



# Wall Modeled Lattice Boltzmann and Navier-Stokes Approaches for Selected RCA Cases

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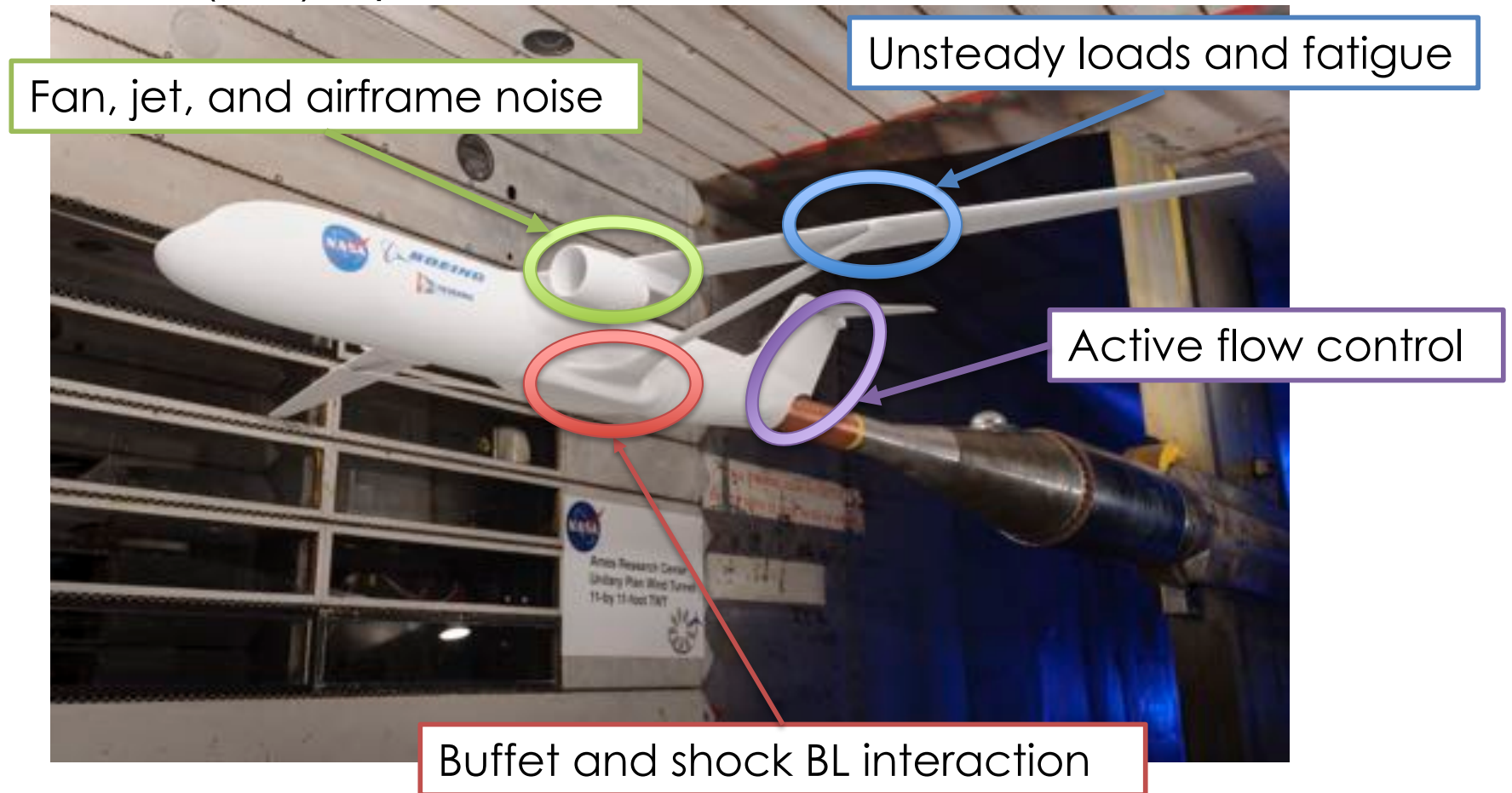


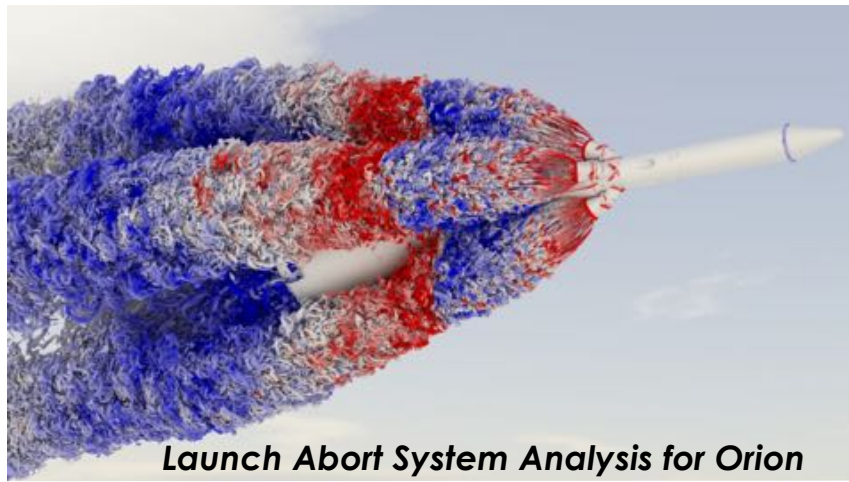
- ✓ **Motivation**
- ✓ **Computational Methodology and Framework**
  - Structured Overset Curvilinear
    - Hybrid RANS/NLES, DDES, ZDES Mode 3
  - Cartesian Lattice Boltzmann Method (LBM)
- ✓ **NASA RCA propulsion case**
  - Round Jet SP7
    - uRANS, DDES, Hybrid RANS/NLES
- ✓ **NASA RCA separated flow case**
  - 2-D NASA Hump
    - RANS, DDES, Zonal DES Mode 3
    - Lattice Boltzmann Method
- ✓ **Summary and Future Work**

# Motivation

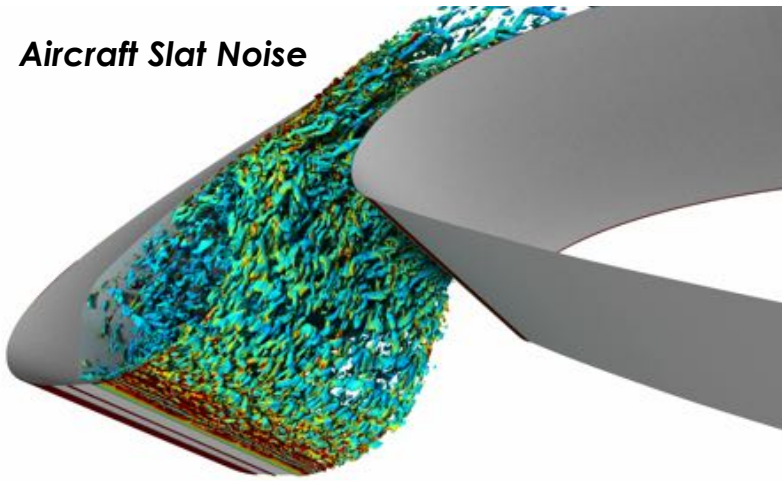


- ✓ **Increase predictive use of computational aerosciences capabilities for next generation aviation and space vehicle concepts.**
  - The next frontier is to use wall modeled and/or wall resolved large-eddy simulation (LES) to predict:

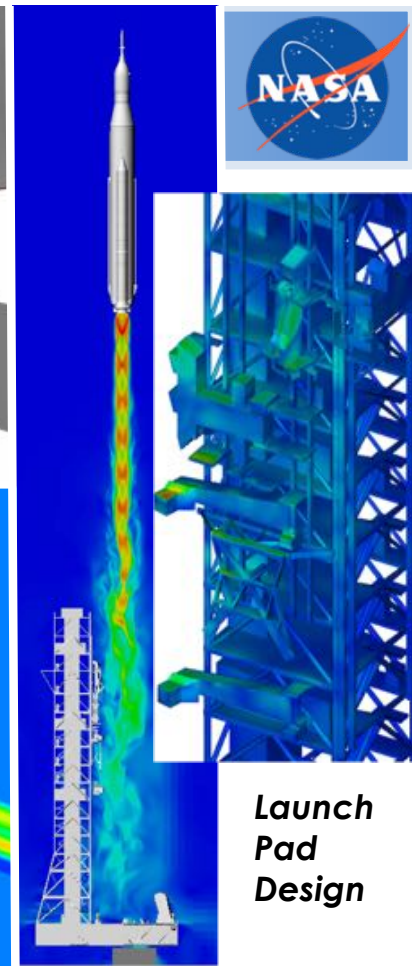




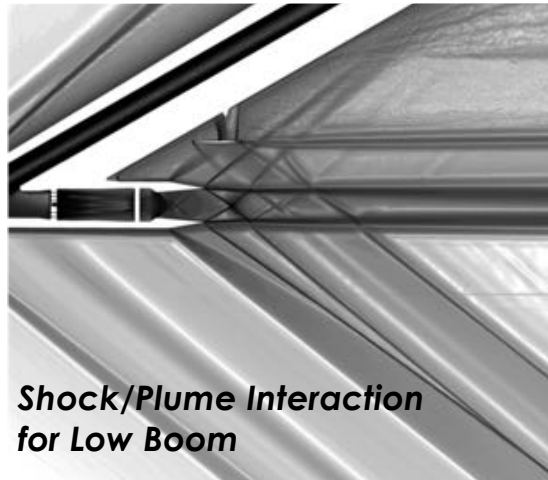
**Launch Abort System Analysis for Orion**



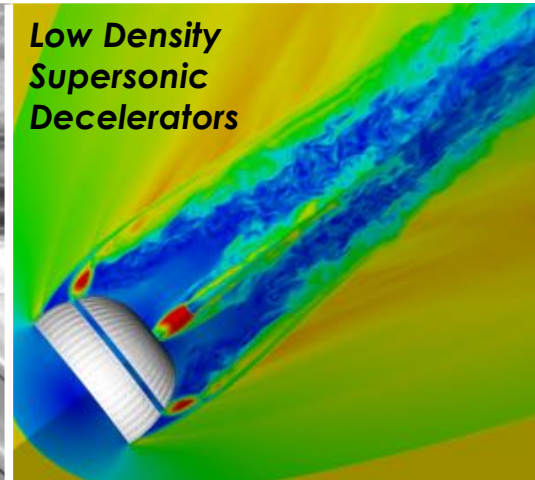
**Aircraft Slat Noise**



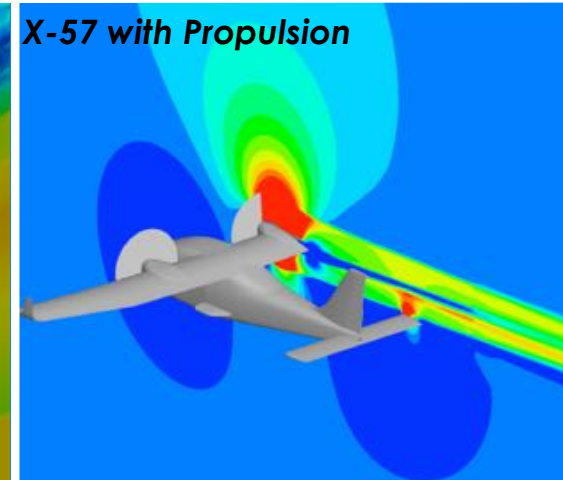
**Launch Pad Design**



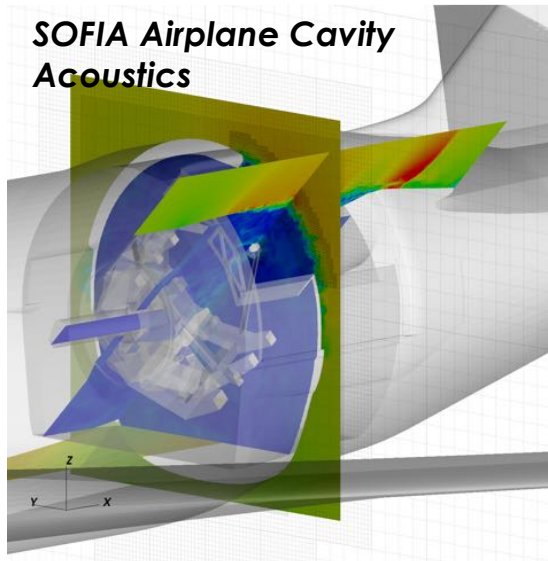
**Shock/Plume Interaction for Low Boom**



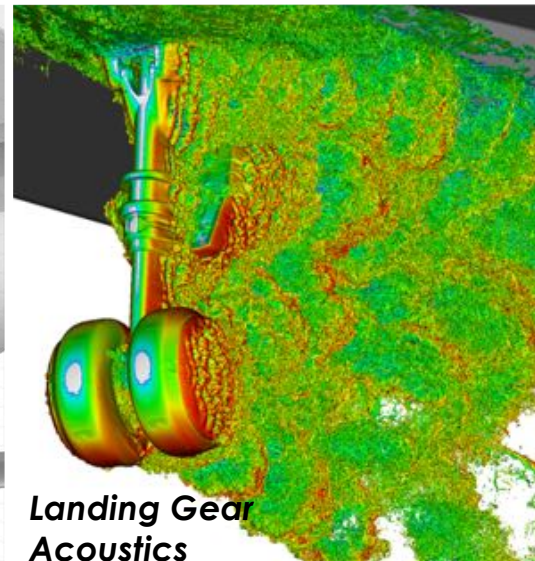
**Low Density Supersonic Decelerators**



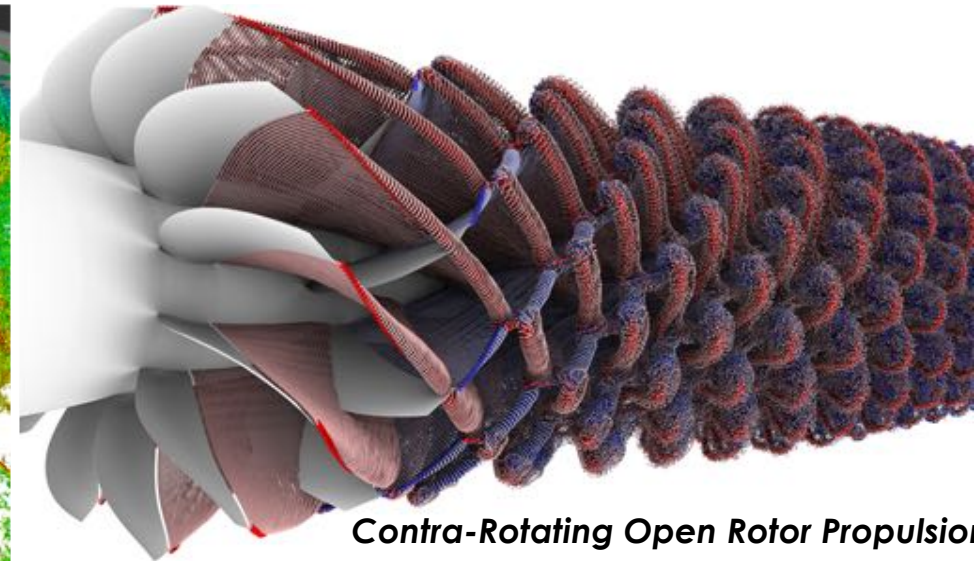
**X-57 with Propulsion**



**SOFIA Airplane Cavity Acoustics**



**Landing Gear Acoustics**

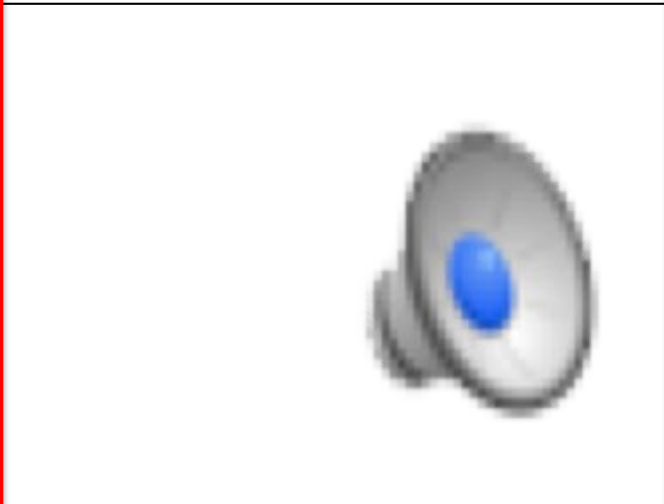
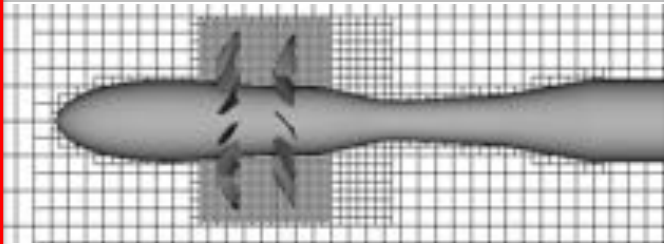


**Contra-Rotating Open Rotor Propulsion**

# Computational Grid Paradigms

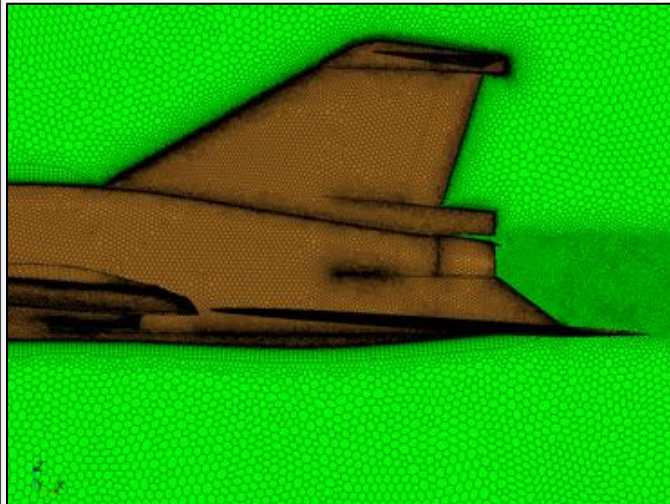
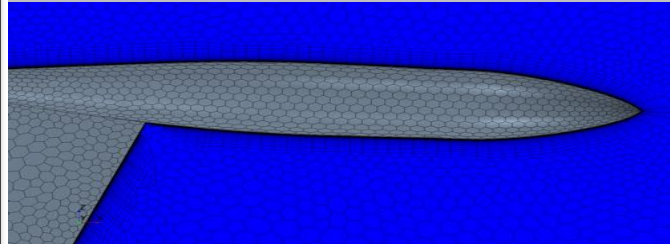


