

# Low-level jets and the convergence of Mars data assimilation algorithms

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## Key Points:

- Assimilating temperature data in UK-LMD Mars climate model weakens, shifts northern winter low-level jet, but has less effect on GFDL model
- Time mean flows generally agree better in the MACDA and EMARS reanalyses than in their associated control runs
- Reanalysis-control run mean state differences suggest that the EMARS control run has smaller biases than the MACDA control run

**Abstract**

Data assimilation is an increasingly popular technique in Mars atmospheric science, but its effect on the mean states of the underlying atmosphere models has not been thoroughly examined. The robustness of results to the choice of model and assimilation algorithm also warrants further study. We investigate these issues using two Mars general circulation models (MGCMs), with particular emphasis on zonal wind and temperature fields. When temperature retrievals from the Mars Global Surveyor Thermal Emission Spectrometer (TES) are assimilated into the U.K.-Laboratoire de Météorologie Dynamique (UK-LMD) MGCM to create the Mars Analysis Correction Data Assimilation (MACDA) reanalysis, low-level zonal jets in the winter northern hemisphere shift equatorward and weaken relative to a free-running control simulation from the same MGCM. The Ensemble Mars Atmosphere Reanalysis System (EMARS) reanalysis, which is also based on TES temperature retrievals, also shows jet weakening (but less if any shifting) relative to a control simulation performed with the underlying Geophysical Fluid Dynamics Laboratory (GFDL) MGCM. Examining higher levels of the atmosphere, monthly mean three-dimensional temperature and zonal wind fields are in generally better agreement between the two reanalyses than between the two control simulations. In conjunction with information about the MGCMs' physical parametrizations, intercomparisons between the various reanalyses and control simulations suggest that overall the EMARS control run is plausibly less biased (relative to the true state of the Martian atmosphere) than the MACDA control run. Implications for future observational studies are discussed.

**Plain Language Summary**

An increasingly popular way to study Martian weather and climate is to combine atmospheric temperature observations with a computer model (specifically, a global climate model). The process of combining model and observations is called “data assimilation”, and the resulting merged data set is called a “reanalysis”. One advantage of reanalyses is that they include variables (such as wind) that are not directly observed. For scientific and practical applications we want these variables to be reasonably accurate—however, it is not clear how well data assimilation algorithms compute them. Our study investigates this issue using two Mars reanalyses and two model simulations that do not assimilate temperature data. We focus on slowly-varying atmospheric phenomena (timescales from 10 Mars days to a season). Assimilating temperature data into two different global

49 climate models changes the strength and/or spatial pattern of east-west winds at low  
50 altitudes. Furthermore, monthly mean three-dimensional temperature and east-west wind  
51 fields agree better between reanalyses than between non-assimilating model simulations.  
52 This suggests that the data assimilation process is basically successful. One non-assimilating  
53 model simulation has less realistic representations of atmospheric physical processes than  
54 the other—we argue that this plausibly gives it larger biases relative to the true state  
55 of the atmosphere.

## 56 **1 Introduction**

57 Data assimilation for the Martian atmosphere has been a subject of research for  
58 more than two decades (Lewis & Read, 1995; Lewis et al., 1996; Houben, 1999) and re-  
59 cent years have seen a proliferation of reanalysis data sets (e.g., Montabone et al., 2014;  
60 Steele et al., 2014; Navarro et al., 2017; Holmes et al., 2018; Greybush, Kalnay, et al.,  
61 2019; Holmes et al., 2019, 2020). The Martian data assimilation problem must be solved  
62 with fewer and different observations than its terrestrial counterpart: to date, Mars re-  
63 analysis efforts have been highly dependent on infrared temperature retrievals (or at least  
64 their underlying radiances) in ways that Earth reanalyses are not (e.g., Lee et al., 2011;  
65 Montabone et al., 2014; Greybush, Kalnay, et al., 2019), (cf. Gelaro et al., 2017; Hers-  
66 bach et al., 2020). This is because other dynamical information, such as surface pres-  
67 sure or wind observations, is available with only very limited spatial coverage (Hinson,  
68 2008; Martínez et al., 2017).

69 From a dynamical perspective, atmospheric temperature structure is most clearly  
70 informative about wind fields via thermal wind or similar balance arguments (e.g., Ban-  
71 field et al., 2004). However, thermal wind is at best a theory of the vertical wind shear—  
72 it cannot constrain the absolute wind at the surface and is also expected to break down  
73 in the tropics. Thus although the large-scale near-surface and tropical atmospheric cir-  
74 culations are basic features of the Martian climate system, it is not obvious how well they  
75 are estimated by data assimilation systems (Lewis et al., 1996, 1997; Hoffman et al., 2010).  
76 Nor are the simulations of these features by free-running Mars general circulation mod-  
77 els (MGCs) easy to validate.

78 Here we begin to address these product quality issues by investigating how assim-  
79 ilating temperature retrievals into MGCs changes their climatological mean states, with

80 particular emphasis on zonal winds. To explore the robustness of our results, we exam-  
 81 ine two different reanalyses and their associated control simulations—the control sim-  
 82 ulations differ from the reanalyses primarily by not assimilating temperature retrievals.  
 83 The use of two reanalysis–control run pairs also allows us to expand on previous inves-  
 84 tigations (Waugh et al., 2016; Greybush, Gillespie, & Wilson, 2019) of whether differ-  
 85 ent data assimilation systems are able to converge on a single atmospheric state. Ulti-  
 86 mately we are able to draw some tentative conclusions about the quality of the reanal-  
 87 yses and control simulations, even without using any independent validation data.

88 The main body of this paper is divided into four major sections. We summarize  
 89 the reanalysis data sets and control simulations in section 2. Results on the low-level zonal  
 90 mean jets are presented in section 3, while the vertical and meridional structure of the  
 91 zonal mean temperature and zonal wind fields is examined in section 4. The extent to  
 92 which data assimilation converges the time mean states of the two MGCMs is addressed  
 93 more formally in section 5. A summary and discussion of implications for future obser-  
 94 vational work concludes the paper, and three appendices present results of sensitivity  
 95 tests and additional statistical details.

## 96 **2 Reanalysis and control simulation data sets**

97 We use the Mars Analysis Correction Data Assimilation version 1.0 (MACDA, Montabone  
 98 et al., 2014) and Ensemble Mars Atmosphere Reanalysis System version 1.0 (EMARS,  
 99 Greybush, Kalnay, et al., 2019) reanalyses, both of which assimilate temperature retrievals  
 100 from the Mars Global Surveyor Thermal Emission Spectrometer (TES, Conrath et al.,  
 101 2000). This gives the two reanalyses similar temporal extents: MY24  $L_s$  141° (103°) to  
 102 MY27  $L_s$  86° (102°) for MACDA (EMARS), where the Mars years (MY) and seasonal  
 103 dates are defined using the Clancy et al. (2000) calendar. However, occasional gaps in  
 104 the availability of TES retrievals mean that the reanalyses are not constrained by ob-  
 105 servations throughout the full lengths of these periods. Ten intervals in which the reanal-  
 106 yses are thought to be poorly constrained are excluded from our study, generally follow-  
 107 ing Table S1 of Mooring and Wilson (2015). (Two more such intervals occur near the  
 108 beginning of the EMARS data set, but are rendered irrelevant by our choice to ignore  
 109 the period prior to MY24  $L_s$  135°. We also do not use the MY28–33 segment of EMARS  
 110 based on Mars Climate Sounder retrievals, as MACDA does not cover this period.)

111 The two reanalyses are underpinned by substantially different MGCMs and data  
 112 assimilation algorithms. MACDA is based on the U.K.-Laboratoire de Météorologie Dy-  
 113 namique (UK-LMD) MGCM with a spectral dynamical core (Forget et al., 1999). The  
 114 MACDA version of this model was integrated with a horizontal resolution of T31 and  
 115 25 sigma levels (Montabone et al., 2006), and the MACDA output data are available on  
 116 a  $5^\circ$  latitude-longitude grid. EMARS uses a version of the Geophysical Fluid Dynam-  
 117 ics Laboratory (GFDL) MGCM with a finite-volume dynamical core on a latitude-longitude  
 118 grid (e.g., Hoffman et al., 2010). The horizontal resolution of this model is  $\sim 5^\circ$  latitude  
 119  $\times 6^\circ$  longitude, and it has 28 hybrid sigma-pressure levels.

120 MACDA assimilates temperature retrievals using the analysis correction method  
 121 (Lewis et al., 2007), which updates the model state every dynamical timestep (480 times  
 122 per sol—a sol is a Martian mean solar day,  $\sim 1.03$  Earth days). In contrast, EMARS as-  
 123 similates temperature retrievals 24 times per sol using an ensemble Kalman filter (Hoffman  
 124 et al., 2010; Zhao et al., 2015). The MACDA data set is available 12 times per sol (Montabone  
 125 et al., 2014), while EMARS analyses are available 24 times per sol (Greybush, Kalnay,  
 126 et al., 2019). Note that the publicly available EMARS output consists of both analyses  
 127 and short (1 Mars hour) background forecasts—although many atmospheric variables  
 128 are available as forecasts only, the pressure, temperature, and wind variables needed for  
 129 this study are available as both analyses and forecasts and we opt to use the former as  
 130 they are (slightly) more observationally constrained.

131 The free-running control simulations are essentially identical to their associated re-  
 132 analyses, except that by definition they do not assimilate temperature retrievals. It is  
 133 important to emphasize that the EMARS control simulation used in this study (version  
 134 1.02) is substantially longer than the (version 1.0) control simulation described in Greybush,  
 135 Kalnay, et al. (2019), which covered only  $\sim 1$  Mars year of the TES era. The MACDA  
 136 and EMARS control simulations will hereinafter be referred to as MCTRL and ECTRL,  
 137 respectively.

