

An Encounter with the Ion and Electron Diffusion Regions at a Flapping and Twisted Tail Current Sheet

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Key Points:

- We analyze signatures of asymmetric reconnection earthward of the X-line in a flapping and reconnecting magnetotail current sheet.
- PIC simulations support MMS key observations and inferences.
- The flapping episode was associated with a substorm onset.

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Abstract

We analyze data returned by the Magnetospheric Multiscale mission (MMS) constellation during a rapid (~ 1.5 s) traversal of a flapping and reconnecting current sheet (CS) in the near-Earth magnetotail ($X \sim -20 R_E$). The CS was highly tilted, with its normal pointing strongly duskward. Its extreme thinness was confirmed by a curvature analysis of the magnetic field lines. The event was associated with a guide field of $\sim 8\%$ of the reconnecting components. From the pitch angle distributions of low-energy electrons we infer that the crossing occurred earthward of the X-line. Traveling practically normal to the CS, MMS encountered an ion diffusion region (IDR) in which was embedded an electron diffusion region (EDR). IDR signatures included breaking of the ion frozen-in condition in the presence of Hall \mathbf{B} and \mathbf{E} fields. EDR signatures included a strong out-of-plane current associated with a super-Alfvénic electron jet, evidence of positive energy transfer, and a temperature anisotropy ($Te_{\parallel} > Te_{\perp}$) which disappeared at the field reversal. Derived scale sizes normal to the CS are: $\sim 6.9 d_e$ (EDR) and $\sim 0.4 d_i$ (IDR) (40 and 100 km). **We estimate the average dimensionless reconnection rate as 0.077 ± 0.050 .** The observations and inferences are supported by PIC numerical simulations. **We find very good agreement in the reconnection rates.** We also discuss the effects of asymmetries in the density, temperature and magnetic field strength on the Hall fields and length of the outflow jets. The event is associated with a substorm onset which began 7 min after the MMS observations.

1 Introduction

Soon after the discovery of the geomagnetic tail at the start of the space age (Ness, 1965), it was found that the tail can sometimes move rapidly in a north-south direction (Speiser and Ness, 1967). This flapping motion was deduced from a reversal in the polarity of the Earth-Sun component of geomagnetic tail field, B_x , concomitant with a decrease in the total magnetic field strength. The typical duration of this up-down motion is a couple of minutes, with an amplitude of a few R_E (Toichi and Miyazaki, 1976, Sergeev et al., 2003, Runov et al., 2009). Tail flapping is now a well-known phenomenon that has been repeatedly reported by spacecraft making observations close to the tail current sheet (CS, or neutral sheet NS) in the near-tail region ($R \sim -15$ to $-30 R_E$). Not well established is what gives rise to it. Over the years both internal (see e.g. Sergeev et al., 2004,

53 Zhang et al., 2005) as well as external (i.e. solar wind origin; e.g., Toicki and Miyazaki
54 (1976), Sergeev et al., 2008, Runov et al., 2009) origins have been proposed.

55 It was Lui et al. (1978) who first pointed out that in tail flapping we are dealing
56 with a wave propagating from the center of the tail towards the flanks. This was inferred
57 from the polarity changes in the east-west component of the field, B_y : these changes re-
58 verse in adjacent crossings of the CS. Our understanding of tail flapping was fostered by
59 multi-spacecraft observations made, in particular, by Cluster and THEMIS. In a num-
60 ber of papers (e.g. Zhang et al., 2002, 2005, Runov et al., 2003, 2005, Sergeev et al., 2003,
61 2004, see also Shen et al., 2008 and references therein) the properties of this wavy mo-
62 tion were investigated. It was proposed that during tail flapping a kink-like disturbance
63 propagates east-west towards the flanks (Sergeev et al., 2003, 2004). The vertical speed
64 of the CS along its normal was calculated to be 60-100 km/s or more (Runov et al., 2003;
65 Sergeev et al., 2004). The flankwise speed of the wave was estimated to be a few tens
66 of km/s (Runov et al. 2009). A statistical analysis (Runov et al., 2005) yielded a cur-
67 rent density of 5-25 nA/m². Sometimes the cross-tail current was also bifurcated, be-
68 ing concentrated in two sheets with a weak magnetic field in between (e.g. Runov et al.,
69 2003).

70 One complication is that the tail current sheet can be locally twisted, with its nor-
71 mal not pointing in the z-direction of the Geocentric Solar Magnetospheric (GSM) co-
72 ordinate system. Further, this tilt can be quite large, with the CS-normal locally point-
73 ing mainly in the east-west direction. In this case, the wavy motion due to flapping would
74 be superposed on an extremely-twisted CS (e.g. Zhang et al., 2002, Sergeev et al., 2003).

75 A note on the possible generating mechanisms is in order. Among the possible ori-
76 gins of tail flapping is that of solar wind Alfvénic waves when the total field is bigger than
77 10 nT and which propagate down the tail with the solar wind. They modulate the tail
78 magnetopause boundary, which is then reflected in CS oscillations. This was proposed
79 by Toichi and Miyazaki (1976). After that the main view was that the origin is inter-
80 nal to the tail, though nothing was nailed down conclusively. However, the possibility
81 of a solar wind origin was raised again in Sergeev et al. (2008) and Runov et al. (2009),
82 in particular, the effects of directional changes in the z-component of the solar wind flow.
83 This will be of great relevance here.

84 Another mechanism was proposed by Erkaev et al. (2008), consisting of a new MHD,
85 ‘double-gradient’ wave model. The theory requires the simultaneous presence of a gra-
86 dient of the transverse magnetic field (B_x) along the normal (z) and of the normal mag-
87 netic field component (B_z) along the transverse (x) directions with respect to the CS.
88 Stable flapping motion requires that the product of these two gradients be positive.

89 We know, of course, that magnetic reconnection can take place in the geomagnetic
90 tail. Here, magnetic field lines which have been opened during reconnection on the day-
91 side are closed again and returned back to the dayside, thus giving rise to a twin-cell plasma
92 circulation pattern and forestalling wholesale erosion of the dayside magnetosphere. The
93 first clear evidence of an ion diffusion region during tail reconnection was given by **Na-**
94 **gai et al. (2001)**. This is consistent with collisionless reconnection.

95 With this background, one would then expect tail reconnection to occasionally hap-
96 pen during tail flapping. This is the situation we focus on here. We discuss MMS data
97 in the near-tail region ($X \sim -20R_E$). We have, namely, a series of tail current sheet flap-
98 ping motions lasting about 24 min where in one instance all the spacecraft traverse the
99 CS very rapidly ($\sim 1-2$ s), implying a very thin CS. In fact we find it was thin enough
100 for ions and electrons to both decouple from the magnetic field. Various reconnection
101 signatures, such as super-Alfvénic electron flow jets in the in-plane and out-of-plane di-
102 rections, energy transfer in the electron frame, Hall electric and magnetic field signatures,
103 etc., are seen during the traversal. The brevity of the CS-passage implies very curved
104 magnetic field lines associated with a thin CS. Its structure can be examined using dif-
105 ferential geometry methods applied to the magnetic field lines and based on the 4-spacecraft
106 MMS configuration. It also implies the possibility of departure from adiabatic motion,
107 when the gyroradii of the particles become of order of, or larger than, the curvature ra-
108 dius of the magnetic field lines (MFLs). In this event the MMS spacecraft do not observe
109 any flow reversals, since they cross on one side of the X-line. We shall also argue that
110 the EDR is crossed earthward of the X-line during this episode, thus providing one of
111 the few published examples of reconnection on one side of the X-line. PIC simulations
112 are also presented and they support this interpretation of the event. **They also sug-**
113 **gest a reconnection process which is steady and occurring at a rate consis-**
114 **tent with that inferred from the observations.**

115 The layout of the paper is as follows. We first give an overview of the longer flap-
116 ping interval, highlighting typical time and length scales, and augmenting it with an anal-
117 ysis of the field line curvature. We then discuss the electron behavior in our 10-s long
118 interval of interest. After that, we give the observational evidence for the presence of an
119 EDR embedded in an IDR and of the claim that the MMS spacecraft are crossing the
120 EDR in an approximately normal direction and earthward of the X-line. A section fol-
121 lows where we present the results of PIC simulations done with initial conditions tailored
122 to fit the event. In the discussion we suggest a likely cause of the flapping motions and
123 also consider the effect of plasma and field asymmetries on the structure of the recon-
124 nection region. We finish with a short summary.

125 **2 Instrumentation**

126 The MMS spacecraft measure electric and magnetic fields using the FIELDS in-
127 strument suite, which consists of three electric field and three magnetic field instruments
128 (Torbert et al., 2016). The analog and digital fluxgate magnetometers (AFG/DFG) mea-
129 sure magnetic fields in the frequency range from DC up to 64 Hz (Russell et al., 2016).
130 The higher frequency range, from 1 Hz up to 6 kHz, is covered by a search-coil magne-
131 tometer (SCM; Le Contel et al., 2016). Level 2 fluxgate magnetometer (FGM) data of
132 version 5.86 and higher (highest available as of submission) were used throughout this
133 study.

134 The Electric Field Double Probe (EDP) components of the FIELDS suite return
135 measurements of the electric field at each spacecraft. The two pairs of spin-plane (SDP)
136 and axial (ADP) double probes allow MMS to make direct measurements of the full 3D
137 electric field, ranging from DC to 100 kHz (Lindqvist et al., 2016, Ergun et al., 2016).
138 These data are combined into the EDP data product for 3D vector \mathbf{E} measurements. Ver-
139 sion 3.0.0 of the level 2 EDP data products was used throughout this study. Level 2 burst
140 mode data was used unless stated otherwise. Level 3 (L3) EDP data were used in some
141 parts of the analysis and were produced specifically for this study. L3 EDP data features
142 reduced uncertainty derived from careful examination and tailoring of the filters used
143 to correct for periodic gain variations and interference from other instruments. This re-
144 quires extensive investigation of the spacecraft status and local environment at the time
145 of measurement, so that intervals of L3 EDP data are generated only on request to the
146 FIELDS team.

147 The Fast Plasma Instrument (FPI) on MMS returns high cadence electron and ion
148 distributions in the energy/charge range from 10 eV/q to 30 keV/q. Each MMS satel-
149 lite is equipped with eight FPI spectrometers which, when combined with electrostatic
150 control of the field-of-view, allows FPI to sample the full electron and ion distributions
151 (Pollock et al. 2016). The core ion distributions may extend beyond the range of FPI,
152 so that actual ion temperatures may be higher than what is calculated using FPI mo-
153 ment data. Level 2 FPI ion moments of version 3.3.0 were used throughout this study.

154 Positions of the individual spacecraft in the MMS fleet are provided using Mag-
155 netic Ephemeris and Coordinates (MEC) data products (Morley, 2015) and are calcu-
156 lated using the LANLGeoMag suite (Henderson et al. 2018). In order to ensure that the
157 formation of the MMS fleet was appropriate for the calculation of spatial gradients, a
158 minimum value of the Tetrahedron Quality Factor (TQF: Fuselier et al. 2016) was re-
159 quired with $TQF \geq 0.8$. All instrument data used in this study are available from the
160 MMS Science Data Center (<https://lasp.colorado.edu/mms/sdc>). Level 2 burst mode
161 data was used throughout this study except where explicitly noted. Calculations of the
162 magnetic field line curvature and curlometer current density were made using the mms-
163 curvature library and is publicly available ([https://github.com/unh-mms-rogers/mms-
164 curvature](https://github.com/unh-mms-rogers/mms-curvature)).

165 Interplanetary data are from *Wind*. The magnetic field (Lepping et al., 1995) and
166 the plasma data from the 3DP instrument (Lin et al., 1995) are at 3s resolution. The
167 geomagnetic indices are obtained from NASA/OMNI data website, and the geomagnetic
168 field data are from the SuperMag website.

169 **3 Observations**

170 **3.1 Overview**

171 By way of an overview, Fig 1 shows magnetic field observations made by MMS1
172 during the 40-min interval from 20:10:00 to 20:50:00 UT, June 17, 2017. The first three
173 panels show the components of the magnetic field in GSM coordinates, followed by the
174 total field strength. The MMS satellites are located in the near-tail at $X \approx -20 R_E$ and
175 on the dawnside ($Y \approx -10 R_E$). The polarity changes in the B_x component provide clear
176 evidence of tail current sheet flapping, and four clear instances may be discerned. The
177 opposite sense of B_y polarity reversals at adjacent current sheet (CS) crossings indicate

178 that the associated waves move toward the flanks (Lui et al., 1978). Typically, each cross-
179 ing lasts from a few tens of sec to a couple of min.

182 An exception to this occurs at $\sim 20:24$ UT (arrowed). Here the CS crossing is very
183 brief, and it took MMS only ~ 1.5 s to go from one side to the other. This implies (a)
184 that it is a very thin CS, and (b) that there is more to this crossing than just a flapping.
185 We shall show below it is a crossing through the EDR of a reconnecting CS. Note that
186 minimum B is not quite 0 nT, so there is a small guide field (see below).

194 Fig 2 shows the MFL curvature and angle relative to the current sheet in the re-
195 gion. For reference, the average magnitude of the magnetic field across all four space-
196 craft is shown in panel a. The MFL curvature is defined as $\mathbf{K} = \mathbf{b} \cdot \nabla \mathbf{b}$, where \mathbf{b} is the
197 unit vector along the field line. It is computed using magnetic field and positional data
198 from the four spacecraft. The encountered X-line was embedded in the second of four
199 consecutive neutral sheet crossings.

200 The calculated radius of curvature (panel c) is never smaller than half the space-
201 craft separation, indicated by the horizontal dashed purple line. The MFL radii of cur-
202 vature during each of these crossings show a compression of the CS evolving over suc-
203 cessive encounters. The first crossing shows a current sheet compressed broadly to near
204 electron scales. The second encounter contains the X-line which is the focus of our study
205 here and displays the thinnest current sheet, indicated by having the smallest radius of
206 curvature of the observed crossings. Later crossings have progressively larger radii of cur-
207 vature, so that the current sheet in the neighborhood of MMS thickened after the X-line
208 encounter.

