



# Integrated Monte Carlo Microstructure and Analytical Temperature Simulations of Additive Manufacturing

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**Additive Manufacturing Benchmark 2022**

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# Outline

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## Introduction / Background / Objective

Kinetic Monte Carlo Modeling of Microstructure Evolution

Analytical vs. Numerical Temperature Field Simulation

- Overview
- Impact of Time Step Choice

Simulation of Ti-6Al-4V PBF-LB Microstructure Evolution

- Comparisons with Experiment
- Effect of Processing Parameters

Conclusions and Summary

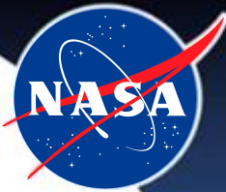
# Introduction

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- Laser beam powder bed fusion (PBF-LB) additive manufacturing (AM) forms complex, impactful microstructures
  - The microstructure impacts the final part performance and is not guaranteed to be removed through post-processing
- The domain space for PBF-LB is massive
  - Hatch spacing, layer thickness, power, velocity, beam diameter, scan rotation angle, scan strategy, pre-heat temperature, material system, etc...
- Surveying the microstructure design space experimentally is difficult, time-consuming, and costly
- Computational microstructure evolution techniques are a way to try to get a handle on the domain space challenge
- This work will focus on the Monte Carlo technique

# Generations of SPPARKS-Based PBF-LB Monte Carlo Simulations



## SPPARKS: Stochastic Parallel PARticle Kinetic Simulator

- Sandia National Laboratory developed Monte Carlo framework
- <https://spparks.github.io/>

## Generation 1 (2017) [1]

### Kinetic Monte Carlo (kMC) method

- Temperature field approximated by ellipsoid and exponential decay
- Solidification approximated by Monte Carlo grain coarsening
- Nucleation of new grains based on melt pool randomization
- Difficult to link laboratory and simulation reference frames

## Generation 2 (2021) [2]

### Physically-Based Monte Carlo (PBMC) method\*

- Temperature field implemented analytically or numerically
- Solidification modeled by dendritic growth approximation
- Nucleation based on undercooling
- Links laboratory and simulation reference frames

[1] Rodgers, T.M., et al. "Simulation of metal additive manufacturing microstructures using kinetic Monte Carlo." *Computational Materials Science* 135 (2017): 78-89. <https://doi.org/10.1016/j.commatsci.2017.03.053>

[2] Rodgers, T.M., et al. "Simulation of powder bed metal additive manufacturing microstructures with coupled finite difference-Monte Carlo method." *Additive Manufacturing* 41 (2021): 101953. <https://doi.org/10.1016/j.addma.2021.101953>

\*While originally called Finite Difference Monte Carlo [2], this work extends the model to use an analytical temperature field so a more general name is used\*

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## Generation 2 (2021) [2]

Physically-Based Monte Carlo (PBMC) method\*

- Temperature field implemented analytically
- Solidification approximated by dendritic growth
- Nucleation based on melt pool cooling
- Linking laboratory and simulation reference frames

**Focus of this work**

[1] Rodgers, T.M., et al. "Simulation of metal additive manufacturing microstructures using kinetic Monte Carlo." *Computational Materials Science* 135 (2017): 78-89., <https://doi.org/10.1016/j.commatsci.2017.03.053>

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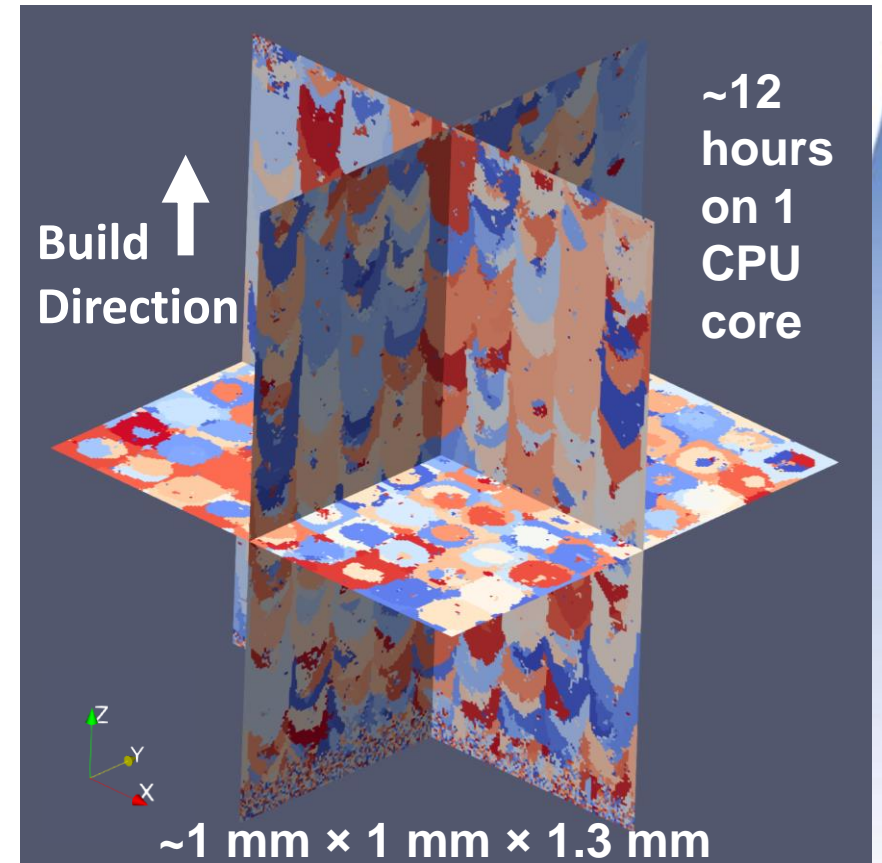
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# Objectives of This Work



- Demonstrate the applicability of the PBMC method for process-to-microstructure modeling of PBF-LB
- Present details on the integration of the model with analytical temperature fields
- Highlight the differences between the analytical and numerical temperature field implementations
- Compare analytical-temperature field PBMC Ti-6Al-4V PBF-LB simulations to experiments
- Present the impact of processing parameters on resulting grain statistics

AMBench Region #2 of  
Inconel 718 Build



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# PBMC Modeling of Microstructure Evolution

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Solidification

Texture

Nucleation

Grain Coarsening

## Critical Components of the PBMC Method

\*Texture modeling represents a new addition to the PBMC method based on previous work incorporating texture [3]



# PBMC Modeling of Microstructure Evolution

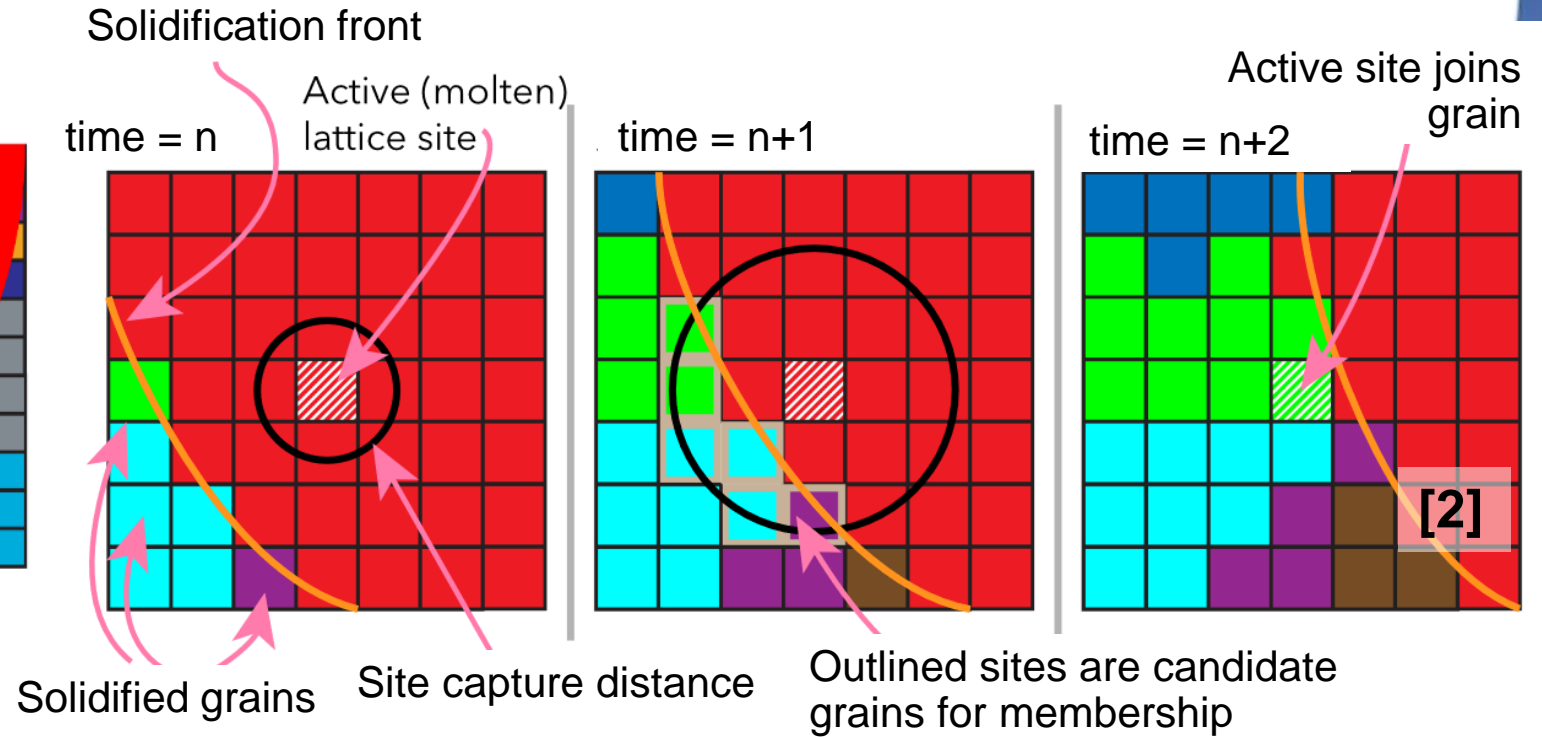
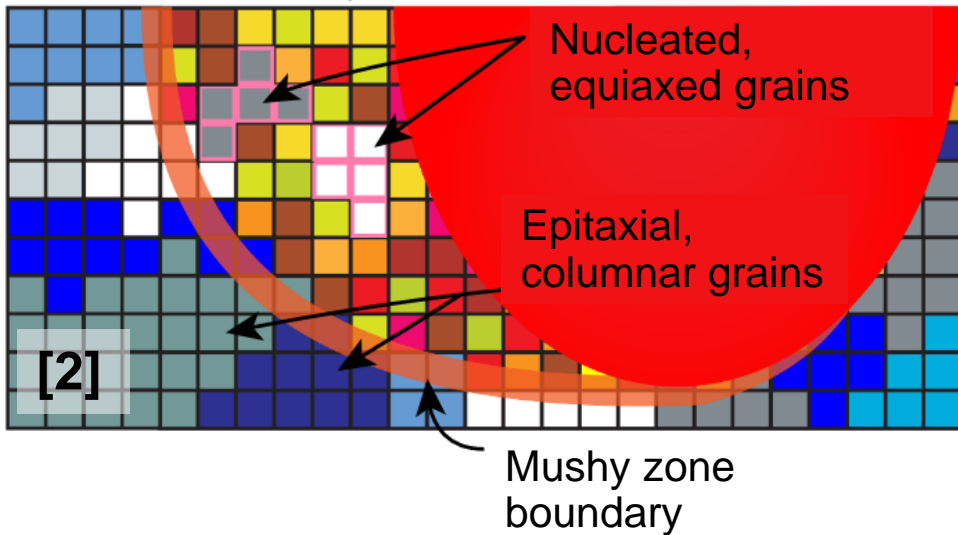
## Solidification

## Texture

## Nucleation

## Grain Coarsening

Melt pool & solidification overview



[2] Rodgers, T.M., et al. "Simulation of powder bed metal additive manufacturing microstructures with coupled finite difference-Monte Carlo method." *Additive Manufacturing* 41 (2021): 101953. <https://doi.org/10.1016/j.addma.2021.101953>  
 Figure used under CC BY 4.0 license <https://creativecommons.org/licenses/by/4.0/>, Fig 1. and Fig 2. cropped and relabeled from original document

