

Meta-shell Approach for Constructing Lightweight and High Resolution X-Ray Optics

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Abstract— Lightweight and high resolution optics are needed for future space-based x-ray telescopes to achieve advances in high-energy astrophysics. Past missions such as Chandra and XMM-Newton have achieved excellent angular resolution using a full shell mirror approach. Other missions such as Suzaku and NuSTAR have achieved lightweight mirrors using a segmented approach. This paper describes a new approach, called meta-shells, which combines the fabrication advantages of segmented optics with the alignment advantages of full shell optics. Meta-shells are built by layering overlapping mirror segments onto a central structural shell. The resulting optic has the stiffness and rotational symmetry of a full shell, but with an order of magnitude greater collecting area. Several meta-shells so constructed can be integrated into a large x-ray mirror assembly by proven methods used for Chandra and XMM-Newton.

The mirror segments are mounted to the meta-shell using a novel four point semi-kinematic mount. The four point mount deterministically locates the segment in its most performance sensitive degrees of freedom. Extensive analysis has been performed to demonstrate the feasibility of the four point mount and meta-shell approach. A mathematical model of a meta-shell constructed with mirror segments bonded at four points and subject to launch loads has been developed to determine the optimal design parameters, namely bond size, mirror segment span, and number of layers per meta-shell. The parameters of an example 1.3 m diameter mirror assembly are given including the predicted effective area. To verify the mathematical model and support opto-mechanical analysis, a detailed finite element model of a meta-shell was created. Finite element analysis predicts low gravity distortion and low thermal distortion. Recent results are discussed including Structural Thermal Optical Performance (STOP) analysis as well as vibration and shock testing of prototype meta-shells.

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1. INTRODUCTION

Advancements in x-ray optics fabrication technologies are required to enable future discoveries by space-based x-ray telescopes [1]. While both lightweight and high resolution mirror fabrication technologies exist, no spaceflight proven technology currently achieves both at once. Lightweight and relatively low cost mirror assemblies have been constructed for both the Suzaku and NuSTAR missions, with relatively low resolution of 110 arc-seconds half-power diameter (HPD) and 60 arc-seconds HPD respectively. The low mass of the optics allows for large photon collecting area at the expense of focusing performance. Mission such as Chandra and XMM-Newton have achieved superior angular resolutions of 0.5 arc-seconds HPD and 15 arc-seconds HPD respectively with relatively small collecting area and at a very high cost. Suzaku and NuSTAR used thin segmented mirrors to achieve their low mass, while Chandra and XMM-Newton used relatively thick full shell optics to achieve their excellent resolution. A hybrid approach, called meta-shells, that combines the benefits of both lightweight segmented optics and stiff full shell optics is being pursued by the Next Generation X-ray Optics (NGXO) team at NASA GSFC with the goal of achieving better than 5 arc-second HPD resolution.

2. META-SHELL APPROACH TO MODULAR X-RAY OPTICS

Full shell versus segmented optics

The basic optical elements of current x-ray mirrors can be divided into two types: full shell mirrors, such as those used on ROSAT, Chandra, and XMM-Newton, and segmented mirrors such as those used for Suzaku and NuSTAR (see Figure 1). While full shell optics have advantages in stiffness, due to the full annulus, and integration, due to symmetry and reduced number of optics to integrate, they are not amenable to making lightweight and large area mirror assemblies due to the extreme thinness required. Thus far, full shell optics with a diameter greater than 1 m and a thickness less than 1 mm have not been successfully fabricated. For example, Chandra's largest shell was 1.2 m in diameter with a thickness of 23 mm [2]. For this reason, the majority of x-ray mirror technology development to enable future large collecting area missions such as Athena and X-Ray Surveyor focuses on thin segmented mirrors [3].

