

1 **Radar-sounding characterization of the subglacial**
2 **groundwater table beneath Hiawatha Glacier,**
3 **Greenland**

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11 **Key Points:**

- 12 • Radiometric and hydrologic analysis of radar-sounding data is consistent with a
13 reflection from a subglacial groundwater table
- 14 • Dual radiometric constraints indicate a layer of either debris-laden ice or fractured
15 bedrock above the subglacial groundwater table
- 16 • This first detection of a subglacial groundwater table was enabled by favorable lo-
17 cal geology, thin ice and the wide bandwidth radar system

Abstract

Radar-sounding surveys associated with the discovery of a large impact crater beneath Hiawatha Glacier, Greenland, revealed bright, flat subglacial reflections hypothesized to originate from a subglacial groundwater table. We test this hypothesis using radiometric and hydrologic analysis of those radar data. The dielectric loss between the reflection from the top of the basal layer and subglacial reflection and their reflectivity difference represent dual constraints upon the complex permittivity of the basal material. Either ice-cemented debris or fractured, well-drained bedrock explain the basal layer's radiometric properties. The subglacial reflector's geometry is parallel to isopotential hydraulic head contours, located 7.5–15.3 m below the interface, and 11 ± 7 dB brighter than the ice–basal layer reflection. We conclude that this subglacial reflection is a groundwater table and that its detection was enabled by the wide bandwidth of the radar system and unusual geologic setting, suggesting a path for future direct radar detection of subglacial groundwater elsewhere.

Plain Language Summary

Recent radar-sounding of the Hiawatha Glacier, which overlies a large impact crater, also found an unusually flat, bright surface about ten meters beneath the bottom of the ice. This surface was suspected to be the groundwater table, which has never been directly detected beneath an ice sheet, but it was not studied in detail. We used two three-layer geologic models to test this hypothesis using the strength of the radar returns. We found that the layer between the ice bottom and this lower surface is likely either debris-laden ice or fractured, well-drained bedrock. This surface's shape and brightness is also consistent with a groundwater table, because it follows expected patterns of water pressure. Our results confirm the detection of a groundwater table beneath Hiawatha Glacier and show the potential for future radar surveys to further probe subglacial groundwater systems.

1 Introduction

Recent airborne radar-sounding surveys revealed a 31-km-wide impact crater beneath Hiawatha Glacier, part of the northwestern Greenland Ice Sheet (Kjær et al., 2018). These radar data were collected with a new ultrawideband (UWB) radar sounder that revealed the glacier's bed topography and internal structure in unprecedented detail (Wang et al., 2016; Yan et al., 2017). Within these data, Kjær et al. (2018) also identified a distinct reflection *beneath* the ice–bed interface that was unusually flat and specular, which they hypothesized to be the groundwater table. However, this observation has yet to be confirmed by radiometric or hydrologic analyses, and the intervening material sandwiched between the glacier and this reflection was not characterized.

The unique geologic setting of a subglacial complex impact crater could be partly responsible for this reflection. While the deglaciated region immediately adjacent to Hiawatha Glacier (Inglefield Land) is composed of highly metamorphosed Paleoproterozoic rock (Kjær et al., 2018), unconsolidated impact breccias are expected to be widespread within the crater floor surrounding the central uplift (Osinski & Pierazzo, 2013). Debris-rich ice is observed outcropping along the base of ice cliffs along the western margin of Hiawatha Glacier, and Kjær et al. (2018) hypothesized that basal material is being actively entrained within Hiawatha Glacier, based on the UWB radar sounding data. A possible second large subglacial impact crater has also been identified in Greenland (MacGregor et al., 2019), but no comparable subglacial reflection was reported there, although the ice is thicker and that structure is likely older.

65 Radar sounders are widely deployed to study subglacial and englacial water bod-
66 ies (e.g., Wright & Siegert, 2012; Chu et al., 2018; Oswald et al., 2018; Jordan et al., 2018;
67 Kendrick et al., 2018). This method often succeeds because the complex permittivity con-
68 trast between ice and water is large and because such bodies are often specular reflect-
69 tors (e.g., Schroeder et al., 2015). Subglacial lakes are now regularly found beneath the
70 Antarctica and Greenland ice sheets and inform our understanding of their subglacial
71 hydrology (Wright & Siegert, 2012; Livingstone et al., 2019). Groundwater sources are
72 an important component of glacier hydrology; they can drive water into till, elevate pore-
73 water pressures, reduce shear strength and significantly influence ice-sheet dynamics (Boulton
74 et al., 1995; Gooch et al., 2016; Key & Siegfried, 2017; Siegert et al., 2018). Relatively
75 few studies have reported detecting the subglacial groundwater table (modeling: Christof-
76 fersen et al., 2014; airborne transient electromagnetics: Mikucki et al., 2015) despite ground-
77 penetrating radar surveys being well-established as a method for identifying groundwa-
78 ter in deglaciated environments (e.g., A. Neal, 2004; Woodward & Burke, 2007).

79 Radar-sounder designs range from ground-based impulse and frequency-modulated
80 continuous-wave systems to multi-channel chirped airborne systems (Li et al., 2019). The
81 UWB chirped radar system developed by the Center for Remote Sensing Ice Sheets and
82 deployed by Kjær et al. (2018) is a relatively new version of the Multi-channel Coher-
83 ent Radar Sounder (MCoRDS v5), characterized by a much larger bandwidth than pre-
84 vious versions, weaker sidelobes and a higher signal-to-noise ratio (SNR) (Rodríguez-Morales
85 et al., 2013; Wang et al., 2016). The technical advances of MCoRDS v5 raise the pos-
86 sibility that its capabilities alone are what enabled the detection of the hypothesized sub-
87 glacial groundwater table.

88 A reflection from a subglacial groundwater table ought to possess a radiometric sig-
89 nature distinct from off-nadir bed reflections, because the dielectric contrast that induces
90 the reflection should be due to the contrast between unsaturated and saturated sediment,
91 rather than between ice and more typical subglacial interfaces (marine sediment or bedrock).
92 This reflection’s subglacial depth should also be consistent with the predicted hydrolog-
93 y of groundwater flow through such systems. If the interface is indeed a water table,
94 then it should be conformal to isopotential contours of hydraulic head (Wright et al., 2008;
95 Flowers, 2015; Rutishauser et al., 2018). Here we test the hypothesis that the subglacial
96 reflection at Hiawatha Glacier is indeed that of a groundwater table using both radio-
97 metric and hydrologic analyses. These tests inform an assessment of the cause of this
98 reflection, prospects of its detectability elsewhere and provide a framework for future in-
99 vestigations of subglacial groundwater systems beneath glaciers and ice sheets.

100 2 Data and methods

101 The MCoRDS v5 data used in this study were collected in May 2016 (Kjær et al.,
102 2018). The radar system is described in detail by Wang et al. (2016) and consists of three
103 eight-element arrays, operating between 150–520 MHz at a 10-kHz pulse repetition fre-
104 quency. These arrays were mounted on the Alfred Wegener Institute’s Polar 6, a Basler
105 BT-67 aircraft. After pulse compression and synthetic aperture processing, the data have
106 a vertical (range) resolution of 0.5 m and an along-track (azimuth) resolution of 15 m.
107 Figure 1 shows the four flight tracks and radargrams from this survey where the puta-
108 tive groundwater table was detected. The peak power of the putative groundwater-table
109 reflection was extracted using a local depth window that was selected manually to bound
110 this reflection. This depth window was also used to re-track some regions where the orig-
111 inal ice–basal layer peak power picks corresponded with the hypothesized groundwater
112 table.

