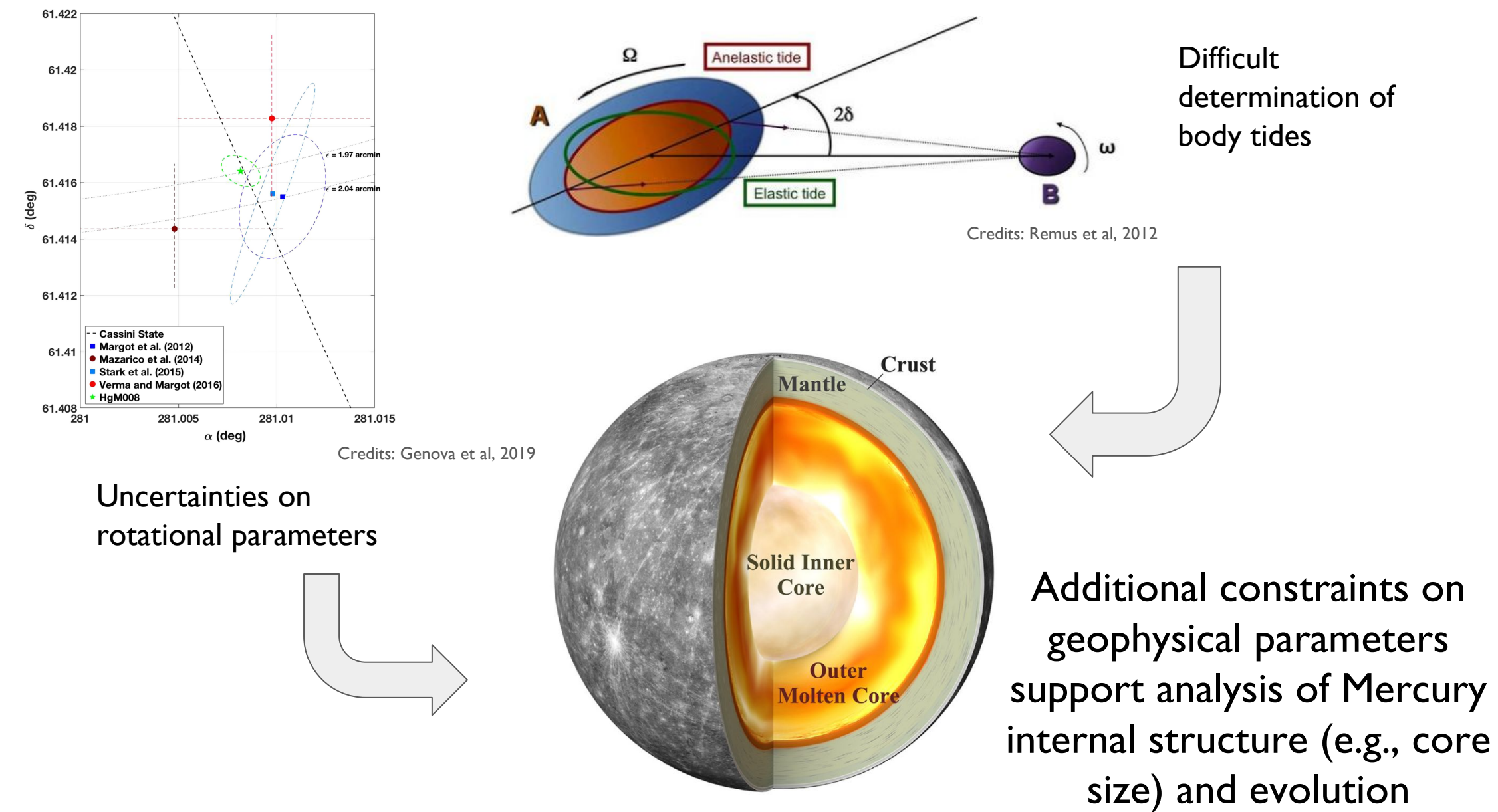


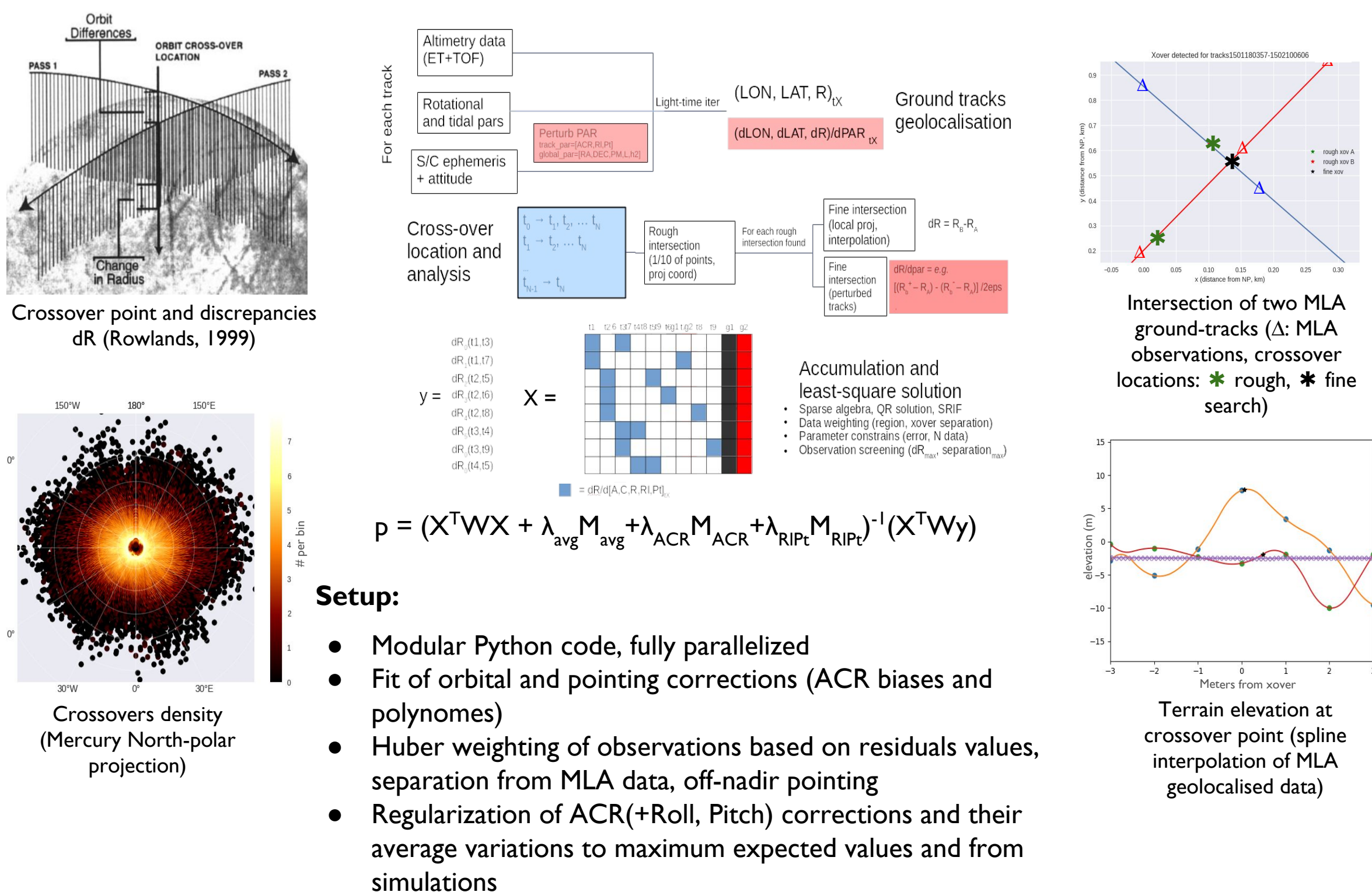
## A. Open questions in Mercury geodesy



## B. Overview of MLA crossovers analysis

- Based on MESSENGER's Mercury Laser Altimetry (MLA) dataset, we improve Mercury geodetic parameters via least squares minimization of crossover discrepancies;
- Simulation and analysis of synthetic MLA data (see C): validation, find an appropriate orbit parametrization and error assessment;
- Solution of Mercury pole RA, DEC coordinates, prime meridian (PM) rate and librations (L) using the full MLA dataset (3.7 millions of crossovers, 2011-2015);
- Verification by: comparing solutions from different a-priori orbits (KinetX, Genova 2018) and parameter solutions (IAU, Genova 2019).

