



An Unbiased CO Survey Toward the Northern Region of the Small Magellanic Cloud with the Atacama Compact Array. II. CO Cloud Catalog

Takahiro Ohno¹, Kazuki Tokuda^{2,3,4}, Ayu Konishi⁴, Takeru Matsumoto⁴, Marta Sewilo^{5,6,7}, Hiroshi Kondo⁴, Hidetoshi Sano⁸, Kisetsu Tsuge⁹, Sarolta Zahorecz^{3,4}, Nao Goto⁴, Naslim Neelamkudan¹⁰, Tony Wong¹¹, Hajime Fukushima¹², Tatsuya Takekoshi¹³, Kazuyuki Muraoka⁴, Akiko Kawamura¹⁴, Kengo Tachihara¹, Yasuo Fukui¹, and Toshikazu Onishi⁴

¹ Department of Physics, Nagoya University, Chikusa-ku, Nagoya 464-8602, Japan; t.ohno4a.phys@gmail.com

² Department of Earth and Planetary Sciences, Faculty of Science, Kyushu University, Nishi-ku, Fukuoka 819-0395, Japan; tokuda.kazuki.369@m.kyushu-u.ac.jp

³ National Astronomical Observatory of Japan, National Institutes of Natural Sciences, 2-21-1 Osawa, Mitaka, Tokyo 181-8588, Japan

⁴ Department of Physics, Graduate School of Science, Osaka Metropolitan University, 1-1 Gakuen-cho, Naka-ku, Sakai, Osaka 599-8531, Japan

⁵ Exoplanets and Stellar Astrophysics Laboratory, NASA Goddard Space Flight Center, Greenbelt, MD 20771, USA

⁶ Department of Astronomy, University of Maryland, College Park, MD 20742, USA

⁷ Center for Research and Exploration in Space Science and Technology, NASA Goddard Space Flight Center, Greenbelt, MD 20771, USA

⁸ Faculty of Engineering, Gifu University, 1-1 Yanagido, Gifu 501-1193, Japan

⁹ Dr. Karl Remels Observatory and ECAP, Universität Erlangen-Nürnberg, Sternwartstrasse 7, D-96049, Bamberg, Germany

¹⁰ Department of Physics, United Arab Emirates University, Al-Ain, 15551, UAE

¹¹ Department of Astronomy, University of Illinois, Urbana, IL 61801, USA

¹² Center for Computational Sciences, University of Tsukuba, Ten-nodai, 1-1-1 Tsukuba, Ibaraki 305-8577, Japan

¹³ Kitami Institute of Technology, 165 Koen-cho, Kitami, Hokkaido 090-8507, Japan

¹⁴ National Astronomical Observatory of Japan, National Institutes of Natural Science, 2-21-1 Osawa, Mitaka, Tokyo 181-8588, Japan

Received 2021 March 23; revised 2023 April 2; accepted 2023 April 3; published 2023 May 31

Abstract

The nature of molecular clouds and their statistical behavior in subsolar metallicity environments are not fully explored yet. We analyzed data from an unbiased CO ($J = 2-1$) survey at the spatial resolution of ~ 2 pc in the northern region of the Small Magellanic Cloud with the Atacama Compact Array to characterize the CO cloud properties. A cloud-decomposition analysis identified 426 spatially/velocity-independent CO clouds and their substructures. Based on the cross-matching with known infrared catalogs by Spitzer and Herschel, more than 90% CO clouds show spatial correlations with point sources. We investigated the basic properties of the CO clouds and found that the radius–velocity linewidth (R – σ_v) relation follows the Milky Way-like power-law exponent, but the intercept is ~ 1.5 times lower than that in the Milky Way. The mass functions (dN/dM) of the CO luminosity and virial mass are characterized by an exponent of ~ 1.7 , which is consistent with previously reported values in the Large Magellanic Cloud and in the Milky Way.

Unified Astronomy Thesaurus concepts: Local Group (929); Small Magellanic Cloud (1468); Molecular clouds (1072); Star formation (1569); Interstellar medium (847); Young stellar objects (1834)

Supporting material: machine-readable tables

1. Introduction

Molecular clouds are the densest phase of the interstellar medium (ISM) and the fundamental cradles for star formation. Although the primary ingredient of molecular gas is hydrogen molecules, its direct measurement is almost impossible due to the lack of a suitable transition under the typical condition of molecular clouds. Alternative tracers, such as low- J transitions of CO and thermal dust emission, have been used to reveal the molecular cloud distribution and properties. In the past few decades, observations with the millimeter-wave facilities improved our understanding of the nature of molecular clouds in the solar neighborhood and the Galactic plane (see the review by Heyer & Dame 2015). Molecular clouds traced by CO observations in the Milky Way (MW) follow a standard size–linewidth relation (see Solomon et al. 1987), and the CO luminosity and the mass are well correlated with each other,

suggesting that the molecular clouds are in virial equilibrium as a whole (e.g., Larson 1981).

These observations have not been limited to the MW, but extended to some of the other galaxies in the Local Group (e.g., Cohen et al. 1988; Rubio et al. 1991; Fukui et al. 1999; Engargiola et al. 2003; Nietten et al. 2006; see the review by Fukui & Kawamura 2010), providing information on the statistical properties of molecular clouds. However, some of the extreme conditions are not fully explored yet in high spatial resolution due to observational difficulties. Among them, low-metallicity environments are a good frontier for understanding the star formation in the early universe. The MW observations indicate that the metallicity decreases with increasing galactocentric radius, down to subsolar values (Fernández-Martín et al. 2017), and thus the outermost part in the Galactic disk is suitable for studying this aspect, and some surveys confirmed the presence of CO clouds (e.g., Dame & Thaddeus 2011b; Izumi et al. 2014; Matsuo et al. 2017). Unfortunately, distance ambiguities and contamination in the same line of sight in the Galactic plane are always problems for us when a uniform sample is to be obtained and statistical analyses are to be performed.



Original content from this work may be used under the terms of the [Creative Commons Attribution 4.0 licence](https://creativecommons.org/licenses/by/4.0/). Any further distribution of this work must maintain attribution to the author(s) and the title of the work, journal citation and DOI.

In this regard, the Small Magellanic Cloud (SMC), with a metallicity of $\sim 0.2 Z_{\odot}$ (Russell & Dopita 1992; Rolleston et al. 1999; Pagel 2003), is above the Galactic plane, providing a suitable condition for observing the entire galaxy and understanding the behavior of the CO cloud through its favorable spatial extension and proximity (~ 62 kpc; Graczyk et al. 2020). The metallicity is close to that in the early universe, showing active star formation (Pei et al. 1999), and thus, it is desirable to obtain the fundamental parameter from spatially resolved observations, such as the CO-to- H_2 conversion factor (hereafter, X_{CO}), to understand the gas properties of more remote galaxies. Rubio et al. (1991) and Mizuno et al. (2001) performed large-scale CO surveys with an angular resolution of $8''.8$ or $2''.6$, corresponding to 160 – 45 pc. They derived an X_{CO} in the SMC of $(2.5\text{--}6) \times 10^{21} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$, which is 10 – 20 times higher than the canonical Galactic value of $\sim 2 \times 10^{20} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$ (e.g., Dame et al. 2001; Bolatto et al. 2013), by comparing the CO luminosity and the dynamical (virial) mass. However, these studies also suggested that the beam-filling factor of CO clouds in the SMC is smaller than that of the Galactic molecular cloud, and the large-beam measurements introduce large uncertainties in the analysis, even if the virial equilibrium assumption is reasonable. Several theoretical studies proposed that the X_{CO} factor depends on metallicity with a power-law index of $-(0.5\text{--}0.8)$ (e.g., Feldmann et al. 2012), indicating that the sub-solar metallicity condition does not significantly change the X_{CO} factor from that of the MW value. Smaller beam size measurements indeed yielded lower values than the above surveys, although the results are based on only partial observations compared to the entire galaxy (e.g., Bolatto et al. 2003; Muraoka et al. 2017; Jameson et al. 2018; O'Neill et al. 2022). The fundamental properties of molecular clouds, such as the mass function and size–linewidth relation, are not necessarily sufficiently obtained by compiling a statistically large sample. Saldaña et al. (2023) recently presented the SMC CO ($2\text{--}1$) survey at a resolution of 9 pc using the Atacama Pathfinder Experiment (APEX) telescope and obtained basic properties of molecular clouds across the galaxy. Nevertheless, higher-sensitivity and higher-resolution data are still needed for a complete census, including low-mass and infrared-quiescent clouds, whose CO intensities are generally weak.

The Atacama Large Millimeter/submillimeter Array (ALMA) has the potential to perform a high-resolution unbiased survey of a relatively small galaxy. Especially, the Atacama Compact Array (ACA), known as the Morita array, is not only sensitive to a low-spatial frequency component, which is probably advantageous for capturing an extended CO cloud, but also has the advantage of a wider field of view than the 12 m array (the ALMA Main array), making it a powerful survey instrument. In our companion paper of Tokuda et al. (2021; hereafter Paper I), we described the ALMA archival CO survey covering $\sim 0.26 \text{ deg}^2$ in the northern SMC, assessed the data quality, and provided the initial results of the data analysis. The present paper includes a detailed discussion of the CO cloud decomposition and a statistical analysis to understand the role of CO as molecular cloud tracer. Section 2 summarizes the CO data that we use in this manuscript, and then we present the identification method of CO clouds and their characterization in Section 3. The discussions and summary are presented in Sections 4 and 5, respectively.

2. The Data

This study uses the ALMA archival CO data in the SMC northern region (2017.A.00054.S), which was proposed by the ALMA observatory as one of the six filler programs¹⁵ for the ACA stand-alone mode. Because Paper I described the survey setting and data reduction in detail, we briefly summarize the data quality here. The available data set includes the CO ($J = 2\text{--}1$) and CO ($J = 1\text{--}0$) lines, and $1.3/2.6$ mm continuum data with a field coverage of $\sim 0.26 \text{ deg}^2$. The angular resolution and sensitivity of CO ($J = 2\text{--}1$) are $6''.9 \times 6''.6$ (~ 2 pc) and ~ 0.06 K, respectively. The Cube data with a velocity-channel width of 0.5 km s^{-1} were used throughout the analysis in this paper. The resultant detection limit in the CO ($J = 2\text{--}1$) luminosity is $\sim 1.0 \text{ K km s}^{-1} \text{ pc}^2$ (Paper I). Note that the angular resolution and sensitivity of the CO ($J = 2\text{--}1$) data are two and four times better than those in the CO ($J = 1\text{--}0$) data, respectively, and thus we mainly use the former data in this study.

3. Results

3.1. Cloud Decomposition

Interstellar molecular clouds generally have hierarchical, complex structures composed of diffuse gas, dense filaments, and cores (e.g., Lada & Adams 1992). The complexity in nature makes it difficult for us to determine clear boundaries of each subcomponent; nevertheless, some decomposition analyses, which have been developed in the last decades (e.g., Williams et al. 1994; Rosolowsky & Leroy 2006; Rosolowsky et al. 2008), are still powerful tools for characterizing cloud properties and their statistical nature, such as the size–linewidth relation and mass function. As described in Paper I, the CO molecular clouds in the SMC are spatially more compact than those in the MW, and the outer boundaries are relatively easy to define. On the other hand, larger clouds in the observed field have multiple local peaks inside, requesting a hierarchical characterization of the structure with different intensity levels. Bolatto et al. (2013) suggested that the properties of the outer and inner regions of molecular clouds are somewhat different in low-metallicity environments, such as the SMC. Therefore, it is useful to treat the large outer and small inner structures separately. The dendrogram algorithm *astrodendro* (Rosolowsky et al. 2008; Shetty et al. 2012; Colombo et al. 2015) is one of the best options to meet our requirements (see also the comparison of different cloud-decomposition methods by Li et al. 2020). Several studies (Wong et al. 2017; Naslim et al. 2018; Nayak et al. 2018; Wong et al. 2019) applied the same scheme to ALMA CO data of molecular clouds in the Large Magellanic Cloud (LMC) at an angular resolution of ~ 1 pc. The CPROPS method of Rosolowsky & Leroy (2006) is also promising, but there are limitations in decomposing physically reasonable objects in highly crowded and low-contrast environments (Colombo et al. 2014). A patchwork-like separation using CLUMPFIND (Williams et al. 1994) enables us to estimate the total flux of discrete objects, but large and small structures cannot be treated separately.

