

# MDC ADCS Primer *We've got attitude*

A. Nguyen, A. Zufall

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- An Attitude Determination Control System is designed to stabilize and orient a spacecraft toward a given direction
- This is often a critical system for mission success, for example:
	- Survival of the spacecraft. If the satellite needs to point its solar panels toward the Sun to charge the batteries.
	- Completion of the mission. If taking images of the Earth the payload must be pointed towards a desired target.





- Attitude: Orientation of a defined spacecraft body coordinate system with respect to a defined external frame
- Attitude Determination: Real-time or post-facto knowledge, within a given tolerance, of the spacecraft attitude
- Attitude Control: Maintenance of desired, specified attitude within a given tolerance
- Attitude Error: 'Low Frequency' spacecraft misalignment; usually the intended topic of attitude control
- Attitude Jitter: 'High Frequency' spacecraft misalignment; usually ignored by ADCS; reduced by good design or fine pointing/optical control



## Terminology





Low accuracy Low precision



Low accuracy High precision

- Accuracy described with maximum bias
- Precision described with standard deviation

**1-σ**

**2-σ**

**3-σ**

- $1$ - $\sigma$  bounds 68.3% (1 in 3.2)
- 2-σ bounds 95.4% (1 in 22.0)
- $\cdot$  3-σ bounds 99.7% (1 in 370.4)
- 6-σ bounds 99.99% (1 in 505 mil.)



High accuracy Low precision



- "Accuracy" is distance from truth
- "Precision" is repeatability
- Be prepared for inconsistency between datasheets and manufacturers







- Do I need an active ADCS system?
	- Some spacecraft systems do not have ADCS requirements
- Do I need to know where I am pointed?
- Why do I need to point there?
- What component on the spacecraft am I pointing there?
- How close is 'close enough'?

#### What are the requirements?



#### ADCS Requirements







#### Steps In Attitude Design







#### Attitude Control Types







**Spin-stabilized**



### Active Attitude Control



• Active Control Systems directly sense spacecraft attitude and supply a torque command to alter it as required. This is the basic concept of feedback control





#### Satellite Dynamics





#### **WARNING: MATH ON NEXT SLIDE**



### Satellite Dynamics - Theory



Degrees of Freedom (DOF): *the number of independent parameters that define its configuration or state*

Total: 6 DOF Translational: x, y, z Rotational: roll, pitch, yaw



5.7.1 Euler's  $1^{st}$  Law:

The resultant force applied to a rigid body  $R$  is equal to the product of the mass of the rigid body and the acceleration of the center of mass of the rigid body in an inertial reference frame  $N$ , that is,

> $F = m^{\mathcal{N}}a$  $(5-225)$

#### 5.7.2 Euler's  $2^{nd}$  Law:

The resultant moment applied to a rigid body  $R$  relative to a point  $O$  fixed point in an inertial reference frame  $N$  is equal to the rate of change of angular momentum of the rigid body relative to point  $O$  in reference frame  $N$ , that is,

$$
\mathbf{M}_O = \frac{\mathcal{N}_d}{dt} \left( \mathcal{N} \mathbf{H}_O \right) \tag{5-226}
$$

The sum of the resultant moment applied to a rigid body relative to an arbitrary reference point Q and the inertial moment due to the acceleration of the reference point Q relative to the center of mass of a rigid body is equal to the rate of change of angular momentum of the rigid body relative to the reference point Q, that is,

$$
\mathbf{M}_Q - (\mathbf{r} - \mathbf{r}_Q) \times m^{\mathcal{N}} \mathbf{a}_Q = \frac{\mathcal{N}_d}{dt} (\mathcal{N} \mathbf{H}_Q)
$$
 (5-235)

$$
M_Q - (\bar{r} - r_Q) \times m^{\mathcal{N}} a_Q = \frac{\mathcal{R}_d}{dt} \left( I_Q^{\mathcal{R}} \right) \cdot {}^{\mathcal{N}} \omega^{\mathcal{R}} + I_Q^{\mathcal{R}} \cdot {}^{\mathcal{N}} \alpha^{\mathcal{R}} + {}^{\mathcal{N}} \omega^{\mathcal{R}} \times \left( I_Q^{\mathcal{R}} \cdot {}^{\mathcal{N}} \omega^{\mathcal{R}} \right)
$$





$$
M_Q - (\bar{r} - r_Q) \times m^{\mathcal{N}} a_Q = \frac{\mathcal{R}_d}{dt} \left( I_Q^{\mathcal{R}} \right) \cdot {}^{\mathcal{N}} \omega^{\mathcal{R}} + I_Q^{\mathcal{R}} \cdot {}^{\mathcal{N}} \alpha^{\mathcal{R}} + {}^{\mathcal{N}} \omega^{\mathcal{R}} \times \left( I_Q^{\mathcal{R}} \cdot {}^{\mathcal{N}} \omega^{\mathcal{R}} \right)
$$