### i. Overview of crossovers analysis workflow

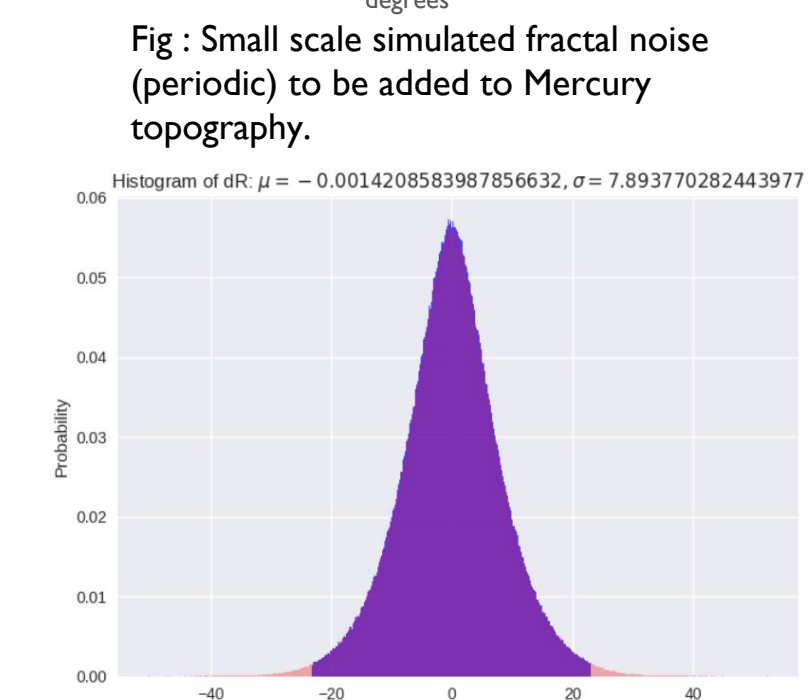
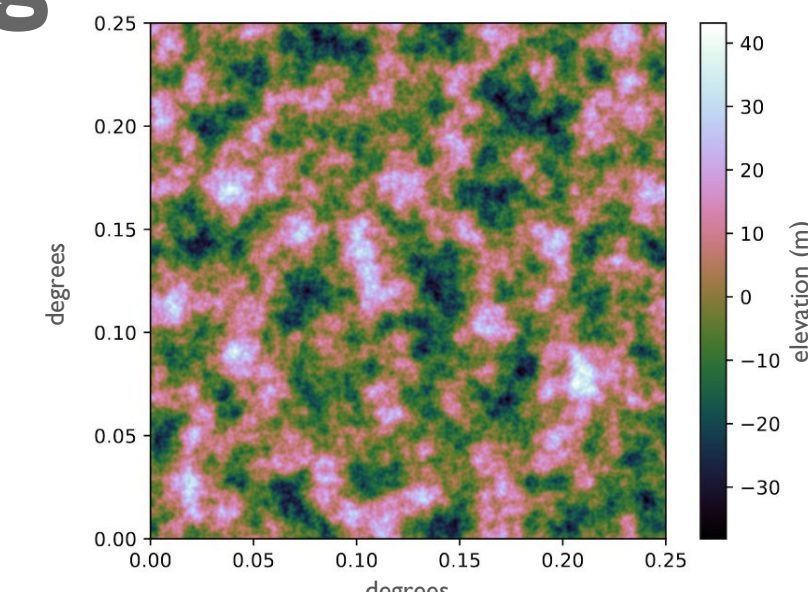


## C. Simulation: data weighting and error assessment

Error source	Value [m]
Instrument	0.2
Pointing & alignment	9.5
Radial orbit errors	1.8
Rotational state	2.0
Interpolation errors	7.7