138 Even though the control simulations are not constrained by temperature retrievals,  
 139 they can still be identified with specific Mars years and seasons because their dust fields  
 140 are time-dependent and constrained by observations. For MACDA and MCTRL, TES-  
 141 based column opacities are assimilated using the analysis correction method (Montabone  
 142 et al., 2014)—however, this particular version of the UK-LMD MGCM does not trans-

143 port dust so the “forecast model” underlying the dust opacity assimilation is simply per-  
 144 sistence. Given the analyzed column opacities, MACDA and MCTRL distribute the opac-  
 145 ity in the vertical using a Conrath-like distribution (Conrath, 1975; Montabone et al.,  
 146 2006). In contrast, the three-dimensional dust fields in EMARS and ECTRL evolve un-  
 147 der the influences of wind advection and sedimentation (Greybush, Kalnay, et al., 2019).  
 148 Agreement with observational data is maintained by nudging the column opacities to-  
 149 wards the time-dependent dust maps of Montabone et al. (2015), which can also be con-  
 150 sidered a simple form of data assimilation. Note that the Montabone et al. (2015) dust  
 151 maps for the period in question are based on retrievals not only from TES, but also from  
 152 the Thermal Emission Imaging System (THEMIS) on Mars Odyssey.

### 153 **3 Low-level zonal jets**

154 We begin our comparison of the reanalysis and control run circulations by exam-  
 155 ining seasonally-resolved zonal mean zonal winds on the  $\sigma = 0.991$  ( $\sim 90$  m above ground)  
 156 level in MACDA and MCTRL. Northern (southern) winter solstice occurs at  $L_s$   $270^\circ$   
 157 ( $90^\circ$ ), and focusing initially on the northern hemisphere during its local winter we see  
 158 that the peak strength of the extratropical zonal jet is lower in MACDA (Figure 1a) than  
 159 in MCTRL (Figure 1b). The control run jet also tends to be farther poleward than its  
 160 reanalysis counterpart. This point is clarified in Figure 1c, which shows the difference  
 161 between the MCTRL and MACDA fields. Figure 1c also reveals qualitatively similar be-  
 162 havior in the southern hemisphere near local winter solstice, which was masked in the  
 163 previously mentioned figure panels by the usually weaker southern winter extratropical  
 164 near-surface jet. Generally similar wind results are found on the  $\sigma = 0.900$  ( $\sim 1.1$  km  
 165 above ground) level (Appendix A, Figure A1). Furthermore, the MACDA–MCTRL jet  
 166 differences are associated with differences in zonal mean surface pressure (Figure 1e). The  
 167 differences in surface pressure shown in Figure 1e are qualitatively consistent with geostrophic  
 168 balance and the wind differences shown in Figure 1c, although the surface geostrophic  
 169 zonal wind differences are often stronger than the actual wind differences at  $\sigma = 0.991$   
 170 (Figure 1d).

171 A comparable analysis of EMARS and ECTRL yields notably different results (Fig-  
 172 ure 2). There is a tendency for the assimilation of temperature data to weaken the ex-  
 173 tratropical winter jets near  $60^\circ$  latitude in both hemispheres (Figure 2a-c). However, in  
 174 contrast to the situation with the UK-LMD MGCM, data assimilation has no obvious

175 effect on the position of the zonal jets—the clear extratropical dipolar structures seen  
 176 in the MACDA–MCTRL jet difference field (Figure 1c) are absent or greatly weakened  
 177 in its EMARS–CTRL counterpart (Figure 2c). The maximum magnitudes of control–  
 178 reanalysis northern winter jet differences appear to be smaller for EMARS–CTRL than  
 179 for MACDA–MCTRL (Figures 1c and 2c). As with the UK-LMD MGCM, comparable  
 180 results are found when winds are evaluated on a model level with  $\sigma \approx 0.905$  ( $\sim 1.0$  km  
 181 above ground, Figure A2). Interestingly, the data assimilation effect on surface pressure  
 182 gradients has a different seasonality in the GFDL MGCM than in the UK-LMD MGCM—  
 183 for example, the structure of the EMARS–CTRL northern hemisphere pressure differ-  
 184 ence field (Figure 2e) changes substantially during the MY24 and MY25  $L_s$   $225^\circ$ – $315^\circ$   
 185 seasonal intervals but the corresponding MACDA–MCTRL field does not (Figure 1e).  
 186 Furthermore, even the typical sign of the data assimilation effect on northern hemisphere  
 187 summer pressure gradients differs between the GFDL and UK-LMD MGCMs (Figure 1e  
 188 and 2e). However, as for MACDA–MCTRL the EMARS–CTRL surface geostrophic  
 189 wind differences (Figure 2d) effectively capture the actual patterns of low-level zonal wind  
 190 differences.

191 Finally, we note in passing a previously undocumented and likely artificial inter-  
 192 annual difference between MY26 and the other Mars years of EMARS. Starting near MY26  
 193  $L_s \sim 0^\circ$  and continuing to  $L_s \sim 105^\circ$ , the zonal near-surface winds are typically westerly  
 194 at the equator (Figures 2a and A2a). This is in stark contrast to the winds at this sea-  
 195 son in MY25 and MY27 of EMARS, and in all Mars years of CTRL (Figures 2b and A2b).  
 196 The abrupt transition to easterly winds near MY26  $L_s$   $105^\circ$  suggests a mechanism for  
 197 this curious behavior: at approximately that time, the TES instrument was returned to  
 198 its low spectral resolution (nominally  $10 \text{ cm}^{-1}$ , Conrath et al. (2000)) observing mode  
 199 after having spent roughly one Mars year generally in the high spectral resolution (nom-  
 200 inally  $5 \text{ cm}^{-1}$ ) mode (Montabone et al., 2014; Holmes et al., 2020). Previous work has  
 201 associated this time-dependent spectral resolution of the observations with spurious in-  
 202 terannual variability (Wilson et al., 2014). Indeed the high-resolution observing mode  
 203 received little or no use in  $L_s \sim 0^\circ$ – $105^\circ$  of the other Mars years, consistent with the idea  
 204 that the anomalous MY26  $L_s \sim 0^\circ$ – $105^\circ$  EMARS winds are a result of that period’s dif-  
 205 ferent spectral resolution. However, further work is needed to determine how the appar-  
 206 ent effect emerges from the assimilated temperature retrievals, which observing mode  
 207 yields more realistic results, why there is no analogous effect in MACDA, and whether

208 the abrupt cutoff of the westerlies is also influenced by a transition between EMARS pro-  
 209 duction streams near MY26  $L_s$  105° (Greybush, Kalnay, et al., 2019).

#### 210 **4 Latitude-pressure structure of zonal mean fields**

211 Unfortunately, there are very few observations directly sensitive to wind in the lower  
 212 atmosphere of Mars—anemometers on a handful of landers (e.g., Martínez et al., 2017),  
 213 geostrophic winds from radio occultations (e.g., Hinson et al., 1999), and arguably cloud-  
 214 tracked winds from orbiter imagery (Wang & Ingersoll, 2003). The potential for a di-  
 215 rect validation of reanalysis-based winds is thus limited. However, we can much more  
 216 readily evaluate the extent to which MACDA and EMARS converge to the same solution—  
 217 as they should, to the extent that the assimilated data can effectively constrain and cor-  
 218 rect biases in the MGCM states. Although our ultimate goal in this paper is to conduct  
 219 a novel intercomparison of the three-dimensional time mean states of MACDA, EMARS,  
 220 and their control simulations, we will lead into such an analysis with an examination of  
 221 zonally-averaged time mean fields.

222 Because of the strong seasonality of the Martian atmosphere, for this analysis we  
 223 will divide the Martian annual cycle into four seasons of nearly equal length and essen-  
 224 tially centered on the solstices and equinoxes. More specifically, we define boreal win-  
 225 ter, spring, summer, and autumn as  $L_s$  216°–322°, 322°–46.7°, 46.7°–123°, and 123°–  
 226 216°. The 2.5 Mars year interval from MY24  $L_s$  216° to MY27  $L_s$  46.7° then consists  
 227 of exactly 10 seasons—three (two) realizations each of boreal winter and spring (sum-  
 228 mer and autumn). In Figures 1 and 2, the beginning and end of this 2.5 Mars year pe-  
 229 riod are marked with solid red lines and the borders between individual seasons are marked  
 230 with dashed red lines.

231 An initial examination of the vertical and meridional structures of zonal mean tem-  
 232 perature and zonal wind fields suggests that assimilating TES temperature retrievals brings  
 233 the UK-LMD and GFDL MGCM states closer together. Results for  $L_s$  123°–216° and  
 234 216°–322° are shown in Figure 3. Although ECTRL is able to basically reproduce the  
 235 seasonal variations seen in EMARS (black contours), the disagreements (red and blue  
 236 shading) between MCTRL and ECTRL (Figure 3a, c, e, g) tend to be larger than those  
 237 between MACDA and EMARS except possibly for the  $L_s$  216°–322° zonal winds (Fig-  
 238 ure 3b, d, f, h). While MACDA is often warmer than EMARS (Figure 3b, f), maximum



239 temperature disagreements for these seasons are larger in the free-running control sim-  
 240 ulations than in the reanalyses: for example, MCTRL can be more than 20 K warmer  
 241 than ECTRL in the polar regions (Figure 3a, e). These patterns of temperature disagree-  
 242 ment are associated with jet disagreement due to thermal wind balance—such disagree-  
 243 ments are often but not always larger in the control simulations, especially in the extra-  
 244 tropics for  $L_s$  123°–216° and in high southern latitudes for  $L_s$  216°–322° (Figure 3c, d,  
 245 g, h). A tendency of temperature assimilation to converge the UK-LMD and GFDL MGCM  
 246 mean states is also seen for the other two seasons (Figure 4). Although the patterns of  
 247 difference between MCTRL and ECTRL are much alike in the two equinox seasons (Fig-  
 248 ures 3e, g and 4e, g), they appear to disagree more strongly during boreal summer than  
 249 during boreal winter (Figures 3a, c and 4a, c).

