

1 **Response of the Quasi-Biennial Oscillation to historical**
2 **volcanic eruptions**

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7 **Key Points:**

- 8 • Historical simulations of Krakatoa and Pinatubo are studied using the high-top
9 NASA GISS Model E2.2
- 10 • Eruptions bias the QBO towards a westerly state, and the period response depends
11 on initial phase
- 12 • The signature of eruptions on QBO amplitude is unclear from these simulations
13 alone

Abstract

The impact of volcanic eruptions on surface climate is well-appreciated, but their *in situ* impact on the Quasi-Biennial Oscillation (QBO) has received comparatively little attention. This study examines the QBO responses to Krakatoa and Pinatubo using five configurations of the NASA Goddard Institute for Space Studies (GISS) Model E2.2 and MERRA-2 reanalysis. A dynamically consistent response is found in terms of static stability, zonal wind, and upwelling. Eruptions are found to bias the QBO towards a westerly state, such that the QBO period response depends upon the phase at the time of eruption. The QBO does not have a clear amplitude response to an eruption, based on these simulations. The underlying mechanisms appear not to be influenced to first-order by interactive composition, sea surface temperatures, or long-term trends in CO₂ and ozone-depleting substances.

Plain Language Summary

In the tropical stratosphere, the winds alternate between easterly and westerly, taking about 28 months to return to their original state. This “Quasi-Biennial Oscillation” (QBO) is ordinarily quite stable, but it can be disturbed by large forcings such as geoengineering and volcanic eruptions. In this study, we consider two volcanic eruptions in the historical record—Krakatoa (1883) and Pinatubo (1991)—and their subsequent effect on the QBO. We simulate them using a climate model, and find that the QBO prefers a westerly state after eruptions. This is important because the QBO state affects surface climate and weather prediction. Our results are largely consistent with observations of Pinatubo, and they can be tested in other climate models.

1 Introduction

It is well-appreciated that large tropical eruptions impact the atmosphere. Injected sulfate aerosols cool the surface and warm the lower stratosphere through absorption of shortwave radiation (Robock, 2000). The impacts of this forcing on the troposphere and extratropical stratosphere have received a great deal of attention, including: an acceleration of the polar vortex (e.g., Graf et al., 1993), changes to planetary waves (e.g., Stenchikov et al., 2002), a reduction in global precipitation (e.g., Iles et al., 2013), and altered surface temperatures (e.g., Robock & Mao, 1995) including winter warming.

However, the *in situ* impact of volcanic aerosols on the Quasi-Biennial Oscillation (QBO) has received much less attention. Some studies have considered geoengineering and supereruptions, which impact the tropical stratosphere on longer timescales than more moderately-sized eruptions. The general finding is that aerosol heating leads to anomalous westerlies, consistent with thermal wind balance (Randel et al., 1999), despite the large Rossby number at low latitudes. Aquila et al. (2014) simulated geoengineering as a time-invariant aerosol forcing and found that sufficiently large SO₂ injections could lengthen or shutdown the QBO in a westerly state, moderated by changes in upwelling. Niemeier and Schmidt (2017) explored a wider variety of forcing scenarios and obtained similar results, noting a dependence on initial QBO phase for transport. Richter et al. (2017) also obtained similar results, finding that interactive chemistry apparently buttressed the QBO against an aerosol-driven shutdown. Lastly, Brenna et al. (2021) simulated the supereruption of Los Chocoyos (75,000 years before present) and found a more complex response, with a long easterly pause followed by a westerly pause.

Hence, the transient impact on the QBO from more moderately sized eruptions is not clear *a priori*, and it appears that little work has been done on the subject. This is the focus of our study. Capturing the correct QBO response after an eruption is important for seasonal prediction (e.g., Garfinkel et al., 2018), QBO teleconnections (e.g., Marshall & Scaife, 2009), and trace gases (e.g., Tweedy et al., 2017). It is also desirable from

a perspective of model verification that models credibly capture the forced response to eruptions. In particular, our model captures a wide range of feedbacks: interactive sourcing of gravity wave drag, a coupled ocean, and interactive chemistry. Of the four studies mentioned above, three employed fixed non-orographic gravity wave drag, and two had specified sea surface temperatures, which may limit dynamical pathways for the QBO to respond to volcanic activity.

2 Experimental setup

In this study, we focus on eruptions in historical integrations from 1850 to 2015. The integrations are performed with the 102-layer high-top NASA Goddard Institute for Space Studies (GISS) Model E2.2 (Rind et al., 2020; Orbe et al., 2020), a contributor to the Sixth Coupled Model Intercomparison Project (CMIP6). The model’s QBO is tethered to convection through an interactive gravity wave drag scheme (Rind et al., 1988, 2014). Historical forcings are as described in Miller et al. (2021); however, the model used in that study had only 40 vertical levels and did not resolve a QBO. Explosive volcanic forcing is purely prescribed, using CMIP6 monthly aerosol extinction coefficients (Arfeuille et al., 2014; Thomason et al., 2018), linearly interpolated in time. In general, aerosol forcing is highly uncertain for both observations (Arfeuille et al., 2013) and models (Clyne et al., 2021), so we focus on dynamical aspects which may be consistent with other simulations.

