

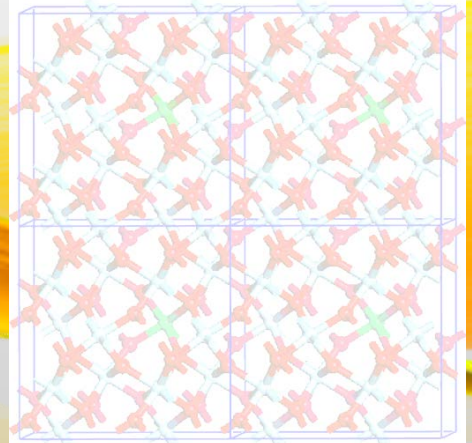
Application of Ab initio Methods in the Development of Advanced Technical Ceramics

Jon Goldsby, PhD , MBA

National Aeronautics and Space Administration
Glenn Research Center
Cleveland, Ohio

$$ZT = \frac{S^2 \sigma T}{\kappa}$$

$$J = AT^2 e^{-\left(\frac{E_w}{kT}\right)}$$

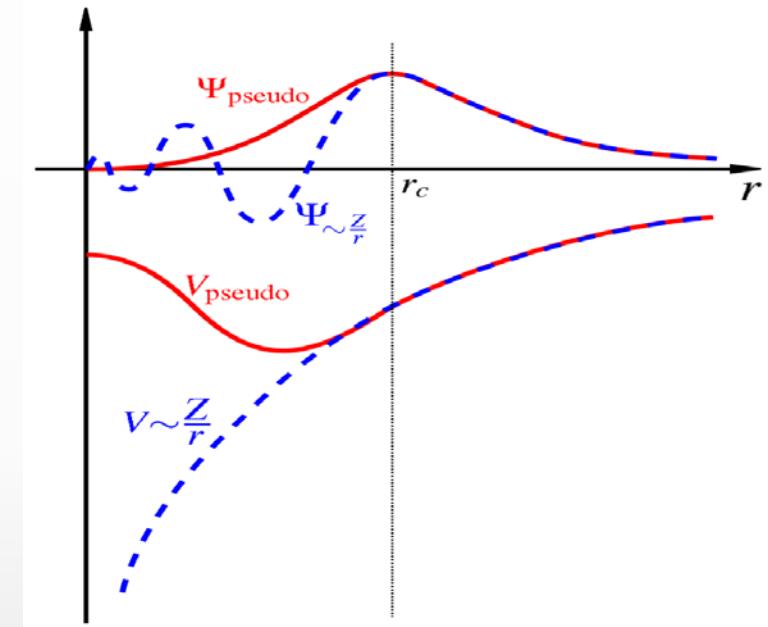


Computational Methods

The Schrödinger Equation

$$\left[\frac{-\hbar^2}{2m} \frac{\partial^2}{\partial x^2} + V(x) \right] \psi(x) = E \psi(x)$$

Hamiltonian operator Wave function Energy

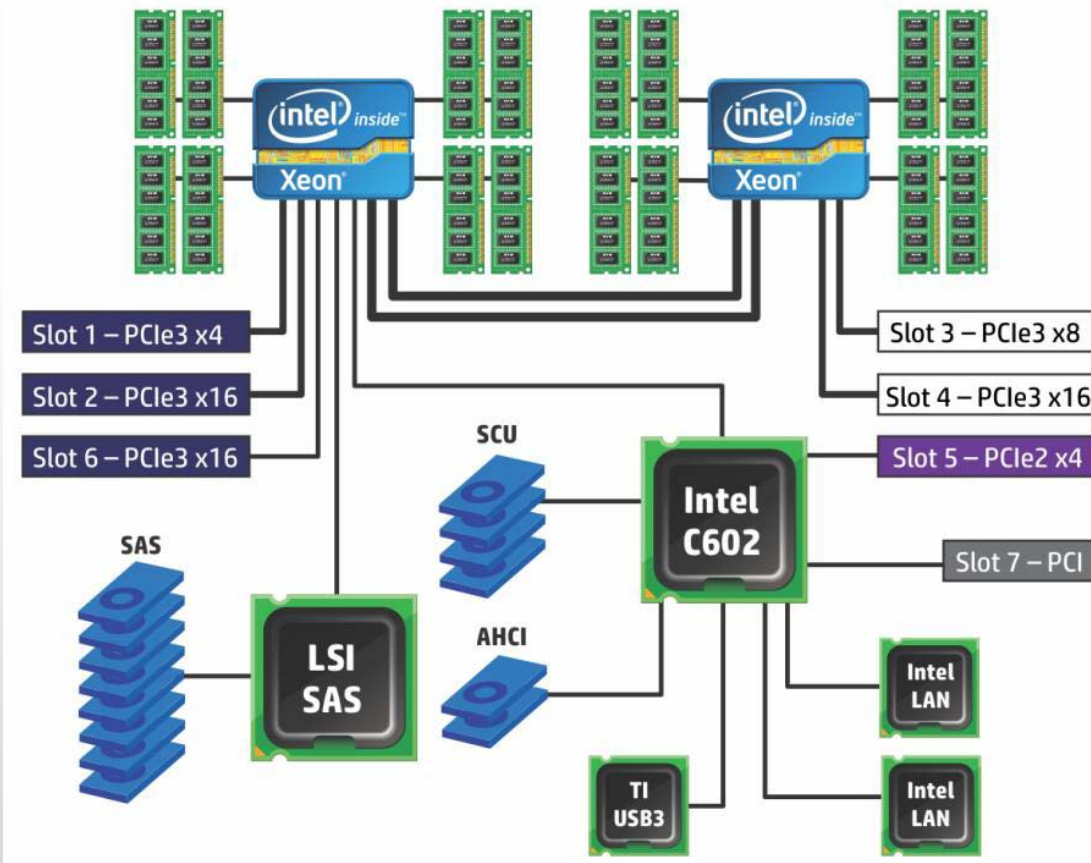


Vienna Ab-initio Simulation Package

The Vienna Ab-initio Simulation Package, better known as **VASP**, is a package for performing ab initio quantum mechanical molecular dynamics using either Vanderbilt pseudopotentials, or the projector augmented wave method, and a plane wave basis set

Computing Platform

Figure 1: HP Z820 Workstation Block Diagram

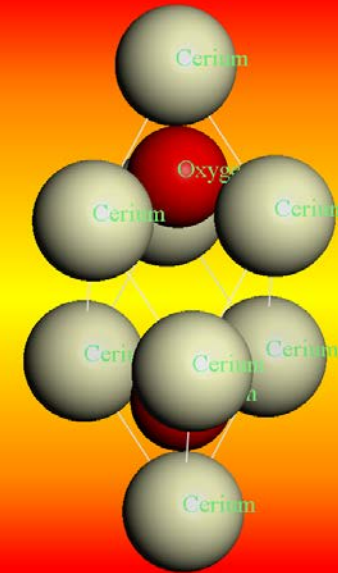
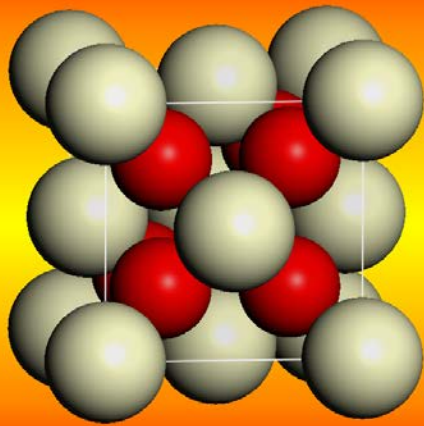


HEWLETT PACKARD HP Z820
WORKSTATION 2 INTEL XENON
PROCESSORS ALLOWING 32 CORES FOR
CALCULATION WITH 192 GB OF RANDOM
ACCESS MEMORY



Dielectric ceramic

A simple case: Cerium Oxide



A change to a simpler symmetry reduces the computational load

Elastic Constants calculated results for Ceria

$$c_{ij}[\text{GPa}] = \begin{bmatrix} 455.0683 & 188.74757 & 188.74757 & 0.00000 & 0.00000 & 0.00000 \\ 188.74757 & 455.06836 & 188.74757 & 0.00000 & 0.00000 & 0.00000 \\ 188.74757 & 188.74757 & 455.06836 & 0.00000 & 0.00000 & 0.00000 \\ 0.00000 & 188.74757 & 0.00000 & 81.48183 & 0.00000 & 0.00000 \\ 0.00000 & 188.74757 & 0.00000 & 0.00000 & 81.48183 & 0.00000 \\ 0.00000 & 188.74757 & 0.00000 & 0.00000 & 0.00000 & 81.48183 \end{bmatrix}$$