209 Calculating the tilt angle (γ_N) between the current density and the normal to the
210 osculating plane of the magnetic field lines (Shen et al. 2007, 2008), we find that the CS
211 tilt increased as its thickness decreased (panel d). The first flapping CS encounter shows
212 a small tilt angle ($< 30^\circ$) while the tilt seen at 20:24:07 UT during the second CS en-
213 counter is significantly larger ($\sim 80^\circ$). In the subsequent CS encounters, the tilt angle
214 reduces progressively to smaller values as the greater flapping event dies down.

3.2 Electron Behavior

We now switch to a coordinate system, LMN , centered on the CS. Carrying out a minimum variance analysis (MVAB) on the magnetic field data (Sonnerup and Scheible, 1998) over the interval 20:24:05 – 20:24:10 UT, we obtain: $\mathbf{L} = (0.930, 0.296, -0.216)$, $\mathbf{M} = (-0.275, 0.176, -0.945)$, and $\mathbf{N} = (-0.242, 0.938, 0.245)$ in GSM coordinates. The intermediate-to-minimum eigenvalue ratio = 15.9, i.e. large enough for the result to be robust. The normal \mathbf{N} is mostly in the positive GSM Y-direction, i.e. pointing towards dusk. So we have a flapping CS which, in addition, is strongly tilted in the YZ plane.

To check how reliable this LMN system is, we need to obtain \mathbf{N} independently, for example, by triangulating a feature seen at different times by all four spacecraft (Russell et al., 1983; Knetter et al., 2004). In Fig 3 we plot on the right the profile of B_z over a 2-s period when it goes from positive to negative values. We can see that the traces of MMS2 and MMS4 (red and blue) are indistinguishable because these two spacecraft cross the CS practically simultaneously. Their separation vector when they are crossing is $\mathbf{D}_{2,4} = (21.8, 6.3, -11.0) R_E$. This makes an angle of 91° with the MVAB \mathbf{N} , which is consistent with the previous result for \mathbf{N} , and implies also that there is no local warping.

The separations of the spacecraft relative to the first one to cross the CS, i.e. MMS3 (green), are shown in the left panels of Fig 3. The average spacecraft separation is about 26 km. At 20:24 UT, MMS3 is at $(-19.3, -10.3, 5.5) R_E$ (GSE). The wave associated with the flapping moves from MMS3 to MMS2/MMS4 to MMS1, advancing towards dawn, as it should (see Introduction). It took ~ 0.5 s to go from MMS3 to MMS1, separated mainly in the Y-direction by ~ 25 km, so the speed toward the flanks is ~ 50 km/s.

We now consider the MFL curvature during the second encounter, the one of interest here. In Fig 4 we plot the curvature parameter (also called “adiabaticity parameter”) $\kappa \equiv (R_c/R_{g_e})^{1/2}$ evaluated at the barycenter of the MMS configuration, where R_c is the radius of curvature of the MFLs, and $R_{g,e}$ is the gyroradius of electrons of perpendicular energy 200 eV, 1 keV and 5 keV, respectively, distinguished by colors. At around 20:24:07 UT, $\kappa < 1$ and the maximum gyroradii are larger than the minimum radius of curvature of the MFL. This implies a very thin CS where the electrons are no longer coupled to the magnetic field and their motion is non-adiabatic. The electrons are scat-

249 tered for $\kappa < 3$ (**horizontal line**, Egedal et al., 2008; Lavraud et al., 2016), and become
250 chaotic for $\kappa < 10$ (Büchner and Zelenyi, 1989).

254 Fig 5 displays features of the electron behavior over an 8-s interval centered around
255 the CS crossing. For reference, the first two panels show the magnetic field components
256 in LMN coordinates, and the field strength. In anticipation of results given below, the
257 vertical guidelines bracket the IDR (orange) and EDR (green). We note the following:
258 (i) there are asymmetries across the CS in B , Ne and Te . Before the CS crossing the elec-
259 trons are more dense, hotter, and lie in a somewhat weaker magnetic field; (ii) There is
260 a strong electron jet peaking at ~ 2200 km/s, which is mainly in the out-of-plane M -direction
261 (panel 6). With an inflow Alfvén speed, $V_{A,in} \sim 400$ km/s, it is super-Alfvénic with M_A
262 ~ 5.5 ; (iii) There is a flow reversal in the L component (panel 5) just after 20:24:08.2
263 UT, as MMS1 approaches the separatrix on leaving the EDR. This reversal is due to the
264 dominant amount of low-energy electrons entering the EDR along the separatrix as well
265 as the deceleration of the higher energy exhaust electrons, both due to a possible am-
266 bipolar electric field, E_L (blue trace in panel 5). This aspect of the EDR dynamics is the
267 subject of future work.

268 We note that the density asymmetry, of about 25%, as well as the asymmetry in
269 B and Te , have a significant effect on the length of the outflow jets (Montag, 2018, Mon-
270 tag et al., 2020). They also affect the temporal profile of the Hall fields. We return to
271 these points in the discussion section.

278 The event exhibits no reconnection-related ion or electron flow reversals (see Fig
279 5 for the electrons and Fig 9, below, for the protons), i.e. the X-line does not pass over
280 the spacecraft. On which side of the X-line are the spacecraft crossing the CS? Fig 6 shows
281 the pitch angle distributions (PADs) of low-energy electrons (20-200 eV) in the order from
282 top to bottom MMS 3-2-1, i.e. moving downward. Before the CS crossing (when $B_L <$
283 0) the flow is parallel to \mathbf{B} , while after (when $B_L > 0$) it is anti-parallel to \mathbf{B} . This be-
284 havior indicates that MMS is crossing the CS earthward of the X-line (see e.g. Wang et
285 al., 2010, their Fig 3). In this way the low-energy electrons are aligned with the mag-
286 netic field and moving towards the X-line on both sides of the CS.

3.3 An EDR embedded in an IDR

In this event the MMS constellation crossed both the IDR as well as the EDR. We now discuss the identification of these diffusion regions, starting with the IDR. Fig 7 shows from top to bottom, the adiabatic expansion parameter, δ_i (Scudder et al., 2008), the current density in the out-of-plane (M) direction, the electric field normal to the CS, E_N , and the out-of-plane magnetic field, B_M . The dotted red line in the last panel is the guide field, B_g ($=-0.8$ nT), calculated from the angle between the ambient reconnecting fields. Parameter δ_i in panel 1 is the ratio of the \mathbf{E}_\perp -to-magnetic forces experienced by an ion. A value ≥ 1 is a good indication of demagnetized ions.

The normal electric field is the Hall \mathbf{E} -field, produced by the differential motion of ions and electrons. It is strong and it points to the CS from both sides. E_N pointing to the CS from both sides is consistent with reconnection under only a small guide field (see Torbert et al. 2018, and references therein.) E_N is also asymmetric, with the negative part being stronger, a feature we return to **when we compare with the PIC simulations** and in the Discussion. The Hall magnetic field, $B_H = B_M - B_g$ goes from negative to positive, as appropriate for a crossing earthward of the X-line. In this case, positive B_H is stronger. Parameter J_M gives an estimate of the duration of the IDR encounter (Zhao et al., 2019), which is shown bracketed by the vertical orange lines. To further support this extent of the IDR we show in Fig 8 the quantity $\mathbf{E} \times \mathbf{B} / B^2$ in black and the perpendicular flow velocity of electrons (in blue) and ions (red). It is seen that within the boundaries shown in Fig 7 the latter are not coupled to the magnetic field. The estimated thickness of the IDR in the normal direction can be obtained from the velocity of the CS along its normal (see below) and the duration of the crossing. We obtain ~ 100 km, i.e. about $0.4 d_i$.

Together with Fig 7, Figs 9 and 10 provide evidence of the presence of an EDR embedded within the IDR. Fig 9 shows the L (red), M (orange), and N (green) components of the magnetic field for reference, the proton velocity components (in black, the total velocity), and **proton temperatures in eV**, the electron velocities parallel (red) and perpendicular to \mathbf{B} , the parallel (red) and perpendicular electron temperatures in eV, the L3 electric field parallel to \mathbf{B} , with error bars included, **and the out-of-plane component of the electric field, E_M** .

333 The proton data show a lack of any ion outflow jetting (in L direction). This is con-
 334 sistent with a spacecraft trajectory which crosses the EDR close to the X-line. **The pro-**
 335 **ton temperatures show no evidence of heating.** The electron temperatures are gen-
 336 erally unequal with $Te_{\parallel} > Te_{\perp}$, an anisotropy which is more pronounced before the
 337 CS crossing. The anisotropy goes away around $B_L \sim 0$ in the time from 7 to 7.8 s. As
 338 the spacecraft cross the DRs, the Te_{\perp} increases, implying that energy is going not only
 339 to produce the electron jets but also to heat the electrons perpendicular to \mathbf{B} (see also
 340 Torbert et al., 2018). The rise is from 500 to 640 eV, i.e. about 28%. The electron ve-
 341 locities show a prominent field-aligned flow (red trace) at the CS crossing. Away from
 342 it, the perpendicular velocities dominate. When the electrons exit the EDR, their par-
 343 allel flow reverses direction, an effect caused by E_{\parallel} .

344 We now consider some relevant scale sizes. The separation vector between MMS1
 345 and MMS3 as they cross the CS is $\Delta(1, 3) = (-4.60, 23.11, 15.0)$ km. This vector makes
 346 an angle of 18.5° with the CS normal (see above), so their separation along \mathbf{N} is 26.5
 347 km. It took 0.42 s for the CS to go from MMS3 to MMS1, so the speed of the CS along
 348 its normal is -63.1 km/s. Compared to quoted values, this is a fairly typical one (see e.g.
 349 Runov et al., 2003, Sergeev et al., 2003). The spacecraft took 1.52 s to cross the IDR
 350 and 0.75 s to cross the EDR in the normal direction. Thus the normal width of the EDR
 351 = 44.2 km, i.e. $6.9 d_e$ (electron inertial length). To further confirm this, we use Ampere's
 352 law. Across the EDR $\Delta B_L \sim 12$ nT and $J_M \sim 200$ nA/m². This yields Δ_N (EDR) =
 353 48 km, consistent with the previous estimate. Further, using the minimum radius of cur-
 354 vature as an estimate for maximum half-width of the CS (Shen et al. 2008), $h \leq R_{C,min} =$
 355 $22.0 km$ implying a width of $\leq 44.0 km$ for the CS near the X-line.

356 In the EDR, a clear electric field parallel to \mathbf{B} is seen. A careful and rigorous anal-
 357 ysis over a 20-s interval gave an error bar of 1.12 mV/m on the L3 values, which has been
 358 overlaid. Thus, the E_{\parallel} is real. **We now use the electric field measurements to es-**
 359 **timate the reconnection rate.**

360 **The reconnection electric field E_R is evaluated as E_M in the velocity frame**
 361 **co-moving with the X-line, i.e., $E_R = \langle E_M + (\mathbf{V}_{Xline} \times \mathbf{B})_M \rangle$. When calculat-**
 362 **ing E_R , errors may arise from improper assessments of the orientation and**
 363 **velocity of the X-line. If the X-line orientation is improperly determined, then**
 364 **the very large E_N may contribute to the much smaller E_M (see for instance**

365 Genestreti et al. 2018, their Fig 5c-d). Given that this is a crossing roughly
 366 normal to the CS, the largest source of error resulting from improper assess-
 367 ment of the X-line velocity will be $B_L V_N$. Following Genestreti et al., we have
 368 determined the correlation between E_M and E_N in the X-line frame, noting
 369 that a strong correlation may indicate coordinate errors. (Results are sum-
 370 marized in Supplementary SFig 1.) We find nearly no correlation and a least-
 371 squares fit of E_N vs E_M has a slope of 0.018 ± 0.008 (middle panel), corre-
 372 sponding to an error of $1.0^\circ \pm 0.5^\circ$ in our coordinate axes, which confirms
 373 that our coordinate system is robust. (For comparison, the robust coordinates
 374 of Genestreti et al.'s Fig 5d had an error of $\sim 1.3^\circ$).

375 The reconnection electric field is determined as the average of E_R within
 376 the EDR interval (20:24:07 – 20:24:07.8 UT). We use E-field data from all four
 377 spacecraft, smooth the data using a 3rd-order Savitzky-Golay filter and a ± 0.05
 378 second convolution window, and exclude points with large $|E_N| > 5$ mV m $^{-1}$.
 379 The slopes of the fit lines, shown in SFig 1, are used to rotate our LMN co-
 380 ordinate system before calculating E_R . The rotation angles are very small,
 381 being $\leq 1.7^\circ$, and this correction therefore has a very minor impact ($\leq 4.5\%$)
 382 on E_R . The result is $E_R = 0.442 \pm 0.281$ mV/m. To obtain the normalized
 383 reconnection rate, we choose an inflow interval from 20:24:10-20:24:11 UT,
 384 which is steady, and divide E_R by the product of the inflow upstream Alfvén
 385 speed (V_{Ai0}) and inflow magnetic field strength (B_{L0}). The resulting dimen-
 386 sionless rate is $E_R/V_{Ai0}B_{L0} = 0.077 \pm 0.050$.

387 This calculation was done using our nominal estimate for the X-line speed
 388 in the normal direction, derived above, i.e. $V_N = 63$ km/s. We consider now
 389 the impact of uncertainties in V_N of ± 20 km/s ($\pm 30\%$) (top and bottom pan-
 390 els). For $V_N = 40$ km/s we use the same approach to obtain $E_R/V_{Ai0}B_{L0} =$
 391 0.078 ± 0.050 and the least-squares fit of E_N vs E_M has a slope of $0.11^\circ \pm 0.46^\circ$.
 392 For $V_N = 80$ km/s we find $E_R/V_{Ai0}B_{L0} = 0.076 \pm 0.050$ and a slope of $1.7^\circ \pm$
 393 0.5° . We conclude that the dimensionless reconnection rate is ~ 0.077 , though
 394 with uncertainty bars of order of $\pm 60\%$ which are predominantly a result of
 395 scatter in E_M . In section 4 this result is compared with that obtained from
 396 PIC simulations.

