

# Habitable Exoplanet Imager

# Optical Telescope Concept Design

H. Philip Stahl

# Contributors

## JPL

- Stefan Martin
- Scott Howe
- Gary Kuan
- Keith Warfield
- Team X

## MSFC

- Thomas Brooks, NASA
- Jacqueline Davis, NASA
- Brent Knight, NASA
- William Arnold, AI Solutions
- Mike Baysinger, ESSA
- Jay Garcia, ESSA
- Ronald Hunt, ESSA
- Andrew Singleton, ESSA
- Mary Caldwell, ESSA
- Melissa Therrell, ESSA

## HabEx

Habitable Exoplanet Imaging Mission (HabEx) is a concept for a mission to directly image and characterize planetary systems around Sun-like stars.

In addition to the search for life on Earth-like exoplanets, HabEx will enable a broad range of general astrophysics science enabled by 100 to 2500 nm spectral range and 3 x 3 arc-minute FOV.

HabEx is one of four mission concepts currently being studied for the 2020 Astrophysics Decadal Survey.

# OTA Specification

Science Requirements  
Launch Vehicle Capacity  
Programmatic Constraints

## Exoplanet

Habitable Zone Size  
Contrast  
Contrast  
Contrast  
Star Size  
Architecture

## General Astrophysics

Diffraction Limit  
Spatial Resolution

## Launch Vehicle

Up-Mass Capacity  
Fairing Size

## Programmatic

Budget



Engineering Specifications

**Minimum Telescope Diameter**  
Mid/High-Spatial Wavefront Error  
**WFE Stability**  
**Polarization**  
**Line of Sight Stability**  
**Unobscured (off-axis)**

Low/Mid-Spatial Wavefront Error  
Line of Sight Stability

Mass Budget  
Architecture (monolithic/segmented)

Maximum Telescope Diameter

# Design Assumptions

Mission will have an Internal Coronagraph which requires:

- Unobscured Aperture – off-axis
- Stable Wavefront.

General Astrophysics:

- 450 nm diffraction limit requires no development effort

Launch Vehicle

- SLS will exist. Therefore, for ‘baseline’ design mass and volume constraints are secondary to wavefront stability.
- ‘Backup’ designs will be considered for EELV.

The Most important Design Constraints are:

- Line of Sight Stability
- Wavefront Stability

# Optical Telescope Assembly (OTA) Specifications

<b>Architecture</b>	<b>Unobscured Off-Axis F/2.5 TMA</b>
<b>Aperture Diameter</b>	<b>4-meters Monolithic (Minimum)</b> 6.5-meters Segmented (Maximum)
Mass Budget	< 10,000 kg (excluding science instruments & spacecraft)
<b>Line of Sight Stability</b>	<b>&lt; 5 milli-arc-second (astrophysics)</b>
Diffraction Limit	450 nm (assumed to be achievable)
Wavefront Error	35 nm rms Total (assumed achievable)
Primary Mirror (cpd = cycles/diameter)	Total SFE < 8.0 nm rms Low-Order (< 3 cpd) < 5.6 nm rms Mid-Spatial (3 to 60 cpd) < 5.6 nm rms High-Spatial (>60 cpd) < 0.6 nm rms Roughness < 0.2 nm rms
<b>Wavefront Stability</b>	<b>Architecture and Coronagraph Specific</b>

# 4-meter Monolithic F/2.5 Off-Axis Concept

fits inside SLS

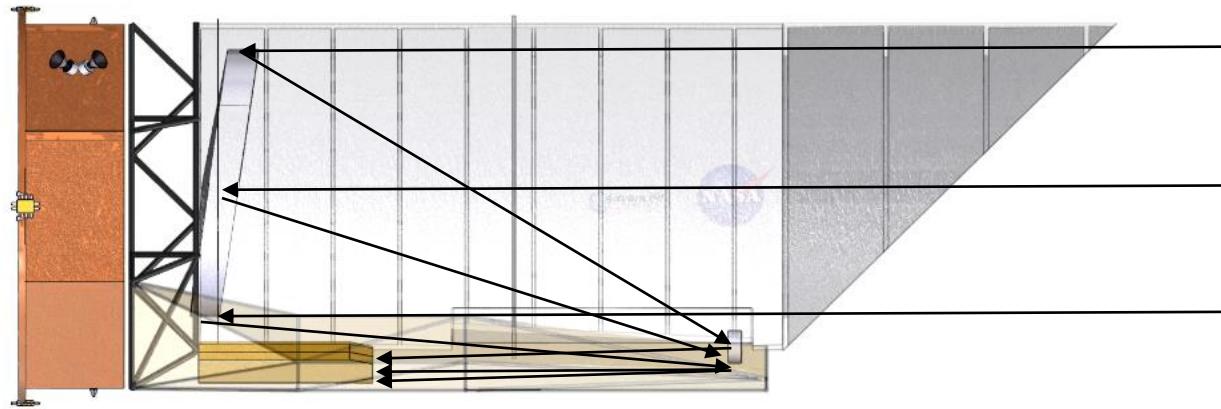
# Mission Architecture Constraints

Mission Architecture design constraints:

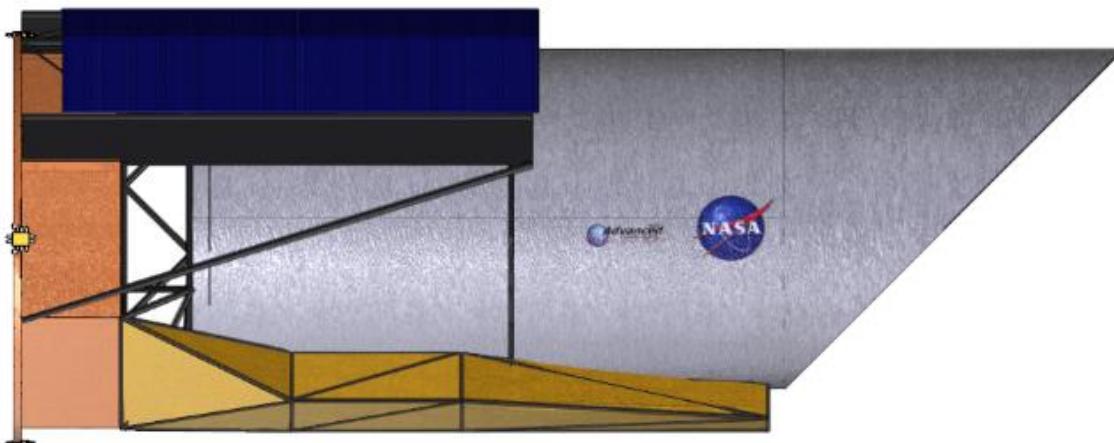
- Minimum Aperture for science is 4 meters.
- Coronagraph desires unobscured off-axis optical design
- Because of coronagraph polarization sensitivity, the primary mirror is F/2.5 which defines a PM/SM distance of  $\sim 9$  meters.
- For thermal stability and polarization, there is a desire to place the science instruments beside the PM rather than behind it.
- Forward Scarf limits close approach angle to Sun.

# HabEx 4-m Off-Axis Initial Concept

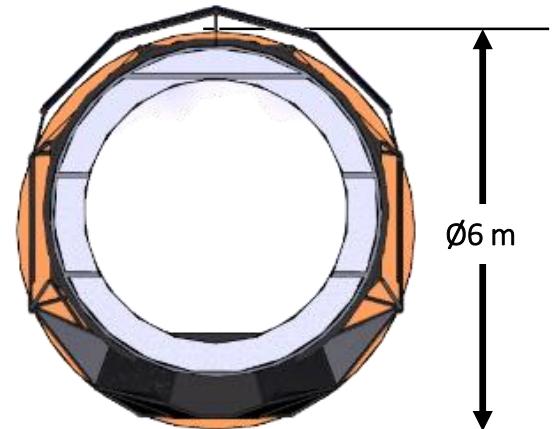
Observatory = OTA (PM/SM/Tube) & Science Instruments.



Observatory  
attaches to  
Spacecraft.



Solar Panels on  
Sunshade attach  
to Spacecraft.



# HabEx 4-m Off-Axis Initial Concept

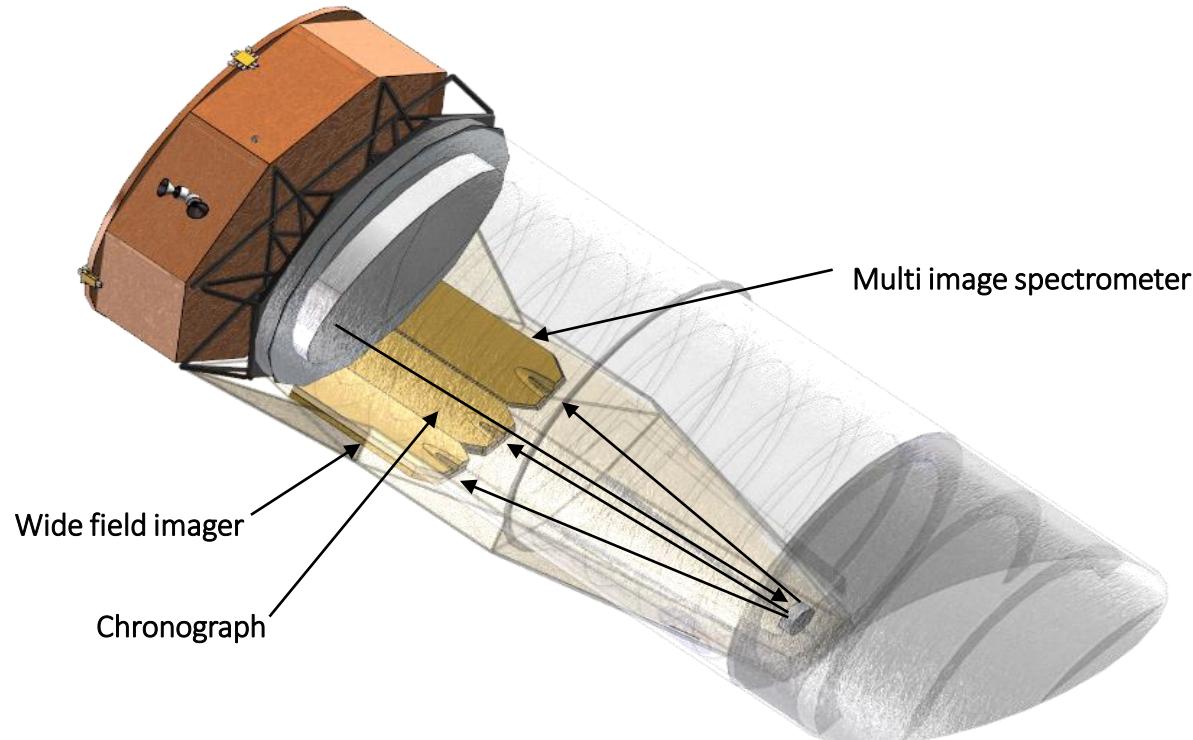
## Four Science Instruments:

Coronagraph (imager and spectrograph)

Starshade Imager (imager and spectrograph)

General Astrophysics Workhorse Camera (imager and spectrograph)

General Astrophysics UV Spectrograph

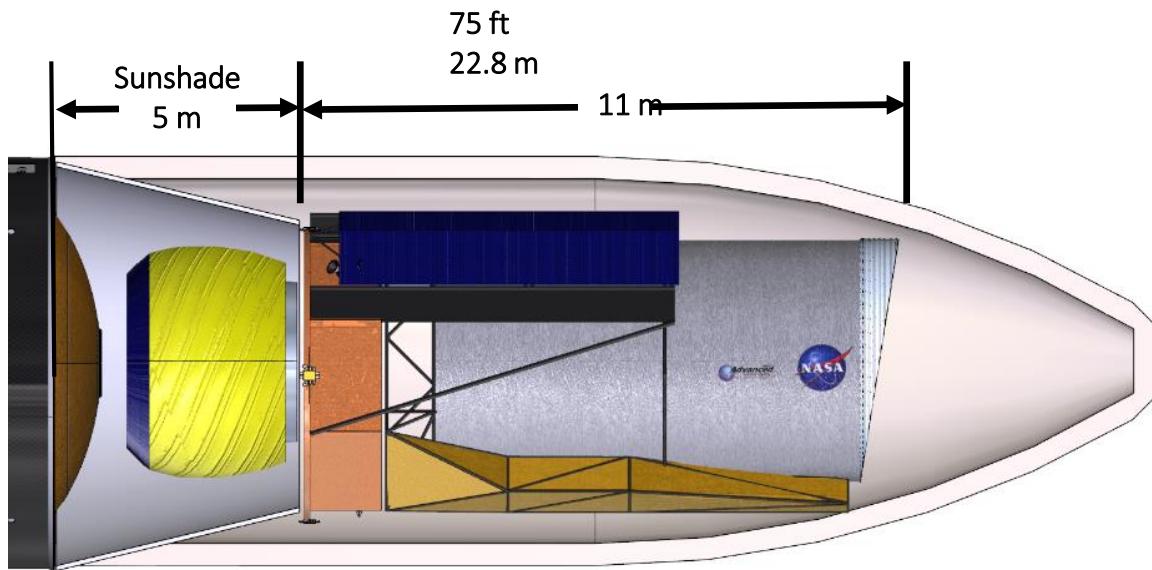
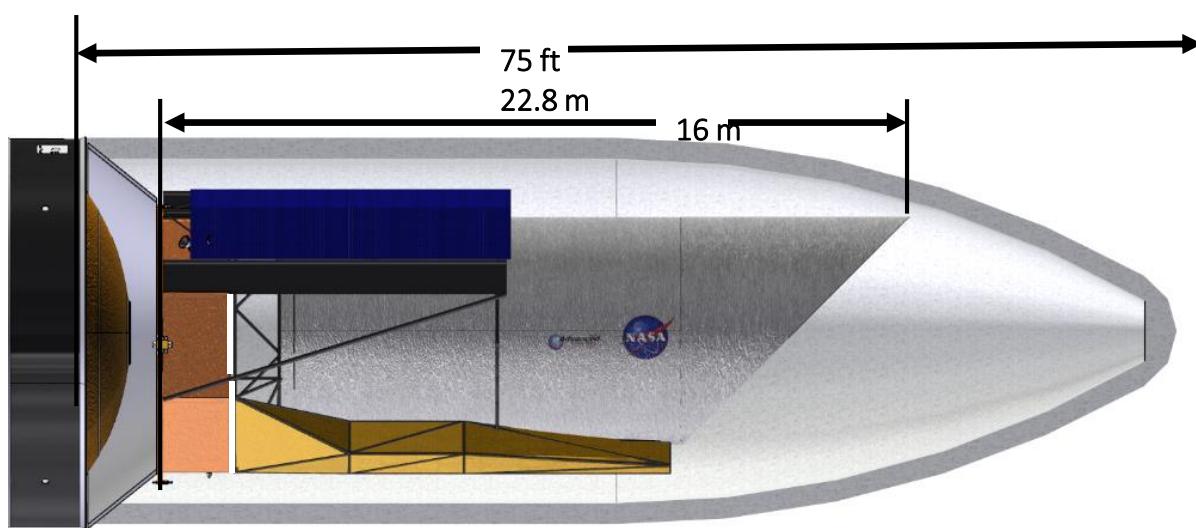


# Mission Architecture vs Launch Vehicle

SLS Volume and Mass Capacity enables Mission Architecture.

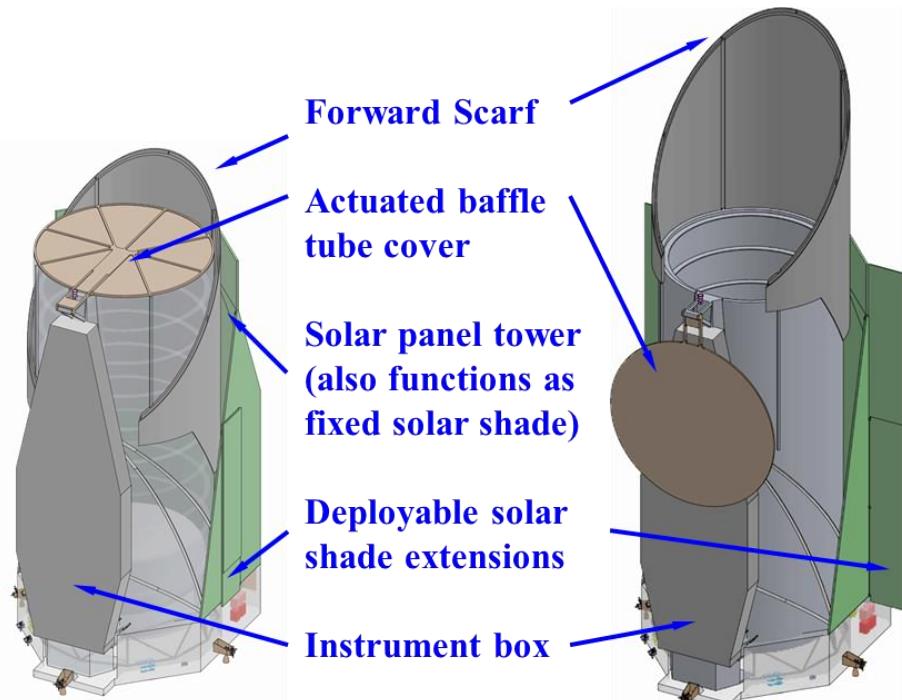
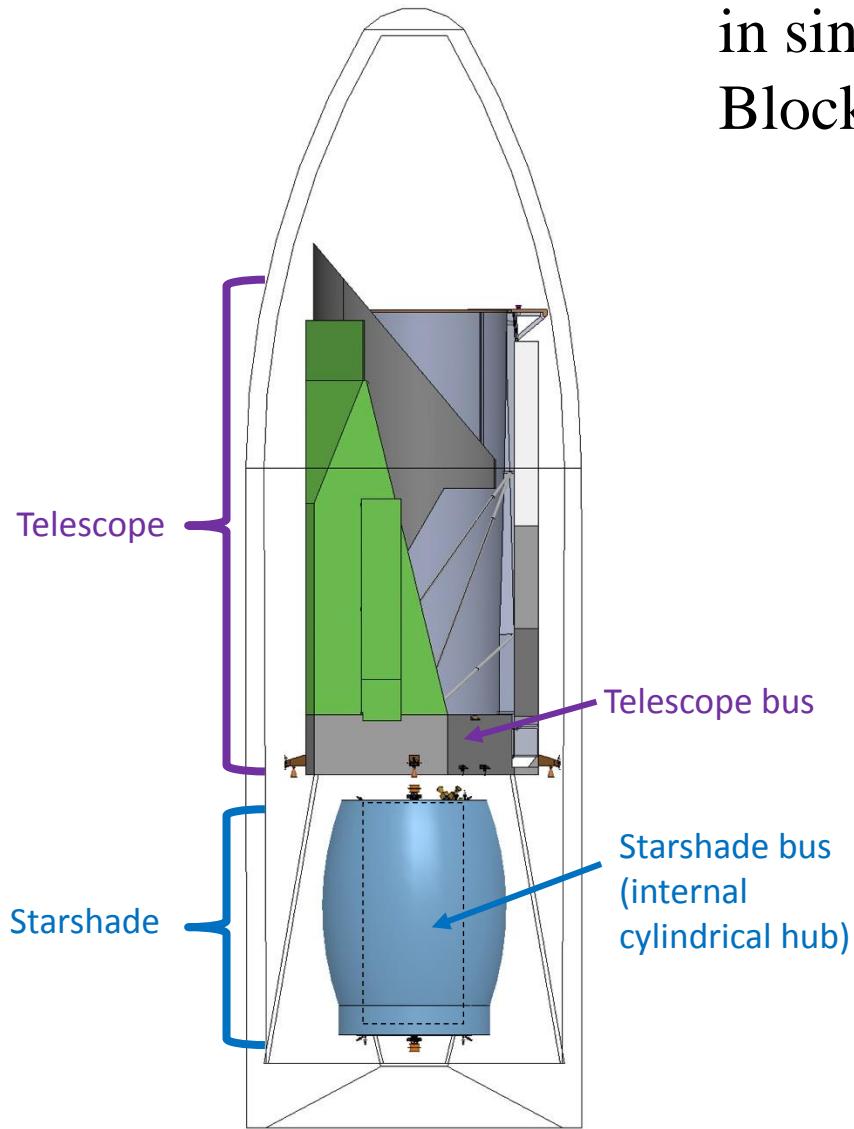
- 8.4-m Long Fairing on Block I Core
- 7.5 meter dynamic envelop enables 4-m PM with SI on side
- 27.4 m height enables dual launch of observatory & star shade
  - Observatory Only could be launched with no deployments.
  - Observatory and Star Shade can be dual launched with deployment of forward scarf
- Mass to SE-L2 = 44 mt

# Initial Launch Configuration Options



# Baseline Concept

Co-Launch Observatory and Star Shade in single SLS 8.4-m Long Fairing on Block 1B core.



# Telescope Specifications

Line of Sight Analysis  
Wavefront Stability Analysis

# Optical Telescope Assembly Structure

A primary purpose of the OTA Structure is to facilitate the alignment of the optical system and maintain that alignment to the required tolerances over all operating conditions: thermal, mechanical, space, etc.

So, the key question is – what are the required tolerances.

Tolerances can be derived from:

Line of Sight Stability Requirement

Wavefront Stability Requirement

# Line of Sight (LOS) Stability Specification

Specification: LOS incident upon the fine/fast steering mirror (FSM) should be stable to less than 5 milli-arc-seconds (mas) rms in any direction.