# PBMC Modeling of Microstructure Evolution



## Solidification

## Texture

## Nucleation

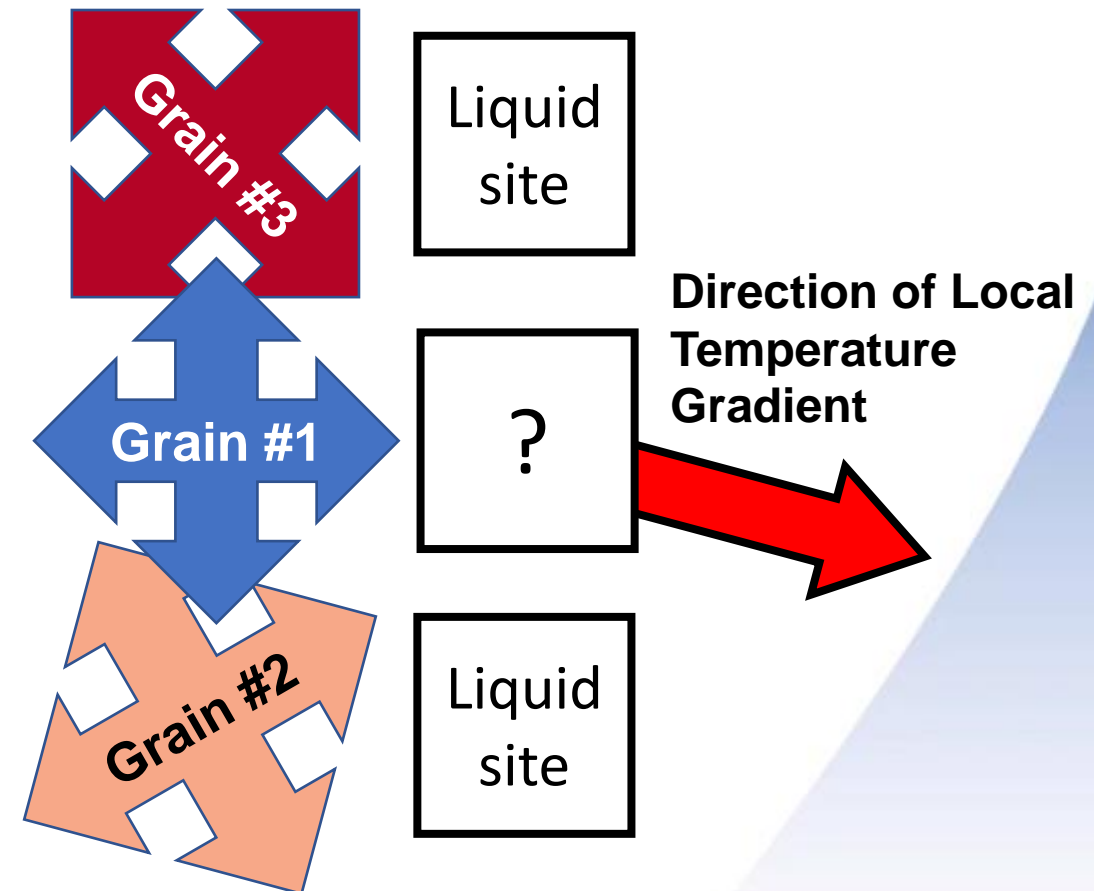
## Grain Coarsening

New addition in current work based on modification of previous implementation [3]

Each site is assigned Euler angles defining its crystallographic texture

The misorientation between a grain crystallographic orientation and the local temperature gradient impacts the capture distance

Favors  $\langle 100 \rangle$  crystal growth



[3] Pauza, J.G. et al., "Computer simulation of microstructure development in powder-bed additive manufacturing with crystallographic texture." *Modelling and Simulation in Materials Science and Engineering* 29.5 (2021): 055019.

<https://doi.org/10.1088/1361-651X/ac03a6>

# PBMC Modeling of Microstructure Evolution



## Solidification

## Texture

## Nucleation

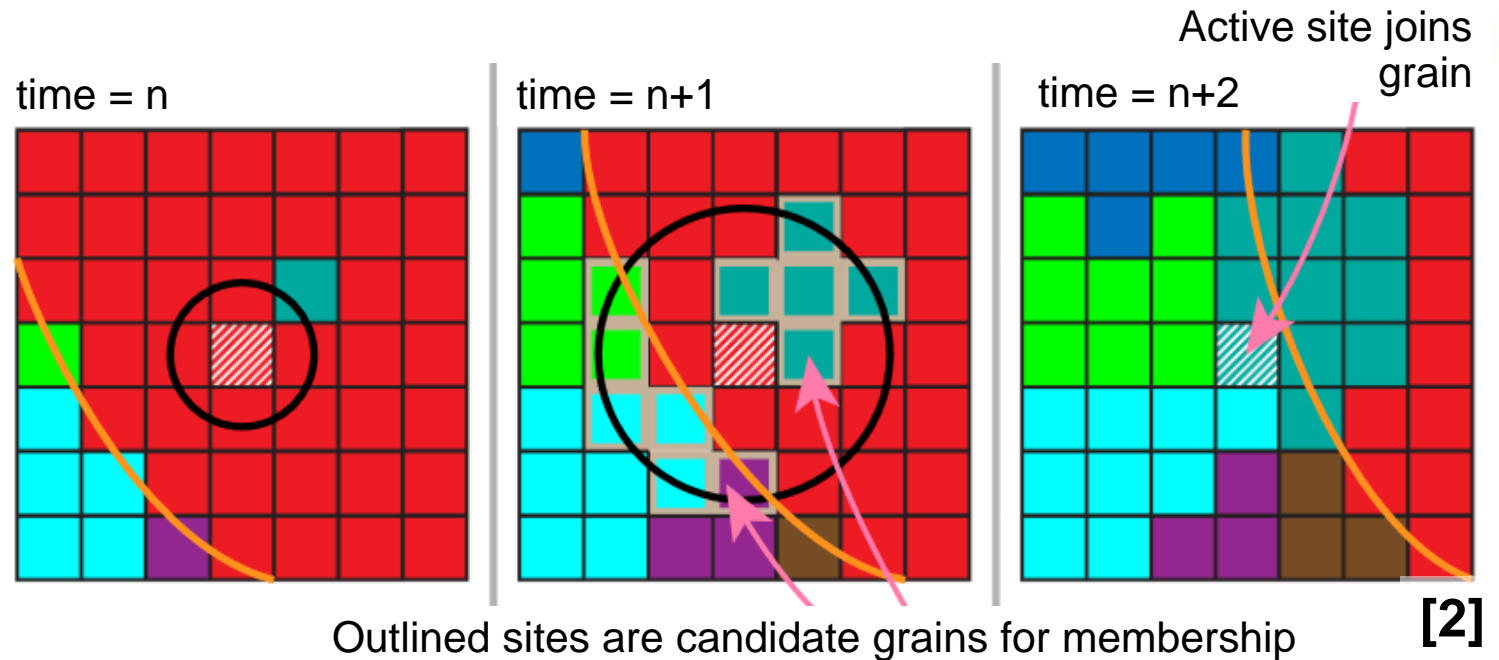
## Grain Coarsening

User defines:

1. Number of nucleation points per unit volume
2. Undercooling at which nucleation takes place

Before the simulation, nucleation sites are probabilistically assigned

If a possible nucleation site reaches the specified undercooling while molten, it solidifies



# PBMC Modeling of Microstructure Evolution




## Solidification

## Texture

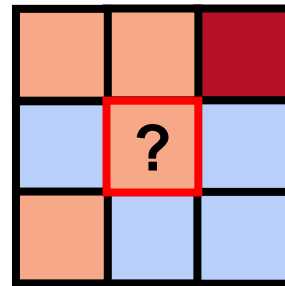
## Nucleation

## Grain Coarsening

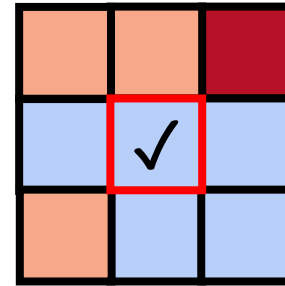
Kinetic Potts Monte Carlo method

-  Grain #1
-  Grain #2
-  Grain #3

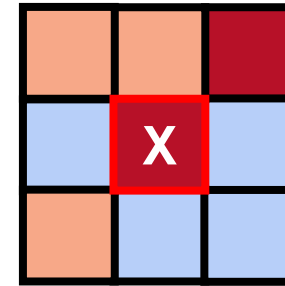
Initial Grains



Flips to Grain #3  
**Accepted** (lowers system energy)



Flips to Grain #2  
**Rejected** (Increases system energy)



$\delta_{ij}$  = Kronecker delta between spin  $i$  and nearest neighbor spin  $j$   
 $n_k$  = nearest neighbor  $k$   
 $N$  = All nodes in the system  
 $E$  = Energy of system

$$E = \frac{1}{2} \sum_i^N \sum_j^{n_k} (1 - \delta_{ij})$$

$$\Delta E = E_{new} - E_{old}$$

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# Analytical vs. Numerical Thermal Field Calculation



## Analytical (Rosenthal)

$$T = T_0 + \frac{AP}{2\pi rk} \exp\left(-\frac{v(\xi + r)}{2\alpha}\right)$$

$$r = \sqrt{\xi^2 + y^2 + (\eta_{z,scale}z)^2}$$

$$\xi = x - vt$$

$T$  = time & location specific temperature

$T_0$  = base temperature

$A$  = absorptivity

$P$  = laser power

$v$  = scanning velocity

$\alpha$  = thermal diffusivity

$c_p$  = specific heat capacity

## Numerical (Finite Difference)

$$\rho c_p \frac{\partial T}{\partial t} = \nabla(-k\nabla T) + H_v = 0$$

Time Integration: Explicit Euler

Spatial Derivatives: Second Order

Central Finite Difference

$\rho$  = mass density

$k$  = thermal conductivity

$H_v$  = volumetric heat flux of laser

$T_m$  = melt temperature

$T_r$  = room temperature

$\eta_{z,scale}$  = scaling factor for melt pool shape

$x, y, z$  = local coordinates with  $x$  in the direction of the laser movement

$\xi$  = shifted coordinate frame with respect to time

# Analytical vs. Numerical Thermal Field Calculation



## Analytical (Rosenthal)

$$T = T_0 + \frac{AP}{2\pi rk} \exp\left(-\frac{v(\xi + r)}{2\alpha}\right)$$




- Analytical solution
  - **Stability Limit: N/A**
  - **Numerical Accuracy: N/A**
- **No boundary conditions**
- **Point source**
- **No radiation, convection, or powder conductivity**

## Numerical (Finite Difference)

$$\rho c_p \frac{\partial T}{\partial t} = \nabla(-k\nabla T) + H_v = 0$$

- Explicit Euler implementation
  - **Stability Limit:  $dt \leq dx^2/4\alpha$**
  - **Numerical Accuracy:  $err \propto dt^2$**
- **Boundary conditions**
- **Volumetric beam**
- **Can include radiation, convection, and powder conductivity**

**Both - Time Step Limitation:  $dt \leq dx/v$**

-  Positive
-  Neutral
-  Negative



# Analytical vs. Numerical Thermal Field Calculation

## Analytical (Rosenthal)

$$T = T_0 + \frac{AP}{2\pi rk} \exp\left(-\frac{v(\xi + r)}{2\alpha}\right)$$

- Analytical solution
  - **S**
  - **N/A**
- **No boundary conditions**
- **Point source**
- **No radiation, convection, or powder conductivity**

**Numerical Speed**

## Numerical (Finite Difference)

$$\rho c_p \frac{\partial T}{\partial t} = \nabla(-k\nabla T) + H_v = 0$$

- Explicit Euler implementation
  - **S**
  - **err  $\propto dt^2$**
- **Boundary conditions**
- **Volume source**
- **Can include radiation, convection, and powder conductivity**