We implement the model in a variety of configurations to test robustness and mechanisms. Each configuration is integrated from 1850 to 2015 in ensembles of 4 or 5 members. The configurations vary according to:

1. SP/AP physics: Standard Physics (SP) and Altered Physics (AP). As described in Rind et al. (2020); Orbe et al. (2020), the configurations differ by a number of technical changes linking model physics with vertical resolution. For our purposes, comparison between SP and AP suggests which of our results may not be robust among other CMIP6 models.
2. OCN/AMIP sea surface temperatures: interactive ocean (OCN) with 40 vertical layers or atmosphere-only (AMIP) with specified observations.
3. OMA/NINT composition: interactive chemistry (OMA; Bauer et al., 2020) or non-interactive chemistry (NINT) with monthly mean composition forcing prescribed from the zonally varying ensemble average of the corresponding OMA AMIP runs.

To investigate the QBO response to volcanoes, we focus on Krakatoa (1883) and Pinatubo (1991). These eruptions are largest in terms of tropically averaged aerosol optical depth (AOD). For Pinatubo, we compare simulations with MERRA-2 reanalysis (Gelaro et al., 2017), using dynamic diagnostics computed by Martineau et al. (2018).

To analyze changes to the QBO, we use the definitions of phase, period, and amplitude presented in DallaSanta et al. (2021). This approach considers the first two principal components of zonally averaged equatorial zonal wind between 10 and 100 hPa, which capture approximately 95% of variance. QBO amplitude is the magnitude of the two principal components, QBO phase is their orientation in phase space, and QBO period is the time elapsed for its phase to progress 360° .

3 Response of the tropical stratosphere to eruptions

In this section, we trace the stratospheric impact of eruptions from aerosol heating to the zonal wind field and hence the QBO. We begin by examining forced AOD, the subsequent heating rate, and the final temperature response. These fields are presented in Figure 1 for one example integration (others are similar) and for reanalysis.

110 The timescale of the equatorial aerosols (row 1) is one to two years, and is some-
 111 what weaker and longer for Pinatubo than for Krakatoa. The amplitude difference is pri-
 112 marily due to their respective latitudes, as the tropical stratosphere experiences smaller
 113 aerosol loading under Pinatubo than Krakatoa. Both are subject to uncertainties: pre-
 114 1979 values in the CMIP6 dataset are parameterized (Arfeuille et al., 2014), and post-
 115 Pinatubo the AOD lifetime is too long in both the model and MERRA-2 (Buchard et
 116 al., 2017). (Since MERRA-2 only provides AOD from all aerosols, we have deseasonal-
 117 ized it using the volcanically quiescent years 1984–1991, such that the remainder is a rea-
 118 sonable approximation to volcanic AOD alone.)

119 Despite ambiguity in historical AOD, its radiative impact is more clear. Specifi-
 120 cally, the presence of the aerosols induces anomalous heating in the mid-stratosphere (row
 121 2) from both shortwave and longwave contributions (Supplementary Figure S1). The strongest
 122 heating rates correspond to the onset of the aerosol forcing and its decay, and are con-
 123 fined to the aerosol location (above about 40 hPa). For Pinatubo, the aerosol appears
 124 to have a more seasonal pulse, consistent with Pinatubo’s off-equatorial location.

125 The net effect is a substantial temperature perturbation superimposed upon the
 126 existing temperature QBO (row 3). For the model example shown, a descending cold branch
 127 is interrupted by Krakatoa, and a descending warm branch is strengthened by Pinatubo.
 128 In reanalysis, a descending cold branch is interrupted by Pinatubo. Thus, the temper-
 129 ature QBO can be overwhelmed by aerosol heating, as was found for the long-term in
 130 the geoengineering and supervolcano studies previously discussed. The temperature anoma-
 131 lies persist beyond the aerosol timescale and propagate downwards below the initial heat-
 132 ing level. This indicates that the anomalies behave as QBO secondary circulations (Randel
 133 et al., 1999; DallaSanta et al., 2019) superimposed upon the background state. We will
 134 diagnose these circulations in terms of stability, upwelling, and zonal wind. Furthermore,
 135 as these anomalies propagate down, critical layer absorption provides a pathway for them
 136 to modify the QBO at higher levels (DallaSanta et al., 2021), even after the aerosols have
 137 decayed. Hence, the background state of the QBO is critical for the subsequent QBO
 138 response. In the remainder of the paper, we quantify this response more precisely.

