



HabEx Error Budget Definition and STOP Modeling

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Executive Summary

HabEx Baseline Architecture-A Optical Telescope Design Closes

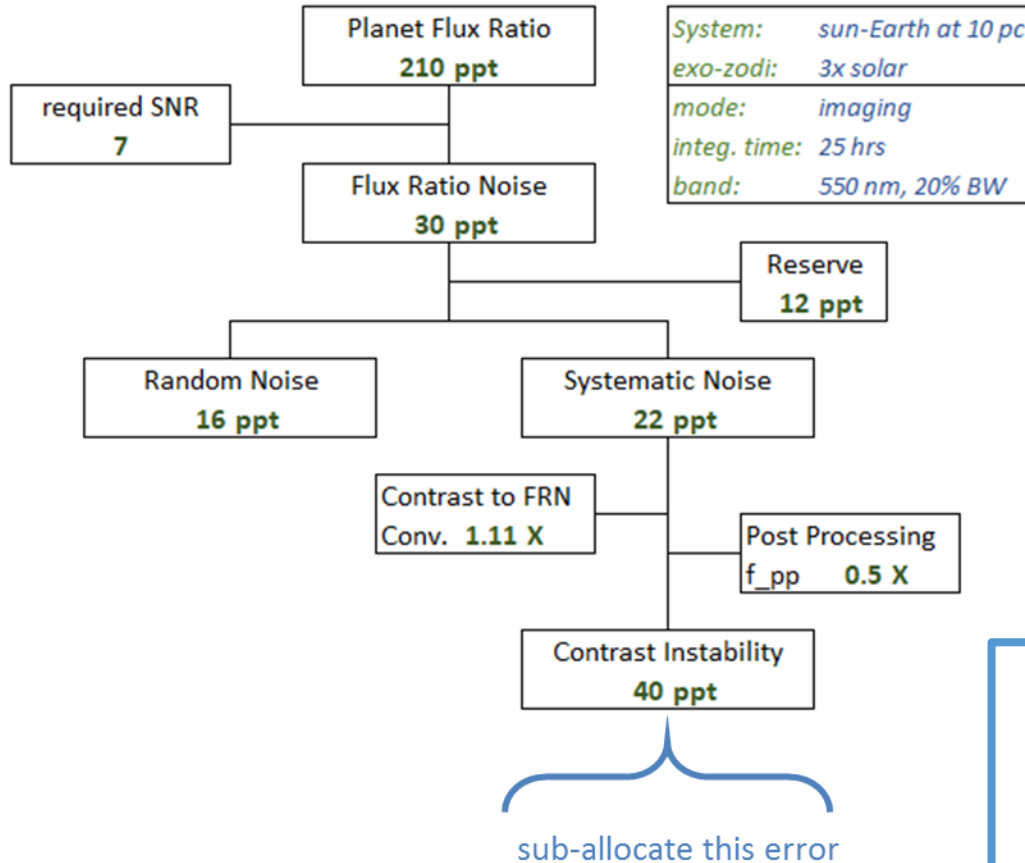
The HabEx Optical Telescope Assembly (OTA) design team is using Science Driven Systems Engineering.

Because HabEx Science Performance depends on the spatial frequency content of the Wavefront Error Stability, a Zernike Polynomial Error Budget has been established and is used to define OTA engineering specification.



WFE Stability Error Budget

Starting with allowable Starlight Leakage through Coronagraph, derive tolerances for 48 (X,Y) Zernikes or 27 (R,θ) Zernikes.



allocation tolerance

$$\epsilon_i = \left(\frac{\partial \epsilon}{\partial x_i} \right) \cdot \delta x_i$$

sensitivity



WFE Stability Error Budget

Derive Tolerance for Zernike polynomials

- Sensitivities per Zernike are Fixed by Coronagraph
- Allocation Adjusted to ‘balance’ errors

$$\epsilon_i = \left(\frac{\partial \epsilon}{\partial x_i} \right) \cdot \delta x_i$$

allocation tolerance
sensitivity

| Order | | | VVC-4 Sensitivity | 40 ppt Allocation | VVC-4 Tolerance | PV to RMS | VVC-4 Tolerance |
|-----------|----|---|-------------------|-------------------|-----------------|-----------|-----------------|
| K | N | M | [ppt/pm] | [ppt] | [pm PV] | | [pm rms] |
| TOTAL RMS | | | | 40.02 | 3062.6 | | 1628.4 |
| 1 | 1 | 1 | 1.96E-04 | 0.47 | 2385.6 | 2.00 | 1192.8 |
| 2 | 2 | 0 | 2.44E-04 | 0.47 | 1920.1 | 1.73 | 1108.6 |
| 3 | 2 | 2 | 0.730 | 6.84 | 9.4 | 2.45 | 3.8 |
| 4 | 3 | 1 | 0.789 | 7.38 | 9.4 | 2.83 | 3.3 |
| 5 | 3 | 3 | 0.539 | 5.04 | 9.4 | 2.83 | 3.3 |
| 6 | 4 | 0 | 1.291 | 8.89 | 6.9 | 2.24 | 3.1 |
| 7 | 4 | 2 | 0.506 | 4.94 | 9.7 | 3.16 | 3.1 |
| 8 | 4 | 4 | 0.527 | 4.94 | 9.4 | 3.16 | 3.0 |
| 9 | 5 | 1 | 0.774 | 7.25 | 9.4 | 3.46 | 2.7 |
| 10 | 5 | 3 | 0.547 | 5.12 | 9.4 | 3.46 | 2.7 |
| 11 | 5 | 5 | 0.680 | 6.37 | 9.4 | 3.46 | 2.7 |
| 12 | 6 | 0 | 1.244 | 8.89 | 7.1 | 2.65 | 2.7 |
| 13 | 6 | 2 | 1.151 | 8.89 | 7.7 | 3.74 | 2.1 |
| 14 | 6 | 4 | 0.863 | 8.10 | 9.4 | 3.74 | 2.5 |
| 15 | 6 | 6 | 0.795 | 7.44 | 9.4 | 3.74 | 2.5 |
| 16 | 7 | 1 | 1.577 | 8.89 | 5.6 | 4.00 | 1.4 |
| 17 | 7 | 3 | 1.353 | 8.89 | 6.6 | 4.00 | 1.6 |
| 18 | 7 | 5 | 1.393 | 8.89 | 6.4 | 4.00 | 1.6 |
| 19 | 7 | 7 | 1.246 | 8.89 | 7.1 | 4.00 | 1.8 |
| 20 | 8 | 0 | 4.338 | 8.89 | 2.0 | 3.00 | 0.7 |
| 21 | 8 | 2 | 2.078 | 8.89 | 4.3 | 4.24 | 1.0 |
| 22 | 8 | 4 | 1.723 | 8.89 | 5.2 | 4.24 | 1.2 |
| 23 | 8 | 6 | 1.461 | 8.89 | 6.1 | 4.24 | 1.4 |
| 24 | 8 | 8 | 1.533 | 8.89 | 5.8 | 4.24 | 1.4 |
| 25 | 9 | 1 | 2.182 | 8.89 | 4.1 | 4.47 | 0.9 |
| 26 | 10 | 0 | 2.344 | 8.89 | 3.8 | 3.32 | 1.1 |
| 27 | 12 | 0 | 1.263 | 8.89 | 7.0 | 3.61 | 2.0 |



VVC-4 is insensitive to Tip/Tilt and Power



Sub-Allocation of Error Budget

Each Zernike term is sub-allocated to LOS, Inertial & Thermal

| | | | RSS Allocation | 100% | 50% | 70% | 50% | 10% |
|-------|----|---|-----------------|----------|----------|----------|----------|----------|
| Order | | | VVC-4 Tolerance | LOS | Inertial | Thermal | Reserve | |
| K | N | M | Aberration | [pm rms] | [pm rms] | [pm rms] | [pm rms] | [pm rms] |
| | | | TOTAL RMS | 1628.4 | 814 | 1140 | 814 | 163 |
| 1 | 1 | 1 | Tilt | 1192.8 | 596.40 | 834.95 | 596.40 | 119.28 |
| 2 | 2 | 0 | Power (Defocus) | 1108.6 | 554.29 | 776.00 | 554.29 | 110.86 |
| 3 | 2 | 2 | Pri Astigmatism | 3.8 | 1.91 | 2.67 | 1.91 | 0.38 |
| 4 | 3 | 1 | Pri Coma | 3.3 | 1.65 | 2.32 | 1.65 | 0.33 |
| 5 | 3 | 3 | Pri Trefoil | 3.3 | 1.65 | 2.32 | 1.65 | 0.33 |
| 6 | 4 | 0 | Pri Spherical | 3.1 | 1.54 | 2.16 | 1.54 | 0.31 |
| 7 | 4 | 2 | Sec Astigmatism | 3.1 | 1.54 | 2.16 | 1.54 | 0.31 |
| 8 | 4 | 4 | Pri Tetrafoil | 3.0 | 1.48 | 2.07 | 1.48 | 0.30 |
| 9 | 5 | 1 | Sec Coma | 2.7 | 1.35 | 1.89 | 1.35 | 0.27 |
| 10 | 5 | 3 | Sec Trefoil | 2.7 | 1.35 | 1.89 | 1.35 | 0.27 |
| 11 | 5 | 5 | Pri Pentafoil | 2.7 | 1.35 | 1.89 | 1.35 | 0.27 |
| 12 | 6 | 0 | Sec Spherical | 2.7 | 1.35 | 1.89 | 1.35 | 0.27 |
| 13 | 6 | 2 | Ter Astigmatism | 2.1 | 1.03 | 1.45 | 1.03 | 0.21 |
| 14 | 6 | 4 | Sec Tetrafoil | 2.5 | 1.25 | 1.76 | 1.25 | 0.25 |
| 15 | 6 | 6 | Pri Hexafoil | 2.5 | 1.25 | 1.75 | 1.25 | 0.25 |
| 16 | 7 | 1 | Ter Coma | 1.4 | 0.70 | 0.99 | 0.70 | 0.14 |
| 17 | 7 | 3 | Ter Trefoil | 1.6 | 0.82 | 1.15 | 0.82 | 0.16 |
| 18 | 7 | 5 | Sec Pentafoil | 1.6 | 0.80 | 1.12 | 0.80 | 0.16 |
| 19 | 7 | 7 | Pri Septafoil | 1.8 | 0.89 | 1.25 | 0.89 | 0.18 |
| 20 | 8 | 0 | Ter Spherical | 0.7 | 0.34 | 0.48 | 0.34 | 0.07 |
| 21 | 8 | 2 | Qua Astigmatism | 1.0 | 0.50 | 0.71 | 0.50 | 0.10 |
| 22 | 8 | 4 | Ter Tetrafoil | 1.2 | 0.61 | 0.85 | 0.61 | 0.12 |
| 23 | 8 | 6 | Sec Hexafoil | 1.4 | 0.72 | 1.00 | 0.72 | 0.14 |
| 24 | 8 | 8 | Pri Octafoil | 1.4 | 0.68 | 0.96 | 0.68 | 0.14 |
| 25 | 9 | 1 | Qua Coma | 0.9 | 0.46 | 0.64 | 0.46 | 0.09 |
| 26 | 10 | 0 | Qua Spherical | 1.1 | 0.57 | 0.80 | 0.57 | 0.11 |
| 27 | 12 | 0 | Qin Spherical | 2.0 | 0.98 | 1.37 | 0.98 | 0.20 |



Line of Sight Tolerance

LOS Jitter causes beam-shear WFE and PSF smear.

LOS Jitter is residual error after active correction. It is assumed that laser-truss or low-order wavefront-sensor (LOWFS) systems can sense and correct LOS drift/vibration at frequencies below 10 Hz.



LOS Stability = Rigid Body Tolerances

System LOS Jitter Specification is < 0.7 mas (56 mas at FSM)

Using Zemax alignment sensitivity analysis, optical component rigid body motion allocation that meets LOS Spec.

| Specification | | | | 56.00 | mas |
|---------------------------|-------|-----------|-------------|--------------|------------|
| ALLOCATION (one sided PV) | | | | | |
| Alignment | ZEMAX | Tolerance | units | RSS | Units |
| PM X-Decenter | DX | 10 | nanometer | 17.20 | mas |
| PM Y-Decenter | DY | 10 | nanometer | 16.70 | mas |
| PM Z-Despace | DZ | 10 | nanometer | 4.30 | mas |
| PM Y-Tilt | TX | 0.5 | nano-radian | 17.32 | mas |
| PM X-Tilt | TY | 0.5 | nano-radian | 17.05 | mas |
| PM Z-Rotation | TZ | 0.5 | nano-radian | 2.15 | mas |
| SM X-Decenter | DX | 20 | nanometer | 30.60 | mas |
| SM Y-Decenter | DY | 20 | nanometer | 29.60 | mas |
| SM Z-Despace | DZ | 20 | nanometer | 8.60 | mas |
| SM Y-Tilt | TX | 1 | nano-radian | 3.05 | mas |
| SM X-Tilt | TY | 1 | nano-radian | 3.00 | mas |
| SM Z-Rotation | TZ | 1 | nano-radian | 0.33 | mas |
| TM X-Decenter | DX | 10 | nanometer | 1.90 | mas |
| TM Y-Decenter | DY | 10 | nanometer | 1.90 | mas |
| TM Z-Despace | DZ | 1000 | nanometer | 0.00 | mas |
| TM Y-Tilt | TX | 10 | nano-radian | 4.17 | mas |
| TM X-Tilt | TY | 10 | nano-radian | 4.17 | mas |
| TM Z-Rotation | TZ | 1000 | nano-radian | 0.74 | mas |
| RSS LOS Error | | | | 56.00 | mas |



WFE Stability LOS Error

Rigid body motion also causes WFE due to wavefront shear.

