



Towards Integrated Computational Materials Engineering for Quantifying Performance Impacts of Microstructure and Defect Interactions in Powder Bed Fusion Parts

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Scenario: A New Alloy was Developed

- Our group has developed a new alloy...
- What build parameters should we use?
- Should we be concerned about defects?
- How will the new material perform?
- How long will this take to qualify?

How should these questions be addressed?

Scanning velocity?

Hatch spacing?

Laser power?

Beam diameter?

Scan strategy?

Contouring parameters?

Location in chamber?

Rotation angle?

Orientation of part?

Plate temperature?

Layer thickness?

And more...



Scenario: A New Alloy was Developed

- Use heuristics?

- Select parameters based on alloys with similar properties?
- Reasonable, but need prior knowledge.
- Also, which properties are the most important?
- Thermophysical, absorptivity, powder, phases...

- Conduct an experimental survey?

- +11 parameters, 2 levels each...
 - 2048 samples. Can down-select parameters, but still may need multiple rounds of printing

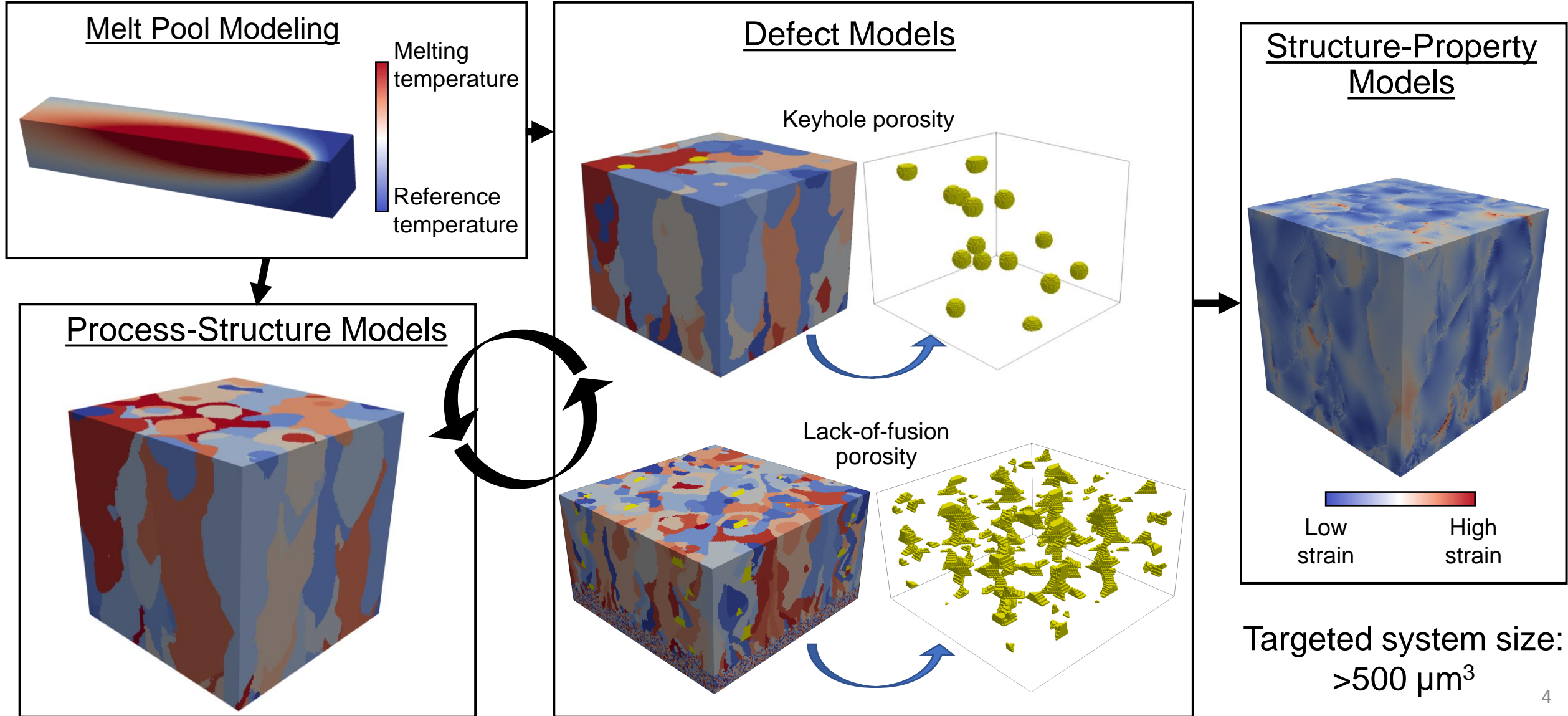
For both, still need to...

- Cross-section, polish, etch, and examine the samples
- Execute x-ray computed tomography scans
- Perform tensile tests, fatigue tests....

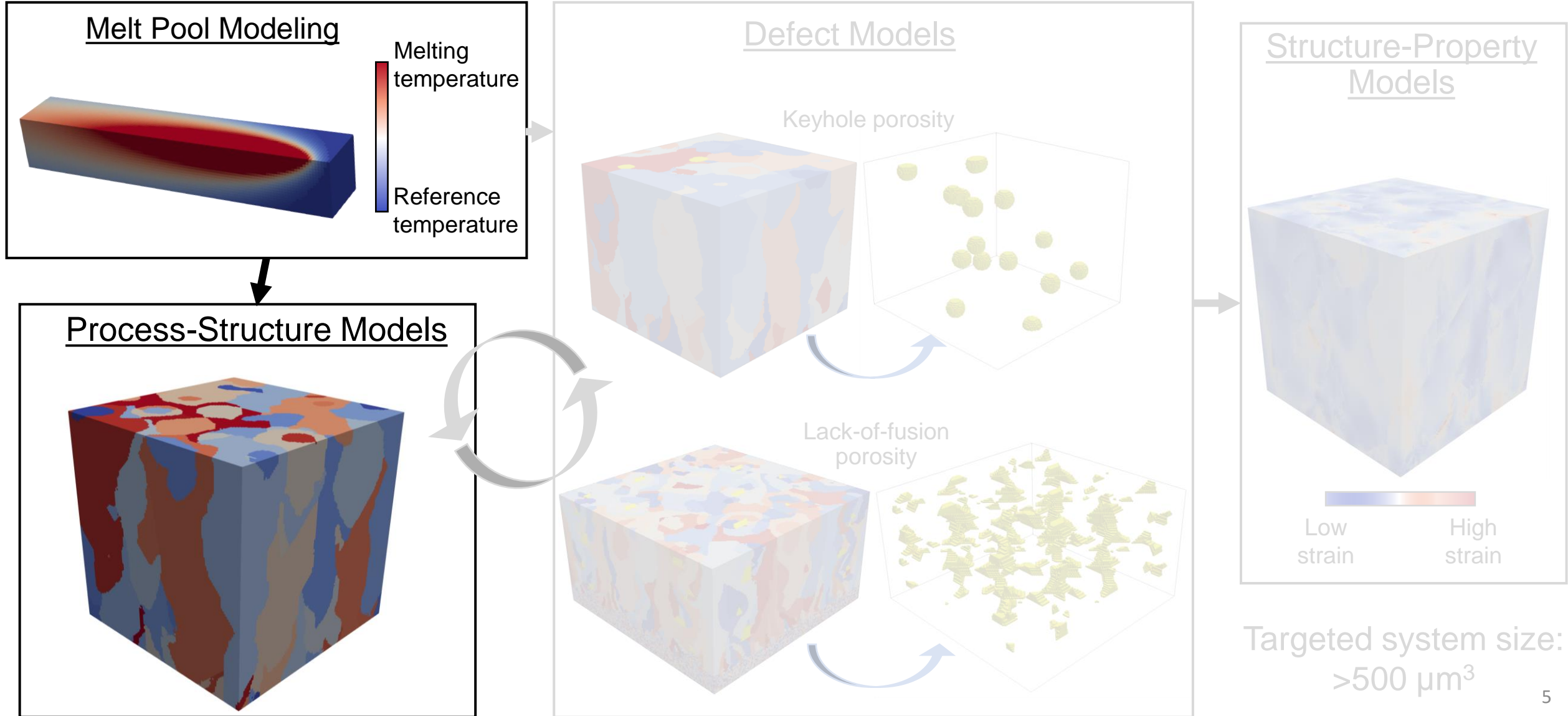
Costs add up fast

Computational Process-Structure-Property (PSP) models provide a way to **augment** these approaches

PSP Models: Our Approach



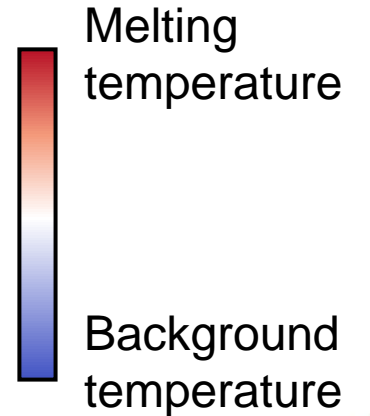
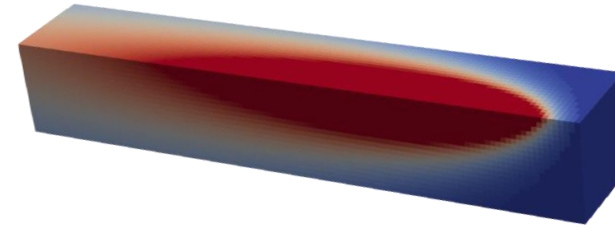
PSP Models: Process-Structure Models



