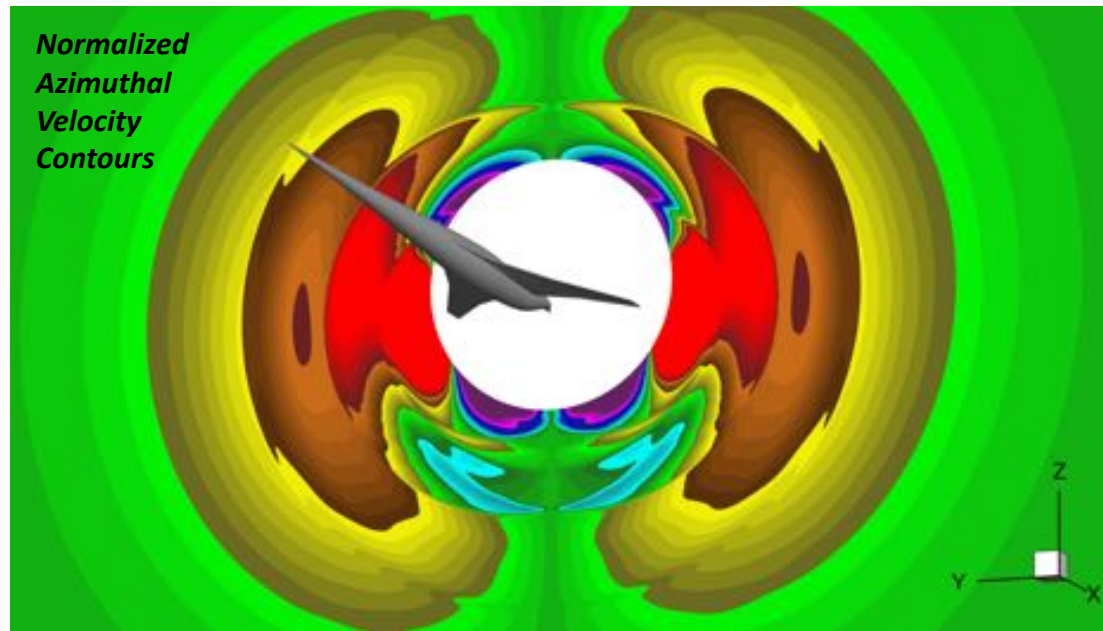


Efficient Near-Field to Mid-Field Sonic Boom Propagation using a High-Order Space Marching Method*

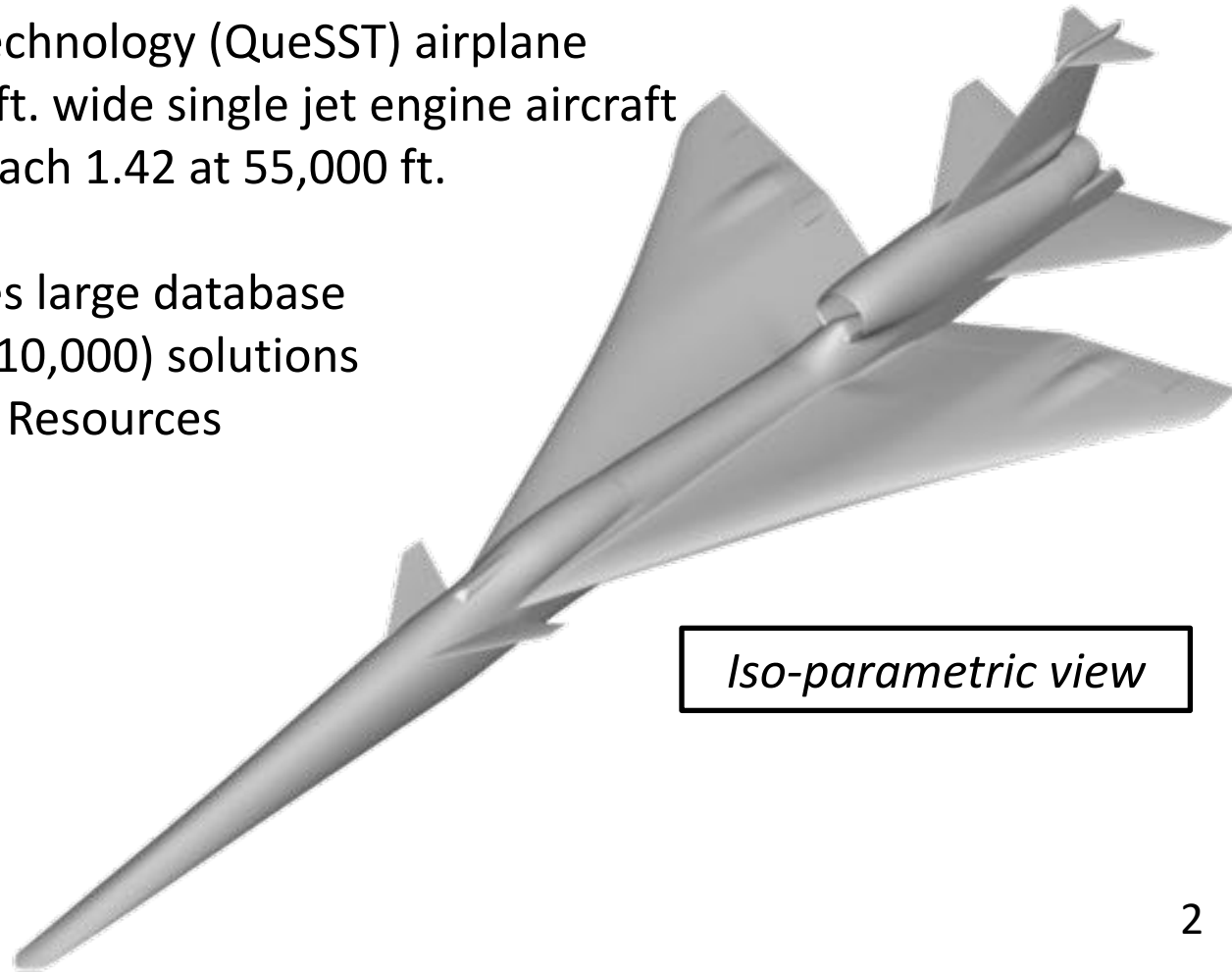


*funded by the NASA's ARMD
Commercial Supersonic
Technologies (CST) project

Jeffrey Housman, Gaetan Kenway, James Jensen, and Cetin Kiris
Computational Aerosciences Branch
NASA Ames Research Center

NASA's Low-Boom Flight Demonstration (LBFD) project

- Primary goal is to demonstrate feasibility of supersonic over-land flight at reduced loudness levels
- X-59 Quiet Supersonic Technology (QueSST) airplane
 - 94 ft. long and 29.5 ft. wide single jet engine aircraft
 - Designed to fly at Mach 1.42 at 55,000 ft.
- Mission planning requires large database consisting of $O(1000)$ - $O(10,000)$ solutions
 - High Computational Resources
 - Must be automated
 - Must be accurate

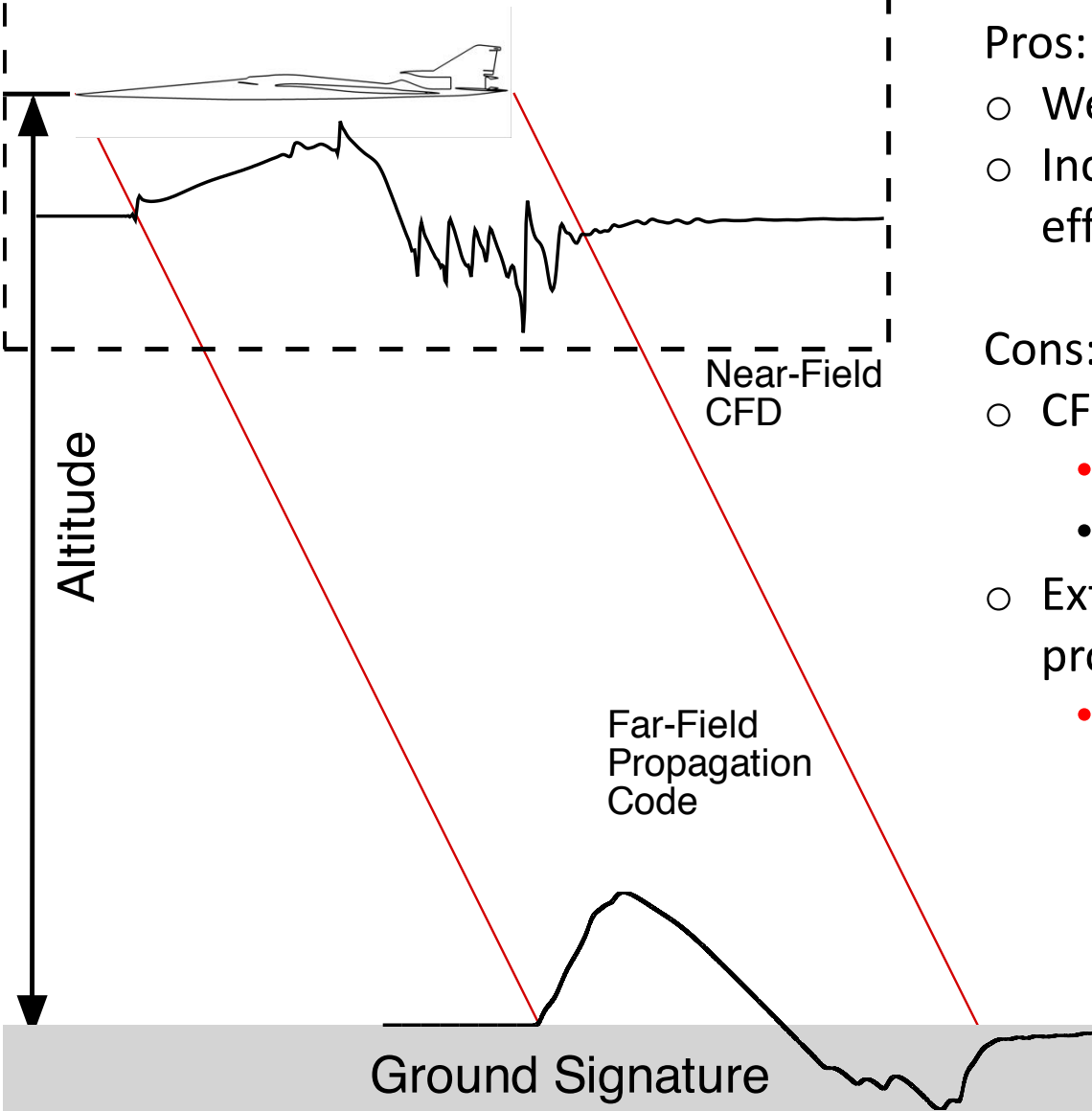


Iso-parametric view

2-Step Ground Level Noise Prediction



Supersonic Aircraft



Pros:

- Well established procedure
- Includes important atmospheric effects

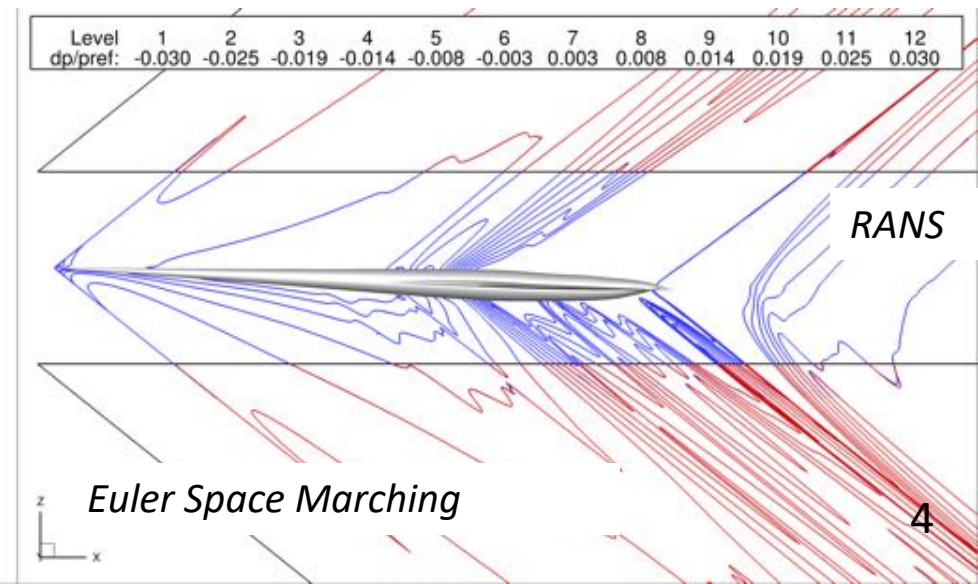
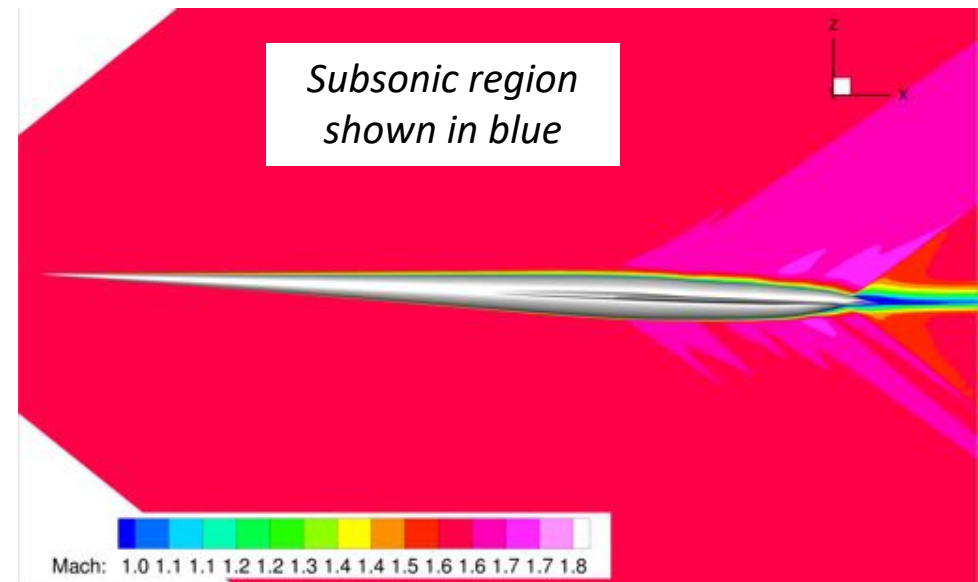
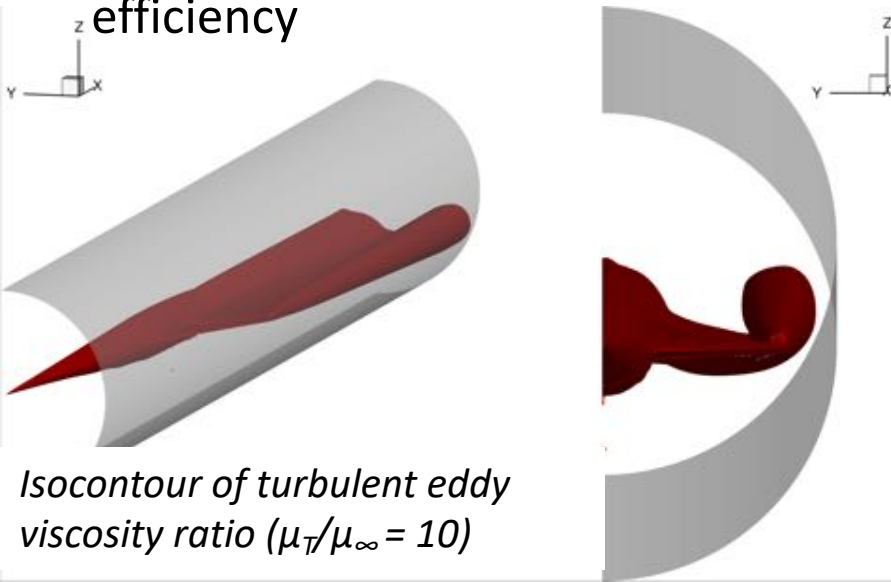
Cons:

- CFD domain is relatively large
 - High Computational Cost
 - Accuracy (2nd order)
- Extraction radius for far-field propagation relatively small
 - Ignores azimuthal effects

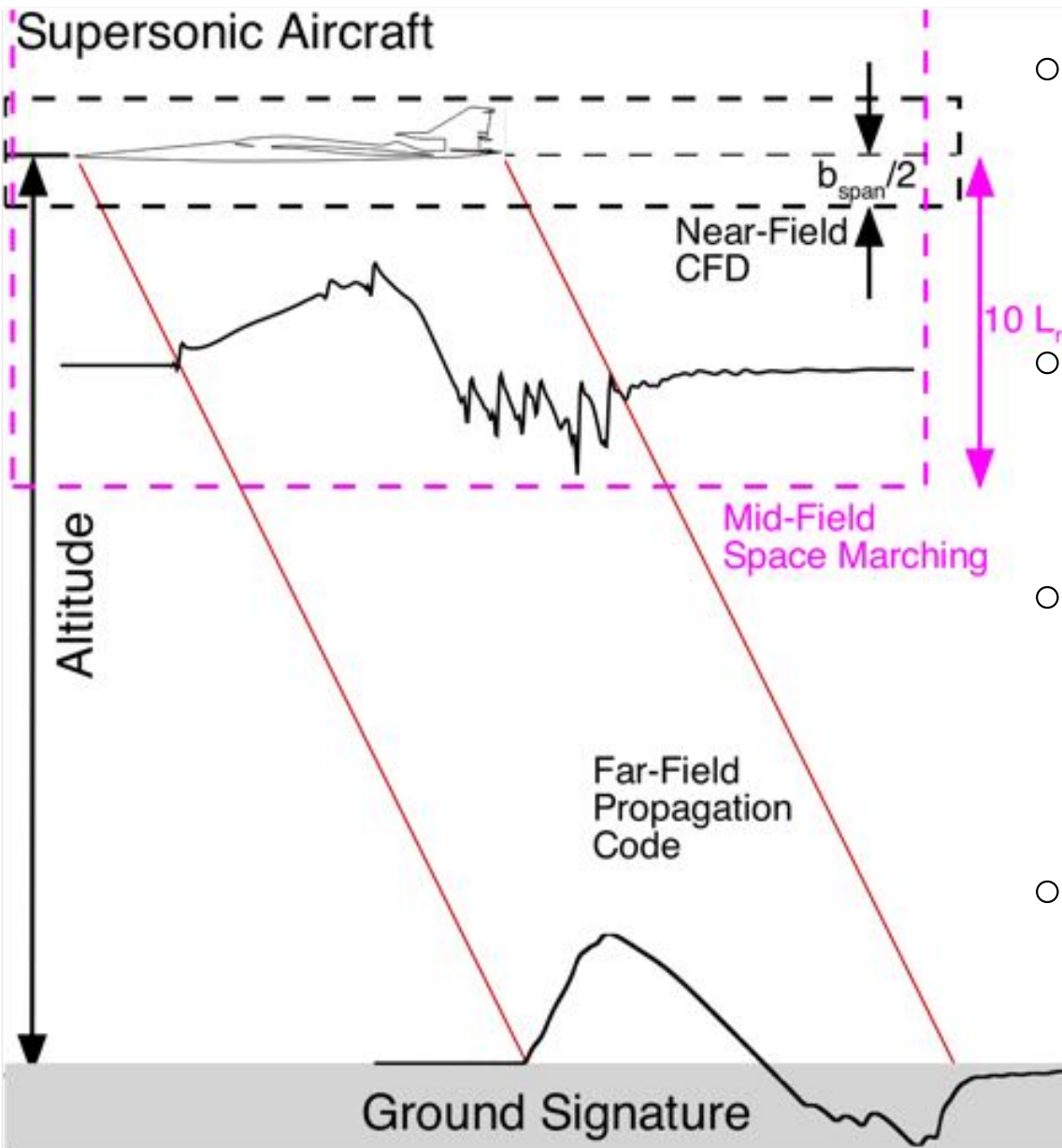
Special Features of Supersonic Flow



- All information travels in a common “time-like” direction along characteristic surfaces
- Viscous effects are only important near the walls of the aircraft
- Space marching is a special discretization/solution strategy which uses these features for computational efficiency