## Discussion:

- Coronagraph wants LOS Stability before FSM of <5.0 mas for two reasons:
  1. Beam Walk on Secondary and Tertiary Mirrors introduces wavefront error
  2. Coronagraph wants internal LOS stability to be < 0.5 mas and assumption is that FSM can produce 10X LOS reduction.
- Assume that General Astrophysics Instruments will not have FSM and requires LOS to be stable to 1/8<sup>th</sup> to 1/10<sup>th</sup> of PSF.
- For the 4-m telescope, PSF (2.44λ/D full-angle) at 450 nm is ~275 nano-radian (~ 57 mas)

# State of Art OTA Line of Sight Stability

HST LOS stability is 8 mas (1/10 full PSF angle)

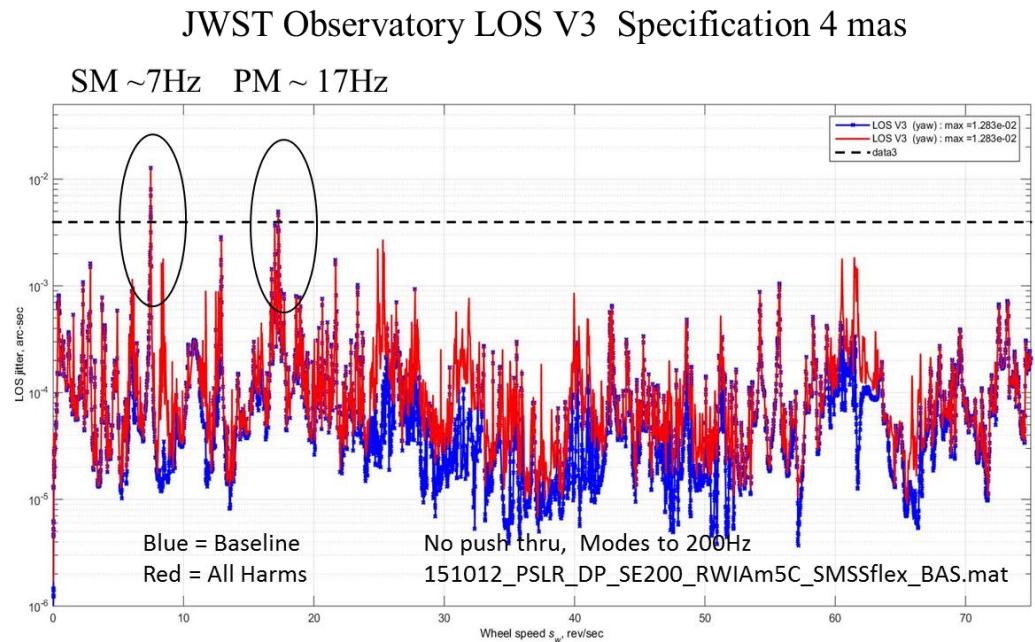
JWST LOS Jitter before FSM is < 7 mas (1/10 half PSF angle)

JWST LOS Jitter specification after FSM < 3.7 mas

- SM motion @ ~7 Hz
- PM motion @ ~17 Hz

Because of dampening, a warm JWST might have LOS stability of < 0.5 mas.

Feinberg, et. al., "A Cost-effective and Serviceable ATLAST 9.2m Telescope Architecture", *Proc. SPIE*. 9143. (August 02, 2014) doi: 10.1117/12.2054915



# LOS Stability Sensitivities

Zemax Tolerance Analysis of the LOS error produced by Rigid Body (6-DOF) Misalignments of the Primary, Secondary and Tertiary Mirrors.

Table 1. LOS Sensitivity to Component Rigid Body Alignment

Alignment	ZEMAX	Tolerance	Units	X-Tilt	Y-Tilt	RSS	Units
PM X-Tilt (Y-Rotation)	TY	1	n-radian	-16.0	0	16.0	mas
PM Y-Tilt (X-Rotation)	TX	1	n-radian	0	16.3	16.3	mas
PM Z-Rotation	TZ	1	n-radian	3.72	0	3.72	mas
PM X-Decenter	DX	1	nm	1.49	0	1.49	mas
PM Y-Decenter	DY	1	nm	0	1.39	1.39	mas
PM Z-Despace	DZ	1	nm	0	0.36	0.36	mas
SM X-Tilt (Y-Rotation)	TY	1	n-radian	-1.12	0	1.12	mas
SM Y-Tilt (X-Rotation)	TX	1	n-radian	0	-1.13	1.13	mas
SM Z-Rotation	TZ	1	n-radian	-0.29	0	0.29	mas
SM X-Decenter	DX	1	nm	-1.32	0	1.32	mas
SM Y-Decenter	DY	1	nm	0	-1.23	1.23	mas
SM Z-Despace	DZ	1	nm	0	-0.36	0.36	mas
TM X-Tilt (Y-Rotation)	TY	1	n-radian	0.32	0	0.32	mas
TM Y-Tilt (X-Rotation)	TX	1	n-radian	0	-0.31	0.31	mas
TM Z-Rotation	TZ	1	n-radian	0	0	0	mas
TM X-Decenter	DX	1	nm	-0.14	0	0.14	mas
TM Y-Decenter	DY	1	nm	0	-0.014	0.14	mas
TM Z-Despace	DZ	1	nm	-0.01	0	0.01	mas

# Preliminary LOS Stability Tolerances

Using alignment sensitivity matrix, excel spreadsheet evaluates different alignment allocations to achieve specification.

Table 2. Rigid Body Stability Specifications for < 5 mas LOS Stability				
Alignment	Specification	Units	RSS	Units
PM X-Tilt (Y-Rotation)	0.1	n-radian	1.60	mas
PM Y-Tilt (X-Rotation)	0.1	n-radian	1.63	mas
PM Z-Rotation	0.5	n-radian	1.86	mas
SM X-Tilt (Y-Rotation)	1	n-radian	1.12	mas
SM Y-Tilt (X-Rotation)	1	n-radian	1.13	mas
SM Z-Rotation	1	n-radian	0.29	mas
SM/PM X-Decenter	1	nm	1.32	mas
SM/PM Y-Decenter	1	nm	1.23	mas
SM/PM Z-Despace	5	nm	1.80	mas
TM X-Tilt (Y-Rotation)	5	n-radian	1.55	mas
TM Y-Tilt (X-Rotation)	5	n-radian	1.62	mas
TM/PM X-Decenter	10	nm	1.40	mas
TM/PM Z-Despace	50	nm	0.50	mas
LOS Stability RSS				5.00 mas

Notes:

- For a 4-meter PM, 0.1 nano-radian of tilt is equal to 200 picometers PV.
- For a 0.5-meter SM, 1 nan-radian of tilt is equal to 250 picometers PV.
- Eliminated TM/PM Y-Decenter by coupling PM to TM in Y-axis.

# WFE Stability

WFE Stability specification is spatial frequency dependent

Different Coronagraphs are sensitive to different spatial frequencies

Initial ROM WFE stability specification

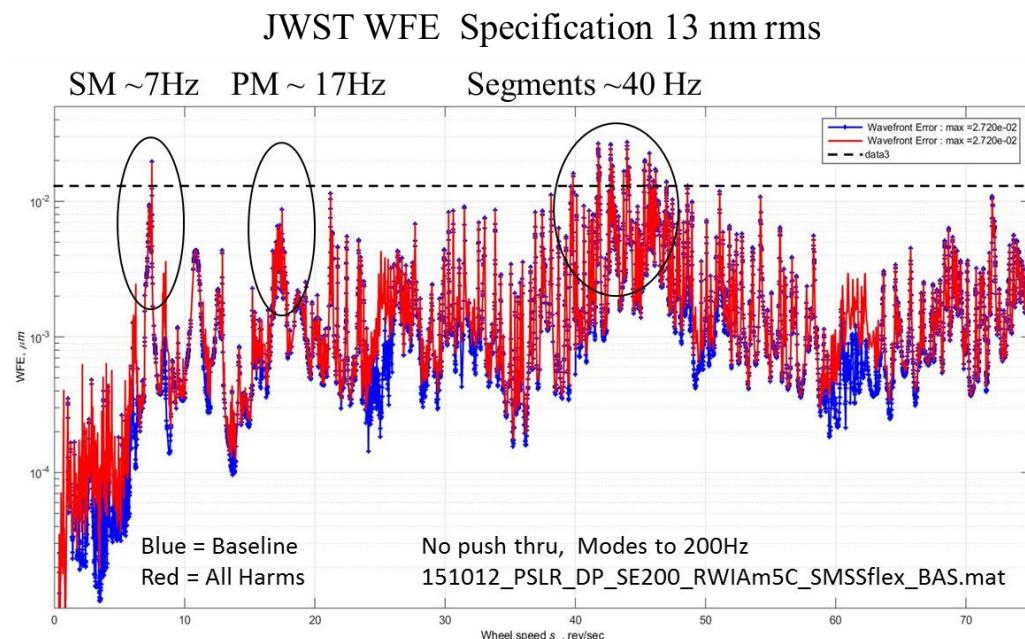
- Low-Order  $< 0.3 \text{ nm rms.}$
- Mid-Spatial Frequency  $< 0.02 \text{ nm pm}$

JWST WFE stability specification  $< 13 \text{ nm rms}$

- SM motion @  $\sim 7 \text{ Hz}$
- PM motion @  $\sim 17 \text{ Hz}$

Per Feinberg, et. al., because of dampening, a warm JWST may have WFE stability of  $< 2 \text{ nm rms.}$

Feinberg, et. al., "A Cost-effective and Serviceable ATLAST 9.2m Telescope Architecture", *Proc. SPIE*. 9143. (August 02, 2014) doi: 10.1117/12.2054915



# Wavefront Error (WFE) Stability Specification

For Vector Vortex, higher charge rejects more WFE

**Implication is that Charge 6 or 8 is better than Charge 4.**

Aberration	Indices		Allowable RMS wavefront error (nm) per mode			
	$n$	$m$	charge 4	charge 6	charge 8	charge 10
Tip-tilt	1	$\pm 1$	1.1	5.9	14	26
Defocus	2	0	0.8	4.6	12	26
Astigmatism	2	$\pm 2$	0.0067	1.1	0.90	5
Coma	3	$\pm 1$	0.0062	0.66	0.82	5
Spherical	4	0	0.0048	0.51	0.73	6
Trefoil	3	$\pm 3$	0.0072	0.0063	0.57	0.67
2 <sup>nd</sup> Astig.	4	$\pm 2$	0.0080	0.0068	0.67	0.73
2 <sup>nd</sup> Coma	5	$\pm 1$	0.0036	0.0048	0.69	0.85
2 <sup>nd</sup> Spher.	6	0	0.0025	0.0027	0.84	1
Quadrafoil	4	$\pm 4$	0.0078	0.0080	0.0061	0.53
2 <sup>nd</sup> Trefoil	5	$\pm 3$	0.0051	0.0056	0.0043	0.72
3 <sup>rd</sup> Astig.	6	$\pm 2$	0.0023	0.0035	0.0034	0.81
3 <sup>rd</sup> Coma	7	$\pm 1$	0.0018	0.0022	0.0036	1.18
3 <sup>rd</sup> Spher.	8	0	0.0018	0.0018	0.0033	1.49

Garrett Ruane, June 2017

Legend:

- not rejected (light red)
- first-order rejection (yellow)
- > first-order rejection (green)

Each Aberration can be mapped to a PM & SM rigid body motions; amplitudes given by Zemax alignment tolerance.

# Preliminary Wavefront Stability Tolerances

Using optical design sensitivity analysis, can calculate the maximum amount of rigid body motion allowed by the primary and secondary mirrors. Tertiary Mirror motion is negligible.

Vector Vortex Telescope Rigid Body Alignment Tolerances					
Zernike	VVC-4	VVC-6	VVC-8	VVC-10	Units
Allowed Focus	0.8	4.6	12	26	nm rms
Allowed Astigmatism	0.0067	1.1	0.9	5	nm rms
Allowed Trefoil	0.0072	0.0063	0.57	0.67	nm rms
Calculated Focus	0.05	4.5	8.5	25	nm rms
Calculated Astigmatism	0.0065	0.5	0.9	5	nm rms
Calculated Trefoil	0.0001	0.0065	0.012	0.07	
DOF					
PM X-Decenter	3	200	400	3000	nm
PM Y-Decenter	3	200	400	3000	nm
PM Z-Despace	5	500	1000	2500	nm
PM X-Tilt	3	200	400	2000	n-rad
PM Y-Tilt	2	150	200	1000	n-rad
PM Z-Rotation	1	100	150	500	n-rad
SM X-Decenter	3	200	400	3000	nm
SM Y-Decenter	3	200	400	3000	nm
SM Z-Despace	5	500	1000	2500	nm
SM X-Tilt	3	200	400	2000	n-rad
SM Y-Tilt	3	200	400	2000	n-rad
SM Z-Rotation	10	200	1000	2000	n-rad

These tolerances are larger than what is allow for LOS Stability.

Note: Analysis does not include dynamic WFE from PM.

# WFE Stability Produced by LOS Tolerances

5 mas LOS Rigid Body Motion Tolerances **DO NOT** produce any WFE larger than even the VVC-4 Specification.

ISO Zernikes	TOTAL RMS WFE	VVC-4	VVC-6	VVC-8	VVC-10
Z1 X-Tilt	0.0014	1.1	5.9	14	26
Z2 Y-Tilt	0.0016	1.1	5.9	14	26
Z3 Focus	0.0209	0.8	4.6	12	26
Z4 X-Astig	0.0021	0.0067	1.1	0.9	5
Z5 Y-Astig	0.0022	0.0067	1.1	0.9	5
Z6 X-Coma	0.0005	0.0062	0.66	0.82	5
Z7 Y-Coma	0.0006	0.0062	0.66	0.82	5
Z8 Sphere	0.0000	0.0048	0.51	0.73	6
Z9 X-Trefoil	0.0000	0.0072	0.0063	0.57	0.67
Z10 Y-Trefoil	0.0000	0.0072	0.0063	0.57	0.67
Z11 X-2nd Astig	0.0000	0.0080	0.0068	0.67	0.73
Z12 Y-2nd Astig	0.0000	0.0080	0.0068	0.67	0.73
Z13 X-2nd Coma	0.0000	0.0036	0.0048	0.69	0.85
Z14 Y-2nd Coma	0.0000	0.0036	0.0048	0.69	0.85
Z15 2nd Sphere	0.0000	0.0025	0.0027	0.84	1
Z16 X-Quadrafoil	0.0000	0.0078	0.0080	0.0061	0.53
Z17 Y-Quadrafoil	0.0000	0.0078	0.0080	0.0061	0.53
Z18 X-2nd Trefoil	0.0000	0.0051	0.0056	0.0043	0.72
Z19 Y-2nd Trefoil	0.0000	0.0051	0.0056	0.0043	0.72
Z20 X-3rd Astig	0.0000	0.0023	0.0035	0.0034	0.81
Z21 Y-3rd Astig	0.0000	0.0023	0.0035	0.0034	0.81
Z22 X-3rd Coma	0.0000	0.0018	0.0022	0.0036	1.18
Z23 Y-3rd Coma	0.0000	0.0018	0.0022	0.0036	1.18
Z24 3rd Sphere	0.0000	0.0018	0.0018	0.0033	1.49

Note: Analysis does not include Dynamic WFE from PM.

# Why is LOS more sensitive than WFE

WFE changes more rapidly with F/# than LOS.

Typically one designs the optical system to be as fast an F/# as possible for the required WFE stability. If the system is sufficiently mechanically stable for WFE, it will be ok for LOS.

HabEx has a slow F/2.5 optical design to minimize Polarization.  
At F/2.5 WFE is not as sensitive to mis-alignments as LOS.

Seidel Coma Sensitivity							
Alignment	Tolerance	Units	F/2.5	F/2	F/1.5	F/1.25	Units
PM X-Tilt	1	micro-degree	642	969	1602	2150	pico-meters
PM Y-Tilt	1	micro-degree	664	1019	1742	2411	pico-meters
SM X-Tilt	1	micro-degree	53	79	129	172	pico-meters
SM Y-Tilt	1	micro-degree	54	83	142	196	pico-meters
SM X-Decenter	10	nanometer	37	69	153	246	pico-meters
SM Y-Decenter	10	nanometer	34	60	117	165	pico-meters
SM Z-Despace	10	nanometer	18	42	119	223	pico-meters

Zernike Defocus Sensitivity							
Alignment	Tolerance	Units	F/2.5	F/2	F/1.5	F/1.25	Units
PM X-Tilt	1	micro-degree	0	0	0	0	pico-meters
PM Y-Tilt	1	micro-degree	7	14	38	70	pico-meters
SM X-Tilt	1	micro-degree	0	0	0	0	pico-meters
SM Y-Tilt	1	micro-degree	6	9	16	22	pico-meters
SM X-Decenter	10	nanometer	0	0	0	0	pico-meters
SM Y-Decenter	10	nanometer	-37	-69	-151	-242	pico-meters
SM Z-Despace	10	nanometer	-145	-217	-353	-467	pico-meters

Line of Sight Sensitivity							
Alignment	Tolerance	Units	F/2.5	F/2	F/1.5	F/1.25	Units
PM X-Tilt	1	micro-degree	35.2	35.4	35.6	35.8	nano-radian
PM Y-Tilt	1	micro-degree	34.6	34.5	34.2	33.9	nano-radian
SM X-Tilt	1	micro-degree	3.93	4.48	5.54	6.50	nano-radian
SM Y-Tilt	1	micro-degree	2.87	2.85	2.79	2.75	nano-radian
SM X-Decenter	10	nanometer	0.91	1.11	1.45	1.71	nano-radian
SM Y-Decenter	10	nanometer	0.89	1.11	1.45	1.71	nano-radian

Zernike Astigmatism Sensitivity							
Alignment	Tolerance	Units	F/2.5	F/2	F/1.5	F/1.25	Units
PM X-Tilt	1	micro-degree	-648	-983	-1643	-2231	pico-meters
PM Y-Tilt	1	micro-degree	-668	-1030	-1780	-2493	pico-meters
SM X-Tilt	1	micro-degree	53	80	133	179	pico-meters
SM Y-Tilt	1	micro-degree	55	84	144	201	pico-meters
SM X-Decenter	10	nanometer	-37	-70	-157	-256	pico-meters
SM Y-Decenter	10	nanometer	36	67	145	228	pico-meters
SM Z-Despace	10	nanometer	-9	-21	-61	-116	pico-meters

# Design for Stability

Wavefront and Line of Sight Stability has design consequences.

- Mechanical
  - Secondary Mirror Support Structure Dynamic Response – make higher
  - Primary Mirror Dynamic Response – make higher
  - Passive/Active Vibration Isolation – lower acceleration/better isolation
  - Passive/Active Dampening/Control – mass damping
- First Order Scaling
  - WFE & LOS Stability is proportional to frequency<sup>^2</sup>.  
3.3X increase in frequency response = 10X improvement in stability
  - WFE & LOS Stability is proportional to acceleration.  
1X decrease in acceleration force = 1X improvement in stability
  - WFE & LOS Stability is proportional to mass. (Mass Dampening)  
1X increase in mass = 1X improvement in stability

# Design for Stability

Wavefront and Line of Sight Stability has design consequences.

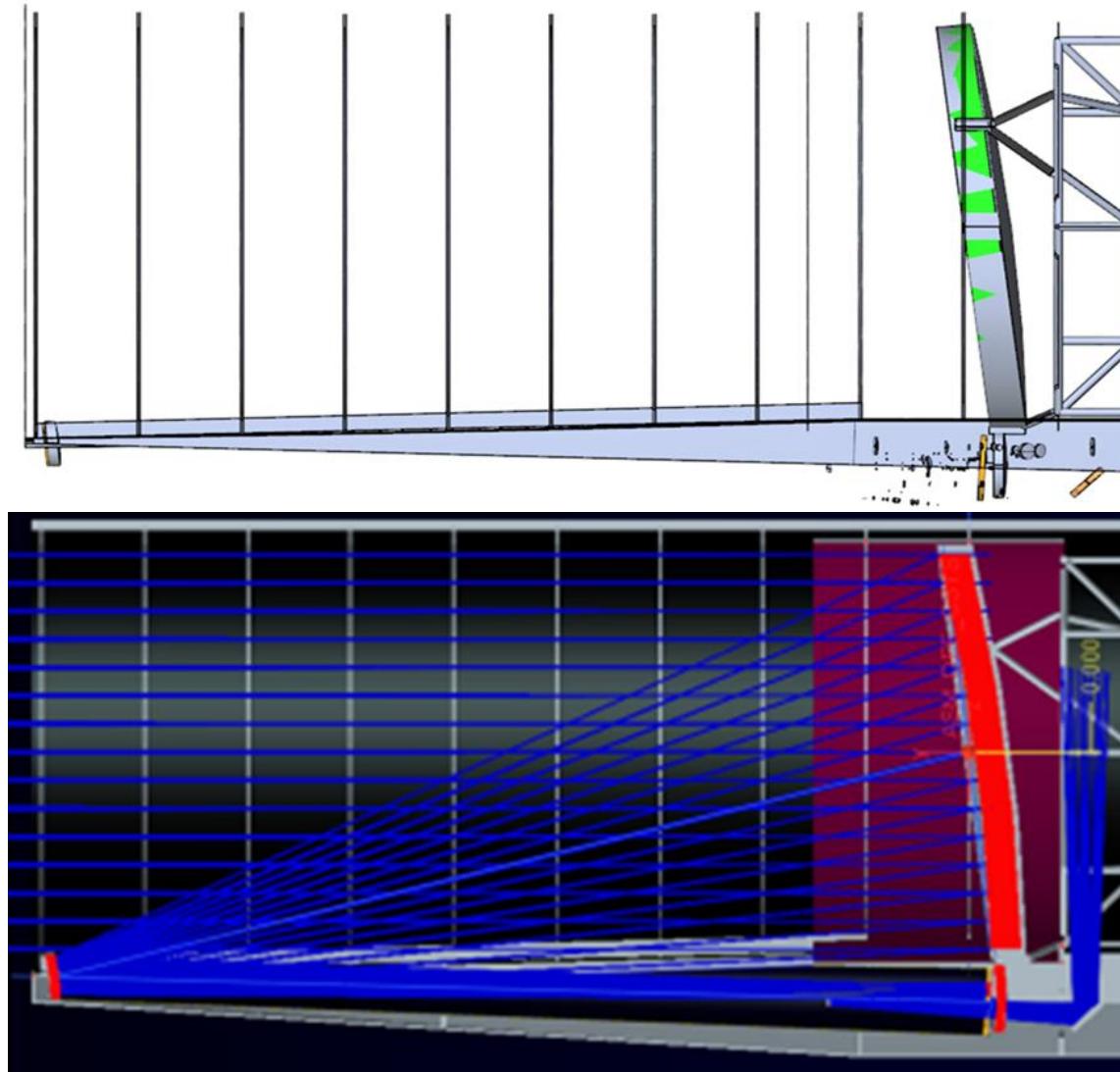
- Thermal
  - PM & SM Mirror CTE – want small and very homogeneous
  - Structure CTE – want small and very homogeneous
  - Passive Thermal Isolation - mass
  - Active Thermal Control – predictive thermal control

