

1
2
3 Non-Gaussian Distributions of TOA SW Flux as Observed by MISR and CERES
4

5 Jae N. Lee^{1,2} and Dong L. Wu²
6

7 ¹Joint Center for Earth Systems Technology, University of Maryland, Baltimore County,
8 Baltimore, Maryland

9 ²NASA Goddard Space Flight Center, Greenbelt, Maryland
10

11 **Key Points:**

- 12 • The probability density function of the TOA SW flux is not normally distributed but
13 positively skewed, with a near-global median value of $\sim 3 \text{ W/m}^2$ less than the mean.
14
- 15 • Hemispheric asymmetry exists with the 10:30 AM local time TOA SW observations from
16 Terra platform. SH reflects about $1 - 4 \text{ W/m}^2$ more SW flux than NH, with the MISR and
17 CERES Single Scanner Footprint (SSF1deg) products observed from Terra.
18
- 19 • While the characteristics of the MISR and CERES SW fluxes are broadly agree with each
20 other, differences in the regional PDF from the two SW fluxes are substantially different
21 over high cloud regions and high altitude regions.
22

Abstract

24 The Top of Atmosphere (TOA) shortwave (SW) flux, converted from Terra Multi-angle Imaging
25 SpectroRadiometer (MISR) narrow band albedos, is compared with that measured from Clouds
26 and the Earth's Radiant Energy System (CERES). We describe the probability density function
27 (PDF) of the monthly TOA SW flux and how the statistical third moment, skewness, can impact
28 the quantification of the flux. The PDF of the SW flux is not normally distributed but positively
29 skewed. In both sets of observations, the near-global (80S-80N) median value of the SW flux is
30 $\sim 3 \text{ W/m}^2$ less than the mean value, due to the positive skewness of the distribution. The near-
31 global mean TOA SW flux converted from MISR is about 7 W/m^2 ($\sim 7\%$) less than CERES
32 measured flux during the last two decades. Surprisingly, hemispheric asymmetry exists with
33 TOA SW observations from Terra platform. SH reflects 3.92 W/m^2 and 1.15 W/m^2 more mean
34 SW flux than NH, from MISR and CERES Single Scanner Footprint products, respectively. We
35 can infer that the offsetting by morning clouds in the SH is greater than the effect of hemispheric
36 imbalance of SW flux caused by different land masses in two hemispheres. While the
37 characteristics of the two SW fluxes broadly agree with each other, differences in the regional
38 PDF from two different SW fluxes are substantially different over high cloud regions and high
39 altitude regions. Our analysis shows that some parts of the different skewness from two
40 measurements may be attributed to the different calibration of the radiance anisotropy over high
41 cloud scenes.

Plain Language Summary

44 In this work, we describe the non-Gaussian probability density functions (PDFs) of the Top of
45 Atmosphere (TOA) reflected shortwave (SW) flux. For non-Gaussian PDFs, the frequency of
46 occurrence is not symmetric with respect to the mean. The TOA SW PDFs are relatively thick in
47 the left tail, because there exists a low boundary of zero reflectance when the Earth don't get
48 solar insolation during the polar nights. In comparison of two satellite measurements, we show
49 that how the statistical third moments of the TOA SW flux can impact the quantification of the
50 averaged flux. Gaussian distributions are naturally assumed in atmospheric data analysis. This,
51 however, is not always true for the TOA SW flux distribution.

52 To quantify the global TOA SW flux, reliable and consistent satellite measurement is required.
53 The two instruments, MISR and CERES, on the Earth Observing System Terra satellite
54 (launched in December of 1999) offer a rare opportunity to observe the TOA reflected SW flux
55 from the same constellation. Hemispheric asymmetry exists in the 10:30 AM local time TOA
56 SW observations from Terra platform. SH reflects about $1 - 4 \text{ W/m}^2$ more SW flux than NH,
57 with the MISR and CERES Single Scanner Footprint (SSF1deg) products observed from Terra.

58

59

60

61

62

63

64

65 **1 Introduction**

66 Quantifying the amount of solar insolation reflected back to space at the top of the atmosphere
67 (TOA) is pivotal for an assessment of Earth's radiation balance (Trenberth , 2009; Stephens et al.
68 2012; Wild et al., 2015; Loeb and Wielicki 2015; L'Ecuyer 2017). This reflected SW energy is
69 initially forced by diurnal and seasonal variations of the incoming solar insolation. Caused by the
70 obliquity of the Earth, each hemisphere receives more solar radiation during its summer when
71 the hemisphere is tilted toward the Sun, and less during winter when it is tilted away.

72 Distribution of TOA reflected SW flux (TOA SW flux) is a mixture of complex multiple
73 processes of surface and atmospheric reflection from different types of surface and atmospheric
74 conditions. Furthermore, the hemispheric asymmetry of the global land and ocean masses builds
75 on additional complexity in characterization of the TOA SW flux. The 11-year solar cycle
76 variation of the solar insolation also can be factored in the decadal variations, however, the effect
77 of solar cycle is expected to be negligible as it's magnitude is less than 0.01% (Kopp and Lean,
78 2011).

79
80 Besides the accurate assessment of mean (μ) and standard deviation (σ) of the flux, a careful
81 examination on the normality of TOA SW flux distribution is meaningful because the TOA SW
82 flux distribution reflects the hemispheric asymmetry of solar insolation and land masses. A
83 Gaussian, or Normal distribution is a type of probability distribution for a random variable, as
84 the probability density function (PDF) is symmetric on either side from the mean with no
85 skewness. Partly due to the central limit theorem (Feller, 1971) which states the average of many
86 observations of a random variable approaches a normal distribution, the mean of the normal
87 distributions are commonly used to represent observed and modeled large scale atmospheric and
88 oceanic variables. However, in fact, normality of the distribution is one of the underlying
89 assumptions in data analysis. When PDFs are deviated from the normal distribution, they are not
90 well characterized by the μ and σ . Not like a normal distribution, it would be insufficient to
91 deduce the states of tail probabilities even if the changes of μ and σ are accurately estimated. The
92 skewness of the distribution can cause a complexity in quantifying trends (Sardeshmukh et al.,
93 2015) because the shape of the heavy tail, high reflected flux in TOA SW case, may not be
94 preserved with fastly vanishing high-latitude snow and ice.

95
96 In this work, we describe the non-Gaussian probability density functions of TOA SW flux, in
97 comparison of two satellite measurements from MISR and CERES, and how the statistical third
98 moments of the TOA SW flux can impact the quantification of the globally averaged flux. We
99 also quantify the hemispheric differences of TOA SW flux between NH and SH and how they
100 are dependent on observing constellation of Terra and Aqua.

101
102 To quantify the global climatology of TOA SW flux, reliable and consistent satellite
103 measurement is required. The two instruments, MISR and CERES, on the Earth Observing
104 System Terra satellite (launched in December of 1999) offer a rare opportunity to observe the
105 TOA reflected SW flux from the same constellation. Since no space-based measurement, so far,
106 can measure radiances in all viewing angles simultaneously, the radiance-to-flux conversion has
107 been recognized as a major source of uncertainty in the satellite derived TOA SW flux (Loeb et
108 al., 2006). Even after considerable improvements in Angular Distribution Models (ADMs),
109 challenges are still remaining in the radiance to flux conversion, due to ADMs' strong

110 dependence on clouds and high-albedo surfaces (Loeb et al.; 2007; 2018; Gristey et al., 2021;
111 and references therein).

112
113 The MISR instrument provides information on bidirectional reflectance anisotropy (Diner et al.,
114 2005) and inconsistency between the MISR and CERES fluxes can be largely attributed to
115 limitations in the integration of bidirectional reflectance and ADMs (Loeb et al., 2006). Over the
116 overcast ocean scenes within 75S-75N, the uncertainty in the MISR albedos due to narrow-to-
117 broadband albedo conversion is ~2%. The difference between the MISR and CERES albedos due
118 to the angular distribution model (ADM) is estimated to be ~4% (Sun et al., 2006).

119 **2 Data**

120 **2.1 MISR**

121
122 MISR's arrangement of nine cameras provides near-simultaneous measurements of reflective
123 SW radiances from multi-angle views in four spectral bands (Diner et al., 1998). Reflected SW
124 spectral radiances are measured at nadir and at 26.1°, 45.6°, 60° and 70.5° forward and aft of
125 nadir along the satellite track, in blue (446±21nm), green (558±15nm), red (672±11nm), and
126 near-infrared (866±20nm) bands. By deriving albedos from nine angular measurements, MISR
127 has an advantage of retrieving accurate albedos for inhomogeneous clouds (Diner et al., 2005;
128 MISR ATBD, <https://eosppo.gsfc.nasa.gov/sites/default/files/atbd/atbd-misr-08.pdf>).

129
130 MISR produces three TOA spectral albedo products; local, restrictive, and expansive albedos.
131 Local albedo estimates the reflected flux passing through an unobscured 2.2 km domain
132 reflecting level of reference altitude. The restrictive albedo is an estimate of the reflected flux
133 which originates from the reflecting surfaces within 35 km domain. The expansive albedo is an
134 estimate of the flux passing through the TOA regardless of where it is reflected.

135 We used the restrictive albedos in this study, since it is a useful measure of scene-dependent
136 properties and most analogous to the CERES determination of the TOA albedo from a single
137 view.

138
139 The methodology applied to compute MISR broadband albedo involves a regression of 4 spectral
140 narrow band albedos onto CERES broadband albedo (Sun et al., 2006). Then broadband MISR
141 restrictive albedo (α) is converted to TOA SW flux by multiplying incident solar insolation (S_0)
142 at a given time and location, i.e., TOA SW flux = $\alpha \cdot S_0$. Incident solar insolation, S_0 , is acquired
143 from CERES SSF1deg product at a given time and location.

144
145 In this study, we utilized the restrictive broadband albedos from MISR Level-3 albedo product
146 (Diner, 2009), since March 2000 to December 2020, from NASA Atmospheric Science Data
147 Center (<https://asdc.larc.nasa.gov/documents/misr/version/pge12b.html>). Given the sampling
148 nature of the MISR observation, we used monthly mean data products.

149 **2.2 CERES**

150
151
152 The CERES Edition 4.1 monthly mean 1 degree gridded Single Scanner Footprint (SSF1deg)
153 TOA SW flux products from Terra and Aqua satellite (Doelling, 2015) and Energy Balanced and
154 Filled (EBAF) products (Doelling, 2019) are analyzed to be compared with converted

155 broadband MISR flux. The SSF1deg product began in March 2000 and provides global coverage
156 sampled only at specific times of the day (Doelling et al., 2013). As well as MISR, the CERES
157 instrument on EOS Terra measures TOA SW flux in a sun-synchronous ascending orbit with an
158 equator crossing time of near 10:30 AM local time. The CERES albedo retrieval is based on a set
159 of combined empirical and theoretical scene-dependent ADMs (Kato, 2005; Loeb et al., 2005;
160 Loeb et al., 2009; Su et al., 2015a; 2015b; Ham et al., 2015; and references there in). The
161 selection of ADMs depends on the cloud types and a cloud parameter which is determined from
162 the cloud fraction, optical depth, cloud height, and phase of clouds.

163
164 In this study, we focused on examining the consistencies and differences of the TOA SW flux
165 from the MISR and CER_SSF_Terra-FM1-MODIS_Edition4A datasets. Where MISR data is not
166 available in high latitudes, we also omitted CERES data for a fair comparison. We obtained the
167 CERES SSF1deg monthly TOA SW and cloud height data from ([https://ceres-
168 tool.larc.nasa.gov/ord-tool/jsp/SSF1degEd41Selection.jsp](https://ceres-tool.larc.nasa.gov/ord-tool/jsp/SSF1degEd41Selection.jsp)).

169 **3 Results**

170 **3.1 Non-Normality of the TOA SW flux**

171
172 In this section, we describe the non-Gaussian distributions of TOA SW flux, in comparison of
173 two satellite measurements from MISR and CERES. As shown in Figure 1, the PDFs of MISR
174 and CERES TOA SW flux are not only non-Gaussian, but are distinctly skewed distributions
175 which have more population of the data on the right side of the maximum population. The PDFs
176 of the monthly broadband TOA SW flux from MISR and CERES are shown in Figure 1(a),
177 where the area under the PDF accounts for the near-global (80S - 80N) distribution of monthly
178 mean TOA SW flux at each 1° by 1° grids. The distribution of the data indicates that monthly
179 mean TOA SW flux extends from 0 to 410 W/m².

180
181 The PDFs of broadband flux show one major peak at 58 W/m² and 65 W/m² for MISR and
182 CERES, respectively. While the general features of PDFs of the near-global TOA SW
183 distribution from the two observations are in good agreement with ~7 W/m² offset at the peak,
184 they commonly show that SW fluxes are obviously not normally distributed. The right side of the
185 distribution is heavily tailed with high reflectance values from snow and ice, but the left side of
186 the distribution has no tails. The PDFs are relatively thick in the left tail, because TOA SW flux
187 cannot be negative with a low boundary of zero reflectance when they don't get solar insolation
188 during the polar nights.

