

1 **Microscale processes determining macroscale evolution of**
2 **magnetic flux tubes along Earth's magnetopause**

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25 **Abstract**

26 An important process affecting solar wind-Earth's magnetosphere coupling is non-steady
27 dayside magnetic reconnection, observationally evidenced by a flux-transfer-event (FTE) that
28 shows a bipolar variation of the magnetic field component normal to the magnetopause. FTEs
29 often consist of two interlinked flux tubes, but, local kinetic processes between the flux tubes are
30 not understood in the context of the FTE structuring, evolution, and impact. An FTE observed by
31 MMS on 18 December 2017 consisted of two flux tubes of different topology. One includes field
32 lines with ends connected to the northern and southern hemispheres while the other includes field
33 lines with both ends connected to the magnetosheath. Reconnection occurring at the flux-tube
34 interface indicates how interacting flux tubes evolve into a flux rope with helical magnetic
35 topology that is either closed or open. This study demonstrates a new aspect of how micro-to-
36 meso-scale dynamics occurring within FTEs determines their macroscale characteristics and
37 evolution.

38 Introduction

39 Solar wind-magnetosphere coupling often occurs in a localized and transient manner,
40 modifying the magnetosphere-ionosphere system. One of the most common and important
41 processes underlying such transient phenomena is non-steady dayside magnetic reconnection.
42 Contrary to continuous or quasi-steady reconnection, transient reconnection gives rise to a
43 localized structure of enhanced magnetic flux. This structure forms and convects over the surface
44 of Earth's magnetosphere called the magnetopause, due to the combination of the anti-sunward
45 magnetosheath flow and tension force exerted on the reconnected flux tube¹. The observational
46 evidence of such transient structures is a bipolar signature in the magnetic field component
47 normal to the magnetopause (B_N) associated with the drifting motion (see dashed blue arrows in
48 Fig. 1a).

49 Since Russell and Elphic² termed this signature a flux transfer event (FTE), numerous *in-*
50 *situ* observations have determined their typical signatures. In addition to the B_N reversal, these
51 signatures include enhanced magnetic field strength (B) due to a strong core field, an increase in
52 the total pressure, and a mixture of magnetosphere and magnetosheath plasmas. These signatures
53 have been explained by their generation via 1) localized bursts of dayside reconnection², 2)
54 multiple X-lines³, or 3) temporal modulation of the reconnection rate during continuous single
55 X-line reconnection⁴. The different generation mechanisms give rise to different magnetic field
56 topology and connectivity to either the northern or southern hemisphere or the magnetosheath
57 (the shocked and slowed solar wind across Earth's bow shock). On the other hand, they
58 commonly invoke formation processes occurring over macroscopic scales, resulting in FTEs
59 with macroscale sizes comparable to one Earth radius (R_E)⁵.

60 Recent observations using the data from the Magnetospheric Multiscale mission (MMS)⁶
61 with its high-resolution measurements and tetrahedral configurations with spacecraft separations
62 varying from a couple of d_i (ion inertial lengths) to a few d_e (electron inertial lengths) have
63 enabled detailed investigations of kinetic boundaries and physical processes occurring
64 within/around FTEs. The observations include evidence for 1) ion-scale secondary flux ropes
65 generated by dayside reconnection^{7,8}, 2) multi-layered substructures within an FTE⁹, 3) electron-
66 or ion-scale current layers at the interface of two coalescing FTEs^{10,11}, 4) reconnection between
67 colliding reconnection jets in a compressed current sheet at the center of an FTE¹², 5)
68 reconnecting current sheet between interlinked flux tubes^{13,14}, and 6) the formation of an FTE
69 driven by the electron vortex¹⁵. These observations indicate that microscale (electron) and
70 mesoscale (ion) physical processes occurring in/around FTEs play a crucial role in the
71 generation, structure, and evolution of FTEs.

72 These local kinetic processes, however, have not received sufficient attention in FTE
73 formation, structuring, and evolution. Yet, they can be essential ingredients in the dynamics of
74 FTEs that may grow into large-scale FTEs drifting down the tail along the magnetopause,
75 forming the basis of magnetospheric activities such as geomagnetic storms and substorms. Thus,
76 the localized physics occurring in FTEs may be key to understanding solar wind-magnetosphere
77 coupling and the global magnetospheric system, which has not yet been explored.

78 This paper presents a new aspect of kinetic processes occurring within FTEs. These kinetic
79 processes can lead to the topological structure and evolution of FTEs (Fig. 1d-e), implying the
80 effect of micro-to-meso-scale dynamics occurring within FTEs on the macroscale characteristics
81 of FTEs. We use an FTE event observed by the MMS on the dayside magnetopause on 18
82 December 2017 to illustrate this new aspect of FTEs. The detailed plasma and field data indicate

83 that the FTE consists of two interlaced flux tubes. Using particle distributions and force analysis,
84 we investigate topological signatures of the FTE and discuss the kinetic processes occurring at
85 the interface of the two flux tubes that lead to the formation of a large-scale flux rope connecting
86 both hemispheres, therefore, potentially regulating magnetic flux transfer into the magnetotail.

87 Results

88 **Propagation, observation location, and scale size of the event.** The MMS spacecraft
89 was located at [9.0, -1.2, 1.3] R_E in Geocentric Solar Magnetospheric coordinates (GSM) at
90 \sim 08:15:00 UT on 18 December 2017. Figs. 2 and 3 present field and particle observations by
91 MMS over 8 s from 08:14:59 UT to 08:15:07 UT. During this period the interplanetary magnetic
92 field (IMF) obtained from ARTEMIS-C was relatively steady, pointing mostly due duskward
93 and southward: [1.8, 8.0, -4.0] nT (not shown) in GSM. The tetrahedral-averaged magnetic field
94 using the measurements from the four MMS spacecraft (Fig. 2a; B_X , B_Y , and B_Z components
95 shown as blue, green, and red profiles), together with the magnetic strength (B ; black) shows that
96 B_X exhibits a bipolar signature, around which B increases, indicating an FTE.

97 All vector parameters displayed in Fig. 2(d-k) and 3 are shown in boundary normal
98 coordinates (LMN; see the top of the right panel of Fig. 1a) that were determined from minimum
99 variance analysis (MVA)¹⁶ and MDD¹⁷: $L = [0.39, -0.61, 0.69]$, $M = [0.45, -0.52, -0.72]$, $N =$
100 $[0.80, 0.60, 0.07]$ in GSM. M , indicating the axis of an FTE, has a large fraction along Z . This
101 indicates a significant deviation of LMN for the present event from nominal magnetopause LMN
102 coordinates (see black arrows in Fig. 4a). The panels of Fig. 2 are obtained using the
103 measurements from the four MMS spacecraft with an average separation of 31.6 km. Fig. 3A and
104 B show MMS4 and MMS2 observations, respectively.

