



### Prediction of Lunar Reconnaissance Orbiter Reaction Wheel Assembly Angular Momentum Using Regression Analysis

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- Study Motivation & Goal
- Lunar Reconnaissance Orbiter (LRO) Overview
  - Spacecraft
  - Angular momentum control
- Methodology
  - Removing effects of maneuvers
  - Forming piece-wise regression model
- Results
  - Test against 2013 2014 telemetry
- Conclusion & Future Work





# Introduction

Study Motivation & Goal

LRO Overview

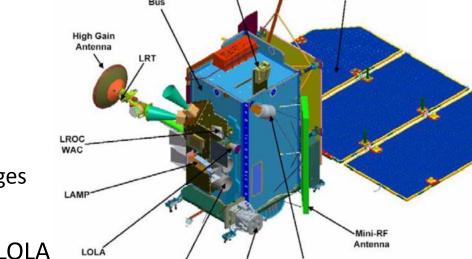
LRO Angular Momentum

#### А

#### Legacy planning procedures often resulted in unloads being performed more frequently than needed

#### Motivation

- Conserve fuel
  - Fuel remaining at start of 2016: ≈ 34 kg
  - Current fuel usage: ≈ 4 kg/yr
    - Thrusters used for momentum unloads ( $\Delta$ Hs)
    - Includes station keeping &  $\Delta Hs$ , but not orbit changes
- Increase science collection
  - Three instruments safed during  $\Delta$ Hs: DLRE, LEND, LOLA
  - One also decontaminated for 24 hrs thereafter: LAMP



LEND

Spacecraft

LROC

NACs (2)

Solar Array

Systen

Divine





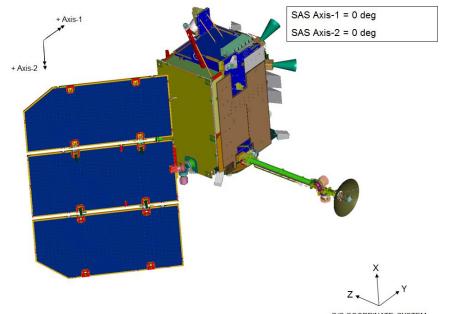
#### GOAL: Build model to accurately predict growth in LRO angular momentum, enabling optimal scheduling



Changed several times, now 20 km x 150 km

LRO Spacecraft Overview

- Nominally nadir-pointing
- Solar Array (SA)
  - Has inner & outer gimbals
  - Uses tracking and parked configurations
    - Tracking
      - $|\beta| < 30^\circ$ : Gimbals track sun, but with +30° outer gimbal offset
      - $30^{\circ} < |\beta| < 35^{\circ}$ : Gimbals track sun, but with -30° outer gimbal offset
    - Parked
      - $35^{\circ} < |\beta| < 55^{\circ}$ : park inner gimbal at -90°, outer gimbal at +45°
      - $|\beta| > 55^\circ$ : park inner gimbal at -90°, outer gimbal at +15°
  - Offsets and fixed angles selected to maintain gimbals < 45° C





## LRO Attitude & Disturbance Torques

- Attitude control
  - Reaction wheel assembly (RWA) used to:
    - Slew spacecraft

Gravity gradient torque

• Maintain attitude, countering disturbance torques

Since lunar orbit, only 2 significant disturbance torques

Solar array dominant term due to large moment arm

Movement of solar array dominates changes in LRO inertia matrix

- RWA angular momentum capacity
  - 115 Nms at nominal bus voltage
  - 80 Nms at minimum bus voltage