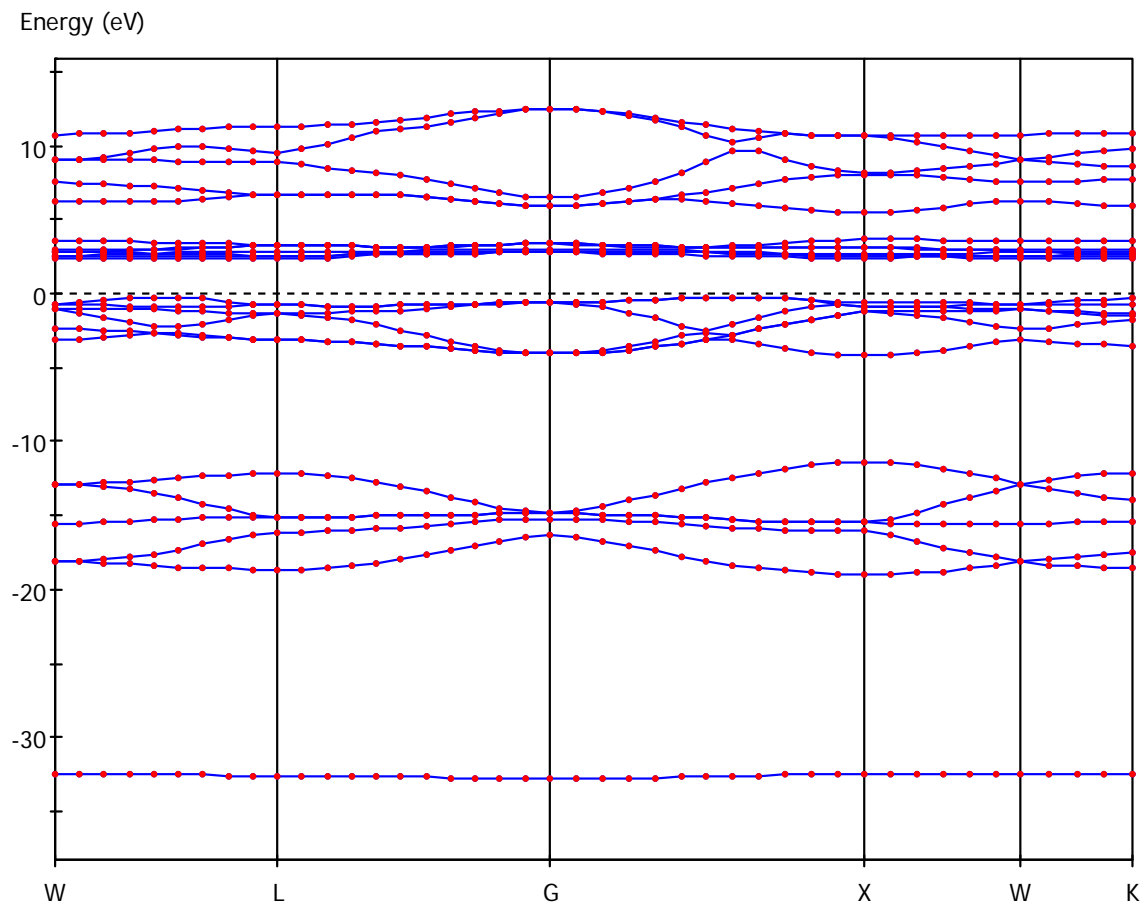
elastic constants c_{11} , c_{12} , c_{14}

and bulk modulus ($B = 277.52117 \pm 0.348$ (GPa)), the mechanical stability criteria

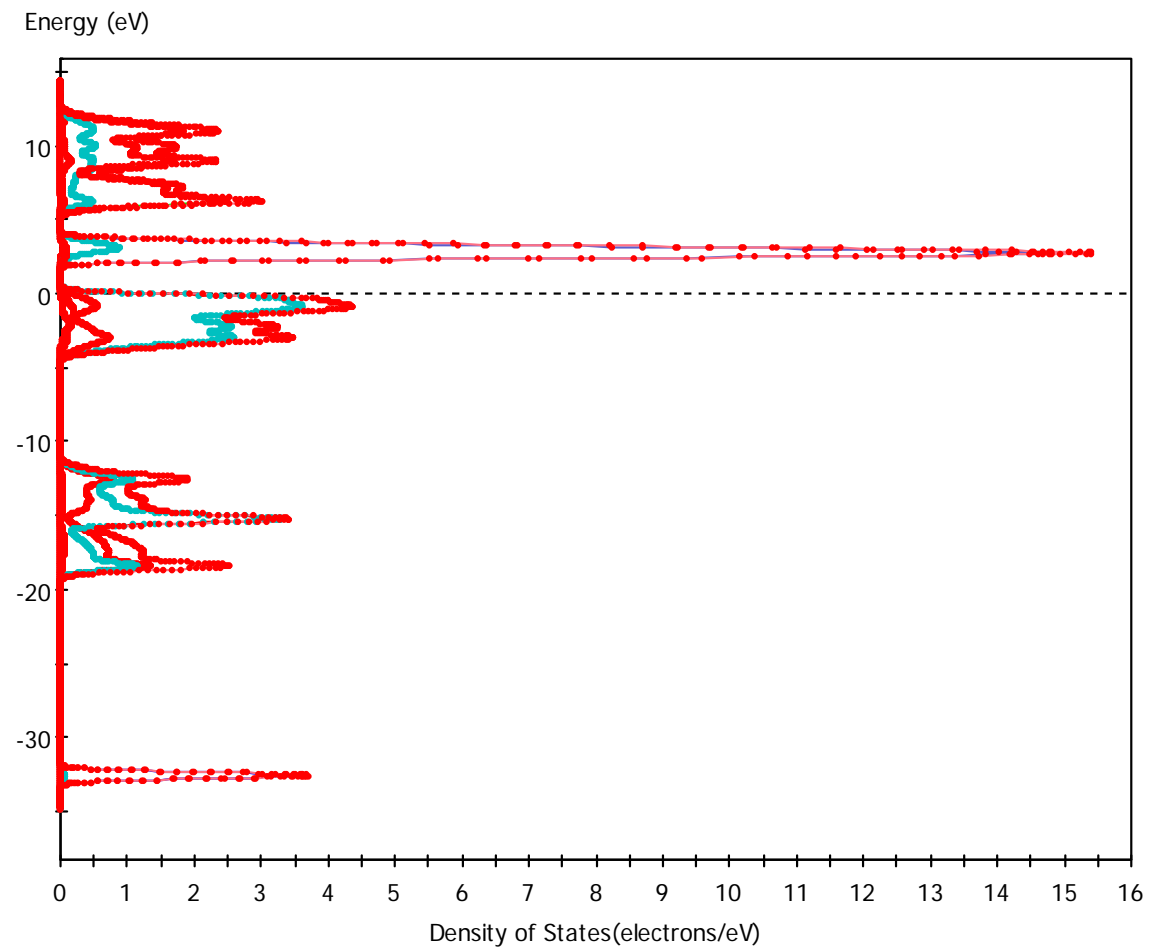
For this case, c_{11} and $c_{44} > 0$ ($c_{11} - c_{12}$) and ($c_{11} + 2c_{12}$).

In addition, the bulk modulus must be greater than c_{12} but less than c_{11} , thus for ceria the mechanical stability requirements are met.