402 Further EDR properties are shown in Fig 10. Panels 3 and 4 give the parallel and
 403 perpendicular current densities. In the center of the EDR the current is primarily in the
 404 parallel direction and generated by electrons moving anti-parallel to the field. At the edges
 405 of the EDR it is primarily in the perpendicular direction. The current densities are very
 406 strong: a couple of hundreds nA/m^2 (Fig 10 panels 3 and 4). Compare these with the
 407 values of a few tens of nA/m^2 resulting from the statistical survey of Runov et al. (2005)
 408 (see Introduction). Fig 11 shows the PADs of low-, mid- (200 eV - 2 keV), and high-energy
 409 (2 - 30 keV) electrons. Mid-energy electron PADs show a 'hole' in the **anti**-parallel di-
 410 rection while the higher energy electrons are isotropic.

414 Fig 10, panel 5 shows the energy transfer term $\mathbf{J}\cdot\mathbf{E}'$, where \mathbf{E}' is the (L3) electric
 415 field (sampling rate of 654 Hz) in the electron rest frame ($\mathbf{E}' = \mathbf{E} + \mathbf{V}_e \times \mathbf{B}$). The cen-
 416 tral EDR is a load region where energy is transferred from electromagnetic fields to par-
 417 ticles. At its edges, roughly between the IDR and EDR boundaries, we have generator
 418 regions, with the electrons feeding energy to the magnetic field. Interestingly, while pos-
 419 itive energy transfer is a good signature of an EDR, the largest, positive energy trans-
 420 fer occurs outside the diffusion regions, north of the CS. This is where the electric field
 421 component E_L is acting on low-energy electrons entering the EDR along the separatri-
 422 ces and on the higher energy exhaust electrons, decelerating them. The electron Mach
 423 number V_e/V_{Te_\perp} is ~ 0.15 .

424 4 PIC Simulations

425 4.1 Simulation Setup

426 We performed 2-1/2 dimensional simulations of this MMS event, using the fully
 427 kinetic particle-in-cell code VPIC (Bowers et al., 2008). The simulation is performed in
 428 the XZ plane and is started from a simple 1-D Harris type current sheet with a weak
 429 guide field. The initial magnetic field and the corresponding number density are set up
 430 as $B_x(z) = B_0 \tanh(z/L_0)$, $B_y = B_g$, and $n_{i,e}(z) = n_0 \text{sech}^2(z/L_0) + n_b$, where B_0 is
 431 the background reconnecting magnetic field component, B_g is the initial, uniform guide
 432 field, n_0 is the Harris density component, n_b is the background density, and L_0 is the half-
 433 thickness of the initial CS. The initial parameters are set up by referring to the observed
 434 values as $n_0/n_b = 1.25$, $T_i/T_e = 6.25$, and $B_g = -0.08B_0$. The ion and electron temper-
 435 atures are set to be uniform. L_0 is set to be $0.6 d_i$, where d_i is the ion inertial length based

436 on n_0 . The ratio between the electron plasma frequency and the gyrofrequency is set to
437 be $\omega_{pe}/\Omega_e = 2.0$. The ion-to-electron mass ratio is $m_i/m_e = 100$. The system size based
438 on d_{i0} is set to be $L_x \times L_z = 80d_i \times 40d_i = 800d_e \times 400d_e = 7680 \times 3860$ cells with a to-
439 tal of 1.2×10^{11} superparticles (4000 particles/cell on average). The boundary conditions
440 are periodic along the x-direction, with conducting walls along the z-direction. A weak
441 initial magnetic field perturbation is added at the center of the simulation domain ac-
442 cording to $\delta\mathbf{B} = \mathbf{z} \times \nabla\Phi$, where $\Phi = 0.02B_0 \sin(x/L_x) \cos(z/L_z)$, such that reconnec-
443 tion starts near the center of the simulation domain $x=0$.

453 4.2 Results

454 Fig 12 shows an overview of the simulation results. As seen in past kinetic simu-
455 lations of reconnection with no or weak guide field, the typical Hall signatures are seen
456 near the X-point; the quadrupolar B_y pattern due to the Hall currents (Fig 12a) and the
457 polarization Hall electric field E_z pointing toward the current sheet center due to the charge
458 separation (Fig 12b). The strong U_{ey} peak, which dominantly sustains the out-of-plane
459 current component, is seen near the X-line, indicating the location of the IDR.

460 To compare these simulation results with the MMS observations, we performed vir-
461 tual observations along the virtual probe path shown in Fig 12. Here the path is cho-
462 sen by (i) determining the $z=0$ point with a similar $|U_{ey}/V_{Ae}|$ to the observed $|U_{ey}/V_{Ae}| \sim$
463 0.15 , corresponding to $|U_{ey}| \sim 2500$ km/s where $V_{Ae} \sim 1.7 \times 10^4$ km/s based on $n \sim$
464 0.5 cm^{-3} and $B_0 \sim 12$ nT), and then (ii) setting the angle from the z-axis in the x-y
465 plane as large as the observation ($\sim 18^\circ$). The path crosses the region on the earthward
466 side of the EDR, where the Hall signatures are strongly seen.

467 Fig 13 shows the virtual observation results. We see the moderate U_{ex} (correspond-
468 ing to the outflow jet) and strong U_{ey} (corresponding to the out-of-plane current) en-
469 hancements near the current sheet center (Fig 13b) sandwiched by the negative-to-positive
470 Hall B_x variation (Fig 13a) and the positive-to-negative Hall E_z variation (Fig 13c). The
471 temperature anisotropy, with $Te_{\parallel} > Te_{\perp}$, is present except near the current sheet cen-
472 ter, that is, in the EDR (see Fig 13d). This could be due to adiabatically trapped in-
473 flowing electrons and the resulting energization by the ambipolar parallel electric field
474 as predicted in past kinetic studies (e.g., Egedal et al., 2013; Le et al., 2016).

475 These variation patterns are very similar to those seen in the observations (see Figs
476 5 and 7). **(SFig2 collects these various observational parameters into one plot.)**
477 In particular, **(i)** the asymmetry in the magnitudes of the positive and negative B_y peaks
478 (compare Fig 13a and Fig 5, panel 1), **(ii)** the flat interval seen near the U_{ey} peak (com-
479 pare Fig 13b and Fig 5, panel 7) and **(iii)** the asymmetric E_z profile (compare Fig 13
480 c with Fig 7, panel 3) show consistency between the simulation and observations. In ad-
481 dition, when taking the normalization parameters as $B_0 \sim 12\text{nT}$, $n \sim 0.5 \text{ cm}^{-3}$, and
482 $V_{Ae} \sim 1.7 \times 10^4 \text{ km/s}$, the peak values of B_y , U_{ex} , U_{ey} and E_z variations seen in the
483 simulation are calculated as about 2.5 nT, 1000 km/s, 2500 km/s and 8 mV/m, all of
484 which are in reasonable agreement with the observations (see Figs 5 and 7). **These con-**
485 **sistencies indicate that the 2-1/2 D geometry on which the simulations are**
486 **based is a good representation of reality.**

487 We now calculate the dimensionless reconnection rate resulting from the
488 simulations. Fig 14 shows the evolution in time of this quantity. After recon-
489 nection onset at $T \sim 10 \Omega_i^{-1}$, the reconnection rate rapidly increases. After
490 $T \sim 35 \Omega_i^{-1}$, it saturates to a value of about 0.085. This is in very good agree-
491 ment with the (average) rate deduced from observations, i.e. $R = 0.077 \pm$
492 0.050 . The time in the simulation, at which the simulation results are com-
493 pared with the MMS data, is in a nearly steady phase of reconnection (i.e.
494 with nearly constant reconnection rate) as shown. In addition, the consisten-
495 cies indicate not only that the reconnection signatures seen in the 2.5 D sim-
496 ulation really occurred in this MMS event, but also that the observed recon-
497 nection process was in a nearly steady phase

499 5 Elements of Geoeffects

500 We now examine some geomagnetic perturbations during this event, in particular,
501 substorm activity. From 17 to 23 UT no geomagnetic storms and only one substorm were
502 recorded (source: OMNI database). Fig 15a (left) shows the north-south (X) component
503 of the geomagnetic field at six stations of the IMAGE magnetometer chain. The stations
504 are located (from top to bottom) at corrected geomagnetic latitudes 67.7 to 66°. In our
505 time of interest ($\sim 20:30$ UT), the magnetometer chain was at ~ 23 MLT. This is an ideal
506 location to monitor substorm activity (Akasofu, 1964, Wang et al., 2005). In an earlier

507 paper, Rogers et al. (2019) found a clear preference for the occurrence frequency of ge-
508 omagnetic tail IDRs to also peak at this MLT sector.

509 The decrease in the X -component (Fig 15a) recorded by the stations at around 20:30
510 UT, i.e ~ 6 min after the MMS crossing of the EDR, signifies the activation of the west-
511 ward electrojet current (WEJ), which is the diversion of the dawn-dusk cross-tail cur-
512 rent to the ionosphere during substorm onset. This being near summer solstice and a
513 sunlit atmosphere, the electrojet signatures are weaker. Fig 15b (right) shows the au-
514 roral electrojet indices AE and AL and the polar cap-north index (PCN; Troshichev et
515 al., 1998), a measure of the strength of magnetospheric plasma convection. At $\sim 20:30$
516 UT a substorm onset is recorded by the auroral indices. Simultaneously, the PCN in-
517 dex gives an indication of enhanced plasma convection. Both dayside as well as night-
518 side reconnection can contribute to increases in magnetospheric convection (Lockwood
519 et al., 1990). Clearly, here the origin of this enhancement is tail reconnection.

524 6 Summary and Discussion

528 We first summarize our work. We have analyzed MMS data at the dawnside, near-
529 tail of a flapping interval containing one very rapid crossing of the current sheet. We ar-
530 gued that this crossing was due to reconnection occurring in a very tilted and thin cur-
531 rent sheet. Using level 3 electric field data, several signatures were found supporting the
532 presence of an IDR and EDR. The pitch angle distributions of low-energy electrons ar-
533 gued in favor of an encounter on the earthward side of the X -line. The absence of ion
534 jetting was ascribed to the proximity of the encounter to the X -line. Ours was a case of
535 asymmetric reconnection (in B , Ne and Te) in the presence of a very-small (8%) guide
536 field. **Comparison with 2.5 D PIC simulations reproduced various aspects of**
537 **the observations, including asymmetries in the temporal profiles, and gave**
538 **a good agreement in the reconnection rate.** We now discuss some points result-
539 ing from this work.

540 Attempts to understand this event have been made before, to which we draw the
541 reader's attention. Huang et al. (2018) observed the ion behavior at the X -line discussed
542 here and determined that it resulted from secondary reconnection between flux ropes in
543 the outflow region of a distant primary X -line. While they note the strongly tilted bound-
544 ary coordinate system, they do not investigate the implications of this in their analysis.

545 They suggest that the event is a case of reconnection on the electron scale. Wang et al
 546 (2018) discuss the tilted nature of the current sheet of interest and associate it with pos-
 547 sible magnetotail flapping. Wang et al. (2018), however, conclude that the electron scale
 548 current sheet does not contain a reconnecting X-line. Although there is some overlap be-
 549 tween our work and these two studies, there are also significant differences. We thus of-
 550 fer here an alternative interpretation to a very intriguing event.

551 As noted in the Introduction, a solar wind origin for tail flapping has not been ruled
 552 out. Two possibilities mentioned were: (a) Alfvén waves with a high field strength (of
 553 order 10 nT), and (b) directional changes in the Z component of the flow velocity, V_z .
 554 We now discuss these briefly in relation to our event.

555 We look first at *Wind* data for the longer period 16:20-22:00 UT. This is a fast so-
 556 lar wind flow and we can show that the field and flow fluctuations satisfy the relation
 557 $\Delta\mathbf{B}_\perp = (\mu_o\rho)^{1/2}\Delta\mathbf{V}_\perp$, with correlation coefficients of ~ 0.8 (over 5015 data points) and
 558 slopes close to unity (shown in SFig 3). These fluctuations are thus Alfvénic. However,
 559 this long time interval contains no cases of tail flapping **aside from that** shown in Fig
 560 1. So Alfvén waves are certainly not a sufficient condition for flapping to occur.

561 We now turn to deflections in the solar wind V_z component (e.g. Runov et al., 2009).
 562 Fig 16 shows solar wind data for the 1-hour interval 19:20 to 20:20 UT. In the third panel
 563 of the correlated field and flow fluctuations (first 3 panels) one can see clear deflections
 564 in V_z . This fast solar wind has otherwise stable plasma parameters, in particular, the
 565 dynamic and thermal pressures. During this interval, the *Wind* spacecraft was at (202.0,
 566 21.9, -10.8) R_E , sufficiently close to the Sun-Earth line for its measurements to affect the
 567 magnetosphere. A minimum variance analysis of the magnetic field in the time interval
 568 19:40 to 20:00 UT gives a plane with normal, $\mathbf{N} = (0.96, -0.25, -0.14)$ (GSM), i.e. in-
 569 clined towards dawn at 76° to the Sun-Earth line. This structure will arrive at the dawn-
 570 side magnetopause in an estimated 37 min, i.e. a few min before the episode of tail flap-
 571 ping shown in Fig 1 is observed by MMS. We thus conclude that this solar wind distur-
 572 bance in the north-south (GSM) flow component is a very plausible cause of the tail flap-
 573 ping reported here.