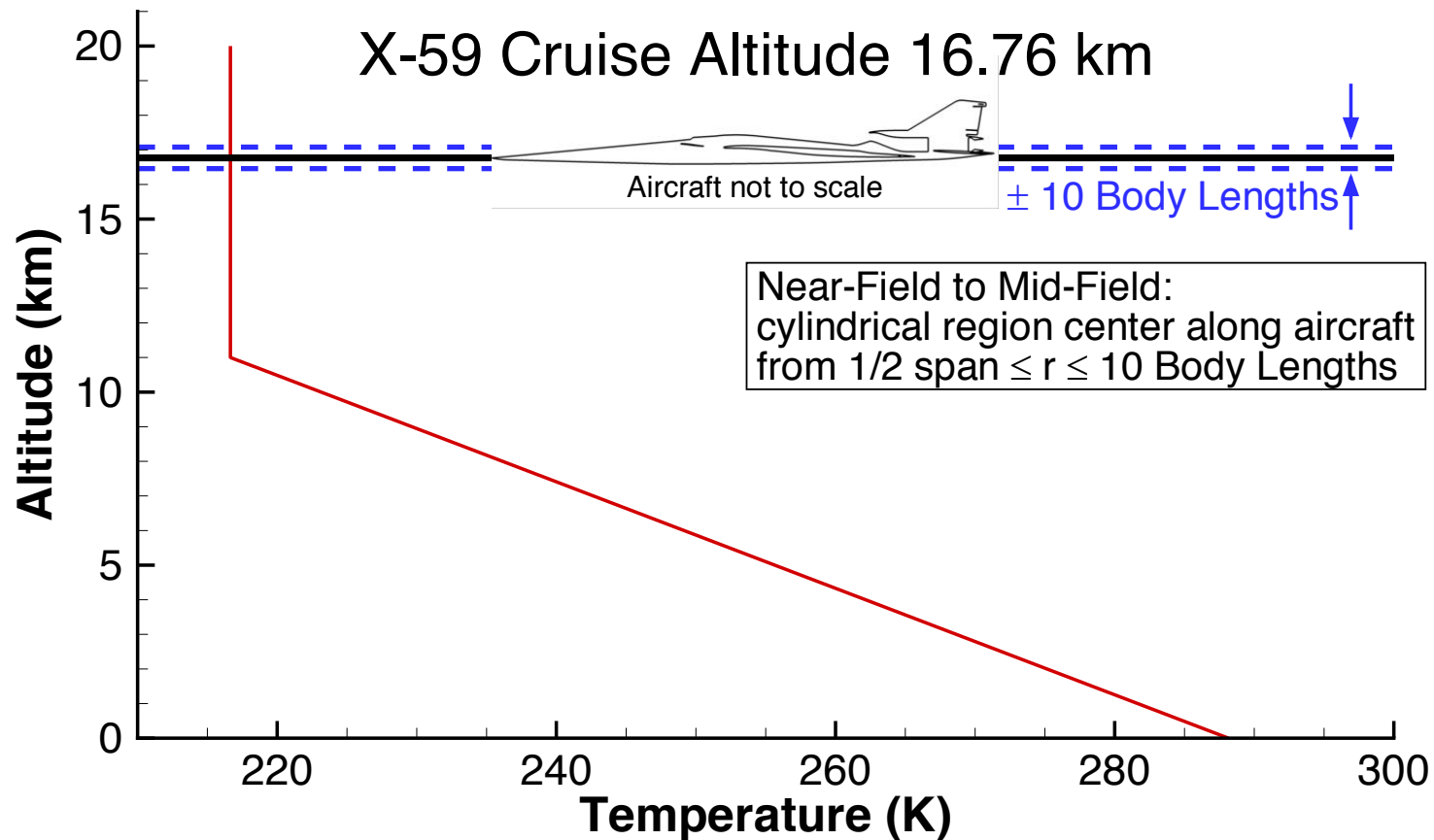


3-Step Ground Level Noise Prediction



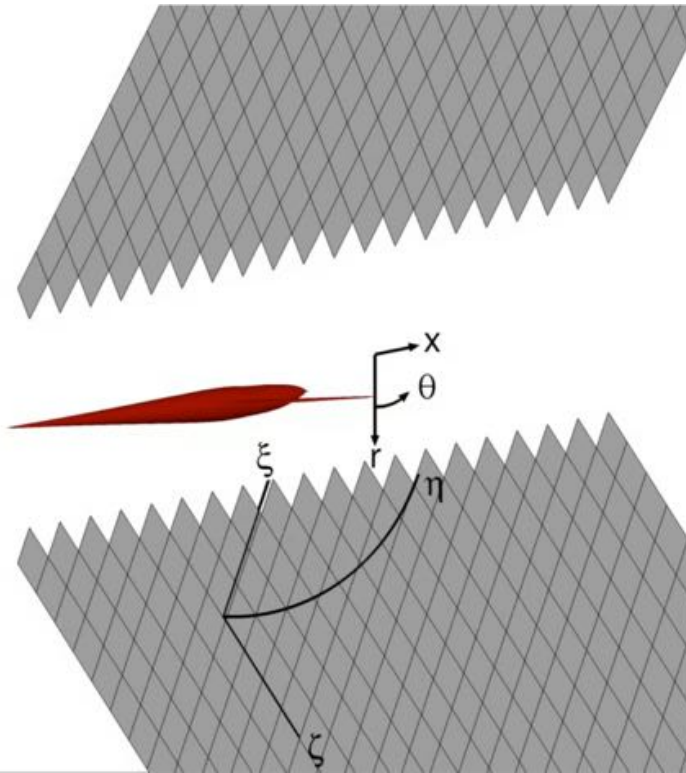
- Pros:
 - Reduced CFD domain
 - Space marching procedure:
 - Automated grid generation
 - Runs on workstation in minutes
 - Includes **all relevant azimuthal effects**
 - Changes from 3D steady into 2D “unsteady-like”
 - More than **50% reduction in total time**
 - Same level of accuracy for ground level noise
- Cons:
 - Introduces additional step in process

Definition of Near-Field to Mid-Field

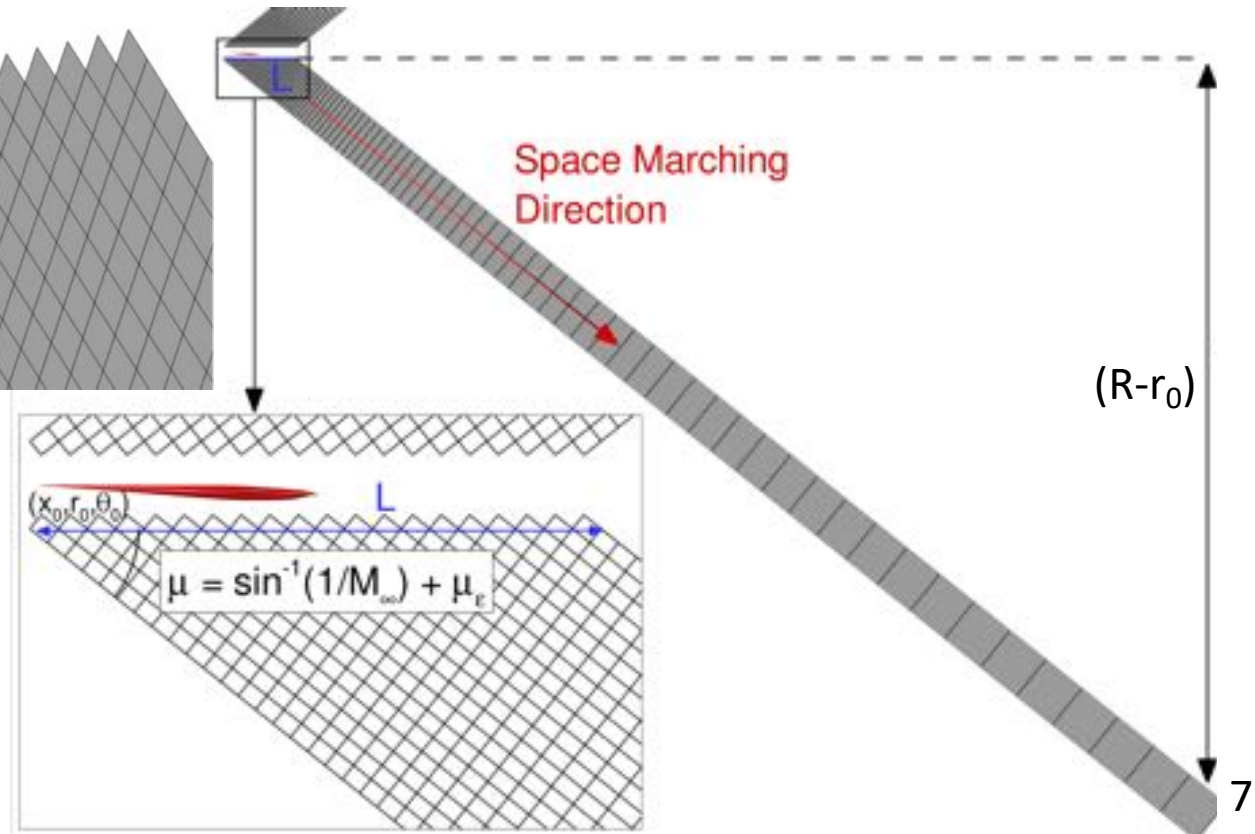


- Plot of altitude versus ICAO standard atmospheric temperature
- No variation in temperature within 10+ body lengths of the aircraft
- Atmospheric effects are neglected in the current approach
 - examples: wind variation, molecular relaxation, and humidity

Mach-cone Aligned Space Marching Grid



- Mach-cone aligned to reduce effect of artificial dissipation
- Small perturbation in alignment to reduce chance of numerical flux crossing sonic line
- Orthogonal to preserve supersonic Mach number in space marching direction