## Structured Cartesian AMR



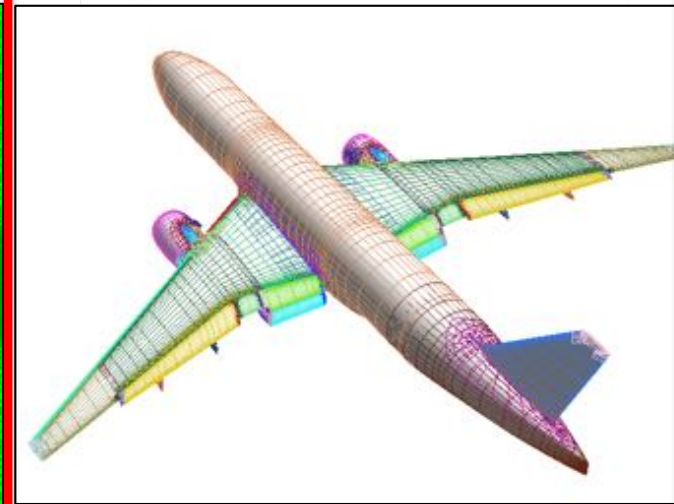
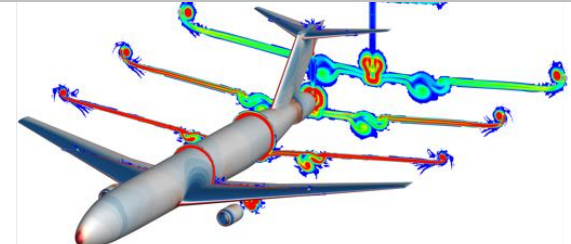
- Essentially no manual grid generation
- Highly efficient Structured Adaptive Mesh Refinement (AMR)
- Low computational cost
- Reliable higher order methods
- **Non-body fitted -> Resolution of boundary layers inefficient**

## Unstructured Arbitrary Polyhedral



- Partially automated grid generation
- Body fitted grids
- **Grid quality can be challenging**
- **High computational cost**
- **Higher order methods yet to fully mature**

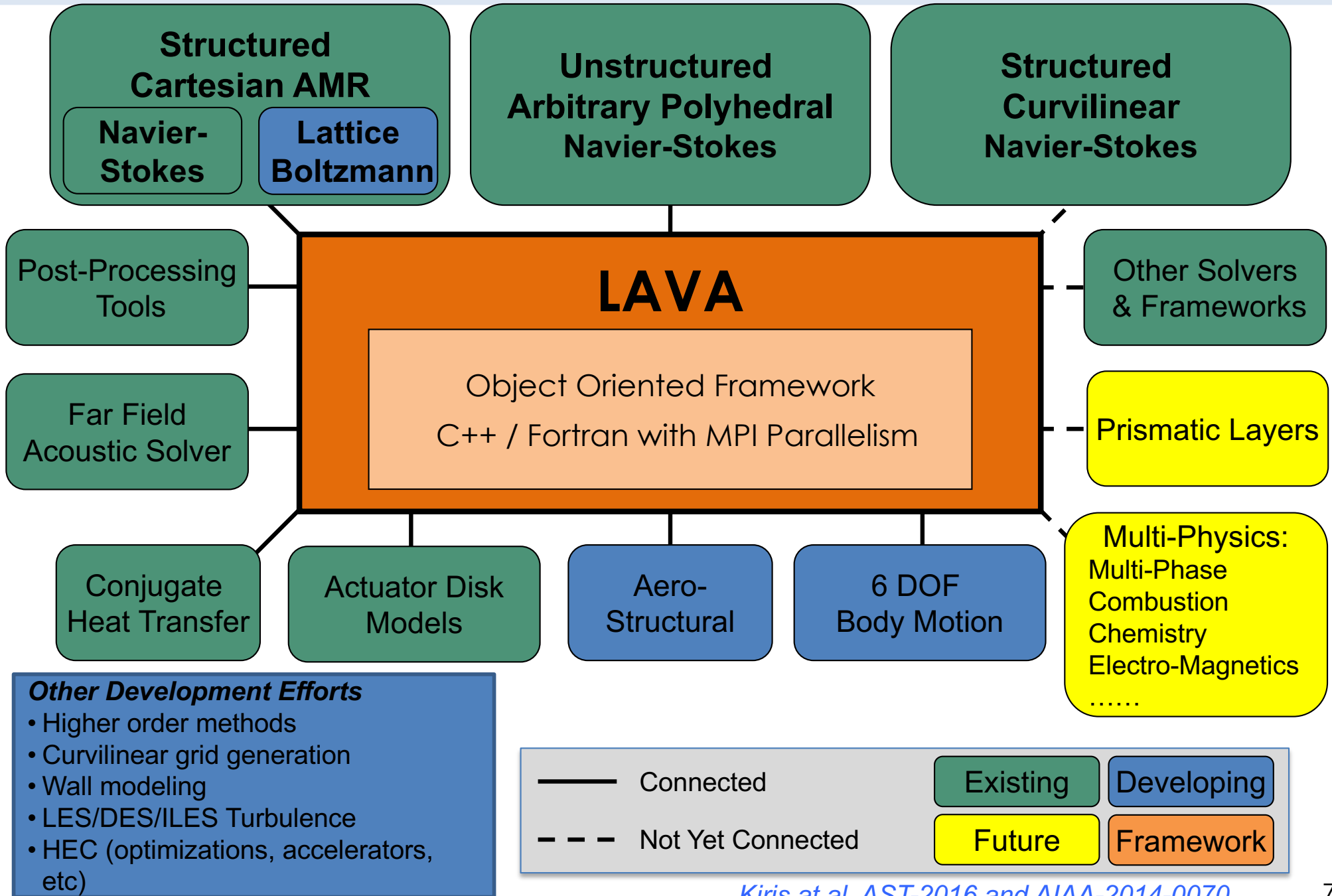
## Structured Curvilinear



- High quality body fitted grids
- Low computational cost
- Reliable higher order methods
- **Grid generation largely manual and time consuming**



## LAVA Framework



# Computational Methodology: Structured Curvilinear Overset



## *3-D Structured Curvilinear Overset Grid Solver*

- ✓ Spalart-Allmaras turbulence model (baseline turbulence model)

## *Low-Dissipation Finite Difference Method (Housman et al. AIAA-2016-2963)*

- ✓ 4th-order Hybrid Weighted Compact Nonlinear Scheme (HWCNS)
- ✓ Numerical flux is a modified Roe scheme
- ✓ 4<sup>th</sup>/3<sup>rd</sup>-order blended central/upwind biased left and right state interpolation
- ✓ 2<sup>nd</sup>-order accurate differencing used for time and viscous flux discretization

## *Hybrid RANS/LES Models*

- ✓ Delayed Detached Eddy Simulation (DDES) model with modified length scale  
*(Chauvet et al. AIAA J. 2007, Shur et al. 2015, Housman et al. AIAA-2017-0640)*
- ✓ Zonal Detached Eddy Simulation (ZDES-Mode3) with user selected RANS, LES, and Hybrid RANS LES zones. *(Deck, S. Theor. Comput. Fluid Dyn. 2012)*
- ✓ Zonal RANS-NLES (numerical LES) with user selected zones of URANS, NLES, and wall-distance based hybrid RANS-NLES *(Housman et al. AIAA-2017-3213)*

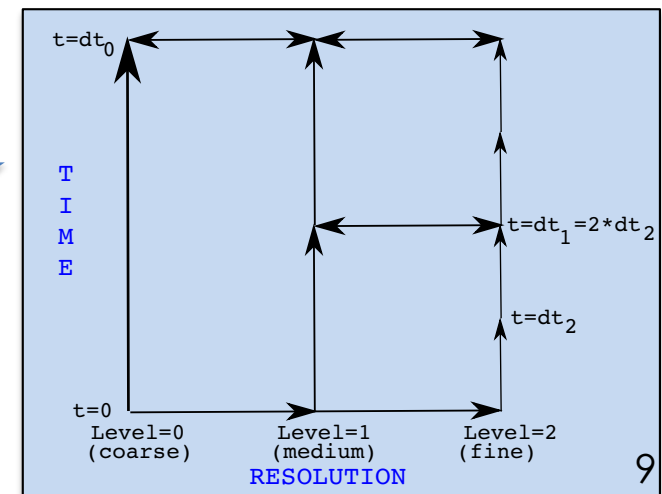
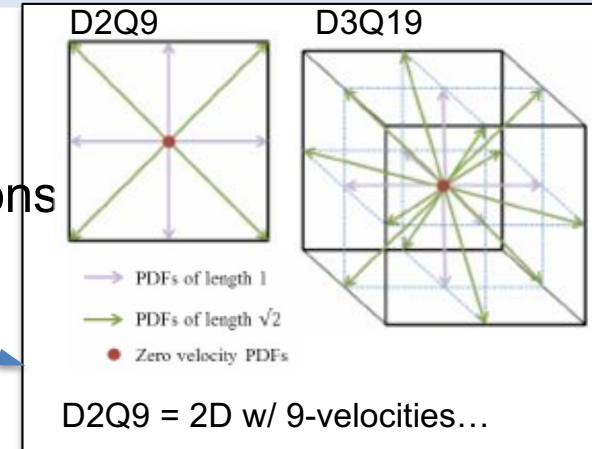
## *Synthetic Eddy Method (SEM) (Jarrin et al. Int. Journal of Heat and Fluid Flow 30)*



# Computational Methodology: Lattice Boltzmann Method – Current Status

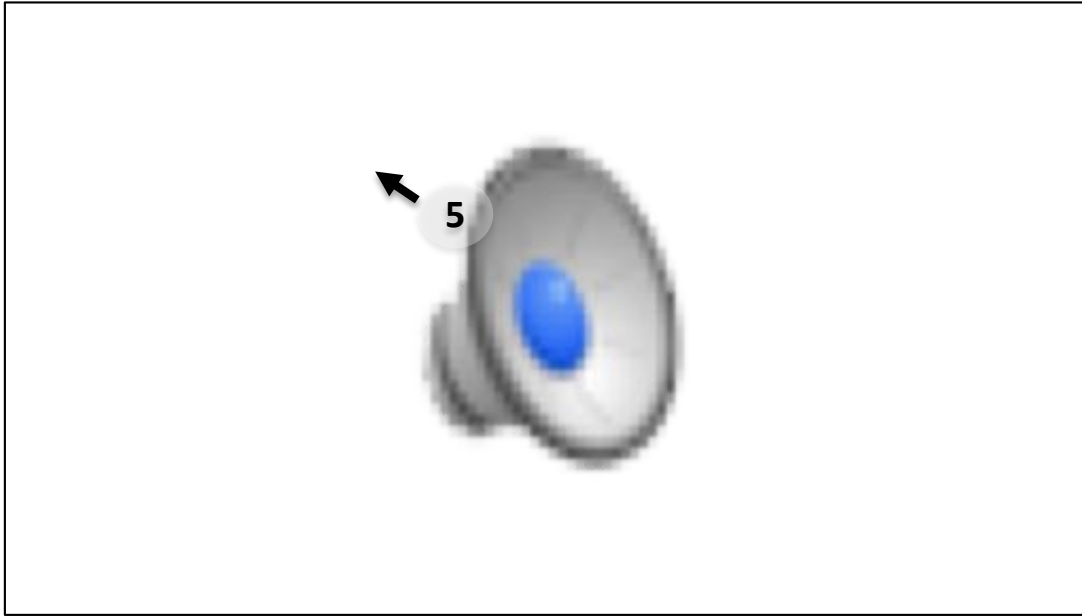
$$\underbrace{f_i(\vec{x} + c\vec{e}_i\Delta t, t + \Delta t) - f_i(\vec{x}, t)}_{\text{Streaming}} = \frac{1}{\tau} \underbrace{(f_i(\vec{x}, t) - f_i^{eq}(\vec{x}, t))}_{\text{Collision}}$$

- Governs space time evolution of Density Distribution Functions
- **Lattices:** including D2Q9, D3Q15, D3Q19, D3Q27, D3Q39 ...
- **Collision Models:**
  - Bhatnagar-Gross-Krook (BGK)
  - Multi-Relaxation Time (MRT)
  - Entropic and positivity preserving variants of BGK
  - Entropic Multi-Relaxation Time (EMRT)
  - Regularized BGK
- **LES Model:** Smagorinsky sub-grid-scale
- **Wall Models:** Tamm-Mott-Smith boundary condition, filter-based slip wall model, or traditional equilibrium wall stress model
- **Parallelization:**
  - Structured adaptive mesh refinement
    - Fine-fine for communication within levels
    - Coarse-fine for communication across levels
    - Efficient parallel I/O
- **Multi-Resolution with Recursive Sub-Cycling**
- **Boundary Conditions:**
  - No-slip and slip bounce back walls
  - Accurate and robust curved walls
  - Inflow/outflow. and periodic





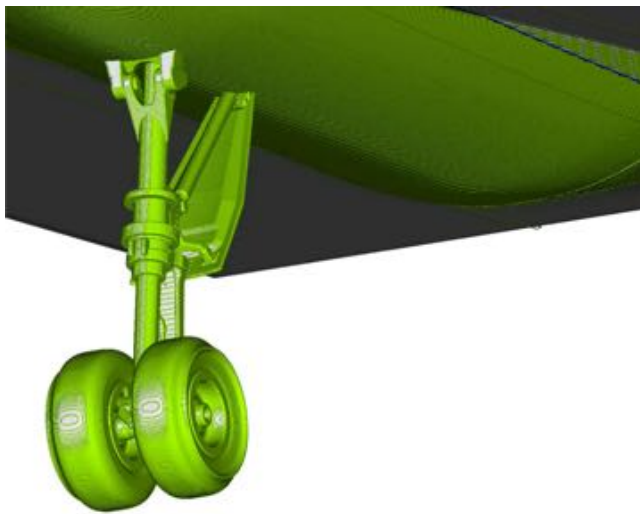
# Recent LAVA Cartesian Lattice-Boltzmann Success: Landing Gear from AIAA BANCIII Workshop (problem 4)



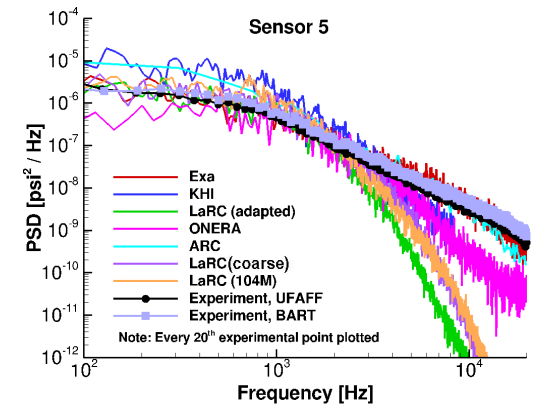
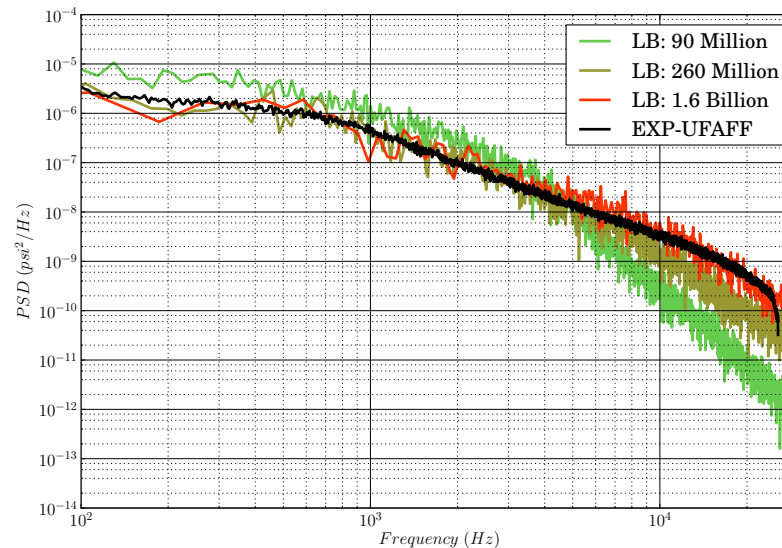
“Lattice Boltzmann and Navier-Stokes Cartesian CFD Approaches for Airframe Noise Predictions”, Barad, Kocheemoolayil, Kiris, [AIAA 2017-4404](#)

Mach = 0.166  
 Re = 66423 ( $D=D_{strut}$ )  
 $U_{ref} = 58.32$  m/s  
 $T_{ref} = 307.05$  K  
 $P_{ref} = 98605$  Pa

LBM @ 1.6 billion – Velocity Magnitude at Centerline



Near Field PSD Channel 5



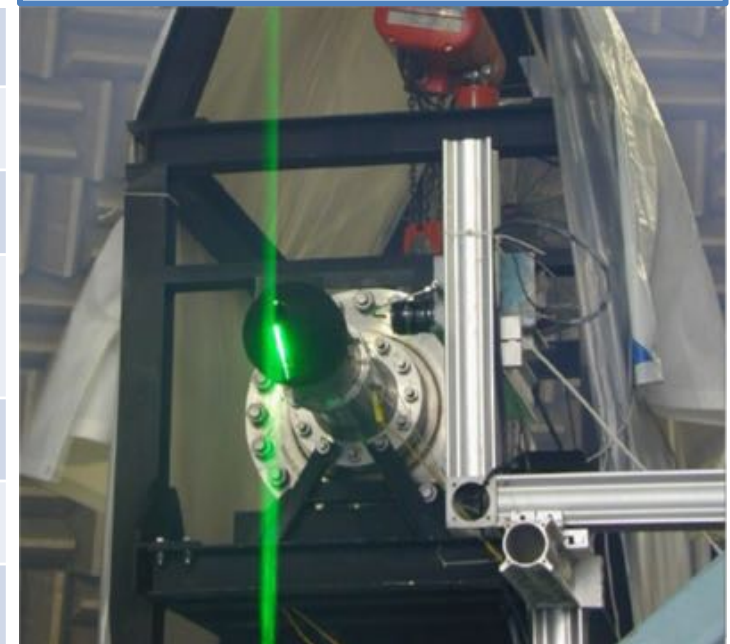
# Round Jet – Experimental Setup SP7



- ✓ Experiment performed by Bridges and Wernet using the Small Hot Jet Acoustic Rig (SHJAR) at NASA Glenn
- ✓ Baseline axisymmetric convergent Small Metal Chevron (SMC000) nozzle at Set Point 7 (SP7)
- ✓ Nozzle axis in downstream flow direction is marked as 180°

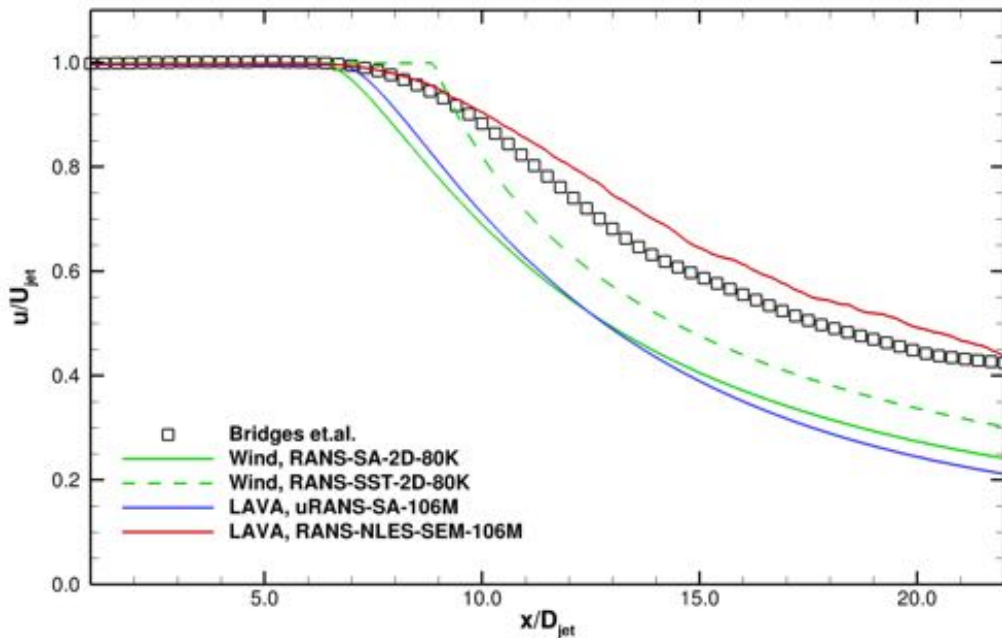
Bridges et. al. (NASA-TM-2011-216807)	SP7
Acoustic Mach number $U_{jet}/c_{\infty}$	0.9
Jet temperature ratio $T_e/T_{\infty}$	0.835
Nozzle pressure ratio $p_t/p_{\infty}$	1.861
Nozzle Diameter D	0.0508 [m] 2.0 [inch]
Reynold number $Re_D$	1 Million
Reynolds number $Re_{\tau}$	800
Boundary layer thickness	0.0128 D

PIV measurement device



Similar conditions were analyzed in Bres *et. al.* AIAA-2015-2535, but the boundary layer thickness is 5.5 times smaller in this study

# Round Jet - Objective & Metrics



## Objective:

- ✓ Improvements in prediction of jets (including developing region, the effect of compressibility, and the effect of temperature).