## 250 5 Convergence of three-dimensional mean fields

251 We can obtain more systematic and quantitative results by computing root mean  
 252 square (RMS) differences between the various free-running MGCM and reanalysis data  
 253 sets. For some three-dimensional time mean field  $F$ , let us denote the (area- and mass-  
 254 weighted, assuming hydrostatic balance) RMS difference between data sets  $X$  and  $Y$  as  
 255  $rmsd(X, Y)$ . More precisely, we define  $rmsd(X, Y)$  by

$$256 \quad rmsd(X, Y) = \sqrt{\frac{\int_{\phi_R} \int_0^{2\pi} \int_{p_t}^{p_b} (F_X - F_Y)^2 dp (\cos \phi d\lambda) d\phi}{\int_{\phi_R} \int_0^{2\pi} \int_{p_t}^{p_b} dp (\cos \phi d\lambda) d\phi}} \quad (1)$$

257 where  $F_X$  and  $F_Y$  are field  $F$  from data sets  $X$  and  $Y$ ,  $p_t$  and  $p_b$  are the pressures of the  
 258 top and bottom of the region of interest, and  $\phi_R$  denotes the latitude range(s) of interest—  
 259 the domain over which the meridional integral is taken need not be continuous.

260 It is worth explaining our definition of the time mean. Our interest is in the mean  
 261 state of the atmosphere, so the averaging period must be chosen long enough to aver-  
 262 age out the transient eddies. However, an excessively long averaging period would need-  
 263 lessly erase information about any shorter-term changes in the mean state. We will again  
 264 analyze the 2.5 Mars year interval from MY24  $L_s$  216° to MY27  $L_s$  46.7° and will at-  
 265 tempt to balance these two competing goals by dividing each of the 10 seasons defined  
 266 in section 4 into four months with approximately equal lengths of  $\sim 41.8$  sols. We then  
 267 take time means over each of the 40 such months—although because we exclude peri-  
 268 ods not well constrained by TES data (section 2, Figures 1 and 2), four of these monthly  
 269 means are based on less than 30 sols of data apiece. Time averaging over  $\sim 41.8$ -sol months

270 should suffice to suppress most transient eddy variability (e.g., Banfield et al., 2004; Moor-  
 271 ing & Wilson, 2015)—to the extent that this goal is achieved, any improvement in the  
 272 agreement of monthly means due to assimilation of TES temperature retrievals should  
 273 come from correcting the MGCMs’ time mean biases and not from synchronizing their  
 274 unforced variability. Indeed, repeating the analyses with a month redefined as one-third  
 275 of a season ( $\sim 55.7$  sols) did not qualitatively change the main results (Appendix B).

276 We evaluate equation 1 for each of the 40 months for two choices of  $F$ , 10 (over-  
 277 lapping) spatial regions of interest, and all six possible unique pairs of data sets. The  
 278 fields used are temperature and zonal wind, and  $p_t$  is either 0.1 or 3 hPa.  $p_b$  is a spatially-  
 279 varying monthly mean surface pressure. Specifically, for each location it is computed as  
 280 the minimum of the four individual data set (MACDA, MCTRL, EMARS, ECTRL) monthly  
 281 means after the data sets have all been interpolated to a single grid. The choice of  $p_t = 0.1$   
 282 hPa excludes altitudes above those directly influenced by TES temperature profile as-  
 283 simulation (Lewis et al., 2007), while using  $p_t = 3$  hPa emphasizes the lower part of the  
 284 atmosphere for greater comparability to the results in section 3.

285 The 10 spatial regions are formed by combining the two pressure ranges with five  
 286 latitude ranges: global ( $90^\circ\text{S}$ – $90^\circ\text{N}$ ), tropics ( $30^\circ\text{S}$ – $30^\circ\text{N}$ ), northern and southern hemi-  
 287 sphere extratropics ( $30^\circ$ – $90^\circ\text{N}$  and  $30^\circ$ – $90^\circ\text{S}$ , respectively) and all extratropics (the union  
 288 of northern and southern extratropics). While the various latitude ranges are clearly not  
 289 all independent, using multiple latitude bands is helpful for checking the robustness of  
 290 the results and investigating whether the effectiveness of temperature assimilation in con-  
 291 verging different MGCM mean states varies meridionally.

292 By comparing the relative sizes of the different  $rmsd(X, Y)$  we provide support for  
 293 two major claims:

- 294 1. Assimilating temperature retrievals into the MGCMs brings their monthly mean  
 295 states into better agreement
- 296 2. ECTRL is plausibly less biased (with respect to the true monthly mean states of  
 297 the Martian atmosphere) than MCTRL

298 Knowledge of the actual values of the  $rmsd(X, Y)$  is not necessary to support these claims—  
 299 instead, the results are presented in Table 1 in terms of the numbers of months (out of  
 300 40 possible) for which various inequalities involving the six  $rmsd(X, Y)$  are satisfied. For

compactness of notation, in these inequalities we will denote MACDA, MCTRL, EMARS, and ECTRL as  $M_R$ ,  $M_C$ ,  $E_R$ , and  $E_C$ , respectively.

We support the first claim by examining the inequality

$$rmsd(M_C, E_C) < rmsd(M_R, E_R) \quad (2)$$

Physically, this inequality will be satisfied if the free-running control simulations are in *better* agreement than the reanalyses are (for the given month, field, and region of interest). If this is the case, it means that assimilating TES temperature retrievals does *not* systematically bring the monthly mean states of the UK-LMD and GFDL MGCMs together—contrary to the impression created by Figures 3 and 4.

In practice, equation 2 is generally not satisfied—Table 1 indicates that equation 2 is true in at most 18 and often many fewer of the 40 total months. If consideration is restricted to the global or all-extratropics meridional regions, the inequality is satisfied for at most four months. These results strongly suggest that assimilation of the same temperature retrievals into UK-LMD and GFDL MGCM simulations tends to bring together not merely their instantaneous weather conditions, but also their climates as measured by monthly means—a more formal statistical analysis suggests that if data assimilation had no effect whatsoever on the MGCMs’ monthly mean states, it is unlikely that these results would have been obtained (Appendix C). Perhaps unsurprisingly, the tendency for data assimilation to converge the monthly means appears stronger for temperature than for zonal wind—for a given region, equation 2 is always satisfied in at least as many months for zonal wind as for temperature.

We begin to support the second claim by examining

$$rmsd(M_R, M_C) < rmsd(E_R, E_C) \quad (3)$$

If satisfied, this inequality indicates that the UK-LMD reanalysis–control run pair is in better agreement than the GFDL reanalysis–control run pair. Across all of the different field–region combinations equation 3 is satisfied in as many as 26 months (Table 1). However if the tropical zonal wind cases are excluded, it is never satisfied in more than 16 months. This is evidence (albeit not always very strong) that EMARS and ECTRL are generally in better agreement than MACDA and MCTRL, at least outside the tropics. One possible explanation for this apparent result is that ECTRL is less biased (relative to the truth) than MCTRL. However, we cannot immediately dismiss the possi-

332 ability that the ECTRL biases are comparable to or larger than those of MCTRL but that  
 333 the EMARS ensemble Kalman filter is simply less effective than the MACDA analysis  
 334 correction scheme at adjusting the mean state of a biased MGCM.

335 We can separate these possibilities using the additional inequalities

$$336 \quad rmsd(E_R, M_C) < rmsd(E_R, E_C) \quad (4)$$

337 and

$$338 \quad rmsd(M_R, E_C) < rmsd(M_R, M_C) \quad (5)$$

339 The former (latter) characterizes how well the two control simulations verify against EMARS  
 340 (MACDA). If ECTRL were clearly superior to MCTRL (in the sense of verifying bet-  
 341 ter against both reanalyses) then equation 5 would often be satisfied and equation 4 would  
 342 not be. Likewise, if MCTRL were superior equation 4 would often be satisfied and equa-  
 343 tion 5 would not be. Alternatively, if both reanalyses were strongly biased toward their  
 344 underlying MGCMs both equation 4 and equation 5 would be only rarely satisfied.

345 The results support the idea that ECTRL is generally less biased than MCTRL—  
 346 equation 4 is satisfied in 7 months at most but equation 5 is satisfied in as many as 28  
 347 months (Table 1). Furthermore, for most field–region combinations equation 5 is satis-  
 348 fied in more months than equation 4—the exceptions are the tropical zonal wind cases.  
 349 Statistical analysis suggests that these results—at least for the spatial regions that have  
 350  $p_t = 0.1$  hPa and are not wholly tropical—are unlikely to be explicable as pure inter-  
 351 val variability. In practice, this implies that ECTRL and MCTRL have distinct climates  
 352 and are not simply different realizations of internal variability from a single climate (Ap-  
 353 pendix C). Note also that for certain field–region combinations both equation 4 and equa-  
 354 tion 5 are rarely or never satisfied, consistent with the idea that the reanalyses have some  
 355 tendency to inherit the climates of their underlying MGCMs. This phenomenon is par-  
 356 ticularly prominent in the tropics.

357 Indeed, there are physical reasons to expect ECTRL to be less biased than MC-  
 358 CTRL. Although both control simulations have their column dust opacities constrained  
 359 to follow similar observational data sets, the constraint method used for ECTRL is more  
 360 clearly consistent with the physics of dust transport in the atmosphere as described in  
 361 section 2. Previous work suggests that this should yield more realistic temperatures (Wilson  
 362 et al., 2008). Also, the Martian atmosphere features water ice clouds which are thought

363 to substantially affect the thermal structure and circulation (e.g., Wilson et al., 2008;  
 364 Mulholland et al., 2016). Parameterizations of the radiative effects of water ice clouds  
 365 have been developed for both the GFDL and UK-LMD MGCMs (e.g., Hinson & Wil-  
 366 son, 2004; Mulholland et al., 2016). They are used in the EMARS–CTRL version of  
 367 the GFDL model, but not in the MACDA–CTRL version of the UK-LMD model (Forget  
 368 et al., 1999; Montabone et al., 2014; Greybush, Kalnay, et al., 2019). Since the physi-  
 369 cal parameterizations of CTRL are a priori more realistic than those of MCTRL, it would  
 370 be unsurprising if the output of the former simulation were closer to the truth.