Physically-based Monte Carlo Modeling

- **Stochastic Parallel Particle Kinetic Simulator (SPPARKS)***
 - Kinetic Monte Carlo framework from Sandia National Laboratories
<https://spparks.github.io/>
 - Initially used for bulk microstructural evolution (e.g., annealing, recrystallization)
- Application to AM: Physically-based Monte Carlo [1,2]
 - Thermal model → temperature field → melt pool

Melt pool from analytical thermal model (Rosenthal equation)



$$T = T_0 + \frac{Q}{2\pi r k} \exp\left(-\frac{v(\xi + r)}{2\alpha}\right)$$

Where:

T : temperature

T_0 : background temperature

Q : absorbed power

v : scan speed

k : thermal conductivity

$\alpha = k/(\rho c_p)$

ρ : mass density

c_p : specific heat capacity

$r = \sqrt{\xi^2 + y^2 + (\eta_z z)^2}$

ξ, y, z : local coordinates

η_z : scale factor to control melt pool depth

[1] T.M. Rodgers et al., 2021

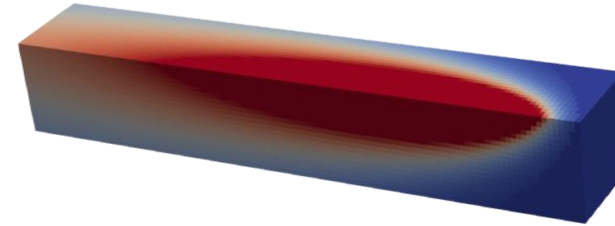
[2] J.G. Pauza et al., 2021

*The use of specific software names does not imply an endorsement by the U.S. Government or NASA.

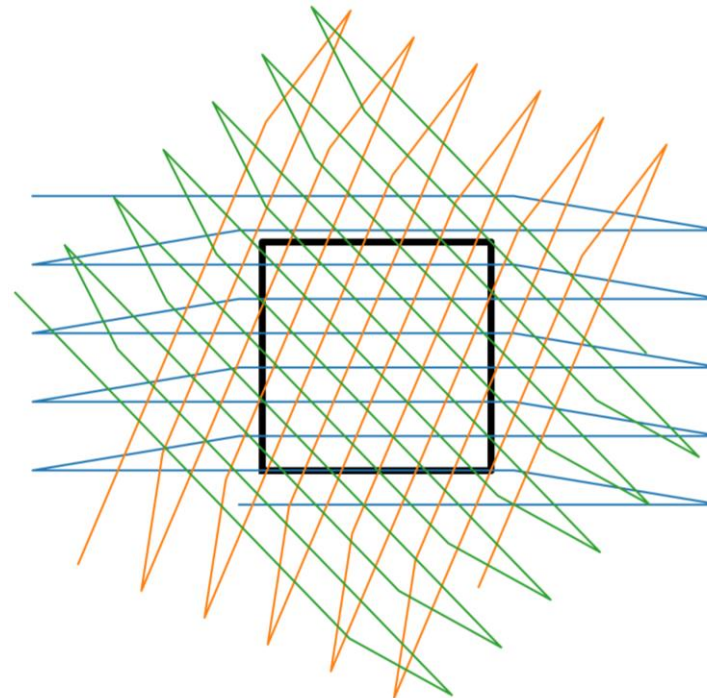
Physically-based Monte Carlo Modeling

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 - Thermal model → temperature field → melt pool
 - Solidification → epitaxial grain growth

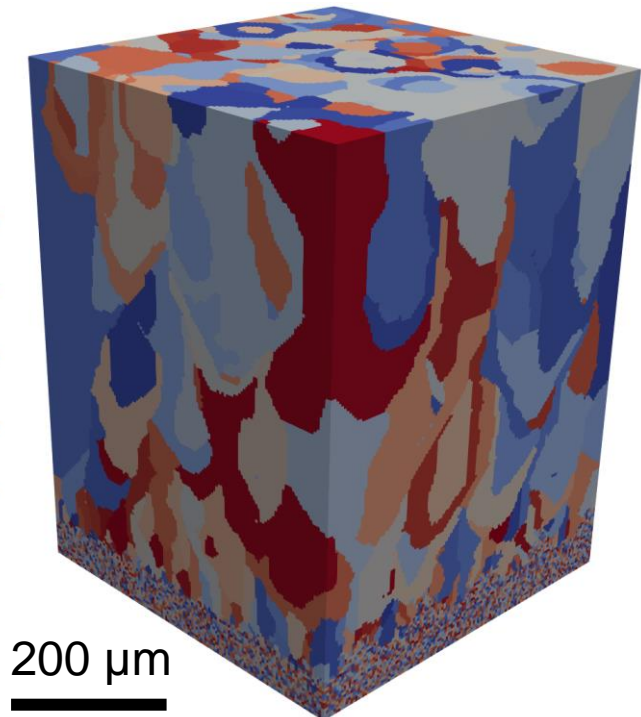
Melt pool from analytical thermal model (Rosenthal equation)



Scan strategy (schematic)



Example microstructure



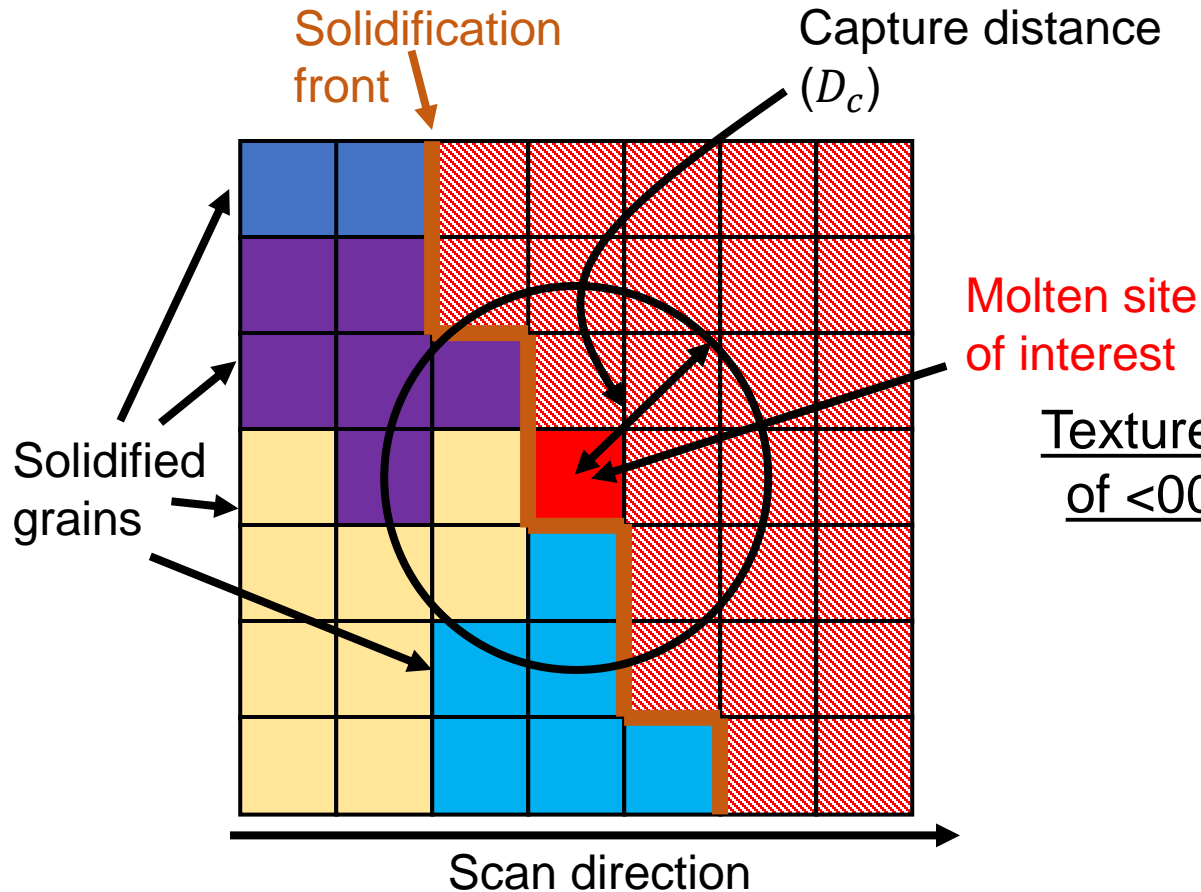
[1] T.M. Rodgers et al., 2021

[2] J.G. Pauza et al., 2021

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Physically-based Monte Carlo Modeling

