

# Bistable Deployable Composite Booms with Parabolic Cross-Sections

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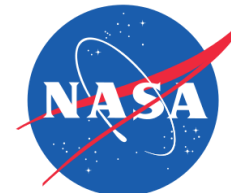
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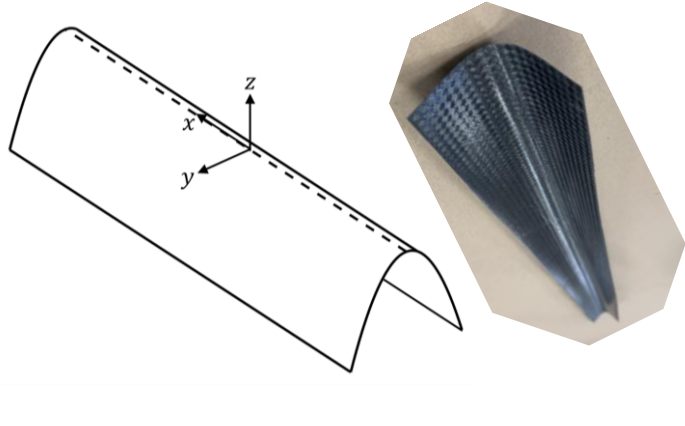
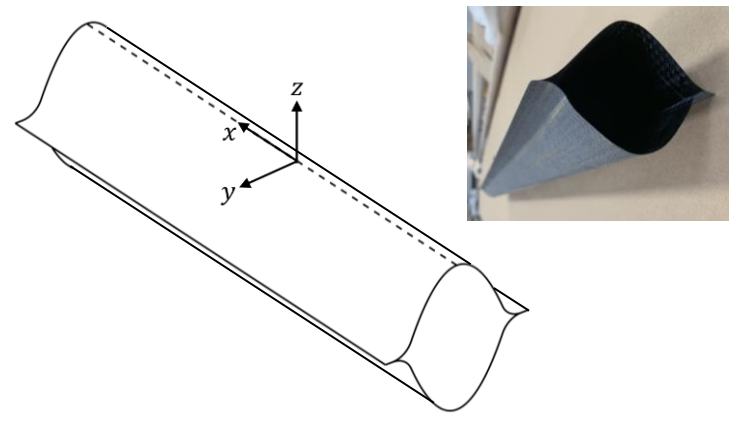
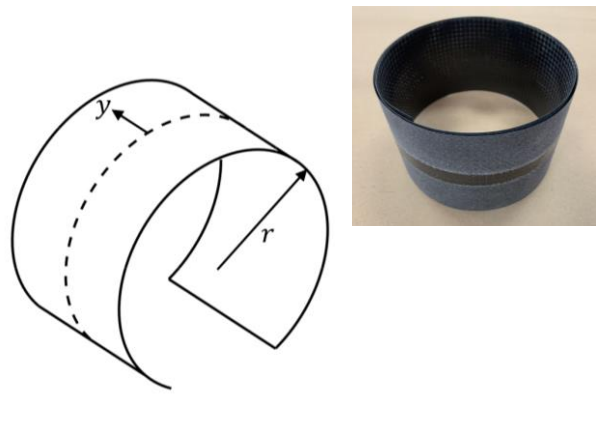
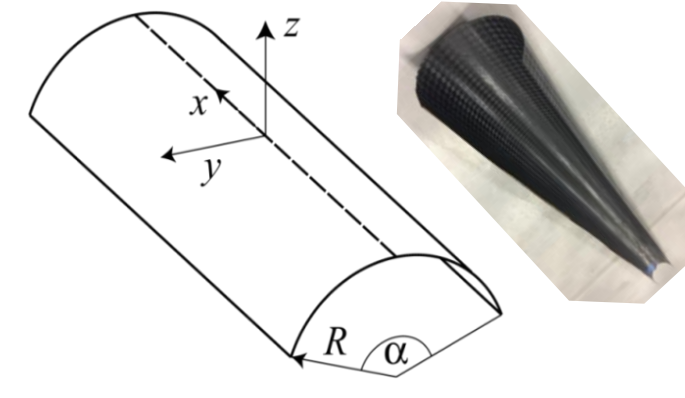
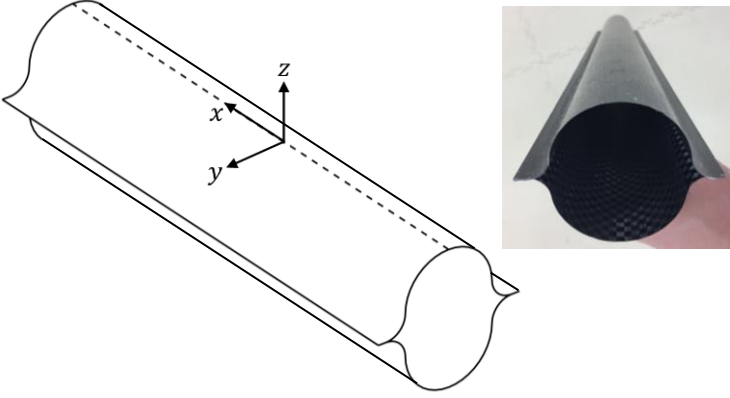
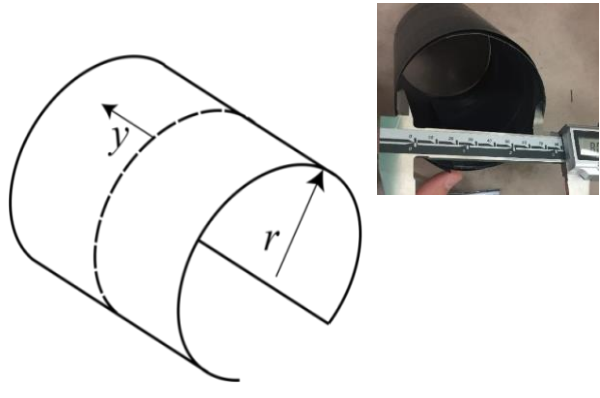
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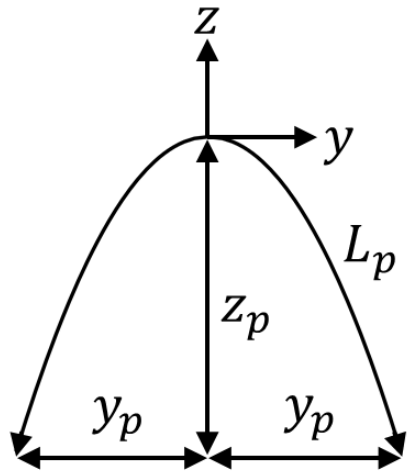
# Background and Objectives