189
190 Similarly, the PDFs of the four narrow band MISR TOA SW fluxes centered at blue (C1:
191 446±21nm), green (C2: 558±15nm), red (C3: 672±11nm), and near-infrared (C4: 866±20nm) are
192 shown in Figure 1(b). The four spectral PDFs also show similar skewed non-Gaussian features.

193
194 For a Gaussian, or Normal distribution, the PDF is symmetric on either side from the mean.
195 Without any prior assumptions, the TOA SW distributions are deviated from the normal
196 distribution, they are not well characterized by the μ and σ . Not like a normal distribution, it
197 would be insufficient to deduce the changes in tail probabilities from the μ and σ , even if the
198 changes of μ and σ are accurately estimated.

199

200 Skewness is a measure of the asymmetry of the probability distribution about its mean.
201 Conventionally, positive skewness indicates that more populations of data are located on the
202 right tail from the maximum population. Reflecting the positive skewness, the TOA SW flux
203 distributions show that more populations are present on the right side of the distribution where
204 the fluxes are larger than the mean or median. The right tail of the SW flux distribution is
205 extremely important, since the high flux greater than 300 W/m^2 is from the Arctic and Antarctic
206 region over high albedo snow and ice surface. The right tail of the SW flux is also related to
207 cloud properties and the estimating the average flux without considering cloud types may cause
208 systematic biases (Barkett et al., 1996). The skewness of the distribution can add complexity in
209 quantifying global TOA SW climatologies and trends because the shape of the distribution may
210 not be preserved with a changing environment. For example, fastly vanishing high-latitude snow
211 and ice can cause a thickening of the right tail without affecting the left tail of the distribution.

212 Figure 2 is a schematic of the MISR TOA SW flux, which shows the PDF deviated from the
213 normal distribution. The mean and the standard deviation of the not area-weighted near-global
214 SW flux from MISR (80S - 80N) is 98.6 W/m^2 , and 66.19 W/m^2 , respectively. The global (90S-
215 90N), annual mean all-sky TOA SW flux from CERES Energy Balanced and Filled (EBAF) data
216 was 99.7 W/m^2 , which is equivalent to a global albedo of 0.293 (Stephens et al., 2015).

217
218 The red curve of the plot is the best-fit normal distribution with the same mean and standard
219 deviation from MISR. The yellow curve is a normal distribution with a mean at the mode, where
220 the most population is located. The blue curve is a best-fit lognormal distribution using the log of
221 TOA SW flux values. The median of the distribution is 83.68 W/m^2 , which is $\sim 15 \text{ W/m}^2$ less
222 than the mean. While the TOA SW flux distribution is deviated from the normal distribution, it is
223 rather close to the lognormal distribution with mean (m) and standard deviation (v) of 4.46 and
224 0.63 W/m^2 , respectively. The lognormal distribution can be potentially utilized to estimate the
225 true mean and variance of the TOA SW flux in future work, however, the conversion of the
226 lognormal to normal distribution is very sensitive to the parameters of the lognormal distribution,
227 i.e. m and v ., since the true mean (μ) and standard deviation (σ) of the original distribution can be
228 acquired from the exponential function of m and v .

229
230 We generated climatologies (2001-2020) for MISR and CERES TOA SW flux on a $1^\circ \times 1^\circ$ spatial
231 scale, by taking not only the monthly mean averages, but also taking median values of SW flux
232 at each grid over a period under study. To find the region where the temporal distribution is
233 deviated from the normal distribution, we estimated the difference of climatology of the mean
234 and the median by subtracting the mean climatology from the median climatology, i.e. MEDIAN
235 - MEAN at each grid point. Figures 3(a)-(b) show the spatial distributions of the difference
236 between the median climatology and the mean climatology within 60S - 60N from MISR and
237 CERES, respectively. The similarities of each figure from two different measurements indicate
238 that the difference between median and mean is a real common feature, not originating from the
239 artifacts of the measurements. The largest difference is shown over the Deccan Peninsula, a dry
240 and elevated plateau where the large annual variation of precipitation and vegetation is evident
241 due to the strong Monsoon.

242
243 Figure 3(c)-(f) show respectively the spatial distributions of the skewness and kurtosis of the
244 TOA SW flux distribution from the MISR and CERES observations. The skewness could be
245 reduced from the daily to monthly averages in accord with the central limit theorem, but it still

246 remains strongly positive in the central Southern Pacific. Regions of large positive skewness
247 generally coincide with regions of large positive kurtosis. Very high skewness and kurtosis
248 values concur over the central Southern Pacific ocean that contain less amounts of clouds
249 resulting from less convective activity in the middle of the Inter tropical convergence zone
250 (ITCZ) and South Pacific Convergence Zone (SPCZ).

251
252 The PDFs of the SW flux show interesting results related to the nature of the flux and the
253 instruments that measure the flux. In Figure 4, the PDFs of the flux over Deccan Peninsula and
254 central Southern Pacific Ocean clearly show distinct features in each area.

255
256 Over the Deccan Peninsula (Figure 4(a)), the PDFs show a long and thick right tail in both
257 observations. Over the central Southern Pacific ocean (Figure 4(b)), the both PDFs show high
258 skewness and high kurtosis but two observations show differences in the mean and median. The
259 mean and the median of the MISR SW flux is $\sim 6 \text{ W/m}^2$ ($\sim 11\%$) and $\sim 7 \text{ W/m}^2$ ($\sim 14\%$) lower
260 than that of CERES, respectively. The SW flux distributions over this Pacific region are
261 leptokurtic, as they show highly non-Gaussian features with large values of kurtosis about 14
262 (MISR) and 22 (CERES). The leptokurtic distribution has long tails that asymptotically
263 approach zero more slowly than a Gaussian, therefore produces more outliers than the normal
264 distribution. With higher skewness and kurtosis than normal distribution, the SW flux has a
265 larger population on the right tail caused by high reflective cloudiness.

266
267 Over the high skewness and kurtosis region in the central Southern Pacific ocean, we find
268 negative correlation between skewness and SW flux values, as shown in Figure 5. The linear
269 correlation coefficients between skewness and SW flux is -0.72 and -0.73 for MISR and CERES,
270 respectively. Besides, the skewness abruptly increases where the SW flux is less than 60 W/m^2
271 with relatively less clouds over the Pacific region. We can infer this negative correlation as
272 skewness can be reduced by clouds by their random scattering of the lights. This result
273 corroborates with Datsis and Stevens (2021) that the zonal and temporal distribution of cloud
274 contribution to atmospheric albedo is mostly attributable to the contribution of cloud fraction.

275

276 3.2 Seasonal cycle and hemispheric asymmetry of annual mean SW

277 The seasonal cycle of satellite-based global mean albedo and reflected fluxes has been discussed
278 in a number of previous works (Kato, 2009; Stephens et al., 2015;2016; Song et al., 2018;
279 Datsis & Stevens, 2021; and reference therein). What is different about this work from earlier
280 studies is that the zonal and temporal median is also shown besides the temporal average of the
281 zonal mean with MISR and CERES SSF data. The seasonal cycles shown in Figure 6 are the
282 mean and median of 20 annual cycles (2001-2020) from MISR and CERES SSF data on Terra
283 satellite. Monthly zonal mean and median fluxes computed from 20 years for each month of the
284 year and area weighted and averaged over a given region. The TOA SW flux observations
285 inferred from MISR and CERES produce consistent features of the seasonal cycle of SW flux, as
286 shown in Figure 6.

287

288 The seasonal cycle of the SW flux generally follows the seasonal cycle of the solar insolation,
289 based on Sun-Earth distance and inclination angle changes, which determine the local incoming
290 solar insolation at a given time of the year. Strong hemispheric asymmetry is evident that the
291 seasonal cycle amplitude of global mean solar insolation is more than one magnitude smaller

292 (25.3 W/m²) than those of NH mean (243.9 W/m²) and SH mean (289.3 W/m²), when they are
293 calculated with solar insolation appeared in CERES SSF product. The reduced amplitude of the
294 near-global seasonal cycle of SW flux (Figure 6(a)) compared to the that of NH and SH (Figure
295 6(b)-(c)) illustrates how the hemispheric asymmetry contributes to the global average of the
296 reflected fluxes.

297 Furthermore, the amount of the reflected SW flux also depends on the atmospheric and surface
298 properties. The global mean SW flux is a combination of the flux over land and ocean, therefore,
299 the seasonal cycle of SW flux is also a combination of land and ocean, depending on the seasonal
300 cycle of cloudiness, vegetation, snow, and ice. The differences of the area weighted near-global
301 mean and median values (mean - median) are about 3 W/m² in both observations due to the over-
302 weighted mean with respect to median, originating from the positive skewness.

303 The amplitudes of the annual cycle over the ocean (Figure 6(h)-(i)) is larger than those over land
304 (Figure 6(e)-(f)) in both hemispheres. The seasonal cycle of land surface albedo has summertime
305 minimum resulting from the vegetation and wintertime maximum resulting from the brighter
306 snow covered lands. In both land and ocean cases, the amplitudes of the annual cycle in the SH
307 (Figure 6(f)-(i)) are ~20W/ m² greater than those in the NH. The large amplitude of the annual
308 cycle over the SH ocean (Figure 6(i)) can be attributed to the reflection from midlatitude clouds
309 over the storm track during the austral winter.

310 Despite the strong seasonal variations in the reflected SW flux, its annual means for the NH and
311 SH are nearly equal. Whether this is accidental or intrinsic to the Earth's climate system or
312 variable with time is subject to research debate (Datseris and Stevens, 2021). Different from
313 earlier studies with CERES EBAF SW flux, we analyzed the CERES Terra, Aqua, and EBAF
314 data separately. Annually averaged TOA SW flux (W/m²) during 2001-2020 is summarized in
315 Table 1 at a given region.

316 For the Terra-only MISR and CERES SW flux, observed at ~10:30 AM local time, the
317 hemispheric asymmetry is evident that the SH reflects 3.92 W/m² and 1.15 W/m² more mean SW
318 flux than the NH, respectively. For the Aqua-only CERES SW flux, obtained at ~1:30 PM local
319 time, the hemispheric asymmetry has the opposite sign, which largely offsets the SH-NH
320 difference in Terra flux to produce a nearly equal TOA SW flux in both hemispheres.

321 The hemispheric symmetry in the annual and long-term mean TOA SW flux has a significant
322 implication for Earth's energy balance, as any inequality would require a compensation from the
323 LW flux or inter-hemispheric energy transfers (e.g., meridional oceanic heat transfer). Compared
324 to the NH, the SH has much more ocean which is less reflective than land, so the SH is expected
325 to reflect less than the NH. However, the hemispheric symmetry of the SW flux with equal
326 amount of reflected flux in each hemisphere has been reported and explained by increased SH
327 clouds offsetting the greater reflection from the NH land masses. We can infer that this offsetting
328 by morning clouds, measured at 10:30AM local time, overwhelms the effect of hemispheric
329 imbalance of land and ocean masses between two hemispheres. The marine stratocumulus has a
330 maximum thickness during the morning and a minimum thickness during the afternoon (Gristey
331 et al., 2017a). We can speculate that the high SW flux in the SH from the Terra observation is
332 due to the thick morning marine stratocumulus, since this type of clouds are more widespread in
333 the SH than the NH. Similarly, less SW is reflected in the SH, by the time of Aqua overpass in
334 the afternoon when those clouds have dissipated. More details on the difference between NH and
335 SH is further discussed in the discussions section.

336

3.3 Height-dependent CERES-MISR differences

337 The multi-year (2001–2020) TOA SW median climatology from MISR and CERES agree fairly
338 well with each other over non-polar regions, with the bias close to 7 W/m^2 and the RMS error of
339 8.5 W/m^2 . As shown in Figure 7, the differences, CERES - MISR, are in general positive
340 everywhere except Greenland and SH high latitude regions, since the near-global mean TOA SW
341 flux from CERES is close to 7 W/m^2 greater than that from MISR. Black and red contour lines in
342 the figure indicate high elevation area ($z > 2 \text{ km}$) and high cloud regions (cloud height $> 9 \text{ km}$),
343 respectively.

344 It is interesting that the largest differences up to 30 W/m^2 are observed over tropical high cloud
345 regions where monthly mean cloud top heights are higher than 9 km . Regions where the elevation
346 is higher than 2 km also show large differences. The cloud top heights are acquired from the same
347 CERES SSF product. The world terrain reference (World Geodetic System 1984) model is used
348 in this study, which is the same data set used by the Terra MISR and CERES algorithms.

349 While TOA SW flux inferred from multiple directions is ideally expected to be independent of
350 satellite viewing geometry by definition, two fluxes from multiple directions over the same scene
351 are not identical due to differences in geometry and algorithm. Differences between the two
352 measurements indicate that there exist uncertainties in spatial and temporal matching, narrow-to-
353 broadband conversion, parallax effects, and algorithms for the angular corrections of the radiance
354 field. Each instrument's algorithms, MISR's Bidirectional Reflectance Factor (BRF) corrections
355 and CERES ADMs, account for the angular distribution of the radiance, which strongly
356 dependent on the physical and optical properties of each scene for a given surface type, cloud
357 fraction, cloud/aerosol optical depth, cloud phase, as well as the illumination angle (Loeb et al.,
358 2006).