578 During each of four successive encounters of MMS1 with the flapping current sheet,
 579 its half-thickness $h = R_{C,min} \cos(\gamma_N)$ was calculated from the minimum radius of MFL
 580 curvature and tilt angle of the current sheet at each encounter (Shen et al. 2008). These

581 show a flapping current sheet thinning to near electron scales before the X-line encounter
582 at 20:19:04 where $h \approx 40km$, and slowly thickening in later encounters with half-thicknesses
583 in the hundreds of km after the X-line. In each of these encounters the current sheet thick-
584 ness is well below ion scales and some Hall effect from demagnetized ions is expected.
585 The magnitude of the out-of-plane (i.e. M) curvature vector, (Fig 17, panel c)) follows
586 the out-of-plane component of the current density (J_M , Fig 7) to a degree much closer
587 than any uncertainty associated with the vector curvature measurement, consistent with
588 the MFL geometry expected from Hall magnetic fields at each encounter near the X-line.

589 The vector curvature in the L-direction at the current sheet encounter at 20:19:04
590 UT before the X-line as well as at 20:24:07 UT at the X-line remain distinctly positive
591 after accounting for measurement uncertainty (Fig 17, panel a). This indicates that MMS1
592 was on the earthward side of the X-line both before and after the low-velocity ion flow
593 reversal at 20:23:09 UT. We believe this contradicts the interpretation by Huang et al.
594 (2018) that the ion flow reversal was associated with a reconnecting X-line passing over
595 MMS, and instead interpret the ion flow reversal as an unrelated event.

596 In our flapping event we have seen that the ions were not accelerated at all (see Fig
597 9, panel 2). Huang et al. (2018) argued in favor of electron-only reconnection, such as
598 found recently in the magnetosheath by Phan et al. (2018) where ions do not partici-
599 pate in the process. However, in our case ion jetting is likely absent because the MMS
600 spacecraft cross close to the X-line. Indeed, the TWINS spacecraft saw a region of ion
601 heating, which we discuss next.

602 In SFig 4 we show observations made by TWINS in the near-tail, using an ion tem-
603 perature calculation technique described by Keese et al. (2014). TWINS saw a region
604 of enhanced ion temperatures in the magnetotail lasting about 10 min around the time
605 MMS encountered the EDR. However, it does not appear in the same location as MMS.
606 The line-of-sight mapping used to generate these images assumes a quiet Fairfield model,
607 which does not apply to our situation due to the flapping. Because of that, while we can
608 rely on the TWINS data here to show that there was ion heating, by roughly a factor
609 of two, in the 10 minutes or so surrounding our EDR encounter in the near tail, the lo-
610 cation of the ion heating shown by TWINS in these images is likely not accurate. Given
611 that (i) there is quite a bit of tail flapping, and (ii) there was no other other activity ob-

612 served, the observation by TWINS is likely to related to the same event seen by MMS,
613 and the disagreement in location is probably a projection/mapping issue.

614 Symmetric reconnection is associated with long current sheets. Adding a density
615 asymmetry, even a small one, shortens them. Our event has a density asymmetry of about
616 ~ 1.25 (far from the EDR) which, while small, may yet have significant effects. These were
617 discussed by Montag (2018) and Montag et al. (2020), who conducted a study of the im-
618 pact of small density asymmetries on antiparallel reconnection and concluded that these
619 include a shortening the length of the outflow jets. For long CSs to form, the \mathbf{B} field lines
620 must bend sharply. This can happen if the magnetic tension force is ~ 0 , i.e., if $P_{\parallel} - P_{\perp} \sim$
621 $2P_B$ (firehose condition). When the magnetic **tension** term in the momentum equation
622 changes sign, the configuration is firehose unstable. CSs can only form when both sides
623 have reached the firehose condition, so that a shortening occurs if this condition is reached
624 first on only one side. Besides, in our case the higher densities occur before the CS is en-
625 countered (see Fig 5, panel 3). Montag et al. (2020) showed that trapped electron dy-
626 namics cause parallel heating that scales strongly with variation in N , magnifying the
627 rate of parallel heating on each side of the outflow. That is probably the reason why Te_{\parallel}
628 is higher before the CS is crossed (see Fig 9). The density asymmetry is also accompa-
629 nied by a small temperature asymmetry (Fig 5, purple trace), and like the density the
630 temperature is also higher before the CS crossing (Fig 5). As the firehose condition scales
631 oppositely with density and temperature this Te -asymmetry tends to weaken the effect
632 of Ne -asymmetry (see Fig 1, Montag et al. 2020). It would be interesting to see what
633 simulations of this event tell us on this issue.

634 Asymmetries in B and Ne have also an effect on the Hall electromagnetic fields.
635 For example, the electric field normal to the CS, E_N , can even become unipolar and ex-
636 ist only on the low-beta side. This was found in observations and simulations on the day-
637 side and at higher latitudes (Mozer et al., 2008, and references therein; Muzamil et al.,
638 2014, and references therein). Evidently, our asymmetry is not strong enough for the bipo-
639 larity to go away. However, on the low-beta side (i.e. after the CS crossing), the E_N is
640 clearly stronger (**Fig 7, third panel**). **This was also present in the PIC simula-**
641 **tions.**

642 The case we studied was one of asymmetric reconnection with a small guide field.
643 We now compare and contrast with the works of Zhou et al, (2019), who discussed cases

644 of symmetric reconnection in the geomagnetic tail with a small guide field. We note that
 645 in the case of Zhou et al. the spacecraft crossed the EDR while going from one side of
 646 X-line to the other. Like Zhou et al., we also used the disappearance of the electron tem-
 647 perature anisotropy as a sign that the EDR is being crossed. The temperature anisotropy
 648 that is induced by electron trapping in a parallel electric field in the upstream region (Egedal
 649 2013) is thereby removed. For asymmetric reconnection, as we have here, Lavraud et al.
 650 (2016) explained the effect in terms of electrons being scattered in phase space while tend-
 651 ing to be isotropic near the X-line. The thicknesses of the IDR in the normal direction
 652 in the two studies are comparable ($0.4 d_i$ versus $0.55 d_i$), while the EDR thickness in our
 653 case is three times as much ($6 d_e$ versus $2 d_e$). The profiles of the parallel and perpen-
 654 dicular current densities through the IDR are similar: In the EDR, the parallel current
 655 dominates in the center and the perpendicular current densities dominate at the edges,
 656 forming a shoulder-like **profile**. Zhou et al. argue that the sudden disappearance of par-
 657 allel electrons within the EDR supports the idea that the magnetic topology there is very
 658 different from in the inflow regions. In the IDR the current density is mainly in the per-
 659 pendicular direction. The reconnection rates, normalized by the inflow magnetic field
 660 and Alfvén speed, are however very different in the two studies: **0.27 ± 0.18 (peak value)**
 661 **versus 0.077 ± 0.050 (our average value).**

662 **The observed reconnection rate is in excellent agreement with the steady-**
 663 **state rate from a 2.5-D PIC simulation, as are also the observed and simu-**
 664 **lated EDR magnetic field, electron velocity, and electron temperature anisotropy**
 665 **profiles. We conclude that the 2.5-D and steady-state approximations are ad-**
 666 **equiate for describing the observed EDR features at the time and location of**
 667 **the crossing. Of course, the reconnection rate will vary during the initial and**
 668 **final phases of a reconnection X-line, hence this caveat. Clearly, 3D struc-**
 669 **ture may be important elsewhere, such as in regions of strong electron-scale**
 670 **turbulence (typically in separatrices or dipolarization fronts, for example).**

672 **A number of interesting questions were raised by this study which we**
 673 **have not addressed. The first is that the acceleration of the current sheet re-**
 674 **sulting from the flapping could affect the reconnection dynamics. This is an**
 675 **interesting point to address in a future analysis of our simulations. The sec-**
 676 **ond is the very good agreement that exists between the simulations and the**

677 observations, despite their being of different dimensionality, as has just been
678 mentioned. This agreement seems to imply that, at least approximately, lo-
679 cal tail reconnection is not necessarily a fully three-dimensional phenomenon.
680 This was a conclusion reached also by Torbert et al. (2018) in another tail
681 reconnection event. In the interests of brevity and not to overburden the anal-
682 ysis we reserve this topic for future work.

683 Sergeev et al. (2006) carried out a statistical study of tail flapping events using Geo-
684 tail observations. Based on a superposed epoch analysis of the auroral AE index, they
685 found that the flapping motions tend to appear during the substorm expansion phase,
686 although a considerable number of events without any electrojet and auroral activity were
687 also observed (see also Runov et al., 2009). By contrast, we find the flapping here to oc-
688 cur during substorm onset.

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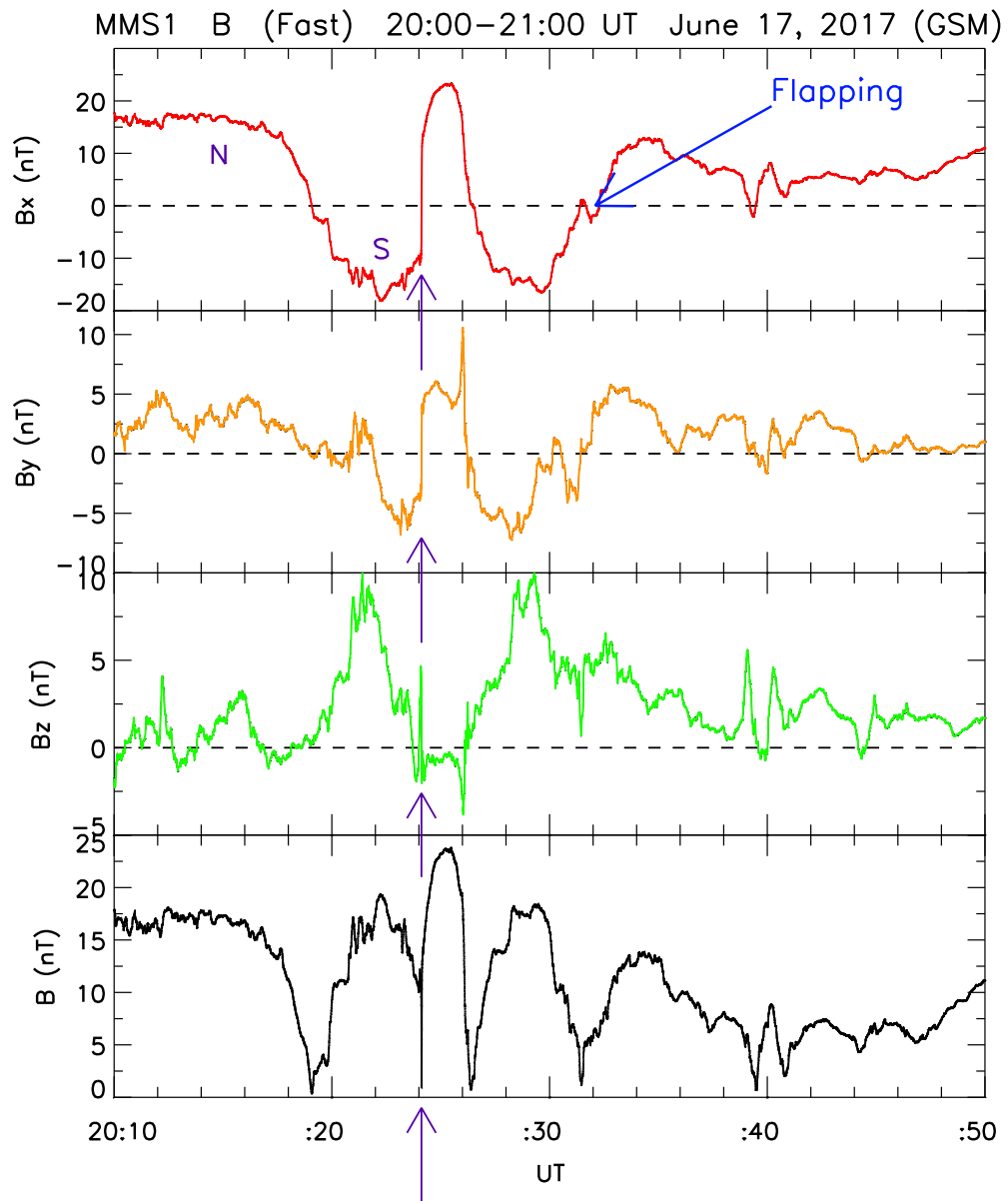
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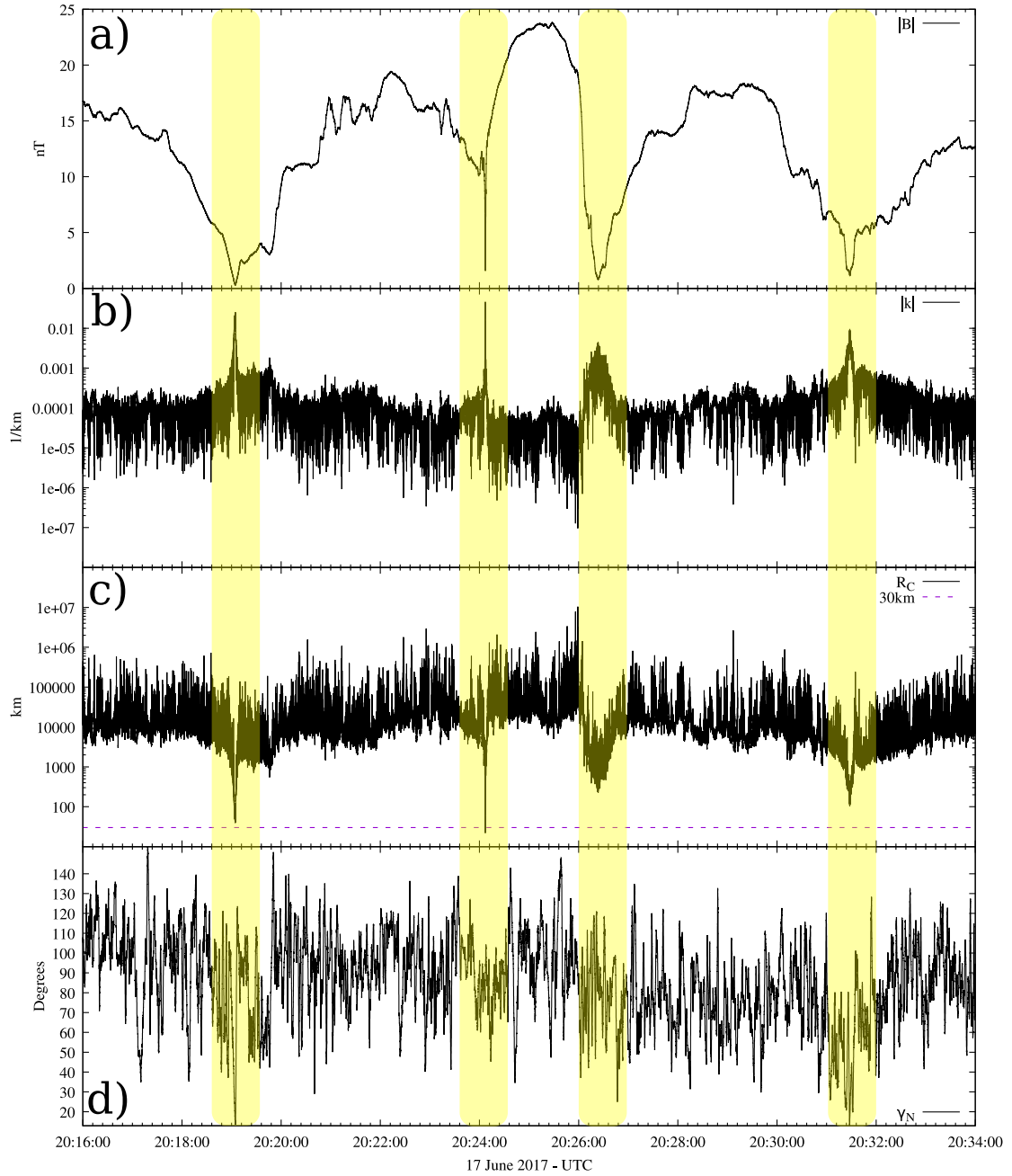
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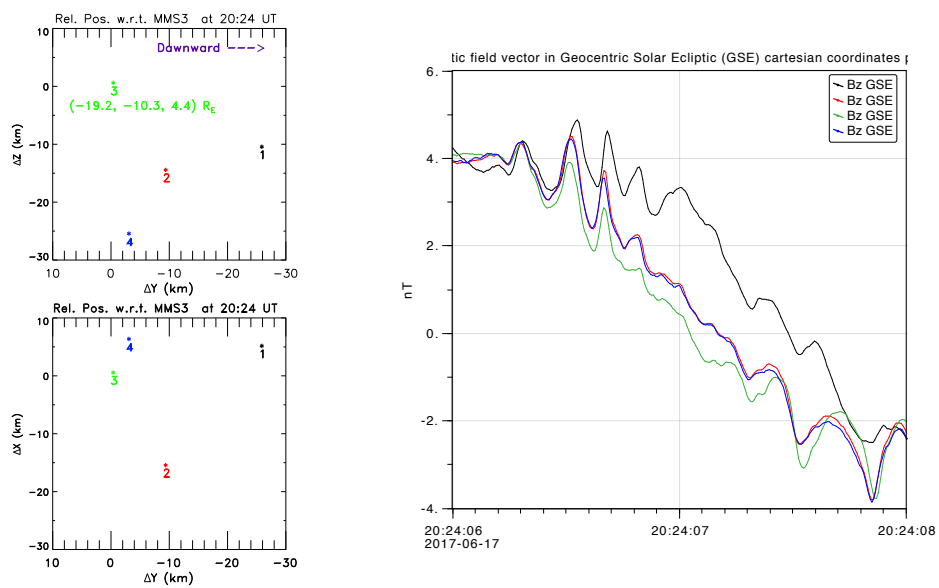
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180 **Figure 1.** Magnetic field data from MMS1 for the overview interval 20:10 to 20:50 UT. The
 181 data are in survey mode. From top to bottom: the GSM components and the total field strength.