- Analytically model bistable configurations of thin-shelled composite booms with parabolic cross-sections
- Compare stiffness properties and stable coiled geometry between parabolic and circular booms
- Verify optimal design cases with finite element analysis (FEA)

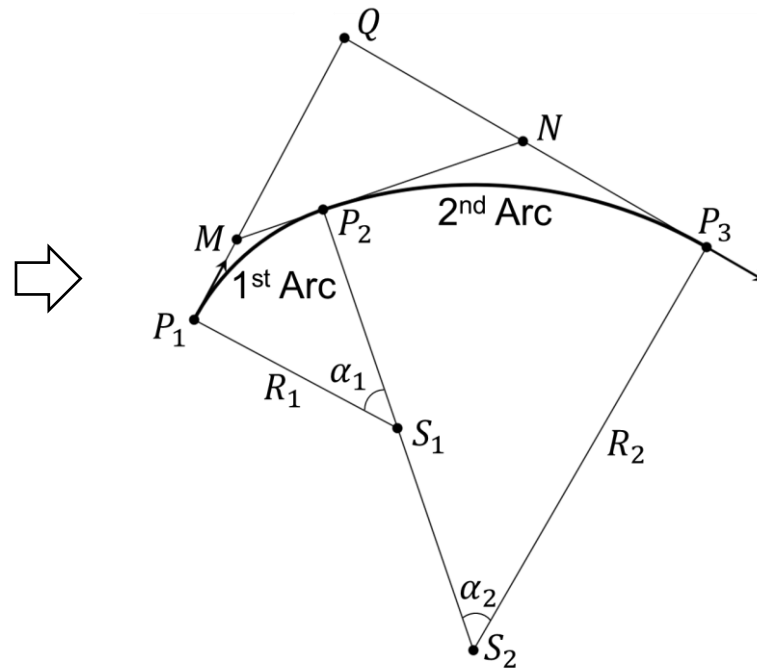
Cross-section	Extended State: Tape Spring	Extended State: Collapsible Tubular Mast (CTM)	Coiled State
Parabolic			
Circular			

# Inextensional Model

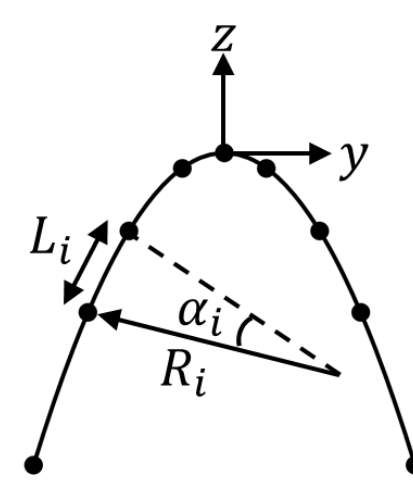
Specify parabolic shape with 2 independent parameters



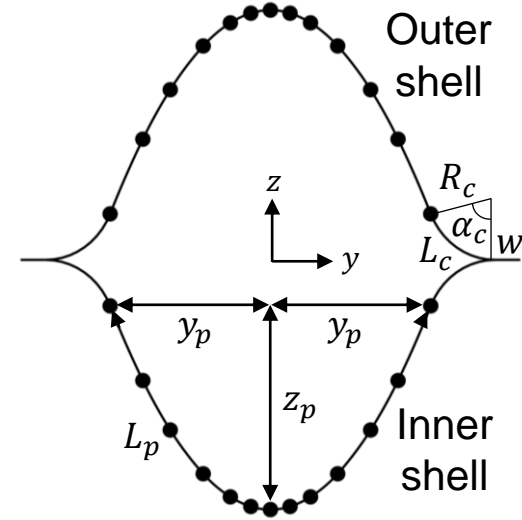
Discretize into circular segments with tangent continuity using biarc spline interpolation



Yields  $n$  circular arcs approximating parabola within a specified error tolerance



Tape spring (TS)



CTM boom

Sum non-dimensionalized strain energy per unit length of all segments and minimize to obtain equilibrium states