CASTEP Band Structure
Band gap is 2.555 eV



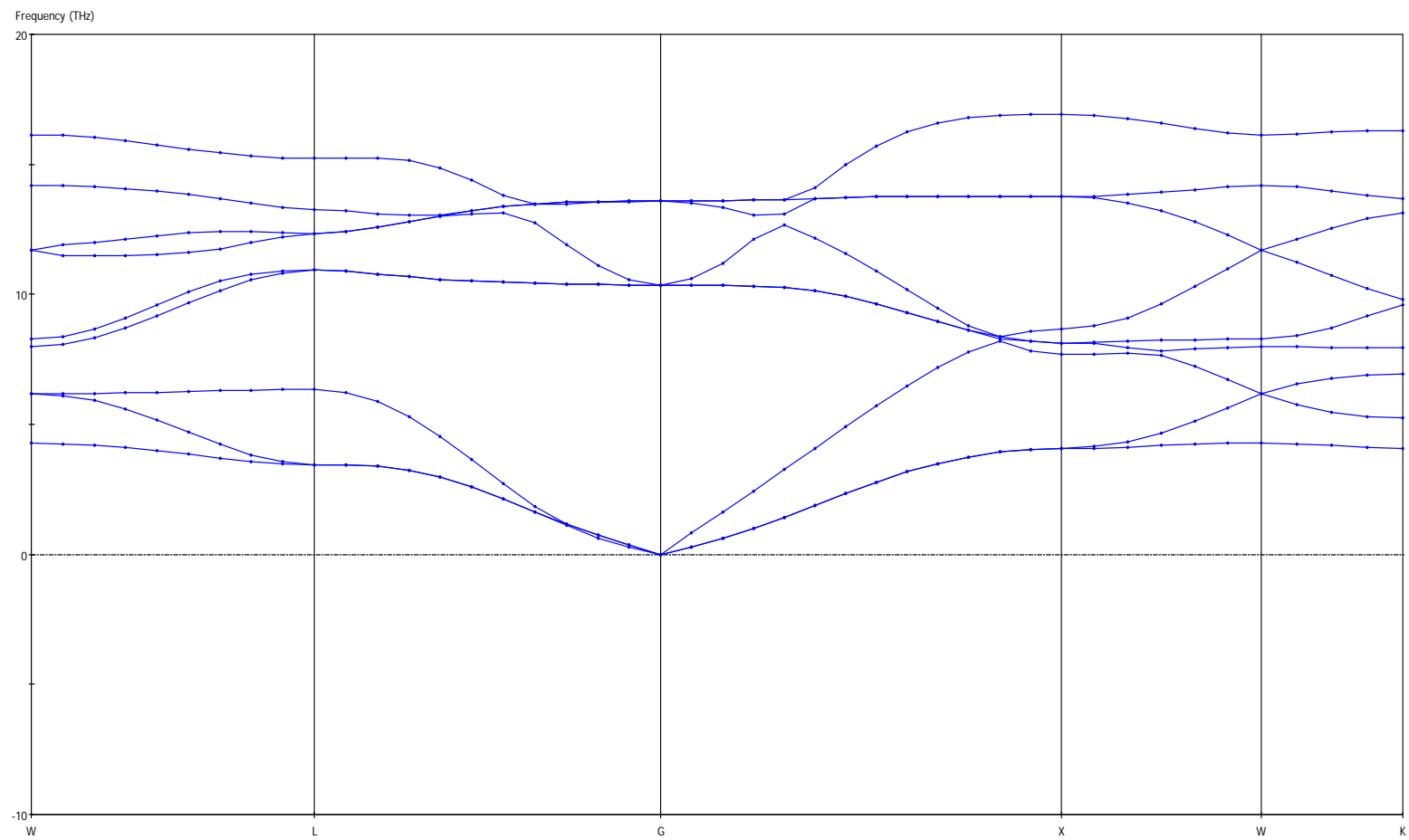
CASTEP Partial Density of States



— s — p — d — f — Sum

Phonon calculation results

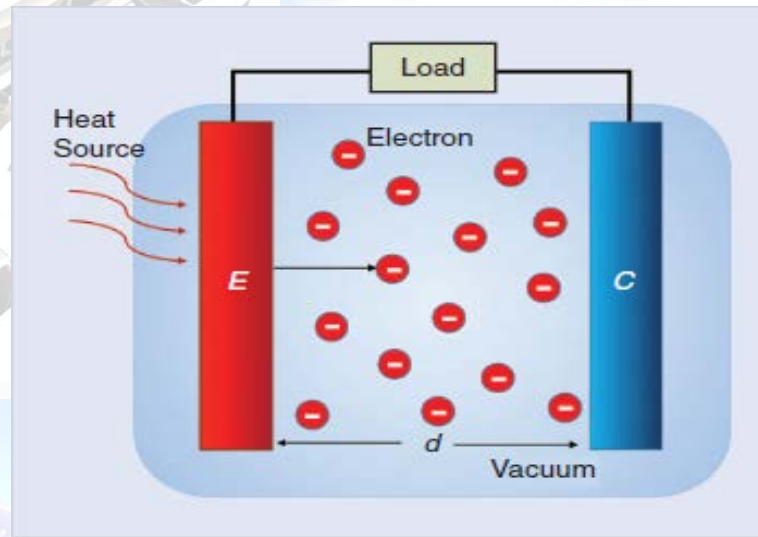
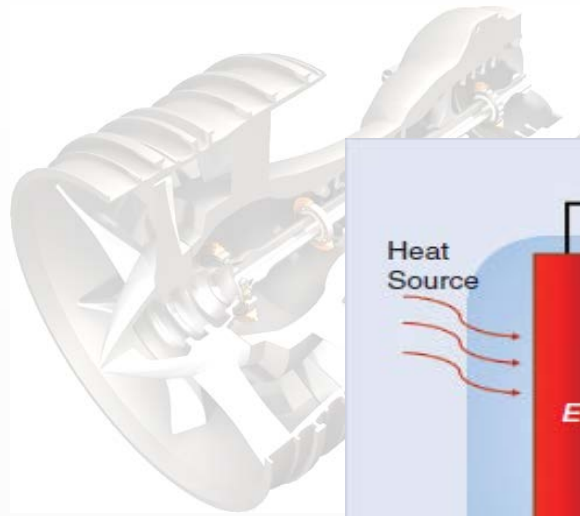
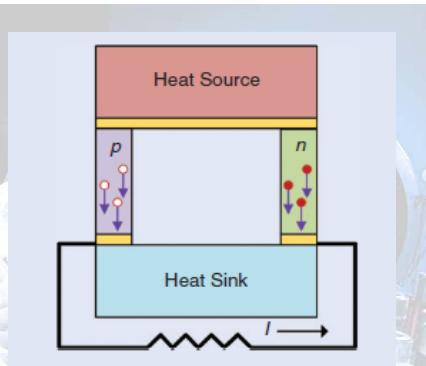
CASTEP Phonon Dispersion





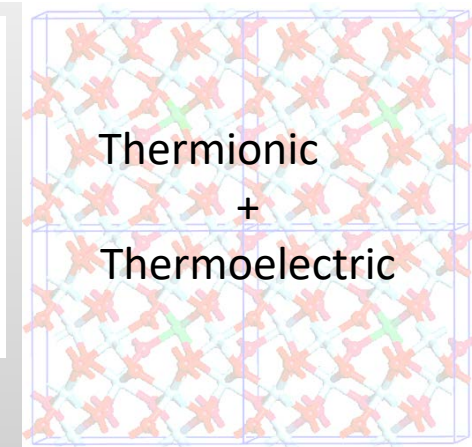
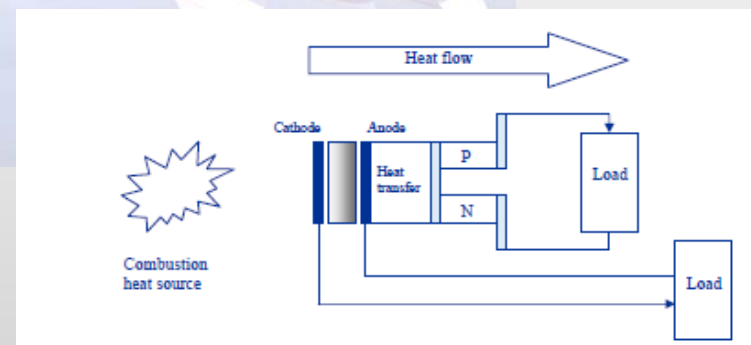
Thermoelectric ceramic

Concept Overview

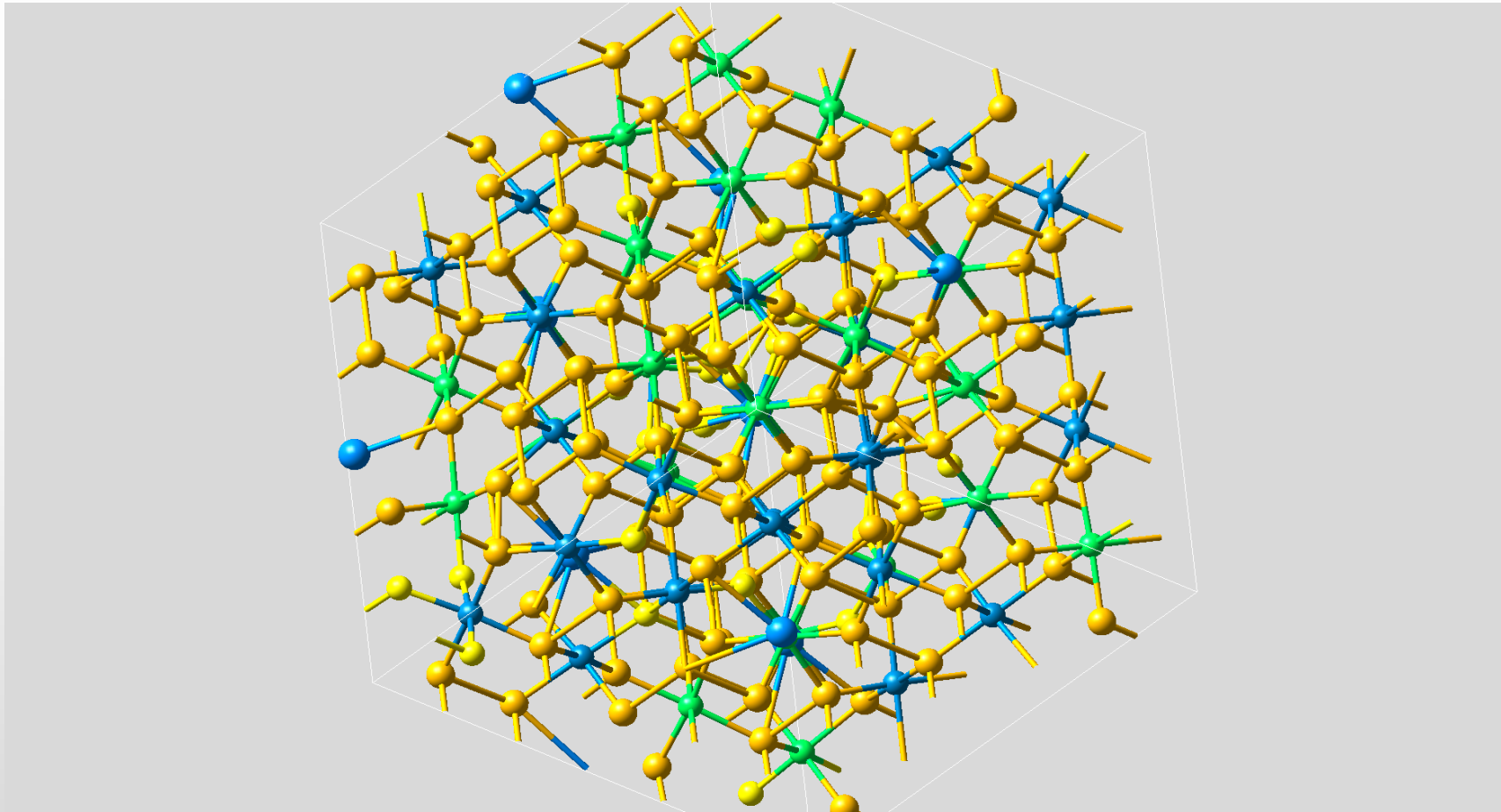


$$J = AT^2 e^{-\left(\frac{E_w}{kT}\right)}$$


- Solid state energy harvesting using waste heat available in gas turbine engine offers potential for power generation to meet growing power needs of aircraft
- Thermoelectric material advances offer new opportunities
- Weight-optimized integrated turbine engine structure incorporating energy conversion devices