WFE produced by rigid body motions that meet LOS Jitter Spec do not meet the WFE Stability Tolerance for VVC4.

| Order | | | Aberration | Allocation LOS [pm rms] | MARGIN | LOS |
|-------|----|---|-----------------|----------------------------|----------|---------------------|
| K | N | M | | | | RSS WFE (pm rms) |
| | | | TOTAL RMS | 814 | 5.41 | 150.5078 |
| 1 | 1 | 1 | Tilt | 596.40 | 27.91 | 21.3665 |
| 2 | 2 | 0 | Power (Defocus) | 554.29 | 3.82 | 145.1984 |
| 3 | 2 | 2 | Pri Astigmatism | 1.91 | 0.06 | 32.5080 |
| 4 | 3 | 1 | Pri Coma | 1.65 | 0.22 | 7.5136 |
| 5 | 3 | 3 | Pri Trefoil | 1.65 | 4.72 | 0.3505 |
| 6 | 4 | 0 | Pri Spherical | 1.54 | 4.08 | 0.3775 |
| 7 | 4 | 2 | Sec Astigmatism | 1.54 | 11.37 | 0.1355 |
| 8 | 4 | 4 | Pri Tetrafoil | 1.48 | 365.93 | 0.0040 |
| 9 | 5 | 1 | Sec Coma | 1.35 | 60.79 | 0.0222 |
| 10 | 5 | 3 | Sec Trefoil | 1.35 | 735.26 | 0.0018 |
| 11 | 5 | 5 | Pri Pentafoil | 1.35 | 27556.76 | 0.0000 |
| 12 | 6 | 0 | Sec Spherical | 1.35 | 1359.22 | 0.0010 |
| 13 | 6 | 2 | Ter Astigmatism | 1.03 | 2140.91 | 0.0005 |
| 14 | 6 | 4 | Sec Tetrafoil | 1.25 | 28299.58 | 0.0000 |
| 15 | 6 | 6 | Pri Hexafoil | 1.25 | 88310.79 | 0.0000 |
| 16 | 7 | 1 | Ter Coma | 0.70 | 11880.47 | 0.0001 |
| 17 | 7 | 3 | Ter Trefoil | 0.82 | 23453.55 | 0.0000 |
| 18 | 7 | 5 | Sec Pentafoil | 0.80 | 53809.89 | 0.0000 |
| 19 | 7 | 7 | Pri Septafoil | 0.89 | 52529.41 | 0.0000 |
| 20 | 8 | 0 | Ter Spherical | 0.34 | 28407.55 | 0.0000 |
| 21 | 8 | 2 | Qua Astigmatism | 0.50 | | |
| 22 | 8 | 4 | Ter Tetrafoil | 0.61 | | |
| 23 | 8 | 6 | Sec Hexafoil | 0.72 | | |
| 24 | 8 | 8 | Pri Octafoil | 0.68 | | |
| 25 | 9 | 1 | Qua Coma | 0.46 | | |
| 26 | 10 | 0 | Qua Spherical | 0.57 | | |
| 27 | 12 | 0 | Qin Spherical | 0.98 | | |

But, non-compliance is only Astig & Coma.

LOS Jitter Spec may meet VVC6 Tolerance.

What is actual predicted LOS Performance for Micro-Thrusters?

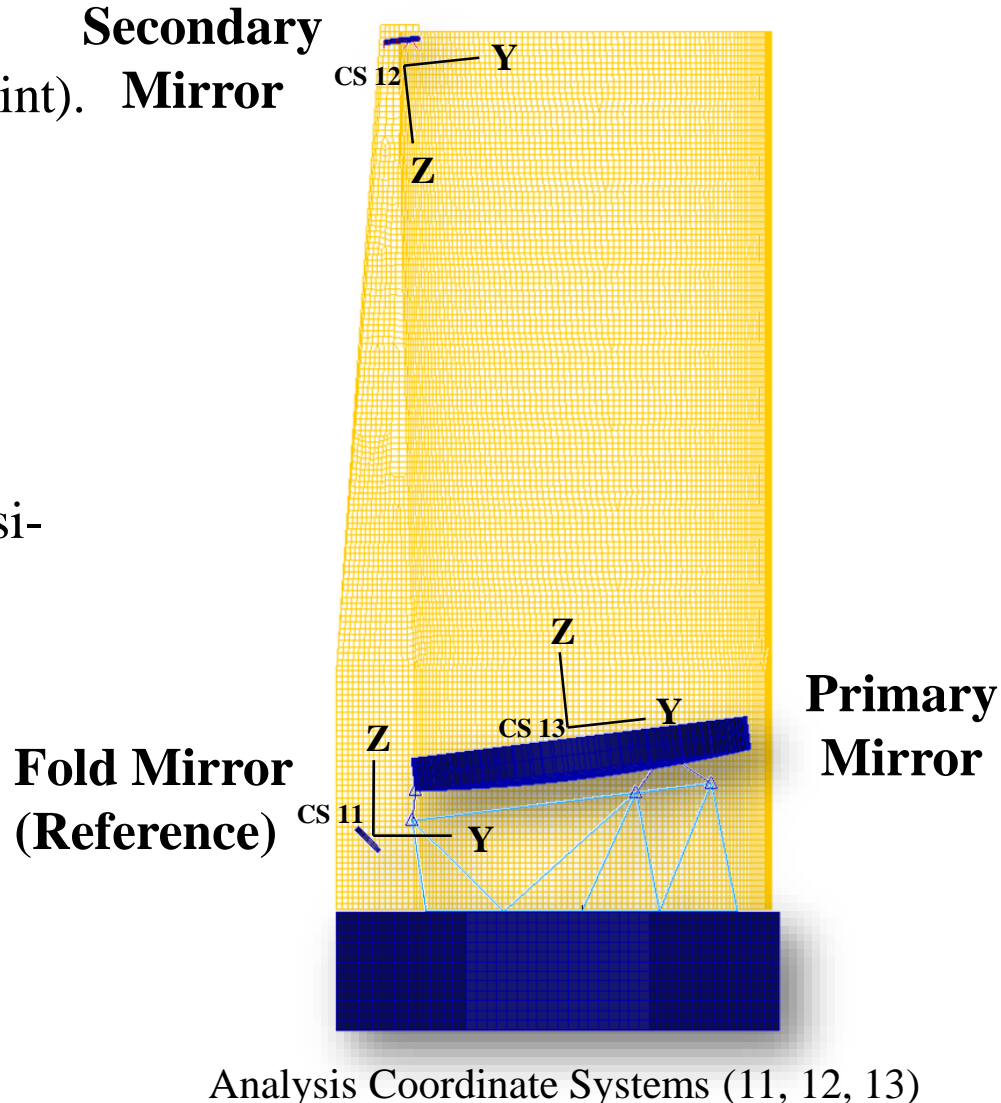


Calculating Predicted PM/SM Rigid Body Motion

- PM, SM motion (relative to Fold Mirror) is calculated using MPC (NASTRAN Multi Point Constraint).
- **Motions are reported in a local optical coordinate system:**
 - PM in CS13,
 - SM in CS12 and
 - **Relative PM/SM in CS11.**
- Material properties based on quasi-isotropic M46J

| Tension | |
|------------------------|----------------|
| 0 degrees, *Et1 | (Msi) 13.55101 |
| 90 degrees, *Et2 | (Msi) 13.55101 |
| Poisson's Ratio, *vt12 | 0.314294 |

M46J Quasi-Isotropic Laminate Properties
(25%0, 50%45, 25%90)
Density = 1.58 gram/cm³ (0.057 lb/in³)





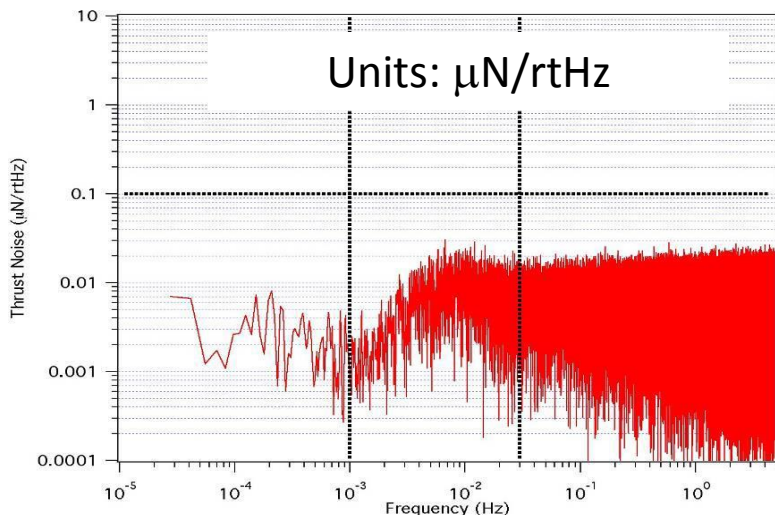
Micro-Thruster Disturbance

Micro-thruster noise excites modes in primary mirror & telescope
Spacecraft has 4 forward thruster pods' and 4 aft pods.

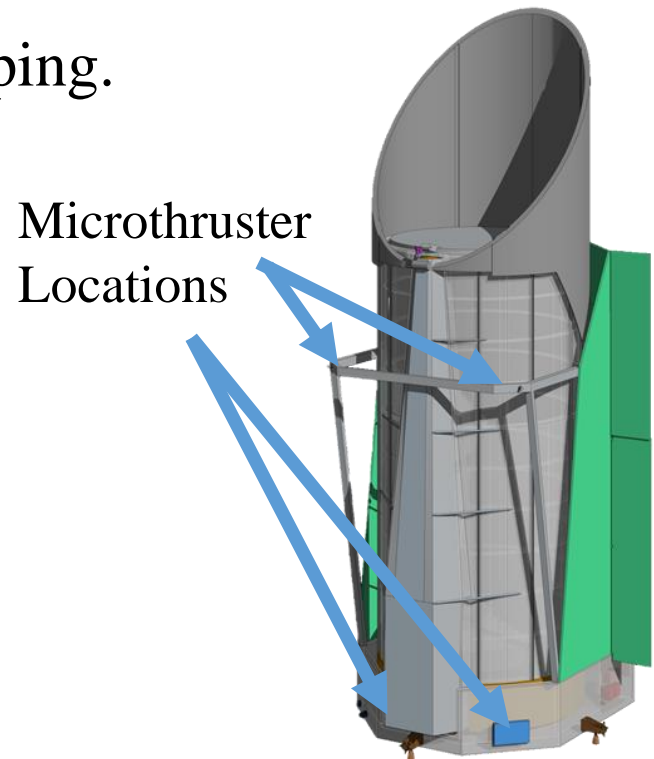
Forward pods have 4 thruster-heads. Aft pods have 8 heads.

Analysis assumes that each head has a flat 0.1 micro-Newton noise spectrum.

Analysis assumes 0.0005% critical damping.



Thruster noise PSD plot for colloidal microthrusters. Max noise above 10^{-3} is likely due to thrust-balance sensor noise limits. (ref: "Colloid Micro-Newton Thrusters For Precision Attitude Control", John Ziemer, et. al, April 2017, CL#17-2067)

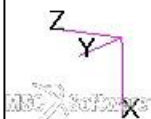
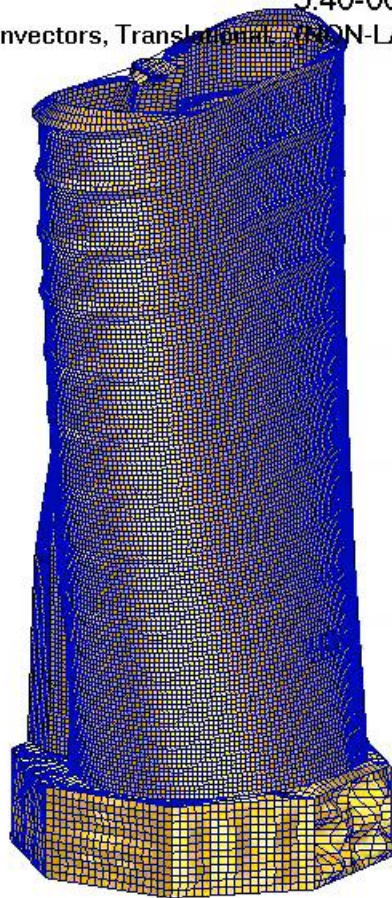