**Physical Fidelity**

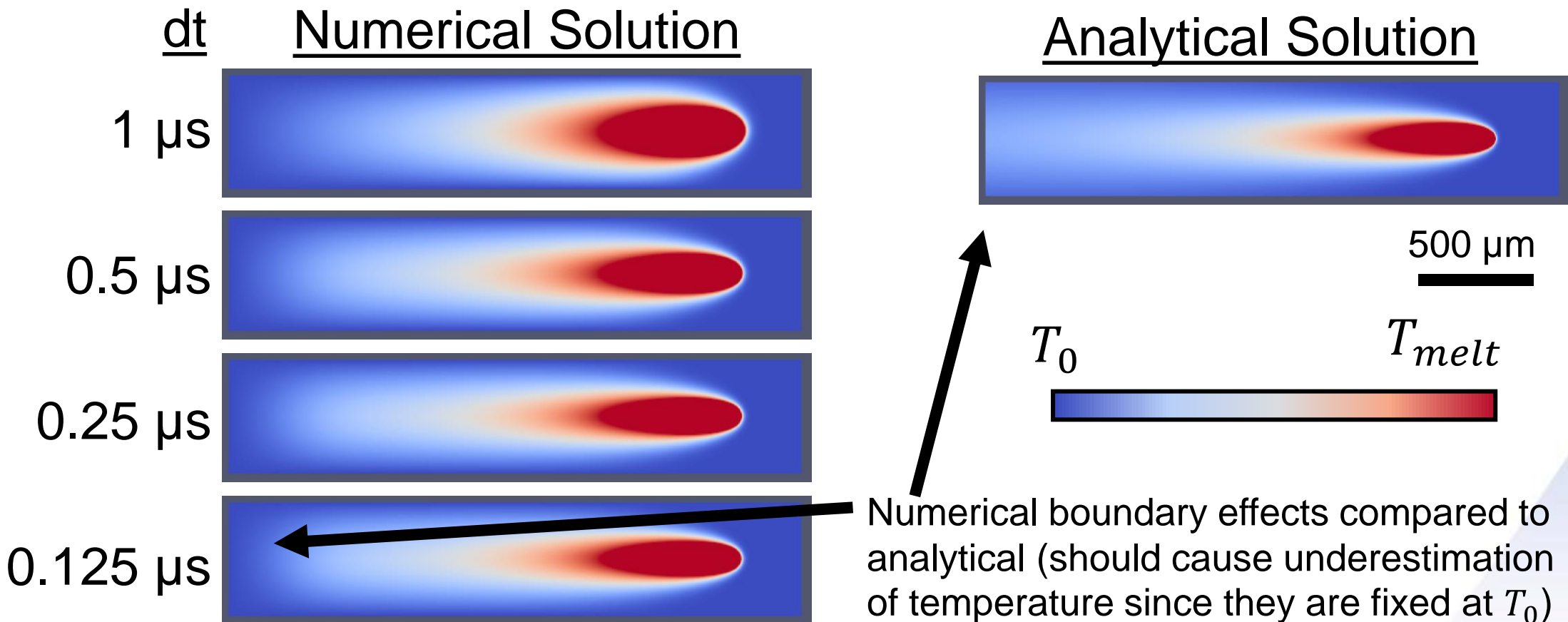
**Both - Time Step Limitation:  $dt \leq dx/v$**

- Positive
- Neutral
- Negative



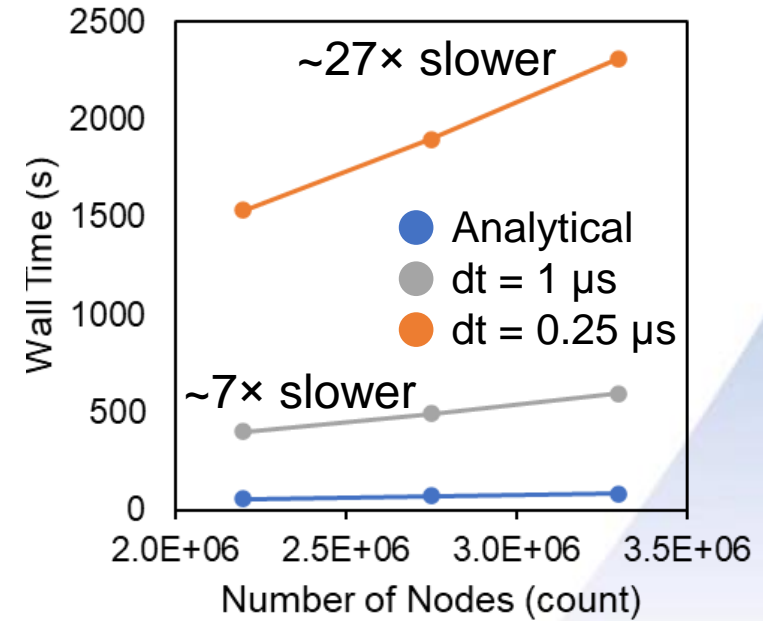
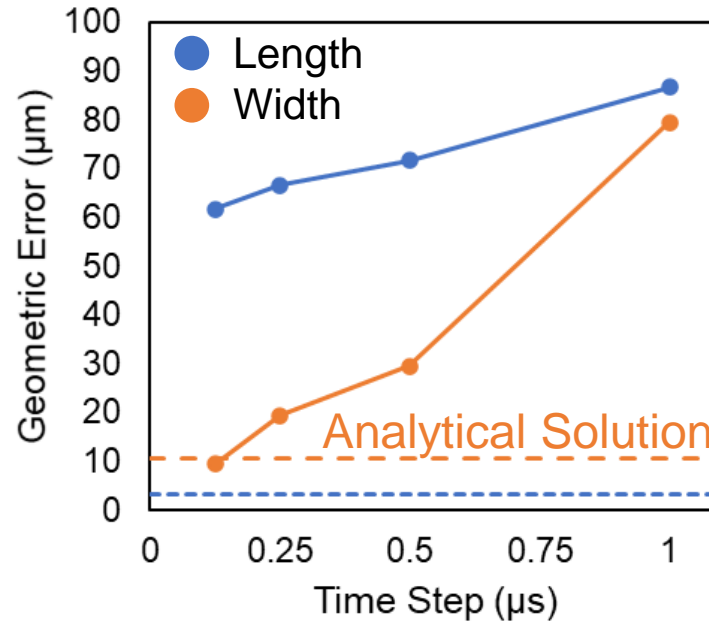
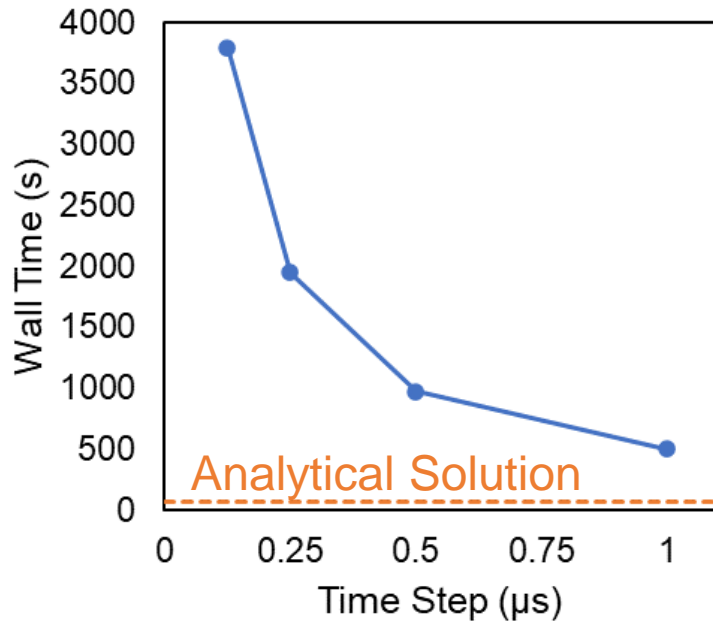
# Influence of Time Step on Temperature

The numerical solution was compared to the analytical solution to estimate accuracy and characterize speed trade-off



# Influence of Time Step on Melt Pool Geometry

- Same voxel size, same thermophysical parameters
  - Analytical solution has geometric error due to voxel size (5  $\mu\text{m}$ )
- Numerical solution approaches analytical solution as time step approaches zero
  - 0.125  $\mu\text{s}$  time step requires  $\sim 50\times$  more wall time

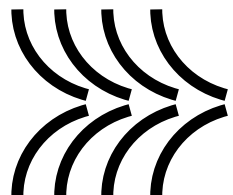


# Influence of Time Step on Grain Structure

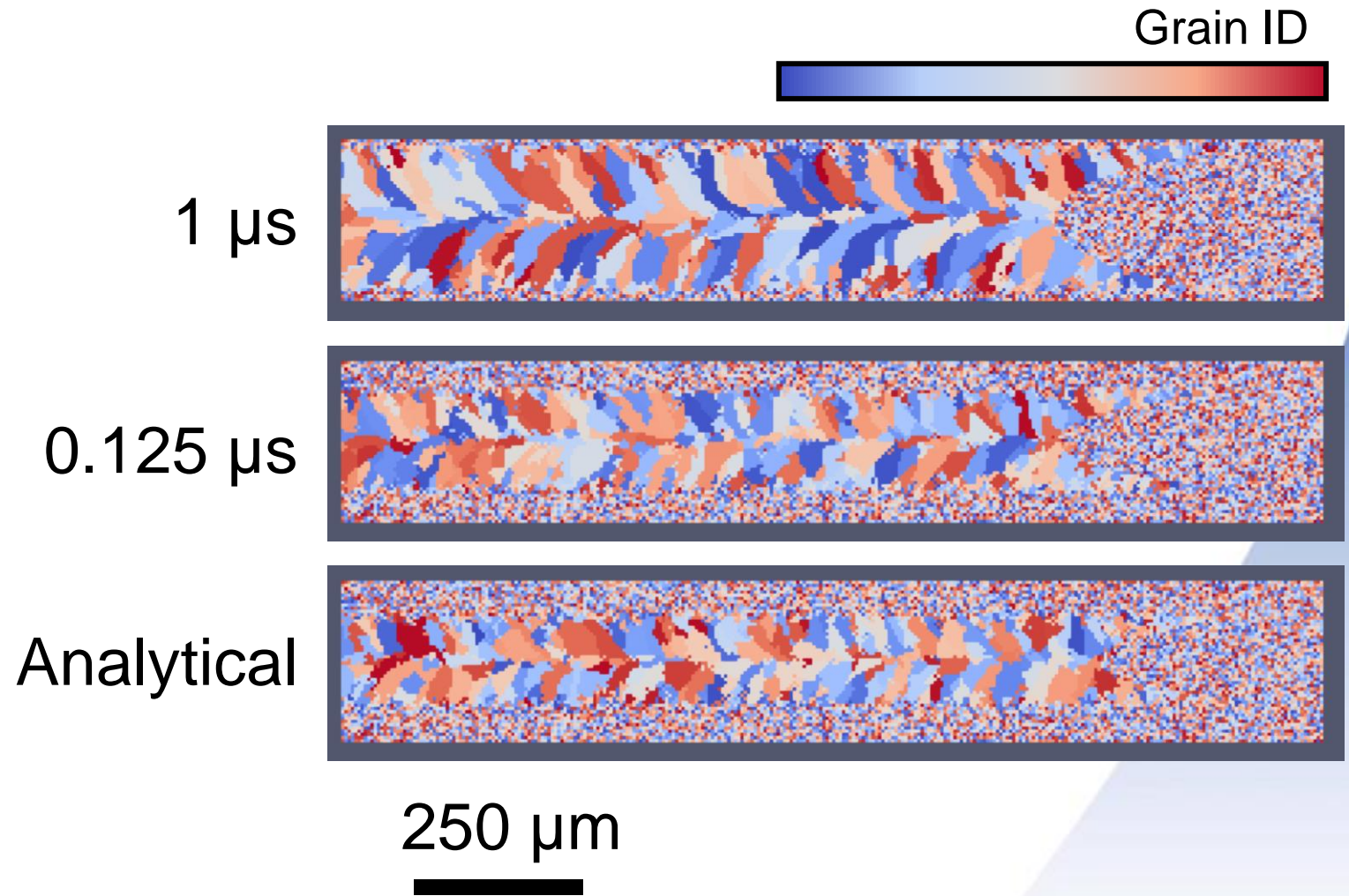
The time step has a big influence on the resulting simulated grain structure

