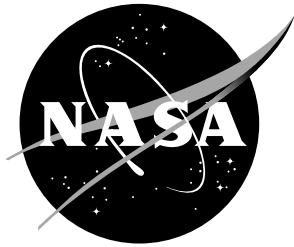


NASA/TM-2019-220285



Bowles-Tatnall Wake Vortex Encounter Hazard Metric

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June 2019

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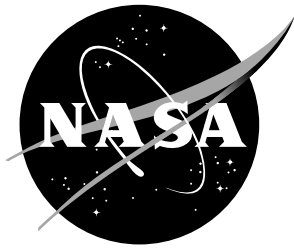
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Nomenclature

Γ_0	Initial vortex circulation (m^2/s)
λ_F	Following aircraft wing taper ratio
Φ	Bank angle of the following aircraft (rad)
$(AR)_G$	Aspect ratio of the generating aircraft wing
b_F	Following aircraft wing span (m)
b_G	Generating aircraft wing span (m)
c_F	Following aircraft wing chord (m)
$C_{L\alpha F}$	Three-dimensional lift-curve slope of following aircraft (rad^{-1})
C_{LG}	Lift coefficient of the generating aircraft
C_{lv}	Vortex-induced rolling moment coefficient
C_{Lv}	Vortex-induced lift coefficient
\bar{q}	Freestream dynamic pressure (kg/m^2)
r_c	Vortex-core radius (m)
s	Half of the vortex pair separation distance (m)
S_F	Following aircraft wings planform area (m^2)
V_F	Velocity of the following aircraft (m/s)
V_G	Generating aircraft velocity (m/s)
Y	Inertial lateral coordinate (m)
Y_F	Lateral location of the following aircraft (m)
Z	Inertial vertical coordinate (m)
Z_F	Vertical location of the following aircraft (m)

1. Introduction

Wake vortex spacing standards constrict the terminal area throughput and impose severe constraints on the overall capacity and efficiency of the National Airspace System. For more than two decades starting in the early 1990s, the National Aeronautics and Space Administration conducted extensive research on characterizing the formation and evolution of aircraft wakes. This multidisciplinary work included comprehensive field experiments (Pruis et al. 2016), flight tests (Vicroy et al. 1998), and wind tunnel tests (Rossow 1994; Chow et al. 1997). Parametric studies using large eddy simulations (Proctor 1998; Proctor et al. 2006) were conducted in order to develop fast-time models for the prediction of wake transport and decay (Ahmad et al. 2016). Substantial effort was spent on the formulation of acceptable vortex hazard metrics (Tatnall 1995; Hinton and Tatnall 1997).

Several wake encounter severity metrics have been suggested in the past, which include the wake circulation strength, vortex-induced rolling moment coefficient (C_{lv}), bank angle, and the roll control ratio (Tatnall 1995; Hinton and Tatnall 1997; Van der Geest 2012). The vortex-induced rolling moment coefficient introduced by Bowles and Tatnall (Tatnall 1995; Gloudemans et al. 2016) has been used extensively for risk and safety analysis of newly proposed air traffic management concepts and procedures. The original method of Bowles and Tatnall assumed a constant wing loading (the wing lift-curve slope, $C_{L\alpha}$ is constant), which resulted in an overestimation of the vortex-induced rolling moment coefficient. Bowles (2014) suggested a correction to the original method that provides more accurate values of C_{lv} and which is also consistent with the underlying physics of the problem. The overestimation of C_{lv} in the original method can be corrected by assuming an elliptical lift distribution. Figure 1.1 illustrates the correction in C_{lv} achieved by the modified method.