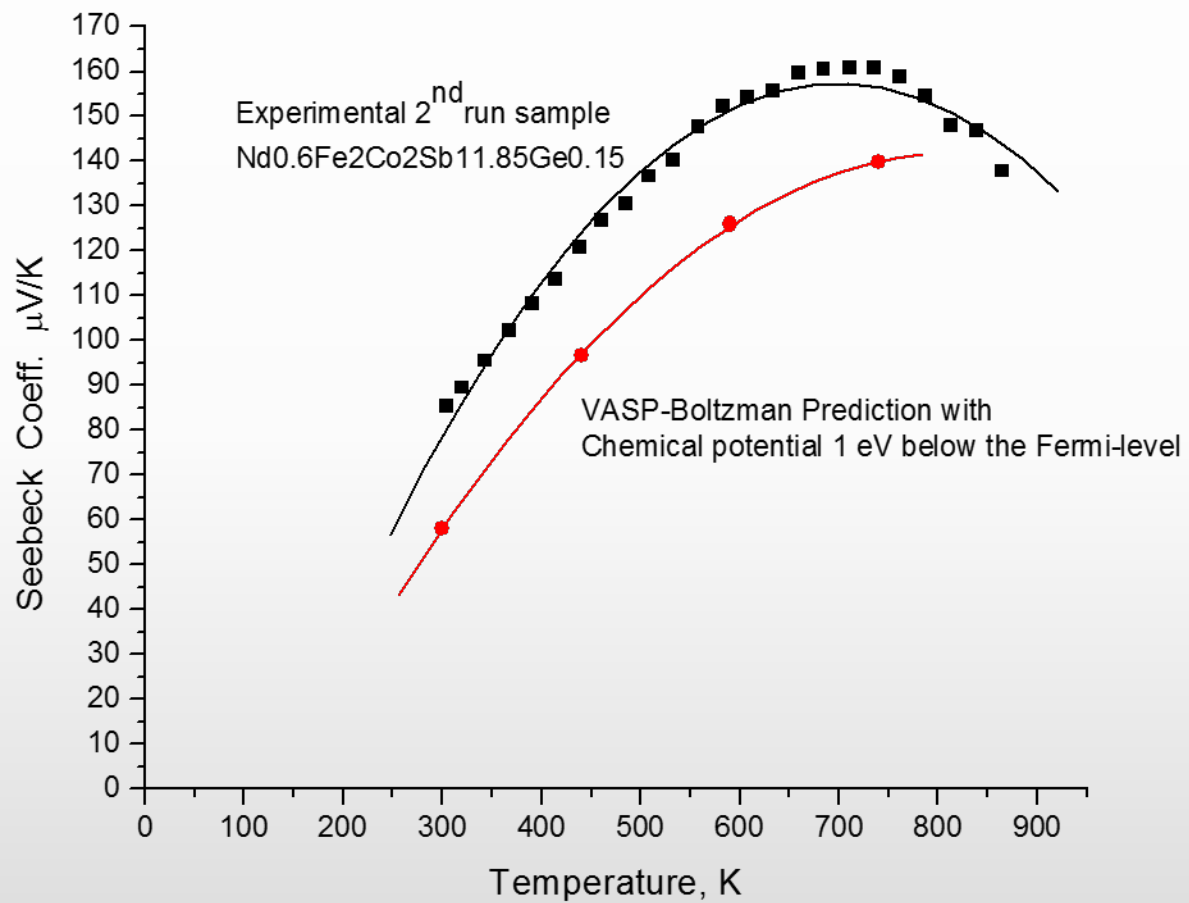


Complex Skutterudites Thermoelectric (Mackey, Dynys)
 $\text{Nd}_{0.6}\text{Fe}_2\text{Co}_2\text{Sb}_{11.85}\text{Ge}_{0.15}$

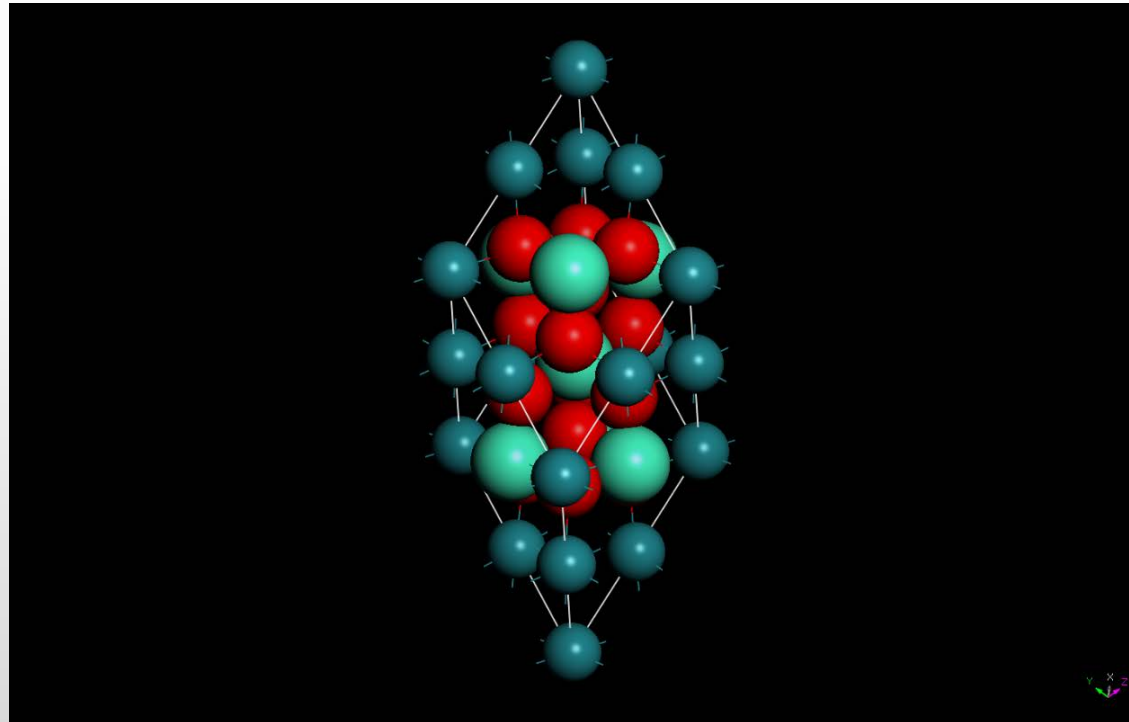


Characteristics for a desirable thermoelectric material

- Seebeck Coefficient $\sim 100\mu\text{V}/\text{K}$
 - Electrical Resistivity $10^{-2} \text{ Ohm}\cdot\text{cm}$
 - Thermal Conductivity $\sim 10 \text{ W}/\text{m}\cdot\text{K}$
 - Electronic Band Gap -must be greater than zero
 - High Temperature Capability
- 



Complex Oxide – based Pyrochlores
mixed cation at B-site $A_2 (B^{3+}, B^{5+}) O_7$
 Gd_2RuTaO_7



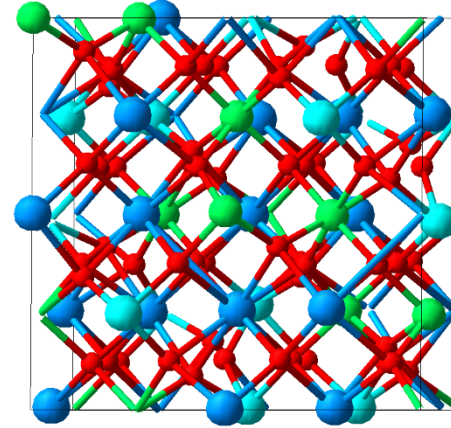
Calculated Cell Parameters

Parameter	Original	change	Final	%
a	10.091900	0.158505	10.250405	1.6
b	10.091900	0.137867	10.229767	1.4
c	10.091900	0.156757	10.248657	1.6
alpha	90.000000	-0.361354	89.638646	-0.4
beta	90.000000	0.392175	90.392175	0.4
gamma	90.000000	0.047839	90.047839	0.1
Volume	1027.824144	46.795542	1074.619686	4.6

Density: 8.759 Mg/m³

Elastic constant matrix (GPa):

	1	2	3	4	5	6
1	303.99	122.74	112.40	0.00	0.00	0.00
2	122.74	342.62	128.66	0.00	0.00	0.00
3	112.40	128.66	289.89	0.00	0.00	0.00
4	0.00	0.00	0.00	98.03	0.00	0.00
5	0.00	0.00	0.00	0.00	76.22	0.00
6	0.00	0.00	0.00	0.00	0.00	88.62



Modulus	Voigt	Reuss	Hill
Bulk	184.90	183.56	184.23 GPa
Shear	90.75	89.78	90.27
Young's	233.98	231.59	232.78
Longitudinal			304.59

Velocity of sound

Calculated from Hill moduli:

