

Adjoint-Based Mesh Adaptation and Shape Optimization for Simulations with Propulsion

Marian Nemec

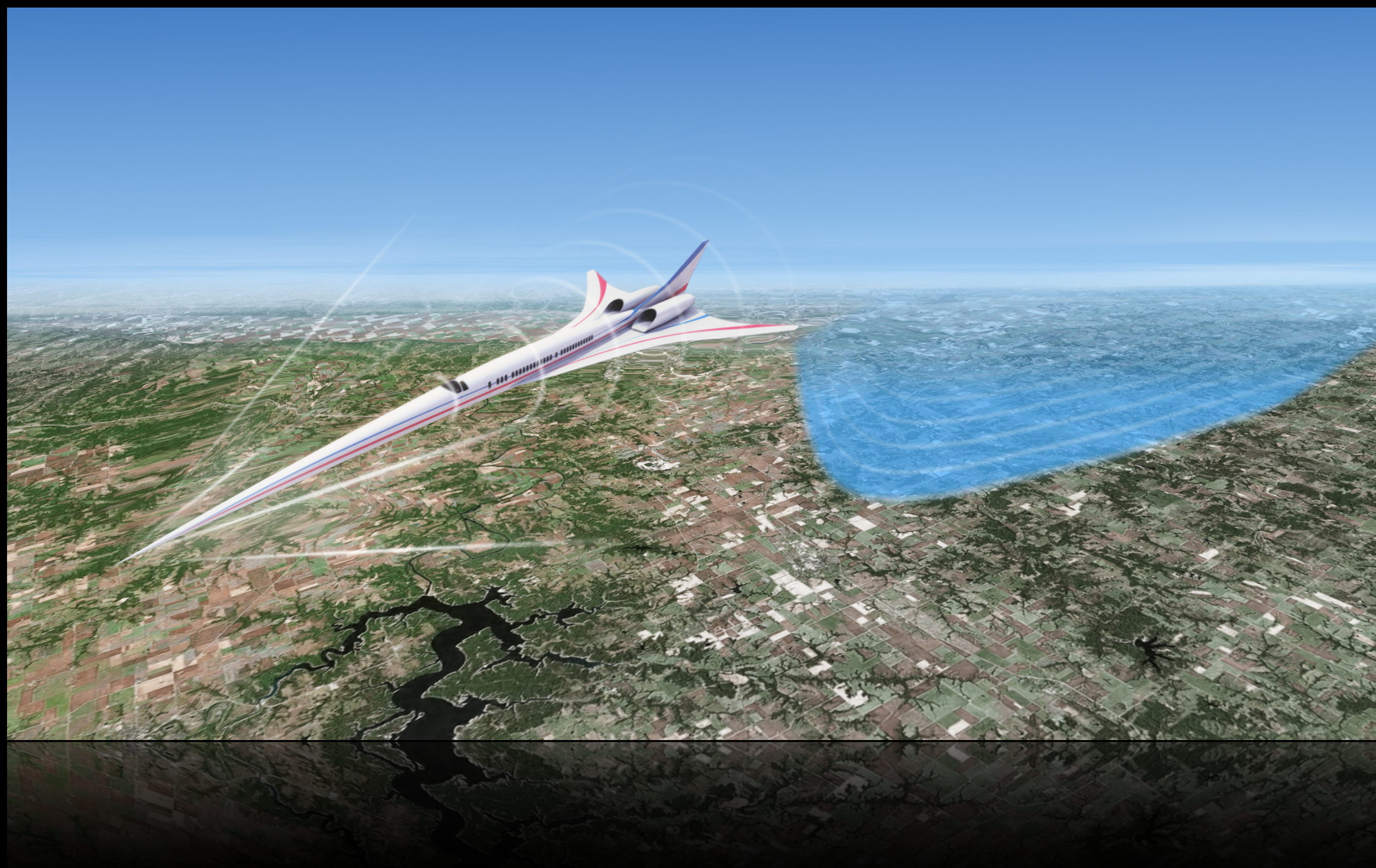
NASA Ames

David Rodriguez

Science & Technology Corp.

Michael Aftosmis

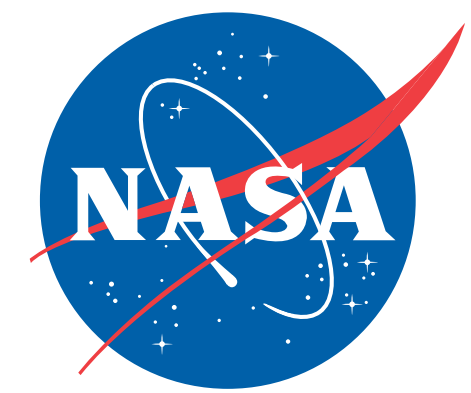
NASA Ames



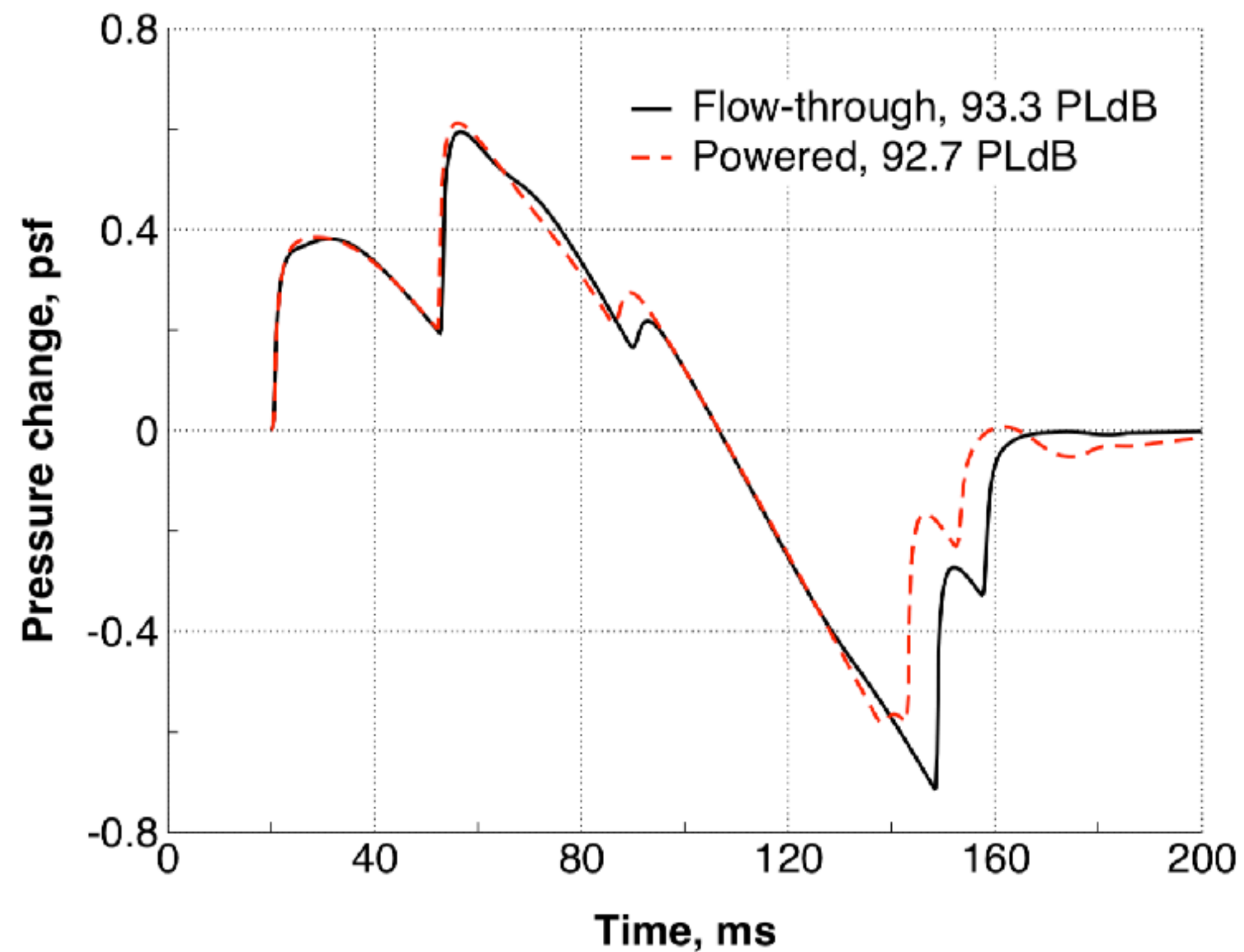
*Computational Aerosciences Branch
NASA Advanced Supercomputing Division*

Commercial Supersonic Technologies III
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June 20, Dallas, TX

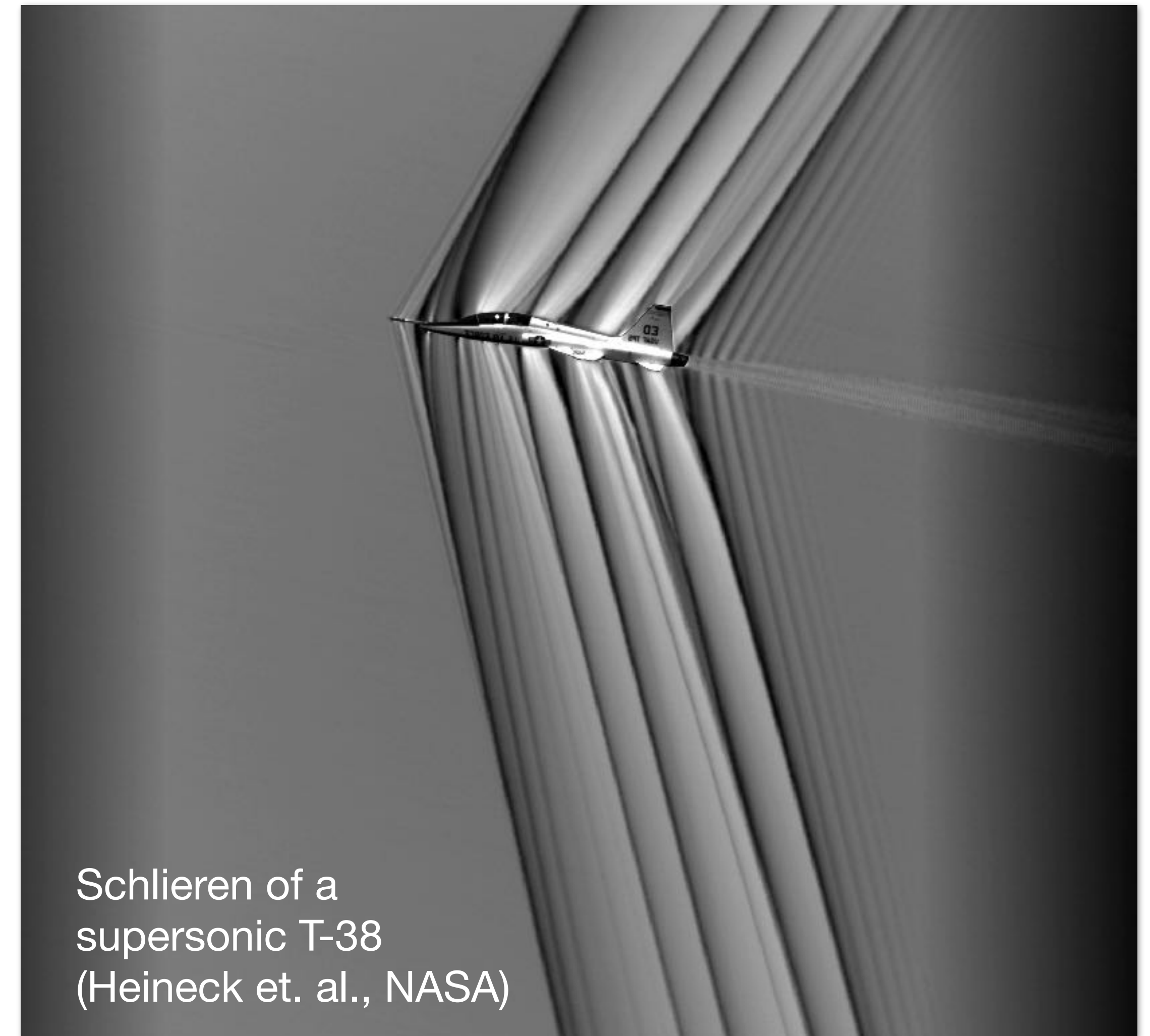




Motivation

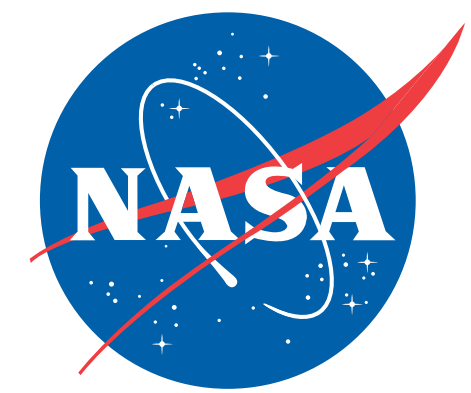


Ground pressure signature from a low drag business jet concept, $M=1.5$ (Wintzer et. al., NASA)

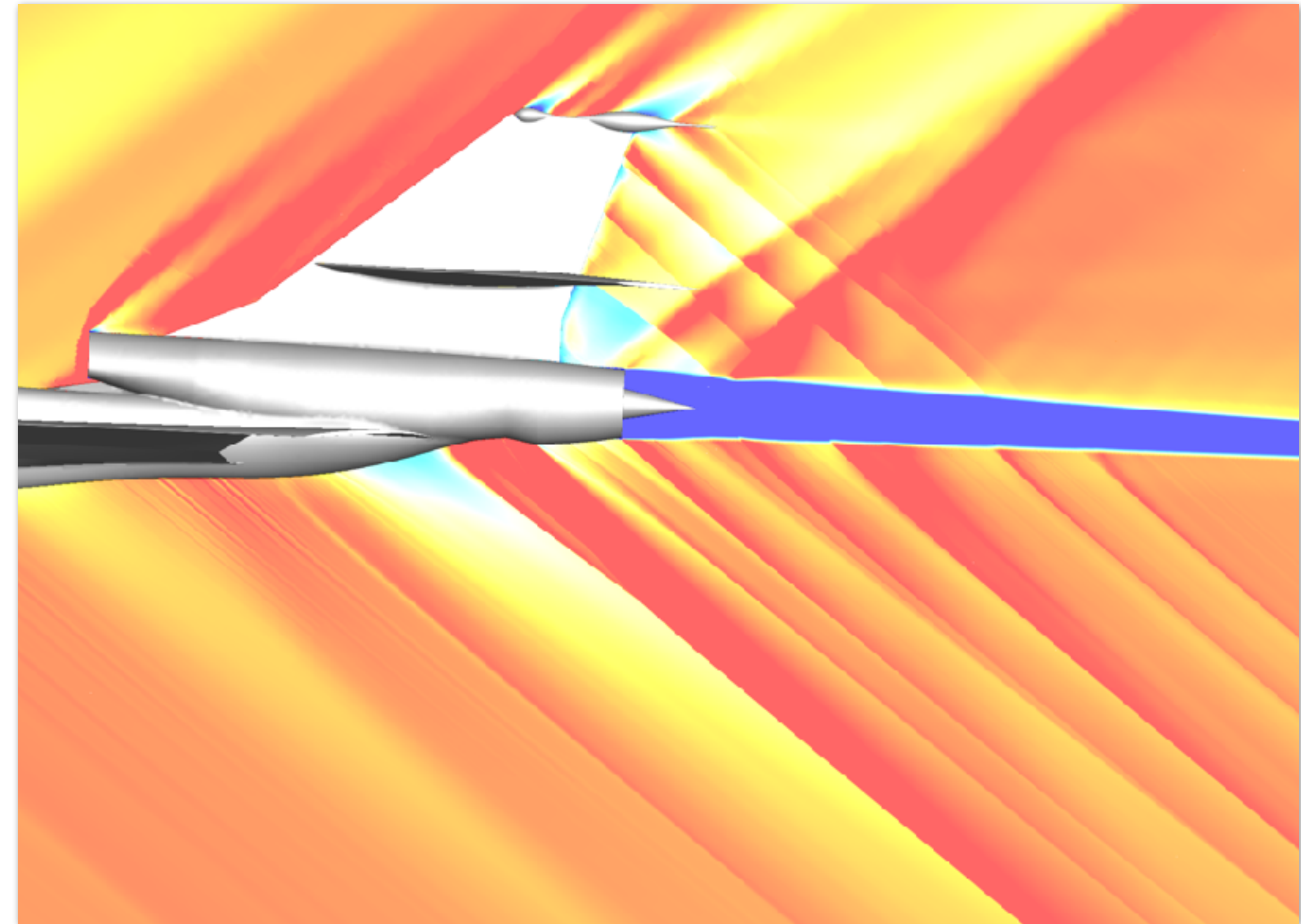
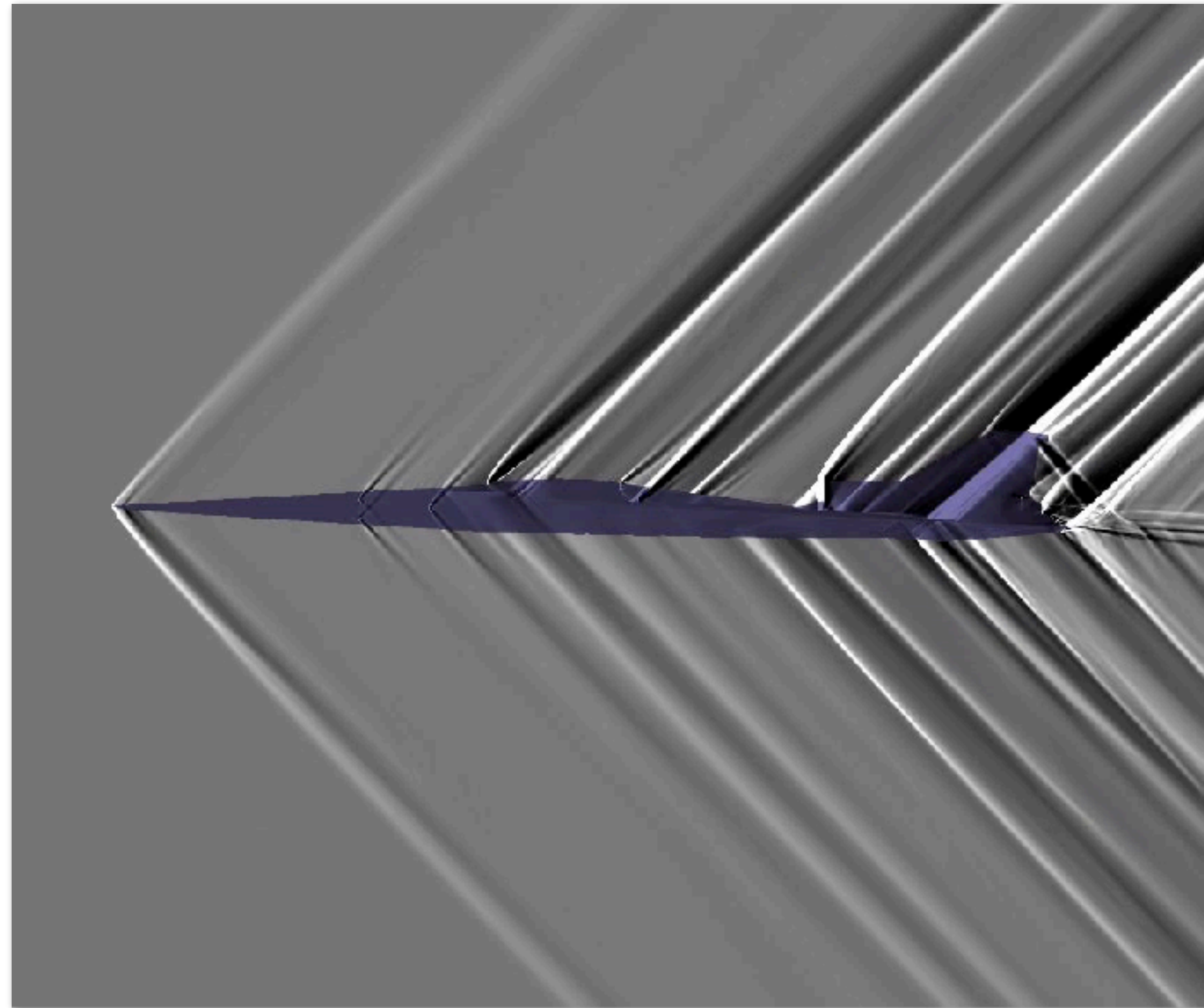
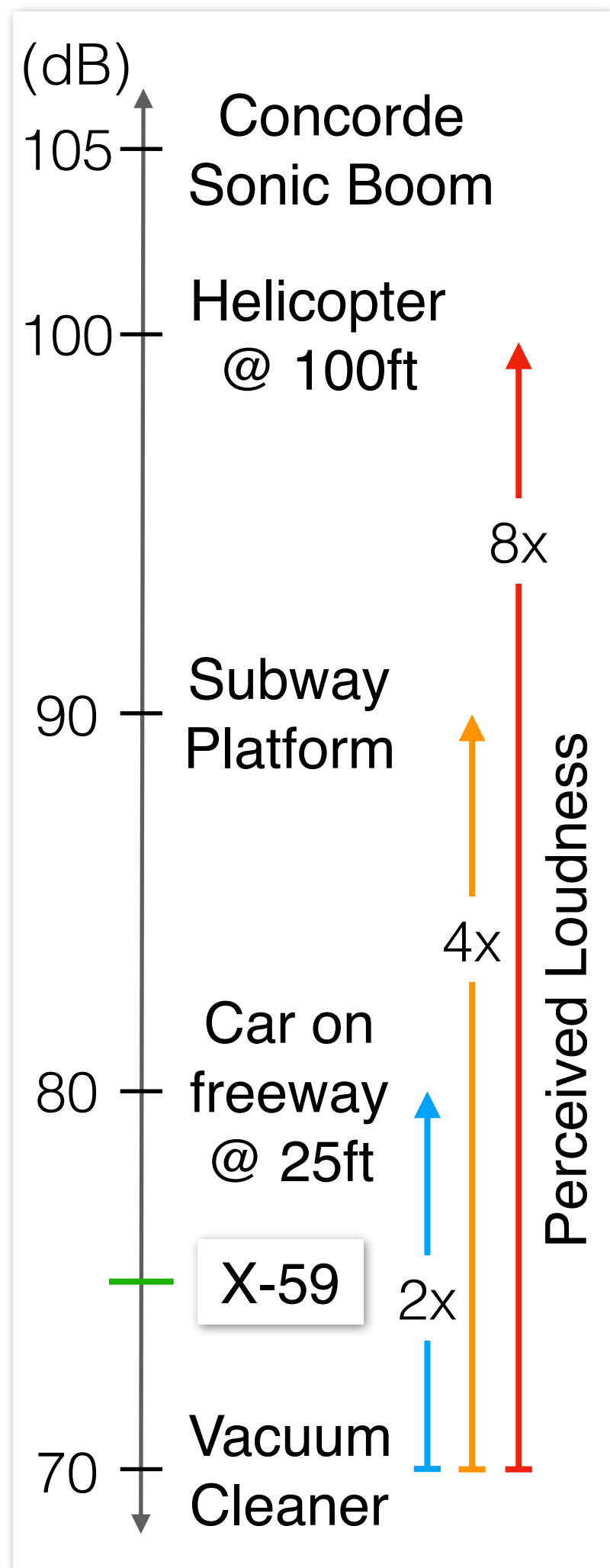


Schlieren of a supersonic T-38 (Heineck et. al., NASA)

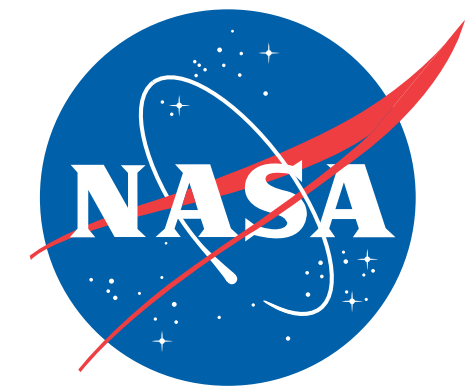
Propulsion effects are secondary when loud sonic-booms are acceptable



Low Sonic-Boom Design



- Shaped pressure signature below aircraft: many shocks, but weaker and of similar strength
- Significant influence of inlet and nozzle exhaust: aft layout critical
- Mass flow rate, stagnation pressure recovery and flow distortion important parameters



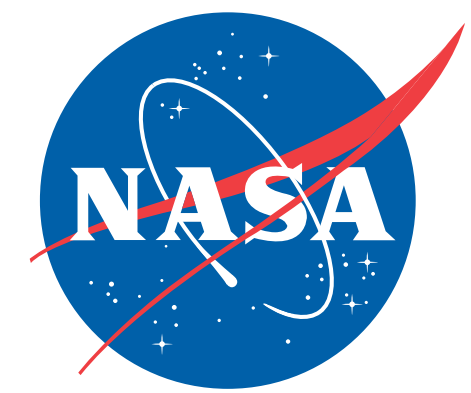
Objectives

Reliable evaluation of mass flow rates through permeable boundaries

- Estimate and control discretization error
- Consider both computational domain outflow and inflow
- Applicable to simulating propulsion-system effects, as well as secondary flow paths
- Explore feasibility of handling more general outputs at domain boundaries

Design optimization subject to mass-flow-rate constraints

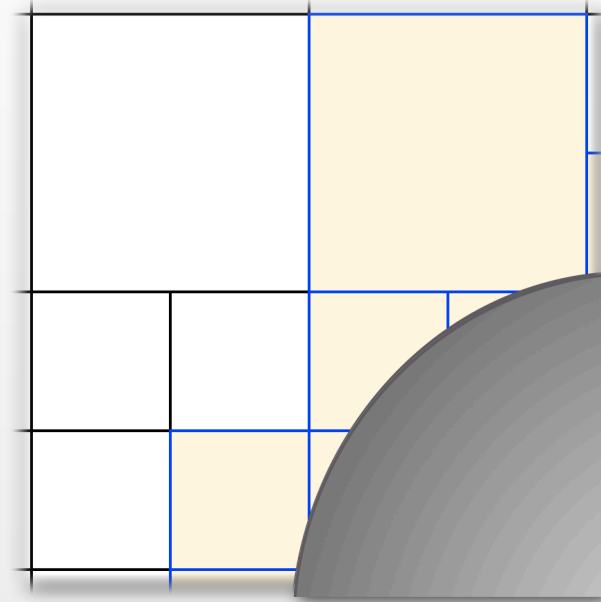
- Improve aerodynamic performance and reduce noise due to sonic boom
- Control discretization error in design space to improve confidence in final designs



Approach & Background

FLOW SIMULATION

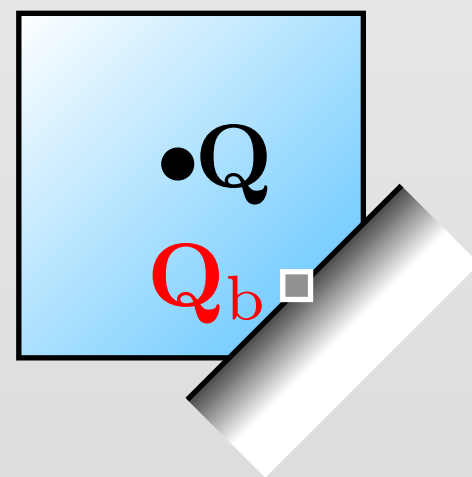
- Steady Euler equations, perfect gas
- Cartesian mesh with cut cells
- Second-order, finite-volume discretization
 - van Leer flux vector splitting
- RK4 with local time stepping, multigrid, and parallel computing



$$R_H(\mathbf{Q}_H) = 0$$

WALL BOUNDARY CONDITIONS

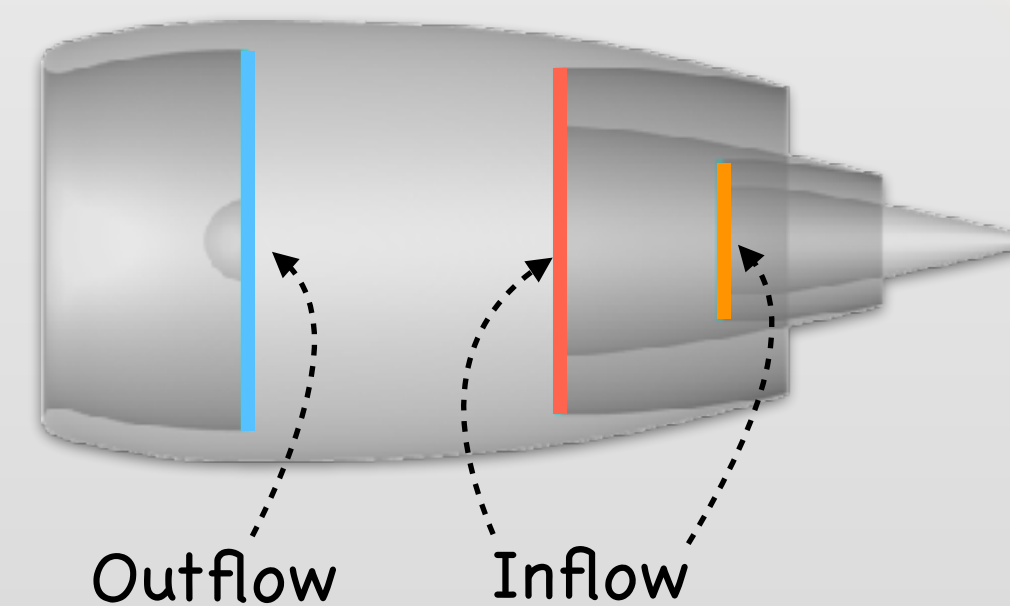
- Weakly enforced: form flux across boundary from boundary state
 - Slip wall: $U_n = 0$
 - Permeable wall: $U_n \neq 0$



$$F \cdot \hat{n} = [0, p \hat{n}, 0]^T$$

OUTPUTS OF INTEREST

- Aerodynamic force and moment coefficients
- Pressure at a point or along a line, equivalent area distribution
- Mass flow rates