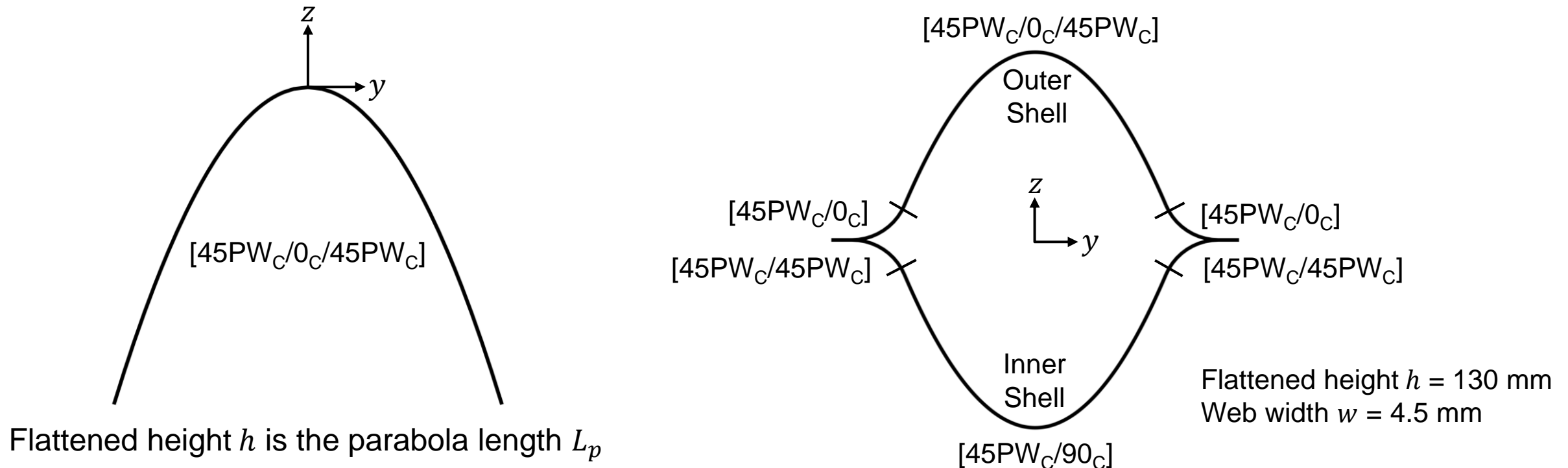
$$\hat{U}_{TS} = \frac{1}{2L_p} \sum_{i=1}^n L_i \hat{\mathbf{k}}_i^T \hat{\mathbf{D}} \hat{\mathbf{k}}_i$$

$$\hat{U}_{CTM} = \frac{1}{h} \left[ \underbrace{L_{c_o} \hat{\mathbf{k}}_{c_o}^T \hat{\mathbf{D}}_{c_o} \hat{\mathbf{k}}_{c_o}}_{\text{Outer shell circular section}} + \underbrace{L_{c_i} \hat{\mathbf{k}}_{c_i}^T \hat{\mathbf{D}}_{c_i} \hat{\mathbf{k}}_{c_i}}_{\text{Inner shell circular section}} + \underbrace{w \hat{\mathbf{k}}_w^T \hat{\mathbf{D}}_w \hat{\mathbf{k}}_w}_{\text{Web section}} + \frac{1}{2} \sum_{i=1}^n \underbrace{L_{i_o} \hat{\mathbf{k}}_{i_o}^T \hat{\mathbf{D}}_{i_o} \hat{\mathbf{k}}_{i_o}}_{\text{Outer shell parabola}} + \underbrace{L_{i_i} \hat{\mathbf{k}}_{i_i}^T \hat{\mathbf{D}}_{i_i} \hat{\mathbf{k}}_{i_i}}_{\text{Inner shell parabola}} \right]$$