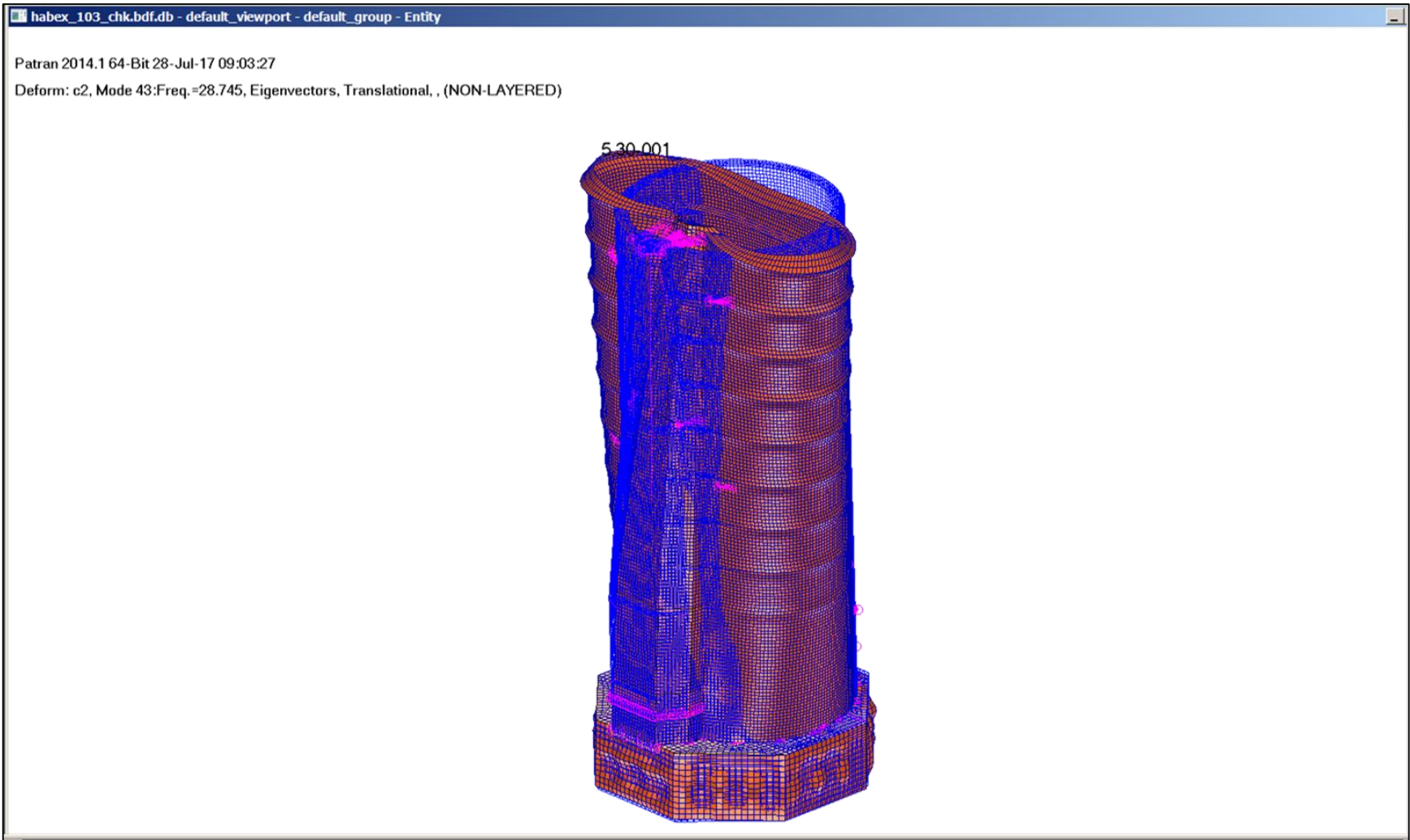


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5.40-001

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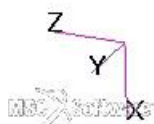
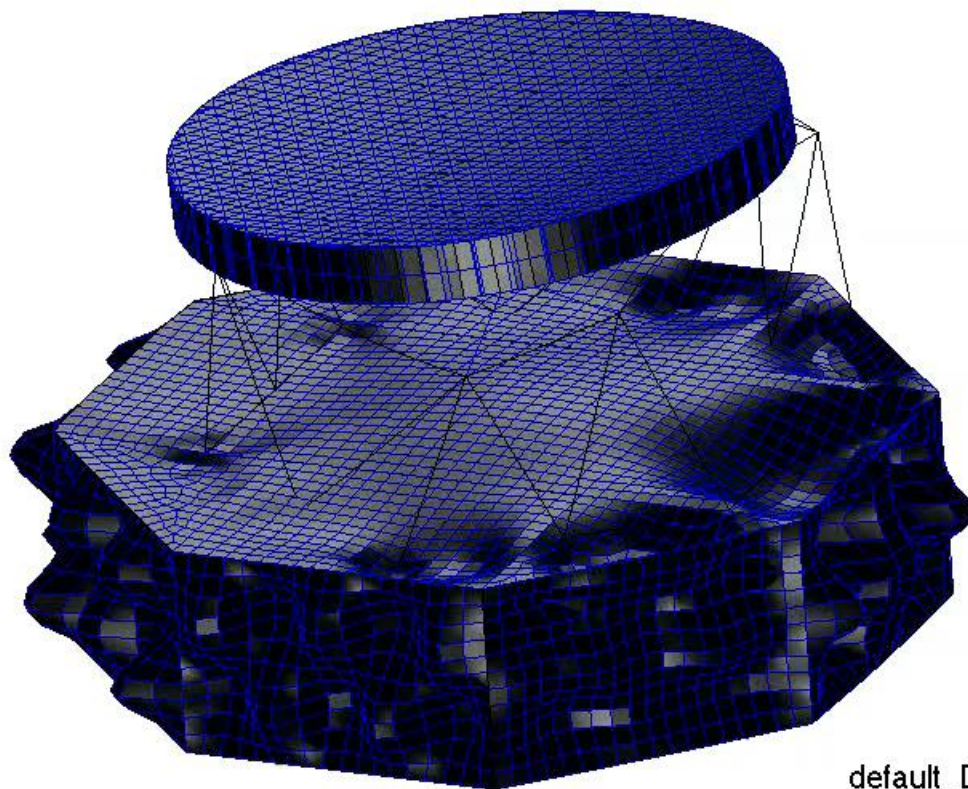


First Tube Mode

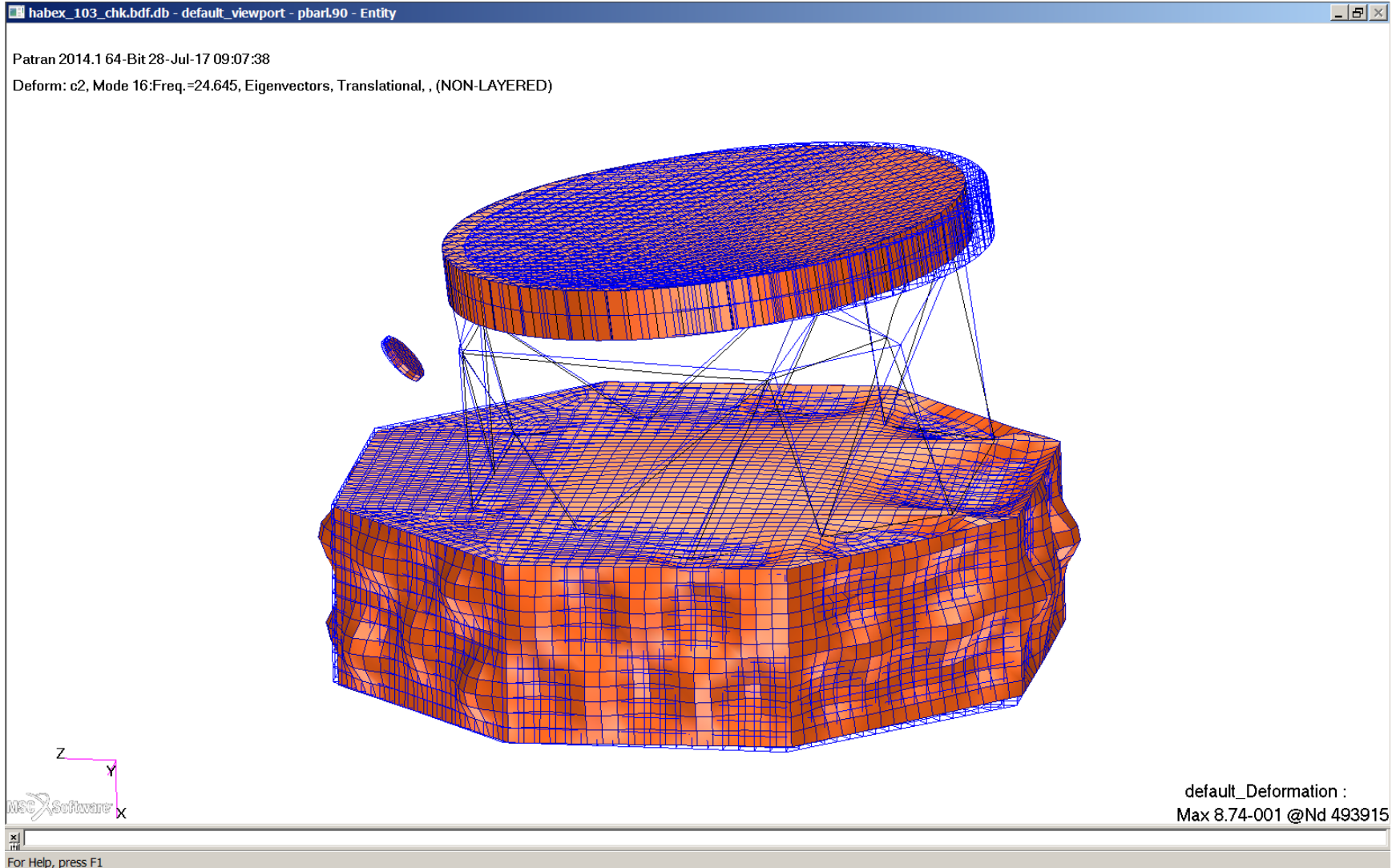


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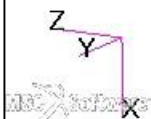
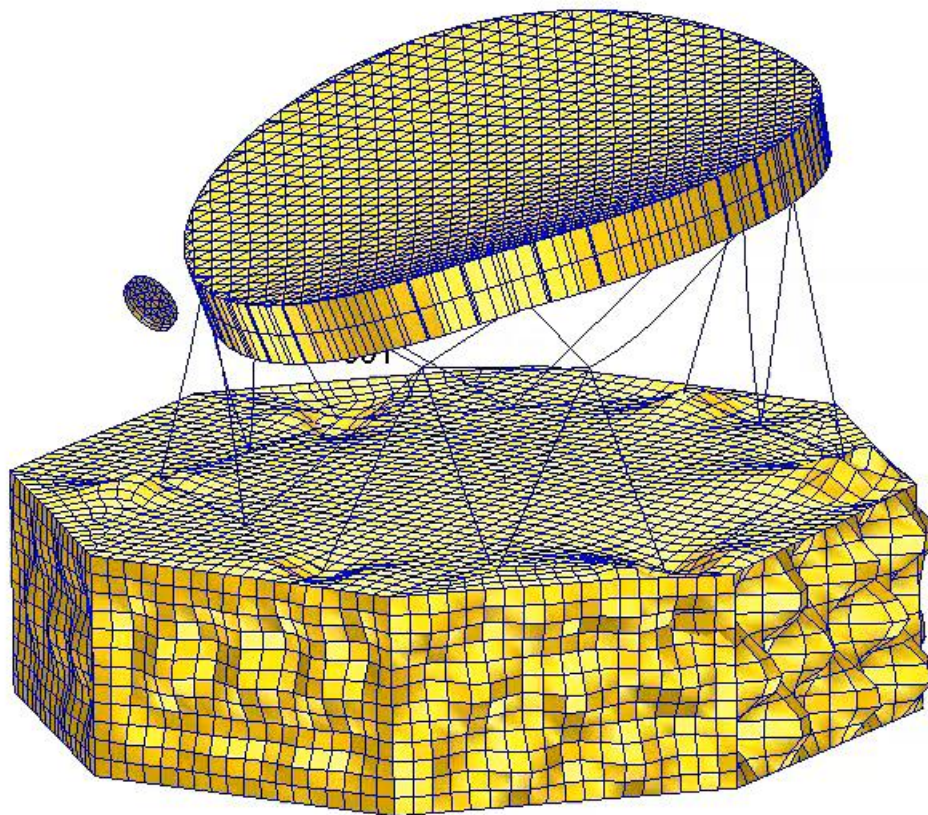