transverse waves:	3271 m/s
longitudinal waves:	6009 m/s
mean:	3649 m/s

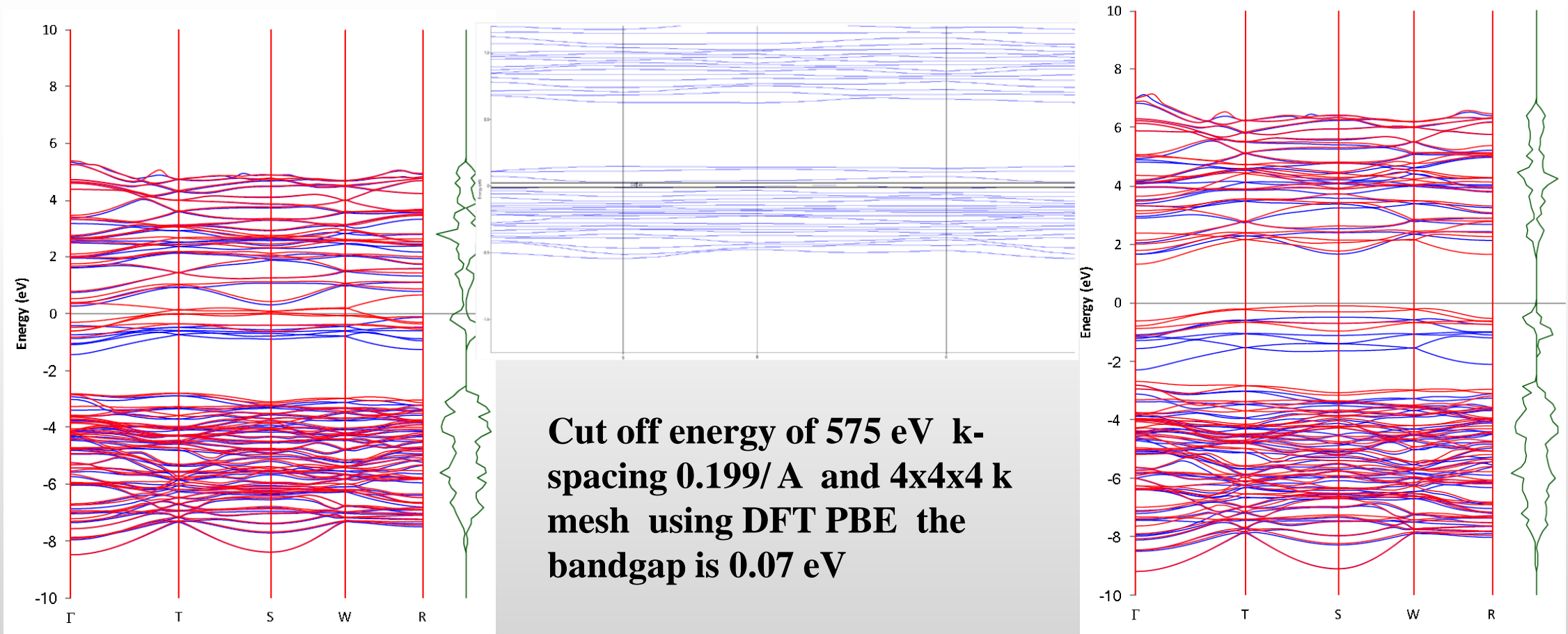
Debye temperature: 465.9 K

the thermal coefficient of linear expansion at 600K = 7.60×10^{-6}

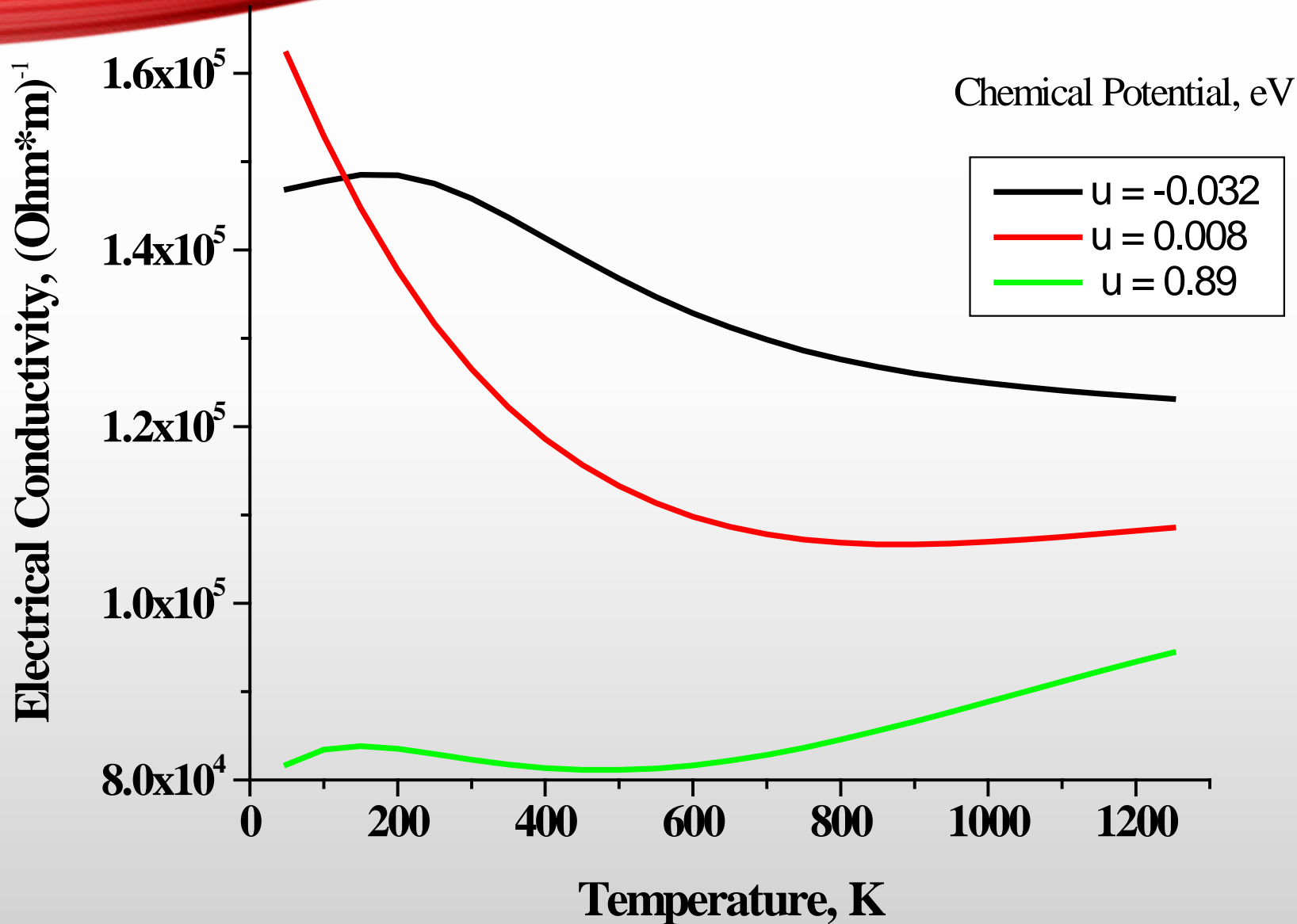
Calculated Electronic Band Structure

Perdew – Ernzerhof – Burke (PBE)

Heyd –Scuseria -Ernzerhof (HSE06)



