

# Inversion of magnetic measurements of the Swarm A satellite of the Bangui magnetic anomaly

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## Abstract

We wanted to make a satellite altitude magnetic anomaly map of the large magnetic anomaly in the Central African Republic, the Bangui magnetic anomaly, with data from the Swarm satellites. In the first part of our study, we summarize the earlier investigations and their interpretation. In the second we discuss our data processing applied to produce a magnetic anomaly map. We used the IGRF 12<sup>th</sup> to remove the long-wavelength regional anomalies. We will use an inverse procedure, which always requires a solution of the direct problem, and a horizontal polygonal prism given in the Descartes coordinate system. For this, reason the total magnetic anomaly was transformed into the Descartes coordinate system. The magnetization and its direction were used from our previous paper. The inverse problem is solved by the Simplex procedure. Our selected polygon has 14 geometrical parameters however, the inverse problem that is the numerical determination of the minimum problem is solved in the 14 dimensions. The result of our inverse problem was the 12 horizontal coordinates and the two upper and lower data of the polygon. The origin of the Bangui anomaly has been discussed in several scientific reports, either as a deep crustal tectonic feature or the result of a large external impactor. However, according to our inversion computations we cannot make any unambiguous finding for the origin of this feature. The inaccuracy in our total anomaly map is given by the Gaussian error propagation.

## Keywords

Swarm A satellite, Bangui total magnetic anomaly, optimization

## Introduction

33 Satellite altitude magnetic measurements originate in the crust. The interpretation of these data  
34 has a longer history. They started with data from Cosmos, POGOs, Magsat, Oersted, CHAMP  
35 and SAC-C satellites. A summary of these satellites is given by Langel and Hinze [1]. The  
36 recent SWARM satellites provide more data.

37 In an earlier papers by Taylor et al. [2], Taylor and Schnetzler [3] they drew attention to the  
38 application of satellite anomalies for resource exploration. They suggested the appropriate  
39 altitude, the required accuracy, and errors of these measurements.

40 We have made several geologic/tectonic interpreted of satellite magnetic anomalies see [15],  
41 [25], [26], [27].

#### 42 **Bangui magnetic anomaly**

43 The Bangui magnetic anomaly is located slightly north of Bangui city in the Central African  
44 Republic (Figure 1). The anomaly is near 6°N, 18°E and is one of the largest anomalies on  
45 Earth.

46 This magnetic anomaly was located by ground magnetic measurements by ORSTOM (Office  
47 de la Recherche Scientifique et Technique Outre-Mer) in 1953 by Godivier and Le Donche [4].  
48 This magnetic anomaly is located in the Precambrian shield and it borders Oubangui, Lobaye  
49 basins and some sub-basins. The rocks are migmatites, charnockites, metadiabases and  
50 metasedimentary (Figure 2).

51 One of the airborne magnetic profiles (No. T-204) recorded by Project Magnet [5] at 3 km  
52 altitude crosses this anomaly. Green [5] found a negative anomaly of -1500 nT (Figure 3).  
53 According to his interpretation an impact by an iron meteor is the cause of this negative  
54 magnetic anomaly.

55 Hastings [6] presented a preliminary interpretation Magsat data of Africa. He interpreted the  
56 Bangui magnetic anomaly as an uplift of the Precambrian shield. The nearly horizontally  
57 magnetized source produces the central negative anomaly.

58 Regan and Marsh [7] interpreted this anomaly as an intrusion of a large mafic pluton into the  
59 crust. They presented the anomalies measured in different altitudes and latitudes (Figure 4).  
60 This intrusion is isostatically compensated because it is warped down into the crust. This  
61 negative Bouguer anomaly is caused by the sedimentary rocks filling the basin. **The depth of**  
62 **the causative body ranges from 3 km to 35 km.** Its magnetic susceptibility is 0.01 (SI), and the

63 density contrast is  $100 \text{ kgm}^{-3}$ . The sedimentary rocks which cover the intrusive body **have** a  
64 susceptibility of  $10^{-6}$  (SI) and a density contrast of  $-150 \text{ kgm}^{-3}$ .

