



**SAGE III**  
**/ISS**

## **Stratospheric Aerosol and Gas Experiment**

**An Earth Science Mission on the International Space Station**

**SAGE III/ISS Science Team Meeting**

**Travis N. Knepp  
Mahesh Kovilakam,  
Stephan J. Miller,  
Larry Thomason**

**Particle Size Distribution Parameters from  
SAGE III/ISS Extinction Spectra, with  
Application to the 2022 Hunga Tonga Eruption**





# Proposed Work

---



- Use Mie theory to identify PSD parameters from SAGE III/ISS data
  - Account for measurement error in PSD estimates
  - Provide confidence intervals for PSD estimates
  - Expand to include other microphysical properties (e.g., SAD and VD)
  - Extend analysis to include bimodal distributions



# Proposed Work



- Use Mie theory to identify PSD parameters from SAGE III/ISS data
  - Account for measurement error in PSD estimates
  - Provide confidence intervals for PSD estimates
  - Expand to include other microphysical properties (e.g., SAD and VD)
  - Extend analysis to include bimodal distributions

Algorithm is complete and all objectives met



# Mie Theory Assumptions

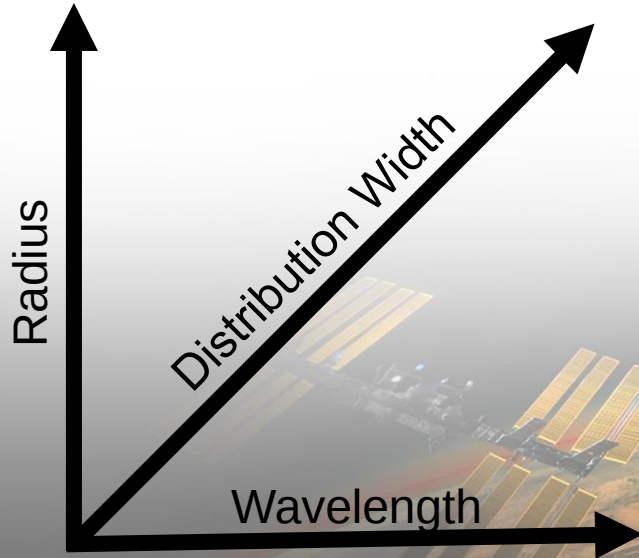


- Invoke standard Mie theory assumptions
  - all particles spherical
  - all distributions are lognormally distributed
  - particles composed of 75% (wt) sulfuric acid, 25% water
    - Palmer and Williams (1975) refractive indices
- above assumptions used in lookup table (LUT) creation



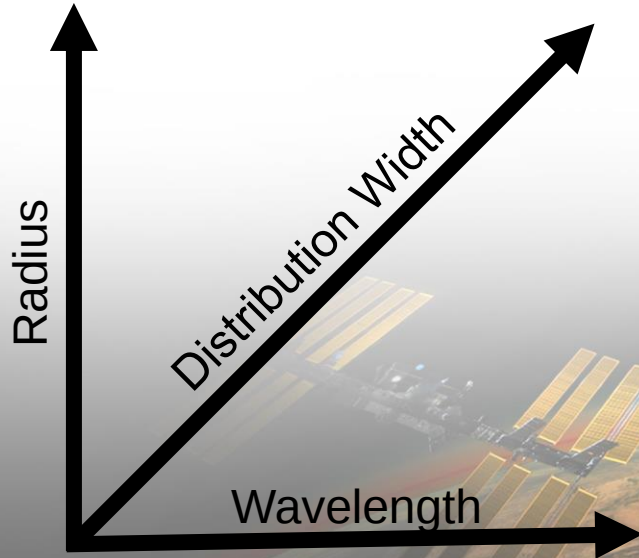
# Lookup Table (LUT)

- Use Mie theory to create lookup tables of extinction coefficients:  $k(r, \lambda, \sigma)$
- Tested for series of extinction ratio combinations



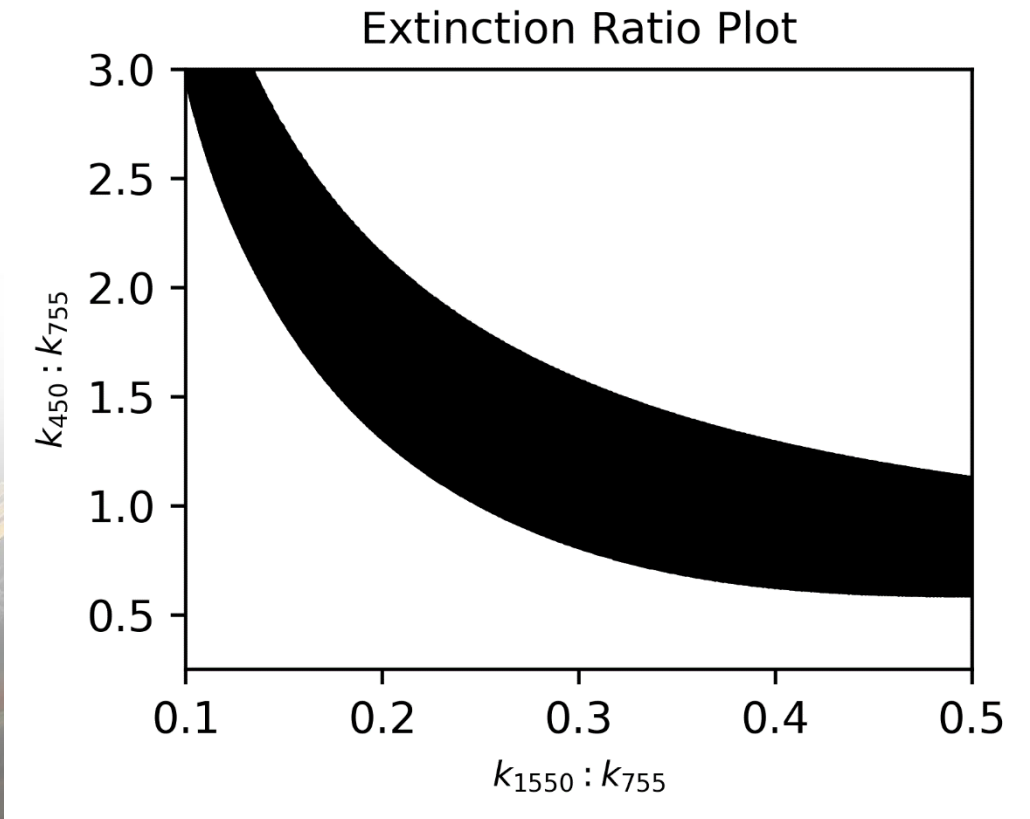
# Lookup Table (LUT)

- Use Mie theory to create lookup tables of extinction coefficients:  $k(r, \lambda, \sigma)$
- Tested for series of extinction ratio combinations

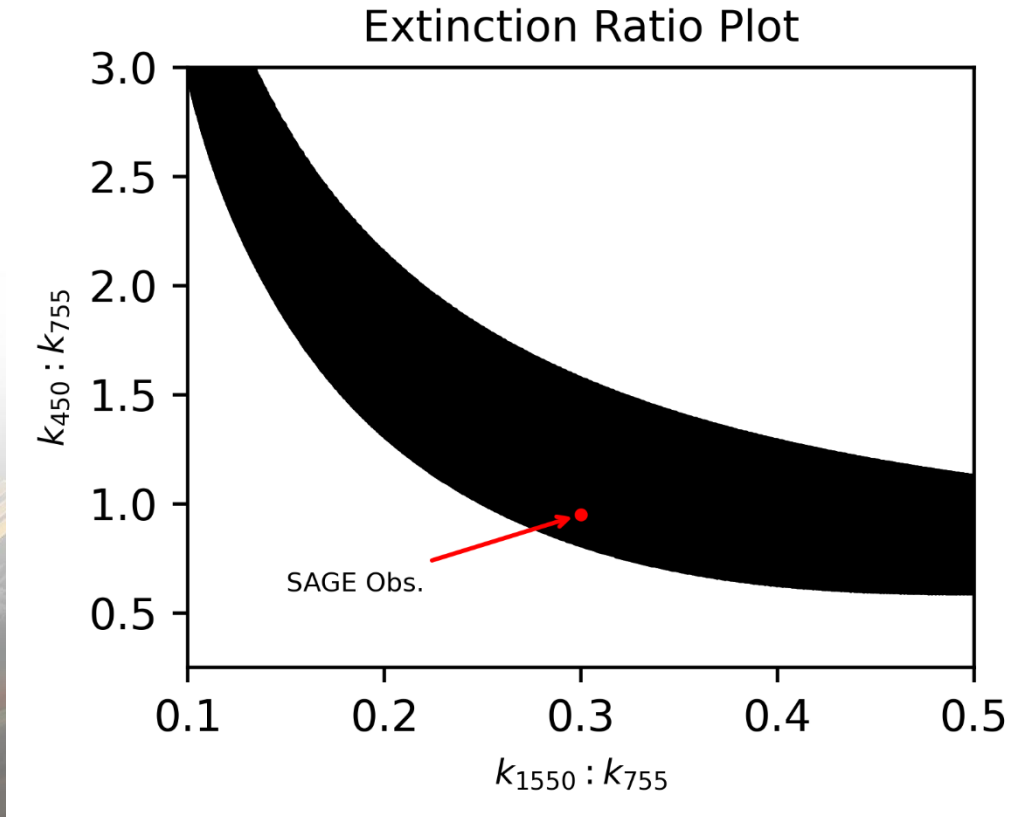


| Condition # | Numerator Wavelengths (nm)    | Denominator Wavelength (nm) |
|-------------|-------------------------------|-----------------------------|
| 0           | 520                           | 1021                        |
| 1           | 448, 520                      | 1021                        |
| 2           | 448, 520, 755                 | 1021                        |
| 3           | 448, 520, 755, 869            | 1021                        |
| 4           | 384, 448, 520, 755, 869       | 1021                        |
| 5           | 384, 448, 520, 755, 869, 1543 | 1021                        |
| 6           | 448, 520, 755, 869, 1543      | 1021                        |
| 7           | 520                           | 1543                        |
| 8           | 448, 520                      | 1543                        |
| 9           | 448, 520, 755                 | 1543                        |
| 10          | 448, 520, 755, 869            | 1543                        |
| 11          | 448, 520, 755, 869, 1021      | 1543                        |
| 12          | 520, 755, 869, 1021           | 1543                        |
| 13          | 384, 448, 520, 755, 869       | 1543                        |
| 14          | 384, 448, 520, 755, 869, 1021 | 1543                        |
| 15*         | 448, 1543                     | 755                         |