2.1 Radiometric analysis

Our radiometric analysis aims to test whether the received power from the ice–basal layer and hypothesized basal layer–groundwater interface, along with the dielectric loss within the intervening basal layer, are consistent with a subglacial groundwater table. We assume that this system can be represented by a three-layer dielectric model, where the relative complex permittivity, $\tilde{\epsilon} = \epsilon' - j\epsilon''$ is uniform within each layer, where $j^2 = -1$ and $\tan \delta = \epsilon''/\epsilon'$ is the loss tangent (dielectric loss). Two different models for the basal layer are explored in parallel, and in each case the basal layer is described by a three-component mixture. We show below that the combination of reflectivity difference between the ice–basal layer and subglacial reflections and $\tan \delta$ within the basal layer provide dual constraints upon $\tilde{\epsilon}_b$.

For our first model, the top layer is polar ice with an assumed permittivity $\tilde{\epsilon}_{ice} = 3.15(1 - j0.0062)$ expressed in the form $\tilde{\epsilon} = \epsilon'(1 - j \tan \delta)$ (Fujita et al., 2000; Peters et al., 2005). The middle layer sandwiched between the ice–basal layer interface and the putative groundwater table has an unknown permittivity $\tilde{\epsilon}_b$ and is assumed to be a mixture of granitic sand, groundwater-saturated till and ice (with initially unknown volume fractions). The bottom layer (groundwater table) is modeled using the dielectric properties of thawed, groundwater-saturated granitic till $\tilde{\epsilon}_{gwt} = 25(1 - j0.0118)$ (Christianson et al., 2016). These assumed layer compositions were selected *a posteriori* by testing a range of plausible subglacial permittivity values to maximize overlap between the dual constraints. We note that the dielectric contrast between the middle layer and the putative groundwater table is so great that our conclusions are not significantly affected by the plausible range of permittivity values for the middle layer.

The second model again includes a top layer of polar ice $\tilde{\epsilon}_{ice}$ and an unknown middle layer, but differs in assuming the bottom layer is a groundwater aquifer in porous or fractured granitic rock (rather than an unsorted till) with higher water content and thus higher permittivity ($\tilde{\epsilon}_{gw}$). In this case, the middle basal layer is assumed to be a mixture of fractured bedrock, water and air (rather than ice).

These two distinct models effectively test whether detection of the subglacial reflection is due to a thermal transition from frozen to thawed material (model 1), or due to a hydraulic transition from drained to saturated bedrock (model 2). Only their differences in the assumed composition of the bottom layer affect the resulting mixture ratios for the sandwiched basal layer. We consider these two cases to be the most plausible, with the primary goal of testing for the existence of the groundwater table rather than robustly identifying nature of the middle layer. For simplicity, the following sections use equations with subscripts and descriptions for model 1 only, but the analysis for model 2 is the same except using groundwater *gw* instead of groundwater-saturated till *gwt*.

The difference in received power between the basal layer–groundwater till (*b-gwt*) and the ice–basal layer (*ice-b*) reflectors is given by

$$\Delta[P] = \Delta[R] - [L_b], \quad (1)$$

where $\Delta[P] = [P_{b-gwt}] - [P_{ice-b}]$, $\Delta[R] = [R_{b-gwt}] - [R_{ice-b}]$ is the reflectivity difference between the basal layer–groundwater and the ice–basal layer reflections, $[L_b]$ is the dielectric attenuation within the basal layer material, and the notation $[X] = 10 \log_{10} X$ is used for power in decibels. For this relation, birefringence loss and the radar system performance cancel out (Fujita et al., 2006; Matsuoka et al., 2012; Haynes, 2020). VHF birefringence within subglacial materials has not been reported so we neglect this possible confounding factor (Jordan et al., 2020). Given the small traveltime differences and plausible range of permittivities, suggesting a basal layer ~ 10 m thick, the difference in geometric spreading loss between the ice–basal layer interface and groundwater interface is negligible and also ignored. To assess the potential effect of interface roughness

161 upon reflection scattering loss and how it might impact interpretation of $\Delta[R]$, we com-
 162 pared the spread of the reflectivity distributions for the ice-basal layer interface and the
 163 basal layer-groundwater interface (see supplement) (Jordan et al., 2018; Grima et al.,
 164 2019).

165 Spatial variation in the thickness of the basal layer between the ice-basal layer in-
 166 terface and the putative groundwater table can be further exploited to estimate the mean
 167 dielectric attenuation rate within this layer (Campbell et al., 2008). This regression as-
 168 sumes that (linear) power decays exponentially with travel time t (equivalent to layer
 169 thickness for uniform ϵ'_b), resulting in a linear relationship between $\Delta[P]$ and t . This method
 170 also assumes that $\tan \delta_b$ is uniform, that volume scattering within the layer is negligi-
 171 ble, and that roughness-induced scattering losses and $[R_{b-gwt}]$ are uncorrelated with t .
 172 By neglecting volume scattering within this middle layer, our estimate of water content
 173 in the basal layer is a conservative upper bound. $[L_b]$ is obtained for each along-track
 174 sample using the regression slope $(-\Delta[P]/\Delta t)$ and $\Delta[R]$ is obtained using Eq. (1). The
 175 loss tangent of the sandwiched basal layer is thus

$$\tan \delta_b = \sqrt{\left\{ 2 \left(\frac{\lambda}{40\pi c \log_{10}(e)} \frac{\Delta[P]}{\Delta t} \right)^2 + 1 \right\}^2} - 1, \quad (2)$$

176 where λ is the radar wavelength in the vacuum (0.9 m), c is its speed in the vac-
 177 uum and Δt is the two-way travel time (Campbell et al., 2008). This approach differs
 178 from the typical procedure to estimate englacial attenuation rates, where power is re-
 179 gressed against ice thickness for an assumed value of ϵ'_{ice} (Jacobel et al., 2009). The ra-
 180 tionale for our approach, which was originally applied to the subsurface of Mars (Campbell
 181 et al., 2008), is that we cannot assume a value for ϵ'_b *a priori*.

182 The derived values of $\Delta[R]$ and $\tan \delta_b$ provide two independent constraints upon
 183 $\tilde{\epsilon}_b$ and hence its composition. To relate these constraints to $\tilde{\epsilon}_b$, we consider a three-component
 184 mixture of granite(considering a range of granitic sand to rock permittivities), ice, and
 185 groundwater-saturated till using a power-law mixing model of the form

$$\tilde{\epsilon}_b^{\frac{1}{\gamma}} = \phi_{gran} \tilde{\epsilon}_{gran}^{\frac{1}{\gamma}} + \phi_{ice} \tilde{\epsilon}_{ice}^{\frac{1}{\gamma}} + \phi_{gwt} \tilde{\epsilon}_{gwt}^{\frac{1}{\gamma}}, \quad (3)$$

186 where $\tilde{\epsilon}_{gran}$ is the complex permittivity of granite and ϕ_{gran} , ϕ_{ice} , ϕ_{gwt} are the fractional
 187 volumes of granite, ice and groundwater-saturated till, respectively (Wilhelms, 2005; Nerozzi
 188 & Holt, 2019). We assume $\gamma=3$ following Looyenga (1965) and a range of values for $\tilde{\epsilon}_{gran}$
 189 between $5(1-j6.8 \times 10^{-5})$ and $9(1-j0.068)$, with a mean value of $7(1-j0.034)$. These
 190 values were determined by converting electrical conductivity σ values for granite from
 191 between $10^{-5} - 10^{-2} \text{ S m}^{-1}$ (Bogorodsky et al., 1985) and considering a real permit-
 192 tivity range of 5 to 9 (Martinez & Barnes, 2001; Nerozzi & Holt, 2019), i.e. $\tilde{\epsilon}_{gran} = \sigma_{gran}/(2\pi f \epsilon'_{gran} \epsilon_0)$
 193 where f is the radar center frequency (335 MHz), ϵ_0 is the permittivity of the vacuum
 194 and $\epsilon'_{gran} = 5$ to 9. Expected values of $\Delta[R]$ and $\tan \delta_b$ were modeled using Eq. (3),
 195 assuming a specular Fresnel reflection for $\Delta[R]$, and evaluated for all possible fractional
 196 combinations of ϕ_{gran} , ϕ_{ice} and ϕ_{gwt} to produce a ternary diagram for each constraint.