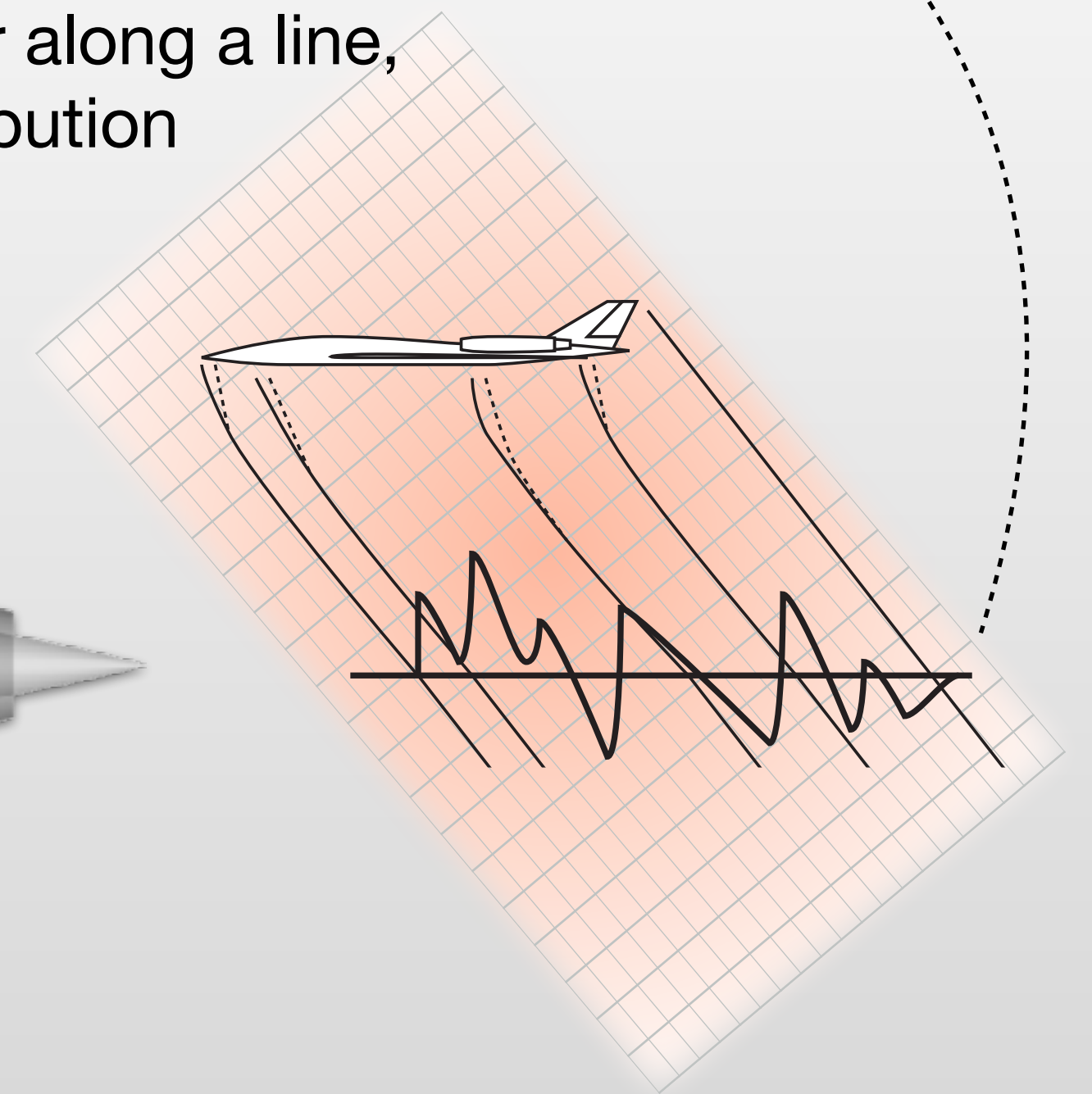


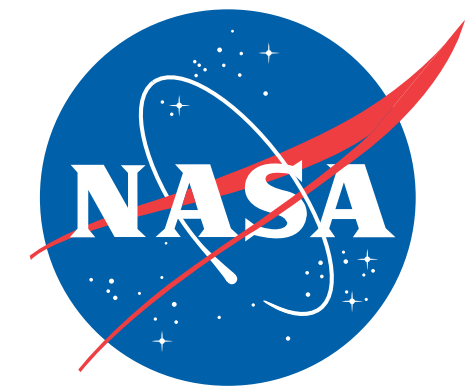
Outflow

Inflow

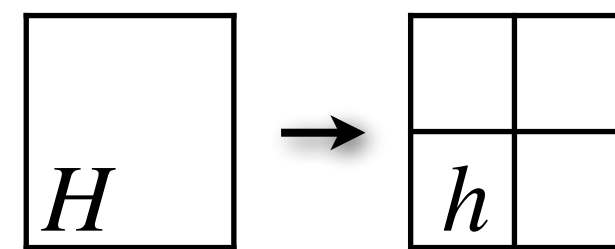
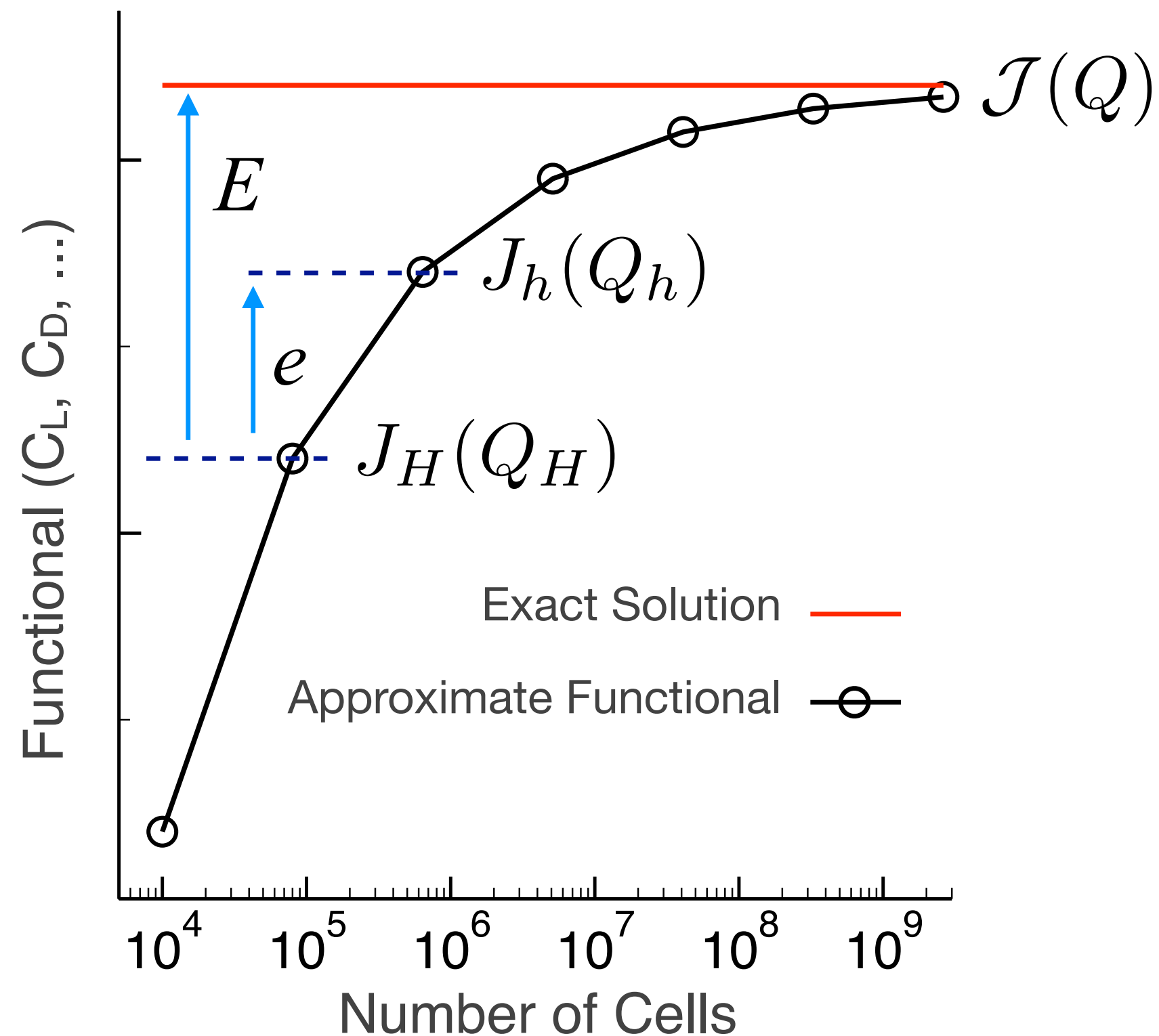
$$J_m = \int_B \rho U_n dA$$

$$J_H(Q_H)$$





Method of Adjoint Weighted Residuals



- Goal is to compute relative error

$$e = |J_h - J_H|$$

- Then use asymptotic analysis to estimate total discretization error

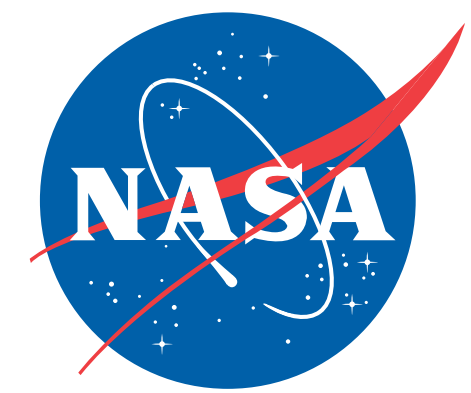
$$E = \left(1 + \frac{1}{r^p - 1}\right) e$$

Refinement Ratio r Order p

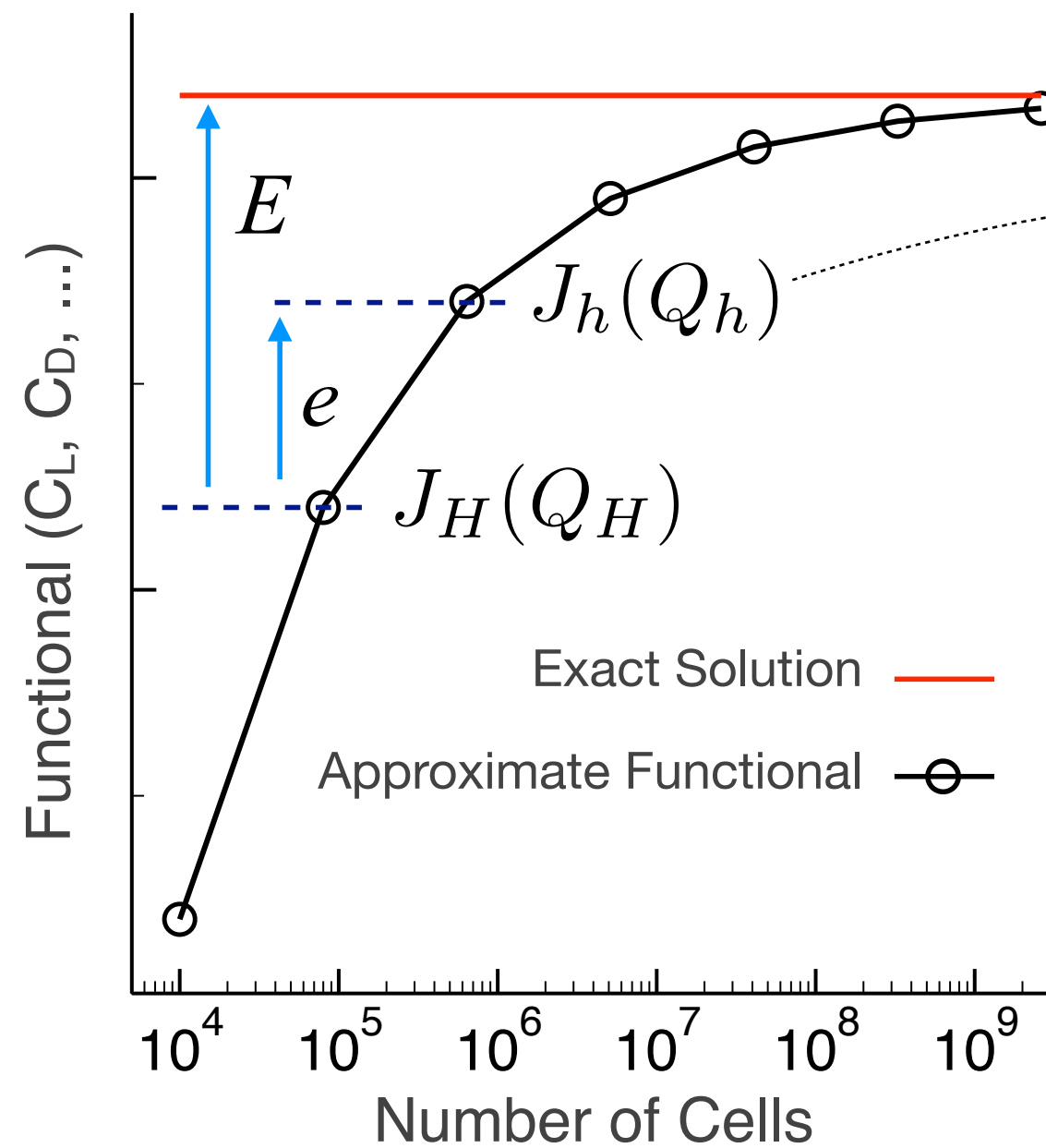
- Key step is to reliably estimate

$$J_h(Q_h)$$

without solving on the fine mesh



Method of Adjoint Weighted Residuals

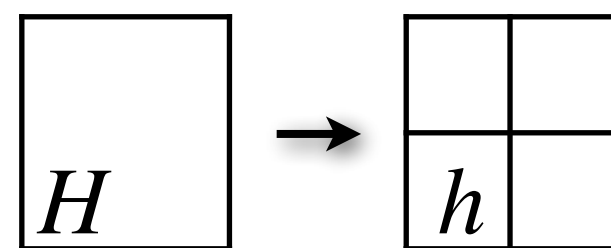


Linearize discrete flow residual and functional to obtain:

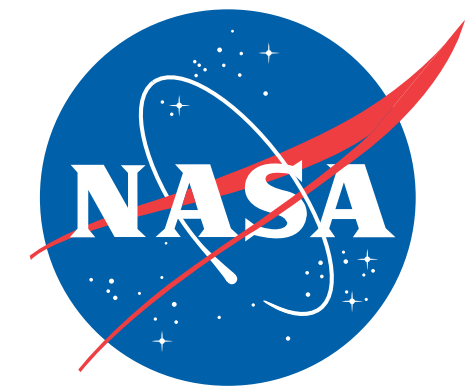
$$J_h(\mathbf{Q}_h) \approx J_h(\mathbf{Q}_h^H) - (\boldsymbol{\psi}_h^H)^T \mathbf{R}_h(\mathbf{Q}_h^H) - (\boldsymbol{\psi}_h - \boldsymbol{\psi}_h^H)^T \mathbf{R}_h(\mathbf{Q}_h^H)$$

Adjoint equation:

$$\left[\frac{\partial \mathbf{R}_H(\mathbf{Q}_H)}{\partial \mathbf{Q}_H} \right]^T \boldsymbol{\psi}_H = \frac{\partial J_H(\mathbf{Q}_H)}{\partial \mathbf{Q}_H}^T$$

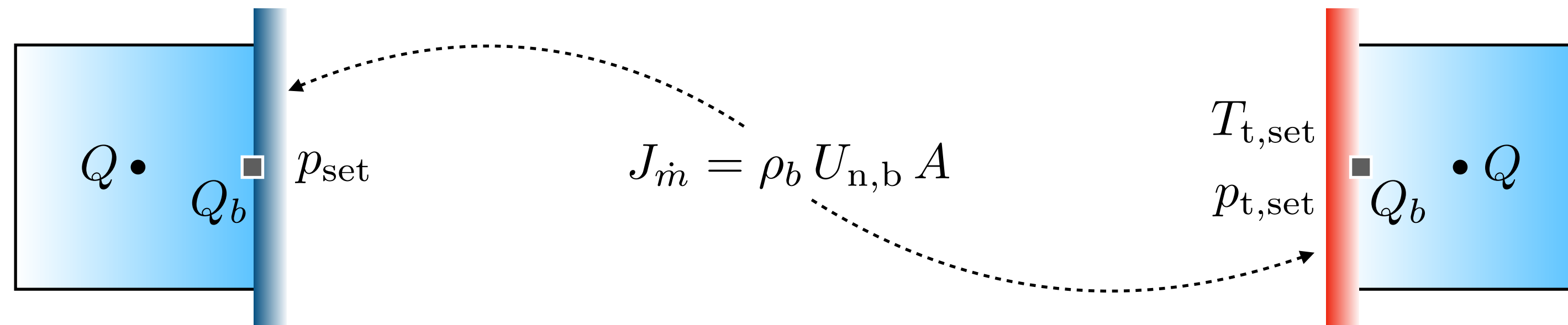


- Large linear system
- Defined by the discrete flow residual and functional
 - Includes all boundary conditions
- Converges to continuous adjoint equation in the fine mesh limit
 - Adjoint inconsistent formulations can generate spurious oscillations near the wall



Adjoints of Permeable Boundary Conditions

- Formulation assumes subsonic flow at boundary and uses one-dimensional Riemann invariants



Subsonic Outflow

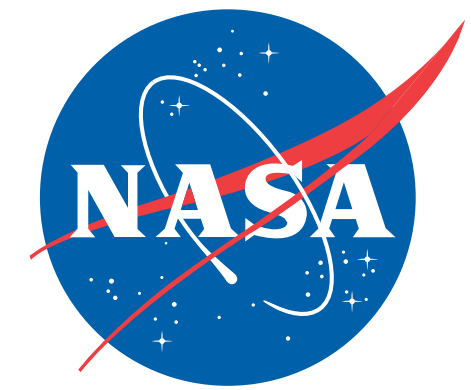
Subsonic Inflow

- Suitable for engine inlets, ECS intakes, secondary flow paths
- Specify exit pressure, all other quantities come from interior

- Suitable for nozzle plenums, turbines, ECS vents
- Specify stagnation temperature and stagnation pressure

$$Q_b = \begin{bmatrix} \rho_b \\ U_{n,b} \\ U_{t,b} \\ p_{set} \end{bmatrix}$$

$$Q_b = \begin{bmatrix} \rho_b \\ U_{n,b} \\ 0 \\ p_b \end{bmatrix}$$



Adjoints of Permeable Boundary Conditions

Subsonic Outflow

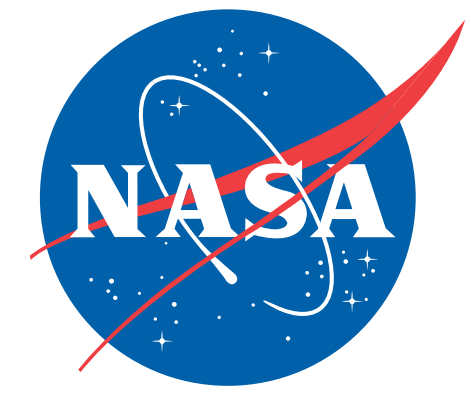
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Subsonic Inflow

$$Q_b = \begin{bmatrix} \rho_b \\ U_{n,b} \\ 0 \\ p_b \end{bmatrix}$$

$$\begin{pmatrix} \frac{\partial \mathbf{F}_b}{\partial \mathbf{Q}_b} & \frac{\partial \mathbf{Q}_b}{\partial \mathbf{Q}} \end{pmatrix}^T \psi = \frac{\partial J_m}{\partial \mathbf{Q}}^T$$

- Rank deficient matrix (rank three in 2D)
- Restricts choice of functionals on RHS to obtain a nonsingular system
 - Mass flow rate output involves 3 free parameters that match matrix rank, preliminary analysis indicates that the adjoint system is well-posed
 - Similar to slip-wall, where output must be a function of pressure because matrix is rank one
 - Perform numerical study to examine near wall adjoint solution

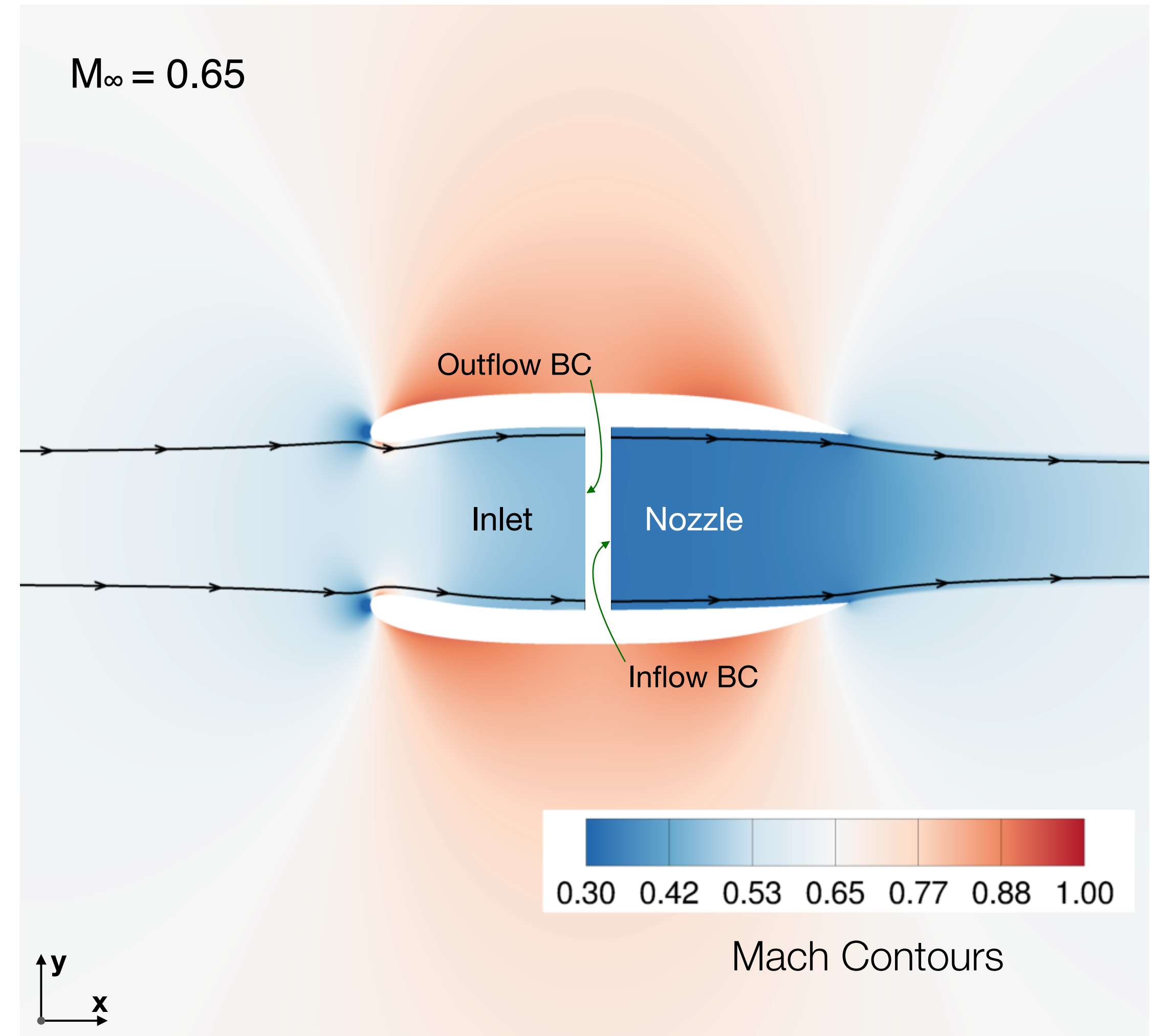


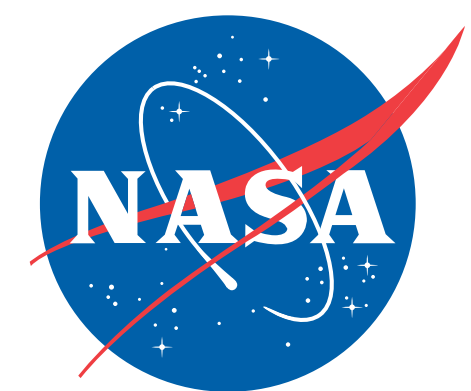
Numerical Study: Near-Wall Adjoint Solutions

- Subsonic, two-dimensional nacelle test case
- Specify exit pressure at the outflow of the inlet
- Specify stagnation temperature and pressure at the inflow of the nozzle
- Slip-wall boundary conditions everywhere else on the wetted surface
- Farfield is ~ 10 chords away

Test Cases

1. Measure mass flow rate at the outflow of the inlet
2. Measure mass flow rate at the inflow of the nozzle



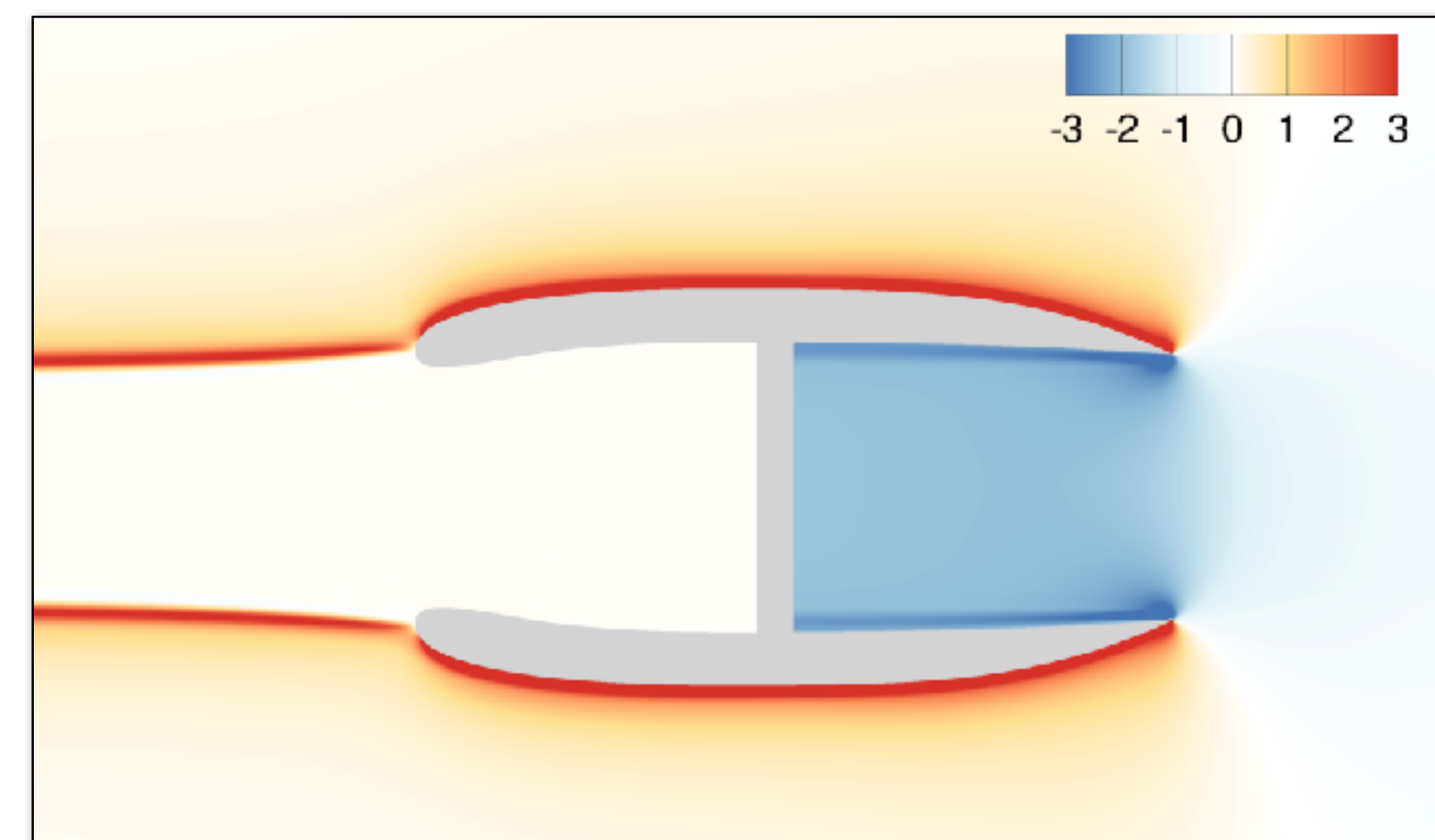
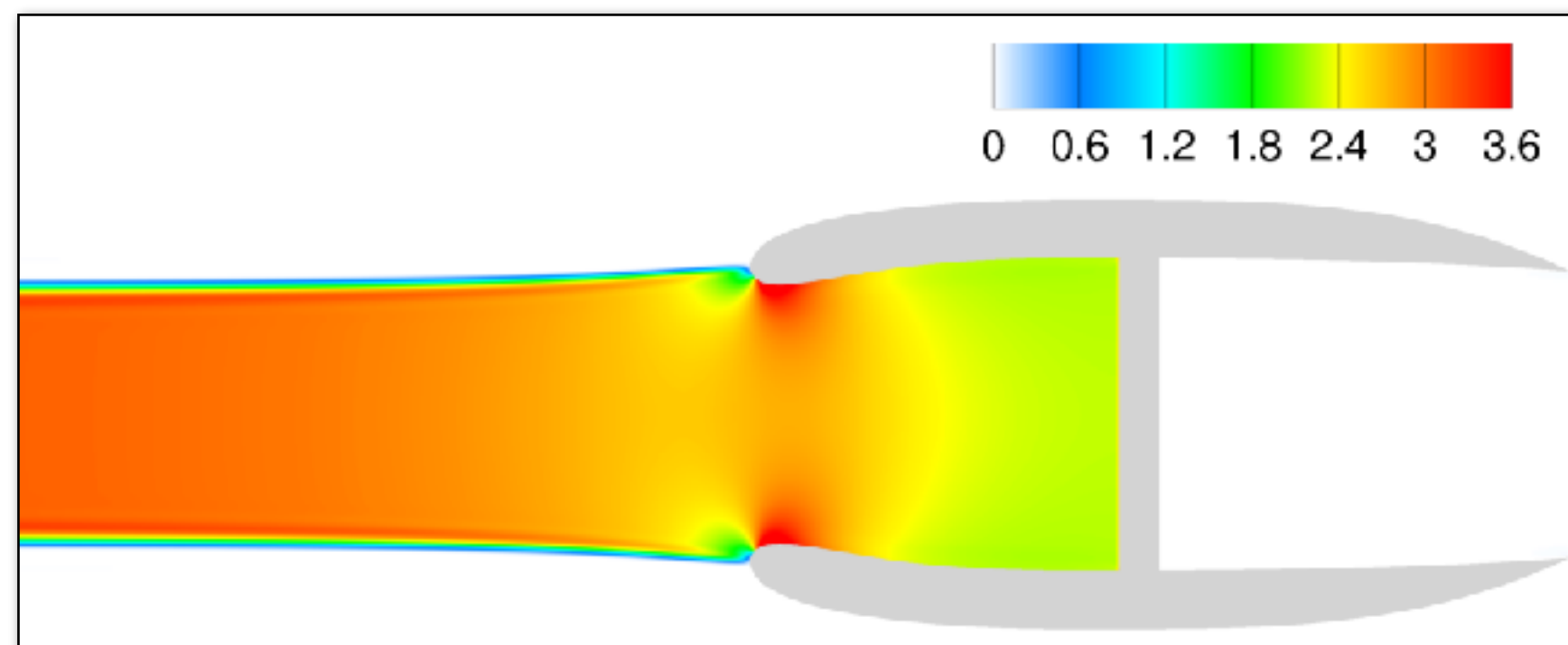