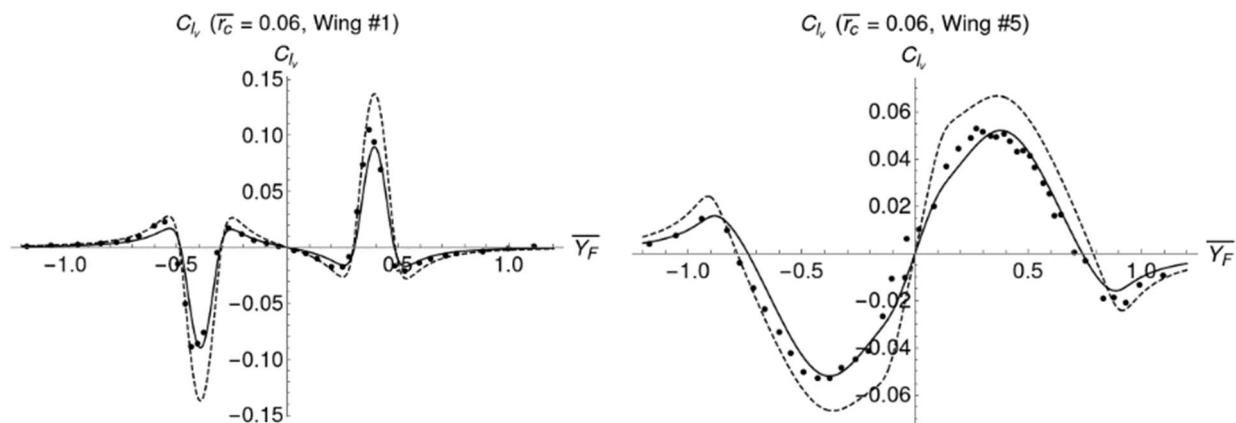


Figure 1.1: Comparison of the vortex-induced rolling moment coefficient using constant and elliptical wing loadings with the wind tunnel data (Rossow 1994). Dashed line denotes a constant wing loading and solid line denotes an elliptical wing loading. The wind tunnel data are given by points in the plots. Results are shown for two different wings used in the wind tunnel test.

The assumption of constant wing loading in their original formulation had allowed Bowles and Tatnall to derive a closed-form analytical solution, which was computationally efficient and convenient to use. The addition of elliptical loading term added complexity that required numerical integration. This brief note presents a closed-form analytical solution to the modified Bowles-Tatnall method. The analytical solutions for both the vortex-induced rolling moment coefficient and the vortex-induced lift are compared with results obtained using numerical integration. The resulting analytical method is robust, computationally efficient (more than ten times faster compared to numerical integration), and convenient to use. The simplicity of the method will allow efficient calculations of large leader-follower aircraft matrices in the safety analyses of new procedures. It can also be used on the flight deck for future operations such as dynamic self-separation of aircraft.

2. Vortex-Induced Rolling Moment and Lift Coefficients

The derivation of the analytical expression for the vortex-induced rolling moment and lift coefficients is given in this section. The axis conventions follow Tatnall (1995) and are shown in Figure 2.1.

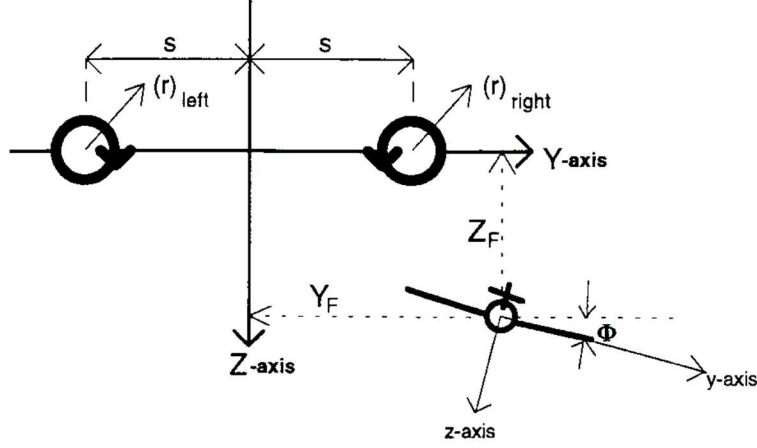


Figure 2.1. Axis conventions and nomenclature as defined by Tatnall (1995).