197 2.2 Hydraulic analysis

198 Hydraulic head is a measure of liquid potential and its spatial pattern determines
 199 where groundwater flows (Freeze & Cherry, 1979). Here, we apply a traditional Darcian
 200 approach of evaluating the aquifers. We assume flow in one direction and a homogeneous
 201 aquifer in both models. For model 1, the total potential at the potentiometric surface
 202 (the elevation of the water table) is evaluated assuming the groundwater till aquifer is
 203 confined and partially driven by pressure from the top and middle layers (frozen basal
 204 layer and the overlying ice sheet). Model 2 considers flow through fractures dominated

205 by gravity. While flow through such fractures is not well described by a simple Darcian
 206 model, for our purposes these simple hydraulic models enable the examination of the range
 207 of depths and shapes of the groundwater potential compared to the groundwater echo,
 208 rather than robustly modeling or supporting either of the two hydraulic scenarios.

209 To determine isopotential contours of hydraulic equilibrium, we calculate the hy-
 210 draulic head as a function of elevation head and pressure head (neglecting velocity head)
 211 as

$$\Phi_1 = \rho_{gwt}gz_{gwt} + \rho_{ice}g(z_{surface} - z_b) + \rho_b g(z_b - z_{gwt}), \quad (4)$$

$$\Phi_2 = \rho_{gw}gz_{gw}, \quad (5)$$

212 where z is elevation, ρ is density and g is the acceleration due to Earth’s gravity
 213 (Shreve, 1972; Rutishauser et al., 2018). Because the basal layer is thin (~ 10 m), un-
 214 certainty in the density of the basal layer does not significantly affect the hydraulic head
 215 calculation and is neglected. We assume the basal layer density is comparable to gran-
 216 ite ($\rho_b = 2700 \text{ kg m}^{-3}$) used in prior studies of northwest Greenland and note that granitic
 217 sand at lower densities would produce similar results (Corbett et al., 2015; Vermassen
 218 et al., 2019). The density of groundwater-saturated till (ρ_{gwt}) and groundwater (ρ_{gw})
 219 are both assumed to be 997 kg m^{-3} assuming the till will not flow (see supplement). To
 220 bound these two end members, both possibilities are shown in Figure 2.

221 2.3 Radar system analysis

222 We evaluate the performance parameters of MCoRDS v5 against those of other com-
 223 monly deployed radar sounders to address whether MCoRDS v5 itself is responsible for
 224 the detection of a subglacial reflection. The characteristic bandwidths, center frequency,
 225 pulse length and windowing techniques are incorporated to generate and compare the
 226 sidelobe patterns of HiCARS (Peters et al., 2007), MCoRDS v3 (Shi et al., 2010) and
 227 MCoRDS v5 (see Table S1 for radar-system parameters used). This comparison tests
 228 whether the observed subglacial reflections are likely to be “visible”, or stronger than
 229 the sidelobes from basal layer echoes.

230 3 Results

231 For our radiometric analysis, the four profiles where the subglacial reflection was
 232 detected were initially analyzed separately (Fig. 1). Best-fit loss tangents range between
 233 0.0102 to 0.0128 (Fig. 2). The reflectivity difference between the ice–basal layer and basal
 234 layer–groundwater reflection, $\Delta[R]$, and hydraulic head are shown for each track section
 235 in Figure 2. The mean reflectivity difference ($\Delta[R]$) for all four profiles is 11.1 ± 6.8 dB,
 236 accounting for both the standard deviation of each segment and the propagated error
 237 in $[L_b]$ from the regression slope. The four reflectivity distributions all satisfy Lilliefors
 238 and Jarque-Bera tests for normality, and their mean spread (one standard deviation about
 239 $\Delta[R]$) is 6.0 dB.

240 To estimate the subglacial material composition, we first used the arithmetic mean
 241 to combined the individual profile-mean estimates of $\tan \delta_b$ and $\Delta[R]$, yielding $\tan \delta_b =$
 242 0.0115 ± 0.0013 and $\Delta[R] = 11.1 \pm 6.8$ dB. The regions of the ternary diagrams con-
 243 sistent with these estimates are shown in Fig. 3. The upper and lower bounds for the
 244 volume fractions consider the intersection of the outlined regions in Fig. 3b-c and Fig.
 245 3e-f, which account for the full ranges of uncertainty in $\tan \delta_b$, ΔR and possible complex
 246 permittivity values of granite and groundwater till.

247 The first hypothesized model (Fig. 3a) results in material volume fractions of $\phi_{gwt} =$
 248 $16 \pm 9\%$, $\phi_{ice} = 74 \pm 10\%$, $\phi_{gran} = 10 \pm 7\%$. Substituting these volume fractions into

Eq. (3), we derive $\tilde{\epsilon}_b = 4.67(1 - j0.007) \pm 2.99(1 - j0.001)$. Using the estimates for ϵ'_b and the mean travel times (Fig. 2a-d), the mean thickness of the basal layer between the ice and groundwater table, averaged over the four sections, is 13 ± 4.7 m. Both this loss and reflectivity analysis indicate the presence of a debris-laden basal ice layer above a groundwater table. The second hypothesized model (Fig. 3d) resulted in material volume fractions of $\phi_{gw} = 1 \pm 1\%$, $\phi_{ice} = 39 \pm 23\%$, $\phi_{gran} = 60 \pm 23\%$, bedrock permittivity of $\tilde{\epsilon}_b = 5.39(1 - j0.009) \pm 5.15(1 - j0.045)$, and indicate the presence of drained, fractured bedrock 9.8 ± 2.8 m thick. While the two models differ, both are consistent with a groundwater table located ~ 10 m below overlying material of either (1) ice-cemented debris or (2) drained, fractured bedrock.

Equipotential hydraulic head lines were compared against the groundwater interfaces for all segments, and the interfaces often followed isocontours (Fig. 2i-l). Thus, the interfaces are qualitatively consistent with a groundwater table in hydrologic equilibrium. The deviations from these isopotential lines appear to be related with deviations of the flight tracks from the local ice-flow direction, especially toward the northwestern margin of the ice sheet. The lateral extent of the groundwater system is ~ 15 km².

Analysis of sidelobe patterns shows the potential of MCoRDS v5 and other systems to detect similar subglacial groundwater tables (Figure 4). MCoRDS v3 could plausibly detect nearly all Hiawatha subglacial groundwater reflections, but many would be on the edge of detectability for HiCARS due to its narrower bandwidth (15 MHz). This interpretation is favored because the subglacial groundwater table reflections only slightly exceed the sidelobes generated by basal layer echoes from these two systems. However, for MCoRDS v5 these subglacial reflections are consistently tens of decibels higher than the sidelobes. Therefore, the combination of high SNR and wide bandwidth – resulting in faster sidelobe fall-off – is likely a significant factor in explaining why the subglacial groundwater table was detected beneath a portion of Hiawatha Glacier. The lack of detection of the subglacial groundwater table in other regions of the crater could be because: 1. No groundwater table is present there; 2. The basal layer is insufficiently frozen or drained to permit substantial radio-wave penetration; 3. The groundwater table is not sufficiently contiguous to identify in the radargrams; or 4. The interface is too deep to be detected.