65 Ravat [8] interpreted this magnetic anomaly to be created by an Fe-Ni-rich meteorite or Fe-  
66 rich iron formation.

67 Girdler et al. [9] presented the LANDSAT topographic image and the Magsat magnetic  
68 anomaly superimposed on the topographic image (Figure 5). This image reveals a double ring  
69 structure with the outer ring diameter of 810 km and the inner ring diameter of 491 km. The  
70 larger diameter of the outer ring suggests that the impact was a very large body whose diameter  
71 could be of the order of 80-200 km. If this structure is caused by an early Precambrian impact  
72 it is the largest crater on Earth's surface. One hundred and twenty terrestrial impact structures  
73 have been recorded (Grieve [29]). Gridler et al. [9] interpreted the anomaly by a simple disk  
74 model with a diameter of 800 km and a thickness of 4.5 km. The top of this depth of 3 km. The  
75 magnetization is assumed to be  $10 \text{ Am}^{-1}$  and its direction is  $D=18^\circ$  and  $I=25^\circ$  respectively. The  
76 direction of the inducing field is  $D=-3^\circ$  and  $I=-12^\circ$ , and  $\kappa=0.63$  (SI) respectively. These values  
77 were used in the inversion calculations. The negative Bouguer anomaly was the result of the  
78 sediment covering the impact structure which has a lower density.

79 Several (Taylor [10], Kim [11]) have investigated the Bangui magnetic anomaly **using** the  
80 CHAMP magnetic measurements.

81 Ouabego et al. [12] investigated the distribution of magnetic rocks to determine the cause of  
82 the Bangui magnetic anomaly. According to their investigation they do not find an impact as  
83 the source of this anomaly. Their interpretation of the source of this anomaly is the African  
84 plate interacted with the old cratons of Gondwanaland, with the anomaly probably the result  
85 of the Neoproterozoic iron rich metasediments.

86 Tchoukeu et al. [28] investigated the Bangui magnetic anomaly and surrounding geological  
87 structures. They concluded that the source of the anomaly are of a crustal origin.

## 88 **Data Processing**

89 The **Swarm** satellites were launched from the Plesetsk cosmodrome on November 22, 2013 it  
90 is operated by the European Space Agency under the Living Planets Program.

91 The Swarm satellites were launched with nearly circular orbits. Two of them (A and C) orbit in  
92 tandem with an initial altitude of 460 km, while the initial altitude of the third satellite (B) is  
93 530 km. The inclination of the A and C satellites is  $87.4^\circ$  while the satellite B has an  $88^\circ$

94 inclination. A and C satellites have their orbit nearly parallel with their approximate spherical  
95 separation of  $1.5^\circ$  at the Equator.

96 We mapped Swarm A's data between February 27, 2015 and July 20, 2015.

97 The Swarm satellites have flux-gate vector magnetometers and an Overhauser scalar  
98 magnetometer [13], they record the field every second. Each day there are 86,400 data records.  
99 Since one period of revolution is *ca.* 90 minutes, one day registration (one file) includes 16  
100 satellite revolutions.

101 The magnetic measurements of the Swarm satellites can be found in the ESA Level 1B folder.  
102 These data are given in CDF (Content Definition File) format.

103 First, we convert the CDF format to the ASCII (American Standard Code) with a public Matlab  
104 program.

105 Our downloaded files contained: date and time of the measurements, spherical coordinates  
106 (latitude, longitude, and spherical radius);  $X$ ,  $Y$ ,  $Z$  components; and the total magnetic field with  
107 their measurements errors were selected for further calculations.

108 Data were selected when the  $K_p$  indices was less than  $2_+$ . The  $K_p$  index are given by the IAGA  
109 International Service of Geomagnetic Indices (<https://www.gfz-potsdam.de/en/kp-index>).

110 The next step of the data processing is the determination of the anomalies. The reference level  
111 of the anomalies is determined by the 12<sup>th</sup> generation of the International Geomagnetic  
112 Reference Field [14]. Susan Macmillan (British Geological Survey) wrote a FORTRAN  
113 program for the calculation of the IGRF which is in home page of the IAGA  
114 (<https://www.ngdc.noaa/IAGA/vmod/igrf13.f>). The reference field can be calculated for the  
115 time and position of the measured satellite data. This program is used to determinate the  $\Delta X$ ,  
116  $\Delta Y$ ,  $\Delta Z$  and  $\Delta T$  anomalies. These components are determined for the entire orbit.

117 The anomalies were selected for our research area. The limits of spherical quadrangle which  
118 covers the Bangui research area are, latitude  $-9.75^\circ \leq \varphi \leq 19.25^\circ$  and longitude  $0.25^\circ \leq \lambda \leq$   
119  $29.5^\circ$ .

