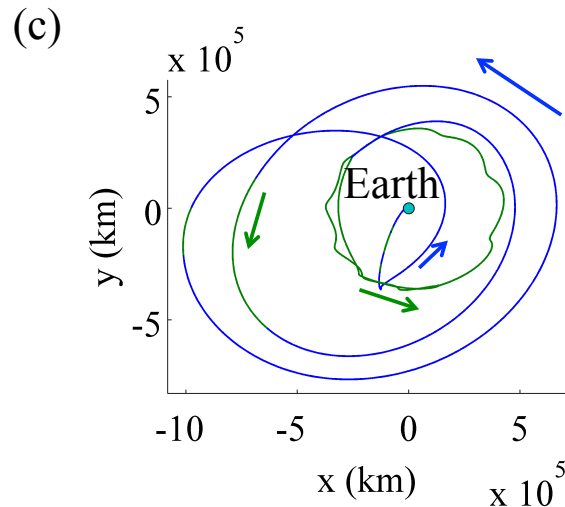
Earth-centered  
Sun-Earth  
rotating frame



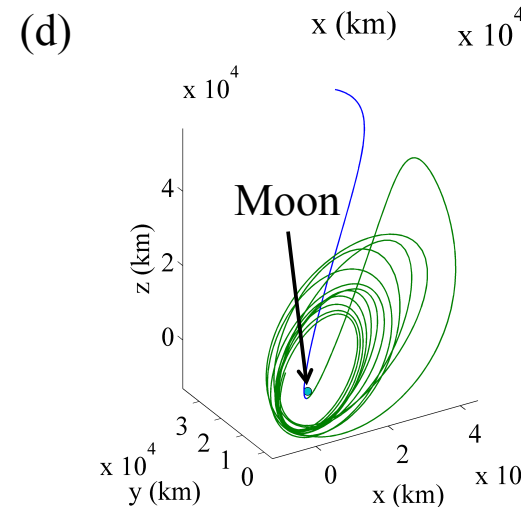
Moon-centered  
Earth-Moon  
rotating frame



Earth-centered  
inertial frame



Moon-centered  
inertial frame



# Trajectory Design Framework

How to design complex path for CubeSat beyond LEO with limited propulsion and constrained deployment state?

- Poincare mapping enables identification of individual transfer arcs to assemble initial guess
- Natural particular solutions offer:
  - Initial guess to connect bounding segments
  - Insight into bounds on motion, transfer geometry
- Supports well-informed and rapid evaluation of complex trajectory design space prior to higher-fidelity analysis

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