4 Discussion and conclusions

Both our radiometric and hydrologic analysis are consistent with the anomalous subglacial reflection originating from a groundwater table beneath either a well-drained or partially frozen basal layer within the Hiawatha impact crater floor. Our radiometric analysis shows the groundwater-table reflection is typically over 10 dB stronger than the overlying ice-basal layer reflection, strongly indicative of the presence of water-saturated material, i.e., a groundwater aquifer.

Our first hypothesized model (Fig. 3a) indicates that an ice-cemented debris layer lies above thawed, saturated groundwater till, consistent of a mixture of groundwater till, granite, and ice, with ratios of approximately 16%, 10%, and 74%, respectively. In this model, water can exist both above and below the aquitard of the frozen basal layer, and the low attenuation rate of the basal layer is the result of its thermal state, i.e., the pores are filled with ice rather than water. The underlying thawed layer might also be trapped by frozen layers above it, a feature observed in firn hydrology (Koenig et al., 2014; Chu et al., 2018). This layer could be liquid because it is confined and pressurized (Steinbrügge et al., 2020), due to refreezing, heat advected by subglacial water flow or higher salinity (Rutishauser et al., 2018).

Our second hypothesized model (Fig. 3d) indicates a basal layer of porous, well-drained rock above the groundwater table consisting of 1% groundwater, 60% granite,

299 and 39% ice. In this case, the low-loss basal layer is the result of efficient vertical drainage
 300 rather than freezing. The impact should have produced a thick layer of impact breccia,
 301 which would be permeable and conducive to rapid subglacial drainage from the overlying
 302 glacier into a groundwater system, and this second model indirectly assumes that
 303 this layer is still present. Thus, the unique detection of this subglacial groundwater table
 304 could be in part due to the uniqueness of its geologic setting.

305 The radar profiles where the groundwater table was detected are found close to each
 306 other, within the northwestern section of the crater (Kjær et al., 2018). A map of the
 307 ice-basal layer reflectivity from the 2016 survey indicates increasing relative reflectivity
 308 from the southeastern corner of the crater toward its northwestern corner (Fig. S3).
 309 Our hydrologic analyses are also consistent with this drainage pattern, in that deviations
 310 of the observed groundwater table depth from equipotential hydraulic contours show a
 311 pattern of decreasing pressure gradient toward the northwest. This pattern suggests that
 312 groundwater is indeed flowing through the crater towards the ice-sheet margin in the same
 313 direction indicated by Kjær et al. (2018). Further investigation into character and flow
 314 of the subglacial and groundwater hydrology of the Hiawatha Glacier region of Green-
 315 land will require more sophisticated modeling, such as considering variations in hydraulic
 316 conductivity and intrinsic permeability.

317 As unusual as the geologic setting of Hiawatha Glacier may be, observation of its
 318 groundwater was also partly enabled by the large bandwidth and SNR of the MCoRDS
 319 v5 system. Additional surveys by similar wideband sounders over other sites with known
 320 or hypothesized groundwater, or surveys of Hiawatha Glacier region by other radar sounders
 321 could validate the potential for wider applications of this work. This conclusion raises
 322 the possibility that other subglacial groundwater systems could be mapped using wide-
 323 band radar sounders, providing new insights into the poorly understood role of ground-
 324 water in the subglacial hydrology of Greenland, Antarctica and other glaciated regions
 325 (Key & Siegfried, 2017; Siegert et al., 2018; Williams et al., 2020).

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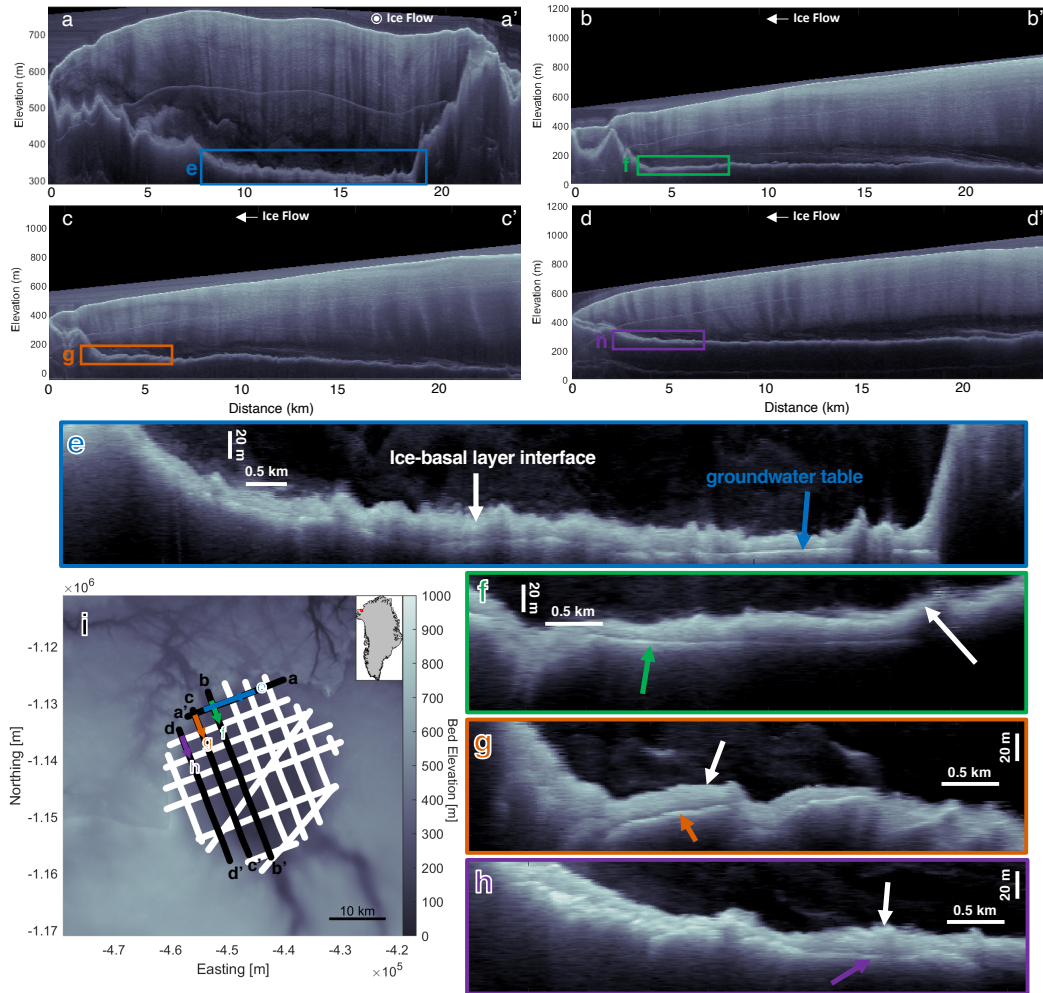


Figure 1. Radargrams from the 2016 Hiawatha Glacier survey and location of the hypothesized groundwater table. Panels a–d show full radargrams across the crater (20160517_03.008, 20160512_02_009, 20160516_02_006 and 20160512_02_007, respectively). Panels e–h are portions of a–d zoomed in on the hypothesized groundwater table. The vertical scale bar in e–h corresponds to the depth range in ice (assuming $\epsilon' = 3.15$), not sediment or rock. Panel i shows the bed topography (Morlighem et al., 2017) overlain by all the 2016 survey flights over the crater (white), with black segments (panels a–d) representing those with a potential subglacial groundwater table beneath a portion thereof (colors, panels e–h).