Electrical Conductivity

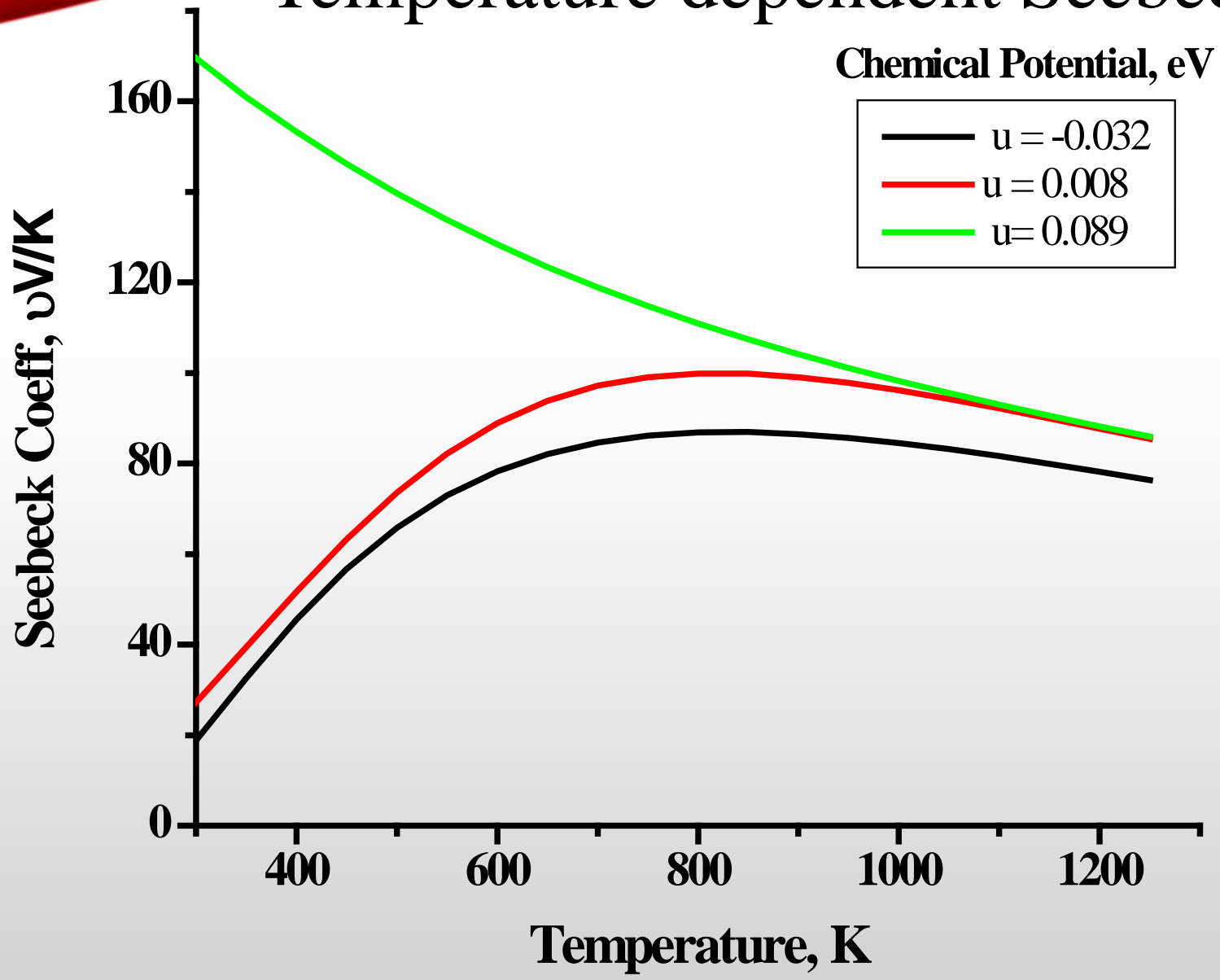


BoltzTraP. A code for calculating band-structure dependent quantities ☆

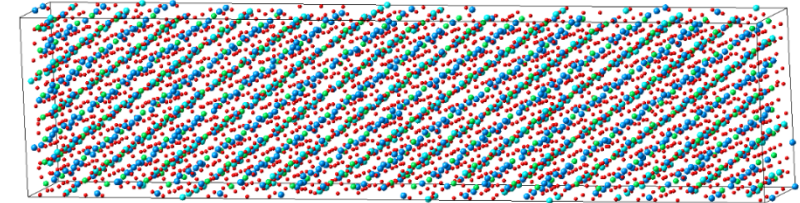
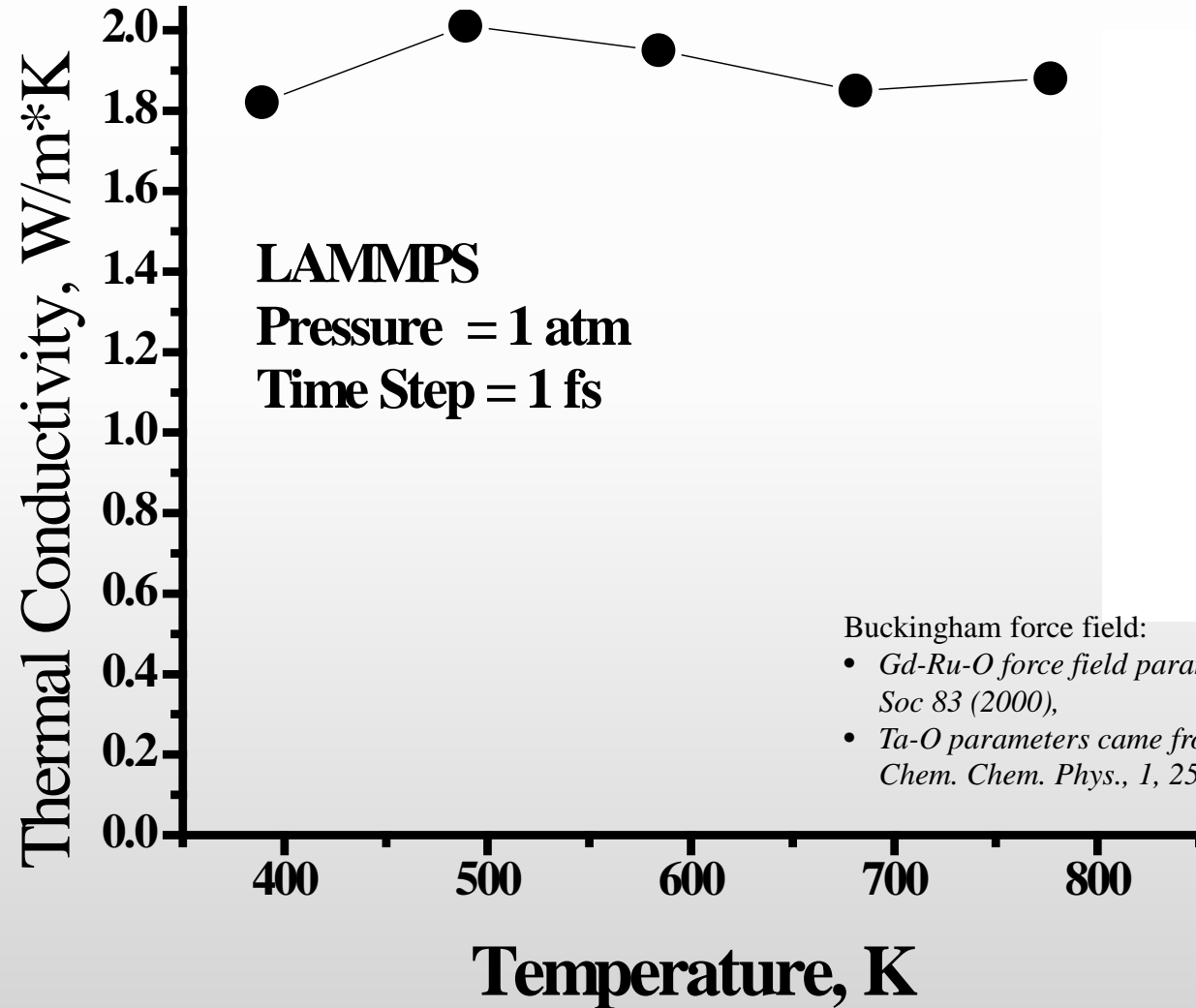
Georg K.H. Madsen ^{a,*}, David J. Singh ^b

Computer Physics Communications 175
(2006) 67–71

Temperature dependent Seebeck coefficient

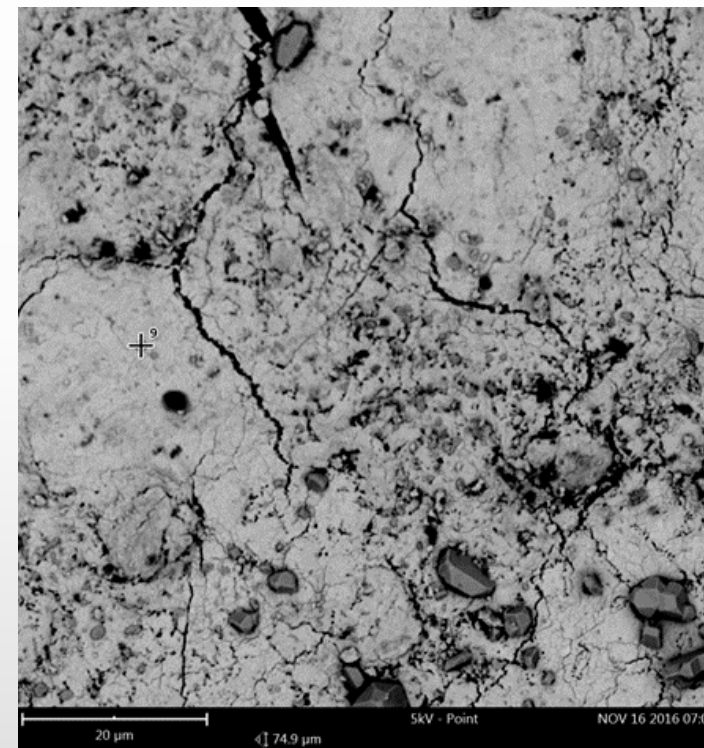
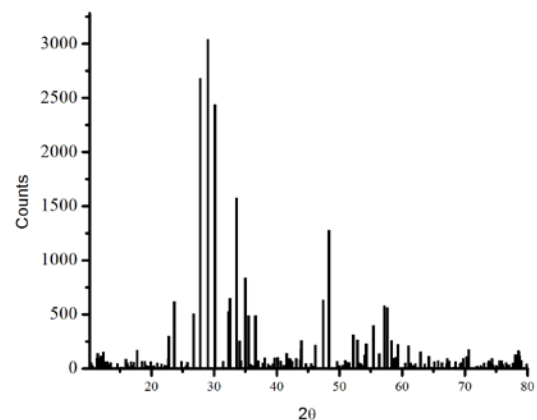
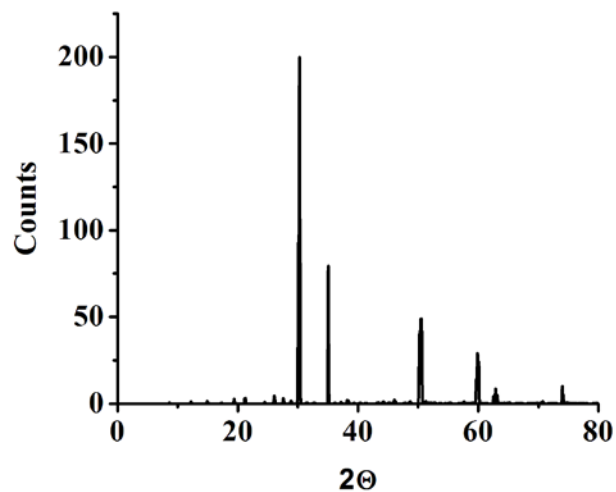
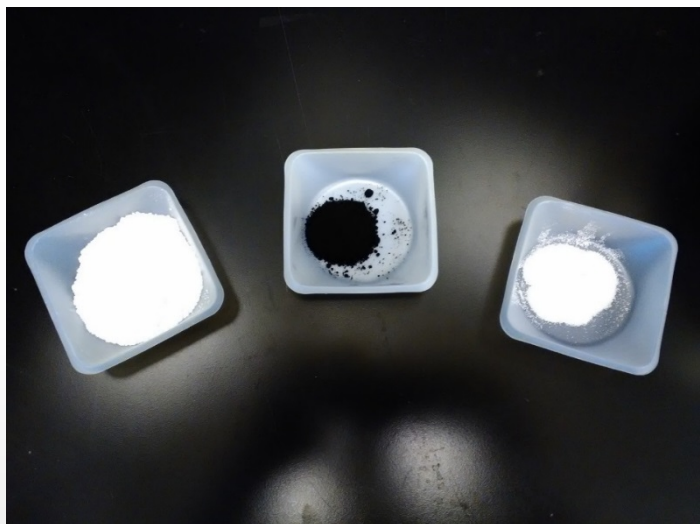


Molecular Dynamic Computational Results: Large-scale Atomic/Molecular Massively Parallel Simulator (LAMMPS)