The Bowles-Tatnall vortex-induced rolling moment coefficient (Tatnall 1995) is given by:

$$C_{iw} = \frac{2C_{L_G} C_{L_{\alpha F}} V_G b_G^2}{\pi^2 (AR)_G b_F^2 (1 + \lambda_F) V_F} \int_{-b_F/2b_G}^{b_F/2b_G} \left[\bar{y} \left(1 - \frac{2b_G(1 - \lambda_F)}{b_F} |\bar{y}| \right) \cdot \left[\frac{\bar{y} + (\bar{Y}_F + \bar{s}) \cos(\Phi) + \bar{Z}_F \sin(\Phi)}{\bar{y}^2 + \bar{y} (2(\bar{Y}_F + \bar{s}) \cos(\Phi) + 2\bar{Z}_F \sin(\Phi)) + ((\bar{Y}_F + \bar{s})^2 + \bar{Z}_F^2 + \bar{r}_c^2)} \right] - \left[\frac{\bar{y} + (\bar{Y}_F - \bar{s}) \cos(\Phi) + \bar{Z}_F \sin(\Phi)}{\bar{y}^2 + \bar{y} (2(\bar{Y}_F - \bar{s}) \cos(\Phi) + 2\bar{Z}_F \sin(\Phi)) + ((\bar{Y}_F - \bar{s})^2 + \bar{Z}_F^2 + \bar{r}_c^2)} \right] \right] d\bar{y}, \quad (2.1)$$

where, C_{L_G} is the lift coefficient of the vortex generator, $C_{L_{\alpha F}}$ is the three-dimensional lift-curve slope of the follower, V_F and V_G are the airspeeds of the follower and the vortex generator, respectively, b_F and b_G are the wingspans of the follower and generator, respectively. $(AR)_G$ is the wing aspect ratio of the generator, λ_F is the wing taper ratio of the follower, s is the half of vortex pair separation, r_c is the vortex core radius size, Φ is the bank angle of the follower, and (Y_F, Z_F) is the follower's center of gravity in inertial coordinates. The overbar symbol implies normalization by the generator wingspan, b_G .

Eq. (2.1) can be rewritten by substituting

$$\Gamma_0 = \frac{2C_{L_G} b_G V_G}{\pi (AR)_G}, \quad (2.2)$$

where, Γ_0 is the circulation strength of the generator's wake vortex,

$$C_{lw} = \frac{\Gamma_0 C_{L_{\alpha F}} b_G}{\pi b_F^2 (1 + \lambda_F) V_F} \int_{-b_F/2}^{b_F/2} \left[\begin{aligned} & \left[\bar{y} \left(1 - \frac{2b_G(1 - \lambda_F)}{b_F} \left| \frac{\bar{y}}{b_F} \right| \right) \right] \bullet \\ & \left[\frac{\bar{y} + (\bar{Y}_F + \bar{s}) \cos(\Phi) + \bar{Z}_F \sin(\Phi)}{\bar{y}^2 + \bar{y} (2(\bar{Y}_F + \bar{s}) \cos(\Phi) + 2\bar{Z}_F \sin(\Phi)) + ((\bar{Y}_F + \bar{s})^2 + \bar{Z}_F^2 + \bar{r}_c^2)} \right] \\ & - \left[\frac{\bar{y} + (\bar{Y}_F - \bar{s}) \cos(\Phi) + \bar{Z}_F \sin(\Phi)}{\bar{y}^2 + \bar{y} (2(\bar{Y}_F - \bar{s}) \cos(\Phi) + 2\bar{Z}_F \sin(\Phi)) + ((\bar{Y}_F - \bar{s})^2 + \bar{Z}_F^2 + \bar{r}_c^2)} \right] \end{aligned} \right] d\bar{y}. \quad (2.3)$$