359 The uncertainties of the TOA albedos from CERES and MISR have been carefully estimated in
360 previous works. Over the overcast ocean scenes within $75\text{S}-75\text{N}$, the uncertainty in the MISR
361 albedos due to narrow-to-broad band albedo conversion is $\sim 2\%$ (Sun et al., 2006). Similarly, the
362 difference between the MISR and CERES albedos due to the angular distribution model (ADM)
363 is estimated to be $\sim 4\%$. Over the Arctic overcast scene, the difference between the two measured
364 albedos are mostly due to differential BRF anisotropic corrections, and it is estimated to be less
365 than 4% when the solar zenith angle (SZA) is less than 70° , while it increases up to 13.5% when
366 the SZA is greater than 80° (Zhan et al., 2018).

367 We further classified the PDFs of MISR and CERES SW flux (W/m^2) over the ocean ($60\text{S}-60\text{N}$)
368 for different cloud heights from 1 to 12 km , as shown in Figure 8. As the cloud heights increase,
369 the difference between two observations grows. Besides, the PDFs are getting close to the
370 normal distribution and the skewness approaches to zero over high cloud regions. This is also
371 shown in a graph of the difference between CERES and MISR (%) and skewness of the PDFs as
372 a function of cloud heights (Figure 9).

373 Besides the cloud properties, i.e., cloud fraction, optical depth, and phase of clouds, magnitude
374 of the SW also depends on three-dimensional (3D) structure of clouds (Ham et al., 2015; Singer
375 et al., 2021). The effects of 3D cloud morphology on SW reflectance, which are not fully
376 resolved in radiative transfer algorithm, may cause additional bias in two measurements for high
377 cloud scenes.

378 4 Discussions

379 4.1 Hemispheric asymmetry in SW flux

380

381 Diurnal sampling plays an important role in the hemispheric asymmetry, SH-NH differences, of
382 the TOA SW flux. As reported in the previous section, this difference is positive in the Terra
383 observations (i.e., MISR and CERES), but negative in the Aqua CERES. As shown in Figure 10,
384 the CERES EBAF result is approximately the average of the Terra and Aqua observation, while
385 different SW flux data show a similar interannual variation. To assess the degree to which the
386 hemispheric symmetry is sensitive to the missing coverage at high latitudes, we compared the
387 annual mean EBAF CERES SW fluxes with various missing portions of high-latitude coverage.
388 Although the interannual variations tend to track each other, the SH-NH differences are
389 relatively small for the global averages with missing latitudes 70° poleward. But the differences
390 start to increase as more polar latitudes are not covered. For example, if the coverage misses 60°
391 poleward, the SH-NH differences can be $\sim 2 \text{ W/m}^2$ with the SH flux being lower, largely because
392 of the extensive coverage from clouds and Antarctic ice. From this analysis we concluded that
393 the missing latitude coverage cannot explain the large difference between MISR and CERES
394 observations from Terra. The MISR-CERES difference is likely due to the underlying
395 assumptions used in their algorithms. For MISR, it requires to convert four narrow-band fluxes
396 to obtain the broadband SW flux, although it measures these narrow-band fluxes from multiple
397 angles along the orbital track. On the other hand, CERES needs to convert the broad-band
398 radiance from a single scan to the full hemispheric SW flux, which requires knowledge of
399 angular distribution models (ADMs) for each scene. In both MISR and CERES SW retrievals,
400 scene type classification is required to carry out the narrow-to-broad-band (MISR) and radiance-
401 to-flux (CERES) conversion.

402

403 Characteristics of the Terra and Aqua CERES sampling are described by Figure 11 in which the
404 NH and SH exhibit very different local time coverages. Thus, the diurnal variations of TOA SW
405 are critical for understanding and interpreting the hemispheric symmetry. If the SW diurnal
406 variation is symmetric about noon, the average of Terra and Aqua data would yield cancellation
407 of the SH-NH asymmetric values observed by each satellite alone. However, if the diurnal
408 variation is not symmetric with respect to noon, their average would not cancel the SH-NH
409 differences. A recent study showed that the SW diurnal variation from the CERES EBAF is
410 somewhat different to the one inferred from the DSCOVR/EPIC observation (Lim et al., 2021).
411 In addition, the rate of daytime cloud fraction changes from DSCOVR/EPIC observations is not
412 symmetric about noon either (Delgado-Bonal et al., 2021). The diurnal variation of albedo
413 estimated from the Earth Radiation Budget Experiment (ERBE) also show that the albedo
414 variations are not always symmetric with respect to noon due to variations of cloudiness
415 throughout the day, which are asymmetric about noon (Rutan et al., 2014). The diurnal variations
416 built in CERES EBAF are largely based on geostationary satellite observations, which cover
417 latitudes up to 60°N/S . Therefore, the uncertainty is likely high in the CERES EBAF data for the
418 SW diurnal variation 60° poleward. This is the region where the Terra and Aqua local time
419 samplings differ most, as shown by Figure 11.

420

421 Our analysis result stresses the importance of diurnal sampling for the SW observations from
422 future missions. Potential constellations of the satellite observations have been suggested to
423 better resolve distinct diurnal signatures of the outgoing Earth radiation (Gristey et al., 2017b;

424 Hakuba et al., 2018; Swartz et al., 2019; and Mefta et al., 2021). As a continuation mission to
425 CERES, NASA's Libera (<https://lasp.colorado.edu/home/libera/>) is planned to fly on the Joint
426 Polar Satellite System-3 (JPSS-3) satellite (1:30 PM equator-crossing time) to maintain the long-
427 term record of TOA radiative fluxes. The Libera's sampling will be similar to Aqua and would
428 require a diurnal cycle model to obtain the daytime mean TOA SW flux. Without correcting the
429 diurnal variation, the Libera's SH-NH difference would be similar to Aqua CERES observations
430 seen in Figure 11.

431

432 4.2 Possible causes of the TOA SW skewness variations

433 We show that monthly mean TOA SW fluxes are obviously not normally distributed, but
434 positively skewed as a mixture of fluxes from land and ocean. According to the central limit
435 theorem, the average of many observations of a random variable approaches a normal
436 distribution. However, in case of TOA SW observation, normality of the distribution is not
437 acquired by taking an average for the monthly mean from the daily means. In global scale, the
438 PDFs of SW flux are relatively thick in the left tail, because there exists a low boundary of zero
439 reflectance when they don't get solar insolation during the polar nights. There also exists
440 extreme high SW flux values above 400 W/m^2 over the summer polar regions.

441 The skewness of the SW flux distribution is not globally uniform, but changes depending on the
442 selection of the spatial and temporal sampling. Besides, the large positive skewness of the
443 observed TOA SW tends to occur in the extreme climatic regions where the seasonal variation of
444 SW flux is relatively high. The PDF of the flux changes with season of the year, as the mean of
445 the flux shows substantial seasonal variations (Figure 6) following the changes of the vegetation,
446 clouds, ice, and atmospheric conditions. For example, the summertime PDF of the flux over land
447 is quite different from the wintertime distribution (not shown) and the PDF over the land is
448 different from that over the ocean. While the negative skewness is often shown over the low- to
449 mid-latitude arid area over the African continent, the positive skewness is generally appeared
450 over the ocean, as can be seen in Figure 3(c) - (d).

451 The PDFs of SW flux over high cloud regions are less skewed, compared to those over low cloud
452 regions (Figure 8-9). Because the interannual variations in SW skewness are derived from
453 variations of clouds, they are sensitive to the outlier years when the flux behaves abnormally,
454 such as those from a strong ENSO event. Skewness often becomes significant in the cases where
455 data variability has a lower or upper boundary. The data with a lower bound tend to have positive
456 skewness while the data with an upper bound are often skewed left. The central Southern Pacific,
457 where the annual mean CERES SWs are lowest and mostly from clear sky, the skewness is
458 positively high. This is the region influenced strongly by the downward branch of both Hadley
459 and Walker circulations on an annual basis, and is apparently sensitive to ENSO-induced
460 circulation changes.

461 5 Conclusions

462 The comparison of twenty years of MISR and CERES observation offers an excellent
463 opportunity to describe their similarities and differences in the TOA SW flux data sets from the
464 two independent instruments on the same Terra platform. The analysis presented in this paper
465 can be summarized in the following:

466

- 467 1. The PDFs of MISR and CERES SW fluxes commonly show that the TOA SW flux is not
468 normally distributed but positively skewed. Distinct PDFs of the TOA SW flux can
469 impact the quantification of the globally averaged flux. In both observations, the near-
470 global median value of the SW flux is $\sim 3 \text{ W/m}^2$ less than the mean of the flux, due to the
471 positive skewness of the SW flux distribution. The near-global mean TOA SW flux
472 converted from MISR narrow bands albedo is about 7 W/m^2 ($< 7\%$) less than CERES
473 measured flux during the last two decades. Gaussian distributions are naturally assumed
474 in atmospheric data analysis, as the central limit theorem states that distributions of
475 random variables approach a normal distribution by taking their mean. This, however, is
476 not always true for the TOA SW flux distribution. The PDFs of SW flux are relatively
477 thick in the left tail, because there exists a low boundary of zero reflectance when they
478 don't get solar insolation during the polar nights.
479
- 480 2. From Terra's AM observation ($\sim 10:30$ AM local time), SH reflects ~ 1 and $\sim 4 \text{ W/m}^2$
481 more SW flux than NH, with MISR and CERES SSF1deg product, respectively.
482 Hemispheric mean SW flux depends on time of satellite measurement, since diurnal
483 sampling plays an important role in determination of the daily mean. Different local time
484 coverage in Terra and Aqua observation can cause sampling bias in estimating SW flux
485 climatology in both hemispheres.
486
- 487 3. While the characteristics of the two SW fluxes broadly agree with each other, differences
488 in the regional PDF from two different SW fluxes are substantially significant over high
489 cloud regions and high altitude regions. Our analysis shows that some parts of the
490 different skewness from two measurements may be attributed to different treatments of
491 the radiance anisotropy over high cloud scenes. More analysis based on the the spatially
492 and temporally collocated merged data set of CERES/MISR radiances (Loeb et al., 2006,
493 Su et al., 2015a; 2015b, Zhan et al., 2018) and TOA albedo observed from Advanced
494 Very High Resolution Radiometer (AVHRR) (Zhan and Liang, 2022) will further help to
495 check the consistencies and uncertainties of the TOA SW flux measurements from the
496 different instruments and to direct to the potential areas requiring improved solutions.

497 **Acknowledgments**

498 We thank the MISR and CERES Science Team for making the TOA albedo and SW flux data
499 available on their websites, and three anonymous reviewers for their suggestions that helped to
500 improve this manuscript. This work is supported by NASA's Sun-Climate research at Goddard
501 Space Flight Center.
502

503

504

505

506

507 **References**

- 508 Barker, H. W., Wielicki, B. A., & Parker, L. (1996). A Parameterization for Computing Grid-
 509 Averaged Solar Fluxes for Inhomogeneous Marine Boundary Layer Clouds. Part II: Validation
 510 Using Satellite Data, *J. of Atmos. Sciences*, 53(16), 2304-2316.
 511 [https://journals.ametsoc.org/view/journals/atsc/53/16/1520-](https://journals.ametsoc.org/view/journals/atsc/53/16/1520-0469_1996_053_2304_apfcga_2_0_co_2.xml)
 512 [0469_1996_053_2304_apfcga_2_0_co_2.xml](https://journals.ametsoc.org/view/journals/atsc/53/16/1520-0469_1996_053_2304_apfcga_2_0_co_2.xml)
 513
- 514 Datsieris, G., & Stevens, B. (2021), Earth's albedo and its symmetry. *AGU Advances*, 2,
 515 e2021AV000440. <https://doi.org/10.1029/2021AV000440>.
 516
- 517 Delgado-Bonal, A., Marshak, A., Yang, Y., & Oreopoulos, L. (2021), Global daytime variability
 518 of clouds from DSCOVR/EPIC observations. *Geophys. Res. Lett.*, 48, e2020GL091511.
 519 <https://doi.org/10.1029/2020GL091511>.
 520
- 521 Diner, D. J., Beckert, J.C., Reilly, T.H., Bruegge, C.J., Conel, J.E., Kahn, R.A., Martonchik, J.V.,
 522 Ackerman, T.P., Davies, R., Gerstl, S.A.W. (1998), Multi-angle Imaging SpectroRadiometer
 523 (MISR) instrument description and experiment overview. *IEEE Trans. Geosci. Remote Sens.*, 36,
 524 1072–1087.
 525
- 526 Diner, D. J., Braswell, B. H., Davies, R., Gobron, N., Hu, J., Jin, Y., Kahn, R. A., Knyazikhin,
 527 Y., Loeb, N., Muller, J.-P., Nolin, A. W., Pinty, B., Schaaf, C. B., Seiz, G., and Stroeve, J.,
 528 (2005), The value of multiangle measurements for retrieving structurally and radiatively
 529 consistent properties of clouds, aerosols, and surfaces, *Remote Sens. Environ.*, 97, 495–518.
 530
- 531 Diner, David. (2009). MISR Level 3 Component Global Albedo product in netCDF format
 532 covering a day - Version 6 [Data set]. NASA Langley Atmospheric Science Data Center
 533 DAAC. https://doi.org/10.5067/TERRA/MISR/MIL3DALN_L3.006
 534
- 535 Doelling, D. R., N. G. Loeb, D. F. Keyes, M. L. Nordeen, D. Morstad, C. Nguyen, B. A.
 536 Wielicki, D. F. Young, M. Sun (2013), Geostationary Enhanced Temporal Interpolation for
 537 CERES Flux Products, *J. of Atmos. and Oceanic Technol.*, 30(6), 1072-1090. doi:
 538 10.1175/JTECH-D-12-00136.1.
 539
- 540 Doelling, David. (2015). CERES Level 3 SSF1deg-Month Terra-MODIS HDF file - Edition 4A
 541 [Data set]. NASA Langley Atmospheric Science Data Center DAAC.
 542 https://doi.org/10.5067/TERRA/CERES/SSF1DEGMONTH_L3.004A
 543
- 544 Doelling, David. (2019). CERES Energy Balanced and Filled (EBAF) TOA and Surface
 545 Monthly means data in netCDF Edition 4.1 [Data set]. NASA Langley Atmospheric Science
 546 Data Center DAAC. https://doi.org/10.5067/TERRA-AQUA/CERES/EBAF_L3B.004.1
 547
- 548 Feller, W., 1971. An introduction to probability theory and its applications, 2d. Ed., volume 2,
 549 New York, Wiley.
 550