## Metrics:

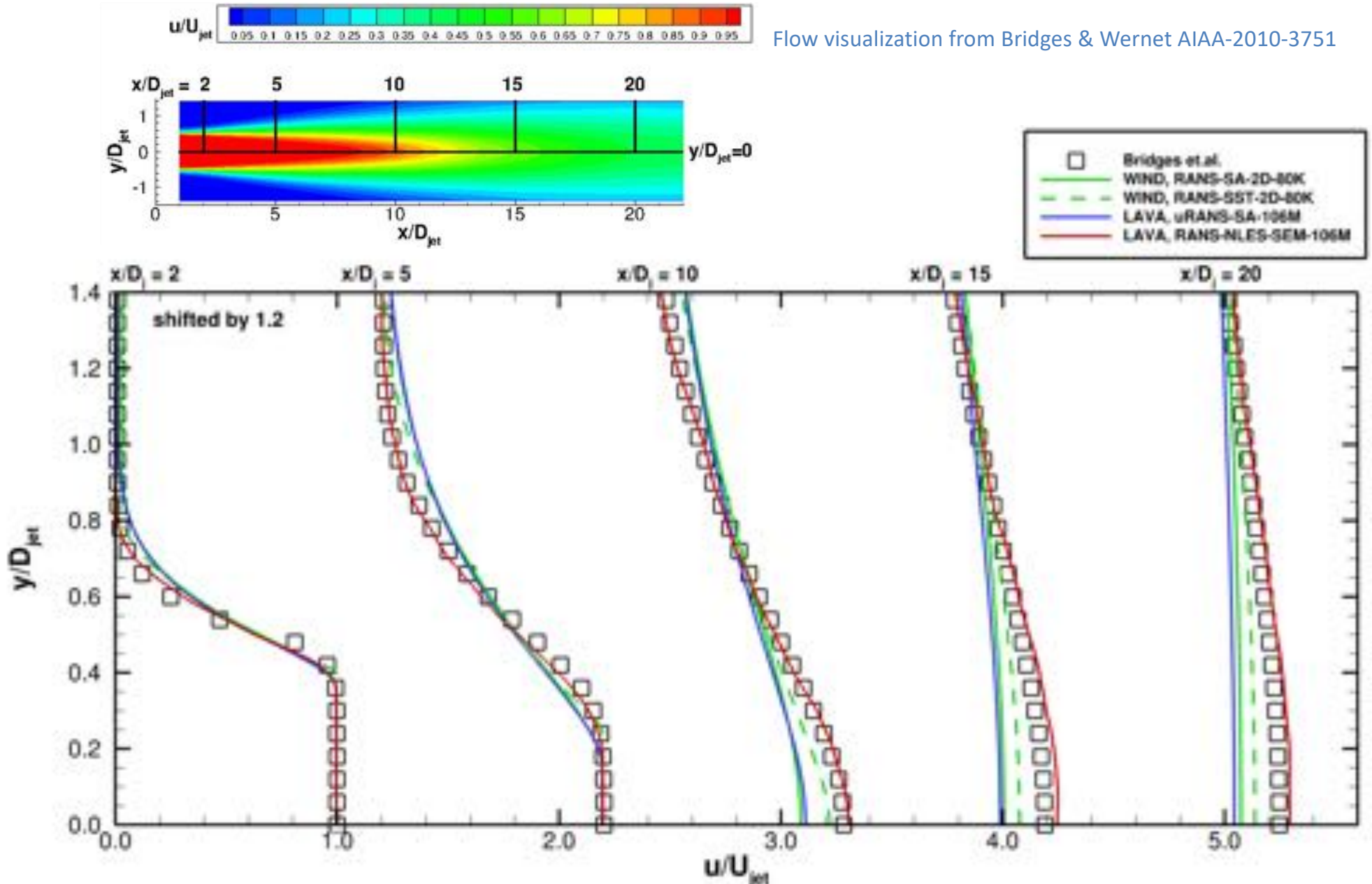
- ✓ Length of the potential core (where  $u/U_{jet} = 0.98$ )
- ✓ Value and location of the peak turbulent kinetic energy on
- ✓ **89.6%** improvement
- ✓ Reynolds stress fields

solver	$x/D_j$ [-]	Error [%]
Bridges & Wernet	7.8	-
Wind, RANS-SA-2D	6.84	-12.3
Wind, RANS-SST-2D	9.01	15.5
LAVA, uRANS-SA-3D	7.22	-7.5
<b>LAVA, RANS-NLES-SEM-3D</b>	<b>7.90</b>	<b>1.2</b>

# Round Jet - Objective & Metrics

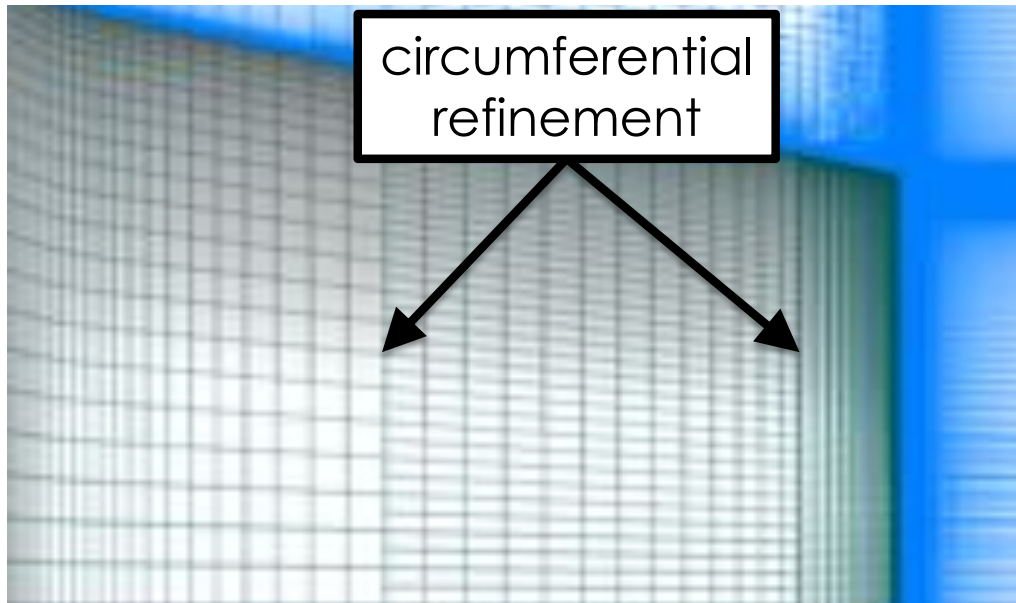


Flow visualization from Bridges & Wernet AIAA-2010-3751



✓ Mean velocity field at locations downstream of nozzle exit shifted by 1.2

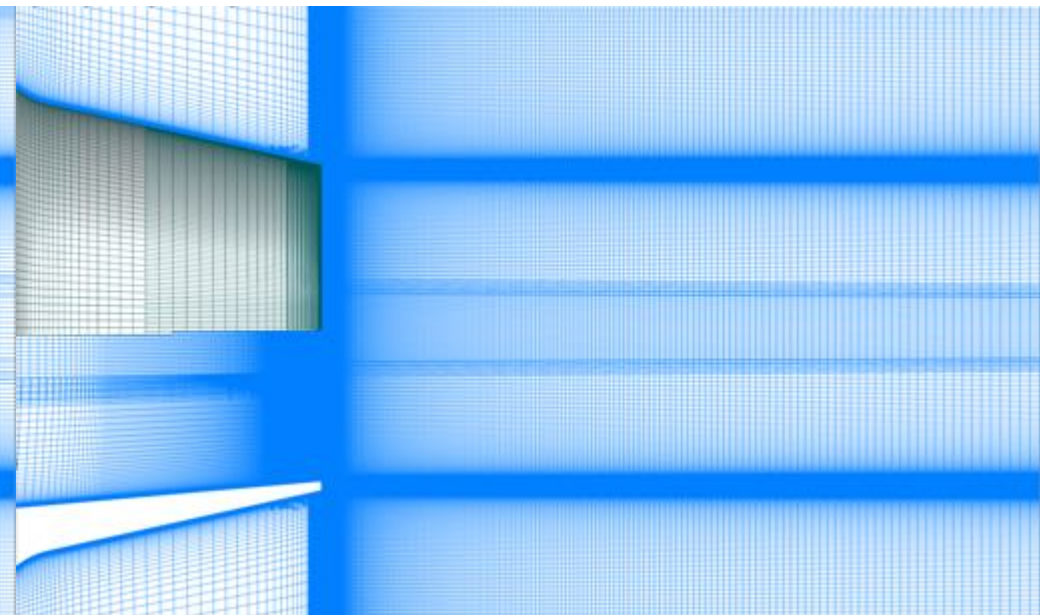
# Round Jet – Structured Overset Grid



- ✓ Coarse (28 M) and Refined (106 M) grid point meshes were generated
- ✓ Seven point overlap
- ✓ No orphan points
- ✓ Minimum stencil quality 0.9
- ✓ Localized circumferential refinement at specified axial and radial locations



Coarse (28 M)

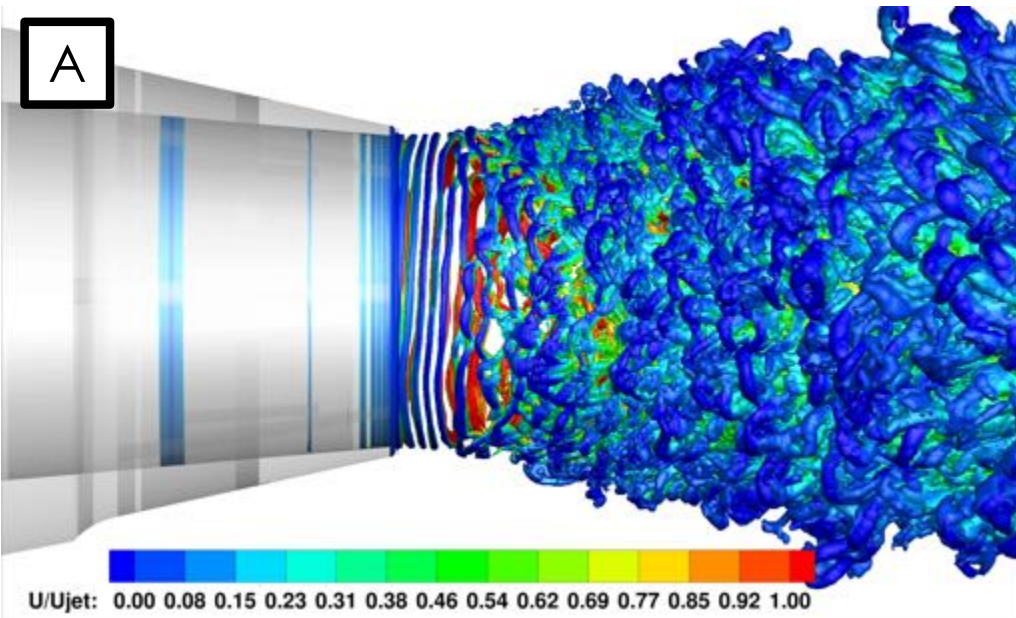


Refined (106 M)