As input data, we used postprocessed CO cube, moment-masked data (see Dame 2011a) whose emission-free pixels were set at zero value judging from a smoothed data cube

¹⁵ <https://almascience.eso.org/news/alma-announces-aca-observatory-filler-programs-for-cycle-6>

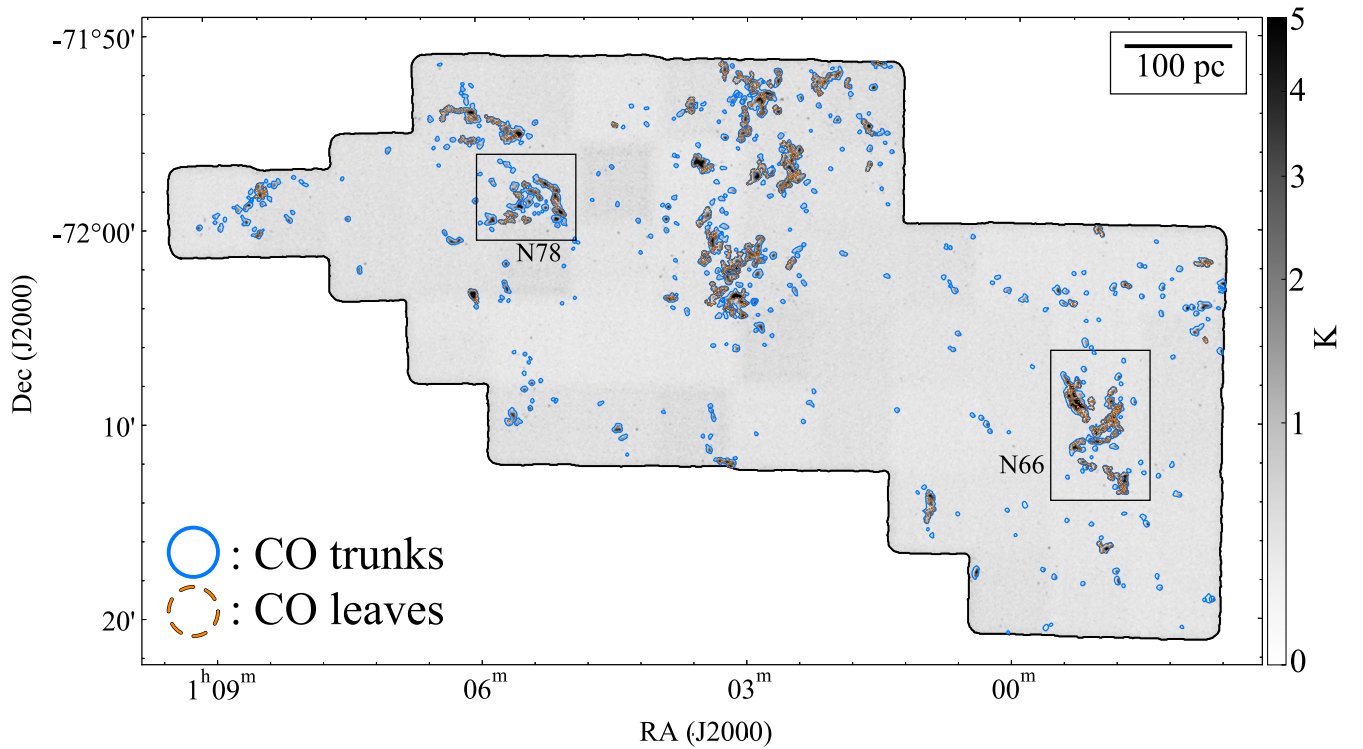


Figure 1. Distributions of the identified structures on the CO ($J = 2-1$) map of the SMC northern region. The grayscale image shows the peak brightness temperature map in CO ($J = 2-1$) obtained with the ACA. The solid cyan and dashed orange contours denote the boundaries of the CO trunks and leaves, respectively, that were identified by the *astrodendro* algorithm. The two rectangles show the areas displayed in Figure 2.

whose signal-to-noise ratio is higher than that of the raw data (see also the detailed description in Section 2 in Paper I). The *astrodendro* algorithm has three input parameters, `min_value`, `min_npix`, and `min_delta`. The first argument is the minimum-intensity value to consider in the cube data. Because most of the noise-component pixels have already been eliminated by the masking analysis, we decided to consider emissions that were as weak as possible by setting `min_value` to 0 K. This zero-level setting minimizes the truncation effect of weak emission and does not account for unreliable weak peaks. The combination with the other two parameters described below resulted in a significant cloud identification with a lowest peak intensity of 0.35 K ($\gtrsim 5\sigma$) among all entities. The second parameter, `min_pix`, is the minimum number of voxels that have significant emission in the three-dimensional (x, y, v) axis needed to be connected as a single component. We set this value of 38 equal to the voxel number of at least a single-beam element in XY space and three pixels in the velocity direction. These two parameters are well defined by the setting of the observation, and thus, we treat them as fixed values, while the last parameter, `min_delta`, can be chosen arbitrarily. The value is a threshold for entities in close proximity to be considered as independent components. Our fiducial value of `min_delta` is 0.18 K, corresponding to a noise level of $\sim 3\sigma$ for the data set. The number of identified structures and statistical results does not change significantly even if this value is changed by a factor of several from the fiducial value. Although we decomposed the cloud and discussed the data using the fixed fiducial value, the parameter dependence is further discussed in the Appendix.

We performed the *astrodendro* analysis and identified 426 structures, called trunks, which are the largest continuous structures. Of these, 361 trunks do not contain internal

structures and are categorized as single CO trunks, which are spatially/velocity-independent entities of the surroundings. In addition, 65 trunks contain internal structures (referred to as CO leaves) for a total of 257 internal leaves. We refer to the 426 trunks and 257 internal leaves as CO trunks and CO leaves, respectively. Figure 1 illustrates the boundary of individual sources of the two categories on the CO map. Figure 2 shows two examples of zoomed-in views toward the N66 and N78 regions to demonstrate how the identified structures are distributed in the two large systems. The CO trunk boundaries are determined by an isosurface close to the minimum-intensity contour level in the data cube, providing a fairly robust identification against the input parameter dependence. The 2D projected map sometimes shows overlapping boundaries, but they are independent entities in velocity space. The dependence of `min_delta` is somewhat more sensitive in the CO leaves than in the trunks. Nevertheless, the CO leaf boundary seems to reasonably trace local peaks on the CO map (see Figure 2).

The *astrodendro* analysis outputs the basic properties of the identified structures, their centroid coordinates in three-dimensional axes ($\bar{x}$, $\bar{y}$, $\bar{v}$), the rms size of the major/minor axes (σ_{maj} and σ_{min}), the rms linewidth σ_v , and the position angle of the major axis (P.A.). Within the isosurface contours of all identified structures, we additionally derived several parameters. The brightness temperature T_{peak} is simply the peak value of the identified voxels. We integrated the flux to obtain the CO ($J = 2-1$) luminosity $L_{\text{CO}(2-1)}$, adopting a distance of 62 kpc (Graczyk et al. 2020). The effective rms size, $\sigma_r = \sqrt{\sigma_{\text{maj}}\sigma_{\text{min}}}$, is multiplied by 1.91, as suggested by Solomon et al. (1987), to derive the observed spherical radius R_{obs} , and then we applied the beam-deconvolution scheme, $R_{\text{deconv}} = \sqrt{R_{\text{obs}}^2 - \theta_{\text{beam}}^2}$, where θ_{beam} is the beam size of the

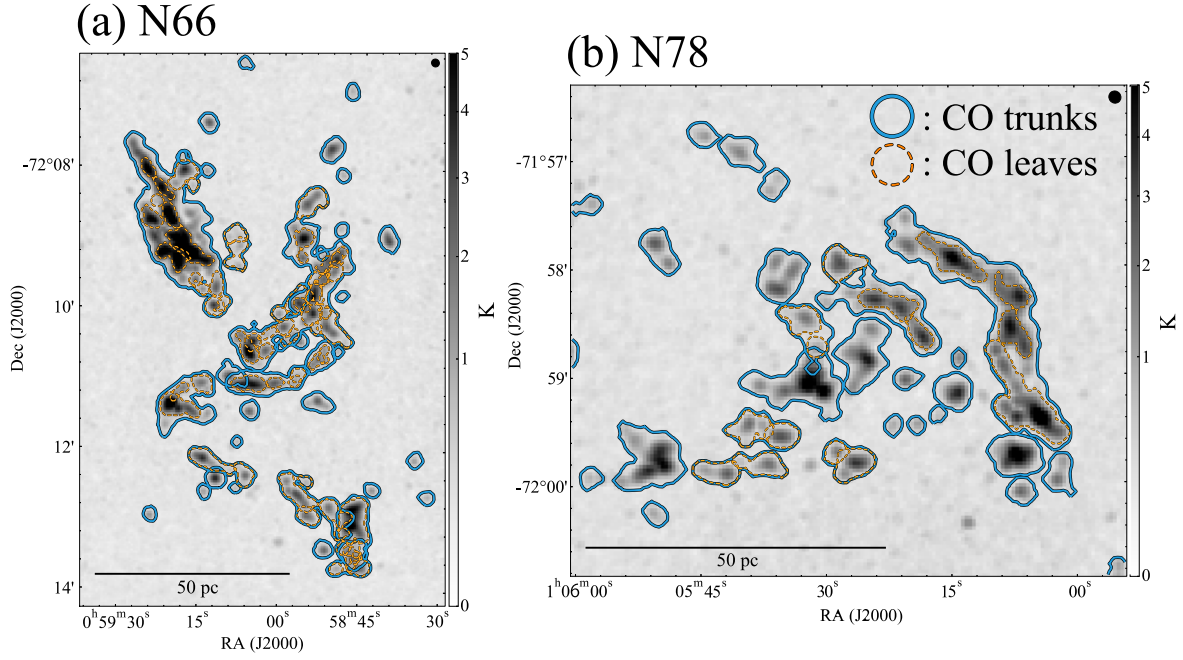


Figure 2. Zoomed-in views of the CO trunks and leaves on the CO ($J = 2-1$) map toward the N66 and N78 regions. (a) The grayscale image, the solid cyan and dashed orange contours show the peak brightness temperature map, the CO trunk and leaf boundaries, respectively, toward the N66 region. The black ellipse in the upper right corner is the angular resolution of the CO ($J = 2-1$) data, $6''.9 \times 6''.6$. (b) Same as (a), but for the N78 region.