# Material Properties and Layups

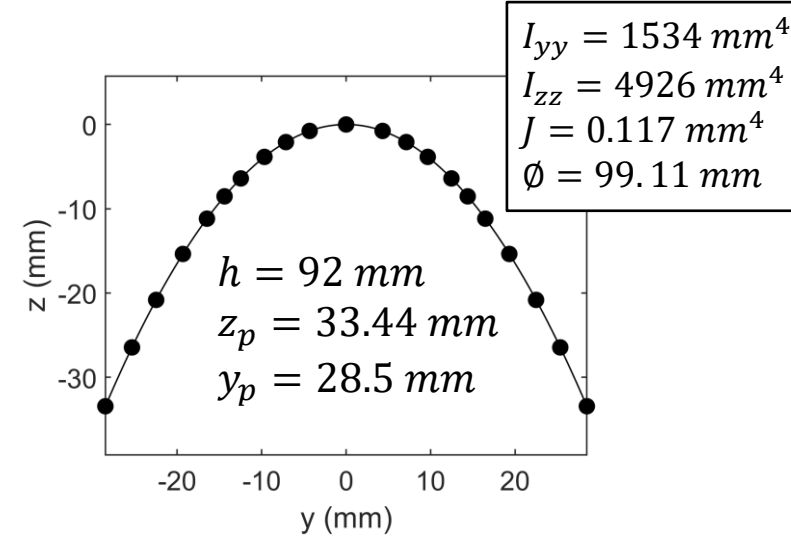
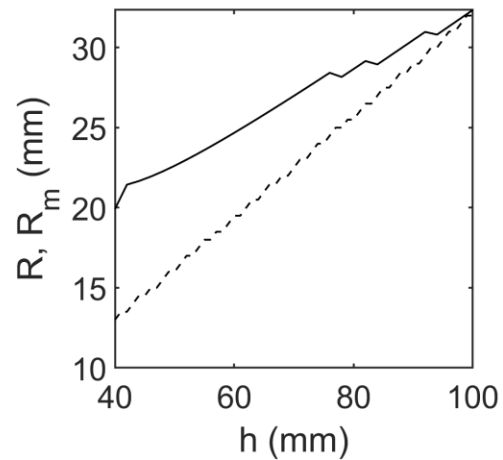
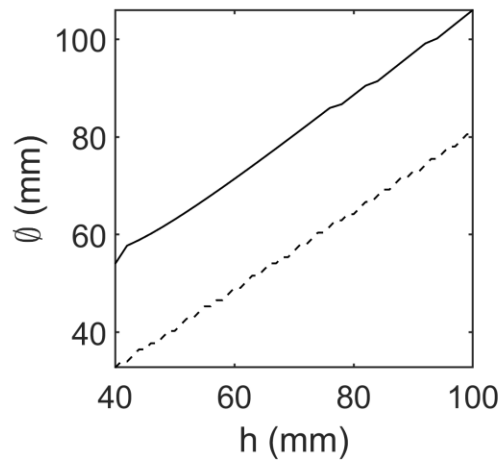
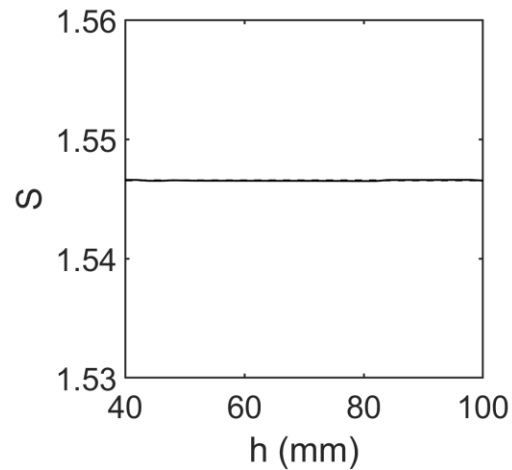
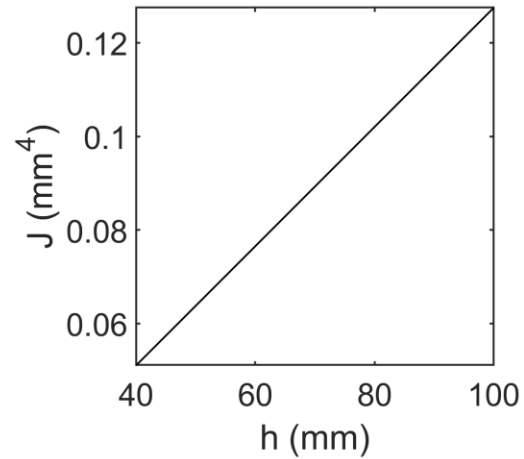
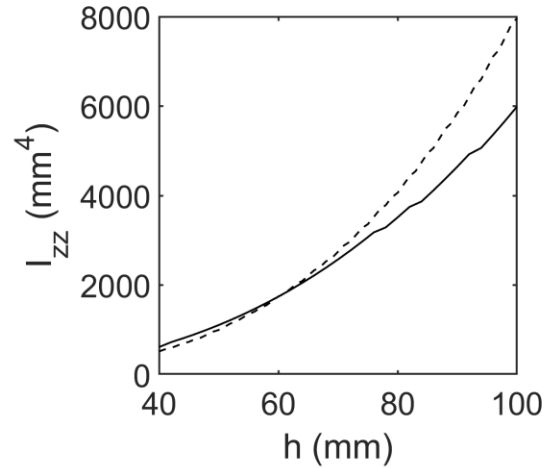
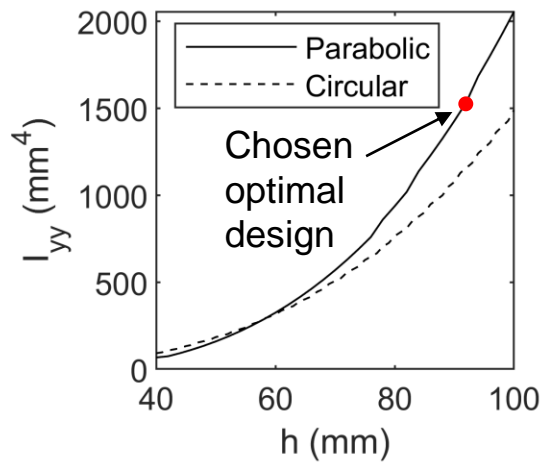
Material properties of thin-ply composites and adhesive

Label	Material Form	Fiber/Resin	$E_1$ (GPa)	$E_2$ (GPa)	$\nu_{12}$	$G_{12}$ (GPa)	Thickness $t$ ( $\mu\text{m}$ )
$C$	Unidirectional Carbon Fiber	MR60H/PMT-F7	144.1	5.2	0.335	2.8	40.0
$PW_C$	Plain Weave Carbon Fiber	M30S/PMT-F7	89.0	89.0	0.035	4.2	58.2
$A$	Hysol EA9696 Film Epoxy	N/A	2.14	2.14	0.030	0.62	85.0

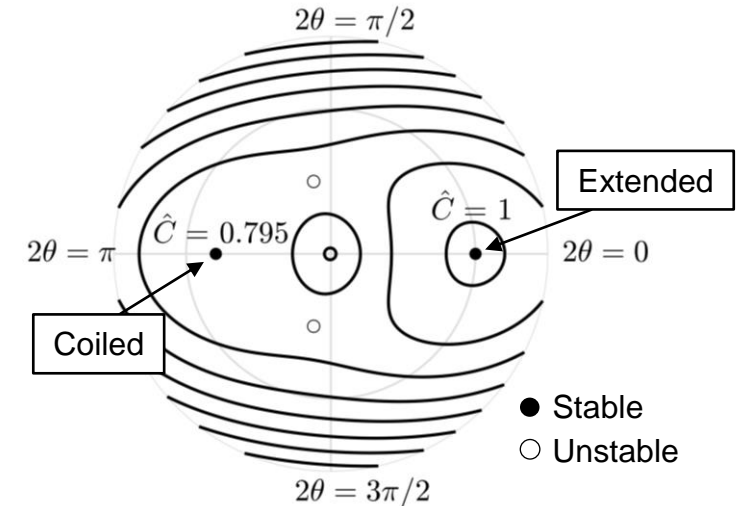


# Tape Spring Comparison and Optimal Design

Parabolic tape spring has superior stiffness properties ( $I_{yy}$ ) for larger  $h$ , but less favorable packaged volume ( $\phi$ ) when compared to circular tape spring