# Visualizing the Solution Space

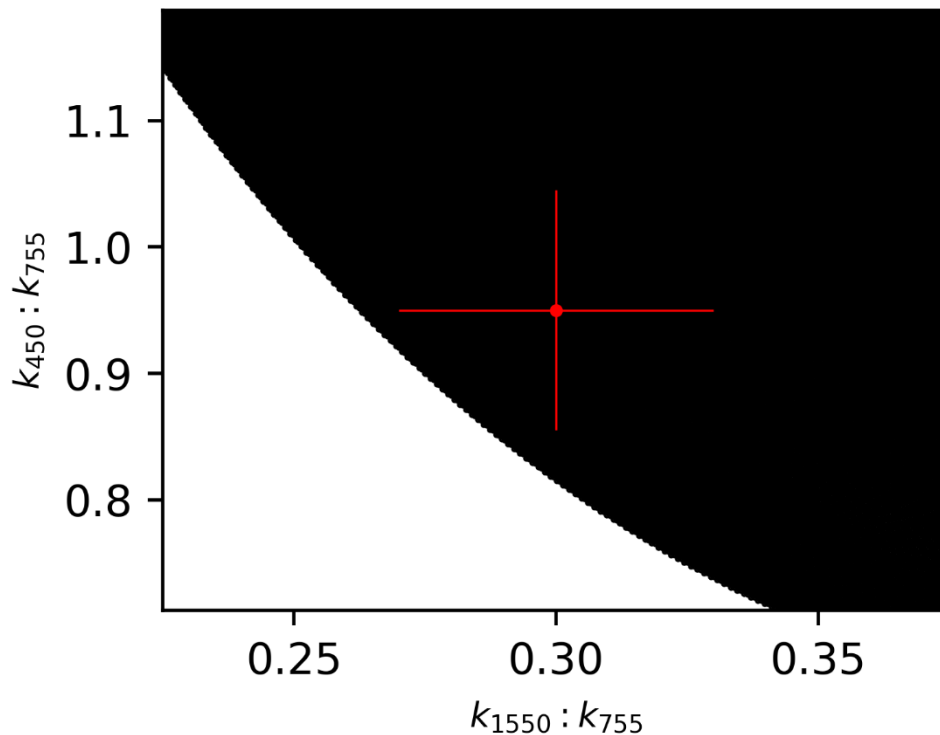


# Visualizing the Solution Space



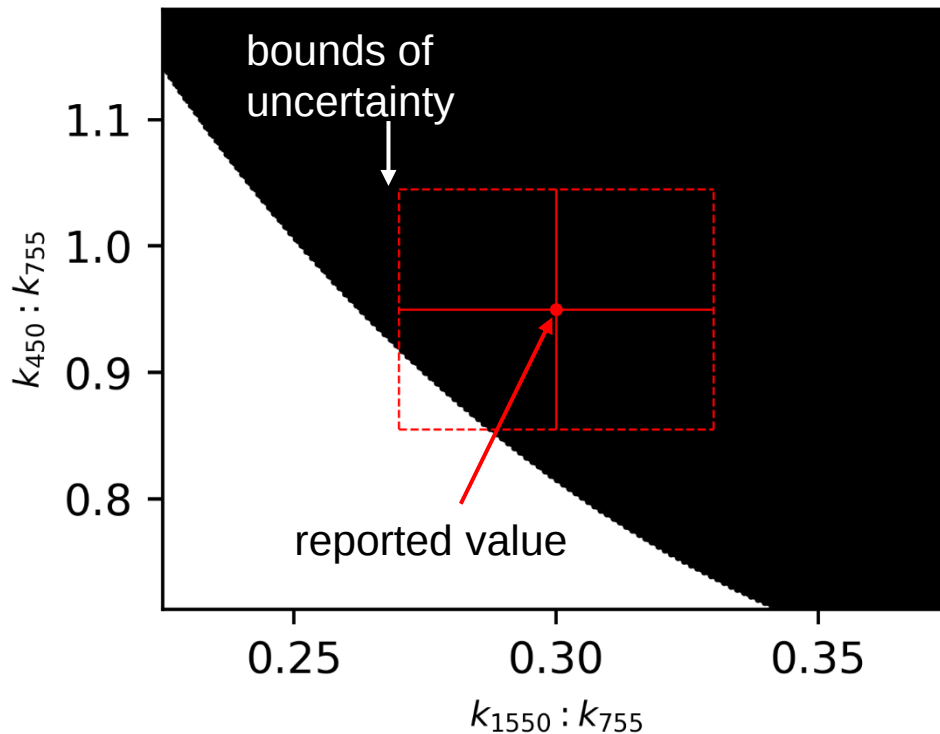
# Visualizing the Solution Space

Extinction Ratio Plot



# Visualizing the Solution Space

Extinction Ratio Plot

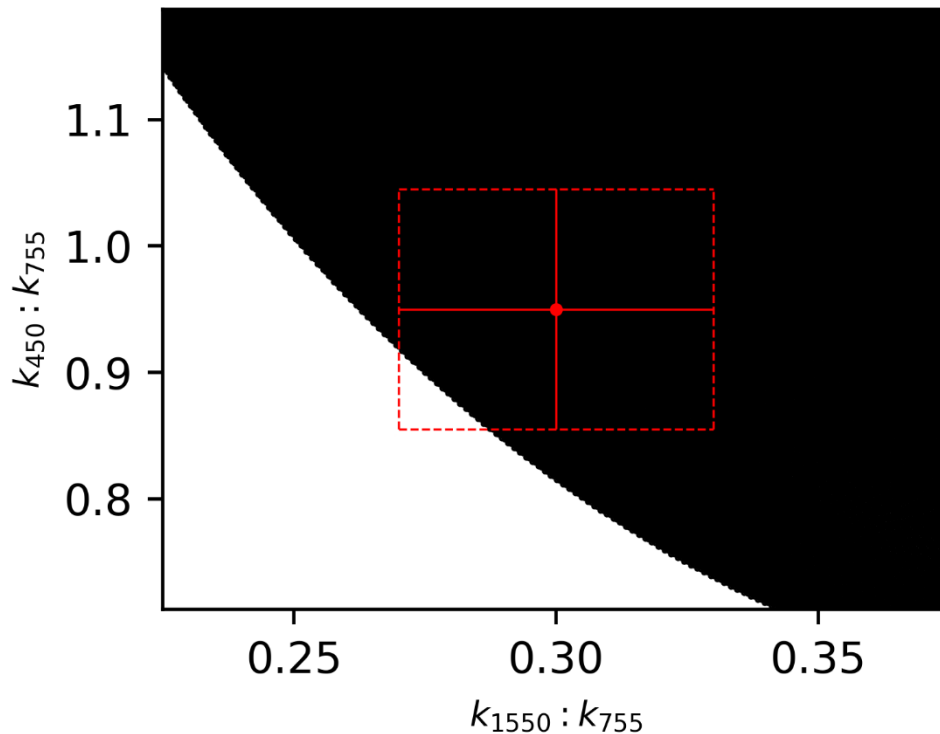


All potential solutions!

Which is right/best?

# Visualizing the Solution Space

Extinction Ratio Plot



Use distance from  
central point as weight

Calculate weighted  
statistics (e.g., median)



# 2022 Hunga Tonga Eruption

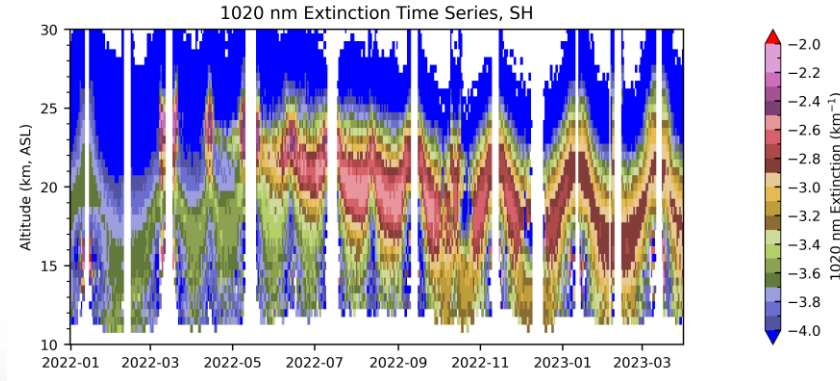


- Hunga Tonga Erupted in January 2022
  - $\text{SO}_2$  injection was modest ( $\sim 0.5$  Tg)
  - $\text{H}_2\text{O}$  injection was large (3,000 – 13,000 Tg)
    - $\sim 5$ -10% stratospheric  $\text{H}_2\text{O}$  content
  - Eruption was violent (injection up to 58 km)
    - VEI 6, comparable to Krakatoa?