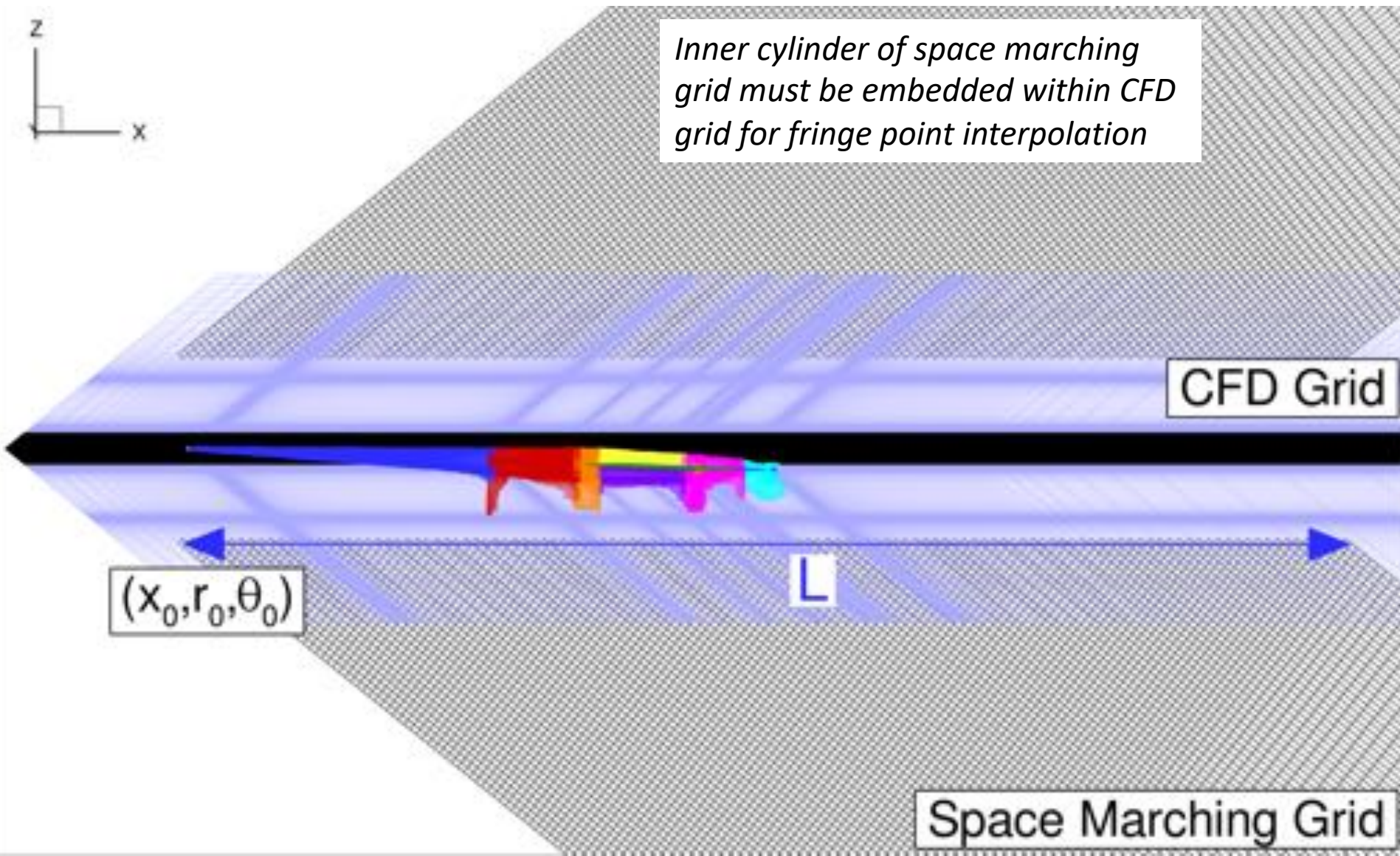


- Standalone grid generation code with limited input parameters
- Generates $O(10)$ - $O(100)$ million grid point grids in seconds on a workstation

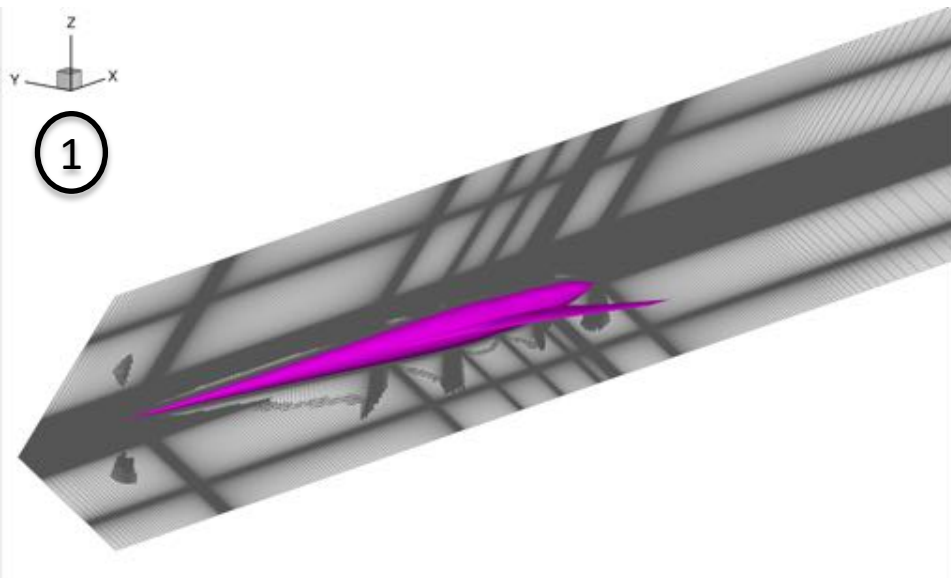
Mach-cone Aligned Space Marching Grid



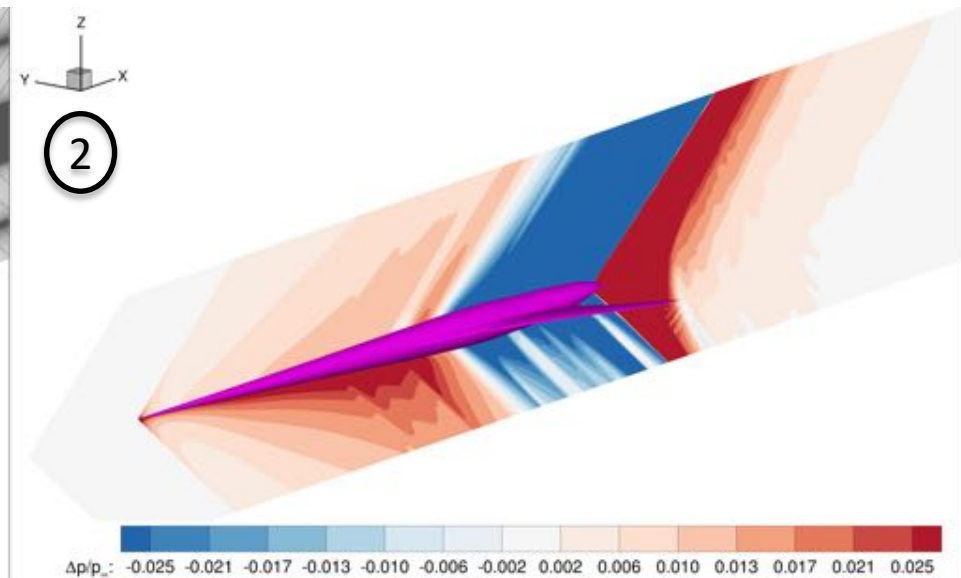
Symmetry plane view of space marching grid and CFD grid