## 371 **6 Summary and discussion**

372 We have presented a systematic intercomparison of slowly-varying components of  
 373 the circulation in two Mars reanalyses and their associated free-running control simu-  
 374 lations. The reanalyses assimilate essentially the same temperature retrievals, but via  
 375 very different algorithms and into two distinct Mars general circulation models. Never-  
 376 theless, the three-dimensional monthly mean temperature and zonal wind fields are gen-  
 377 erally in better agreement for the reanalyses than for the control simulations. This sug-  
 378 gests a certain robustness of Mars reanalyses to the choice of MGCM and assimilation  
 379 algorithm, in agreement with Waugh et al. (2016) and Greybush, Gillespie, and Wilson  
 380 (2019).

381 We devote particular attention to the low-level extratropical zonal mean zonal jets.  
 382 Assimilating temperature retrievals into the UK-LMD MGCM to create MACDA tends  
 383 to weaken the northern hemisphere winter jet and to shift it equatorward. Roughly sim-  
 384 ilar shift behavior is found for southern hemisphere winter as well. Weakening of low-  
 385 level winter jets also results when temperatures are assimilated into the GFDL MGCM,  
 386 although the overall effect is more subtle than for the UK-LMD MGCM. Furthermore,  
 387 changes in surface pressure gradients occur in response to temperature assimilation—  
 388 these are qualitatively consistent with geostrophic balance, most evidently for northern  
 389 hemisphere winter in the UK-LMD MGCM.

390 Finally, we have produced evidence that (at least in an average sense) the EMARS  
 391 control simulation is less biased than the MACDA control simulation. Note that this re-  
 392 sult is not guaranteed to hold for individual meridional or vertical regions, such as the

393 tropics or pressures  $>3$  hPa—indeed, our results are consistent with the idea that the  
 394 reanalyses inherit biases from their underlying MGCMs for at least some regions and fields.

395 Our results suggest that the low-level zonal jets of MGCMs may be biased and that  
 396 similar biases might be shared across multiple MGCMs. Studies of low-level circulations  
 397 in the Martian atmosphere would thus benefit from collection of additional data more  
 398 sensitive to near-surface wind or pressure fields. Technological options for collecting such  
 399 data include lander networks (e.g., Harri et al., 2017), radio occultation constellations  
 400 (e.g., Kursinski et al., 2012), and orbiting wind lidars (e.g., Cremons et al., 2020). Al-  
 401 ternatively, it may be possible to derive improved constraints on low-level zonal geostrophic  
 402 winds from existing radio occultation and/or lander data. Further MGCM experiments  
 403 and reanalysis diagnostic studies are also needed to understand the origins of the MGCM-  
 404 reanalysis and inter-reanalysis disagreements documented here.

## 405 **Appendix A Sensitivity of low-level jets to altitude**

406 Our primary examination in section 3 of the seasonal and meridional variations of  
 407 low-level zonal jets evaluated them on model levels roughly 0.1 km above ground (Fig-  
 408 ures 1 and 2). To make sure our findings are not strongly sensitive to this arbitrary al-  
 409 titude choice, we repeated the analysis on model levels roughly 1 km above ground and  
 410 show the results in Figures A1 and A2. Jet behavior at the two altitudes is basically sim-  
 411 ilar.

## 412 **Appendix B RMS difference calculation with 30 $\sim$ 55.7-sol months**

413 To verify that our results concerning the three-dimensional time mean states are  
 414 robust to the somewhat arbitrary choice of averaging period, we repeated the root mean  
 415 square (RMS) difference calculations with each of the 10 seasons divided into three months  
 416 of  $\sim$ 55.7 sols apiece. Tables B1 and B2 are the  $\sim$ 55.7-sol month counterparts of Tables 1  
 417 and C1, respectively. While the exact quantitative results differ from those obtained with  
 418 the  $\sim$ 41.8-sol months, the qualitative summary text in section 5 is based on all four ta-  
 419 bles and as such is robust to the choice of a  $\sim$ 41.8-sol or  $\sim$ 55.7-sol averaging period.

## Appendix C Statistical analyses of RMS difference results

The arguments about reanalysis convergence and the relative sizes of the MCTRL and ECTRL biases made in section 5 are based on qualitative interpretation of Tables 1 and B1 and physical reasoning. It is therefore worth investigating quantitatively how likely we are to have obtained these results under some relevant null hypotheses—could the apparent signals really just be internal variability noise?

Let us first consider the apparent convergence of the UK-LMD and GFDL Mars general circulation model (MGCM) mean states when temperature data are assimilated (Tables 1 and B1, “ $rmsd(M_C, E_C) < rmsd(M_R, E_R)$ ” columns). We will assume (implausibly) that assimilating temperature data has no effect whatsoever on the monthly mean states of the MGCMs. If this is so, then the MACDA–EMARS RMS differences should be drawn from the same probability density functions as the MCTRL–ECTRL RMS differences and for any given month both data set pairs should have an equal probability of having the smaller RMS difference.

We will further postulate that the values of  $rmsd(M_C, E_C)$  and  $rmsd(M_R, E_R)$  for individual months are independent. This assumption seems reasonable, as Martian atmospheric variability that has timescales longer than our  $\sim 41.8$ -sol months and that is not strongly radiatively forced by the annual cycle or via coupling to the dust field is apparently rare [e.g., *Banfield et al.*, 2004]. (The last qualifier is important because the dust fields in all four data sets are being constrained by observations and therefore we are interested only in forms of variability compatible with the prescribed dust fields.) Given this postulate, it is easy to see that (under our null hypothesis of no data assimilation effect) the number of months for which  $rmsd(M_C, E_C) < rmsd(M_R, E_R)$  is satisfied is drawn from a binomial distribution with a success probability of 0.5 (Wilks, 2019a).

The probability of  $rmsd(M_C, E_C) < rmsd(M_R, E_R)$  being satisfied for a number of months *less than or equal to* that actually observed is often quite small under the null hypothesis (Tables C1 and B2, “reanalyses not converging” columns). In conjunction with the physical knowledge that data assimilation does in fact affect the MACDA and EMARS states, we conclude that assimilation of temperature retrievals into the MGCMs is bringing their monthly mean states closer together. It seems unlikely that this result is solely due to data assimilation synchronizing the instantaneous weather states of models with the same underlying climate—this is because the (time-varying) weather should

452 have been largely removed by taking the monthly means prior to computing the RMS  
 453 differences. We thus conclude that data assimilation is converging distinct MGCM cli-  
 454 mates.

455 The first step in our argument that the EMARS control simulation is likely less bi-  
 456 ased than its MACDA counterpart is that the inequality  $rmsd(M_R, M_C) < rmsd(E_R, E_C)$   
 457 is satisfied in only a minority of months for nearly all field–region combinations of in-  
 458 terest. Next we will compute whether these results could have been obtained if  $rmsd(M_R, M_C)$   
 459 and  $rmsd(E_R, E_C)$  are in fact drawn from the same probability density functions—one  
 460 reasonable way to operationalize the null hypothesis that MCTRL and ECTRL agree  
 461 equally well with their associated reanalyses.

462 Our analysis of this case parallels that used to investigate whether data assimila-  
 463 tion brings the MGCMs’ mean states together. We see that under our null hypothesis  
 464 that  $rmsd(M_R, M_C)$  and  $rmsd(E_R, E_C)$  are drawn from the same probability density  
 465 functions, the number of months for which  $rmsd(M_R, M_C) < rmsd(E_R, E_C)$  is satis-  
 466 fied is again drawn from a binomial distribution with a success probability of 0.5. Un-  
 467 der this null hypothesis, the probability of  $rmsd(M_R, M_C) < rmsd(E_R, E_C)$  being sat-  
 468 isfied for a number of months *as or more extreme* than actually observed is often fairly  
 469 low (Tables C1 and B2, “control–reanalysis differences same” columns). In other words,  
 470 if there are  $N_{tot}$  months total and  $rmsd(M_R, M_C) < rmsd(E_R, E_C)$  is actually satis-  
 471 fied in  $N_{obs}$  of them the listed value is the probability (under the null hypothesis) of it  
 472 being satisfied in  $N$  months, where  $0 \leq N \leq N_{obs}$  or  $(N_{tot} - N_{obs}) \leq N \leq N_{tot}$ . ( $N_{tot}$   
 473 is of course 40 (30) for the  $\sim 41.8$ -sol ( $\sim 55.7$ -sol) month case.)

474 We use this two-tailed statistical test because both very small *and* very large val-  
 475 ues of  $N_{obs}$  are unlikely to be observed under the stated null hypothesis. This contrasts  
 476 with our use of an implicitly one-tailed test when examining whether data assimilation  
 477 converges the MGCM states—a one-tailed test was appropriate in that case because sat-  
 478 isfaction of  $rmsd(M_C, E_C) < rmsd(M_R, E_R)$  in a large number of months would be  
 479 inconsistent with the alternative hypothesis that data assimilation brings the MGCMs’  
 480 mean states together.

481 The second step of our argument for smaller ECTRL biases involved comparing  
 482 the rightmost two columns of Tables 1 and B1. We noted that  $rmsd(M_R, E_C) < rmsd(M_R, M_C)$   
 483 was generally satisfied in at least as many months as  $rmsd(E_R, M_C) < rmsd(E_R, E_C)$ .



484 Let us define a test statistic  $S$ , where  $S$  is the number of months in which  $rmsd(M_R, E_C) <$   
 485  $rmsd(M_R, M_C)$  was satisfied minus the number of months in which  $rmsd(E_R, M_C) <$   
 486  $rmsd(E_R, E_C)$ . Further denoting an observed value of  $S$  as  $S_{obs}$ , we essentially argued  
 487 that ECTRL was less biased because we usually found  $S_{obs} \geq 0$ .