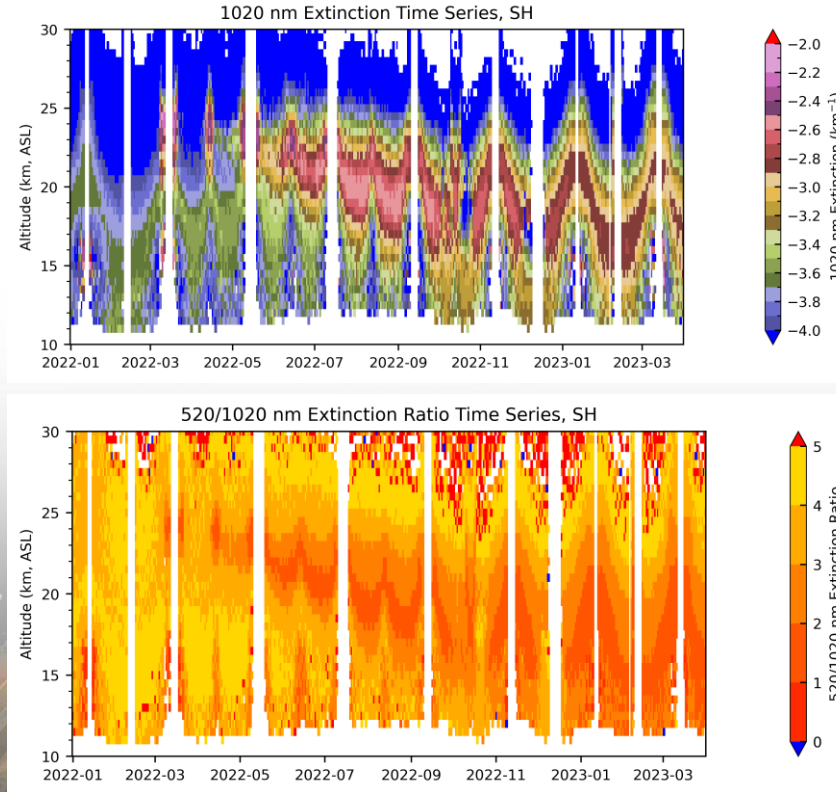




# SAGE III/ISS Observation of HTHH: Aerosol

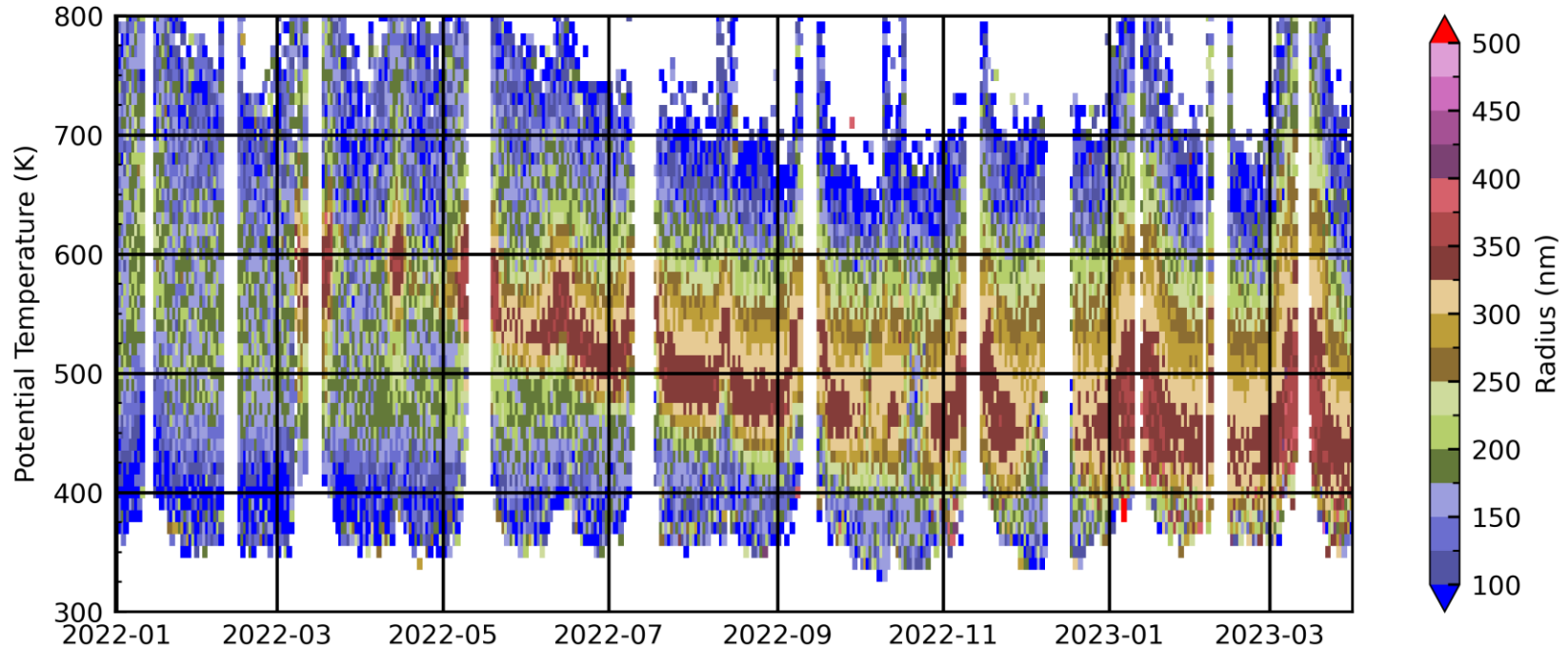


# SAGE III/ISS Observation of HTHH: Aerosol

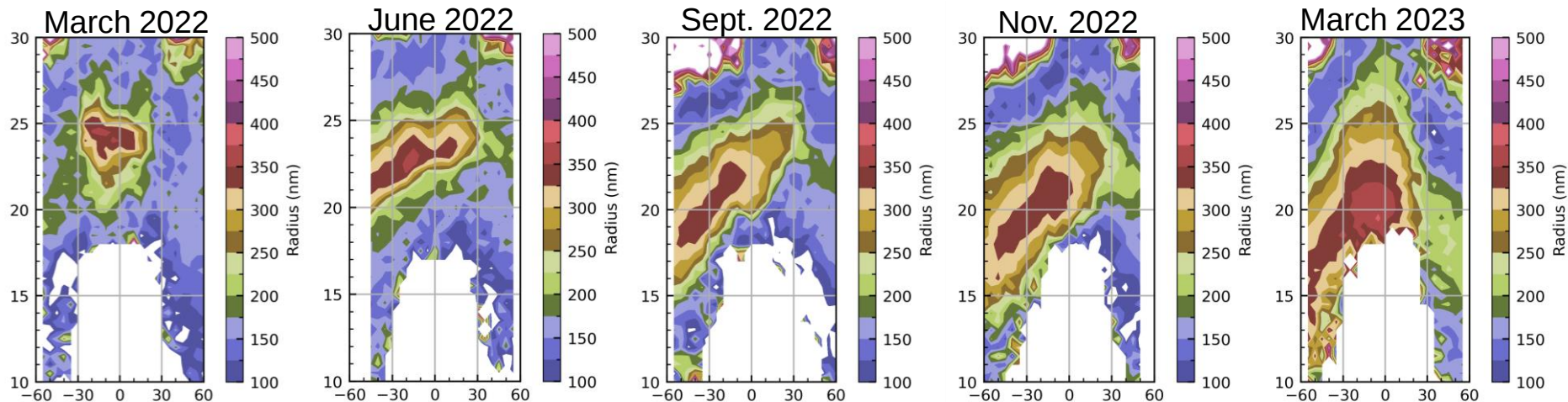




# PSD Algorithm Applied to SAGE III/ISS



# Particle Transport and Descent



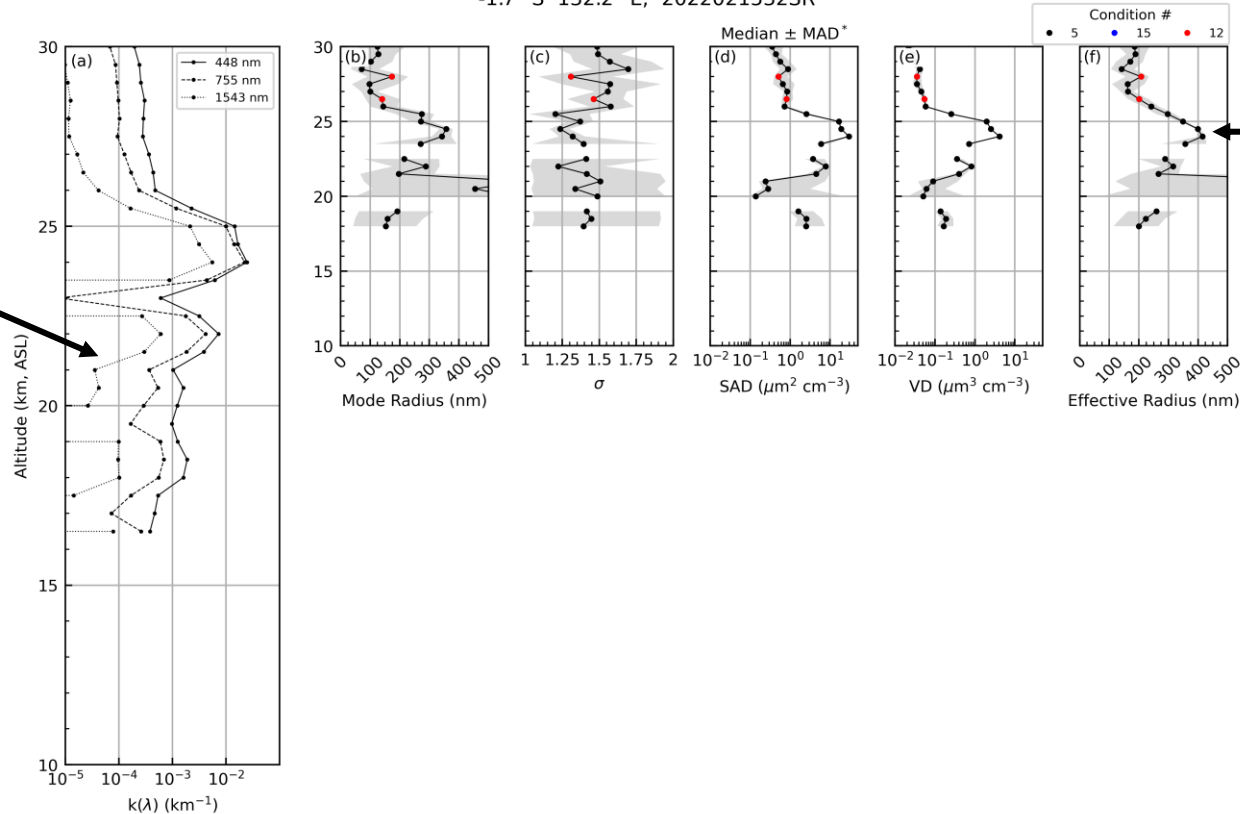
All particles moved south

Separation of largest/smallest at high altitude

# HTHH Individual Profile

21:23 Feb-15 2022  
-1.7° S 132.2° E, 2022021532SR

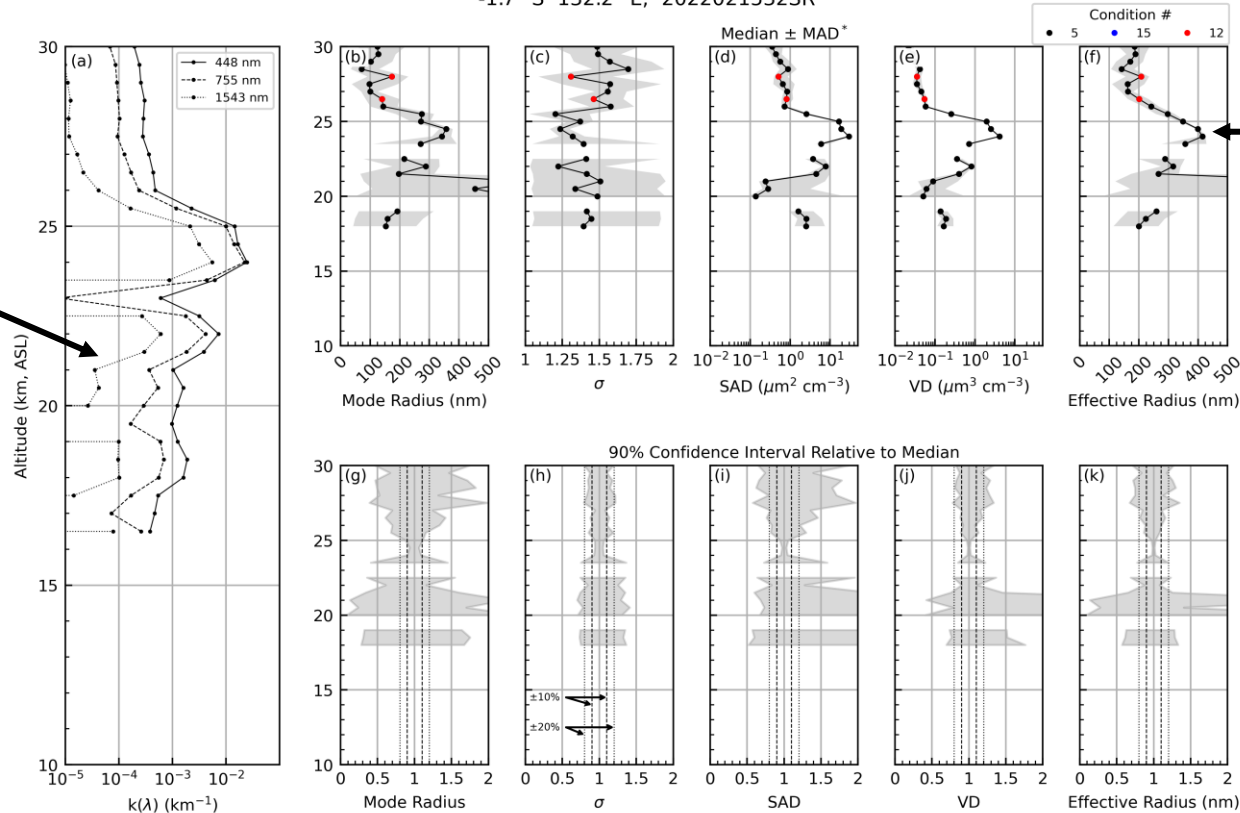
Measurement error  
large



# HTHH Individual Profile

21:23 Feb-15 2022  
-1.7° S 132.2° E, 2022021532SR

Measurement error large

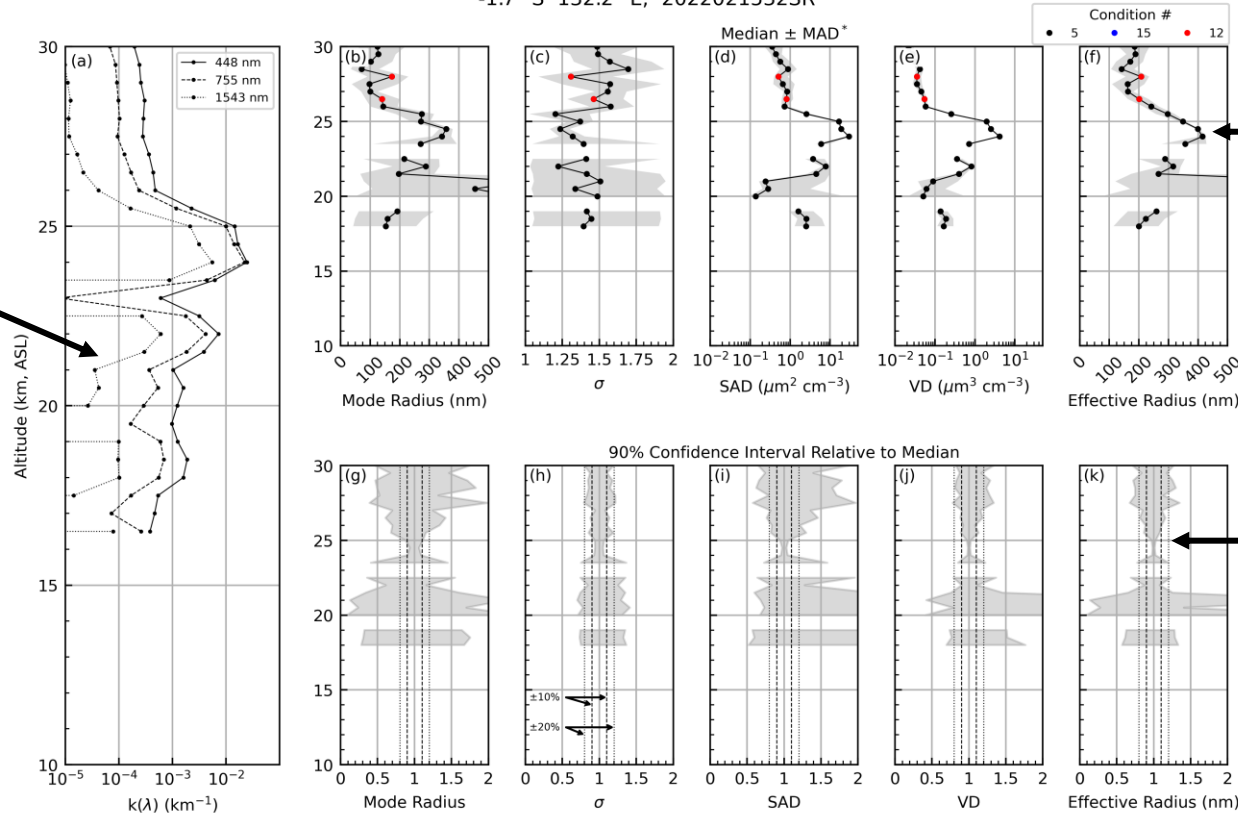


Comparable to  
POPS (460 nm)