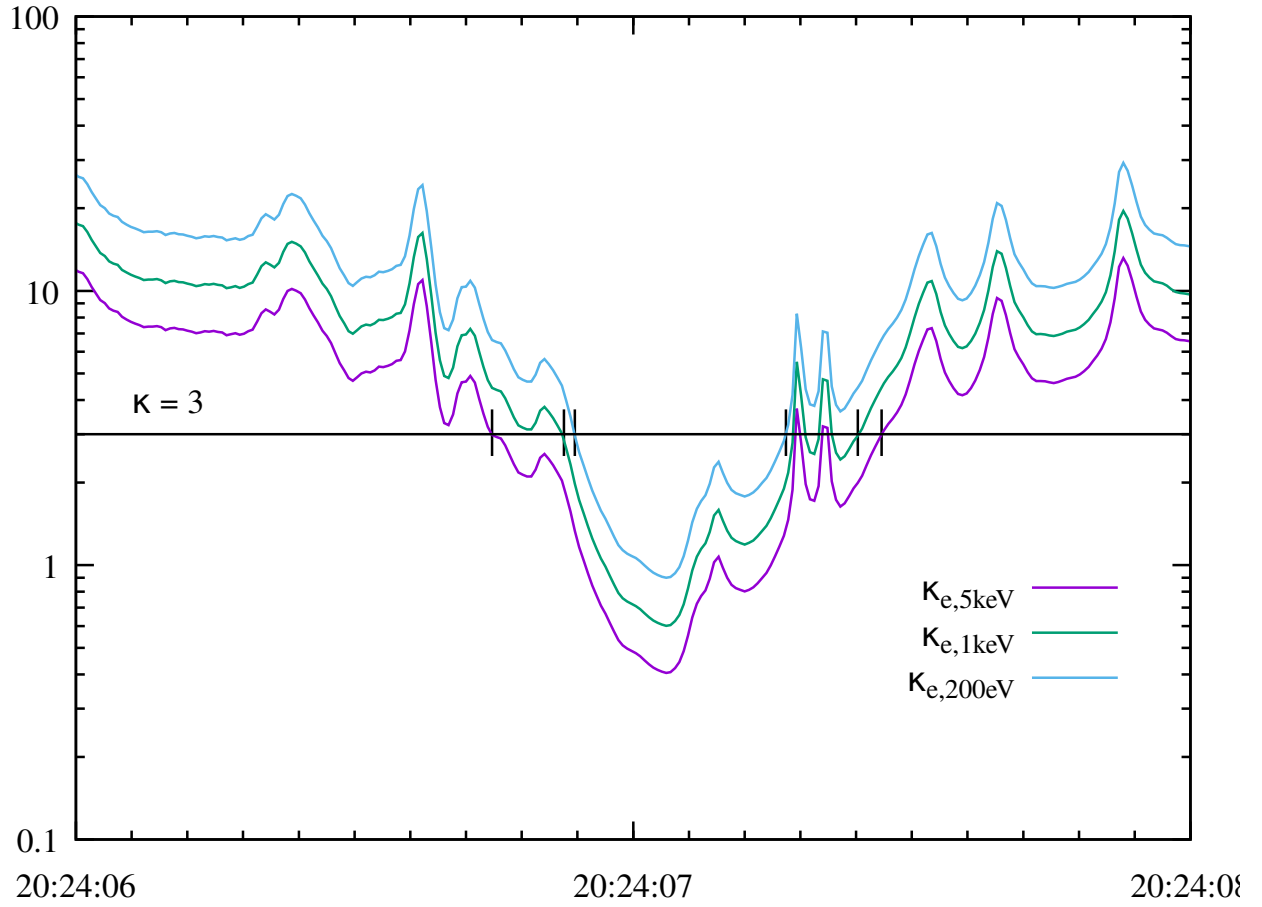


187 **Figure 2.** Magnetic Field Line (MFL) geometry parameters for the 18 minutes surrounding
 188 the EDR encounter at $\sim 20:24:07$ UT on June 17, 2017. Current sheet (CS) encounters during
 189 this period are highlighted in yellow and the magnitude of the magnetic field is provided for con-
 190 text (panel a) Parameter $|k|$ is shown in panel b and is large at each CS crossing. Panel c shows
 191 the MFL radius of curvature, where $R_C = |k|^{-1}$ with the nominal spacecraft separation of MMS
 192 during this period shown as a dashed purple line. γ_N (panel d) is the angle between the plane of
 193 MFL curvature and the current vector.

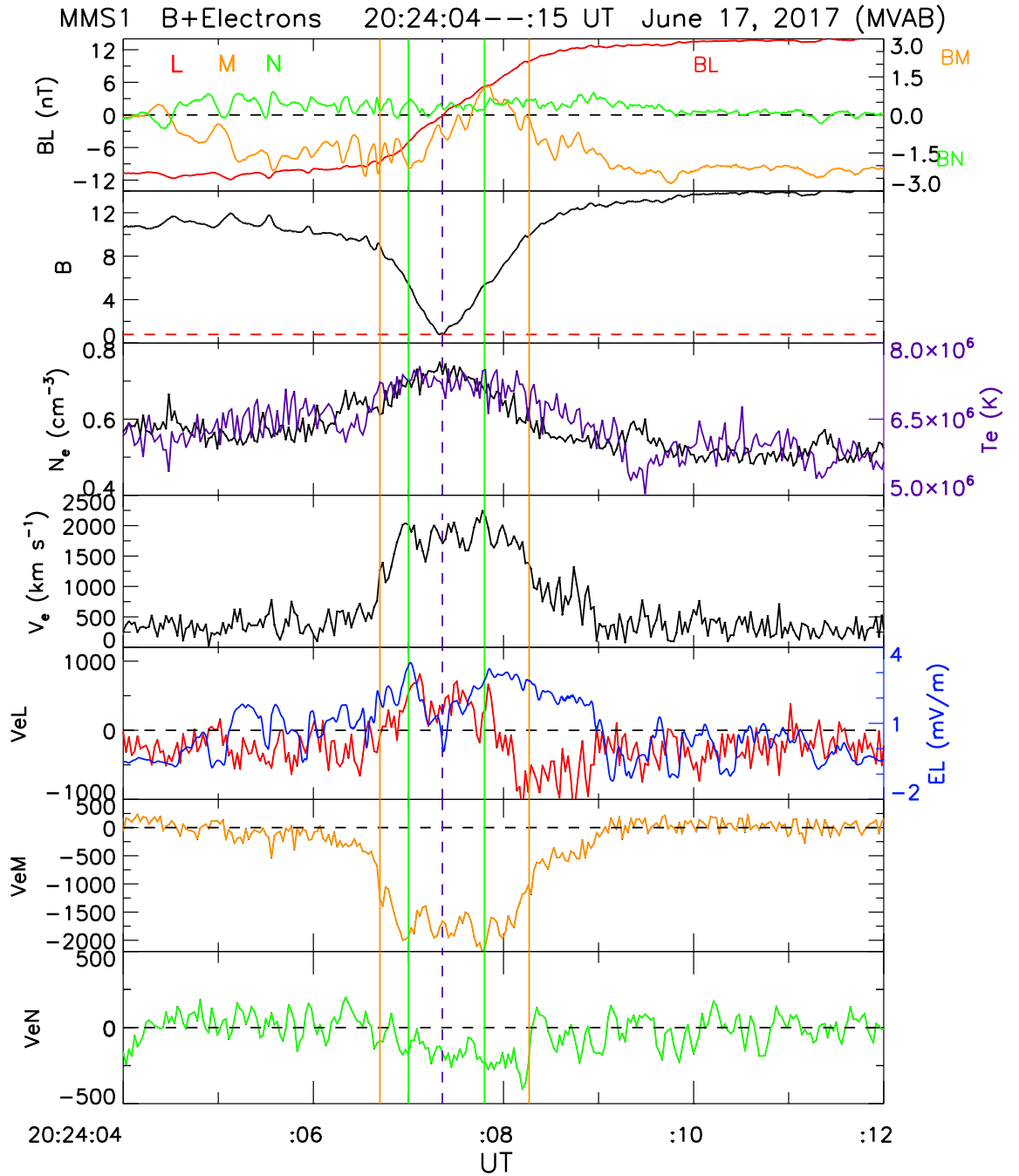


215 **Figure 3.** *Left:* The positions of the spacecraft relative to MMS3 at 20:24 UT. GSE coordi-
 216 nates are used. The YZ plane (top) and the YX plane. *Right:* Profiles of B_z (GSE) over a 2 s
 217 interval. The temporal order is MMS3 (green) to MMS2/MMS4 (red, blue) to MMS1 (black).