488 The null hypothesis we will evaluate in this case is that the ECTRL and MCTRL  
 489 simulations are simply different realizations of internal variability and that these versions  
 490 of the free-running GFDL and UK-LMD MGCMs actually have the same underlying cli-  
 491 mate (given the imposed dust fields). We thus postulate that the ECTRL and MCTRL  
 492 monthly mean states are drawn from same (month-dependent) probability density func-  
 493 tions, and also continue to assume that the monthly mean states for a given month are  
 494 drawn independently of those for all other months.

495 If this null hypothesis is true, for each of the  $N_{tot}$  total months we are essentially  
 496 drawing two monthly mean states from a (month-dependent) probability density func-  
 497 tion and randomly assigning the label “ECTRL” to one mean state and “MCTRL” to  
 498 the other. We can thus evaluate the null hypothesis using a permutation test (Wilks, 2019b):  
 499 for each of the  $N_{tot}$  months, we can independently choose to exchange (or not exchange)  
 500 the “ECTRL” and “MCTRL” labels attached to the monthly mean states. There are  
 501 thus  $2^{N_{tot}}$  possible distinct synthetic labelings of the ECTRL and MCTRL monthly mean  
 502 states. Exactly one of these labelings (the one without any exchanges) matches the ac-  
 503 tual ECTRL and MCTRL states, but if the null hypothesis is true *we are equally likely*  
 504 *to have observed any of these labelings.*

505 For each field–region combination of interest, we can thus use these synthetic la-  
 506 belings of the monthly mean states to compute the appropriate null distribution for  $S$ .  
 507 In practice, generating all  $2^{N_{tot}}$  ( $>10^9$  even for  $N_{tot} = 30$ ) synthetic sets is computa-  
 508 tionally intractable—we therefore approximate the  $S$  null distribution by drawing  $10^6$   
 509 of the sets at random. We then calculate  $S_{obs}$  values (Tables C1 and B2, “ $S_{obs}$ ” columns)  
 510 and use the approximate null distributions to determine the probability of obtaining an  
 511  $S$  value *as or more extreme* than actually observed. By “as or more extreme” we mean  
 512  $|S| \geq |S_{obs}|$ —we are thus conducting a two-tailed test, as both large and small values  
 513 of  $S_{obs}$  would argue against our chosen null hypothesis. Our results are shown in the right-  
 514 most columns of Tables C1 and B2 (“more extreme  $S$ ”).

515 Although for some field–region combinations the  $S_{obs}$  value is found to be fully con-  
 516 sistent with the null hypothesis, in most cases with  $p_t = 0.1$  hPa the probability of  
 517 getting an  $S$  value at least as extreme as observed is substantially less than 1. In con-  
 518 junction with the known structural differences between the two MGCMs, this finding fur-  
 519 ther supports the idea that the UK-LMD and GFDL MGCMs do in fact have different  
 520 climates and that the apparent superiority of ECTRL over MCTRL is not simply a ran-  
 521 dom manifestation of internal variability.

## 522 Acknowledgments

523 We particularly thank Tiffany A. Shaw for her support of this work—she provided much  
 524 helpful input on early versions of this paper and financially supported TAM and GED.  
 525 R. John Wilson read drafts of the paper and pointed out the TES spectral resolution changes  
 526 as the likely source of the EMARS MY26 tropical westerlies issue. Pragallva Barpanda  
 527 also read an early draft of the paper. TAM was funded through Prof. Shaw’s fellowship  
 528 from the David and Lucile Packard Foundation, while GED was funded through National  
 529 Science Foundation grant AGS-1742944 via Leadership Alliance. GED also acknowledges  
 530 participation in the Leadership Alliance Summer Research Early Identification Program  
 531 at the University of Chicago. SJG is supported by NASA Mars Data Analysis Program  
 532 grant 80NSSC17K0690 and 80NSSC20K1054. Reduced data necessary to reproduce all  
 533 figures and tables of this paper are available in Mooring et al. (2021). The full MACDA  
 534 reanalysis data set is available in University of Oxford et al. (2011), while the full MACDA  
 535 control simulation is available in University of Oxford et al. (2022). The full EMARS  
 536 reanalysis and control simulation are available in Greybush et al. (2018).