139 To do so, we first present all model members alongside reanalysis. Given the timescales
 140 of Figure 1 and the importance of the seasonal cycle, we time-average over the one-year
 141 interval following each eruption. In the extratropics, temperature and zonal wind are quan-
 142 titatively related by thermal wind balance. This relationship becomes more qualitative
 143 at lower latitudes, due to the vanishing of the Coriolis parameter. Hence, temperature
 144 and zonal wind evolve in tandem with changes to upwelling and wave breaking. We con-
 145 vert temperature to static stability $S_p = -T \partial \ln \theta / \partial p$ to facilitate comparison. The re-
 146 sulting anomalies are shown in Figure 2. We interpret the key points as follows:

- 147 1. There is a consistent relationship between the static stability, zonal wind, and up-
 148 welling responses. This can be seen as a correlation among the vertical profiles of
 149 each member, color-coded by their initial phase.
- 150 2. Variation in the sign, magnitude, and height of these responses is closely related
 151 to differences in initial QBO phase. For instance, in a westerly phase (light blue),
 152 an increase in static stability above 20 hPa inhibits upwelling above this level, and
 153 a decrease in static stability below 20 hPa enhances upwelling below.
- 154 3. Krakatoa and Pinatubo are very comparable in their effects on static stability, zonal
 155 wind, and upwelling. This occurs despite the difference in aerosol loading (Fig-
 156 ure 1) and the difference in background conditions, suggesting that long-term cli-
 157 matology is not a primary factor for the results.
- 158 4. The NINT runs have comparable dynamical responses to OMA, despite having
 159 prescribed composition that does not correspond to their initial QBO phase. This
 160 implies that variations in composition are also less important for obtaining the cor-
 161 rect dynamical response.

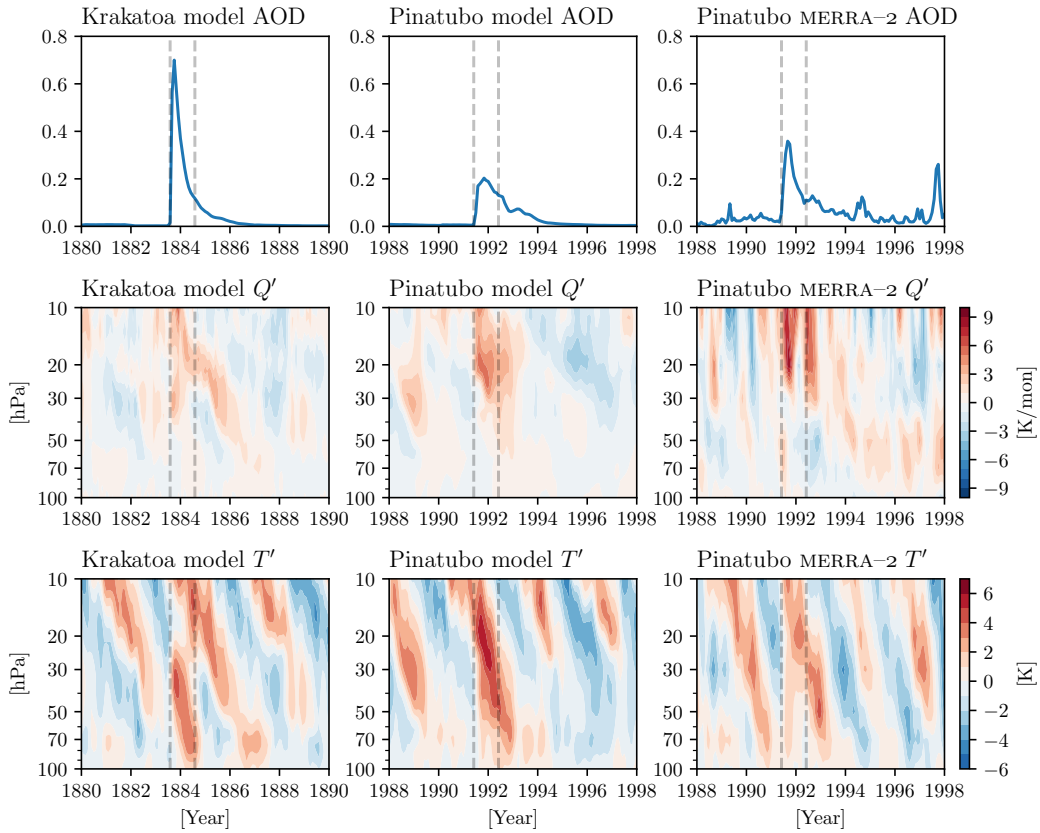


Figure 1. Equatorial AOD, aerosol heating (Q'), and temperature anomalies (T') for an example integration (columns 1 and 2) and for MERRA-2 reanalysis (column 3). Anomalies are defined as departures from the climatological average over the decade preceding the eruption. Since diagnostics solely of volcanic aerosol heating are not available, proxies are taken as the solar heating rate (model) and the longwave clear sky heating rate (reanalysis), with the seasonal and quasi-biennial cycles subtracted. The dashed lines indicate the one-year interval following the eruption, used for subsequent analysis. Values are gently smoothed for plotting, using a 3-month filter.

