



# Welcome





# Estimating Static Equivalent Load Factors from Interface Force Response Results using a Finite Element Analysis Approach in the Frequency Domain

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# Overview

## Problem:

- It is difficult to produce vector sums of interface forces in random response analyses because of the need to track positive and negative signs.
  - *Power Spectral Density (PSD) values are (positive) squared results.*
- The traditional approach rigidizes interfaces using a Rigid Body Element (RBE).
  - *Rigidizing the interface is desired for shaker tests.*
  - *Rigidizing the interface is not desired for system analyses of flight like assemblies.*

## Goal:

- To compare two methods of creating a Center of Gravity (CG) load factor using interface forces in the frequency domain.
  - *The traditional base drive approach is to excite from one grid ID and recover the forces from a single element.*
  - *The generalized method is to recover the interface forces at multiple interface locations using relative displacements.*

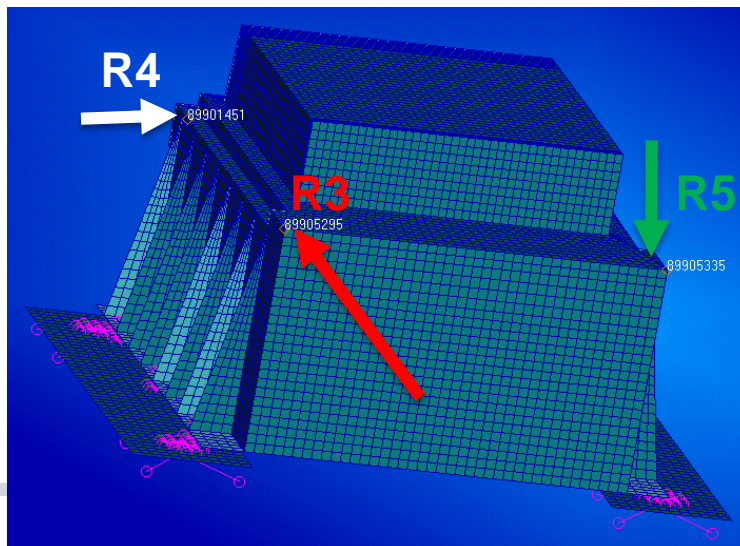
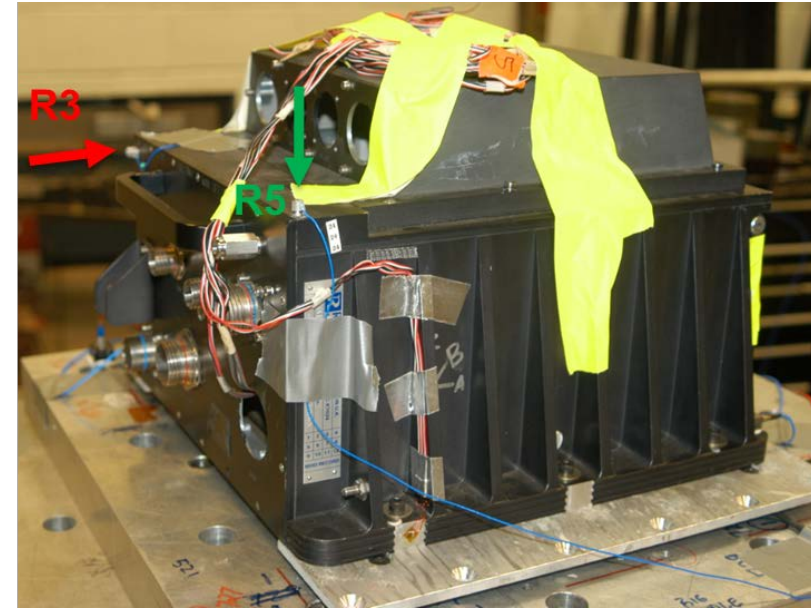


# Agenda

- Map Shaker Test Response Measurements To FEM
- Finite Element Model (FEM) Assumptions/Approach to Shaker Simulation
- FEM Simulation (Traditional Approach)
- FEM Simulation (Generalized Approach)
- Generalized Approach Verification (for Shaker Test Case Simulation)
- Forward Work - Evaluate and Report system response using Generalized Approach
- Conclusions