The integrals in Eq. (2.1) and (2.3) assume a constant lift distribution across the wingspan, which simplifies the integral and allows closed-form solution for the rolling moment coefficient:

$$C_{lw} = K_{lw} (I_1 - I_2), \quad (2.4)$$

where,

$$K_{lw} = \left(\frac{\Gamma_0}{\pi} \right) \left(\frac{C_{L_{\alpha F}} b_G}{b_F^2 V_F} \right) \left(\frac{1}{1 + \lambda_F} \right). \quad (2.5)$$

I_1 and I_2 are defined as follows:

$$I_i = \frac{1}{2} \left[(C_i^2 - A_i^2) \Omega - C_i \right] \ln \left[\frac{C_i^2 + A_i^2}{(C_i - B)^2 + A_i^2} \right] + \frac{1}{2} \left[(C_i^2 - A_i^2) \Omega + C_i \right] \ln \left[\frac{C_i^2 + A_i^2}{(C_i + B)^2 + A_i^2} \right] + A_i \left[4C_i \Omega \tan^{-1} \left(\frac{C_i}{A_i} \right) + (1 - 2C_i \Omega) \tan^{-1} \left(\frac{C_i - B}{A_i} \right) - (1 + 2C_i \Omega) \tan^{-1} \left(\frac{C_i + B}{A_i} \right) \right] \quad i = 1, 2. \quad (2.6)$$

The parameters, C_1 , C_2 , A_1 , A_2 , B , and Ω in Eq. (2.6) are given by

$$C_1 = (\bar{Y}_F + \bar{s}) \cos(\Phi) + \bar{Z}_F \sin(\Phi), \quad (2.7)$$

$$C_2 = (\bar{Y}_F - \bar{s}) \cos(\Phi) + \bar{Z}_F \sin(\Phi), \quad (2.8)$$

$$A_1^2 = [(\bar{Y}_F + \bar{s}) \sin(\Phi) - \bar{Z}_F \cos(\Phi)]^2 + \bar{r}_c^2, \quad (2.9)$$

$$A_2^2 = [(\bar{Y}_F - \bar{s}) \sin(\Phi) - \bar{Z}_F \cos(\Phi)]^2 + \bar{r}_c^2, \quad (2.10)$$

$$B = \frac{b_F}{2b_G}, \quad (2.11)$$

$$\Omega = \frac{1 - \lambda_F}{B}. \quad (2.12)$$

The overbar symbol implies normalization by the generator wingspan, b_G , e.g., $\bar{Z}_F = \frac{Z_F}{b_G}$.

The modification to Eq. (2.3) with elliptical wing loading proposed by Bowles is given in Eq. (2.13). This addition complicated the integral by introducing a square root term and until now required numerical integration for its solution,

$$C_{lv} = K_{lv} \int_{-B}^B \left[\bar{y}(1 - \Omega|\bar{y}|) \sqrt{1 - \left(\frac{\bar{y}}{B}\right)^2} \left(\frac{\bar{y} + C_1}{(\bar{y} + C_1)^2 + A_1^2} - \frac{\bar{y} + C_2}{(\bar{y} + C_2)^2 + A_2^2} \right) \right] d\bar{y}. \quad (2.13)$$

The analytical solution of Eq. (2.13) can be found by first separating the integral given in Eq. (2.13) according to

$$\int_{-a}^a f(|x|) dx = \int_{-a}^0 f(-x) dx + \int_0^a f(x) dx, \quad \text{if } a > 0. \quad (2.14)$$

The resulting integrands are factored into terms of the form $\frac{p_1(x)\sqrt{p_2(x)}}{p_2(x)}$, where $p_n(x)$ is a polynomial of degree n . Applying rule-based integration (Rich et al. 2018) leads to an analytical solution. These rules are described below:

If $e^2 - 4df \neq 0$, $p = \frac{1}{2}$, and $q = -1$, then

$$\begin{aligned} & \int (g + hx)(a + cx^2)^p (d + ex + fx^2)^q dx \\ &= \frac{h(a + cx^2)^p}{2fp} \\ &+ \frac{1}{2fp} \int (a + cx^2)^{p-1} (d + ex + fx^2)^q (ahcp - ap(he - 2gf) - 2hp(cd - af)x - (hcep + cp(he - 2gf))x^2) dx. \end{aligned} \quad (2.15)$$

If $n = 2$, and $p = \frac{1}{2}$, then

$$\int (a + bx^n)^p dx = \frac{x(a + bx^n)^p}{np + 1} + \frac{anp}{np + 1} \int (a + bx^n)^{p-1} dx. \quad (2.16)$$

If $b^2 - 4ac \neq 0$, then

$$\int \frac{A + Bx + Cx^2}{(a + bx + cx^2)\sqrt{d + fx^2}} dx = \frac{C}{c} \int \frac{1}{\sqrt{d + fx^2}} dx + \frac{1}{c} \int \frac{Ac - aC + (Bc - bC)x}{(a + bx + cx^2)\sqrt{d + fx^2}} dx. \quad (2.17)$$

Let $q = \sqrt{(cd - af)^2 + b^2df}$, and if $b^2 - 4ac < 0$, then

$$\begin{aligned} & \int \frac{g + hx}{(a + bx + cx^2)\sqrt{d + fx^2}} dx \\ &= \frac{1}{2q} \int \frac{hbd - g(cd - af - q) + (h(cd - af + q) + gbf)x}{(a + bx + cx^2)\sqrt{d + fx^2}} dx \\ &- \frac{1}{2q} \int \frac{hbd - g(cd - af + q) + (h(cd - af - q) + gbf)x}{(a + bx + cx^2)\sqrt{d + fx^2}} dx. \end{aligned} \quad (2.18)$$

Let $u = \frac{gb - 2ah - (bh - 2gc)x}{\sqrt{d + fx^2}}$, and if $b^2 - 4ac \neq 0$, and $bh^2d - 2gh(cd - af) - g^2bf = 0$, then

$$\int \frac{g + hx}{(a + bx + cx^2)\sqrt{d + fx^2}} dx = -2g(gb - 2ah) \int \frac{1}{g(gb - 2ah)(b^2 - 4ac) - bdu^2} du. \quad (2.19)$$

If $a > 0$, and $b < 0$, then

$$\int \frac{1}{\sqrt{a+bx^2}} dx = \frac{\sin^{-1}\left(\frac{\sqrt{-bx}}{\sqrt{a}}\right)}{\sqrt{-b}}. \quad (2.20)$$

If $\frac{a}{b} > 0$, then

$$\int \frac{1}{a+bx^2} dx = \frac{\sqrt{\frac{a}{b}} \tan^{-1}\left(\frac{x}{\sqrt{a/b}}\right)}{a}. \quad (2.21)$$

If $\frac{a}{b} < 0$, then

$$\int \frac{1}{a+bx^2} dx = \frac{\sqrt{-\frac{a}{b}} \tanh^{-1}\left(\frac{x}{\sqrt{-a/b}}\right)}{a}. \quad (2.22)$$

After applying these rules in Mathematica® and simplifying, the vortex-induced rolling moment coefficient can be written as,

$$C_{lv} = \frac{K_{lv}}{2B} \sum_{j=1}^4 \left\{ (-1)^j I_j \left[(\pi - 2B\Omega) I_j + \sqrt{B^2 + I_j^2} \left(2\Omega \tanh^{-1}\left(\frac{B}{\sqrt{B^2 + I_j^2}}\right) I_j - \pi \right) \right] \right\}, \quad (2.23)$$

where,

$$I_j = \sqrt{\left[(\bar{Y}_F - (-1)^j \bar{s}) \sin(\Phi) - \bar{Z}_F \cos(\Phi) \right]^2 + \bar{r}_c^2} + i \left[\cos\left(\frac{j\pi}{2}\right) + \sin\left(\frac{j\pi}{2}\right) \right] \left[(\bar{Y}_F - (-1)^j \bar{s}) \cos(\Phi) + \bar{Z}_F \sin(\Phi) \right]. \quad (2.24)$$