Table 1
Physical Properties of the CO Trunks

id	R.A. (J2000.0)	Decl. (J2000.0)	$\bar{v}$	σ_v	$\delta\sigma_v$	σ_{maj}	σ_{min}	P.A.	T_{peak}	$L_{\text{CO}(2-1)}$	$\delta L_{\text{CO}(2-1)}$
(1)	(hms)	(dms)	(km s^{-1})	(km s^{-1})	(km s^{-1})	(arcsec)	(arcsec)	(deg)	(K)	($\text{K km s}^{-1} \text{pc}^2$)	($\text{K km s}^{-1} \text{pc}^2$)
0	0 ^h 57 ^m 46 ^s .8	−72°19′04″.8	116.1	0.52	0.13	5.5	3.4	94.5	2.5	41.7	0.6
1	0 ^h 59 ^m 52 ^s .3	−72°14′24″.0	117.0	0.37	0.18	4.3	2.7	110.4	2.8	21.3	1.1
2	0 ^h 59 ^m 33 ^s .4	−72°20′34″.8	121.2	0.34	0.27	2.5	1.7	−156.6	1.1	3.9	1.4
3	0 ^h 59 ^m 37 ^s .0	−72°20′42″.0	122.1	0.70	0.15	3.4	2.6	71.0	2.9	31.9	0.8
4	0 ^h 59 ^m 58 ^s .3	−72°15′57″.6	121.7	0.38	0.28	2.1	1.9	−142.1	0.4	1.9	0.8
5	1 ^h 00 ^m 37 ^s .7	−72°14′56″.4	128.1	0.43	0.22	2.4	2.2	114.9	1.4	6.7	0.9
6	0 ^h 59 ^m 04 ^s .1	−72°11′02″.4	144.3	2.02	0.06	14.4	3.5	−175.8	4.4	343.0	0.3
7	0 ^h 58 ^m 22 ^s .6	−72°12′46″.8	144.6	0.55	0.21	2.7	2.4	76.2	2.0	13.5	0.9
8	0 ^h 58 ^m 52 ^s .6	−72°10′40″.8	145.1	1.55	0.06	5.8	3.6	48.4	1.9	72.9	0.3
9	0 ^h 58 ^m 04 ^s .6	−72°20′31″.2	145.2	0.39	0.24	2.3	1.9	138.1	0.8	3.5	1.1

id	R_{deconv}	δR_{deconv}	M_{vir}	δM_{vir}	N_{H_2}	M_{CO}	n_{H_2}	IR source
(13)	(pc)	(pc)	($M_{\odot}$)	($M_{\odot}$)	(10^{21} cm^{-2})	($M_{\odot}$)	(10^2 cm^{-3})	(21)
0	2.26	0.08	634	310	3.0	751	6	B
1	1.66	0.11	235	239	1.9	385	8	A
2	0.63	0.24	74	144	0.9	69	27	B
3	1.38	0.10	696	301	4.3	574	21	A
4	0.51	0.23	78	147	0.5	34	24	B
5	0.88	0.18	167	192	1.3	120	17	B
6	3.98	0.04	16871	924	12.1	6183	9	A
7	1.05	0.13	332	258	2.4	243	20	A
8	2.41	0.06	6000	467	4.3	1315	9	A
9	0.65	0.20	101	148	0.8	62	21	B

Note. δ denotes the errors, and they are derived using the bootstrap method (see the text in Section 3.1). Column density (N_{H_2}), CO luminosity masses (M_{CO}), and H_2 volume density (n_{H_2}) assuming $X_{\text{CO}} = 7.5 \times 10^{20} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$ and a CO (2–1)/(1–0) ratio of 0.9. A and B represent the Spitzer + Herschel YSO candidate and other Spitzer catalog sources, respectively (see the text in Section 3.3). The full catalog is available as online material.

(This table is available in its entirety in machine-readable form.)

Table 2
Physical Properties of the CO Leaves

id	R.A. (J2000.0) (hms)	Decl. (J2000.0) (dms)	$\bar{v}$ (km s ⁻¹)	σ_v (km s ⁻¹)	$\delta\sigma_v$ (km s ⁻¹)	σ_{maj} (arcsec)	σ_{min} (arcsec)	P.A. (deg)	T_{peak} (K)	$L_{\text{CO}(2-1)}$ (K km s ⁻¹ pc ²)	$\delta L_{\text{CO}(2-1)}$ (K km s ⁻¹ pc ²)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)
0	0 ^h 58 ^m 56 ^s .9	-72°10'55" 2	140.5	1.30	0.22	2.6	2.0	-140.9	0.9	9.6	0.3
1	0 ^h 59 ^m 01 ^s .0	-72°11'02" 4	142.8	0.75	0.25	2.8	1.5	-173.0	2.4	21.1	0.3
2	0 ^h 59 ^m 05 ^s .5	-72°11'02" 4	145.3	1.08	0.11	6.5	2.2	176.3	4.4	142.3	0.3
3	0 ^h 59 ^m 14 ^s .6	-72°11'06" 0	146.4	1.45	0.13	3.3	2.5	155.2	1.9	38.6	0.4
4	0 ^h 58 ^m 53 ^s .3	-72°10'44" 4	144.0	0.47	0.33	3.5	1.7	46.1	1.9	11.9	0.4
5	0 ^h 58 ^m 57 ^s .1	-72°11'02" 4	144.3	0.44	0.29	2.2	1.7	-139.0	1.1	5.1	0.7
6	0 ^h 57 ^m 54 ^s .7	-72°01'40" 8	146.7	0.99	0.09	5.0	3.0	171.0	3.2	71.4	0.4
7	0 ^h 58 ^m 52 ^s .1	-72°10'37" 2	146.2	0.62	0.30	3.6	1.5	79.8	1.3	10.0	0.2
8	0 ^h 58 ^m 53 ^s .5	-72°09'46" 8	147.4	0.87	0.17	4.0	1.6	105.1	1.2	9.1	0.3
9	0 ^h 59 ^m 18 ^s .5	-72°11'09" 6	147.2	0.50	0.31	4.9	1.4	-137.3	1.7	10.3	0.3

id	R_{deconv} (pc)	δR_{deconv} (pc)	M_{vir} ($M_{\odot}$)	δM_{vir} ($M_{\odot}$)	N_{H_2} (10 ²¹ cm ⁻²)	M_{CO} ($M_{\odot}$)	n_{H_2} (10 ² cm ⁻³)
(13)	(14)	(15)	(16)	(17)	(18)	(19)	(20)
0	0.80	0.15	1406	514	1.9	173	32
1	0.59	0.14	346	256	4.5	381	180
2	1.93	0.07	2367	472	10.0	2565	34
3	1.31	0.10	2870	533	5.1	696	30
4	0.94	0.16	216	314	1.8	214	25
5	0.41	0.24	82	155	1.2	93	132
6	1.97	0.10	2026	399	5.7	1286	16
7	0.88	0.19	355	364	2.0	180	26
8	1.07	0.16	847	368	1.6	165	13
9	1.11	0.17	292	374	1.9	186	13

Note. Same as Table 1, but for CO leaves. Information of infrared source associations to the CO leaves is included in the final column (see Section 3.3). The full catalog is available as online material.

(This table is available in its entirety in machine-readable form.)

present study. We used an approach to estimate the uncertainties of the cloud properties following the bootstrap method (Rosolowsky & Leroy 2006). We generated 100 realizations to sample the derived parameters. Tables 1 and 2 summarize the properties of some of the identified CO trunks and leaves, respectively, and the full catalogs are available as online material.

Figure 3 shows histograms of the R_{deconv} , σ_v , $L_{\text{CO}(2-1)}$, and T_{peak} of the CO trunks and leaves. The total number of luminous large structures is not very large with respect to the full population. The most CO luminous source ($L_{\text{CO}(2-1)} \sim 2500$ K km s⁻¹ pc²) is the northern filamentary complex in N66 (see also Neelamkodan et al. 2021), as shown at the upper left side of Figure 2(a). For the smaller structure, the CO trunks and leaves seem to exhibit relatively similar properties as a whole.

The physical quantities described above are purely determined from the observational data. Although additional assumptions are needed, we calculated the following properties to further characterize the identified CO sources. We derived the virial mass, $M_{\text{vir}} = 1040\sigma_v^2 R_{\text{deconv}}$ (Solomon et al. 1987) assuming the density profile of $\rho \propto r^{-1}$, ignoring the effect of external pressure and magnetic field. The peak-integrated intensity was used to calculate the H₂ column density (N_{H_2}) with the assumptions of a CO-to-H₂ conversion factor, $X_{\text{CO}} = 7.5 \times 10^{20} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$ (Muraoka et al. 2017) in the SMC and an intensity ratio of CO ($J = 2-1$)/CO ($J = 1-0$), $R_{2-1/1-0}$ of 0.9 (Bolatto et al. 2003; Paper I). Note that the X_{CO} factor in the low-metallicity SMC environment is not as

tightly constrained as the Galactic value. Based on the recent measurement in the literature, the mass determination accuracy is presumably a factor of two or three at best (see also the discussion and our independent estimation using the current CO data set in Section B). M_{CO} is the total gas mass integrated over the regions inside the lowest contour level of the identified structure. We estimated the average H₂ number density using the following equation: $n_{\text{H}_2} = 3M_{\text{CO}}/4\pi\mu m_{\text{H}}R_{\text{deconv}}^3$, where μ is the mean molecular weight per hydrogen (2.7), and m_{H} is the H atom mass.

We further explain the relation among the cloud properties, such as the size–linewidth relation, and the cloud mass function in Sections 3.2, 4.1 and 4.2. We also perform cross-matching analyses with the CO trunks and infrared young stellar sources in Section 3.3.

3.2. Size–Linewidth Relation

Large-scale molecular cloud surveys found the famous scaling relation between the molecular cloud radius R in pc units and the velocity dispersion σ_v : that is, $\sigma_v \approx 0.72R^{0.5} \text{ km s}^{-1}$ (e.g., Larson 1981; Solomon et al. 1987; Heyer et al. 2001). This relation is established over a wide spatial range from ~ 1 pc to several hundred pc. The sizes (radii) of our CO cloud sample identified as trunks range from ~ 1 pc to a few dozen pc, which allows us to test whether a similar relation to the MW is also valid in the SMC over an order of magnitude. Figure 4 shows the $\sigma_v - R_{\text{deconv}}$ plot of the CO trunks and leaves: σ_v becomes larger as R_{deconv} increases.