# Map Shaker Test Response Measurements To FEM

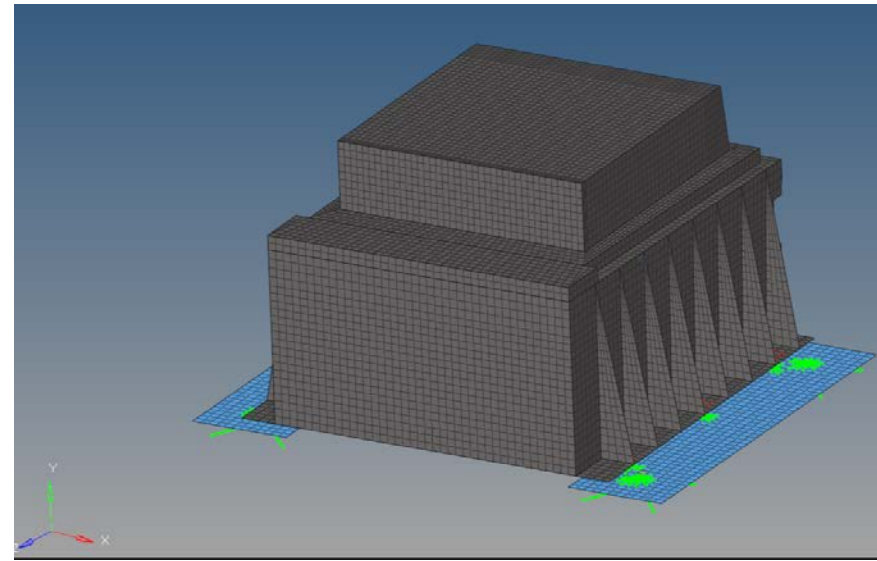
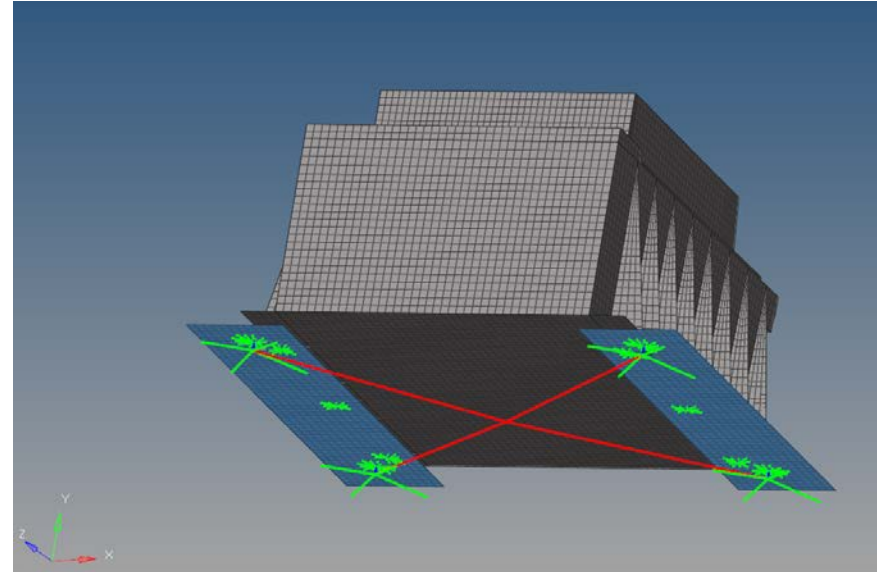
- A flight like avionics box was excited to random vibration inputs.
- Vibration responses were measured by three uni-axial accelerometers.
  - *One for each drive direction*
  - *R5 is featured in excitation cases normal to the box*
- An FEM was created to compare results to the test.





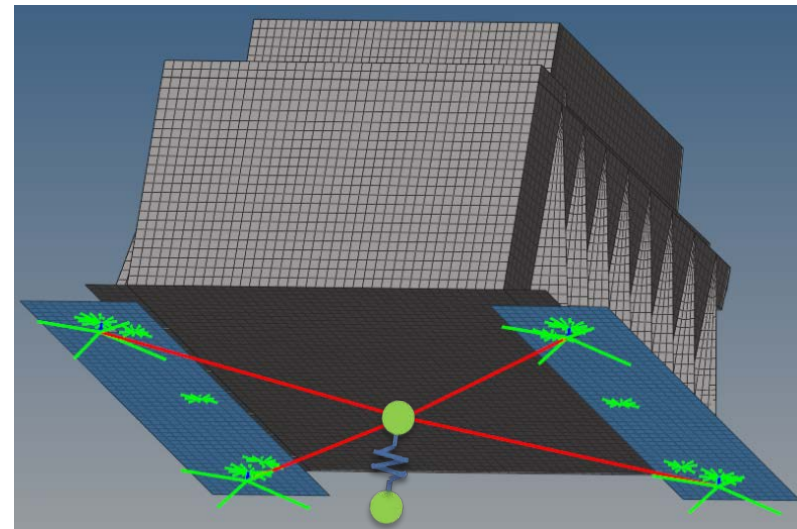
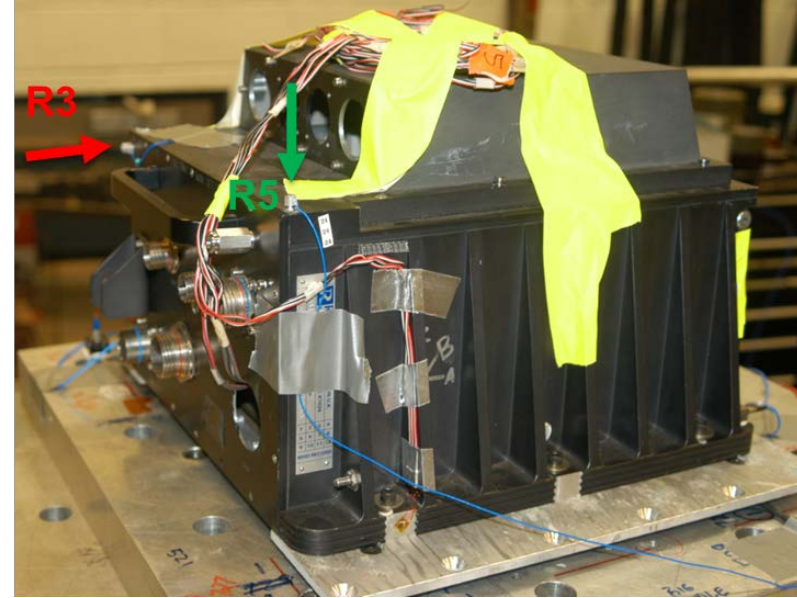
# FEM Assumptions/Approach Shaker Simulation

- Weight: 52.4 lbs
- $Q = 9.1$  (5.5 % Critical Damping)
  - *Adjust damping to reasonably simulate the development testing results.*
- Use an FEM with reasonable Multiple Degree of Freedom (MDOF) detail.
- Set up a tuned base drive response study of the Avionics Box.
- Recover interface reactions as forces.
  - *Force Spectral Density, Root Mean Squared (RMS) Force.*
  - *Use broadband reaction forces to develop equivalent static load factors (20-2000 Hz).*
  - $F = ma = \text{Weight (lb)} * \text{Load Factor (g)}$
  - *Random Vibration Loads at NASA/MSFC are calculated using 3-sigma standard deviation.*
- Applying the static load factor to FEM produces the same net interface force as the dynamic solution.