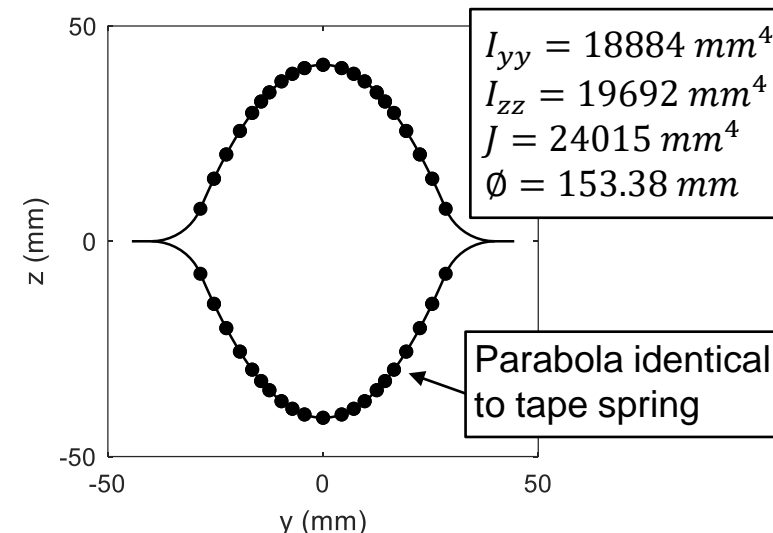
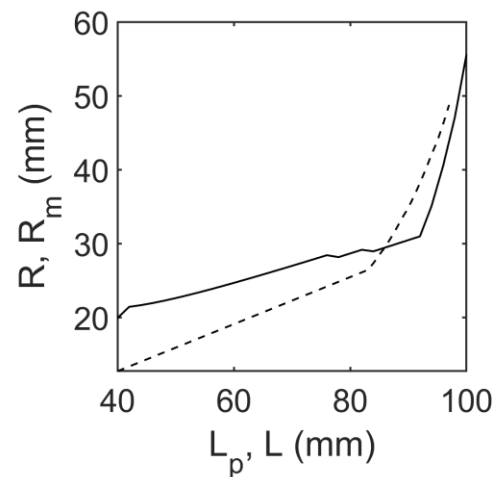
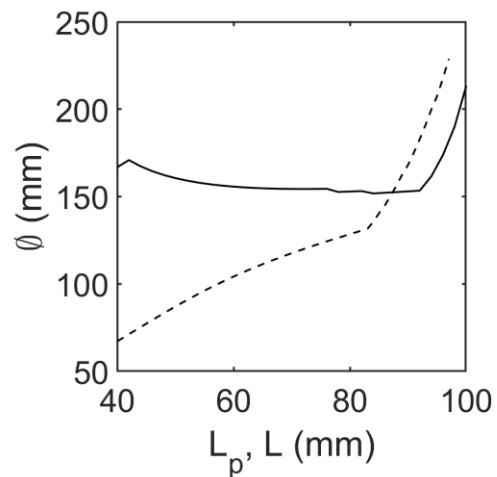
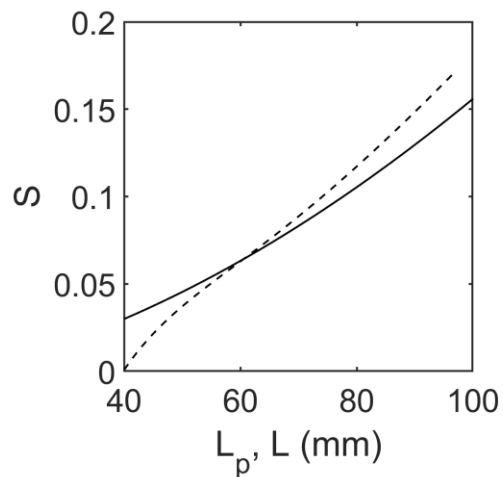
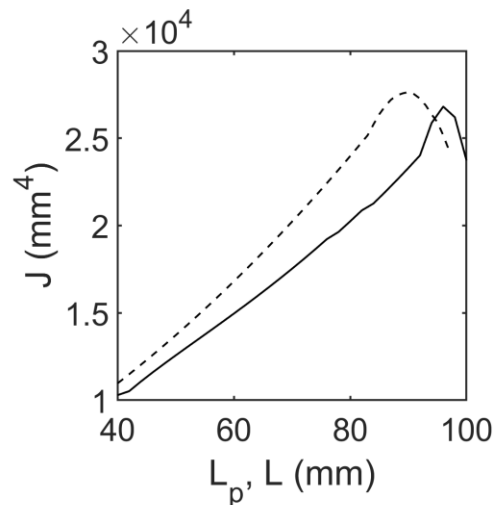
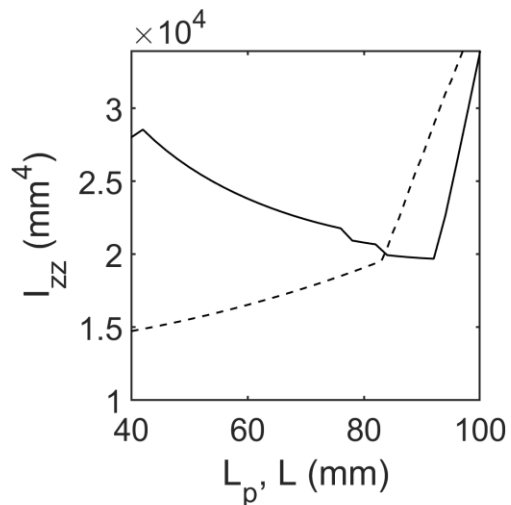
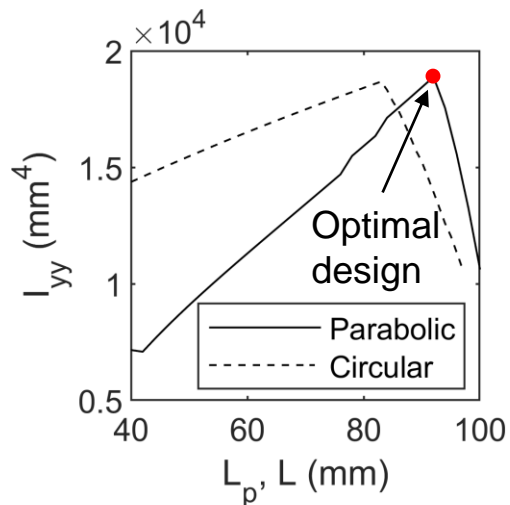
Optimal design cross-section