# HTHH Individual Profile

21:23 Feb-15 2022  
-1.7° S 132.2° E, 2022021532SR

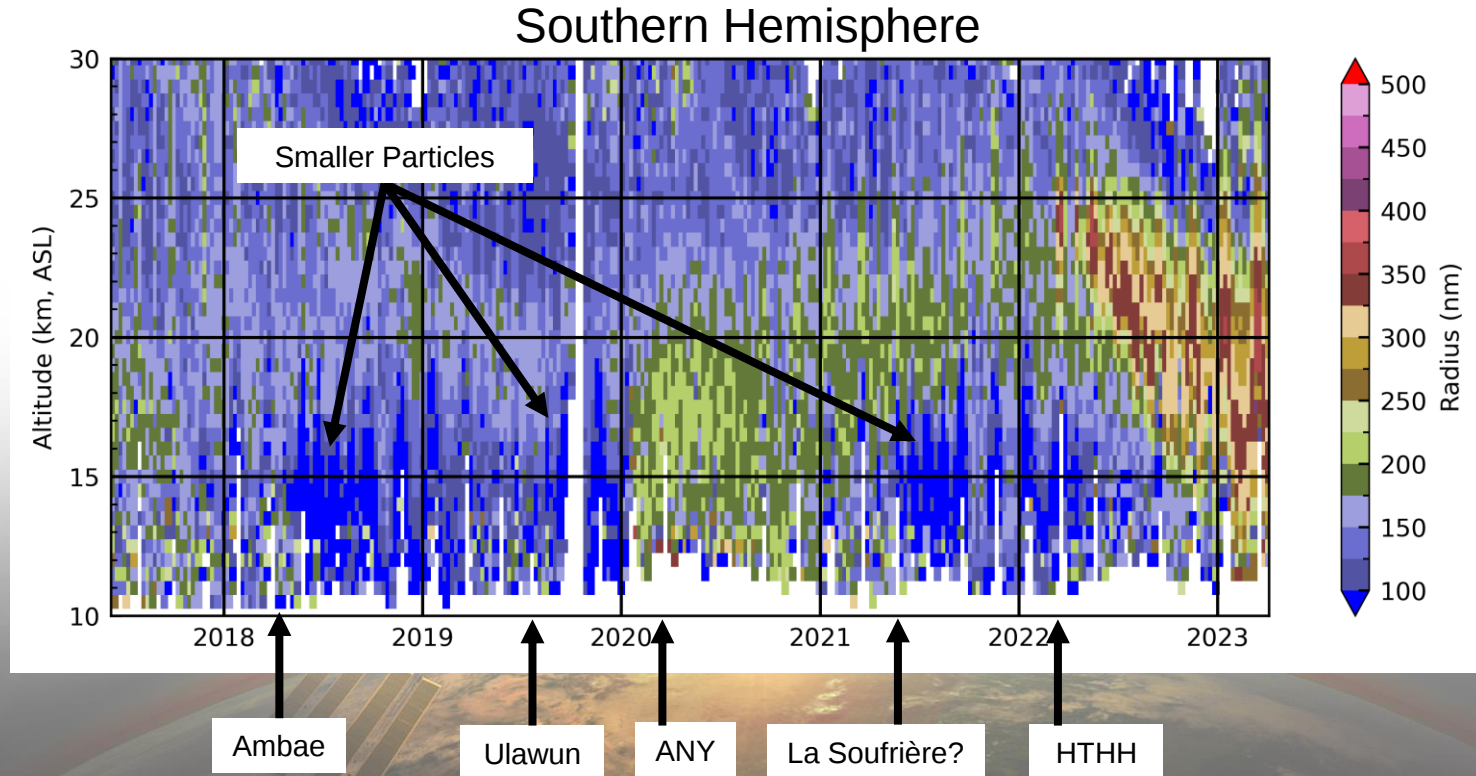
Measurement error large



Comparable to POPS (460 nm)

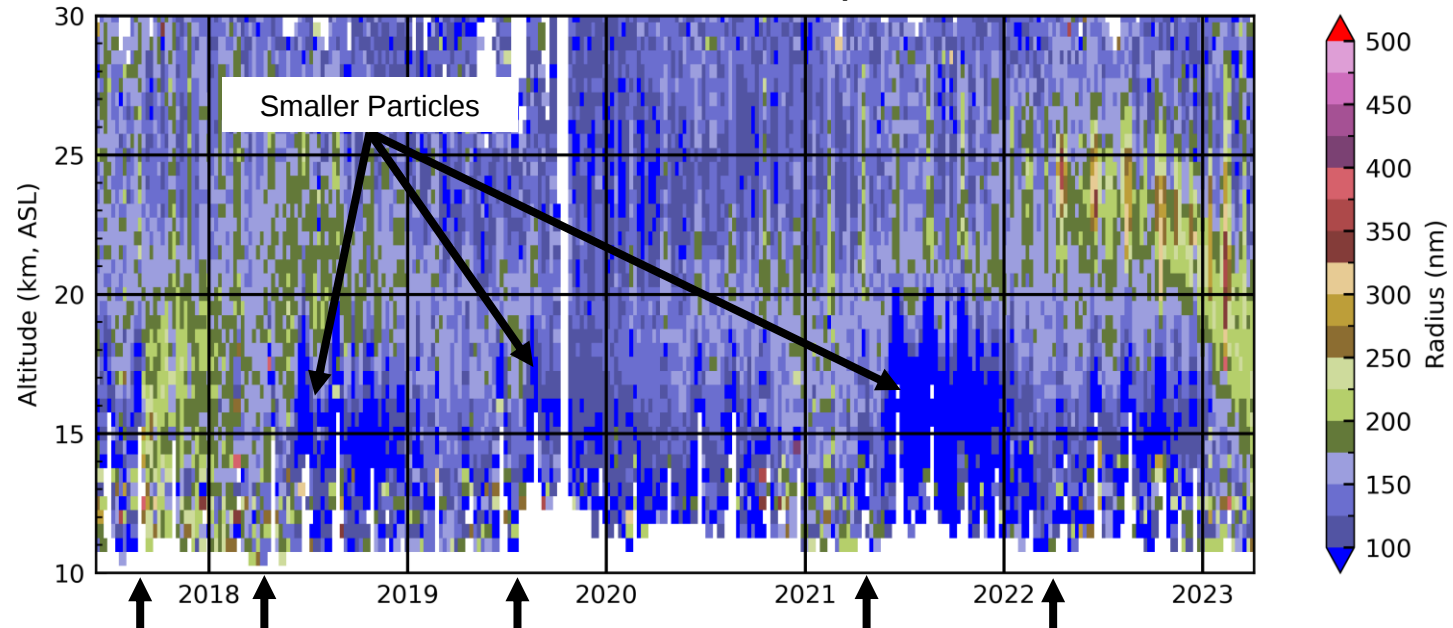
90% confident that PSD estimates are within 10% of median