# Telescope Structure Design:

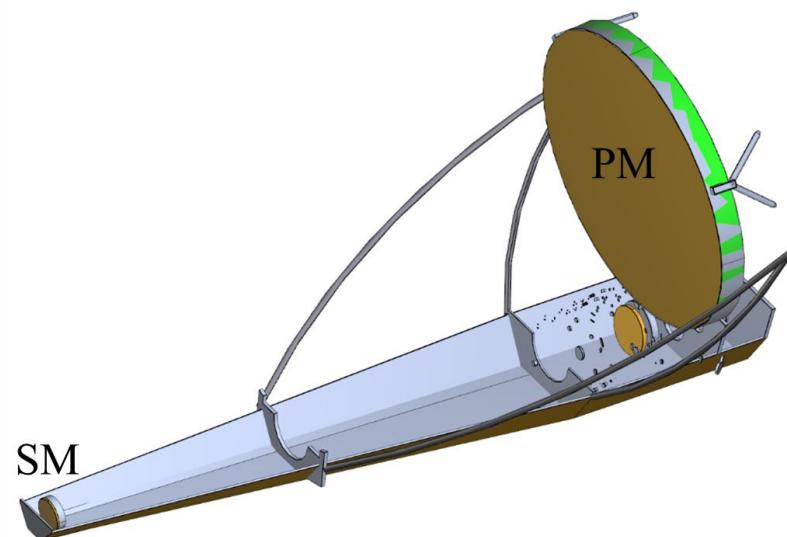
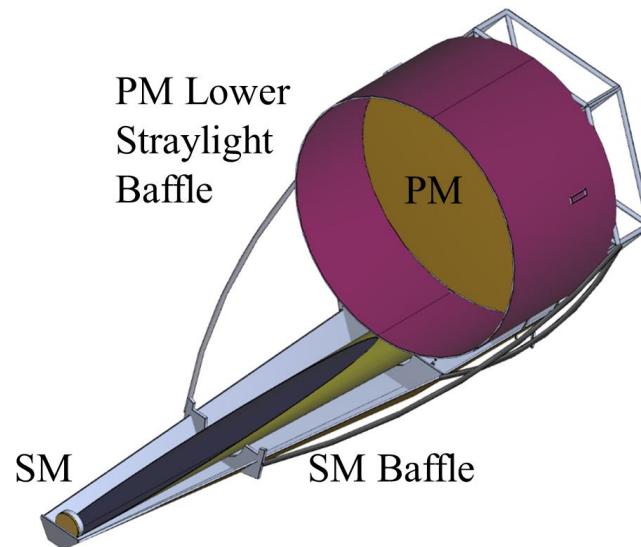
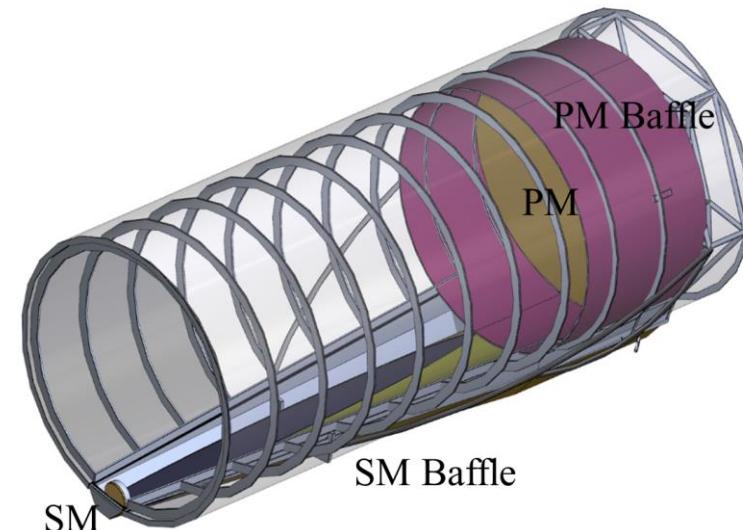
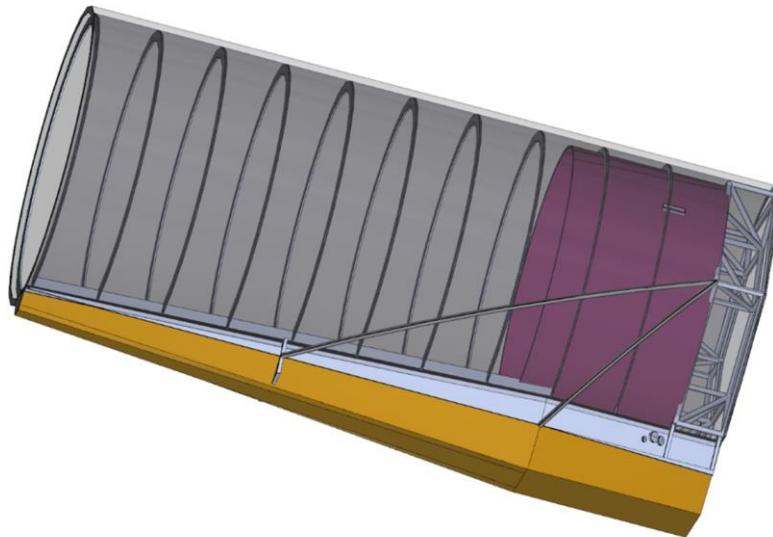
## Volume & Mass

# HabEx Telescope Design: CAD

Imported OTA & Instrument Optical Designs (via STEP files).



# Select CAD views



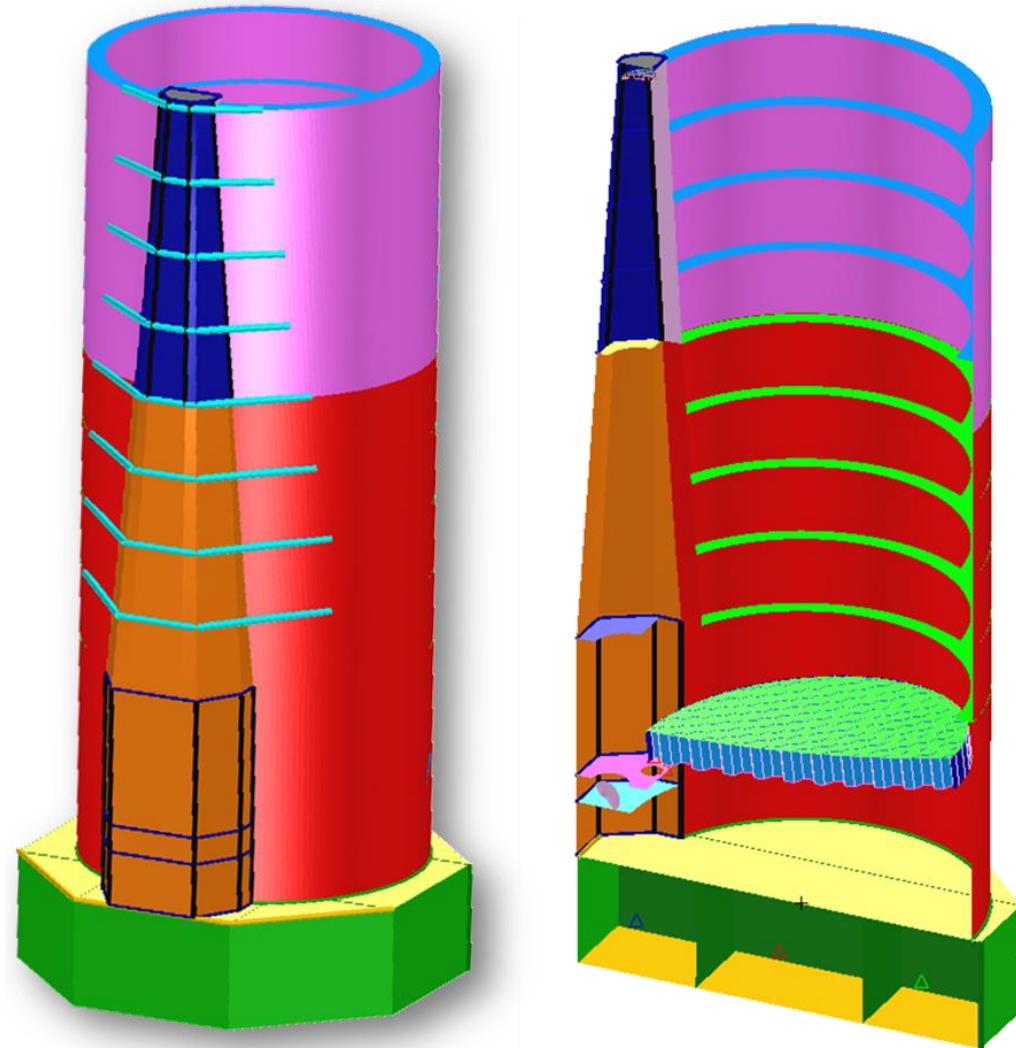
# HabEx Telescope Design: FEM

To evaluate opto-mechanical performance, created FEM of Structural Elements.

Changed exo-skeleton to lateral exo-truss elements connecting to the internal straylight baffles.

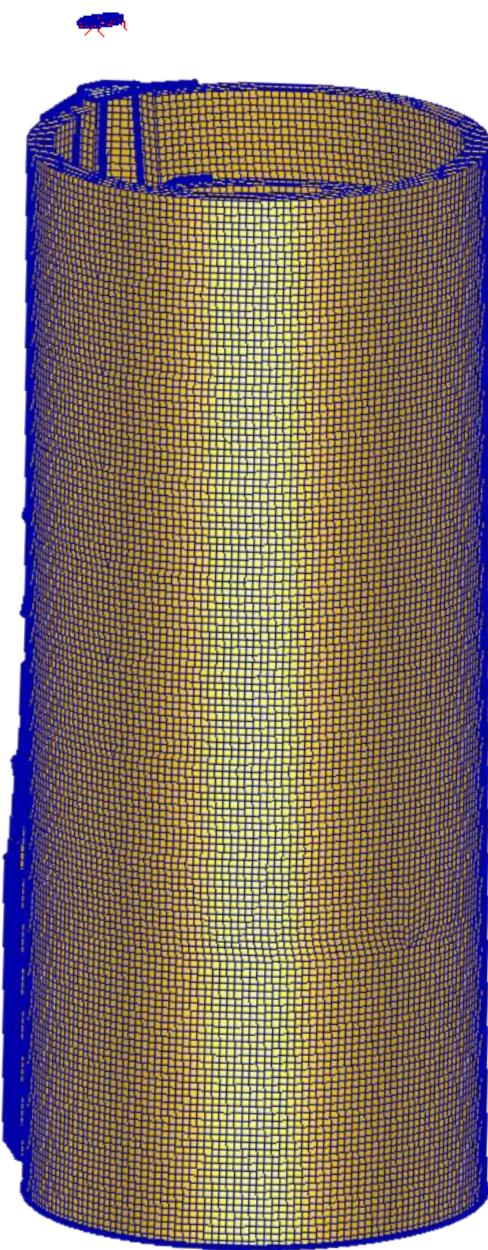
Internal straylight baffles are not continuous, because of PM to SM light beam.

**PM Truss depth arbitrarily set at 2-meters based on available SLS fairing height. Could be less.**



# HabEx Telescope Design: Mass Estimate

Secondary Mirror  
Mass = 10 kg

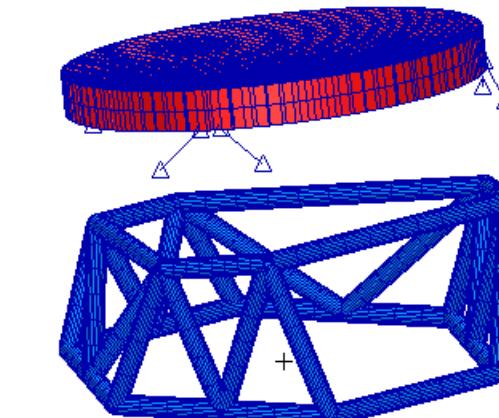


Tube / Tower  
Mass = 3052 kg

Sci Instruments  
Mass = 1300 kg

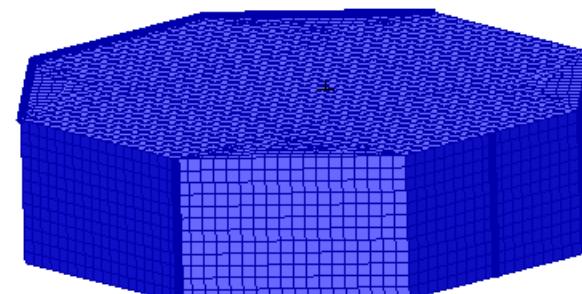
**Optical Telescope Assembly**  
**Mass = 5910 kg**  
**(excluding BUS & Instruments)**

Primary Mirror Assembly  
Mass = 2850 kg



Primary Mirror  
Mass = 1652 kg

PM Truss  
Mass = 1198 kg



Spacecraft BUS  
Mass = 4745 kg

# Telescope Structure:

## Predicted LOS Performance

# Dynamic Analysis

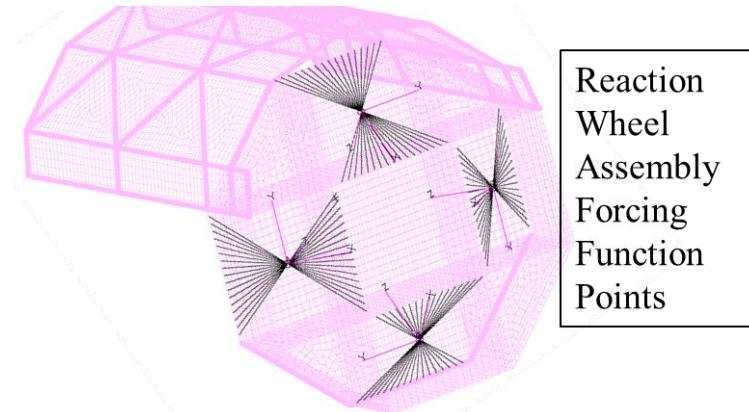
To determine OTA dynamic opto-mechanical performance:

- Construct a finite element model of the OTA structure.
- Expose model to expected mechanical disturbances:
  - JWST Reaction Wheel Specification
- Calculate Rigid Body motions of SM and PM relative to OTA coordinate system and relative to each other
  - X-, Y-, Z-despace
  - X-, Y-, Z-rotation
- Are Rigid Body motions less than Specification?
- Apply Vibration Isolation:
  - JWST 1-Hz Passive Vibration Isolation
  - Active Isolation
  - Micro-Thrusters

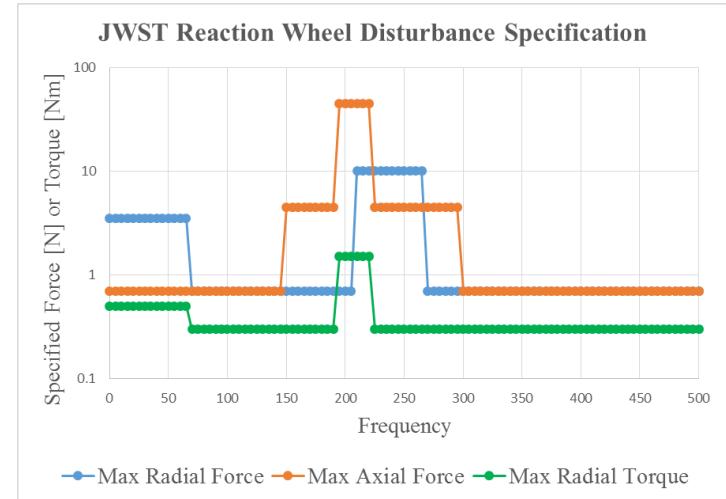
# Mechanical Disturbance Input

JWST reaction wheel specification is input into spacecraft at 4 points for standard pyramid arrangement.

This is very conservative worst case.



- Radial force and moment disturbances are applied in 10 degree increments around wheel rotation axis. Result is 144 load cases.
- Radial force and moment disturbances are swept through 360 degree wheel rotation to calculate maximum relative displacement between primary and secondary mirror for each wheel.
- Critical Damping is set at 1%



#### 3.3.1.6 Wheel Unbalance

After exposure to the environments defined in section 3.2.5 of this specification, the unbalance magnitude of the RWA rotating components shall not exceed the following values:

- a. Static Unbalance: Less than 1.0 (g-cm) over the operating speed range.
- b. Dynamic Unbalance: Less than 14.0 (g-cm<sup>2</sup>) over the operating speed range.
- c. The peak radial forces and moments produced by the RWA at any operating speed (including resonant conditions) shall not exceed the values listed in the table below:

Peak Radial Disturbance Limits Including Resonant Conditions		
Parameter	Frequency	Max. Limit
Force (F <sub>x</sub> )	0-70 Hz	3.5 N
	70-210 Hz	0.7 N
	210-270 Hz	10 N
	270-500 Hz	0.7 N
Torque (M <sub>x</sub> )	0-70 Hz	0.5 N-m
	70-195 Hz	0.3 N-m
	195-225 Hz	1.5 N-m
	225-500 Hz	0.3 N-m

#### 3.3.1.7 Axial Induced Vibration

The peak force (amplitude) produced by the RWA in the direction parallel to its spin axis shall not exceed 0.2 N within the frequency range 2-200 Hz, when measured at constant speeds that are within the operational speed range and that are free of major structural resonances. The peak axial force produced by the RWA at any operating speed (including resonant conditions) shall not exceed the following limit values:

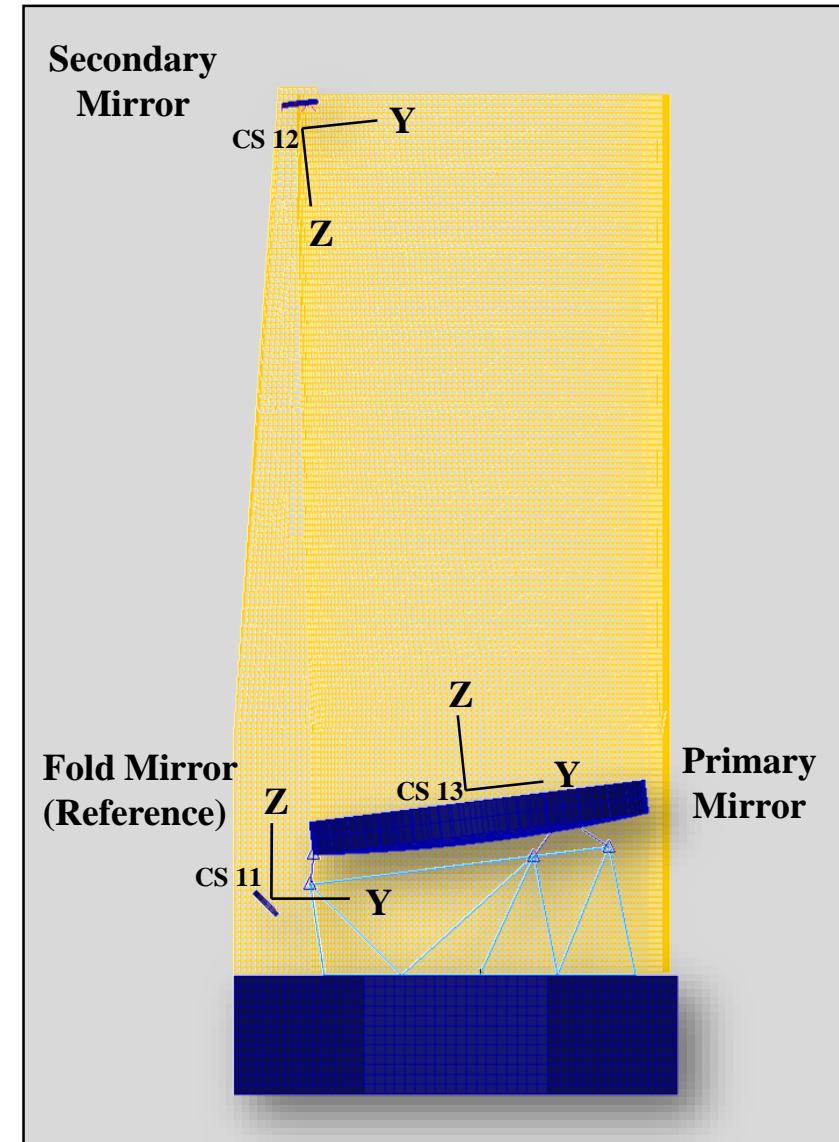
Frequency Range (in Hz):	0-150	150-195	195-225	225-300	300-500
Axial Force (F <sub>z</sub> ) Limit:	0.7 N	4.5 N	45 N	4.5 N	0.7 N

# PM/SM Rigid Body Motion vs Disturbance

- PM, SM motion (relative to Fold Mirror) is calculated using MPC (NASTRAN Multi Point Constraint).
- **Motions are reported in a local optical coordinate system:**
  - PM in CS13,
  - SM in CS12 and
  - Relative PM/SM in CS11.
- Material properties based on quasi-isotropic M46J

Tension	
0 degrees, *Et1	(Msi) 13.55101
90 degrees, *Et2	(Msi) 13.55101
Poisson's Ratio, *vt12	0.314294

M46J Quasi-Isotropic Laminate Properties  
(25%0, 50%45, 25%90)  
Density = 1.58 gram/cm<sup>3</sup> (0.057 lb/in<sup>3</sup>)



Analysis Coordinate Systems (11, 12, 13)

# Secondary Mirror Rigid Body Motion

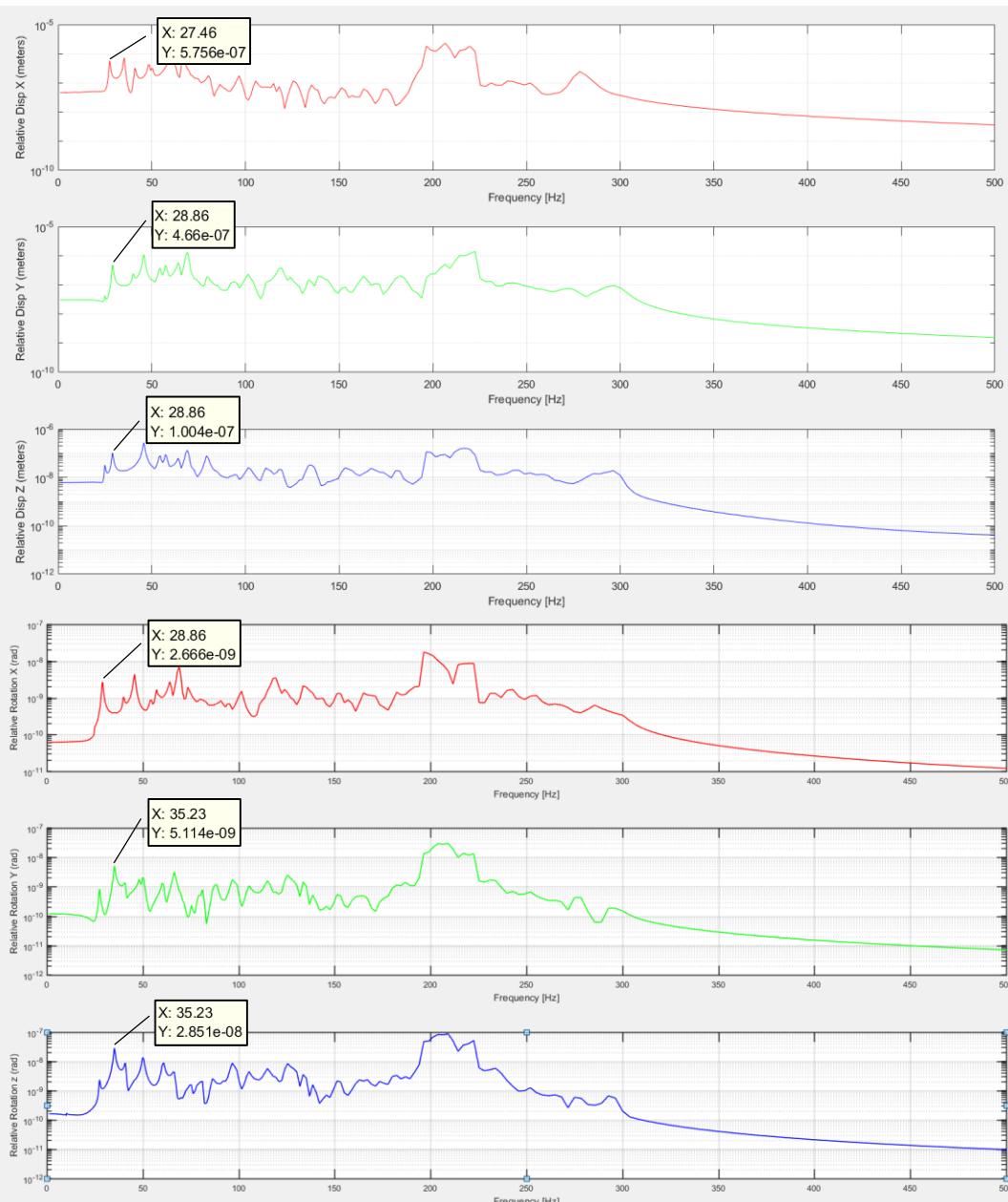
SM first mode motion  
relative to Fold Mirror:

- $\Delta X = 0.6 \mu\text{m}$  at 28 Hz
- $\Delta Y = 0.5 \mu\text{m}$  at 29 Hz
- $\Delta Z = 0.1 \mu\text{m}$  at 29 Hz
- $\Theta X = 2.6 \text{nrad}$  at 29 Hz
- $\Theta Y = 5 \text{nrad}$  at 35 Hz
- $\Theta Z = 29 \text{nrad}$  at 35 Hz

Are all larger than specified  
LOS Tolerances:

- $\Delta X = 1 \text{ nm}$
- $\Delta Y = 1 \text{ nm}$
- $\Delta Z = 5 \text{ nm}$
- $\Theta X = 1 \text{ nrad}$
- $\Theta Y = 1 \text{ nrad}$
- $\Theta Z = 1 \text{ nrad}$

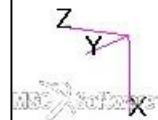
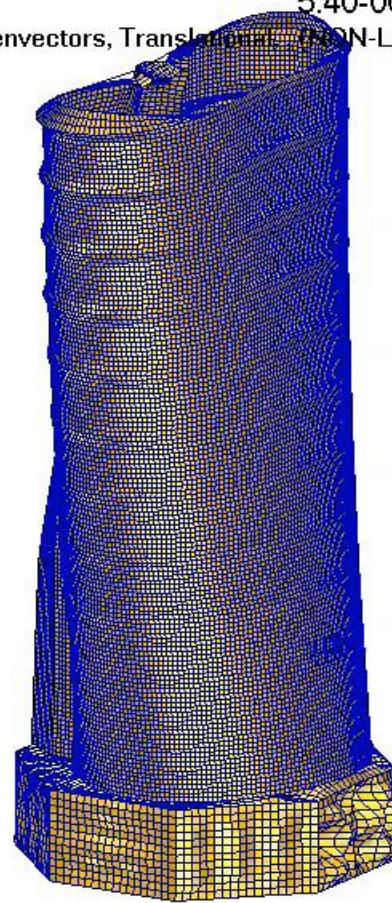
Need Vibration Isolation

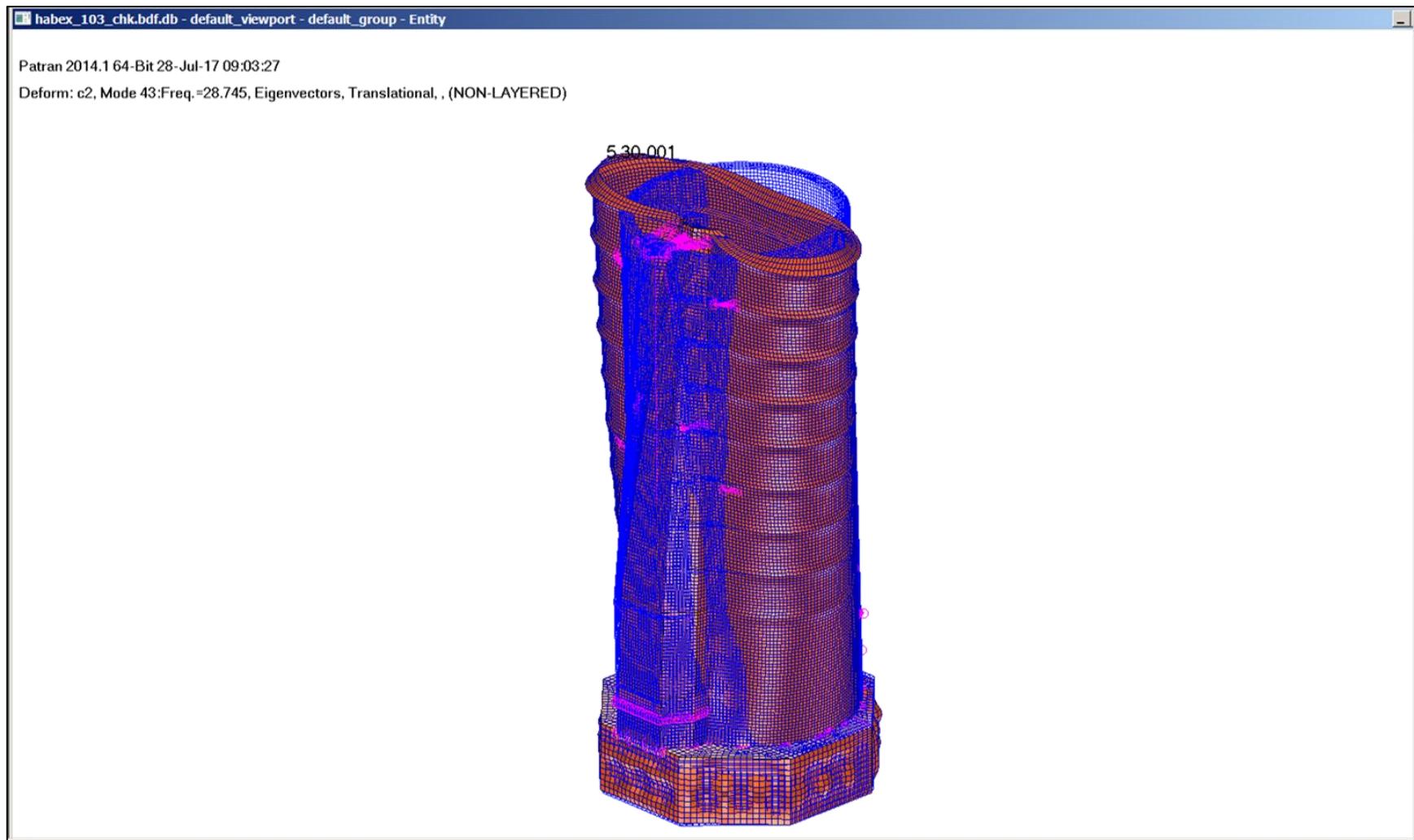


Patran 2014.1 64-Bit 25-Jul-17 13:09:14

5.40-001

Deform: Default, Mode 7:Freq.=29.044, Eigenvectors, Translation (NON-LAYERED)





First Tube Mode

# Primary Mirror Rigid Body Motion

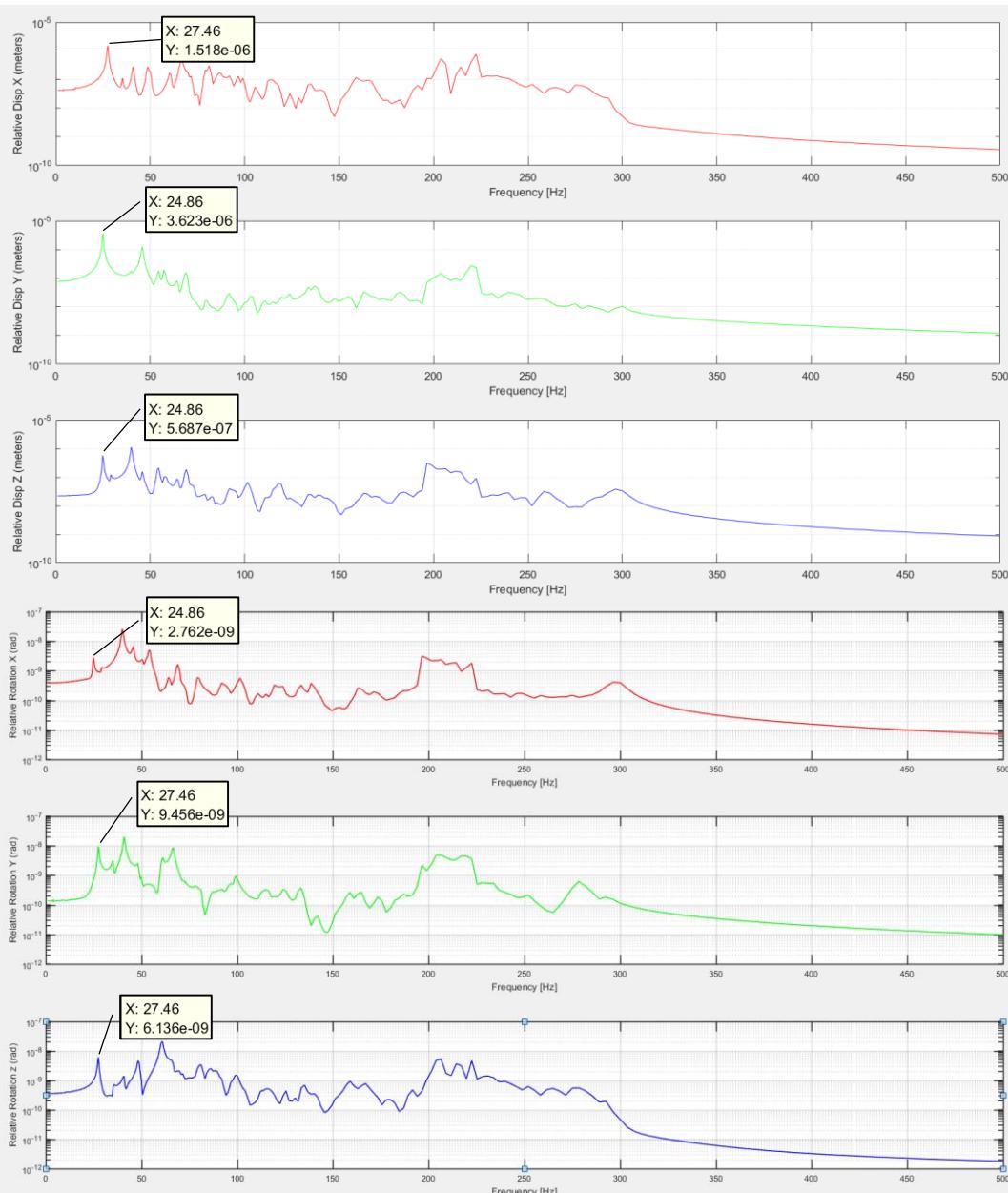
PM first mode motion  
relative to Fold Mirror:

- $\Delta X = 1.5 \mu\text{m}$  at 27 Hz
- $\Delta Y = 3.6 \mu\text{m}$  at 25 Hz
- $\Delta Z = 0.6 \mu\text{m}$  at 25 Hz
- $\Theta X = 2.7 \text{ nrad}$  at 25 Hz
- $\Theta Y = 9.5 \text{ nrad}$  at 27 Hz
- $\Theta Z = 6.1 \text{ nrad}$  at 27 Hz

Are all larger than specified  
LOS Tolerances:

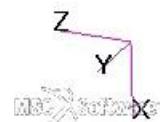
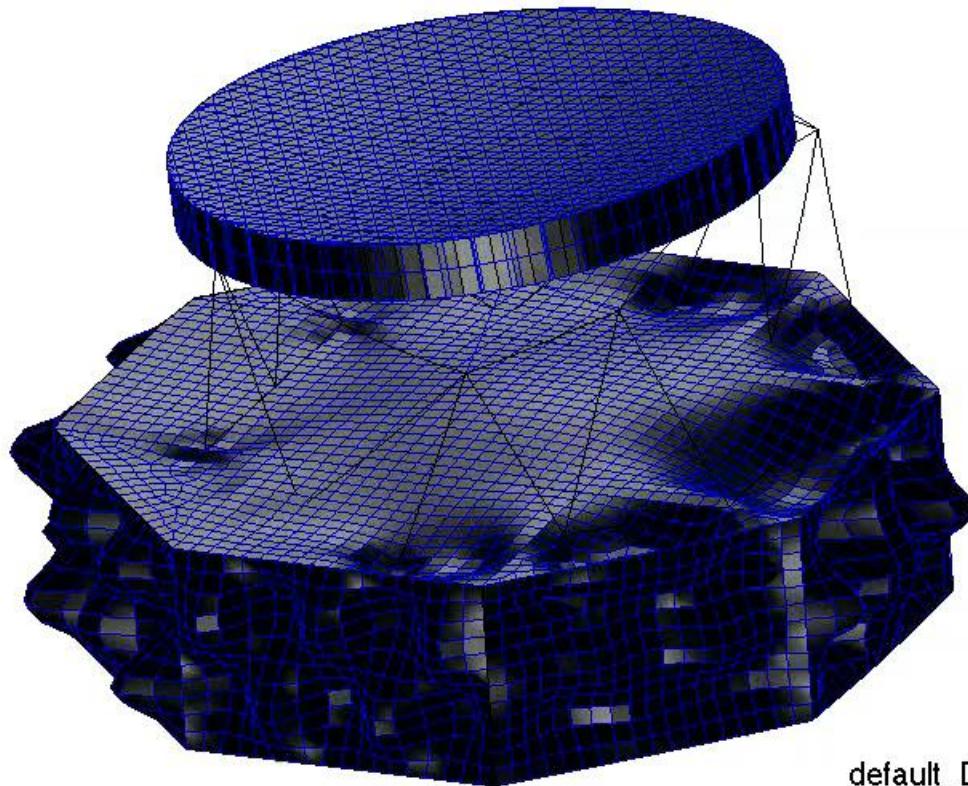
- $\Delta X = 1 \text{ nm}$
- $\Delta Y = 1 \text{ nm}$
- $\Delta Z = 5 \text{ nm}$
- $\Theta X = 0.1 \text{ nrad}$
- $\Theta Y = 0.1 \text{ nrad}$
- $\Theta Z = 0.5 \text{ nrad}$

Need Vibration Isolation

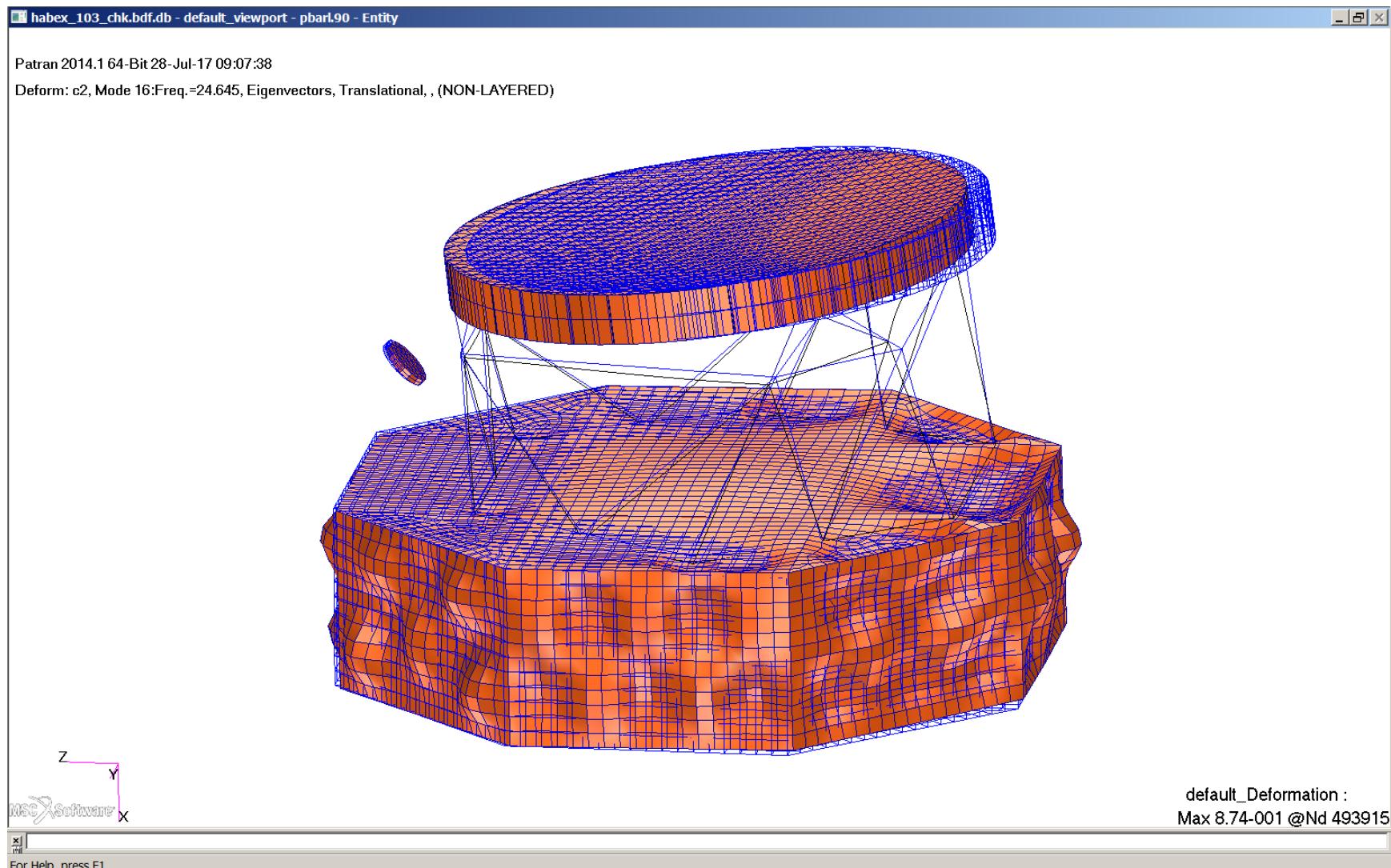


Patran 2014.1 64-Bit 26-Jul-17 12:22:32

Deform: DEFAULT.SC1, Mode 3:Freq.=24.904, Eigenvectors, Translational, , (NON-LAYERED)



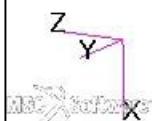
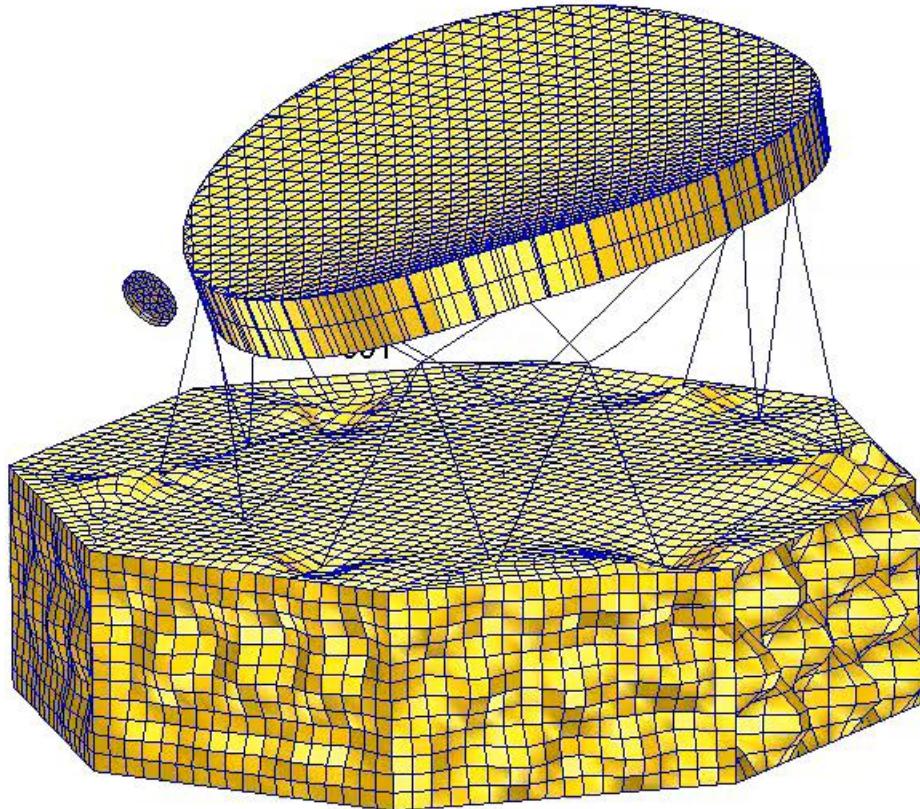
default\_Deformation :  
Max 5.49-001 @Nd 493915  
Frame: 1  
Scale = 1.00+000