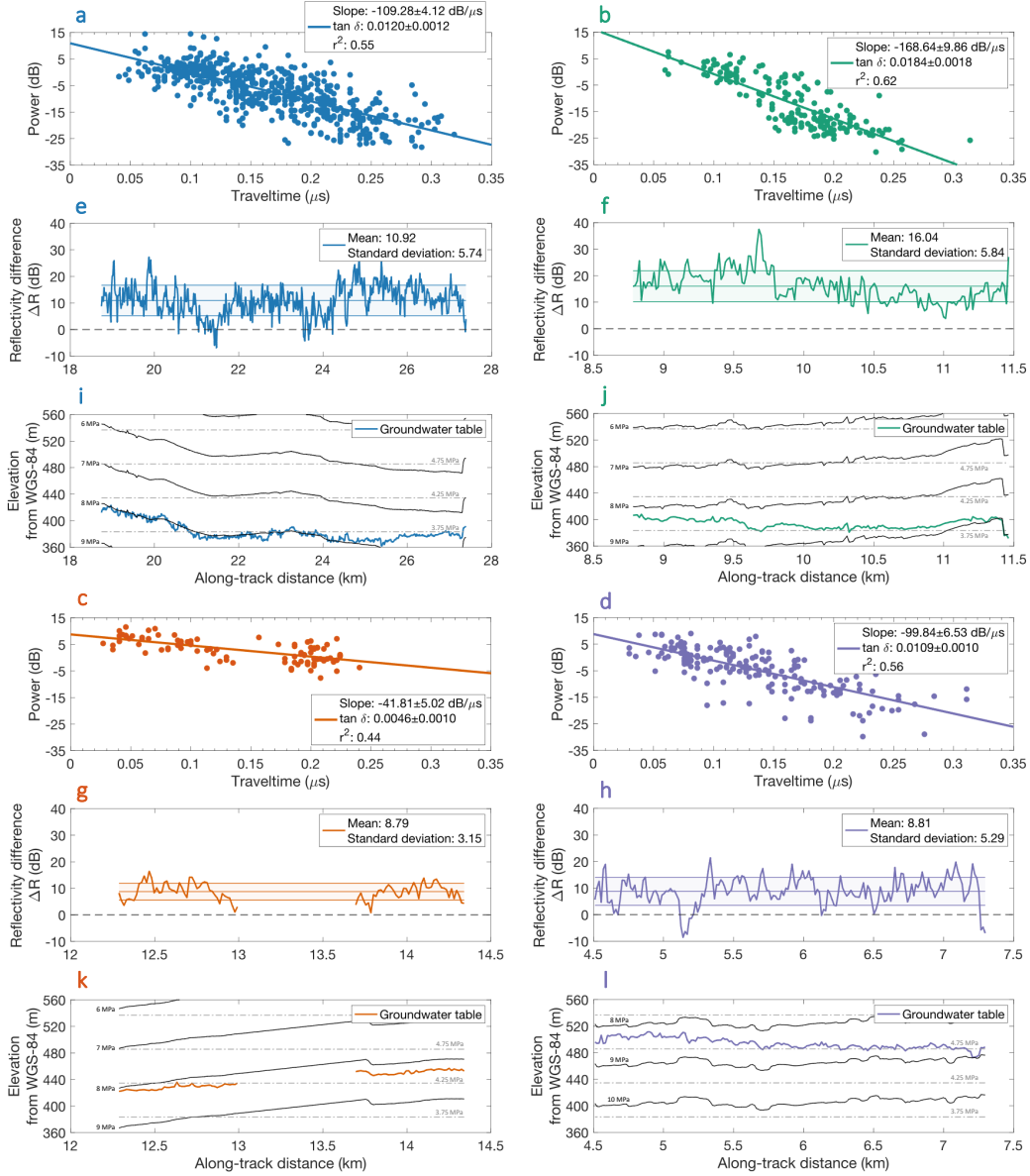


Figure 2. Radiometric data analysis for profiles shown in Fig. 1 e-h. Panels a-d show power loss in the basal layer material versus two-way travel time. The loss tangents are obtained from the regression slopes. Reflectivity difference between the basal layer-groundwater and ice-basal layer reflectors are shown in e-h and isopotential hydraulic head contours for the putative groundwater table in i-l.

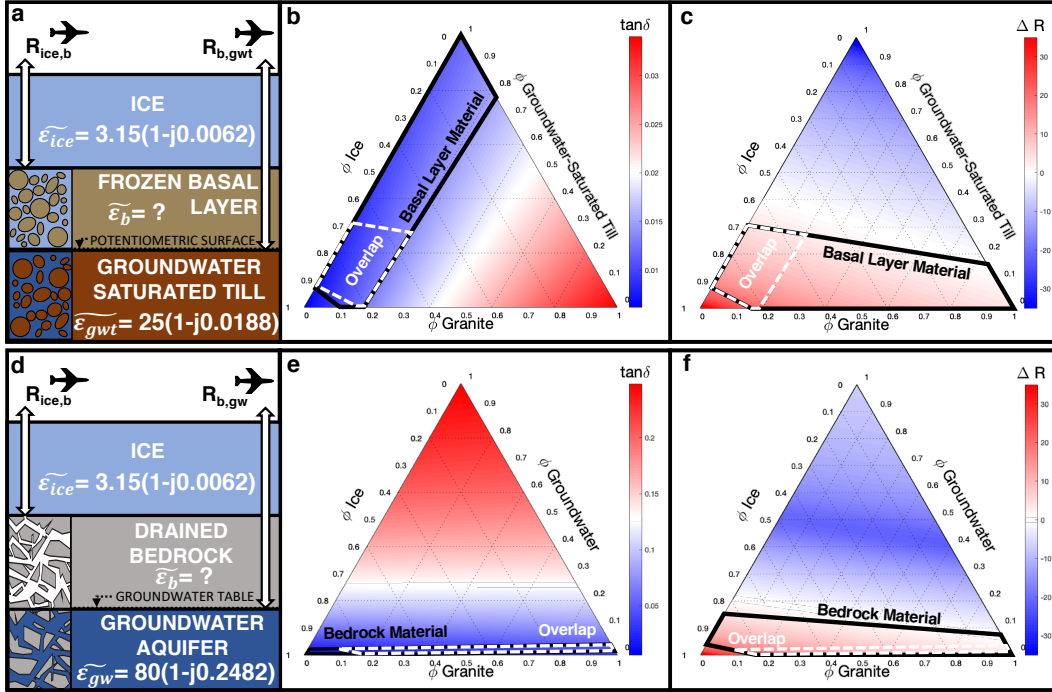


Figure 3. (a) Three-layer dielectric model of ice, a basal layer (constrained by the radiometric analysis), and groundwater-saturated till. (b) Ternary diagrams for $\tan \delta_b$ and (c) ΔR . The second row shows (d) a second hypothesized three-layer dielectric model of ice, bedrock, and groundwater. (e) Ternary diagrams for $\tan \delta_b$ and (f) ΔR with respect to the second model. Black outlined regions show most likely basal layer volume fractions, and dotted white outline showing the overlapping area of both the loss-tangent- and reflectivity-analysis probability regions. These ternary diagrams assume $\tilde{\epsilon}_{\text{gran}} = 7(1 - j0.034)$, $\tilde{\epsilon}_{\text{gwt}} = 25(1 - j0.0188)$ and $\tilde{\epsilon}_{\text{gw}} = 80(1 - j0.2482)$ (Christianson et al., 2016), but the outlined regions encompass permittivity and conductivity ranges $5(1 - j6.8 \times 10^{-5}) < \tilde{\epsilon}_{\text{gran}} < 9(1 - j0.068)$ (Bogorodsky et al., 1985; Martinez & Barnes, 2001; Nerozzi & Holt, 2019) and $20(1 - j0.005) < \tilde{\epsilon}_{\text{gwt}} < 30(1 - j0.015)$ (Christianson et al., 2016).