- 551 Gristey, J.J.; Chiu, J.C.; Gurney, R.J.; Morcrette, C.J.; Hill, P.G.; Russell, J.E.; Brindley, H.E.
552 (2017a). Insights into the diurnal cycle of global Earth outgoing radiation using a numerical
553 weather prediction model. *Atmos. Chem. Phys.*, 18, 5129–5145.
554
- 555 Gristey, J. J., J. C. Chiu, R. J. Gurney, S.-C. Han, and C. J. Morcrette (2017b), Determination of
556 global Earth outgoing radiation at high temporal resolution using a theoretical constellation
557 of satellites, *J. Geophys. Res. Atmos.*, 122, 1114–1131, doi:10.1002/2016JD025514.
558
- 559 Gristey, J. J., W. Su, N. G. Loeb, T. H. Vonder Haar, F. Tornow, K. S. Schmidt, M. Z. Hakuba,
560 P. Pilewski, and J. E. Russell (2018), Shortwave Radiance to Irradiance Conversion for Earth
561 Radiation Budget Satellite Observations: A Review, *Remote Sens.*, 13(13), 2640.
562
- 563 Hakuba, M. Z. *et al.* (2019). Earth's Energy Imbalance Measured From Space, *IEEE Trans.*
564 *Geosci. Remote Sens.*, vol. 57, no. 1, pp. 32-45, Jan. 2019, doi: 10.1109/TGRS.2018.2851976.
565
- 566 Ham, S.-H., Kato, S., Barker, H.W., Rose, F.G. and Sun-Mack, S. (2015), Improving the
567 modelling of short-wave radiation through the use of a 3D scene construction algorithm. *Q. J. R.*
568 *Meteorol. Soc.*, 141, 1870-1883. <https://doi.org/10.1002/qj.2491>.
569
- 570 Kato, S. Top-of-atmosphere shortwave broadband observed radiance and estimated irradiance
571 over polar regions from Clouds and the Earth's Radiant Energy System (CERES) instruments on
572 Terra (2005), *J. Geophys. Res.*, 110(D7), D07202, doi: 10.1029/2004JD005308.
573
- 574 Kato, S. Interannual Variability of the Global Radiation Budget, (2009), *J. of Climate*, 22, 18
575 (2009): 4893-4907, doi: 10.1175/2009JCL1295.1.
576
- 577 Kopp, G., and Lean, J. L. (2011), A new, lower value of total solar irradiance: Evidence and
578 climate significance, *Geophysical Research Letters*, 38, L01706, doi:10.1029/2010GL045777.
579
- 580 L'Ecuyer, T.S. (2017). Earth's Energy Balance. In International Encyclopedia of Geography:
581 *People, the Earth, Environ. and Tech.*, <https://doi.org/10.1002/9781118786352.wbieg1132>
582
- 583 Lim, Y.-K.; Wu, D.L.; Kim, K.-M.; Lee, J.N. (2021), An Investigation on Seasonal and Diurnal
584 Cycles of TOA Shortwave Radiations from DSCOVR/EPIC, CERES, MERRA-2, and ERA5,
585 *Remote Sens.*, 13, 4595. doi: 10.3390/rs13224595.
- 586 Loeb N. G., Kato S, Loukachine K, Manalo-Smith N. (2005), Angular distribution models for
587 top-of-atmosphere radiative flux estimation from the Clouds and the Earth's Radiant Energy
588 System instrument on the Terra satellite. Part I: Methodology. *J. Atmos. Oceanic Technol.* 22:
589 338 – 351, doi: 10.1175/JTECH1712.1.
590
- 591 Loeb, N. G., Sun, W., Miller, W. F., Loukachine, K., and Davies, R. (2006), Fusion of CERES,
592 MISR, and MODIS measurements for top-of-atmosphere radiative flux validation, *J. Geophys.*
593 *Res.*, 111, D18209, doi:10.1029/2006JD007146.
594
- 595 Loeb N. G., Kato S, Loukachine K, Manalo-Smith N. (2007). Angular distribution models for
596 top-of-atmosphere radiative flux estimation from the Clouds and the Earth's Radiant Energy

- 597 System instrument on the Terra satellite. Part II: Validation. *J. Atmos. Oceanic Technol.* 24: 564
598 – 584, doi: 10.1175/JTECH1983.1.
599
- 600 Loeb, N. G., Wielicki, B. A., Doelling, D. R., Smith, G. L., Keyes, D. F., Kato, S., Manalo-
601 Smith, N., & Wong, T. (2009). Toward Optimal Closure of the Earth's Top-of-Atmosphere
602 Radiation Budget, *J. of Climate*, 22(3), 748-766.
603 <https://journals.ametsoc.org/view/journals/clim/22/3/2008jcli2637.1.xml>
604
- 605 Loeb, N. G. and B.A. Wielicki (2015), SATELLITES AND SATELLITE REMOTE SENSING |
606 Earth's Radiation Budget, Encyclopedia of Atmospheric Sciences (Second Edition),
607 Academic Press, 2015, 67-76, <https://doi.org/10.1016/B978-0-12-382225-3.00349-2>.
608
- 609 Loeb, N. G., Doelling, D. R., Wang, H., Su, W., Nguyen, C., Corbett, J. G., Liang, L., Mitrescu,
610 C., Rose, F. G., and Kato, S. (2018). Clouds and the Earth's Radiant Energy System (CERES)
611 Energy Balanced and Filled (EBAF) Top-of-Atmosphere (TOA) Edition-4.0 Data Product. *J. of*
612 *Climate* 31, 2, 895-918, <https://doi.org/10.1175/JCLI-D-17-0208.1>.
613
- 614 Meftah, M., Boutéraon, T., Dufour, C., Hauchecorne, A., Keckhut, P., Finance, A., et al. (2021).
615 The UVSQ-SAT/INSPIRESat-5 CubeSat Mission: First In-Orbit Measurements of the Earth's
616 Outgoing Radiation. *Remote Sens.*, 13(8), 1449. <https://doi.org/10.3390/rs13081449>.
617
- 618 Rutan, D. A., Smith, G. L., & Wong, T. (2014). Diurnal Variations of Albedo Retrieved from
619 Earth Radiation Budget Experiment Measurements. *J. of Appl. Met. and Clim.*, 53(12), 2747–
620 2760. <http://www.jstor.org/stable/26176466>.
621
- 622 Sardeshmukh, P. D, G. P. Compo and C. Penland (2015). Need for Caution in Interpreting
623 Extreme Weather Statistics. *J. of climate*, 28 (23), 9166-9187. doi:10.1175/JCLI-D-15-0020.1.
624
- 625 Singer, C. E., Lopez-Gomez, I., Zhang, X., & Schneider, T. (2021). Top-of-Atmosphere Albedo
626 Bias from Neglecting Three-Dimensional Cloud Radiative Effects, *J. of the Atmos. Sciences*,
627 78(12), 4053-4069. <https://journals.ametsoc.org/view/journals/atsc/78/12/JAS-D-21-0032.1.xml>
- 628 Song, Z.; Liang, S.; Wang, D.; Zhou, Y.; Jia, A. (2018). Long-term record of top-of-
629 atmosphere albedo over land generated from AVHRR data, *Remote Sens. Environ*, 211, 71–
630 88.
- 631 Stephens, G., Li, J., Wild, M. *et al.* An update on Earth's energy balance in light of the latest
632 global observations. *Nature Geosci.* 5, 691–696 (2012). <https://doi.org/10.1038/ngeo1580>.
- 633 Stephens, G. L., O'Brien, D., Webster, P. J., Pilewski, P., Kato, S., and Li, J. (2015), The
634 albedo of Earth. *Rev. Geophys.*, 53, 141– 163. doi: 10.1002/2014RG000449.
- 635 Stephens, G. L., Hakuba, M. Z., Hawcroft, M., Haywood, J. M., Behrangi, A., Kay, J. E., &
636 Webster, P. J. (2016), The curious nature of the hemispheric symmetry of the Earth's water

637 and energy balances. *Current Climate Change Reports*, 2(4), 135– 147.
638 <https://doi.org/10.1007/s40641-016-0043-9>.

639 Swartz, W., Lorentz, S., Papadakis, S., Huang, P., Smith, A., Deglau, D., et al. (2019).
640 RAVAN: CubeSat Demonstration for Multi-Point Earth Radiation Budget Measurements.
641 *Remote Sens.*, 11(7), 796. <https://doi.org/10.3390/rs11070796>.

642 Su, W., J. Corbett, Z. Eitzen, and L. Liang (2015a), Next-generation angular distribution
643 models for top-of-atmosphere radiative flux calculation from CERES instruments:
644 Methodology. *Atmos. Meas. Tech.*, 8, 611–632, doi:10.5194/amt-8-611-2015.

645 Su, W., Corbett, J., Eitzen, Z., and Liang, L. (2015b), Next-generation angular distribution
646 models for top-of-atmosphere radiative flux calculation from CERES instruments: validation,
647 *Atmos. Meas. Tech.*, 8, 3297–3313, <https://doi.org/10.5194/amt-8-3297-2015>.

648
649 Sun, W., N. G. Loeb, R. Davies, K. Loukachine, and W. F. Miller (2006), Comparison of MISR
650 and CERES top-of-atmosphere albedo, *Geophys. Res. Lett.*, 33, L23810,
651 doi:10.1029/2006GL027958.

652
653 Wild, M., Folini, D., Hakuba, M.Z. *et al.* (2015). The energy balance over land and oceans: an
654 assessment based on direct observations and CMIP5 climate models. *Clim. Dyn.* **44**, 3393–3429.
655 <https://doi.org/10.1007/s00382-014-2430-z>.

656
657 Zhan, C. and S. Liang (2022), Improved estimation of the global top-of-atmosphere albedo from
658 AVHRR data, *Remote Sens. Environ.*, 269, 112836, ISSN 0034-4257,
659 <https://doi.org/10.1016/j.rse.2021.112836>.

660
661 Zhan, Y.; Di Girolamo, L.; Davies, R.; Moroney, C. Instantaneous Top-of-Atmosphere Albedo
662 Comparison between CERES and MISR over the Arctic (2018), *Remote Sens.*, 10, 1882.
663 <https://doi.org/10.3390/rs10121882>.

664

665

666

667

668

669

670

671 **Figure captions**

672 Figure 1. (a) PDFs of the monthly mean near-global (80S-80N) distribution of all-sky broadband
 673 TOA SW Flux (W/m^2) measured from MISR and CERES. We analyze 240 monthly samples at
 674 each grid points for 2001-2020. MISR broadband (BB) TOA SW flux (W/m^2) is converted from
 675 four narrow band albedos. The bin size is $1 W/m^2$, and the total integration of the area under each
 676 PDF is normalized to be one. (b) Four narrow bands, Channel 1 - Channel 4 (C1 - C4) MISR
 677 TOA SW flux (W/m^2) centered at blue, green, red, and near-infrared. MISR broadband flux is
 678 overlaid with a black curve.

679
 680 Figure 2. Deviation of PDF of MISR TOA SW flux (W/m^2) from normal distribution. The PDF
 681 is for MISR TOA SW Flux, as described in Figure 1(a). The blue curve is a best-fit lognormal
 682 distribution of the TOA SW flux values. The red curve is a best-fit normal distribution using the
 683 mean and the standard deviation of the TOA SW flux. The yellow curve is a
 684 hypothetical normal distribution with a mean at the mode of the flux distribution. The black and
 685 blue dotted line represents the mean and median value of the SW flux, respectively.

686
 687 Figure 3. Difference of median and mean climatology of TOA SW flux (W/m^2) ((a)-(b)) and
 688 spatial distribution of temporal skewness ((c)-(d)) and kurtosis ((e)-(f)) of TOA SW flux from
 689 MISR and CERES.

690
 691 Figure 4. PDFs of the SW flux over the (a) Deccan Peninsula and (b) central Southern Pacific
 692 ocean.

693
 694 Figure 5. Scatter plot of skewness of the TOA SW flux with respect to the TOA SW flux values
 695 over the high skewness area in the central Southern Pacific ocean.