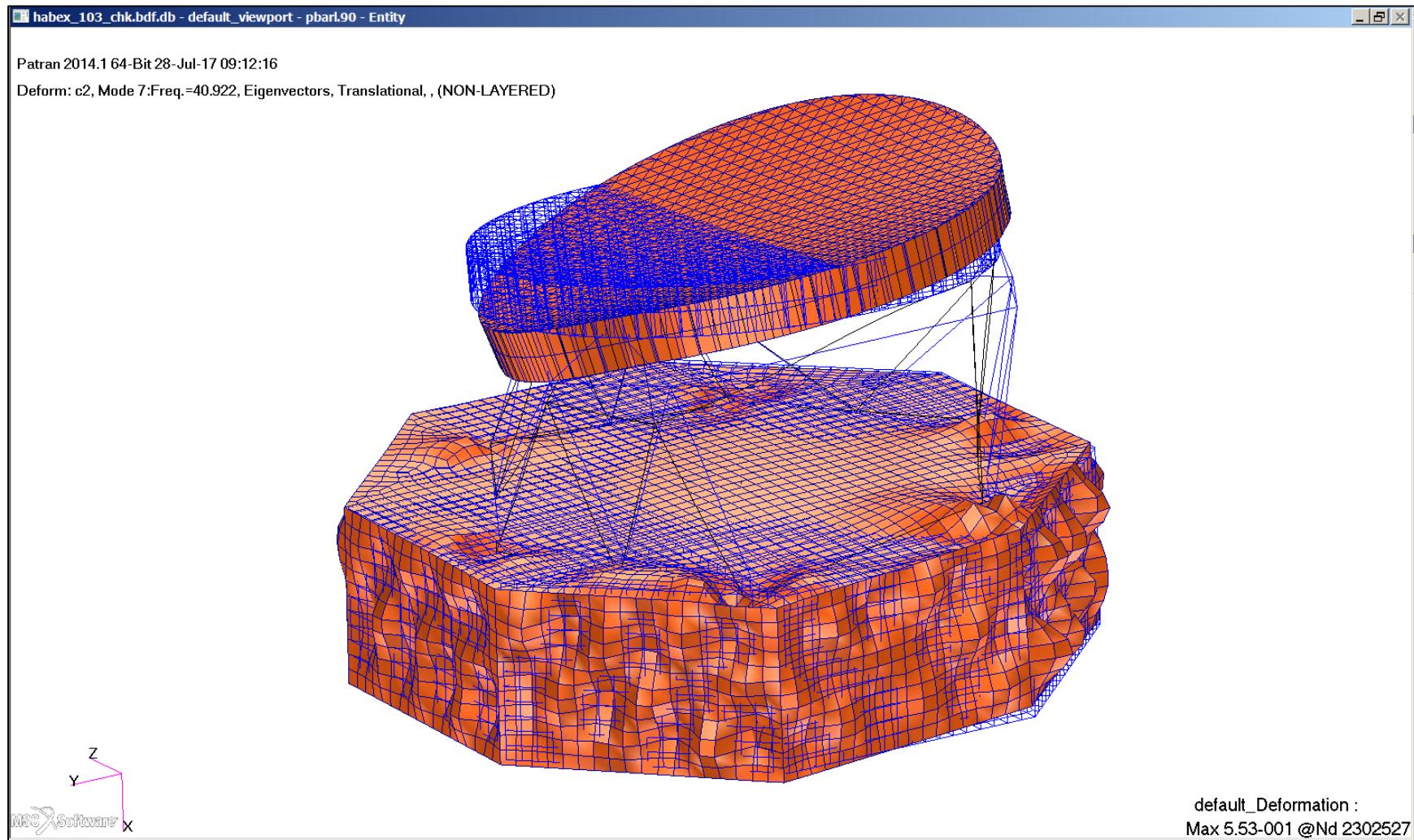


First Mirror Mode

Patran 2014.1 64-Bit 25-Jul-17 13:08:02

Deform: Default, Mode 18:Freq.=42.154, Eigenvectors, Translational, , (NON-LAYERED)

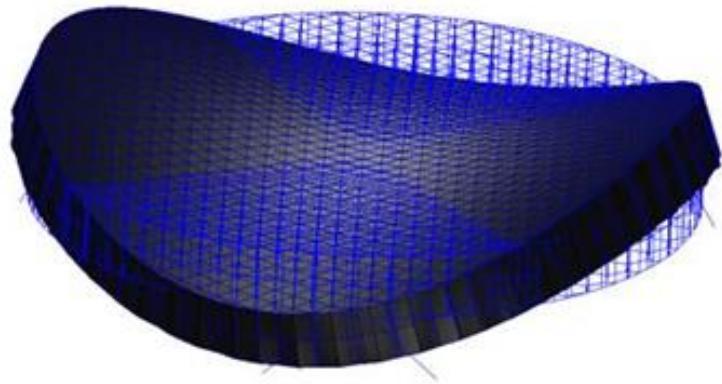




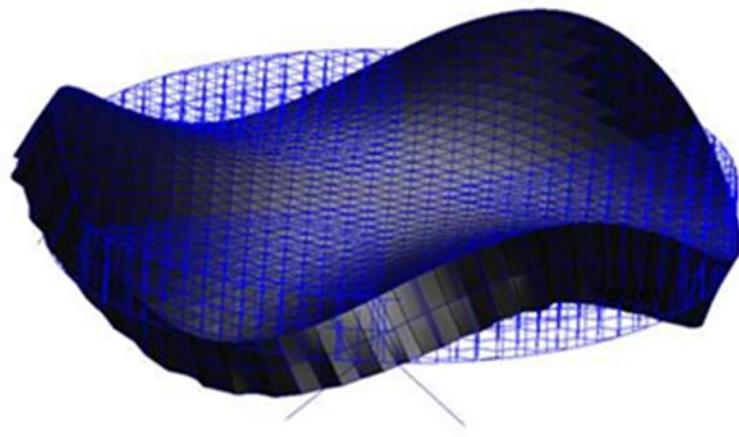
Second Mirror Mode

# Primary Mirror Bending Modes

1<sup>st</sup> Bending Mode at 80 Hz

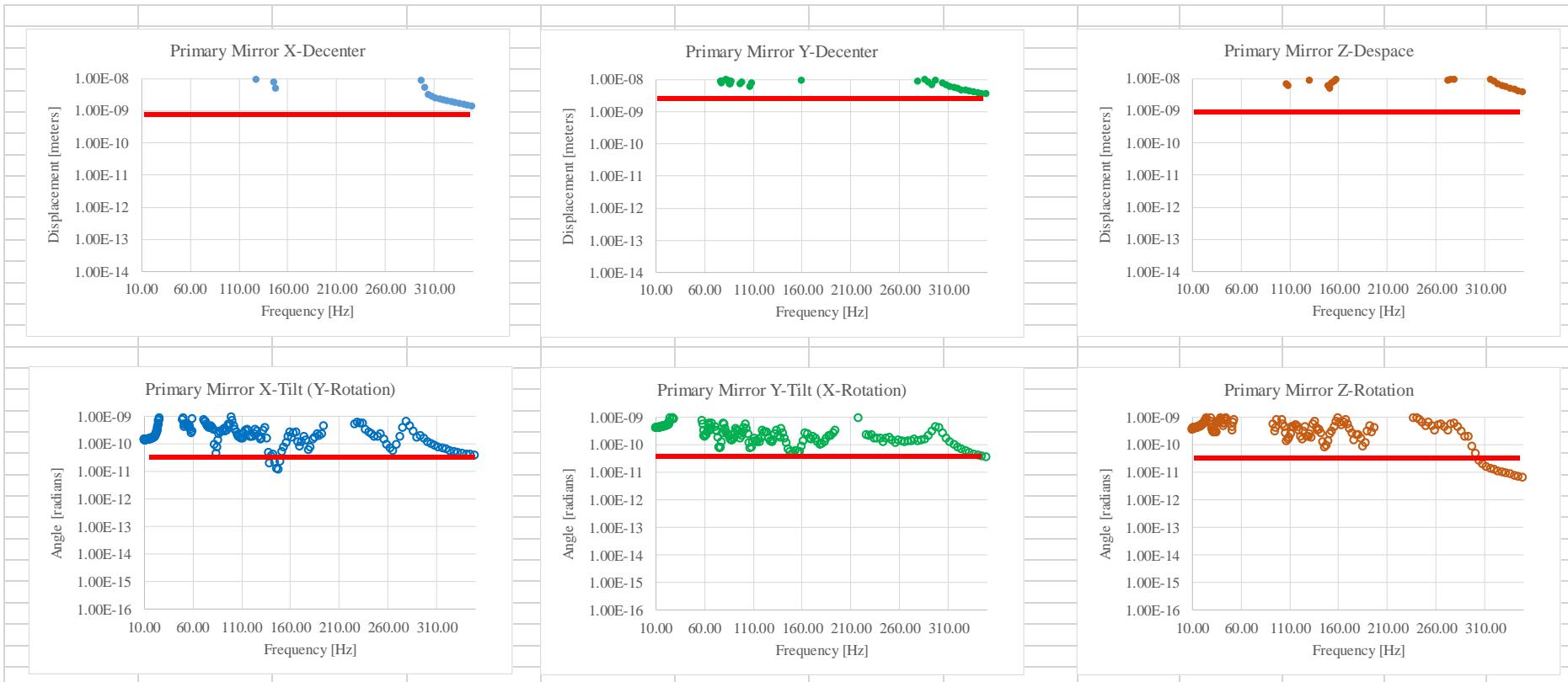


2<sup>nd</sup> Bending Mode at 180 Hz



# Telescope Structure LOS Stability: PM Tolerances

HabEx LOS Stability Tolerances can not be achieved without isolation. Motions induced by a JWST RWA Mechanical Disturbance Spectrum exceeds the LOS Tolerances (red lines)



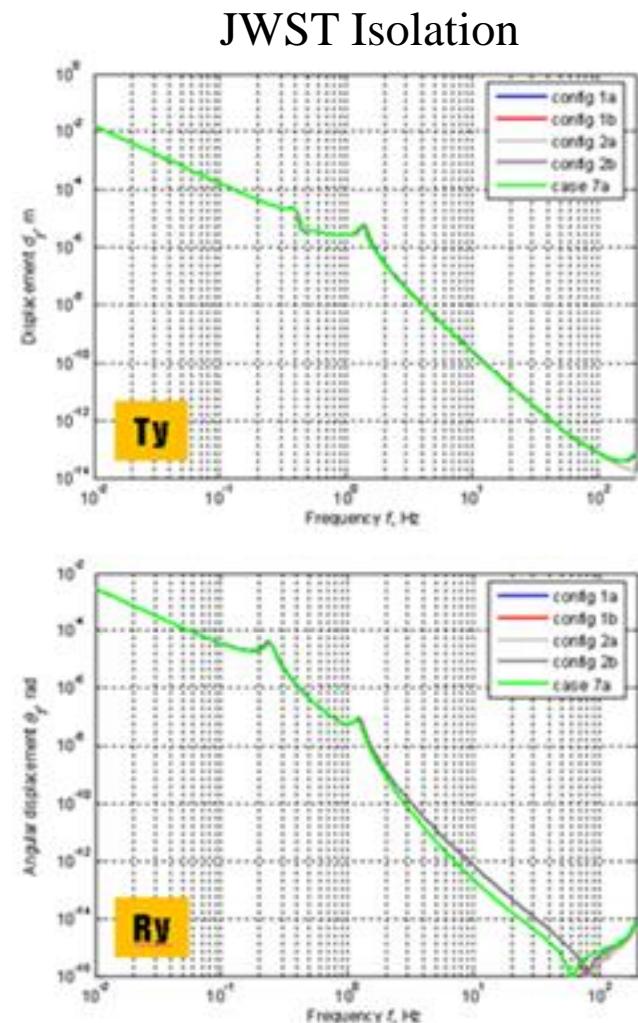
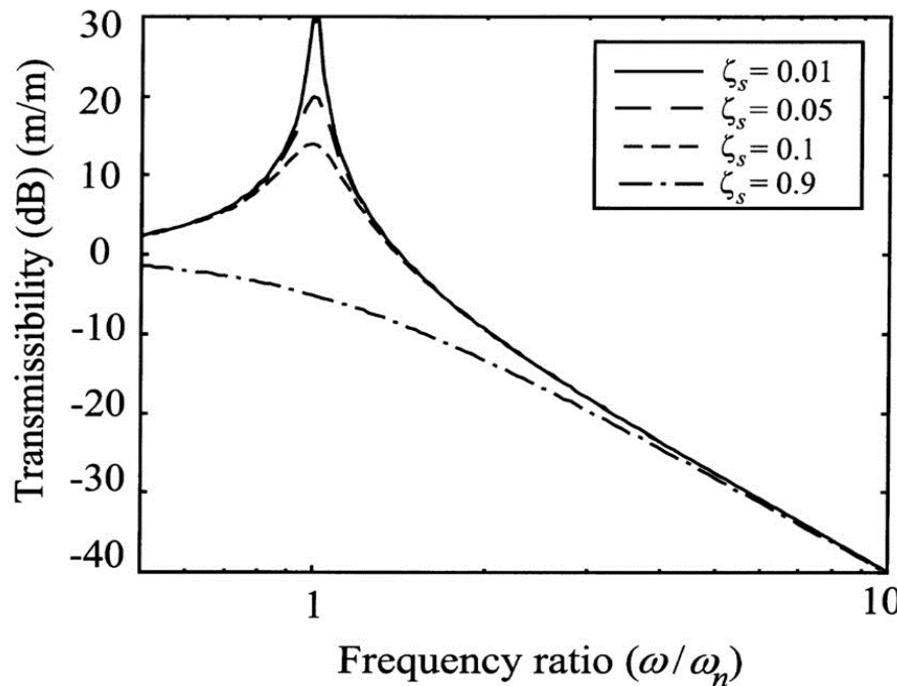
# Vibration Isolation

JWST has 2 passive stages producing 70dB of isolation:

- 8-Hz between reaction wheels & spacecraft.
- 1-Hz between spacecraft and OTA.

## Passive Isolation

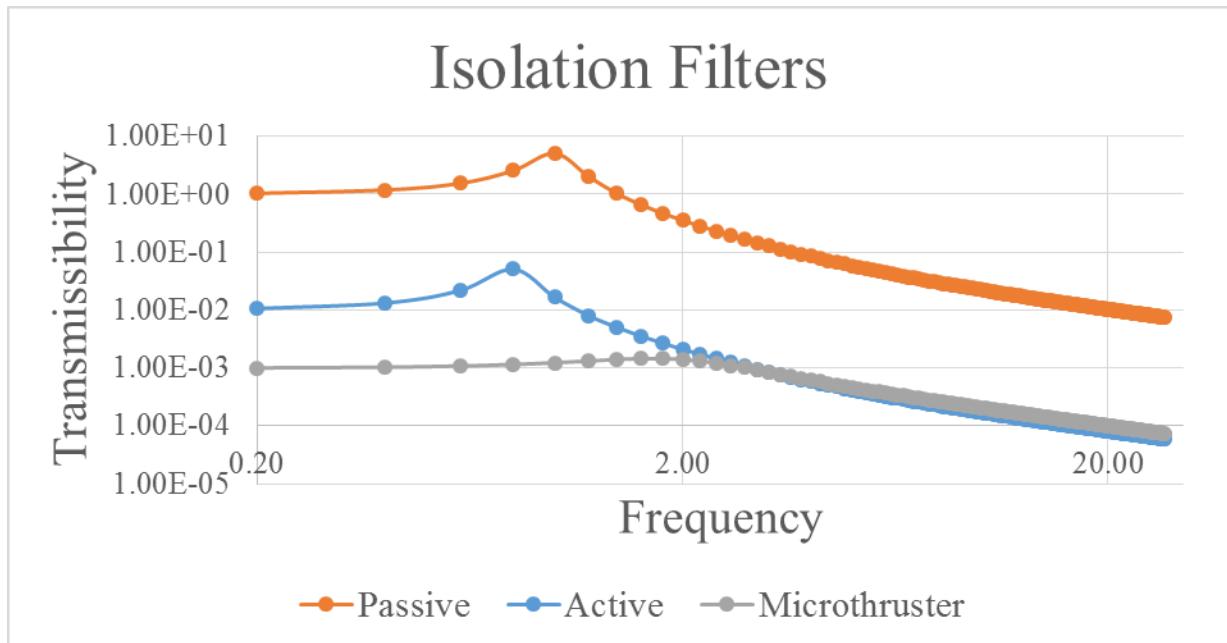
- $\sim 10\text{dB/octave}$
- Damping is important



# Passive vs Active Vibration Isolation

## Theoretical Isolation Filters:

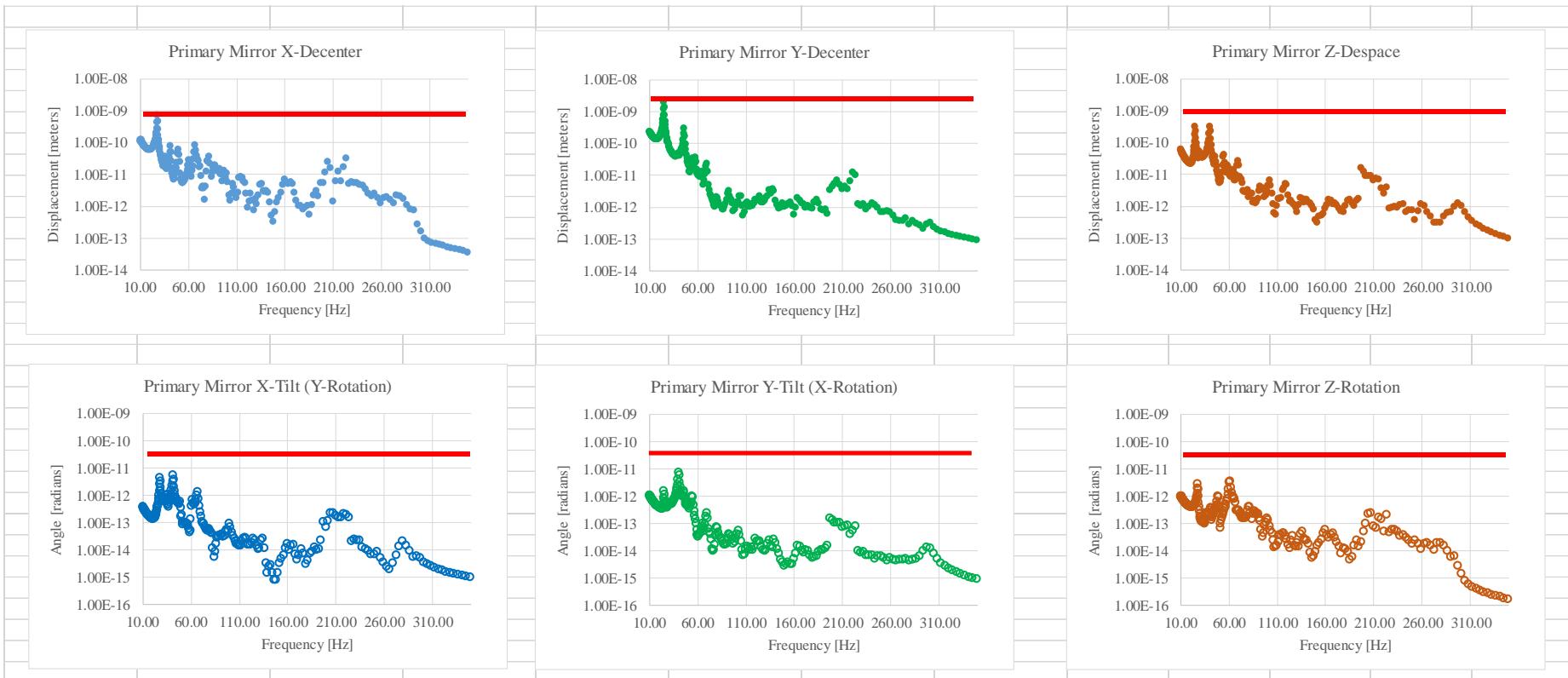
- Passive = 1 Hz, 10% damping
- Active = 40 dB initial reduction, 0.8 Hz, 10% damping
- Micro-Thrusters initial 60 dB reduction, 2 Hz 50% damping



# Telescope Structure LOS Stability: PM Tolerances

THabEx LOS Stability Tolerances can be achieved via applying a Passive 0.5 Hz with 1% damping isolation filter to the rigid body dynamic opto-mechanical response data.

Red Lines are ‘new’ tolerance limits – X-Decenter & Y-Decenter



# Alignment Stability Tolerances

Structural Response (with Isolation) analysis shows that the most important parameter is PM X- & Y-Decenter.

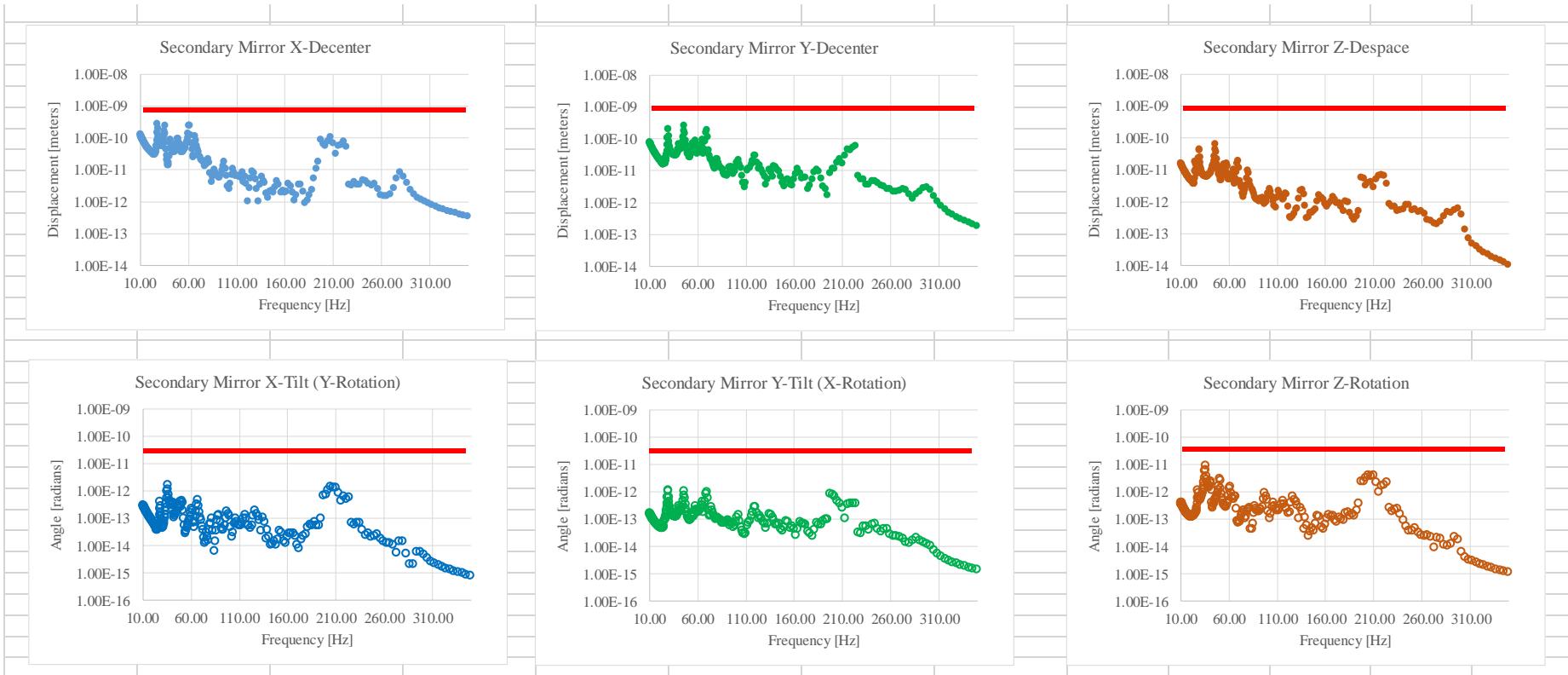
Structural Response analysis allows reallocation of tolerances.