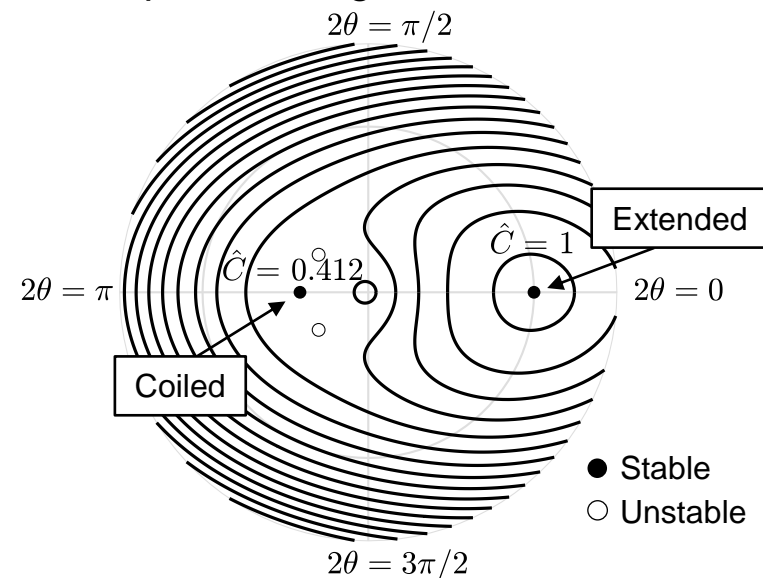
Polar contour plot of  $\hat{U}(\hat{C}, \theta)$

# CTM Boom Comparison and Optimal Design

Parabolic CTM has superior stiffness properties ( $I_{yy}$ ) and packaged volume ( $\phi$ ) for larger  $L_p, L$  and vice versa for smaller  $L_p, L$  when compared to circular CTM