# Other Events



# Other Events

## Northern Hemisphere



Canadian  
PyroCb

Ambae

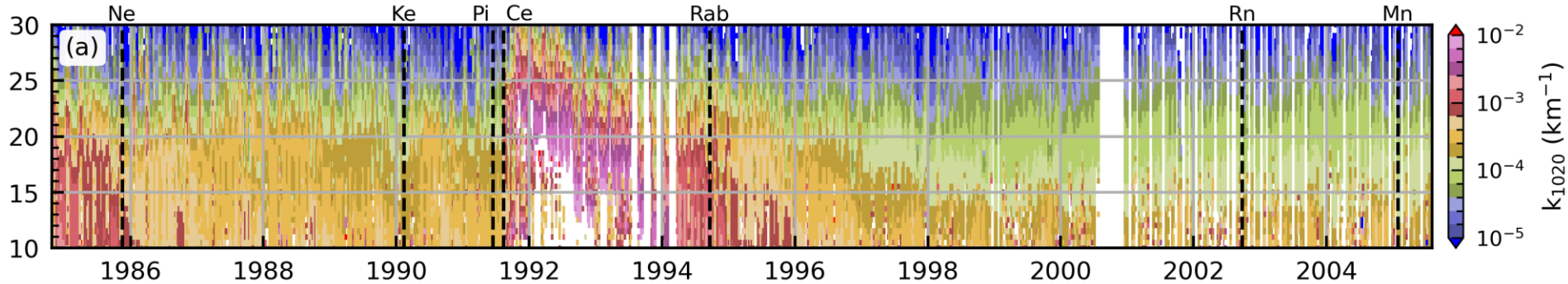
Ulawun &  
Raikoke

La Soufrière

HTHH

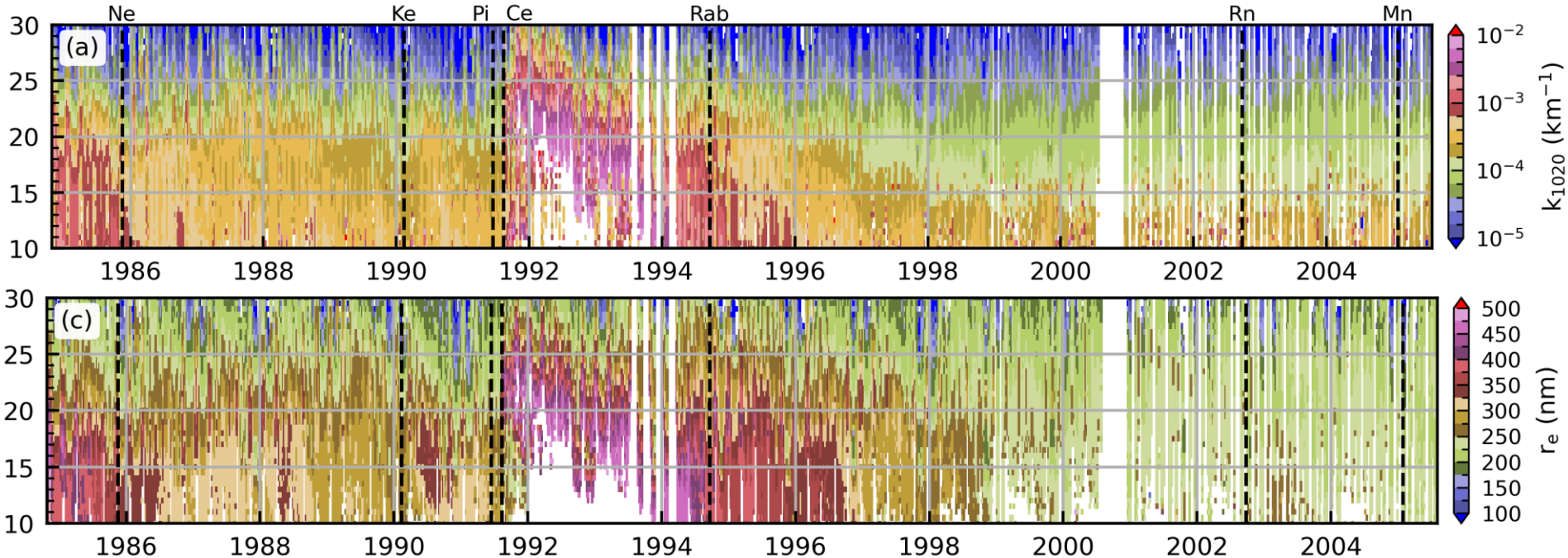
# Application to SAGE II

Southern Hemisphere

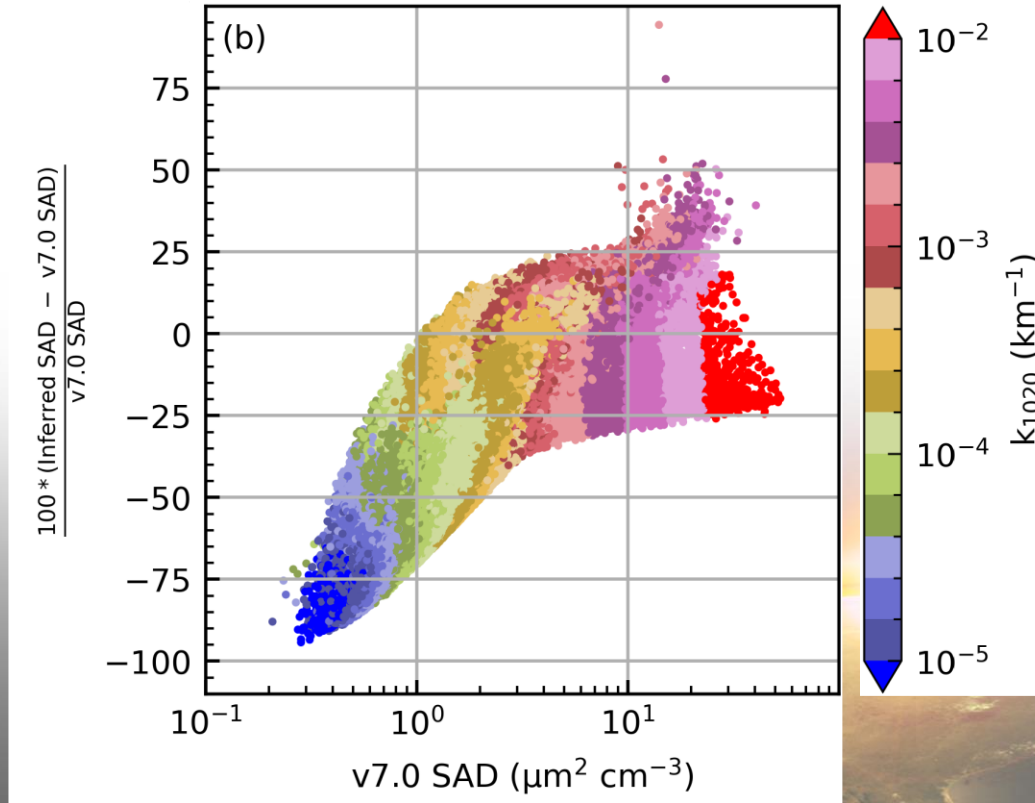


# Application to SAGE II

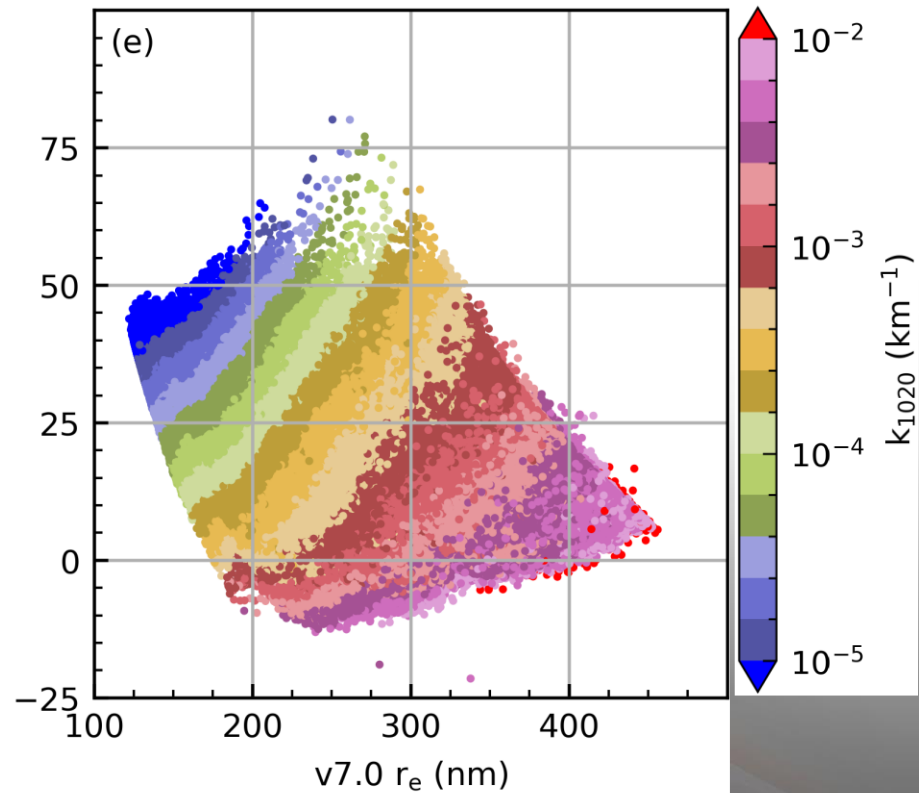
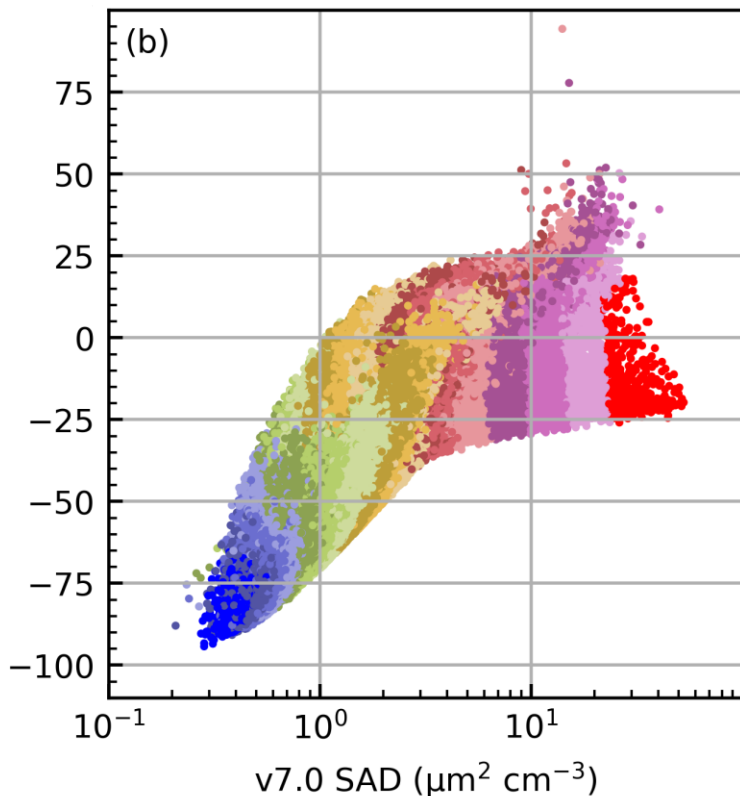
Southern Hemisphere



# Comparison with SAGE II v7.0 Products



# Comparison with SAGE II v7.0 Products





# Conclusions from SAGE II comparison

---



Our products are consistent with the SAGE II products



# Recap



- Method to infer PSD parameters from SAGE III/ISS extinction data was developed
  - Method allows computation of confidence intervals
- Hunga Tonga increased particle size  $>400$  nm
  - Good agreement with POPS observations
- Observed smaller particle formation from smaller eruptions
- SAD and  $r_e$  products were in good agreement with the SAGE II products



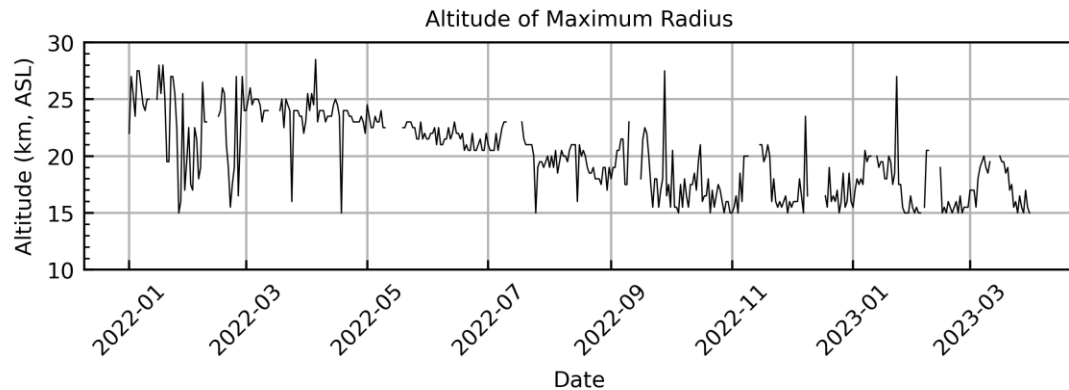
# Questions

---



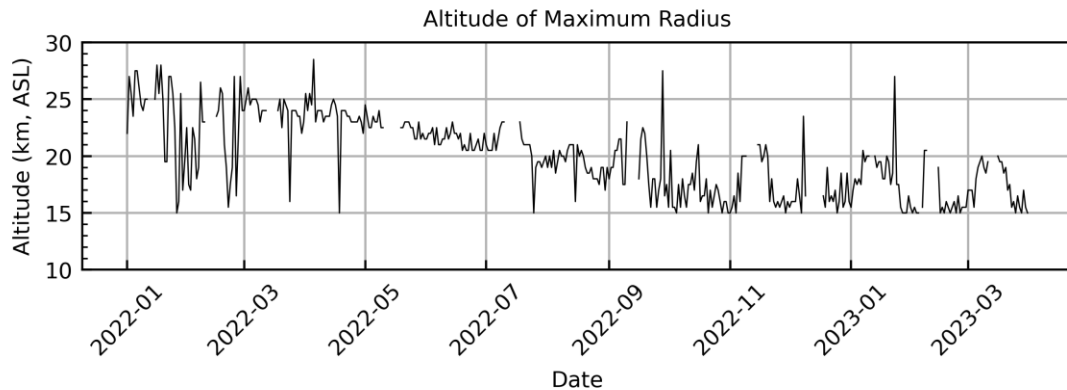


# Sedimentation Rate Estimates



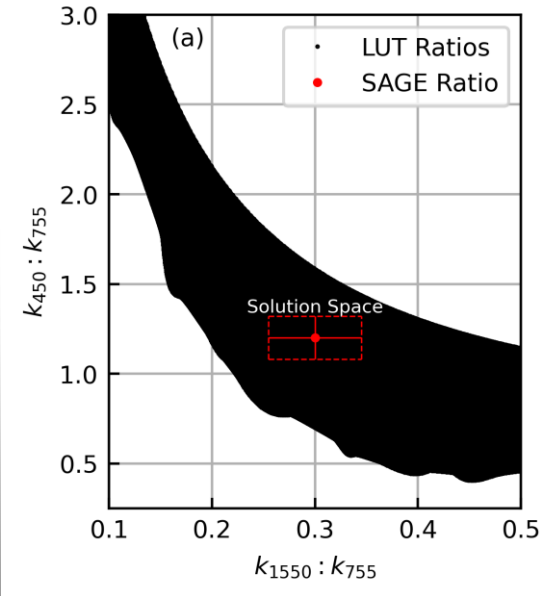


# Sedimentation Rate Estimates

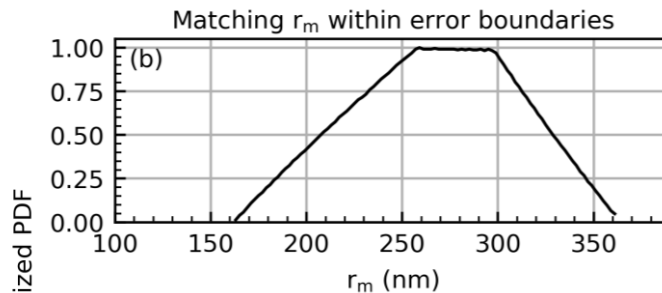
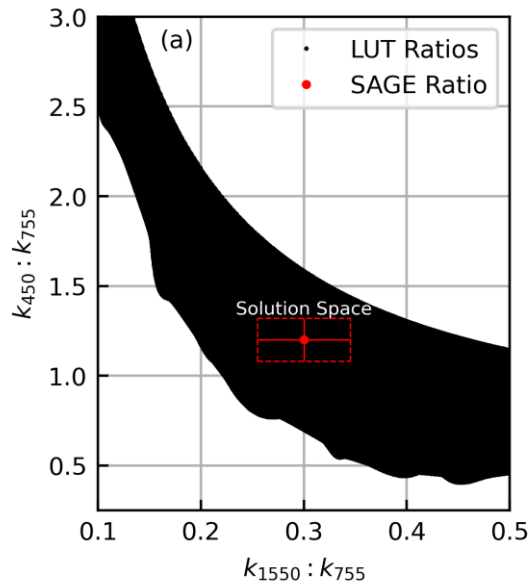


| Latitude (S) | Descent Rate (mm/s) |
|--------------|---------------------|
| 0 - 10       | 0.1                 |
| 10 - 20      | 0.13                |
| 20 - 30      | 0.13                |
| 30 - 40      | 0.23                |
| 40 - 50      | 0.25                |
| 50 - 60      | 0.21                |
| 60 - 70      | 0.32                |