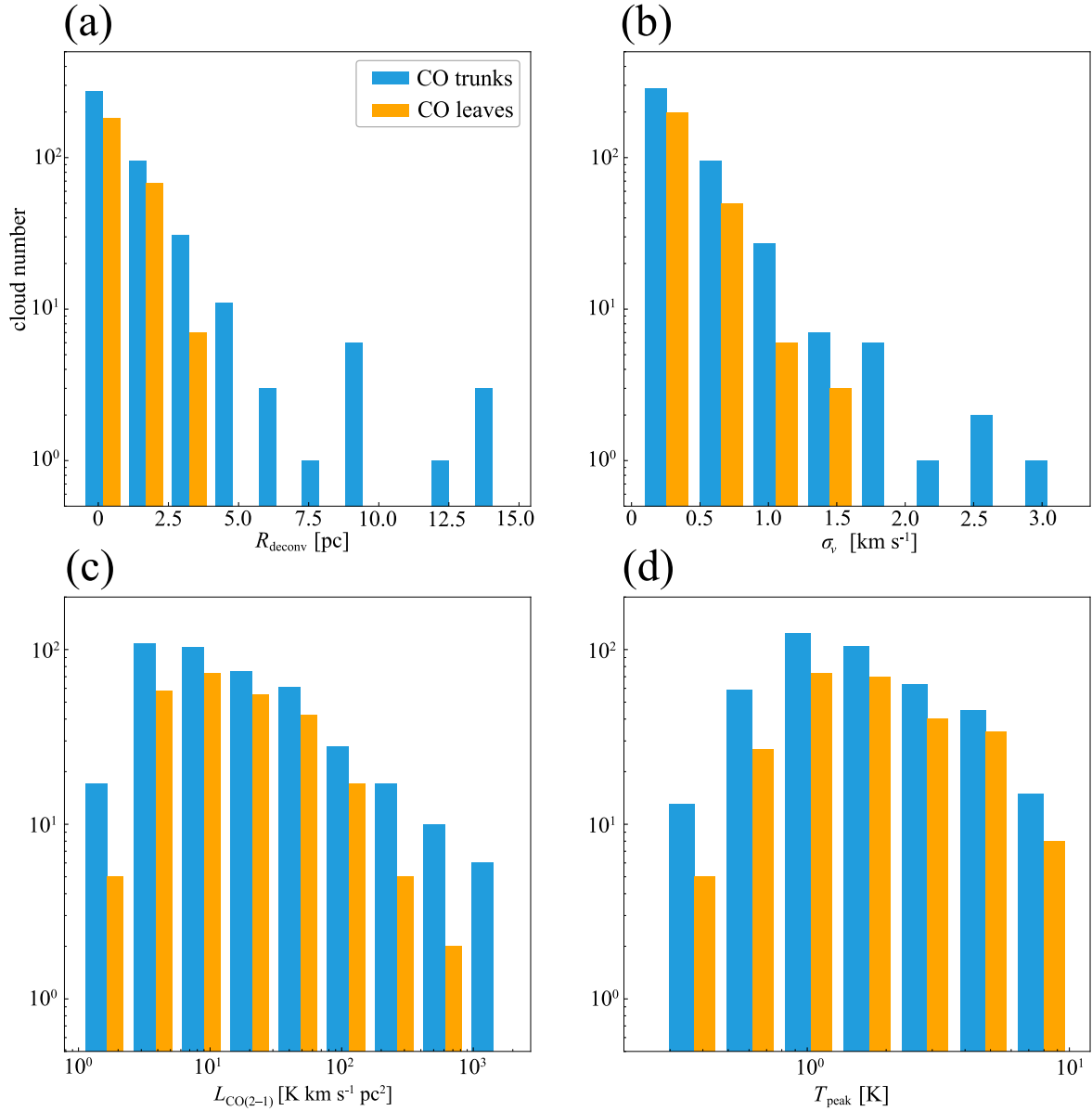


Figure 3. Histograms of the physical properties of the CO trunks (cyan) and leaves (orange) in the SMC northern region. Panels (a), (b), (c), and (d) show the deconvolved radius R_{deconv} , the velocity dispersion σ_v , the luminosity $L_{\text{CO}(2-1)}$, and the peak brightness temperature T_{peak} , respectively.

We performed an orthogonal distance regression (ODR) fitting, taking into account the errors in both axes (`scipy.odr`; Virtanen et al. 2020), to determine the intercept and slope of $\sigma_v = \alpha_0 R^{-\beta}$. As shown in Figure 4, the best-fit values are $(\alpha_0, \beta) = (0.46 \pm 0.01, 0.56 \pm 0.02)$ for the CO trunks and $(\alpha_0, \beta) = (0.49 \pm 0.01, 0.46 \pm 0.04)$ for the CO leaves. The fitted intercepts are ~ 0.2 lower than that in the MW standard relation, while the power-law index is comparable to that of the MW. The recent CO (2–1) SMC survey at a 9 pc resolution also reproduced a similar trend (Saldaña et al. 2023). We discuss the implications of the size–linewidth relation in Section 4.1.

3.3. Cross-matching Analysis between CO and Infrared Sources

We investigated whether the CO trunks have known infrared sources with their categories of (1) Spitzer + Herschel young stellar object (YSO) candidates and (2) not necessarily categorized

as YSO, but infrared point sources discovered by Spitzer. Based on a better infrared position accuracy than the beam size of the ACA, we regarded a CO trunk as an associated source if there was at least a single infrared source within its cloud boundary.

Gordon et al. (2011) obtained a comprehensive point-source catalog from the Spitzer Space Telescope Surveying the Agents of Galaxy Evolution in the Tidally Stripped, Low Metallicity Small Magellanic Cloud (SAGE–SMC) Legacy Program. The SAGE–SMC IRAC (InfraRed Array Camera) Single Frame + Mosaic Photometry Catalog has an angular resolution of $\sim 2''$ at IRAC bands (3.5/4.5/5.8/8.0 μm) with a pointing accuracy of $\sim 0''.3$ (see the documentation by Gordon et al. 2014¹⁶), which is sufficiently high to be compared with the ACA CO map at $\sim 7''$ resolution. The Spitzer/SAGE–SMC point-source catalog includes not only YSOs, but also many normal stars, evolved

¹⁶ https://irsa.ipac.caltech.edu/data/SPITZER/SAGE-SMC/docs/sage-smc_delivery_nov09.pdf

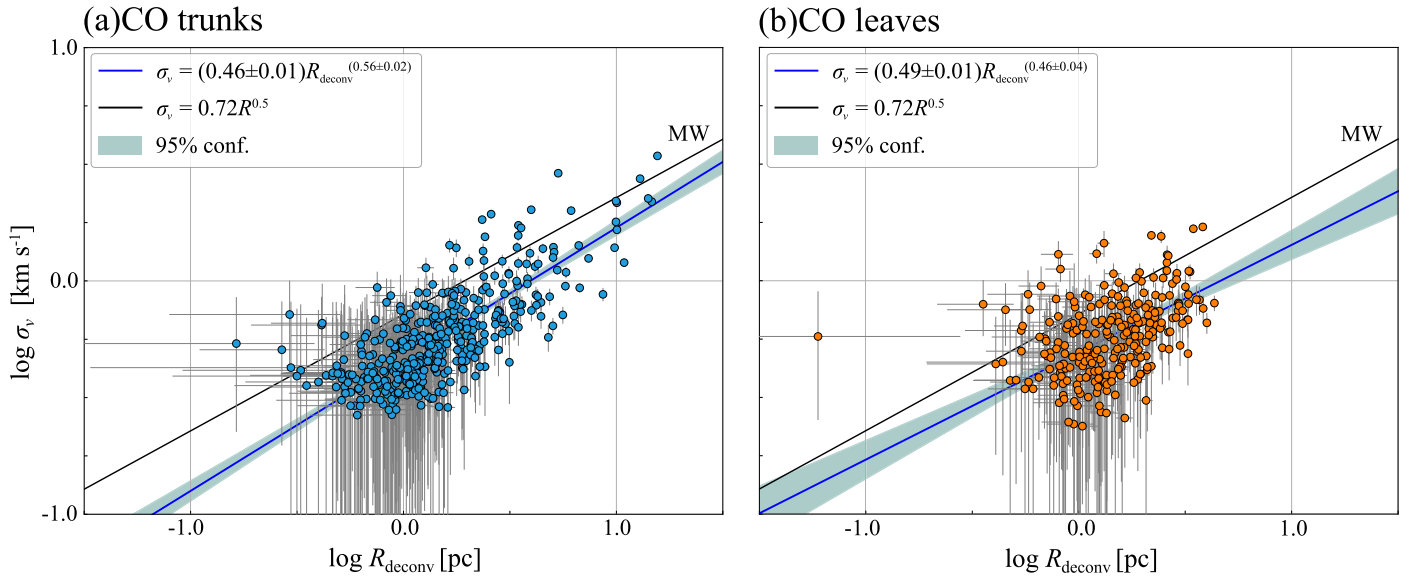


Figure 4. Size(R_{deconv})-linewidth(σ_v) plots of the CO trunks and leaves. Cyan and orange circles denote CO trunks and leaves, respectively. The blue line shows the best-fit functions with the ODR fitting. The constants and power-law indices are shown in the figure legend. The cyan hatch represents the 95% confidence interval for linear regression. The black line denotes the size–linewidth relation derived in CO ($J = 1-0$) observations of MW molecular clouds (Solomon et al. 1987).

stars, and background galaxies (see, e.g., Boyer et al. 2011). Several studies identified and characterized the young population based on the color–magnitude diagram (CMD) spectral energy distribution (SED) modeling by combining data from other wavelengths. There is a list of 4927 objects in the SMC that has at least two or more band identifications as point sources in the IRAC(3.5/4.5/5.8/8.0 μm) or MIPS 24 μm detectors and that satisfy certain CMD criteria to exclude contamination from background galaxies and evolved stars (see Section 4.1 in Sewilo et al. 2013). Sewilo et al. (2013) identified 742 high-reliability YSO candidates across the SMC based on the CMD color–magnitude cuts, image inspection, SED fitting, and a CMD score (a measure of confidence that a source is not a non-YSO contaminant, based on its position in CMDs used for the initial source selection). Out of these, 452 candidates are well characterized by YSO SED models (Robitaille et al. 2006). Within the ACA observed field, the total number of the Spitzer-based YSO candidates is 254; they are plotted in Figure 5(a). Seale et al. (2014) extended the YSO search to longer wavelengths based on the HERschel Inventory of the Agents of Galaxy Evolution (HERITAGE) data (Meixner et al. 2013). Figure 5(b) shows the identified candidates, which are the high-reliability + possible YSOs in the Seale et al. (2014) catalog. In the ACA observed field, there are 25 YSO candidates that were not cataloged in the Spitzer mid-infrared studies above, indicating that they are likely younger. We call them (1) Spitzer + Herschel YSO candidate list and investigate whether they are contained within the lowest contours of the CO trunks.

The positions of the Spitzer + Herschel YSO candidates show a good spatial correlation with the CO cloud distributions, indicating that they are true YSOs enveloped in their natal molecular material. However, due to the CMD selection criteria, these highly reliable YSO samples are mostly biased toward high- and intermediate-mass objects (Sewilo et al. 2013). In addition, the angular resolution of the previous CO survey (e.g., $\sim 160''$; Mizuno et al. 2001) was two orders of magnitude coarser than that of Spitzer, making it impossible to

accurately investigate whether the IRAC point sources are spatially correlated with molecular clouds. Our analysis of the CO cloud association with the full IRAC/MIPS catalog potentially allows us to search for additional YSO candidate samples. We conducted a cross-matching between the SAGE-SMC catalog sources and our CO data and found that 336 CO trunks were associated, while the remaining 90 entities did not match the catalog. Additionally, we compared with the S³MC (Spitzer Survey of the Small Magellanic Cloud) catalog (Bolatto et al. 2007; Simon et al. 2007), which is based on a deeper survey than SAGE-SMC. The combined SAGE-SMC and S³MC source lists are collectively referred to as “other Spitzer catalog sources”. We first checked whether the list (1) is in the CO clouds, and if it was not, (2) we investigated whether the other Spitzer source list was attached within them. For display purposes, we only plot the (2) sources with a CO detection within the lowest contours of the trunks (Figure 5(c)).

If there is no other Spitzer catalog source in the CO trunks, it is regarded as a starless cloud candidate, highlighted in blue contours in Figure 5(c). It should be noted that according to the current criteria for infrared catalog extraction, these candidates are still considered to be in a purely starless phase. Upon our visual inspection of the IRAC maps, some sources with extended emission also have local peaks that appear to be associated with CO clouds. Furthermore, even in sources that are completely dark in the Spitzer survey, high-resolution molecular gas studies have sometimes discovered molecular outflow as a strong indicator of protostar formation in infrared-quiet regions in the MW (e.g., Tan et al. 2016) and the LMC (e.g., Tokuda et al. 2019, 2022). The James Webb Space Telescope (JWST) will enable us to detect these faint sources that are missed with Spitzer. However, because these sources are low-mass sources or are in an early stage of high-mass star formation, we believe that their feedback effect on the parental cloud itself is negligible on a large scale, and it is not deeply explored in this work.