Larger time steps cause longer and wider melt pools

These melt pools cause a smoother grain structure with a characteristic



shape



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- Comparisons with Experiment
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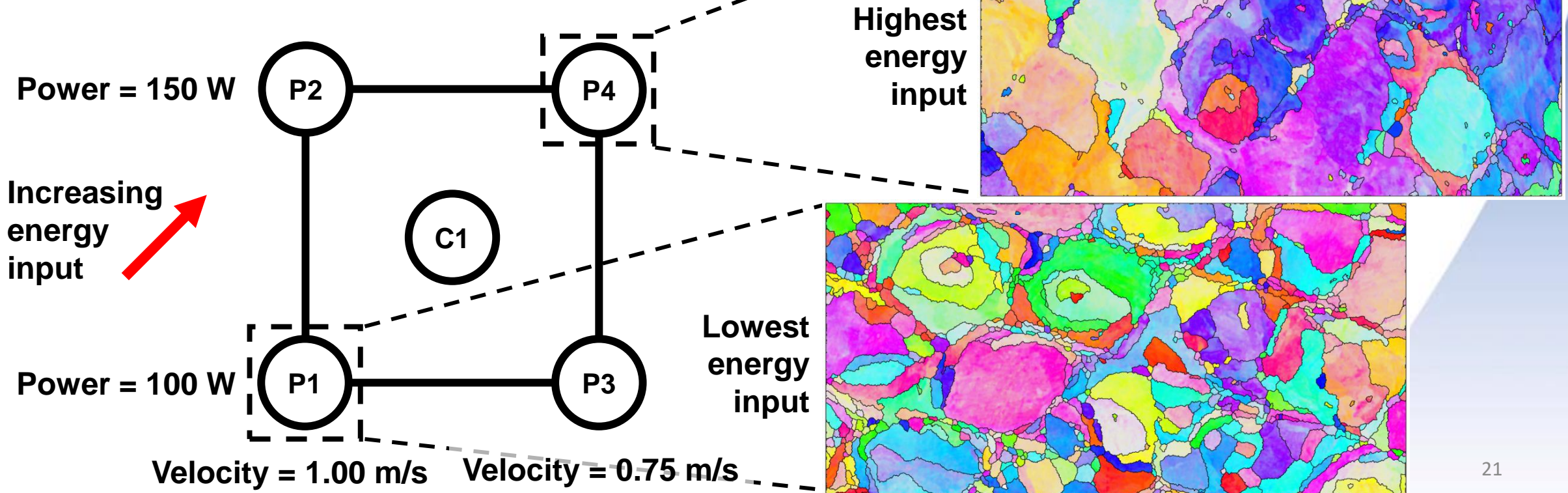
Conclusions and Summary

# Experimental Samples and Numerical Study

2<sup>2</sup> Factorial Design with Center Point (values half-way between end points)

- 600  $\mu\text{m}$  x 600  $\mu\text{m}$  x 695  $\mu\text{m}$  numerical domain (20 layers)
- Experimentally characterized P1 & P4
- Hatch Spacing = 100  $\mu\text{m}$
- Layer Thickness = 30  $\mu\text{m}$
- Rotation between layers = 67°

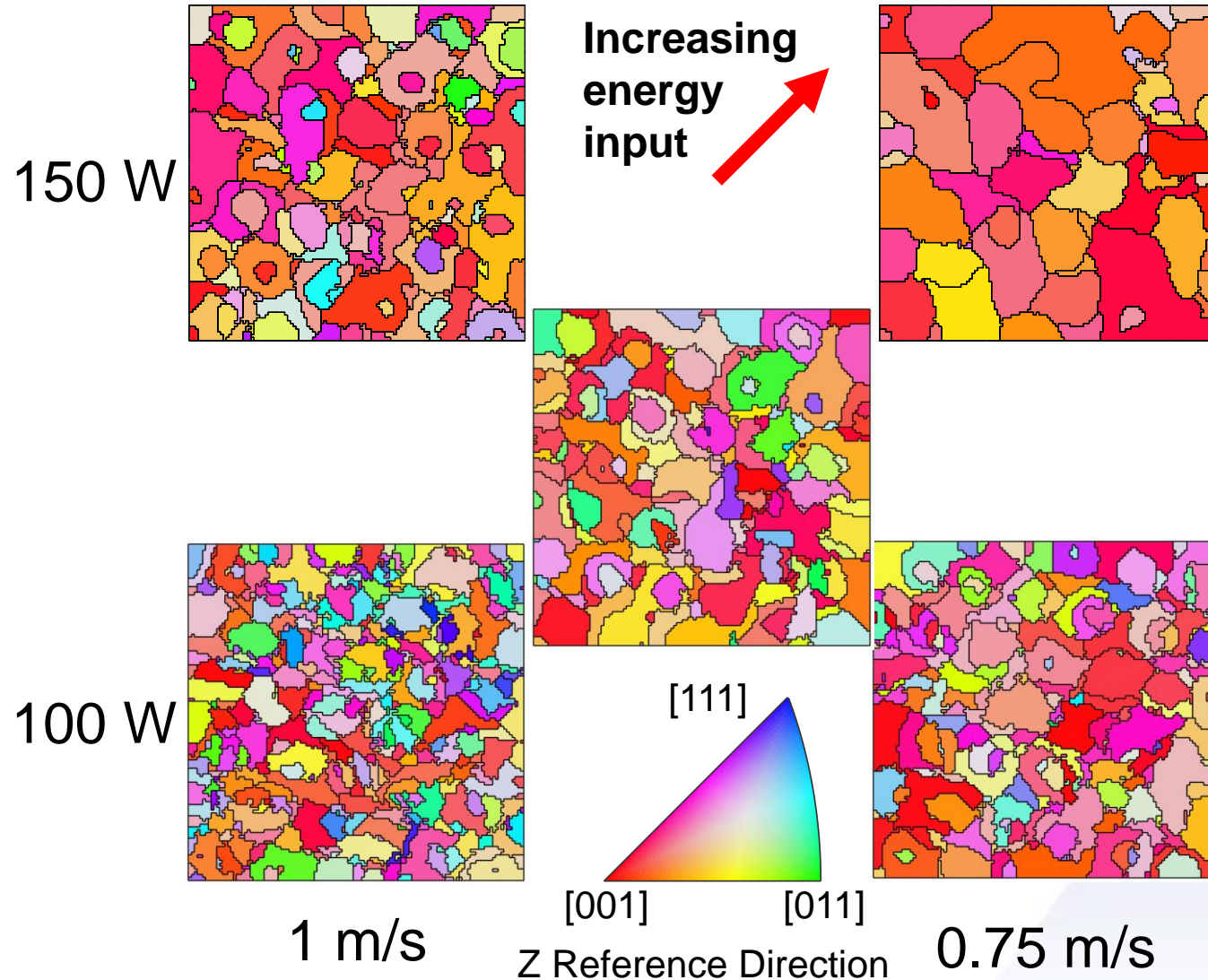
256  $\mu\text{m}$  x 512  $\mu\text{m}$  X-Y Plane



# Simulated Regions – X-Y Plane

As the input energy gets higher (low velocity and high power):

- The average grain size gets larger
- The  $\langle 001 \rangle$  texture becomes dominant
- Inner circular regions appear then disappear

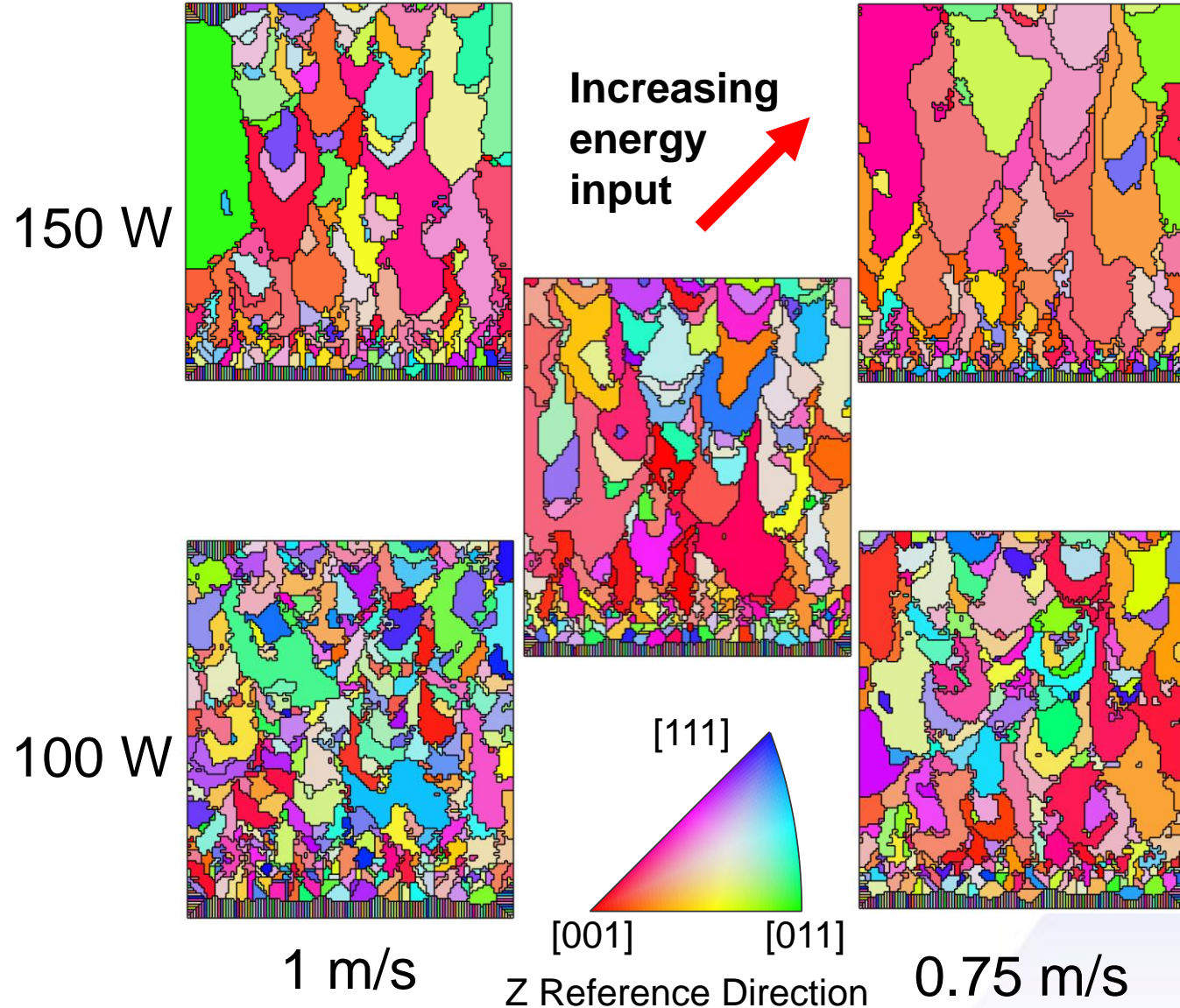


# Simulated Regions – X-Z Plane

As the input energy gets higher (low velocity and high power):

- A columnar grain structure appears
- The  $\langle 001 \rangle$  texture becomes stronger