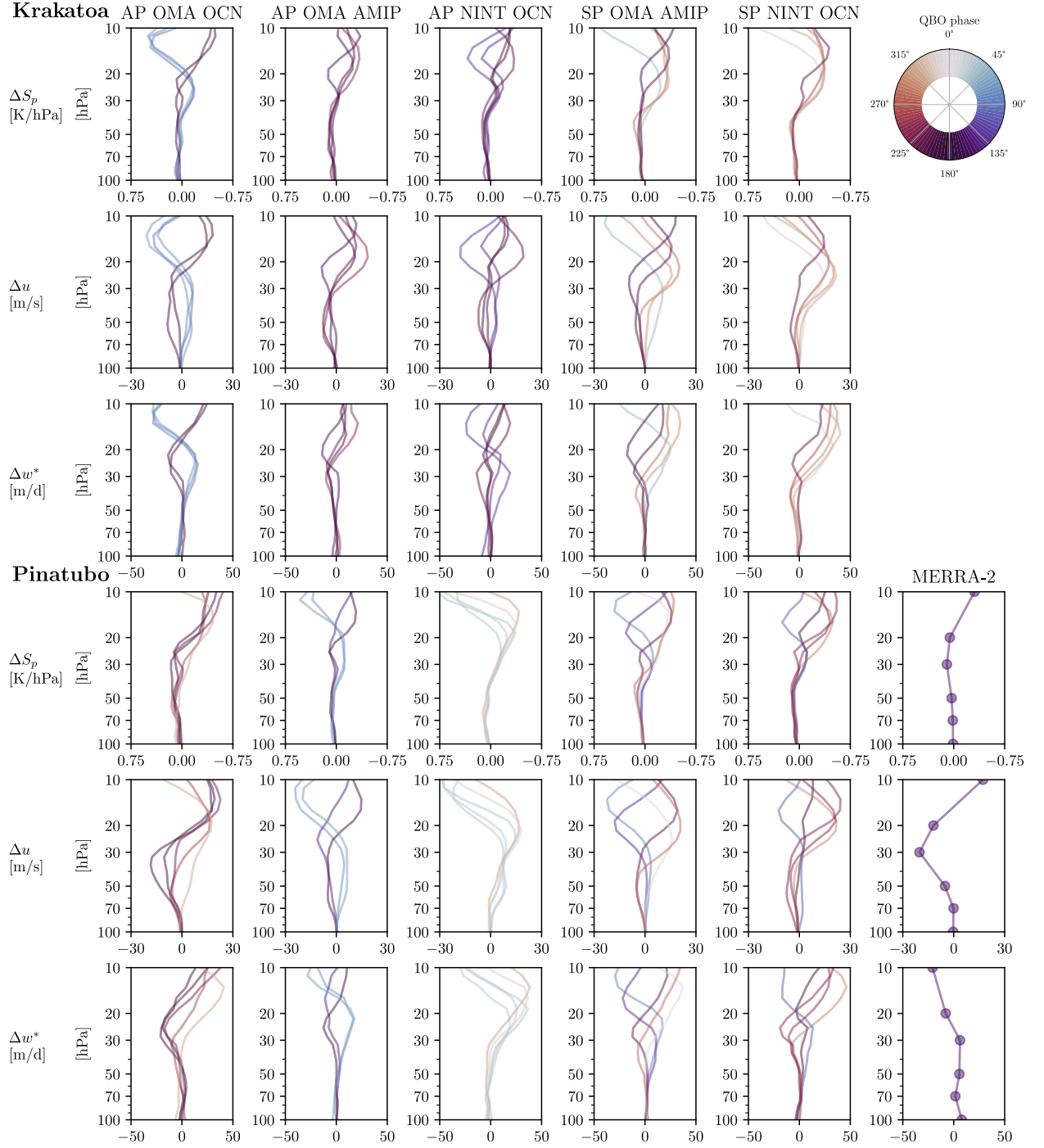


Figure 2. Responses of tropical static stability (S_p , shown with reversed abscissa), zonal wind (u), and residual vertical velocity (w^*), expressed as anomalies Δ from the decadal climatology, averaged over the one-year interval after Krakatoa (rows 1–3) and Pinatubo (rows 2–4). Each line denotes an individual ensemble member. Static stability and zonal wind are equatorial, for consistency with QBO analysis; vertical velocity is tropically averaged from $[-10, 10]$ degrees latitude, due to its high spatial variability. The colorwheel indicates the QBO phase at the time of eruption, to show which members have similar/contrasting initial phases. Dots indicate MERRA-2 levels provided by (Martineau et al., 2018).