105 At \sim 08:15:03.2 UT, B_N (red profile in Fig. 2d and Fig. 3a) changed from negative to
106 positive (vertical dashed black line, ‘C’ shown on the top of Fig. 2 and 3). Coincidentally, the
107 magnetic field strength (B , black profile) increased. These magnetic perturbations are associated
108 with the overall motion of an FTE along $-L$ (see the dashed blue arrow in Fig. 1a that represents a
109 relative trajectory of the spacecraft across an FTE mostly along L , observing a negative, and
110 then, positive B_N). To investigate the propagation of the FTE, we performed multiple
111 triangulation analysis (MTA)¹⁸ using a four-spacecraft timing analysis^{19,20}. The direction of the
112 propagation vector was duskward and southward: [-0.45, 0.54, -0.71] in GSM or [-0.99, 0.07, -
113 0.14] in LMN, with a speed of 204 km/s. This result is consistent with the prediction from the
114 maximum shear model²¹ using the solar wind IMF condition for this event. White traces in Fig.
115 4(a) show primary X-lines over the surface of the magnetopause when viewed from the Sun. A
116 component reconnection X-line is located dawnward and northward of the MMS location (blue
117 rectangle), leading to a duskward and southward motion of an FTE (black lines departing from
118 the blue rectangle). The MTA-derived propagation vector (thick magenta arrow in Fig. 4a)
119 together with the L and M axes (black arrows) shows a good agreement between the observation
120 and the model prediction. Fig. 4(b) illustrates the FTE structure (to be detailed below) embedded
121 in the southern outflow region of the X-line when viewed mostly from the $-M$ direction.

122 We define the location where B_N becomes negative before the B_N reversal as the leading
123 boundary of the FTE (‘L’ at the top of Fig. 2 and 3, marked by vertical dashed magenta line) and
124 the location where B_N is reduced after the B_N reversal as the trailing boundary of the FTE (‘T’ at
125 the top of Fig. 2 and 3, marked by vertical dashed cyan lines). The cross-sectional scale of the
126 FTE is then estimated to be 736 km, which is \sim 12.2 d_i (ion inertial length: \sim 60 km for this event).
127 The existence of the X-line above the FTE along L is also evidenced by the ion PAD (Fig. 3f).

128 When B_L fluctuated around zero between \sim 'L' and 'T' (Fig. 3a), the ion flow mostly directed
129 perpendicularly to \mathbf{B} . When B_L was negative before \sim 'L' (positive around/after 'T'), the ion PAD
130 exhibited a significant parallel flux (mostly perpendicular and slightly anti-parallel flux). This is
131 consistent with thin magenta arrows along with the MMS trajectory (dashed cyan arrow) in the
132 Fig. 4(b) illustration.

133 **Observation of the FTE consisting of two interlinked flux tubes.** While the B_N and B
134 profiles suggest a typical southward-moving FTE across the spacecraft, we note a consecutive
135 weak variation of a negative-to-positive B_L during 'L'-'C' and 'C'-'T', as marked by '1', '2', '3',
136 and '4' in Fig. 2(d) and 3(a). The most invariant axis (Fig. 2b) is primarily along X for the earlier
137 interval ('L'-'C'), but significantly toward Y and Z for the later interval ('C'-'T'). When
138 averaged over each interval under the error indicator (Fig. 2c) ≤ 0.5 , the invariant axis in LMN
139 directs to $[-0.24, -0.38, -0.89]$ for 'L'-'C', and $[0.01, -0.83, 0.56]$ for 'C'-'T'. This result is
140 consistent with the result from MVA, particularly for 'C'-'T', during which the bipolar B_L
141 signature is clearer (Fig. 2d). The two invariant axes make an angle of 79.3° . This observation
142 indicates that the FTE consisted of the two flux tubes²². Fig. 4(b) shows a schematic diagram of
143 the two flux tubes oriented almost perpendicularly. Numbers, '1', '2', '3', and '4' as observed by
144 MMS crossing the structure along the trajectory (dashed cyan arrow) correspond well to those in
145 Fig. 2(d) and 3(a).

146 Plasma parameters also show notable differences across 'C': ion density (temperature) is
147 lower (higher) during the interval between 'L' and 'C' than between 'C' and 'T' (Fig. 3b); $V_{i,M}$
148 changes from negative to positive across 'C' (green arrows in Fig. 3c). Most importantly, we
149 note that the electron PAD exhibit dramatic changes across 'C': the low and mid energy electron
150 fluxes (Fig. 3j, k) were lower between 'L' and 'C' than between 'C' and 'T'; 90° pitch-angle
151 electrons often greatly enhanced in the high-energy range (Fig. 3l) only before 'C'. These
152 significant differences in the electron PAD across the FTE center indicate two interlaced flux
153 tubes¹⁴: the intense 90° -focused energetic population is likely to be trapped on the field lines
154 connected to both hemispheres (supported by the low density and high temperature of the plasma
155 in Fig. 3b; to be discussed below); the absence or reduction of such populations between 'C' and
156 'T' indicates magnetosheath field lines or open field lines that allow hot magnetospheric
157 populations to escape. Completely different magnetic connectivity before and after the center of
158 the FTE inferred from the electron PAD strongly supports the interpretation of two interlinked
159 flux tubes, instead of a single flux-rope-type FTE (such as an FTE illustrated in Fig. 1a).

160 For a commonly observed relatively force-free flux rope³⁸ ($\mathbf{J} \times \mathbf{B} \approx 0$), the current density is
161 mostly parallel to \mathbf{B} ($J_{\parallel} > J_{\perp}$). Both the curl of the magnetic field and the curl of mostly field-
162 aligned flow vectors are predicted to be symmetric for the axial (M) component (with a single
163 peak at the center) and bipolar for the tangential (L or N) component across the center. During
164 $\sim 08:15:3.1-3.6$ UT around 'C', J_{\parallel} is significantly greater than J_{\perp} (Fig. 2f). The predicted
165 signature is, however, ambiguous in the current density (Fig. 2e) and even opposite in the ion
166 vorticity (bipolar $\Omega_{i,M}$ and relatively symmetric $\Omega_{i,N}$ in Fig. 2k) across \sim 'C'. J_{\parallel} shows double
167 peaks around 'C', instead of a single peak (blue arrows in Fig. 2f). These peaks coincide with
168 bipolar peaks in $\Omega_{i,M}$ (green arrows in Fig. 2k). Also, the magnetic curvature (Fig. 2h-j) that is
169 expected to be bipolar along L and N across the center of a typical flux rope, exhibits complicated
170 profiles, in particular, showing consecutive bipolar signatures in the L component (Fig. 2h). These
171 observations further support that the present FTE consisted of two flux tubes.