Solidification: select probabilistically from eligible grains*



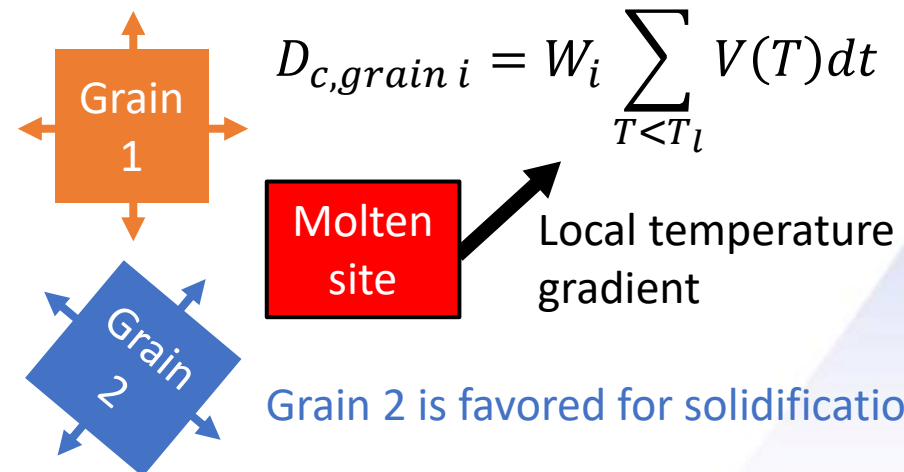
Capture distance is related to local undercooling and dendrite interface kinetics

$$D_c = \sum_{T < T_l} V(T) dt$$

$$V(\Delta T) = a \Delta T^b$$

dt: time step

Texture develops by weighing (W_i) based on alignment of <001> crystal directions with temperature gradient



$$D_{c, grain i} = W_i \sum_{T < T_l} V(T) dt$$

Local temperature gradient

Grain 2 is favored for solidification

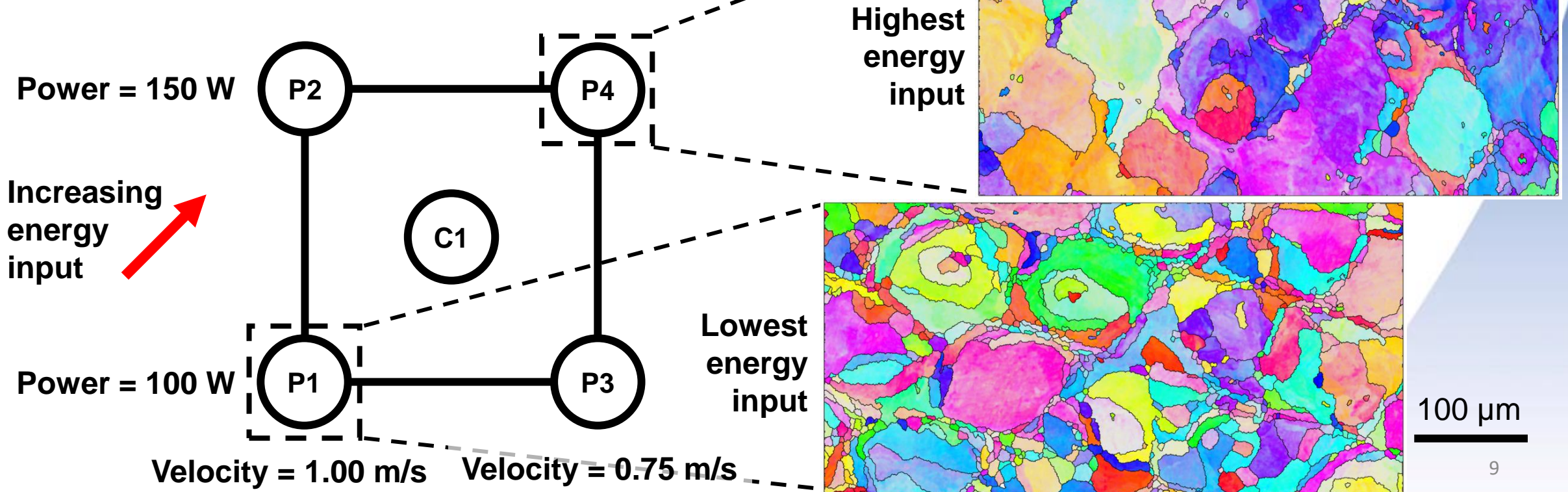
*Adapted from Rodgers, T.M. et al., 2021 [1]

Experimental Samples and Numerical Study

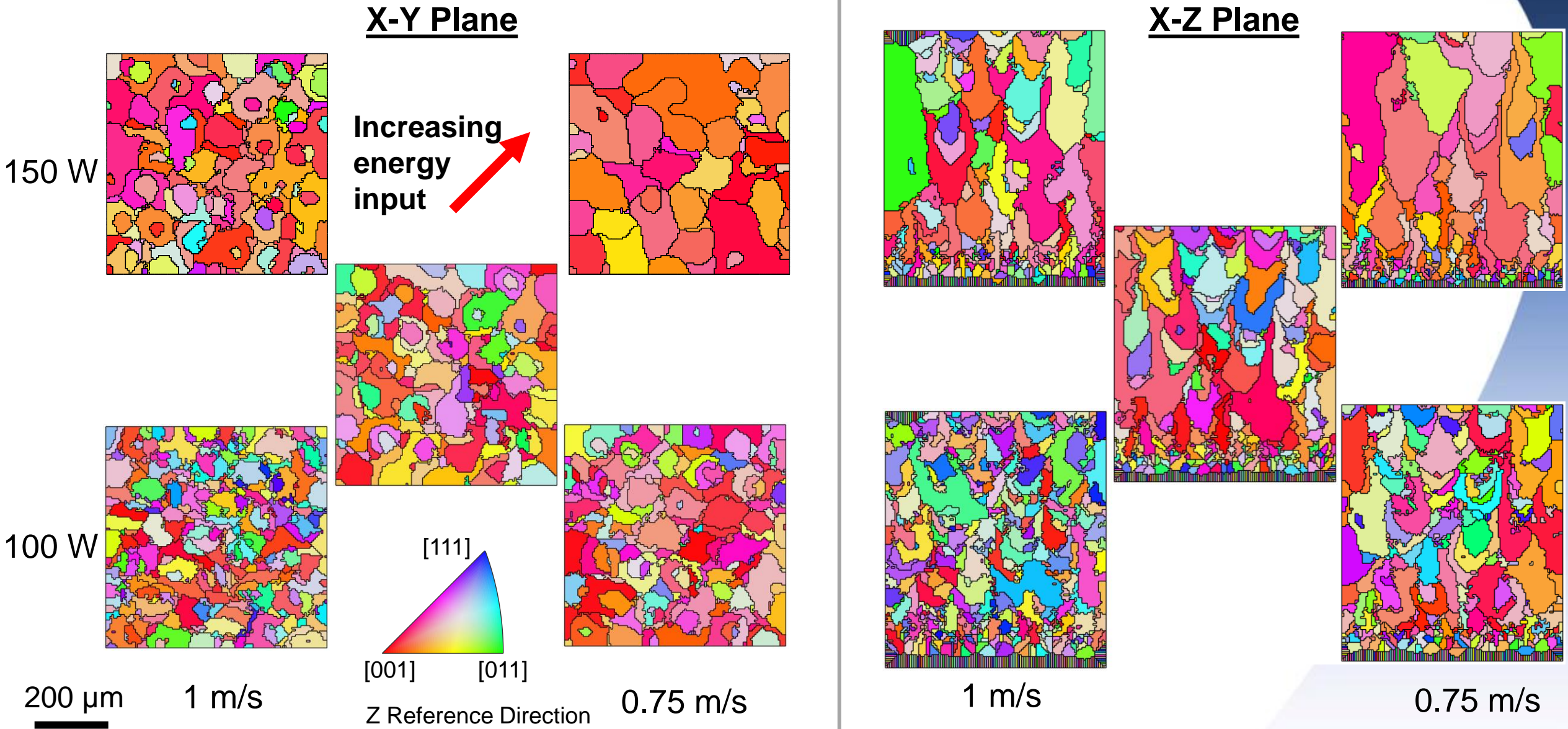
2² Factorial Design with Center Point (values half-way between end points) Results adapted from B. Richter et al., 2022 [3]

- 600 μm x 600 μm x 695 μm numerical domain (20 layers)
- Experimentally characterized P1 and P4
- Hatch Spacing = 100 μm
- Layer Thickness = 30 μm
- Rotation between layers = 67°