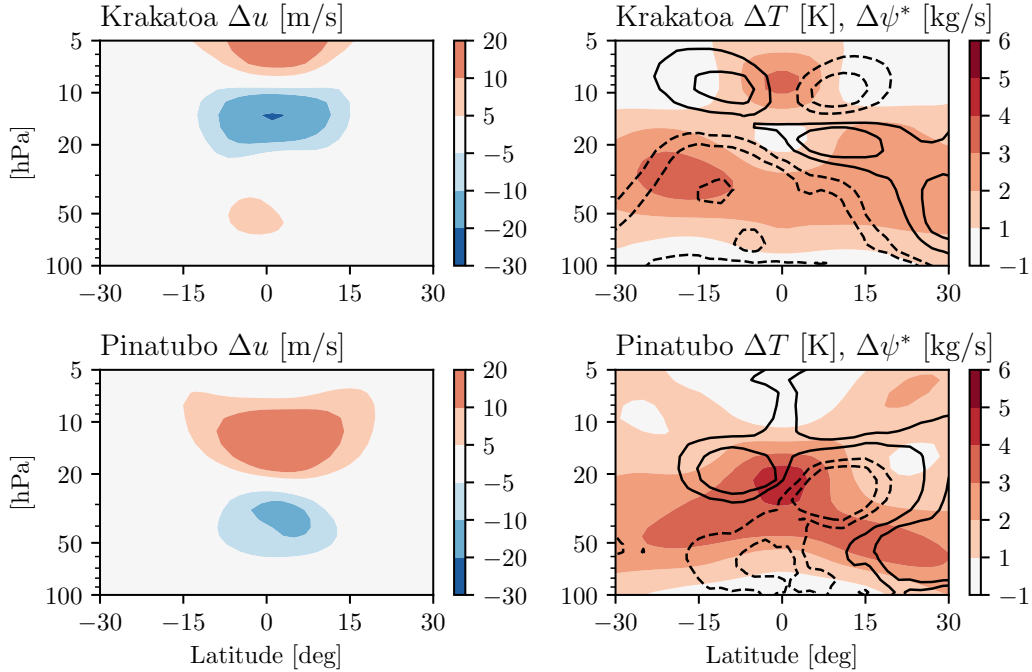


Figure 3. Responses of tropical zonal wind (column 1), temperature (column 2, colors), and residual circulation (column 2, arbitrary contours) for the example in Figure 1. As before, these are expressed as anomalies Δ from the decadal climatology, averaged over the one-year interval after Krakatoa (row 1) and Pinatubo (row 2).

- 162 5. Similarly, ocean variability does not appear to be critical, given the modest dif-
 163 ferences (Supplementary Table S1). However, variability in sea surface temper-
 164 atures can impact convection, which we will argue matters for the QBO response
 165 only if it is sufficiently weak.
- 166 6. MERRA-2 has a comparable dynamical response to the model, in terms of its am-
 167 plitude, vertical structure, and dependence on initial phase. This is despite the
 168 fact that the model does not capture the observed ozone response in its entirety,
 169 at least above 30 hPa (Supplementary Figure S2), due to underestimated chlorine
 170 activation in the post-CFC background state (Tie & Brasseur, 1995; Klobas et al.,
 171 2017; Hegglin & Tegtmeier, 2017). Thus, the ozone response does not appear to
 172 be fundamental to capturing the overall dynamical response.
- 173 7. The AP and SP configurations yield consistent results, suggesting that these dy-
 174 namical responses are not highly sensitive to model physics. However, such a sen-
 175 sitivity becomes more apparent in QBO phase space, as we will demonstrate.

176 Physically, the response is interpretable as a secondary circulation (Randel et al.,
 177 1999; DallaSanta et al., 2019), as seen in Figure 3. Although the mean circulation is pre-
 178 dominately mechanically driven, the anomaly is largely thermally forced (c.f. Garcia, 1987),
 179 and the heating contribution to $\Delta\psi^*$ exceeds the mechanical contribution (not shown).
 180 Thus, a localized decrease in stability is associated with enhanced upwelling and asso-
 181 ciated westerly torque, and vice versa. As this example member shows, the altitude of
 182 this circulation again depends on initial QBO phase, which we now examine more closely.

3.1 Response of QBO period to eruptions

In this section, we explore the quantitative responses of the QBO period and amplitude to eruptions. Overall, we find that aerosol injections bias the QBO towards a westerly phase (see Figure 4a for reference). This is consistent with the aforementioned geo-engineering and supervolcano studies. For our simulations, where aerosols decay on a timescale of one to two years, it may be expected that an eruption during a westerly phase prolongs the QBO, and an eruption during an easterly phase hastens the QBO. This is qualitatively suggested by Figure 1, and quantitatively confirmed by Figure 4bc, which shows the QBO period for each member immediately following the eruption. As expected, models in a westerly phase at the time of eruption (i.e., left of the dotted line) have substantially longer periods than climatology (horizontal lines), up to a factor of 2. In contrast, models in an easterly phase at the time of eruption (i.e., right of the dotted line) have faster periods than climatology. We now discuss these features in greater detail.