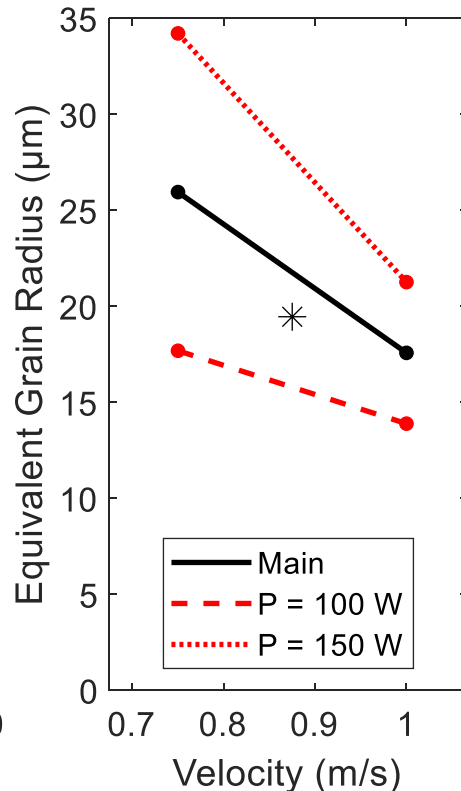
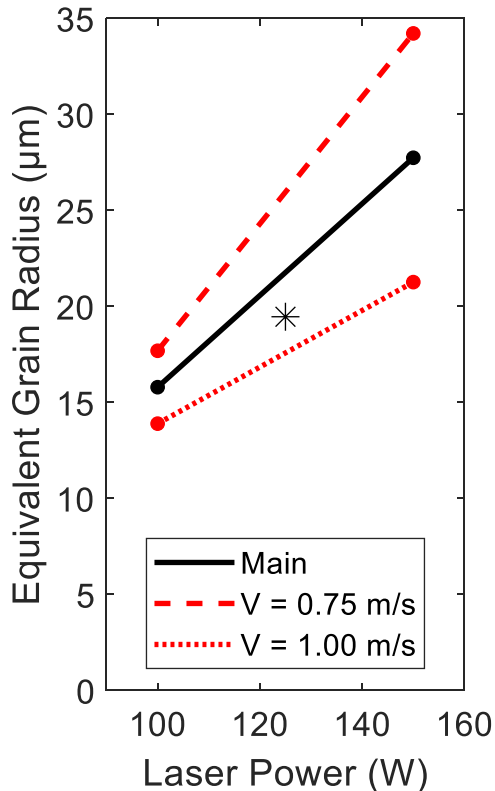
A pseudo-steady state in grain structure is reached in the middle of the simulation domain



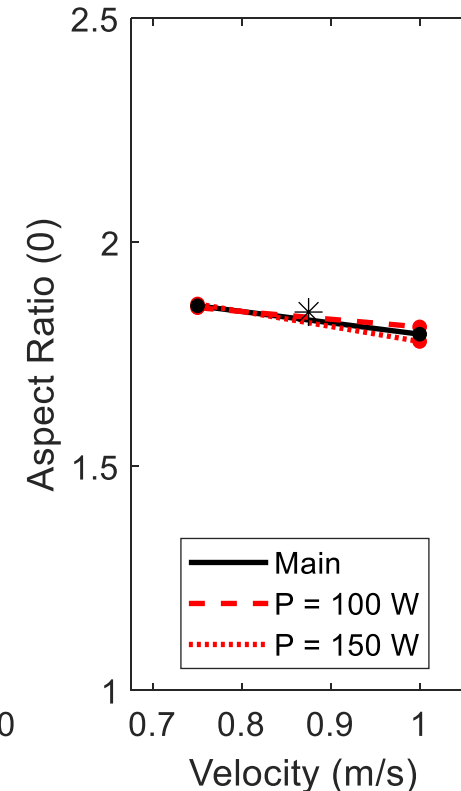
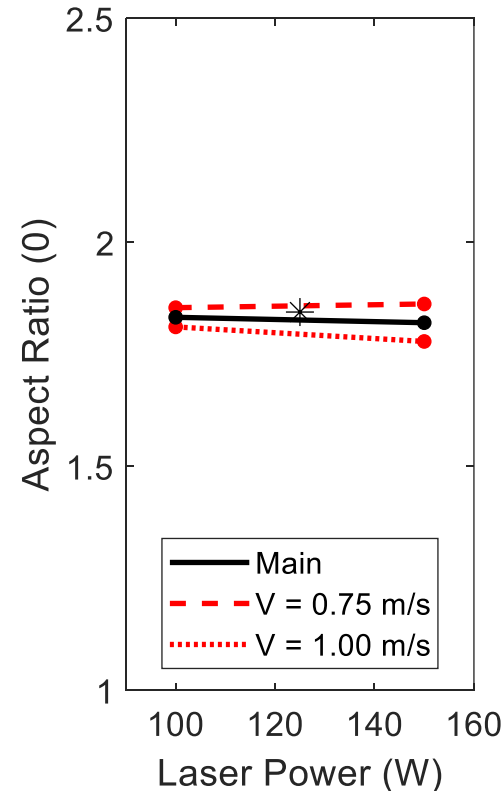
# Simulated Main and Interaction Effects

- Strong main effect of power and velocity on equivalent grain radius
- Medium interaction effect between power and velocity on equivalent grain radius
- Weak main effect velocity on aspect ratio

Equivalent Grain Radius



Aspect Ratio



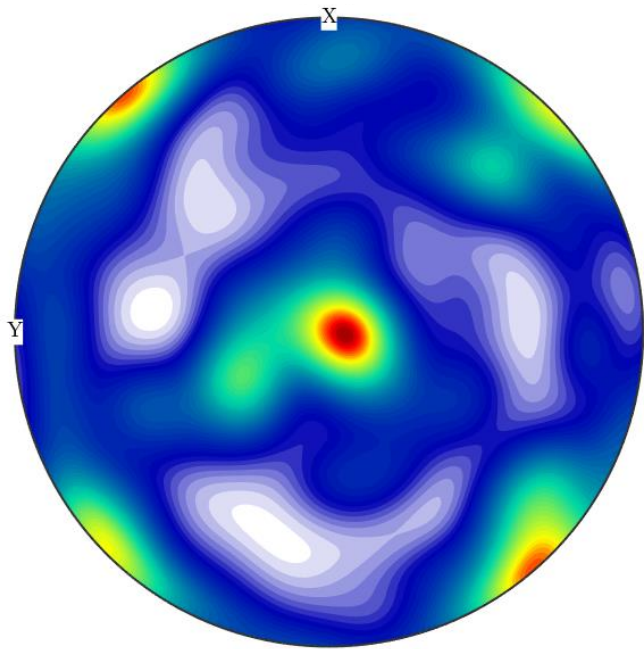
X-Y Plane,  
14 layers  
up (420 µm  
up from  
build plate



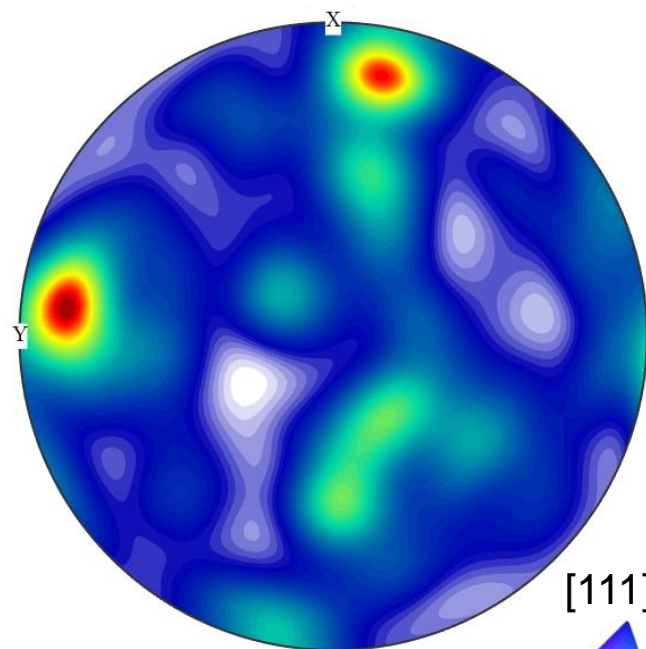
# Comparison with Experiment – Low Energy

- Simulation overestimates  $\langle 001 \rangle$  texture development (analyzed with MTEX [4])

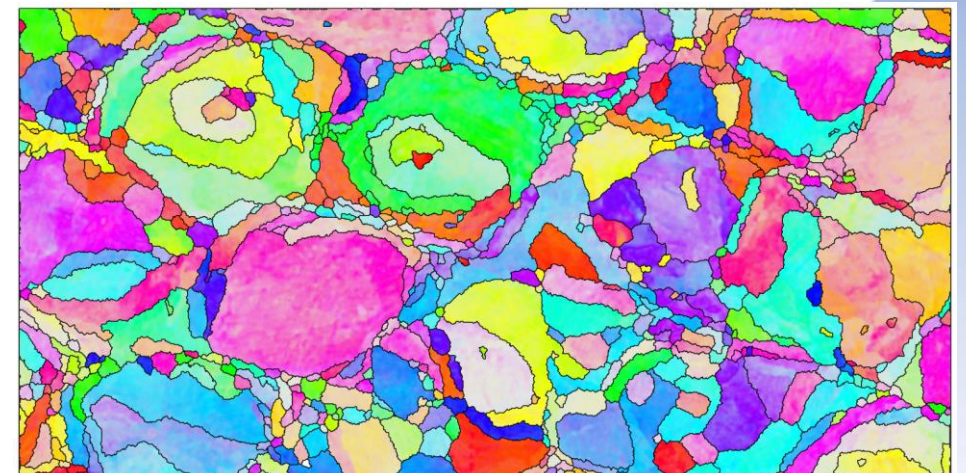
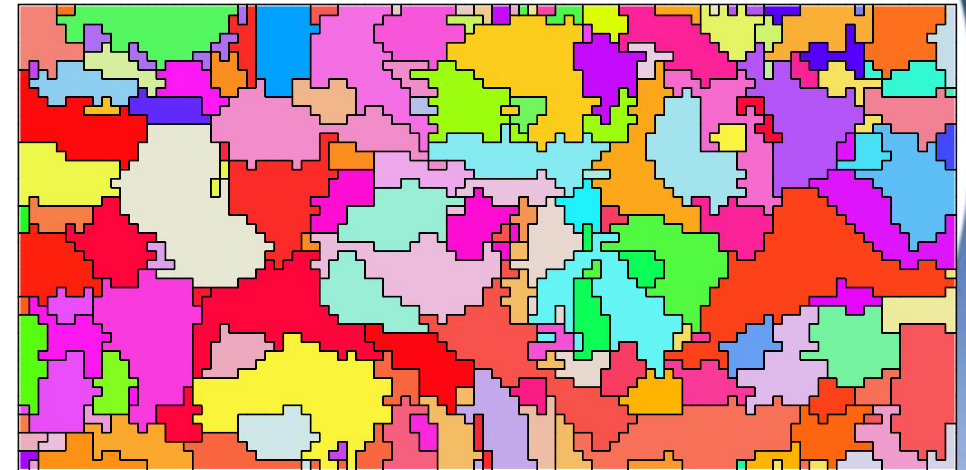
Simulation  
(100)



Experimental  
(100)



Simulation (top) and Experiment (bottom)