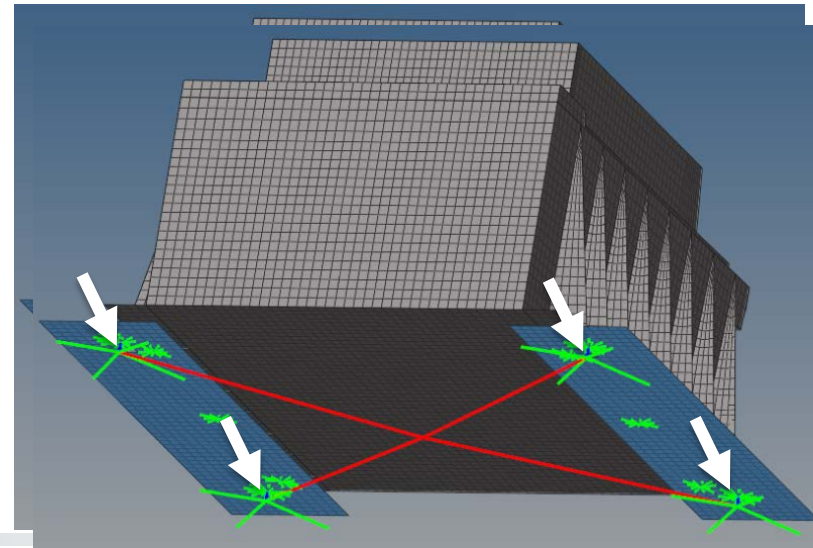
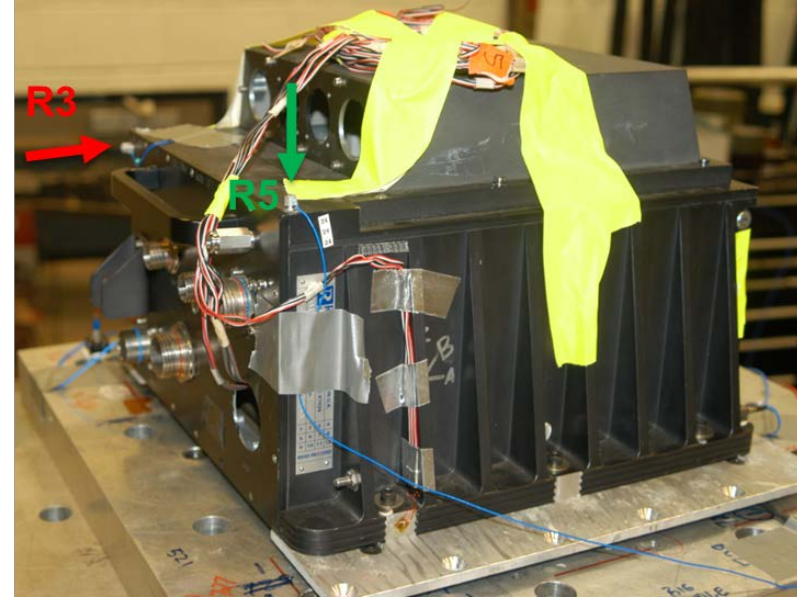
# FEM Simulation (Traditional Approach)

- Use of massive, high impedance fixtures and enforcing piston like translational motion in the test lab makes simulation easier.
- The traditional approach:
  - *Excitation forces can be applied using an RBE2 which rigidizes the interface bolt locations in 6 DOF is an appropriate assumption for the base drive shaker test.*
  - *In this approach we can recover the total interface forces from a single spring element and redundant node at the central independent grid location for the RBE2.*
  - *Use FEM with reasonable MDOF detail.*
- The traditional approach rigidizes interfaces and this would not be desired in a system analysis of a flight like assembly.



# FEM Simulation (Generalized Approach)

- Instead of recovering the forces from the centrally located spring, relative displacements were recovered at each of four interface locations.
- The relative displacements were used to calculate interface forces at each of the four interface locations.
- Afterward the vector sum of the interface forces was determined for each mode shape.
- In the end, the RMS interface forces were determined in a similar way to the traditional approach from the broadband response of the net interface forces.
- White arrows denote relative deflection recovery locations used in MPC equations. The displacement difference between coincident nodes is calculated at 4 interface locations.







# FEM Simulation (Generalized Approach)

Working with SPOINTS and MPCs to store Relative Displacements and calculate Net Interface Forces

```

• $2345678$2345678$2345678$2345678$2345678$2345678$2345678$2345678
• MPCADD 10 300001 300002 300003 300004 300005
• $***1***$***2***$***3***$***4***$***5***$***6***$***7***$***8***$***9***$***10***
• SPOINT 200001 200002 200003 200004 200005
• $***1***$***2***$***3***$***4***$***5***$***6***$***7***$***8***$***9***$***10***

```

```

• MPC 300001 200001 1 -1.0 900024812 1.0
• 900003132 -1.0
• MPC 300002 200002 1 -1.0 900024802 1.0
• 900003162 -1.0
• MPC 300003 200003 1 -1.0 900017732 1.0
• 900003152 -1.0
• MPC 300004 200004 1 -1.0 900017762 1.0
• 900003142 -1.0
• $
• MPC 300005 200005 1 -1. 200001 1 1.E8
• 200002 1 1.E8 200003 1 1.E8
• 200004 1 1.E8

```

Equations 1 through 4 store relative deflections:

- Calculated for each interface spring
- Determined in the drive direction
- Corresponding SPOINT Scalar storage location

The 5<sup>th</sup> Equation Provides:

- The vector Sum of the Forces in the drive direction

# FEM Simulation (Generalized Approach)



Working with SPOINTS and MPCs to store Relative Displacements and calculate Net Interface Forces