As a function of initial phase, the QBO response is fairly smooth with a discontinuity near the westerly onset ($\phi \approx 140^\circ$) at 10 hPa. As the initial phase approaches this critical value, heating by volcanic aerosols prolongs the westerly phase. To the right of the discontinuity, the aerosol heating interferes with the easterly phase of the QBO, hastening the downward migration of the westerly branch. This acceleration is more clear for Krakatoa than Pinatubo, likely because Krakatoa has a larger aerosol injection in the QBO region (Figure 1). For Pinatubo, MERRA-2 lies to the right of the discontinuity, with a period slightly shorter than its average value, although the initial response was a westerly lengthening (Labitzke, 1994).

Notably, the SP OMA AMIP ensemble (in red) appears to be an exception to the QBO period results. Its members near the critical phase have little departure from climatology. We attribute this limitation to the ensemble’s weak momentum flux due to convection. Specifically, the zonal wind tendency due to convective gravity wave drag is in-phase with the total tendency, and short-term variations in phase speed are positively correlated with momentum flux due to convection (DallaSanta et al., 2021). Ignoring all other contributions to the wind tendencies, one can thus derive a lower bound on the QBO period resulting solely from momentum deposition associated with parameterized convective gravity wave drag, as detailed in the Appendix. Figure 4de shows the QBO periods as a function of post-volcanic momentum flux due to convection, comparing them with these respective lower bounds inferred from climatology. Essentially, the weak momentum flux in SP OMA AMIP limits the rate at which the QBO can descend, such that the post-eruption response is close to the theoretical maximum phase progression (i.e., the theoretical minimum period). Even if these members begin in the optimal phase $\phi > 140^\circ$, the relatively weak convection inhibits their period response, unlike the other ensembles. Our estimate involves a number of assumptions and quantitative uncertainties, but it is nevertheless qualitatively helpful for understanding why some members may be outliers.

Thus, we draw the following interpretation. First, the QBO period response in the model is set by the initial QBO phase, with a bias towards a westerly state and away from an easterly state, related to the onset of upper-level westerlies. Second, if the model is initially in an easterly state—optimal for enhancing the subsequent phase speed—then insufficient convection will limit the period response obtained. The intra-ensemble spread in convective flux is less than the inter-ensemble spread, pointing to differences in model configuration as key rather than sample uncertainty. The OCN ensembles have larger intra-ensemble spread than AMIP, indicating that both the sea surface and the free atmosphere increase variance.

To summarize, eruptions bias the QBO phase towards lower stratospheric westerlies, such that the QBO progresses relatively slowly when initialized in a westerly phase, and relatively quickly when initialized in an easterly phase. In the latter case, the avail-