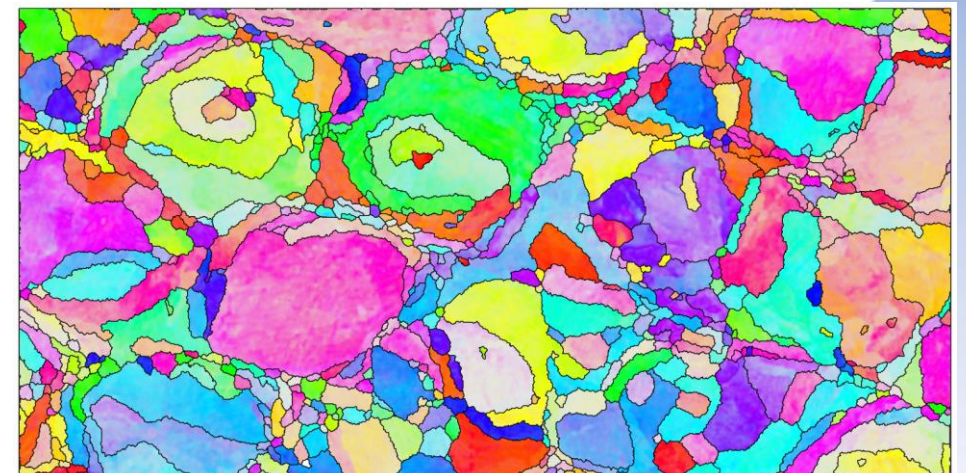
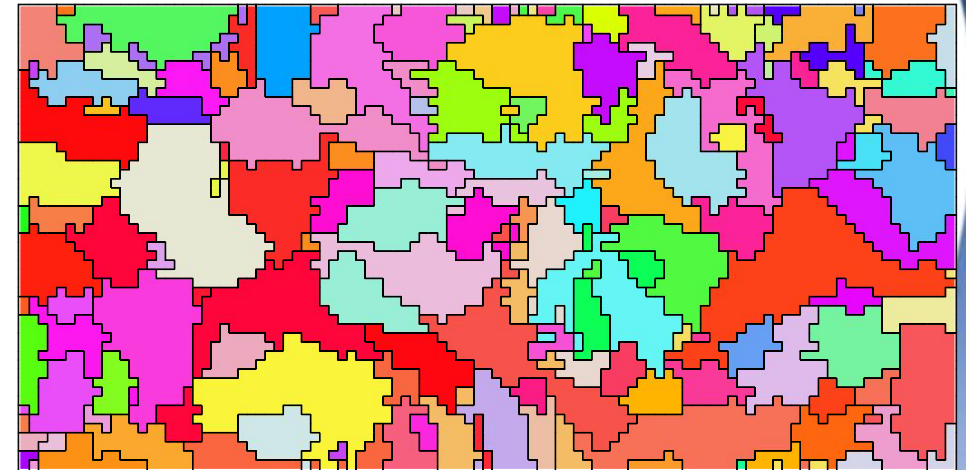
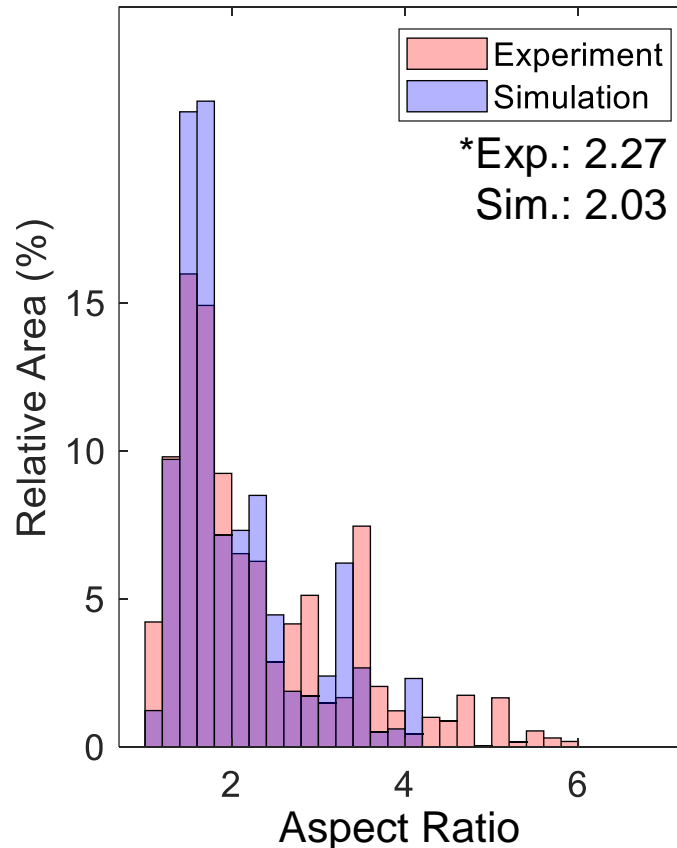
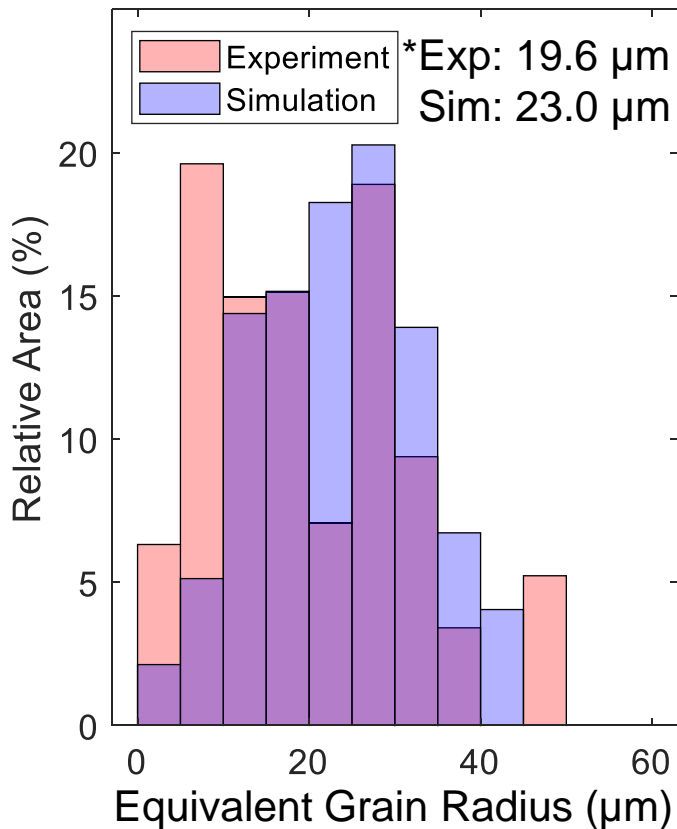


[4] Niessen, F., et al. "Parent grain reconstruction from partially or fully transformed microstructures in MTEX." *Journal of Applied Crystallography* 55.1 (2022). 180-194. <https://doi.org/10.1107/S1600576721011560>

# Comparison with Experiment – Low Energy

- Simulation overestimates equivalent radius approximately 17%
- Good agreement for aspect ratio (~12% difference)

Simulation (top) and Experiment (bottom)

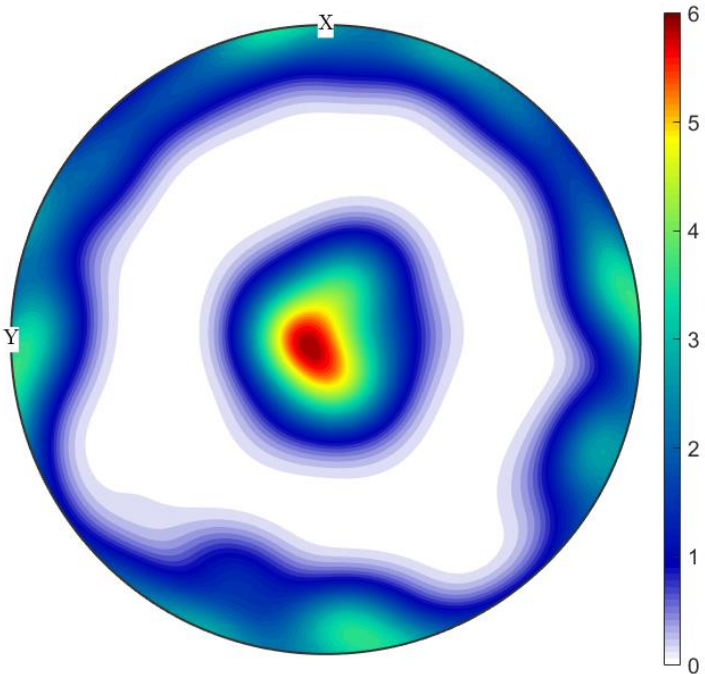


\*Area Weighted Mean Values

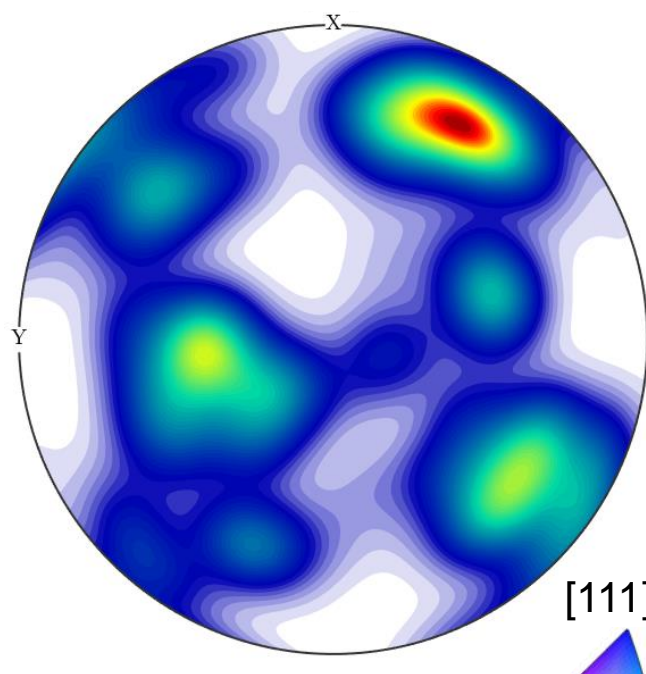
# Comparison with Experiment – High Energy

- Simulation overestimates  $\langle 001 \rangle$  texture development (analyzed with MTEX [4])

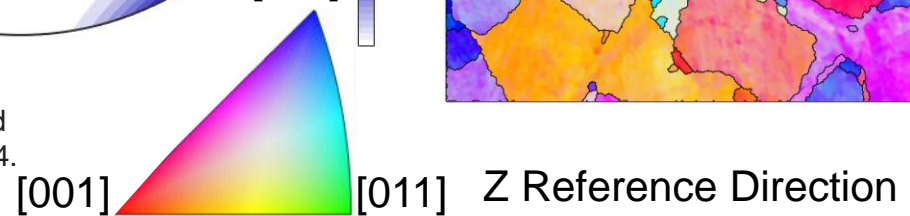
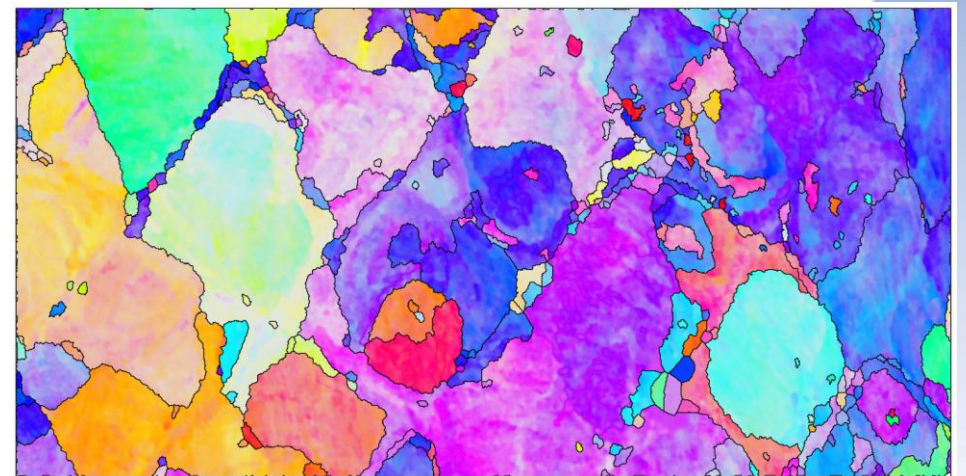
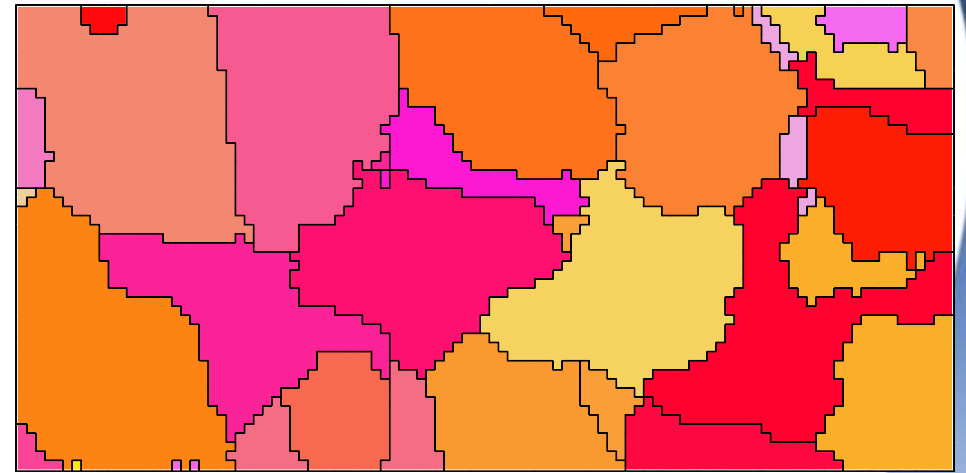
Simulation  
(100)