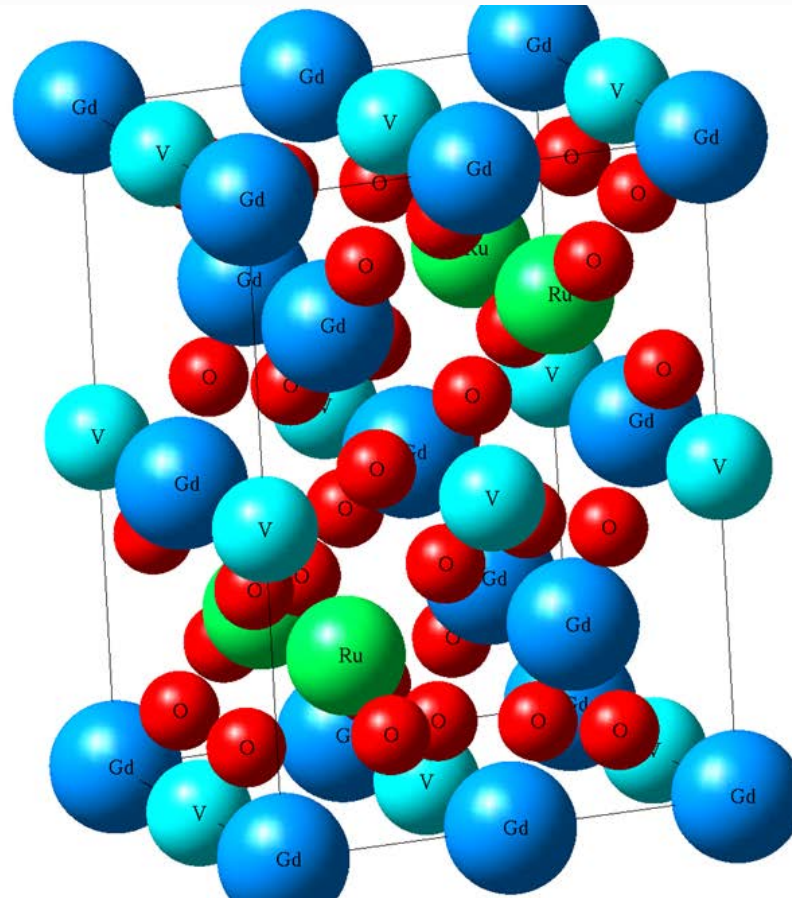
Buckingham force field:

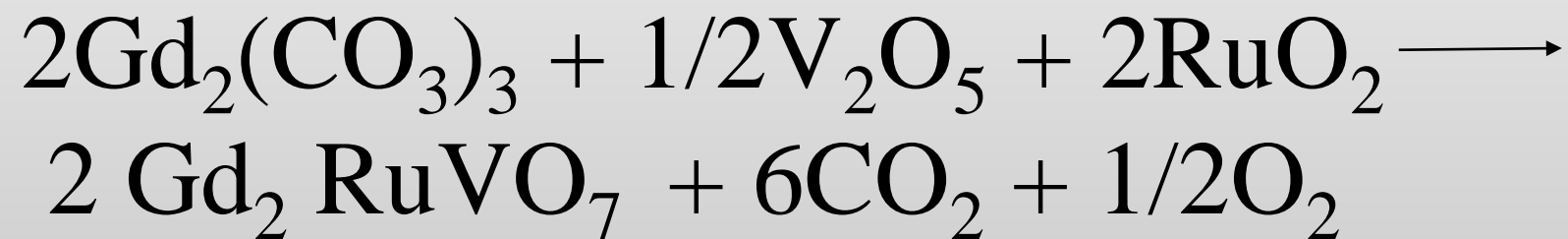
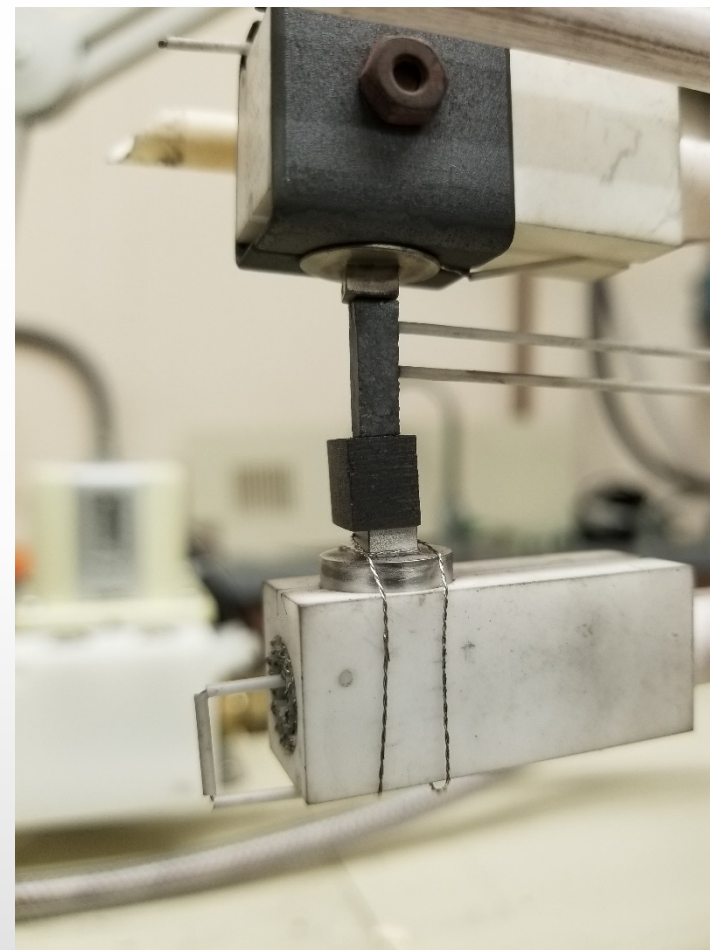
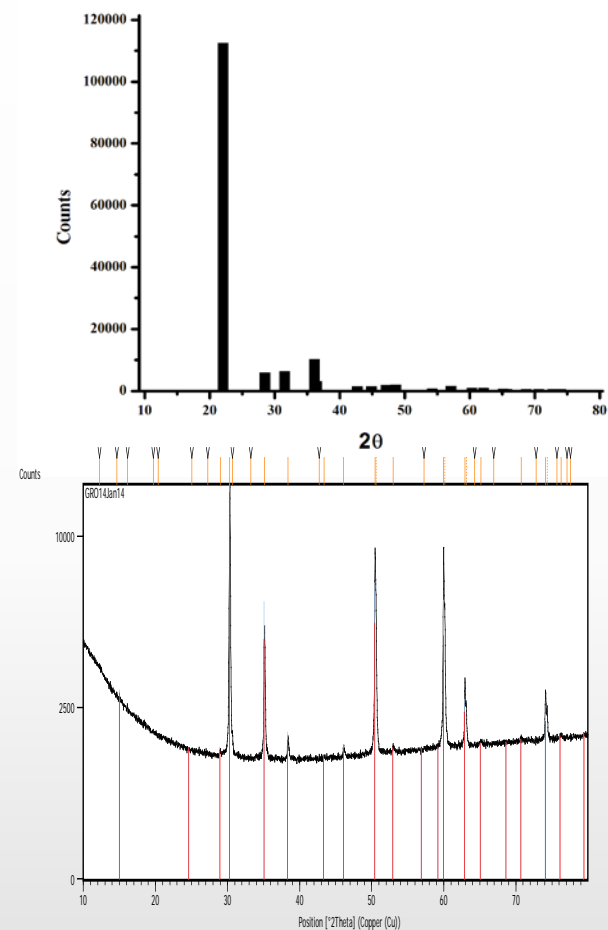
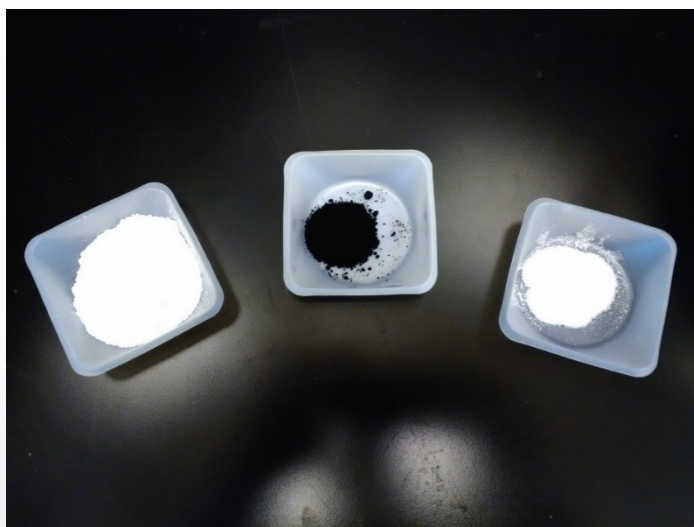
- *Gd-Ru-O force field parameters came from Minervini, RW Grimes, KE Sickafus J Am Ceram Soc 83 (2000),*
- *Ta-O parameters came from S.M.Woodley, P.D.Battle, J.D.Gale and C.R.A.Catlow Phys. Chem. Chem. Phys., 1, 2535-2542 (1999).*