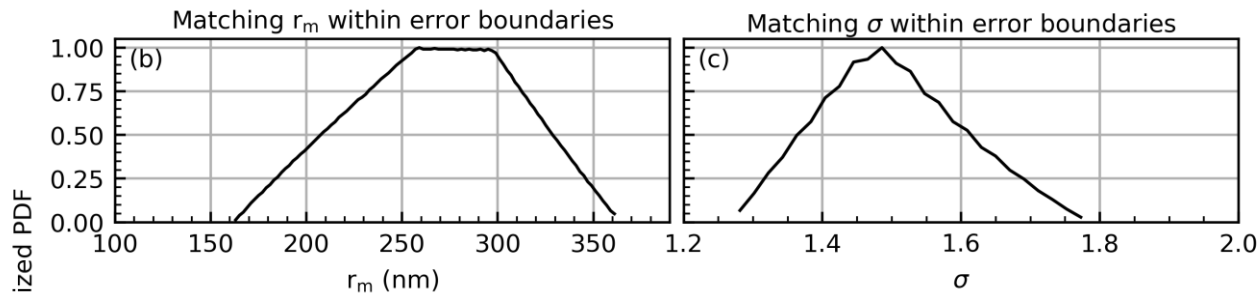
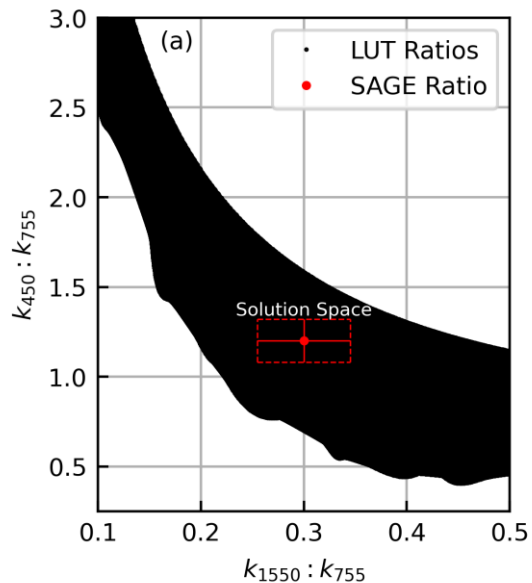
# Estimating Solution Space Variability



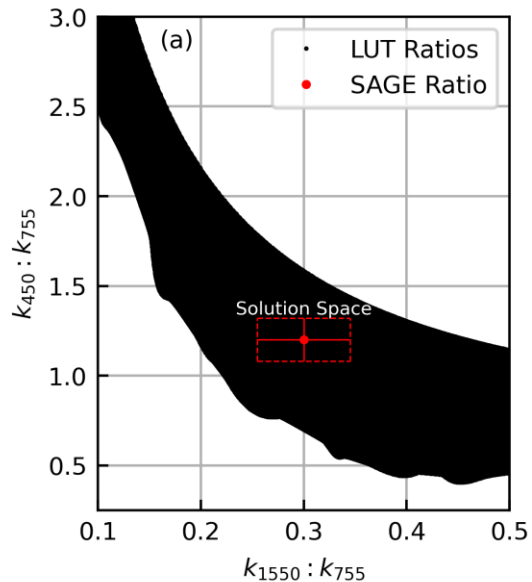
# Estimating Solution Space Variability



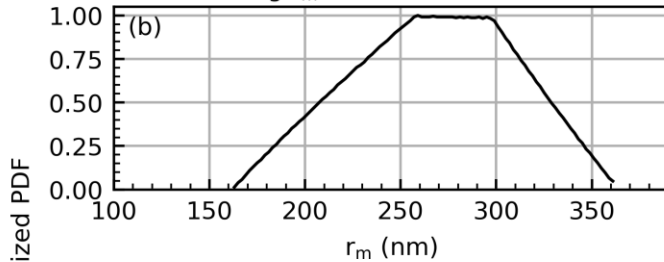
# Estimating Solution Space Variability



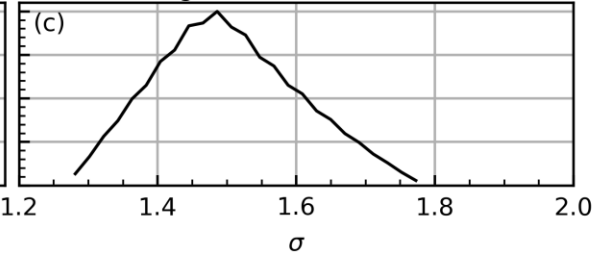
# Estimating Solution Space Variability



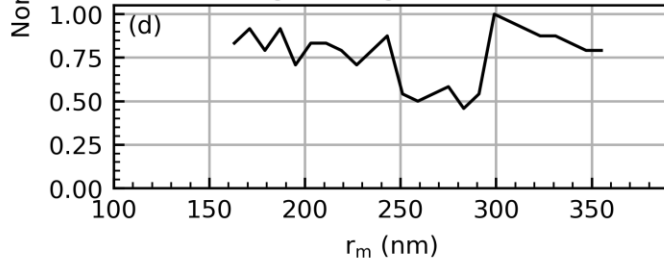
Matching  $r_m$  within error boundaries



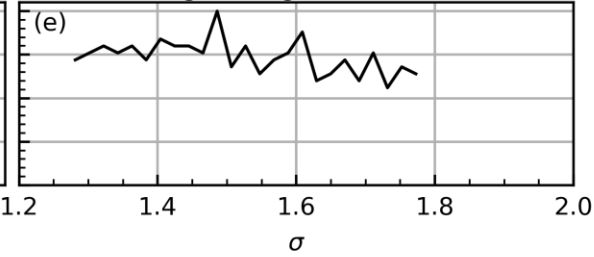
Matching  $\sigma$  within error boundaries



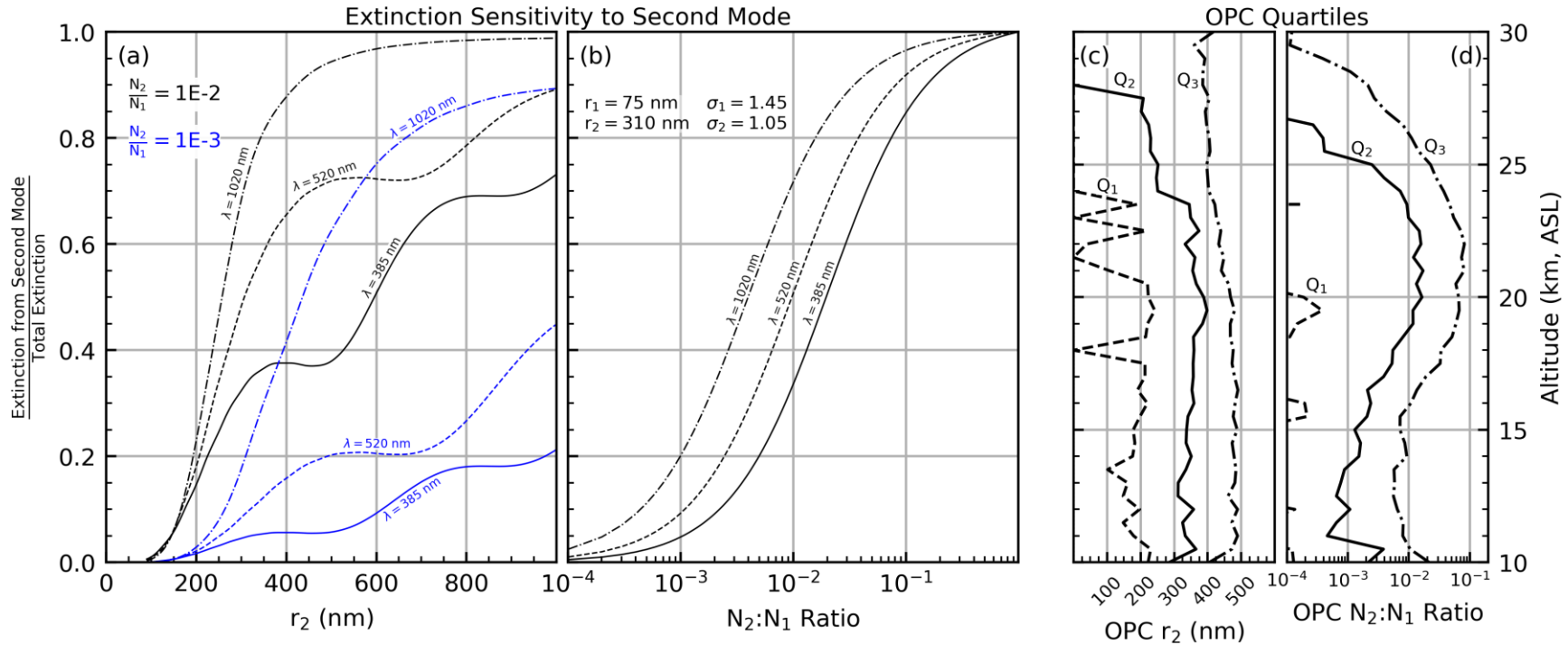
Matching  $r_m$  along error boundaries



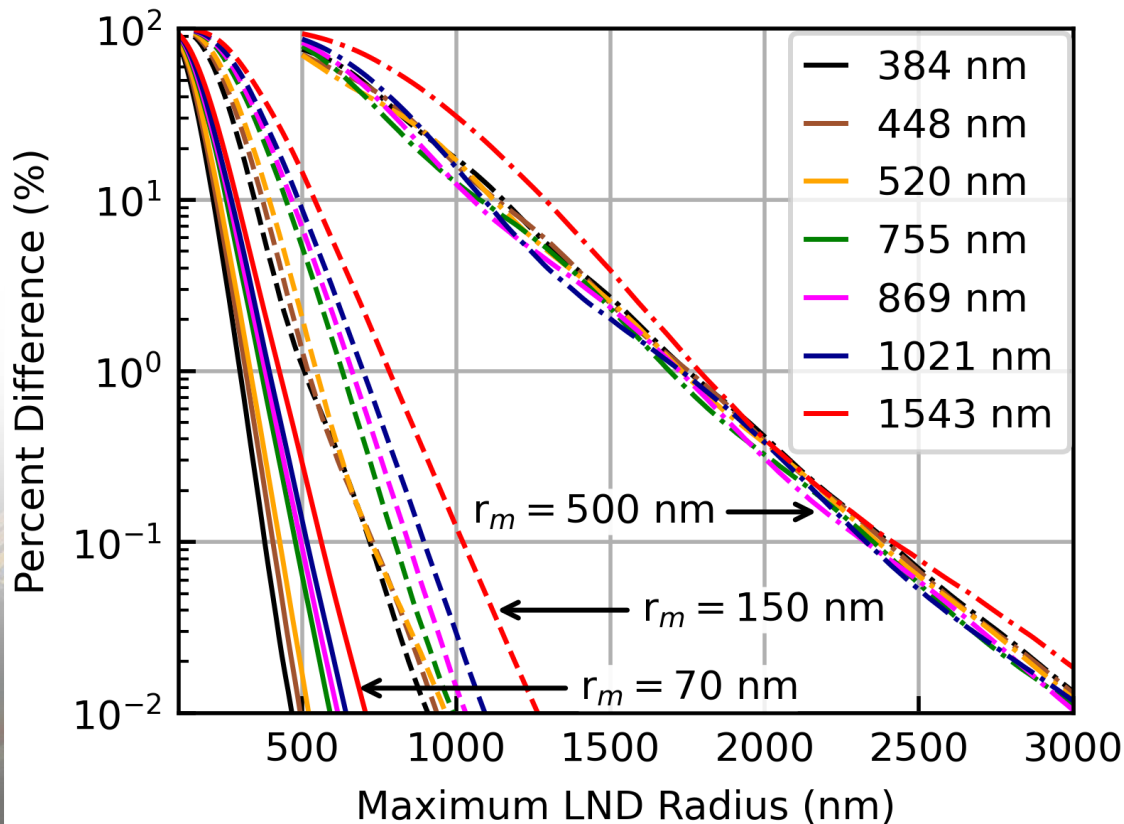
Matching  $\sigma$  along error boundaries