172 **Reconnection at the interface of two interlinked flux tubes.** At the center of the B_N
 173 reversal around ‘C’, B (black profile in Fig. 2d and Fig. 3Aa) and the magnetic pressure (P_B ; blue
 174 in Fig. 3Ae) display a (weak) local depression. MMS2 (Fig. 3Ba and e) also observed a
 175 suppressed peak in these profiles around ‘C’. This is a so-called ‘M’-shaped crater FTE²³. The
 176 plasma pressure (P_{pl} ; red profiles in Fig. 3e) was locally enhanced at the center of the FTE. These
 177 P_B and P_{pl} variations constitute a relatively single P_{tot} (black profiles in Fig. 3e) enhancement
 178 around ‘C’.

179 The B reduction/suppression at ‘C’ might result from local reconnection. This is supported
 180 by the existence of an abrupt change in B_N (rather than sinusoidal bipolar B_N), indicating a local
 181 current sheet (red profile in Fig. 2d and Fig. 3a). [Note that the present L , M , and N axes
 182 correspond to N , $-M$, and L axes, respectively, in nominal 2-D reconnection geometry, where L
 183 directs along the current sheet and N points to the current sheet normal.] Correspondingly, ion
 184 outflow jets directed along N (red arrows in Fig. 3c) and out-of-plane electron jets along M
 185 (vertical green arrow in Fig. 3d) carried a significant electric current (Fig. 3m). $\mathbf{J} \cdot \mathbf{E}'$ fluctuated,
 186 showing negative values before/around ‘C’ (Fig. 3n). These observations are consistent with
 187 typical signatures of reconnection, particularly under a large guide field^{24,25}. The negative
 188 (positive) $\mathbf{J} \cdot \mathbf{E}'$ represents a transfer of energy from plasmas to the magnetic fields (from the
 189 fields to plasmas). The highly fluctuating $\mathbf{J} \cdot \mathbf{E}'$ indicates strong interactions between the
 190 magnetic fields and plasmas with the negative values implying the outer edge of the electron
 191 diffusion region²⁶ or associations with waves²⁷.

192 Fig. 5 shows 2-D cuts of 3-D electron distributions at three selected times before, around,
 193 and after ‘C’ (Fig. 5a, b, and c), denoted by black arrows at the bottom of Fig. 3A. The upper and
 194 lower panels show the electron distributions as a function of $(V_{\parallel}, V_{\perp 1})$ and $(V_{\perp 1}, V_{\perp 2})$,
 195 respectively. Parallel and perpendicular directions are defined with respect to the local magnetic
 196 field (\mathbf{B}). The two perpendicular directions are chosen to be perpendicular to \mathbf{B} approximately
 197 along the ion bulk velocity (\mathbf{V}_i), $\mathbf{V}_{\perp 1} = \mathbf{B} \times (\mathbf{V}_i \times \mathbf{B})$ and $\mathbf{V}_{\perp 2} = \mathbf{B} \times \mathbf{V}_i$.

198 Fig. 5(a) shows a low-density, high-temperature (Fig. 3b) magnetospheric electron
 199 distribution. Fig. 5(c) shows a heated, antiparallel-streaming magnetosheath electron distribution.
 200 Fig. 5(b) shows a mixture of the two populations. Note the superposition of a magnetosheath
 201 electron population shaped as a half shell in $(-V_{\parallel}, V_{\perp 1})$ plane. At the same time, the $(V_{\perp 1}, V_{\perp 2})$
 202 distribution shows a certain level of agyrotropy, i.e., a lack of axisymmetry (red arrow in the
 203 lower middle panel in comparison to lower left and right panels showing almost gyrotropic
 204 distributions). The half-shell shape in the $(V_{\parallel}, V_{\perp 1})$ distributions together with a weak electron
 205 agyrotropy indicates the outer edge of the electron diffusion region²⁶. These simultaneous
 206 observations of B_N reversal, ion outflow jets, out-of-plane electron jets, non-zero $\mathbf{J} \cdot \mathbf{E}'$, and anti-
 207 parallel half-shell/slightly agyrotropic electron distribution manifest that reconnection was
 208 occurring in the interface between two interlinked flux tubes.

209 Discussion

210 **Magnetic topology of two interlinked flux tubes.** Our analyses indicate that the present
 211 FTE consisted of two interlaced flux tubes. The electron PAD showed energy-dependent
 212 variations that infer different magnetic topologies^{8,28,29} across the center of the FTE (Fig. 3j-l).

213 In particular, dramatic changes in the electron PADs were observed before and after ‘C’.
 214 This includes a significant reduction in the low and mid energy electron fluxes (Fig. 3j, k)
 215 immediately before ‘C’, during ~08:15:02.75-3.20 UT (‘A’-~‘L’ at the top of Fig. 3A) for
 216 MMS4 and during ~08:15:02.70-3.15 UT (‘A’-~‘L’ at the top of Fig. 3B) for MMS2. These low

217 (and mid) energy electrons were mostly counter-streaming between ‘L’ and ‘C’, while low-
218 energy electrons were mostly one-directional (anti-parallel) immediately after ~‘C’ during
219 ~08:15:03.20-3.65 UT (~‘L’-‘B’ at the top of Fig. 3A) for MMS4 and during ~08:15:03.15-3.55
220 UT (~‘L’-‘B’ at the top of Fig. 3B) for MMS2. The 90° pitch-angle electrons were greatly
221 enhanced in the high-energy range (Fig. 3l) only before ‘C’.

222 These 90°-focused energetic electrons can be either locally energized or trapped on the
223 field lines connected to both hemispheres. The former corresponds to trapped electrons locally
224 bouncing within the exhaust region with a large magnetic gradient/curvature, showing a pitch-
225 angle broadening at magnetic-strength minima in accordance with the first adiabatic invariant⁸.
226 We over-plot black and magenta dotted contours over the electron PADs (Fig. 3j-l) that represent
227 loss-cone angles under an assumption that there is a mirror point with a magnetic strength of 109
228 nT (black) or 100 nT (magenta). These contours appear to generally separate the 90°-focused
229 energetic population from field-aligned ($< \sim 45^\circ$) and weaker anti-parallel ($> \sim 135^\circ$) populations
230 (Fig. 3l). This signature is, however, mostly seen before ‘C’, during which the pitch-angle
231 broadening often shows a deviation from the expectation. Furthermore, the locally
232 bouncing/focusing population will result in a balance in fluxes between parallel and anti-parallel
233 components. The parallel population prevails over the anti-parallel throughout the period shown
234 in Fig. 3 (compare Fig. 3g and 3i). There is also an interval during which the anti-parallel
235 population is more dominant (e.g., red arrows at the top of Fig. 3l). Although the former can be
236 explained by the fact that the overall structure was embedded in the southern outflow region of
237 an X-line (Fig. 4b), the latter is hardly explained. Thus, the local energization cannot fully
238 explain these 90°-focused energetic electrons that were exclusively observed before ‘C’, and
239 accompanied by the imbalanced parallel and anti-parallel fluxes.