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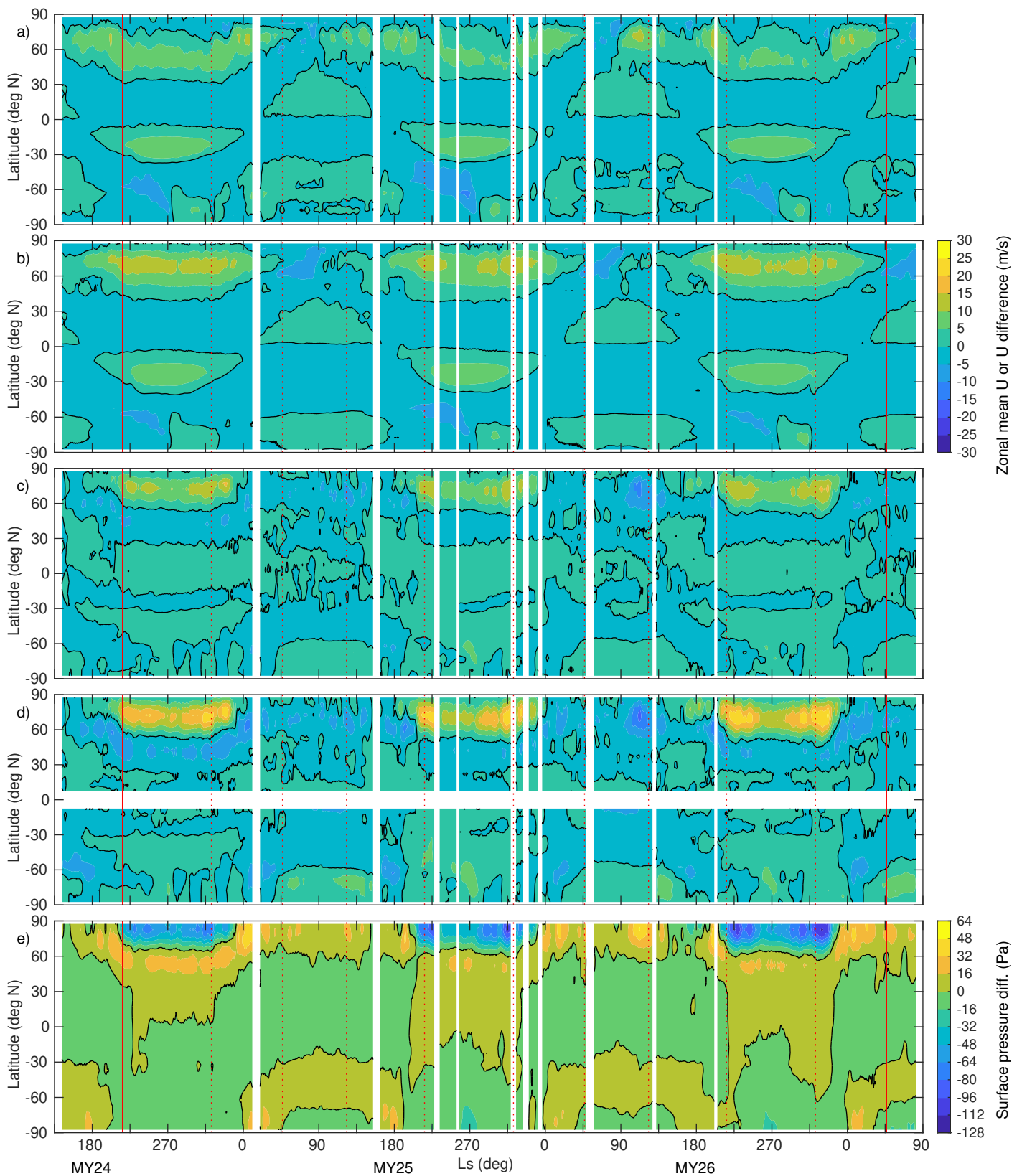
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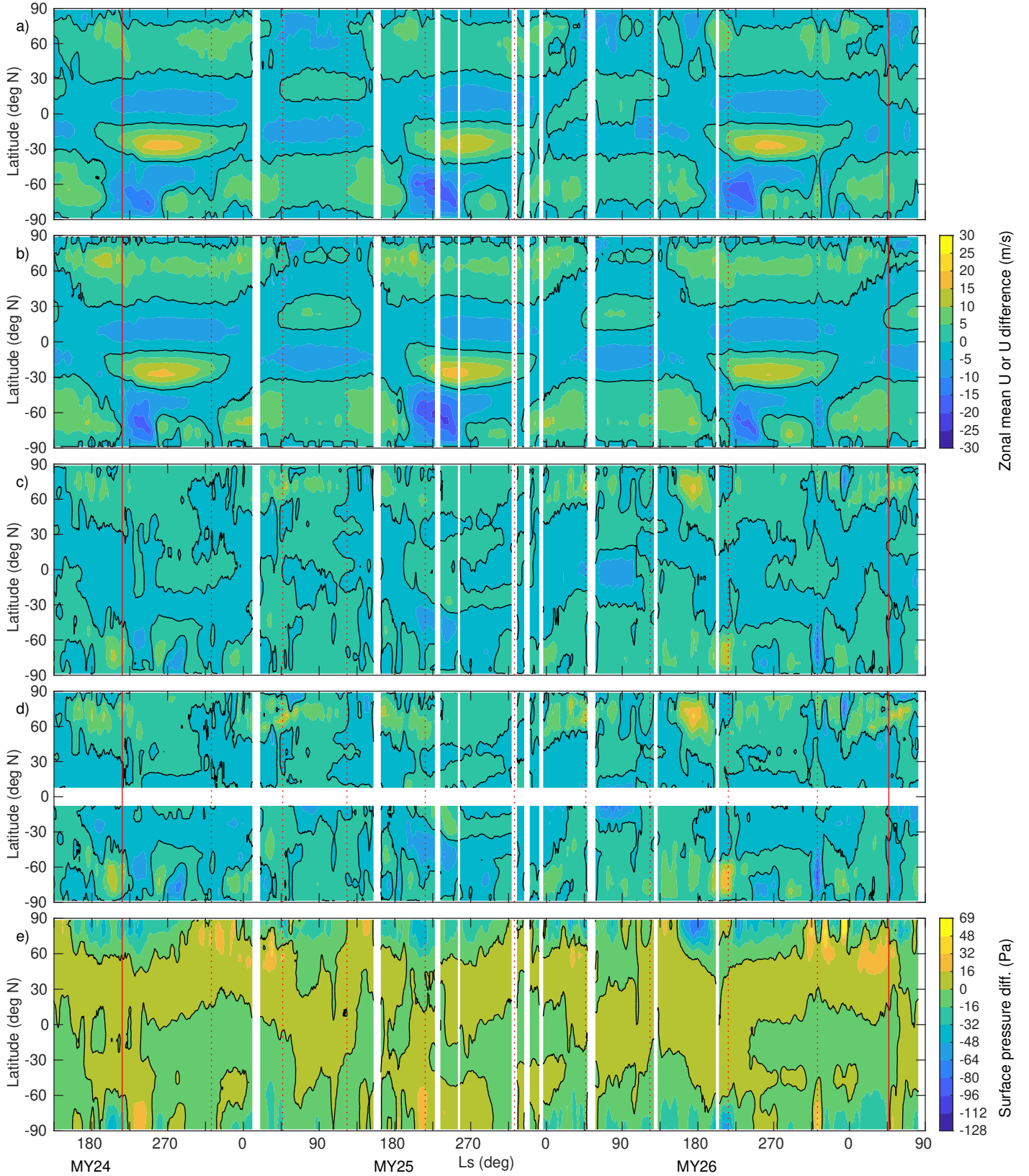
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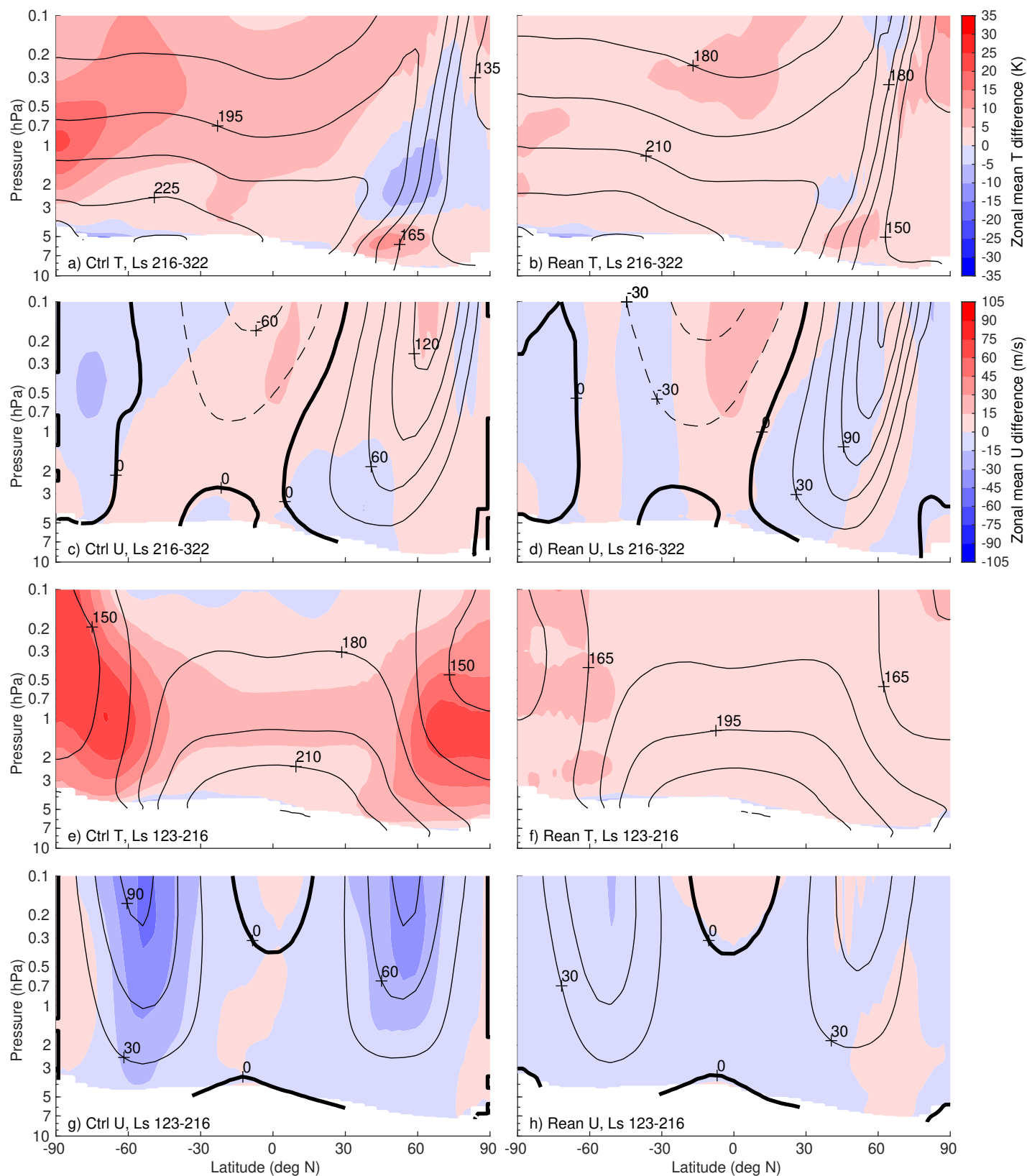


**Figure 1.** Zonal mean zonal winds on the  $\sigma = 0.991$  level ( $\sim 90$  m above ground) for MACDA (a) and MCTRL (b). Differences between MCTRL and MACDA are shown in (c–e)— $\sigma = 0.991$  zonal winds in (c), surface geostrophic zonal winds in (d) and surface pressures in (e). The time range shown is MY24  $L_s$  135° to MY27  $L_s$  90°. All fields have been smoothed with a 10-sol running mean. The surface geostrophic wind difference in (d) was computed from surface pressure and temperature data from the lowest model level, following equation 4 of Mooring and Wilson (2015). (Geostrophic wind differences are not plotted within 7.5° of the equator.) The global mean atmospheric mass difference at each timestep was removed before plotting (e). The black line is the zero contour, notable gaps in the availability of TES retrievals are masked out in white, and the limits of the seasons used in Figures 3 and 4 are marked with red lines.

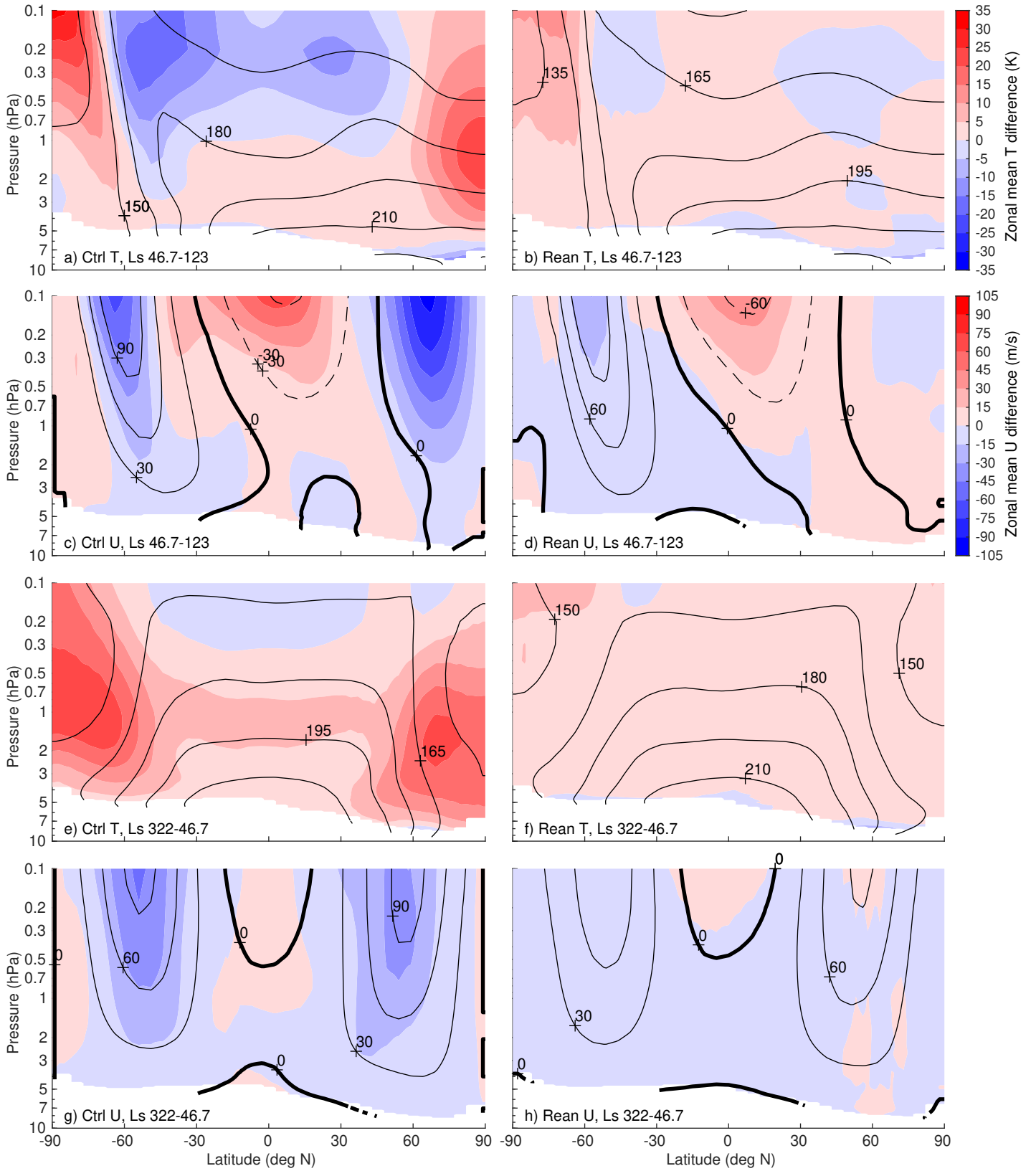




**Figure 2.** As Figure 1 but for EMARS and CTRL. Zonal winds in (a-c) are evaluated on the model level with  $\sigma \approx 0.988$  ( $\sim 120$  m above ground).