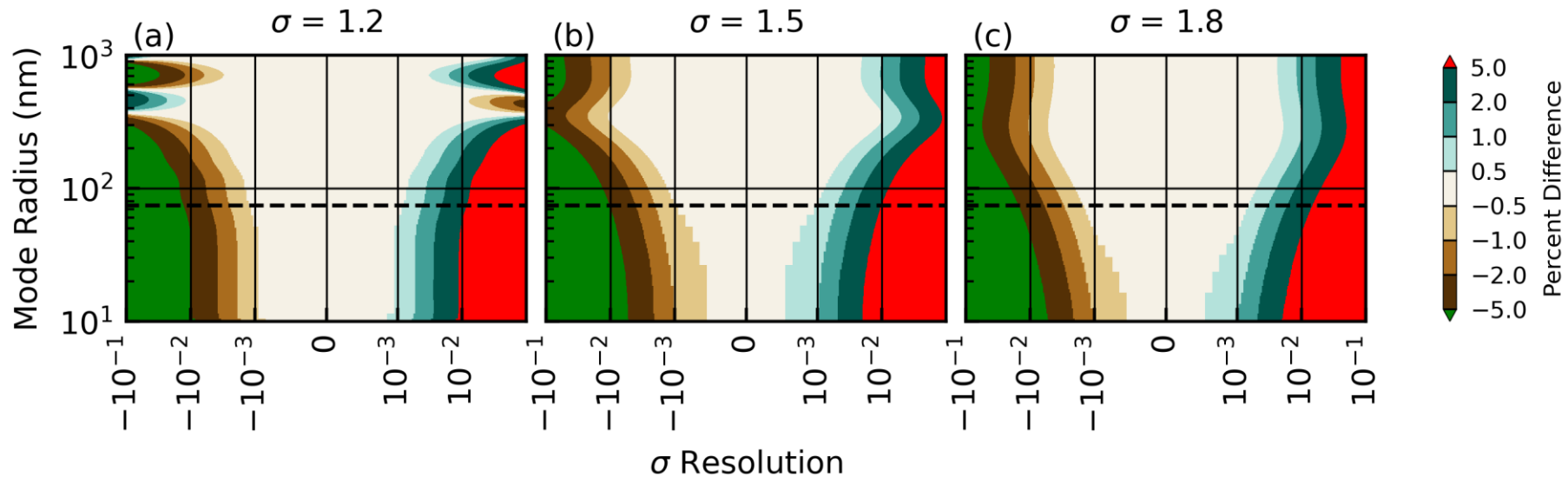
# Influence of Second Mode on Extinction



# Justification of LUT PSD Radius Range

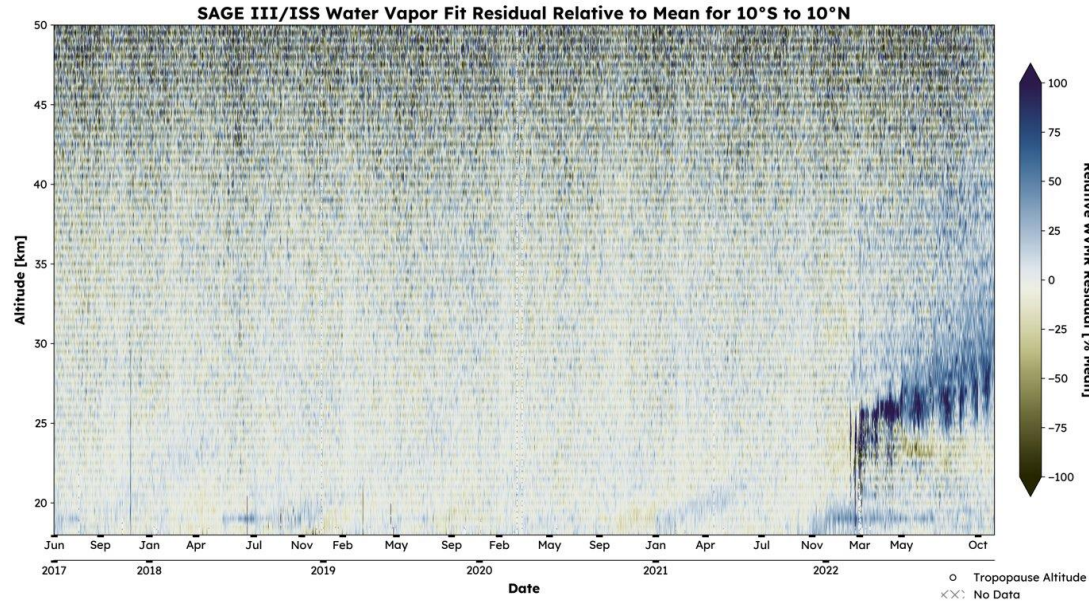


# Justification of LUT PSD sigma Resolution



# HTHH Eruption

- Hunga Tonga Erupted in January 2022
  - $\text{SO}_2$  injection was modest ( $\sim 0.5$  Tg)
- $\text{H}_2\text{O}$  injection was large (3,000 – 13,000 Tg)
- Eruption was violent (injection up to 58 km)

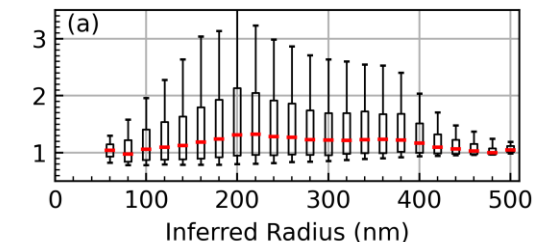


# Sensitivity Study Continued

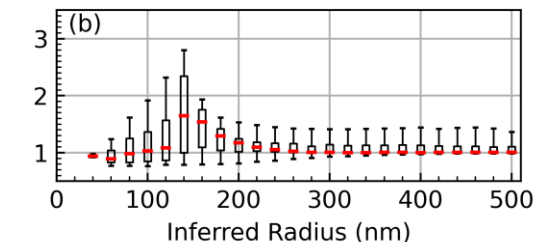
## Influence of Error

Inferred / Target

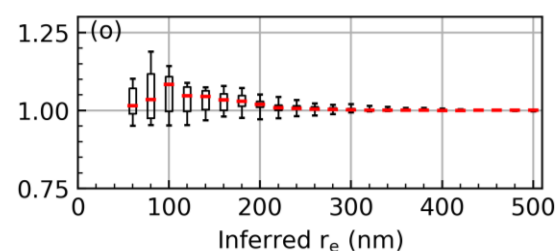
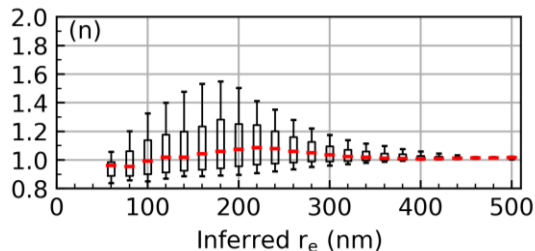
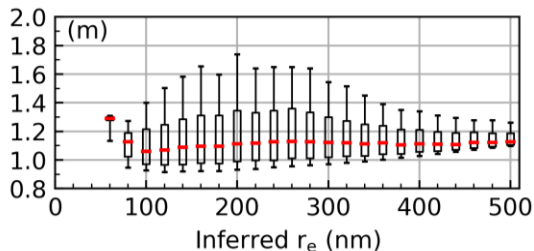
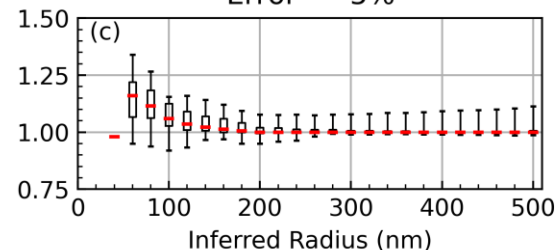
Error = 50%



Error = 20%



Error = 5%





# Sensitivity Study Continued Influence of Error

---

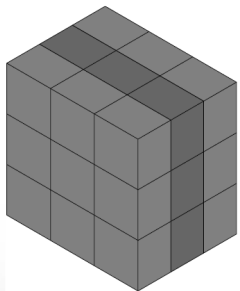


PSD estimates are LARGER than target values  
- higher moments have better agreement

# Sensitivity Study: **Incorrect** Composition

Imaginary atmosphere

**NOT** 75%  $\text{H}_2\text{SO}_4$

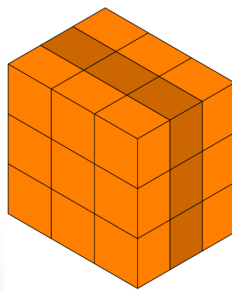


$k(r, \lambda, \sigma) + \text{err}$



Find matches in 75%

$\text{H}_2\text{SO}_4$  LUT



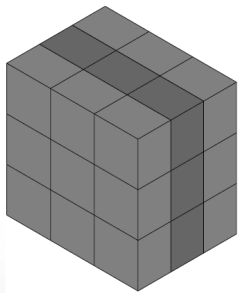
Stats ( $S_1$ )



# Sensitivity Study: **Incorrect** Composition

Imaginary atmosphere

**NOT** 75%  $\text{H}_2\text{SO}_4$

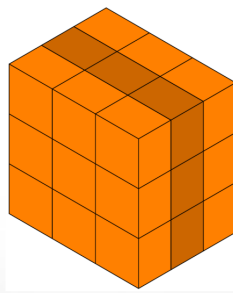


$k(r, \lambda, \sigma) + \text{err}$



Find matches in 75%

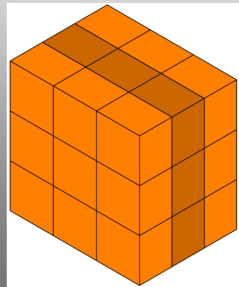
$\text{H}_2\text{SO}_4$  LUT



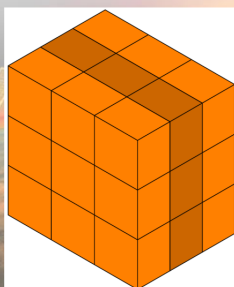
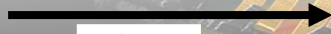
Stats ( $S_1$ )

Imaginary atmosphere

75%  $\text{H}_2\text{SO}_4$



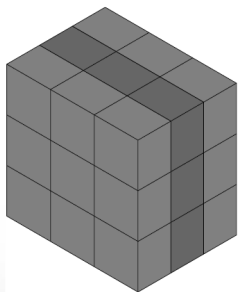
$k(r, \lambda, \sigma) + \text{err}$



Stats ( $S_2$ )

# Sensitivity Study: **Incorrect** Composition

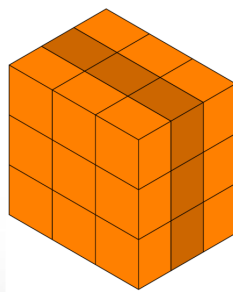
Imaginary atmosphere  
**NOT** 75%  $\text{H}_2\text{SO}_4$



$k(r, \lambda, \sigma) + \text{err}$



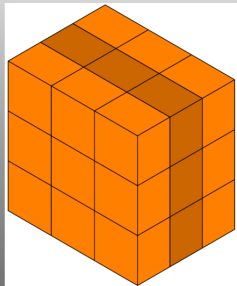
Find matches in 75%  
 $\text{H}_2\text{SO}_4$  LUT