240 For electrons being trapped on the field lines with their ends connected to the northern and
241 southern hemispheres, it takes ~ 5 s (2 s) for 1 keV (10 keV) electrons to travel 5 R_E along the
242 magnetopause field lines. The most energetic electrons on recently-closed field lines (via
243 reconnection at the interface of the two flux tubes) will constitute the 90°-focused population,
244 while less energetic electrons will lead to the imbalance between the parallel and anti-parallel
245 fluxes. On the other hand, the most energetic electrons on early-closed field lines can escape
246 away from the field lines, while less energetic ones remain trapped at 90°. This feature is exactly
247 seen as an inverse energy-time dispersion of high-energy electrons with perpendicular (or anti-
248 parallel) pitch angles (red arrows in Fig. 3h and 3i).

249 The absence or reduction of these 90°-focused energetic electrons after ‘C’ indicates
250 magnetosheath field lines or open field lines with one end connected to the northern or southern
251 hemisphere (Fig. 3l). During ‘C’-‘T’, the parallel high-energy population was still denser than
252 the anti-parallel one, possibly due to the background effect associated with the location of the
253 overall structure. Before/around ‘B’, a notable reduction in these energetic electrons, together
254 with uni/bi-directional low-energy electrons (Fig. 3j) indicates the magnetosheath field lines
255 (with neither end connected to the hemisphere), on which the low-energy magnetosheath
256 electrons flow along one direction or both directions with respect to **B**.

257 Thus, the energy-dependent PAD variations across the center of the FTE infer that the two
258 flux tubes contain field lines of different magnetic topologies: one with the field lines connected
259 to both hemispheres and the other with open field lines connected to the magnetosheath. This
260 was further evidenced by the plasma density and temperature (Fig. 3b) and particle distribution
261 functions (Fig. 5).

262 Fig. 1(b-e) illustrates the generation of such interlinked flux tubes and their connectivity to
263 either both hemispheres or the magnetosheath. For the southward and duskward IMF during this
264 event (Fig. 1b), reconnected field lines at '1' in Fig. 1(c) (generating cyan field lines) can
265 constitute a flux tube 'ft1'-'ft2' in Fig. 1(d), with one end connected to the northern hemisphere.
266 Reconnected field lines at '2' in Fig. 1(c) (generating magenta field lines) can constitute a flux
267 tube 'ft3'-'ft4', with one end connected to the southern hemisphere (Fig. 1d). When the interface
268 of the interlaced flux tubes undergoes reconnection (dashed violet arrows in Fig. 1d), 'ft1' and
269 'ft4' field lines are reconnected, constituting "ft C-T" with both ends connected to the
270 magnetosheath (blue arrows in Fig. 1e), and 'ft2' and 'ft3' field lines are reconnected,
271 constituting "ft L-C" with both ends connected to the magnetosphere (red arrows in Fig. 1e).
272 When these newly intertwined flux tubes move southward/duskward past by MMS4 as depicted
273 by blue arrows in Fig. 1(e) mostly along L , "ft L-C" is first traversed by MMS, then, "ft C-T" is
274 traversed, consistent with the observations of Fig. 4(b) and the electron PADs.

275 We note that the reconnecting flux tubes (Fig. 1d) result in a more complicated structure
276 (Fig. 1e). This structure will exert strong magnetic tension force toward the interface of the two
277 interlinked flux tubes, which facilitates an interaction of the interface. The plasma and field data
278 showed that the two flux tubes were reconnecting at the interface (dashed violet arrows in Fig.
279 1e). The magnetic curvature, $(\mathbf{B} \cdot \nabla \mathbf{B})_N / \mu_0$ (black in Fig. 2j) reverses its sign from positive to
280 negative across 'C', as expected for "ft L-C" and "ft C-T" in Fig. 6d. The strong, clearly-bipolar
281 feature across the FTE center, thus, supports the complicated interlaced flux tubes, Fig. 1e.

282 The N component of the magnetic curvature (black profiles in Fig. 2l) is not balanced by
283 any of the pressure gradients (red, blue, and green profiles in Fig. 2l). The L and M components
284 (black profiles in Fig. 2i and j) are, however, partly balanced by the gradient of the total pressure,
285 ∇P_{tot} (green) or the magnetic pressure (∇P_B , blue). Around 'C', the current density parallel to \mathbf{B}
286 is larger than the perpendicular component, which is, however, significant ($J_{\parallel} = \sim 1800 \text{ nA/m}^2$; J_{\perp}
287 $= \sim 1000 \text{ nA/m}^2$; Fig. 2f). These suggest that the FTE is neither force-free nor force-balanced.
288 This might indicate that the FTE was under evolution, explaining the highly variable plasma
289 flows (Fig. 3c, d), current (Fig. 2e, f; Fig. 3m), and $\mathbf{J} \cdot \mathbf{E}'$ (Fig. 2g; Fig. 3n) within the FTE.
290 Depending on the evolutionary phase of the interlinked flux tubes, a portion of field lines within
291 the FTE can be either connected to either hemisphere (Fig. 6c) or both hemispheres (Fig. 6d).

292 **Implications and conclusion.** The complex magnetic field topology and various magnetic
293 connectivity including field lines with both ends connected to the magnetosphere within the FTE
294 result from the kinetic process, i.e., reconnection locally occurring at the center of the FTE (not
295 occurring outside or at the periphery of the FTE). This makes a striking distinction from the
296 previous multiple X-line FTE model³ (Fig. 1a) that can also involve either newly-opened
297 magnetosheath field lines or completely closed field lines within an FTE^{28,29}. When connected to
298 both hemispheres, the flux tube becomes an efficient channel for solar wind transfer into the
299 magnetosphere. The resulting complicated structure (Fig. 1e) resembles a typical flux rope
300 structure, and consecutive interface reconnection (e.g., dashed violet arrow in Fig. 1e) will lead
301 further evolution to a flux rope (twining flux tubes). The interlinking of flux tubes will also
302 potentially suppress magnetic flux transfer into the magnetotail, via which FTEs act for the main
303 driver of the magnetospheric dynamics such as substorms and storms³⁰. The magnetic
304 connectivity will continuously vary during different epochs in the evolution, both regulating the
305 transfer of the solar wind into the magnetosphere and the magnetic flux transfer from the dayside
306 to the magnetotail.