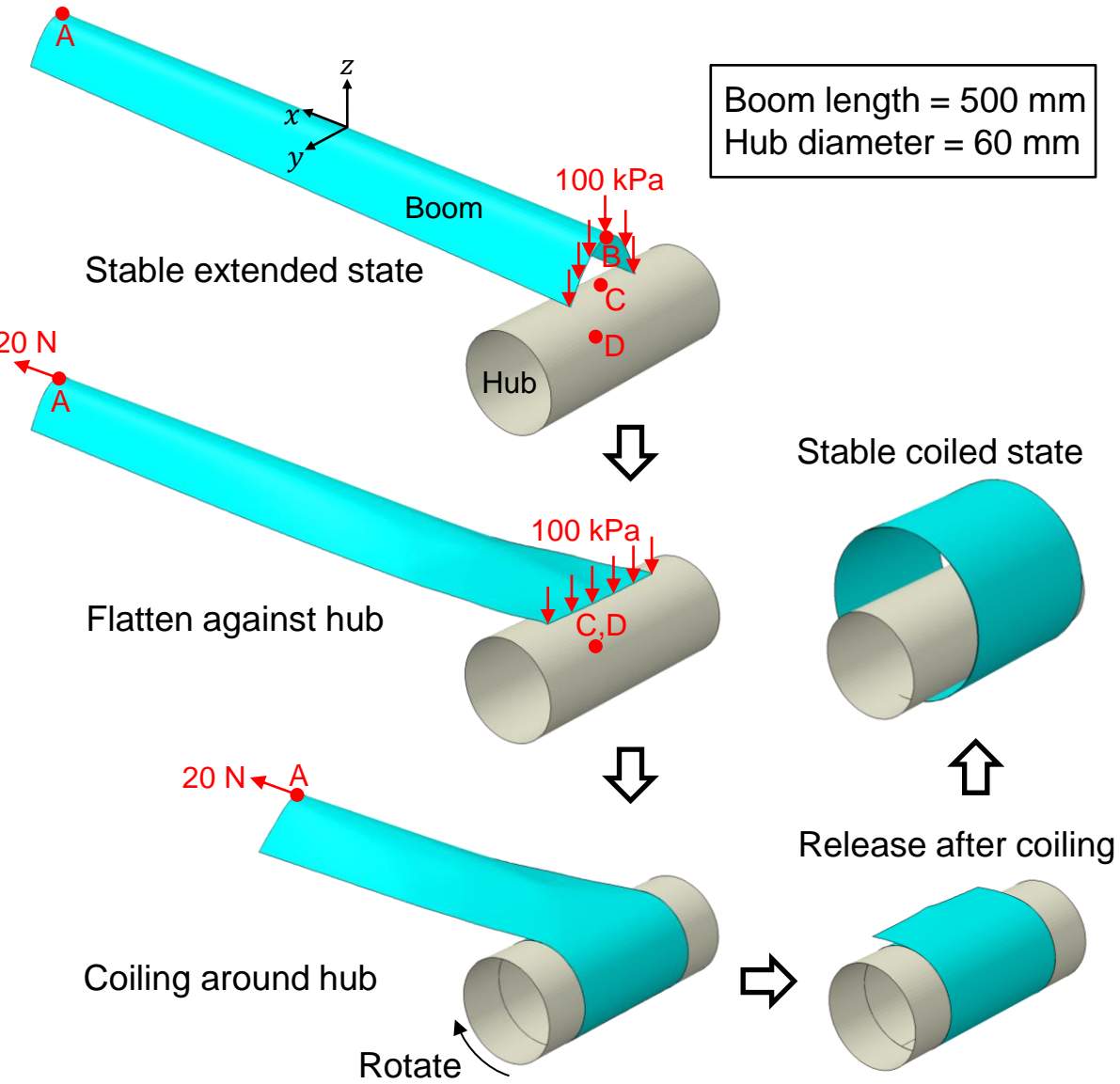
Optimal design cross-section



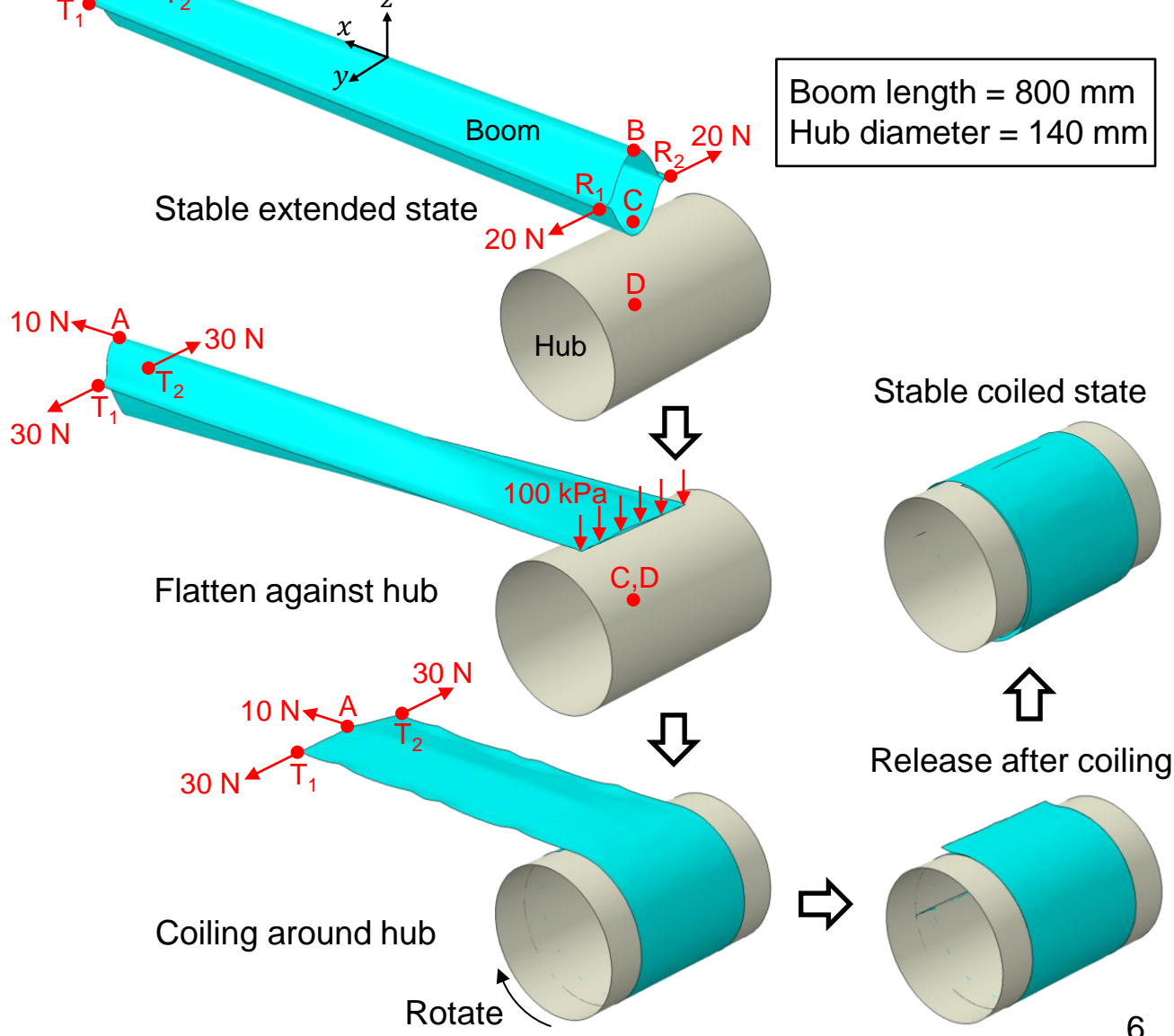
Polar contour plot of  $\hat{U}(\hat{C}, \theta)$