Numerical Study: Near-Wall Adjoint Solutions

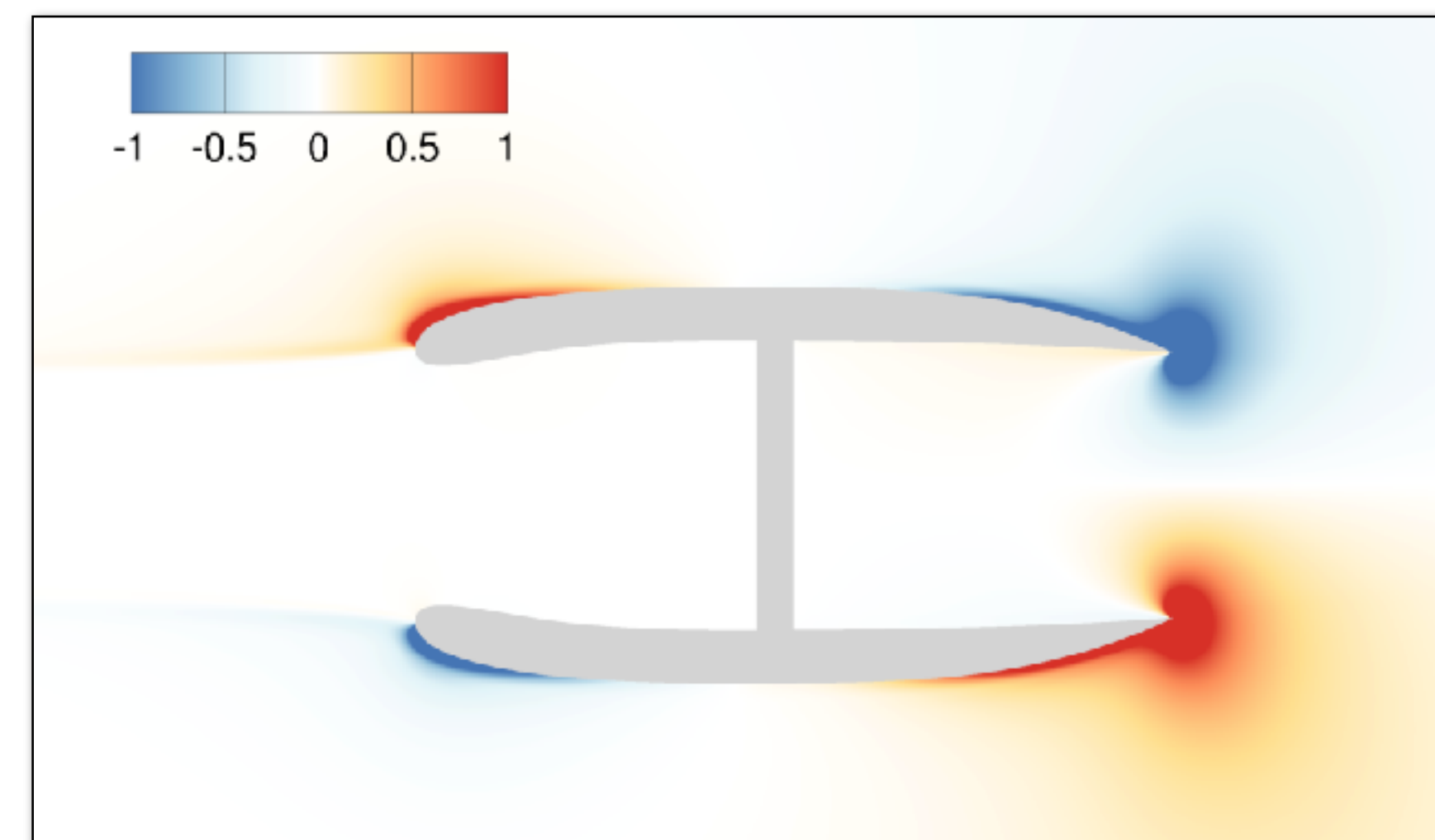
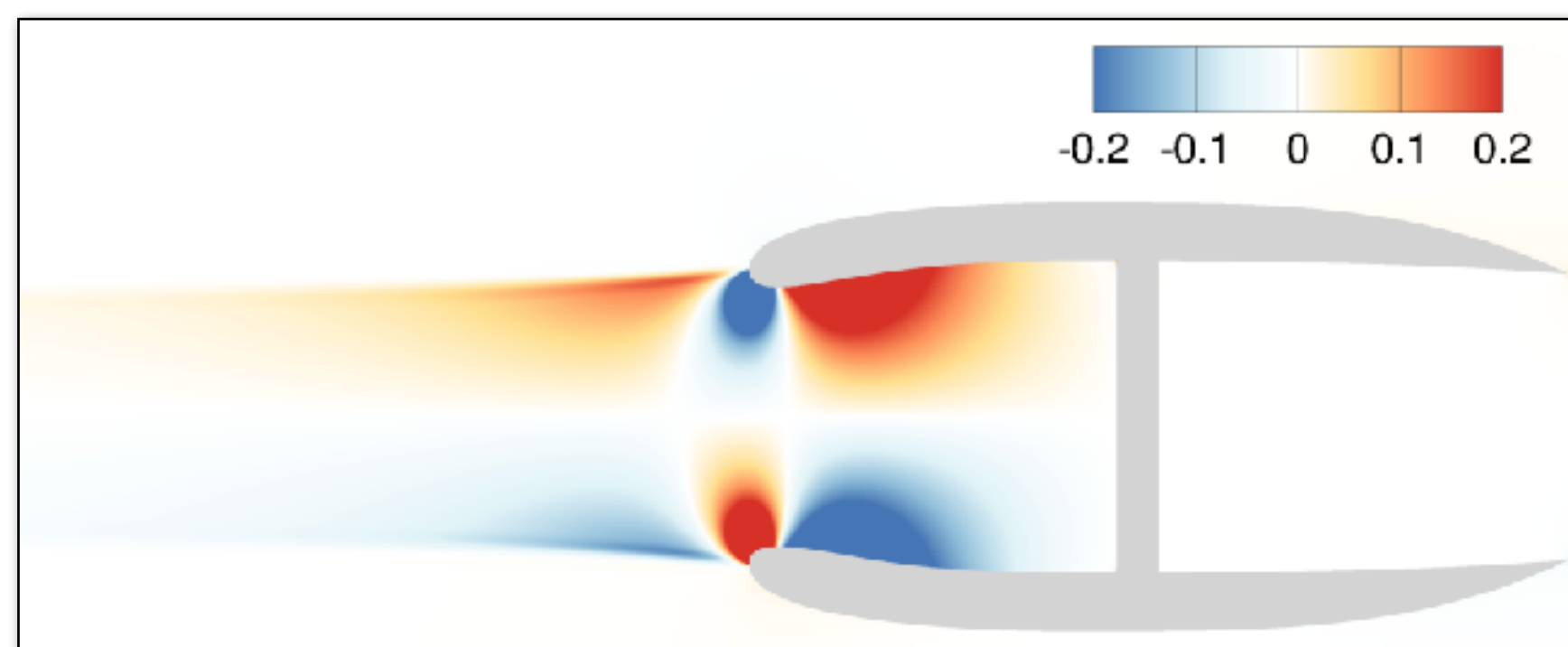
Test Case 1: Inlet Mass Flow Rate

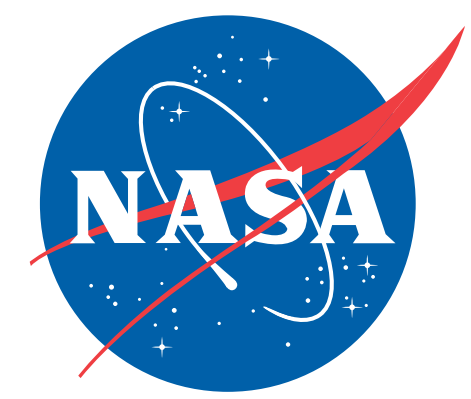
Test Case 2: Nozzle Mass Flow Rate

x-momentum
Adjoint



y-momentum
Adjoint





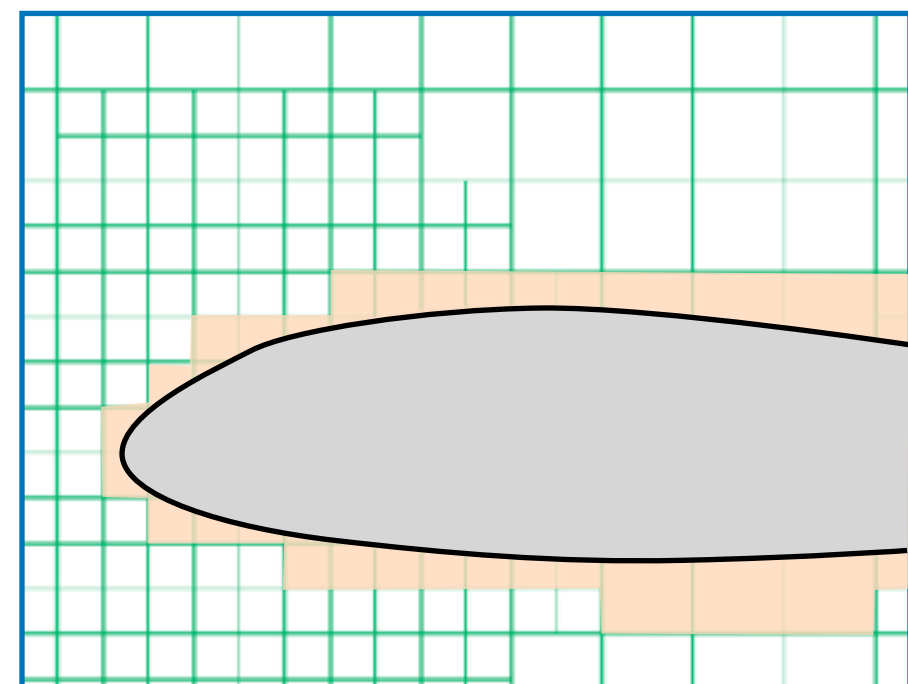
Aerodynamic Shape Optimization

$$\begin{aligned} \min_X \quad & J(X, \mathbf{Q}) \\ \text{subject to} \quad & R(X, \mathbf{Q}) = 0 \quad \forall X \in \Omega \end{aligned}$$

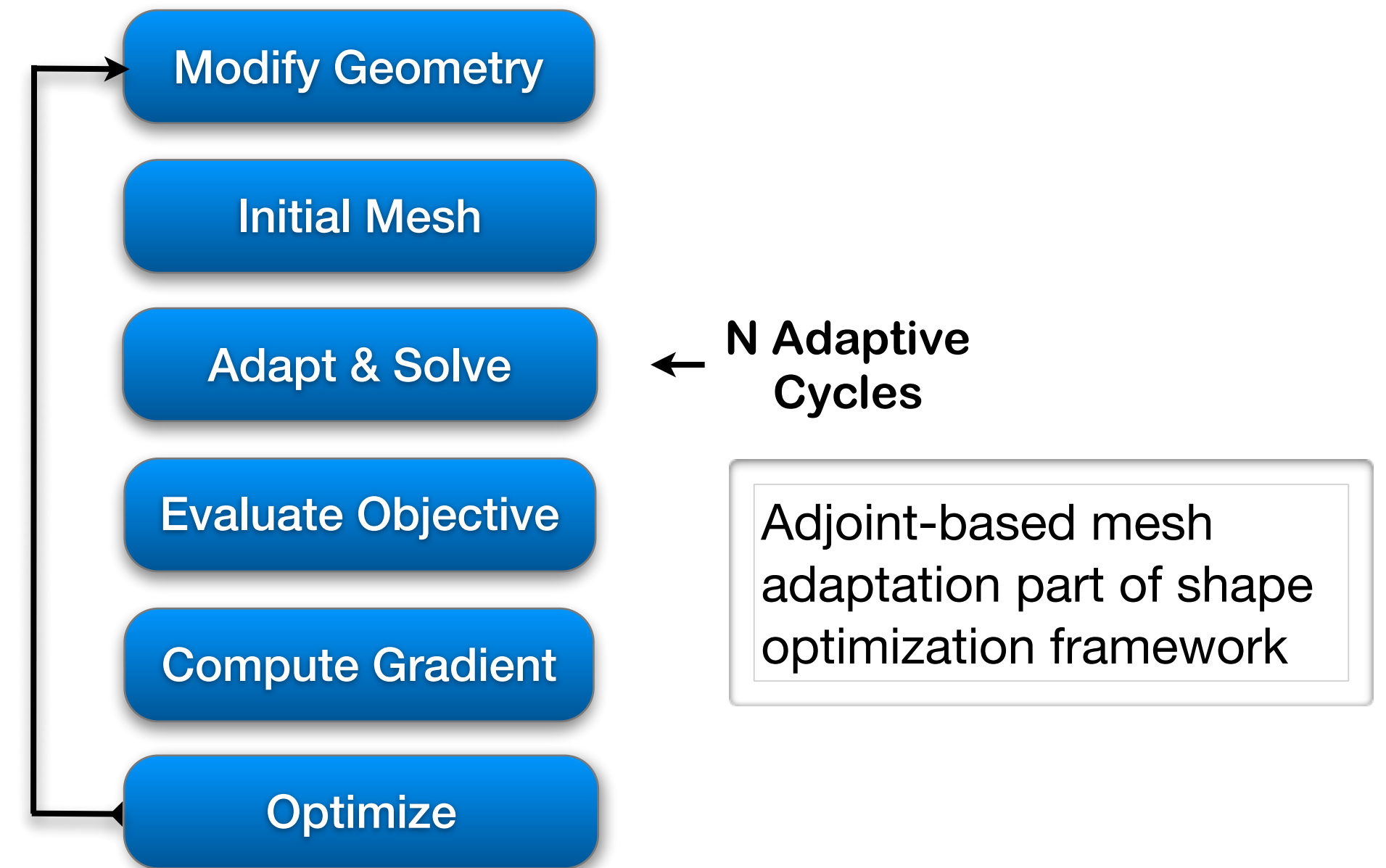
- Gradient-based approach

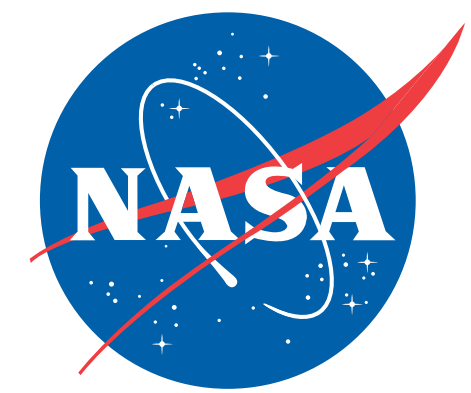
$$\frac{dJ}{dX} = \frac{\partial J}{\partial X} - \psi^T \frac{\partial \mathbf{R}}{\partial X}$$

- Mesh sensitivities confined to cutcells, triangulation connectivity and topology allowed to change



Adjoint Optimization Framework





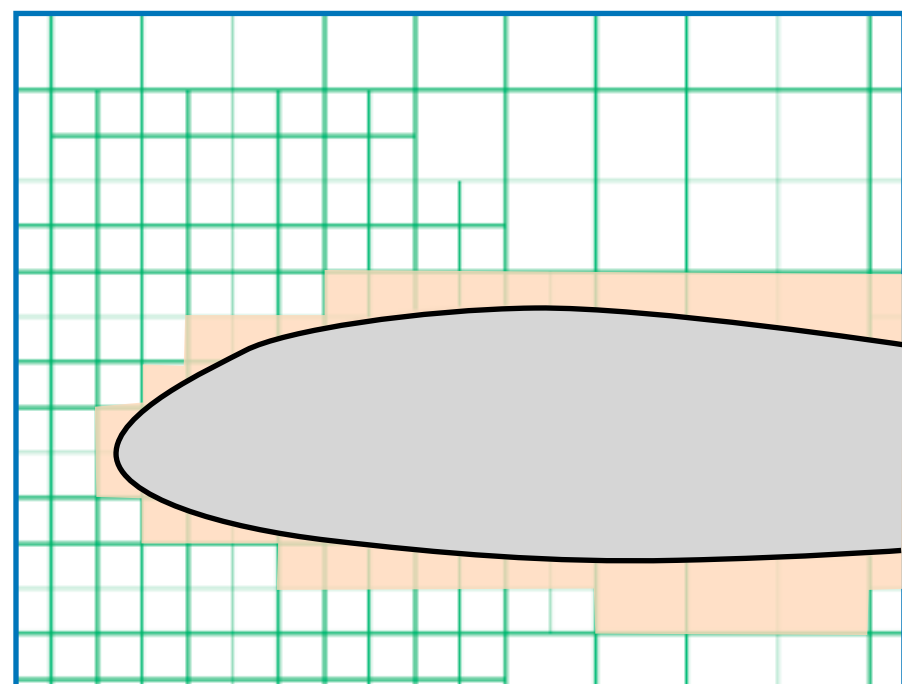
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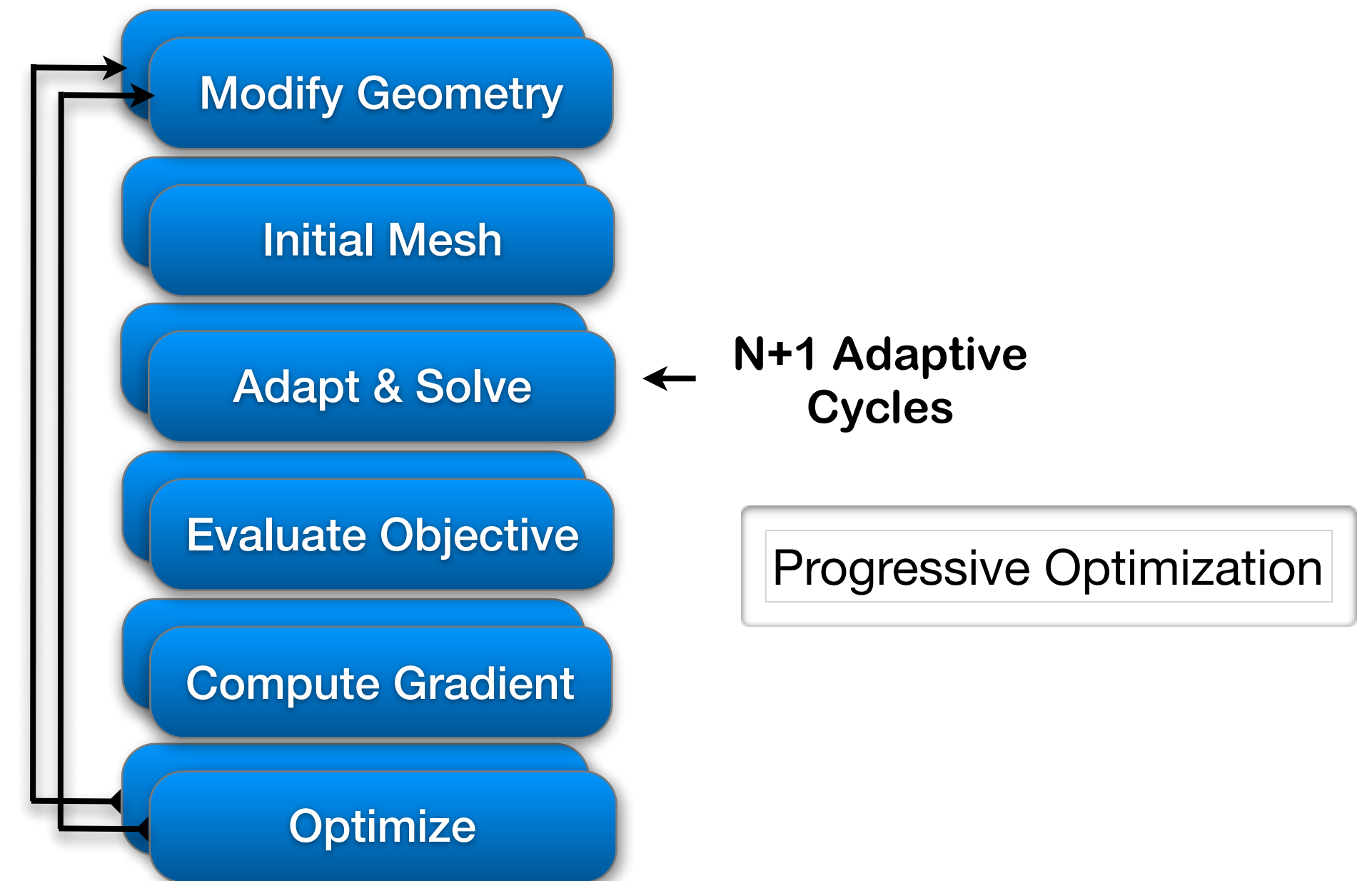
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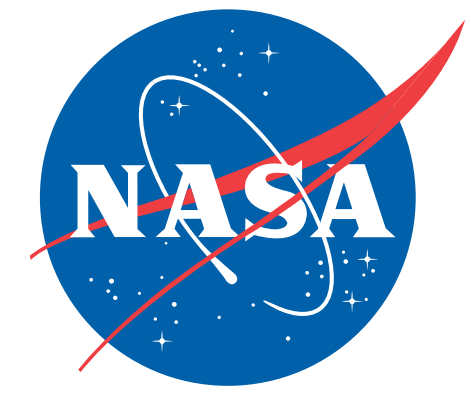
$$\frac{dJ}{dX} = \frac{\partial J}{\partial X} - \psi^T \frac{\partial \mathbf{R}}{\partial X}$$

- Mesh sensitivities confined to cut cells, triangulation connectivity and topology allowed to change



Adjoint Optimization Framework





Results

1. Verification

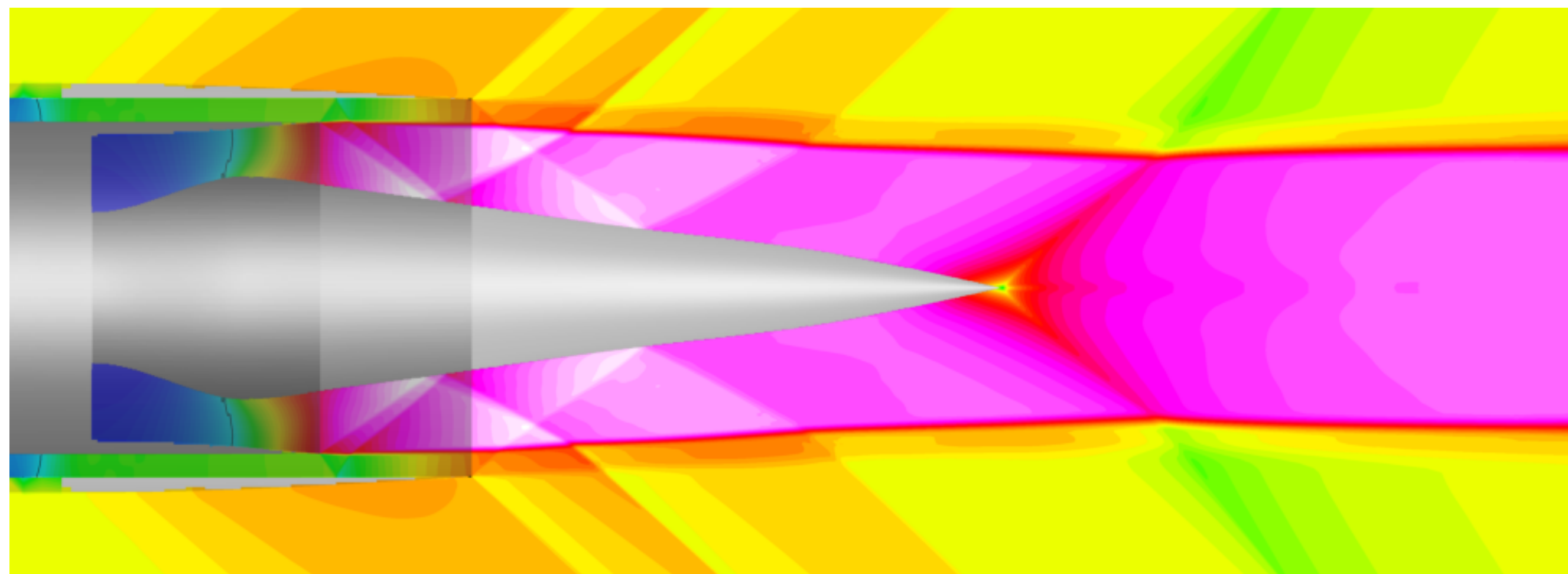
- Two-shock diffuser

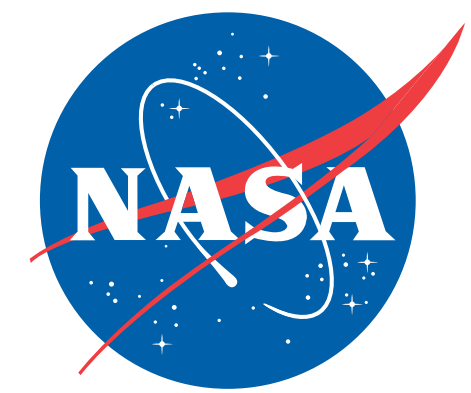
2. Analysis

- LBFD prototype example

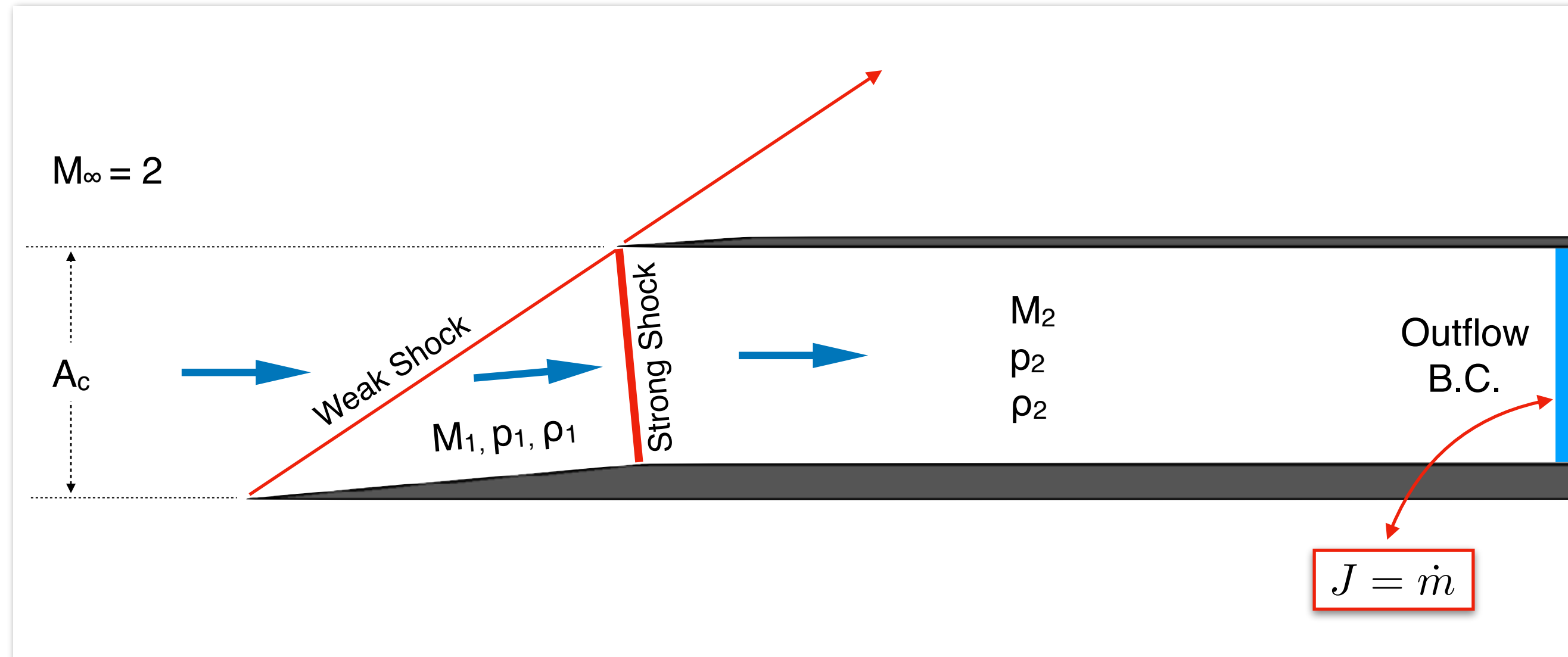
3. Optimization

- Supersonic Nozzle Shape Optimization



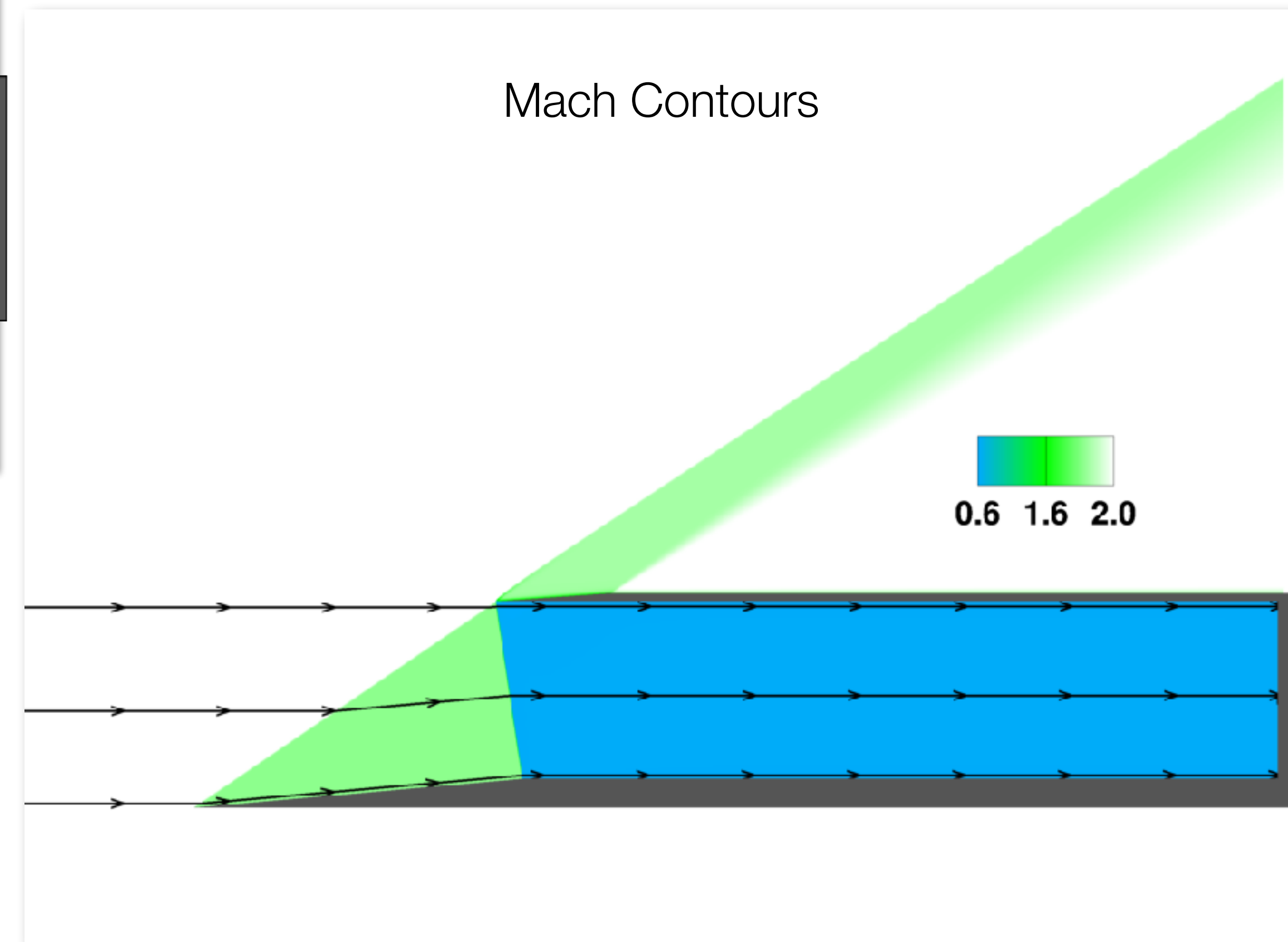


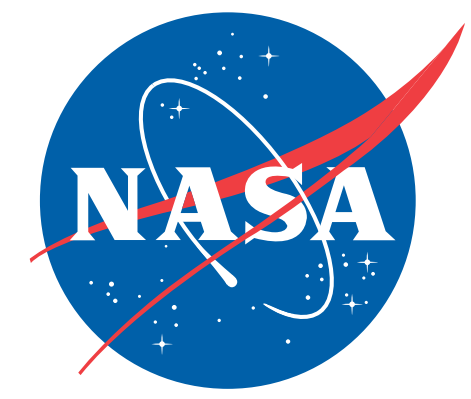
Mass Flow Verification Test



- 2D test case that mimics a supersonic inlet
- Two shock system with no spillage at upper lip
 - 5° wedge
 - Analytic outflow exit pressure specified
- Exact mass flow rate independent of flow state inside inlet
- Slip-wall on wetted surface except for inlet outflow