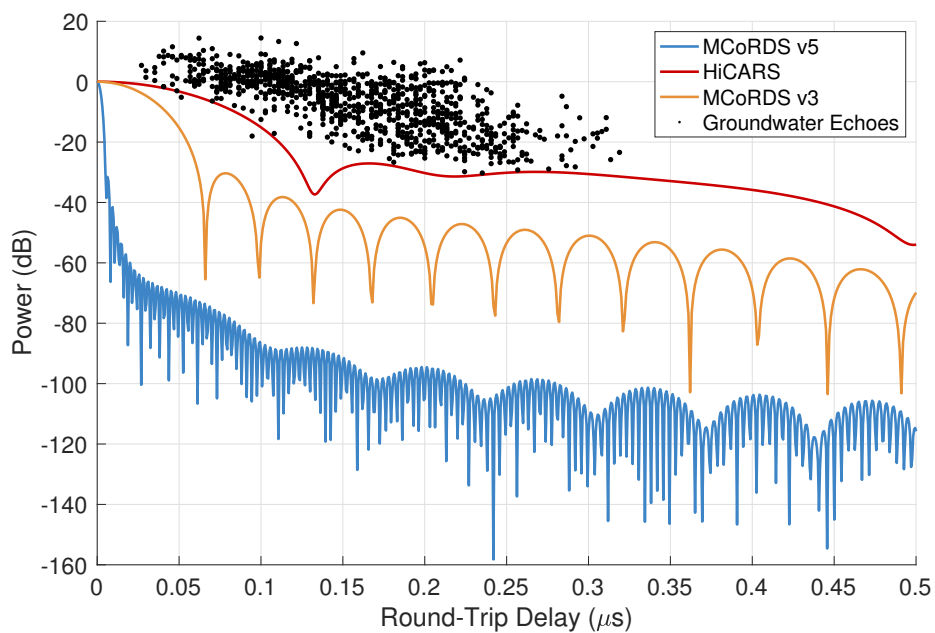


Figure 4. Antenna patterns for three radar systems (Table S1) compared against the putative groundwater echoes as a function of traveltime through the basal layer. The groundwater echoes are shown as in Fig. 2a-d. For each radar system, the potential detectability of any echo increases with the difference in power between the echo and the radar system’s antenna pattern, e.g., at a traveltime of 0.1 μs , the putative groundwater echoes are ~ 70 dB above the noise floor of MCoRDS v5, but < 15 dB above that of HiCARS.

Figure 1.

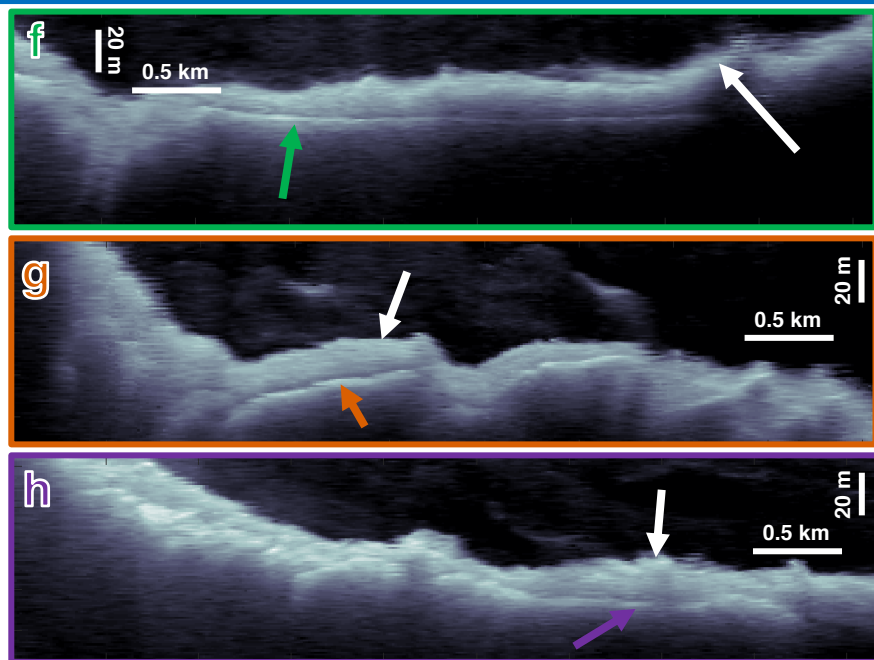
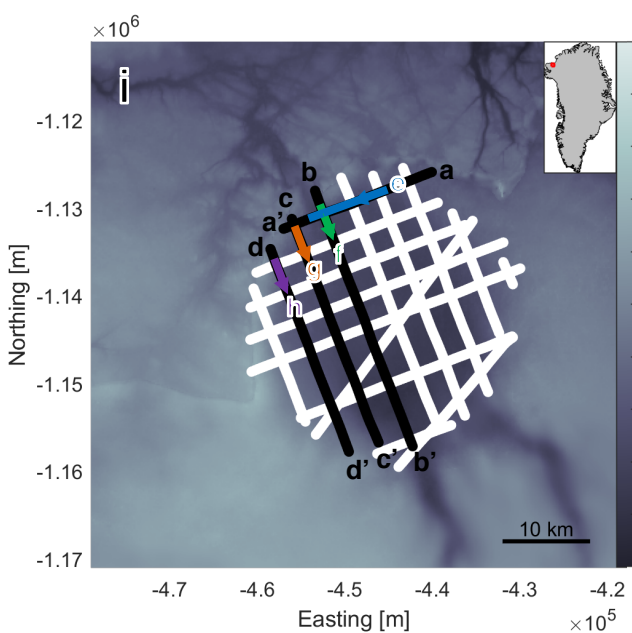
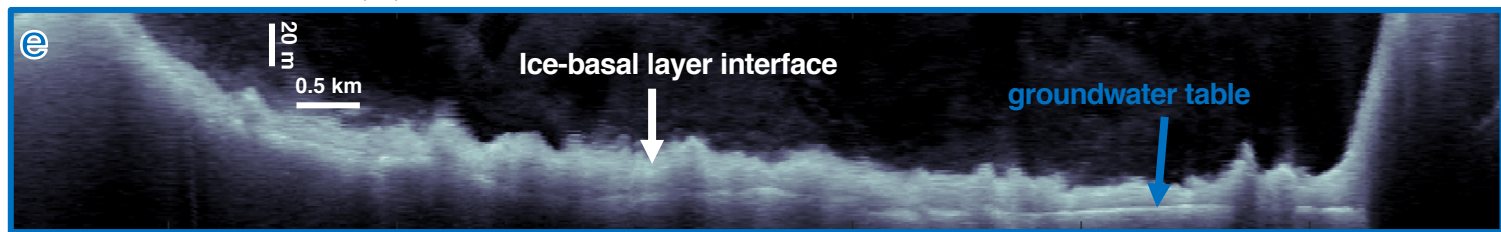
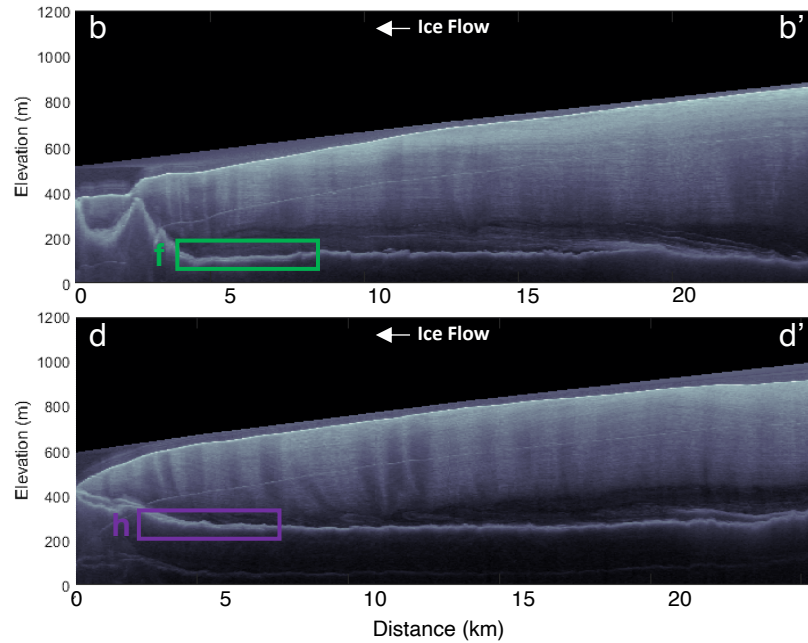
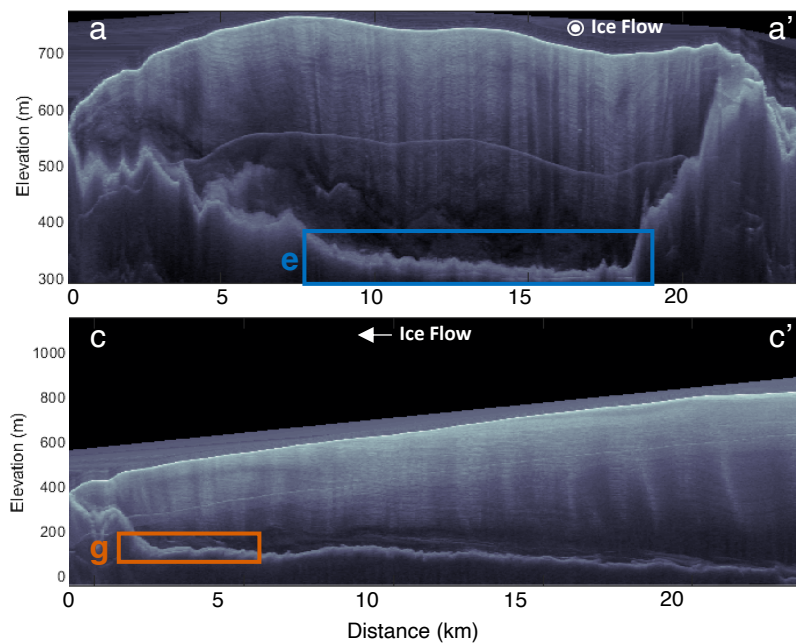