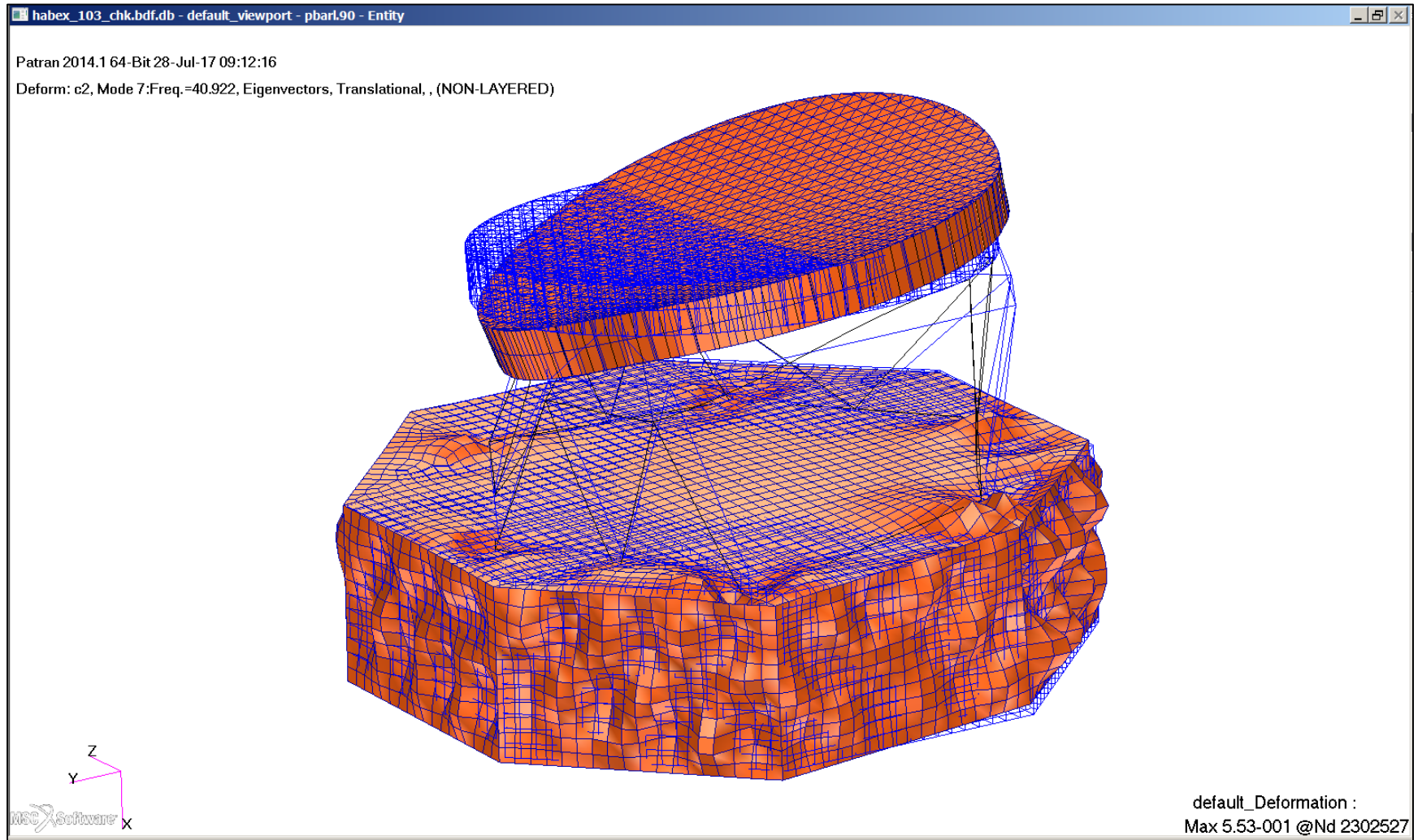
First Mirror Mode



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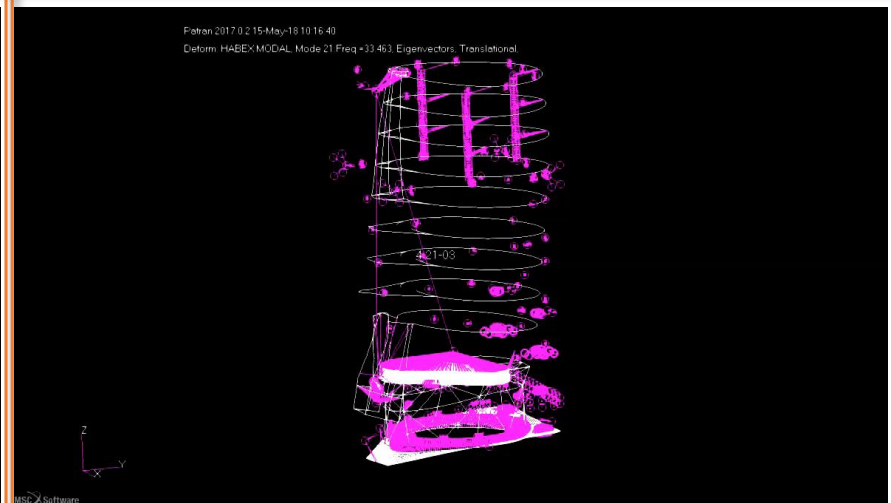
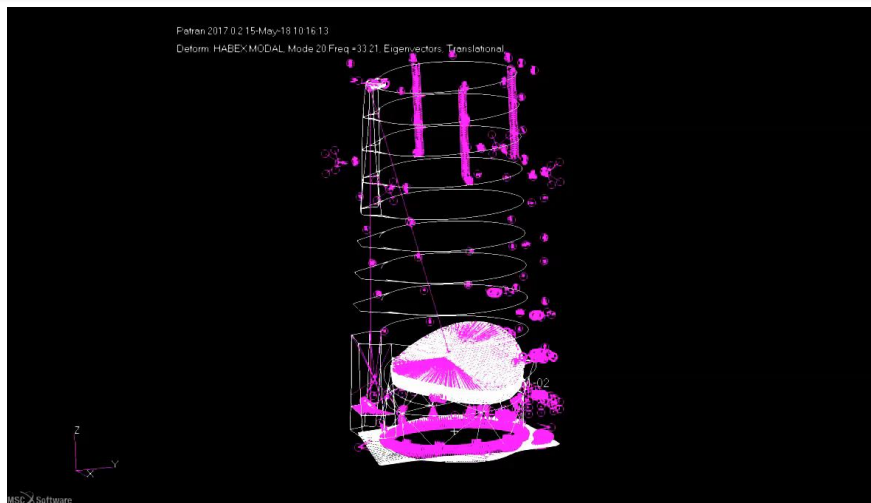
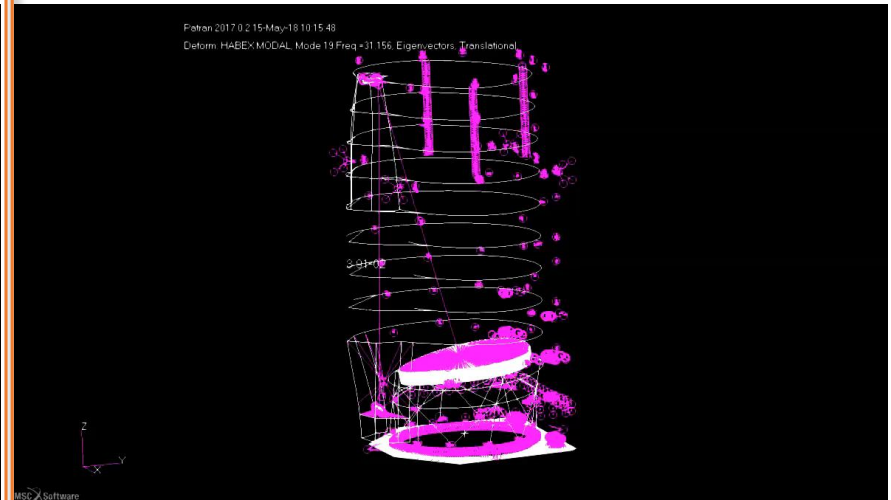
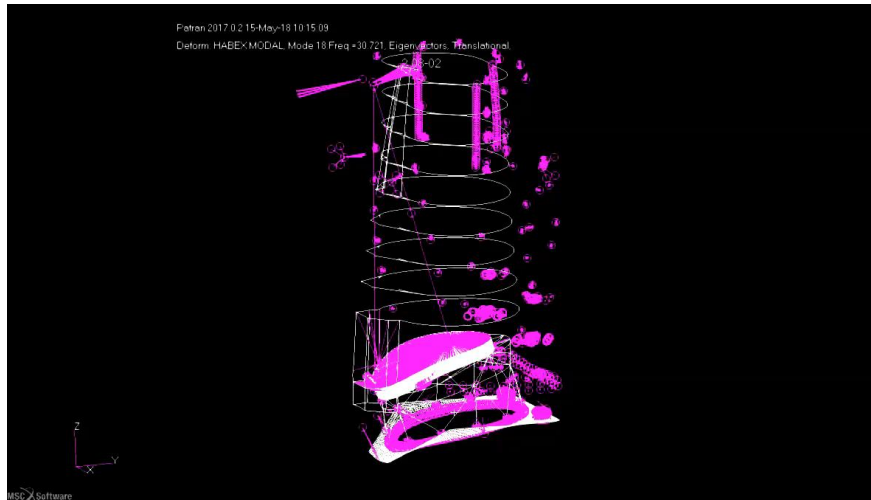




Second Mirror Mode



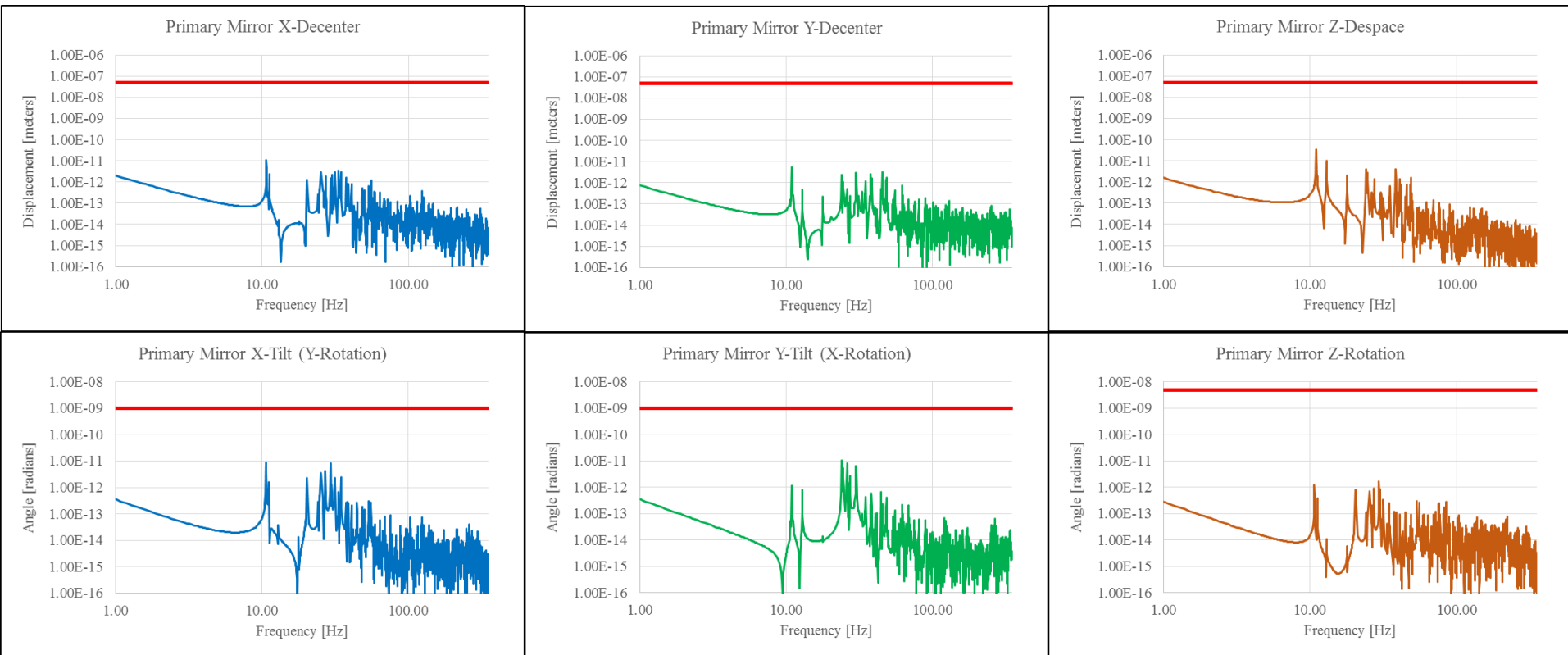
Structure Modes





Predicted Primary Mirror Motion

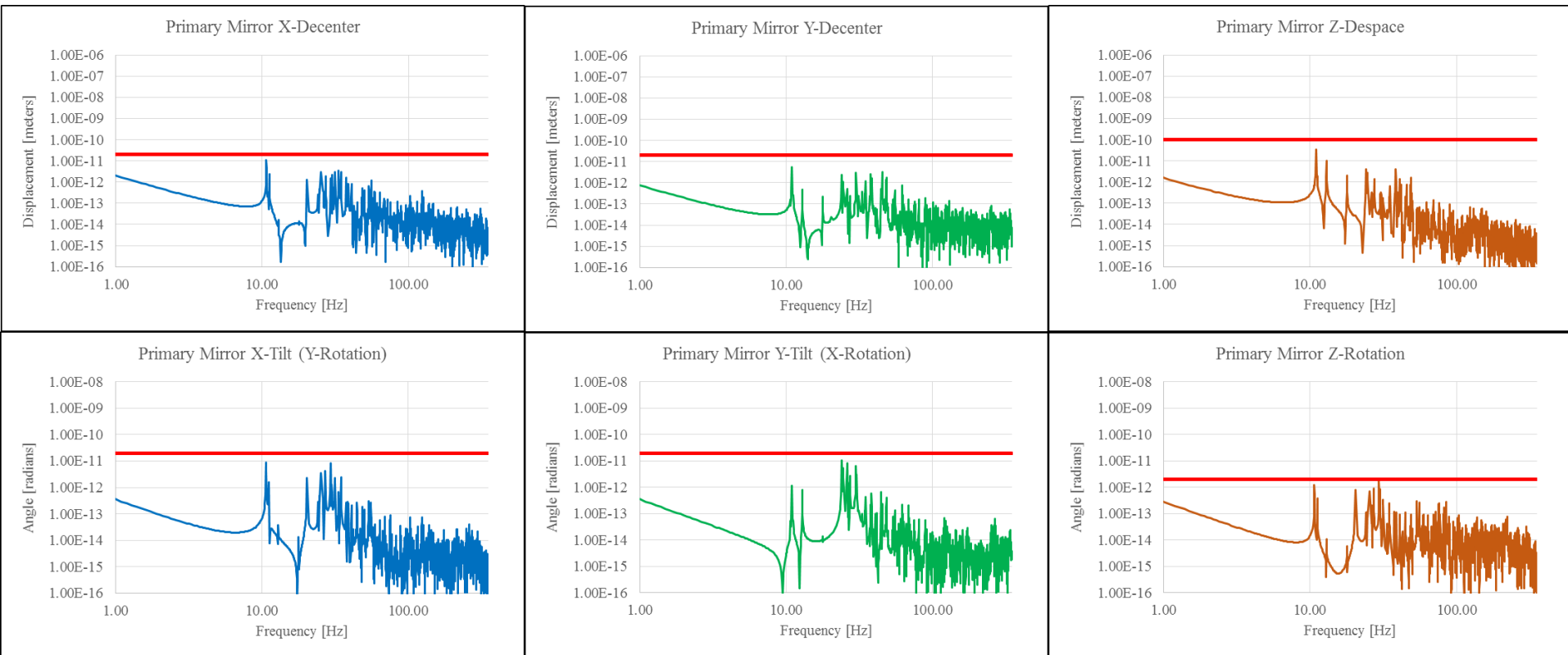
Predicted primary mirror rigid body motion (with 4X MUF) caused by the micro-thruster noise is several orders of magnitude below the tolerance that meets the LOS Jitter Specification.





Predicted Primary Mirror Motion

Thus allowing significantly tighter rigid-body motion tolerances.