307 The importance of the local kinetic processes occurring inside FTEs is, therefore, two-fold.
308 First, they lead to the topological structure and evolution of FTEs. Second, they determine
309 macroscale characteristics of FTEs (magnetic connectivity and magnetic content), including their
310 global effects. Using the MMS observation of the FTE event, we emphasized the importance and
311 impact of one of the local kinetic processes, i.e., reconnection, occurring within FTEs, implying
312 that the kinetic process can play a crucial role in the generation, structure, evolution, and impact
313 of FTEs.

314 **Methods**

315 **Instrumentation and data availability.** The MMS spacecraft⁶ flying in low-inclination
316 and highly elliptical orbits provide the measurements at/near Earth's magnetopause, bow shock,
317 and magnetotail. The four spacecraft are identically equipped with instruments including plasma
318 instruments (FPI)³¹, magnetometers (FGM)³², and electric field instruments (EDP) consisting of
319 the spin-plane double probe (SDP)³³ and the axial double probe (ADP)³⁴. We used the magnetic
320 field data from FGM with a time resolution of 10-ms in burst mode, the DC electric field data
321 with a 0.122-ms time resolution in burst mode, and particle data in burst mode from the FPI/DIS
322 for ions and FPI/DES for electrons with a 150-ms and 30-ms time resolution, respectively, a
323 11.25° angular resolution, and an energy range of ~10 eV–26 keV. The MMS data are accessible
324 through the public link provided by the MMS science working group teams:
325 <http://lasp.colorado.edu/mms/sdc/public/>.

326 The Moon-orbiting ARTEMIS spacecraft³⁵, designed to investigate the Moon's interaction
327 with the solar wind, also provide high time resolution (3-s) data of solar wind conditions. We use
328 the data from the fluxgate magnetometer (FGM) and electrostatic analyzer (ESA) to obtain
329 interplanetary magnetic field (IMF) orientation and solar wind speed for the present FTE event.
330 The ARTEMIS data are available at <http://themis.ssl.berkeley.edu/>. The data were lagged by 13
331 minutes in this event to account for the transit time of the solar wind from ARTEMIS-C, located
332 at [64.2, 3.3, 3.3]_{RE} in GSM to MMS at [9.0, -1.2, 1.3]_{RE} in GSM.

333 **Determination of boundary normal coordinates (LMN).** We determined boundary
334 normal coordinates (LMN) by we performing 1) minimum variance analysis (MVA)¹⁶ and 2)
335 minimum directional derivative (MDD) analysis¹⁷. The former method using the four-spacecraft
336 magnetic field data during 0815:01.0-04.5 UT derived $L = [0.35, -0.72, 0.60]$, $M = [0.46, -0.43, -$
337 $0.78]$, and $N = [0.82, 0.55, 0.17]$ in GSM. To comply with conventions, N points outward from
338 the magnetopause and L points northward along the dayside magnetopause, partly aligning the
339 magnetospheric magnetic field (see the top of the right panel of Fig. 1a). The medium-to-
340 minimum (maximum-to-medium) eigenvalue ratio was ~3.3 (4.5), indicating a relatively reliable
341 calculation³⁶. The MDD result is shown in Fig. 2(b-c). The eigenvector of the matrix,
342 $(\nabla\mathbf{B})(\nabla\mathbf{B})^T$ corresponding to the minimum eigenvalue significantly fluctuated (Fig. 2b). At
343 ~0815:03.5 UT, around which the sign of B_X was reversed (Fig. 2a) and the error was minimized
344 (Fig. 2c), the three eigenvectors of $(\nabla\mathbf{B})(\nabla\mathbf{B})^T$ pointed $L = [0.39, -0.61, 0.69]$, $M = [0.45, -0.52,$
345 $-0.72]$, and $N = [0.80, 0.60, 0.07]$ in GSM, where M corresponds to the (negative/positive)
346 eigenvector for the minimum eigenvalue of $(\nabla\mathbf{B})(\nabla\mathbf{B})^T$ (Fig. 2b), representing the most invariant
347 axis. The difference between MVA-derived and MDD-derived L , M , and N ranged from 5.8° to
348 8.3°. We used the averaged MVA and MDD result: $L = [0.38, -0.66, 0.65]$, $M = [0.46, -0.48, -$
349 $0.75]$, and $N = [0.81, 0.58, 0.12]$ in GSM.