Figure 2.

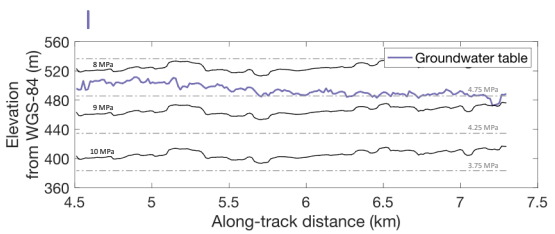
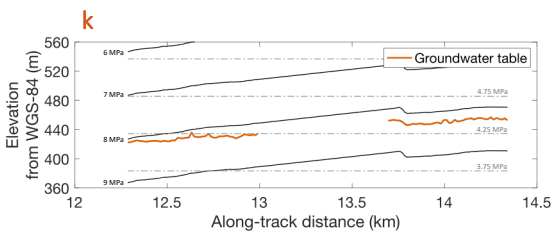
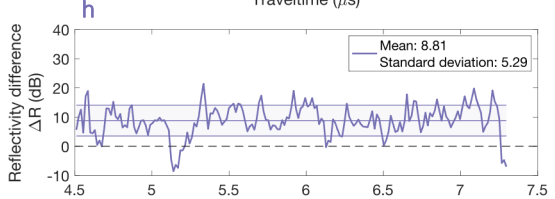
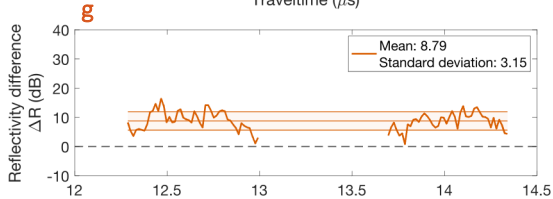
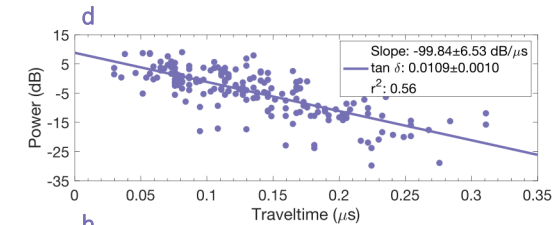
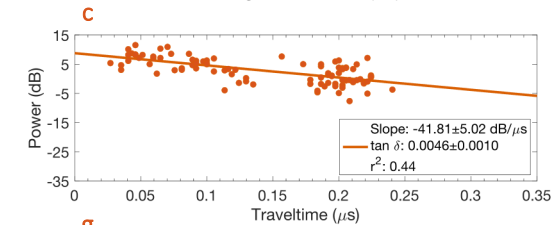
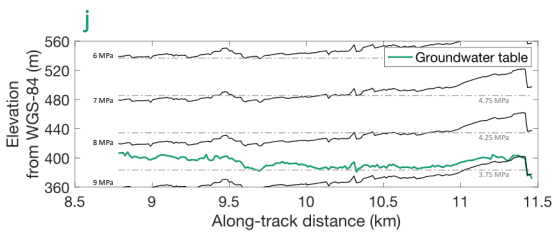
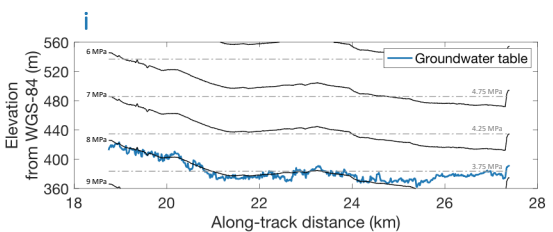
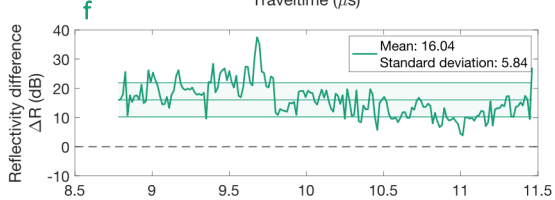
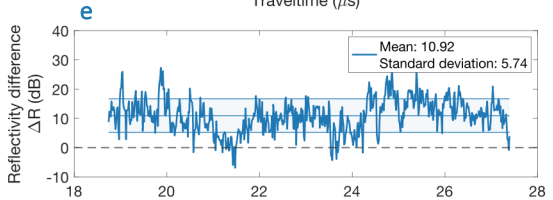
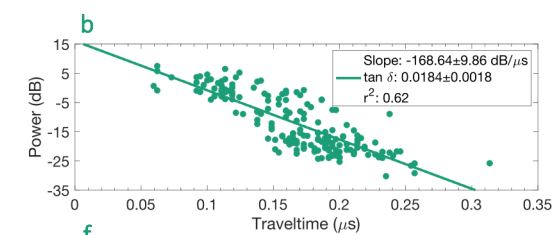
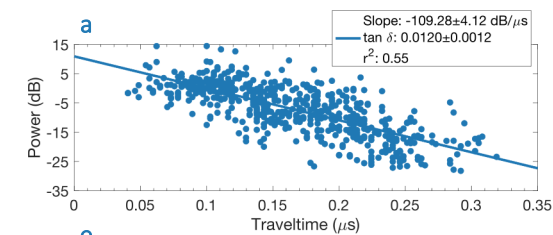


Figure 3.