Column (21) of Table 1 denotes the cross-matched results. The 426 CO trunks in total (see Section 3.1) can be divided into three categories: 94 Spitzer + Herschel YSO sources, 303

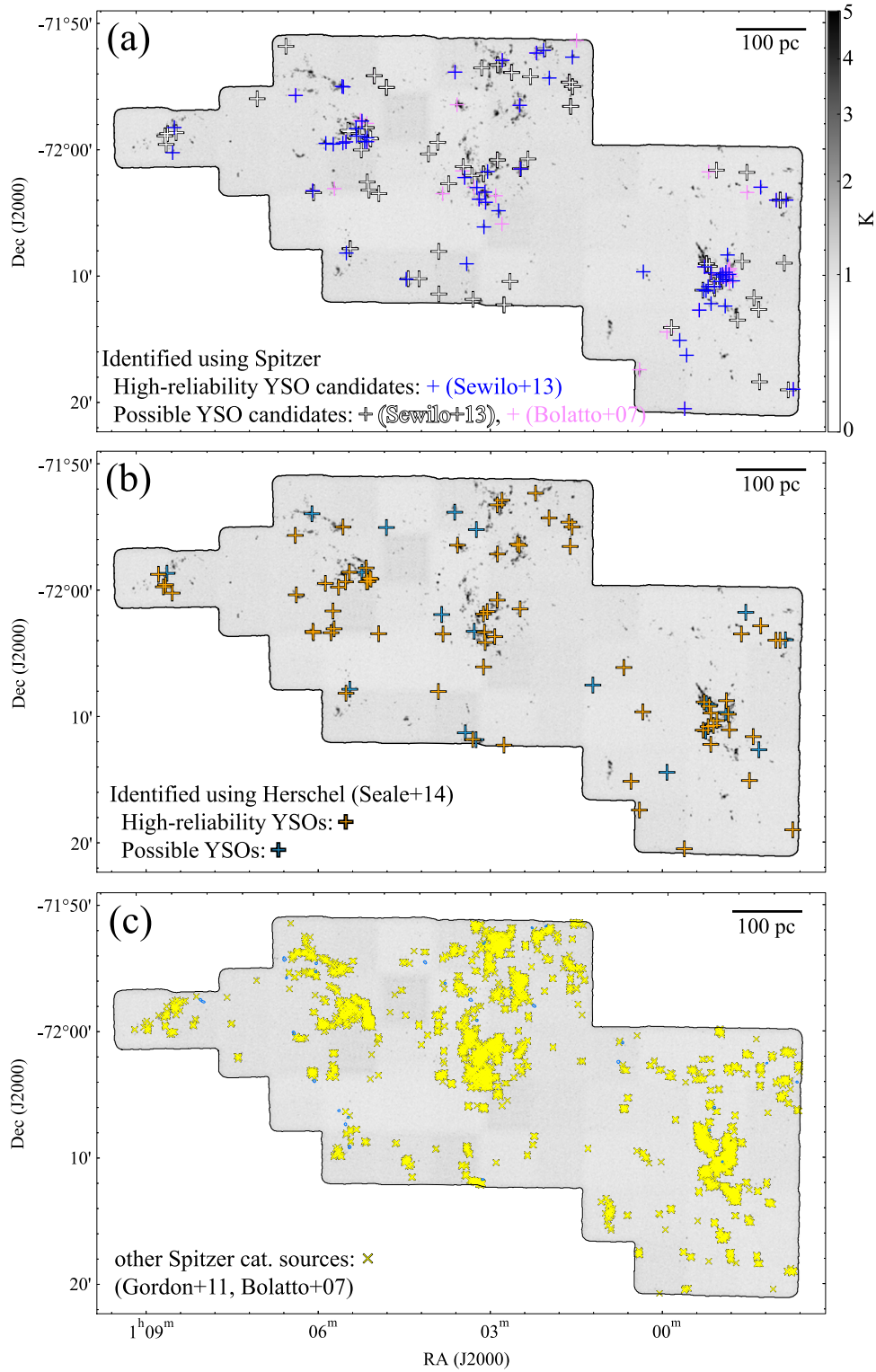


Figure 5. Distributions of infrared sources on the CO ($J = 2-1$) peak brightness temperature map of the SMC northern region. (a) Blue crosses denote high-reliability YSO candidates, and white and pink crosses denote possible YSO candidates (Bolatto et al. 2007; Sewilo et al. 2013). Panel (b): Same as panel (a), but the orange and cyan crosses denote the highly reliable and possible YSOs, respectively, identified by Seale et al. (2014) using Herschel data. Panel (c): Same as panel (a), but the yellow crosses denote the position of the other Spitzer catalog sources (Bolatto et al. 2007; Gordon et al. 2011) associated with the CO clouds. Blue contours highlight the starless cloud candidates (see the text).

Spitzer catalog sources, and 29 starless cloud candidates. To facilitate the comparison among the categories, the following analysis excludes the CO trunks with CO leaves, i.e., complex, large structures. Table 3 summarizes the typical (median)

properties of the single CO trunks of each category. The resulting numbers of Spitzer + Herschel sources, other Spitzer catalog sources, and starless cloud candidates are 57, 275, and 29, respectively. We performed a Kolmogorov-Smirnov (KS)

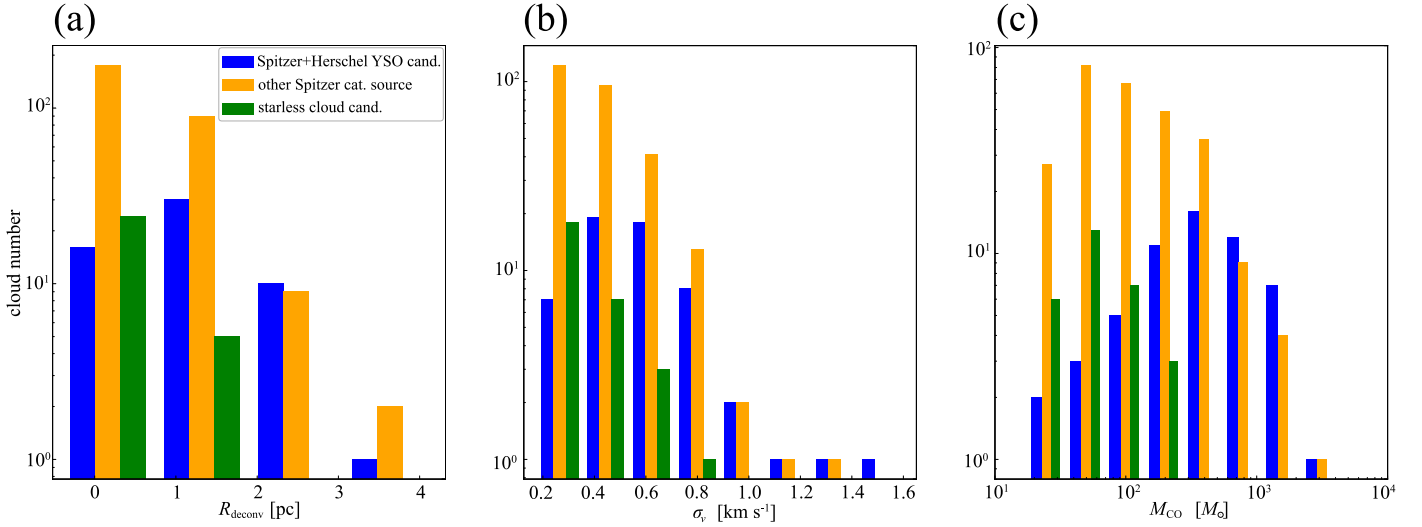


Figure 6. Histograms of the physical properties of the single CO trunks in the SMC northern region. Panels (a), (b), and (c) show the deconvolved radius R_{deconv} , the velocity dispersion σ_v , and the CO luminosity-based mass M_{CO} , respectively. Blue, orange, and green bars denote the number of single CO trunks with Spitzer + Herschel YSO, other Spitzer catalog sources, and starless candidate sources, respectively.

Table 3
The Median Properties of the Three Categories of the Single CO Trunks in the SMC North

Category	Number	σ_v (km s ⁻¹)	$\pm\sigma_v$ (km s ⁻¹)	$L_{\text{CO}(2-1)}$ (K km s ⁻¹ pc ²)	$\pm L_{\text{CO}(2-1)}$ (K km s ⁻¹ pc ²)	R_{deconv} (pc)	$\pm R_{\text{deconv}}$ (pc)
Spitzer + Herschel YSO candidate	57	0.66	0.25	31.9	47.3	1.57	0.80
other Spitzer catalog source	275	0.46	0.17	7.2	20.9	1.14	0.66
Starless cloud candidate	29	0.40	0.13	4.2	4.1	0.91	0.38
Category	N_{H_2} (10 ²¹ cm ⁻²)	$\pm N_{\text{H}_2}$ (10 ²¹ cm ⁻²)	M_{CO} ($M_{\odot}$)	$\pm M_{\text{CO}}$ ($M_{\odot}$)	n_{H_2} (10 ² cm ⁻³)	$\pm n_{\text{H}_2}$ (10 ² cm ⁻³)	Total M_{CO} [10 ⁴ $M_{\odot}$]
Spitzer + Herschel YSO candidate	3.9	2.5	574	853	14	23	4.8
other Spitzer catalog source	1.1	1.1	130	377	10	49	7.1
Starless cloud candidate	0.7	0.4	75	73	10	29	0.3

Note. $\pm$ denotes the standard deviation of each physical property. We adapted $X_{\text{CO}} = 7.5 \times 10^{20} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$ to obtain the column density (N_{H_2}), cloud mass (M_{CO}), and number density (n_{H_2}). The total M_{CO} is the sum of M_{CO} in each category.

test to determine whether the physical properties belonged to different populations. The p -values for the Spitzer + Herschel YSO, other Spitzer catalog, and starless candidate source properties are all below 0.05, except for n_{H_2} . Nevertheless, we argue that all the samples belong to distinct populations.

The total number and M_{CO} of the starless sources correspond to $\sim 8\%$ and $\sim 2\%$, respectively, with respect to the total population (see Table 3). σ_v and M_{CO} appear to be larger as the star formation activity becomes energetic. The typical σ_v in the Spitzer + Herschel YSO sources is indeed larger than the value that we expect from the global size–linewidth relation (Section 3.2) at the R_{deconv} . Figure 6 shows the comparison histogram of the physical properties. The general trend is that large physical quantities are in the two categories: Spitzer + Herschel YSO candidate, and other Spitzer catalog source.

Single-dish Galactic and ALMA LMC studies also obtained a higher velocity dispersion and a larger radius/mass at star-forming clouds (Kawamura et al. 1998; Ikeda & Kitamura 2009; Nayak et al. 2016; Naslim et al. 2018). They discussed that feedback from protostellar objects, such as high-radiation

pressure of shocks and molecular outflow/jets, enhances the linewidth. The increase in M_{CO} suggests that there is a mass accumulation during the star and/or cloud formation phase. The possible mass-supply sources are CO-dark- H_2 and/or H I gas around the CO clouds, as suggested in LMC studies (e.g., Fukui et al. 2019; Tokuda et al. 2019, 2022). According to some theoretical studies, atomic gas is a more important reservoir to promote star formation in a lower-metallicity environment (e.g., Krumholz 2012; Fukushima et al. 2020).