256 μm x 512 μm X-Y Plane

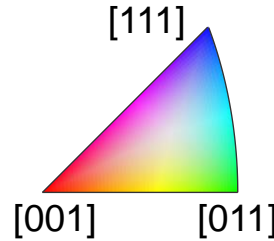


Simulated Microstructure vs. Energy Input

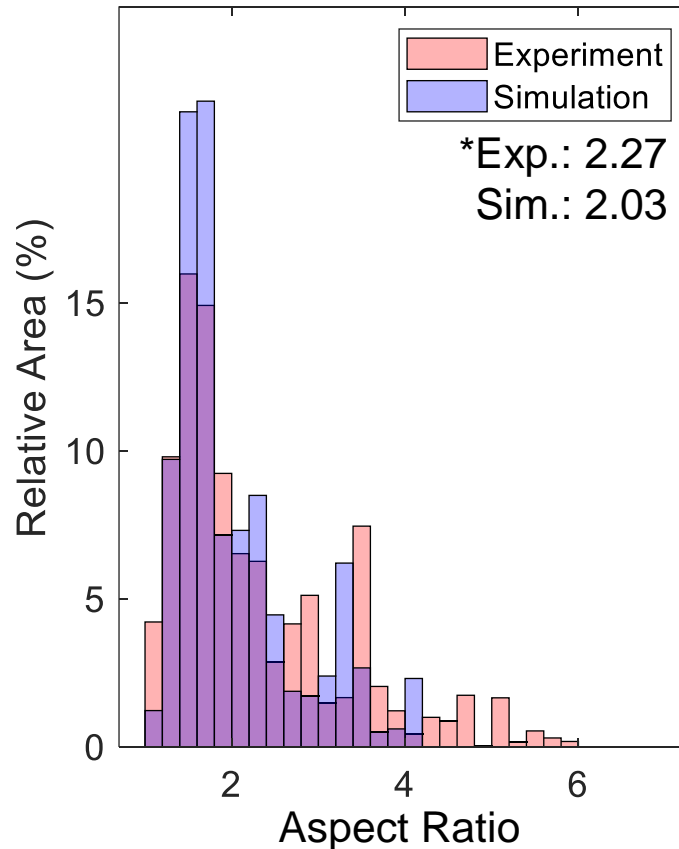
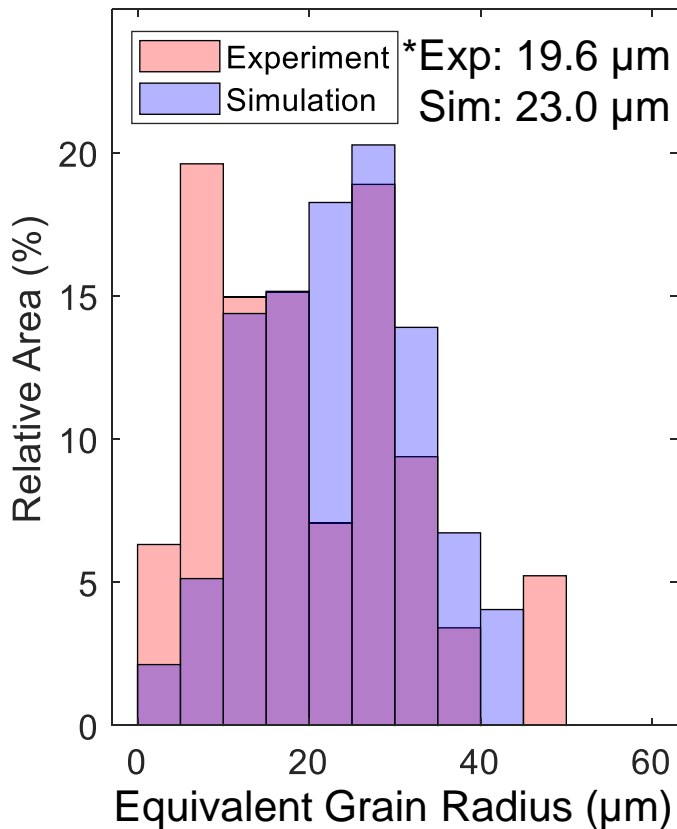
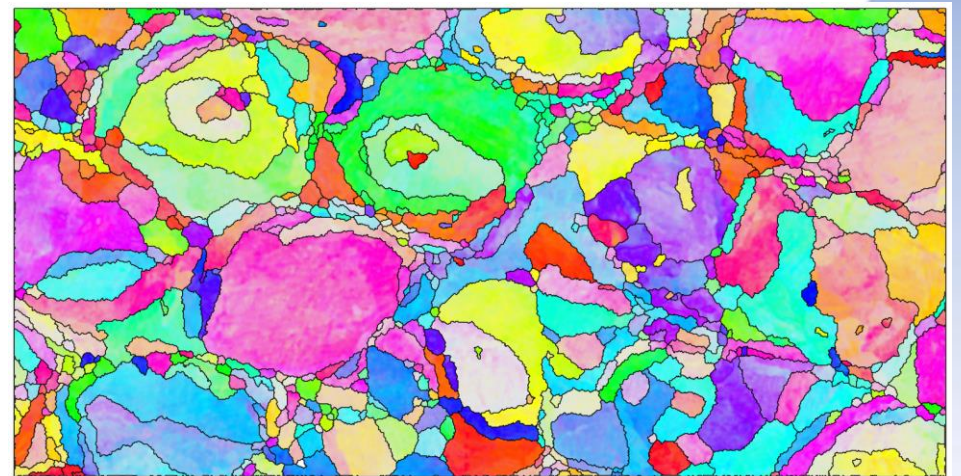
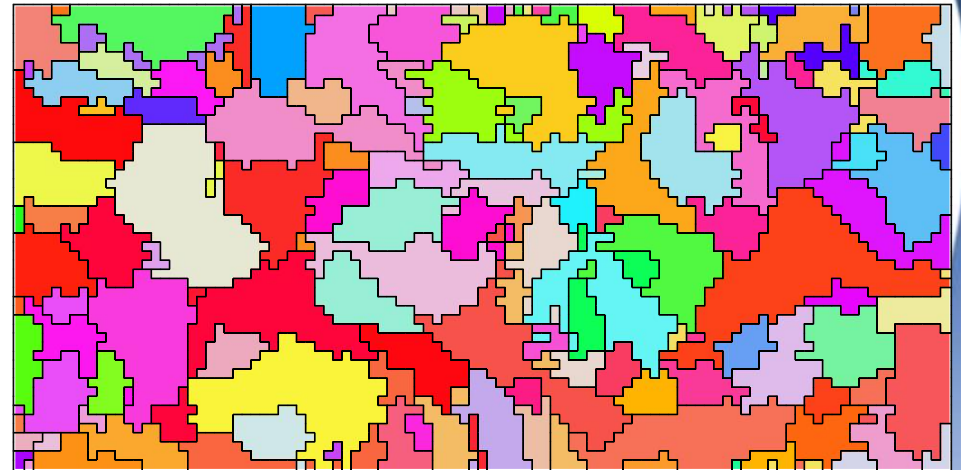


Comparison with Experiment – Low Energy

- Simulation overestimates equivalent radius approximately 17%
- Good agreement for aspect ratio (~12% difference)



Simulation (top) and Experiment (bottom)