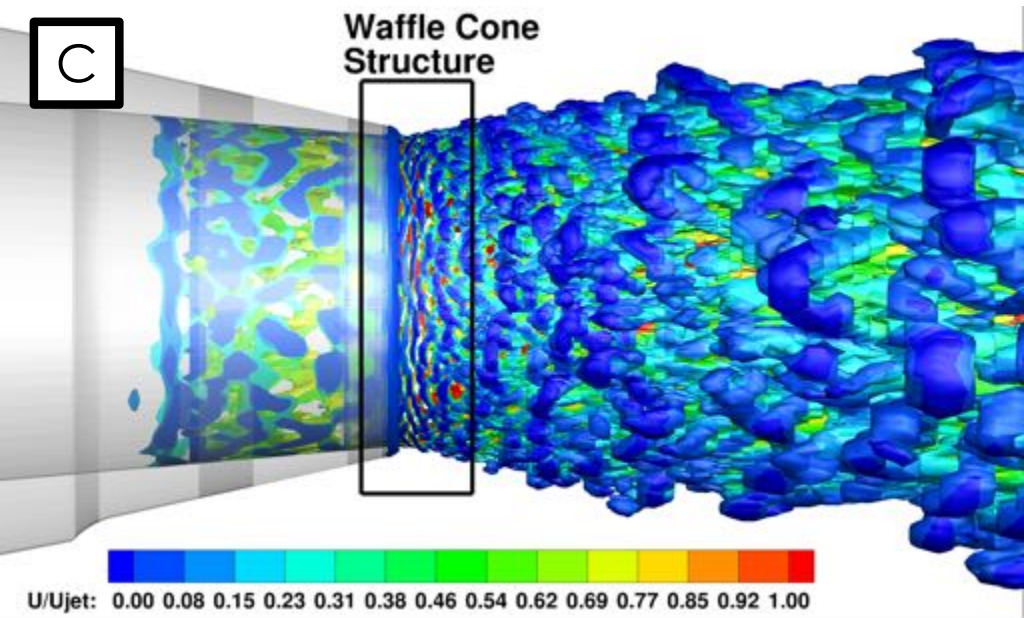
# Round Jet - Computational Results



A

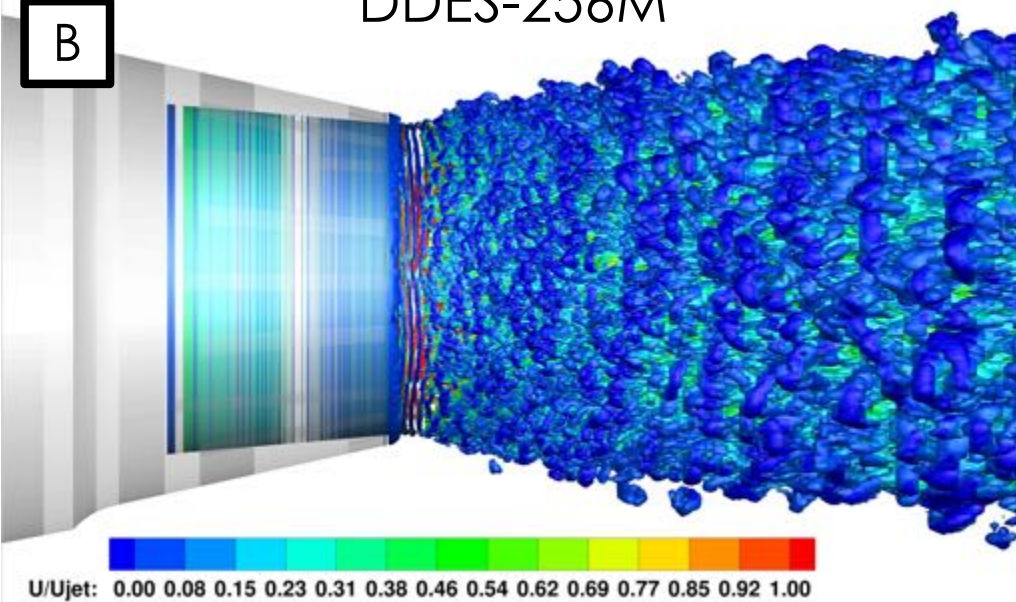


C



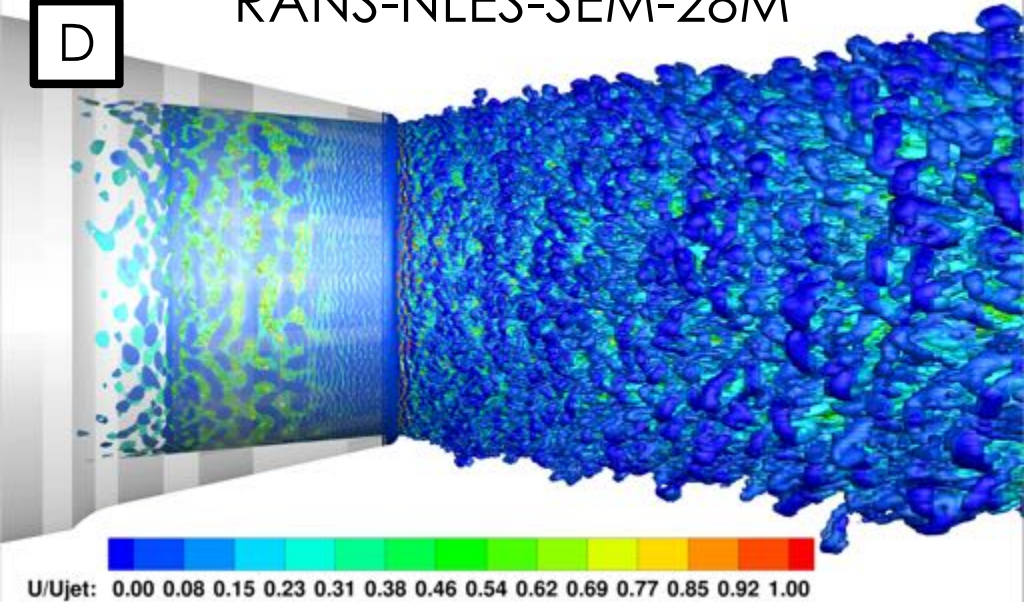
B

DDES-256M



D

RANS-NLES-SEM-28M



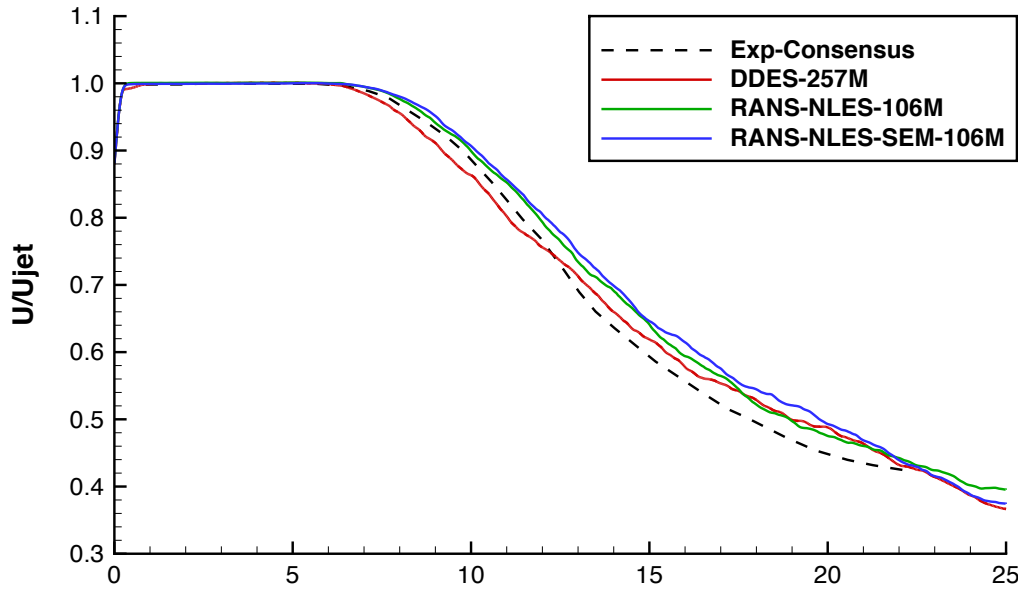
RANS-NLES-106M

RANS-NLES-SEM-106M

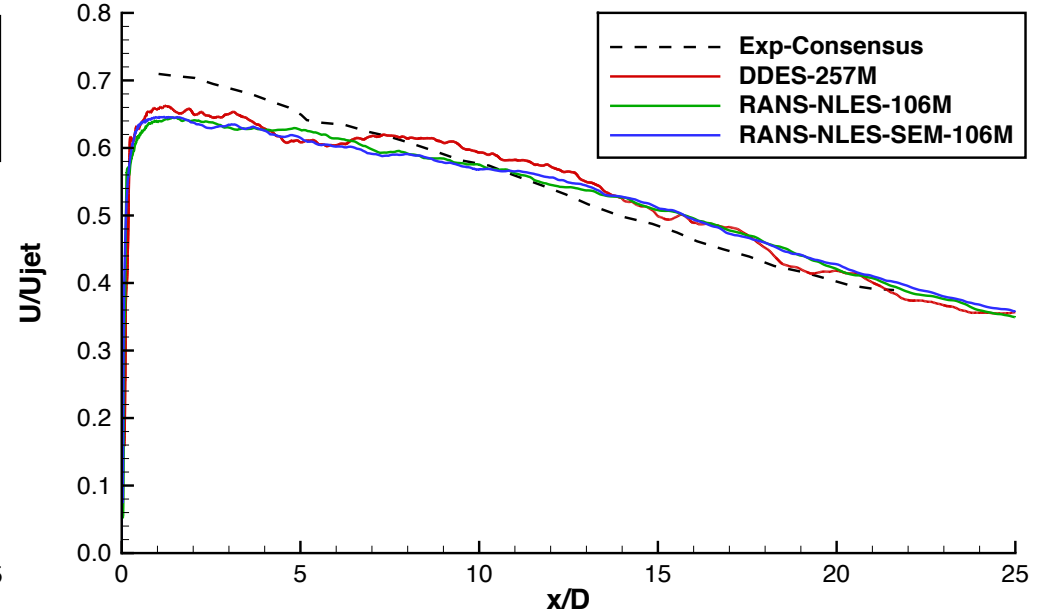
# Round Jet – Near-Field Results



### Time-averaged center-line velocity

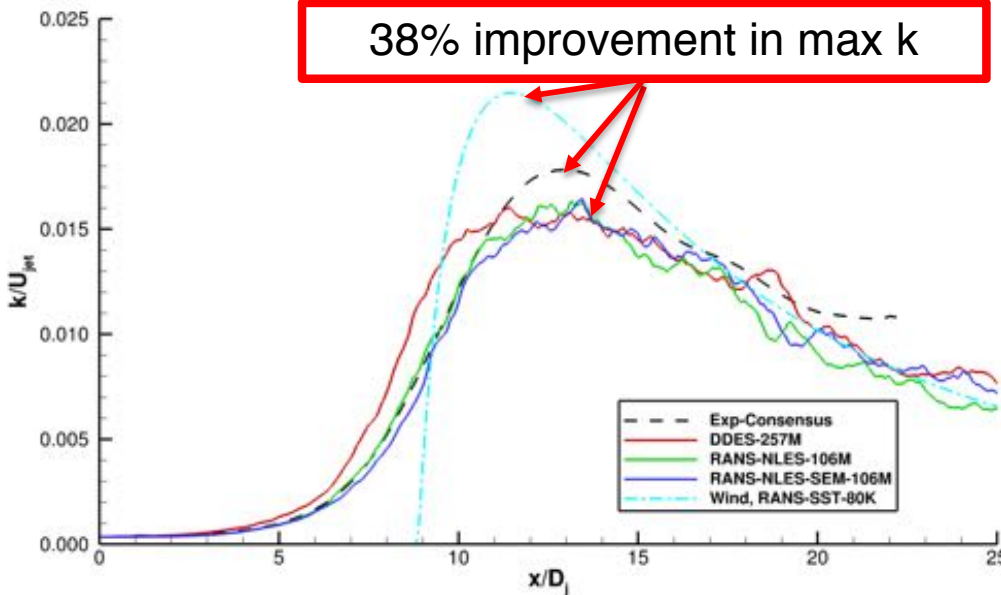


### Time-averaged lip-line velocity

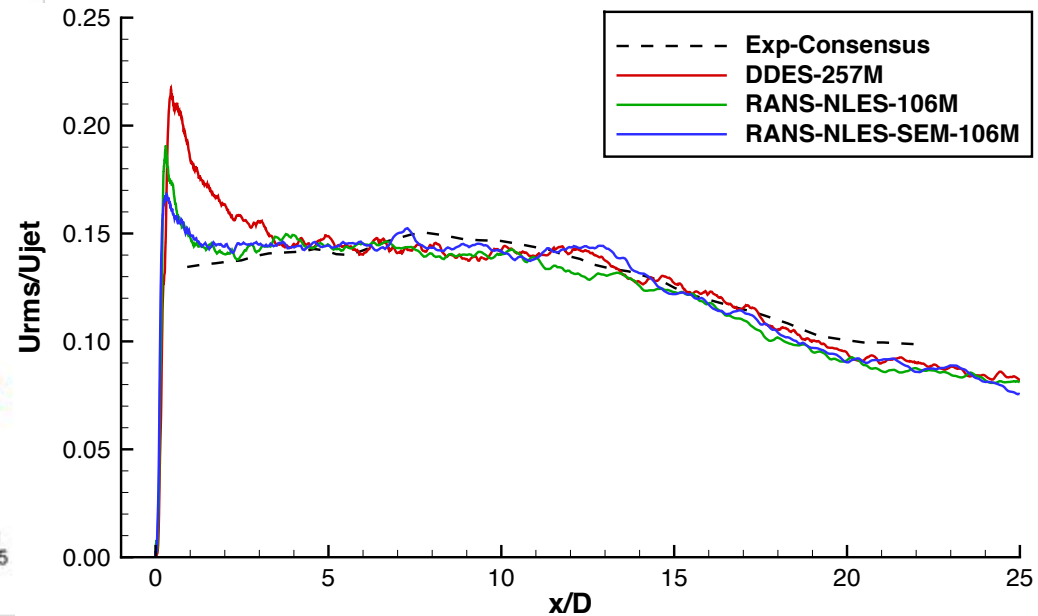


### center-line $k = (u'u' + v'v' + w'w')/2$

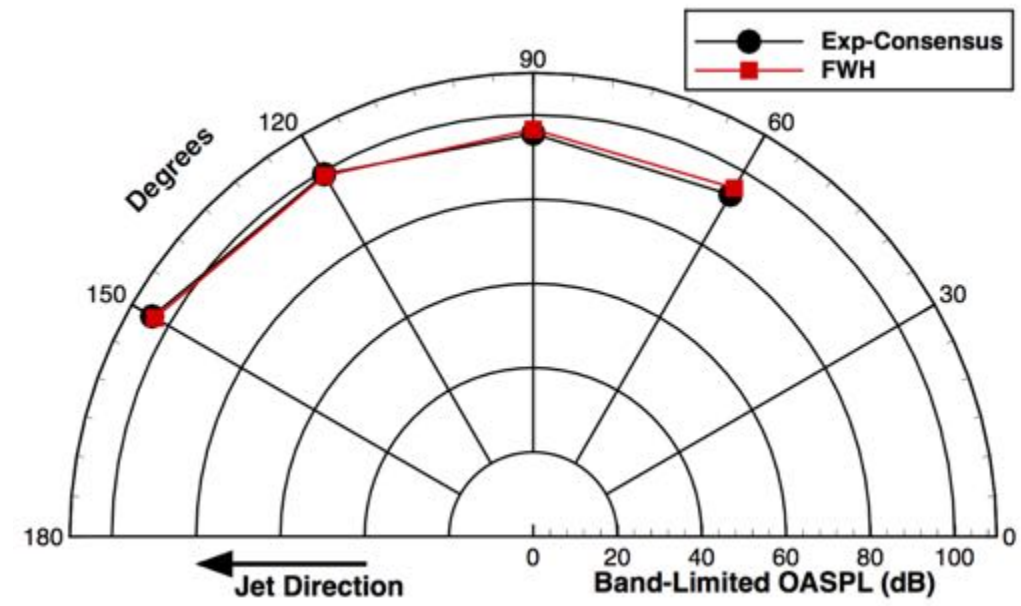
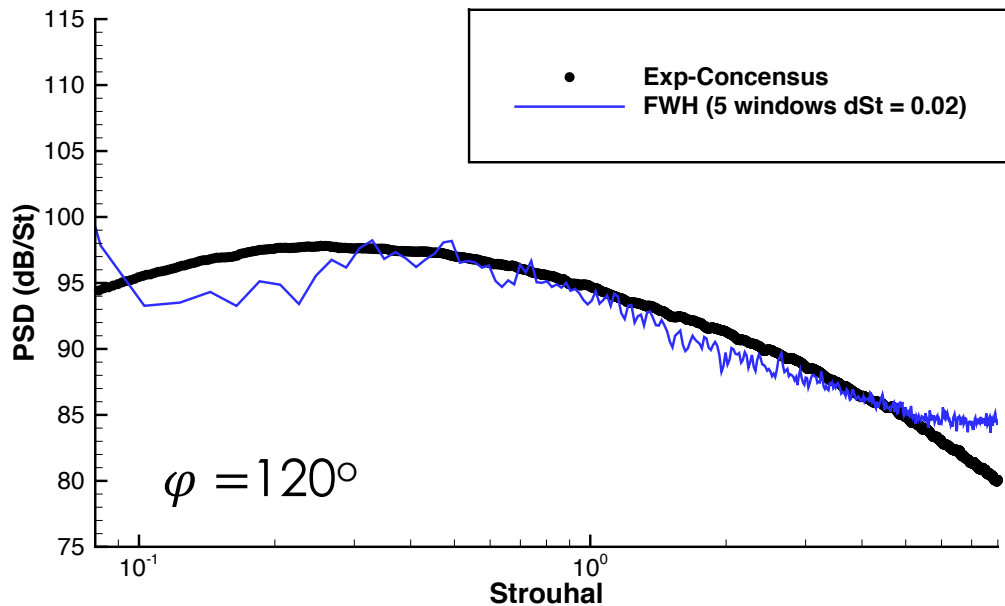
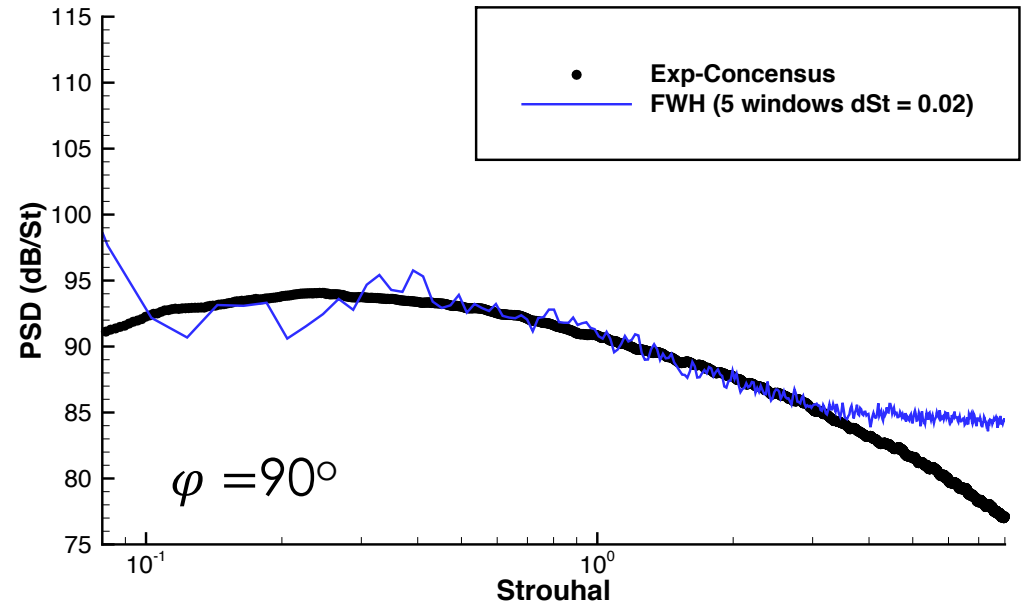
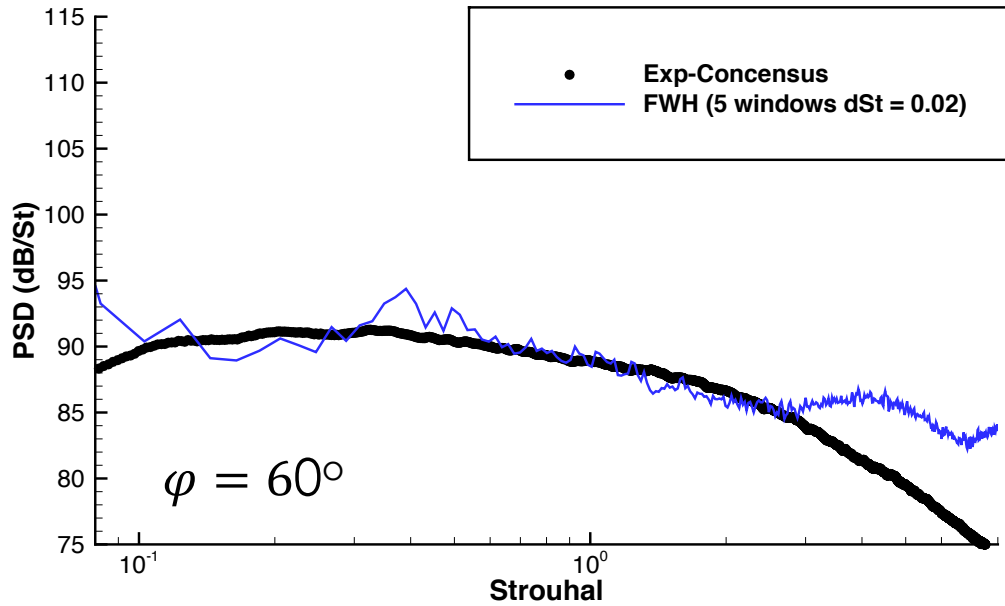
38% improvement in max k



### RMS lip-line velocity



# Round Jet – Far Field at 100D

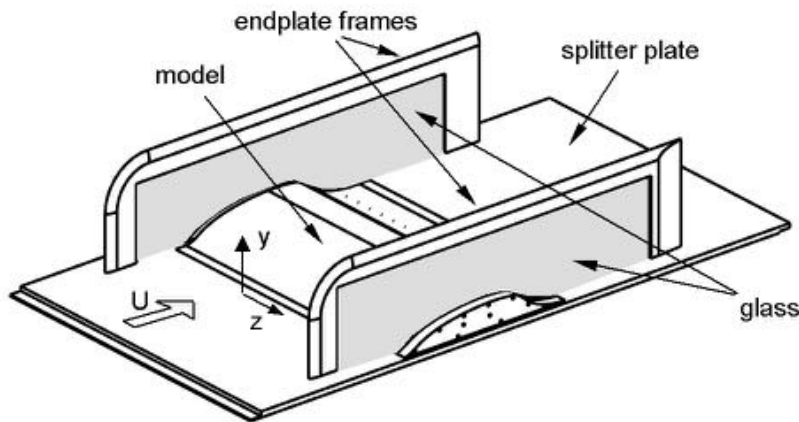




# NASA 2-D Hump – Experimental Setup



- ✓ Assess ability of CFD solvers to predict flow separation from a smooth body (caused by adverse pressure gradient) as well as subsequent reattachment and boundary layer recovery.



- ✓ Experiments described in Detail in Greenblatt<sup>1</sup> and NASA CFDVAL 2004 Workshop<sup>2,3</sup>.
- ✓ RANS known to perform poorly.
- ✓ Eddy-resolving methods have been successfully applied.

<sup>1</sup> Greenblatt et. Al. "Experimental Investigation of Separation Control Part 1: Baseline and Steady Suction". AIAA Journal, vol 44, no. 12, pp. 2820-2830, 2006

<sup>2</sup> Rumsey C, "Turbulence Modeling Resource", <https://turbmodels.larc.nasa.gov>

<sup>3</sup> Rumsey C, "CFD Validation of Synthetic Jets and Turbulent Separation Control", <http://cfdv2004.larc.nasa.gov>

# NASA 2-D Hump – Experimental Setup



- ✓ Assess ability of CFD solvers to predict flow separation from a smooth body (caused by adverse pressure gradient) as well as subsequent reattachment and boundary layer recovery.