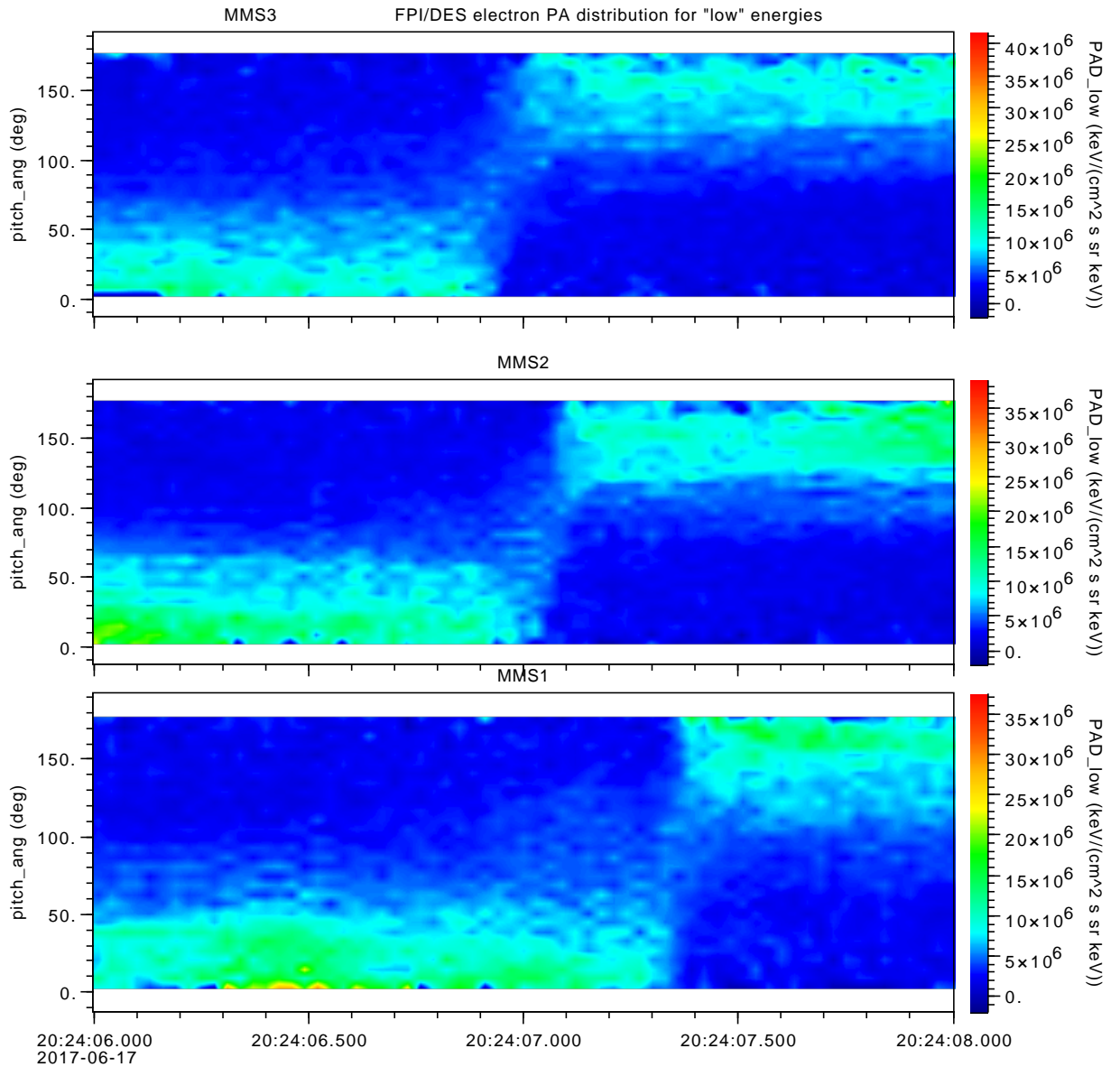
$\kappa_{\text{electrons}} = \sqrt{R_C/R_{g,e}}$ at Mesocenter
 17 June 2017 - BRST



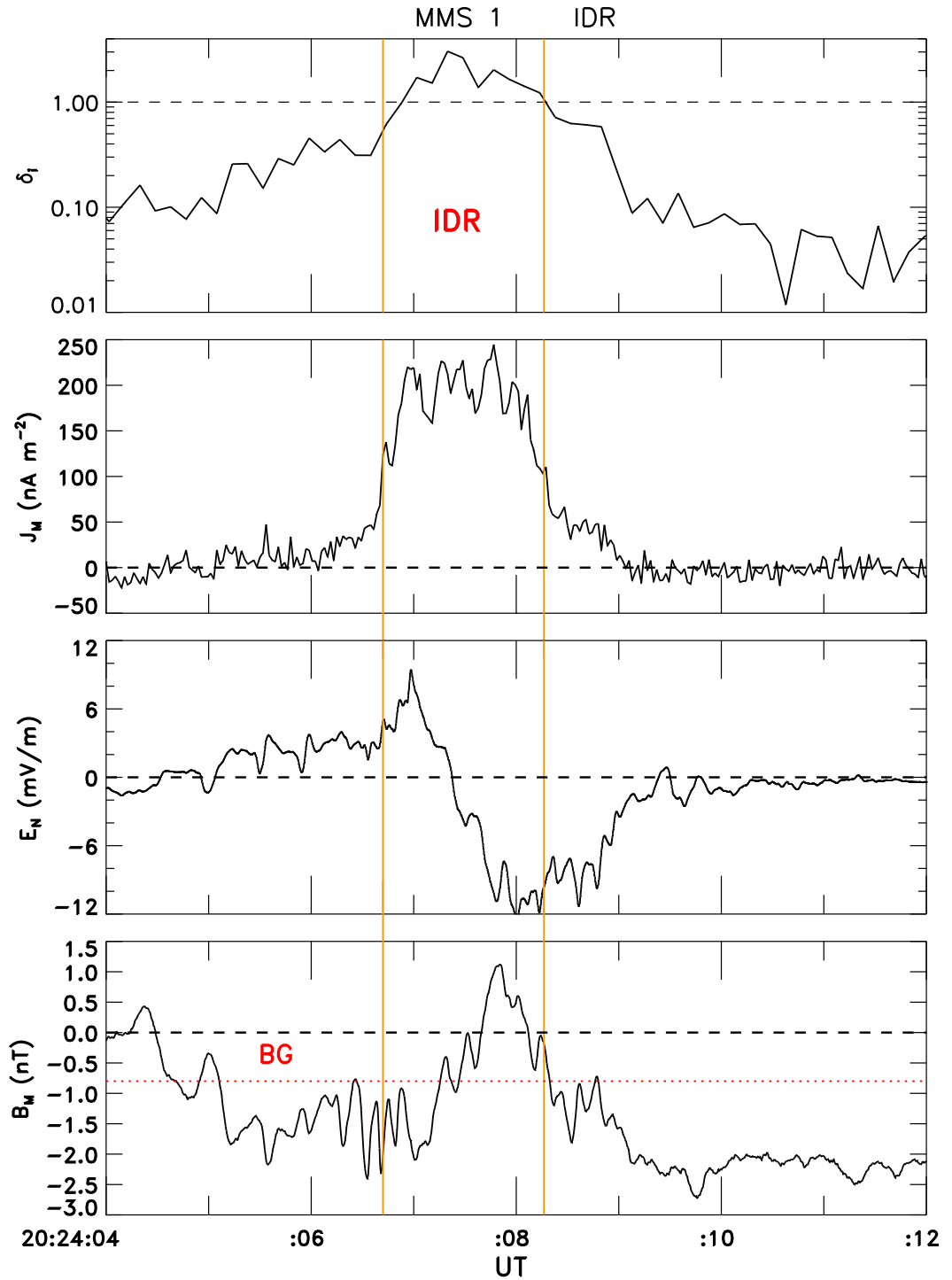
251 **Figure 4.** The curvature parameter κ , defined at the top of the figure, calculated at the
 252 mesocenter of the spacecraft configuration, for the 3 perpendicular energies of electrons shown at
 253 bottom right. For κ less than 10, chaotic behavior, and for κ less than 3 scattering, are expected.



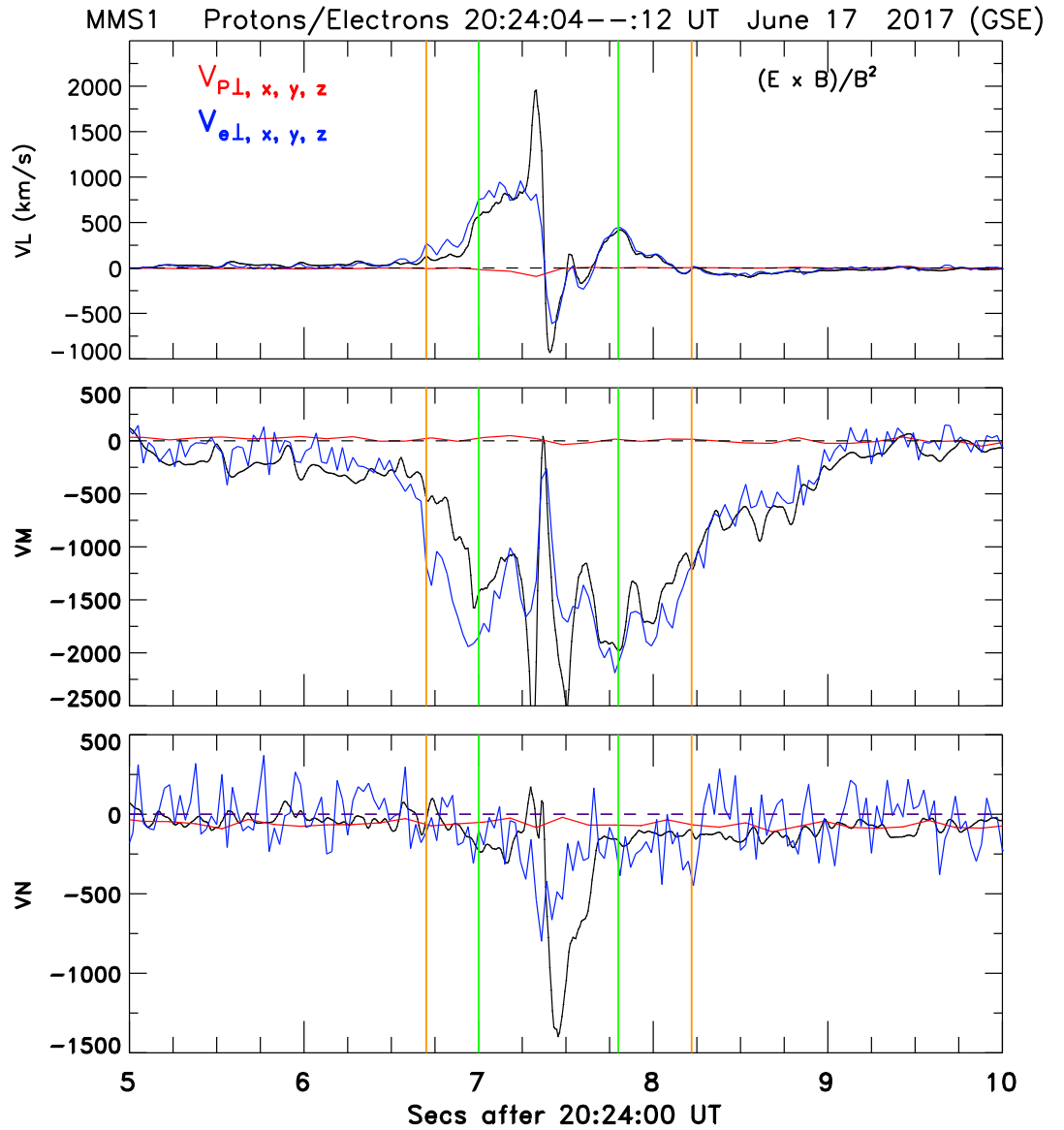
272 **Figure 5.** Electron behavior. From top to bottom: the magnetic field in *LMN* coordinates,
 273 the total field strength, the electron density and, overlaid in purple with scale on the right,
 274 the electron temperature, the bulk flow speed, and the electron velocity in *LMN* coordinates.
 275 In panel 1 the scale of B_M and B_N is shown on the right. **The dashed horizontal red line**
 276 **in panel 2 shows the size of the guide field.** In the V_{eL} panel is overlaid in blue the L-
 277 component of the level 3 electric field.



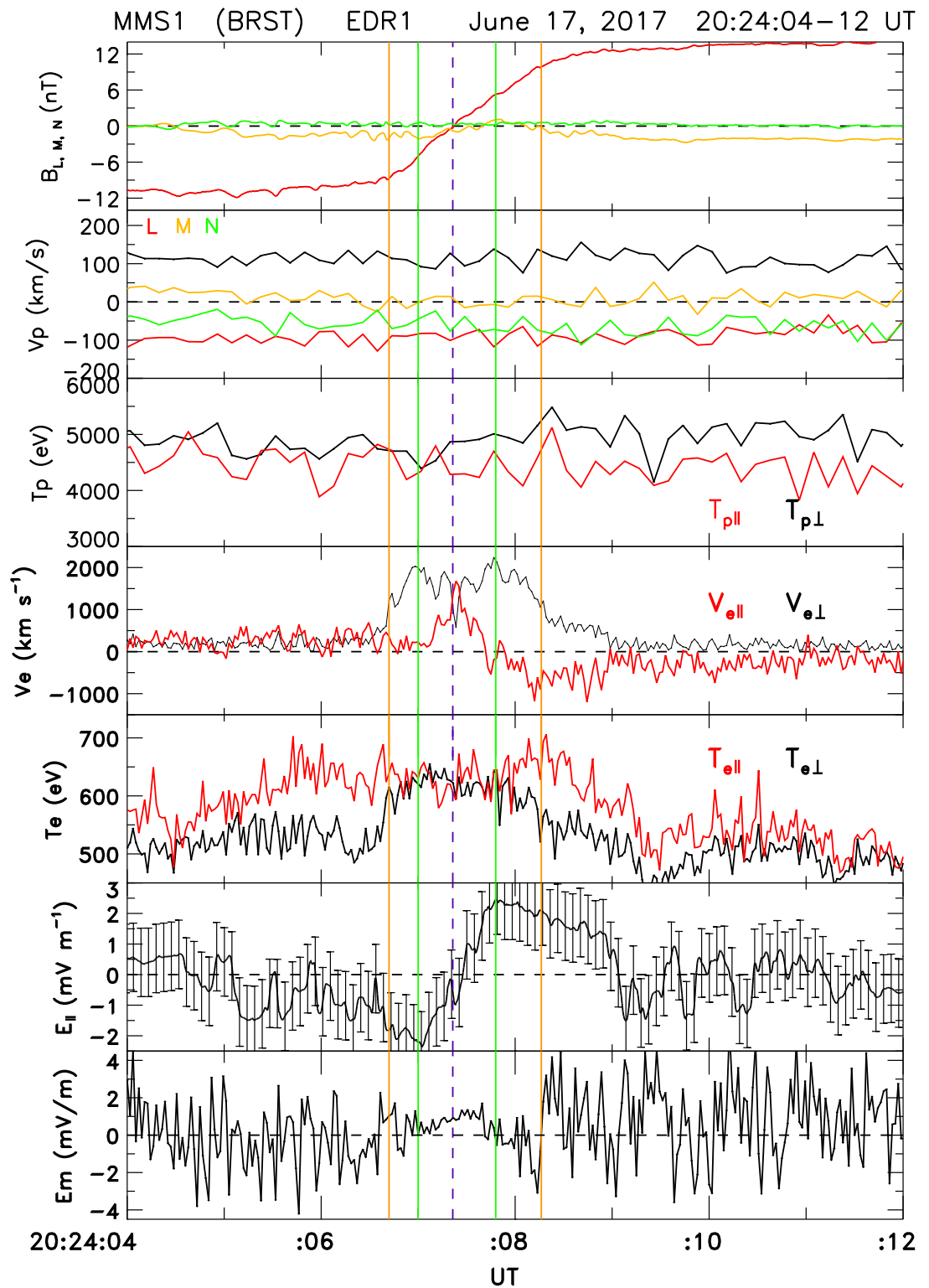
287 **Figure 6.** For a 2-s interval centered on the CS crossing, the figure shows the pitch angle
 288 distributions of electrons with energies in the range 20-200 eV for, from top to bottom, MMS3,
 289 MMS2, and MMS1.