696
 697 Figure 6. Annual cycles of the mean and median climatology of the SW flux (W/m^2) from MISR
 698 and CERES for near-global (left), NH (center), and SH (right). The second and third rows are
 699 NH and SH land and ocean, respectively. The filled marks represent median values of the fluxes
 700 and unfilled marks represent mean of the fluxes.

701
 702 Figure 7. Differences of median climatology (2001-2020) of TOA SW flux (W/m^2) between
 703 MISR and CERES from the Terra satellite. Black and red contour lines indicate high elevation
 area ($z > 2\text{km}$) and high cloud regions (cloud height $> 9\text{km}$), respectively.

704
 705 Figure 8. PDFs of MISR and CERES SW flux (W/m^2) over the ocean for different cloud heights
 from 1 to 12 km.

706
 707 Figure 9. The difference between two median values (CERES - MISR)/CERES in % and
 skewness of the TOA SW distribution over the ocean, as a function of cloud height.

708
 709 Figure 10. Time series of annual mean NH and SH TOA SW fluxes from CERES EBAF,
 710 CERES-Terra, CERES-Aqua, and MISR-Terra (upper) and CERES EBAF TOA SW flux
 711 differences with various missing latitudes (lower). The poleward missing latitudes are indicated
 712 by the plot legend.

713 Figure 11. Local time coverage from Terra (red) and Aqua (blue) CERES. Jan 1, 2008 is used to
714 illustrate the differences between the NH and SH sampling in local time.

715

716

717

718 **Table Caption**

719 **Table 1.** Annual mean TOA reflected SW flux (W/m^2) from 2001-2020 for different regions
720 from MISR, CERES SSF, and CERES EBAF products. Numbers in parenthesis are calculated
721 with zonal median, instead of zonal mean.

722

723

724

725

726

727

728

729

730

731

732

733

734

735

736

737

738

739

740

741

Figure 1.

PDFs of GLOBAL ALL-SKY TOA SW FLUX

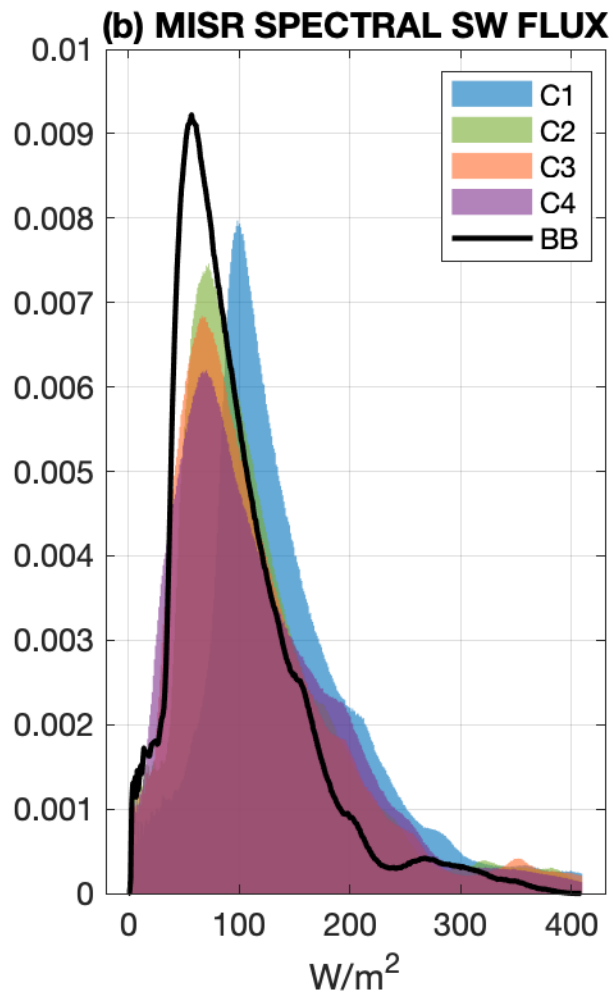
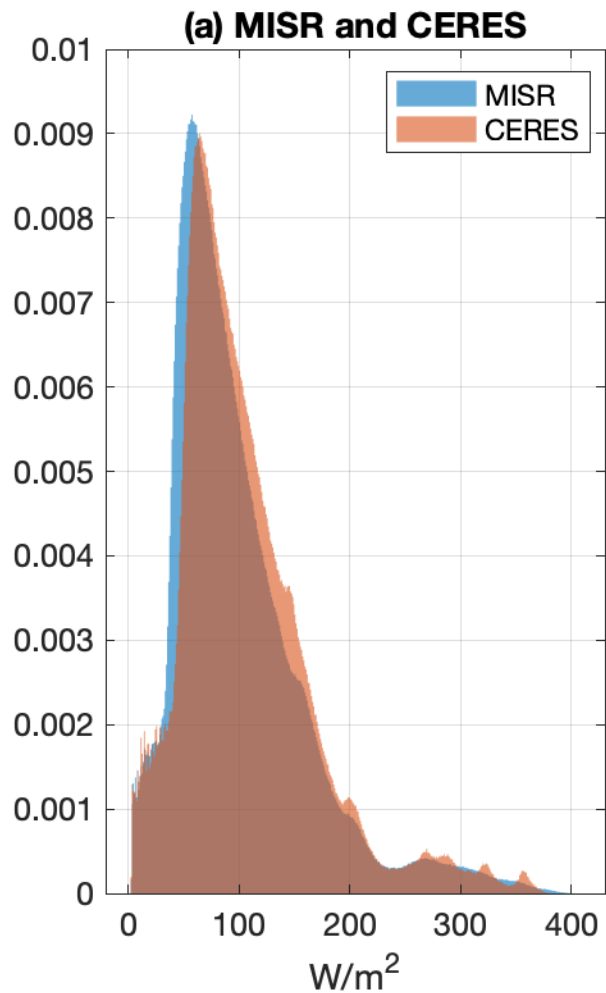


Figure 2.

PDF of MISR SW (W/m^2)

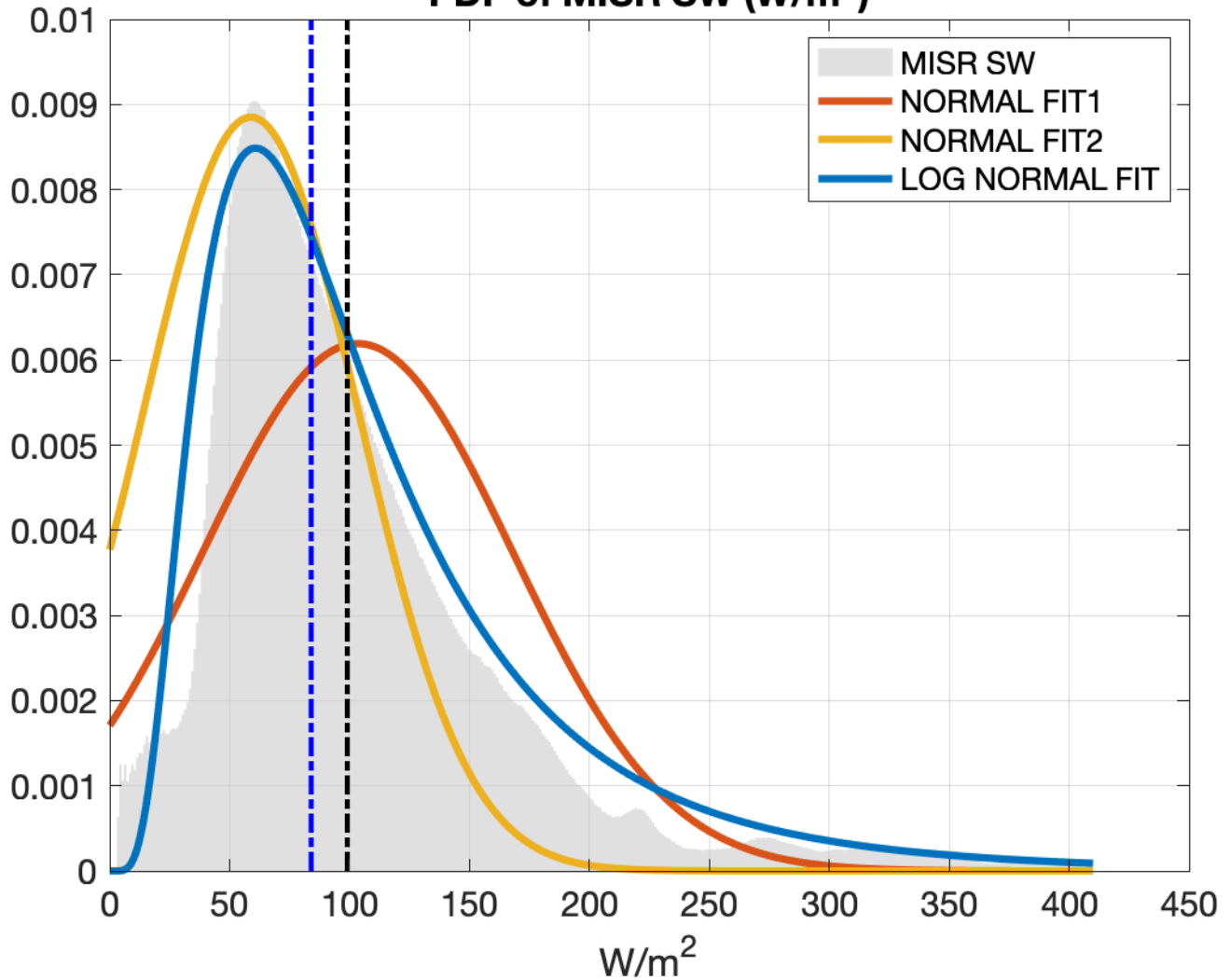
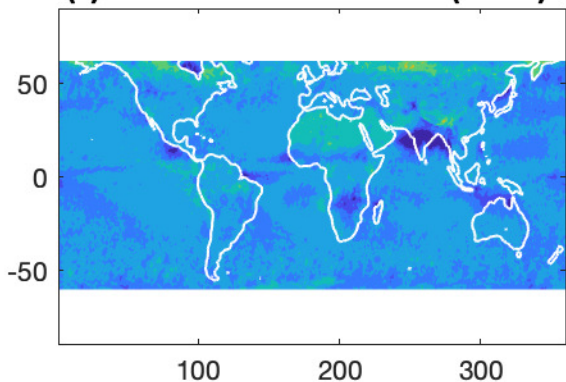
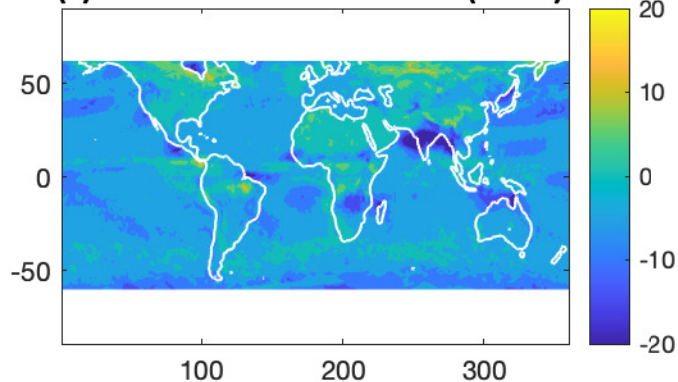


Figure 3.

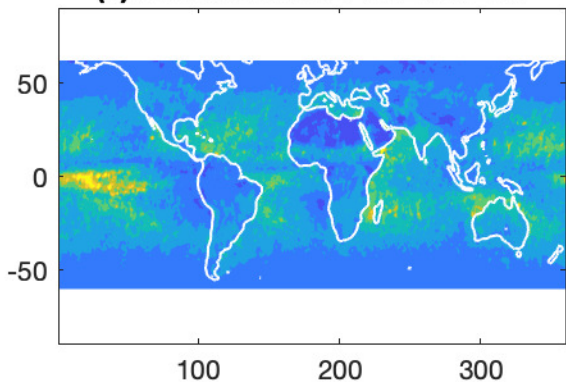
(a) MISR : MEDIAN - MEAN (W/m^2)



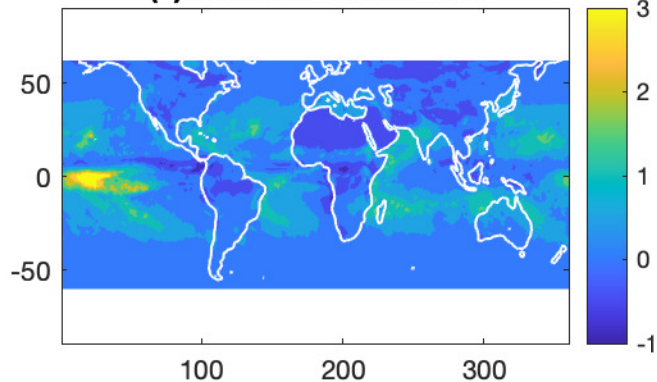
(b) CERES : MEDIAN - MEAN (W/m^2)



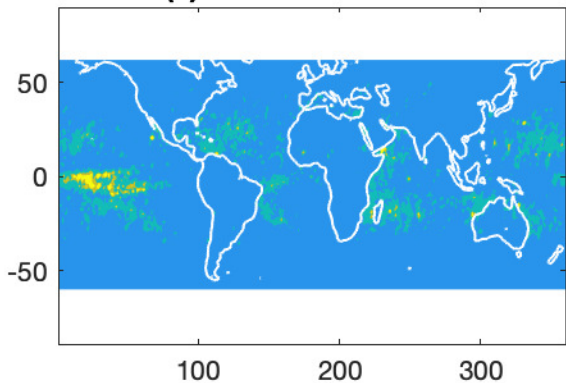
(c) MISR TOA SW : SKEWNESS



(d) CERES : SKEWNESS



(e) MISR : KURTOSIS



(f) CERES : KURTOSIS

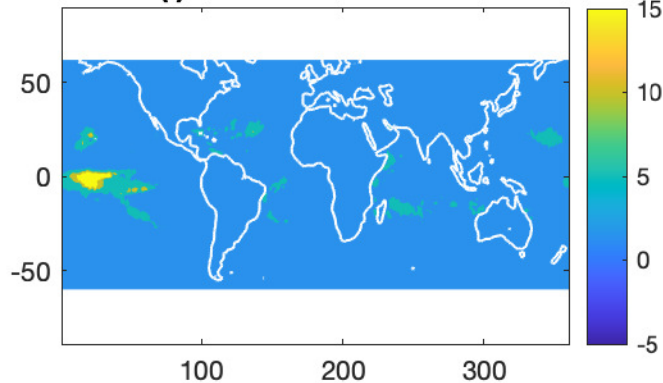


Figure 4.