## Wall-resolved LES:

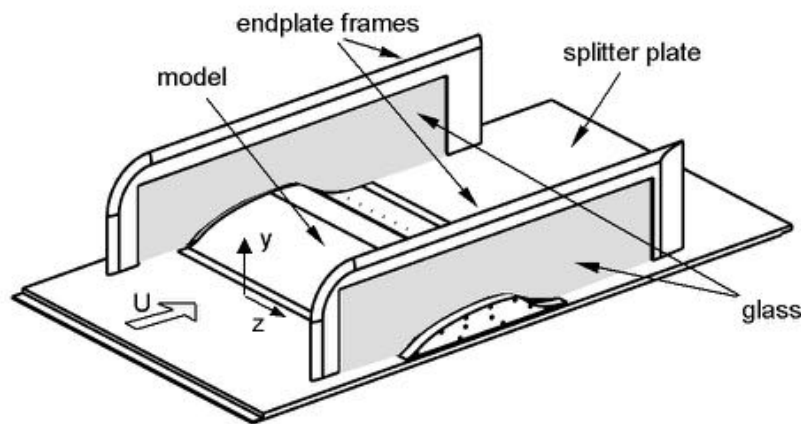
- ✓ Uzun, A. and Malik, M. (AIAA 2017-5308)

## Wall-modeled LES:

- ✓ Iyer, P. and Malik, M. (AIAA 2016-3186)

## Lattice Boltzmann Methods:

- ✓ Duda, B. and Fares, E. (AIAA 2016-1836)

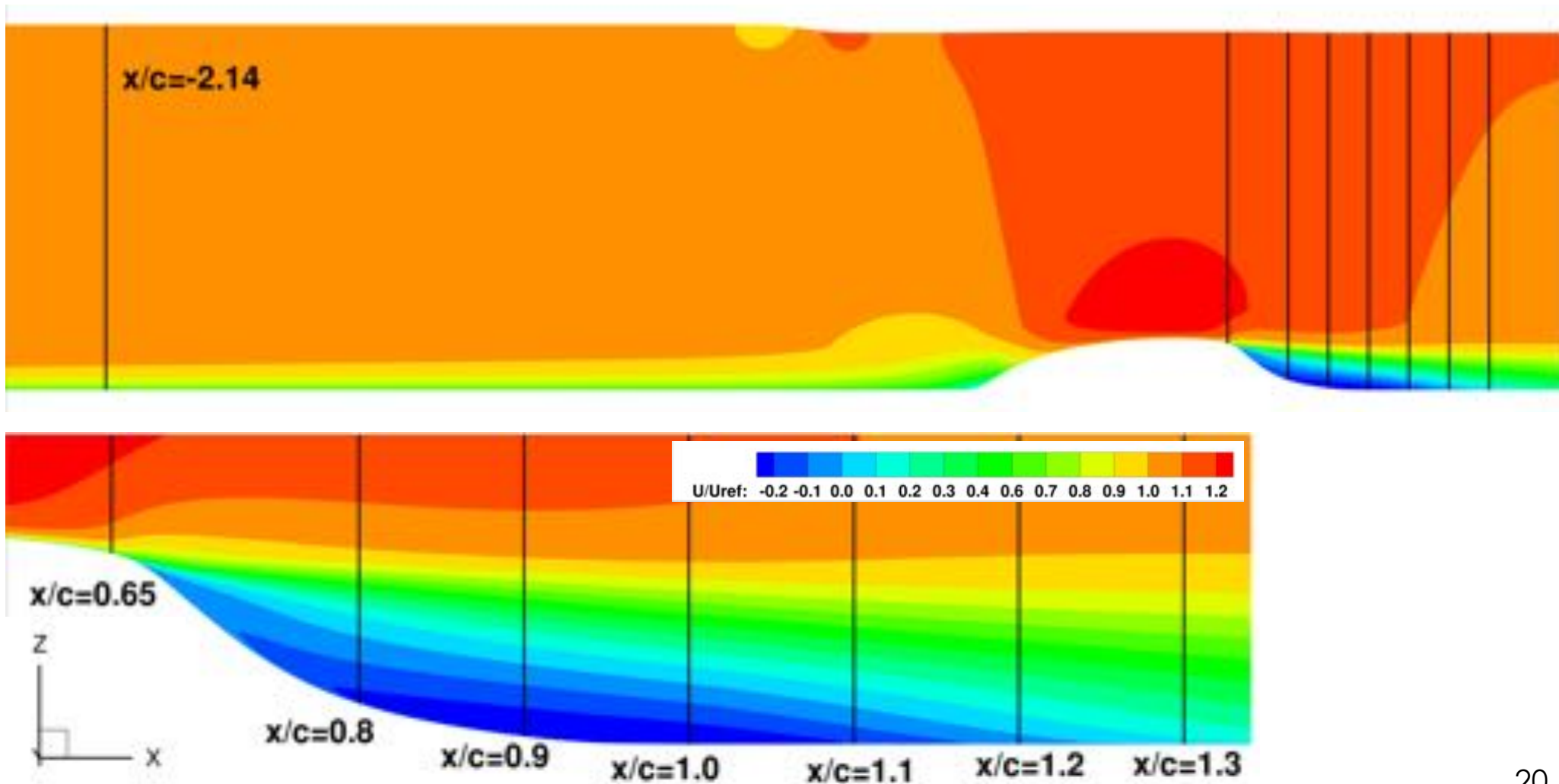


<sup>1</sup> Greenblatt et. Al. "Experimental Investigation of Separation Control Part 1: Baseline and Steady Suction". AIAA Journal, vol 44, no. 12, pp. 2820-2830, 2006  
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<sup>3</sup> Rumsey C, "CFD Validation of Synthetic Jets and Turbulent Separation Control", <http://cfdval2004.larc.nasa.gov>

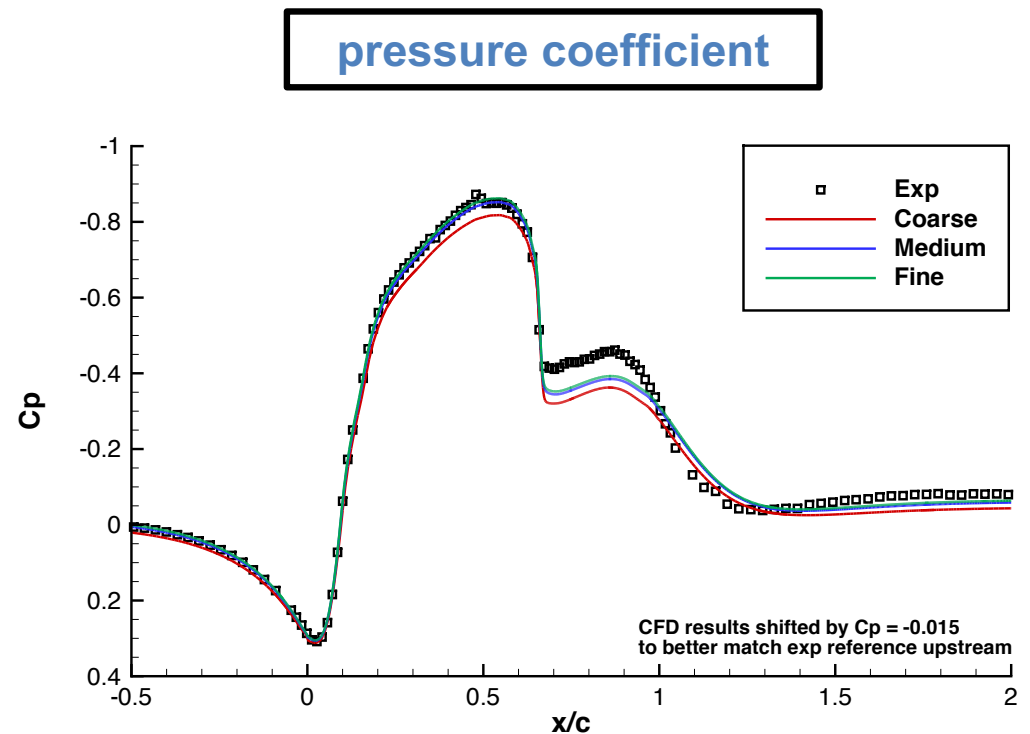
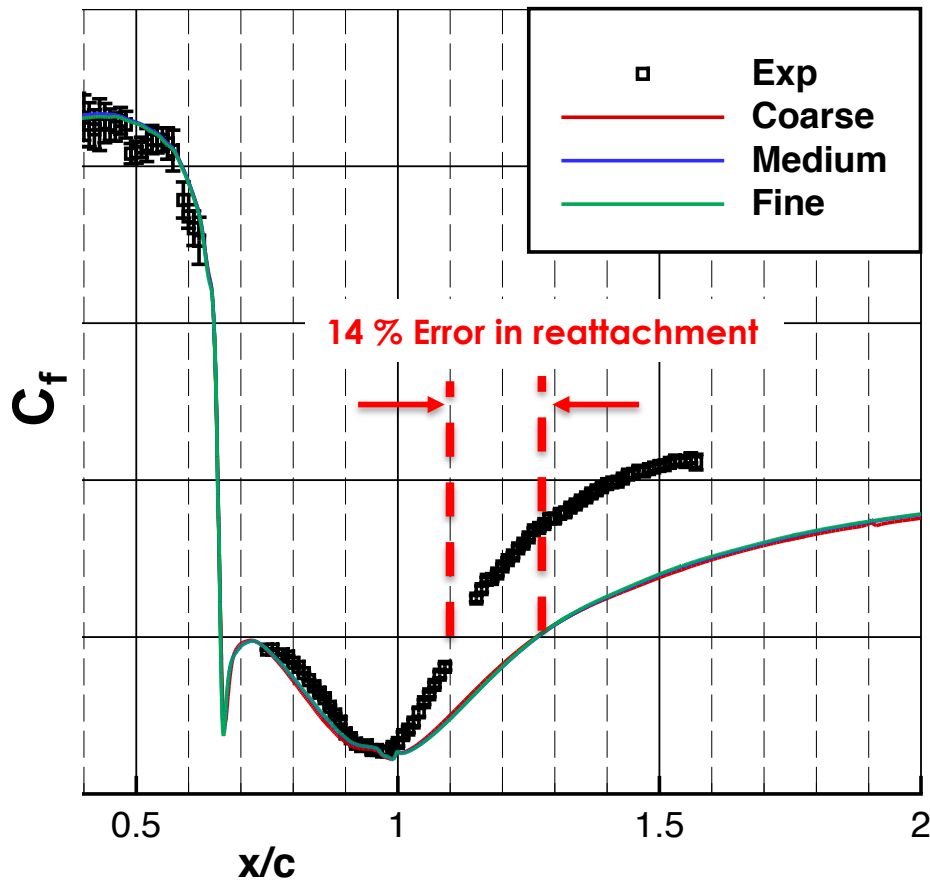
# NASA 2-D Hump



- ✓ Mach = 0.1 ; chord  $C = 0.42$  [m] ;  $Re_C = 936,000$  ;  $T_{ref} = 298.3$  [K]
- ✓ Top wall contoured to mimic side-wall effect
- ✓ Experimental data at locations marked below available



# NASA 2-D Hump – LAVA RANS Validation



- ✓ Consistent convergence to a mesh refined solution is observed in each of the quantities
- ✓ Under prediction of  $C_p$  in the separated flow region and over prediction of the reattachment length is consistent with the SA results for CFL3D, FUN3D, and OVERFLOW (reported on the TMR)
- ✓ RANS solvers typically over predict bubble size by 35%



# NASA 2-D Hump – Application of Zonal DES

SEM interface

RANS

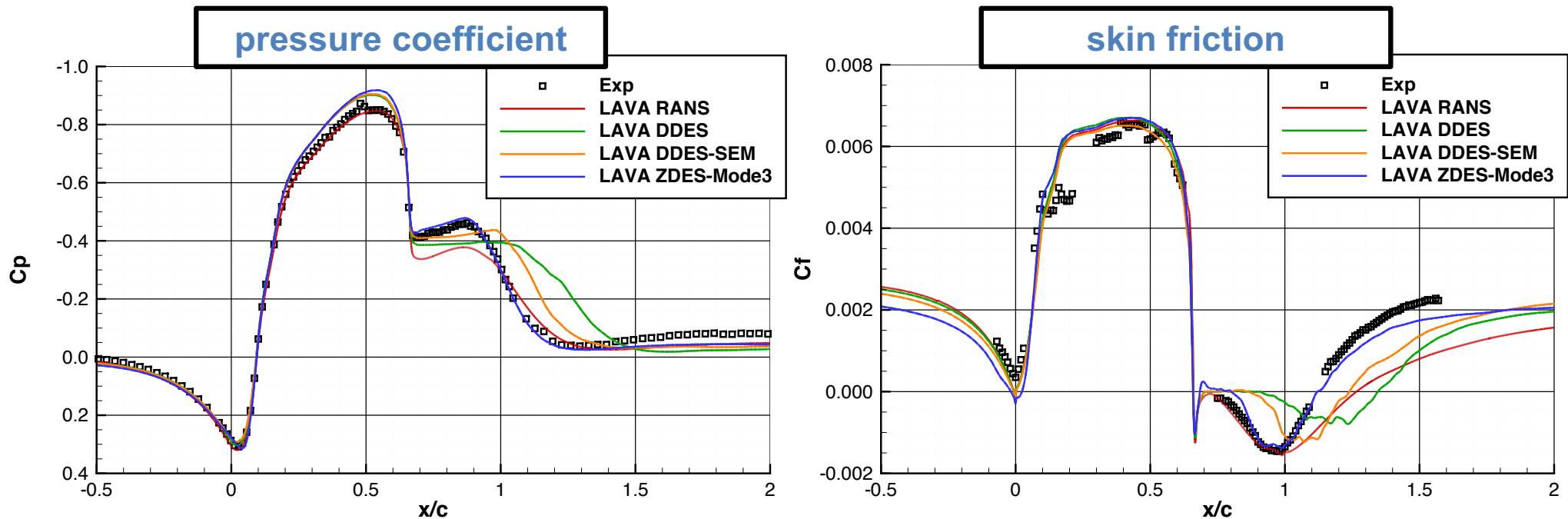
Hybrid RANS/LES

RANS

3 zones 11.3 million grid points  
Zone 1 (RANS): 57x57x149  
Zone 2 (ZDES): 1225x57x149  
Zone 3 (RANS): 47x57x149  
0.2c in span  
double fringe, no orphans  
 $dx/\delta_0 = 0.1$ ,  $dy_{wall}^+ = 0.8$ ,  $dz/\delta_0 = 0.05$

clustering

# NASA 2-D Hump – Application of Delayed DES (SA)



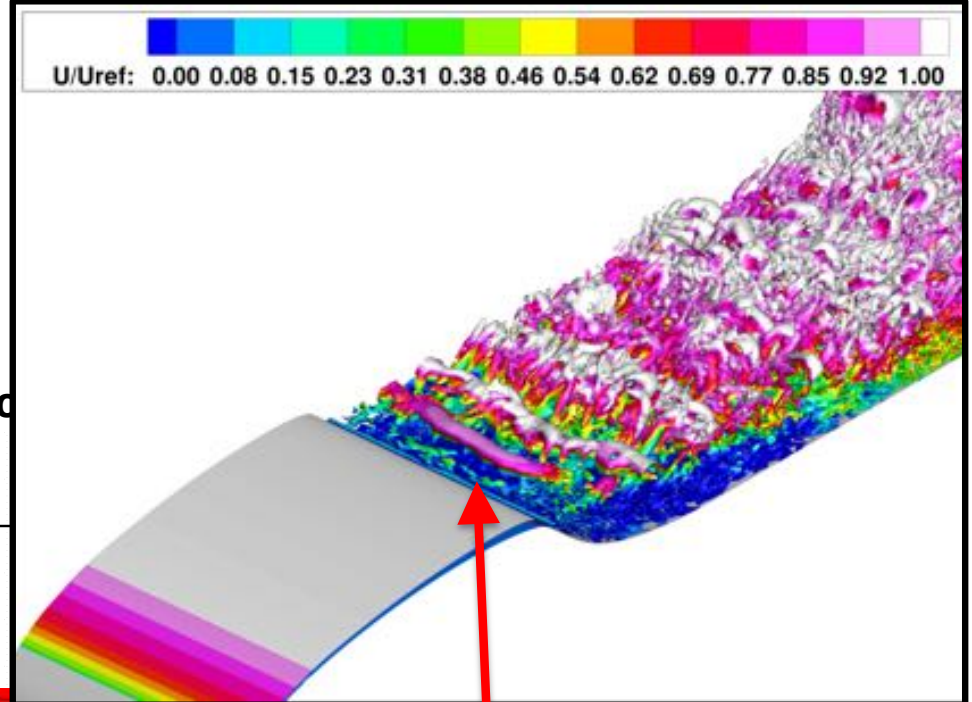
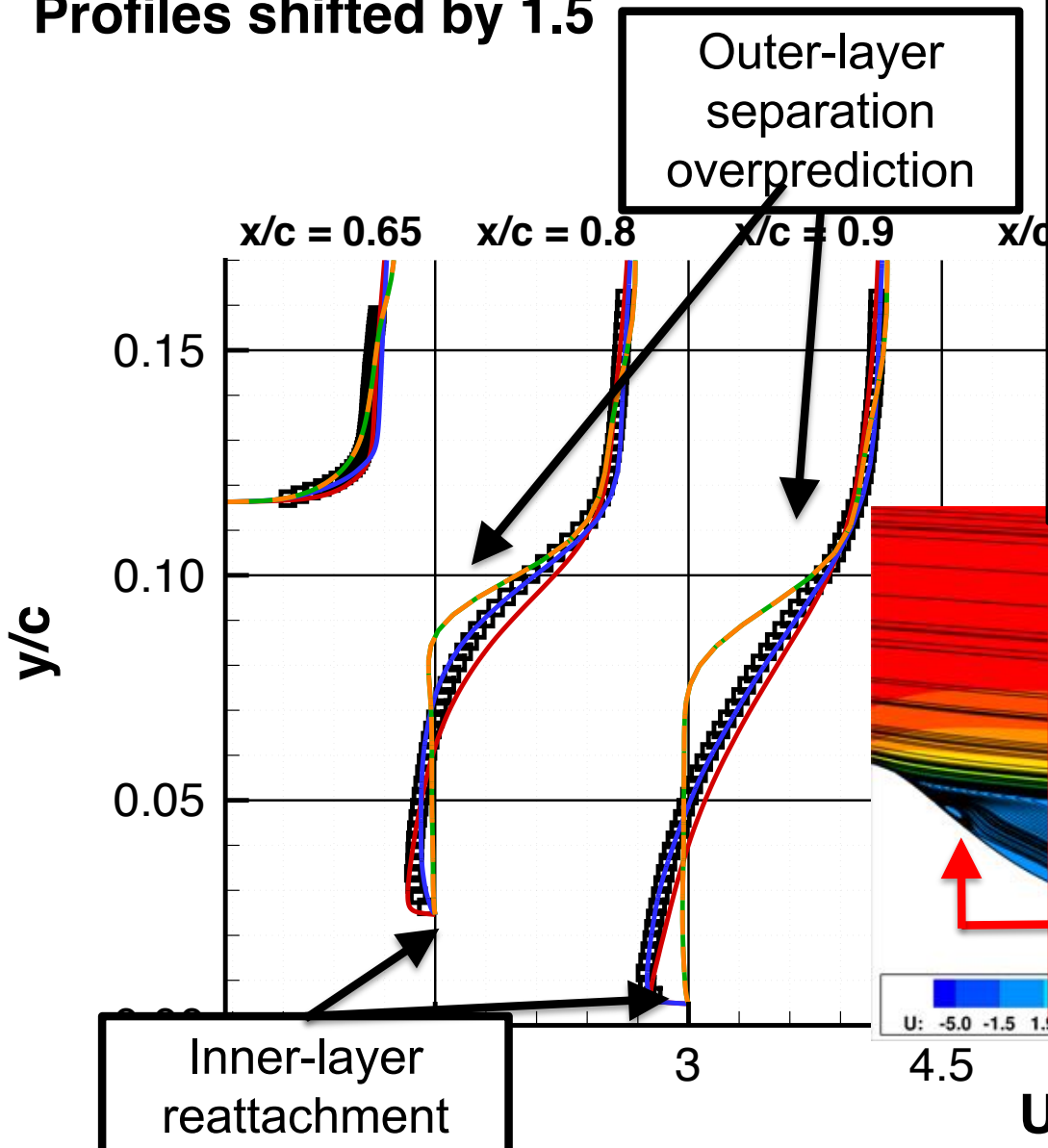
- ✓ Upstream of the separation point the SA-DDES results fall on-top of the SA-RANS results indicating the attached boundary layer is staying in RANS mode as expected.
- ✓ SA-ZDES-Mode3 shows slightly lower skin friction upstream of the bump
- ✓ Downstream of the separation point SA-DDES shows a shallow reattachment region with the larger separated flow region reattaching near the SA-RANS result.
- ✓ The separated flow region is very well-predicted using the SA-ZDES-Mode3 with almost no difference between the experiment and the computation

# NASA 2-D Hump – Application of Delayed DES (SA)

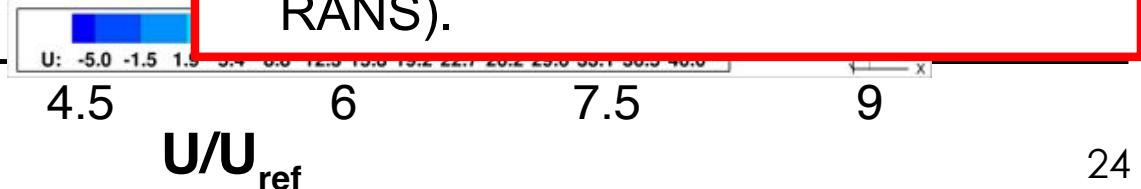


streamwise velocity

Profiles shifted by 1.5



- ✓ Similar to Jet Case SP7 DDES observations.
- ✓ Delay in generation of 3D structures
- ✓ Delay can be improved by resolving structures in BL upstream of separation (instead of modeling with RANS).