Interestingly, we found many compact CO clouds whose location is relatively isolated from the larger clouds in the field (see also Paper I). In these clouds, massive YSOs do exist at some of the isolated compact clouds, and they could be suitable targets in which to explore the initial condition of high-mass star formation because the relatively simple configuration provides an easier way than typical molecular cloud complexes that harbor well-developed H II regions and/or supernova remnants. Extragalactic studies are more appropriate for discovering such an object, and recent ALMA observations have been studying similar targets in the LMC (Harada et al. 2019). Follow-up

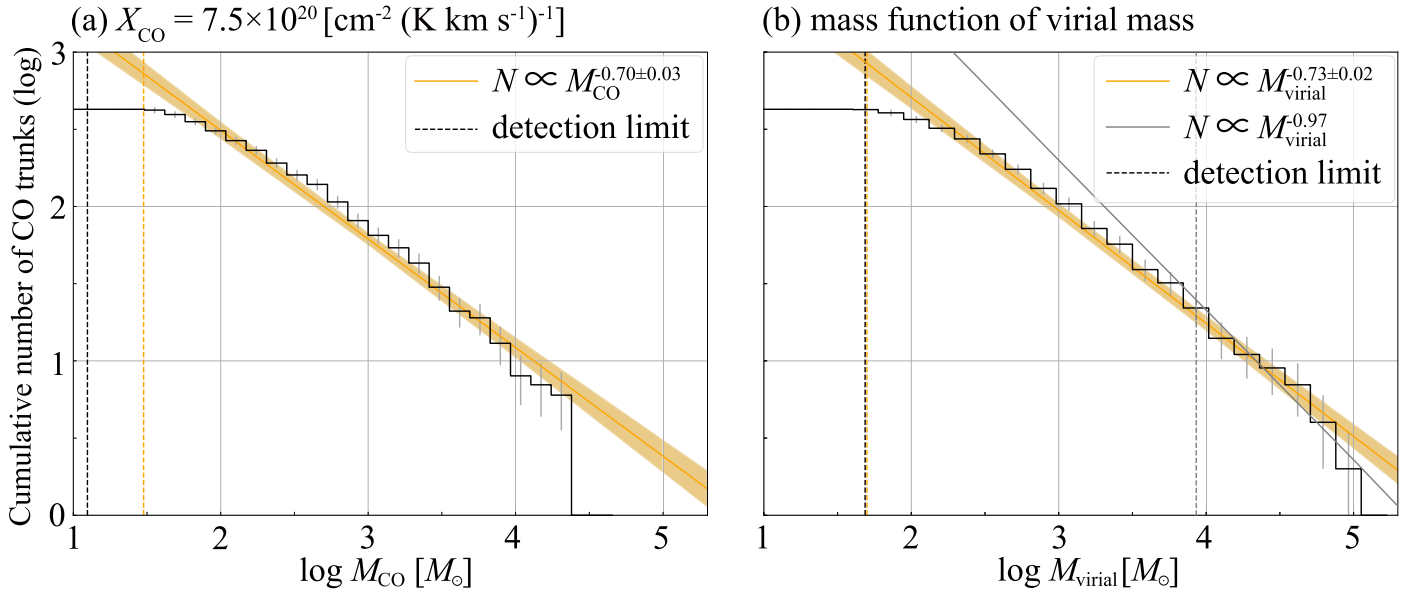


Figure 7. Cumulative M_{CO} spectra of the CO trunks using the luminosity-based mass (a) and virial mass (b). Mass ranges larger than the vertical dashed orange line were used for the ODR fitting, and the best-fit power-law function for each fitting is shown in the figure legend. The orange hatch denotes the 95% confidence interval for the fitting. Mass detection limits are shown by dashed black lines in each panel. The solid gray line in panel (b) indicates the fitted slope with a mass range of $> 8.6 \times 10^3 M_{\odot}$.

ALMA 12 m array observations in the SMC are desired to further understand the nature of these isolated clouds and the star formation therein.

4. Discussions

4.1. Meaning of the Size–Linewidth Relation

Bolatto et al. (2008) already described that the velocity dispersions are smaller for clouds with the same sizes compared with the MW relation by a factor of two in lower-metallicity targets of their sample (see also Saldaño et al. 2023). They probably overestimated the cloud sizes due to the larger beam size of ~ 10 pc. Our ACA observations show that the size–linewidth relation is closer to that in the MW than the Bolatto et al. (2008) result, possibly thanks to the improved spatial resolution. However, we still see a departure from the MW relation toward the lower side in velocity dispersions with a factor of ~ 1.5 . Bolatto et al. (2008) discussed two possibilities for this trend: (1) the column density is lower than the MW under the condition of virial equilibrium, or (2) the turbulent motion is not strong enough to stabilize the core, and the clouds are supposed to be unstable against the freefall collapse. In the former case, the column density is proportional to the square of linewidth, i.e., our finding of ~ 1.5 times lower velocity dispersion in the SMC predicts a factor of ~ 2 lower column density. The second idea is highly unlikely in the MW because statistical counting methods using a large number of starless cores with respect to star-forming cores tell us that the lifetime of dense objects until protostar formation is generally longer than the freefall time (Onishi et al. 2002; Ward-Thompson et al. 2007) unless their central density exceeds $\sim 10^6 \text{ cm}^{-3}$ (Tokuda et al. 2020). The derived density range of the CO clouds is on the order of 10^2 cm^{-3} (Table 3), and although it might be slightly higher, around 10^4 cm^{-3} , as suggested by early studies (Muraoka et al. 2017; Paper I), it is unlikely that all of these less-dense clouds are undergoing freefall collapse. We note that the above-mentioned dense core

surveys in the MW (e.g., Ward-Thompson et al. 2007) constrained the starless cloud densities using multiple molecular lines with a higher spatial resolution as well as independent measurements, such as millimeter/submillimeter continuum observations. Our current SMC study has a single CO line with a lower spatial resolution, and thus it is likely that the uncertainty of the density estimation is quite large compared to the above MW surveys. Moreover, it is difficult to prove whether the starless sources are truly “starless” down to a low-mass star regime in the SMC as well. These observational limitations should be overcome to constrain the timescale of starless molecular clouds more precisely and to further explore the implications of the size–linewidth relations by future studies.

4.2. The CO Cloud Mass Spectrum

The frequency distribution of the mass of the molecular cloud is presented as $dN/dM \propto M^{-\alpha}$ or in the cumulative form, $N(>M) \propto M^{-(\alpha-1)}$. This observed quantity is relevant to the fundamental problem of star formation, how molecular clouds transform into stars, i.e., the origin of the initial mass function. From a galactic perspective, an ensemble of formation and destruction processes of molecular clouds likely determines the cloud mass function (Inutsuka 2015; Kobayashi & Inutsuka 2017). Although various CO surveys have been revealed, the cloud population along the MW Galactic plane and nearby galaxies, weak CO emission in metal-poor environments, such as the SMC, makes it difficult for us to accumulate a sufficient sample to know the cloud mass function. Saldaño et al. (2023) obtained a sufficient number (> 100) of CO clouds in the SMC for the first time and derived the mass spectrum. Our ACA observations still give us further constraints down to the low-mass regime where the CO emission is not clearly visible in the previous single-dish measurement.

We use the trunks, which are spatially or velocity-isolated components defined by a low-level contour and are assumed to be less sensitive against the astrodendro parameters.

Figure 7 represents the cloud mass spectra of the luminosity and virial mass with the cumulative form. The features are very similar between the two spectra, except for the presence of massive clouds in the virial mass plot. We performed the ODR fitting to the mass spectra and reasonably characterized them by a single power law across two of three orders of magnitudes in the mass range with an exponent of ~ 0.7 , corresponding to $\alpha \sim 1.7$. Takekoshi et al. (2017) reported a similar value, $\alpha = 1.76$, with their completeness limit of $8 \times 10^3 M_\odot$, by compiling the 1.1 mm continuum selected Giant Molecular Clouds (GMCs) across the SMC.

We compare the derived mass spectrum index, ~ 1.7 with the previous CO study in the SMC. Saldaño et al. (2023) reported a steeper power-law index of $\alpha = 3.1\text{--}3.5$ in the same region, N66 + NE, in their paper. The discrepancy is presumably caused by the following three factors. (1) The field coverage of our ACA study is wider than that of the APEX observations (Saldaño et al. 2023). The molecular clouds in the SMC northern region are more sparsely distributed than in the southwestern region. The limited field coverage with APEX did not capture some of the massive CO clouds. The SW region, where many CO clouds are densely packed into almost the same area as the NE coverage, shows shallower mass spectra. (2) The fitting mass ranges are different from each other. We performed a fitting to the M_{vir} function of our data in the same range as Saldaño et al. (2023), $> 8.6 \times 10^3 M_\odot$, and obtained a steeper index, $\alpha \sim 2$ (see Figure 7(b)). (3) The resultant index of the cloud mass function somewhat depends on the observation sensitivity and the decomposition algorithm (e.g., Pineda et al. 2009). Their analysis using CPROPS (Rosolowsky & Leroy 2006) extracted local maxima of the CO emission, possibly causing an oversegmentation for larger clouds. It is not necessarily consistent with our trunk-based identification, whose cloud boundaries are well characterized by the lowest contour level. Considering some observational and methodological limitations, $\alpha \sim 1.7$ derived by our study in the SMC northern region and/or $\alpha \sim 2$ derived by Saldaño et al. (2023) in the other SMC regions would currently be appropriate values to represent the CO cloud mass function of the galaxy.

We subsequently compare the CO cloud mass spectrum in the SMC with the spectra in the MW and LMC studies at galactic scales. Heyer et al. (2001) and Fukui et al. (2008) reported that the indices α of CO cloud spectra are ~ 1.8 in the MW and LMC. These are consistent with our results. Note that a higher-resolution survey in the LMC by Wong et al. (2011) reported a much steeper value, possibly because the larger clouds are resolved into smaller ones, which probably is the same as the third issue in the previous paragraph. Although the CO emission likely cannot trace a large amount of molecular material in the metal-poor environment (e.g., Glover & Clark 2012; Bisbas et al. 2021; Fukushima et al. 2020, see also Paper I), it is still intriguing that the Local Group of galaxies shows a similar behavior in CO cloud mass function. M. I. N. Kobayashi et al. (2023, in preparation) numerically demonstrated that mass functions of cold neutral medium, which eventually evolve into molecular clouds, show a spectrum index of 1.7 and do not largely depend on the metallicity condition with $Z = 0.2\text{--}1.0 Z_\odot$ after sufficient cooling time under the same converging H I flow setting. It will be important in the future to develop a theory and/or numerical

models of molecular cloud formation that take into account the CO abundance and compare these models with observations.

Inutsuka (2015) formulated that the exponent of the mass function is determined by the ratio of the formation and destruction timescale (T_f and T_d) of molecular clouds and suggested that the theory explains the observed indices of $\alpha = 1.5\text{--}2.0$ well if T_d is longer than T_f (see also Kobayashi & Inutsuka 2017). We also remark that there is a mass truncation at $\sim 10^4\text{--}10^5 M_\odot$ in the SMC northern spectra. The mass truncation is determined by the total amount of parental material, i.e., H I (Kobayashi & Inutsuka 2017). These environments do not harbor many high-mass stars, making superbubble-type H I flows, which would be a supply source that might trigger massive GMC formation, and thus can provide the mass truncation in quiescent interarm regions in the MW and in M51 (Kobayashi & Inutsuka 2017; Kobayashi et al. 2018). Because Saldaño et al. (2023) also argued that low-mass clouds are dominant in the SMC, additional interferometric studies such as our ACA observations toward other regions would provide further insight into the CO cloud mass function and its regional dependence in the low-metallicity SMC.