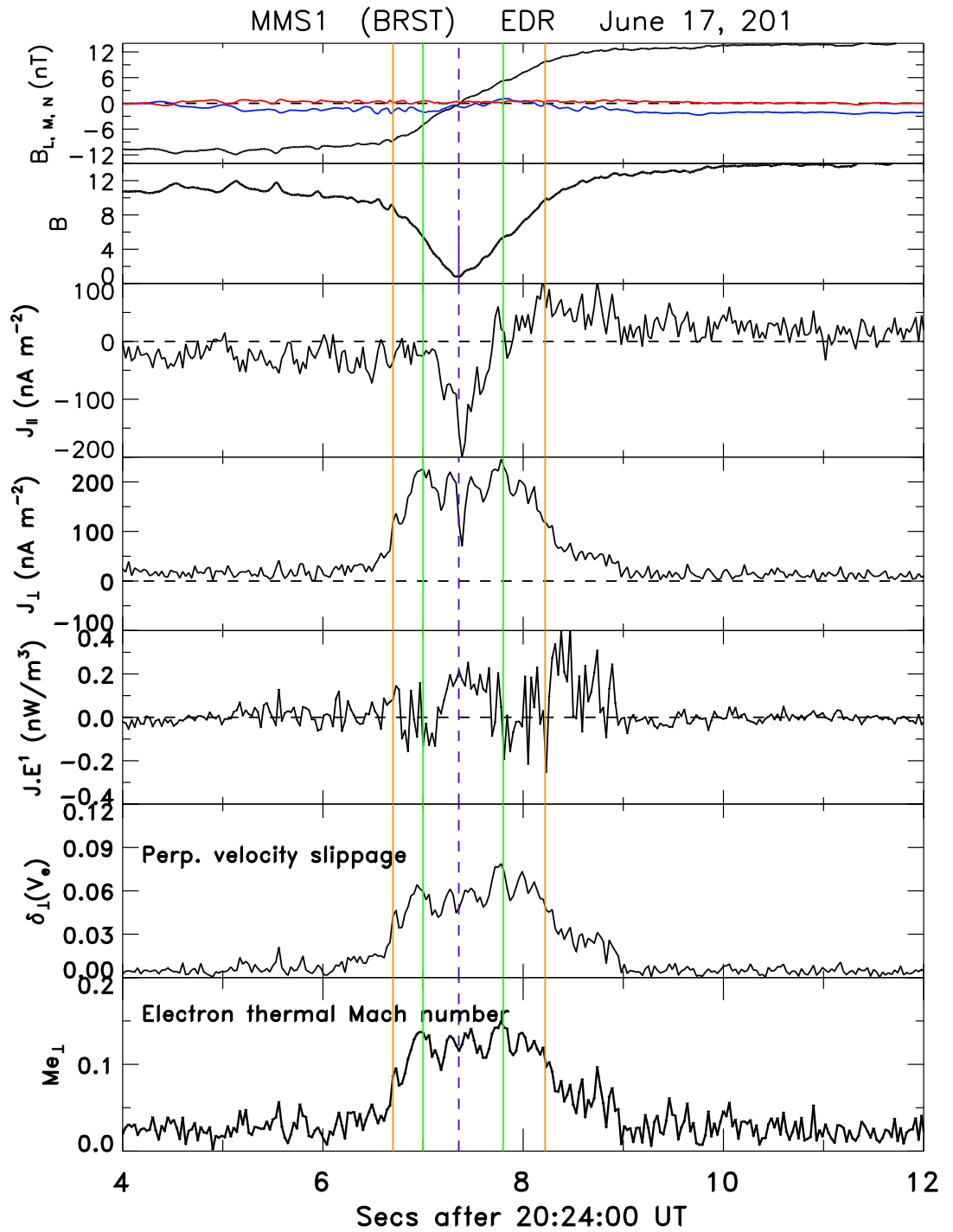
291 **Figure 7.** Physical quantities used to identify the ion diffusion region, IDR: the adiabatic
 292 expansion parameter, δ_i , the out-of-plane current density, J_M , the (Hall) electric field component
 293 normal to the CS, E_N , and the (Hall) out-of-plane magnetic field B_M . The guide field is shown
 294 by the horizontal red trace. The orange guidelines bracket the IDR.



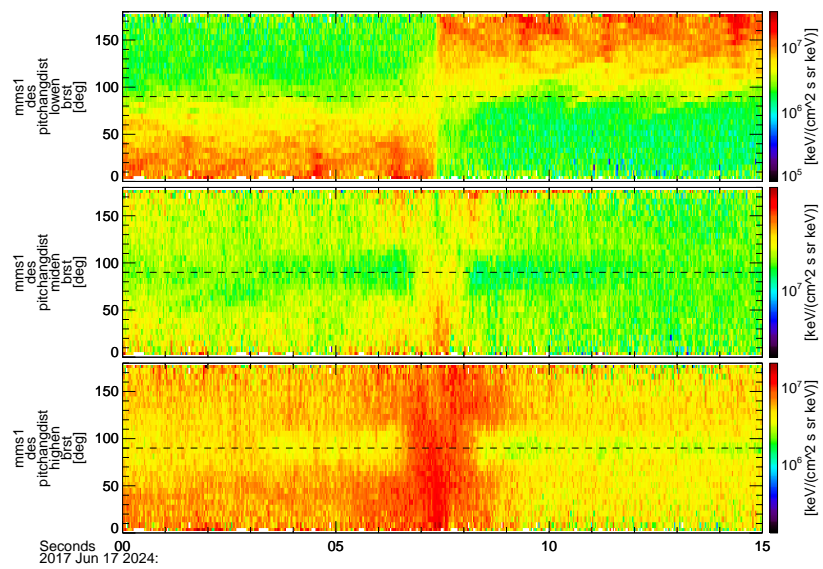
318 **Figure 8.** An overlay of the velocity of protons (red) and electrons (blue) perpen-
 319 dicular to the magnetic field and the $E \times B$ drift velocity in black. The vertical
 320 lines mark the boundaries of the IDR (magenta) and EDR (green).



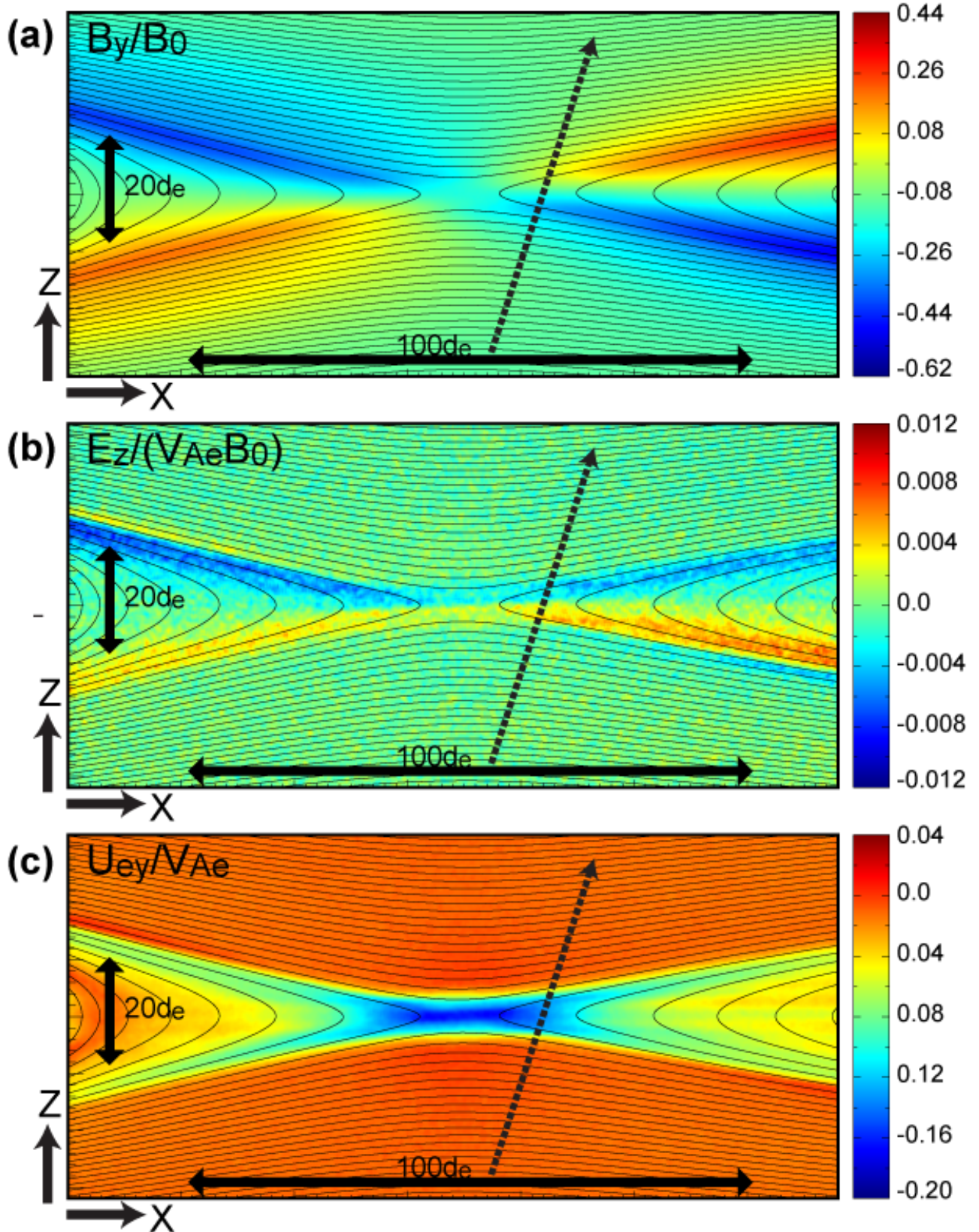
328 **Figure 9.** From top to bottom, the panels show: the components of the magnetic field in
 329 *LMN* for reference, the proton bulk velocities, the parallel (red) and perpendicular proton tem-
 330 peratures, the electron velocities parallel (red) and perpendicular to the magnetic field, the
 331 parallel (red) and perpendicular electron temperatures, the parallel electric field with error bars
 332 included, and the electric field in the out-of-plane direction, E_M .



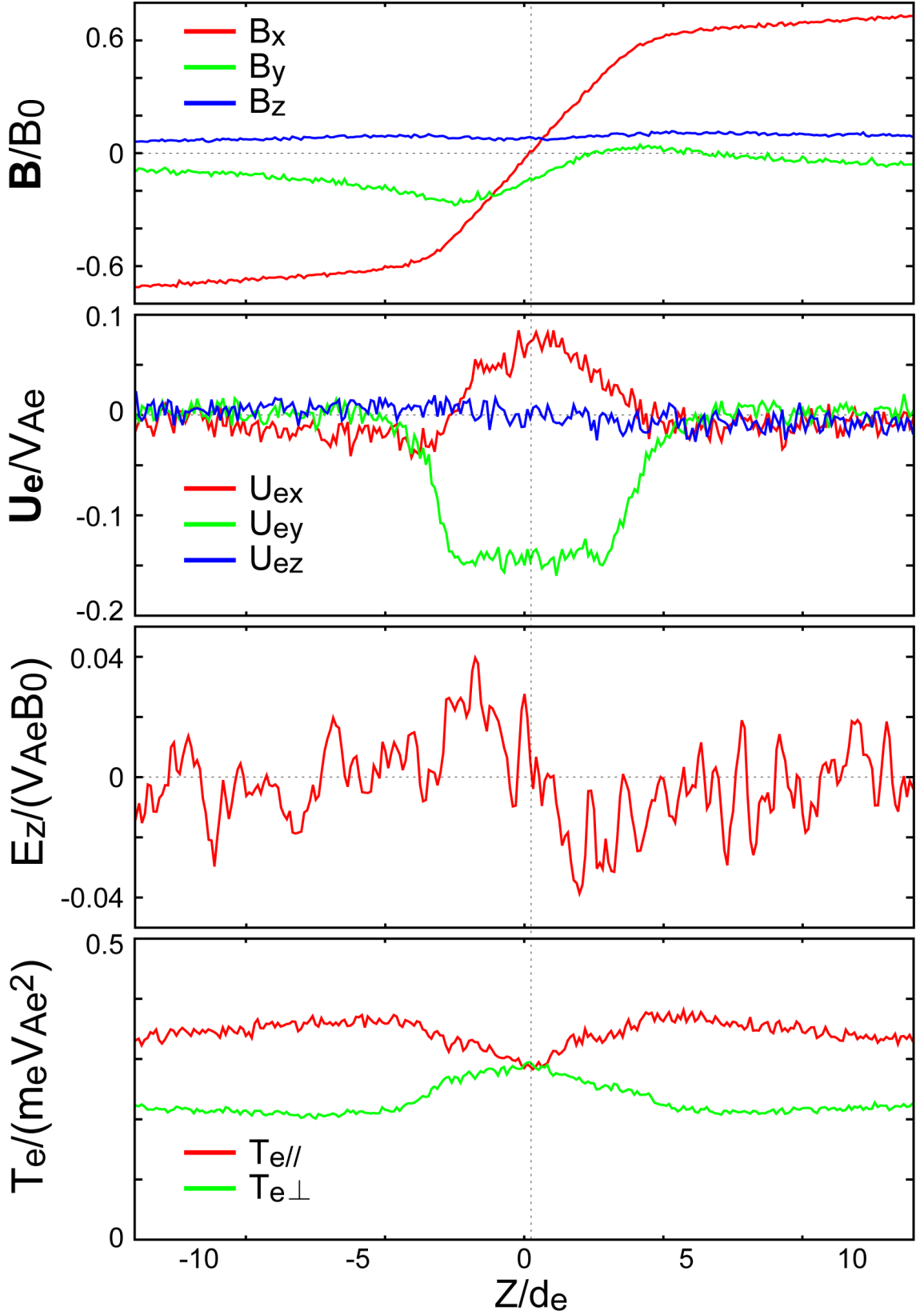
397 **Figure 10.** From top to bottom, the panels give the magnetic field components and field
 398 strength for reference, the current densities parallel and perpendicular to the magnetic field,
 399 the energy transfer term $\mathbf{J}\cdot\mathbf{E}'$, the perpendicular velocity slippage, and the electron thermal
 400 Mach number. In the first panel, the B_L , B_M , and B_N are shown by black, blue and red traces,
 401 respectively.