LOS RSS Error										
Alignment	ZEMAX	Input	units	Tolerance	Sensitivity at FSM		ERROR		RSS	Units
					Units	Y-Tilt	X-Tilt	Y-Tilt		
PM X-Decenter	DX	1.5	nanometer	1	nanometer	1.49	0	2.24	0.00	2.24 mas
PM Y-Decenter	DY	2.5	nanometer	1	nanometer	0	1.39	0.00	3.48	3.48 mas
PM Z-Despace	DZ	1	nanometer	1	nanometer	0	0.36	0.00	0.36	0.36 mas
PM Y-Tilt	TX	0.05	nano-radian	1	mas	0.19	79.08	0.00	0.82	0.82 mas
PM X-Tilt	TY	0.05	nano-radian	1	mas	-77.75	-0.08	-0.80	0.00	0.80 mas
PM Z-Rotation	TZ	0.05	nano-radian	1	mas	18.05	0.02	0.19	0.00	0.19 mas
SM X-Decenter	DX	1	nanometer	1	nanometer	-1.32	0	-1.32	0.00	1.32 mas
SM Y-Decenter	DY	1	nanometer	1	nanometer	0	-1.23	0.00	-1.23	1.23 mas
SM Z-Despace	DZ	1	nanometer	1	nanometer	0	-0.36	0.00	-0.36	0.36 mas
SM Y-Tilt	TX	0.05	nano-radian	1	mas	-0.01	-5.46	0.00	-0.06	0.06 mas
SM X-Tilt	TY	0.05	nano-radian	1	mas	5.45	0.01	0.06	0.00	0.06 mas
SM Z-Rotation	TZ	0.05	nano-radian	1	mas	-1.41	0	-0.01	0.00	0.01 mas
TM X-Decenter	DX	10	nanometer	1	nanometer	-0.14	0	-1.40	0.00	1.40 mas
TM Y-Decenter	DY	1	nanometer	1	nanometer	0	-0.14	0.00	-0.14	0.14 mas
TM Z-Despace	DZ	50	nanometer	1	nanometer	-0.01	0	-0.50	0.00	0.50 mas
TM Y-Tilt	TX	3	nano-radian	1	mas	0	-1.5	0.00	-0.93	0.93 mas
TM X-Tilt	TY	3	nano-radian	1	mas	1.57	0	0.97	0.00	0.97 mas
TM Z-Rotation	TZ	100	nano-radian	1	mas	0.02	0	0.41	0.00	0.41 mas
							SUM	-0.17	1.94	1.94 mas

# Telescope Structure LOS Stability: SM Tolerances

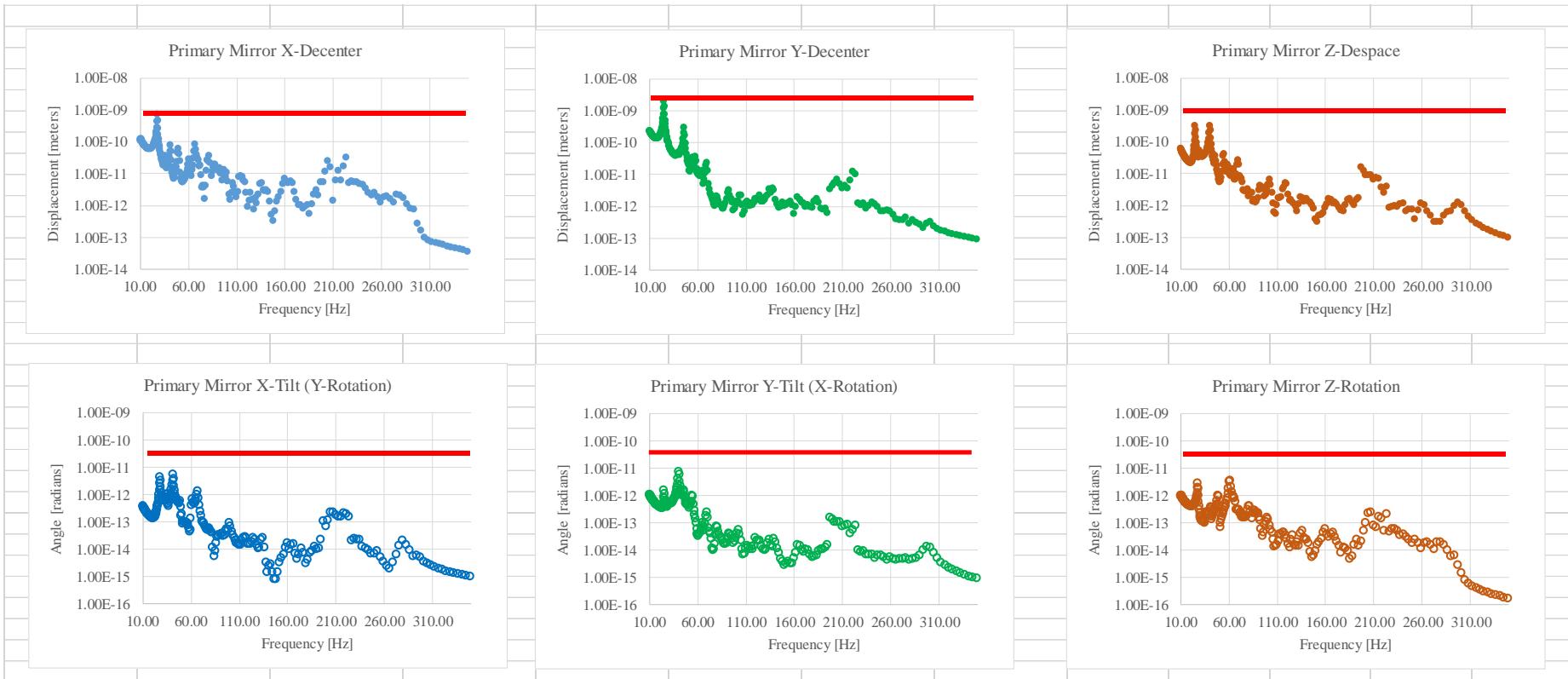
Secondary Mirror rigid body motions have margin against the tolerance limits.

Again, X-Decenter & Y-Decenter are the biggest challenging.



# Telescope Structure LOS Stability: PM Tolerances

Passive 0.5 Hz resonance frequency filter with 1% damping just barely meets LOS Stability Tolerances.

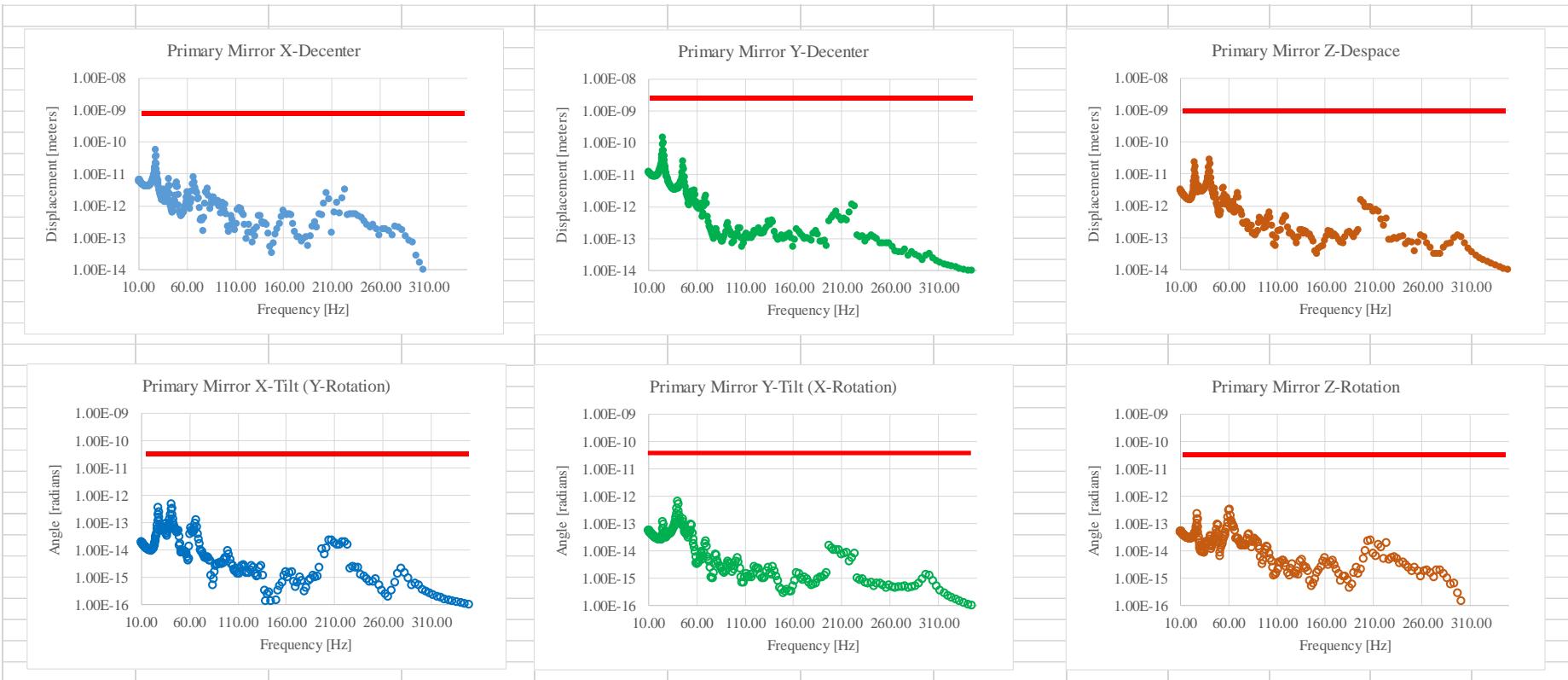


# Telescope Structure LOS Stability: Margin

LOS Stability Tolerances met with margin with:

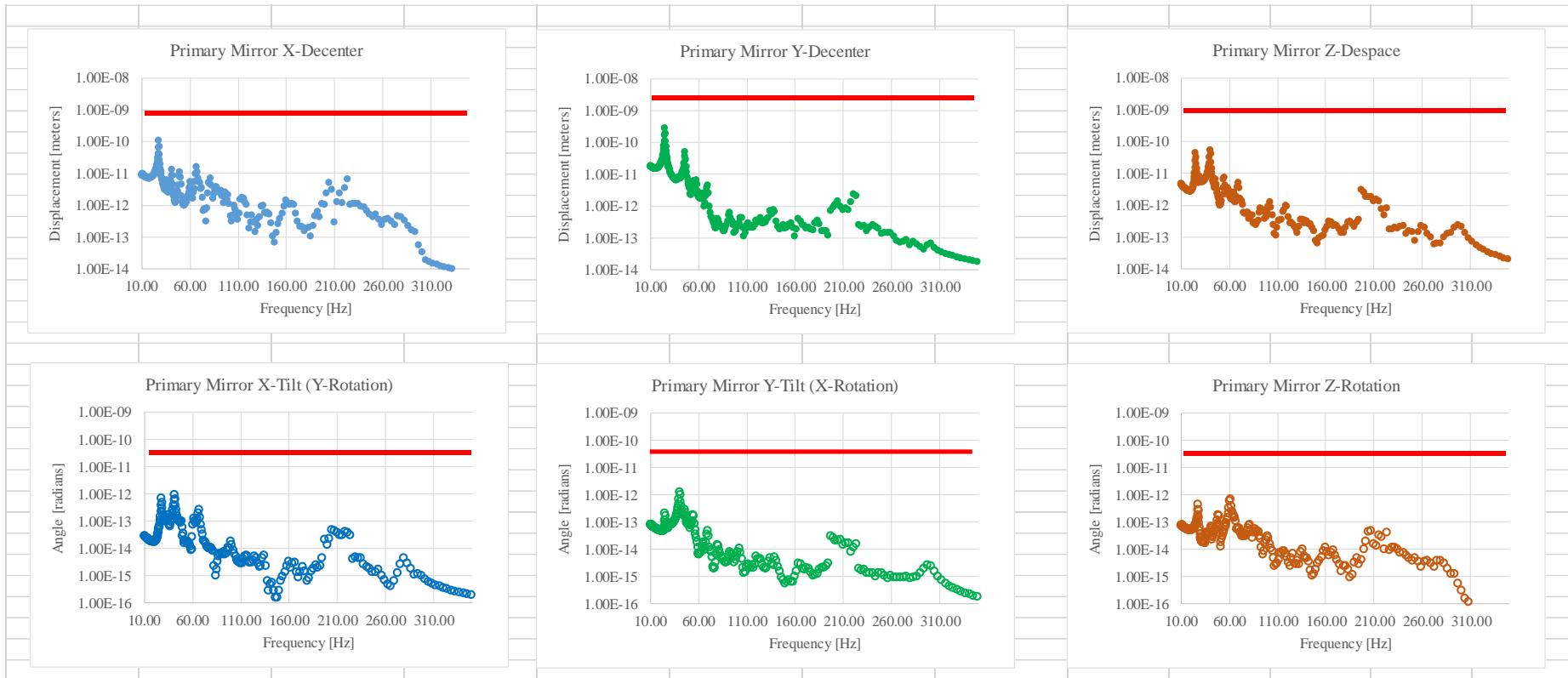
- Active -40dB, 1-Hz filter with 5% damping

Specification similar to Lockheed Disturbance Free Payload (DFP) Vibration Isolation System



# Telescope Structure LOS Stability: Micro-Thrusters

Micro-Thrusters reduce jitter amplitude by a uniform 0.001 (-60dB isolation) with 2 Hz resonant frequency and 50% damping.

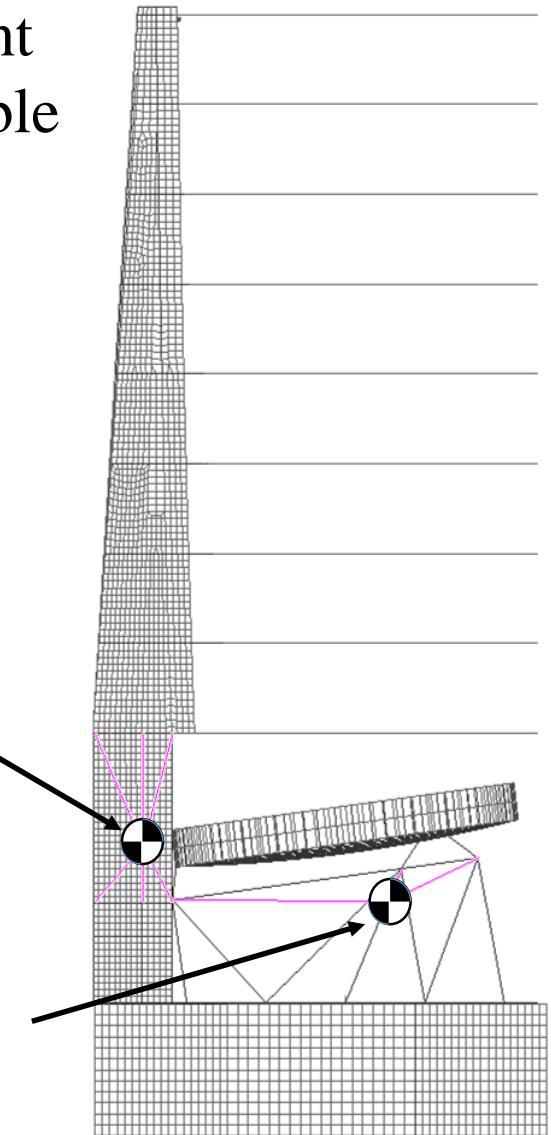


# Science Instrument Mass

Analysis with and without Science Instrument  
lump mass in telescope structure has negligible  
effect on dynamic line of sight performance.

UV Spectrometer	170kg
Coronagraph	650kg
Wide Field Imager	230kg
Star Shade Camera	210kg

UV Spectrometer  
Focal Plane 40kg



# Dynamic Wavefront Error: Mechanical Stability

# Primary Mirror Dynamic Wavefront Error

Dynamic PM WFE arises from two sources:

- Mechanical
- Thermal

Mechanical Vibrations have a temporal spectrum:

- Specific vibration frequencies induce harmonic modal response.
- All other vibration frequencies cause inertial response.

These responses produce structural motions that cause:

- Optical mis-alignment aberrations
- Optical component bending and deformations from mount stress

# Primary Mirror Dynamic WFE

PM Dynamic Error is proportional to Gravity Sag.

- 1 G acceleration = 1 Gravity Sag
- 1  $\mu$ G acceleration = 1  $\mu$ \_Gravity Sag

To minimize PM Dynamic WFE:

- Design the PM Substrate to be as stiff as possible
- Consider the Mount stiffness and location.

Depending on mirror design (stiffness) & mount (3 vs 6 point)

- If Trefoil Gravity sag is 60 micrometers.
- And, if Coronagraph requires < 6 nm of Trefoil
- Then mirror acceleration must remain < 100  $\mu$ G.

# Primary Mirror Dynamic WFE

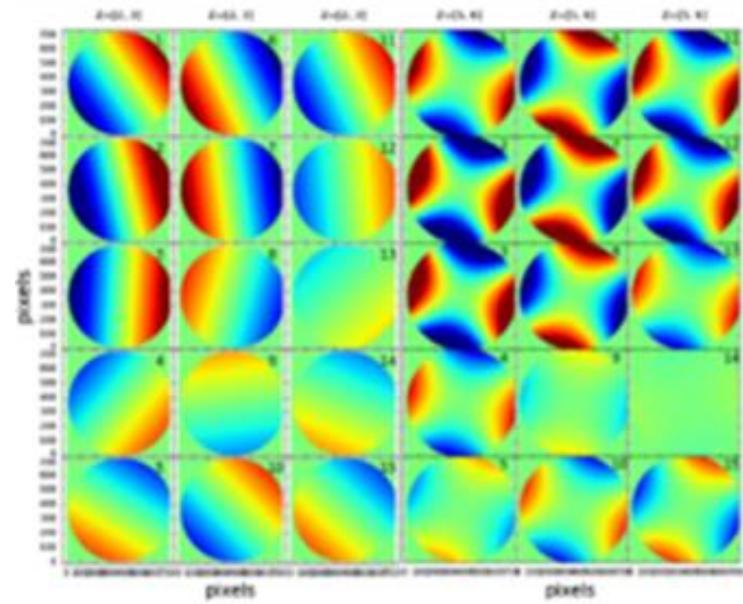
Dynamic WFE depends on the mirror's mounted self-weight deflection (G-sag) and its inertial response function.

G-sag defines the maximum possible WFE for a 1G driving force and a unity response function.

G-sag depends on stiffness of mirror substrate and how it is mounted.

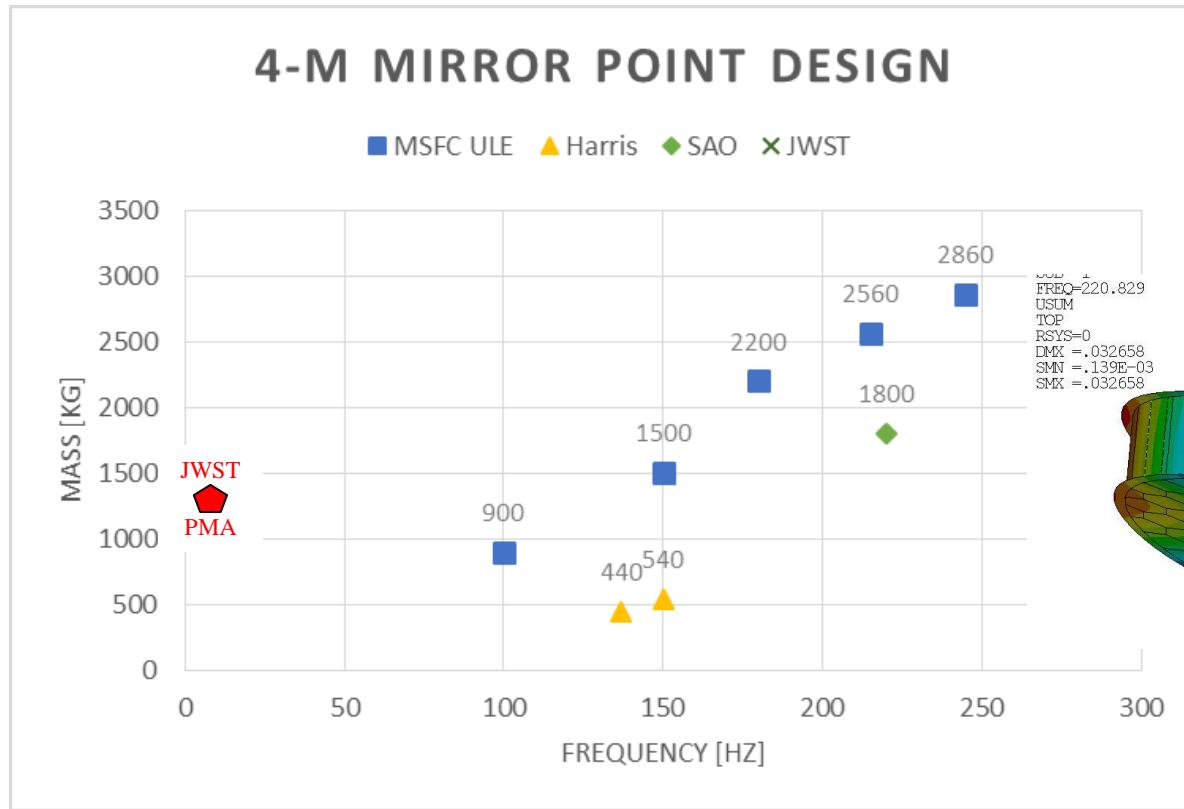
For example, JWST's 220-Hz open-back beryllium primary mirror segments on a 3-point mount have a static horizontal G-sag of approximately 200 nm.

When driven at 87.3 Hz, they have a dynamic Astigmatic WFE of 220 nm per G of driving force.



# ULE 4-m Mirror Trade Studies

MSFC explored range of higher mass, more robust designs.  
Harris Corporation explored lower limit of mass.



JWST total mass of primary mirror segment assemblies (PMSA) is 700 kg, Total PM Assembly mass is 1250 kg. Individual JWST PM substrates are 220 Hz. Individual PMSA are 40 Hz. Total PMA is 16 Hz.