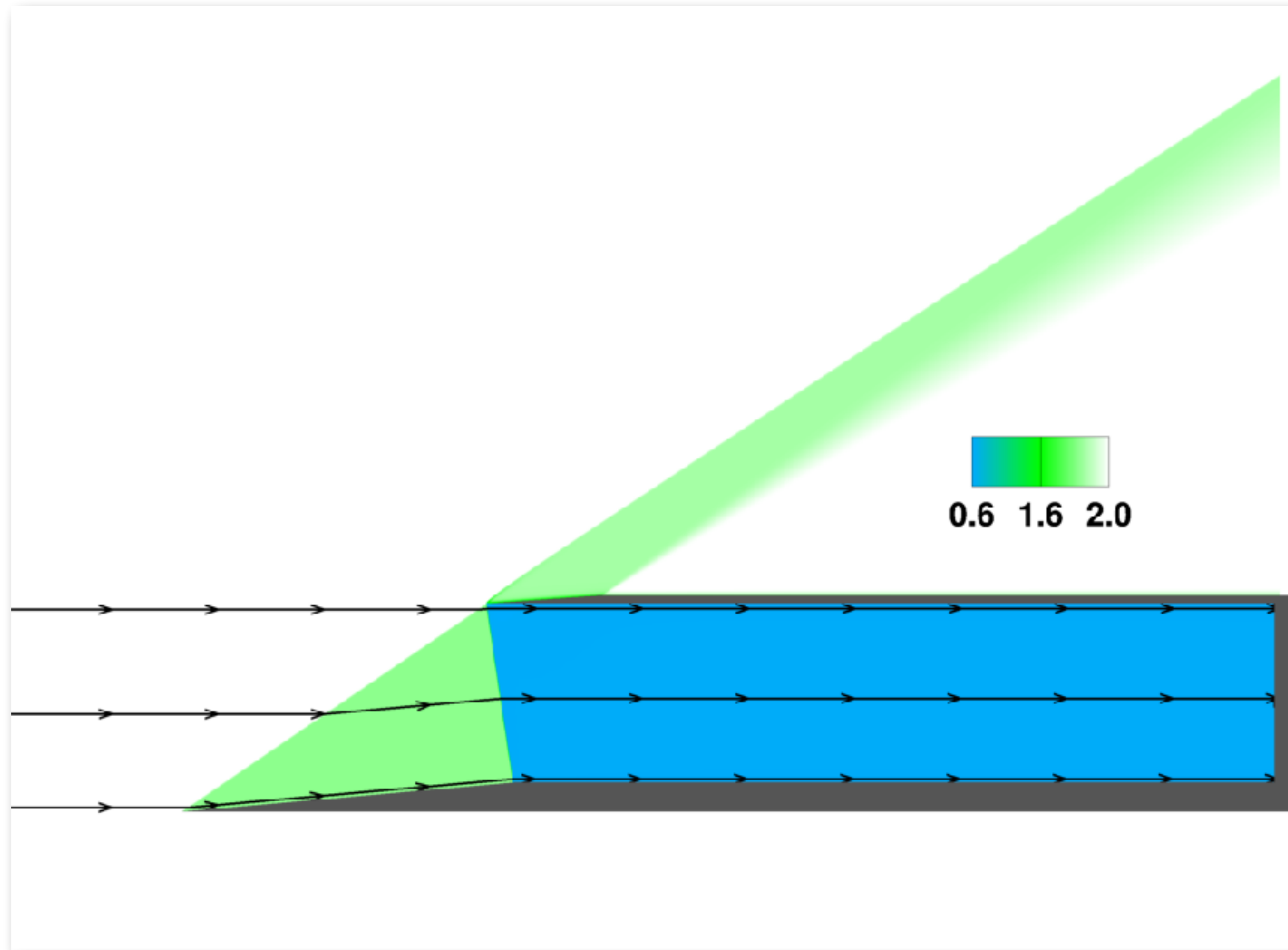
Two-Shock Wedge



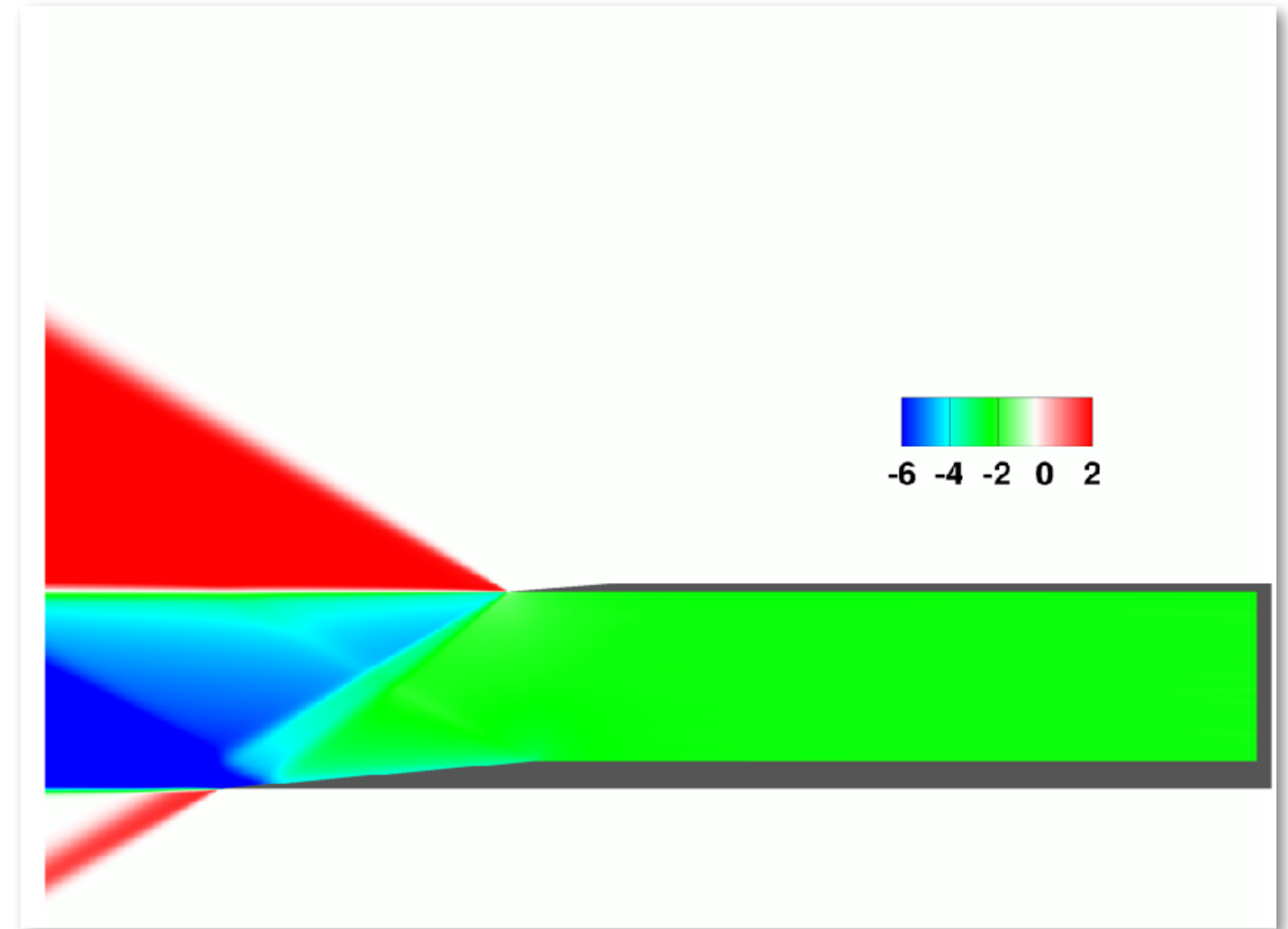


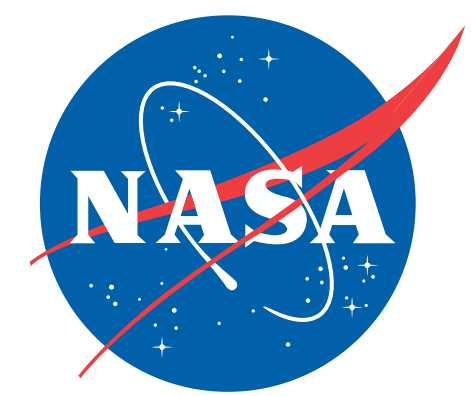
Flow and Adjoint Solutions

Mach Contours



Density Adjoint





Uniform Refinement

Exact Error

$$E = |\mathcal{J} - J_H|$$

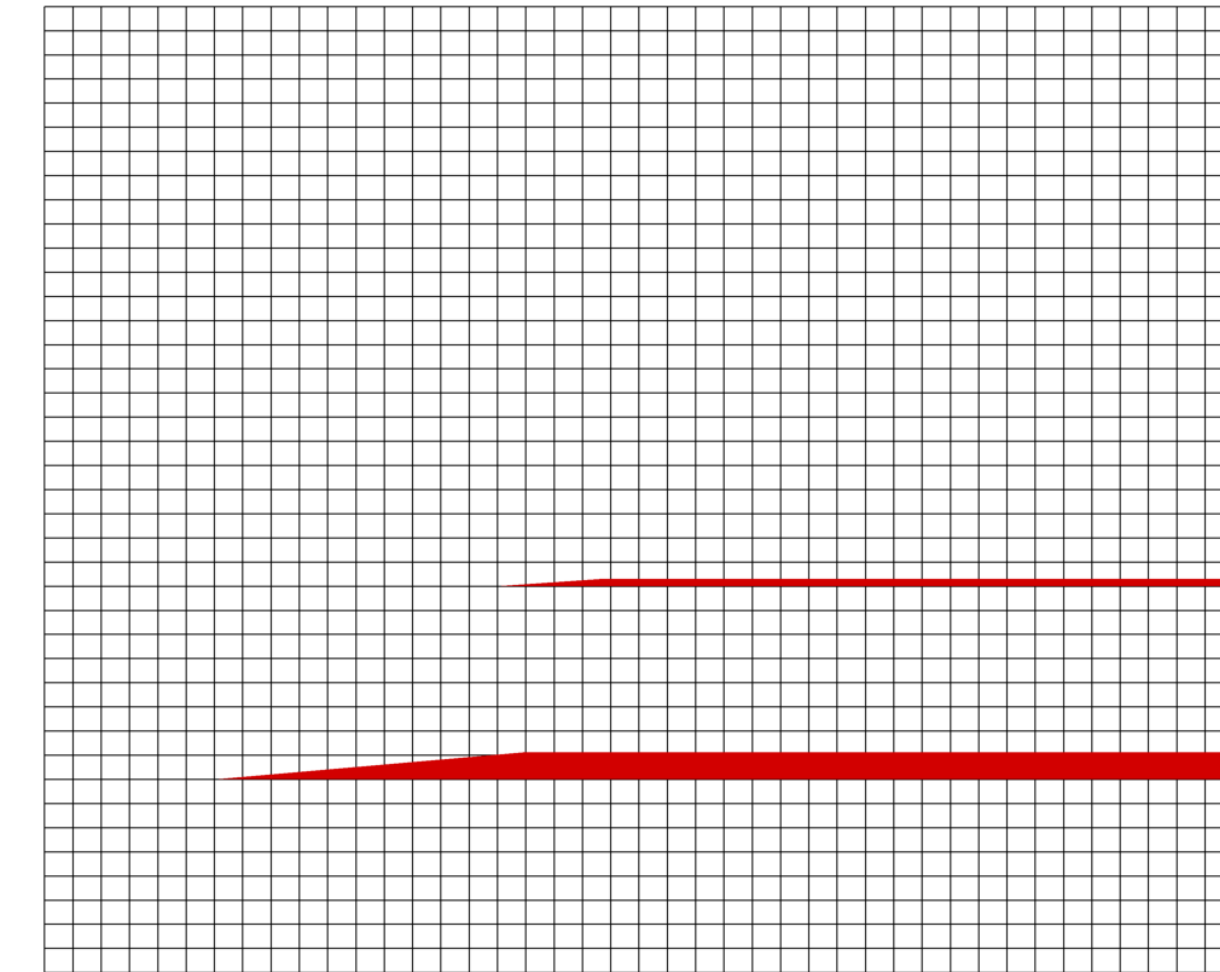
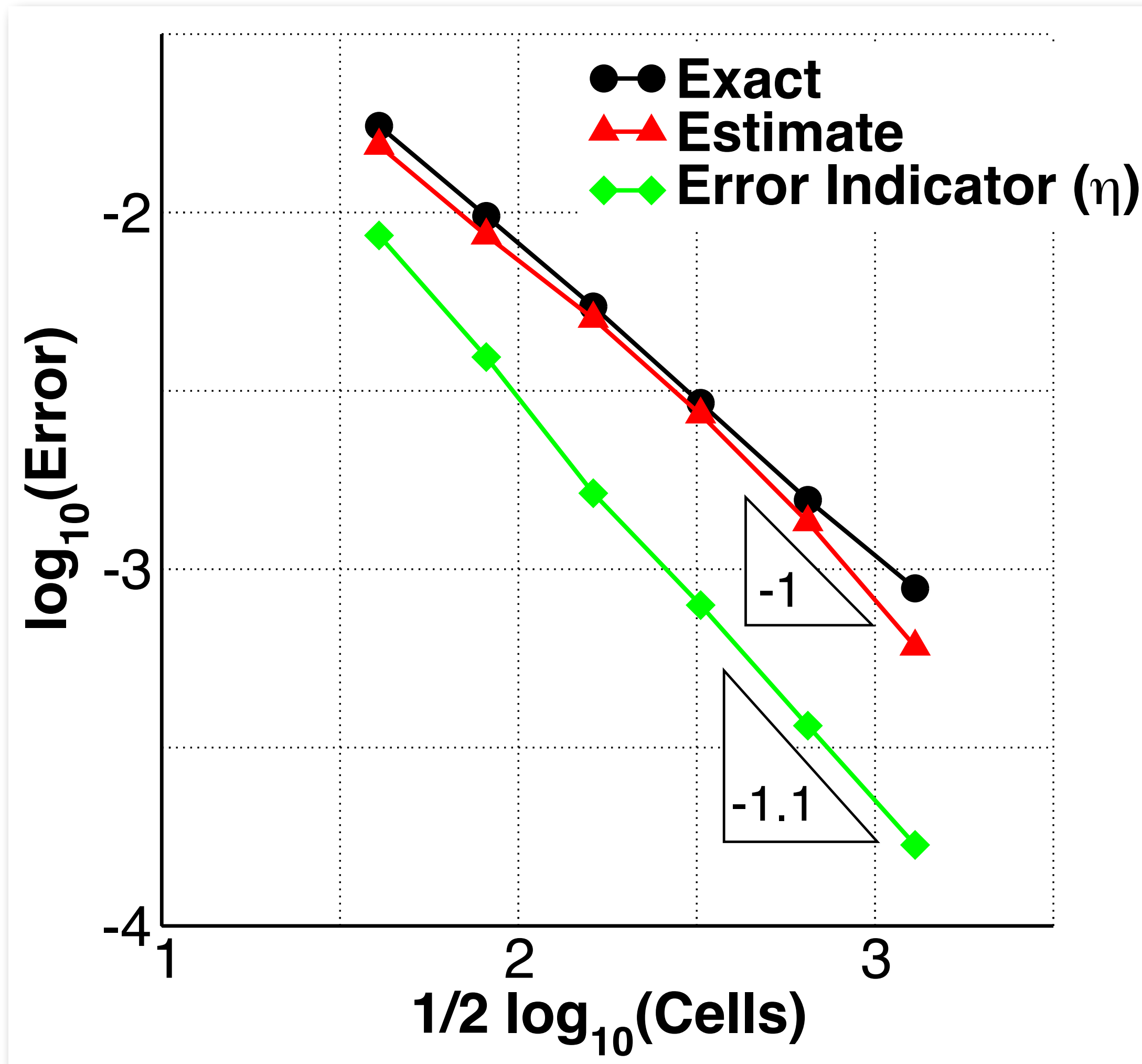
Error Estimate

$$E \approx |J_c - J_H|$$

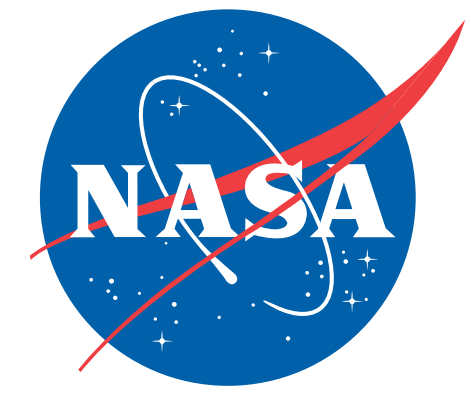
$$J_c = J_h(\mathbf{Q}_L) - \psi_{TQ}^T \mathbf{R}_h(\mathbf{Q}_L)$$

Error Indicator

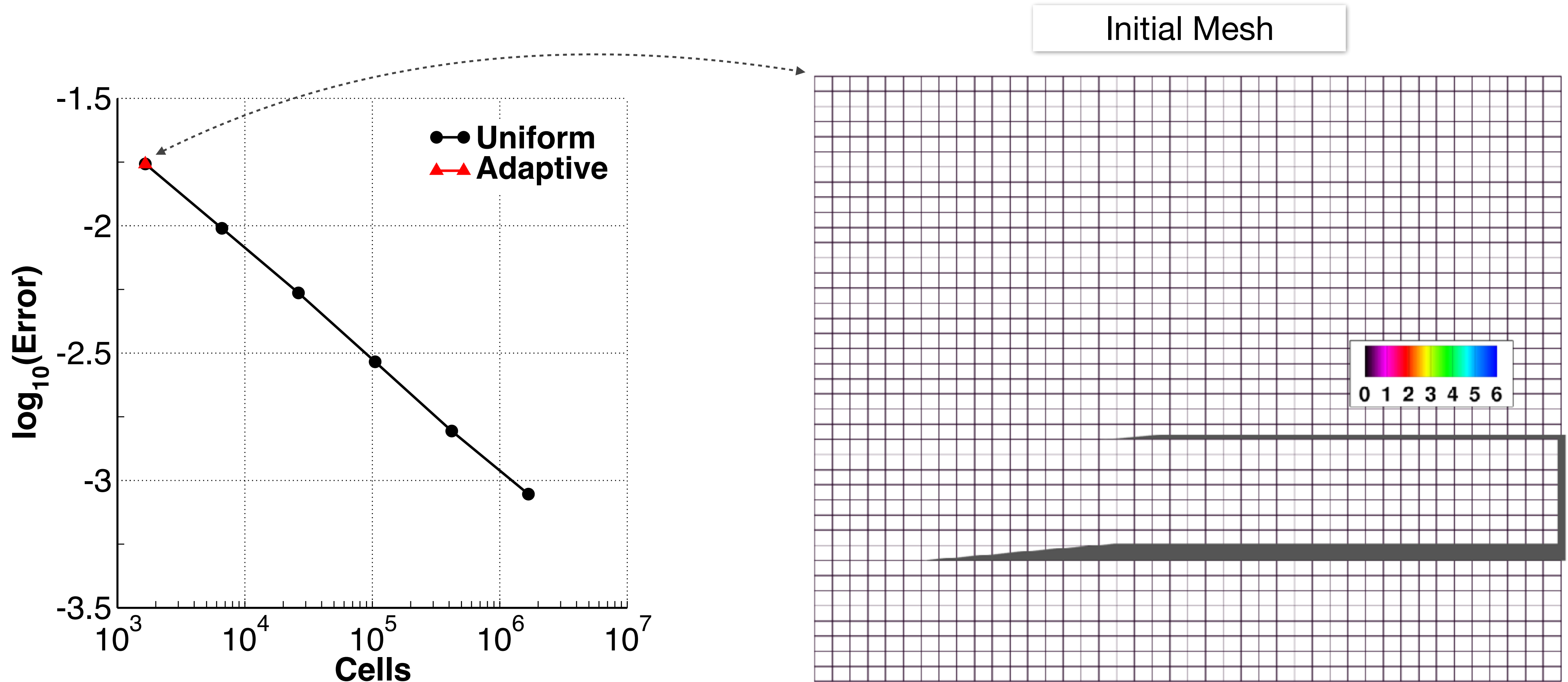
$$\eta_H = \left| (\psi_{TQ} - \psi_{TL})^T \mathbf{R}_h(\mathbf{Q}_L) \right|$$

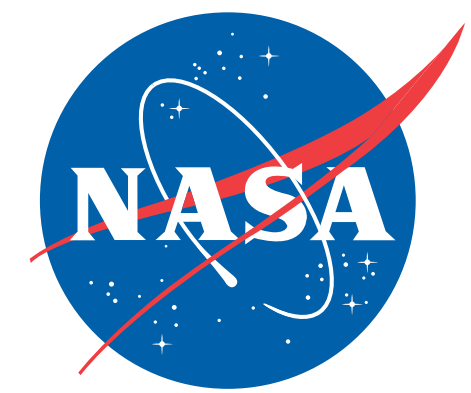


Initial Mesh

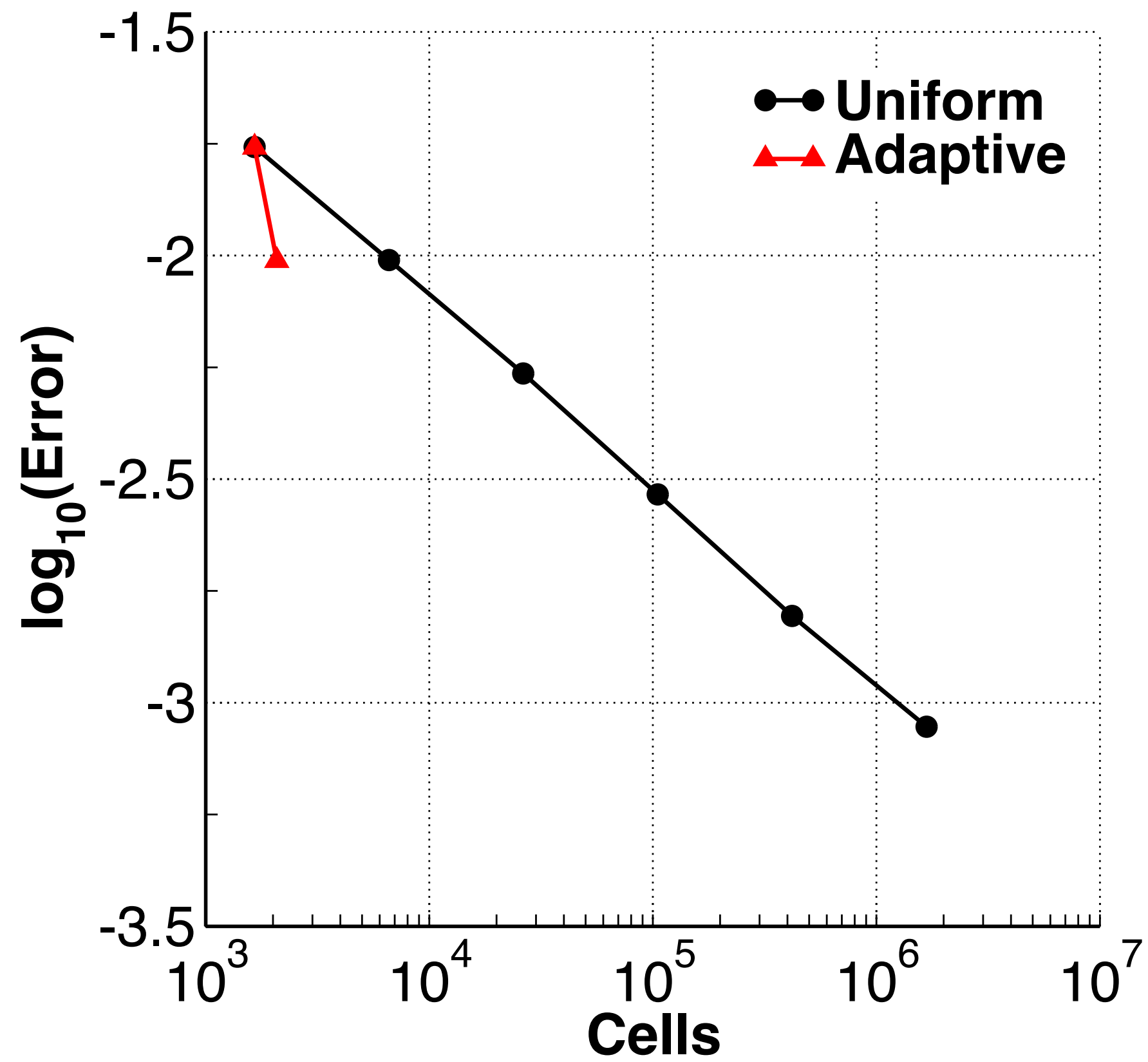


Adaptive Refinement

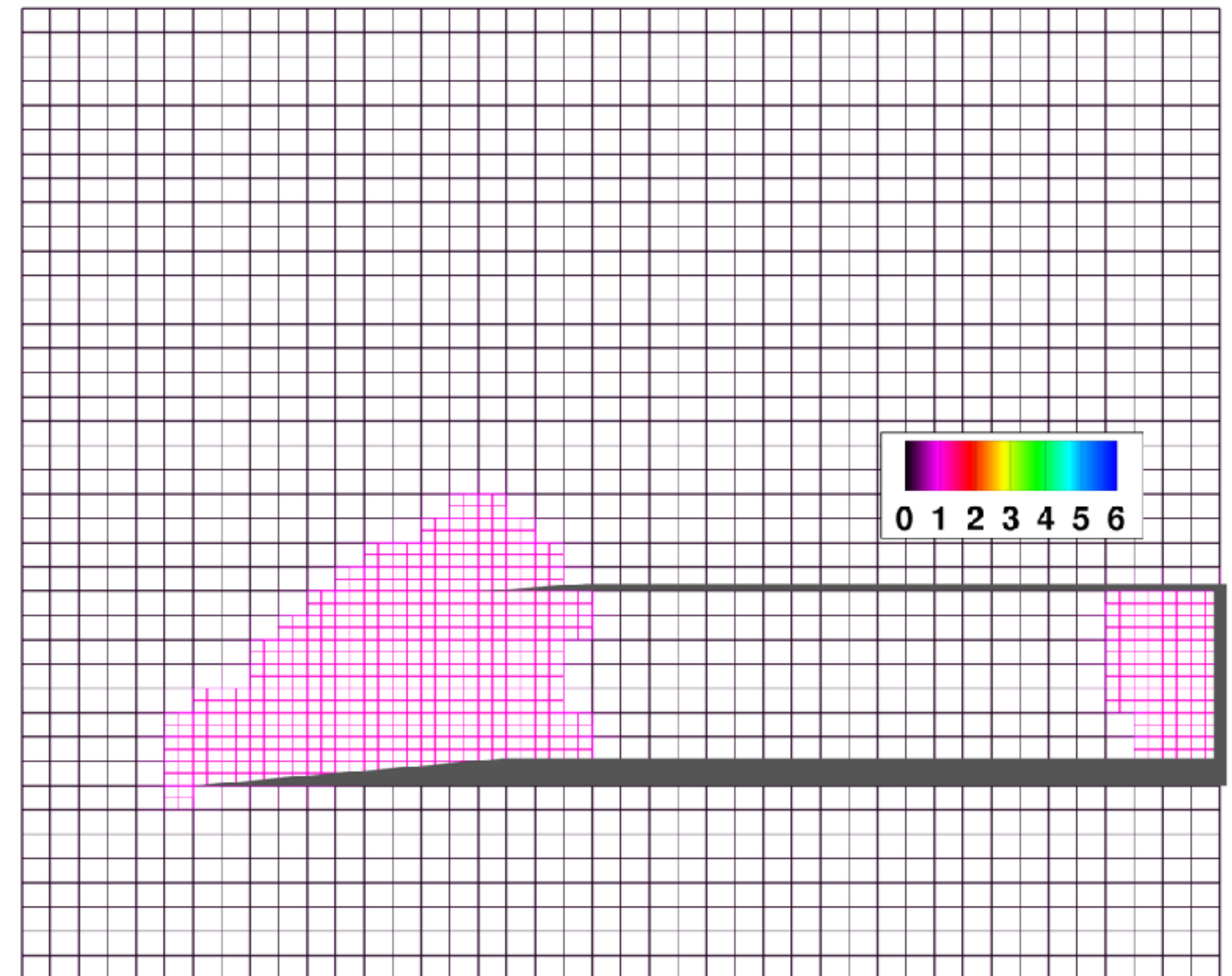


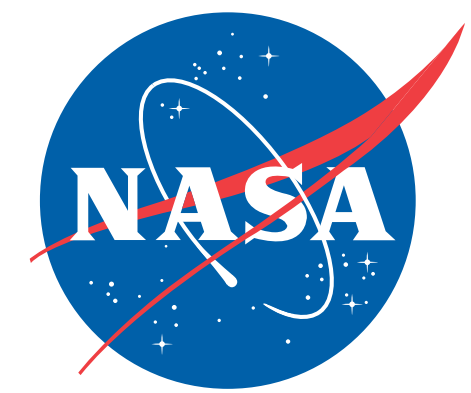


Adaptive Refinement



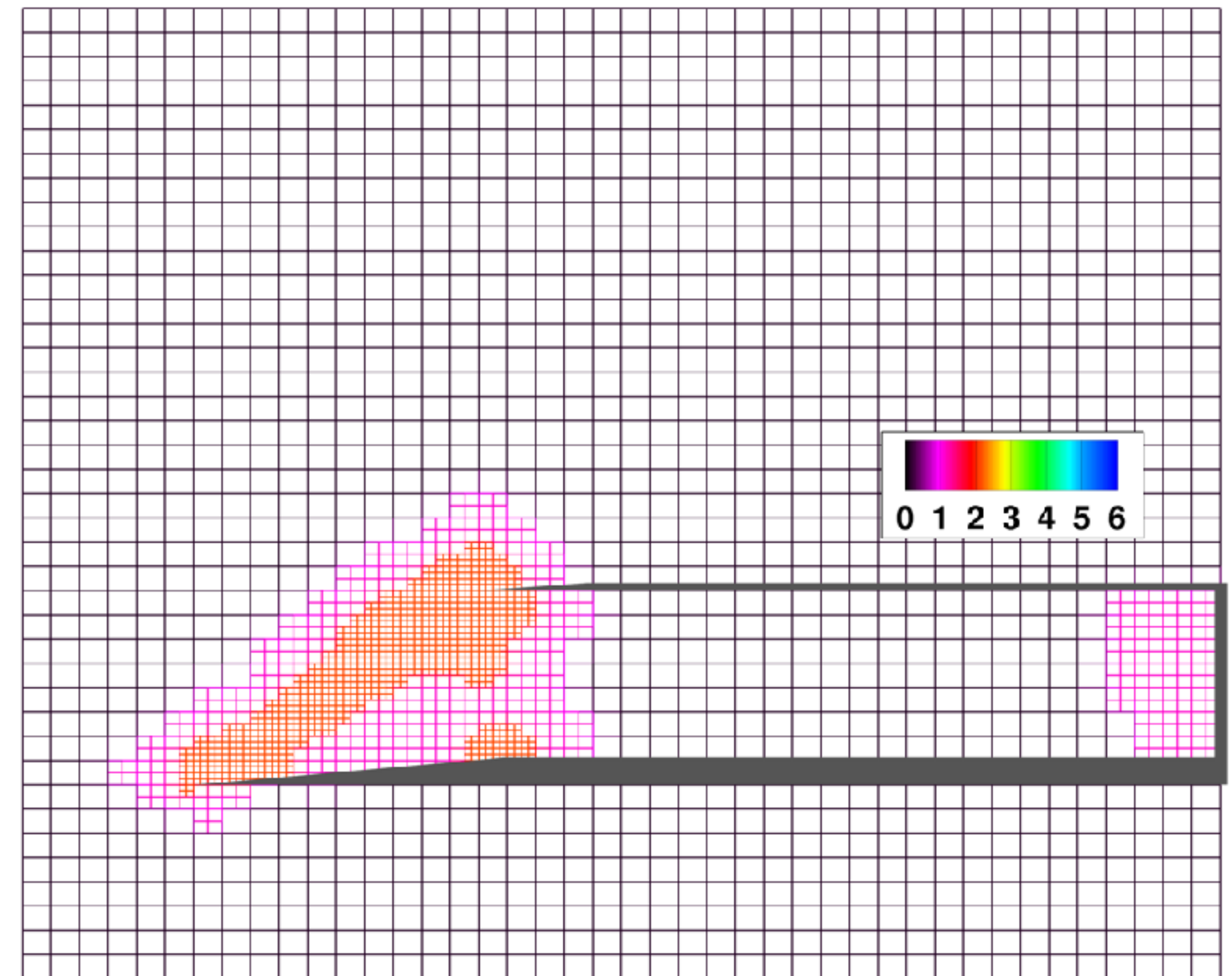
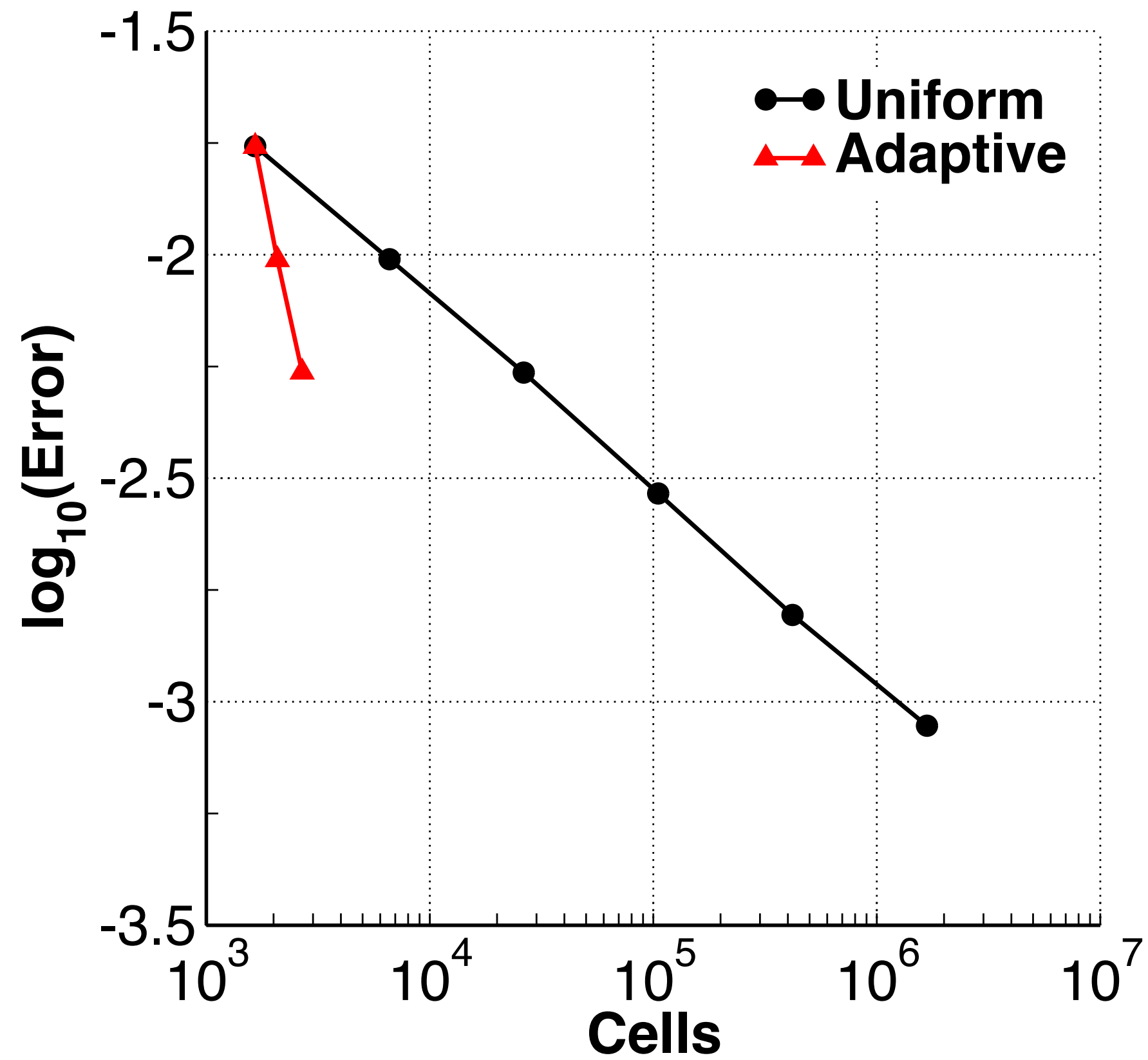
Adaptation Cycle: 1