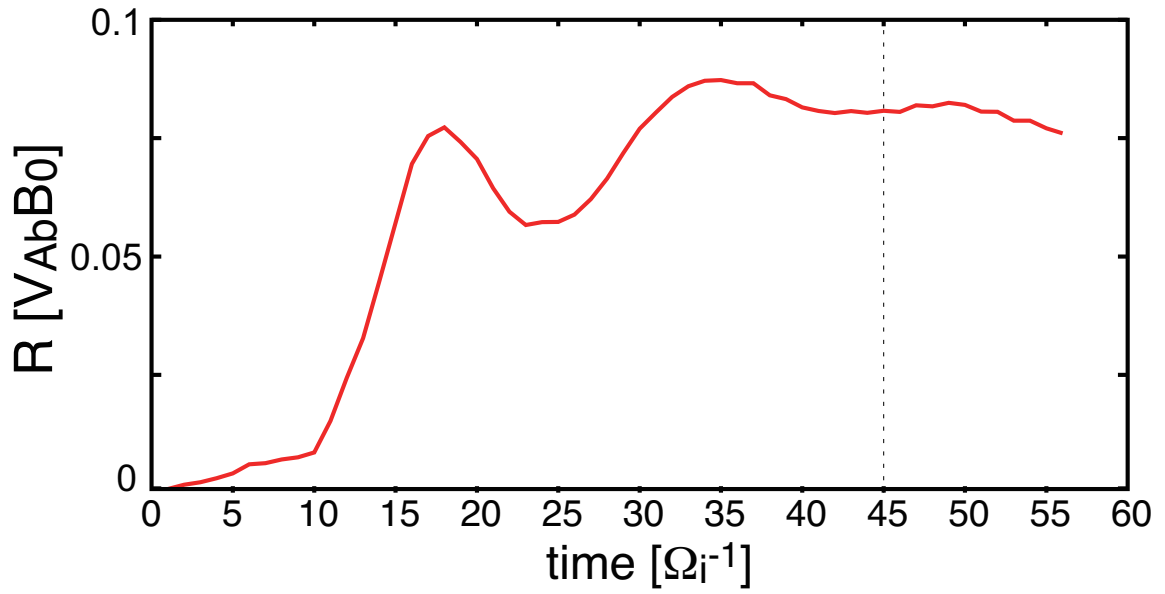
411 **Figure 11.** The PAD distribution of, from top to bottom, low (2-0.200 eV), middle and high
 412 energy electrons recorded by MMS1. Note the depletion of anti-parallel mid-energy electrons
 413 during the EDR encounter.



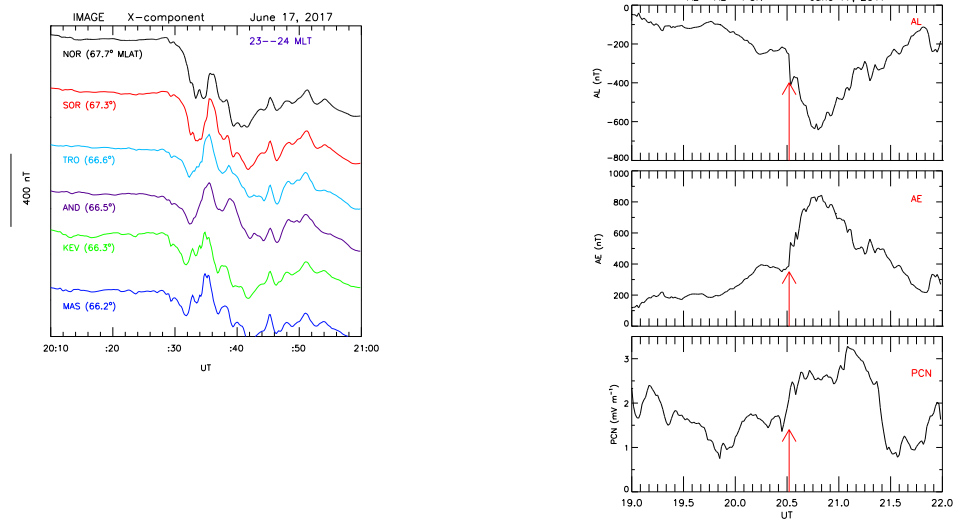
444 **Figure 12.** Zoomed-in views of 2-D contours near the IDR at $t=45 \Omega^{-1}$, at which the growth
 445 of reconnection is in an almost steady phase, of (a) B_y , (b) E_z , and (c) the electron velocity com-
 446 ponent U_{ey} , all of which are normalized by B_0 , and the electron Alfvén speed V_{Ae} based on B_0
 447 and n_0 . The black curves show the in-plane magnetic field lines. The black arrow shows a path of
 448 a virtual observation probe. See text for more details on the probe path.



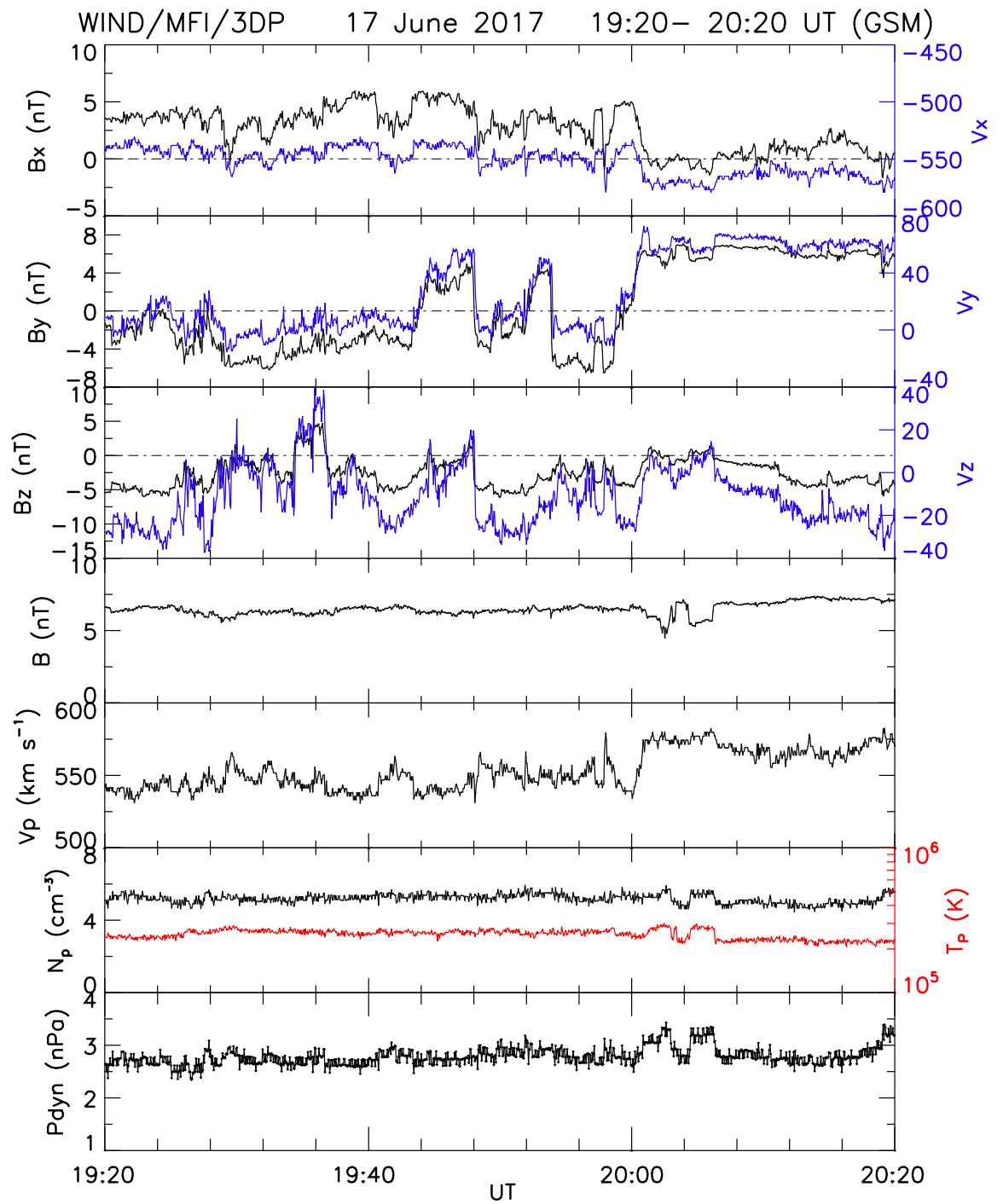
449 **Figure 13.** Virtual observations along the path shown in Fig 12 of (a) the three components
 450 of the magnetic field \mathbf{B} , (b) the three components of the electron bulk velocity U_e , (c) the z
 451 component of the electric field E_z , and (d) the parallel ($T_{e\parallel}$) and perpendicular ($T_{e\perp}$) compo-
 452 nents of the electron temperature, all of which are normalized by B_0 , V_{Ae} and m_e .



498 **Figure 14.** The evolution of the normalized reconnection rate resulting from the simulations.

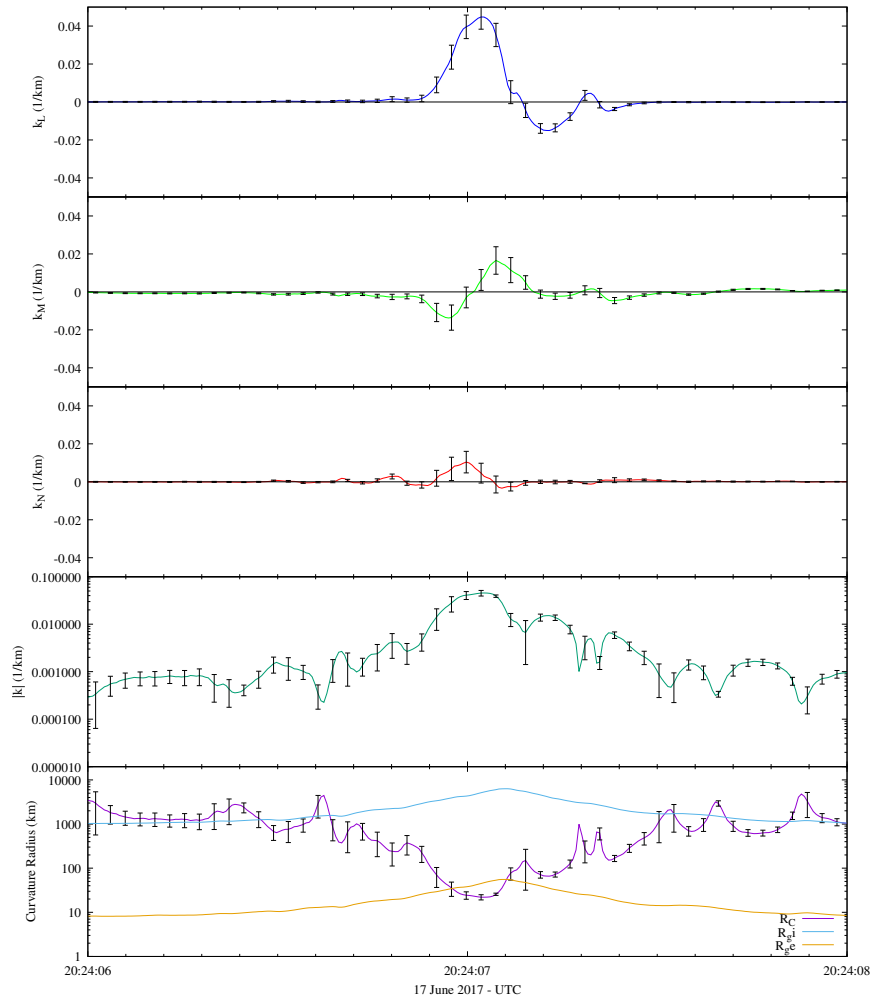


520 **Figure 15.** *a* (left): The north-south (X) component of the geomagnetic field from 6 sta-
 521 tions of the IMAGE magnetometer chain at corrected geomagnetic latitudes from 67.7 to 66°. *b*
 522 (right): For the 3-hour interval 19-22 UT, the figure shows the auroral AL and AE indices and
 523 the polar cap north index. The time of substorm onset is indicated by the red arrow.



525 **Figure 16.** *Wind* data for a 1-hr interval. From top to bottom, the magnetic field (black) and
 526 flow (blue) components, the total field, bulk flow, density and temperature (red) and the dynamic
 527 pressure.

Curvature with error
(With proper positional and magnetic error)



574 **Figure 17.** The components of the magnetic field line (MFL) curvature vector in LMN co-
 575 ordinates, its total value, and the radius of curvature of the MFL, all including uncertainty.
 576 Overlaid in the bottom panel are the gyroradii of ions (blue) and electrons (magenta) at their
 577 thermal mean energies.