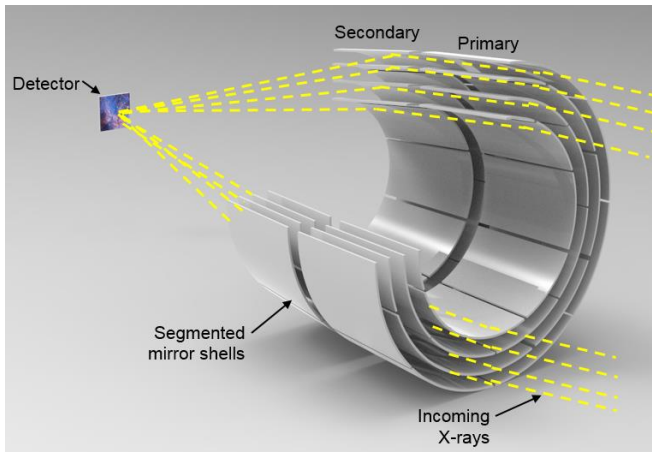


Figure 1 – Incoming X-rays are focused by concentric shells of mirror segments.

Wedge shaped modules versus meta-shells

Large mirror assemblies envisioned for future missions have typically been divided up both radially and azimuthally into many wedge shaped modules [4,5] as shown in Figure 2. This paradigm has the advantage of requiring many identical modules of modest size. However, it has distinct disadvantages. First, it sacrifices the rotational symmetry inherent in full shell optics leading to difficulty in establishing an optical axis and high sensitivity to roll misalignment (about the modules center of gravity) during module integration. Second, mounting to the module structure leads to over-constraint of the mirror segment which generates mounting distortion.

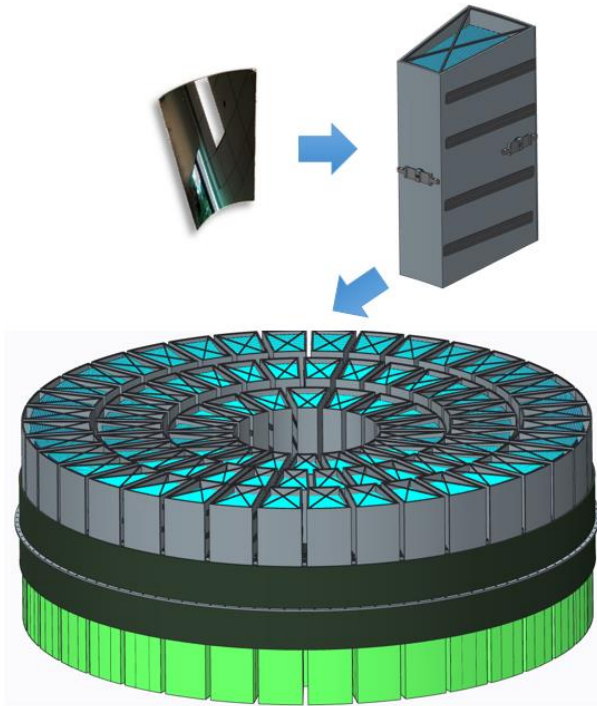


Figure 2 – Mirror assembly constructed from wedge-shaped modules.

The meta-shell approach divides the mirror assembly up radially, similar to Chandra, but with each radial division

containing dozens of optical shells rather than a single shell. Each radial element, or meta-shell, consists of a thick structural shell (non-optical) onto which many thin shells are layered in an interlocking pattern as shown in Figure 3. This paradigm has the advantage of creating a lightweight and stiff optic with a large collecting area. The meta-shell approach is similar to the construction of the NuSTAR mirrors [6] though it is designed to be scalable for larger mirror assemblies and differs in the particulars of the mirror segment mounting as described in Section 2.3 below. Additionally, the meta-shell is rotationally symmetric which simplifies aligning several meta-shells into a mirror assembly. The same approaches used to align and mount full shell optics for Chandra and XMM-Newton can be used with meta-shells. Finally, the continuous annular structure simplifies thermal design by allowing a conduction path through the structural shell as opposed to wedge-shaped modules which must be individually thermally controlled.