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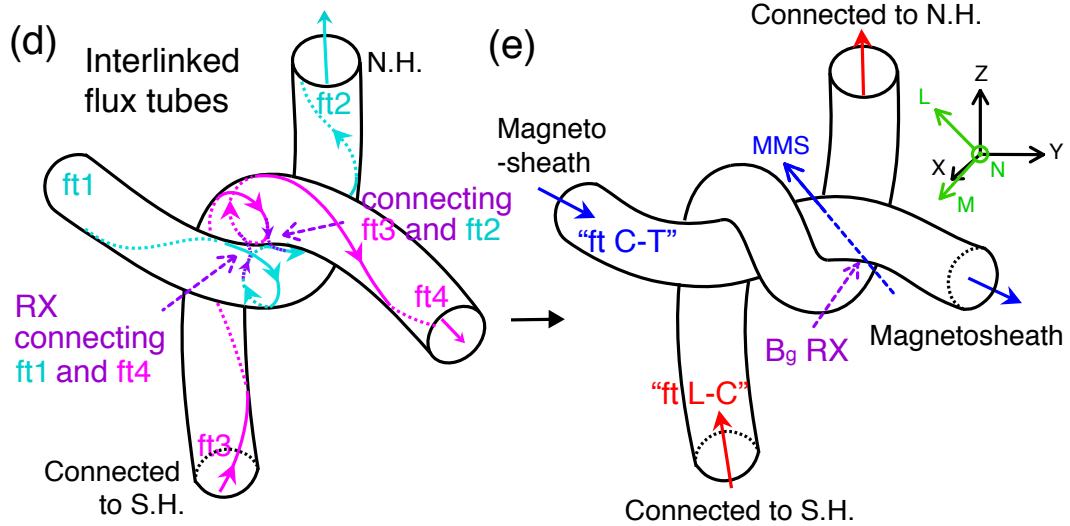
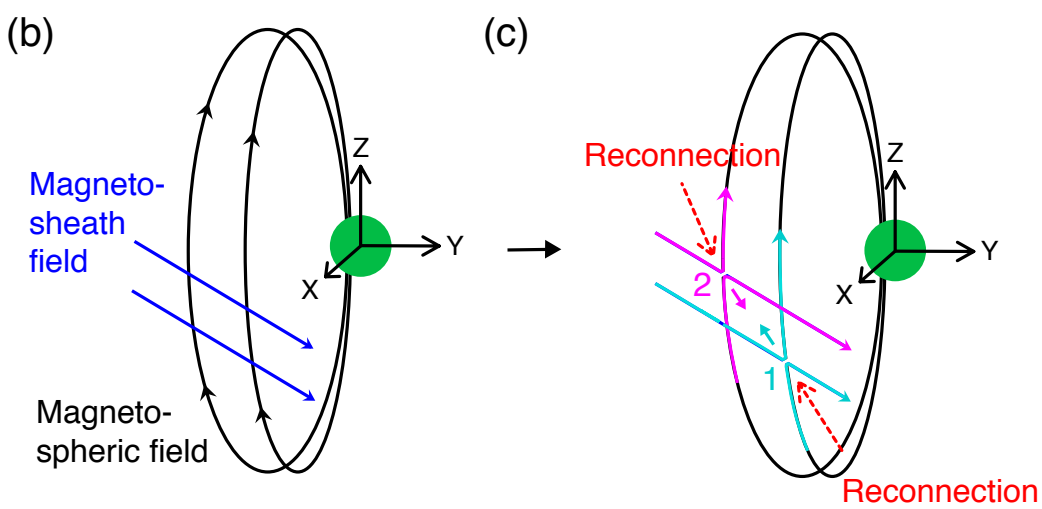
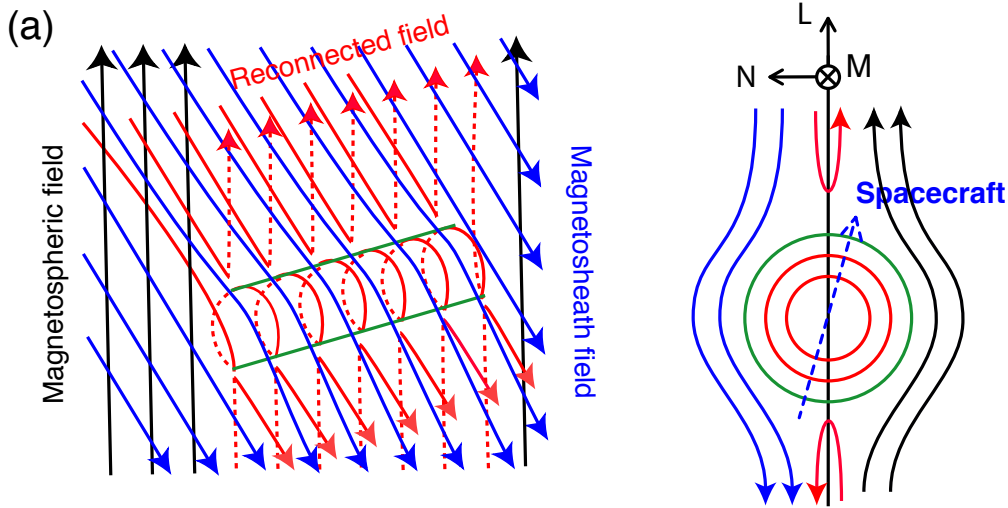
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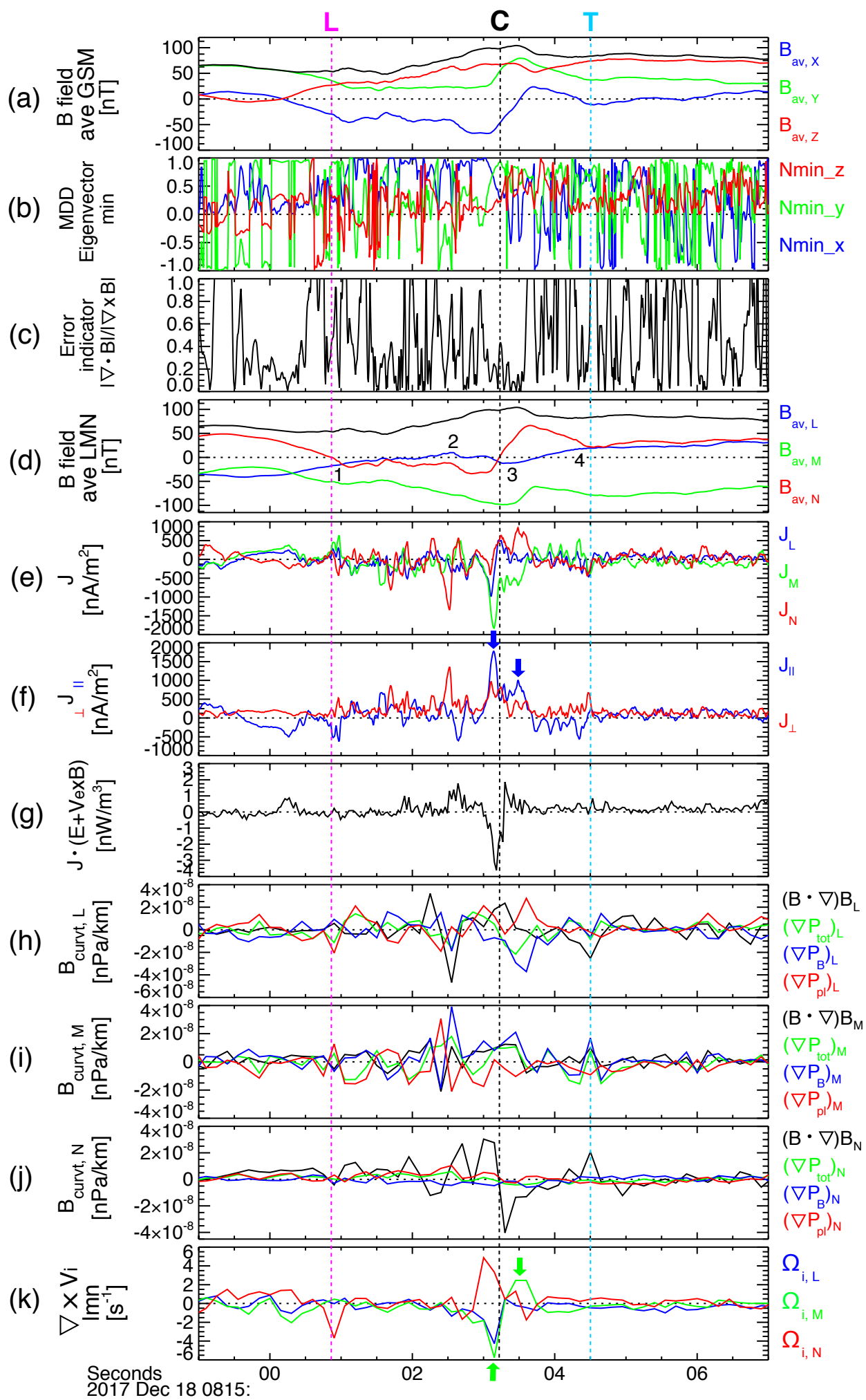
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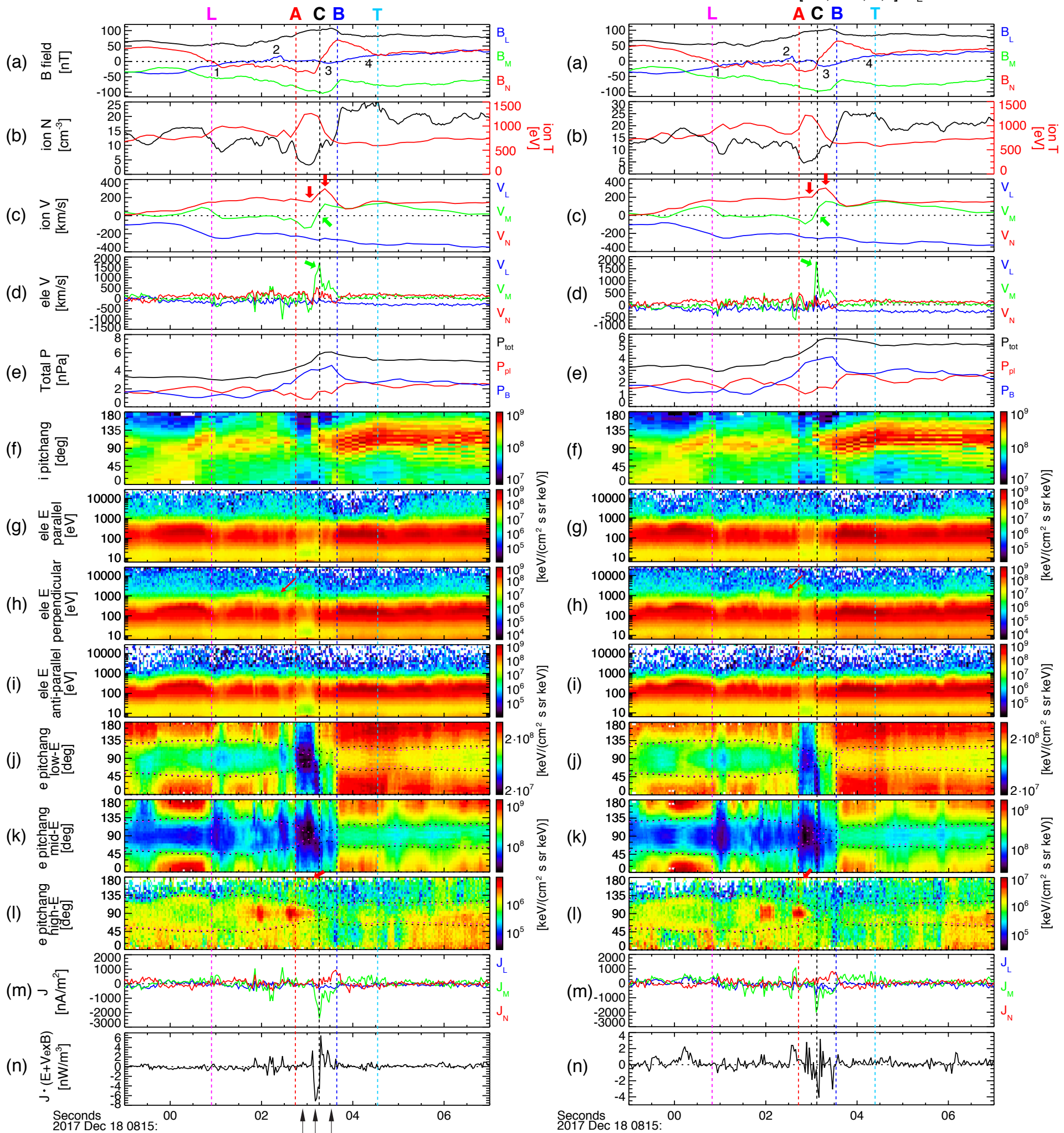
440 **Figure 1.** (a) The multiple X-line FTE model for the southward and dawnward IMF. The
441 unreconnected magnetospheric and magnetosheath magnetic field lines are shown by black and
442 blue arrows, respectively. Red arrows represent reconnected magnetic field lines. The edge of the
443 FTE is shown in green. The left panel shows a view from the Sun (the normal to the
444 magnetopause surface) and the right panel shows a view from dawn to dusk (along the direction
445 tangential to the magnetopause). The nominal LMN coordinates for the FTE are shown at the top
446 of the right panel. (b-d) Illustration of the generation of interlinked flux tubes under the
447 southward and duskward IMF and (e) their connectivity to either hemisphere or both
448 hemispheres: reconnected field lines at '1' in (c) (generating cyan field lines) can constitute a
449 flux tube 'ft1'-'ft2' in (d), with one end connected to the northern hemisphere. Reconnected field
450 lines at '2' in (c) (generating magenta field lines) can constitute a flux tube 'ft3'-'ft4', with one
451 end connected to the southern hemisphere (d). When the interface of the interlaced flux tubes
452 undergoes consecutive reconnection (dashed violet arrows in d), 'ft1' and 'ft4' field lines are
453 reconnected, constituting "ft C-T" with both ends open (blue arrows in e), and 'ft2' and 'ft3'
454 field lines are reconnected, constituting "ft L-C" with both ends connected to the magnetosphere
455 (red arrows in e).