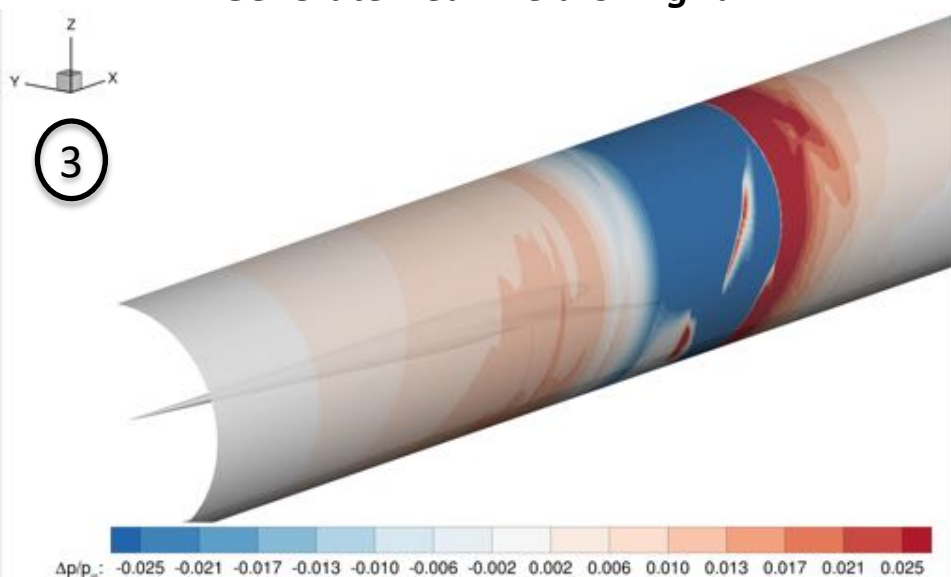
Near-Field to Mid-Field Procedure



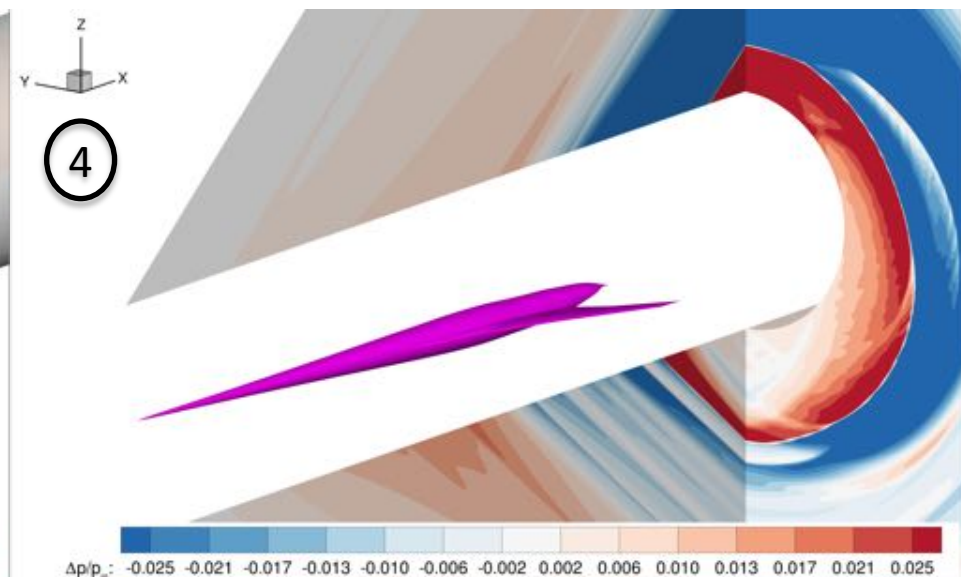
Generate Near-Field CFD grid



Compute Near-Field Solution



Interpolate Fringe Points



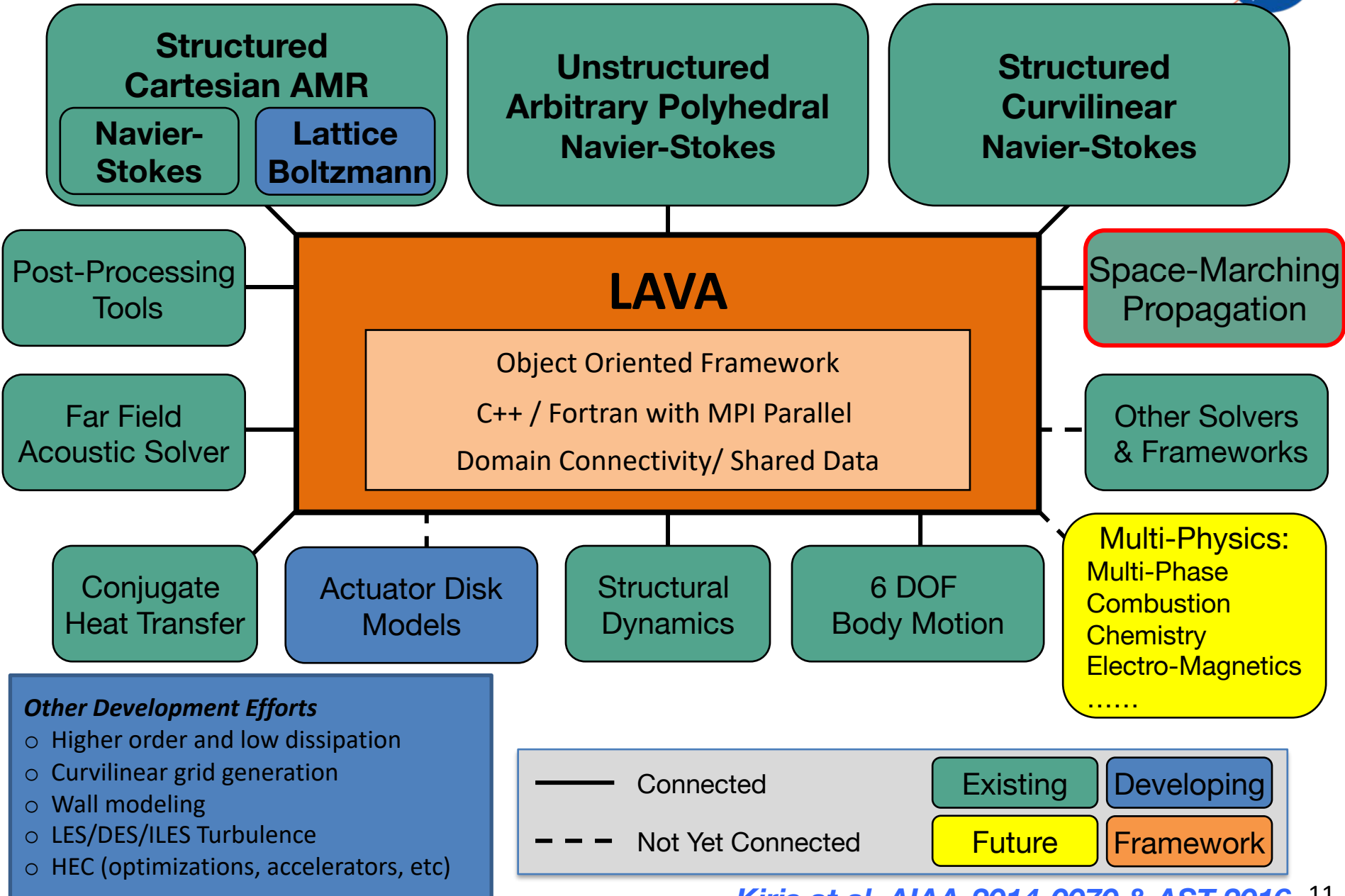
Space March through Mid-Field

Numerical Discretization (Space Marching Propagation)

- Governing equations are the steady-state 3D Euler equations transformed to a general curvilinear coordinate system in strong conservation law form
- Second-order BDF2 is used in the space marching direction
- High-order Hybrid Weighted Compact Nonlinear Scheme (HWCNS) is used in the other two coordinate directions
 - Interface (half-point) fluxes are evaluated with modified Roe
 - Left/Right interface states use 3rd or 5th order WENO interpolation
 - 4th order centered finite difference using a combination of fluxes at the grid points and the half-points
- Identical finite-difference operators (BDF2 and HWCNS) used in metric term evaluation for free-stream preservation
- 2D nonlinear system is solved at each space marching station using an alternating line Jacobi relaxation

See paper for details

LAVA Framework



○ JAXA Wing Body

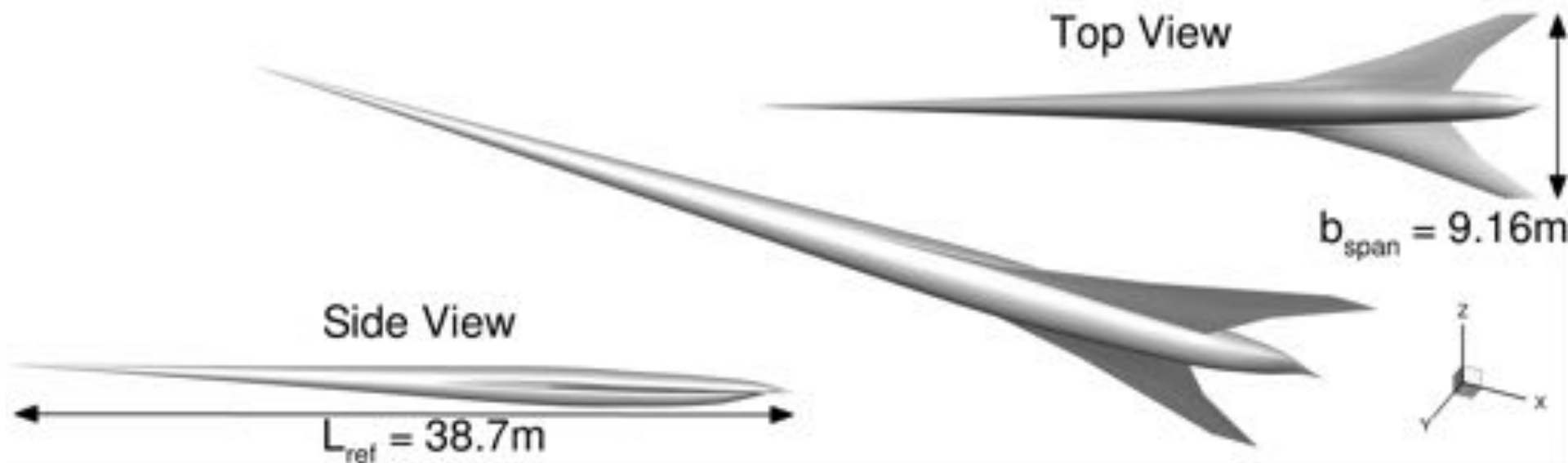
- Sensitivity Studies: (see paper for all sensitivity studies)
 - *Mach cone perturbation angle*
 - *Stretching ratio*
 - *Maximum aspect ratio*
 - *Streamwise resolution*
 - *Circumferential resolution*
 - *Circumferential extent*
 - *Metric term evaluation*
 - *Convective flux discretization*
 - *Nonlinear convergence tolerance*
- Azimuthal Dependence of Nonlinear Wave Propagation
 - Near-Field to Mid-Field
 - Mid-Field to Ground

○ Low Boom Aircraft Wind Tunnel Model

- Space Marching Grid and Solution
- Wind Tunnel Comparison

JAXA Wing Body (JWB) configuration from 2nd AIAA Sonic Boom Workshop (SBPW2)

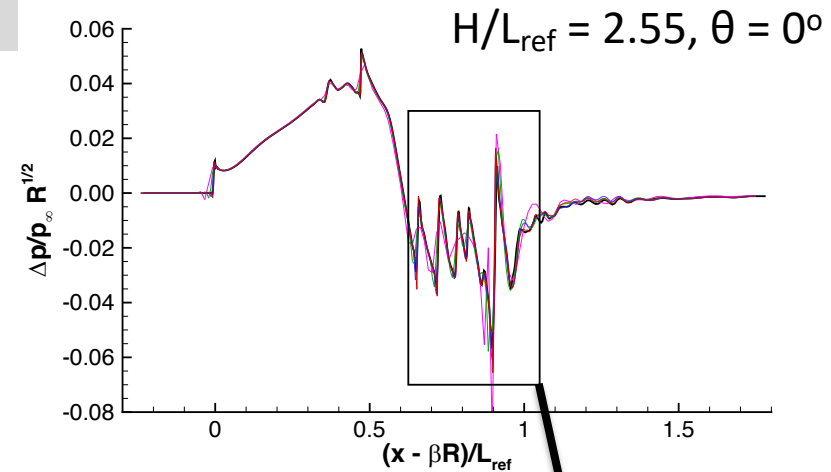
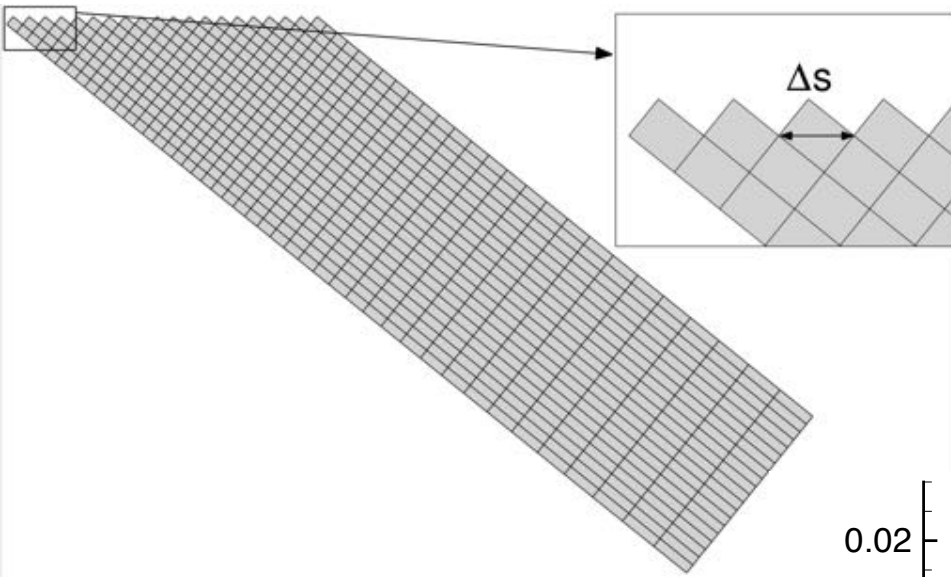
- Designed to achieve low boom levels
- Reference length: $L_{\text{ref}} = 38.7$ m
- Mach = 1.6, $\text{Re}/\text{m} = 5.7$ million, and $\alpha = 2.3^\circ$
- Near-field CFD results using LAVA reported at SBPW2