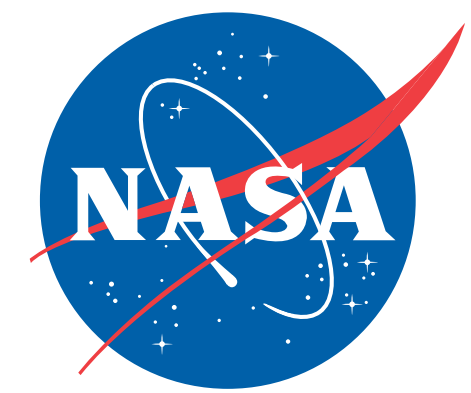




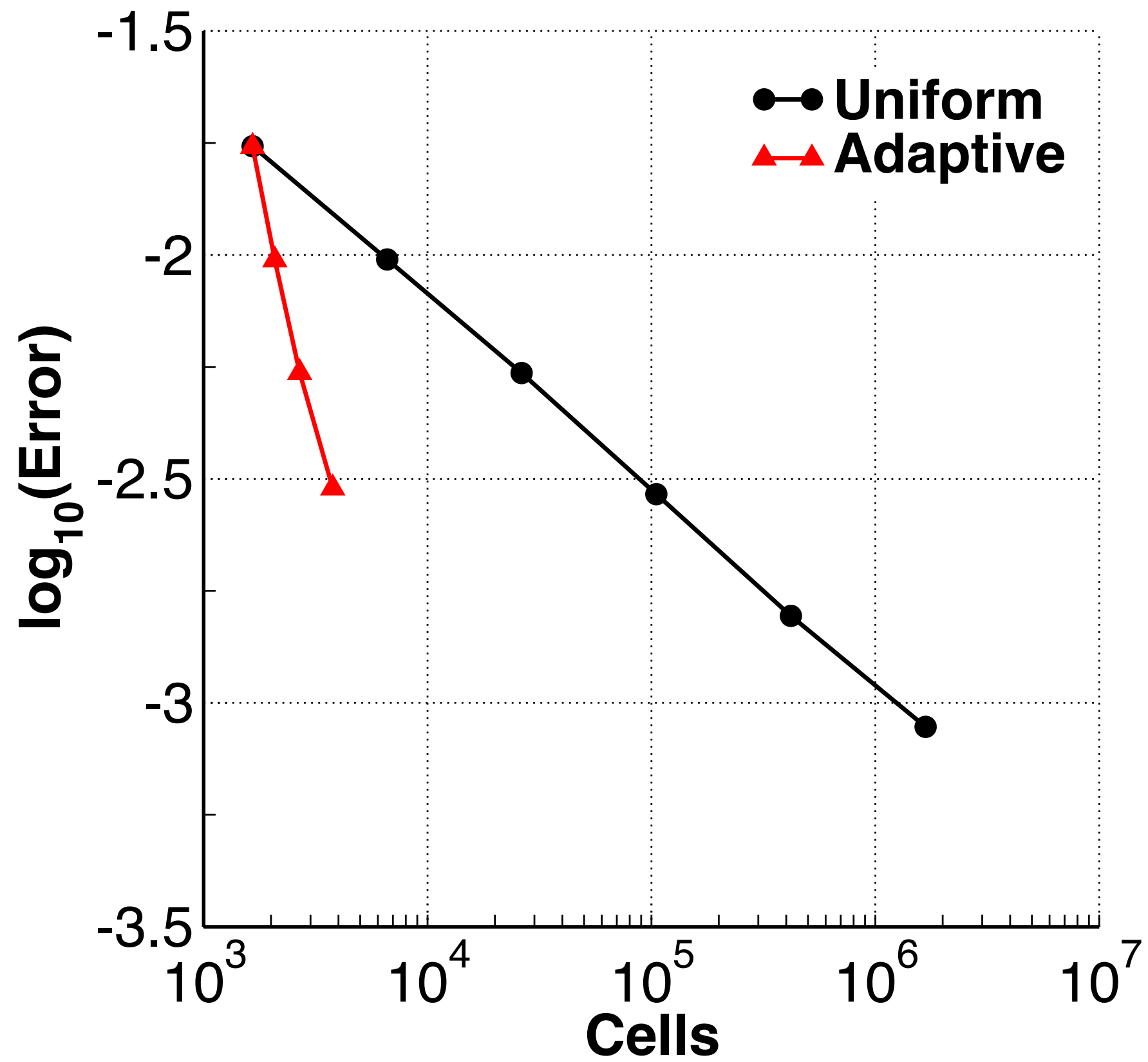
Adaptive Refinement

Adaptation Cycle: 2

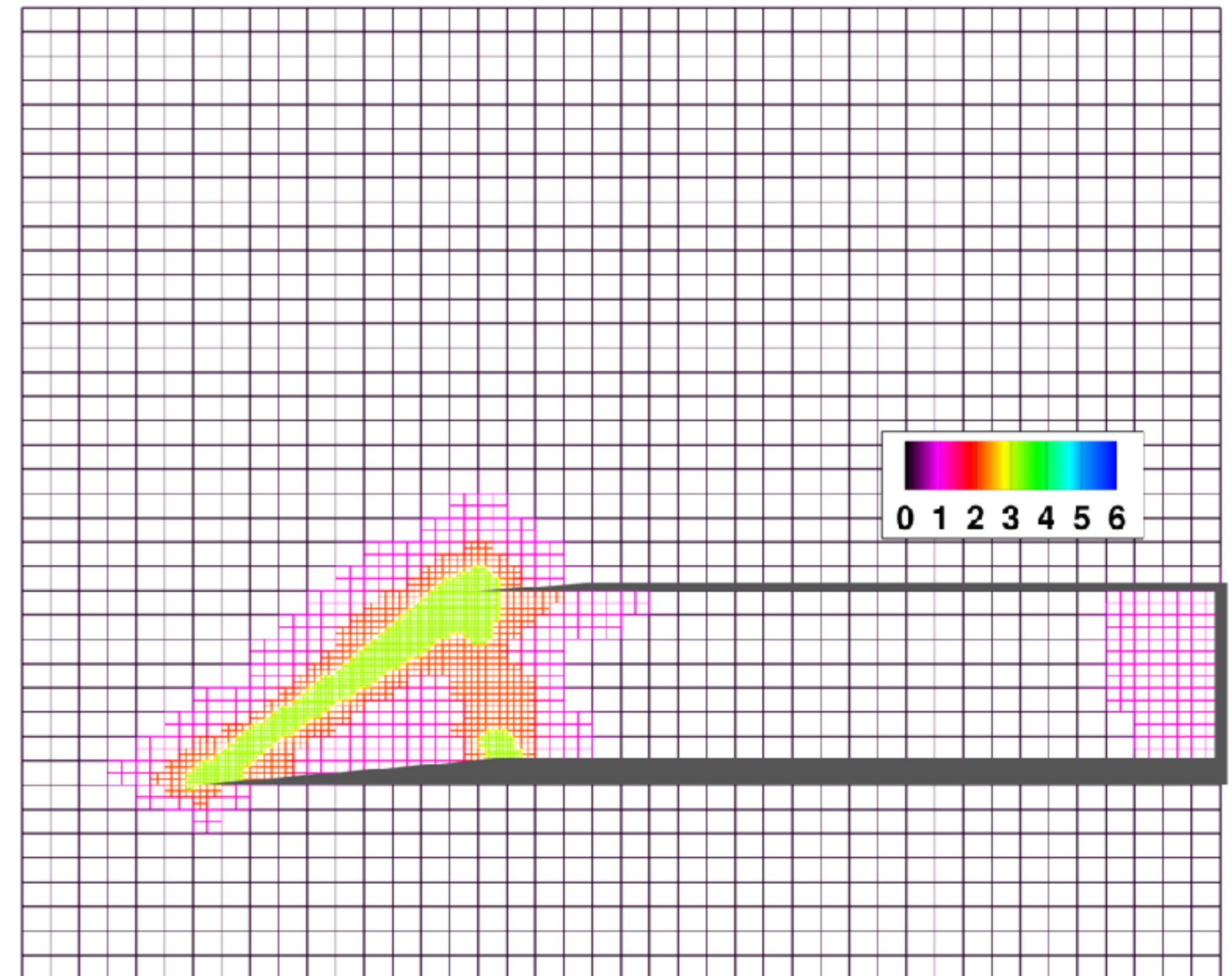


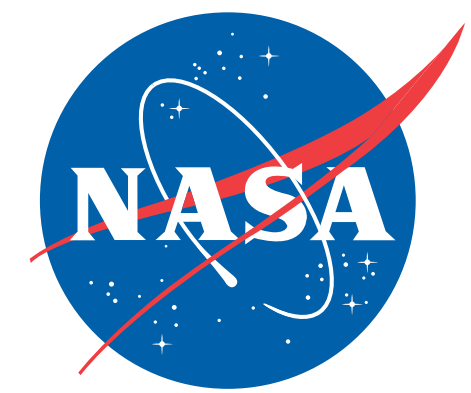


Adaptive Refinement



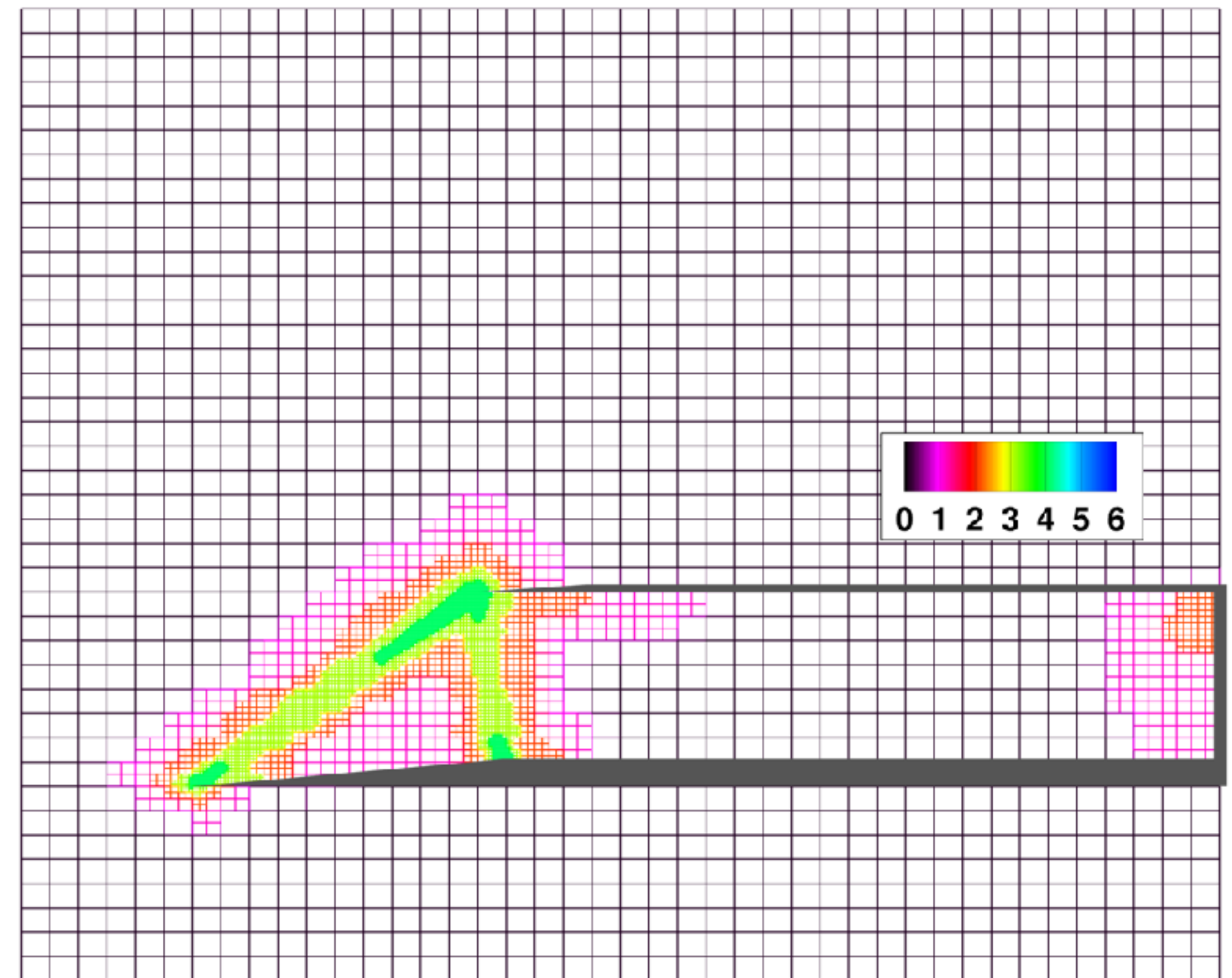
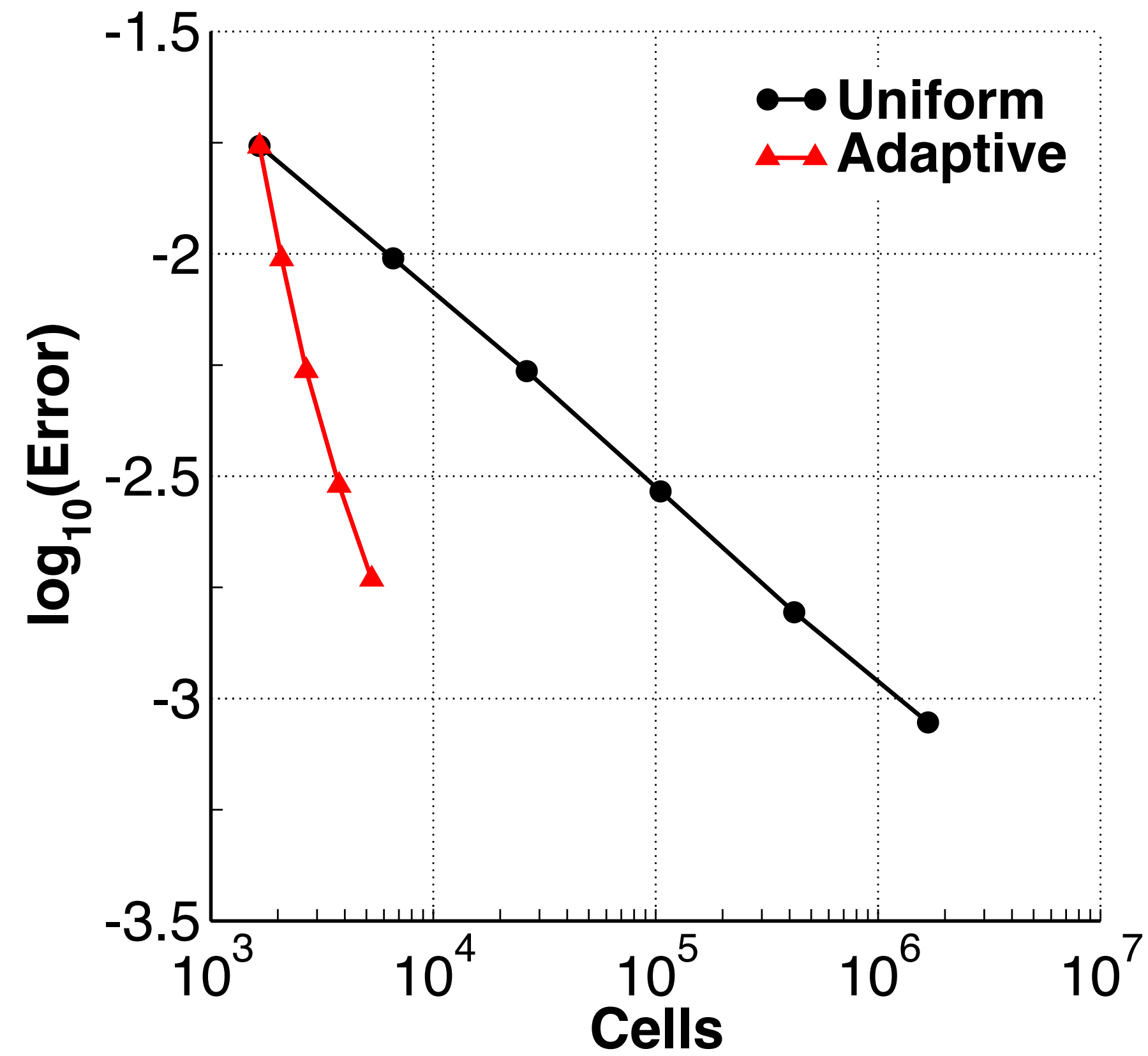
Adaptation Cycle: 3

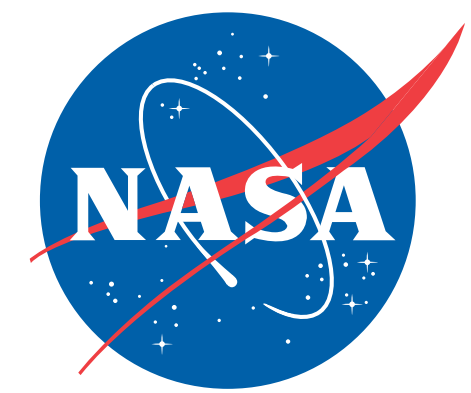




Adaptive Refinement

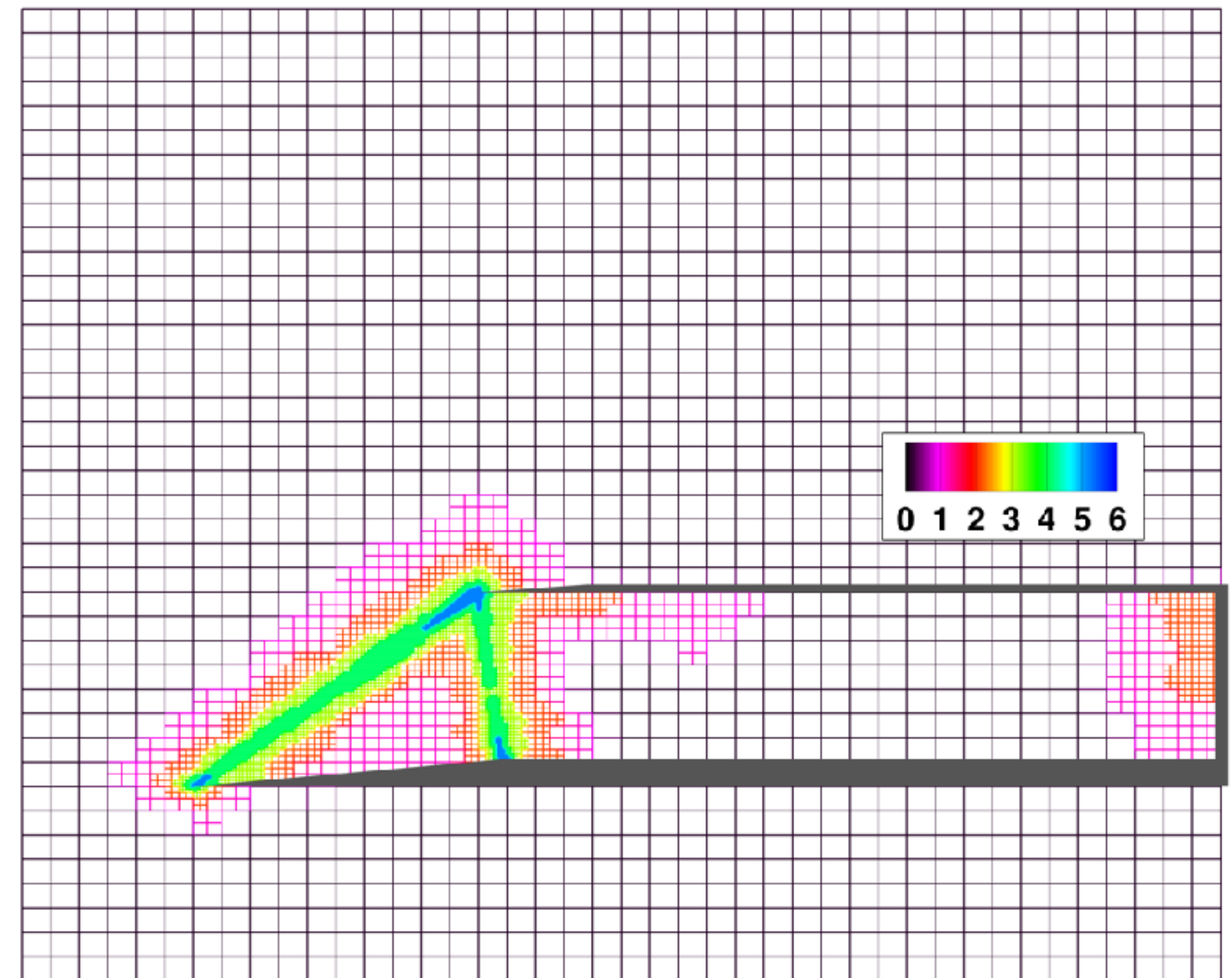
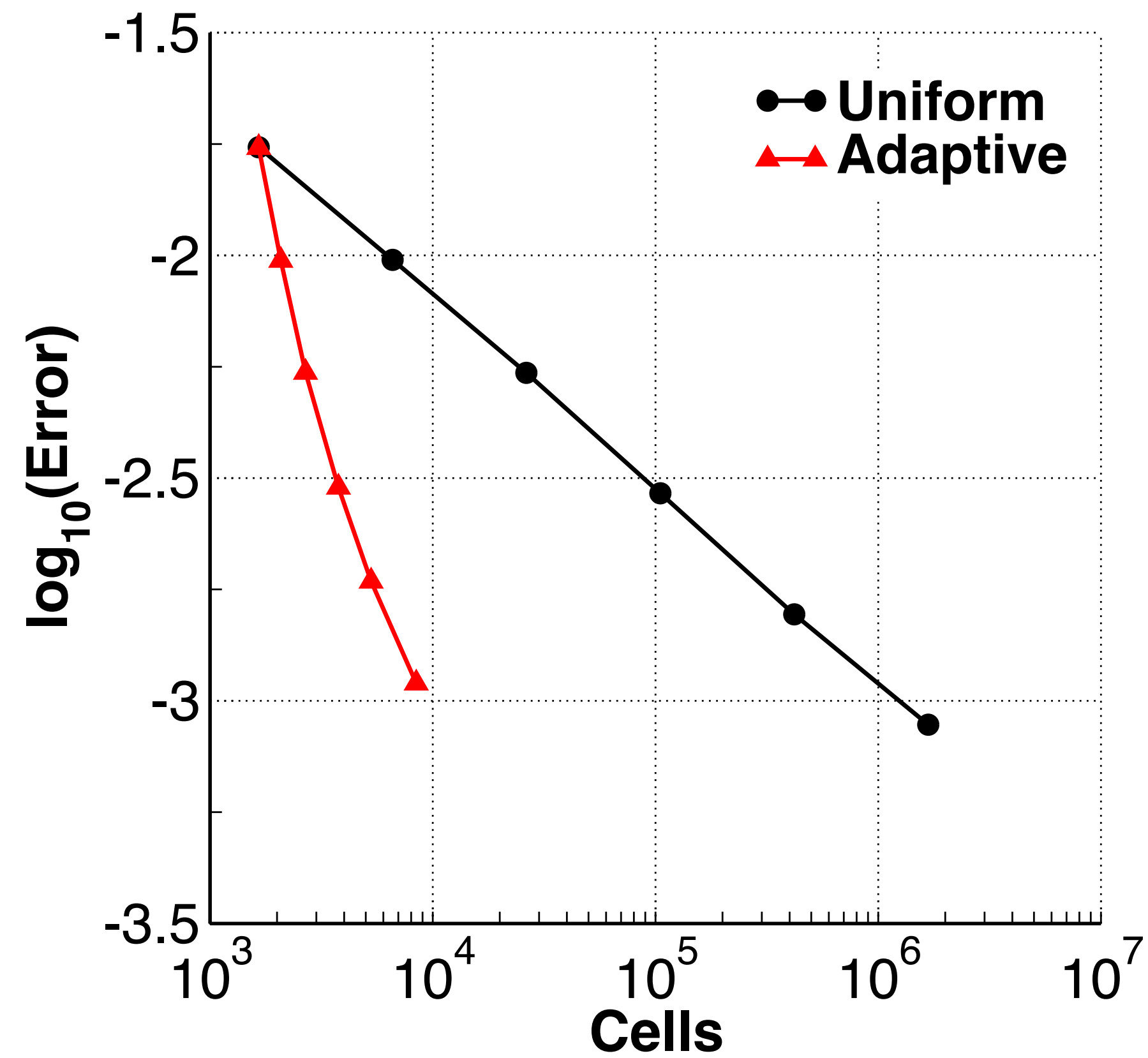
Adaptation Cycle: 4