Solar radiation pressure (SRP) torque

LRO Reaction Wheel Assembly

All disturbance torque orbitaveraged values are simply functions of  $\beta$ 

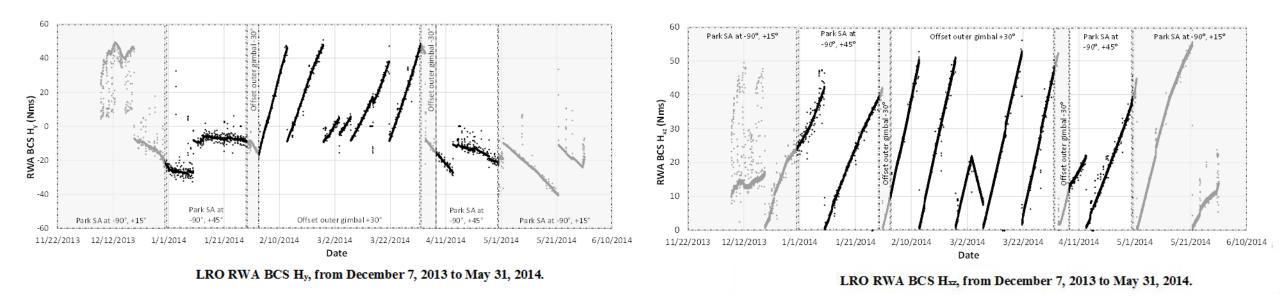












- Body Coordinate System (BCS)  $H_y$  very dependent on solar array configuration (and hence  $\beta$ )
- Activities, like pitch & yaw campaigns in Dec 2013 can overwhelm trend

Model must include both regression against  $\beta$  and adjustments for activities





# Methodology

Overview

Determining effects of maneuvers

Forming piece-wise regression model



# Methodology Overview

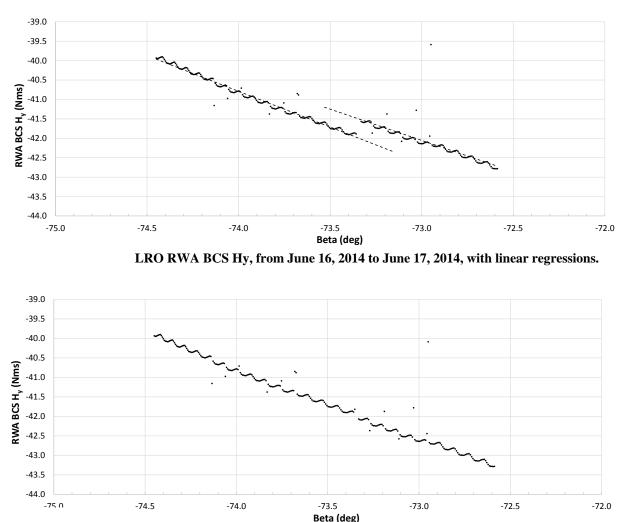


- Piece-wise polynomial least-squares regression
  - One year's worth of data
    - Regress Hy and Hxz against beta separately, with Htot simply being RSS
    - October 2014 October 2015
    - Covers full cycle of beta values
  - Linear and cubic regressions
  - Define piece boundaries based on SA modes
- First remove effects of slews & unloads to see 'natural' trend
  - Analyze angular momentum in vicinity of each and every activity
  - Collect perturbations induced by activities & make ruleset
  - Perform regression
  - Use regression coefficients—and perturbations—to predict future momentum

#### LRO RWA BCS H<sub>y</sub>, from June 16, 2014 to June 17, 2014, without effect of roll maneuver. nuary 2017. 10

# Determining Effects of Maneuvers

- Perform linear regressions on either side of activity
  - Perturbance is vertical step change
  - Remove step change to smooth data
  - Repeat several hundred times
  - Example: 0.5-Nms increase in Hy caused by 59° LROC roll
- Make "ruleset"
  - Group slews by type and beta regime at time of slew
  - Define changes in angular momentum due to slew/beta pairs

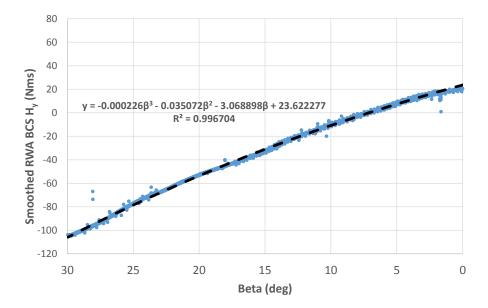




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## Forming Piece-Wise Regression Model

- Perform regressions with now smooth data
  - Least squares
  - On Hy & Hxz
  - SA modes guide boundary selection
  - Example at right: beta going from 30° to 0°
- Record six decimal places for coefficients for sufficient precision in angular momentum
- R<sup>2</sup> values > 0.99 typical



Smoothed LRO RWA BCS  $H_{_V}\!,$  for  $\beta$  spanning from 30° to 0°.