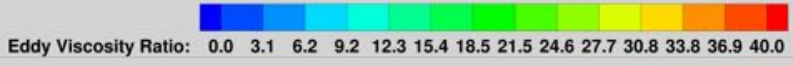
# NASA 2-D Hump – Application of Zonal DES

indicator function



- ✓ Sharp transition between RANS and LES
- ✓ Modeled stress acts as dynamics SGS model in LES region
- ✓ Discontinuous length scale
- ✓ RANS acts as WM in BL

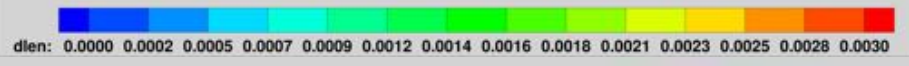
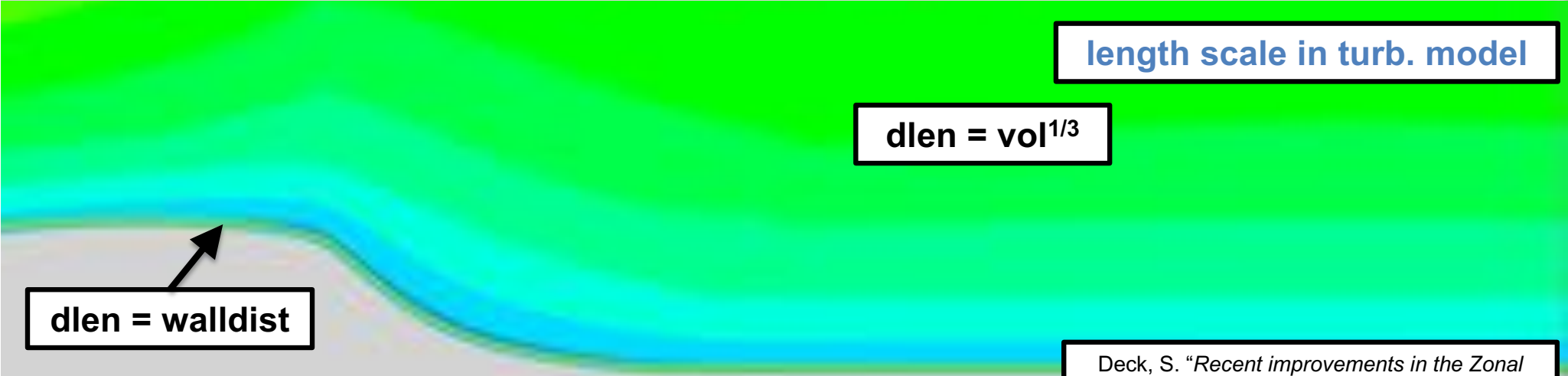
eddy viscosity



length scale in turb. model

$$dlen = vol^{1/3}$$

dlen = walldist



Deck, S. "Recent improvements in the Zonal Detached Eddy (ZDES) formulation", Theor. Comput. Fluid. Dyn., 2012



# NASA 2-D Hump – Application of Zonal DES



DDES

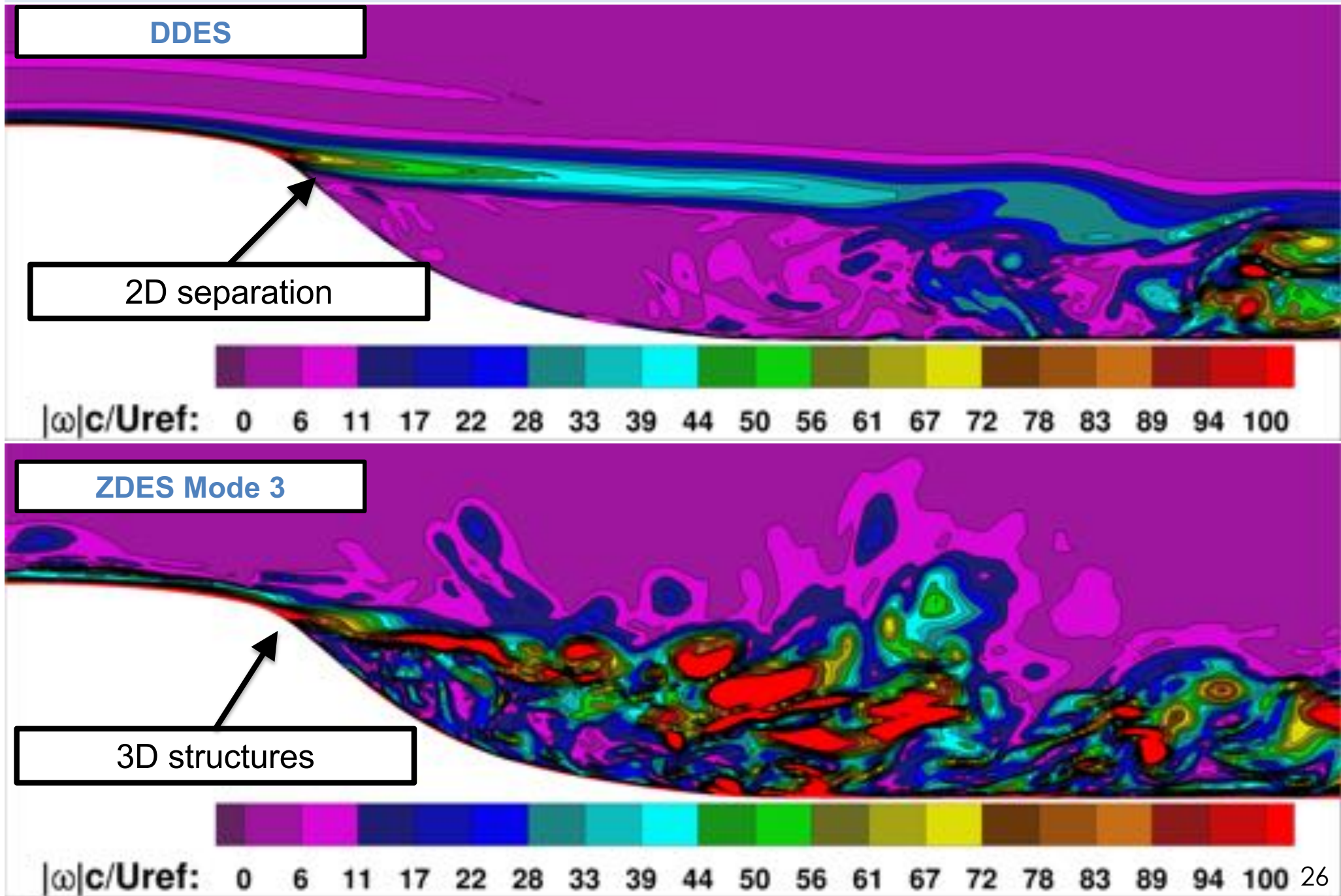
2D separation

$|\omega|c/U_{ref}$ : 0 6 11 17 22 28 33 39 44 50 56 61 67 72 78 83 89 94 100

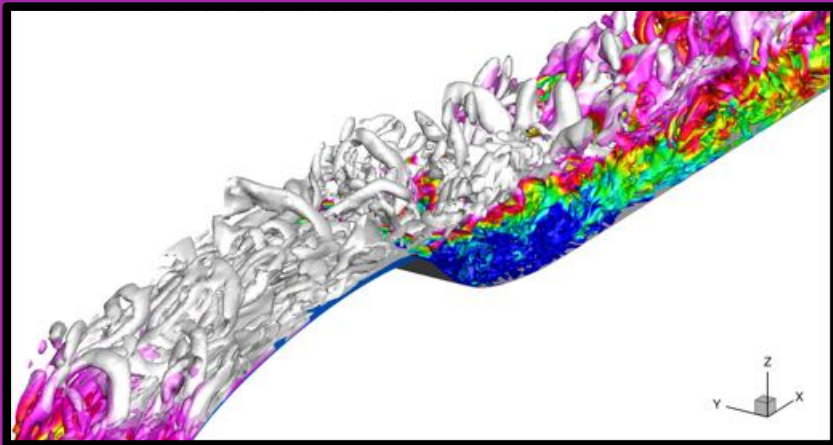
ZDES Mode 3

3D structures

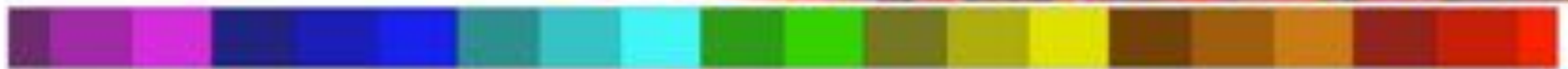
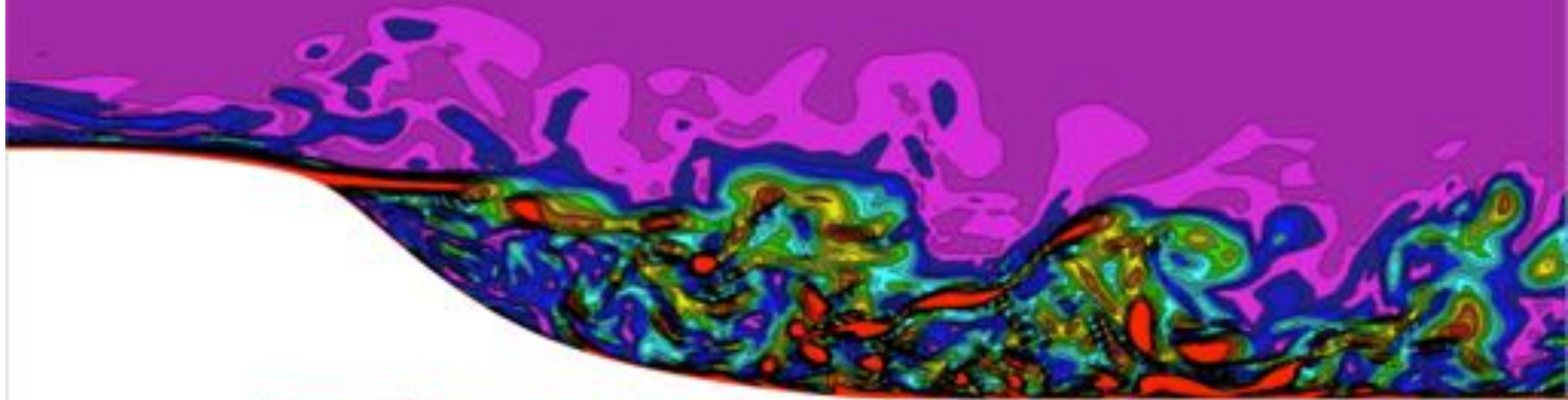
$|\omega|c/U_{ref}$ : 0 6 11 17 22 28 33 39 44 50 56 61 67 72 78 83 89 94 100 26



# NASA 2-D Hump – Application of Zonal DES



Q-criterion

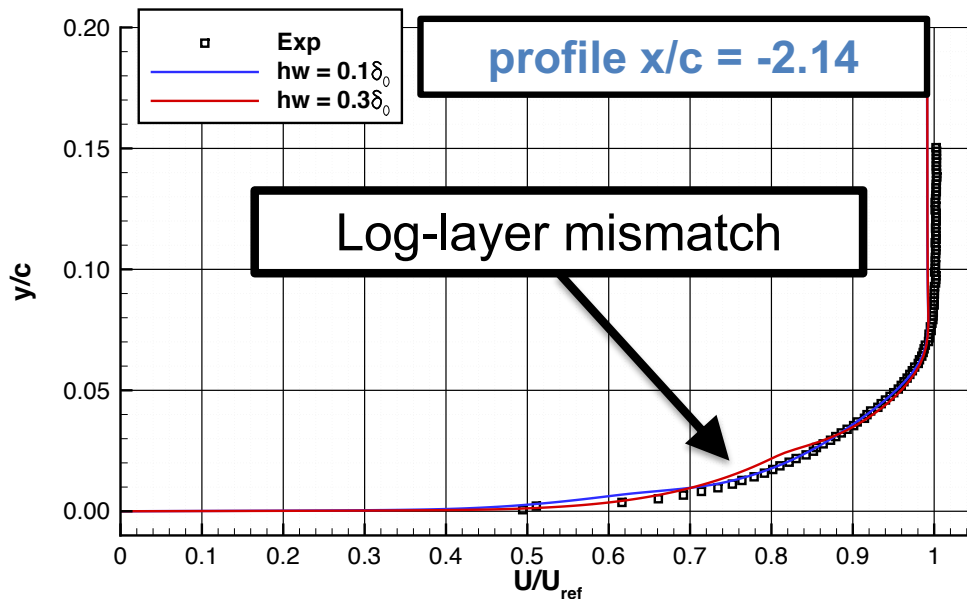
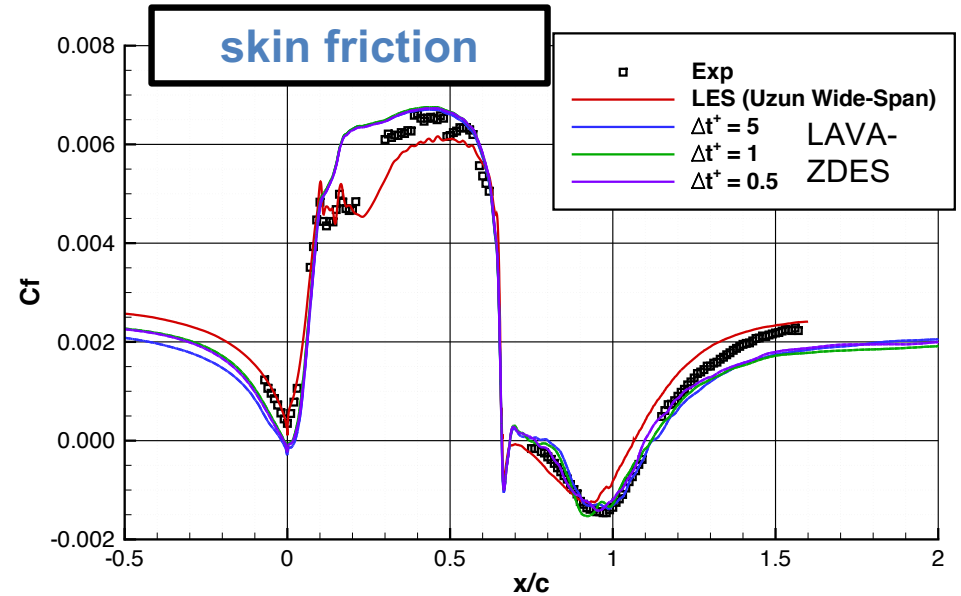
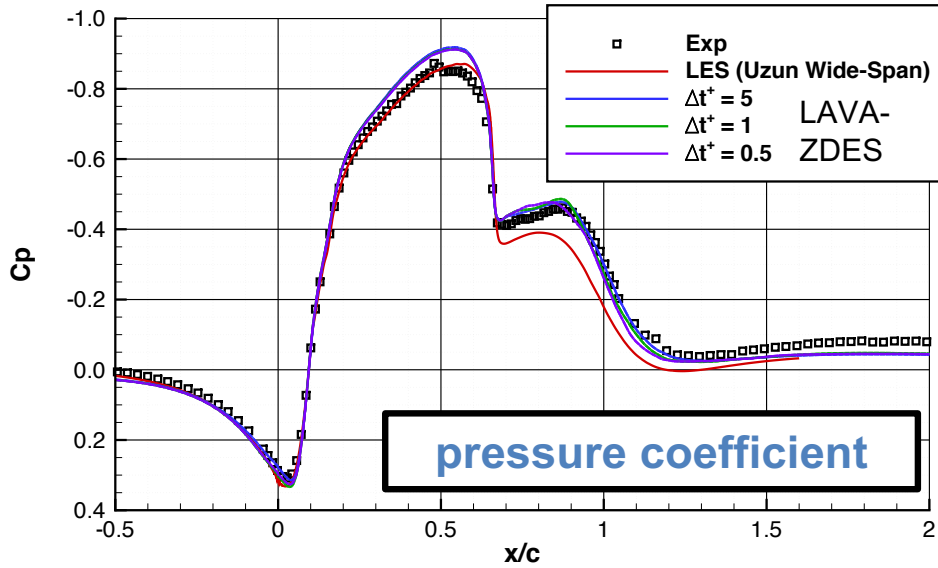


$|\omega|c/U_{ref}$ : 0 6 11 17 22 28 33 39 44 50 56 61 67 72 78 83 89 94 100



# NASA 2-D Hump – Application of Zonal DES

<sup>1</sup> Uzun, A. : [https://turbmodels.larc.nasa.gov/Other\\_LES\\_Data/nasa\\_hump\\_uzun\\_2017.html](https://turbmodels.larc.nasa.gov/Other_LES_Data/nasa_hump_uzun_2017.html)