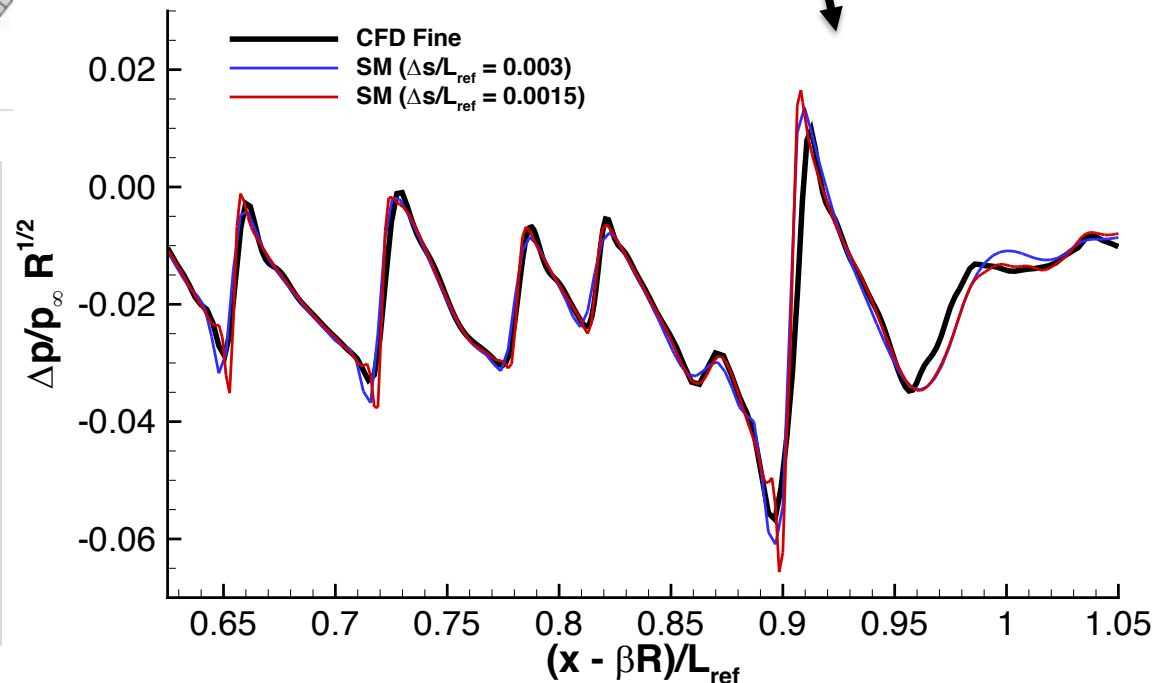
Sensitivity Study (Streamwise Spacing)



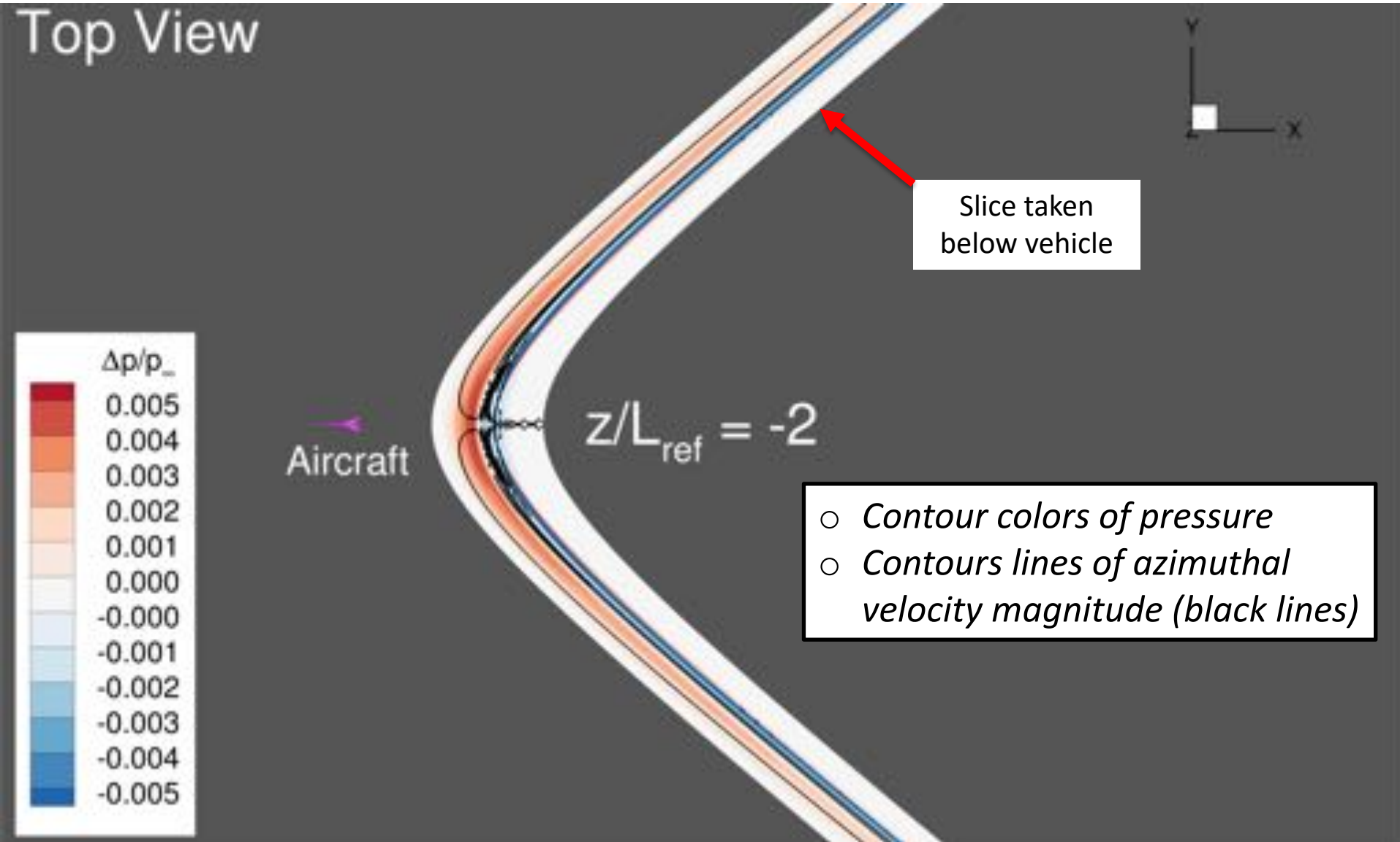
Streamwise Spacing $\Delta s/L_{\text{ref}} = 0.012, 0.006, 0.003, 0.0015$



- Generated 4 space marching grid resolutions
- $\Delta s/L_{\text{ref}} = 0.003$ appears adequate for JWB
- Space marching solution converges to CFD