Equations 1 through 4 store relative deflections:

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- Determined in the drive direction
- Corresponding SPOINT Scalar storage location

$$\begin{aligned} S_{200001} &= -[U_{90002481}^2 - U_{90000313}^2] && (300001) \\ S_{200002} &= -[U_{90002481}^2 - U_{90000313}^2] && (300002) \\ S_{200003} &= -[U_{90002481}^2 - U_{90000313}^2] && (300003) \\ S_{200004} &= -[U_{90002481}^2 - U_{90000313}^2] && (300004) \end{aligned}$$

The 5<sup>th</sup> Equation Provides:

- The vector Sum of the Forces in the drive direction

$$U = \text{Displacement} \begin{bmatrix} U \text{ direction} \\ \text{node id} \end{bmatrix}$$

$$S_{200005} = -[(1.0 \times 10^8)S_{200001} + (1.0 \times 10^8)S_{200002} +$$



# FEM Simulation (Generalized Approach)

Working with SPOINTS and SPCs to store Relative Displacements and calculate Sum of the Interface Forces

- NASTRAN Provides the Modal SPOINT Stored Result of MPC Equations

Notice 5 S Values are given for each mode corresponding to the number of SPOINTS we specified (not the DOF direction)

EIGENVALUE = 4.817140E+06  
CYCLES = 3.493130E+02 REAL EIGENVECTOR NO. 1

POINT ID.	TYPE	T1	T2	T3	R1	R2	R3
200001	S	5.1290850E-03	-5.4028140E-03	-5.0572730E-03	5.5583820E-03	2.2738030E+04	
89898387	G	2.6419700E-02	-3.0772690E+00	2.4324770E-01	4.7854010E-01	-1.2574830E-02	-1.1625890E-01
89898413	G	2.8900490E-02	2.7703850E+00	2.4504700E-01	4.9861470E-01	1.6007990E-02	-1.0554770E-01
89901451	G	2.9918510E+00	-8.1665870E-02	2.1155750E+00	1.0726280E-02	4.4485650E-01	-2.0338290E-02
89905295	G	3.2222130E+00	-5.3658200E-02	-3.2379330E+00	-1.0075900E-02	4.4238290E-01	-8.8893540E-03
89905335	G	3.2294870E+00	-4.8981750E-02	-3.1454500E+00	2.2788360E-02	4.4267460E-01	8.0113650E-03

- But the user must relate these to the ascending SPOINT ID

Frequency [Hz]	Mode	SPOINT 200001 [in]/unit	SPOINT 200002 [in]/unit	SPOINT 200003 [in]/unit	SPOINT 200004 [in]/unit	SPOINT 200005 [lb]/unit
349.3	1	0.0051	-0.0054	-0.0051	0.0056	22738.0
406.8	2	0.0054	0.0049	0.0051	0.0059	2133910.0
443.9	3	0.0069	0.0063	-0.0065	-0.0070	-30279.4
456.9	4	-0.0040	-0.0035	-0.0027	-0.0034	-1368776.0
892.9	5	0.0005	-0.0002	-0.0002	0.0006	72975.3

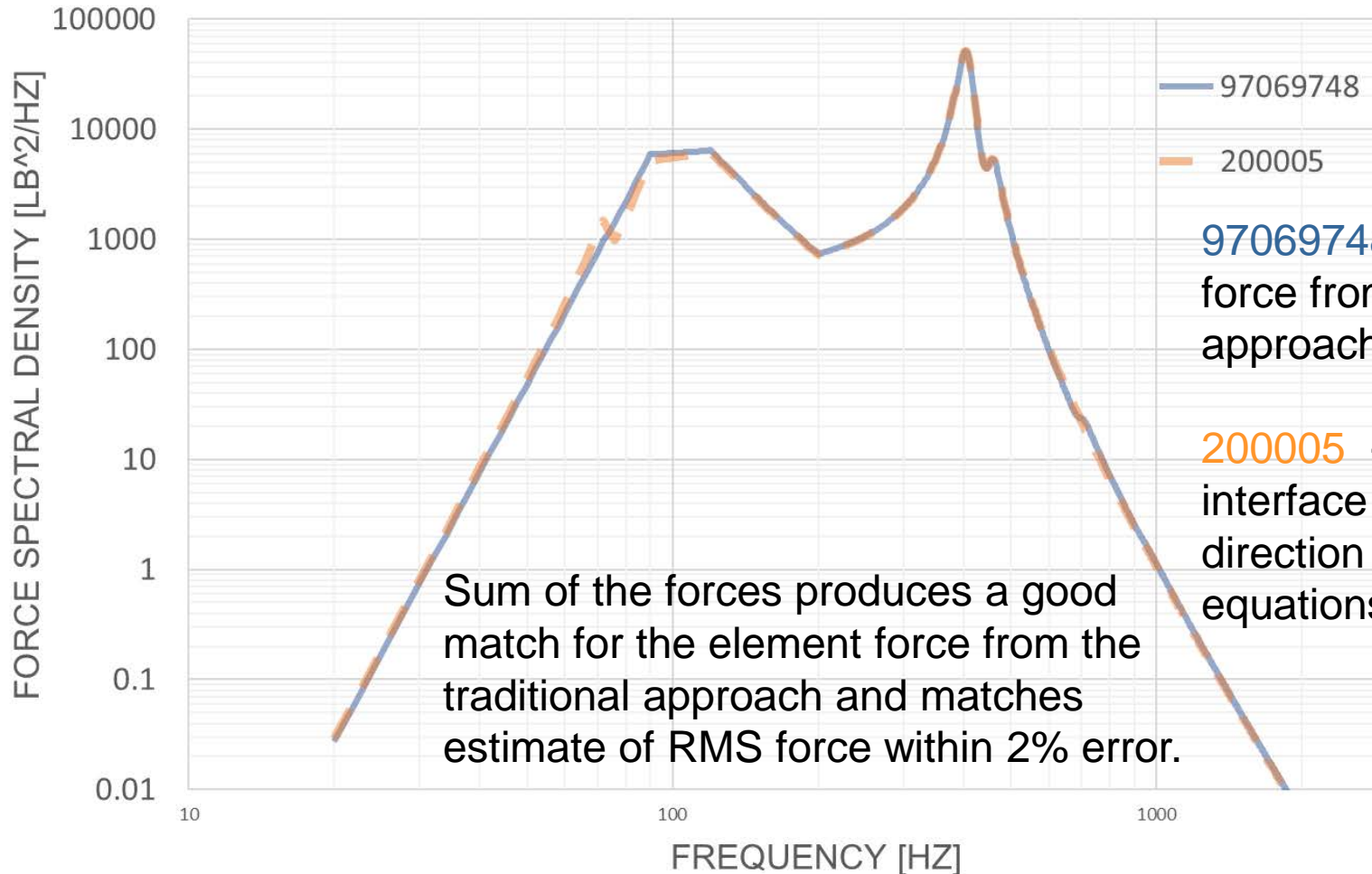
The 5<sup>th</sup> Equation Provided the Sum of the forces in the drive direction of the Sol 111 for each mode.