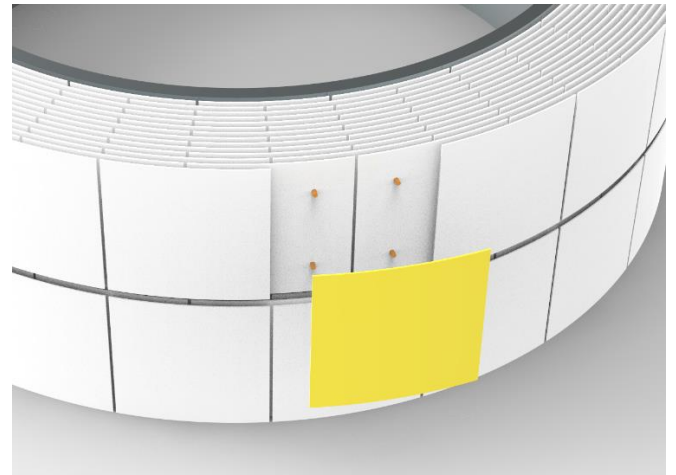


Figure 3 – Mirror segment (yellow) being integrated onto four posts (orange) to complete a meta-shell with overlapping layers of mirror segments mounted to a central structural shell (grey).

2.3 Four post kinematic mount

To minimize mirror distortion, a kinematic mount is desired. With a kinematic mount, the stress state is deterministic and the distortion due to gravity can be easily calculated and optimized using Finite Element Analysis (FEA). In comparison, an over-constrained mount can distort a thin mirror segment in ways that are difficult to predict and measure, since the sensitivity to displacement of over-constrained mounts can be as high as 35 arc-seconds HPD / μm [7]. To this end, a kinematic mount using four posts of a prescribed height has been developed.

As three points describe the location and orientation of a plane, so four points describe the location and orientation of a cylinder or cone. A mirror segment mounted on four points has its four most crucial degrees of freedom (dof) constrained, namely de-center (2 dof), pitch, and yaw. The remaining two degrees of freedom are roll, which has no effect on the focus quality due to rotational symmetry, and de-space, which is orders of magnitude less sensitive. Roll and de-space are constrained only by friction at the four posts and can easily be adjusted by nudging the mirror segment. Once the mirror is

so located, it can be bonded in place to a CTE matched structure (silicon in this case) with minimal distortion. Axially, the mounts are located at the Airy points to minimize axial distortion, and azimuthally the mounts are located at the 1/4 points to allow for staggered mounting of the subsequent layer of mirror segments as shown in Figure 3.

Gravity, which provides the nesting force needed to ensure the mirror contacts all four points, distorts the mirror by a predictable amount. The distortion of a 300 mm diameter silicon mirror segment with gravity acting radially, as during mounting to the meta-shell, is 2.2 arc-seconds HPD. If the mounted mirror is then turned 90 degrees, such that gravity acts azimuthally, the distortion reduces to 0.5 arc-seconds, allowing the mirror to be tested in a horizontal x-ray beam line. With gravity completely absent on orbit, only 0.2 arc-seconds of distortion, frozen in during the bonding process, remain. The minimal distortion of the four post mount has been verified experimentally as shown in Figure 4.

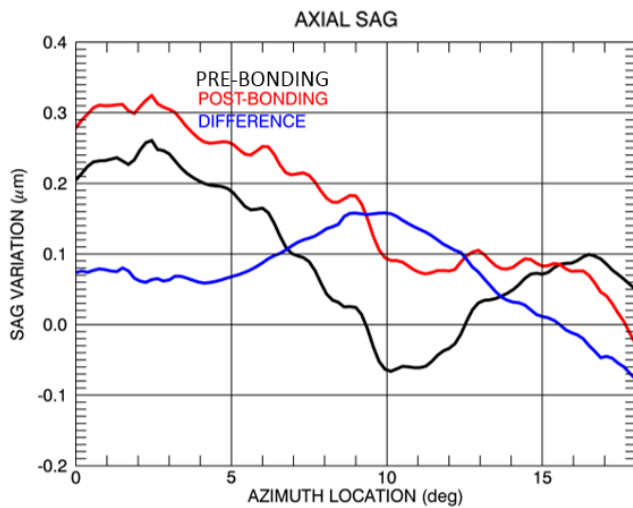


Figure 4 – The difference between the pre-bonded mirror figure and post-bonded mirror figure is within the metrology system repeatability of 0.15 μm .