# ULE PM Trade Study: Substrate Stiffness

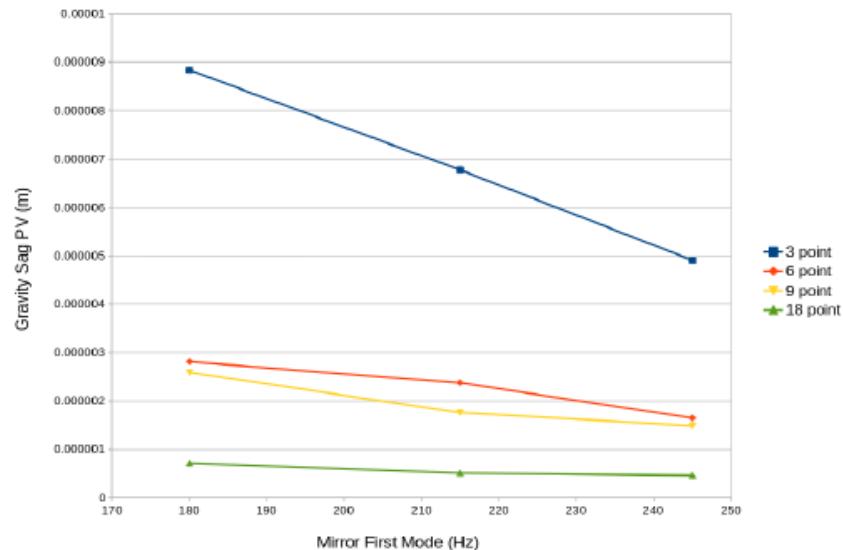
ULE mirrors can be Closed-Back Architectures.

State of Practice Thickness is 35 cm, SOA is 40 cm, 60-cm is developmental.

<b>depth (m)</b>	0.45	0.6	0.75
<b>mass (kg)</b>	1388	1707	1835
<b>cell size (m)</b>	0.167	0.167	0.167
<b>front fs (m)</b>	0.0277	0.0277	0.0277
<b>back fs (m)</b>	0.0231	0.0231	0.0231
<b>1st mode (Hz)</b>	180	215	245

Gravity Sag:

- Stiffer mirror less G-Sag
- More Mount Points less G-Sag

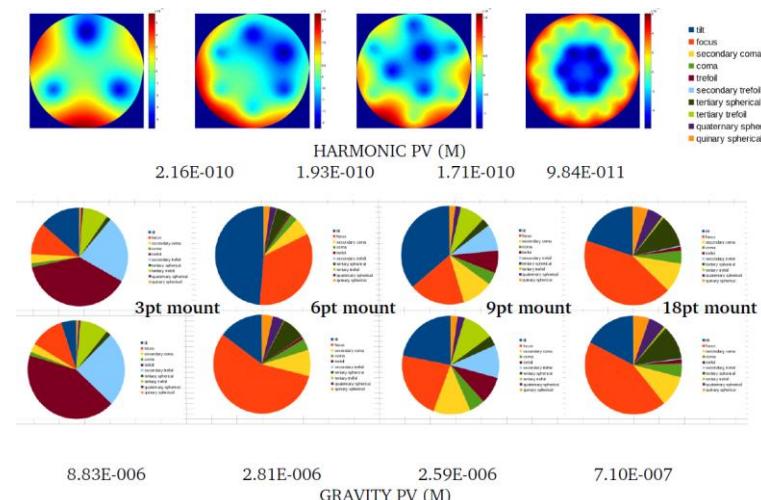


# ULE PM Trade Study: Dynamic WFE

Dynamic WFE for 4-m off-axis 180-Hz 1388-kg Mirror as a function of mount support system when excited at 49.9-Hz by a 1 Newton sinusoidal driving force.

	3POINT	6POINT	9POINT	18POINT
1ST MOUNTED MODAL (HZ)	47.2	50.4	54.1	55.4
HARMONIC PV (M)	2.16E-010	1.93E-010	1.71E-010	9.84E-011
AT FREQUENCY (HZ)	49.9	49.9	49.9	49.8
GRAVITY PV (M)	8.83E-006	2.81E-006	2.59E-006	7.10E-007
SCALE	2.45E-005	6.86E-005	6.61E-005	1.38E-004

Dynamic WFE amplitude is similar to gravity sag.



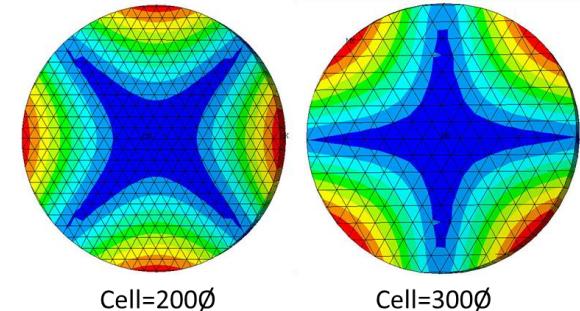
# ZERODUR PM Trade Study: Substrate Stiffness

ZERODUR mirrors are constrained to Open-Back architectures with a maximum thickness of 42 cm.

## Trade Studies:

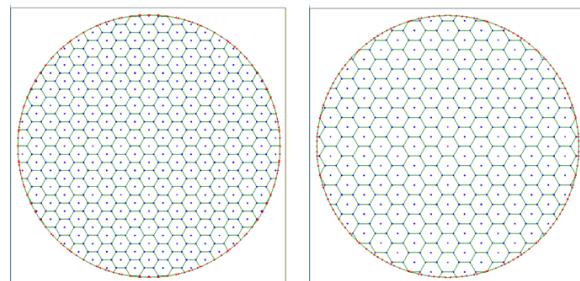
### #1: Isogrid (triangular) Pockets

- First mode ~ 70 Hz.
- Mass ~ 2600 kg



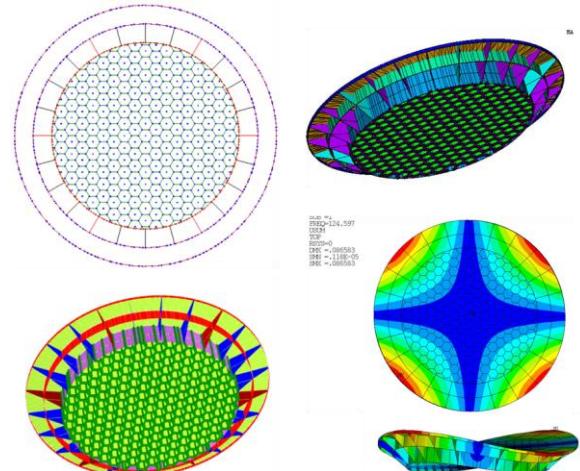
### #2: Hex Pockets with T-back

- First mode ~ 120 Hz.
- Mass ~ 1800 kg

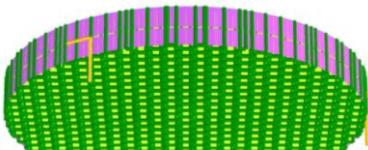
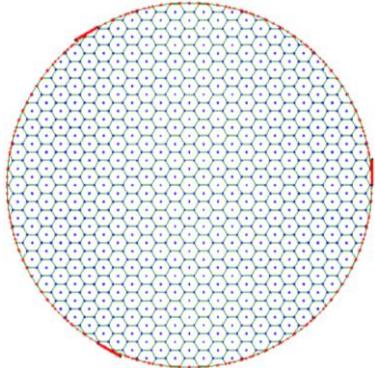


### #3: SOFIA Style

- First mode ~ 125 Hz.
- Mass ~ 1350 kg

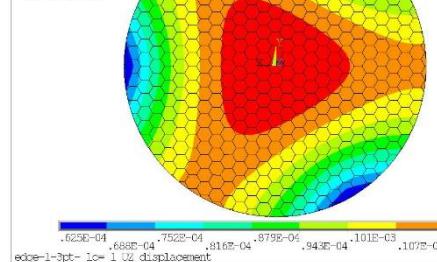


# Support trade studies



STATIC RESPONSE

1. NODAL SOLUTION  
S1E=1  
S2E=1  
T1E=1  
UZ  
TOP  
S2E=0  
DMX = .120E-03  
S2P0=27.0729  
SMX = .020E-04  
SMX = .020E-05



edge-1-3pt- 1c = 1 (processed)

UZ  
S2  
S1

DMX

S2P0

SMX

S2E

SMX

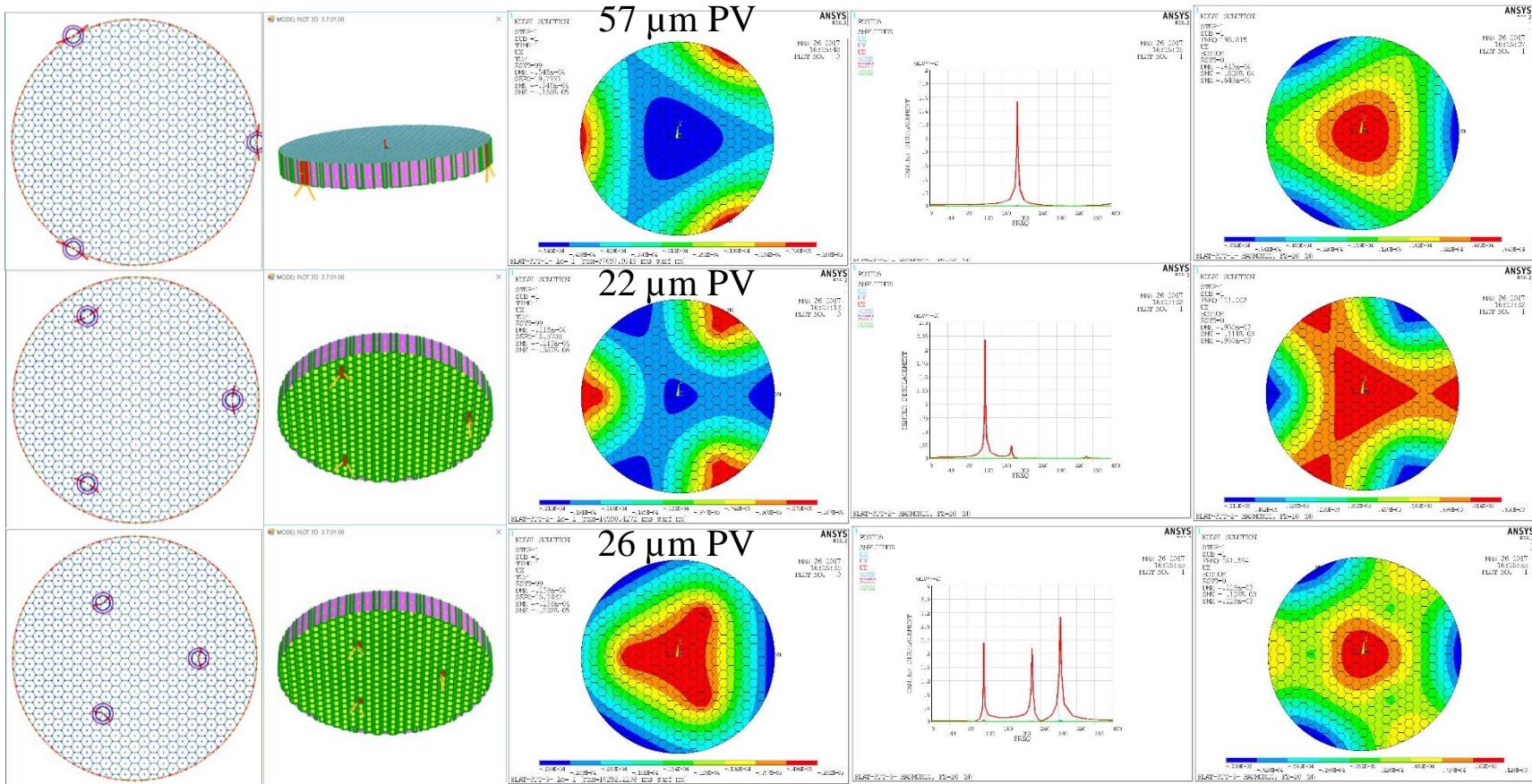
S1E

SMX

S2E

SMX

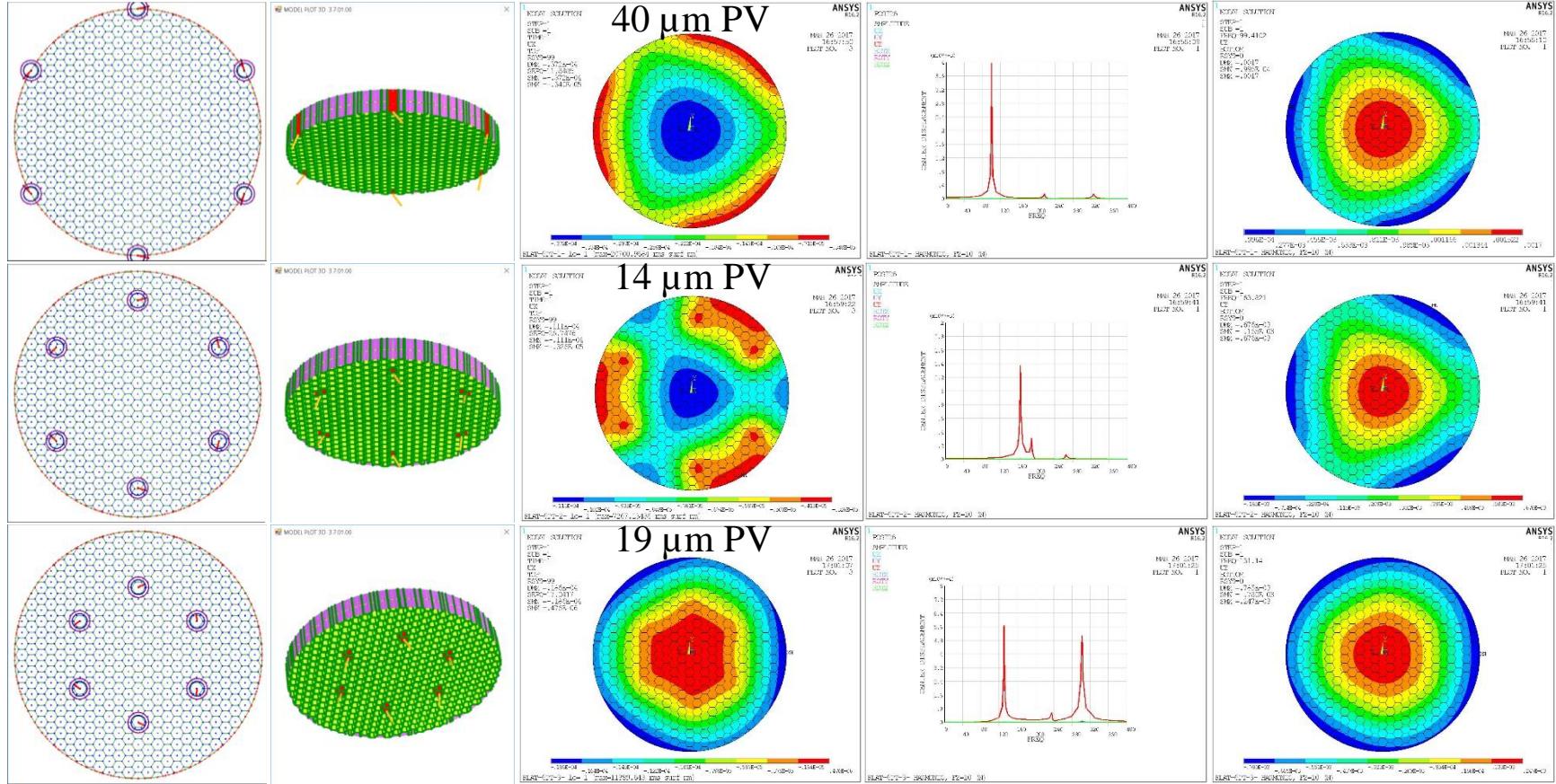
# FLAT 3PT TRADE STUDY



Suspension system consists of beam elements with the desired stiffness and geometry.

Mirror and Mount system assumes 0.5% dampening give a Q (amplification factor) about 100X on transmissibility.

# FLAT 6PT TRADE STUDY

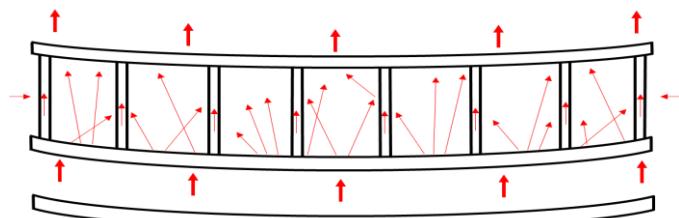
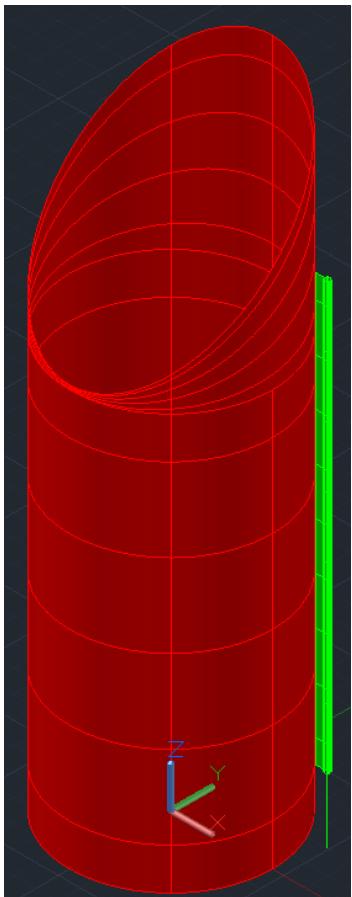


# Dynamic Wavefront Error:

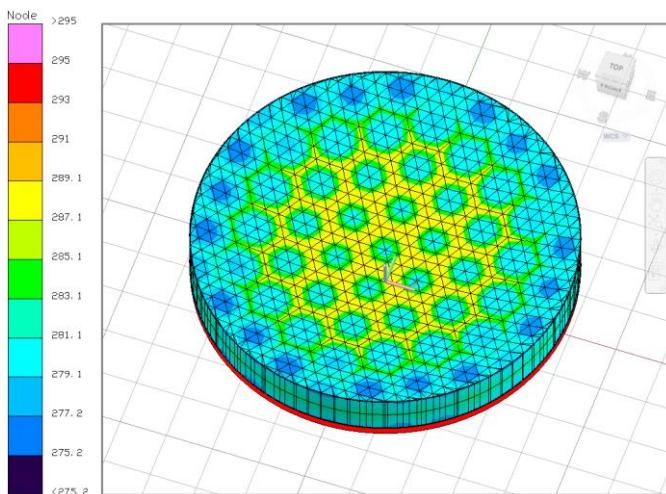
## Thermal Stability

Thermal changes produce structural and component motions as a result of material response (bulk CTE and CTE homogeneity)

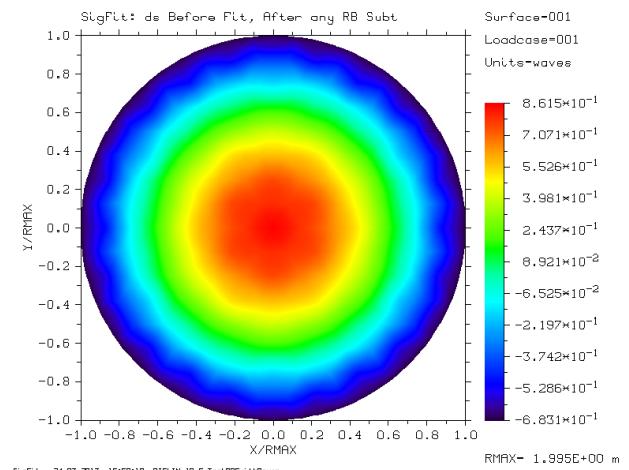
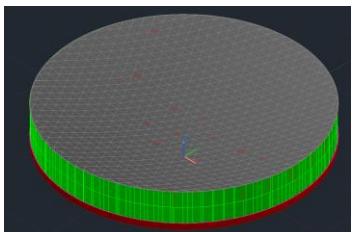
# Static Thermal WFE



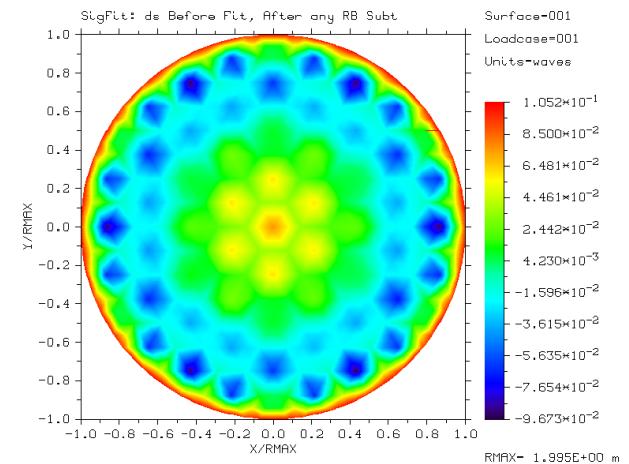
0.5 m thick closed-back ULE mirror  
 Radial Gradient depends on view factor  
 and side insulation.



Temperature gradient  
 Keeping Front Surface > 273K  
 20C Axial; 10C Radial



SFE from isothermal with defocus  
 SFE = 977 nm PV; 288 nm RMS



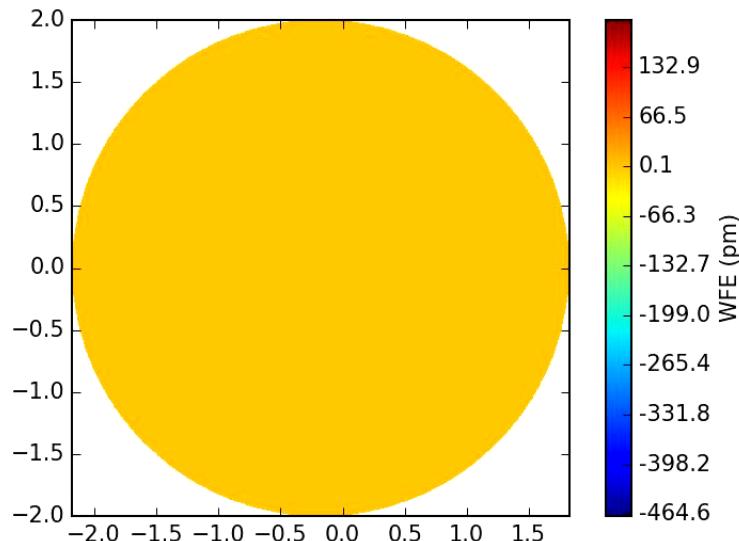
SFE from with defocus removed  
 SFE = 128 nm PV; 24 nm RMS

# Dynamic Thermal WFE Video

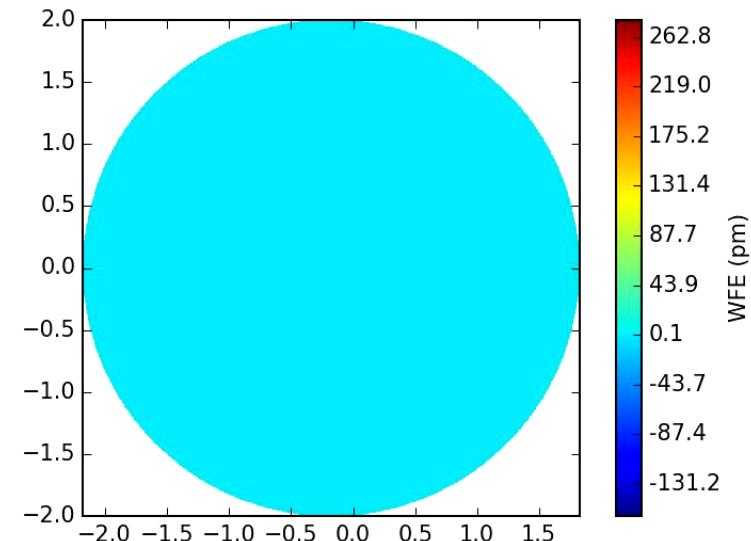
Passive Wavefront Error from 1 hour exposure.