## 120 **Determination of the Bangui total magnetic anomaly**

121 The appropriate satellite data are separated into downward and upward orbits. These orbits  
122 show approxamitly North and South directions. A median filter is applied for the eliminations  
123 of the outlier measurements. After this procedure, a different degree of polynomials was fitted

124 to the separate downward and upward orbits. Because the linear trends are dominant, they were  
 125 subtracted from the downward and upward orbits. Since the appropriate orbits show a similar  
 126 character their means were processed for the further calculations. In the last step a low-pass  
 127 filter was applied. This the low-pass filter was selected for calculating the dipole field at 460  
 128 km altitude. The resulting total anomaly field of our research is given in Figure 6. It is on a  
 129 Transverse Mercator projection and the inversion procedure, a reduced size of the total anomaly  
 130 field is applied (in latitude  $-3^\circ \leq \varphi \leq 13^\circ$  and longitude  $5^\circ \leq \lambda \leq 29.5^\circ$ ). The reduced size anomaly  
 131 field is shown on a Transverse Mercator projection (Figure 7).

132 It is often required to transform satellite data from spherical polar coordinates to the Cartesian  
 133  $xyz$  coordinate system. This procedure was applied see [15]. The transformation can be done in  
 134 two steps: a translation and a rotation.

### 135 **Forward problem**

136 The basic idea of the inversion is the selection an appropriate forward problem. The inversion  
 137 always determines the parameters of the model of the forward problem. Among several  
 138 possibilities the Plouff's [16] model is applied as a solution to the forward problem. His  
 139 polygonal prism model has a horizontal top ( $z_1$ ) and bottom ( $z_2$ ) faces.

140 The total magnetic field of the polygonal prism is given by the equation:

$$141 \quad T(x, y, z) = \frac{\mu_0}{4\pi} [J_x (lV_1 + mV_2 + nV_3) + J_y (lV_4 + mV_4 + nV_5) + J_z (lV_3 + mV_5 + nV_6)],$$

142 (1)

143 where  $\mu_0$  is the permeability of a vacuum,  $J_x$ ,  $J_y$  and  $J_z$  are the magnetic components of the  
 144 anomalous body,  $l$ ,  $m$  and  $n$  are direction cosines of the Earth's magnetic field:

$$145 \quad l = \cos I \cos D, m = \cos I \sin D \text{ and } n = \sin I, \quad (2)$$

146 In the previous equations  $D$  and  $I$  are the declination and inclination of the Earth's magnetic  
 147 field, respectively,  $V_1, \dots, V_6$  are the volume integrals determined by the polygonal prism.

148 Ignoring the effects of demagnetization, the components of the total magnetization vector are

$$149 \quad J_x = \kappa T l + J_r L \quad (3)$$

$$150 \quad J_y = \kappa T m + J_r M \quad (4)$$

$$151 \quad J_z = \kappa T n + J_r N, \quad (5)$$

152 where  $\kappa$  is the magnetic volume susceptibility,  $T$  is the magnitude of the Earth's magnetic field  
153 in the vicinity of the body, the  $L$ ,  $M$  and  $N$  are the direction cosines of the remanent  
154 magnetization,  $J_r$  is the intensity of remanent magnetization.

155 The direction cosines of the remanent magnetization are determined by the following:

156 
$$L = \cos \alpha \cos \beta, M = \cos \alpha \sin \beta, N = \sin \alpha \quad (6)$$

157  $\alpha$  and  $\beta$  are the inclination and declination of the remanent magnetization, respectively.

158 According to Girdler et al. [9] the remanent magnetization is assumed to be  $10 \text{ Am}^{-1}$  and its  
159 direction is  $\beta=18^\circ$  and  $\alpha=25^\circ$  respectively. The susceptibility is  $\kappa=0.63$  (SI). The direction of  
160 the Earth's magnetic field is  $D=-3^\circ$  and  $I=-12^\circ$  respectively. These values will be used in the  
161 inversion calculations.

162 After some trial and error an elongated polygonal prism with 6 edges (6  $x$  and 6  $y$  coordinates)  
163 and with  $z_1$  and  $z_2$  vertical depths was selected. The horizontal parameters (6  $x$  and 6  $y$   
164 coordinates) and two depth parameters  $z_1$  and  $z_2$  are determined. The position of the horizontal  
165 parameters are shown in Figure 8. These 14 geometrical parameters were determined by the  
166 inversion procedure.

### 167 **The inversion of the Bangui total magnetic field anomaly**

168 The Bayesian inference is applied to the inversion of the Bangui magnetic anomaly. The  
169 Bayesian inference is widely used in the inversion procedures and is summarized by Box and  
170 Tiao [17], Tarantola [18], Duijndam [19] and [20], Menke [21], Gregory [22], Kis et al. [15]  
171 [26].