Constructing a meta-shell

Constructing a meta-shell involves five major steps. First, the structural shell is fitted with temporary end-caps and mounted to an air bearing spindle. The axis of rotation defines the optical axis of the meta-shell. Second, posts are bonded to the structural shell to provide the mounting points for the first layer of mirror segments. To simplify alignment, both primary and secondary mirrors are mounted to the same structural shell. Third, the post heights are set using in-situ machining to the required tolerance. The post heights are verified by installing a mirror segment and checking its focus. Fourth, a layer of mirror segments are bonded on top of the posts. Steps two, three, and four are repeated for each layer of mirror segments. The number of mirror segments in a meta-shell is determined by the optical design and bond strength as described in Section 3 below. Finally, the temporary end caps are removed and the meta-shell is mounted to a Ground Support Equipment (GSE) structure for transportation, testing, and alignment into the mirror assembly.

Meta-shell mirror assembly

Several meta-shells can be aligned and bonded onto a carrier structure to form a mirror assembly. Proven techniques from Chandra and XMM-Newton have been adapted. Similar to XMM-Newton, the meta-shells, which combine primary and secondary mirrors, are mounted at the forward (primary mirror) end to a carrier structural with thin radial spokes called the spider [8] as shown in Figure 5. During integration they are supported by the GSE structure at the secondary mirror end where they can be manipulated for alignment. As with Chandra, alignment can be checked with a steerable auto-collimated beam at the focus which is retro-reflected off a flat mirror at the aperture [9]. Once aligned, the meta-shell is bonded to flexures allowing a radial degree of freedom, again following the Chandra approach [2].

The spider structure, being at the space-facing end of the mirror, can be used to mount stray-light baffles and can also be heated to provide a warm surface to radiate to the mirror segments. The completed mirror assembly includes the spider with mounted meta-shells, the interface ring to provide mounting for the telescope tube and spacecraft, and a thermal pre-collimator as shown in Figure 5. The thermal design is also adapted from Chandra and previous x-ray mission studies [10].

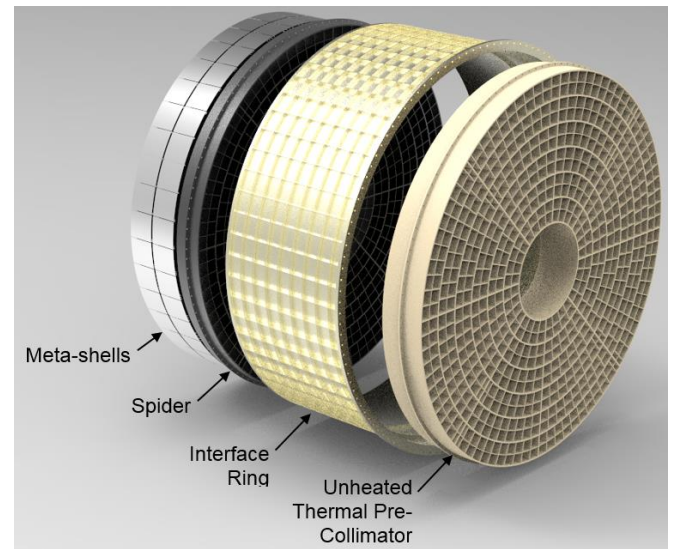


Figure 5 – Mirror assembly components.

3. META-SHELL STRUCTURAL ANALYSIS

To verify the feasibility of the meta-shell approach and to optimally size the meta-shell components, structural and opto-mechanical analysis has been performed to check the launch stress in the assembly, the distortion due to gravity, and distortion due to thermal gradients.