# Quasi-static FEA of Boom Coiling in Abaqus/Standard

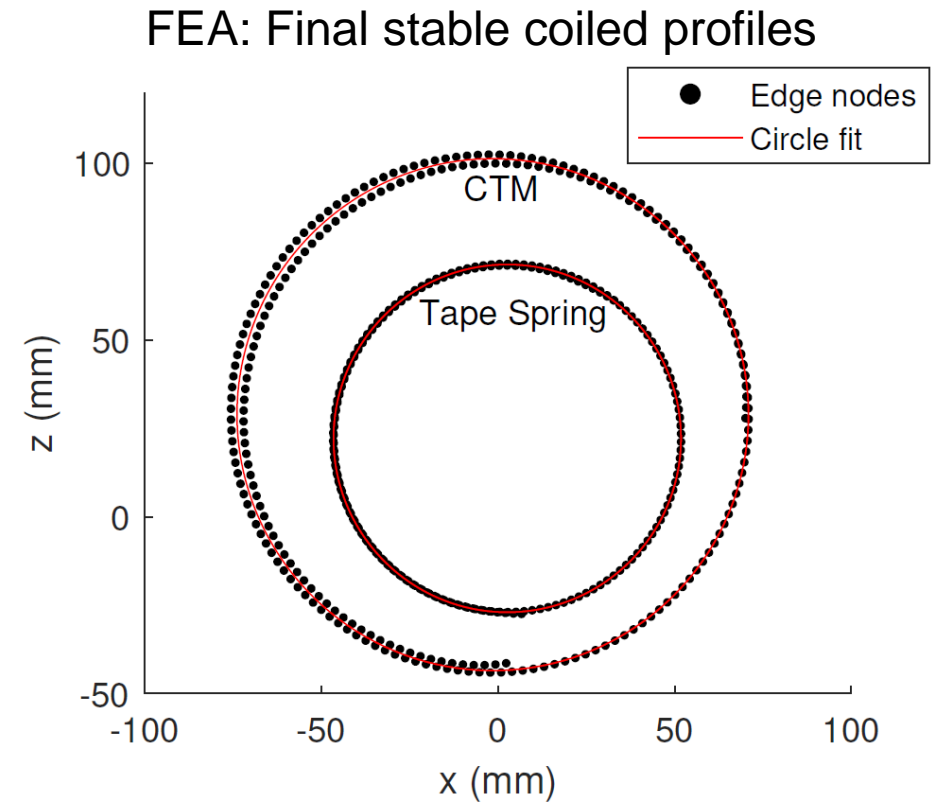
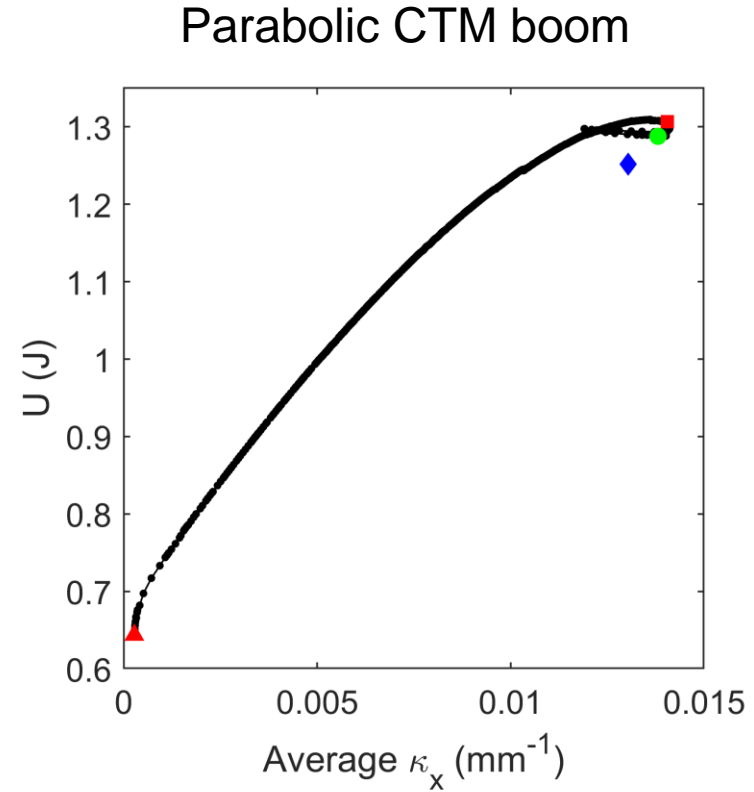
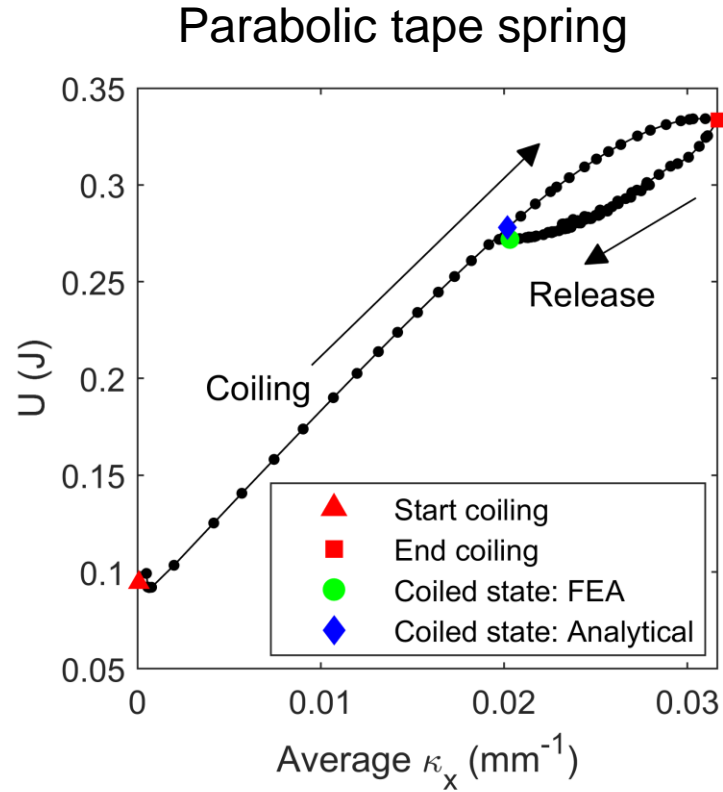
## Parabolic Tape Spring



## Parabolic CTM Boom



# FEA Results and Analytical Predictions



Model	Tape Spring $\phi$ (mm)	Tape Spring $U$ (J)	CTM $\phi$ (mm)	CTM $U$ (J)
Analytical	99.11	0.278	153.38	1.252
FEA	98.42	0.272	144.87	1.288
Percent Error	0.70%	2.16%	5.55%	2.88%

# Conclusions

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- Analytical approach developed to model stable coiled configuration of deployable composite booms with parabolic cross-sections
  - Discretized parabolic section into circular segments with biarc spline interpolation
  - Summed and minimized strain energy of every discretized segment to obtain equilibrium states
  - Implemented for both parabolic tape spring and CTM booms
- Parabolic booms generally found to have better stiffness performance at the cost of larger coiled diameter when compared to circular booms
  - This difference is more minor for the CTM than for the tape spring
- Finite element analysis of optimal parabolic tape spring and CTM booms verify analytical predictions of the stable diameter and strain energy of the coiled state
  - Future work will compare these predictions with experimental measurements from manufactured parabolic booms at NASA LaRC