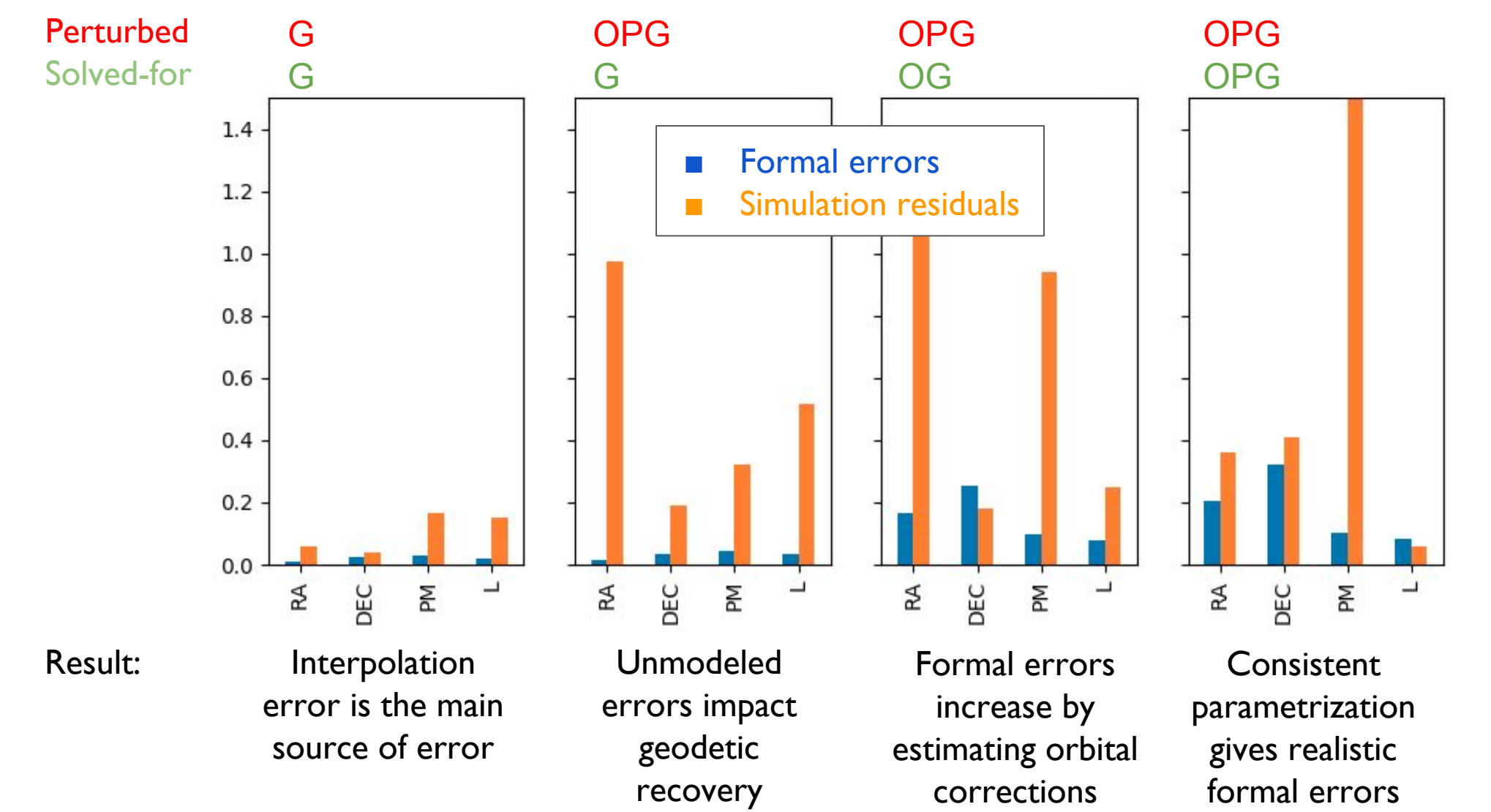
Table : Main errors affecting altimetry crossover analysis (Steinbrugge, 2018)

- We test the impact of most error sources on crossovers discrepancies in our simulation environment
- Unperturbed tests with small scale roughness provide measurement sensitivity to interpolation error
- Option to perturb orbit, pointing and geodetic parameters and test different constrainings for recovery



i. Tests on 500 tracks of synthetic MLA data with different error sources and parametrizations

- GG : RA (as), DEC (as), PM (as/y), L (as)
- OO : Orbit corrections (ACR bias, linear, quadratic)
- PP : Pointing corrections (roll, pitch)