# Generalized Approach Verification (for Shaker Test Case Simulation)



Comparing Two Analysis Approaches to determine the total interface force:

Model Y-direction Response to Excitation in Y (Normal)



**97069748** - The element force from the traditional approach

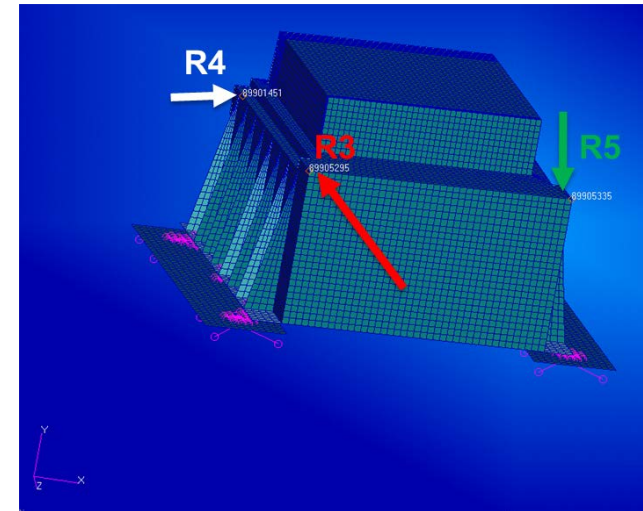
**200005** - Sum of the interface forces in Normal direction from MPC equations



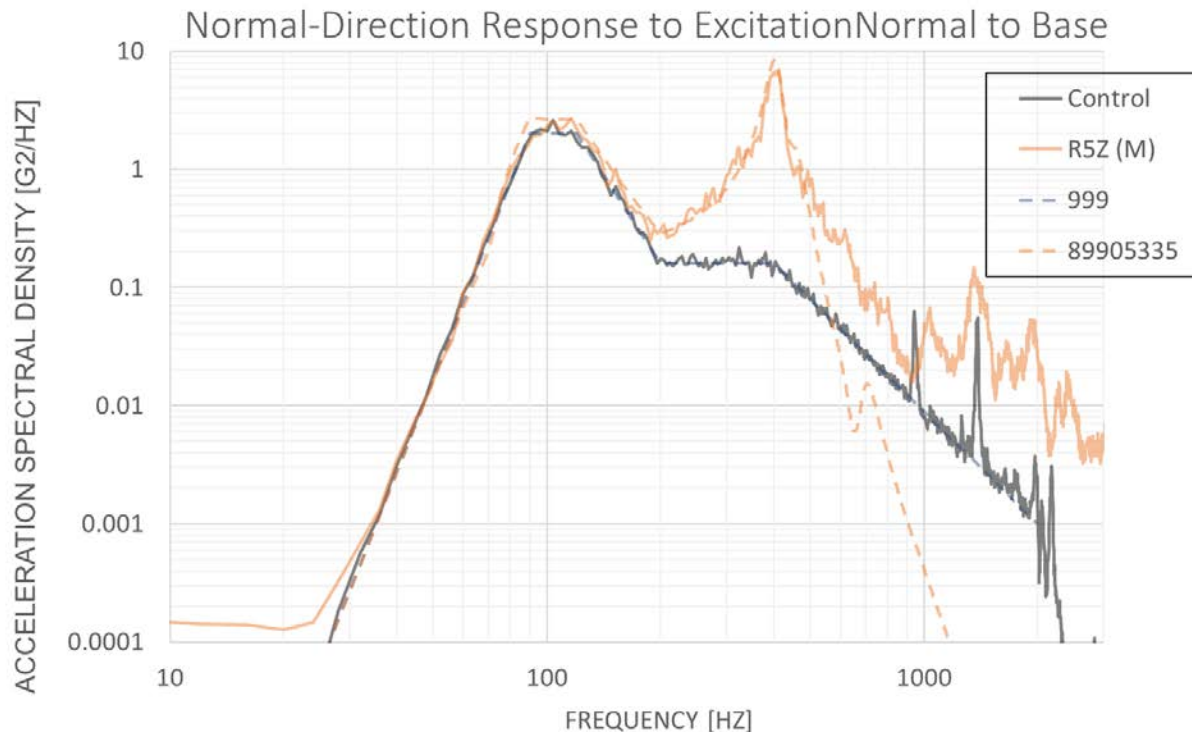
# Base Drive Response Verification

*Comparing Acceleration PSD from Test to analysis Simulation*

- Solid lines are processed test measurements.
- Dashed lines are NASTRAN solution 111 FEM results for nodes at response accelerometer locations.