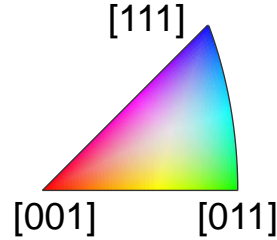


* Mean values

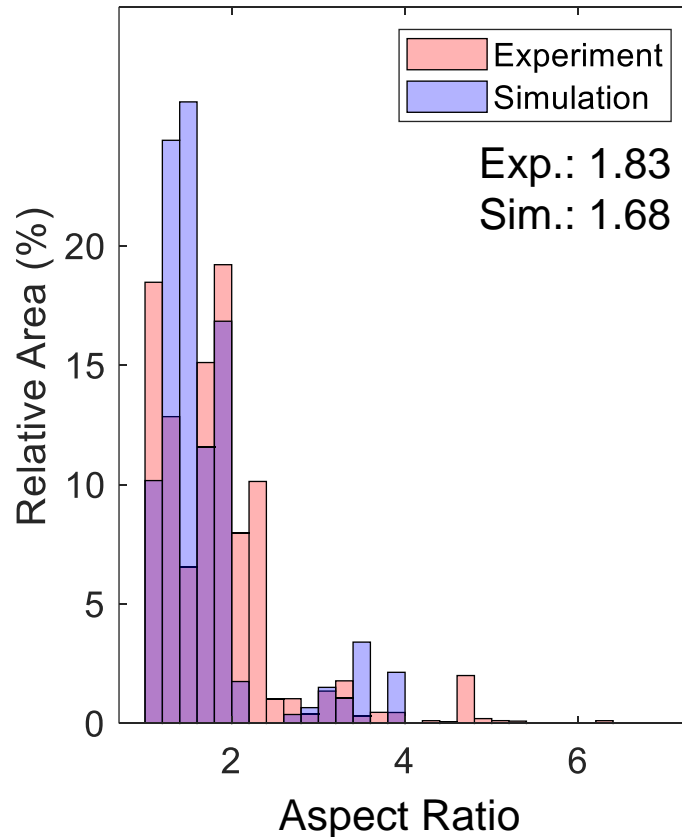
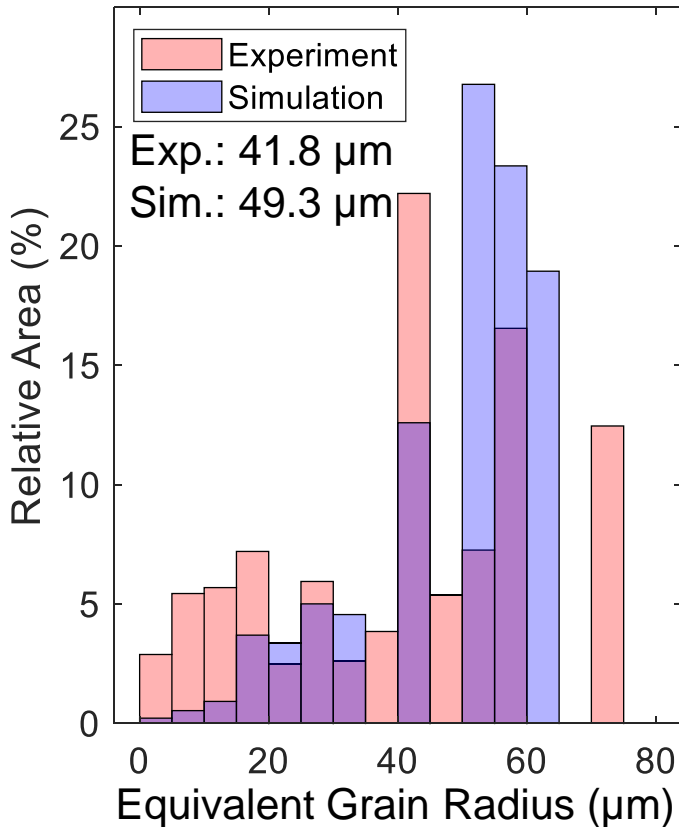
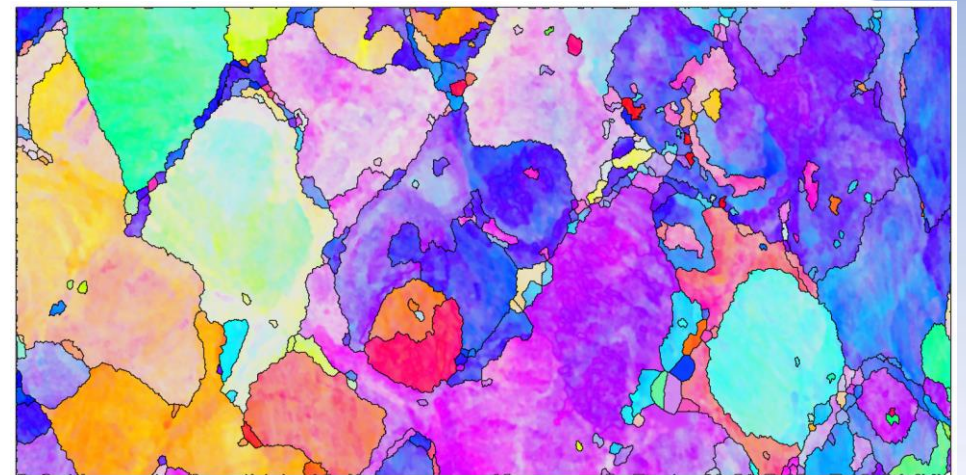
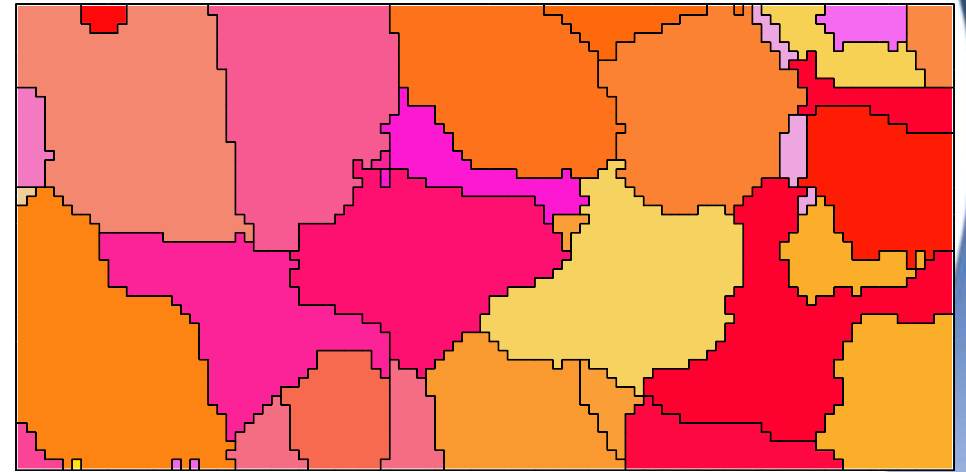
100 μm

Comparison with Experiment – High Energy

- Simulation overestimates equivalent radius approximately 18%
- Good agreement for aspect ratio (~9% difference)



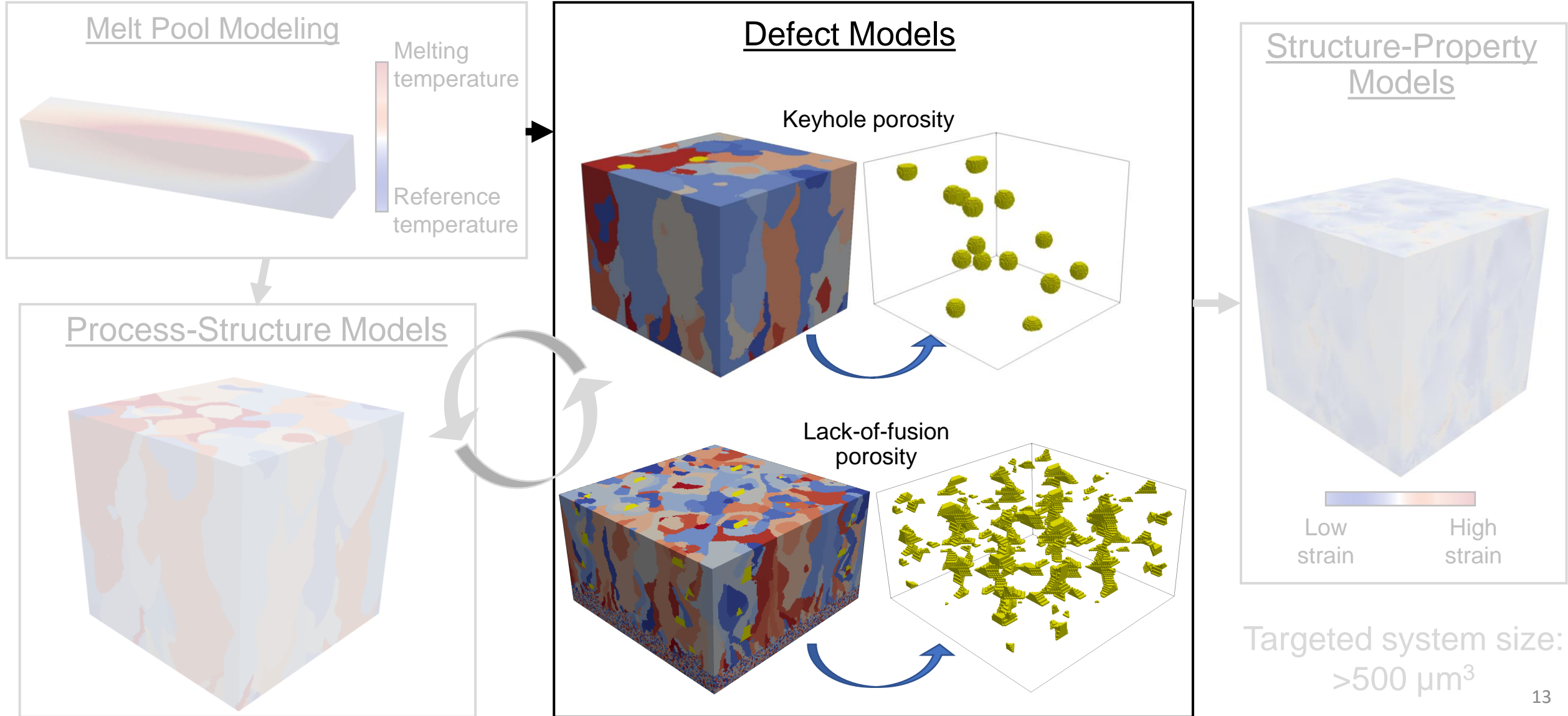
Simulation (top) and Experiment (bottom)