Bond strength versus meta-shell parameters

With hundreds of thin optical elements bonded onto the structural shell, the strength of the meta-shell when subject to launch loads is an obvious concern. Analysis shows that the weakest point in the design is the bond stress in the adhesive between the structural shell and the innermost mounting post where the load from all the subsequent cantilevered layers of

mirrors must be transferred. A mathematical model which calculates the adhesive stress at the bond joints was developed. The model calculates the shear, tensile, and bending stresses in the bond joint and finds the margin of safety based on a conservative safety factor of 3.0. Launch loads of 12.3 g axial and 3.4 g axial were applied based on the International X-Ray Observatory (IXO) mission study coupled loads analysis with a model uncertainty factor of 2.0 applied to the loads [7]. The meta-shell design parameters effecting the bond stress are (1) the diameter of the bond between the mirror segment / structural shell and mounting post (2) the azimuthal span of the mirror segment, which determines the number of bonds around the meta-shell circumference and (3) the number of mirror layers on the meta-shell, which determines how much load must be carried by the inner-most bonds. Based on these three parameters, the mathematical model was iterated to determine the feasible design region shown in Figure 6. Designs with parameters below the surface shown are feasible, while those above the surface have a negative margin of safety.

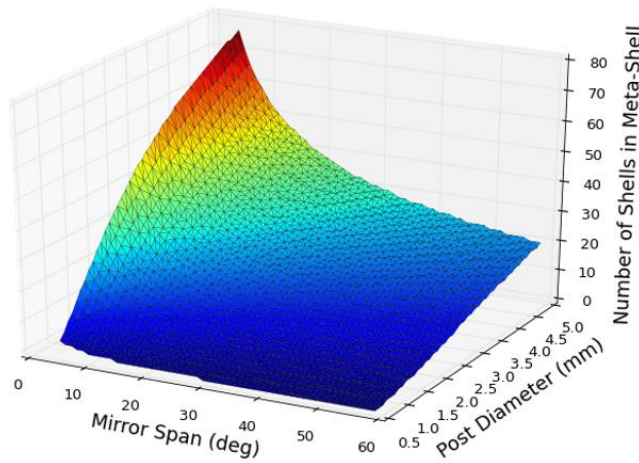


Figure 6 – Feasible designs for a 300 mm diameter meta-shell with various parameters. Designs with positive stress margins are below the plotted surface.

The three parameters must be traded against each other to develop an optimal design considering bond strength, mirror effective area, and manufacturability. Increasing the bond size increases the bond strength but blocks incoming x-rays, reducing the effective area. Decreasing the mirror span increases the bond strength but results in more mirror segments that must be fabricated and assembled into the meta-shell. Decreasing the number of layers per meta-shell increases the bond strength but reduces the effective area requiring additional meta-shells to be fabricated. An example of a feasible 1.3 m mirror assembly design using 0.4 mm thick silicon mirror segments is shown in Table 1. For this design, the azimuthal span, determined by degree of segmentation of the annulus, was selected to yield a mirror segment chord width approximately equal to the 100 mm axial length of segments. The approximately square length-to-width aspect ratio is convenient for fabrication, metrology, and mounting. The bond diameter was selected to be 4 mm, which blocks 9% of the mirror area. The feasibility of the design, accuracy of the mathematical model, and assumption that bond strength is

the limiting factor were verified using a detailed Finite Element Model (FEM) of the meta-shells shown in Figure 8.

Table 1 – Example of a 1.3 m diameter, 5 m focal length mirror assembly made from five meta-shells.

Meta-shell number	Mirror diameters (mm)	Layers in meta-shell	Mirror segments in meta-shell	1 keV effective area (cm ²)
1	1156 - 1296	17	1428	827
2	966 - 1106	19	1368	759
3	791 - 922	20	1200	616
4	625 - 752	22	1056	487
5	480 - 597	23	920	338
Totals		101	5972	3028

Gravity distortion analysis

A high fidelity FEM of a meta-shell was generated using a custom software tool that reads in the optical prescription and outputs a NASTRAN compatible FEM with hundreds of mirror shells accurately represented. This model was used to perform opto-mechanical analyses wherein the distortions determined by FEA are ray-traced to predict the resulting x-ray performance. This method was used to verify the gravity distortions are sufficiently small to support ground based x-ray testing. Figures 7 and 8 show the distortion and performance of a meta-shell subjected to an axial gravity load, resulting in a negligible distortion of 0.2 arc-seconds relative to the 5 arc-second goal.