5. Summary

The CO($J = 2\text{--}1$) ACA survey in the SMC northern region with a field coverage of $\sim 0.26 \text{ deg}^2$ is a powerful map based on which the CO cloud population and properties can be comprehensively understood. Its size scale ranges from ~ 1 pc to a few dozen pc. Our analysis and the obtained implications are summarized as follows:

1. Using the `astrodendro` package, we have decomposed the observed CO clouds into 426 spatially and velocity-isolated components surrounded by a low-level isosurface contour (trunks) and 257 smaller internal structures (leaves). Out of all of the identified structures, $\sim 85\%$ of the trunks do not have internal leaf substructures (single CO trunks), indicating that many compact/isolated clouds exist throughout the observed field. Based on the cross-matching analysis with the known infrared sources that are cataloged based on Spitzer and Herschel studies, a large fraction (more than 90%) of the single CO trunks harbors infrared sources are most likely YSOs.
2. The size–linewidth relation for CO clouds (trunks and leaves) tends to show a smaller linewidth as a whole than that in the MW with a factor of ~ 1.5 . Although an independent single-dish CO study (Saldaño et al. 2023) also confirmed this trend, our parsec-size beam size measurement further constrains this down to small radii of the CO clouds in the unbiased higher-resolution study. One possible interpretation of the lower velocity dispersion is that the column density is a factor of ~ 2 lower than the densities in the MW clouds, assuming that the cloud is well supported against freefall collapse.
3. The CO-luminosity-based mass and virial mass spectra of the CO trunk in the cumulative form follow power-law indices of ~ -0.7 , corresponding to $dN/dM \propto M^{-1.7}$. The power-law index is similar to the indices from CO surveys of the MW and LMC. Although the CO dark fraction with respect to the total molecular material in the SMC is likely higher than in the two galaxies, the striking similarity of the CO cloud mass function may be one of the milestones for understanding molecular cloud

formation and their metallicity (in)dependence from a theoretical perspective.

We would like to thank the anonymous referee for useful comments that improved the manuscript. This paper makes use of the following ALMA data: ADS/ JAO. ALMA#2017. A.00054.S. ALMA is a partnership of ESO (representing its member states), NSF (USA) and NINS (Japan), together with NRC (Canada), MOST and ASIAA (Taiwan), and KASI (Republic of Korea), in cooperation with the Republic of Chile. The Joint ALMA Observatory is operated by ESO, AUI/ NRAO, and NAOJ. This work was supported by NAOJ ALMA Scientific Research grant Nos. 2022-22B and Grants-in-Aid for Scientific Research (KAKENHI) of Japan Society for the Promotion of Science (JSPS; grant Nos. JP18K13582, JP18H05440, JP21K13962, and JP21H00049). The material is based upon work supported by NASA under award numbers 80GSFC21M0002 and 80NSSC22K0168 (M.S.). The National Radio Astronomy Observatory is a facility of the National Science Foundation operated under cooperative agreement by Associated Universities, Inc. T.W. acknowledges support from collaborative NSF AAG award 2009849. T. Ohno was supported by the ALMA Japan Research Grant of NAOJ ALMA Project, NAOJ-ALMA-286. We thank Dr. Masato I.N.

Kobayashi for the discussion on the cloud mass spectrum from theoretical aspects.

Software: CASA (v5.4.0; CASA Team et al. 2022), Astropy (Astropy Collaboration et al. 2018), APLpy (Robitaille & Bressert 2012).

Appendix A

Input Parameter Dependence of the Cloud Identification

As explained in Section 3.1, `min_delta` is a relatively arbitrary parameter among the `astrodendro` arguments, especially for spatially compact objects with a well-defined outer boundary. We investigate the `min_delta` dependence of the number of identified leaves/trunks (Figure 8). The number of identified clouds decreases sharply in the range of `min_delta` above 1 K. This is because the emission does not satisfy the requirement that they should have a difference of more than 1 K of the brightness temperature within their structure and thus cannot be considered as a single leaf or trunk. As a result, in the range with a large `min_delta`, only structures with a strong intensity contrast (i.e., the maximum intensity is high as well) survive.

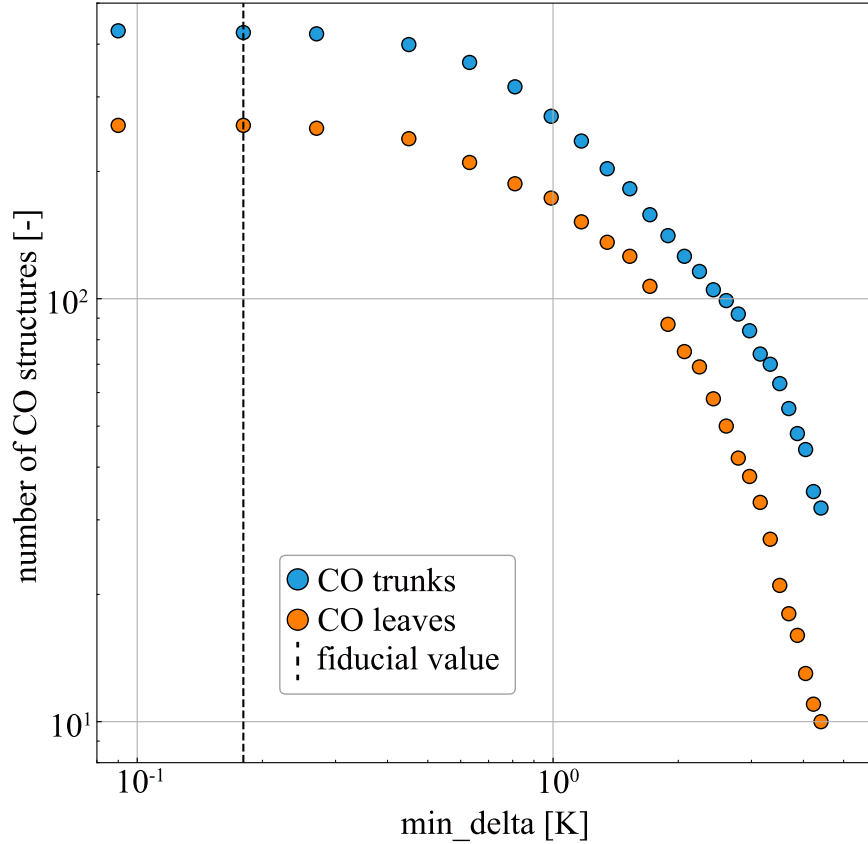


Figure 8. Parameter dependence of the `astrodendro` algorithm on `min_delta`. The dashed black lines correspond to the fiducial value of 0.18 K used for our cloud decomposition.

Appendix B

Virial Mass–CO Luminosity Relation

Figure 9 shows the $L_{\text{CO}(1-0)}$ versus M_{vir} relations of the trunk/leaf structures. Note that we converted the observed $L_{\text{CO}(2-1)}$ into the equivalent CO ($J = 1-0$) luminosity, $L_{\text{CO}(1-0)}$, by adopting an $R_{2-1/1-0}$ of 0.9 (Bolatto et al. 2003; Paper I). The $L_{\text{CO}(1-0)}$ and M_{vir} are well correlated with each other as a whole over the range of two orders of magnitude, indicating that the clouds in the observed region are virialized and that the CO luminosity can be a good tracer of mass.

In the extragalactic perspective, the comparison between the two quantities is an almost unique method for estimating the X_{CO} factor with CO measurements alone (Bolatto et al. 2013) using the following equation:

$$X_{\text{CO}} = \frac{M_{\text{vir}}/(m_{\text{H}}\mu)}{L_{\text{CO}(1-0)}}. \quad (\text{B1})$$

The median values of X_{CO} for the trunks and leaves are $1.3^{+0.8}_{-4.3} \times 10^{21} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$ and $8.4^{+9.6}_{-1.4} \times 10^{20} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$, respectively, with the plus and minus signs indicating the first and third quartiles. As seen in Figure 9, all of the data points are well above the MW canonical relation, $X_{\text{CO}}^{\text{MW}} = 2.0 \times 10^{20} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$, indicating that the conversion factor X_{CO} in the SMC northern region is higher than that in the MW.

We obtained two X_{CO} factors from the identification results for trunks and leaves. We compare the newly derived X_{CO} with that of previous studies in the SMC CO surveys. The NANTEN survey (Mizuno et al. 2001) with an angular resolution of 45 pc reported X_{CO} of $\sim 2.5 \times 10^{21} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$ based on the

same virial-mass-based method. Although their values are close to the value derived in our trunk structure, the lower value is obtained because the fine-beam measurement eliminates the overestimation of the cloud size.

Bolatto et al. (2013) cautioned that this virial-mass-based X_{CO} derivation likely overestimates in the weaker CO regime because the total amount of H_2 of an extended envelope in CO-free/weak positions is highly ambiguous. They recommended using CO-bright regions reflecting a fairly uniform condition in X_{CO} estimate and implied that their derived X_{CO} value is not significantly different from that in the MW CO clouds. Our derived X_{CO} for the leaves is close to this context because the smaller structure inside the clouds tends to reflect the nature of CO-bright local peaks. The X_{CO} for the leaves is also consistent with the SEST and ALMA studies toward the N83/N84 regions (Bolatto et al. 2003; Muraoka et al. 2017). O’Neill et al. (2022) performed an alternative X_{CO} calibration using the optically thin ^{13}CO column density estimation in the NGC 602 region and obtained X_{CO} of $3.4 \times 10^{20} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$. Valdivia-Mena et al. (2020) derived virial-mass-based X_{CO} , $(3-7) \times 10^{20} \text{ cm}^{-2} (\text{K km s}^{-1})^{-1}$ depending on the star formation activities in the Magellanic Bridge (see also Kalari et al. 2020), where the metallicity is the same as or somewhat lower than that in the SMC main body. The 9 pc observations through the SMC yielded an estimate X_{CO} based on virial mass and millimeter continuum emission of 2.5 and 6.5 times that of the MW, respectively. The X_{CO} value in the SMC is not tightly constrained with high accuracy, but it seems certain that on average, X_{CO} is several times higher than that in the galaxy. Theoretical studies (e.g., Feldmann et al. 2012) indicate that the metallicity dependence of the X_{CO} factor is a power-law function with an exponent of $-(0.5-0.8)$.

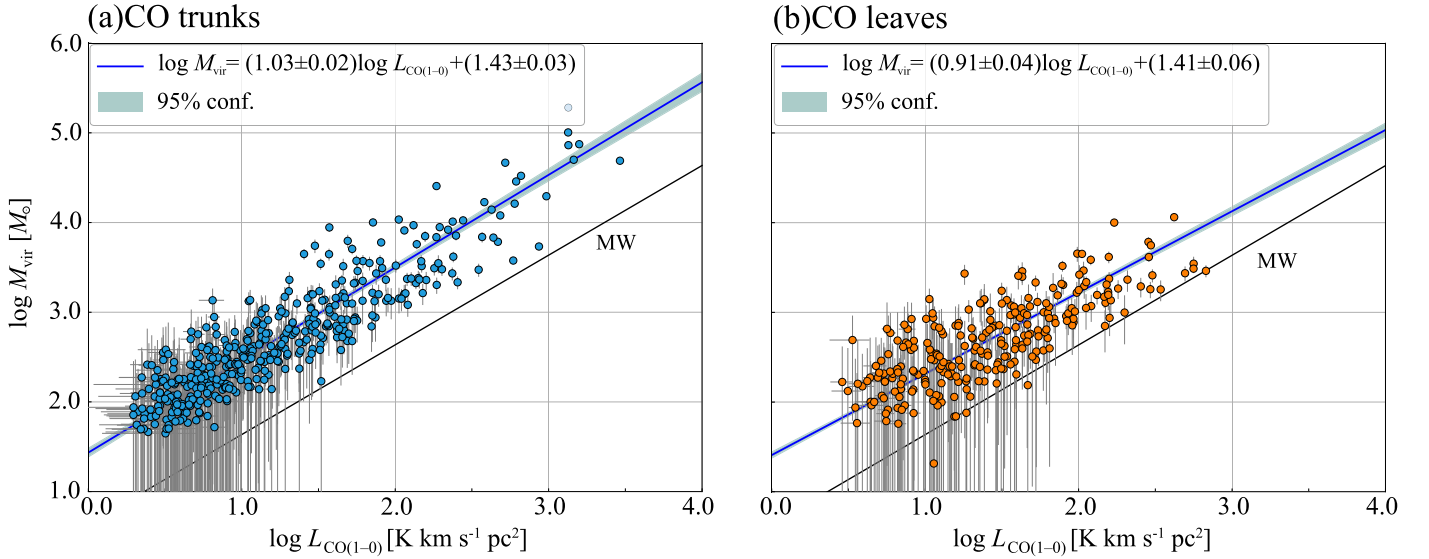


Figure 9. M_{vir} vs. equivalent $L_{\text{CO}(1-0)}$ plots for the CO trunks (a) and leaves (b). Cyan and orange circles denote CO trunks and leaves, respectively. The blue lines and cyan hatches are the best-fit functions and the 95% confidence interval for linear regression with the least-squares method. The intercept and slope of the fitting function are shown in the figure legend with errors.