#### Euler's Second Law (1/3)



Vector to Vector to Forces acting Torque acting each item ref. point on the system on the system mass • *Prop.* • *ADCS Actuators Center of Geometry*• *Drag* • *Drag*



## Euler's Second Law (2/3)





#### Euler's Second Law (3/3)









$$
\mathbb{M}_{\mathbb{Q}} - \left(\bar{\mathbf{r}} - \mathbf{r}_{\mathbb{Q}}\right) \times \eta \mathbf{M}_{\mathbf{Q}} = \frac{\mathbb{R}_{d}}{dt}\left(\mathbf{I}_{\mathbb{Q}}^{\mathcal{R}}\right).\mathbf{W}_{\mathbf{Q}}\mathbf{R} + \mathbf{I}_{\mathbb{Q}}^{\mathcal{R}}\ \mathbf{M}_{\mathbf{Q}}\mathbf{R} + \mathbf{M}_{\mathbf{Q}}\mathbf{R} \times \left(\mathbf{I}_{\mathbb{Q}}^{\mathcal{R}}\ \mathbf{M}_{\mathbf{Q}}\mathbf{R}\right)
$$

"Relative to inertial ref. frame"

Require to describe the motion of a satellite

- · Inertial Earth (IE) coordinate system,
- · Satellite's Body (B) coordinate system
- · Local-Vertical-Local-Horizontal (LVLH) coordinate system (assigned for nadir pointing)





#### Disturbance Torques







#### Typical Disturbances



- Gravity Gradient: "Tidal" Force due to  $1/r^2$  gravitational field variation for long, extended bodies (e.g. Space Shuttle, Tethered vehicles)
- Aerodynamic Drag: "Weathervane" Effect due to an offset between the CM and the drag center of Pressure (CP). Only a factor in LEO.
- Magnetic Torques: Induced by residual magnetic moment. Model the spacecraft as a magnetic dipole. Only within magnetosphere.
- Solar Radiation: Torques induced by CM and solar CP offset. Can compensate with differential reflectivity or reaction wheels.
- Mass Expulsion: Torques induced by leaks or jettisoned objects
- Internal: On-board Equipment (machinery, wheels, cryocoolers, pumps etc...). No net effect, but internal momentum exchange affects attitude.







## Typical Disturbance Torques

- Generally, gravity gradient and third-body are largest disturbances
	- In LEO, third largest is aerodynamic drag
	- In MEO+, third largest is solar radiation pressure
- Aerodynamic Drag and Solar Radiation Pressure
	- Both depend on mass and geometric distribution
		- Center of Pressure vs Center of Mass
		- Drag Area/Flight configuration









#### Reference Attitude











- Coordinate system definition and consistency important
- ADCS can be used to mitigate Thermal, Power, Comm risks



## Field of Views (FOV)

- ConOps impacted by FOV of sensors and other equipment
- Typical Sensors FOV
	- Sun sensors 170-180 °
	- Star Trackers 10-20°
		- With moon and sun keepout 30-60°
- Communications narrow at higher frequencies, highly variable on antenna design and link budget
	- UHF typically omnidirectional
	- S-band 20-60°
	- K-band  $1-10^\circ$
	- Optical < 1°
- Payloads are mission dependent
	- For earth-pointing, FOV and orbital altitude determines swath width











#### Traditional Sensor Types





#### *Not typical of CubeSat class*



## CubeSat Sensor Overview



- Sun sensors (\$-\$\$): measures solar intensity hitting detector
- Magnetometer  $(\xi)$ : measures magnetic field strength and direction with respect to body axis
- Inertial Measurement Unit (IMU) (\$)
	- Gyro: measures angular velocity with respect to the body axis
	- Accelerometer: measures acceleration with respect to body axis
- Star tracker (\$\$\$\$): determines attitude through comparing visible stars to star catalogue
- Horizon sensor (\$\$\$): orients through viewing edge of earth's atmosphere