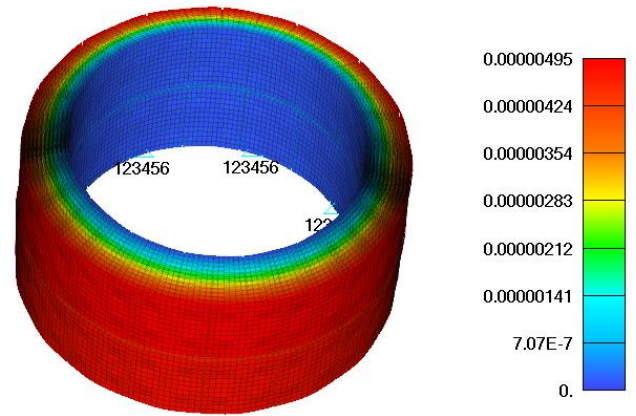


Figure 7 – Deformation of a meta-shell under axial gravity load (units are meters).

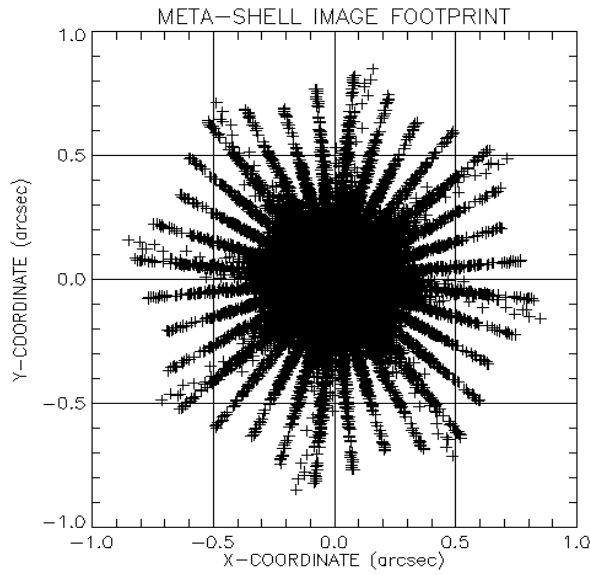


Figure 8 – Predicted x-ray performance of meta-shell under axial gravity load.

Structural Thermal Optical Performance (STOP) analysis

Temperature results from a detailed thermal model of a Mirror Assembly were mapped to the FEM to complete a STOP analysis of a meta-shell. As shown in Figure 9, the temperature gradient over the Mirror Assembly is 2.6°C while the gradient over an individual segment is 0.01°C as shown in Figure 10. The small temperature gradient over the mirror segments is due to the high thermal conductivity ($150\text{ W/m}\cdot\text{K}$) and relatively low CTE (2.5 ppm/C) of single crystal silicon and results in a negligible thermal distortion of 0.33 arc-sec HPD .

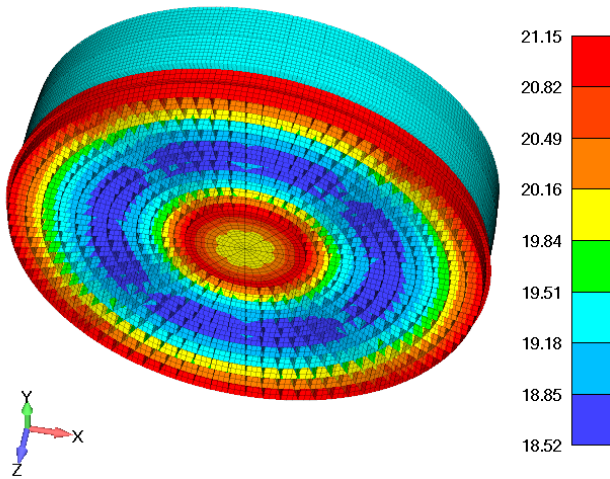


Figure 9 – Thermal analysis temperature predictions for a Mirror Assembly ($^{\circ}\text{C}$).