ORCID iDs

Takahiro Ohno  <https://orcid.org/0000-0003-3330-218X>
 Kazuki Tokuda  <https://orcid.org/0000-0002-2062-1600>
 Ayu Konishi  <https://orcid.org/0000-0002-4098-8100>
 Marta Sewilo  <https://orcid.org/0000-0003-2248-6032>
 Hidetoshi Sano  <https://orcid.org/0000-0003-2062-5692>
 Sarolta Zahorecz  <https://orcid.org/0000-0001-6149-1278>
 Naslim Neelamkodan  <https://orcid.org/0000-0001-8901-7287>
 Tony Wong  <https://orcid.org/0000-0002-7759-0585>
 Hajime Fukushima  <https://orcid.org/0000-0002-0547-3208>
 Tatsuya Takekoshi  <https://orcid.org/0000-0002-4124-797X>
 Kazuyuki Muraoka  <https://orcid.org/0000-0002-3373-6538>
 Akiko Kawamura  <https://orcid.org/0000-0001-7813-0380>
 Kengo Tachihara  <https://orcid.org/0000-0002-1411-5410>
 Yasuo Fukui  <https://orcid.org/0000-0002-8966-9856>
 Toshikazu Onishi  <https://orcid.org/0000-0001-7826-3837>

References

- Astropy Collaboration, Price-Whelan, A. M., Sipőcz, B. M., et al. 2018, *AJ*, **156**, 123
- Bisbas, T. G., Tan, J. C., & Tanaka, K. E. I. 2021, *MNRAS*, **502**, 2701
- Bolatto, A. D., Leroy, A., Israel, F. P., & Jackson, J. M. 2003, *ApJ*, **595**, 167
- Bolatto, A. D., Leroy, A. K., Rosolowsky, E., Walter, F., & Blitz, L. 2008, *ApJ*, **686**, 948
- Bolatto, A. D., Simon, J. D., Stanimirović, S., et al. 2007, *ApJ*, **655**, 212
- Bolatto, A. D., Wolfire, M., & Leroy, A. K. 2013, *ARA&A*, **51**, 207
- Boyer, M. L., Srinivasan, S., van Loon, J. T., et al. 2011, *AJ*, **142**, 103
- CASA Team, Bean, B., Bhatnagar, S., et al. 2022, *PASP*, **134**, 114501
- Cohen, R. S., Dame, T. M., Garay, G., et al. 1988, *ApJL*, **331**, L95
- Colombo, D., Hughes, A., Schinnerer, E., et al. 2014, *ApJ*, **784**, 3
- Colombo, D., Rosolowsky, E., Ginsburg, A., Duarte-Cabral, A., & Hughes, A. 2015, *MNRAS*, **454**, 2067
- Dame, T. M. 2011a, arXiv:1101.1499
- Dame, T. M., Hartmann, D., & Thaddeus, P. 2001, *ApJ*, **547**, 792
- Dame, T. M., & Thaddeus, P. 2011b, *ApJL*, **734**, L24
- Engargiola, G., Plambeck, R. L., Rosolowsky, E., & Blitz, L. 2003, *ApJS*, **149**, 343
- Feldmann, R., Gnedin, N. Y., & Kravtsov, A. V. 2012, *ApJ*, **747**, 124
- Fernández-Martín, A., Pérez-Montero, E., Vilchez, J. M., & Mampaso, A. 2017, *A&A*, **597**, A84
- Fukui, Y., & Kawamura, A. 2010, *ARA&A*, **48**, 547
- Fukui, Y., Kawamura, A., Minamidani, T., et al. 2008, *ApJS*, **178**, 56
- Fukui, Y., Mizuno, N., Yamaguchi, R., et al. 1999, *PASJ*, **51**, 745
- Fukui, Y., Tokuda, K., Saigo, K., et al. 2019, *ApJ*, **886**, 14
- Fukushima, H., Yajima, H., Sugimura, K., et al. 2020, *MNRAS*, **497**, 3830
- Glover, S. C. O., & Clark, P. C. 2012, *MNRAS*, **426**, 377
- Gordon, K. D., Meixner, M., Meade, M. R., et al. 2011, *AJ*, **142**, 102
- Graczyk, D., Pietrzyński, G., Thompson, I. B., et al. 2020, *ApJ*, **904**, 13
- Harada, R., Onishi, T., Tokuda, K., et al. 2019, *PASJ*, **71**, 44
- Heyer, M., & Dame, T. M. 2015, *ARA&A*, **53**, 583
- Heyer, M. H., Carpenter, J. M., & Snell, R. L. 2001, *ApJ*, **551**, 852
- Ikeda, N., & Kitamura, Y. 2009, *ApJL*, **705**, L95
- Inutsuka, S.-i., Inoue, T., Iwasaki, K., & Hosokawa, T. 2015, *A&A*, **580**, A49
- Izumi, N., Kobayashi, N., Yasui, C., et al. 2014, *ApJ*, **795**, 66
- Jameson, K. E., Bolatto, A. D., Wolfire, M., et al. 2018, *ApJ*, **853**, 111
- Kalari, V. M., Rubio, M., Saldaña, H. P., Bolatto, A. D., et al. 2020, *MNRAS*, **499**, 2534
- Kawamura, A., Onishi, T., Yonekura, Y., et al. 1998, *ApJS*, **117**, 387
- Kobayashi, M. I. N., Inutsuka, S.-I., Kobayashi, H., & Hasegawa, K. 2017, *ApJ*, **836**, 175
- Kobayashi, M. I. N., Kobayashi, H., Inutsuka, S.-I., Fukui, Y., et al. 2018, *PASJ*, **70**, S59
- Krumholz, M. R. 2012, *ApJ*, **759**, 9
- Lada, C. J., & Adams, F. C. 1992, *ApJ*, **393**, 278
- Larson, R. B. 1981, *MNRAS*, **194**, 809
- Li, C., Wang, H.-C., Wu, Y.-W., Ma, Y.-H., & Lin, L.-H. 2020, *RAA*, **20**, 031
- Matsuo, M., Nakanishi, H., Minamidani, T., et al. 2017, *PASJ*, **69**, L3
- Gordon, K., Babler, B., Block, M., et al. 2014, The SAGE-SMC Data Description: Delivery 1 Nov 2009, https://irsa.ipac.caltech.edu/data/SPITZER/SAGE-SMC/docs/sage-smc_delivery_nov09.pdf
- Meixner, M., Panuzzo, P., Roman-Duval, J., et al. 2013, *AJ*, **146**, 62
- Mizuno, N., Rubio, M., Mizuno, A., et al. 2001, *PASJ*, **53**, L45
- Muraoka, K., Homma, A., Onishi, T., et al. 2017, *ApJ*, **844**, 98
- Naslim, N., Tokuda, K., Onishi, T., et al. 2018, *ApJ*, **853**, 175
- Nayak, O., Meixner, M., Fukui, Y., et al. 2018, *ApJ*, **854**, 154
- Nayak, O., Meixner, M., Indebetouw, R., et al. 2016, *ApJ*, **831**, 32
- Neelamkodan, N., Tokuda, K., Barman, S., et al. 2021, *ApJL*, **908**, L43
- Nieten, C., Neininger, N., Güélin, M., et al. 2006, *A&A*, **453**, 459
- O'Neill, T. J., Indebetouw, R., Sandstrom, K., et al. 2022, *ApJ*, **938**, 82
- Onishi, T., Mizuno, A., Kawamura, A., Tachihara, K., & Fukui, Y. 2002, *ApJ*, **575**, 950
- Pagel, B. E. J. 2003, in ASP Conf. Ser. 304, CNO in the Universe (San Francisco, CA: ASP), 187
- Pei, Y. C., Fall, S. M., & Hauser, M. G. 1999, *ApJ*, **522**, 604
- Pineda, J. E., Rosolowsky, E. W., & Goodman, A. A. 2009, *ApJL*, **699**, L134
- Robitaille, T., & Bressert, E. 2012, APLpy: Astronomical Plotting Library in Python, Astrophysics Source Code Library, ascl:1208.017
- Robitaille, T. P., Whitney, B. A., Indebetouw, R., Wood, K., & Denzmore, P. 2006, *ApJS*, **167**, 256
- Rolleston, W. R. J., Dufton, P. L., McErlean, N. D., & Venn, K. A. 1999, *A&A*, **348**, 728
- Rosolowsky, E., & Leroy, A. 2006, *PASP*, **118**, 590
- Rosolowsky, E. W., Pineda, J. E., Kauffmann, J., & Goodman, A. A. 2008, *ApJ*, **679**, 1338
- Rubio, M., Garay, G., Montani, J., & Thaddeus, P. 1991, *ApJ*, **368**, 173
- Russell, S. C., & Dopita, M. A. 1992, *ApJ*, **384**, 508
- Saldaña, H. P., Rubio, M., Bolatto, A. D., et al. 2023, *A&A*, **672**, A153
- Seale, J. P., Meixner, M., Sewilo, M., et al. 2014, *AJ*, **148**, 124
- Sewilo, M., Carlson, L. R., Seale, J. P., et al. 2013, *ApJ*, **778**, 15
- Shetty, R., Beaumont, C. N., Burton, M. G., Kelly, B. C., & Klessen, R. S. 2012, *MNRAS*, **425**, 720
- Simon, J. D., Bolatto, A. D., Whitney, B. A., et al. 2007, *ApJ*, **669**, 327
- Solomon, P. M., Rivolo, A. R., Barrett, J., & Yahil, A. 1987, *ApJ*, **319**, 730
- Takekoshi, T., Minamidani, T., Komugi, S., et al. 2017, *ApJ*, **835**, 55
- Tan, J. C., Kong, S., Zhang, Y., et al. 2016, *ApJL*, **821**, L3
- Tokuda, K., Fujishiro, K., Tachihara, K., et al. 2020, *ApJ*, **899**, 10
- Tokuda, K., Fukui, Y., Harada, R., et al. 2019, *ApJ*, **886**, 15
- Tokuda, K., Kondo, H., Ohno, T., et al. 2021, *ApJ*, **922**, 171
- Tokuda, K., Minami, T., Fukui, Y., et al. 2022, *ApJ*, **933**, 20
- Valdivia-Mena, M. T., Rubio, M., Bolatto, A. D., Saldaña, H. P., & Verdugo, C. 2020, *A&A*, **641**, A97
- Virtanen, P., Gommers, R., Oliphant, T. E., et al. 2020, *NatMe*, **17**, 261
- Ward-Thompson, D., André, P., Crutcher, R., et al. 2007, in Protostars and Planets V (Tucson, AZ: Univ. Arizona Press), 33
- Williams, J. P., de Geus, E. J., & Blitz, L. 1994, *ApJ*, **428**, 693
- Wong, T., Hughes, A., Ott, J., et al. 2011, *ApJS*, **197**, 16
- Wong, T., Hughes, A., Tokuda, K., et al. 2017, *ApJ*, **850**, 139
- Wong, T., Hughes, A., Tokuda, K., et al. 2019, *ApJ*, **885**, 50