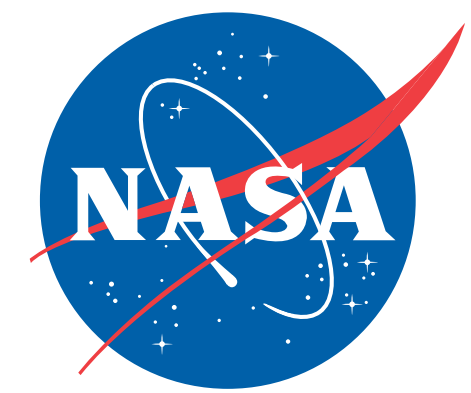




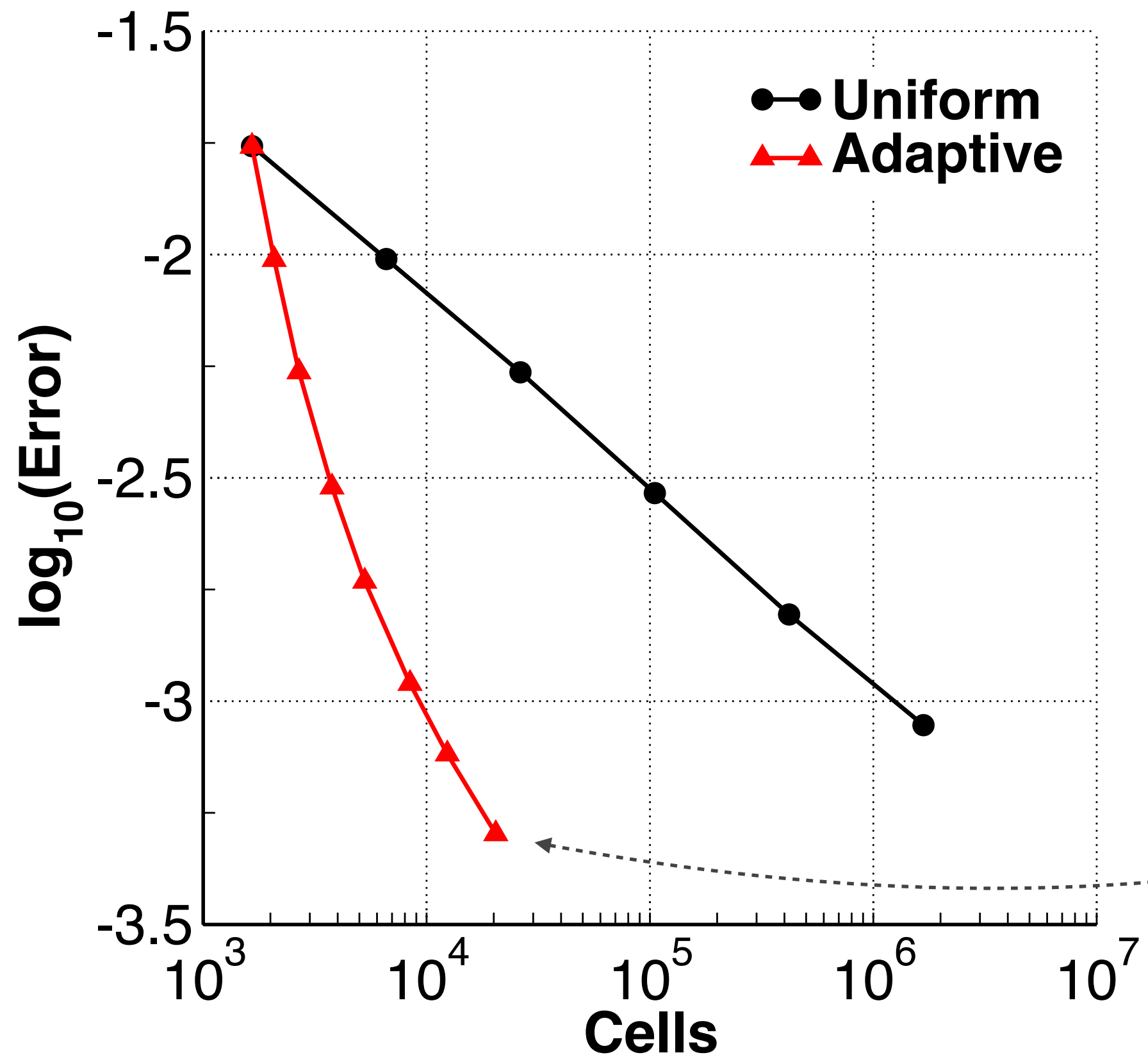
Adaptive Refinement

Adaptation Cycle: 5

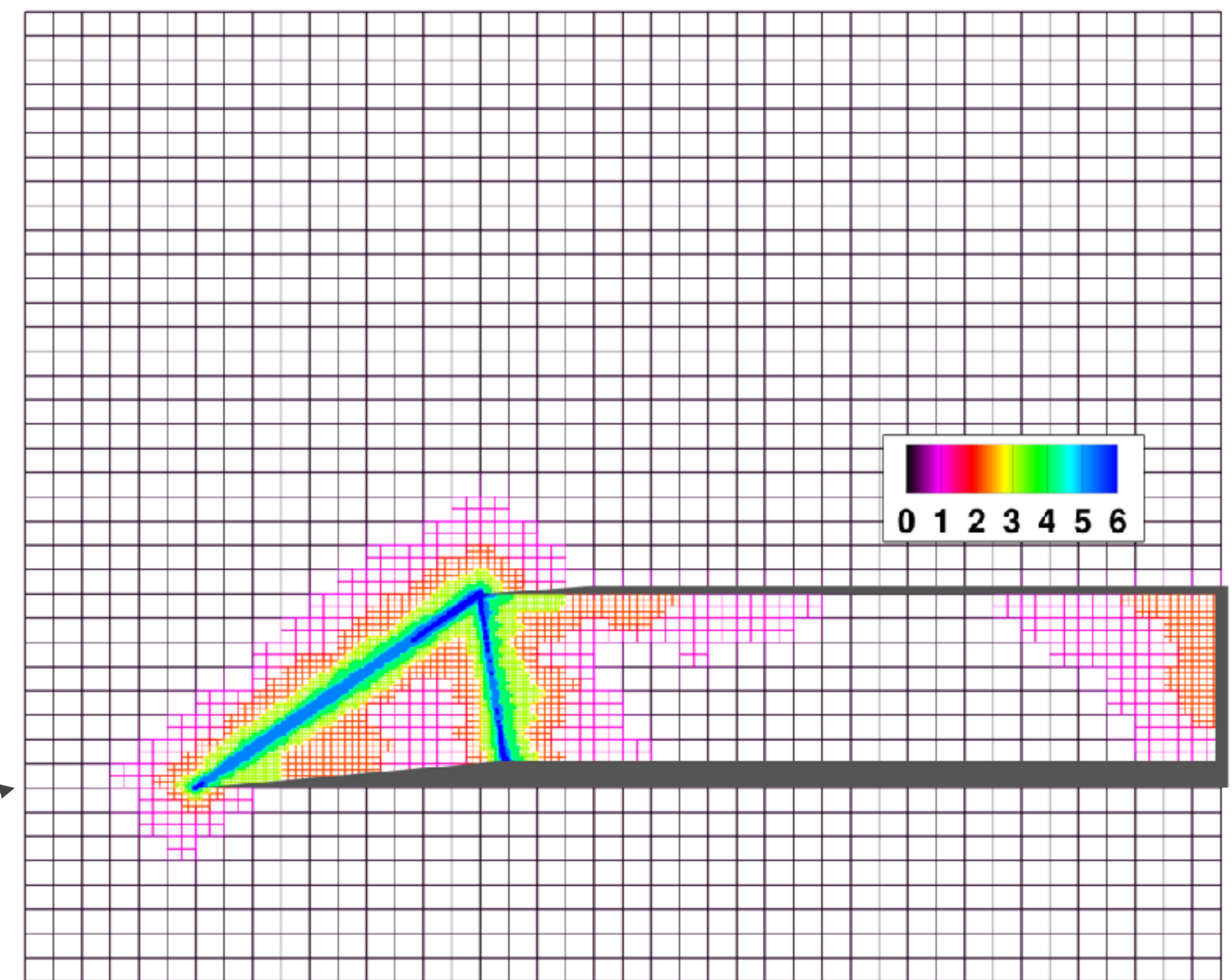


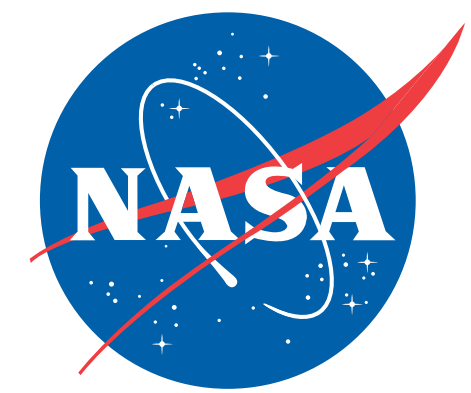


Adaptive Refinement



Final Mesh





Adaptation Convergence History

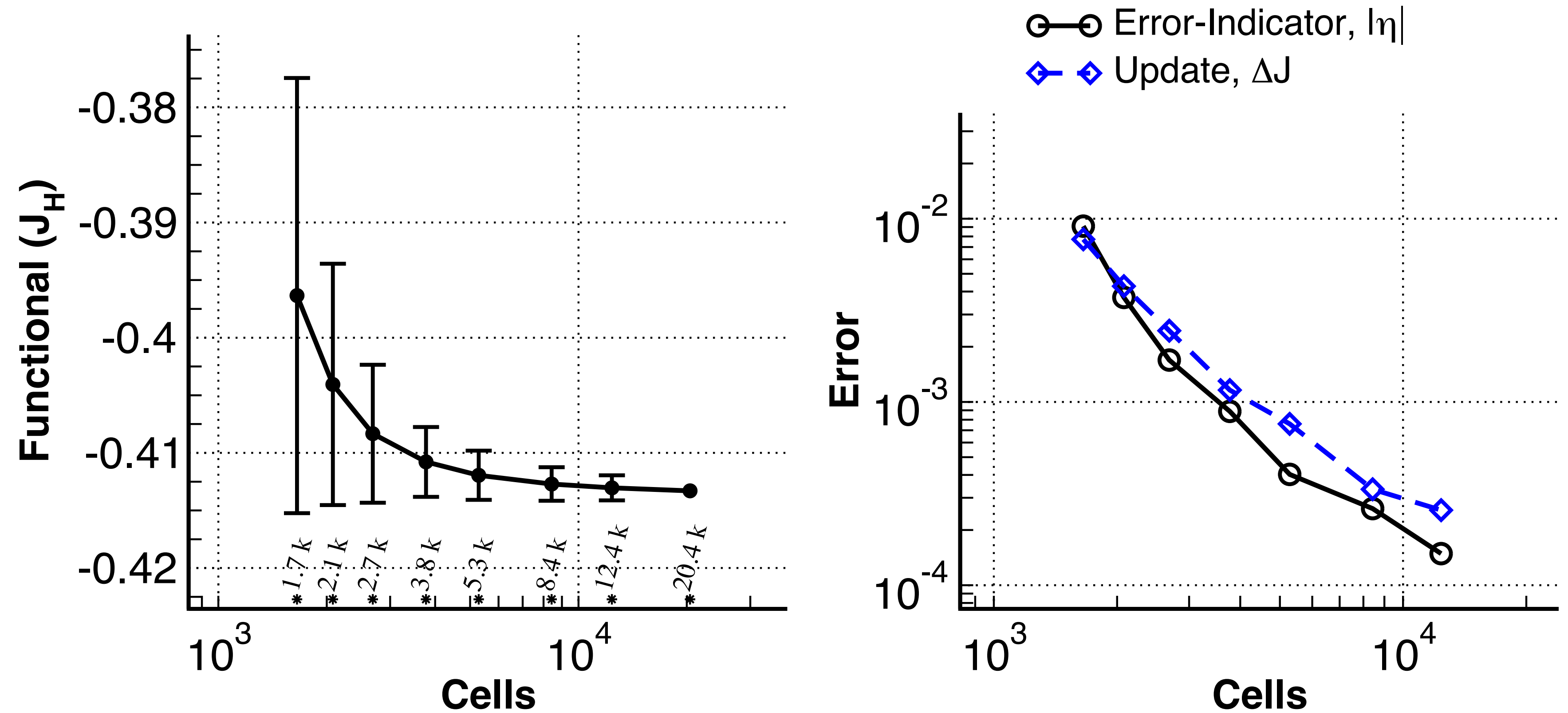
Error Bars

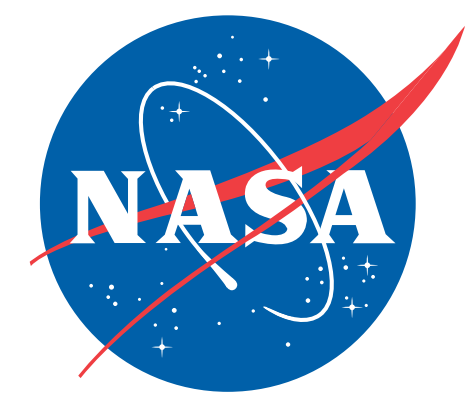
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$$J_c = J_h(\mathbf{Q}_L) - \psi_{TQ}^T \mathbf{R}_h(\mathbf{Q}_L)$$

Error Indicator

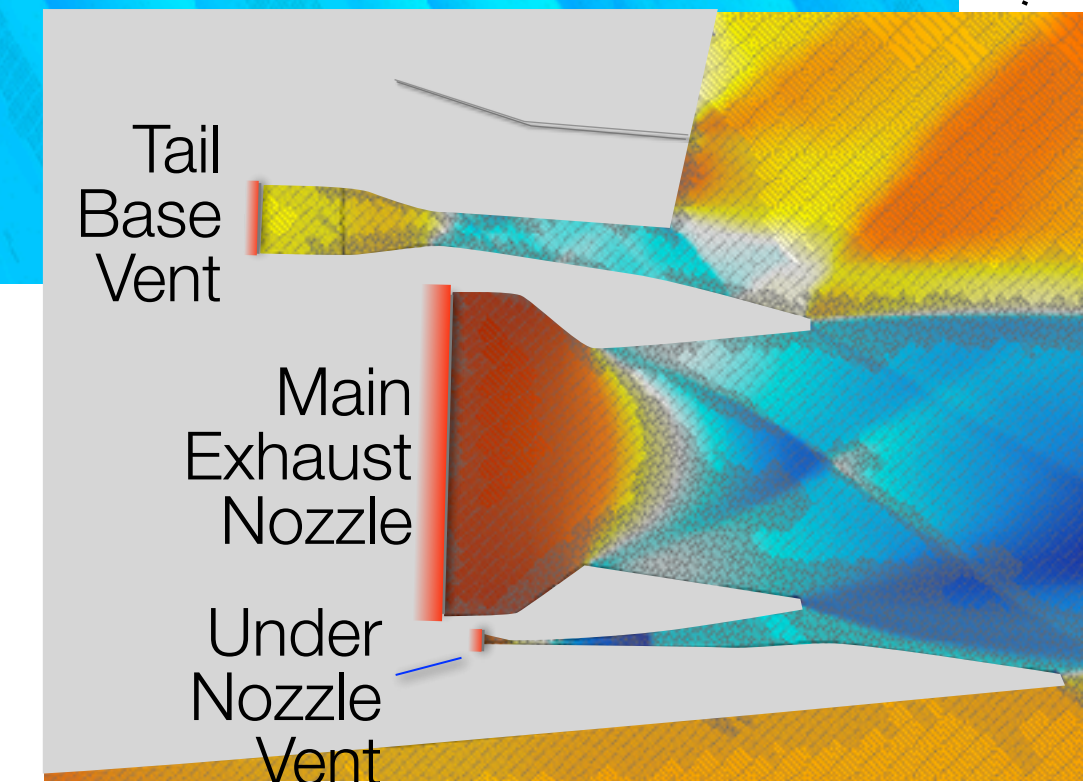
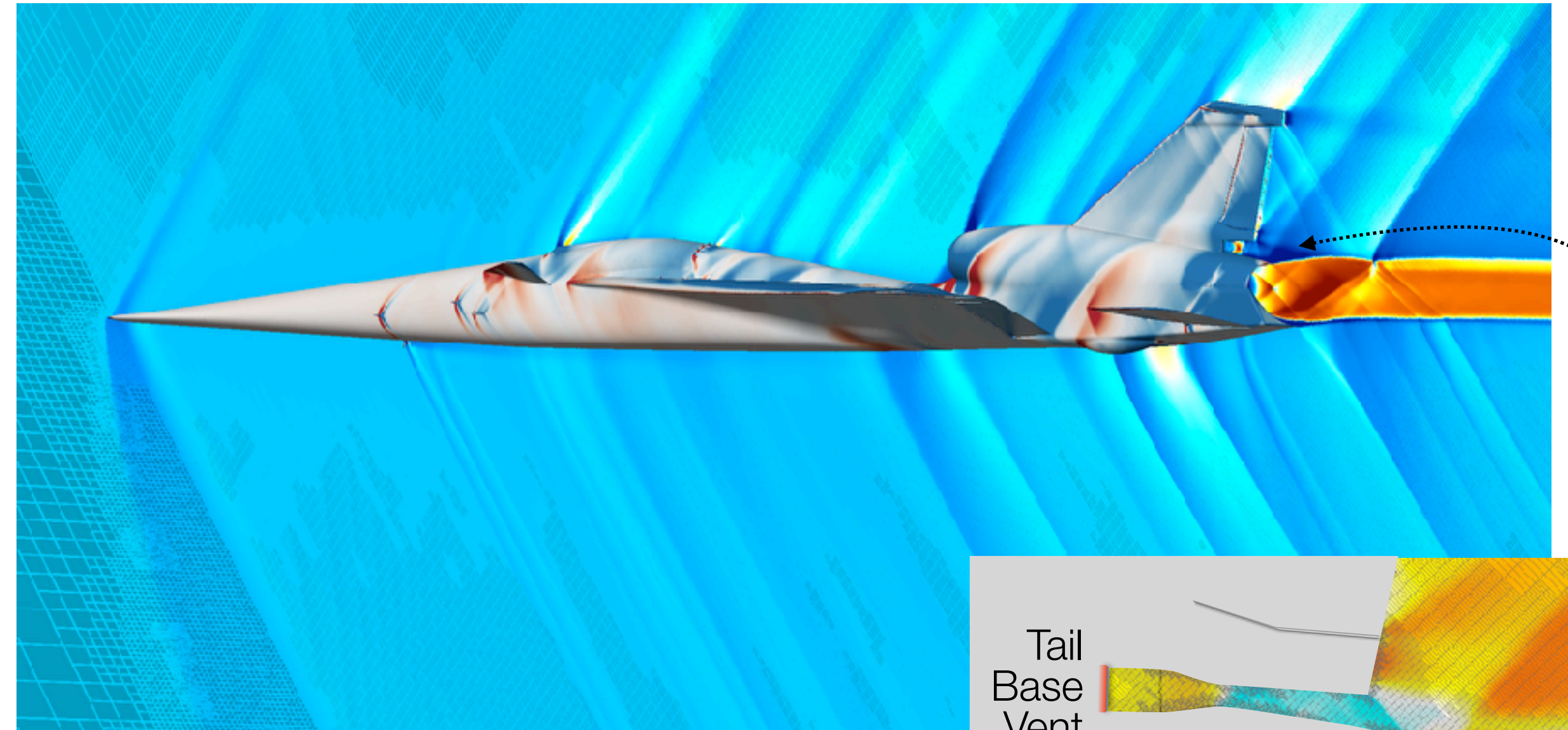
$$\eta_H = \left| (\psi_{TQ} - \psi_{TL})^T \mathbf{R}_h(\mathbf{Q}_L) \right|$$





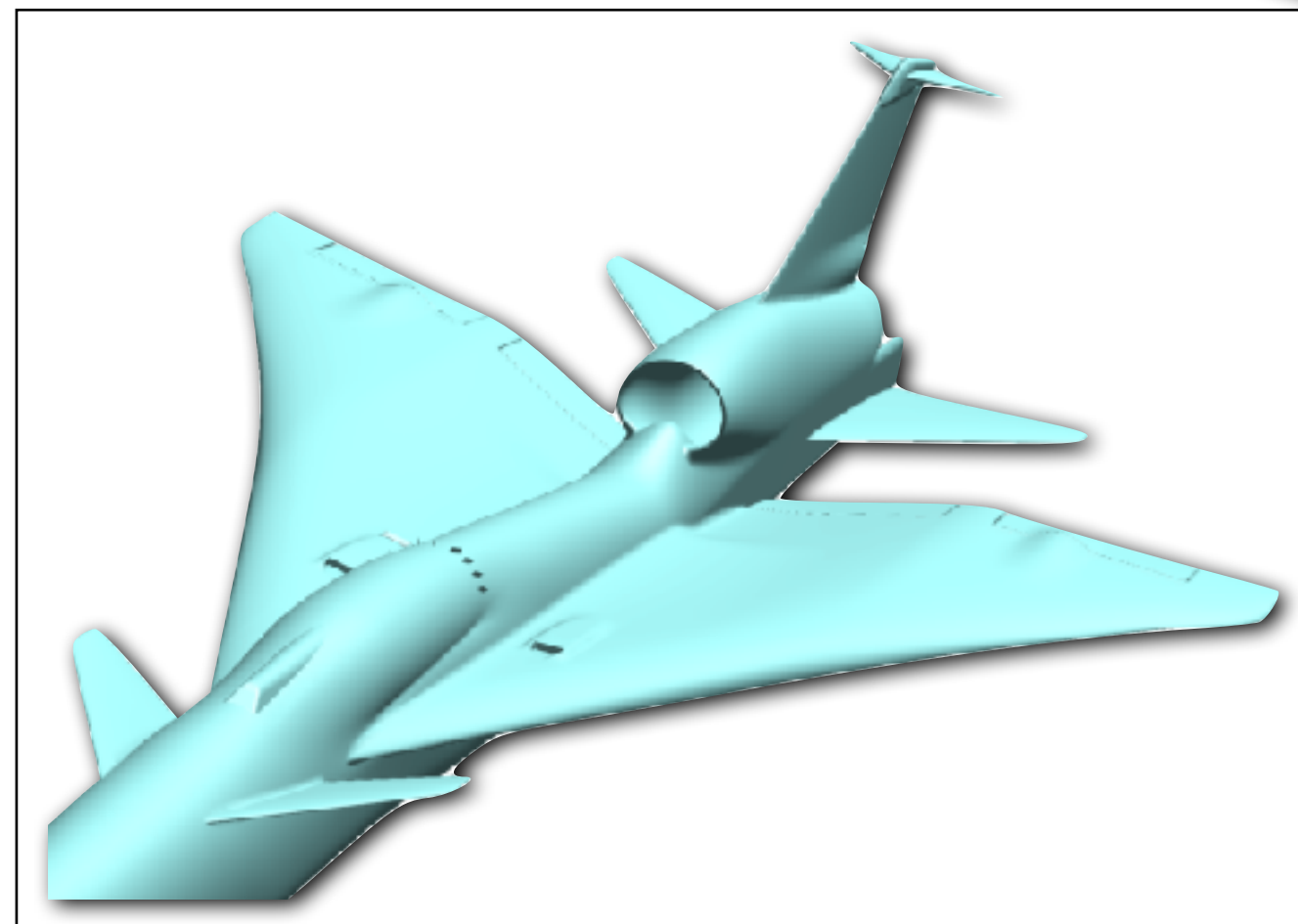
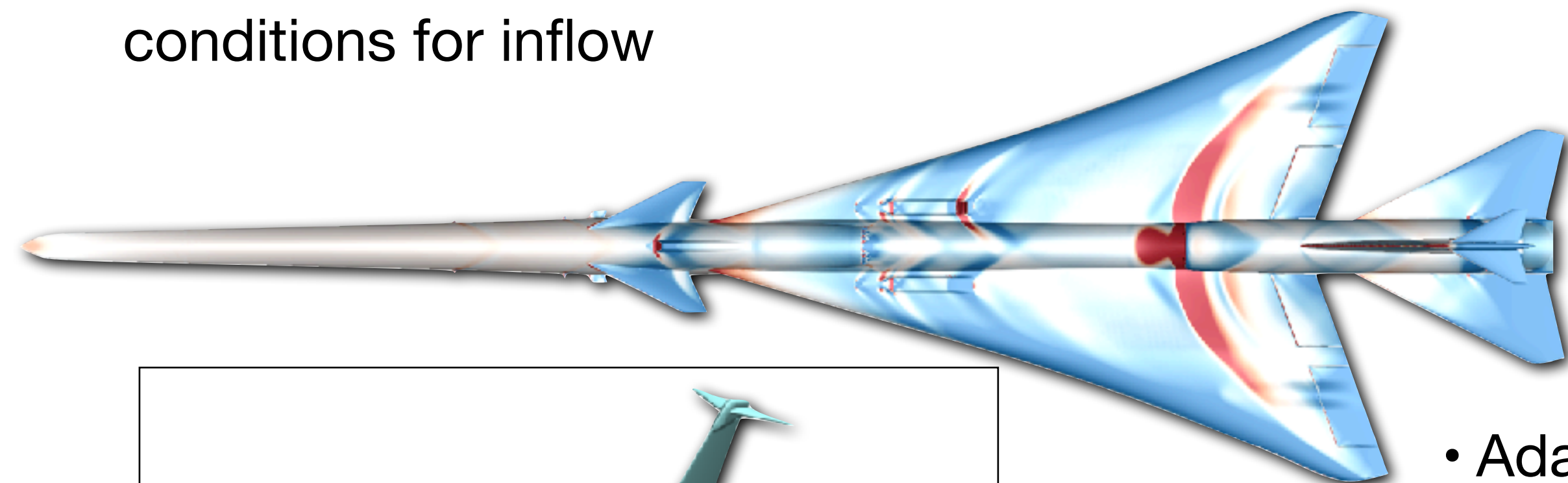
X-59 / LBFD Prototype Test Case

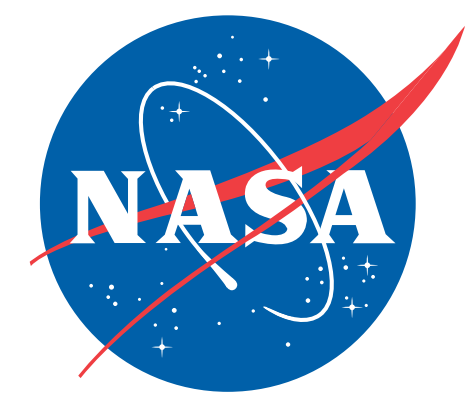
- Typical analysis case: $M=1.4$ and $\alpha = 2.05^\circ$
- Assess accuracy of simulations with and without mass-flow-rate outputs
- 3 inlets and 4 exhausts
- Specified exit pressure outflow and stagnation conditions for inflow



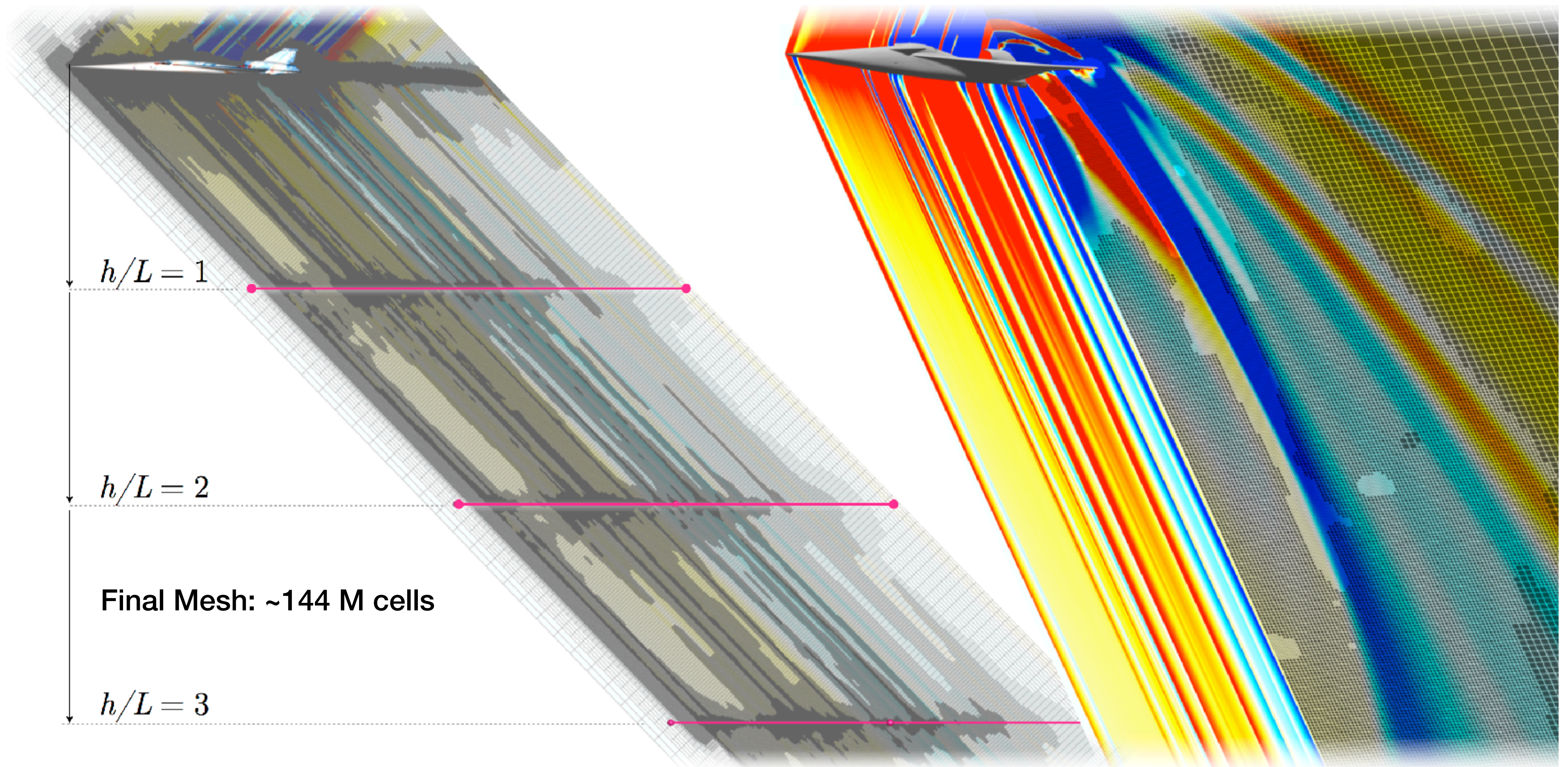
- Adaptation functional is a combination of off-body line sensors and mass flow rates

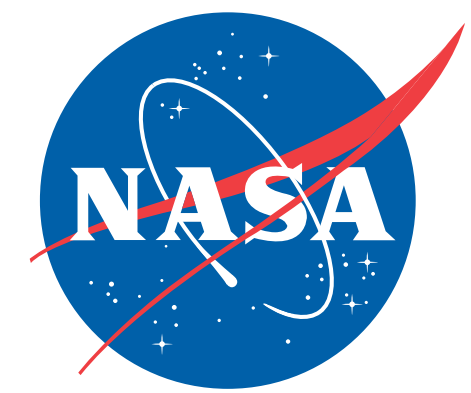
$$J = w_l J_l + w_m J_m$$
$$J_l = \int_0^L \left(\frac{\Delta p}{p_\infty} \right)^2 ds$$
$$J_m = \int \rho U_n dA$$





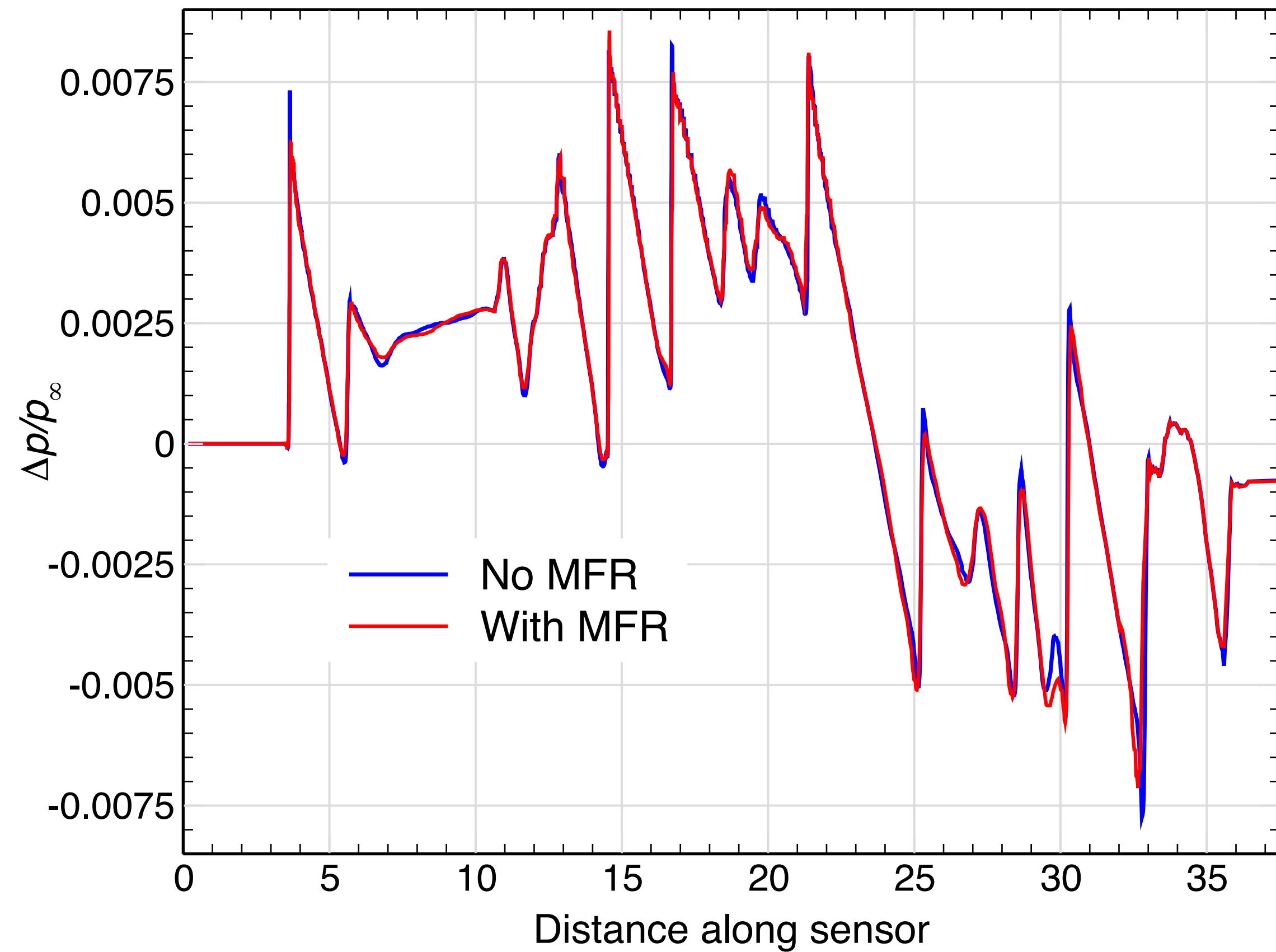
Adapted Mesh for Multiple Sensor Locations