PDF of TOA SW FLUX (W/m^2)

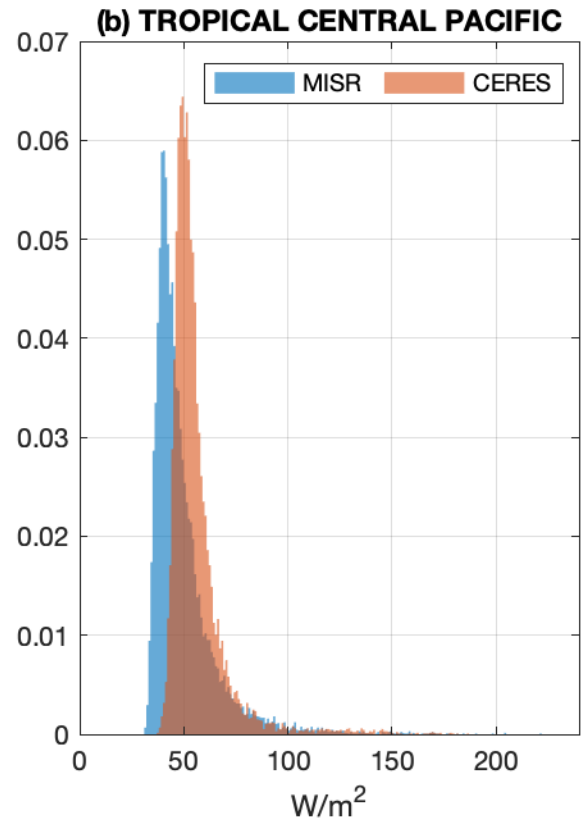
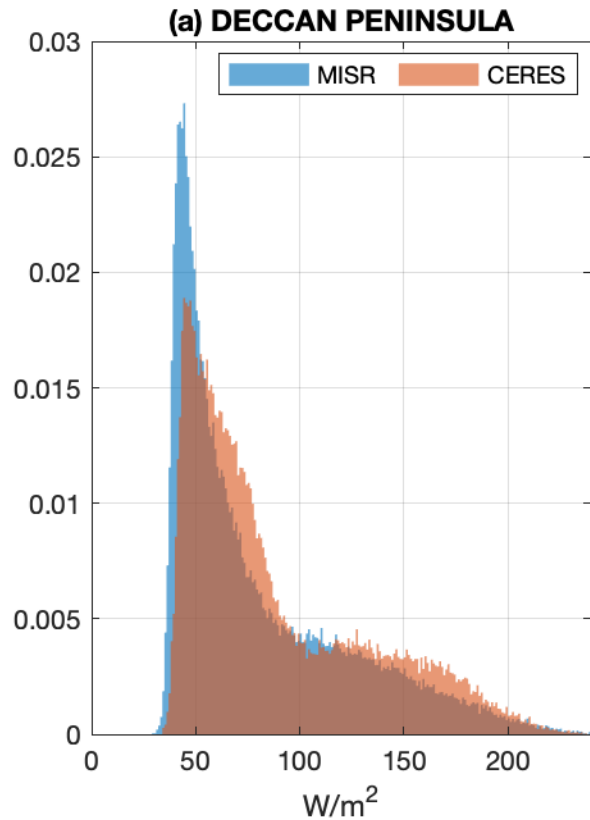


Figure 5.

Skewness vs. SW Flux

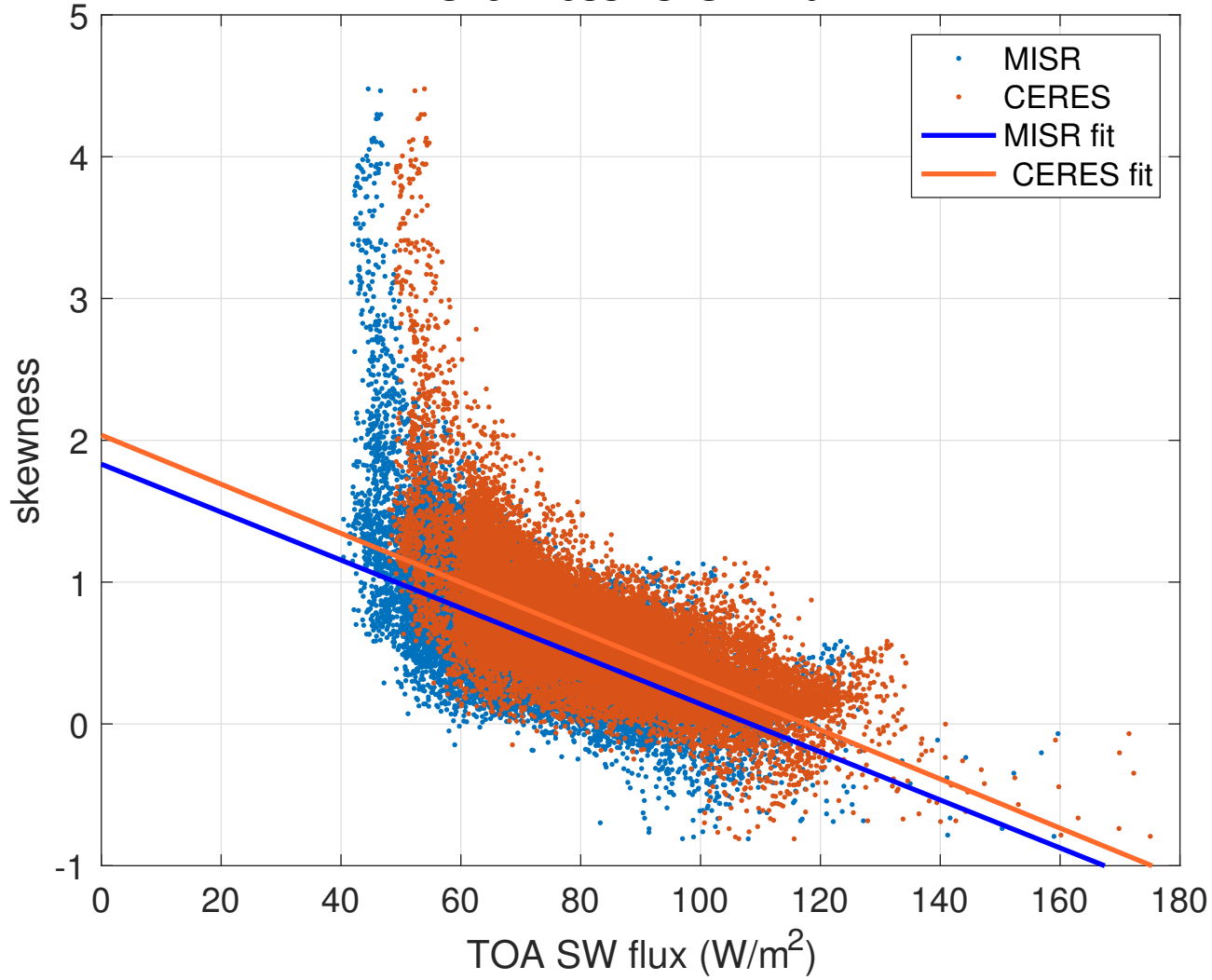


Figure 6.

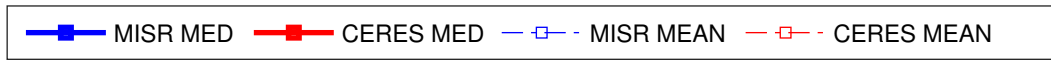
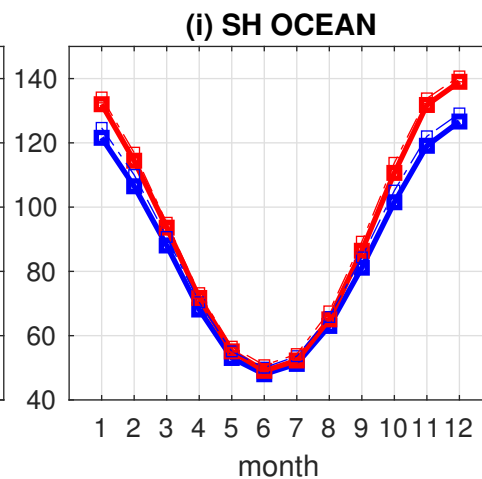
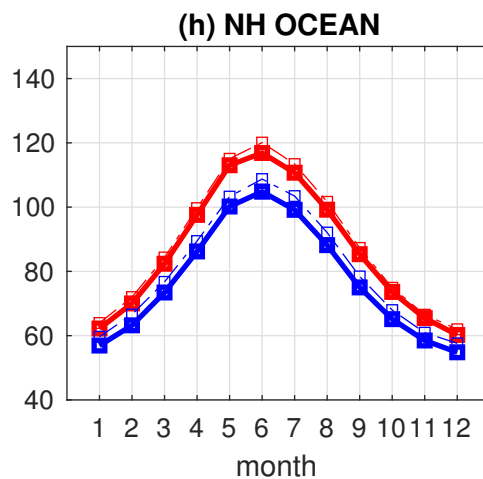
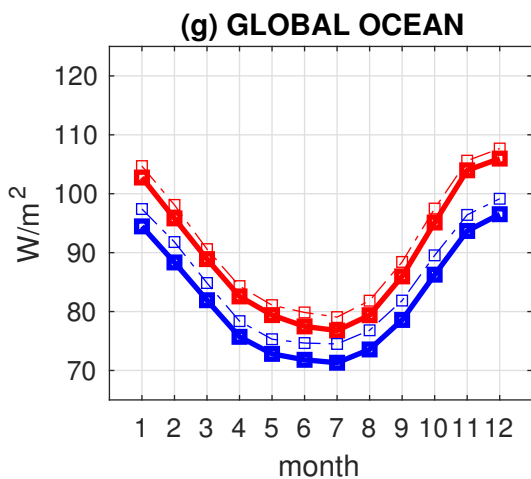
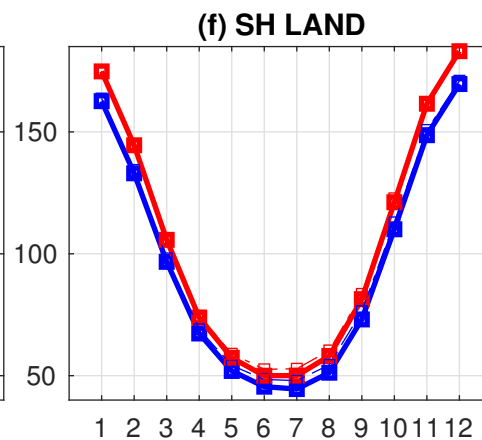
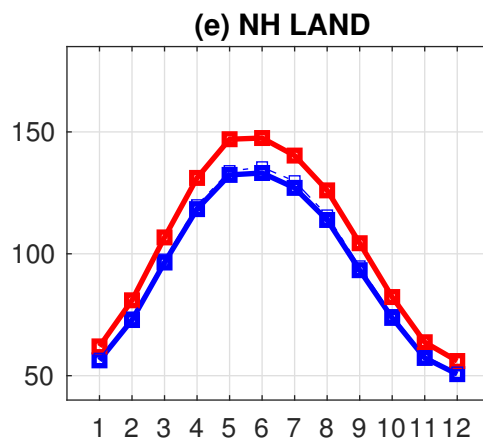
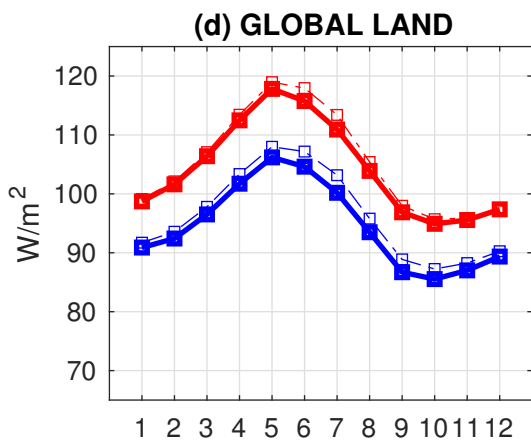
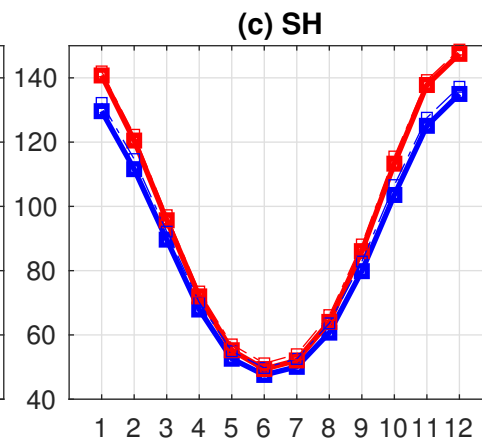
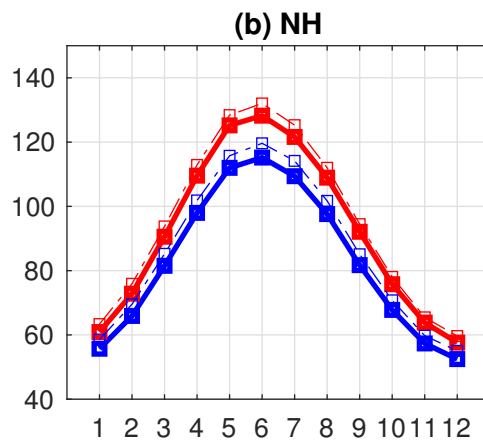
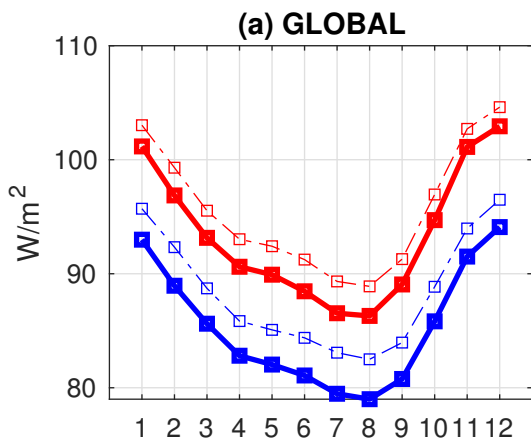