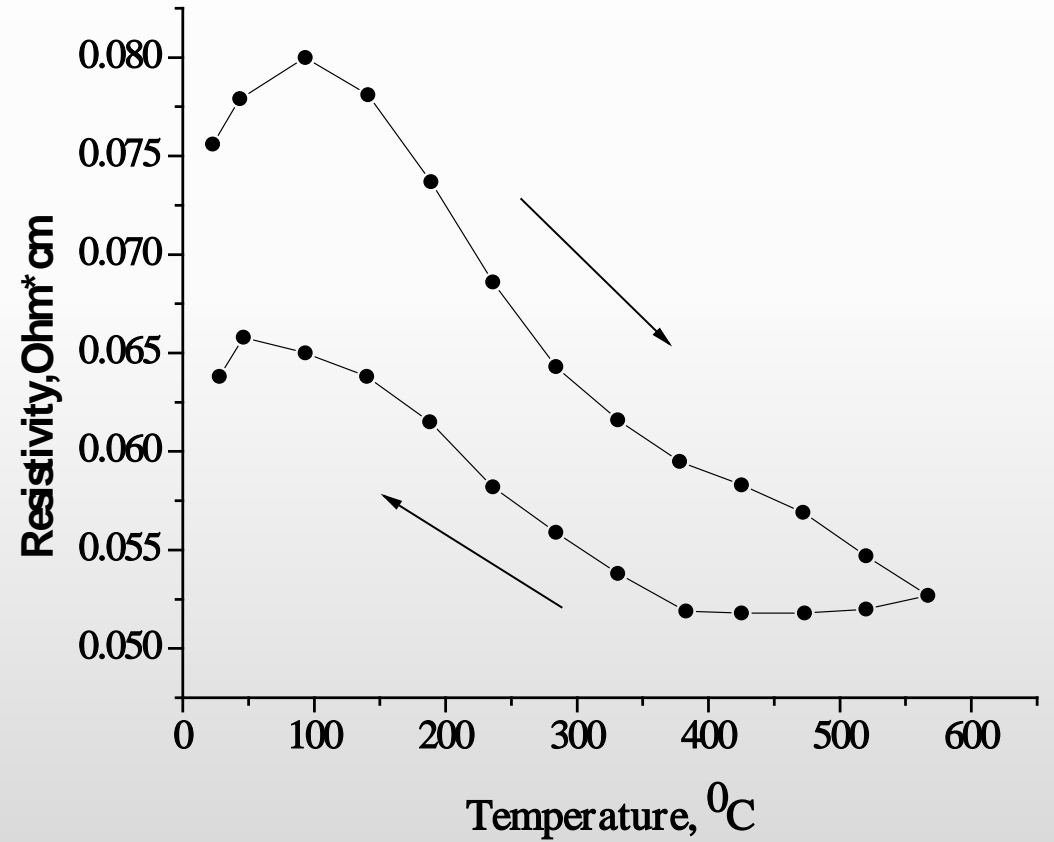
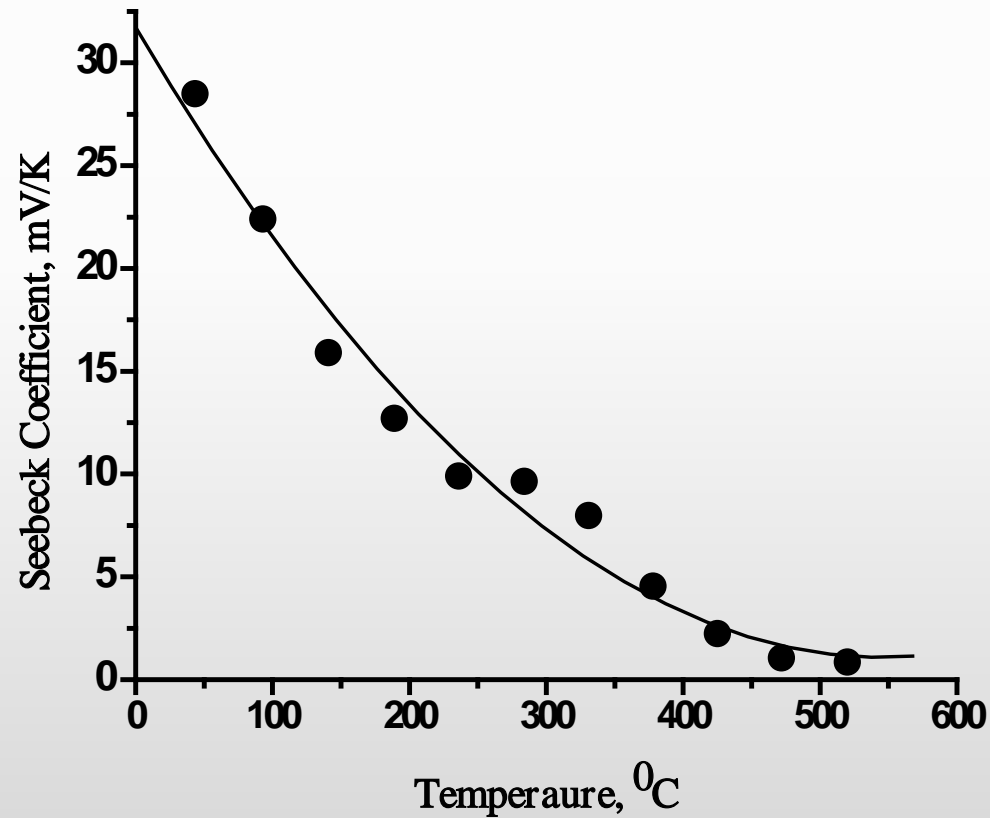
Solid state reaction, mechanical mixing, sintering in air, hot pressing

Complex Oxide – based Pyrochlores
mixed cation at B-site $A_2 (B^{3+}, B^{5+}) O_7$
 Gd_2RuVO_7





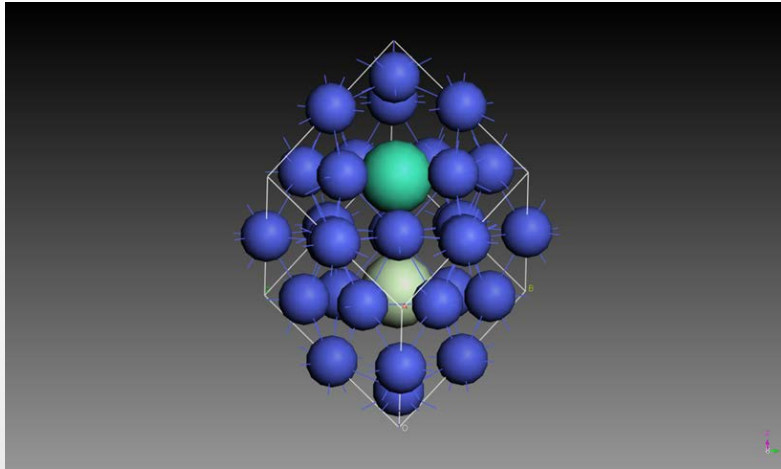
Experimental Seebeck coefficient and Resistivity data for $Gd_2 RuVO_7$

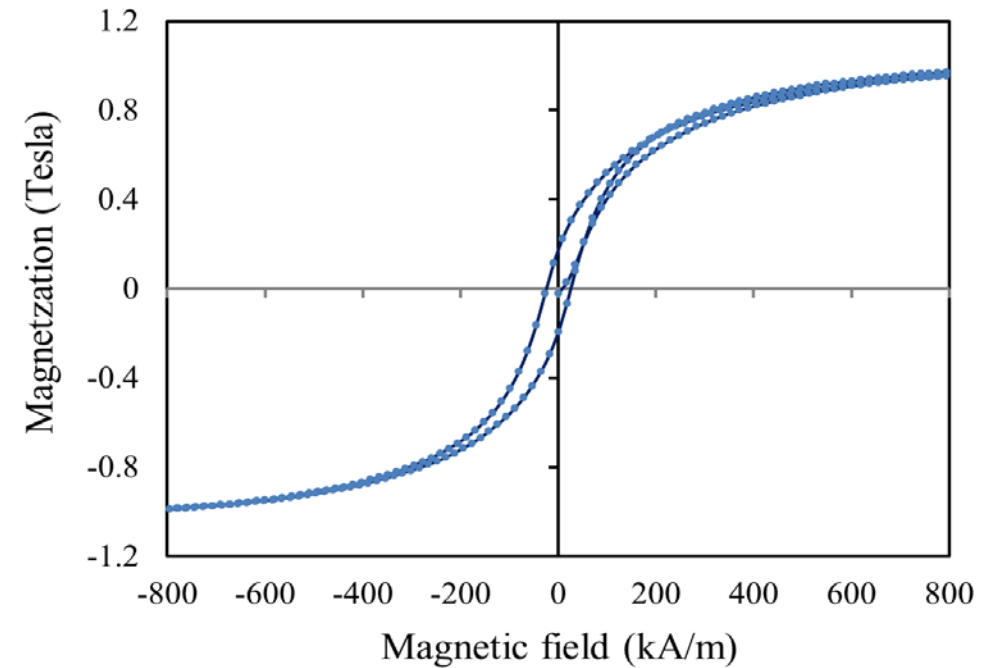
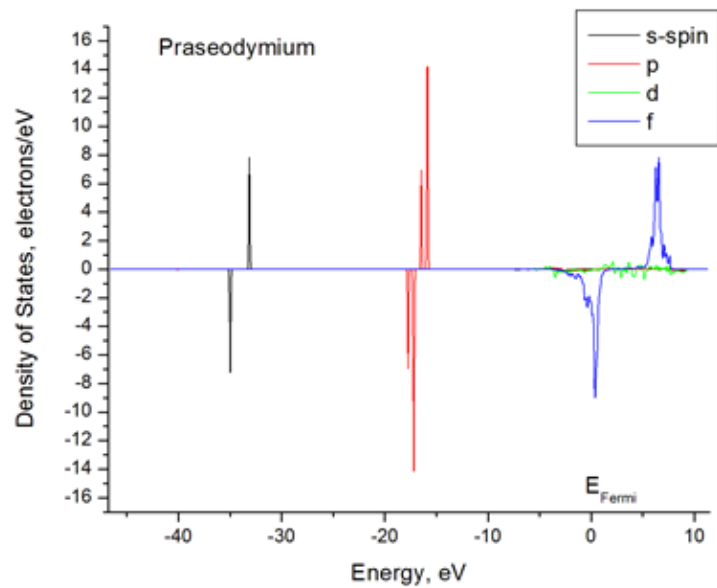




Magnetic material

First-Principle and Experimental Study of a Gadolinium Praseodymium Cobalt Pseudo-binary Intermetallic Compound





Parameter	Ferromagnetic	Paramagnetic	Antiferromagnetic	Ferrimagnetic
2*Integrated Spin Density	nonzero, the same magnitude	zero	zero	non-zero
2*Integrated Spin Density	nonzero, the same magnitude	zero	non-zero	non-zero larger magnitude

GdPrCo17	Density (g/cm³)	Lattice Parameter (Angstrom)	Magnetization (Amperes*meter² per kg)
CASTEP	8.37	a=b=8.46, c=12.47	158
VASP	8.82	a=b=8.35, c=12.17	110
Experiment	8.46	a=b=8.41, c=12.23	93

CONCLUSIONS

- Computational methods parameters can be used for predictions and to aid in the development of ceramic materials.
- Some descriptions (band structure) are very sensitive to such things as mesh density.
- Ceramics such oxide pyrochlores have potential as thermoelectric materials.
- Nature is always right!