New LOS Jitter Prediction

Micro-thruster OTA has predicted on-sky LOS Jitter of 0.018 mas and WFE Stability with 2.5X Astig margin for VVC4.

| LOS RSS Error | | | Specification | 56.00 mas | |
|---------------------------|-------|-----------|---------------|-----------|-------|
| ALLOCATION (one sided PM) | | | | | |
| Alignment | ZEMAX | Tolerance | units | RSS | Units |
| PM X-Decenter | DX | 0.02 | nanometer | 0.03 | mas |
| PM Y-Decenter | DY | 0.02 | nanometer | 0.03 | mas |
| PM Z-Despace | DZ | 0.10 | nanometer | 0.04 | mas |
| PM Y-Tilt | TX | 0.02 | nano-radian | 0.69 | mas |
| PM X-Tilt | TY | 0.02 | nano-radian | 0.68 | mas |
| PM Z-Rotation | TZ | 0.002 | nano-radian | 0.01 | mas |
| SM X-Decenter | DX | 0.50 | nanometer | 0.77 | mas |
| SM Y-Decenter | DY | 0.50 | nanometer | 0.74 | mas |
| SM Z-Despace | DZ | 0.01 | nanometer | 0.00 | mas |
| SM Y-Tilt | TX | 0.02 | nano-radian | 0.06 | mas |
| SM X-Tilt | TY | 0.02 | nano-radian | 0.06 | mas |
| SM Z-Rotation | TZ | 0.20 | nano-radian | 0.07 | mas |
| TM X-Decenter | DX | 0.10 | nanometer | 0.02 | mas |
| TM Y-Decenter | DY | 0.10 | nanometer | 0.02 | mas |
| TM Z-Despace | DZ | 0.10 | nanometer | 0.00 | mas |
| TM Y-Tilt | TX | 0.01 | nano-radian | 0.00 | mas |
| TM X-Tilt | TY | 0.01 | nano-radian | 0.00 | mas |
| TM Z-Rotation | TZ | 0.01 | nano-radian | 0.00 | mas |
| RSS LOS Error | | | | 1.45 | mas |

| Order | | | Allocation LOS | | LOS |
|-------|----|---|-----------------|----------|---------|
| K | N | M | Aberration | [pm rms] | RSS WFE |
| | | | TOTAL RMS | 814 | 1.2703 |
| | | | Tilt | 596.40 | 0.4765 |
| 1 | 1 | 1 | Power (Defocus) | 554.29 | 0.8883 |
| 2 | 2 | 0 | Pri Astigmatism | 1.91 | 0.7545 |
| 3 | 2 | 2 | Pri Coma | 1.65 | 0.1676 |
| 4 | 3 | 1 | Pri Trefoil | 1.65 | 0.0081 |
| 5 | 3 | 3 | Pri Spherical | 1.54 | 0.0034 |
| 6 | 4 | 0 | Sec Astigmatism | 1.54 | 0.0031 |
| 7 | 4 | 2 | Pri Tetrafoil | 1.48 | 0.0001 |
| 8 | 4 | 4 | Sec Coma | 1.35 | 0.0005 |
| 9 | 5 | 1 | Sec Tetrafoil | 1.35 | 0.0000 |
| 10 | 5 | 3 | Sec Trefoil | 1.35 | 0.0000 |
| 11 | 5 | 5 | Pri Pentafoil | 1.35 | 0.0000 |
| 12 | 6 | 0 | Sec Spherical | 1.35 | 0.0000 |
| 13 | 6 | 2 | Ter Astigmatism | 1.03 | 0.0000 |
| 14 | 6 | 4 | Sec Tetrafoil | 1.25 | 0.0000 |
| 15 | 6 | 6 | Pri Hexafoil | 1.25 | 0.0000 |
| 16 | 7 | 1 | Ter Coma | 0.70 | 0.0000 |
| 17 | 7 | 3 | Ter Trefoil | 0.82 | 0.0000 |
| 18 | 7 | 5 | Sec Pentafoil | 0.80 | 0.0000 |
| 19 | 7 | 7 | Pri Septafoil | 0.89 | 0.0000 |
| 20 | 8 | 0 | Ter Spherical | 0.34 | 0.0000 |
| 21 | 8 | 2 | Qua Astigmatism | 0.50 | |
| 22 | 8 | 4 | Ter Tetrafoil | 0.61 | |
| 23 | 8 | 6 | Sec Hexafoil | 0.72 | |
| 24 | 8 | 8 | Pri Octafoil | 0.68 | |
| 25 | 9 | 1 | Qua Coma | 0.46 | |
| 26 | 10 | 0 | Qua Spherical | 0.57 | |
| 27 | 12 | 0 | Qin Spherical | 0.98 | |



Inertial WFE Stability

Inertial WFE Stability is bending of the mirror as it reacts against its mount when exposed to a noise acceleration.



Primary Mirror Inertial WFE

Inertial WFE is not a resonant mode. It is response to acceleration.

Inertial Error may be proportional to Gravity Sag.

- 1 G acceleration = 1 Gravity Sag
- 1 μ G acceleration = 1 μ Gravity Sag

To minimize Inertial WFE:

- Design the PM Substrate to be as stiff as possible. The stiffer the mirror the smaller the Gravity Sag.
- Consider the Mount stiffness and location.
- If Astigmatism 1G sag is 50 micrometers surface.
- And, if Coronagraph requires < 2 pm wavefront
- Then mirror acceleration must remain < 0.02 μ G.

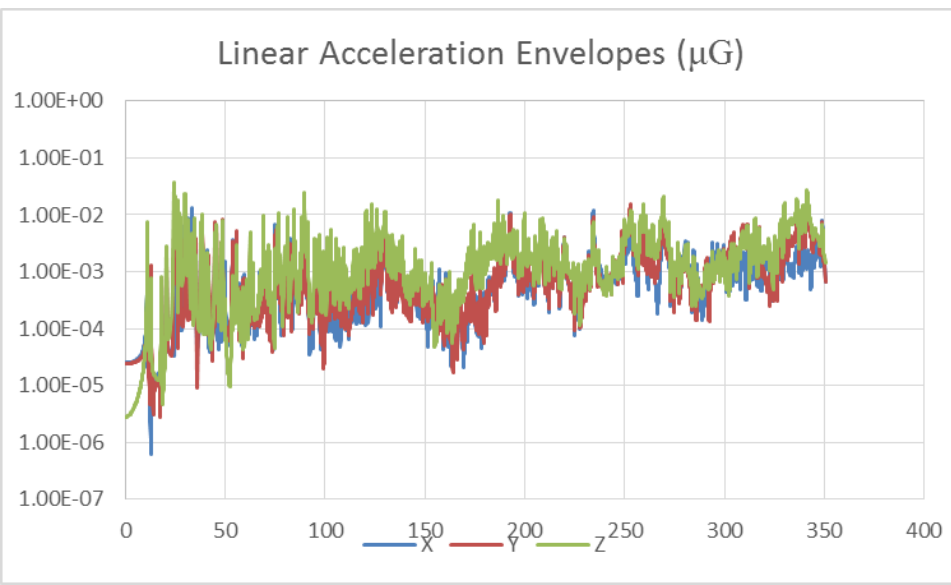
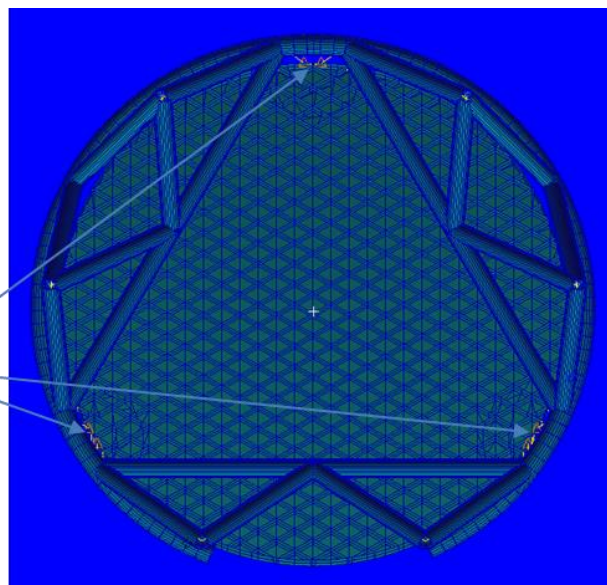


Predicted Acceleration at Primary Mirror

Micro-Thruster noise propagates through Spacecraft Structure, through Interface Ring to the OTA and through the PM Truss Structure to the 3 Primary Mirror Mount Interfaces.

Acceleration at PM Mount Interfaces:

| | X | X | Z | RSS | |
|-----|-------|-------|-------|-------|---------------|
| RMS | 0.001 | 0.002 | 0.003 | 0.003 | μG |
| MAX | 0.013 | 0.016 | 0.037 | 0.037 | μG |

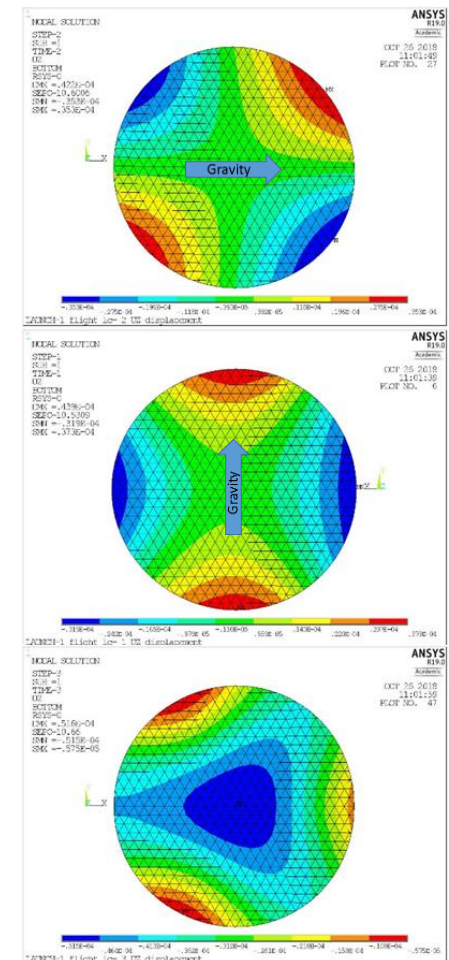




Primary Mirror Inertial Deformation

Primary Mirror has sufficient stiffness (86 Hz free-free) that its predicted Micro-Thruster noise gravity deflection has 2X Astigmatism margin for the VVC4.

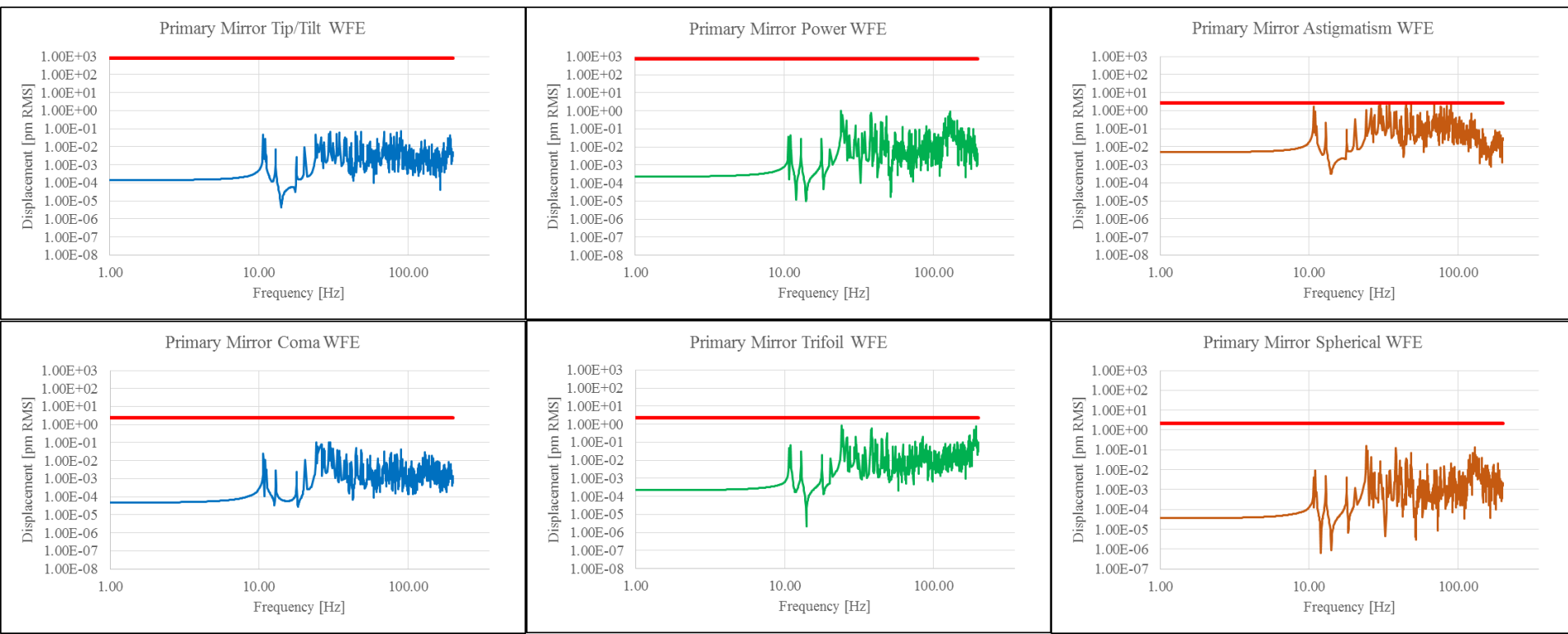
| Inertial WFE Stability | | | | Acceleration [μG] | | | Scaled G-Sag Zernikes | | |
|------------------------|----|---|-----------------|--------------------------------|-----------------------|---------------|-----------------------|-----------------------|-----------------------|
| | | | | Allocation | 0.024 | μG | 0.01 | 0.01 | 0.02 |
| | | | | Inertial | RSS-Zernikes | | X-Zern | Y-Zern | Z-Zern |
| Order | | | | MARGIN | [$\mu\text{m rms}$] | | [$\mu\text{m rms}$] | [$\mu\text{m rms}$] | [$\mu\text{m rms}$] |
| K | N | M | Aberration | [$\mu\text{m rms}$] | | | | | |
| TOTAL RMS | | | | 1139.91 | 1.425 | | 0.743 | 0.736 | 1.007 |
| 1 | 1 | 1 | Tilt | 834.95 | 0.146 | | 0.11 | 0.092 | 0.028 |
| 2 | 2 | 0 | Power (Defocus) | 776.00 | 0.593 | | 0.036 | 0 | 0.592 |
| 3 | 2 | 2 | Pri Astigmatism | 2.67 | 1.047 | | 0.728 | 0.725 | 0.2 |
| 4 | 3 | 1 | Pri Coma | 2.32 | 0.014 | | 0.003 | 0.007 | 0.012 |
| 5 | 3 | 3 | Pri Trefoil | 2.32 | 0.722 | | 0.047 | 0.001 | 0.72 |
| 6 | 4 | 0 | Pri Spherical | 2.16 | 0.074 | | 0.006 | 0 | 0.074 |
| 7 | 4 | 2 | Sec Astigmatism | 2.16 | 0.054 | | 0.037 | 0.037 | 0.012 |
| 8 | 4 | 4 | Pri Tetrafoil | 2.07 | 0.090 | | 0.062 | 0.062 | 0.018 |
| 9 | 5 | 1 | Sec Coma | 1.89 | 0.002 | | 0 | 0.001 | 0.002 |
| 10 | 5 | 3 | Sec Trefoil | 1.89 | 0.114 | | 0.008 | 0 | 0.114 |
| 11 | 5 | 5 | Pri Pentafoil | 1.89 | 0.054 | | 0.037 | 0.038 | 0.012 |
| 12 | 6 | 0 | Sec Spherical | 1.89 | 0.004 | | 0 | 0 | 0.004 |
| 13 | 6 | 2 | Ter Astigmatism | 1.45 | 0.003 | | 0.002 | 0.002 | 0.002 |
| 14 | 6 | 4 | Sec Tetrafoil | 1.76 | 0.009 | | 0.006 | 0.006 | 0.004 |
| 15 | 6 | 6 | Pri Hexafoil | 1.75 | 0.042 | | 0.003 | 0 | 0.042 |
| 16 | 7 | 1 | Ter Coma | 0.99 | 0.002 | | 0 | 0 | 0.002 |
| 17 | 7 | 3 | Ter Trefoil | 1.15 | 0.022 | | 0.001 | 0 | 0.022 |
| 18 | 7 | 5 | Sec Pentafoil | 1.12 | 0.009 | | 0.006 | 0.006 | 0.002 |
| 19 | 7 | 7 | Pri Septafoil | 1.25 | 0.020 | | 0.014 | 0.014 | 0.004 |
| 20 | 8 | 0 | Ter Spherical | 0.48 | 0.082 | | 0.002 | 0 | 0.082 |
| 21 | 8 | 2 | Qua Astigmatism | 0.71 | 0.002 | | 0 | 0 | 0.002 |
| 22 | 8 | 4 | Ter Tetrafoil | 0.85 | 0.000 | | 0 | 0 | 0 |
| 23 | 8 | 6 | Sec Hexafoil | 1.00 | 0.024 | | 0.002 | 0 | 0.024 |
| 24 | 8 | 8 | Pri Octafoil | 0.96 | 0.009 | | 0.006 | 0.006 | 0.002 |
| 25 | 9 | 1 | Qua Coma | 0.64 | 0.000 | | 0 | 0 | 0 |
| 26 | 10 | 0 | Qua Spherical | 0.80 | 0.170 | | 0.004 | 0 | 0.17 |
| 27 | 12 | 0 | Qjn Spherical | 1.37 | 0.218 | | 0.005 | 0 | 0.218 |