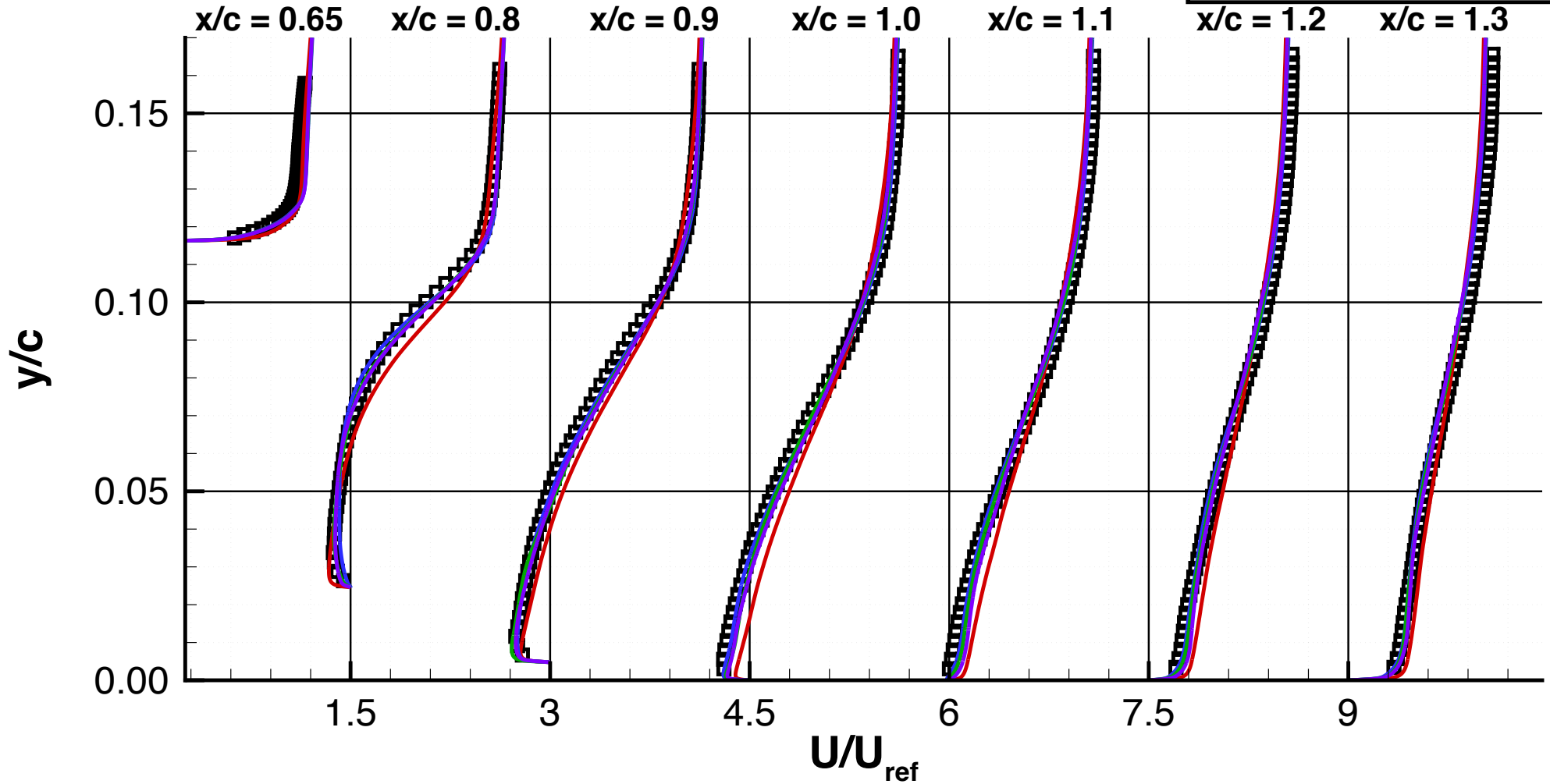
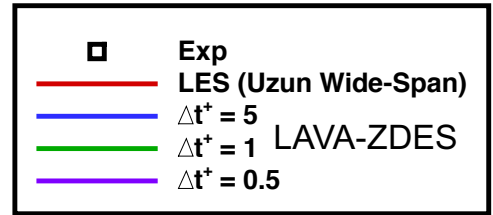
- ✓ ZDES (11.3m) compares well with wall resolved LES<sup>1</sup> (420m) and experiment .
- ✓ The skin-friction is under-predicted in the upstream attached BL
- ✓ Very good agreement in the re-attachment location
- ✓ Noticeable log-layer mismatch in the upstream BL profile

# NASA 2-D Hump – Application of Zonal DES



Profiles shifted by 1.5

streamwise velocity



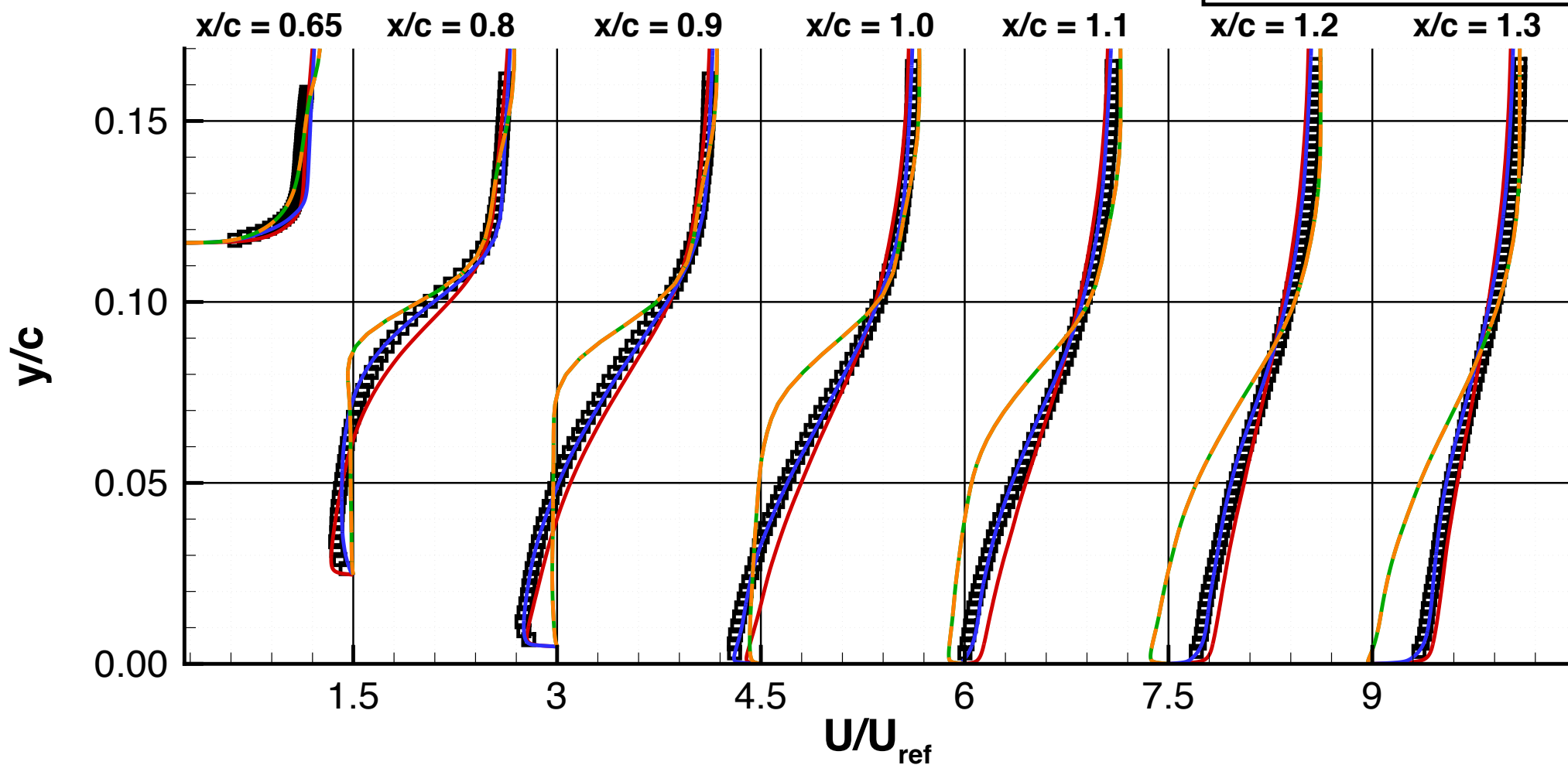
✓ Wall resolved LES mesh has 420m points, ZDES 11.3m points

# NASA 2-D Hump – Hybrid RANS-LES



Profiles shifted by 1.5

streamwise shear stress

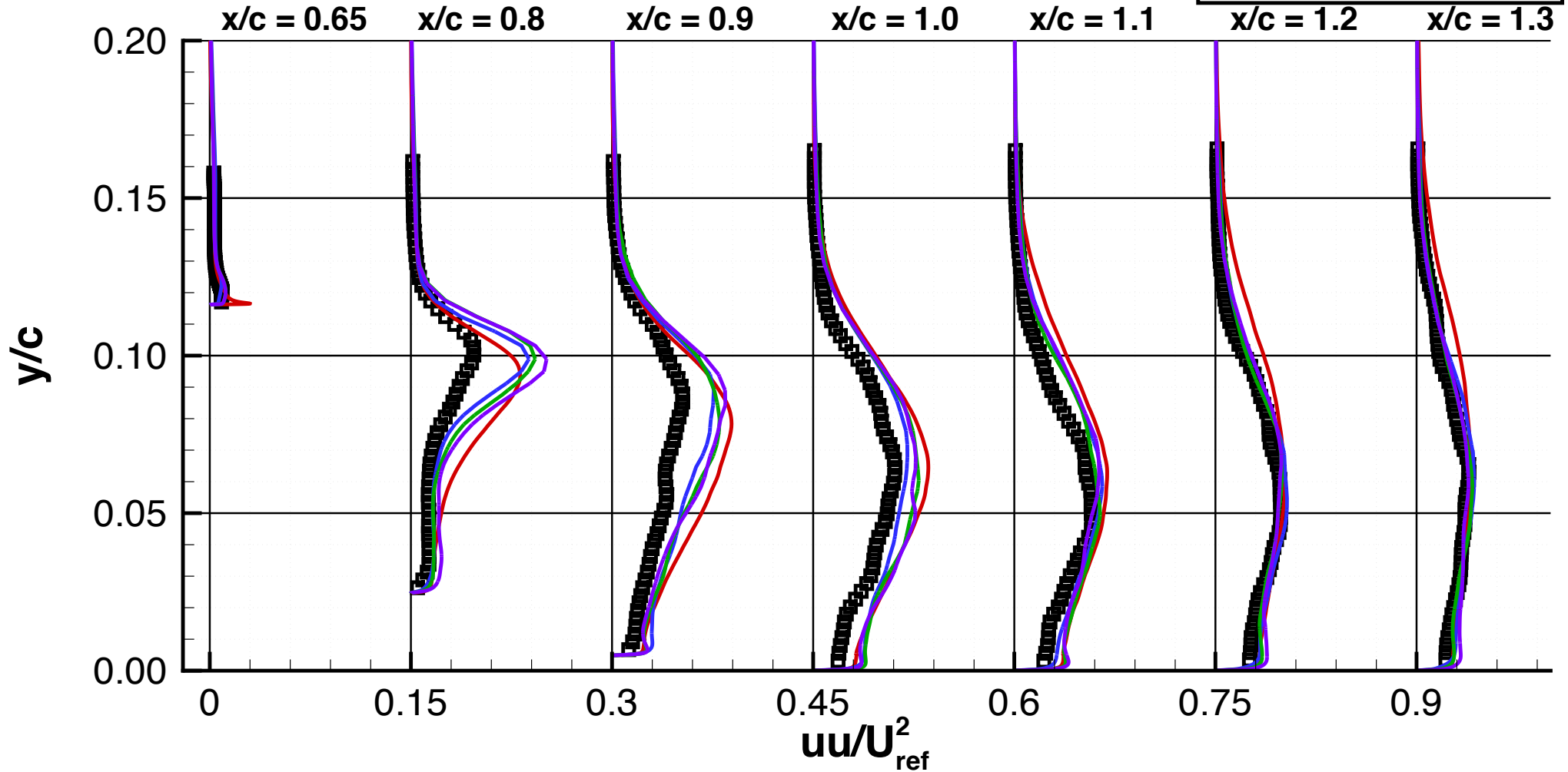


# NASA 2-D Hump – Application of Zonal DES



Profiles shifted by 0.15

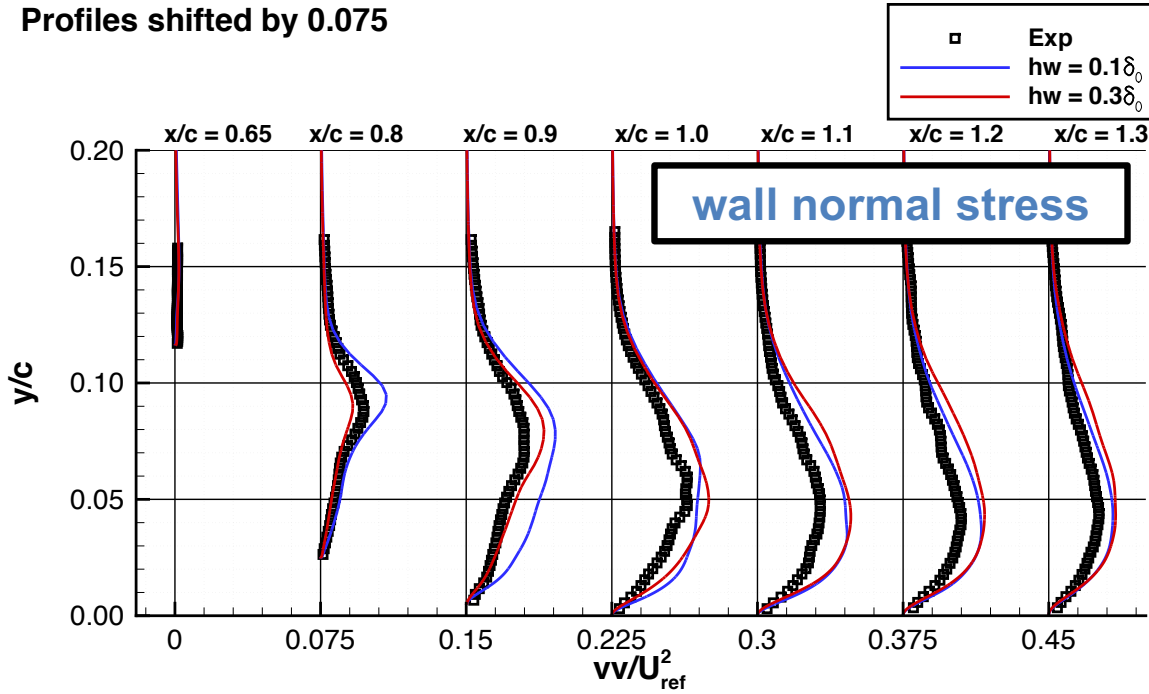
streamwise shear stress



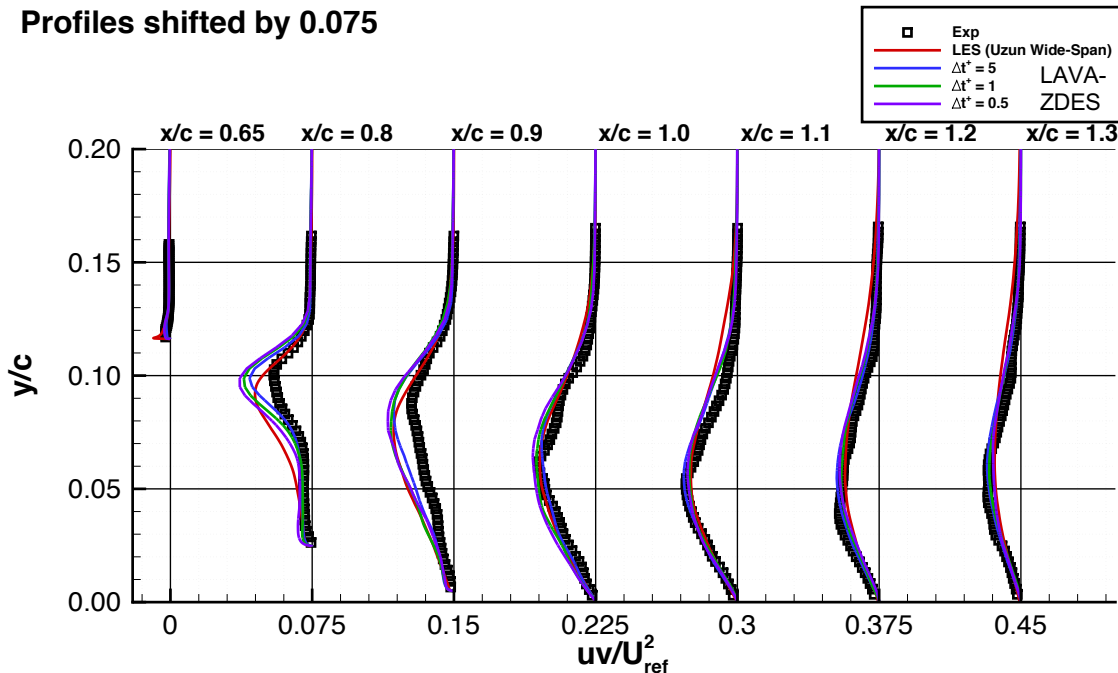


# NASA 2-D Hump – Application of Zonal DES

Profiles shifted by 0.075

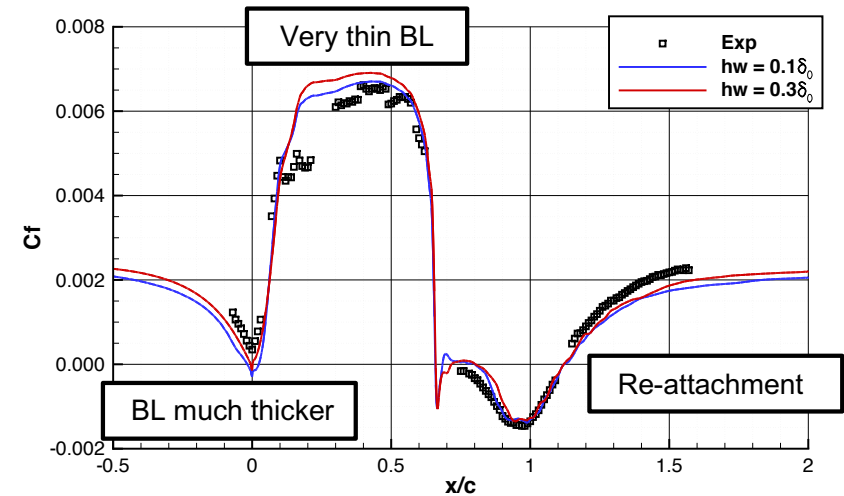


Profiles shifted by 0.075



- ✓ Interface location based on BL thickness on top of hump
- ✓ Interface location constant across whole domain

skin friction coefficient for different interface locations

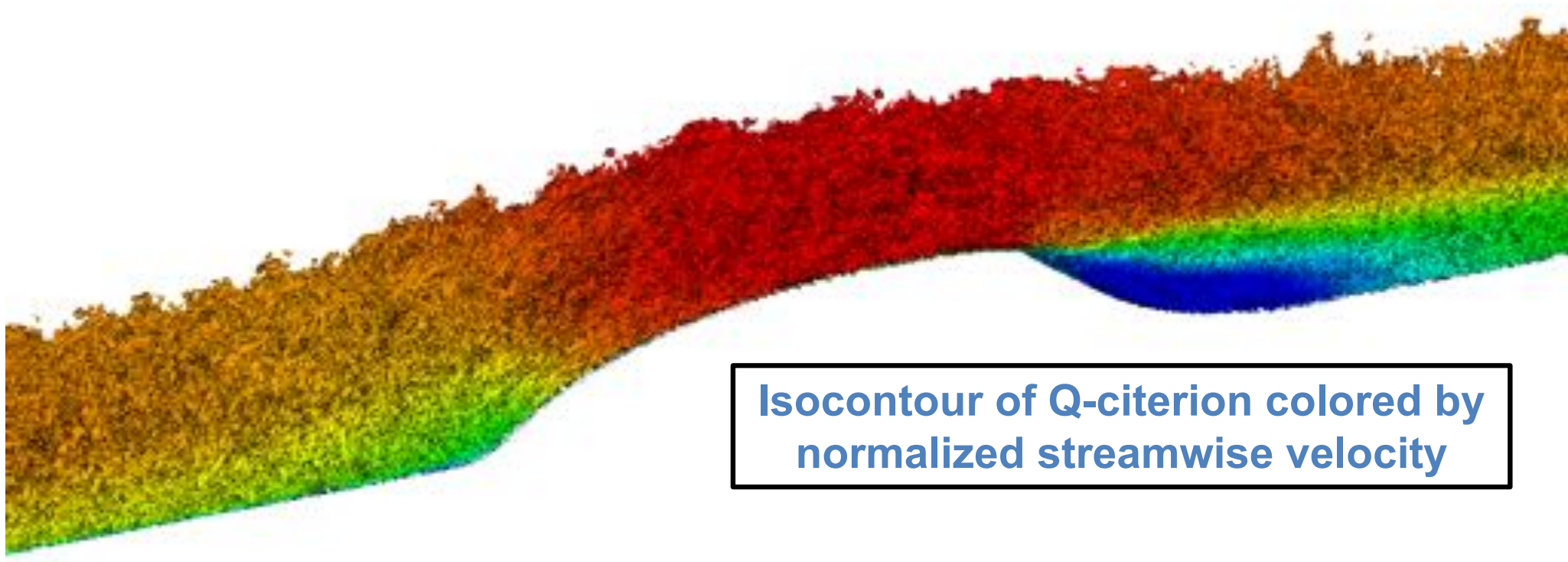


## Future work:

- ✓ Implement interface sensor based on local BL thickness (e.g. from vorticity magnitude)