Figure 7.

CERES-MISR : Median TOA SW (W/m^2): JUL

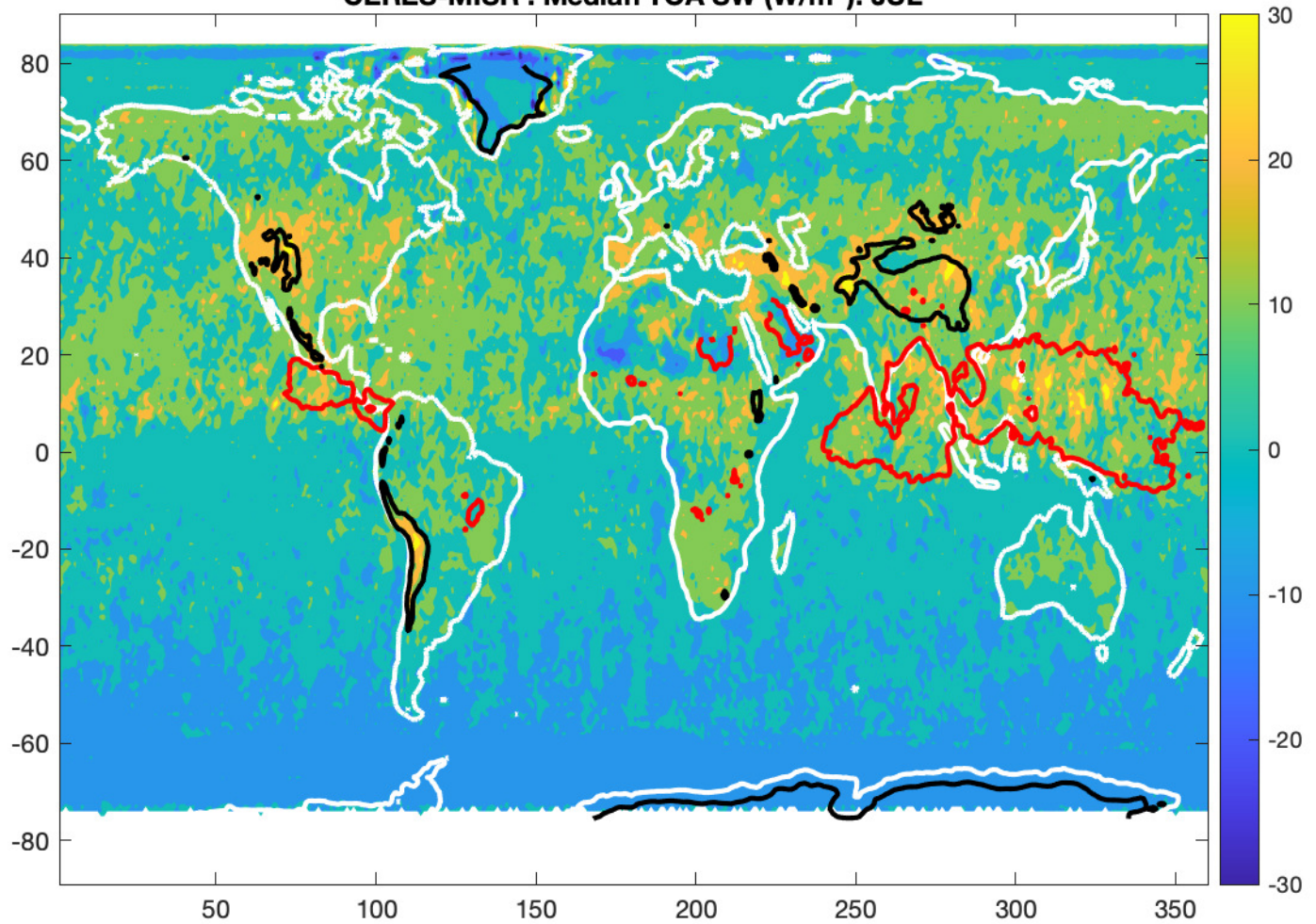
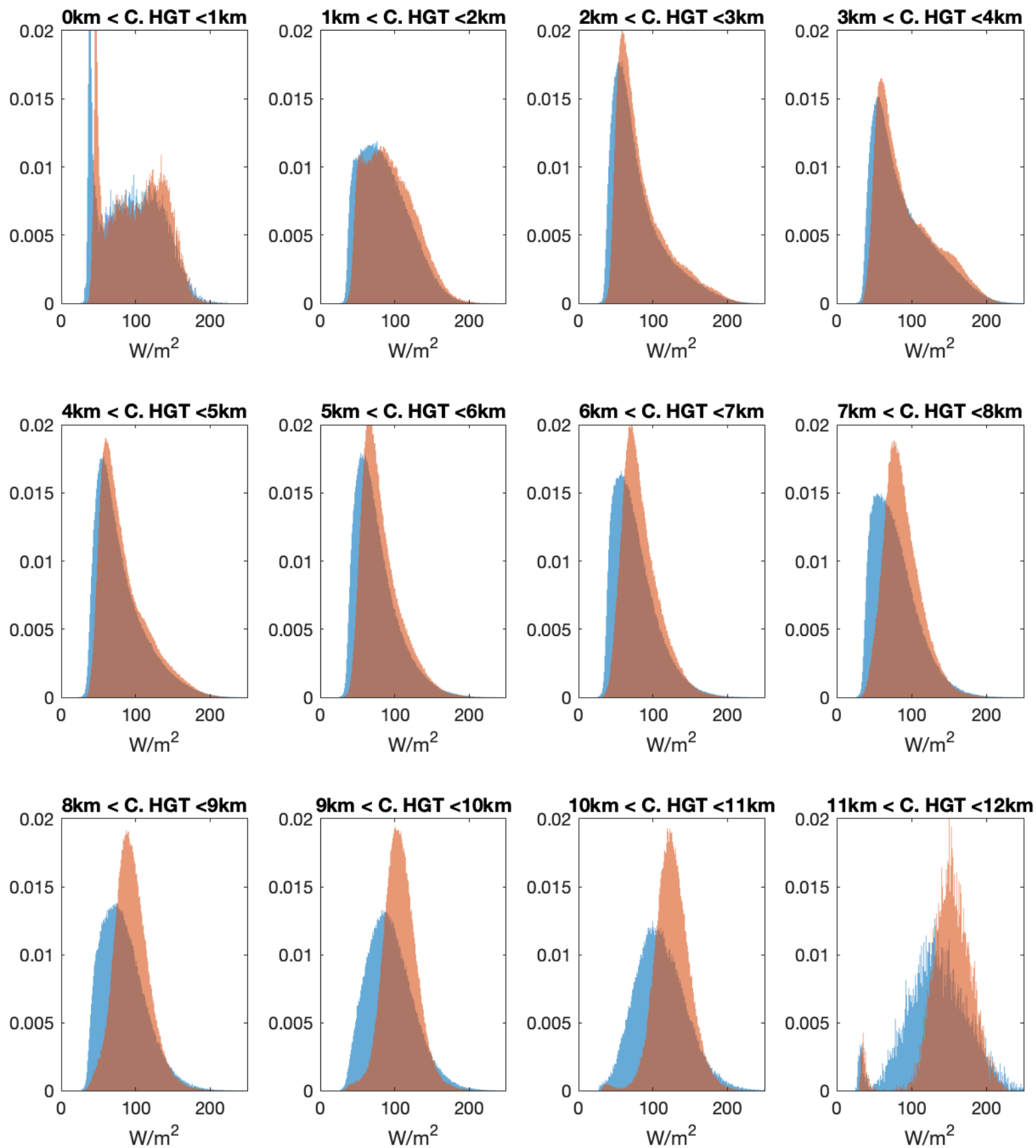


Figure 8.



MISR CERES

Figure 9.

TOA SW Distribution vs Cloud Height

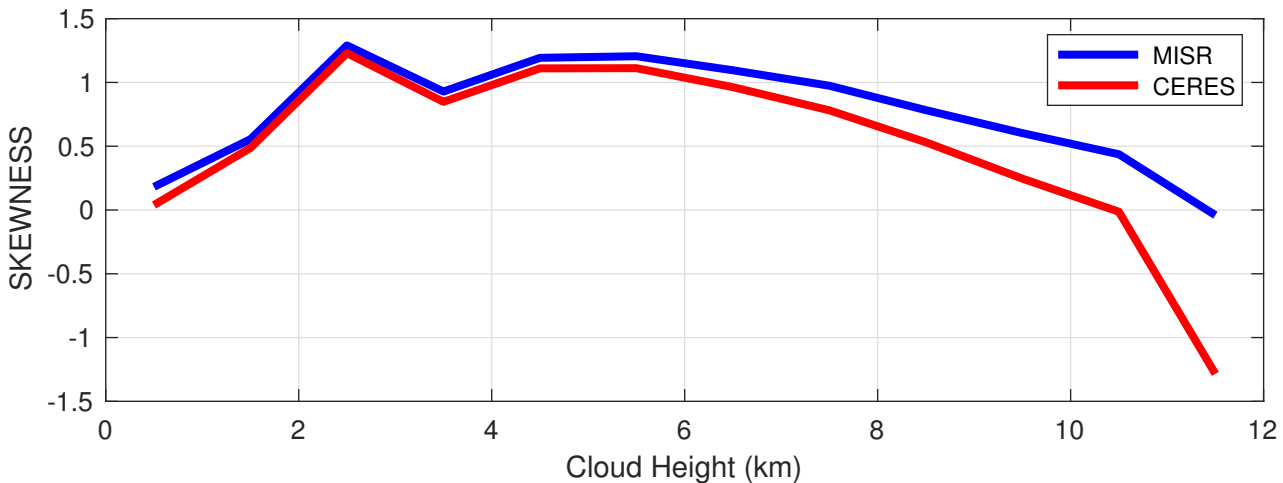
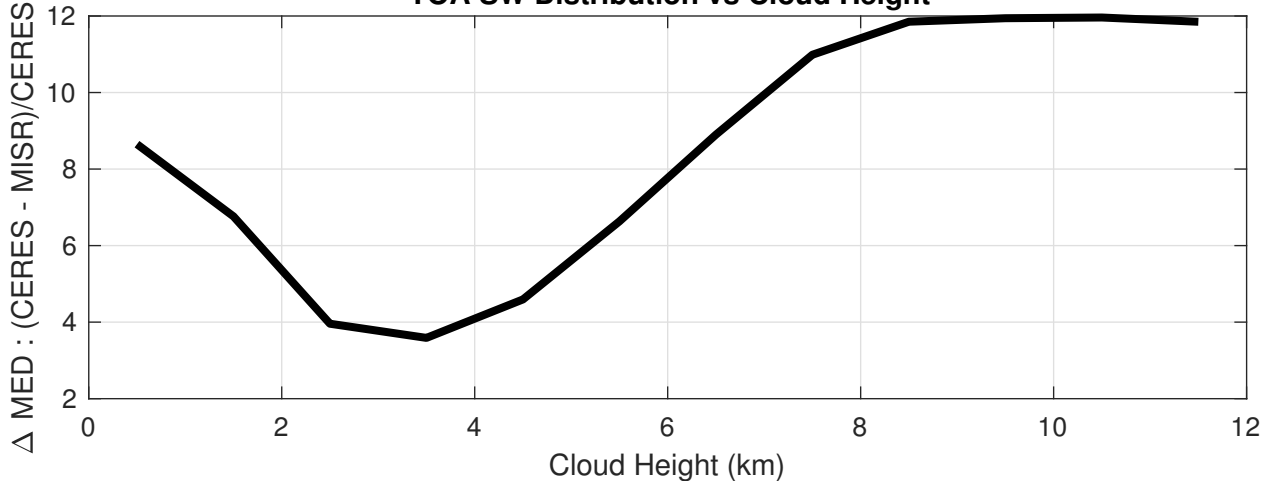


Figure 10.