Predicted Primary Mirror Inertial Bending

- SigFit and NASTRAN used to determine Zernike decomposition.
- Predicted primary mirror inertial bending (with 4X MUF) caused by the micro-thruster noise specification of $0.1 \mu\text{N}$ broad band is below the error budget tolerance (red line).
- Micro-thruster noise roll off at higher frequencies will reduce error.
- Tolerance for Astig, Coma & Spherical is higher for VVC6.





Inertial Deformation Cross Check

Inertial WFE was calculated by two methods:

- Linear Scaling of Gravity Sag
 - Scale from (1,1,1) G to (0.01, 0.01, 0.02) μG
- Dynamic Deformation Analysis vis SigFit and NASTRAN
 - Calculate RMS of Zernike term from 1 to 200 Hz and multiply by 4

| Zernike Term | 0.024 μG Scaled G-Sag | Dynamic Analysis |
|--------------|----------------------------------|------------------|
| Tip/Tilt | 0.156 pm rms | 0.038 pm rms |
| Power | 0.593 pm rms | 0.465 pm rms |
| Astigmatism | 1.047 pmrms | 1.151 pm rms |
| Coma | 0.014 pm rms | 0.031 pm rms |
| Trefoil | 0.772 pm rms | 0.344 pm rms |
| Spherical | 0.074 pm rms | 0.069 pm rms |



Thermal WFE Stability

Temperature changes result in WFE caused by CTE and CTE homogeneity.

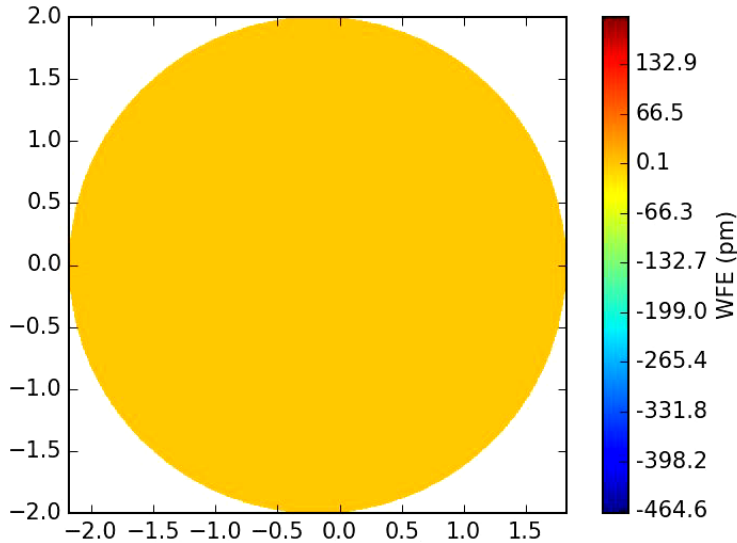


Initial Concept - Dynamic Thermal WFE Video

Passive Wavefront Error from 1 hour exposure.

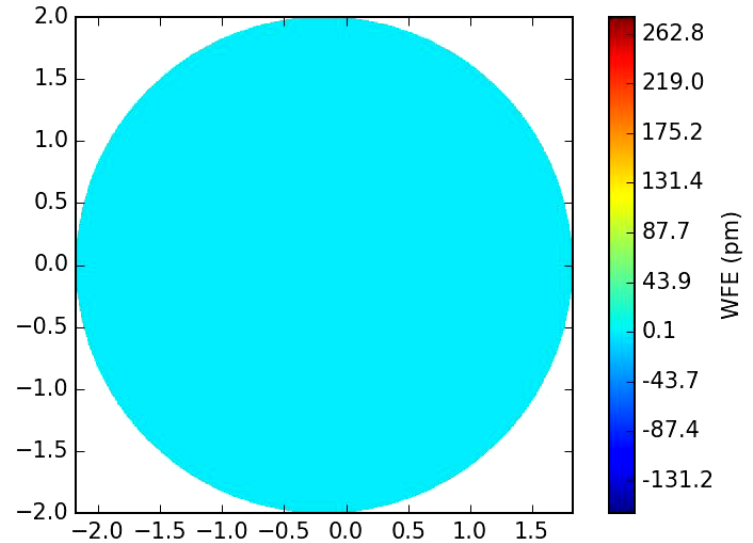
Sun angle changes by 0.0411 degree per hour.

All Errors



WFE/1-hour = 233 pm PV
WFE/20-min = 28 pm

Power Removed



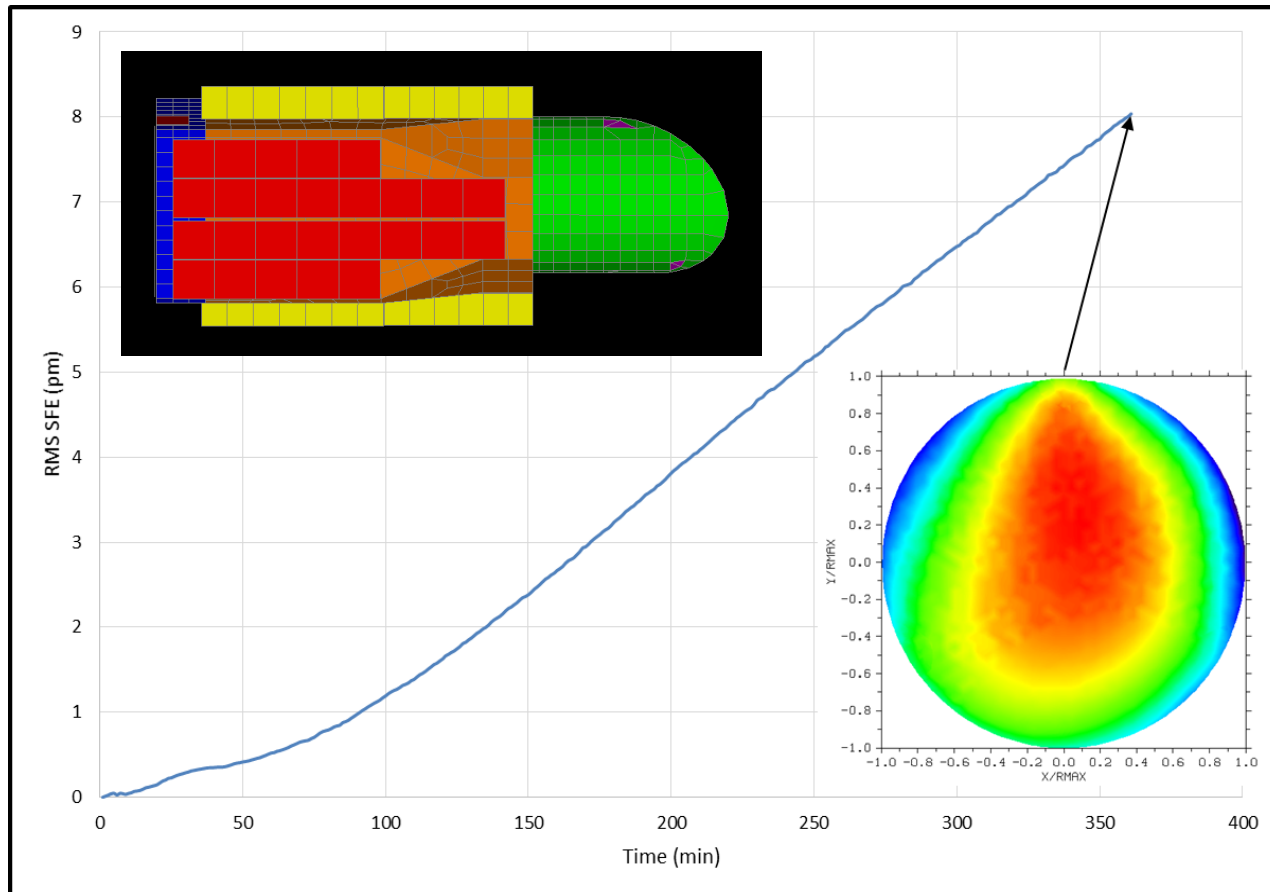
WFE/1-hour = 101 pm PV
WFE/20-min = 13 pm



Thermal WFE Stability Analysis – Passive

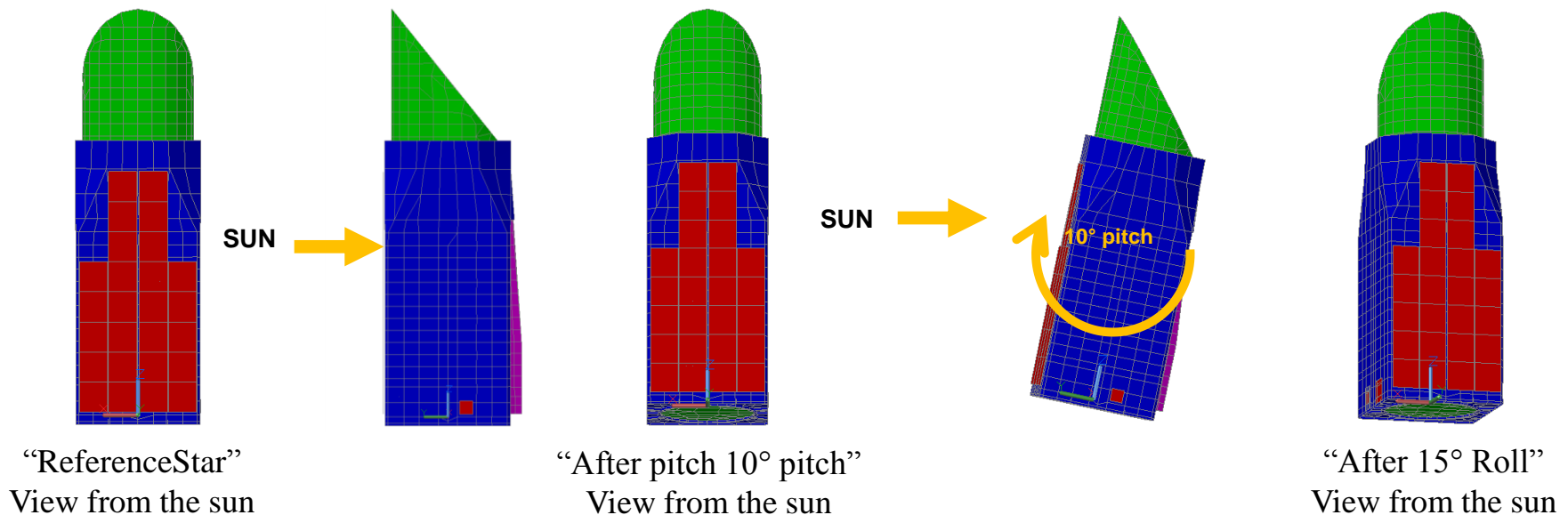
Baseline 4m telescope (with open-back Zerodur mirror, sun-shield, MLI) thermal WFE stability analysis for a 20 deg slew.

WFE changes by less than 1 pm rms over 90 minutes.