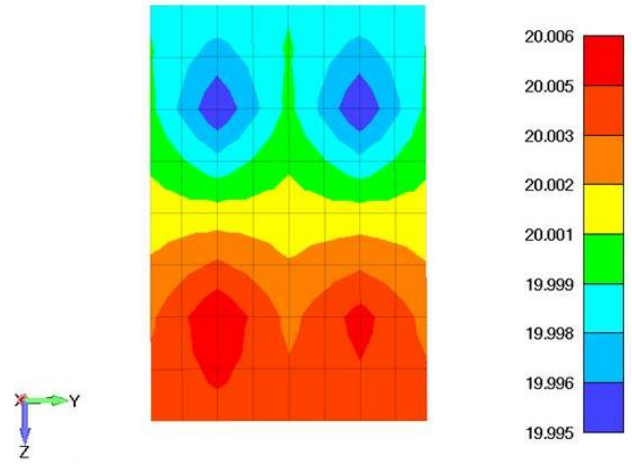


Figure 10 – Thermal gradient over a mirror segment ($^{\circ}\text{C}$).

4. PROTOTYPE LOAD TESTING

Two prototype units were assembled and tested to characterize the meta-shell dynamics under vibration loads and verify the strength of the bonded joints, assumed to be the structural weak point as described in section 3.

The first prototype, shown in Figure 11, was a single silicon mirror segment with a mass simulator bonded to the back, sized to create bond stresses equivalent to the maximum expected in a full meta-shell with many layers cantilevered off the structural shell. This prototype test article was subjected to notched workmanship random vibration loads per GSFC-STD-7000 in the axial and lateral axis as well as 200 g shock load without mechanical degradation. The test article was subsequently tested in random vibration until failure at the $+6\text{ dB}$ level (13 g root mean square acceleration). As expected, the failure was at the innermost bond, which simulates the bond between the post and structural shell.

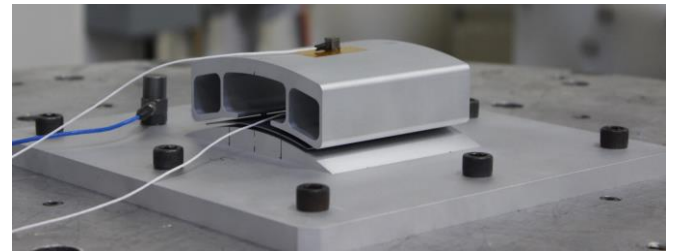


Figure 11 – Prototype test article with a cantilevered mass simulator.

The second prototype was a mechanical model of a full meta-shell, as shown in Figure 12, consisting of 54 glass mirror segments (3 layers) and 216 posts bonded to an aluminum structural shell (432 total bonds). The meta-shell was mounted to the vibration fixture with eight flexures, compliant in the radial direction, simulating the mount to the spider carrier structure. This prototype survived 12.3 g quasi-static loads (sine burst) and workmanship random vibration loads in the axial and lateral directions without degradation. These tests give us confidence our integration approach can meet spaceflight launch load requirements [7].