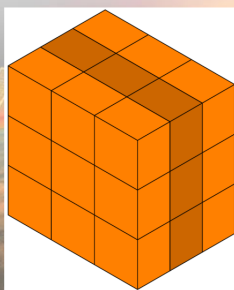
Stats ( $S_1$ )

$$\frac{S_1}{S_2}$$

Imaginary atmosphere  
75%  $\text{H}_2\text{SO}_4$



$k(r, \lambda, \sigma) + \text{err}$

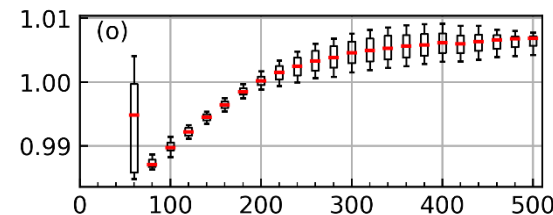
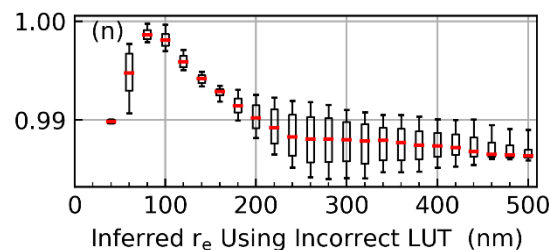
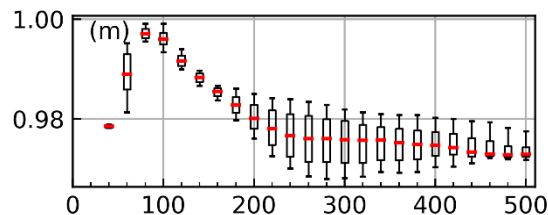
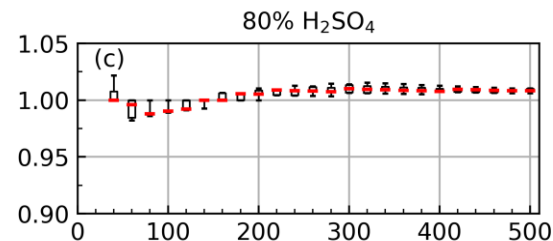
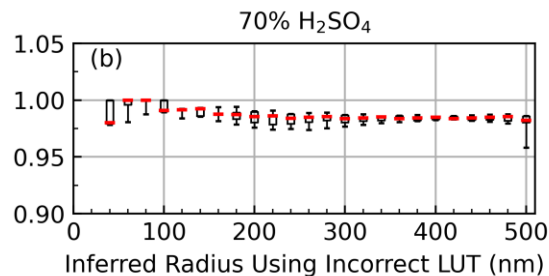
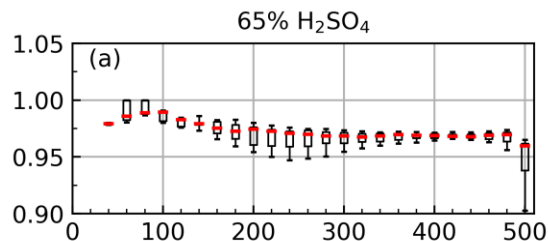


Stats ( $S_2$ )

# Sensitivity Study Continued

## Wrong $\text{H}_2\text{SO}_4$ Composition

Inferred PSD Value Using Incorrect LUT  
Inferred PSD Value Using Correct LUT





# Sensitivity Study Continued

## Wrong $\text{H}_2\text{SO}_4$ Composition

---



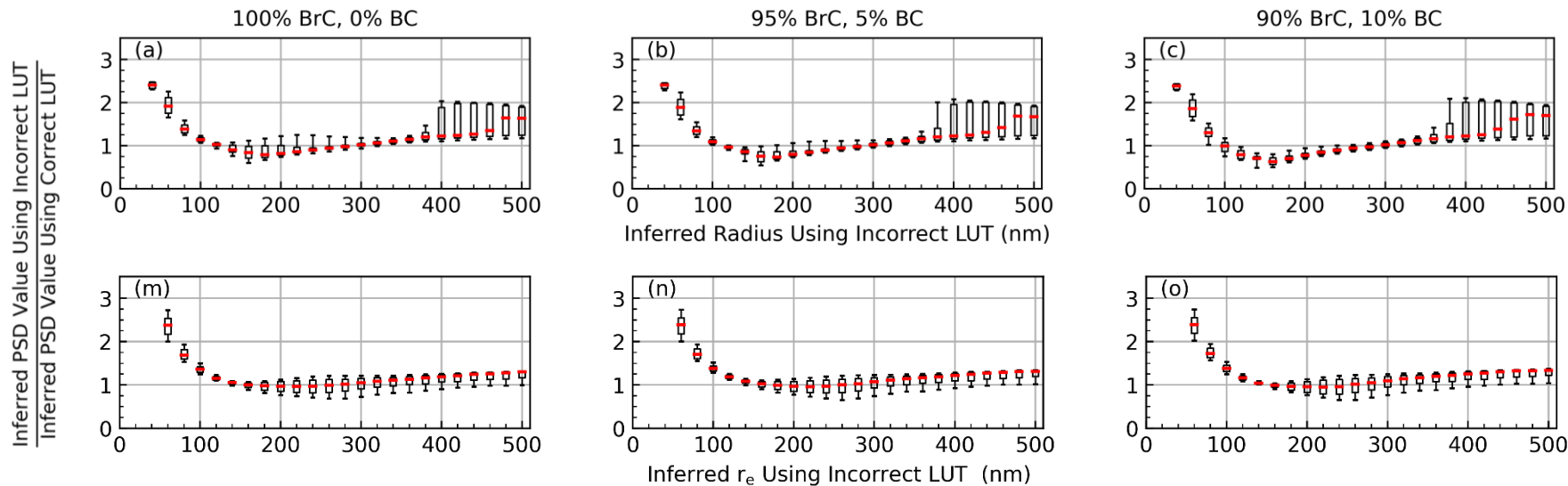
Almost no difference compared to getting composition correct

- PSD estimates are SMALLER than target values
- higher moments have better agreement



# Sensitivity Study Continued

## Wrong Composition: **With smoke**





# Sensitivity Study (Abridged Edition)

---



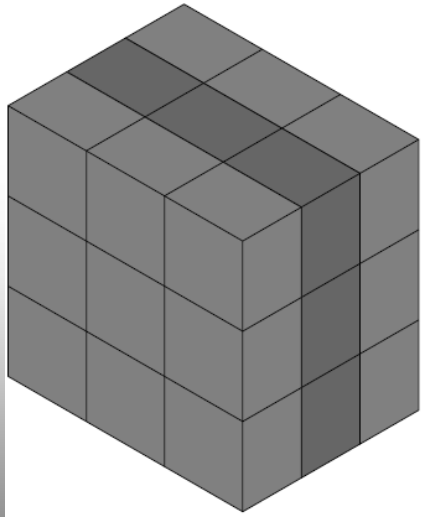
- How accurately can we reproduce “known” values?
  - How does this change as a function of measurement uncertainty?
- Evaluate under 2 scenarios:
  - We get the composition correct
  - We get the composition wrong



# Sensitivity Study (Abridged Edition)



Imaginary atmosphere  
Variable Composition



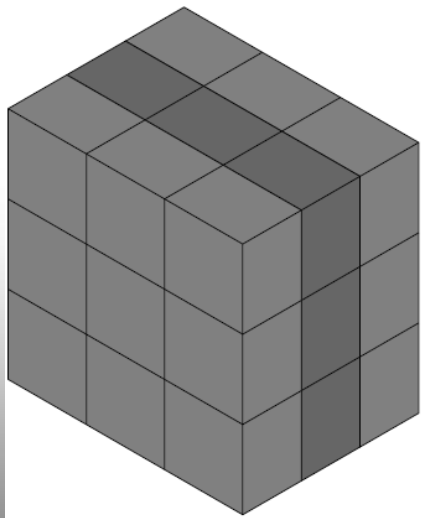


# Sensitivity Study (Abridged Edition)



Imaginary atmosphere  
Variable Composition

Pull out single  
extinction ratio of  
known  $r$ ,  $\lambda$ ,  $\sigma$

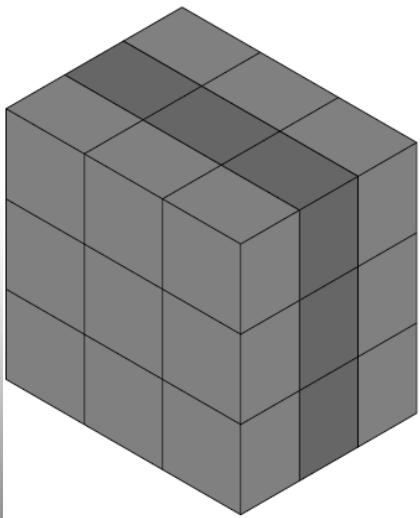


$k(r, \lambda, \sigma) + \text{err}$



# Sensitivity Study (Abridged Edition)

Imaginary atmosphere  
Variable Composition

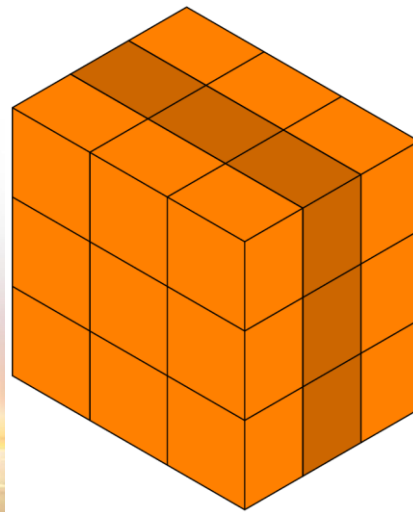


Pull out single  
extinction ratio of  
known  $r$ ,  $\lambda$ ,  $\sigma$

$k(r, \lambda, \sigma) + \text{err}$

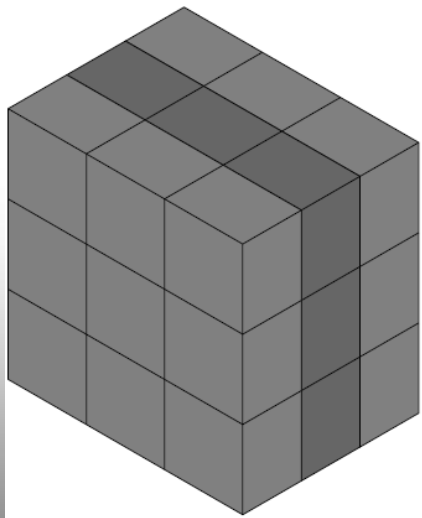


Find matches in  
75%  $\text{H}_2\text{SO}_4$  LUT



# Sensitivity Study (Abridged Edition)

Imaginary atmosphere  
Variable Composition

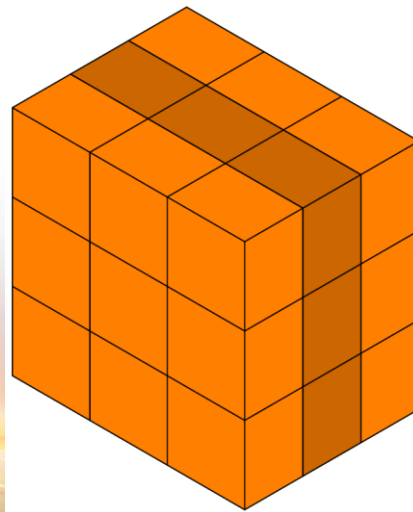


Pull out single  
extinction ratio of  
known  $r$ ,  $\lambda$ ,  $\sigma$

$k(r, \lambda, \sigma) + \text{err}$



Find matches in  
75%  $\text{H}_2\text{SO}_4$  LUT



Calculate statistics  
for inferred values

mean  
median  
Q1, Q3,  
.  
.  
.



# Sensitivity Study: Summary

---



- Correct composition:
  - overestimated PSD parameters by ~20%





# Sensitivity Study: Summary

---



- Correct composition:
  - overestimated PSD parameters by ~20%
- Wrong  $\text{H}_2\text{SO}_4$  content:
  - minimal impact (~5% worse than getting composition correct)



# Sensitivity Study: Summary

---



- Correct composition:
  - overestimated PSD parameters by ~20%
- Wrong  $\text{H}_2\text{SO}_4$  content:
  - minimal impact (~5% worse than getting composition correct)
- Incorrect composition (smoke):
  - When smoke particles are small: ~300% worse than correct composition





# Sensitivity Study: Summary



- Correct composition:
  - overestimated PSD parameters by ~20%
- Wrong  $\text{H}_2\text{SO}_4$  content:
  - minimal impact (~5% worse than getting composition correct)
- Incorrect composition (smoke):
  - When smoke particles are small: ~300% worse than correct composition
  - When smoke particles are reasonable: ~25% worse than correct composition



# Sensitivity Study: Summary



- Correct composition:
  - overestimated PSD parameters by ~20%
- Wrong  $\text{H}_2\text{SO}_4$  content:
  - minimal impact (~5% worse than getting composition correct)
- Incorrect composition (smoke):
  - When smoke particles are small: ~300% worse than correct composition
  - When smoke particles are reasonable: ~25% worse than correct composition

Higher moment parameters are less impacted in each scenario