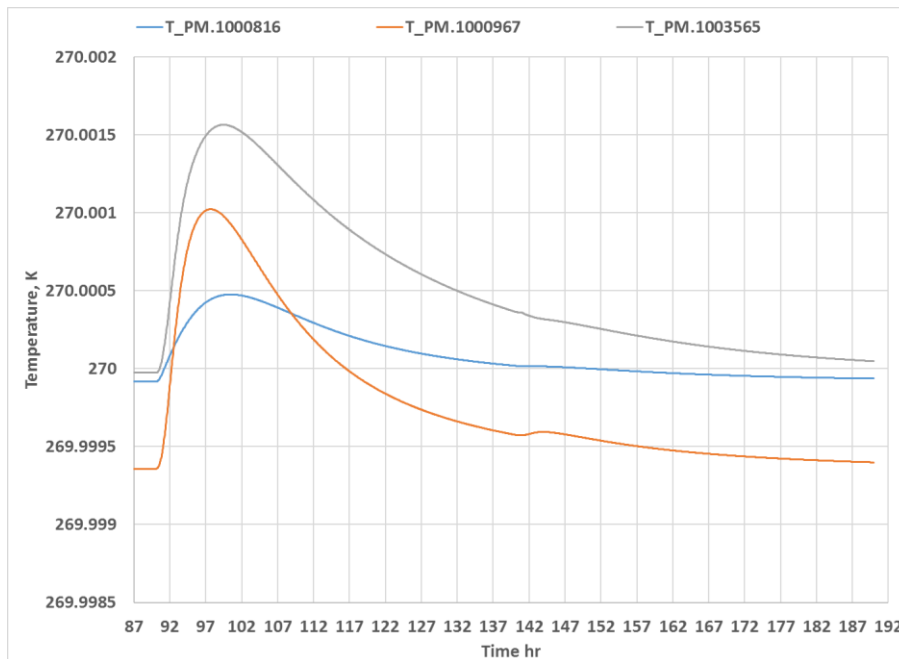


1. Telescope points at a Reference Star to dig a dark hole in the coronagraph and reaches a steady state in this orientation.
2. After reaching steady state the telescope performs a 10° pitch to point at the Target Star and stays at this position for 50hrs
3. For Speckle Subtraction, Telescope performs a 15° roll and stays at this position for 50hrs

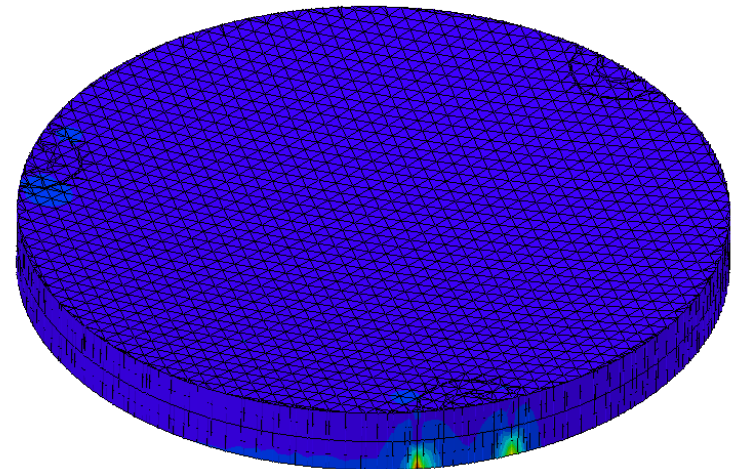




10 deg pitch causes maximum 1.6 mK change to the Primary Mirror at the hexapod strut mount locations – indicating need to heat struts.



Max Delta T from reference
star after pitch maneuver
Average ΔT 1.6mK

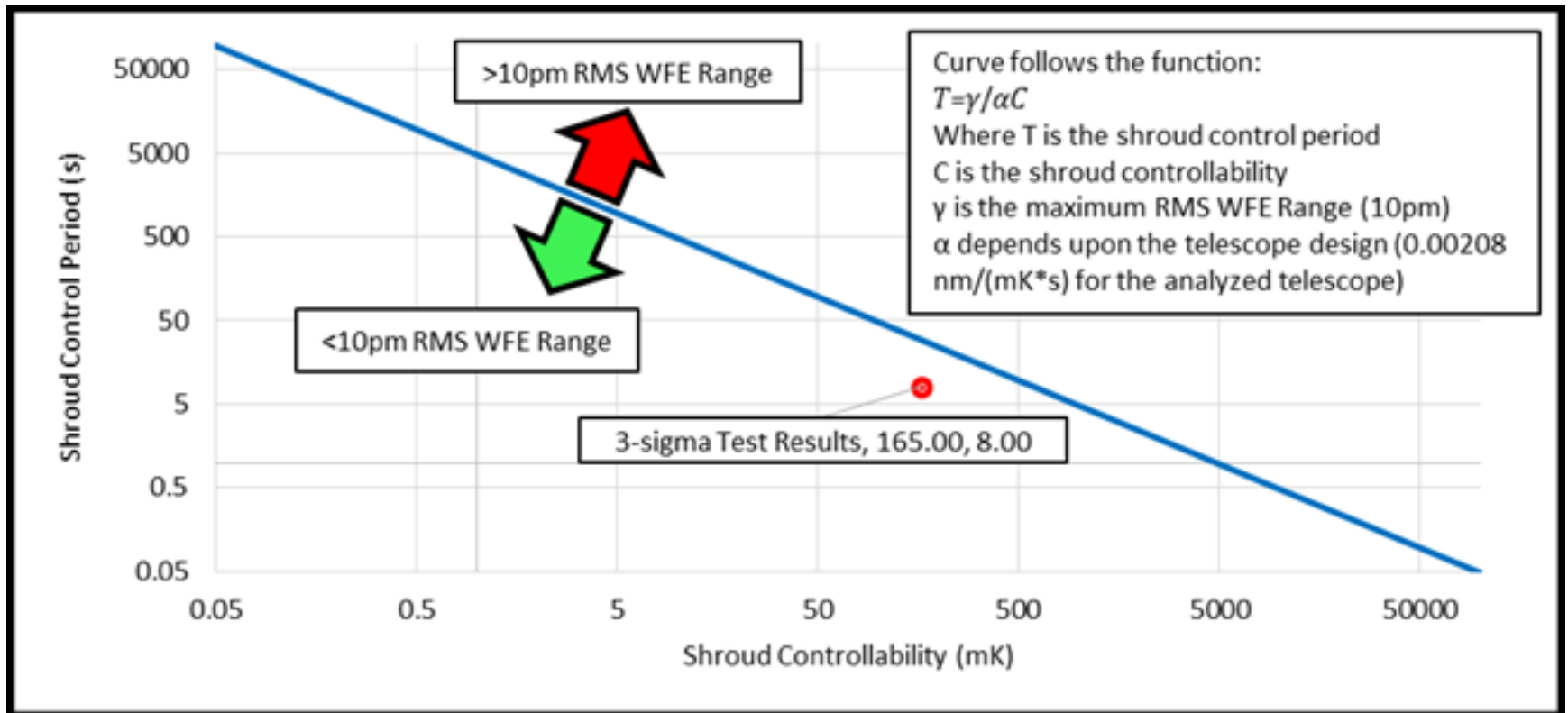




Active Thermal Stability

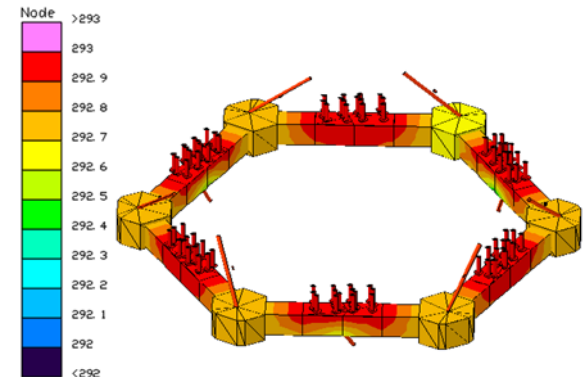
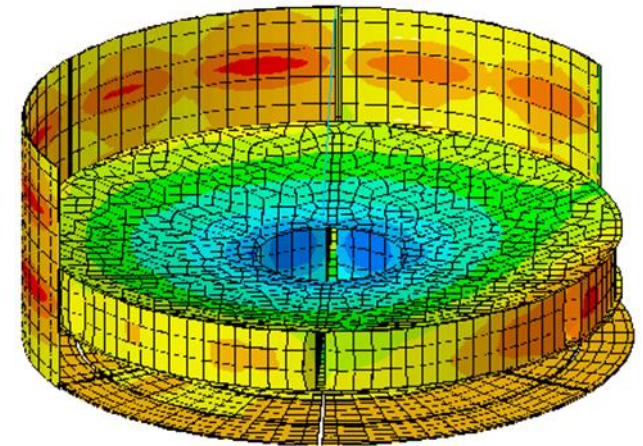
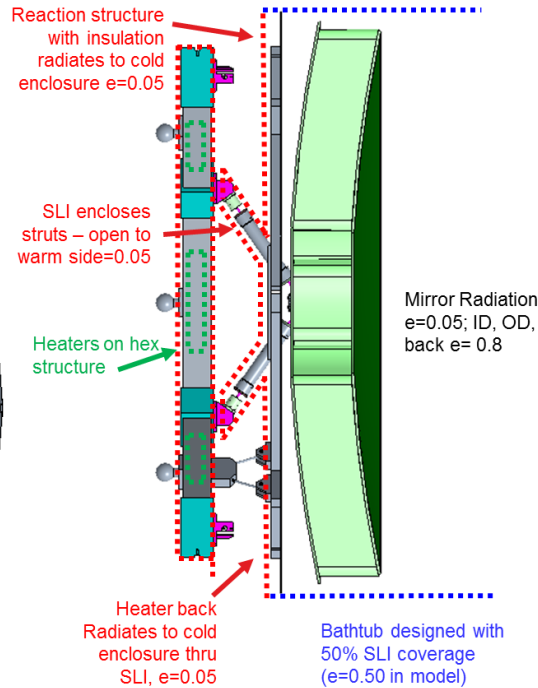
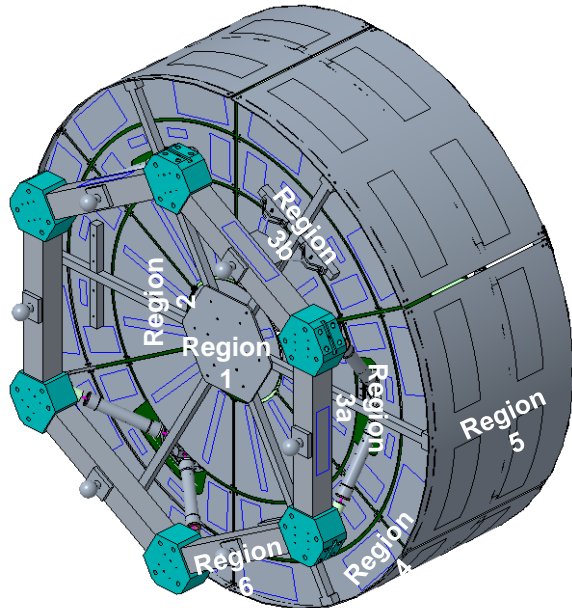
The ability to achieve any required wavefront stability depends on:

- Mirror Substrate Properties: CTE, Thermal Mass, Conductivity, etc.
- Thermal Environment Controllability
- Control Period.

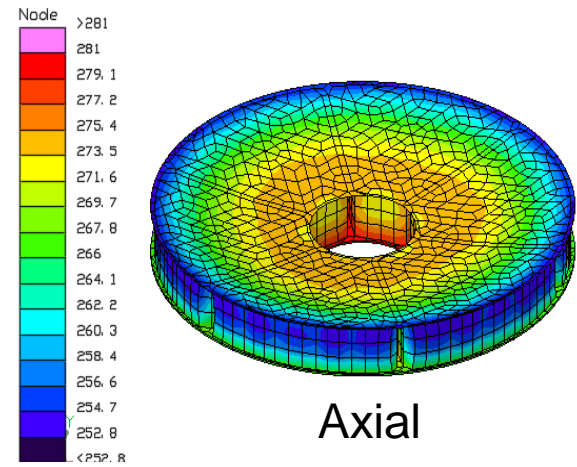
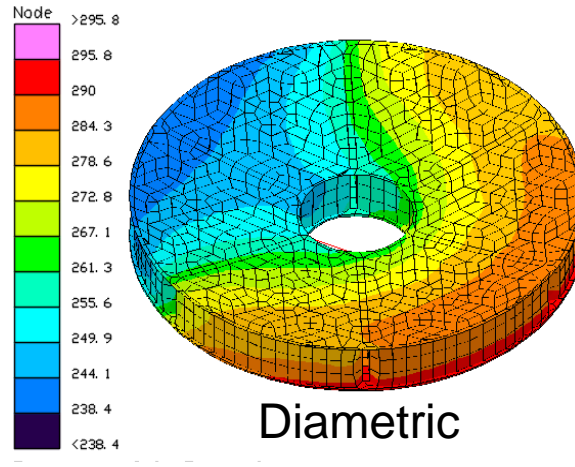
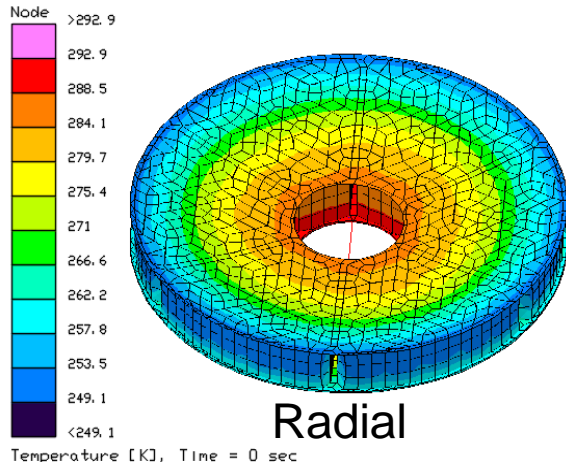


Additional Stability can be achieved using active thermal control.