**Figure 3.** Agreement between reanalysis and free-running control zonal mean temperature and zonal wind fields for boreal winter (a-d) and autumn (e-h). Black contours in the left (right) column show full fields from ECTRL (EMARS), with the zero contour marked with a heavy black line. Red and blue shading in the left (right) column shows MCTRL minus ECTRL (MACDA minus EMARS). Interannual means are computed across all available realizations of each season, while each single-Mars year seasonal mean is computed from four monthly means. The months have lengths of  $\sim 41.8$  sols, as described in section 5.



**Figure 4.** As Figure 3, but for boreal summer (a-d) and spring (e-h).

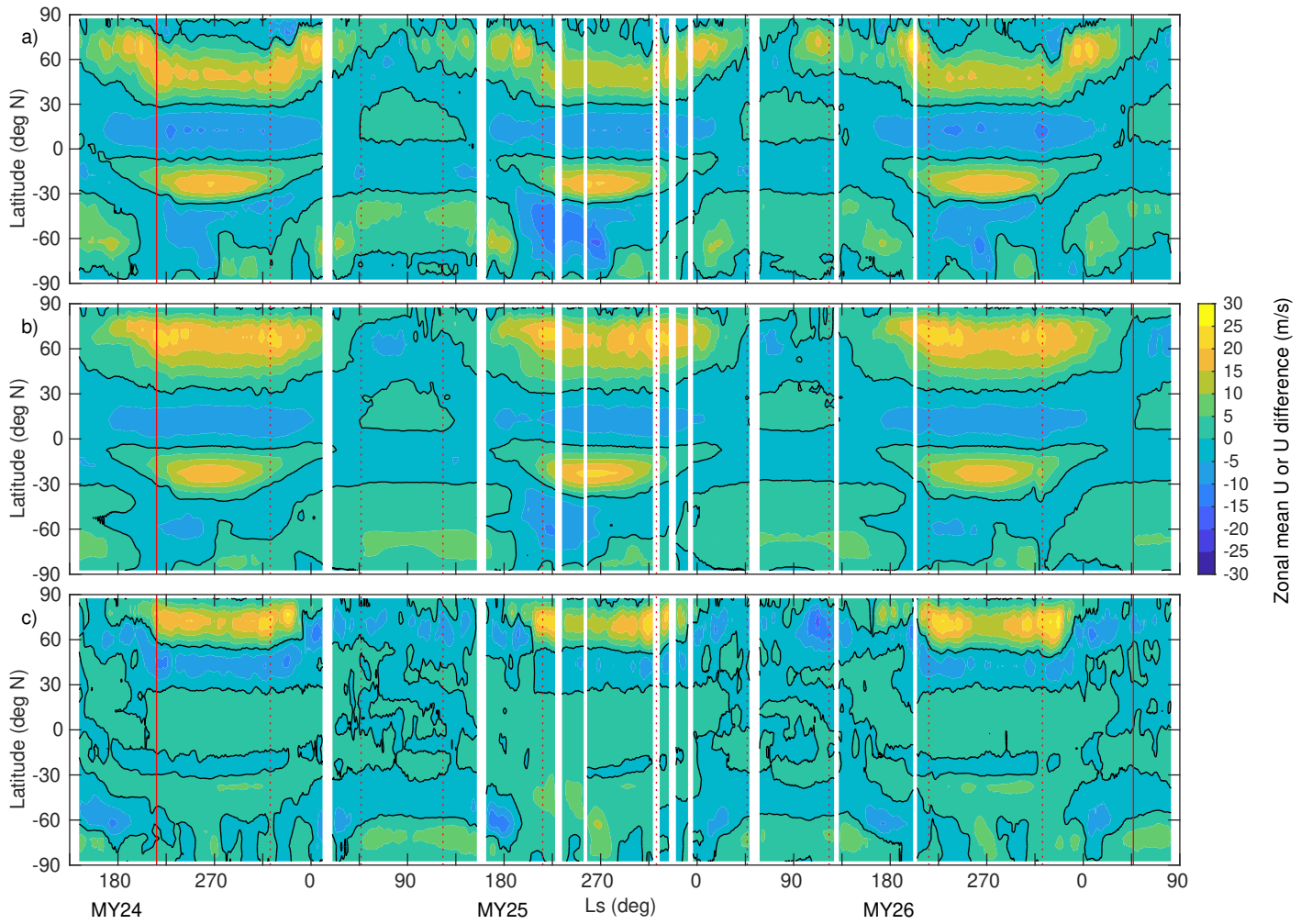
**Table 1.** Relative sizes of RMS differences between reanalyses and control simulations

Field	Domain top (hPa)	Meridional domain	$rmsd(M_C, E_C) <$ $rmsd(M_R, E_R)$	$rmsd(M_R, M_C) <$ $rmsd(E_R, E_C)$	$rmsd(E_R, M_C) <$ $rmsd(E_R, E_C)$	$rmsd(M_R, E_C) <$ $rmsd(M_R, M_C)$
T	0.1	Global		7		14
T	0.1	Tropics	1	5		6
T	0.1	SH extratropics		12	2	11
T	0.1	NH extratropics		12	7	24
T	0.1	All extratropics		8	3	18
T	3	Global		11	2	7
T	3	Tropics	3	4		3
T	3	SH extratropics	5	12	3	8
T	3	NH extratropics		15	6	15
T	3	All extratropics		12	3	7
U	0.1	Global	1	10		19
U	0.1	Tropics	17	18		
U	0.1	SH extratropics	8	6	1	14
U	0.1	NH extratropics	1	9	6	28
U	0.1	All extratropics		4		28
U	3	Global	4	16	2	13
U	3	Tropics	18	26	5	
U	3	SH extratropics	13	11	3	4
U	3	NH extratropics	8	11	6	20
U	3	All extratropics	2	11	1	15

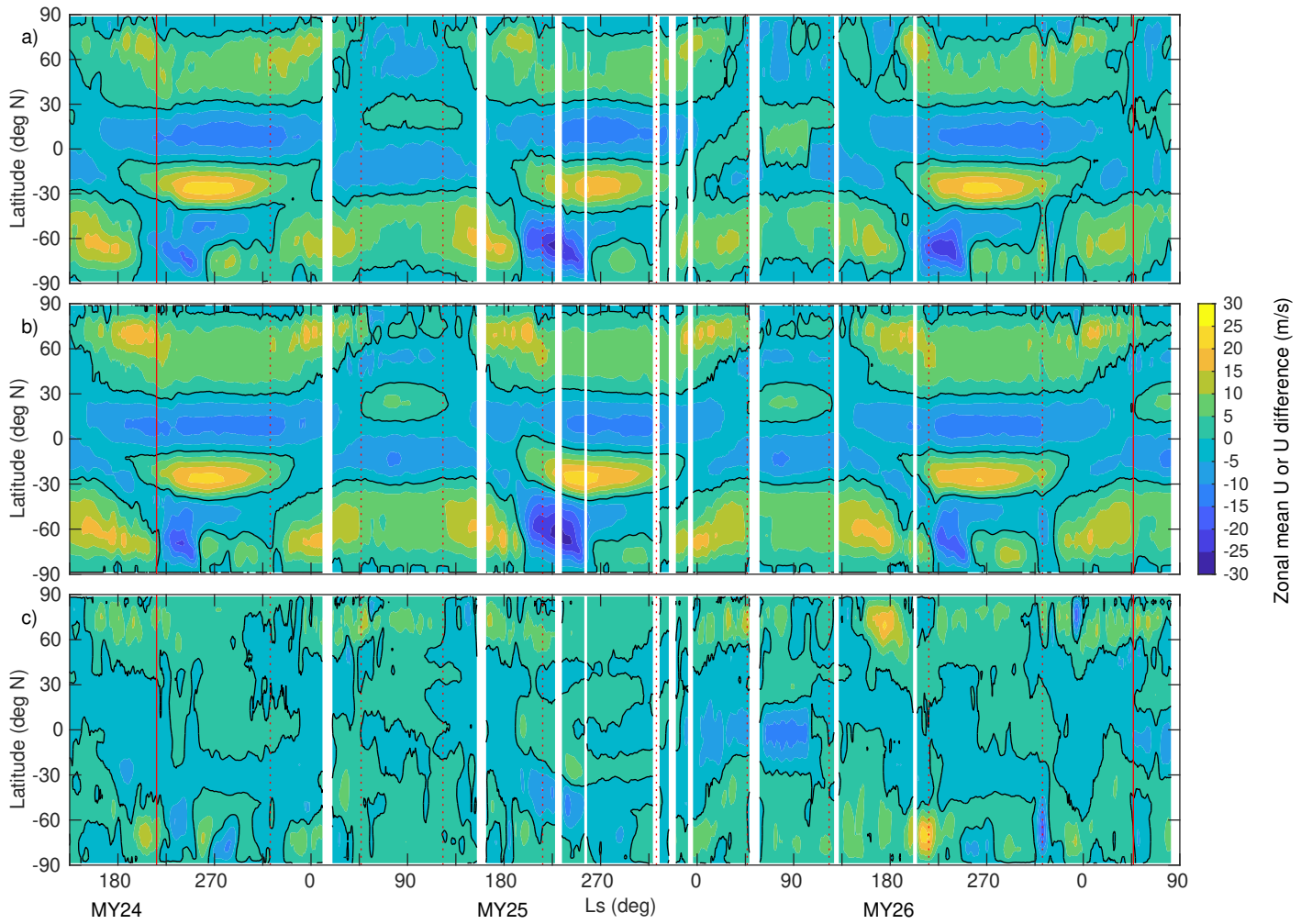
This table contains information about relative levels of agreement between the various reanalysis and control simulation data sets. We denote the RMS difference between data sets  $X$  and  $Y$  as  $rmsd(X, Y)$ .