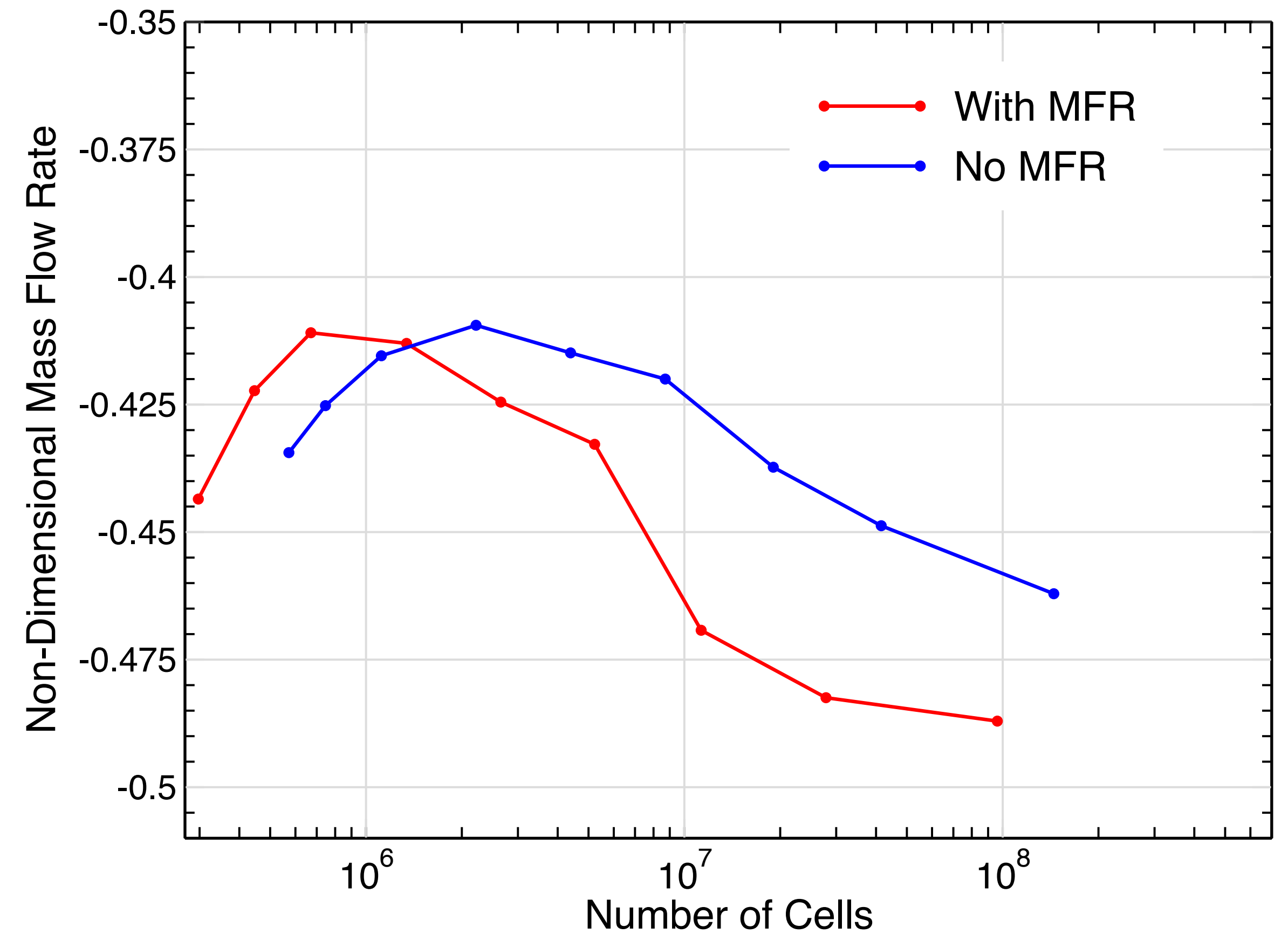


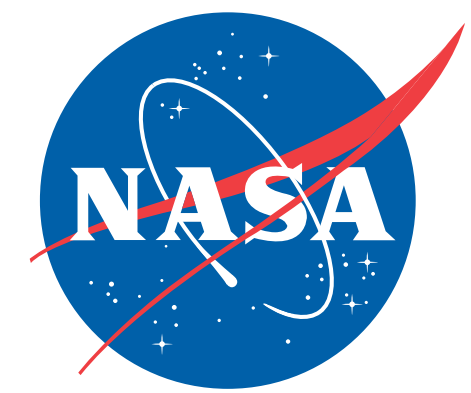
Output Convergence

Pressure Signature at h/L=3

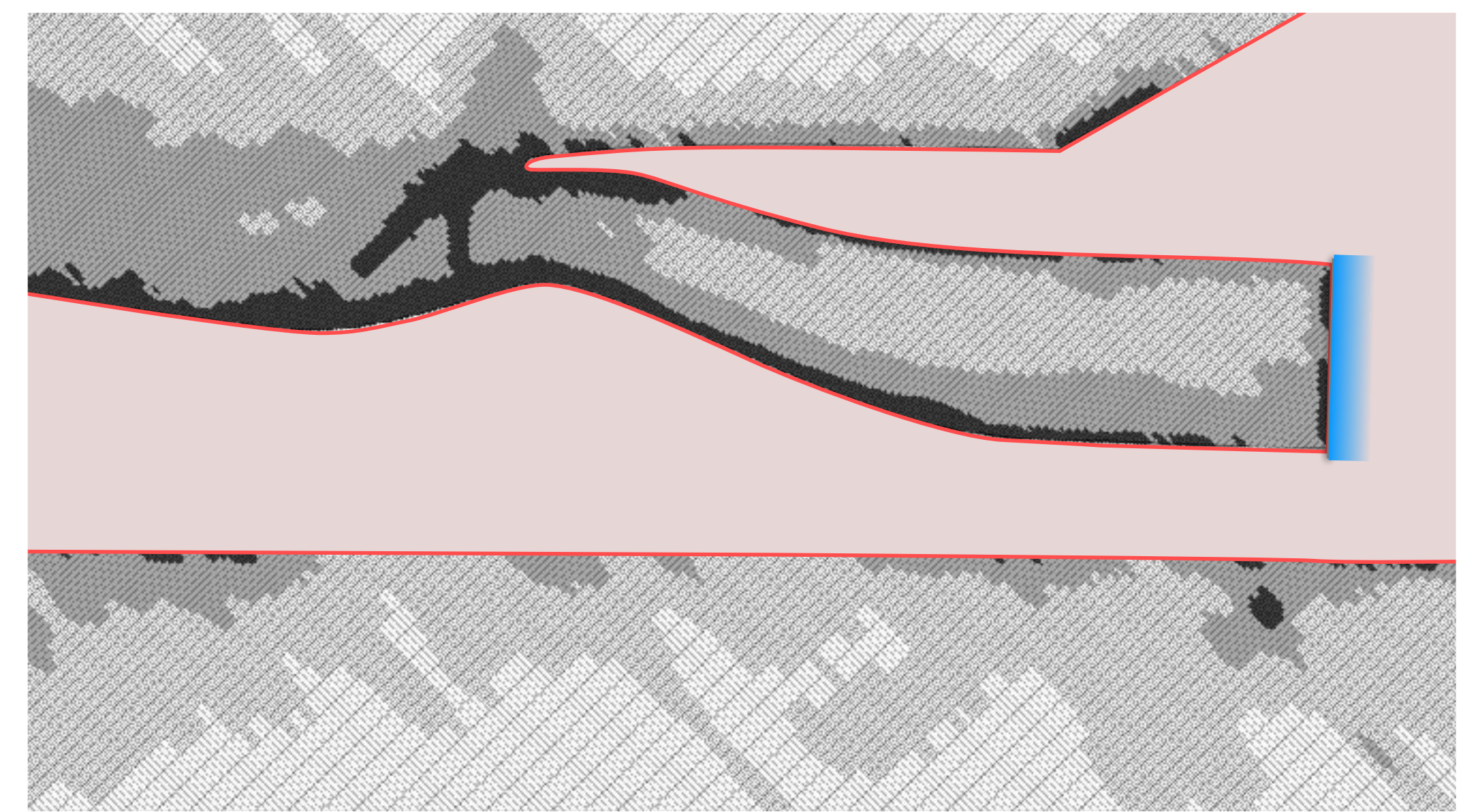
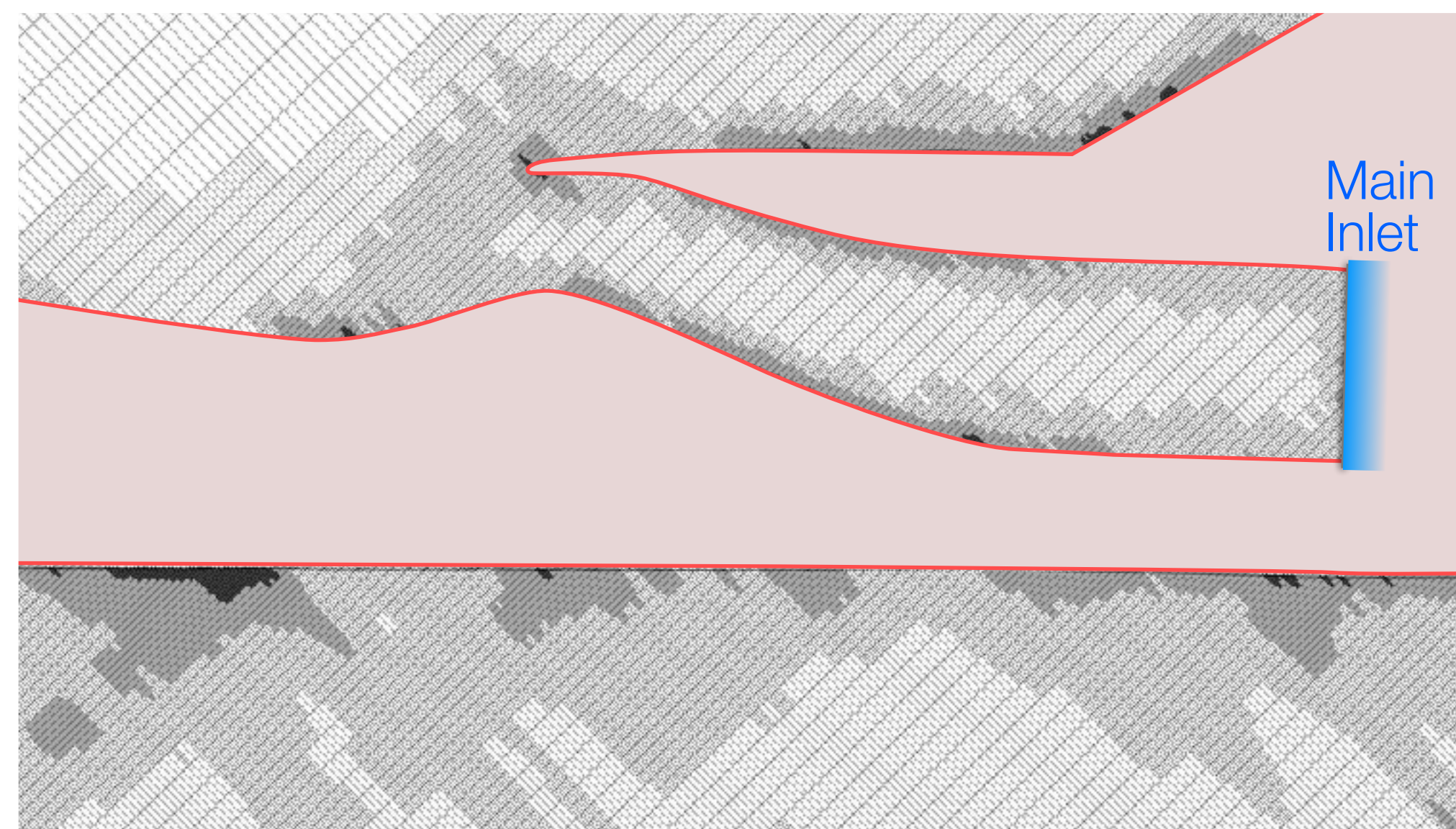
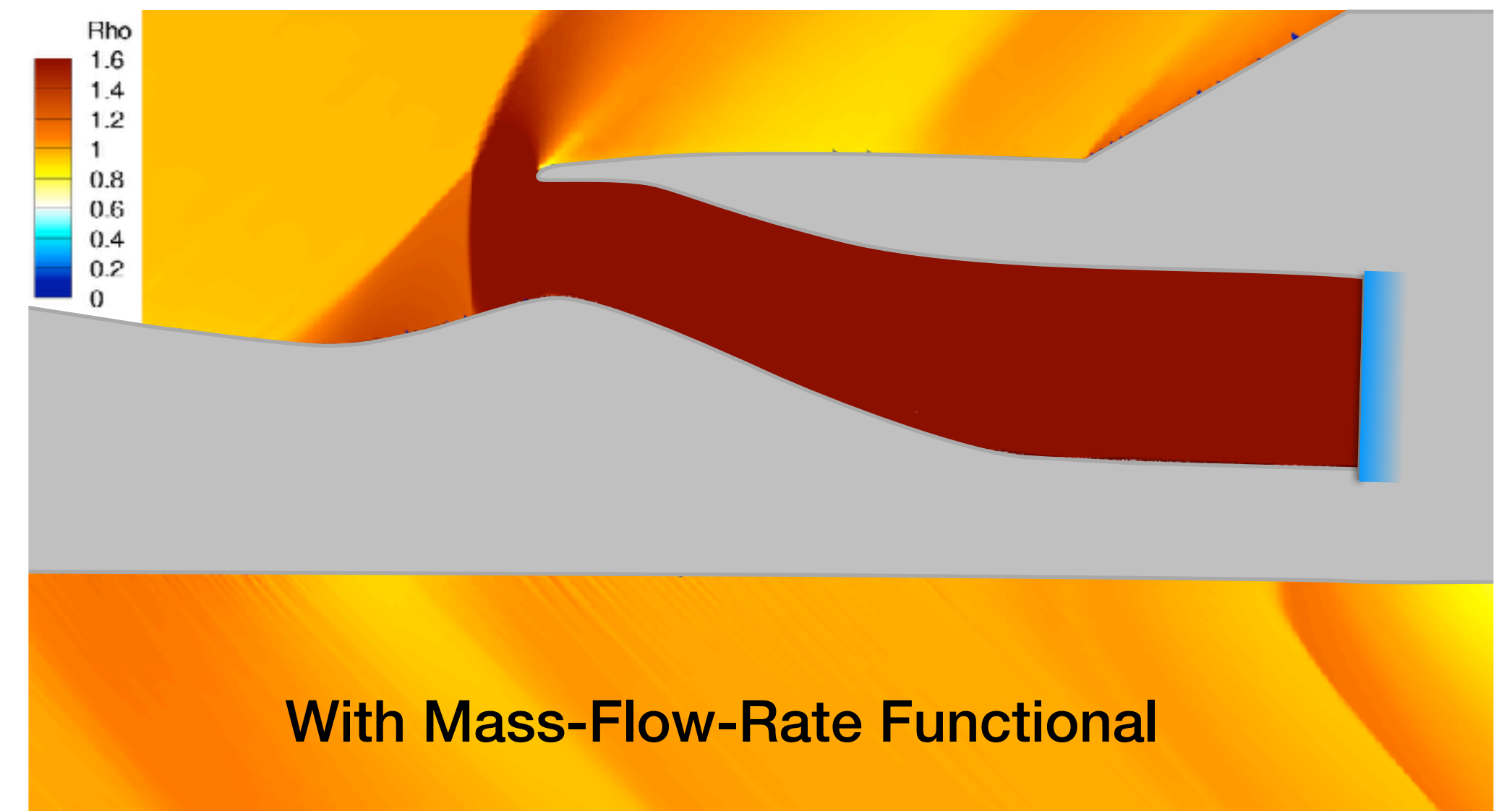
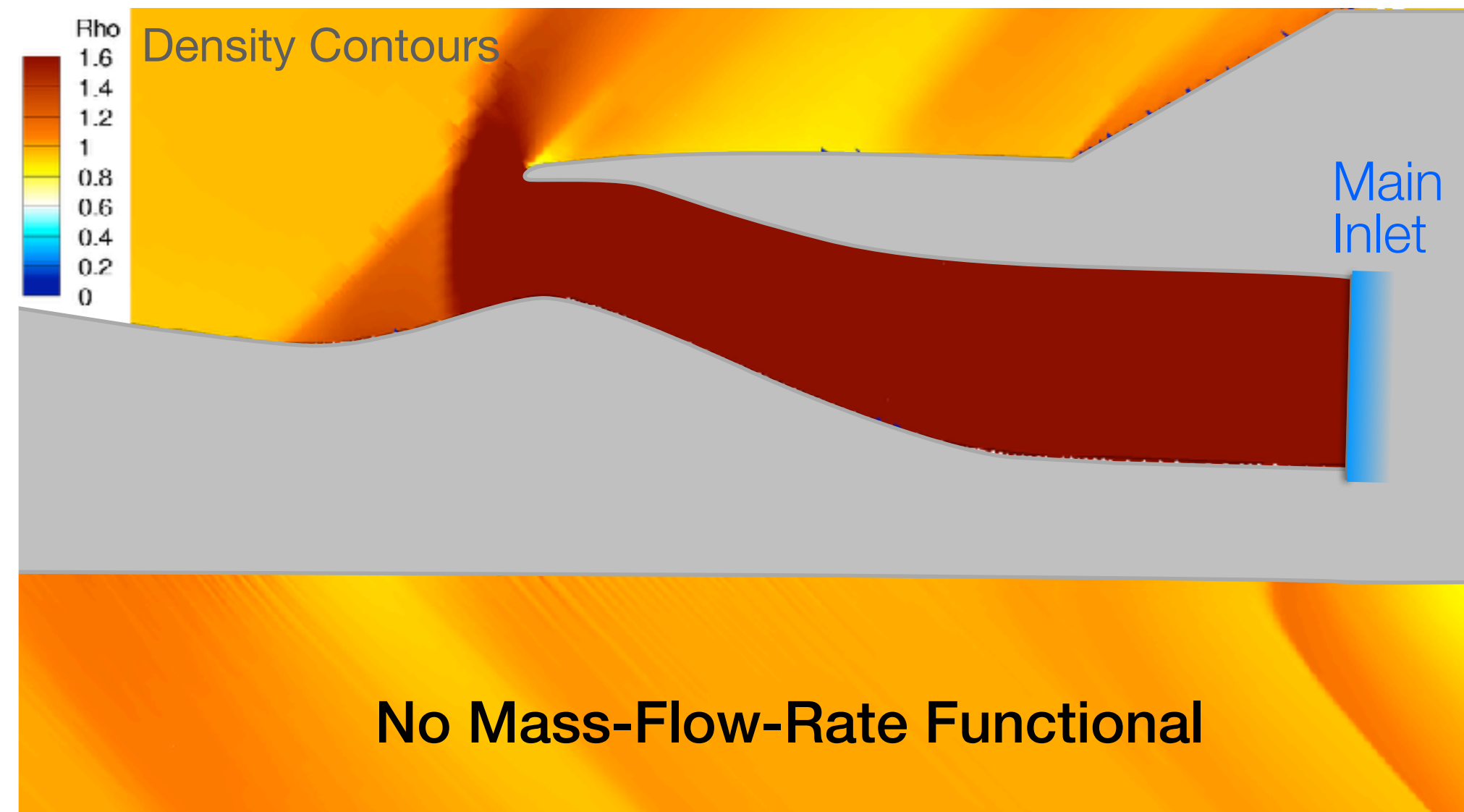


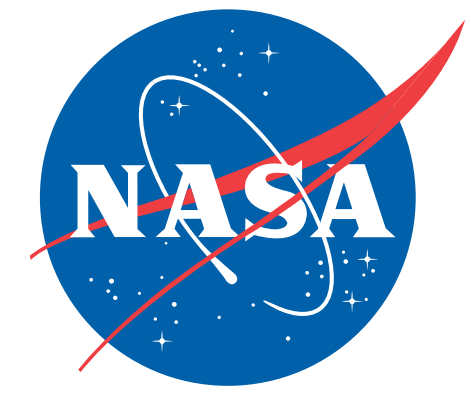
Engine-Inlet Mass Flow Rate





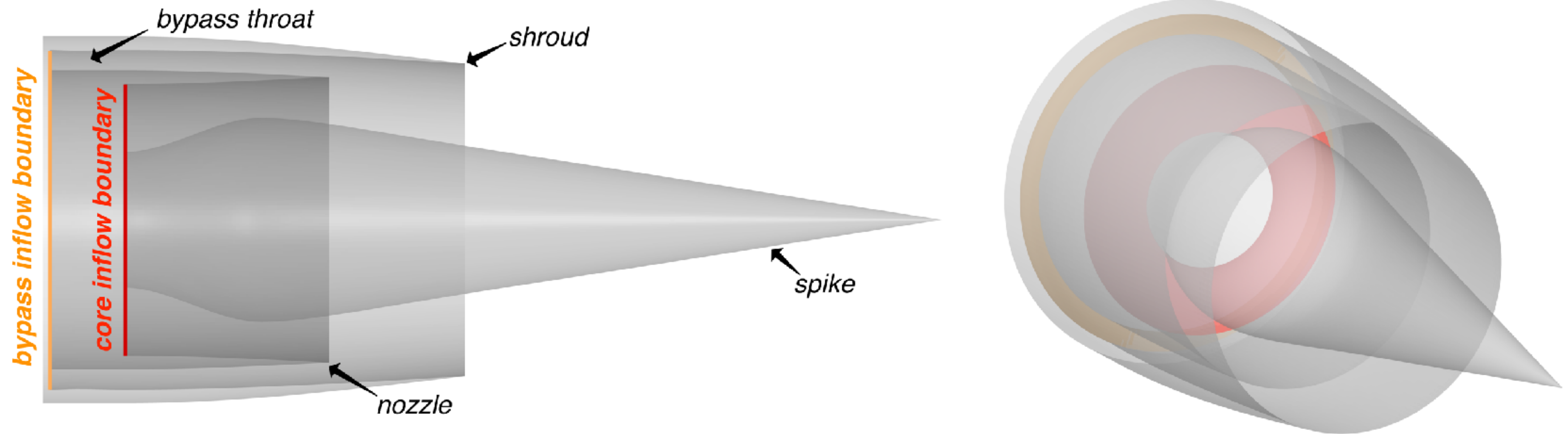
Comparison of Flow Solution and Mesh



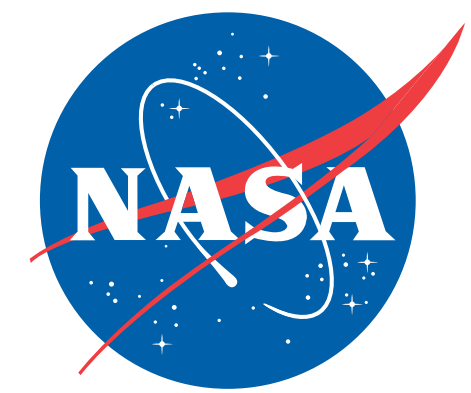


Supersonic Nozzle Shape Optimization

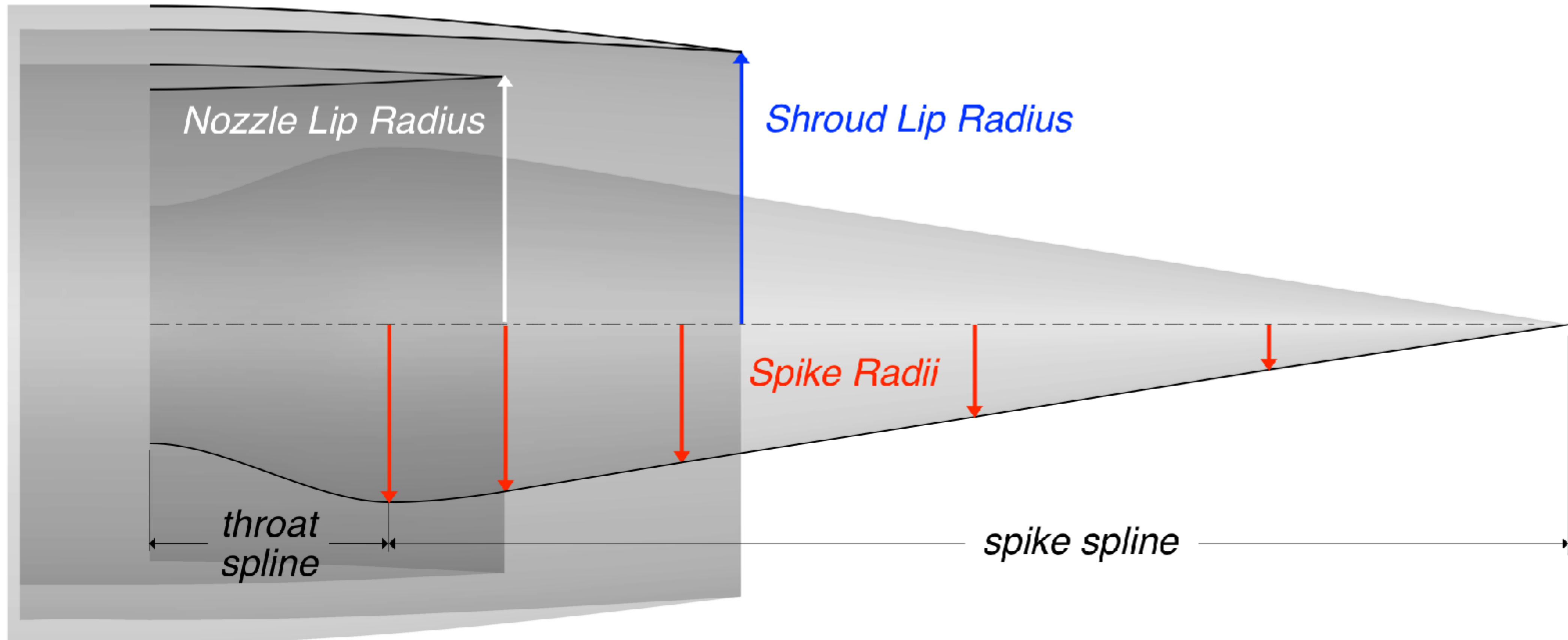
Dual-Stream Supersonic Spike Nozzle



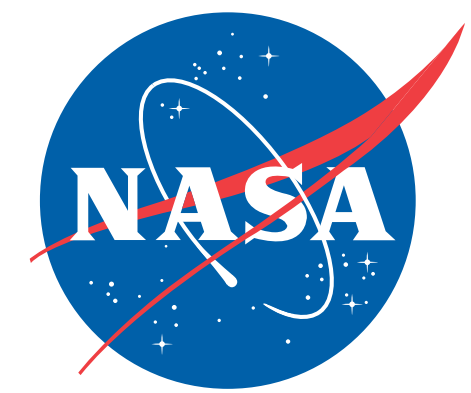
- $M=1.4$
- 2 inflow boundaries: hot core stream and cooler bypass stream
- Goal is to maximize thrust and minimize nearfield shock disturbances subject to fixed mass flow rates