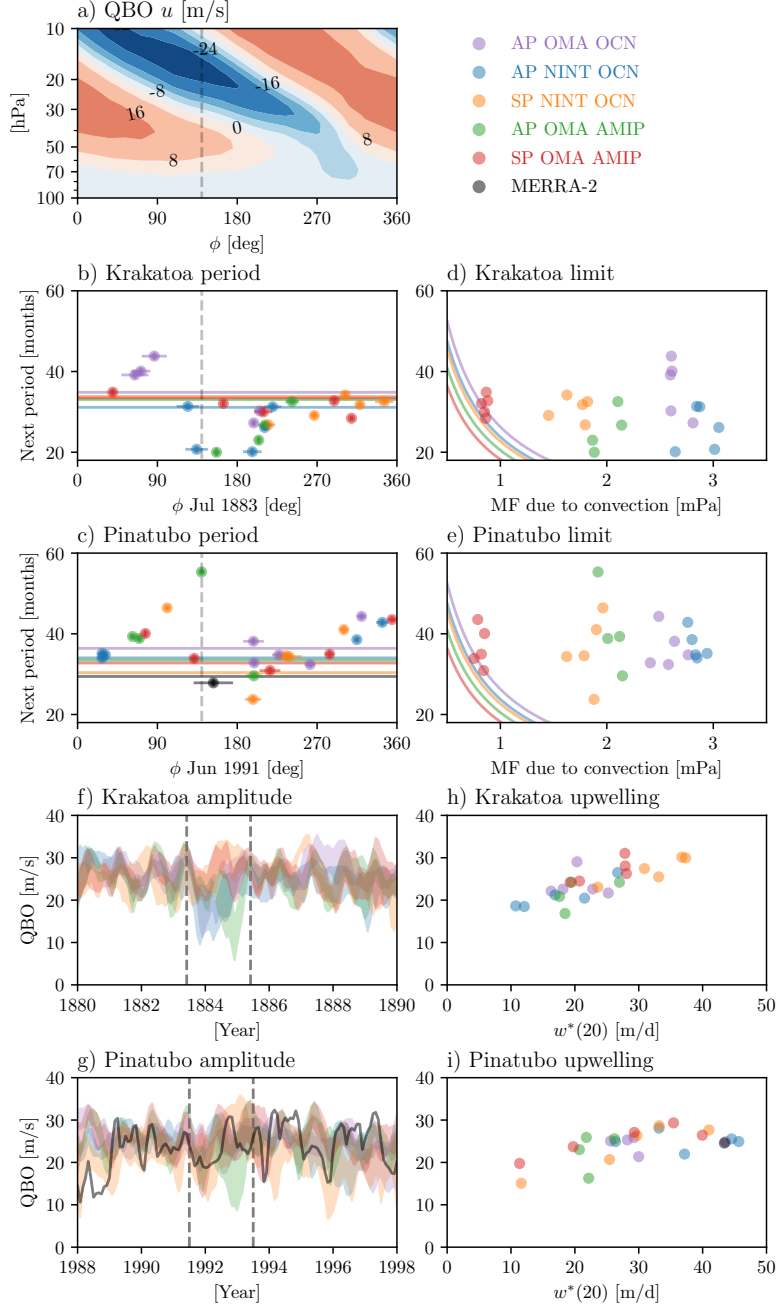


Figure 4. (a) Composit ed equatorial zonal wind as a function of QBO phase ϕ , shown for reference and labeled in m/s. The dotted line indicates the westerly onset. (b,c) Responses of the QBO period to eruptions, quantified as the length of the period immediately following each eruption. Colors denote ensembles as labeled. Horizontal lines indicate the climatological period for each ensemble. Crosses indicate uncertainty stemming from the sampling frequency. (d,e) Responses of the QBO period to eruptions, but as a function of momentum flux due to convection averaged over the one-year interval following the eruption. Momentum flux is tropically averaged from $[-5, 5]$ degrees latitude, which maximizes correspondence with phase speed (DallaSanta et al., 2021). The colored curves indicate the estimated lower bound for each ensemble, as discussed in text. (f,g) QBO amplitude around eruptions, shown as the $\pm 2\sigma$ range for each ensemble. Dashed lines indicate the 2-year period following the eruption. (h,i) QBO amplitude and 20 hPa residual vertical velocity w^* , averaged over the 2-year period after each eruption. Vertical velocity is tropically averaged from $[-10, 10]$ degrees latitude.

235 ability of momentum flux due to convection can limit the resulting QBO progression in
 236 our model.

237 3.2 Response of QBO amplitude to eruptions

238 Lastly, we consider the impact of volcanic eruptions on QBO amplitude, plotted
 239 in Figure 4fg. The results suggest that the AP configurations have some probability of
 240 a weakened amplitude post-eruption, but the SP configurations and MERRA-2 reanal-
 241 ysis do not. The timescale of these amplitude responses appears to be within the first
 242 two years of the eruption, and the response is not uniform among members, indicating
 243 that internal variability is at play.

244 To quantify individual members, we plot in Figure 4hi the amplitude as a function
 245 of vertical velocity. The amplitude evidently varies by a factor of 2, and is strongly cor-
 246 related with vertical velocity at 20 hPa. MERRA-2 reanalysis lies within the model spread,
 247 supporting the model results. Therefore, simple correlation suggests that the QBO am-
 248 plitude decrease is associated with reduced upwelling in that region.

249 Intriguingly, the amplitude response is positively rather than negatively correlated
 250 with upwelling. Could the short-term QBO response to perturbations involve a positive
 251 correlation, rather than the negative correlation generally seen for long-term trends (e.g.,
 252 Kawatani & Hamilton, 2013; Richter et al., 2020; DallaSanta et al., 2021)? This is dif-
 253 ficult to assess from these simulations alone, as any relationship could be direct (through
 254 advection) or indirect (e.g., involving changes to planetary wave activity). In particu-
 255 lar, we find that the correlation between QBO amplitude and upwelling depends upon
 256 vertical level. However, 20 hPa was a key altitude for many members in Figure 2, sug-
 257 gesting that any QBO amplitude response may be associated with the secondary circula-
 258 tion. This imparts a complexity to the amplitude–upwelling relationship that has be-
 259 come more recently appreciated, even in the context of longer-term CO₂-induced trends
 260 (Richter et al., 2020). Given this complexity, we refrain from drawing a mechanistic in-
 261 terpretation of the amplitude weakening, without additional investigation.