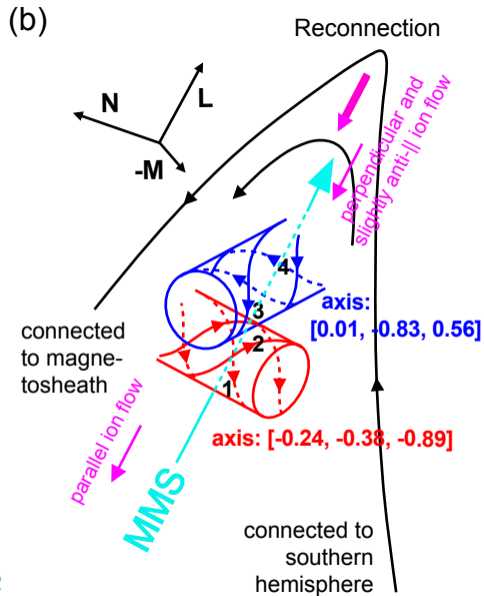
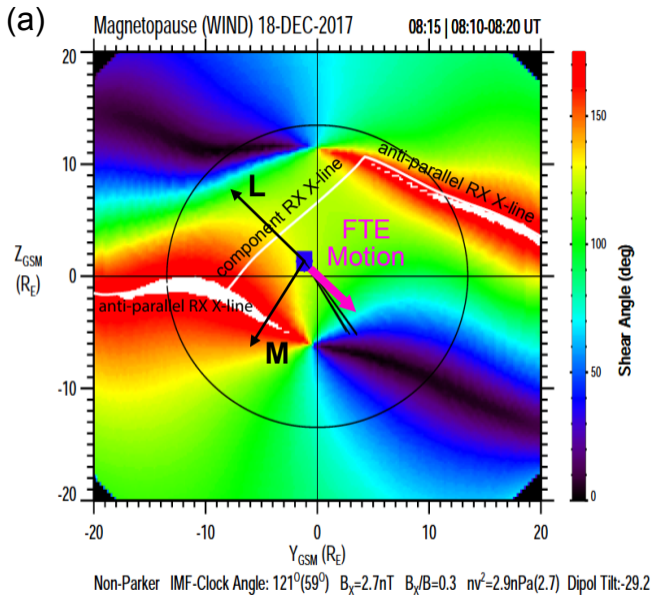
456 **Figure 2.** Four MMS observations of an FTE detected on 18 December, 2017: (a) the
 457 tetrahedral-averaged magnetic field using the measurements from the four MMS spacecraft: B_X ,
 458 B_Y , and B_Z components (blue, green, and red profiles) in GSM, together with the magnetic
 459 strength (B ; black); (b) the result of minimum directional derivative (MDD) analysis¹⁷ showing
 460 the eigenvector of the matrix, $(\nabla\mathbf{B})(\nabla\mathbf{B})^T$ in GSM, corresponding to the minimum eigenvalue,
 461 with an error indicator, $|\nabla \cdot \mathbf{B}|/|\nabla \times \mathbf{B}|$ (c). All vector parameters in the lower panels are shown in
 462 boundary normal coordinates, LMN that were determined from minimum variance analysis
 463 (MVA)¹⁶ and MDD¹⁷: $L = [0.39, -0.61, 0.69]$, $M = [0.45, -0.52, -0.72]$, $N = [0.80, 0.60, 0.07]$ in
 464 GSM: (d) the tetrahedral-averaged magnetic field (\mathbf{B}) with B_L , B_M , and B_N components (blue,
 465 green, and red profiles), together with the magnetic strength (black); (e, f) the current densities
 466 (\mathbf{J} ; e) that are decomposed into two components (f) parallel (blue profiles; J_{\parallel}) and perpendicular
 467 (red; J_{\perp}) to \mathbf{B} calculated from the curlometer technique³⁸; (g) Joule dissipation in the electron rest
 468 frame, $\mathbf{J} \cdot \mathbf{E}'$, where \mathbf{E}' is the electric field in the electron frame of reference, $\mathbf{E}' = \mathbf{E} + \mathbf{V}_e \times \mathbf{B}$; (h-j)
 469 the L , M , N component of the magnetic curvature, $(\mathbf{B} \cdot \nabla\mathbf{B})/\mu_0$ (black) and the gradients of the
 470 total pressure (∇P_{tot} , green), the plasma pressure (∇P_{pl} , red), and the magnetic pressure (∇P_B ,
 471 blue); (k) ion flow vorticity ($\mathbf{\Omega}_i = \nabla \times \mathbf{V}_i$). Vertical dashed magenta, black, and cyan lines denote
 472 the leading edge, center, and trailing edge of the FTE.