- Sun sensors: measures solar intensity hitting detector
- Typical accuracy 5°, down to 1° for high performance
	- Sun angular size in LEO is 0.5° accuracy (3-σ), 0.1° precision
- Variants: array (pyramidal/strip), slot, diode
- Placement and operational concerns
	- Must know spacecraft and the sun position for use as attitude reference (typically)
	- Antennae, solar arrays, and other deployables can interfere
	- Solar panel currents can be used as a 'coarse sun sensor'
	- Inoperable in eclipse, must handle case in FSW to avoid attitude determination solution issue







Sun sensor array

Single sun sensor



#### Magnetometer



- Magnetometer: measures magnetic field strength and direction with respect to body axis
- Typical accuracy 1-15°, varies by quality of sensor and implementation
- Can be used as science payloads or attitude determination
- Consumer COTS (\$10) to precision instruments (\$1000s)
- Placement and operational concerns
	- Spacecraft induced dipole (esp. magnetorquers, RWs) can ruin measurements (20°+)
	- Place far from high current components and ferromagnetic materials (stainless steel, regulators, etc.)
	- Must use up-to-date Earth magnetic field models (~1° error)
	- Tilted dipole model of earth's field
	- Not useful on bodies/environments with unknown magnetic models





• Integrating rates without other reference sensor measurements will diverge



• Inertial Measurement Unit (IMU)

IMU

- Gyro: measures angular velocity with respect to the body axis
- Accelerometer: measures acceleration with respect to body axis
- Consumer COTS (\$10) to precision instruments (\$10k)
	- Mechanical systems (Apollo Capsule IMU)
	- Micro Electro Mechanical System (MEMS), "sensor on a chip", < 10 deg/hr
	- Fiber Optic Gyros (FOGs), "military grade", < 0.01 deg/hr
- Placement and operational concerns
	- Only useful when using Kalman filter; does not provide attitude determination solution alone
	- Notorious for bias, must calibrate or characterize
	- Electrical noise can interfere, place away from high current/dipole areas



Apollo Capsule IMU











- Star tracker: determines attitude through comparing visible stars to star catalogue
- Accuracy down to < 10 arc-seconds (0.003°)
	- Less accurate (< 100 arc-seconds) about boresight
- Minimum  $\frac{1}{4}$  U size, depending on baffle and quality of optics
- Placement and operational concerns
	- Baffle for sun and earth keep-out (30°+)
		- Not uncommon to use 2 orthogonal trackers to improve probability of continuous coverage, Sensitive optics can be damaged if active when pointing at the sun
	- Must keep slew rate down (< 2°/s typical)
	- 5-25° FOV typical
	- Thermal and mechanical misalignment must be controlled or calibrated out
	- Cleanliness of the optics





#### Horizon/IR Sensor

- Horizon sensor: orients through viewing edge of earth's atmosphere
- Fixed telescopes for nadir pointing, accuracy  $< 0.1$ °
- Cheaper electronics for scanning, accuracy < 1°
	- Earth limb is about 2° wide depending on orbit
- Most useful for mission-specific pointing
	- Can achieve full 'nadir' attitude solution with 3 simultaneous measurements





#### Attitude Estimation







#### Attitude Estimation



- Deterministic Methods, e.g. "TRIAD" or "Q-method"
	- Minimum of 2 measured vectors whose directions in reference frame are known
		- Most commonly sun and magnetic field direction
	- In TRIAD specifically, one vector given priority and attitude solution is rotated such that other vector is aligned as closely as possible
- Probabilistic Estimator, aka some flavor of Kalman Filter
	- Wide variety of potential measurements and estimated elements ("state")
		- State is typically position, attitude, angular rates, but also can include sensor bias estimate
		- Can incorporate all sensors (and their performance) to achieve probabilistically optimal estimate
	- At each time step, propagate state with model of dynamics, then update estimated state based on how well sensor readings match expected measurements
	- Must initialize with a beginning estimated state, typically use deterministic method



## Typical Attitude Determination Systems



#### 0-axis

- Nothing
- 1-axis
	- Sun sensor (on all faces) only when sunlit, no positional knowledge
	- Magnetometer, no positional knowledge
- 2-axis
	- Sun sensor (on all faces) only when sunlit, positional knowledge
	- Magnetometer, positional knowledge
	- 3x Horizon Sensors

3-axis

- Sun sensor (on all faces), magnetometer [only when sunlit]
- 1x Star tracker









### CubeSat Actuator Overview

- Magnetorquers
- Reaction Wheels
- Propulsion
- Others not covered here
	- Control Moment Gyros
	- Drag devices: Sails/deployables