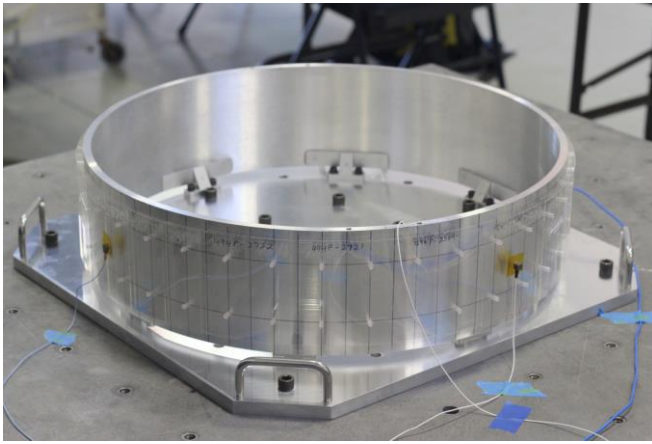


Figure 12 – Meta-shell A mechanical model, consisting of 54 thin glass mirror segments and 432 epoxy bonds.

The next prototype planned is a higher fidelity single crystal silicon meta-shell, shown in Figure 13, which will also be x-ray tested before and after environmental testing to ensure the performance has not degraded.

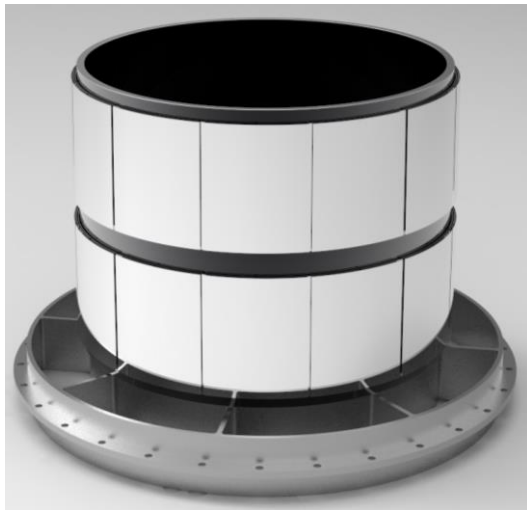


Figure 13 – Planned silicon meta-shell prototype.

5. CONCLUSIONS

The meta-shell approach combines the fabrication advantages of segmented x-ray optics with the integration advantages of full shell optics. A meta-shell construction method using a four point semi-kinematic mount to layer interlocking mirror segments onto a central structural shell has been developed. Initial testing shows the distortion of the four point mount is minimal. Extensive analysis was performed to demonstrate the feasibility of the four point mount and meta-shell approach. A mathematical model was developed to aid in the selection of meta-shell design parameters and verify the assembly can accommodate launch loads. A detailed FEM of a meta-shell was used to verify the mathematical model, predict gravity distortion, and perform STOP analysis. Two prototypes were successfully tested in various loading conditions to demonstrate the mechanical strength of the meta-shell approach.

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REFERENCES

- [1] Bookbinder, J. A., Smith R. K., Hornschemeier, A., et al, "The Constellation-X Observatory," Proc. SPIE 7011, (2008).
- [2] Cohen, L. M., et al., "Structural considerations for fabrication and mounting of the AXAF HRMA optics," Proc. SPIE 1303, (1990).
- [3] Weisskopf, M. C., et al., "Beyond Chandra – the X-ray Surveyor," Proc. SPIE 9510, (2015).
- [4] McClelland, R. S., et al., "Design and analysis of the International X-Ray Observatory mirror modules," Proc. SPIE 7732, (2010).
- [5] Collon, M. J., et al., "Silicon Pore Optics development for ATHENA," Proc. SPIE 9603, (2015).
- [6] Craig, W. W., et al., "Fabrication of the NuSTAR flight optics," Proc. SPIE 8147, (2011).
- [7] McClelland, R. S., et al., "Design and analysis of modules for segmented X-ray optics," Proc. SPIE 8443, (2012)
- [8] Gondoin, P., et al., "X-ray spectroscopy mission (XMM) telescope development," Proc. SPIE 2209, (1994)
- [9] Waldman, M., "The alignment test system for AXAF-I's High Resolution Mirror Assembly," Proc. SPIE 2515, (1995)
- [10] Choi, M. K., "Thermal Considerations for Meeting 20°C and Stringent Temperature Gradient Requirements of IXO SXT Mirror Modules," Proc. SAE 2009-01-2391, (2009)

BIOGRAPHY



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