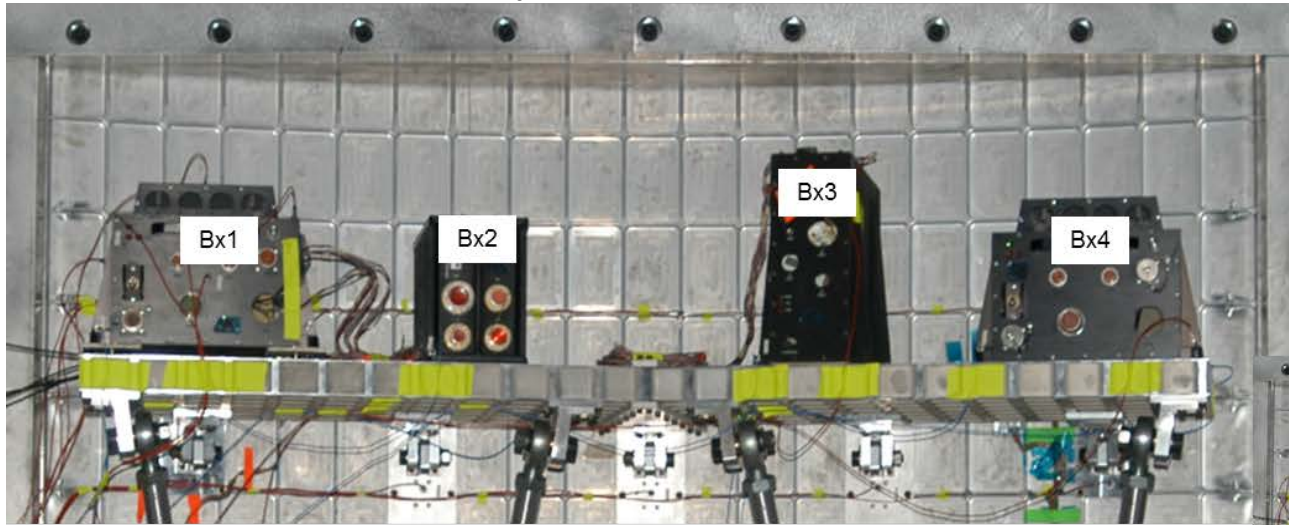
- Grid ID 999 corresponds to the drive location in the FEM.
- Grid ID 89905335 corresponds to the R5 uniaxial response measurement location as represented by the FEM.



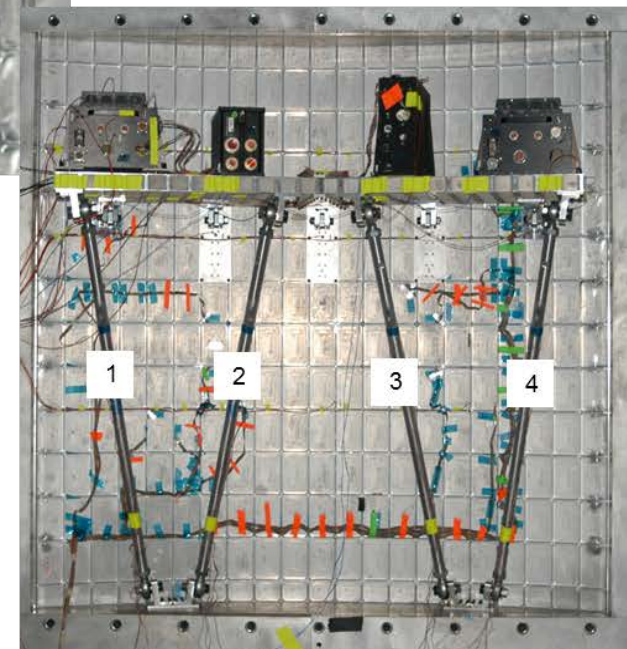
# Forward Work - Evaluate and Report System Response Using Generalized Approach



## a) System Test



## b)



- During Test 1 a set of 4 Tri-Axial Force Transducers were Located at the Base of Box 1.
  - *Figure a) Presents the Box Designations.*
  - *Figure b) Presents the Strut Numbering.*