- ✓ Lattice: D3Q27
- ✓ Collision Model: EMRT
- ✓ Synthetic Eddy Method with scaled DNS Flat plate Data at  $x/c = -3.0$



Isocontour of Q-criterion colored by normalized streamwise velocity

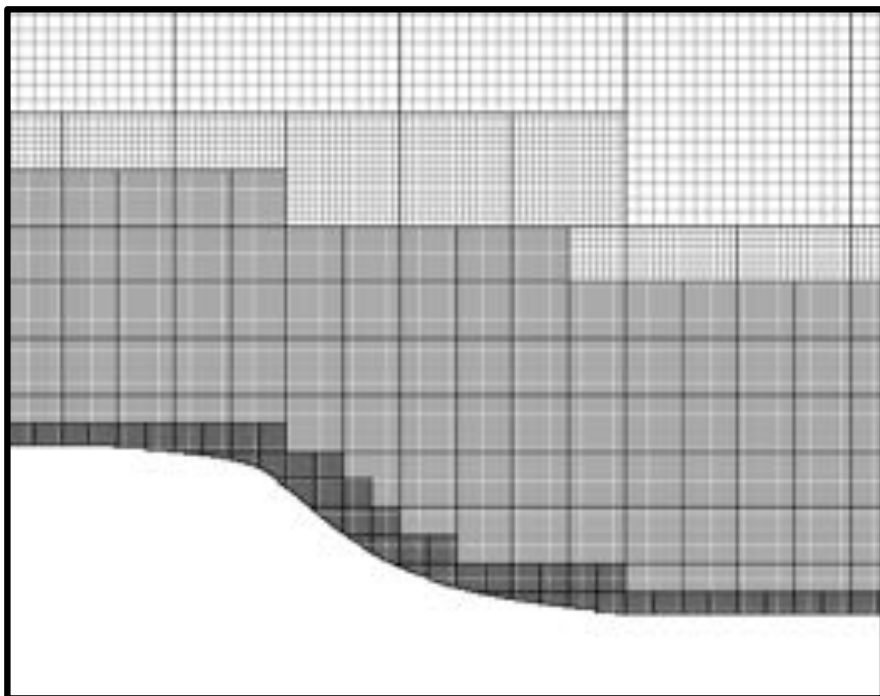
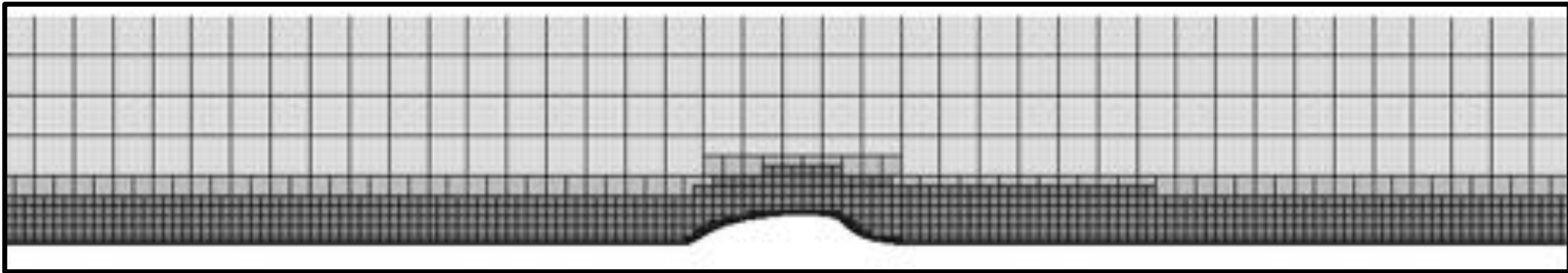
- ✓ Synthetic eddy method created realistic turbulent structures
- ✓ Initial run without included top-wall to simulate side-wall effects



# NASA 2-D Hump – Application of Lattice Boltzmann



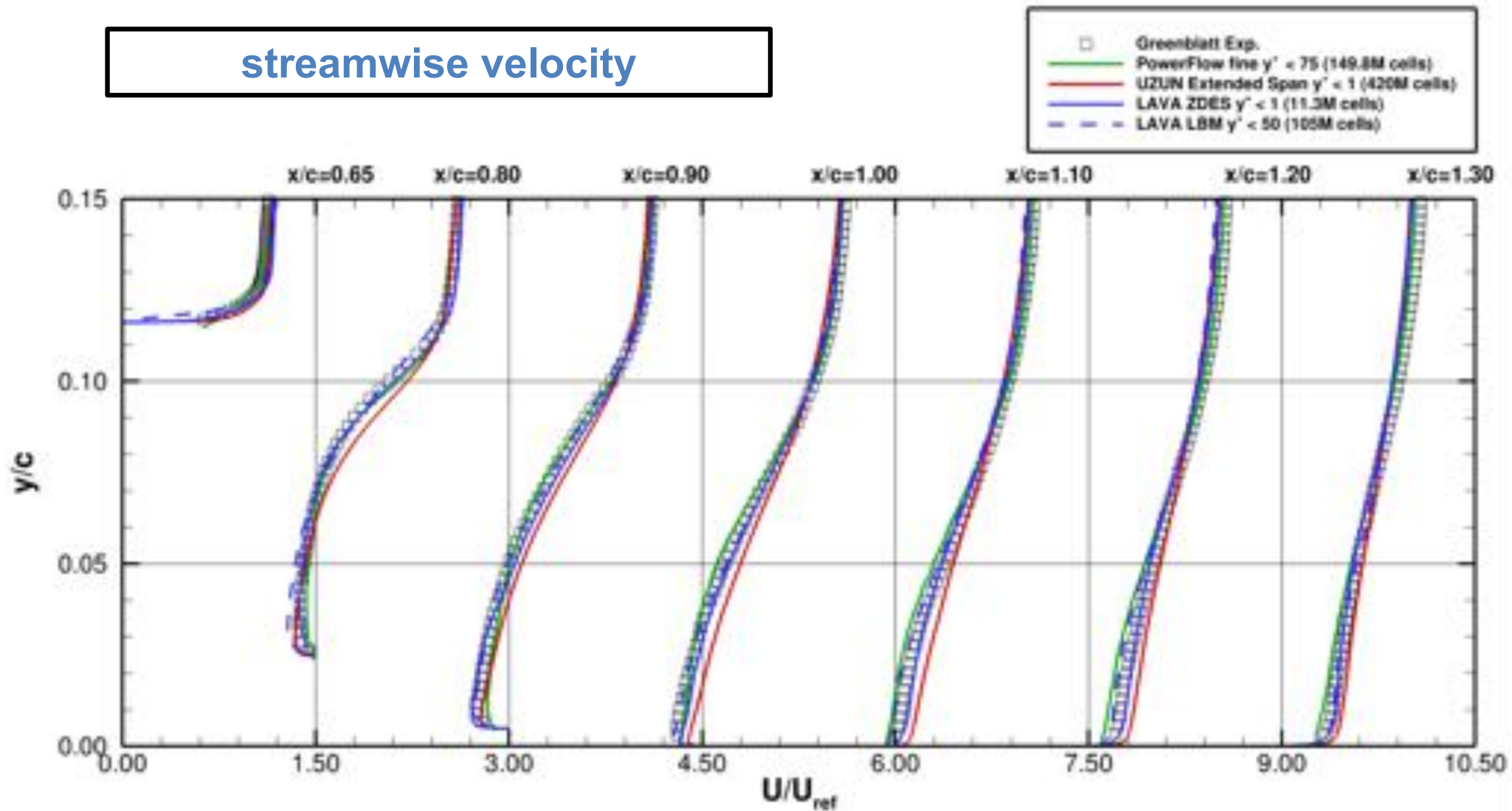
- ✓ Local as well as adaptive mesh refinement well tested in our Cartesian framework.



- ✓ Total of 5 Levels with
- ✓ Refinement ratio of 2
- ✓ Level 3 in regions of high vorticity
- ✓ Level 4 on all viscous walls
- ✓ Level 5 from  $x/c = -0.2$  to  $1.3$
- ✓ 105 million points
- ✓ Spanwise extend 0.2 chord
- ✓  $dy^+ \approx 50$  in wall normal direction



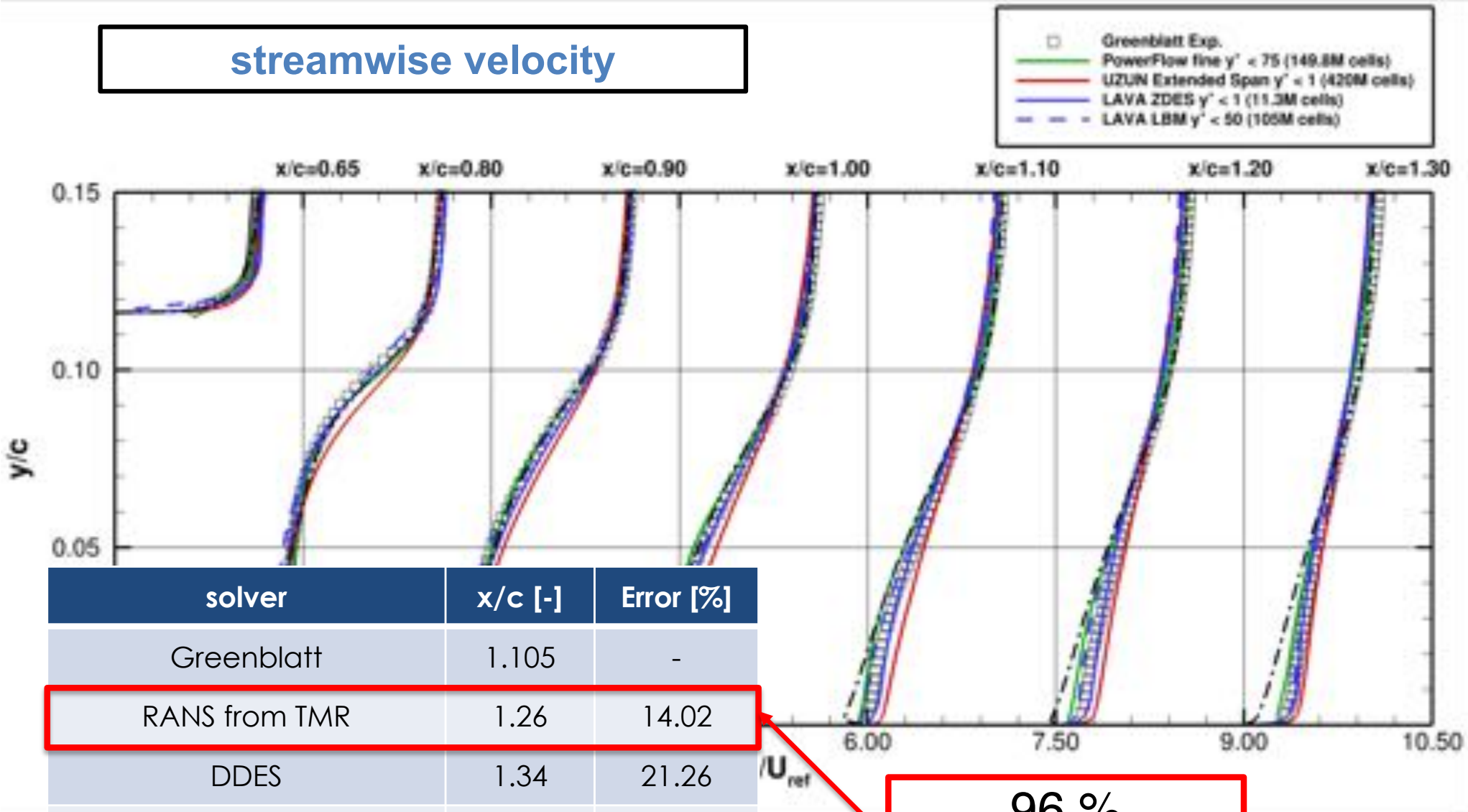
streamwise velocity



✓ Further improvement in coarse fine interface operation necessary



## streamwise velocity

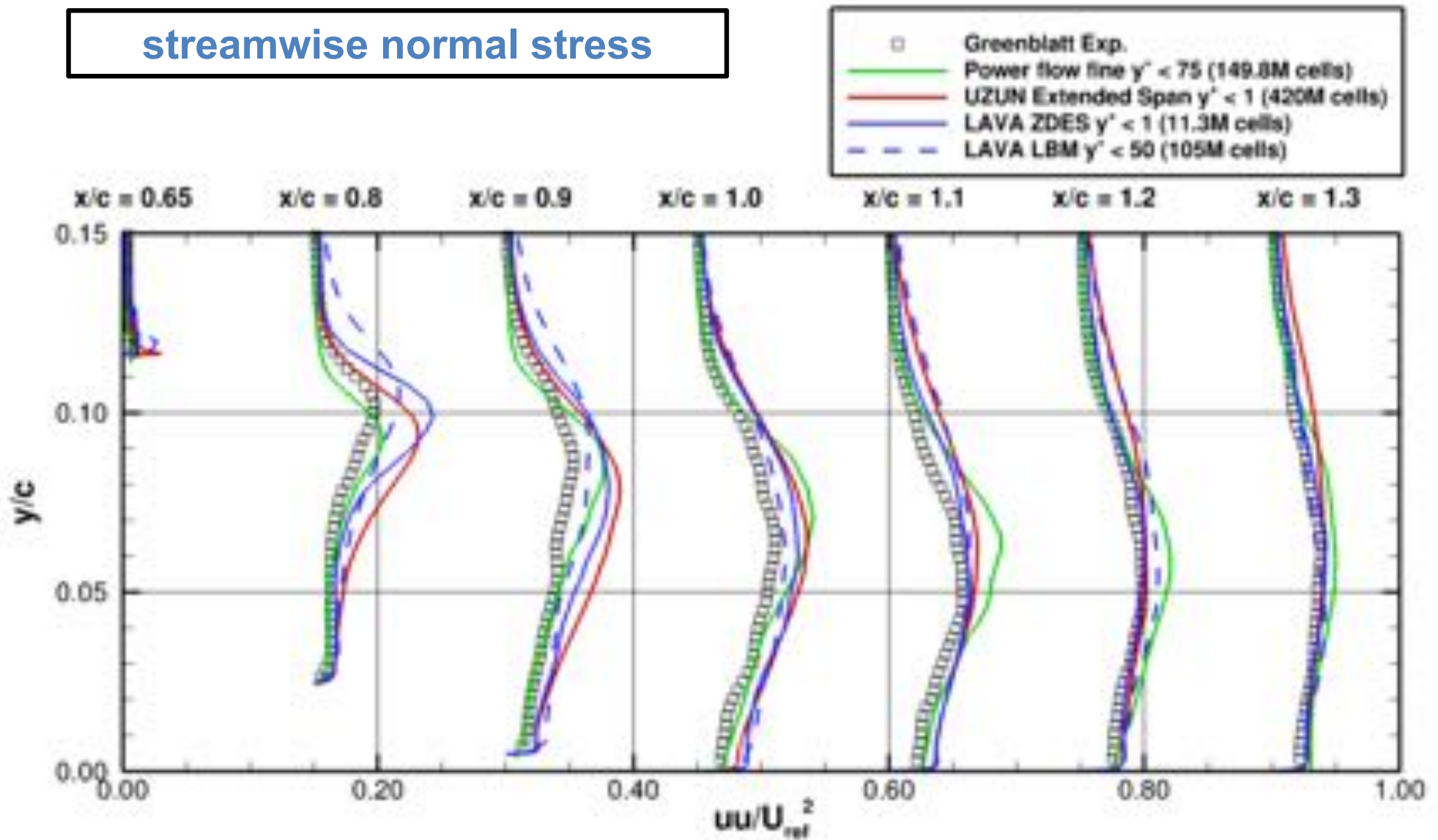


<b>solver</b>	<b>x/c [-]</b>	<b>Error [%]</b>
Greenblatt	1.105	-
RANS from TMR	1.26	14.02
DDES	1.34	21.26
DDES + SEM	1.23	11.31
<b>ZDES + SEM</b>	<b>1.11</b>	<b>0.45</b>

**96 %  
improvement**



streamwise normal stress



✓ Further improvement in coarse fine interface operation necessary

# Summary



## **Overset Curvilinear:**

- ✓ Excellent agreement with state-of-the-art wall-resolved LES (Uzun) for Hump achieved with a significant smaller mesh (11.3M ZDES vs 420M WR-LES).
- ✓ DDES over-predicts the shear-layer strength and causes a spurious inner-layer attached region for Hump and delays development of 3D structures at nozzle exit.
- ✓ Some sensitivity to interface height for ZDES Mode 3 has been observed.

## **Cartesian Lattice Boltzmann:**

- ✓ Hump case has proven to be very challenging on a Cartesian mesh, accurate wall-model crucial for accuracy and efficiency.
- ✓ Coarse-Fine interface very sensitive at higher Reynolds-number, conservative interface necessary.
- ✓ Good agreement achieved once coarse-fine interface was improved and enough grid resolution was provided.

## **Future work:**

- ✓ Add sensor to determine local boundary layer thickness for defining the interface location in ZDES Mode 3.
- ✓ Further enhance wall-models in LBM implementation for higher Reynolds-numbers, e.g. filtered wall-model and equilibrium wall model.
- ✓ Add higher order accurate coarse-fine interface operations.
- ✓ Implement a hybrid RANS-LBM model to add modeled stress in highly under resolved regions.

# Acknowledgments



- ✓ This work was partially supported by the NASA ARMD's Transformational Tools and Technologies (T<sup>3</sup>) and Advanced Air Transport Technology (AATT) projects
- ✓ LAVA team members in the Computational Aerosciences Branch at NASA Ames Research Center for many fruitful discussions
- ✓ Tim Sandstrom (optimized ray-tracing kernels, and particle visualizations) NASA Ames Research Center
- ✓ Computer time provided by NASA Advanced Supercomputing (NAS) facility at NASA Ames Research Center

# Questions?