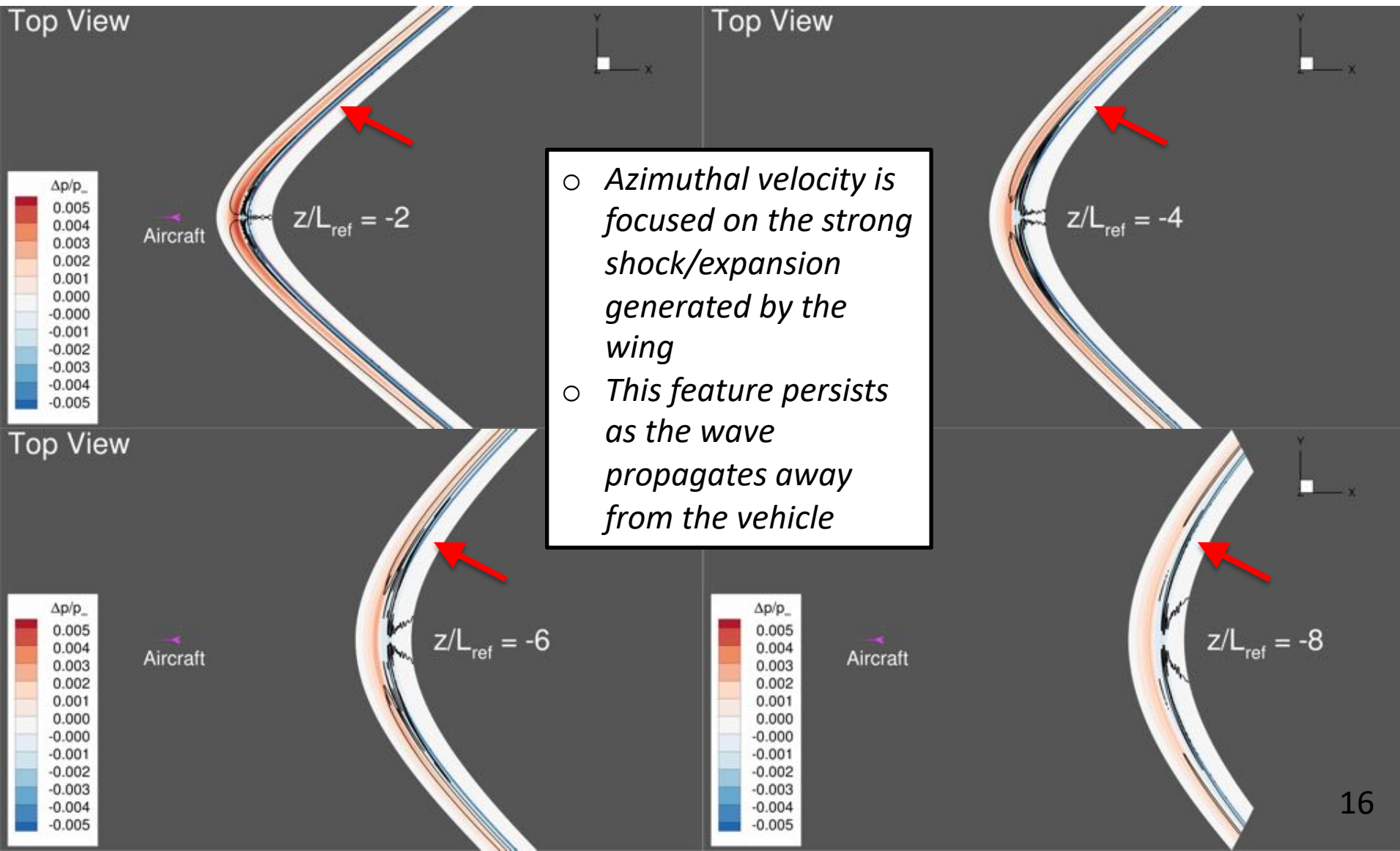


Top View



Azimuthal Dependence of Nonlinear Wave Propagation

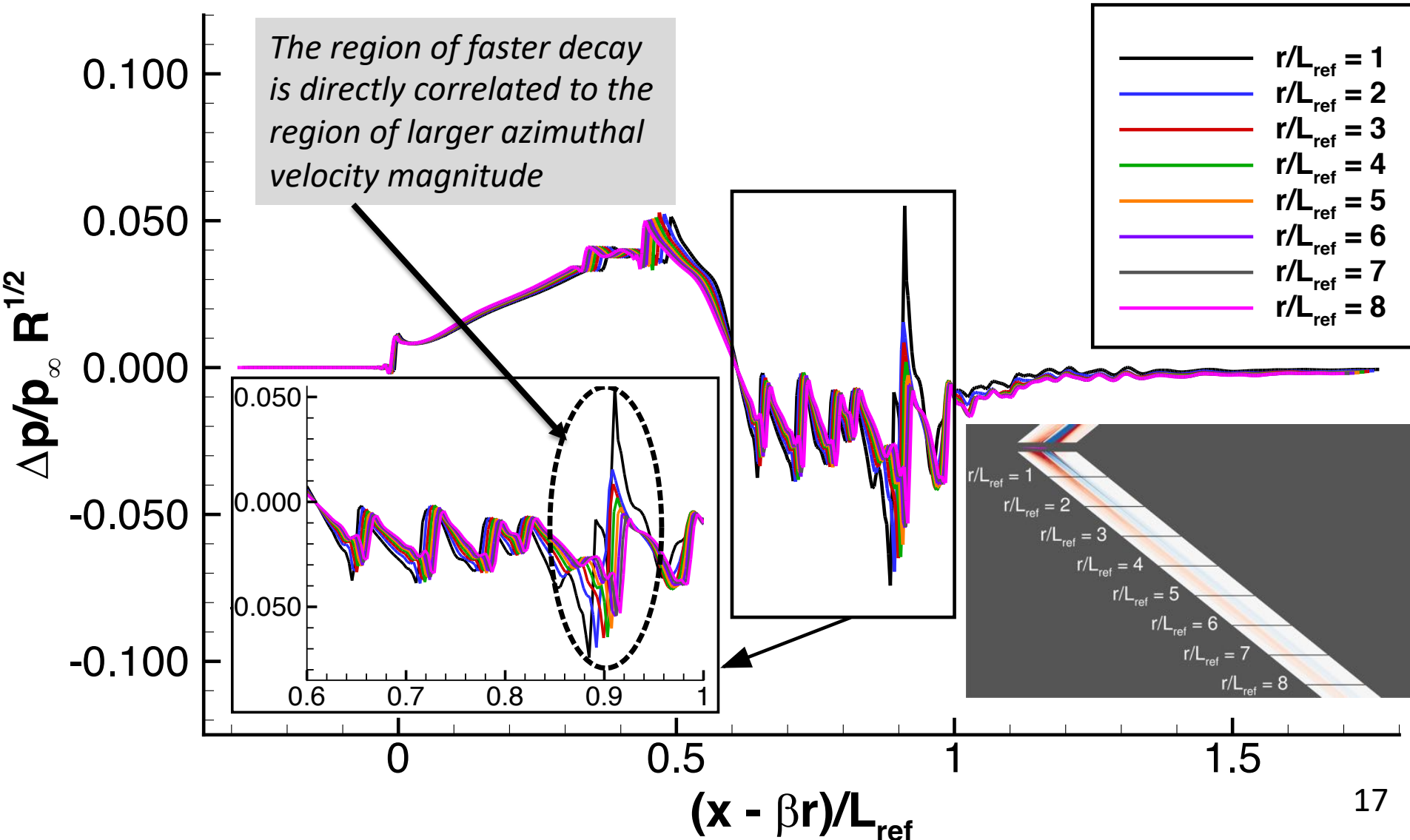
Pressure contour colors with contour lines of azimuthal velocity magnitude



Azimuthal Dependence: Near-Field to Mid-Field



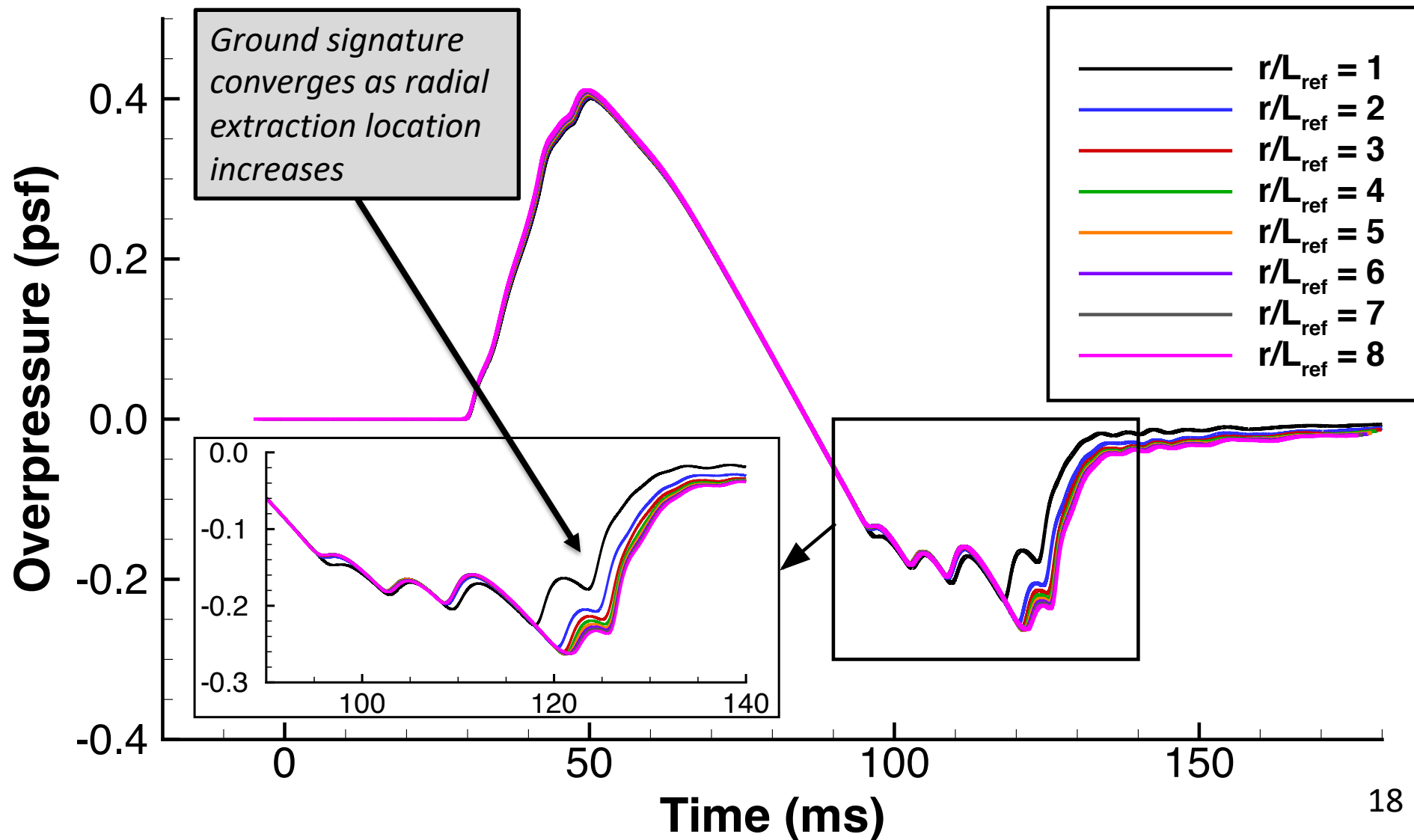
Scaled pressure signatures extracted at 8 different radial locations below the aircraft



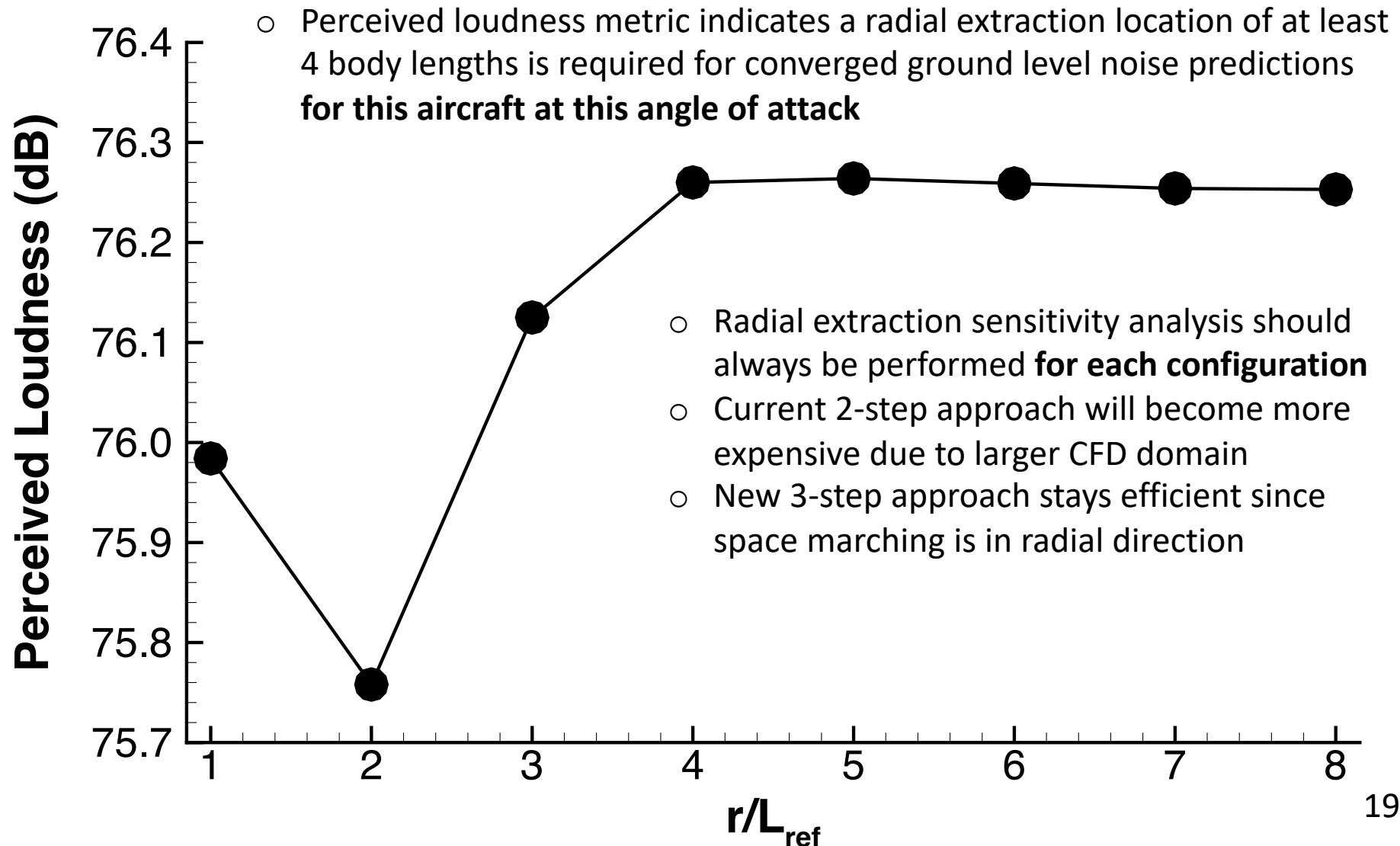
Azimuthal Dependence: Mid-Field to Ground