Complex numbers have been used to condense Eq. (2.23)-(2.24). An equivalent but less elegant form with only real terms can be obtained by using the conversion formulae, e.g.,

$$\tanh^{-1}(z) = \frac{1}{2} \left[\ln(1+z) - \ln(1-z) \right], \quad \ln(z) = \ln(r) + i\theta, \quad \text{and } z = x + iy = re^{i\theta} = r(\cos(\theta) + i \sin(\theta)).$$

The modified vortex-induced lift coefficient with elliptical loading is given by,

$$C_{Lv} = K_{Lv} \int_{-B}^B \left(1 - \Omega |\bar{y}| \right) \sqrt{1 - \left(\frac{\bar{y}}{B}\right)^2} \left(\frac{\bar{y} + C_1}{(\bar{y} + C_1)^2 + A_1^2} - \frac{\bar{y} + C_2}{(\bar{y} + C_2)^2 + A_2^2} \right) d\bar{y}. \quad (2.25)$$

An analytical expression can be found for the lift coefficient by using the same substitution rules described earlier in Eq. (2.14)-(2.22),

$$C_{Lv} = \frac{K_{Lv}}{2B} \left[4(\pi - 2B\Omega) \bar{s} \cos(\Phi) + i \sum_{j=1}^4 \left[\cos\left(\frac{(j+1)\pi}{2}\right) + \sin\left(\frac{(j+1)\pi}{2}\right) \right] \sqrt{B^2 + I_j^2} \cdot \left(2\Omega \tanh^{-1}\left(\frac{B}{\sqrt{B^2 + I_j^2}}\right) I_j - \pi \right) \right] \quad (2.26)$$

where, I_j is defined as in Eq. (2.24), and K_{L_v} is given by:

$$K_{L_v} = -\frac{2C_{L_G} C_{L_{\alpha F}} V_G}{\pi^2 (AR)_G (b_F / b_G) (1 + \lambda_F) V_F}. \quad (2.27)$$

Figures 2.2 and 2.3 show the comparison of analytical method with the results obtained using numerical integration for the vortex-induced rolling moment and lift coefficients, respectively.

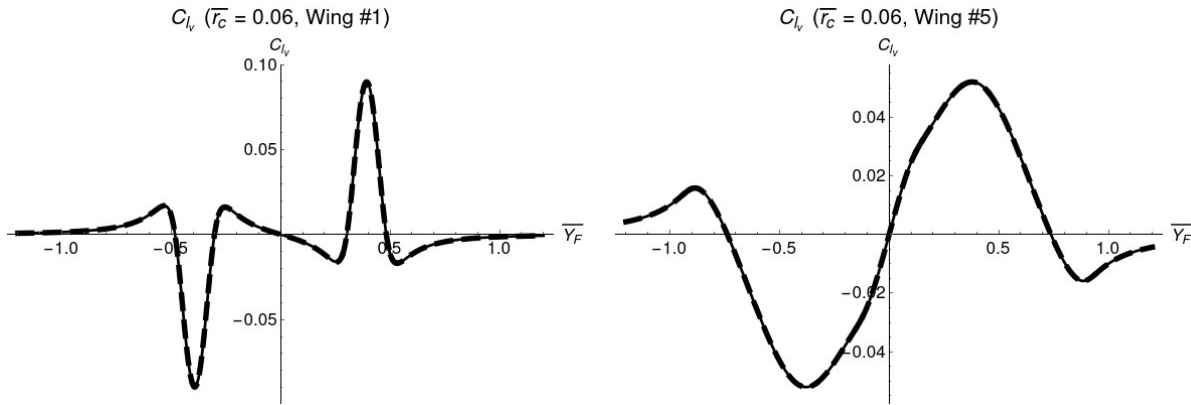


Figure 2.2: Comparison of vortex-induced rolling moment coefficient using analytical method and numerical integration. Dashed line denotes the results obtained using numerical integration and the solid line denotes the analytical solution. Results are shown for the two different wings used in the wind tunnel test.