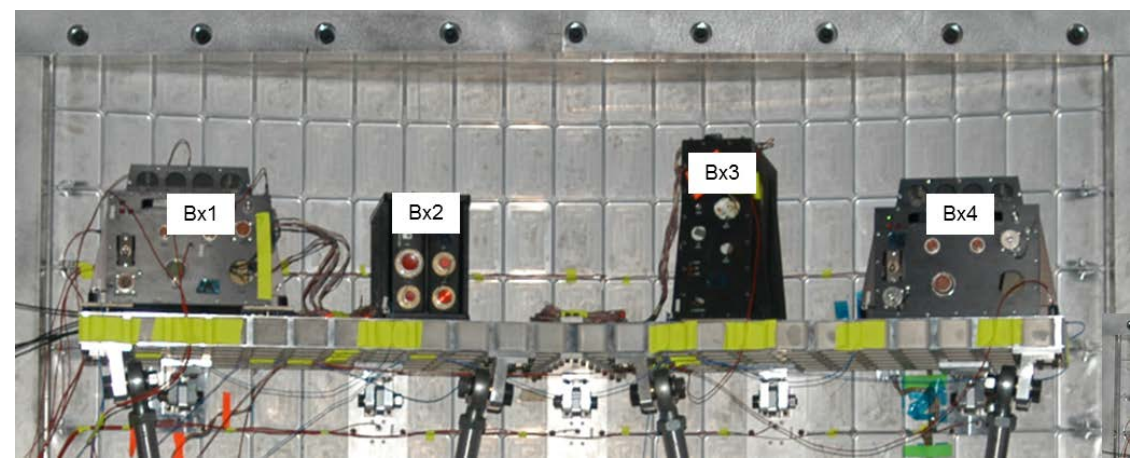
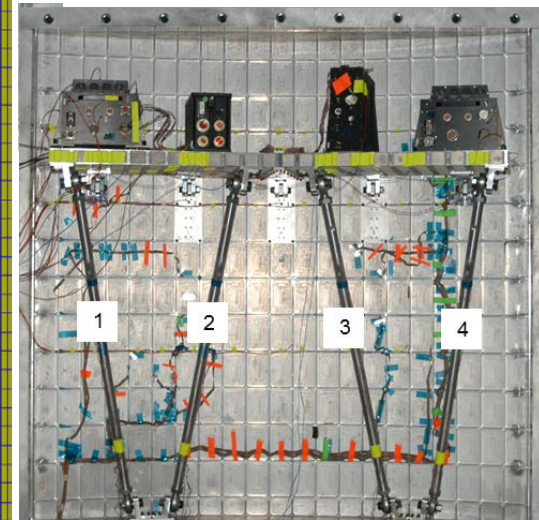
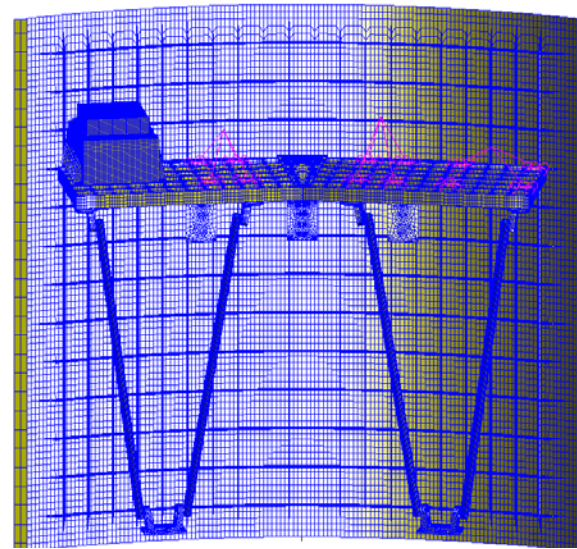


# Forward Work - Evaluate and Report Using Generalized Approach



## *Intro: System Test Configuration and FEM Simulation*

- The Generalized Approach can be implemented within a system model response solution. Response provides interface forces and/or moments in 3 orthogonal axes.
- Provides an estimate of “Net CG Acceleration” suitable for development of 3 sigma load factor.
- Does not require the interface to be stiff or have high impedance.
- Reporting on a system level response solution is to be the subject of future work.

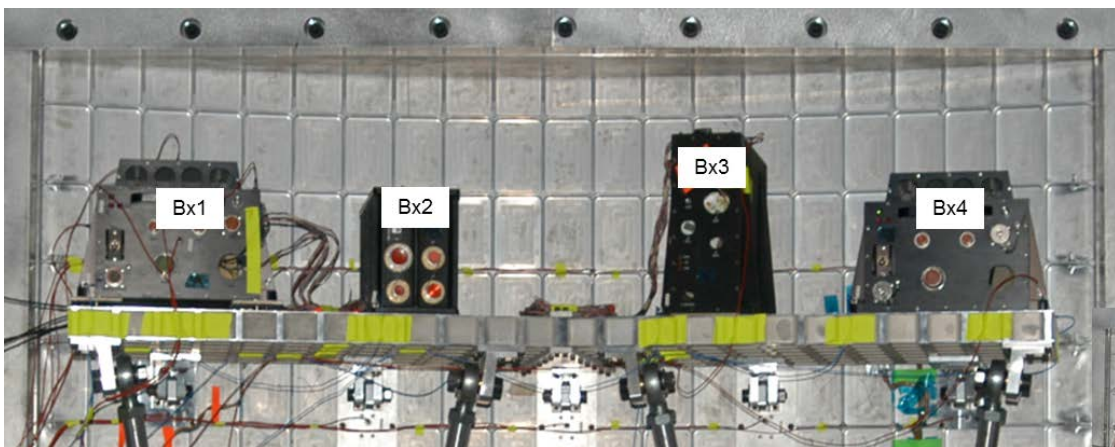
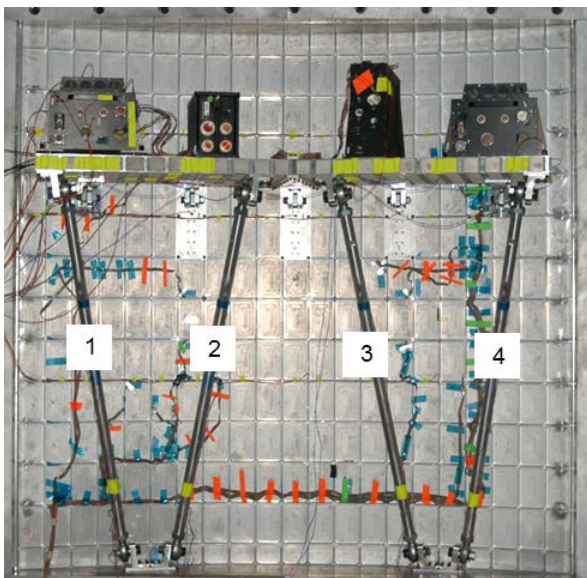
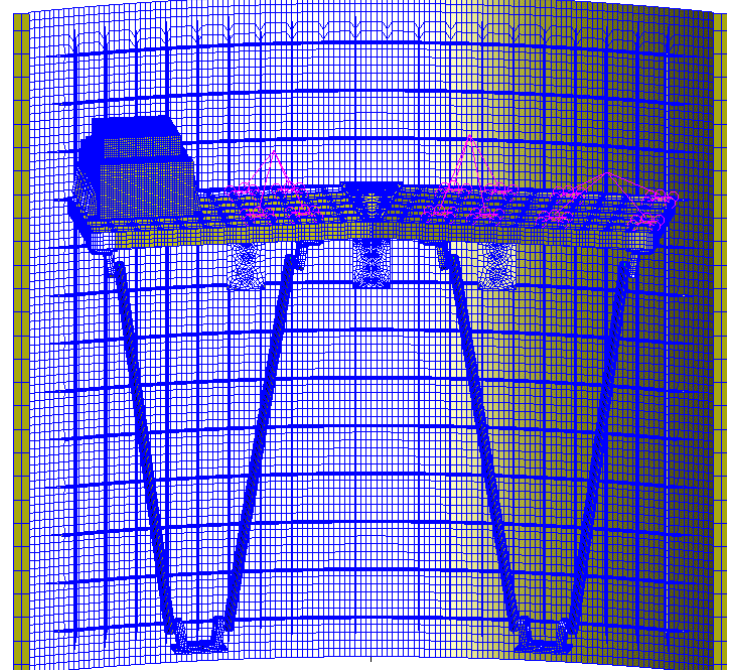