Overpressure ground signatures propagated with sBOOM from each radial extraction



Perceived loudness on the ground as a function of radial extraction location



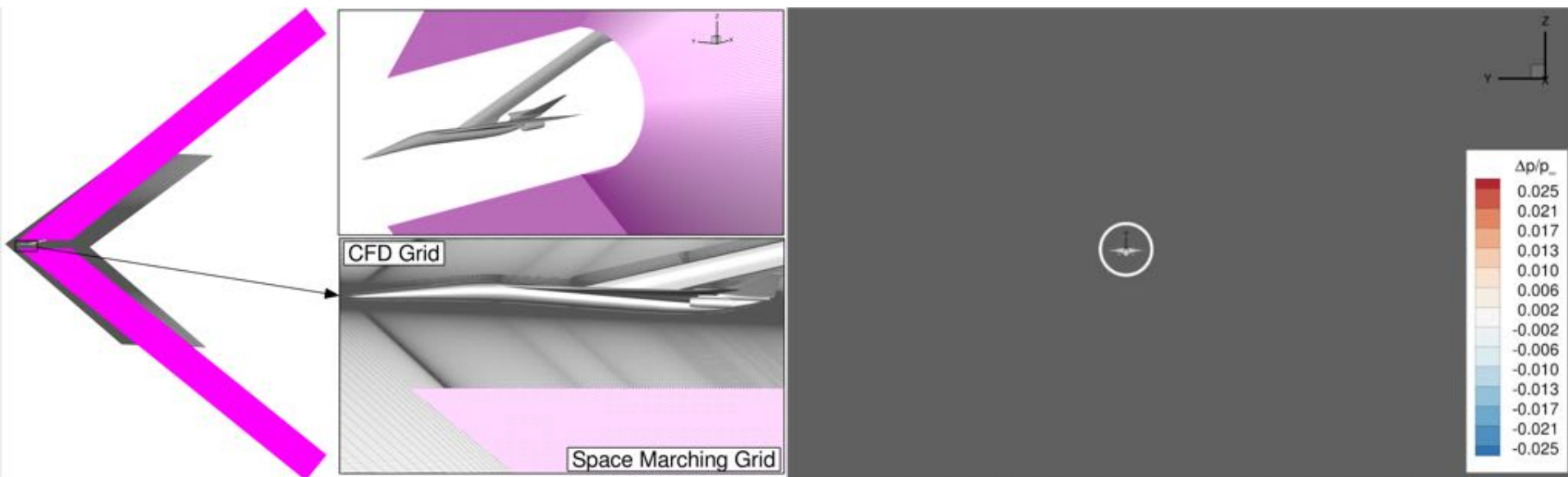
Low Boom Aircraft Wind Tunnel Model



Lockheed Martin Phase I low boom model from 1st AIAA Sonic Boom Workshop (LM1021)

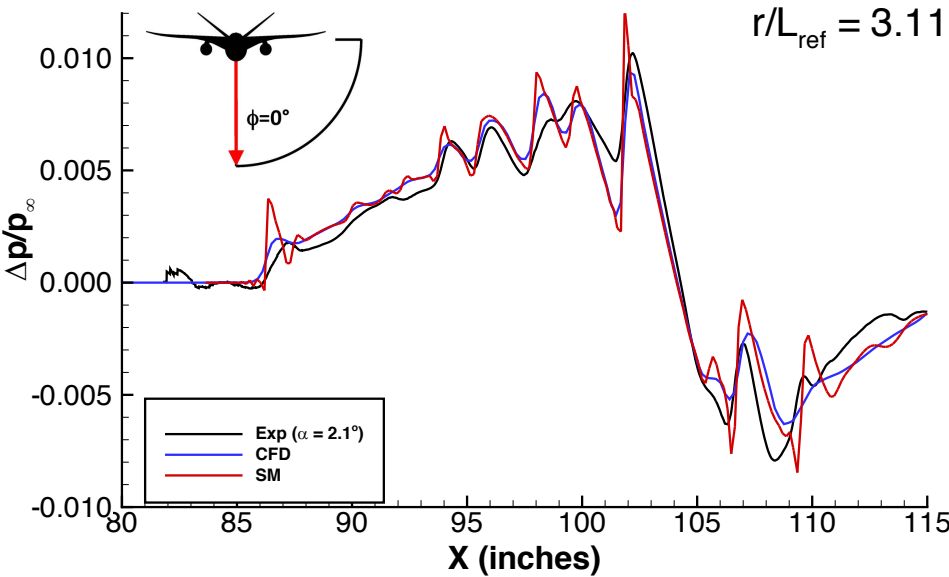
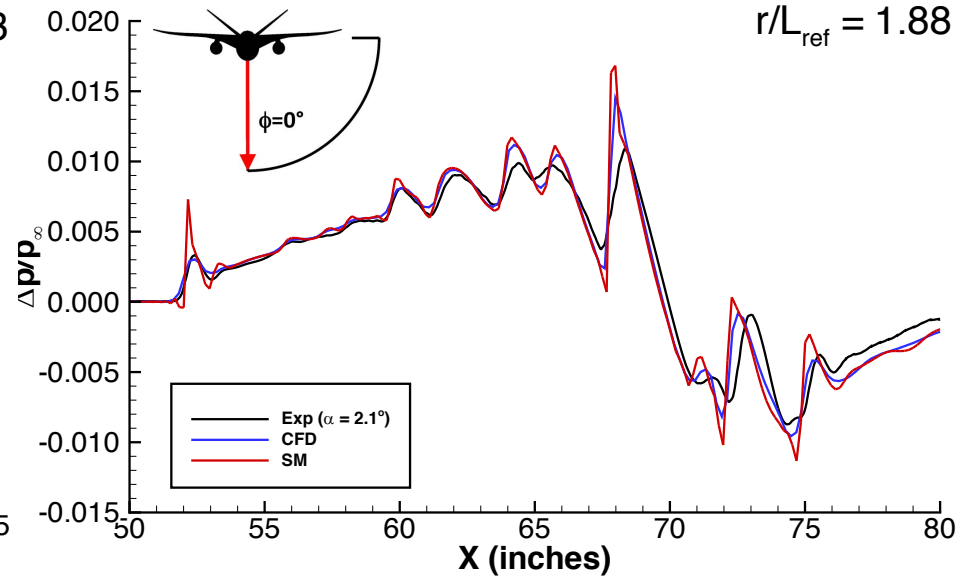
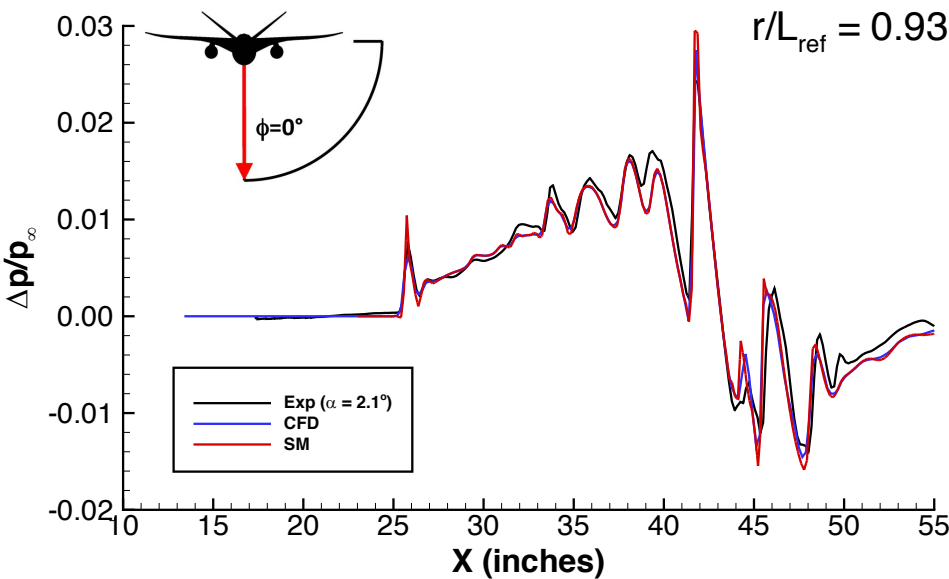
- Designed to achieve low boom on-track signatures
- Reference length: $L_{\text{ref}} = 22.365$ inch (0.568 m) 0.008 percent scale
- Mach = 1.6, $Re/m = 4.36$ million, and $\alpha = 2.1^\circ$
- Experimental data reported in *Cliff et. al.* (AIAA-2014-0560)
- Near-field CFD results using LAVA reported in *Housman et. al.* (AIAA-2014-2008)





- Inputs for space marching grid generation were taken from grid sensitivity studies (see paper for details)
- $SR = 1.05$, $AR_{max} = 20$, $\Delta s/L_{ref} = 0.003$, $\Delta\theta = 1^\circ$, $\theta_{max} = 180^\circ$, $R = 10 L_{ref}$
- Grid Dimensions: 351 x 181 x 564 (35.8 Million points, 4.2 seconds to generate)
- Inputs for space marching solver parameters were taken from solver sensitivity study (HWCNS4-ZWENO5)
- Space marching wall-clock time 106 seconds using 80 threads on single workstation

LM1021 Wind Tunnel Comparison



- Space marching and CFD solutions match wind tunnel data well at $r/L_{ref} = 0.93$
- As r/L_{ref} increases pressure peaks in wind tunnel data appear smoothed (averaging procedure see Cliff 2014)
- Space marching and CFD solutions retain sharp peaks at larger r/L_{ref}
- Space marching solution shows higher amplitudes than 2nd order CFD

Computational Savings



Example: JAXA Wing Body (66% reduction)

Measured Time (JWB)	2-Step Approach	3-Step Approach
CFD (RANS)	1920 core hrs. ($R = 7L_{\text{ref}}$)	640 core hrs. ($R \sim b/2$)
Space Marching*	NA	3 min. 6 seconds ($R = 10L_{\text{ref}}$)
sBOOM (1 azimuth)	~30 seconds	~30 seconds
Total Time	1920 hrs. 30 sec.	640 hrs. 3 min. 36 sec.

- Total time dominated by near-field CFD with both approaches
- Reduction of CFD domain extend lead to the reduction in total time
- Space marching approach time is small:
 - Space marching grid generation (116.4 Million points 13.6 sec.)
 - Interpolation of CFD solution onto fringe points (7.5 sec. 40 cores)
 - Space marching solution (164.9 sec. 80 threads)

- ***A high-order accurate space marching method was developed for efficient near-field to mid-field sonic boom propagation***
 - A Mach-cone aligned curvilinear grid using *ibanking* technology was developed which is appropriate for space marching
 - Thorough grid and solver parameter sensitivity studies reported in paper
 - Important **azimuthal effects** on near-field to mid-field wave propagation and mid-field to ground level noise prediction was demonstrated
 - Completed validation of the near-field to mid-field approach on the LM1021 wind tunnel model
- ***A three-stage process for computing ground level noise from an aircraft was developed***
 - Reduces CFD domain extent by 40 – 60 %
 - Introduces new near-field to mid-field space marching method
 - Space marching grid generated in seconds (automatically)
 - Interpolation from CFD to space marching grid
 - Space marching propagation (up to 10 body lengths) in minutes on a workstation
 - Total **time reduction of 66%** compared to current approach for the JAXA wing body configuration