- Requires magnetic field
	- Often used in low-earth orbit
- Commonly used for:
	- Initial acquisition maneuvers (i.e. detumble)
	- Coarse attitude control
	- Momentum dumping in reaction wheel systems





#### How Magnetorquers work



- Torque rods are long helical coils
- Use current to generate a magnetic field
- This field will try to align with the Earth's magnetic field, thereby creating a torque on the spacecraft
- Size of dipole varies based on application
	- 6U CubeSat 0.2  $A \cdot m^2$  dipole = 0.01 mNm torque





Solar Panel Embedded Coils Torque Rods



Magnetic Field generated here is INTO the page





#### Magnetorquer Pros & Cons







#### Reaction Wheels

- Flywheel with fixed rotation axis, variable rotation speed
- Provide fast; continuous feedback control
- Number of Axis-control = number of wheels each axis
- Sizing varies widely based on application
	- CubeSat: 1 mNm torque, 10 mNms storage, < 1 W
	- Flagship: 100 mNm torque, 10k+ mNms storage, 20 W



Four wheels allows for three-axis control in the event of single wheel failure



### How Reaction Wheels Work



- Torques are created on a spacecraft by creating equal but opposite torques on Reaction Wheels (flywheels on motors)
- For three-axes of torque, three wheels are necessary. Use four wheels for redundancy
- If external torques exist, wheels will angularly accelerate to counteract these torques
- They will eventually reach a max RPM limit at which time they must be desaturated





Ang. Momentum = MOI x Ang. Velocity  $\vec{H} = I * \vec{\omega}$ 



## Reaction Wheel Pros and Cons







## Reaction Control System (RCS)

- Typically cold gas propulsion
- Quick, effective way to dump momentum
- 1 mNm 10 Nm torque, 10-10k Nms storage
	- Varies based on propellant type, thruster size, length of moment arm, fuel storage
	- CubeSat typically 1-100 mNm, 10-100 Nms range
- Operational concerns
	- Generally cannot generate pure torque, creates some undesirable translational force
	- Minimum bit results in uncontrollable deadband
	- Special controls to reduce fuel usage
	- Amount of fuel directly determines mission lifetime
		- Unmodeled disturbances increase fuel usage, but too much fuel wastes mass and volume





Double canted thrusters give control in all three axis



#### Attitude Controller







### Attitude Controller



- Receive data from vehicle sensors and derive the appropriate commands to the actuators to rotate the vehicle to the desired attitude.
- Algorithms range from very simple, e.g. proportional control, to complex nonlinear or adaptive functions, depending on mission requirements.
	- Remember to KISS!
- The design of the control algorithm depends on the actuator to be used for the specific attitude maneuver although using a simple proportional– integral–derivative controller (PID controller) satisfies most control needs.
	- Prop systems most common cause to use non-linear control



#### PID Control Example for a Reaction Wheel

















## Other System Considerations

- On-board computer, processing power
- Ground processing
- Simulation
- Testing
- Maneuvers
	- Attitude/Translation Coupling



## ADCS Modeling and Simulation



- 
- Flight Software half Running on the spacecraft (more or less)
- Spacecraft + Environmental Model half Dynamics and disturbances
	-
	- Model fidelity vs time and effort
- Helps guide and validate mission design
- Answer questions to reduce mission risk at lower<br>: cost and effort than physical testing. For example cost and effort than physical testing. For example:<br>• "What is the impact on mission success if we suffer a
	- reaction wheel failure?"
	- "How long will detumble last?"
	- "What is the expected pointing error if our sun sensors are not calibrated correctly?"
	- "How goes the center of mass offset from center of geometry affect fuel use over mission lifetime?
- Helps guide analysis of downlinked health data





- "Test-as-you-fly" mentality
	- Risk reduction efforts
	- FSW development
	- End-to-end tests
- Procedures
	- Test plan, "as-run"
	- Documentation, signatures
- ADCS-specific challenges
	- Environmental disturbances
	- Measuring actuator response
	- Complicated end-to-end behavior







**Fig. 2: Million dollar knots**





#### Adam Zufall ([adam.b.zufall@nasa.gov](mailto:adam.b.zufall@nasa.gov))

#### More resources here:

- <https://ntrs.nasa.gov/archive/nasa/casi.ntrs.nasa.gov/20110007876.pdf>
- https://www.faa.gov/about/office org/headquarters offices/avs/offices/aam/cami/library/online librari es/aerospace\_medicine/tutorial/media/III.4.3.1\_Space\_Vehicle\_Control\_Systems.pdf