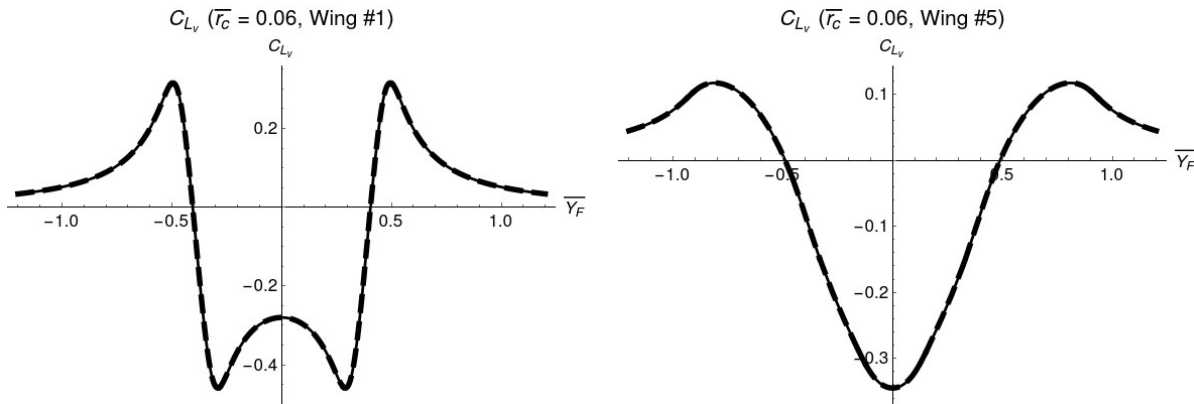


Figure 2.3: Comparison of vortex-induced lift coefficient using analytical method and numerical integration. Dashed line is used for numerical integration and solid line for the analytical solution. Results are shown for the two different wings used in the wind tunnel test.

Summary

A computationally efficient analytical solution for the modified Bowles-Tatnall method has been derived. The computational efficiency of the method will be valuable in performing wake turbulence risk mitigation and safety analyses of newly proposed air traffic management concepts and procedures. These analyses require a significant amount of computations based on large generator-follower matrices of aircraft. It can be also used on the flight deck for advanced future operations such as dynamic self-separation of aircraft.

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14. ABSTRACT Wake vortex spacing standards constrict the terminal area throughput and impose severe constraints on the overall capacity and efficiency of the National Airspace System. For more than two decades starting in the early 1990s, the National Aeronautics and Space Administration conducted extensive research on characterizing the formation and evolution of aircraft wakes. This multidisciplinary work included comprehensive field experiments (Pruis et al. 2016), flight tests (Vicroy et al. 1998), and wind tunnel tests (Rossow 1994; Chow et al. 1997). Parametric studies using large eddy simulations (Proctor 1998; Proctor et al. 2006) were conducted in order to develop fast-time models for the prediction of wake transport and decay (Ahmad et al. 2016). Substantial effort was spent on the formulation of acceptable vortex hazard metrics (Tatnall 1995; Hinton and Tatnall 1997). Several wake encounter severity metrics have been suggested in the past, which include the wake circulation strength, vortex-induced rolling moment coefficient (Clv), bank angle, and the roll control ratio (Tatnall 1995; Hinton and Tatnall 1997; Van der Geest 2012). The vortex-induced rolling moment coefficient introduced by Bowles and Tatnall (Tatnall 1995; Gloudemans et al. 2016) has been used extensively for risk and safety analysis of newly proposed air traffic management concepts and procedures. The original method of Bowles and Tatnall assumed a constant wing loading (the wing lift-curve slope, CLa is constant), which resulted in an overestimation of the vortex-induced rolling moment coefficient.					
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