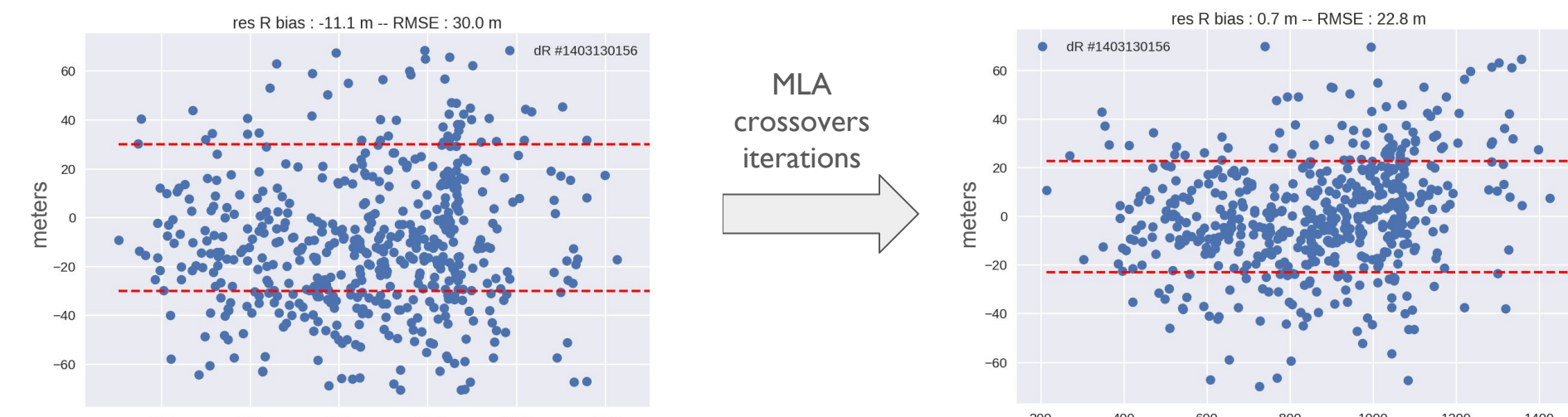
Reliability and rescaling of formal errors from closed-loop simulations

## D. Processing of MLA crossovers

### i. Improvement of orbital and geophysical parameters

- Iterative solution, convergence on parameters changes below formal errors (10-20 iterations)
- Complex pattern in orbital errors, regularisation of ACR biases
- Checking quality of pre-fit and post-fit orbit residuals by:

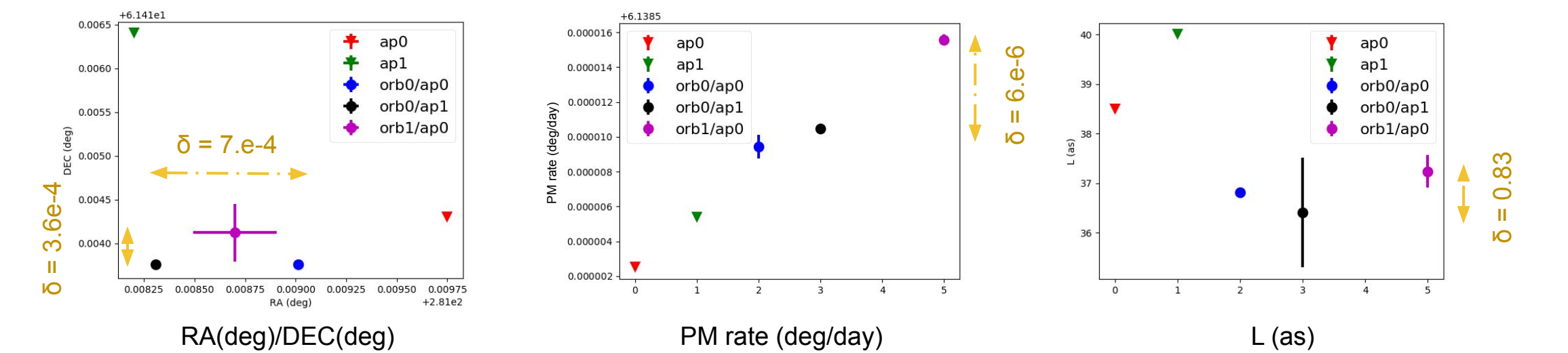
1. Pseudo-time series including dR of all crossovers for a single MLA track: RMSE of post-fit residuals (by ACR bias + rotational pars fit to dR) reduced from 30 m to 22.8 m, trends still visible



2. Reconstructed topography from geolocalised MLA residuals; interpolation and shadowing highlight inconsistencies due to orbital and orientation errors; comparison shows crossovers fit contribution



### ii. Check independence from a priori orbits and parameters



- Dataset: crossovers among 500 chosen MLA tracks (homogeneously distributed in spacetime)
- Consistent parametrization with ACR biases (constraint: 100 m) and [RA, DEC, PM rate, L]
- Comparison of multiple solutions based on: KinetX (orb0) and Genova 2018 (orb1) Doppler orbit reconstruction and IAU (ap0, Archinal, 2017) and Genova 2019 (ap1) a priori values.

Dispersion at convergence contributes to realistic error assessment

### iii. Comparison with previous solutions by other groups/techniques

- Weighted least square solution based on full MLA dataset
- Solutions from Earth radar, MESSENGER (camera and altimetry, Doppler, crossovers)