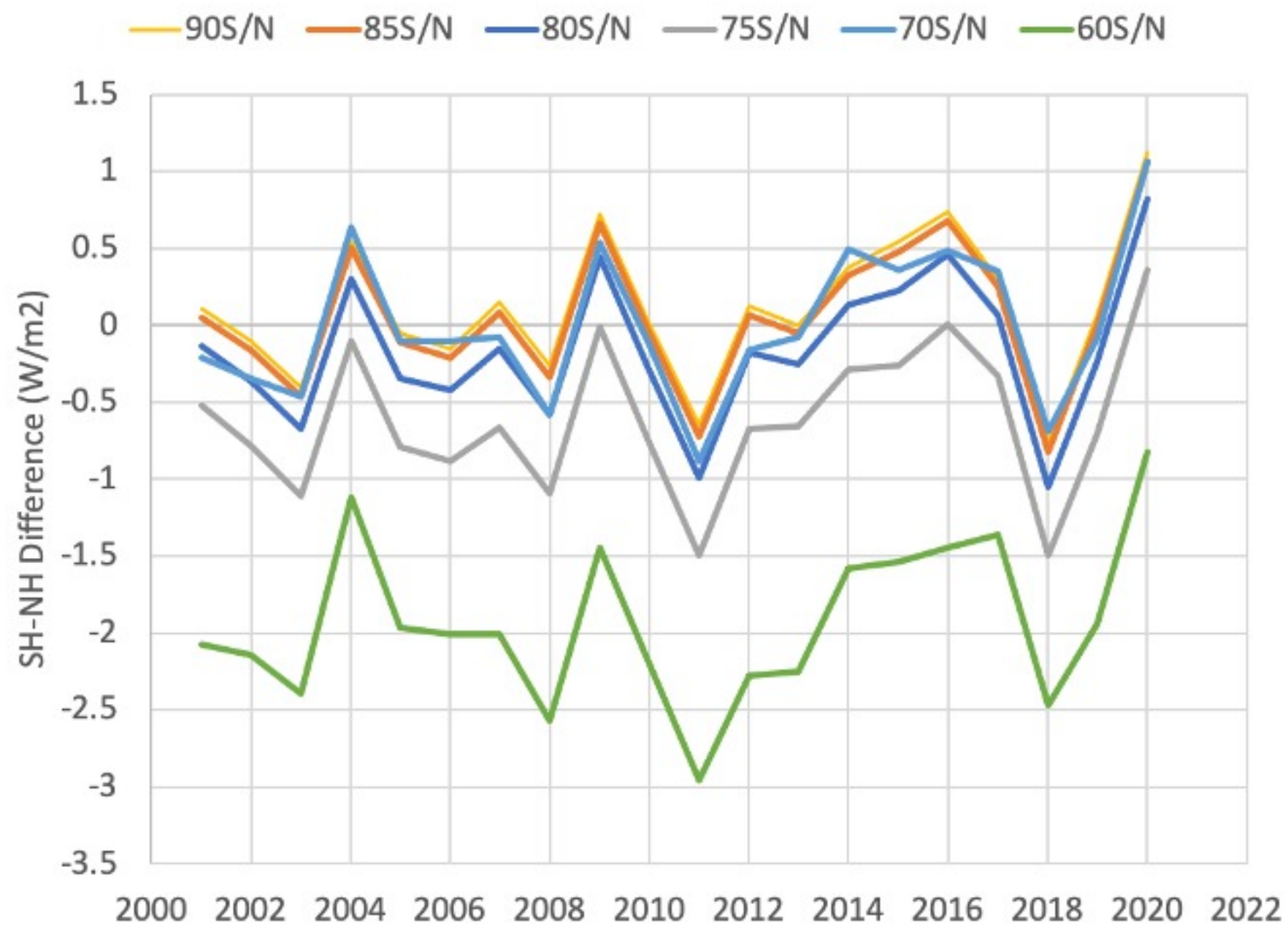
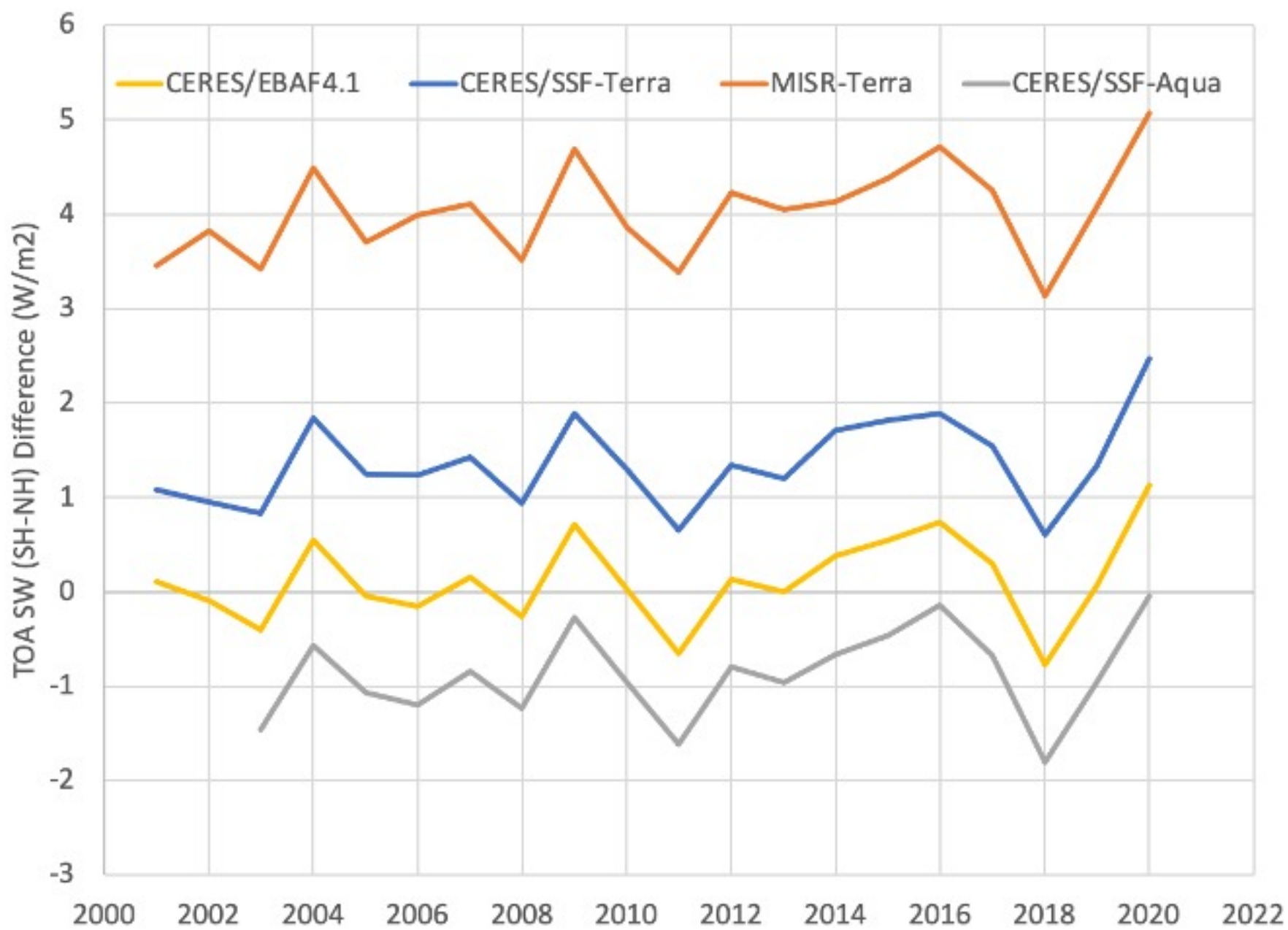


Figure 11.

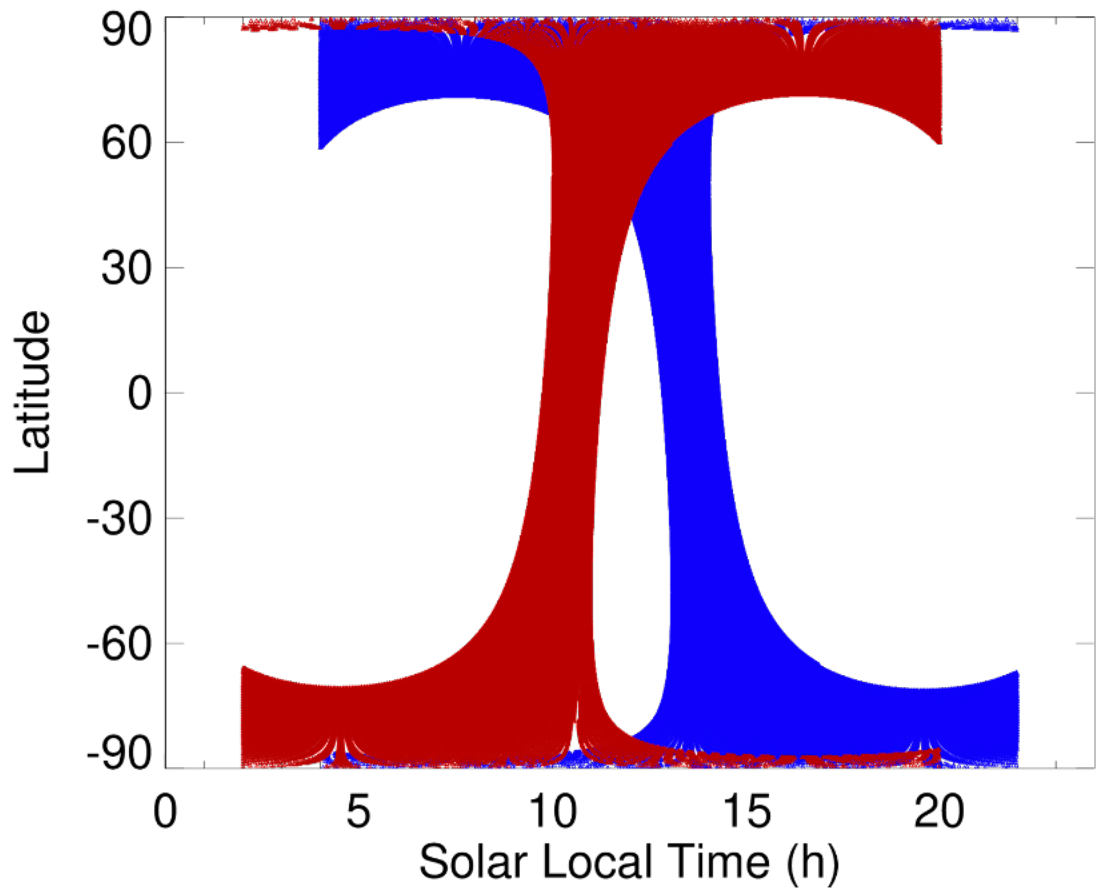


Table 1

	MISR (W/m ²) (80S-80N)	CERES SSF(W/m ²) (80S-80N)	CERES SSF (W/m ²) (90S-90N)	CERES EBAF (W/m ²) (90S-90N)
Global	88.41 (85.34)	95.68 (93.40)	96.26 (93.98)	99.04 (96.92))
NH	86.43 (82.88)	95.11 (92.26)	95.53 (92.67)	98.94 (96.29)
SH	90.35 (87.76)	96.26 (94.52)	96.99 (95.27)	99.14 (97.54)
SH - NH	3.92 (4.89)	1.15 (2.26)	1.47 (2.60)	0.20 (1.60)
LAND	96.26 (94.55)	105.37 (104.35)	105.38 (104.37)	110.36 (109.52)
OCEAN	85.05 (82.08)	91.56 (89.51)	91.59 (89.53)	94.21 (92.18)
NH LAND	95.21 (93.76)	104.89 (103.98)	104.90 (103.99)	108.18 (107.31)
SH LAND	98.45 (96.19)	106.36 (105.16)	105.14 (104.90)	114.87 (114.10)
NH OCEAN	80.40 (77.12)	88.39 (86.38)	88.44 (86.44)	92.59 (90.62)
SH OCEAN	88.42 (85.66)	93.84 (91.76)	93.86 (91.77)	95.38 (93.31)