172 The basic equation of the Bayesian inference is:

173 
$$p(\mathbf{m}|\mathbf{d}) = p(\mathbf{d}|\mathbf{m}) p(\mathbf{m}), \quad (7)$$

174

175 where  $p(\mathbf{m}|\mathbf{d})$  is the *a posteriori* conditional probability density,  $p(\mathbf{d}|\mathbf{m})$  is the *likelihood*  
176 conditional probability density,  $p(\mathbf{m})$  is the *a priori* probability density. The vector  $\mathbf{m}$  is the  
177 estimated parameters of the forward model and the vector  $\mathbf{d}$  was recorded by the magnetic field  
178 anomalies from Swarm A. The *a posteriori* conditional probability density for Gaussian  
179 multivariate distribution can be expressed in the following form:

180 
$$p_{\text{a posteriori}}(\mathbf{m}) = \textit{konst} \exp \left\{ -\frac{1}{2} \left[ (\mathbf{m} - \mathbf{m}_{\text{a priori}})^T \mathbf{C}_M^{-1} (\mathbf{m} - \mathbf{m}_{\text{a priori}}) + \right. \right.$$

181 
$$\left. (\mathbf{g}_{\text{model}}(\mathbf{m}) - \mathbf{d}_{\text{observed}})^T \mathbf{C}_D^{-1} (\mathbf{g}_{\text{model}}(\mathbf{m}) - \mathbf{d}_{\text{observed}}) \right\} \quad (8)$$

182 where vector  $\mathbf{m}_{\text{a priori}}$  is the parameters estimated by the interpreter,  $\mathbf{C}_m$  is the covariance matrix  
 183 of the estimated parameters, vector  $\mathbf{d}_{\text{observed}}$  are the measured Swarm A anomalies,  $\mathbf{g}_{\text{model}}(x,y,\mathbf{m})$   
 184 is the calculated values at the coordinate  $(x,y)$ , calculated for the  $\mathbf{m}$  parameters. The subscript  
 185 model means the parameter of the forward problem.  $\mathbf{C}_D$  is the covariance matrix of the Swarm  
 186 A measured field, superscript  $T$  is the transposed vector.

187 We want to maximize the *a posteriori* probability density given by the Equation (8) as a  
 188 function of the parameter  $\mathbf{m}$ . This is equivalent to minimizing the sum of exponent of the  
 189 Equation (8). The functions  $E(\mathbf{m})$  which will be minimized for multivariate Gaussian parameter  
 190 distribution is:

191

192 
$$E(\mathbf{m}) = (\mathbf{m} - \mathbf{m}_{\text{a priori}})^T \mathbf{C}_m^{-1} (\mathbf{m} - \mathbf{m}_{\text{a priori}}) + (\mathbf{T}_{\text{model}}(x, y, \mathbf{m})$$

193 
$$- \mathbf{T}_{\text{observed}}(x, y))^T \mathbf{C}_D^{-1} (\mathbf{T}_{\text{model}}(x, y, \mathbf{m}) - \mathbf{T}_{\text{observed}}(x, y)). \quad (9)$$

194

195 The minimum problem or optimization is solved by the nonlinear Simplex method Walsh [23]  
 196 in 14 dimensions. In the present investigation the *a priori* covariance matrix is a diagonal one  
 197 whose variances is  $10 \text{ km}^2$ , the *likelihood* covariance matrix is also diagonal one whose  
 198 variances is  $2 \text{ nT}^2$ . The upper and lower depths of 5.2 km and 6.4 km are obtained by this  
 199 inversion. The result of the solution of the minimum problem is shown in Figure 9b. Figure 9a  
 200 shows the input Bangui magnetic anomaly.

201 Figure 10 shows the difference between the input Bangui magnetic anomaly (Figure 9a) and  
 202 the solution of the minimum problem (Figure 9b). The difference is less than the determined by  
 203 the error calculations. The relatively greater difference can be seen at edges of the Figure 10.  
 204 Figure 10 demonstrates the similarity of the two anomalies.

205

## 206 **Error calculations**

207 The anomaly field  $\Delta T_M$  is determined by the Simplex method is plotted in Figure 9. The errors  
 208 of these anomaly field are calculated by the Gaussian law of error propagation (Clifford [24]).  
 209 The anomaly field is the functions of the  $x_1, y_1, x_2, \dots, z_1$  and  $z_2$  parameters which have the  $\Delta x_1,$

210  $\Delta y_1, \Delta x_2, \dots \Delta z_1$  and  $\Delta z_2$  average errors. The average errors of the horizontal parameters  $\Delta$  are  
 211 estimated by the forward problem which are 5 km even though it is **somewhat** overestimated.