Selected linear regression when strongly linear, arbitrarily selected cubic otherwise—it's all about simply achieving a good fit







# Results

Hy

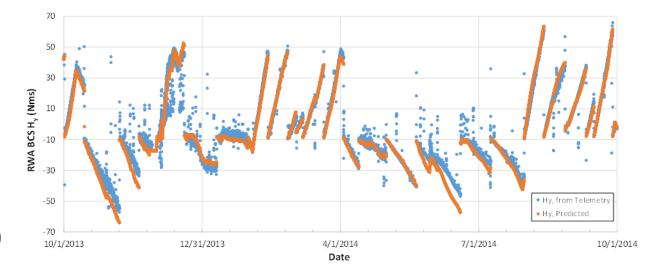
Hxz

Total H

## 2013 – 2014 Test: Hy

- Use regression from Oct 2014 Oct 2015 to predict angular momentum in previous year
- Immediately after each unload
  - Initialize model to values from telemetry (Hy≈-9 Nms, Hxz≈0 Nms)
  - Predict angular momentum until next unload
    - 'Baseline' prediction based on:
      - Regression coefficients
      - Beta values predicted at time by FD
    - Add step changes using list of performed slews

Achieved very good fit, even during times when spacecraft activities completely obscured underlying trend



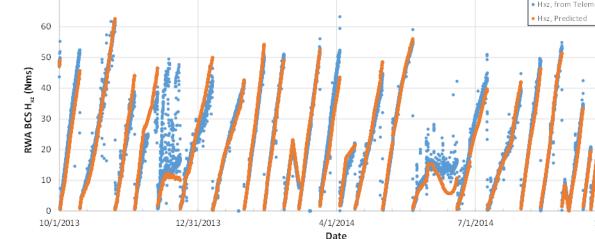


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10/1/2014

Achieved good fit, though most challenging period is when beta has just retreated away from ± 90°



- Largely very good agreement except for Dec 2013 & June 2014
  - Corresponds to when beta has just retreated away from ± 90°
  - Morphology of predicted trend not matching observations
  - Max prediction errors approaching 10 Nms
- Have since formed new regression equations with better, though not perfect fit
- Total H is most important



### 2013 – 2014 Test: Hxz

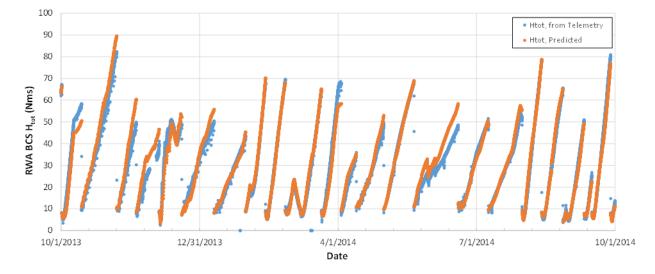




## 2013 – 2014 Test: Total H



- Total H used for unload planning
- Small prediction errors at time of next unload:
  - Mean = 3.7 Nms
  - Median = 2.7 Nms
  - Max = 10.6 Nms
- Operational results would likely be even better than here
  - OPSCON would include using tool intermittently
  - Opportunities for re-synching model against telemetry



Prediction capabilities vastly outperform legacy method employed by mission





# Conclusion

Summary

Future Work

Discussion





- LRO operations now uses these accurate angular momentum predictions
  - Especially accurate if schedule known far in advance
  - Currently schedule 1 2 weeks in advance
  - Mission investigating scheduling farther out based on results of study
- Momentum unloads now performed more optimally
  - Momentum target now selected depending on trend experienced after unload
    - For example, don't select -10 Nms if trend is to become more negative
    - Delays next unload by 3 9 days, depending on trend
  - Have waited as much as 42 days between unloads
- Study has enabled other improvements
  - Identified slews that counteract trend in angular momentum
  - Hope to eventually control angular momentum without using propellant

## Future Work

- Developing tool to deliver to operations team
- Analyzing angular momentum behavior as beta retreats from ± 90°
- Testing the use of select operational slews to decrease angular momentum
  - Off-nadir attitude providing beneficial gravity-gradient torque
  - SRP smaller factor



LRO Mission Operations Center







# Thank you for your attention

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