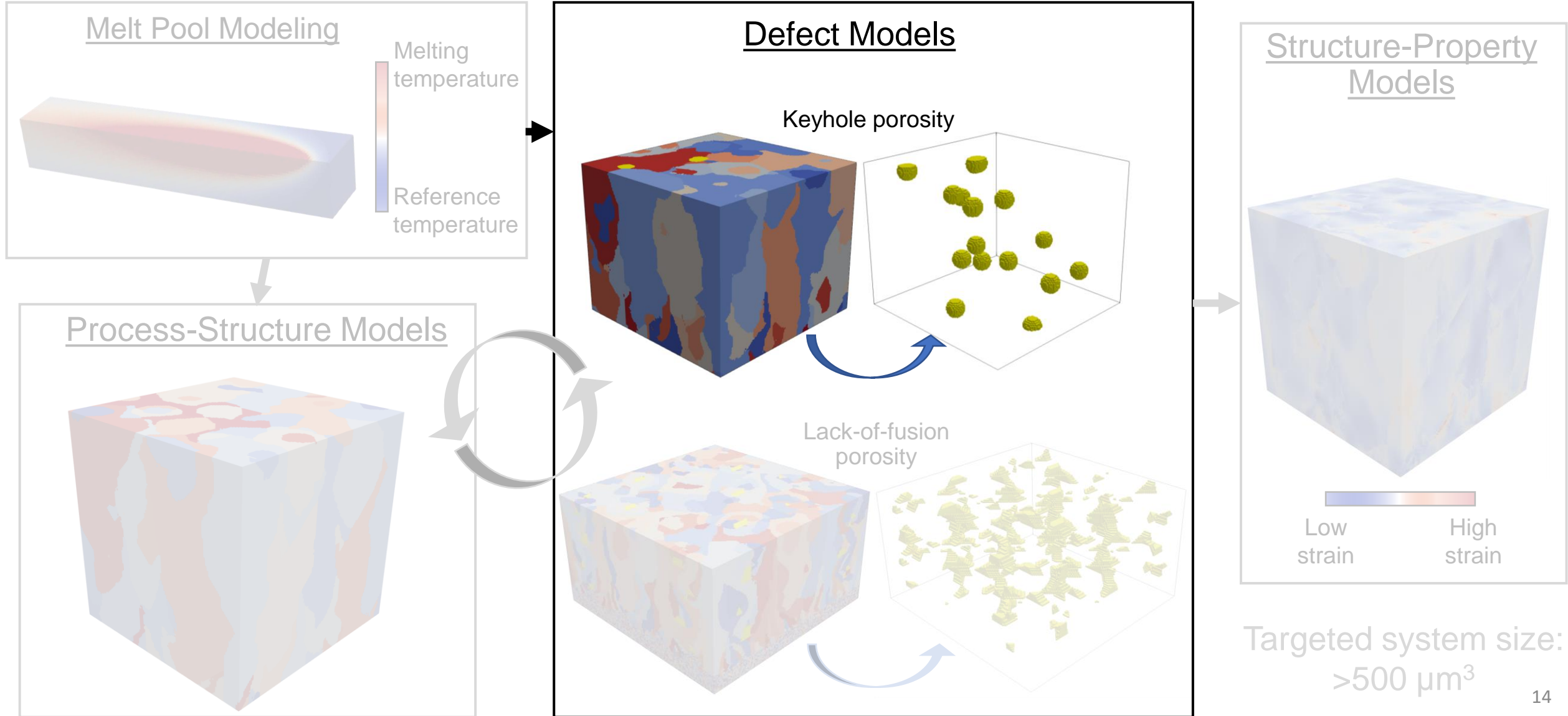
* Mean values

100 μm

PSP Models: Defect Models



PSP Models: Defect Models



Defects Models: Keyhole Porosity

- Stochastic process
- Keyhole size and instability depends on material constant and laser parameters
- Keyhole number (Ke) used to relate keyhole behavior to processing

$$Ke = C \frac{P}{\sqrt{VR^3}}$$

C : Material constant
 P : Laser power
 V : Scanning velocity
 R : Beam radius

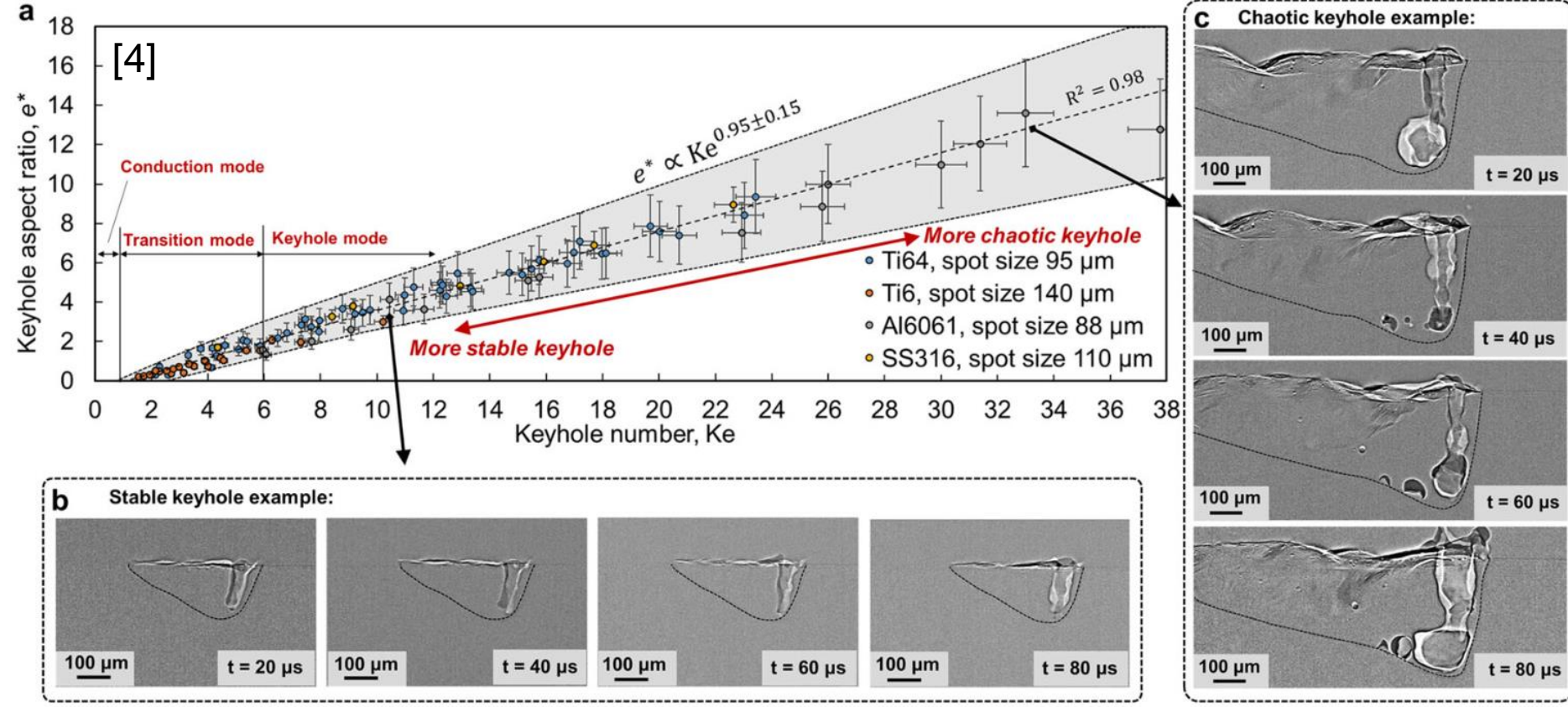


Fig. 1 One-dimensional law for keyhole aspect ratio controlled by the Keyhole number.

[4] Gan, Z. et al., 2021

Fig. 1 from [4] used under CC BY 4.0 <https://creativecommons.org/licenses/by/4.0/>