Heater zones behind, surrounding & in front of mirror



Heater design induces gradients to compensate thermal environment



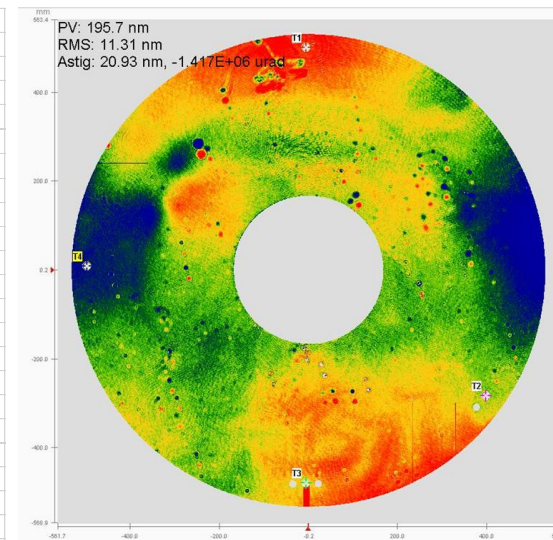


Predicted Thermal Performance

For HabEx we are assuming a linear scaling of the measured 11.3 nm rms per 62K cryo-deformation performance of a 1.2-meter Zerodur mirror owned by Schott decomposed into Zernikes.

Mirror achieves 2X Astig margin for ~2 mK thermal stability.

| | | | Delta Temperature | | | | 62000.0 mK | | | | | |
|-------|------------|---|-------------------|-----------|-------------|---------------|------------|---|--------------------------------------|----------|----------|--|
| | | | Thermal Stability | | | | 2.0 mK | | | | | |
| | | | | | | | | | Measured Delta-SFE 292-230K | | | |
| | | | | | | | | | Zernike Coefficient [nm] RMS Surface | | | |
| | | | | | | | | | RMS-Zern | X-Zern | Y-Zern | |
| | | | | | | | | | [nm rms] | [nm rms] | [nm rms] | |
| Order | Allocation | | Thermal | MARGIN | Zernikes | WFE/dT | | | N | M | | |
| K | N | M | [pm rms] | | Thermal WFE | RMS-Zern | | | | | | |
| | | | | | RMS pm/mK | [pm rms / mK] | | | | | | |
| | | | 814.22 | | 0.822 | | | | | | | |
| | | | TOTAL RMS | | 0.822 | | | | | | | |
| 1 | 1 | 1 | 596.40 | 195503.42 | 0.003 | 0.002 | 1 | 1 | 0.095 | 0.055 | 0.077 | |
| | | | Tilt | | 0.003 | | | | | | | |
| 2 | 2 | 0 | 554.29 | 41266.52 | 0.013 | 0.007 | 2 | 0 | 0.416 | 0.416 | | |
| | | | Power (Defocus) | | 0.013 | | | | | | | |
| 3 | 2 | 2 | 1.91 | 2.83 | 0.675 | 0.338 | 2 | 2 | 20.940 | -19.960 | -6.330 | |
| | | | Pri Astigmatism | | 0.675 | | | | | | | |
| 4 | 3 | 1 | 1.65 | 20.18 | 0.082 | 0.041 | 3 | 1 | 2.541 | -2.539 | 0.109 | |
| | | | Pri Coma | | 0.082 | | | | | | | |
| 5 | 3 | 3 | 1.65 | 8.42 | 0.196 | 0.098 | 3 | 3 | 6.089 | -3.970 | -4.617 | |
| | | | Pri Trefoil | | 0.196 | | | | | | | |
| 6 | 4 | 0 | 1.54 | 79.67 | 0.019 | 0.010 | 4 | 0 | 0.599 | 0.599 | | |
| | | | Pri Spherical | | 0.019 | | | | | | | |
| 7 | 4 | 2 | 1.54 | 20.93 | 0.074 | 0.037 | 4 | 2 | 2.283 | -2.046 | -1.012 | |
| | | | Sec Astigmatism | | 0.074 | | | | | | | |
| 8 | 4 | 4 | 1.48 | 8.39 | 0.176 | 0.088 | 4 | 4 | 5.471 | -3.683 | 4.046 | |
| | | | Pri Tetrafoil | | 0.176 | | | | | | | |
| 9 | 5 | 1 | 1.35 | 16.16 | 0.084 | 0.042 | 5 | 1 | 2.591 | -1.050 | 2.369 | |
| | | | Sec Coma | | 0.084 | | | | | | | |
| 10 | 5 | 3 | 1.35 | 8.70 | 0.155 | 0.078 | 5 | 3 | 4.811 | 0.912 | -4.724 | |
| | | | Sec Trefoil | | 0.155 | | | | | | | |
| 11 | 5 | 5 | 1.35 | 22.78 | 0.059 | 0.030 | 5 | 5 | 1.838 | 1.713 | -0.666 | |
| | | | Pri Pentafoil | | 0.059 | | | | | | | |
| 12 | 6 | 0 | 1.35 | 39.23 | 0.034 | 0.017 | 6 | 0 | 1.067 | 1.067 | | |
| | | | Sec Spherical | | 0.034 | | | | | | | |
| 13 | 6 | 2 | 1.03 | 9.24 | 0.112 | 0.056 | 6 | 2 | 3.465 | 3.341 | -0.918 | |
| | | | Ter Astigmatism | | 0.112 | | | | | | | |
| 14 | 6 | 4 | 1.25 | 35.69 | 0.035 | 0.018 | 6 | 4 | 1.089 | -0.647 | 0.876 | |
| | | | Sec Tetrafoil | | 0.035 | | | | | | | |
| 15 | 6 | 6 | 1.25 | 8.13 | 0.154 | 0.077 | 6 | 6 | 4.772 | -4.569 | -1.376 | |
| | | | Pri Hexafoil | | 0.154 | | | | | | | |
| 16 | 7 | 1 | 0.70 | 7.11 | 0.099 | 0.050 | 7 | 1 | 3.073 | 0.786 | -2.971 | |
| | | | Ter Coma | | 0.099 | | | | | | | |
| 17 | 7 | 3 | 0.82 | 3.71 | 0.221 | 0.111 | 7 | 3 | 6.863 | -1.165 | 6.763 | |
| | | | Ter Trefoil | | 0.221 | | | | | | | |
| 18 | 7 | 5 | 0.80 | 12.67 | 0.063 | 0.031 | 7 | 5 | 1.953 | -0.487 | 1.891 | |
| | | | Sec Pentafoil | | 0.063 | | | | | | | |
| 19 | 7 | 7 | 0.89 | | | 0.000 | | | | | | |
| | | | Pri Septafoil | | | | | | | | | |
| 20 | 8 | 0 | 0.34 | 14.54 | 0.024 | 0.012 | 8 | 0 | 0.729 | -0.729 | | |
| | | | Ter Spherical | | 0.024 | | | | | | | |
| 21 | 8 | 2 | 0.50 | 91.63 | 0.006 | 0.003 | 8 | 2 | 0.171 | -0.091 | -0.144 | |
| | | | Qua Astigmatism | | 0.006 | | | | | | | |
| 22 | 8 | 4 | 0.61 | 9.43 | 0.064 | 0.032 | 8 | 4 | 1.999 | 1.262 | -1.550 | |
| | | | Ter Tetrafoil | | 0.064 | | | | | | | |
| 23 | 8 | 6 | 0.72 | | | 0.000 | | | | | | |
| | | | Sec Hexafoil | | | | | | | | | |
| 24 | 8 | 8 | 0.68 | | | 0.000 | | | | | | |
| | | | Pri Octafoil | | | | | | | | | |
| 25 | 9 | 1 | 0.46 | 3.86 | 0.118 | 0.059 | 9 | 1 | 3.659 | 3.220 | -1.738 | |
| | | | Qua Coma | | 0.118 | | | | | | | |
| 26 | 10 | 0 | 0.57 | 9.41 | 0.061 | 0.030 | 10 | 0 | 1.883 | -1.883 | | |
| | | | Qua Spherical | | 0.061 | | | | | | | |
| 27 | 12 | 0 | 0.98 | 11.49 | 0.085 | 0.043 | 12 | 0 | 2.635 | 2.635 | | |
| | | | Qin Spherical | | 0.085 | | | | | | | |





Conclusions



Error Budget Closes for LOS, Inertial & Thermal

Error budget closes for VVC4. VVC6 relaxes Astig and Coma.

| RSS Allocation | | | 100% | 50% | 70% | 50% | 10% | Predicted Performance Margin | | | | |
|----------------|----|---|------|-----------------|-----------------|----------|----------|------------------------------|----------|-------------|---------------|--------------|
| Order | K | N | M | Aberration | VVC-4 Tolerance | LOS | Inertial | Thermal | Reserve | LOS | Inertial [uG] | Thermal [mK] |
| | | | | | [pm rms] | [pm rms] | [pm rms] | [pm rms] | [pm rms] | | 0.02 | 2 |
| | | | | TOTAL RMS | 1628.4 | 814 | 1140 | 814 | 163 | | | |
| 1 | 1 | 1 | | Tilt | 1192.8 | 596.40 | 834.95 | 596.40 | 119.28 | 1251.51 | 5714.58 | 195503.42 |
| 2 | 2 | 0 | | Power (Defocus) | 1108.6 | 554.29 | 776.00 | 554.29 | 110.86 | 623.99 | 1308.40 | 41266.52 |
| 3 | 2 | 2 | | Pri Astigmatism | 3.8 | 1.91 | 2.67 | 1.91 | 0.38 | 2.53 | 2.56 | 2.83 |
| 4 | 3 | 1 | | Pri Coma | 3.3 | 1.65 | 2.32 | 1.65 | 0.33 | 9.87 | 162.98 | 20.18 |
| 5 | 3 | 3 | | Pri Trefoil | 3.3 | 1.65 | 2.32 | 1.65 | 0.33 | 203.32 | 3.21 | 8.42 |
| 6 | 4 | 0 | | Pri Spherical | 3.1 | 1.54 | 2.16 | 1.54 | 0.31 | 458.99 | 29.04 | 79.67 |
| 7 | 4 | 2 | | Sec Astigmatism | 3.1 | 1.54 | 2.16 | 1.54 | 0.31 | 497.39 | 40.20 | 20.93 |
| 8 | 4 | 4 | | Pri Tetrafoil | 3.0 | 1.48 | 2.07 | 1.48 | 0.30 | 15756.44 | 23.15 | 8.39 |
| 9 | 5 | 1 | | Sec Coma | 2.7 | 1.35 | 1.89 | 1.35 | 0.27 | 2872.33 | 845.83 | 16.16 |
| 10 | 5 | 3 | | Sec Trefoil | 2.7 | 1.35 | 1.89 | 1.35 | 0.27 | 31963.42 | 16.55 | 8.70 |
| 11 | 5 | 5 | | Pri Pentafoil | 2.7 | 1.35 | 1.89 | 1.35 | 0.27 | 1251062.38 | 34.78 | 22.78 |
| 12 | 6 | 0 | | Sec Spherical | 2.7 | 1.35 | 1.89 | 1.35 | 0.27 | 121850.21 | 472.62 | 39.23 |
| 13 | 6 | 2 | | Ter Astigmatism | 2.1 | 1.03 | 1.45 | 1.03 | 0.21 | 95757.25 | 417.34 | 9.24 |
| 14 | 6 | 4 | | Sec Tetrafoil | 2.5 | 1.25 | 1.76 | 1.25 | 0.25 | 2352446.64 | 187.09 | 35.69 |
| 15 | 6 | 6 | | Pri Hexafoil | 2.5 | 1.25 | 1.75 | 1.25 | 0.25 | 20917403.44 | 41.59 | 8.13 |
| 16 | 7 | 1 | | Ter Coma | 1.4 | 0.70 | 0.99 | 0.70 | 0.14 | 625089.60 | 493.29 | 7.11 |
| 17 | 7 | 3 | | Ter Trefoil | 1.6 | 0.82 | 1.15 | 0.82 | 0.16 | 3719658.50 | 52.21 | 3.71 |
| 18 | 7 | 5 | | Sec Pentafoil | 1.6 | 0.80 | 1.12 | 0.80 | 0.16 | 17228267.14 | 128.13 | 12.67 |
| 19 | 7 | 7 | | Pri Septafoil | 1.8 | 0.89 | 1.25 | 0.89 | 0.18 | 18000287.24 | 61.85 | |
| 20 | 8 | 0 | | Ter Spherical | 0.7 | 0.34 | 0.48 | 0.34 | 0.07 | 8063896.81 | 5.83 | 14.54 |
| 21 | 8 | 2 | | Qua Astigmatism | 1.0 | 0.50 | 0.71 | 0.50 | 0.10 | 0.00 | 352.98 | 91.63 |
| 22 | 8 | 4 | | Ter Tetrafoil | 1.2 | 0.61 | 0.85 | 0.61 | 0.12 | 0.00 | 0.00 | 9.43 |
| 23 | 8 | 6 | | Sec Hexafoil | 1.4 | 0.72 | 1.00 | 0.72 | 0.14 | 0.00 | 41.69 | |
| 24 | 8 | 8 | | Pri Octafoil | 1.4 | 0.68 | 0.96 | 0.68 | 0.14 | 0.00 | 109.75 | |
| 25 | 9 | 1 | | Qua Coma | 0.9 | 0.46 | 0.64 | 0.46 | 0.09 | 0.00 | 0.00 | 3.86 |
| 26 | 10 | 0 | | Qua Spherical | 1.1 | 0.57 | 0.80 | 0.57 | 0.11 | 0.00 | 4.71 | 9.41 |
| 27 | 12 | 0 | | Qin Spherical | 2.0 | 0.98 | 1.37 | 0.98 | 0.20 | 0.00 | 6.27 | 11.49 |



Conclusions

The HabEx Baseline Telescope Design ‘Closes’.

It meets the WFE Stability Error Budget

The design uses standard engineering practice.

Baseline design is enabled by two capabilities:

- 8-m fairing volume provided by SLS
- Low mechanical disturbance provided by micro-thrusters.