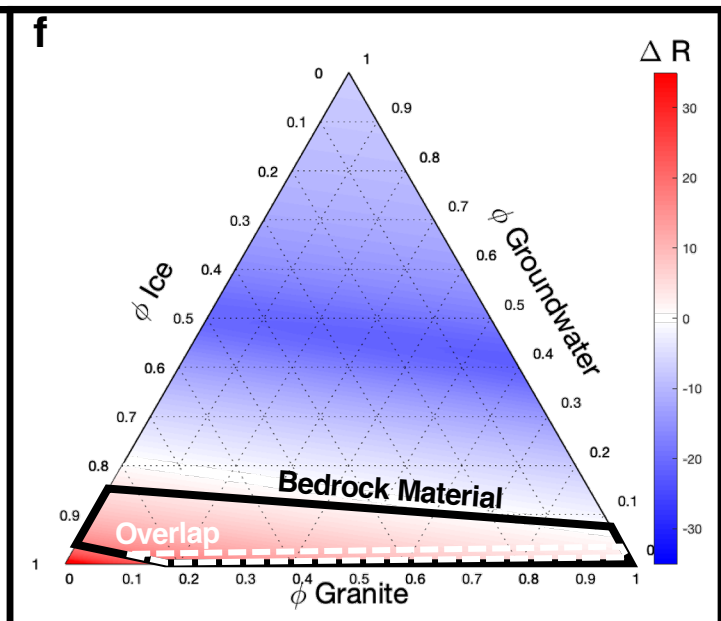
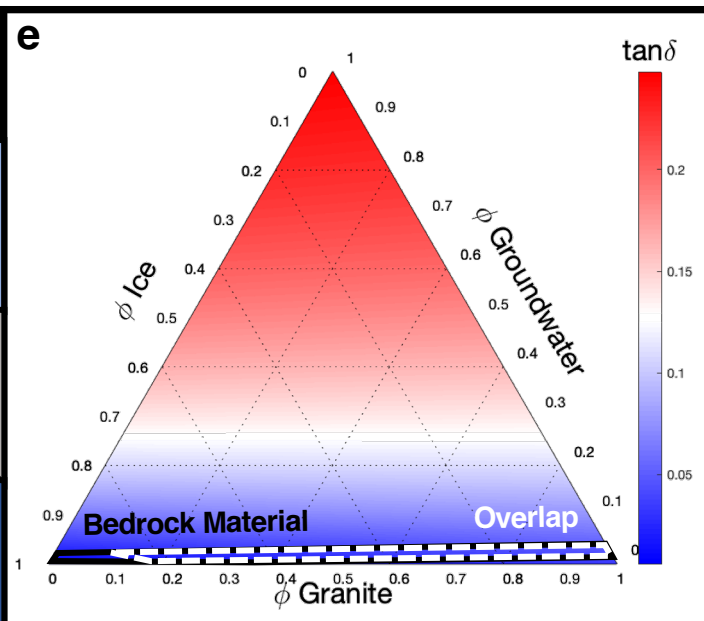
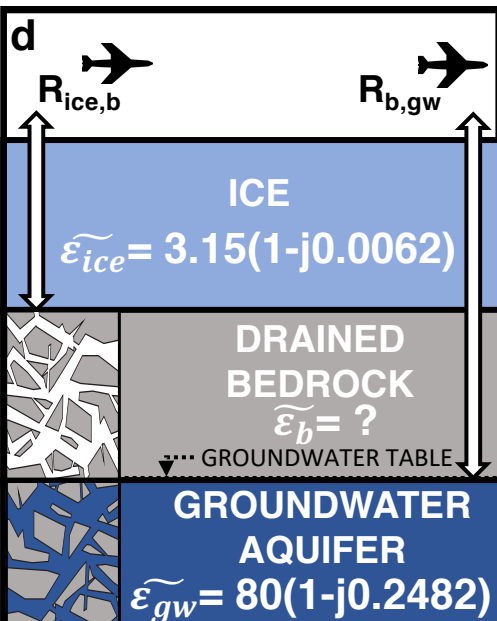
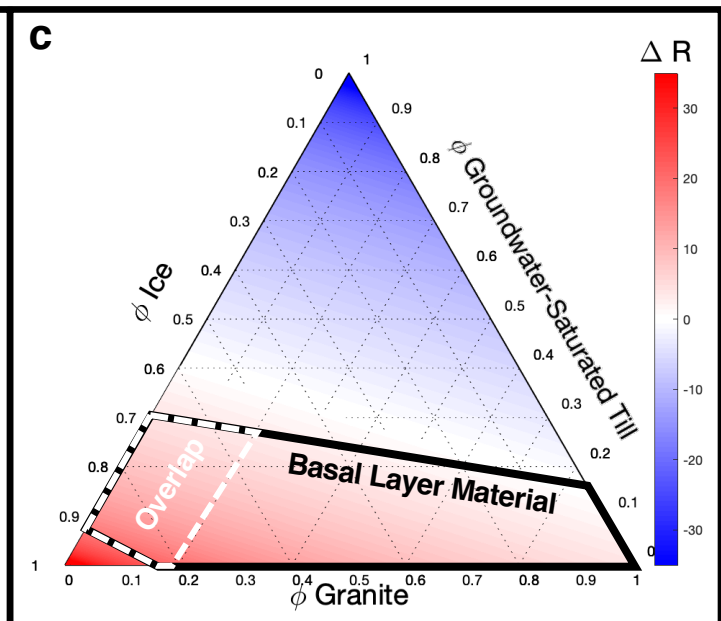
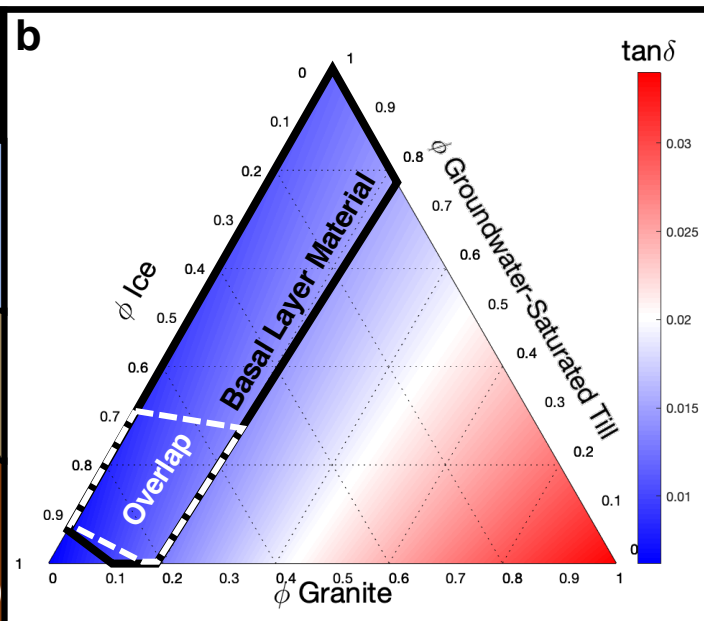
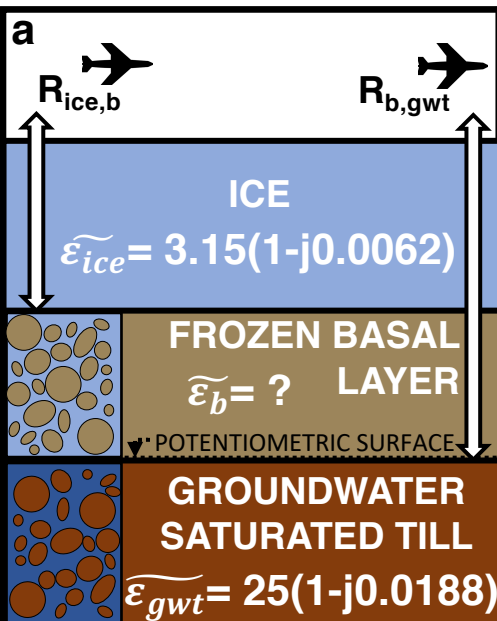


Figure 4.