Defects Models: Keyhole Porosity

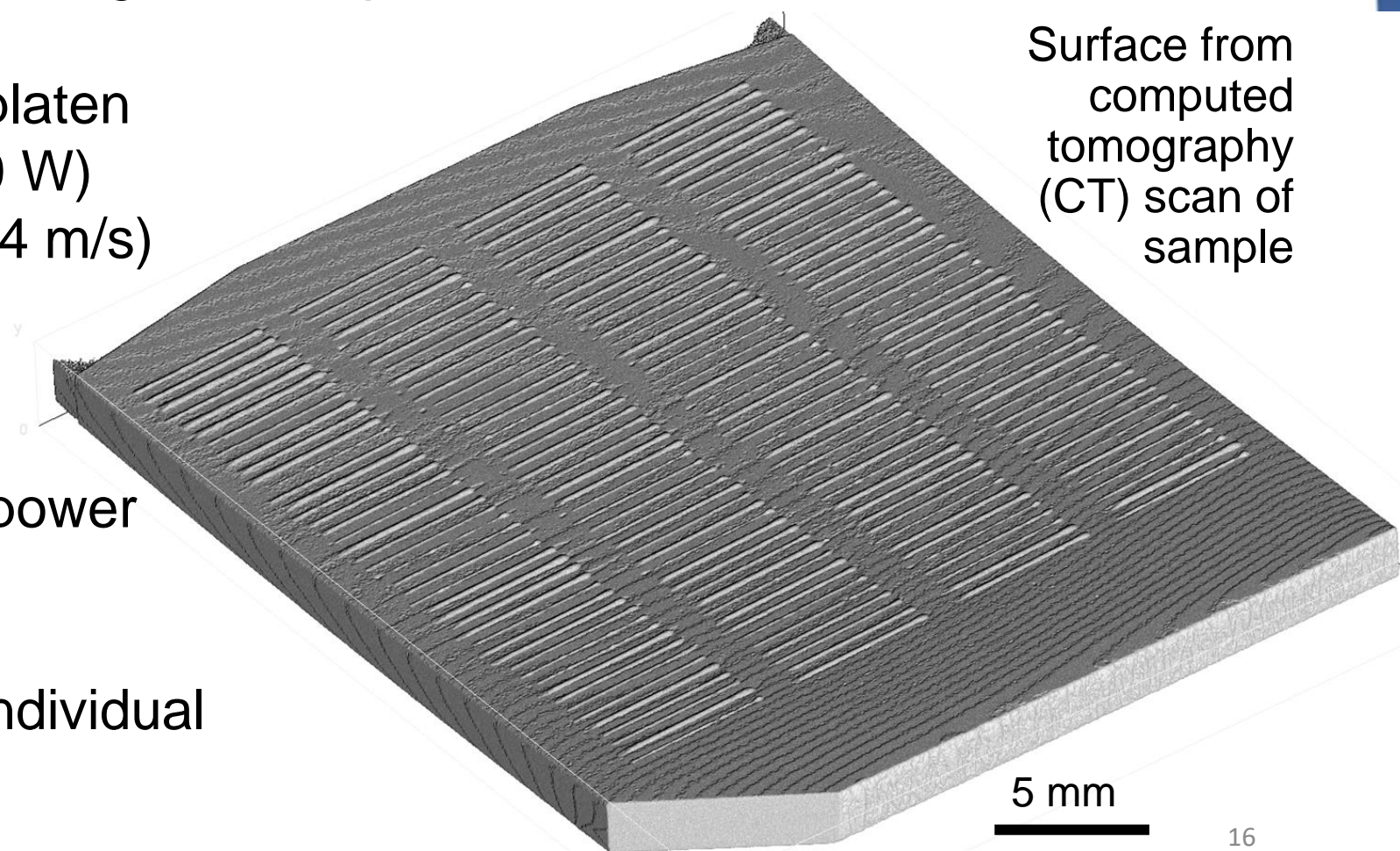
- By characterizing keyhole porosity across a range of processing conditions, can fit distributions to integrate alongside computational models

Example of an experimental platen

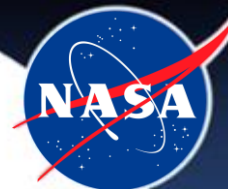
- 2 powers (~260 W and 360 W)
- 14 velocities (0.25 m/s – 1.4 m/s)
- 5 mm lines, 6 repetitions

Purposely had many low scanning velocities and high power to induce keyhole porosity

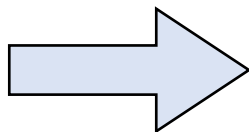
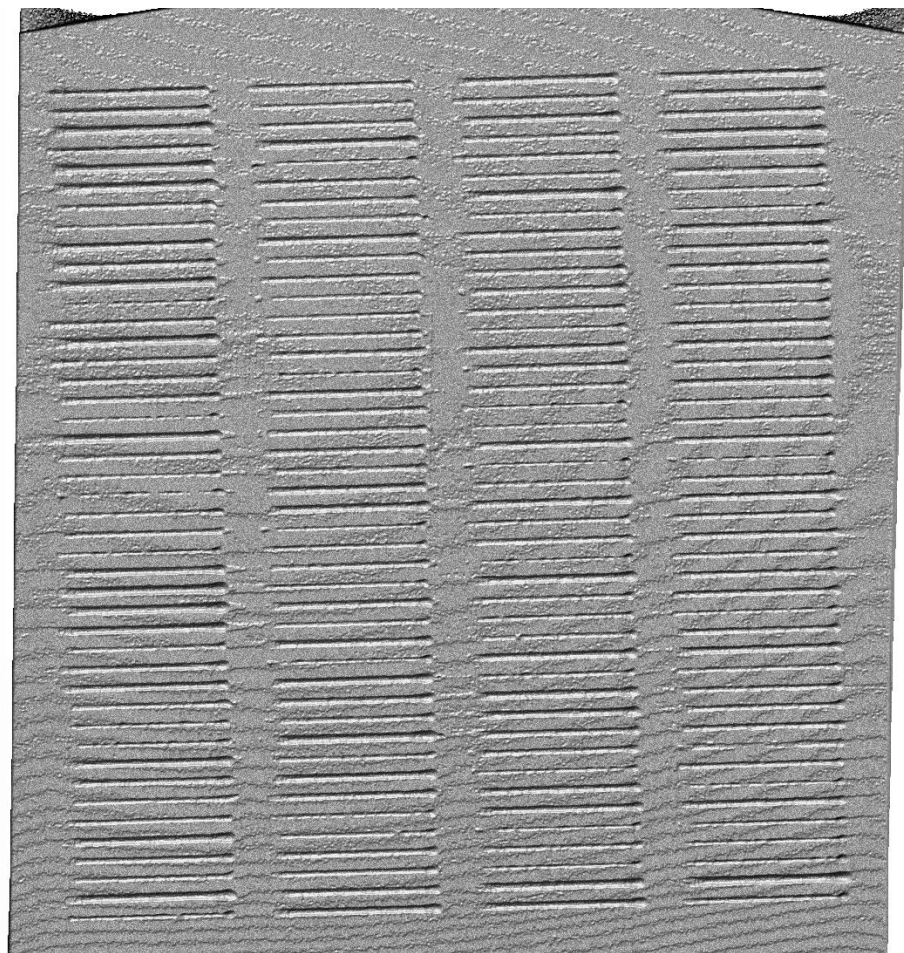
Analyzed porosity based on individual line location