The left three columns name the variable being analyzed and the region over which RMS differences are being computed.

The right four columns contain the results, expressed as the number of months (of 40 total) for which the inequality given at the top of each column is satisfied. Zeros have been omitted for clarity. As an example of how to read the table, the large number of values  $\ll 40$  in the  $rmsd(E_R, M_C) < rmsd(E_R, E_C)$  column means that EMARS is in robustly better agreement with ECTRL than with MCTRL.



**Figure A1.** As Figure 1a-c, but for the  $\sigma = 0.900$  level ( $\sim 1.1$  km above ground).



**Figure A2.** As Figure 2a-c, but on the model level with  $\sigma \approx 0.905$  ( $\sim 1.0$  km above ground).

**Table B1.** Relative sizes of RMS differences between reanalyses and control simulations

Field	Domain top (hPa)	Meridional domain	$rmsd(M_C, E_C) <$ $rmsd(M_R, E_R)$	$rmsd(M_R, M_C) <$ $rmsd(E_R, E_C)$	$rmsd(E_R, M_C) <$ $rmsd(E_R, E_C)$	$rmsd(M_R, E_C) <$ $rmsd(M_R, M_C)$
T	0.1	Global		5		12
T	0.1	Tropics	1	3		5
T	0.1	SH extratropics		7	1	8
T	0.1	NH extratropics		11	5	17
T	0.1	All extratropics		8	3	14
T	3	Global		7		6
T	3	Tropics	2	1		2
T	3	SH extratropics	4	9	2	7
T	3	NH extratropics		10	7	10
T	3	All extratropics		8		7
U	0.1	Global	1	5		15
U	0.1	Tropics	14	13		
U	0.1	SH extratropics	5	3	1	12
U	0.1	NH extratropics		6	5	22
U	0.1	All extratropics		3	1	20
U	3	Global	4	10	1	8
U	3	Tropics	14	20	3	
U	3	SH extratropics	11	7	3	4
U	3	NH extratropics	6	7	4	16
U	3	All extratropics	2	7		12

As Table 1, but using 30  $\sim$ 55.7-sol months instead of 40  $\sim$ 41.8-sol months.

**Table B2.** Information about probabilities of obtaining the observed results under various null hypotheses

Field	Domain top (hPa)	Meridional domain	Reanalyses not converging	Control- reanalysis differences same	$S_{obs}$	More extreme $S$
T	0.1	Global	$9.31 \times 10^{-10}$	$3.25 \times 10^{-4}$	12	$4.44 \times 10^{-4}$
T	0.1	Tropics	$2.89 \times 10^{-8}$	$8.43 \times 10^{-6}$	5	$6.24 \times 10^{-2}$
T	0.1	SH extratropics	$9.31 \times 10^{-10}$	$5.22 \times 10^{-3}$	7	$3.89 \times 10^{-2}$
T	0.1	NH extratropics	$9.31 \times 10^{-10}$	$2.00 \times 10^{-1}$	12	$1.69 \times 10^{-2}$
T	0.1	All extratropics	$9.31 \times 10^{-10}$	$1.61 \times 10^{-2}$	11	$1.25 \times 10^{-2}$
T	3	Global	$9.31 \times 10^{-10}$	$5.22 \times 10^{-3}$	6	$3.14 \times 10^{-2}$
T	3	Tropics	$4.34 \times 10^{-7}$	$5.77 \times 10^{-8}$	2	$5.00 \times 10^{-1}$
T	3	SH extratropics	$2.97 \times 10^{-5}$	$4.28 \times 10^{-2}$	5	$1.80 \times 10^{-1}$
T	3	NH extratropics	$9.31 \times 10^{-10}$	$9.87 \times 10^{-2}$	3	$6.30 \times 10^{-1}$
T	3	All extratropics	$9.31 \times 10^{-10}$	$1.61 \times 10^{-2}$	7	$1.56 \times 10^{-2}$
U	0.1	Global	$2.89 \times 10^{-8}$	$3.25 \times 10^{-4}$	15	$5.90 \times 10^{-5}$
U	0.1	Tropics	$4.28 \times 10^{-1}$	$5.85 \times 10^{-1}$	0	1
U	0.1	SH extratropics	$1.62 \times 10^{-4}$	$8.43 \times 10^{-6}$	11	$3.45 \times 10^{-3}$
U	0.1	NH extratropics	$9.31 \times 10^{-10}$	$1.43 \times 10^{-3}$	17	$4.31 \times 10^{-4}$
U	0.1	All extratropics	$9.31 \times 10^{-10}$	$8.43 \times 10^{-6}$	19	$1.70 \times 10^{-5}$
U	3	Global	$2.97 \times 10^{-5}$	$9.87 \times 10^{-2}$	7	$3.95 \times 10^{-2}$
U	3	Tropics	$4.28 \times 10^{-1}$	$9.87 \times 10^{-2}$	-3	$2.50 \times 10^{-1}$
U	3	SH extratropics	$1.00 \times 10^{-1}$	$5.22 \times 10^{-3}$	1	1
U	3	NH extratropics	$7.15 \times 10^{-4}$	$5.22 \times 10^{-3}$	12	$1.17 \times 10^{-2}$
U	3	All extratropics	$4.34 \times 10^{-7}$	$5.22 \times 10^{-3}$	12	$5.07 \times 10^{-4}$

As Table C1, but using 30 ~55.7-sol months.

This table should be used to help interpret the results given in Table B1.



**Table C1.** Information about probabilities of obtaining the observed results under various null hypotheses

Field	Domain top (hPa)	Meridional domain	Reanalyses not converging	Control- reanalysis differences same	$S_{obs}$	More extreme $S$
T	0.1	Global	<b><math>9.09 \times 10^{-13}</math></b>	<b><math>4.23 \times 10^{-5}</math></b>	14	$1.14 \times 10^{-4}$
T	0.1	Tropics	<b><math>3.73 \times 10^{-11}</math></b>	<b><math>1.38 \times 10^{-6}</math></b>	6	$3.13 \times 10^{-2}$
T	0.1	SH extratropics	<b><math>9.09 \times 10^{-13}</math></b>	$1.66 \times 10^{-2}$	9	$2.26 \times 10^{-2}$
T	0.1	NH extratropics	<b><math>9.09 \times 10^{-13}</math></b>	$1.66 \times 10^{-2}$	17	$3.32 \times 10^{-3}$
T	0.1	All extratropics	<b><math>9.09 \times 10^{-13}</math></b>	$1.82 \times 10^{-4}$	15	$1.46 \times 10^{-3}$
T	3	Global	<b><math>9.09 \times 10^{-13}</math></b>	$6.43 \times 10^{-3}$	5	$1.80 \times 10^{-1}$
T	3	Tropics	<b><math>9.73 \times 10^{-9}</math></b>	<b><math>1.86 \times 10^{-7}</math></b>	3	$2.50 \times 10^{-1}$
T	3	SH extratropics	<b><math>6.91 \times 10^{-7}</math></b>	$1.66 \times 10^{-2}$	5	$2.27 \times 10^{-1}$
T	3	NH extratropics	<b><math>9.09 \times 10^{-13}</math></b>	$1.54 \times 10^{-1}$	9	$7.87 \times 10^{-2}$
T	3	All extratropics	<b><math>9.09 \times 10^{-13}</math></b>	$1.66 \times 10^{-2}$	4	$3.44 \times 10^{-1}$
U	0.1	Global	<b><math>3.73 \times 10^{-11}</math></b>	$2.22 \times 10^{-3}$	19	<b><math>3.00 \times 10^{-6}</math></b>
U	0.1	Tropics	$2.15 \times 10^{-1}$	$6.36 \times 10^{-1}$	0	1
U	0.1	SH extratropics	<b><math>9.11 \times 10^{-5}</math></b>	<b><math>8.36 \times 10^{-6}</math></b>	13	$1.02 \times 10^{-3}$
U	0.1	NH extratropics	<b><math>3.73 \times 10^{-11}</math></b>	$6.80 \times 10^{-4}$	22	$1.82 \times 10^{-4}$
U	0.1	All extratropics	<b><math>9.09 \times 10^{-13}</math></b>	<b><math>1.86 \times 10^{-7}</math></b>	28	<b>0</b>
U	3	Global	<b><math>9.29 \times 10^{-8}</math></b>	$2.68 \times 10^{-1}$	11	$7.55 \times 10^{-3}$
U	3	Tropics	$3.18 \times 10^{-1}$	$8.07 \times 10^{-2}$	-5	$6.27 \times 10^{-2}$
U	3	SH extratropics	$1.92 \times 10^{-2}$	$6.43 \times 10^{-3}$	1	1
U	3	NH extratropics	<b><math>9.11 \times 10^{-5}</math></b>	$6.43 \times 10^{-3}$	14	$9.19 \times 10^{-3}$
U	3	All extratropics	<b><math>7.47 \times 10^{-10}</math></b>	$6.43 \times 10^{-3}$	14	$5.36 \times 10^{-4}$

See text of Appendix C for further details, including descriptions of the columns.

Calculations were done using 40 ~41.8-sol months, and thus this table should be used to help interpret the results given in Table 1. Probabilities  $< 10^{-4}$  are written in **bold**, while probabilities  $< 10^{-2}$  are *italicized*.