212 We also estimated the horizontal derivatives in the direct problem (Equation 1). It is estimated  
 213 by the variation of the field when it has unit changes in the direction  $x$  and  $y$ . The derivatives of  
 214 the horizontal parameters are minor and they are the order of 0.02 nT/km.

215 The error of the vertical parameters  $z_1$  and  $z_2$  is estimated by the values presented in the home  
 216 page of Swarm A satellite. The error depends on changes in the vertical position of the satellite.  
 217 The main effects are influenced by the plasma drag on the satellite and the eccentric orbit. The  
 218 order of the vertical derivatives is 1 nT/km. The  $\Delta T_M$  error of the plotted anomaly field is  $\pm 6$   
 219 nT.

220

$$221 \quad \Delta T_{M_{error}} = \pm \left( \begin{array}{l} \left( \frac{\partial T}{\partial x_1} \Delta x_1 \right)^2 + \left( \frac{\partial T}{\partial y_1} \Delta y_1 \right)^2 + \left( \frac{\partial T}{\partial x_2} \Delta x_2 \right)^2 + \left( \frac{\partial T}{\partial y_2} \Delta y_2 \right)^2 + \\ \left( \frac{\partial T}{\partial x_3} \Delta x_3 \right)^2 + \left( \frac{\partial T}{\partial y_3} \Delta y_3 \right)^2 + \left( \frac{\partial T}{\partial x_4} \Delta x_4 \right)^2 + \left( \frac{\partial T}{\partial y_4} \Delta y_4 \right)^2 + \\ \left( \frac{\partial T}{\partial x_5} \Delta x_5 \right)^2 + \left( \frac{\partial T}{\partial y_5} \Delta y_5 \right)^2 + \left( \frac{\partial T}{\partial x_6} \Delta x_6 \right)^2 + \left( \frac{\partial T}{\partial y_6} \Delta y_6 \right)^2 + \\ \left( \frac{\partial T}{\partial z_1} \Delta z_1 \right)^2 + \left( \frac{\partial T}{\partial z_2} \Delta z_2 \right)^2 \end{array} \right)^{\frac{1}{2}} \quad (10)$$

## 222 **Conclusions**

223 It can be concluded that the inverse calculation of 14 parameters represents the anomaly field.  
 224 The anomaly field obtained by inversion shows a proper range but the origin of the anomaly  
 225 field has not been decided unambiguously. The determined depths by inversion are consisted  
 226 with the depths obtained by Girdler et al. [9]. The error in the calculated anomaly field mainly  
 227 depends on the vertical parameters. We have to emphasize that the determined error is  
 228 overestimated.

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307

## Captions

308

309

310 Figure 1. This figure maps the border of the African counties, the Central African Republic  
311 is indicated.

312 Figure 2. Simplified geological map of the region of the Bangui magnetic anomaly in the  
313 Central African Republic. The double circles show (later discussed) the position of the  
314 impact structure (Girdler et al. [9]).

315 Figure 3. Bangui magnetic anomaly at 3 km altitude. Several profiles are presented with  
316 Profile T 204 showing the Bangui total magnetic anomaly. The positions of the flight lines  
317 are shown in the left side (Green [5]).

318 Figure 4. Magsat data indicating the Bangui magnetic anomaly at different altitudes and  
319 longitudes (Regan and Marsh [7])

320 Figure 5. The Bangui Magsat magnetic anomaly superimposed on a topographic image  
321 (upper), the Bangui Magsat anomaly map superimposed on the topographic image with the  
322 double ring structure (lower) (Girdler et al. [9])

323 Figure 6. Bangui total magnetic anomaly plotted on a Transverse Mercator projection.

324 Figure 7. Reduced extension of the Bangui total magnetic anomaly applied to the inversion  
325 procedure, the anomaly is plotted on a Transverse Mercator projection.

326 Figure 8. The horizontal coordinates of the applied points of the forward problem are plotted  
327 in Descartes coordinate system. The origin of the Descartes coordinate system is positioned  
328 in the point of (polar distance)  $\theta=86^\circ$  and (longitude)  $\lambda=19^\circ$ .

329 Figure 9. The reduced extension of the Bangui total magnetic anomaly (the input of the  
330 inversion) (a) and the anomaly map determined by the inversion (b) the anomalies are  
331 plotted in the Descartes coordinate system. The origin of the Descartes coordinate system  
332 is positioned in the point of (polar distance)  $\theta=86^\circ$  and (longitude)  $\lambda=19^\circ$ .

333 Figure 10. The difference between the input Bangui anomaly and the anomaly determined  
334 by inversion.