# Forward Work - Evaluate and Report Using Generalized Approach



## *Intro: System Test Configuration and FEM Simulation*

- Use of an RBE2 to rigidize the interface underneath the box is not desired for the flight-like system FEM simulation.
- Therefore the Traditional approach to recover net interface forces is not viable.
- The Generalized approach is recommended.







# Conclusions

- We illustrated the recovery of net interface forces for a traditional single direction base shake simulation.
- The Generalized approach for the recovery of net interface forces was also demonstrated and compared very favorably with the Traditional result.
  - *The Generalized approach has promise for removing conservatism from Equivalent Static Load Factors.*
  - *The Generalized recovery can be derived from system FEM response analyses without over-stiffening the component to backup structure interface.*
  - *The Generalized recovery can be implemented without over-rigidizing the flight-like interface backup structure of the system response FEM.*
- Future work will validate this for system response recoveries from measured test response (Part 2).

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Thank you







# Backup Slides

## Equations for Generalized Approach with System FEM

# Generalized Approach For the System FEM Response



*Working with SPOINTS and SPCs to store Relative Displacements and calculate Sum of the Interface Forces*

```

$2345678$2345678$2345678$2345678$2345678$2345678$2345678$2345678$2345678$2345678
$***1***$***2***$***3***$***4***$***5***$***6***$***7***$***8***$***9***$***10***
SPOINT    200001    200002    200003    200004    200005    200201    200202    200203
           200204    200205    200301    200302    200303    200304    200305
$***1***$***2***$***3***$***4***$***5***$***6***$***7***$***8***$***9***$***10***
MPC       300001    200001    1          -1.0      900024812      1.0
           900003132      -1.0
MPC       300002    200002    1          -1.0      900024802      1.0
           900003162      -1.0
MPC       300003    200003    1          -1.0      900017732      1.0
           900003152      -1.0
MPC       300004    200004    1          -1.0      900017762      1.0
           900003142      -1.0
$
MPC       300005    200005    1          -1.       200001    1          1.E8
           200002    1          1.E8     200003    1          1.E8
           200004    1          1.E8
$ in the example
$   there is a range of IDs for scalar points    200001-1001233
$   there is a range of IDs for GridPoints at CBUSH RBE Dep 3001101-100110
$   there is a range of IDs for GridPoints at CBUSH 3001201-1001210
    
```

# Generalized Approach For the System FEM Response



*Working with SPOINTS and SPCs to store Relative Displacements and calculate Sum of the Interface Forces*

```
$2345678$2345678$2345678$2345678$2345678$2345678$2345678$2345678$2345678$2345678
$***1***$***2***$***3***$***4***$***5***$***6***$***7***$***8***$***9***$***10***
SPOINT 200001 200002 200003 200004 200005 200201 200202 200203
        200204 200205 200301 200302 200303 200304 200305
$***1***$***2***$***3***$***4***$***5***$***6***$***7***$***8***$***9***$***10***
MPC    300001 200201 1          -1.0    900024811      1.0
        900003131          -1.0
MPC    300002 200202 1          -1.0    900024801      1.0
        900003161          -1.0
MPC    300003 200203 1          -1.0    900017731      1.0
        900003151          -1.0
MPC    300004 200204 1          -1.0    900017761      1.0
        900003141          -1.0
$
MPC    300005 200205 1          -1.     200201 1          1.E8
        200202 1          1.E8    200203 1          1.E8
        200204 1          1.E8
$ in the example
$   there is a range of IDs for scalar points 200001-1001233
$   there is a range of IDs for GridPoints at CBUSH RBE Dep 3001101-100110
$   there is a range of IDs for GridPoints at CBUSH 3001201-1001210
```

# Generalized Approach For the System FEM Response



*Working with SPOINTS and SPCs to store Relative Displacements and calculate Sum of the Interface Forces*

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$2345678$2345678$2345678$2345678$2345678$2345678$2345678$2345678$2345678$2345678
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SPOINT    200001    200002    200003    200004    200005    200201    200202    200203
           200204    200205    200301    200302    200303    200304    200305
$***1***$***2***$***3***$***4***$***5***$***6***$***7***$***8***$***9***$***10***
MPC       300001    200301    1          -1.0      900024813      1.0
           900003133      -1.0
MPC       300002    200302    1          -1.0      900024803      1.0
           900003163      -1.0
MPC       300003    200303    1          -1.0      900017733      1.0
           900003153      -1.0
MPC       300004    200304    1          -1.0      900017763      1.0
           900003143      -1.0
$
MPC       300005    200305    1          -1.      200301    1          1.E8
           200302    1          1.E8     200303    1          1.E8
           200304    1          1.E8
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