Sun angle changes by 0.0411 degree per hour.

All Errors



Power Removed



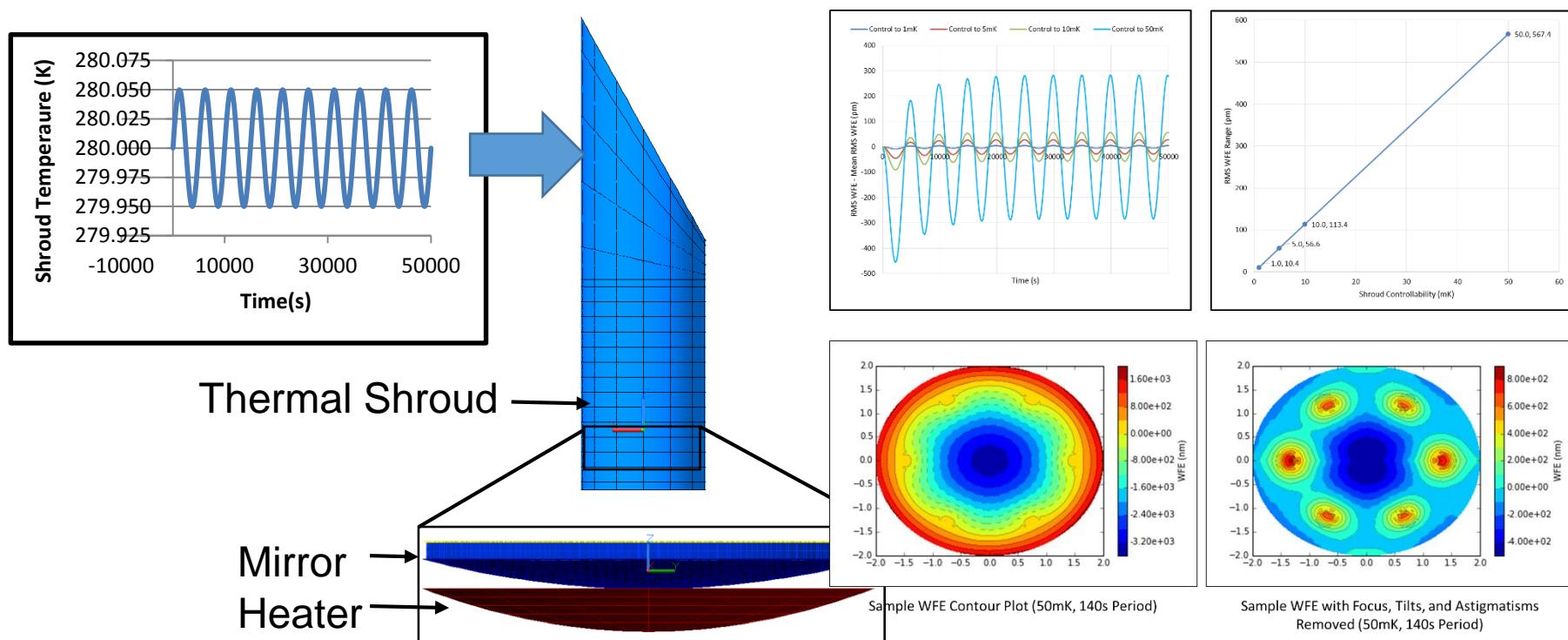
WFE/1-hour = 233 pm PV  
WFE/20-min = 28 pm

WFE/1-hour = 101 pm PV  
WFE/20-min = 13 pm

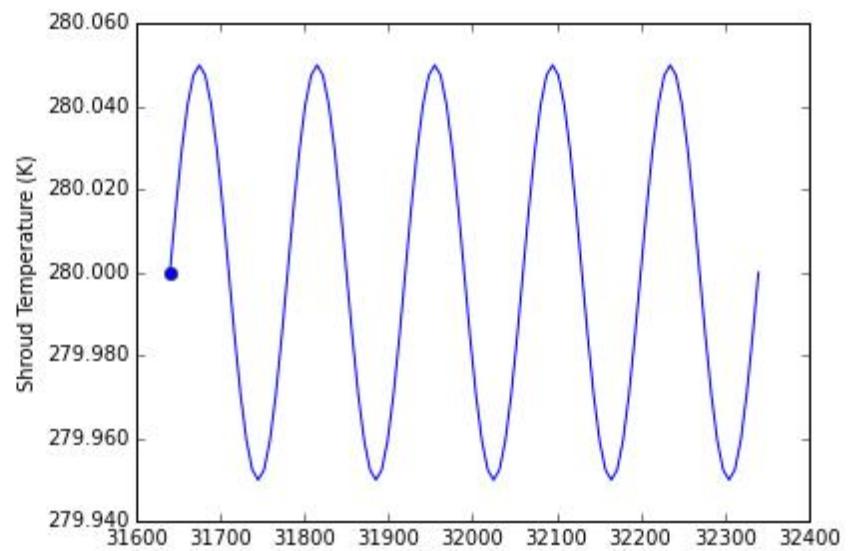
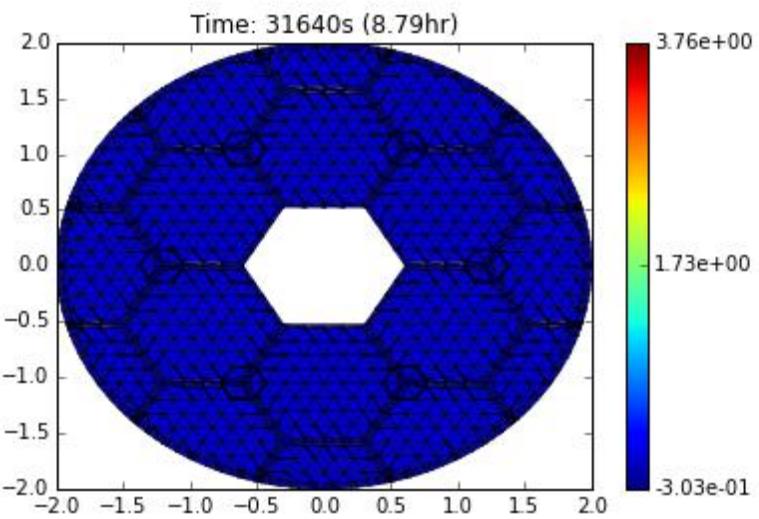
# Dynamic Thermal WFE

Primary mirror responds to dynamic external thermal load

Required stability (10 pm per 10 min) can be achieved by controlling the telescope thermal environment.



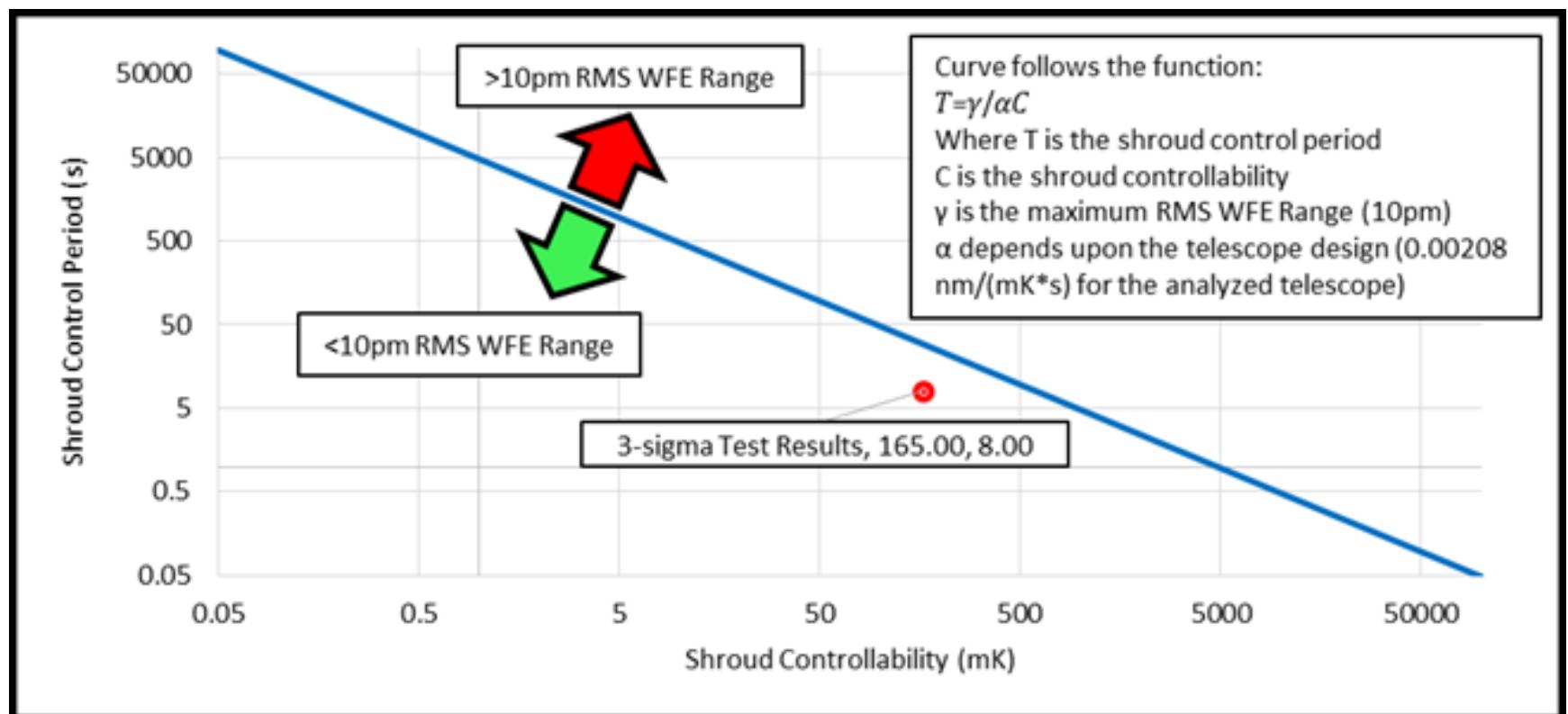
# 4m Aperture Transient WFE Video



# Thermal Stability

The ability to achieve any required wavefont stability depends on:

- Mirror Substrate Properties: CTE, Thermal Mass, Conductivity, etc.
- Thermal Environment Controllability
- Control Period.



# Conclusions

# Conclusions

HabEx requires an OTA with unprecedented stability.

Baseline Design Closes for LOS Stability using TRL9 technology

Baseline Design enhanced via active isolation or micro-thrusters

Design Philosophy – Passive First, then Active as Required.

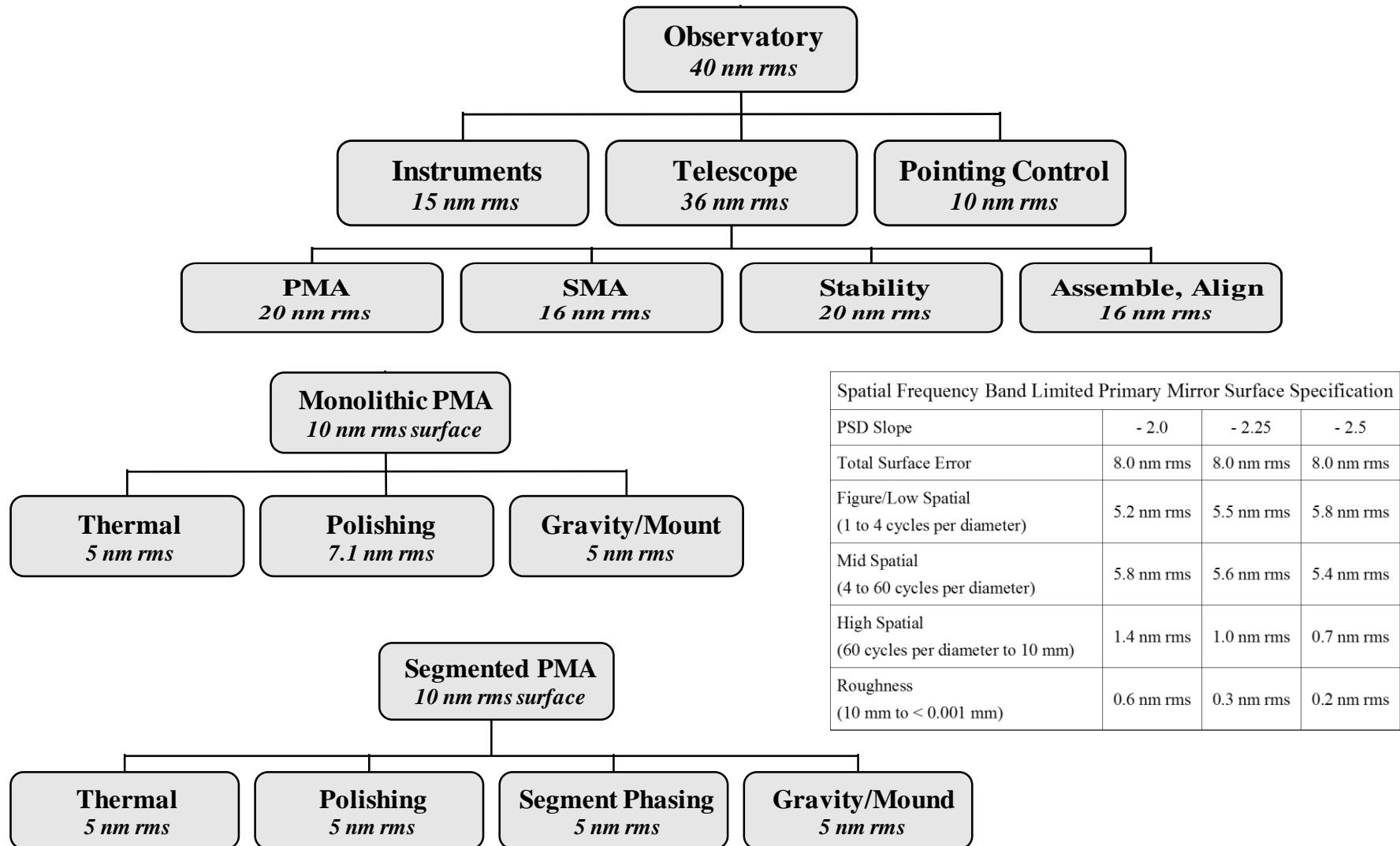
Baseline Design may require Predictive Thermal Control

Because of the optical designs sensitivity to LOS over WFE, to verify Baseline Design – may not need to measure picometers of WFE – instead measure 5 mas LOS stability (LOFS  $\sim$  0.2 mas).

# BACKUP: WFE Specification

# Diffraction Limit WFE

Diffraction Limit of 500 requires total system WFE  $\sim 38$  nm rms



# PM SFE Spatial Frequency Specification

Shaklan shows that a UVOIR mirror similar to Hubble (6.4 nm rms) or VLT (7.8 nm rms) can meet the requirements needed to provide a  $< 10^{-10}$  contrast ‘dark hole’.

- If PM is conjugate with the DM, then PM low-order errors are compensated by DM.
- Recommends  $< 4$  nm rms above 40 cycles
- Both HST & VLT surface figure error is so small enough that there is negligible Contrast reduction from frequency folding
- Because VLT is larger, stiffer and not light-weighted, it is actually smoother at frequencies of concern

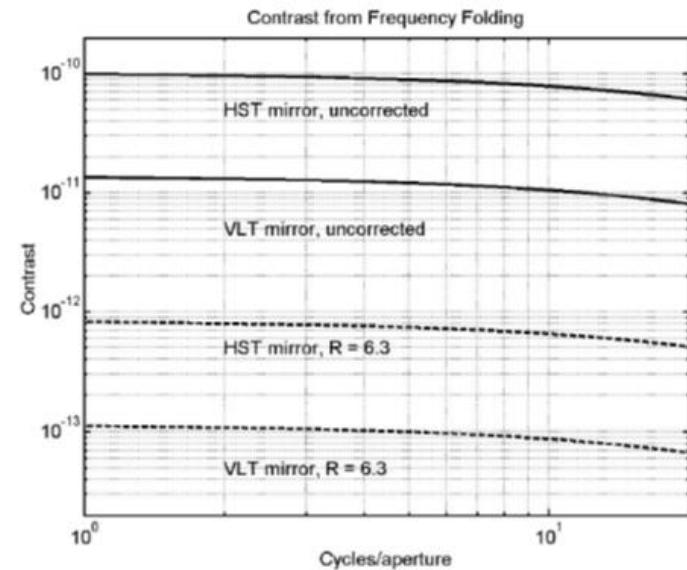


Figure 7. Contrast from frequency folding for spatial frequencies above 48 cycles per aperture, for an 8-m VLT primary and the 2.4 m HST primary. The uncompensated effect is above the required level of  $10^{-12}$  for both mirrors. The sequential DM configuration provides about  $\sim 100$ x reduction of the contrast when it compensates the center of a 100 nm bandpass centered at 633 nm. Both mirrors are acceptable after compensation. The frequency folding effect can be perfectly compensated by the Michelson configuration and is not present in the Visible Nuller.

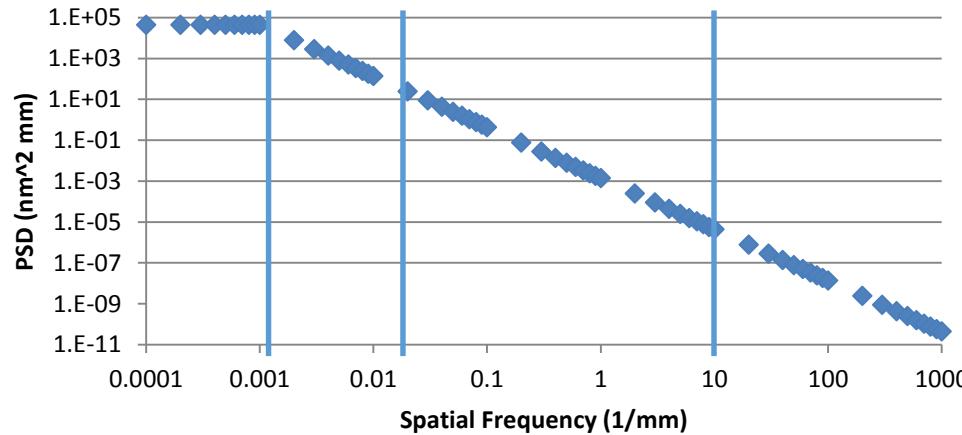
# PM Manufacturing Specification

Define band-limited or spatial frequency specifications

Figure/Low	(1 to SF1 cycles/aperture)
Mid Spatial	(SF1 to SF2 cycles/aperture)
High Spatial	(SF2 cycles/aperture to 10 mm)
Roughness	(10 mm to < 1 micrometer)

Assume that Figure/Low Frequency Error is Constant

Key questions is how to define SF1 and SF2



Also, what is proper PSD Slope

# Low/Mid Spatial Frequency Specification

To best of my knowledge, there is no precise definition for the boundary between Figure/Low and Mid-Spatial Frequency.

Have seen values ranging from 4 cycles to 10 cycle.

Many assert that Zernike Polynomial Set defines Figure/Low  
Harvey defines Figure/Low errors as removing energy from core  
without changing shape of core, and Mid errors as changing the  
shape of the core:

We choose 4 cycles

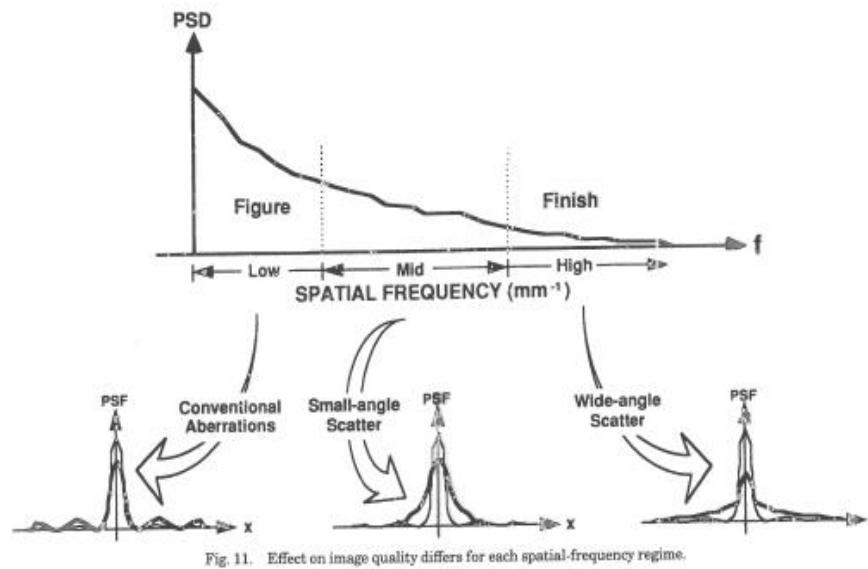


Fig. 11. Effect on image quality differs for each spatial-frequency regime.

# Mid/High Spatial Frequency Specification

Exo-Planet Science requires a Deformable Mirror to correct wavefront errors and create a ‘Dark Hole’ for the coronagraph.

A 64 x 64 DM can theoretically correct spatial frequencies up to 32 cycles per diameter to create the ‘dark hole’ but in practice, the limit is approx 20 cycles per diameter.

3X aliasing can cause spatial frequency errors to put energy into the ‘dark hole’; need smooth WFE up to 60 cycles/diameter.

Higher spatial frequencies scatter energy outside of ‘dark hole’.

We will use 60 cycles as the Mid/High boundary.

HabEx is planning to use 96 x 96 DM (or larger) to get as large of an OWA as possible. Thus, PM must be smooth to maybe 100 cycles per diameter.

# Intuition Cross-Check

JWST WFE Stability spec < 13 nm rms

Because of dampening, a warm JWST may have WFE < 2 nm rms.

HabEx Design SM Tower is ~28 Hz or ~4X higher frequency and ~16X lower amplitude than JWST.

Mass dampening gives 2X reduction.

Total SM WFE ~ 25 pm rms (coma)

JWST PM is 17 Hz, HabEx PM is 120 Hz (Zerodur) to 180 Hz (ULE) or 7X to 10X higher frequency and 50X to 100X lower amplitude.