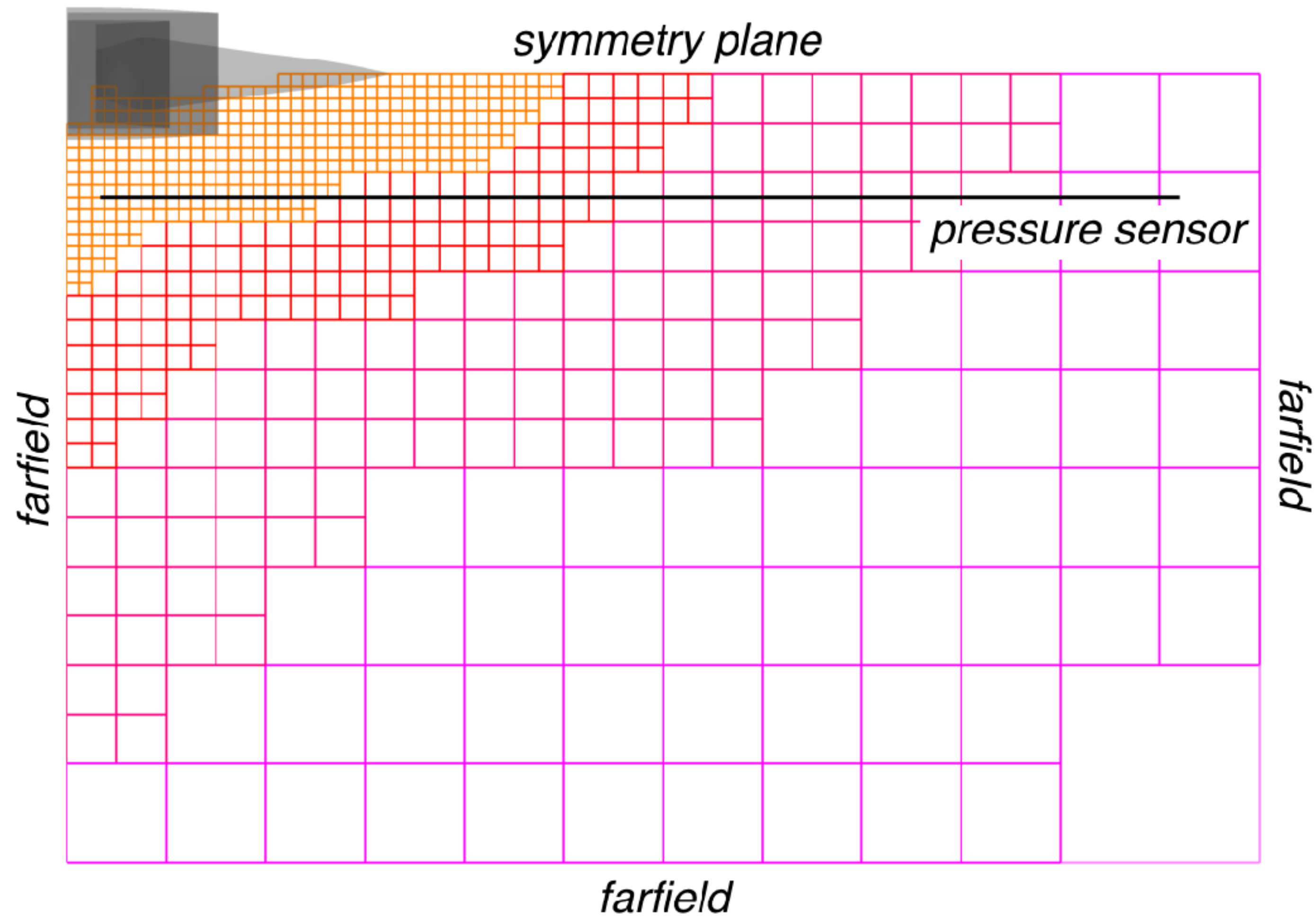
Design Variables

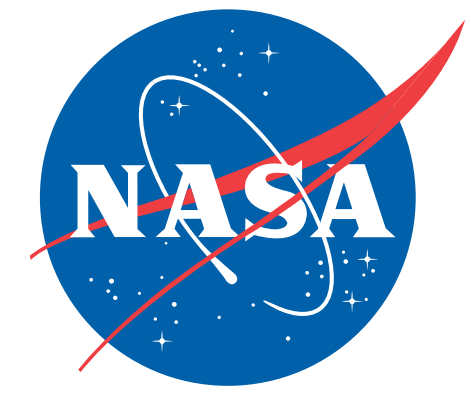


- Design Variables: 7
- Fixed length and minimum radii bounds

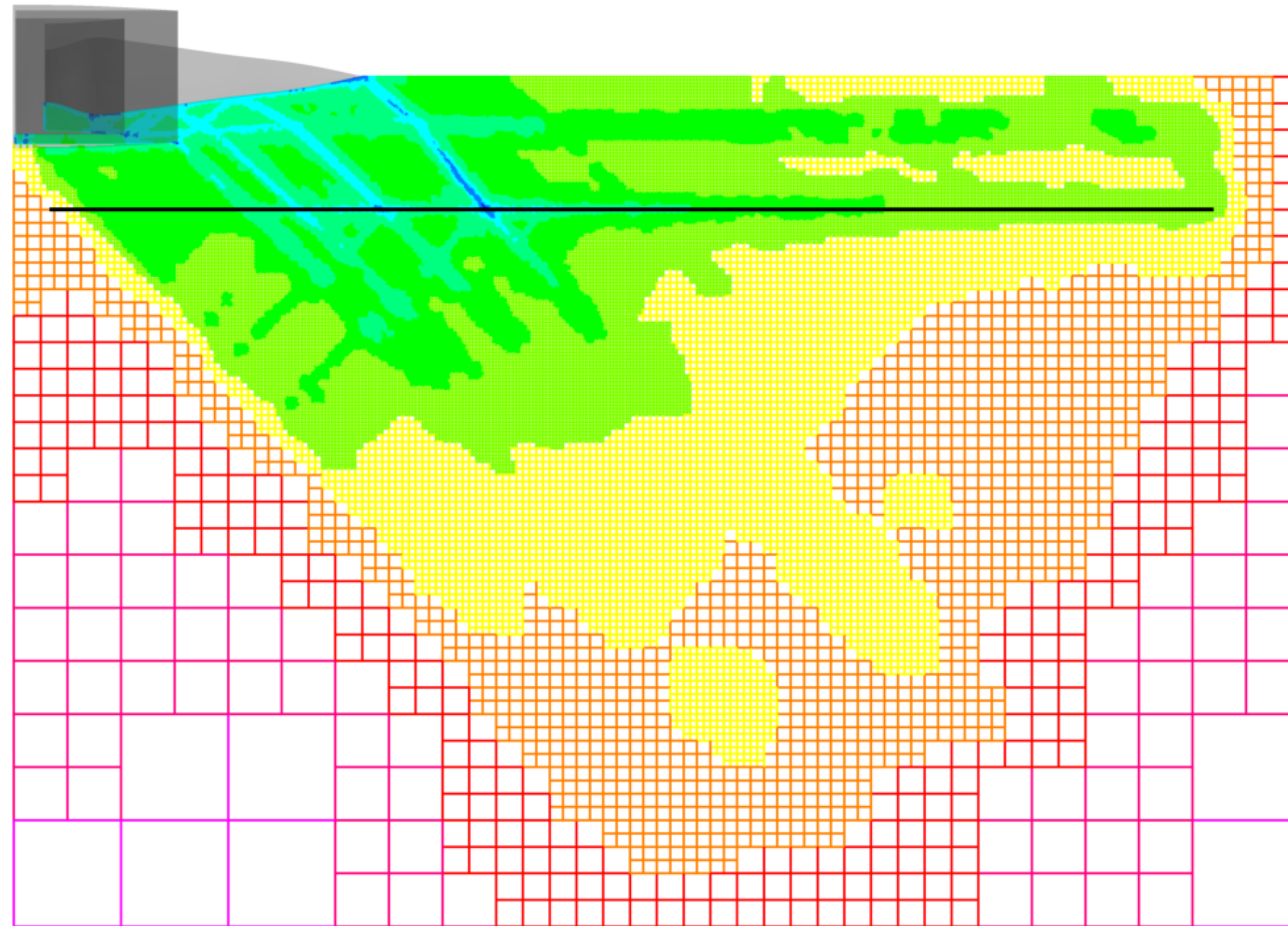


Initial Mesh and Computational Domain

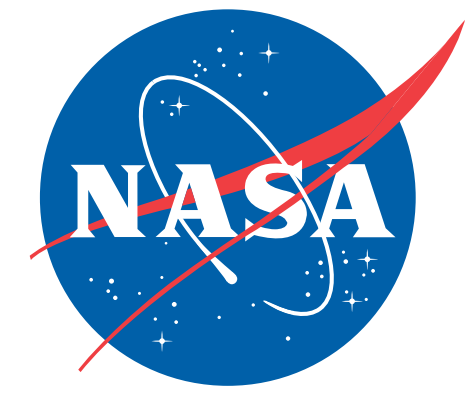




Final Mesh for Baseline Design

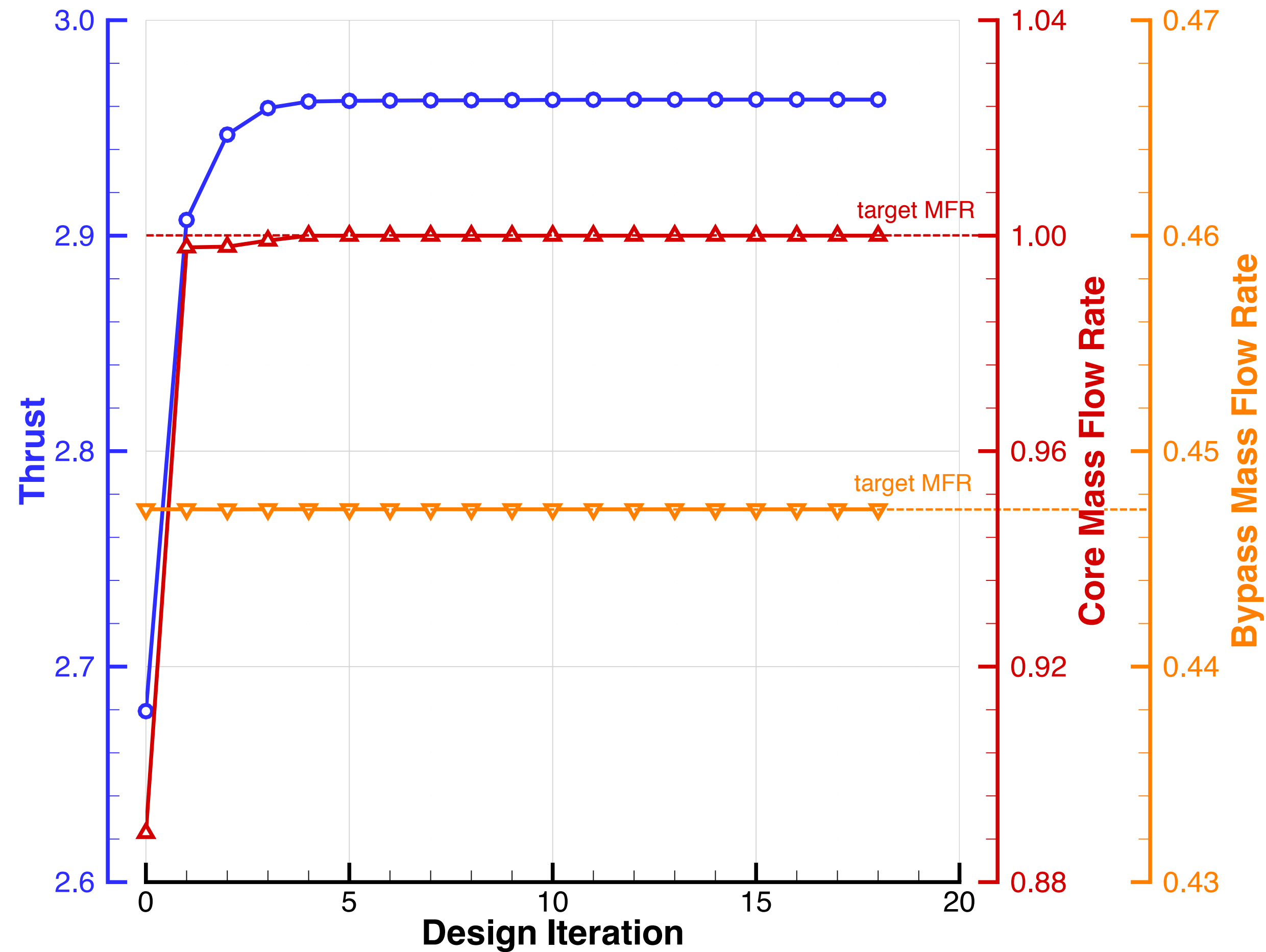


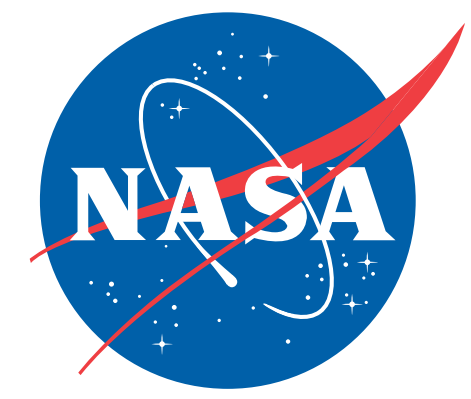
- Each design iteration uses 8 mesh adaptations
- Final mesh ~ 20M cells
- Adaptation functional is sum of thrust, mass flow rates, and line sensor



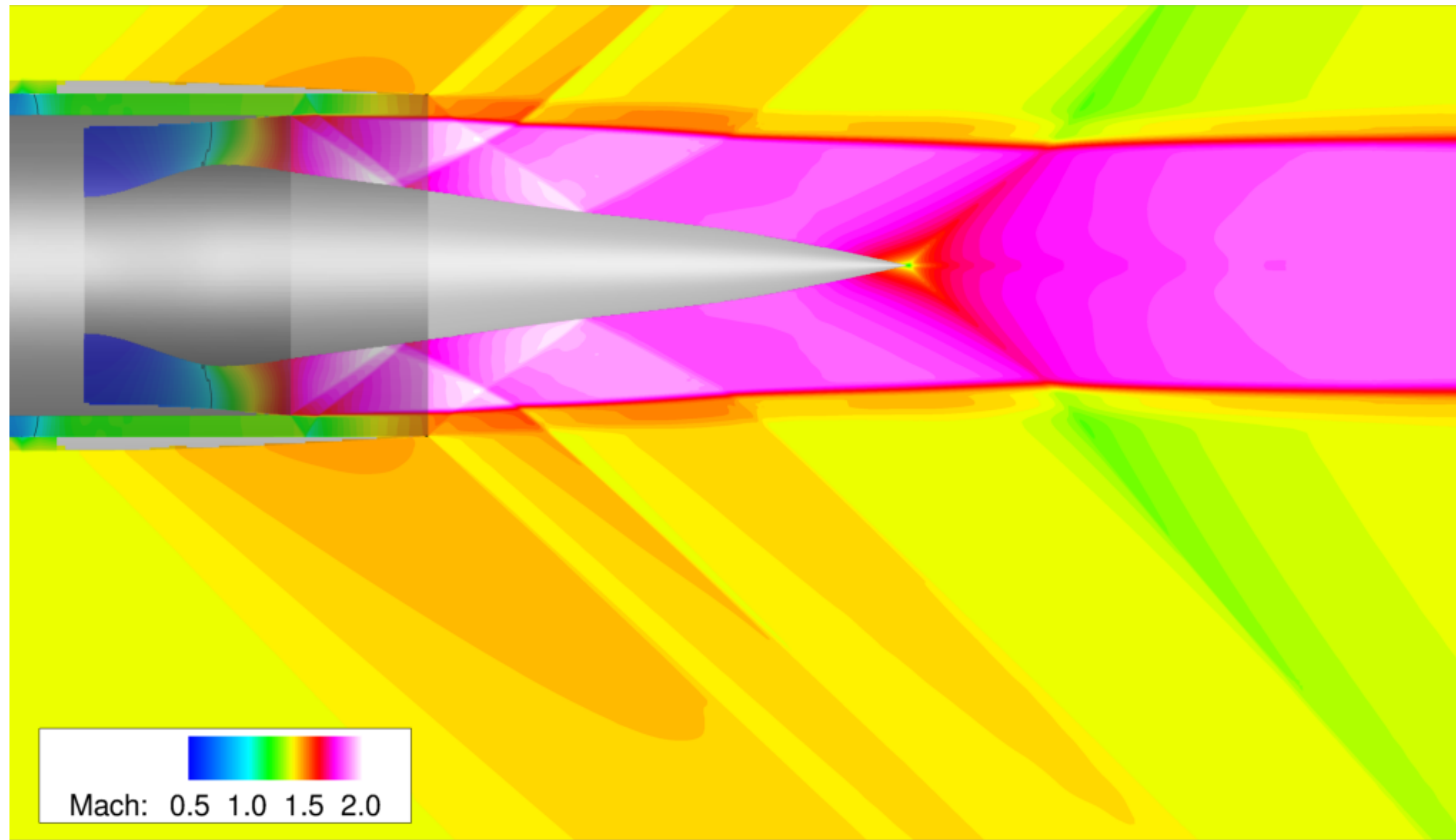
Optimization Convergence History

Baseline optimization: Maximize Thrust

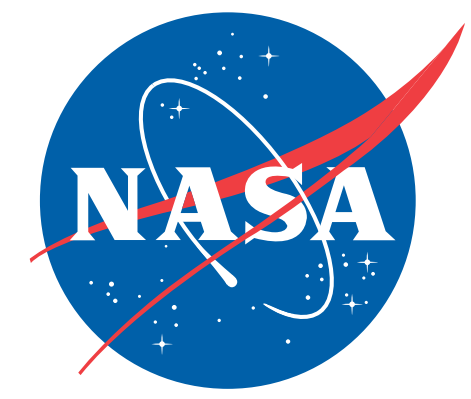




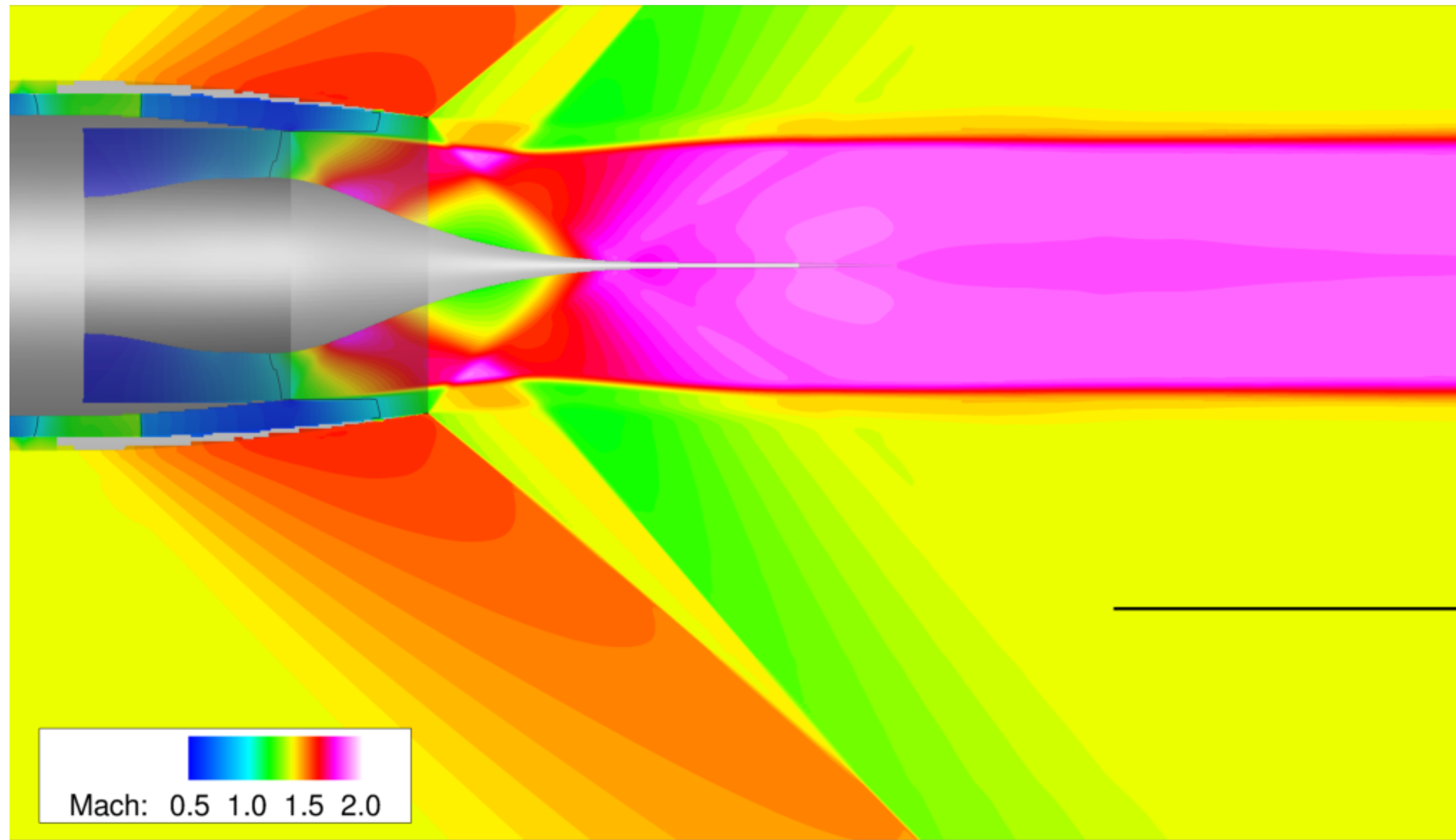
Maximize Thrust



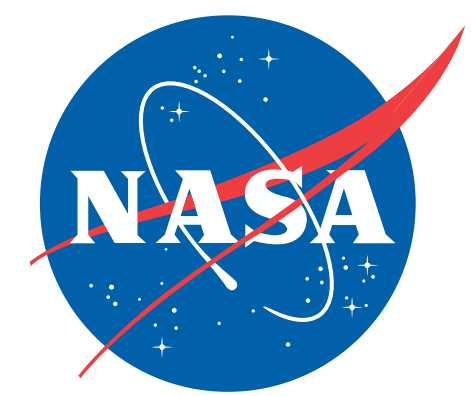
Several strong shocks in nearfield from cowl, shroud and spike tip



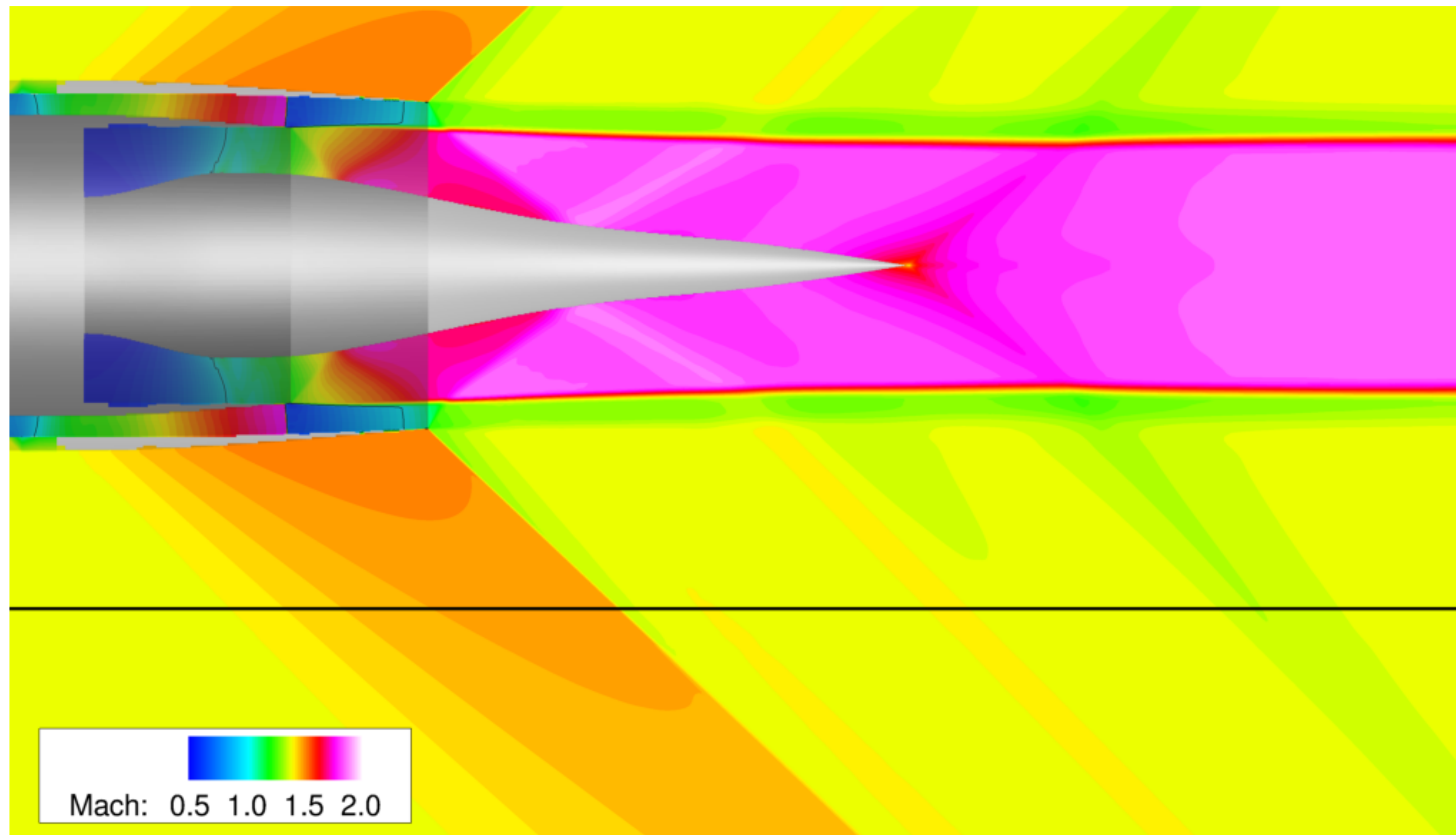
Maximize Thrust and Eliminate Aft Shock



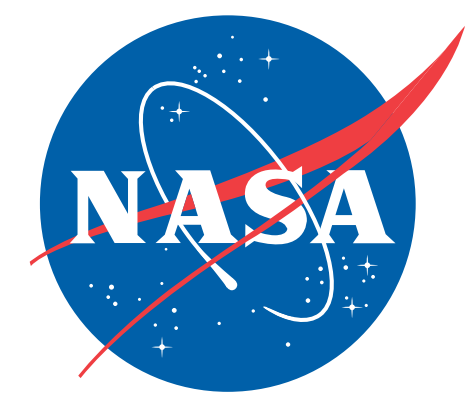
Shock-free at spike tip, but thrust reduced by 2.7%



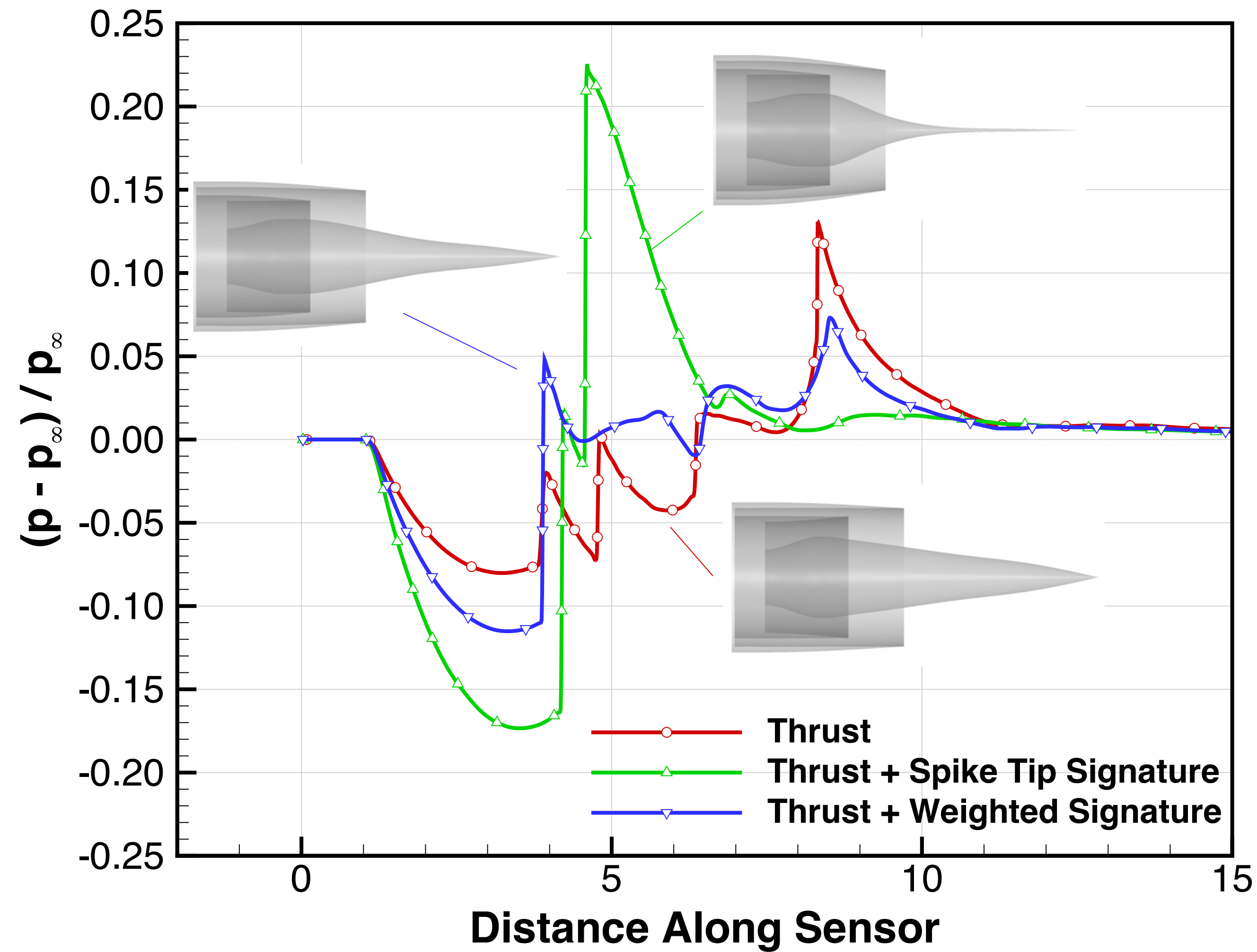
Maximize Thrust and Attenuate All Shocks

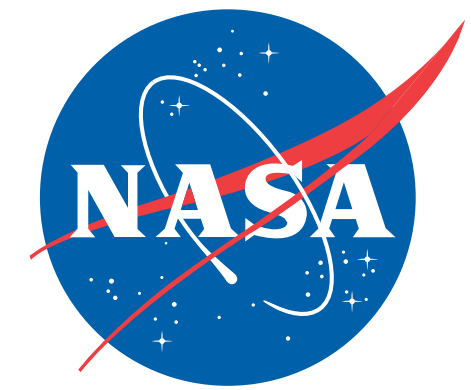


Weak boat-tail and spike-tip shocks, and thrust within 1.7% of baseline



Comparison of Pressure Signatures





Conclusions

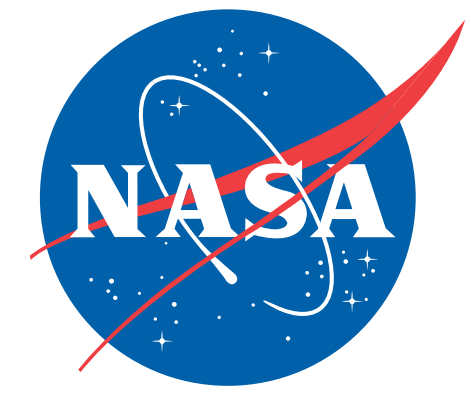
Reliable evaluation of mass flow rates at permeable boundaries

- Adjoint consistent implementation of permeable boundary conditions
- Numerical studies show no spurious oscillations in the near-wall adjoint
- Verification test problem demonstrates convergence to the exact solution at the expected rate
- *Specifying mass-flow-rate outputs in practical, low-boom simulations significantly improves prediction of these outputs without compromising pressure-signature accuracy*

New capability to handle design optimization problems subject to mass-flow-rate constraints

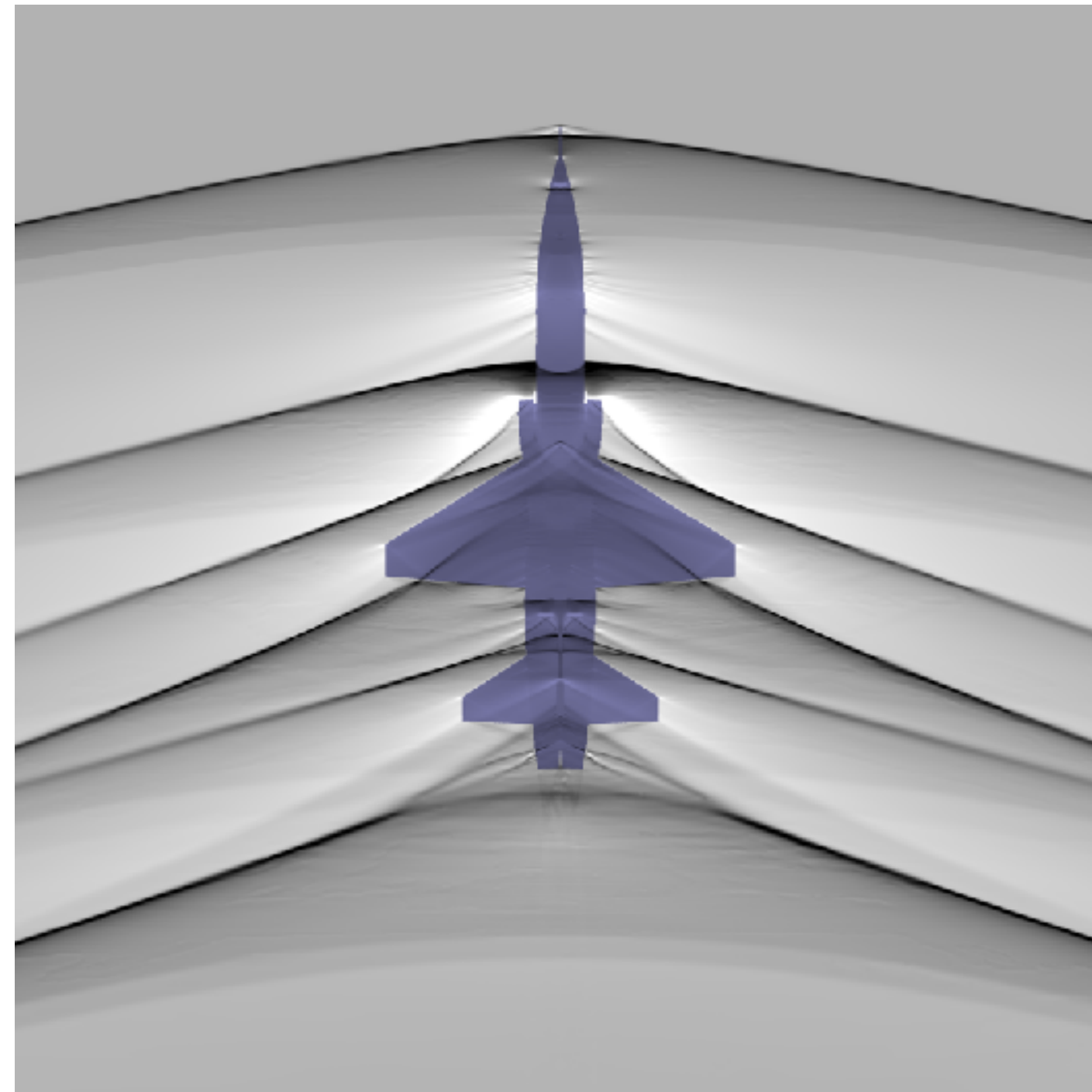
- Efficient reuse of adjoint solutions and error control in low-boom shape optimization

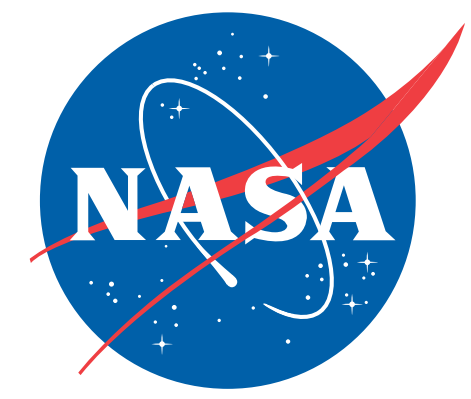
Next step: Investigate adjoint consistency of more general outputs, e.g. total pressure recovery and flow distortion



Acknowledgements

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Questions?



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