Experimental  
(100)



Simulation (top) and Experiment (bottom)

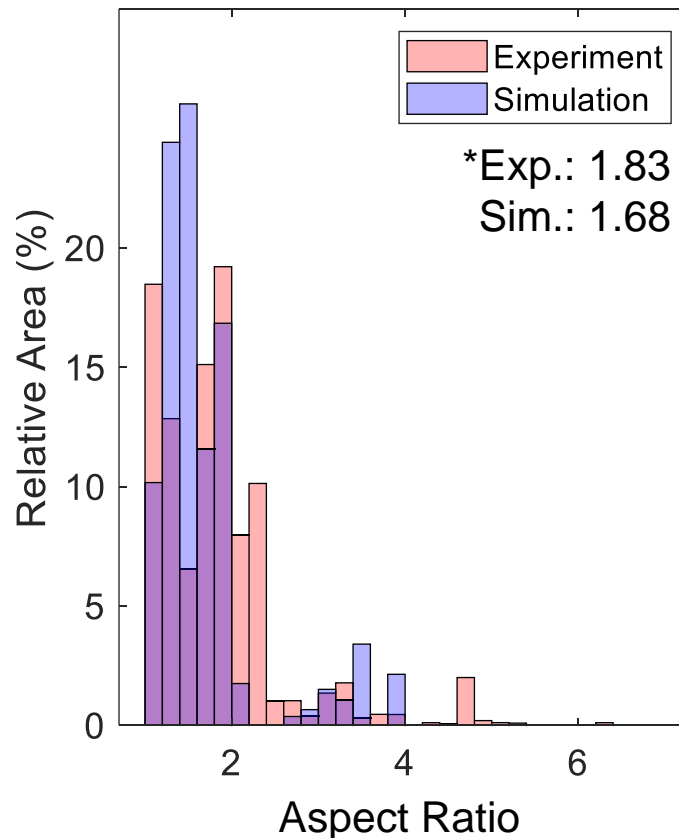
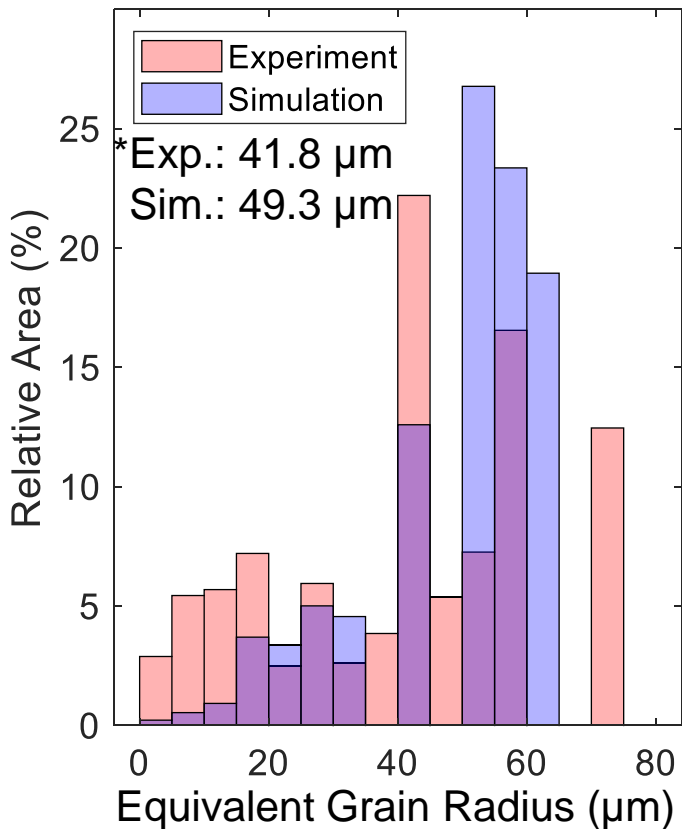


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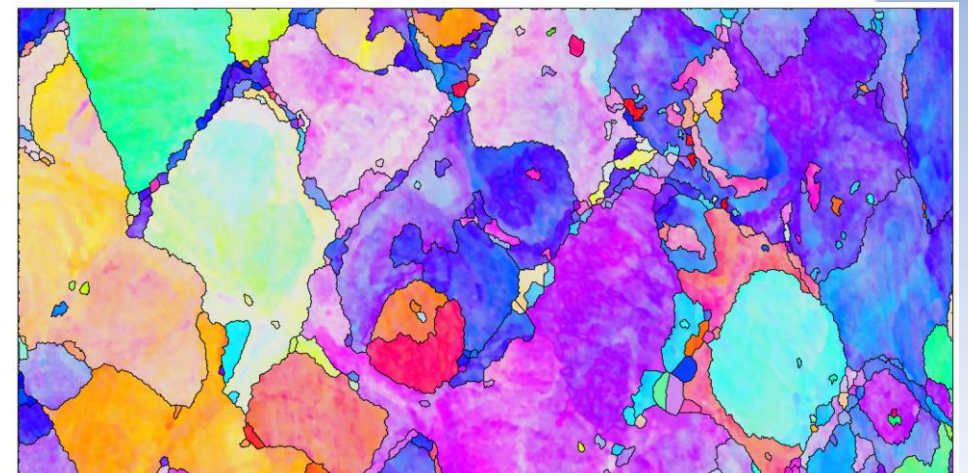
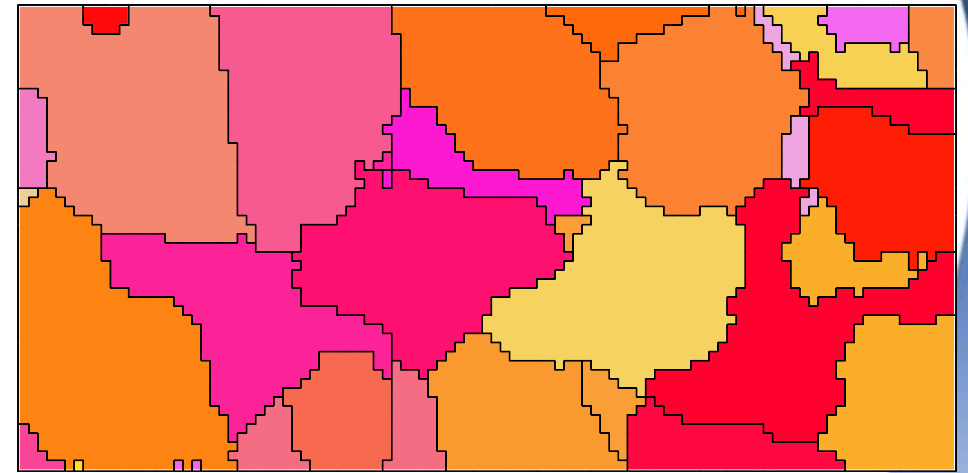
# Comparison with Experiment – High Energy



- Simulation overestimates equivalent radius approximately 18%
- Good agreement for aspect ratio (~9% difference)



Simulation (top) and Experiment (bottom)



\*Area Weighted Mean Values

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**Conclusions and Summary**

# Summary of Findings

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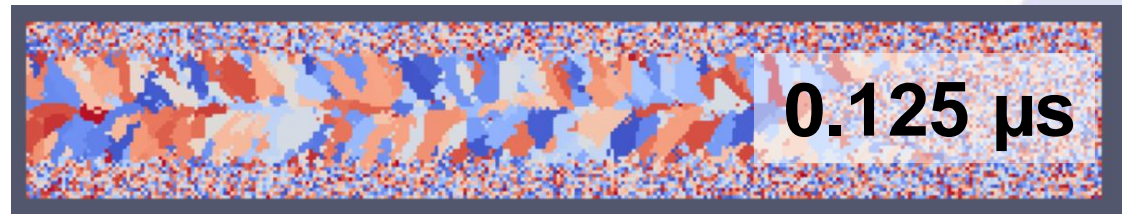
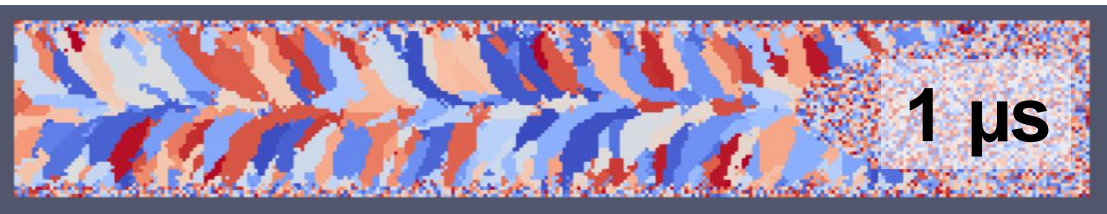


- Analytical temperature field tied Monte Carlo simulations were used to simulate Ti-6Al-4V PBF-LB
- Reasonable grain structure agreement between the simulation and experiment were observed
- A high laser power and low scanning velocity caused an increase in equivalent grain radius
- Aspect ratio was weakly impacted by the laser parameters
- The simulated crystallographic texture developed too quickly in the  $\langle 001 \rangle$  direction compared to experimental measurements

# Key Takeaways

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- The Monte Carlo method represents a suitable technique for simulating PBF-LB microstructure evolution
- There are advantages and disadvantages to using either an analytical or numerically-calculated temperature field
  - Analytical: higher computational efficiency, lower physical fidelity
  - Numerical: greater physical fidelity, numerical accuracy considerations
- If a numerical-temperature field is used, careful consideration of time step is required



# End & Acknowledgements

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Thank you!

Questions?

If you have further questions, I will be at AMBench on Wednesday and Thursday or email me at:

[brodan.m.richter@nasa.gov](mailto:brodan.m.richter@nasa.gov)

Interested in this work and engaging with us on it?  
Reach out to us....

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# Additional Slides

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# Meso-scale Modeling of Microstructure Evolution

Solidification

Texture

Nucleation

Grain Coarsening

Linking the numerical and laboratory domains are critical for conducting accurate simulations. It is very easy to overestimate the amount of coarsening present

Numerical spatial and temporal domain



Laboratory spatial and temporal domain

$dx$  = Voxel side length

$dt_{MC}$  = Numerical/Monte Carlo time step

$dt_{lab}$  = Laboratory time step

$K_{MC}$  = Simulation Constant

$K_0$  = Experimental pre-exponential

$Q$  = Experimental activation energy

$\bar{R}$  = Ideal Gas Constant

$T_{max}$  = Maximum simulation temperature

$$dt_{MC} = \frac{dx^2 K_{MC}}{K_0} \exp\left(\frac{Q}{\bar{R}T_{max}}\right) dt_{lab}$$

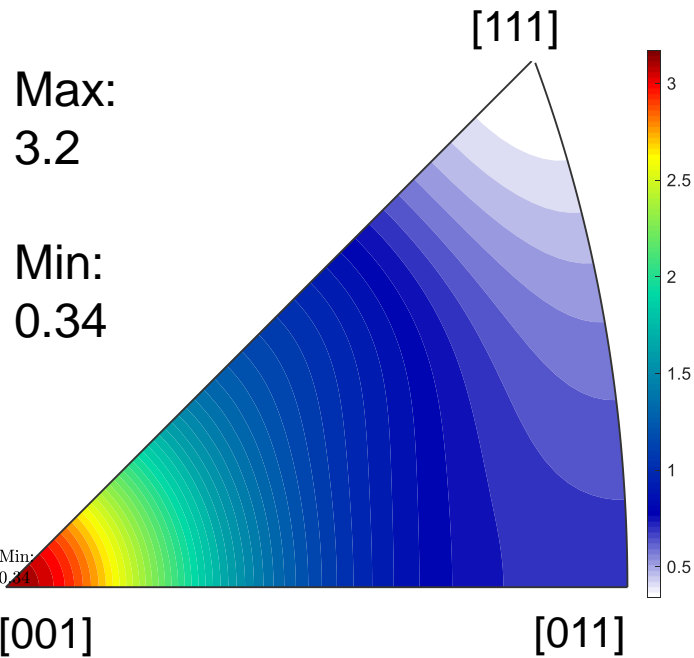
Domains are linked through heat treatment studies of grain size vs. time vs. temperature