473 **Figure 3.** MMS4 (A) and MMS2 (B) observations of the FTE: (a) magnetic field (\mathbf{B}), B_L , B_M ,
474 and B_N components (blue, green, and red profiles), together with the magnetic strength (black);
475 (b) ion density (black) and temperature (red); (c) ion velocity (\mathbf{V}_i); (d) electron velocity (\mathbf{V}_e); (e)
476 plasma (red) and magnetic (blue) pressures, and the sum of plasma and magnetic pressures
477 (black); (f) ion pitch angle distribution (PAD); (g-i) energy spectrograms of electrons of parallel
478 ($0^\circ\sim 30^\circ$; g), perpendicular ($60^\circ\sim 120^\circ$; h), and anti-parallel ($150^\circ\sim 180^\circ$; i) pitch angles; (j-l) pitch
479 angle distributions (PAD) of the low- ($\sim 10 \text{ eV} \leq \text{energy} < 100 \text{ eV}$; j), mid- ($100 \text{ eV} \leq \text{energy} < 1$
480 keV; k), and high- ($1 \text{ keV} \leq \text{energy} < 26 \text{ keV}$; l) energy electrons; (m) the current densities
481 obtained from the particle data; (n) Joule dissipation in the electron rest frame, $\mathbf{J} \cdot \mathbf{E}'$, using the
482 single spacecraft data. All vector parameters are shown in LMN coordinates. Vertical dashed
483 dashed magenta, black, and cyan lines denote the leading edge, center, and trailing edge of the
484 FTE. Vertical dashed red and black lines mark the location where abrupt changes in the low and
485 mid energy electron fluxes (Fig. 3j, k) appear.

A. MMS4 at [9.0, -1.2, 1.3] R_EB. MMS2 at [9.0, -1.2, 1.3] R_E

486 **Figure 4.** Modeled shear angles between the magnetosheath and magnetospheric magnetic field
487 lines using the solar wind IMF condition and Earth's dipole tilt for the event shown in Fig. 2 and
488 3 (a). White traces represent primary X-lines over the surface of the magnetopause when viewed
489 from the Sun. A blue rectangle denotes the location of the MMS spacecraft. Black lines and a
490 thick magenta arrow show the model prediction and the observation, respectively, of the plasma
491 bulk flow or the motion of the FTE observed at the MMS location. (b) a schematic diagram of
492 the FTE structure consisting of two interlinked flux tubes embedded in the southern outflow
493 region of the reconnection X-line when viewed mostly from the $-M$ direction.



494 **Figure 5.** MMS4 observations of 2-D cuts of 3-D electron distributions (integrated over $\pm 11.25^\circ$
495 from the cut) at three selected times before, around, and after the center of FTE (a, b, and c),
496 denoted by black arrows at the bottom of Fig. 3A. The upper and lower panels show the electron
497 distributions as a function of $(V_{\parallel}, V_{\perp 1})$ and $(V_{\perp 1}, V_{\perp 2})$, respectively. Parallel and perpendicular
498 directions are defined with respect to the local magnetic field (\mathbf{B}). The two perpendicular
499 directions are chosen to be perpendicular to \mathbf{B} approximately along the ion bulk velocity velocity
500 (\mathbf{V}_i), $\mathbf{V}_{\perp 1} = \mathbf{B} \times (\mathbf{V}_i \times \mathbf{B})$ and $\mathbf{V}_{\perp 2} = \mathbf{B} \times \mathbf{V}_i$. A lack of axisymmetry in the $(V_{\perp 1}, V_{\perp 2})$ distribution is
501 denoted by a red arrow in the lower middle panel in comparison to lower left and right panels
502 showing almost gyrotropic distributions.