262 Further analysis of individual members does not find a relation between initial phase
 263 and the QBO amplitude response, in the same way a relationship was found for the QBO
 264 period. Hence we cannot confidently conclude that eruptions weaken QBO amplitude,
 265 as any response appears to be sensitive to model physics (SP versus AP) and the details
 266 of a given eruption (Krakatoa versus Pinatubo). This null-hypothesis result underscores
 267 the importance of using multiple configurations: had we only integrated AP, we would
 268 have concluded that volcanic eruptions do lower QBO amplitude.

269 4 Conclusions

270 We have studied the impact of Krakatoa and Pinatubo on the QBO using the NASA
 271 GISS Model E2.2. Our main conclusions are:

- 272 1. Krakatoa and Pinatubo have a similar signature on static stability, zonal wind,
 273 and upwelling. The responses of these fields are dynamically consistent as resid-
 274 ual circulation anomalies, and their sign and height are strongly modulated by the
 275 initial QBO phase.
- 276 2. Volcanic eruptions bias the QBO towards lower-stratospheric westerlies via aerosol-
 277 induced heating, such that the QBO period response to eruptions also depends
 278 on initial QBO phase.
- 279 3. When the eruption occurs after the onset of upper-level westerlies, the model’s pe-
 280 riod response is further modulated by the availability of momentum flux due to
 281 convection. This is related to the convective sourcing of gravity wave drag.

- 282 4. The amplitude response is overall unclear. There is no decrease for reanalysis and
283 the SP configurations, but there is some decrease in the AP configurations.

284 With respect to the geoengineering and supereruption simulations discussed in the
285 introduction, our results are broadly in dynamical agreement. Aerosol forcing nudges the
286 models toward a westerly phase, mediated primarily by changes in upwelling. We hy-
287 pothesize that under longer-term sulfate loading (from geoengineering or supereruptions)
288 our model QBO would similarly be prolonged and eventually freeze in a westerly phase.
289 However, Brenna et al. (2021) found an initial easterly response to supereruptions. Our
290 more moderately sized eruptions do not appear to induce an initial easterly response.
291 We intend to investigate these aspects along with the QBO amplitude in a future study,
292 using a range of more targeted simulations. The impact of interactive aerosols also mer-
293 its further attention, as the magnitude of the response (and other quantitative details)
294 may depend on the background state and the evolution of the aerosols.

295 The amplitude decreases for some of the AP ensemble members suggests that the
296 QBO may be more unstable after an eruption. As previous work has found the QBO to
297 shutdown in response to sufficiently strong forcing, we plan to test a wider range of forc-
298 ing amplitudes to explore possible collapse and recovery.

299 We conjectured that the period response to eruptions may have a lower bound if
300 convection is sufficiently weak. The true magnitude of tropical gravity wave momentum
301 flux is on the same order as the model configurations, but is difficult to estimate precisely
302 (Geller et al., 2013), so we do not know if it lies near this hypothetical lower bound. A
303 physical link between convection and gravity wave drag is recognized (e.g., Alexander
304 et al., 2010), so more precise observations or future high-resolution simulations would
305 provide insight regarding the relevance of our result.

306 The clear signal in the QBO period response, underscored by its dynamical ration-
307 ale, suggests that it should be straightforward to test our findings in other QBO-resolving
308 models, even with one or few members. We hypothesize that models with fixed gravity
309 wave sources might obtain a similar period result, as long as the prescribed momentum
310 flux exceeds the estimated lower bound. Further investigation may be fruitful using his-
311 torical output available from other CMIP6 models.

312 Appendix A Period limit set by convective flux

313 We estimate a lower bound on the model’s QBO period. Considering the compos-
314 ited momentum budget (DallaSanta et al., 2021), the downward propagation of the QBO
315 is predominantly driven by tropical momentum flux due to convection, which is in-phase
316 with the total tendency. Suppose that all of this momentum flux, and only this momen-
317 tum flux, is used to drive the QBO. Let u_t be the composited zonal wind tendency as
318 a function of phase ϕ and level p , and let $\phi_t = u_t/u_\phi$ be the phase speed. Then:

$$319 \text{ momentum flux} = \int_0^{p_s} |u_t|/g \, dp = \phi_t \int_0^{p_s} |u_\phi|/g \, dp \equiv \phi_t I \quad (\text{A1})$$

320 Here $I(\phi)$ is the inertia of the QBO, requiring momentum deposition to drive its
321 characteristic downward propagation. We find *a posteriori* that I is reasonably uniform
322 as a function of phase, so both sides can be averaged in ϕ . This yields an estimated max-
323 imum phase velocity associated with momentum flux due to convection. The equivalent
324 period is obtained by inverting this phase velocity. Composites are constructed across
325 the ensemble average of each configuration; the resulting lower bound on the period is
326 shown for each ensemble in Figure 4de.

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Data availability: All integrations are uploaded at <https://zenodo.org/record/512925>. ModelE source code is maintained at <https://www.giss.nasa.gov/tools/modelE/>. MERRA-2 reanalysis data are maintained at <https://disc.gsfc.nasa.gov>.

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