# Comparison with Experiment – Low Energy

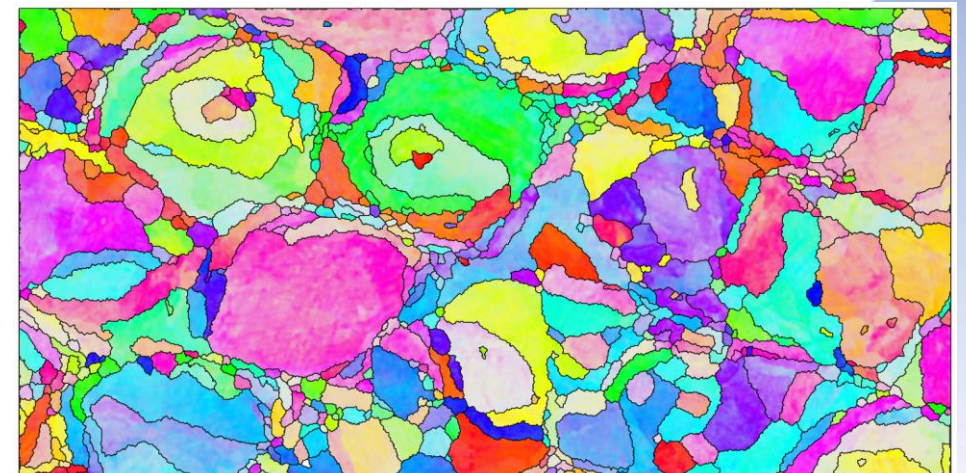
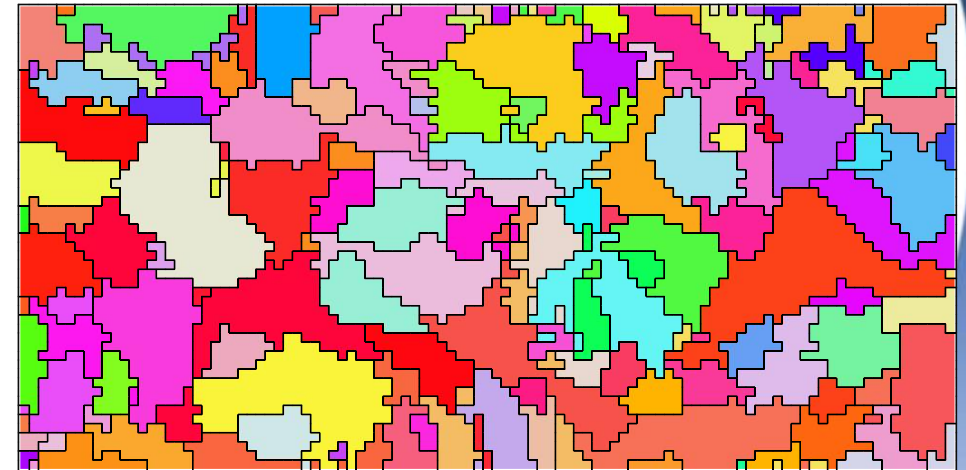
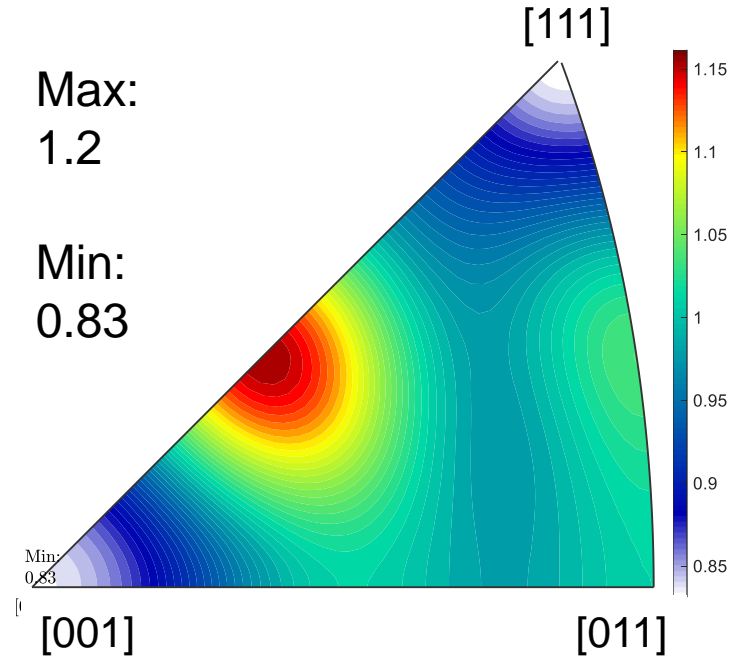
- Simulation overestimates  $\langle 001 \rangle$  texture development and overall texture strength

Simulation (top) and Experiment (bottom)

Simulation  
(100) Z-Direction IPF [4]



Experimental  
(100) Z-Direction IPF [4]



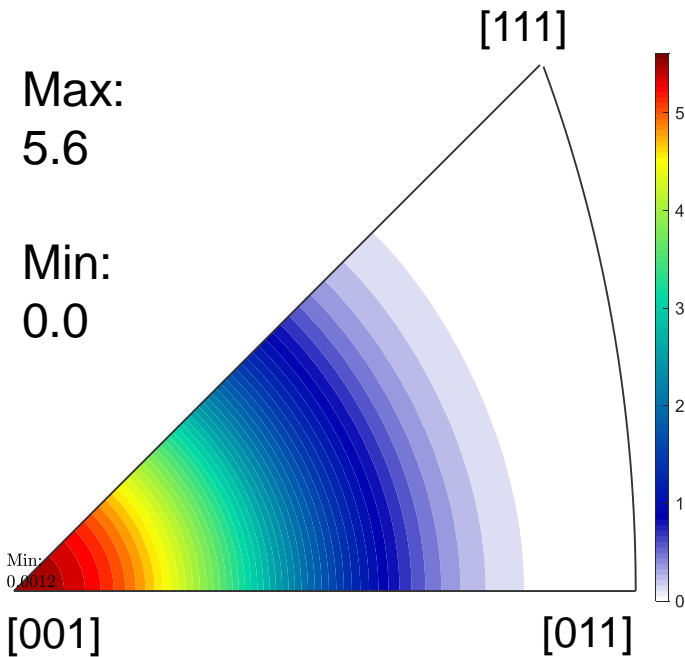
[4] Niessen, F., et al. "Parent grain reconstruction from partially or fully transformed microstructures in MTEX." *Journal of Applied Crystallography* 55.1 (2022). 180-194. <https://doi.org/10.1107/S1600576721011560>

# Comparison with Experiment – High Energy

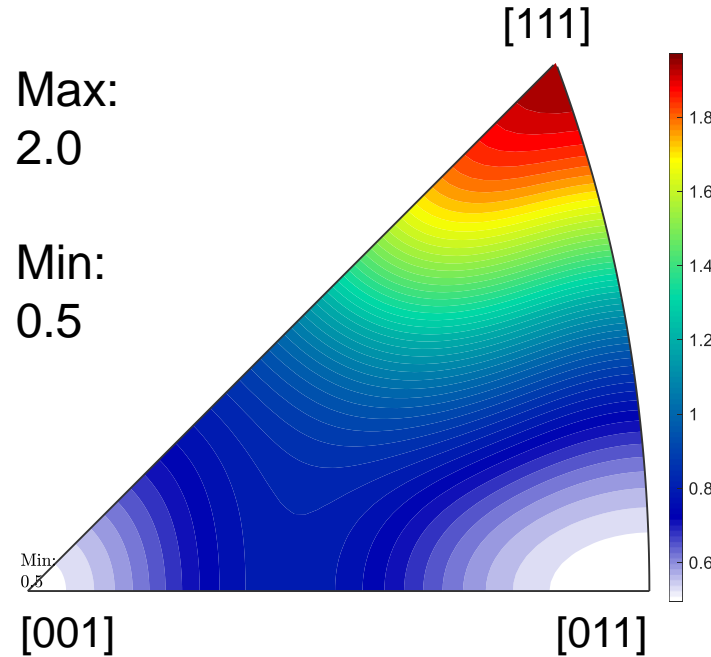


- Simulation overestimates  $\langle 001 \rangle$  texture development and overall texture strength

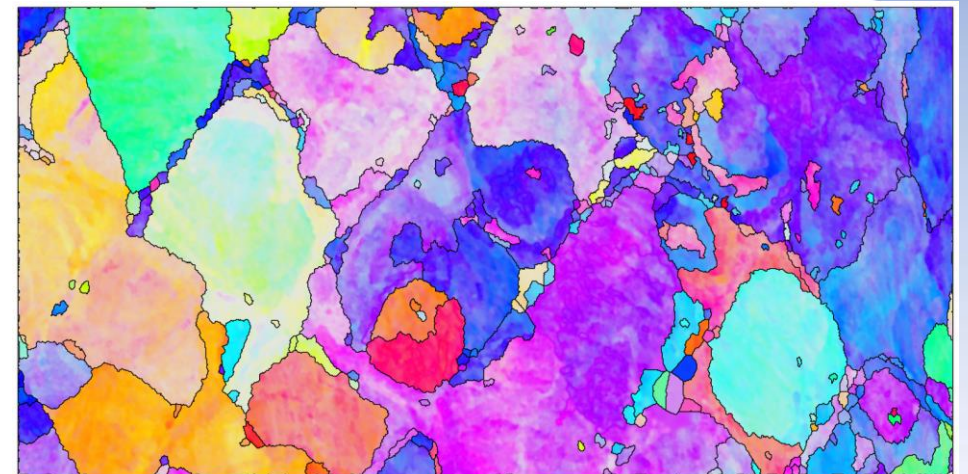
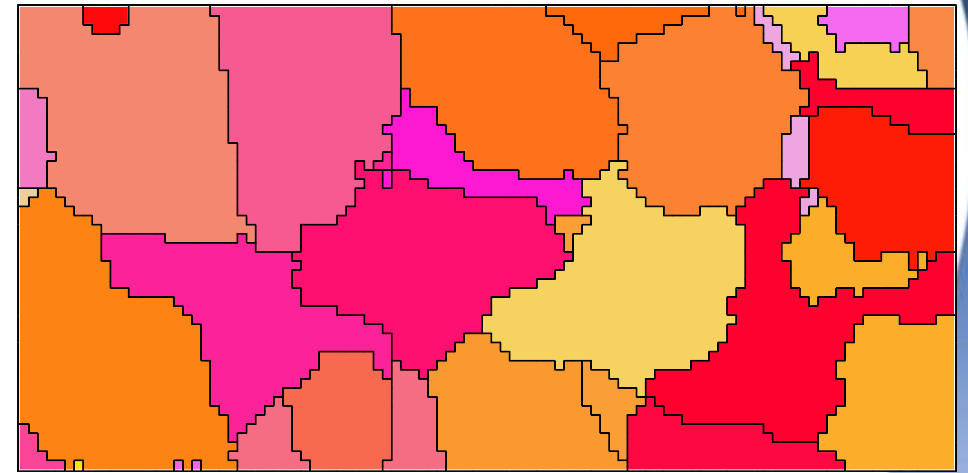
Simulation  
(100) Z-Direction IPF [4]



Experimental  
(100) Z-Direction IPF [4]



Simulation (top) and Experiment (bottom)



[4] Niessen, F., et al. "Parent grain reconstruction from partially or fully transformed microstructures in MTEX." *Journal of Applied Crystallography* 55.1 (2022). 180-194. <https://doi.org/10.1107/S1600576721011560>