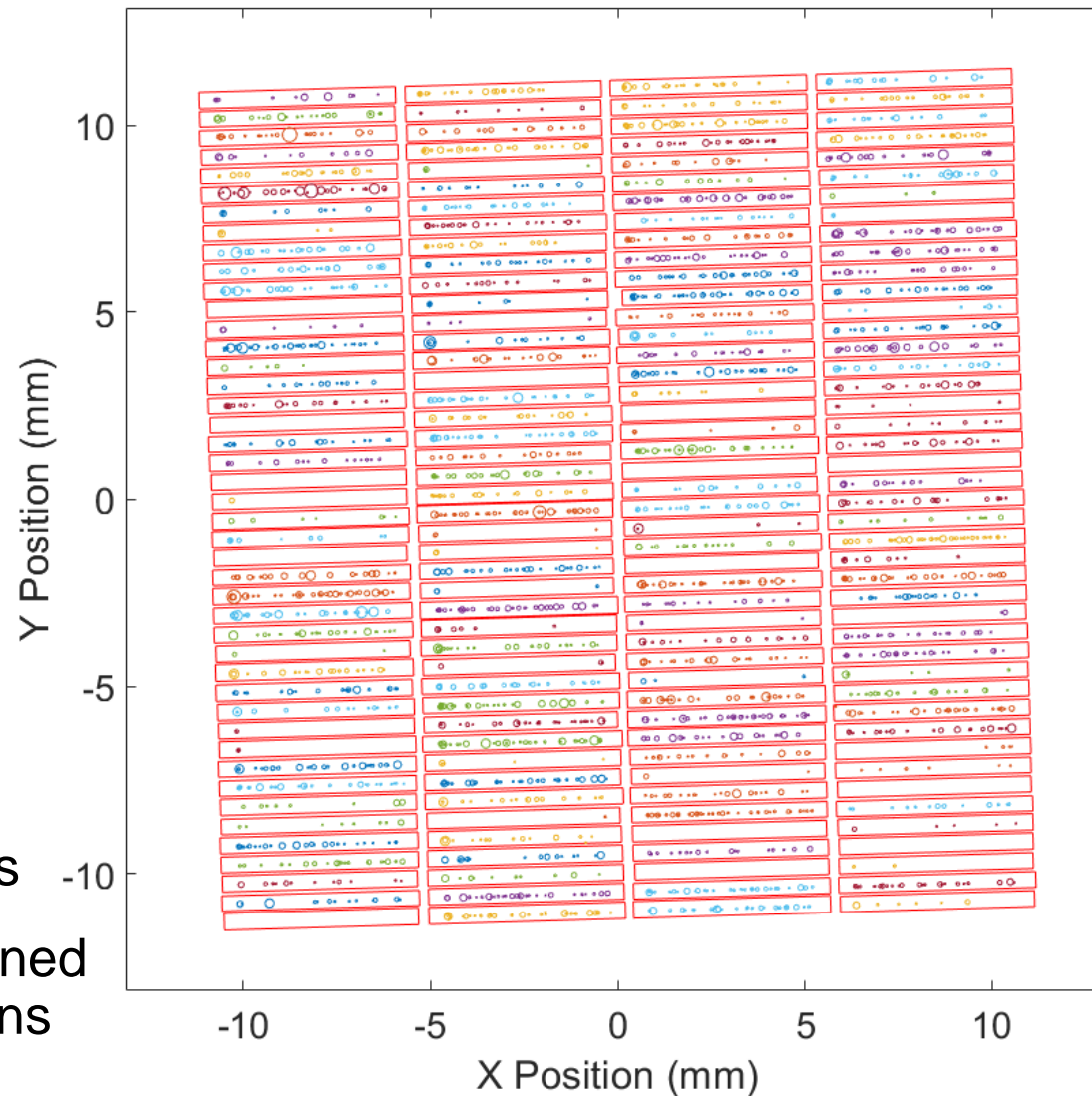
Defects Models: Keyhole Porosity



CT scan of surface of sample

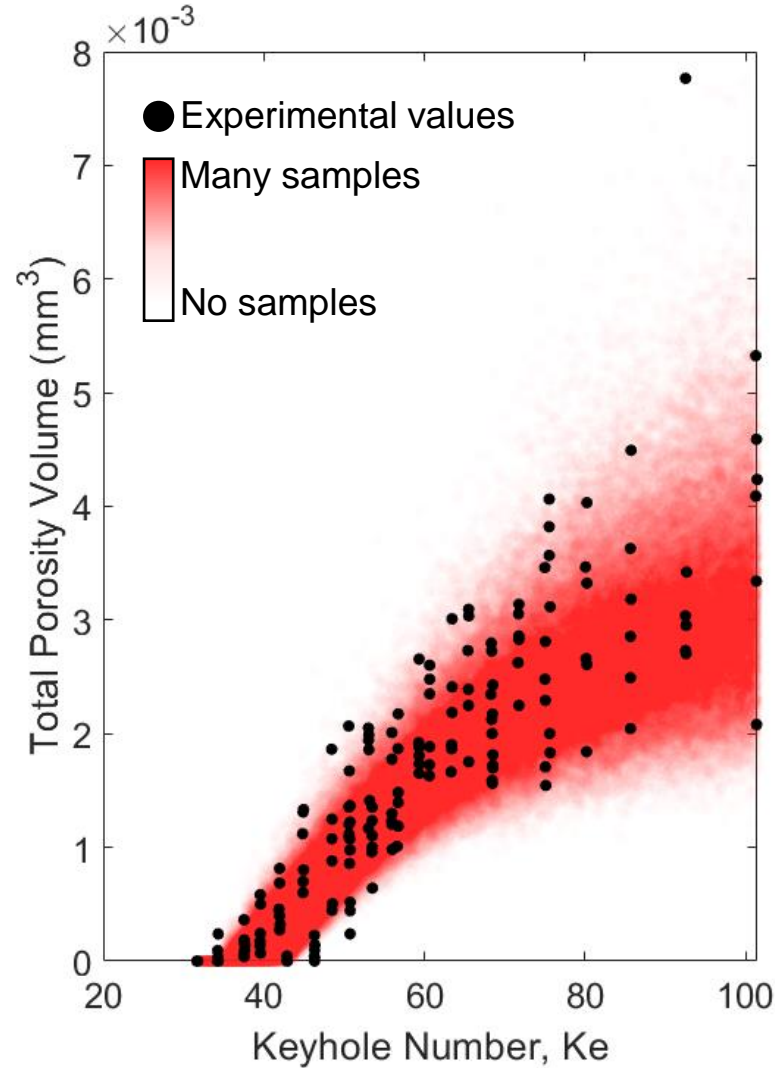


Segmented porosity

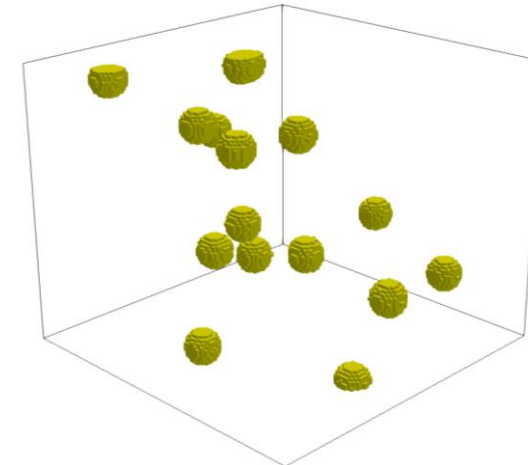
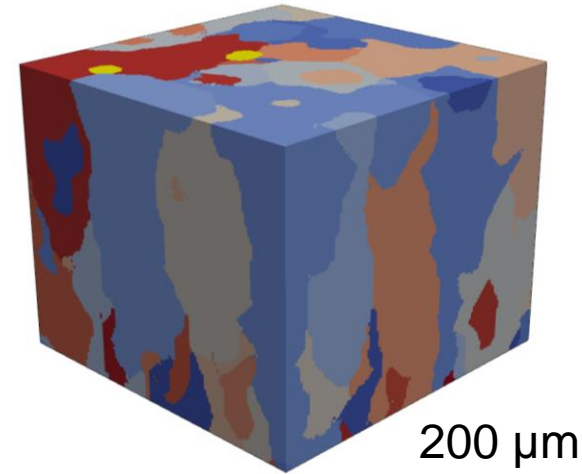


Defects Models: Keyhole Porosity

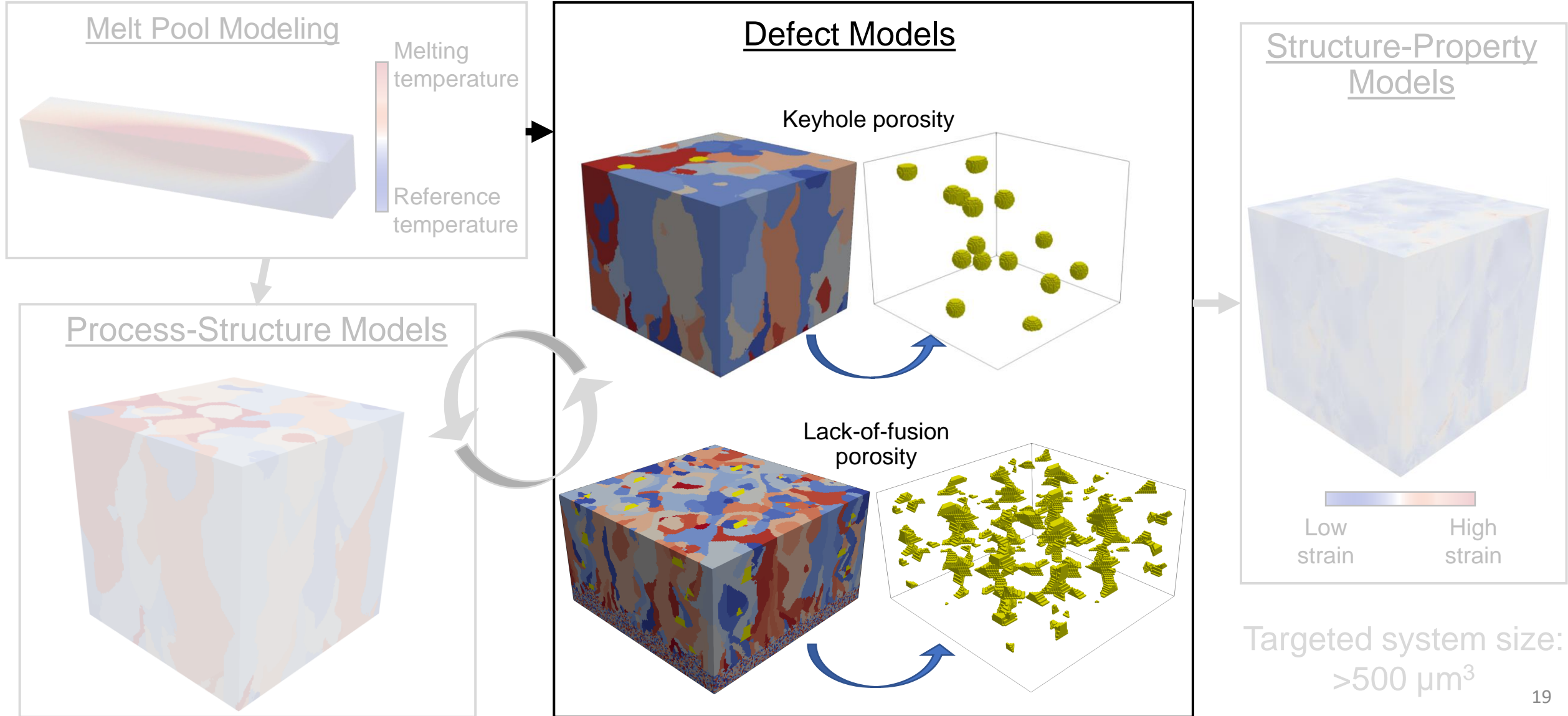
- From keyhole porosity data, can relate porosity to processing parameters
- Can sample distributions and seed into models while they're running



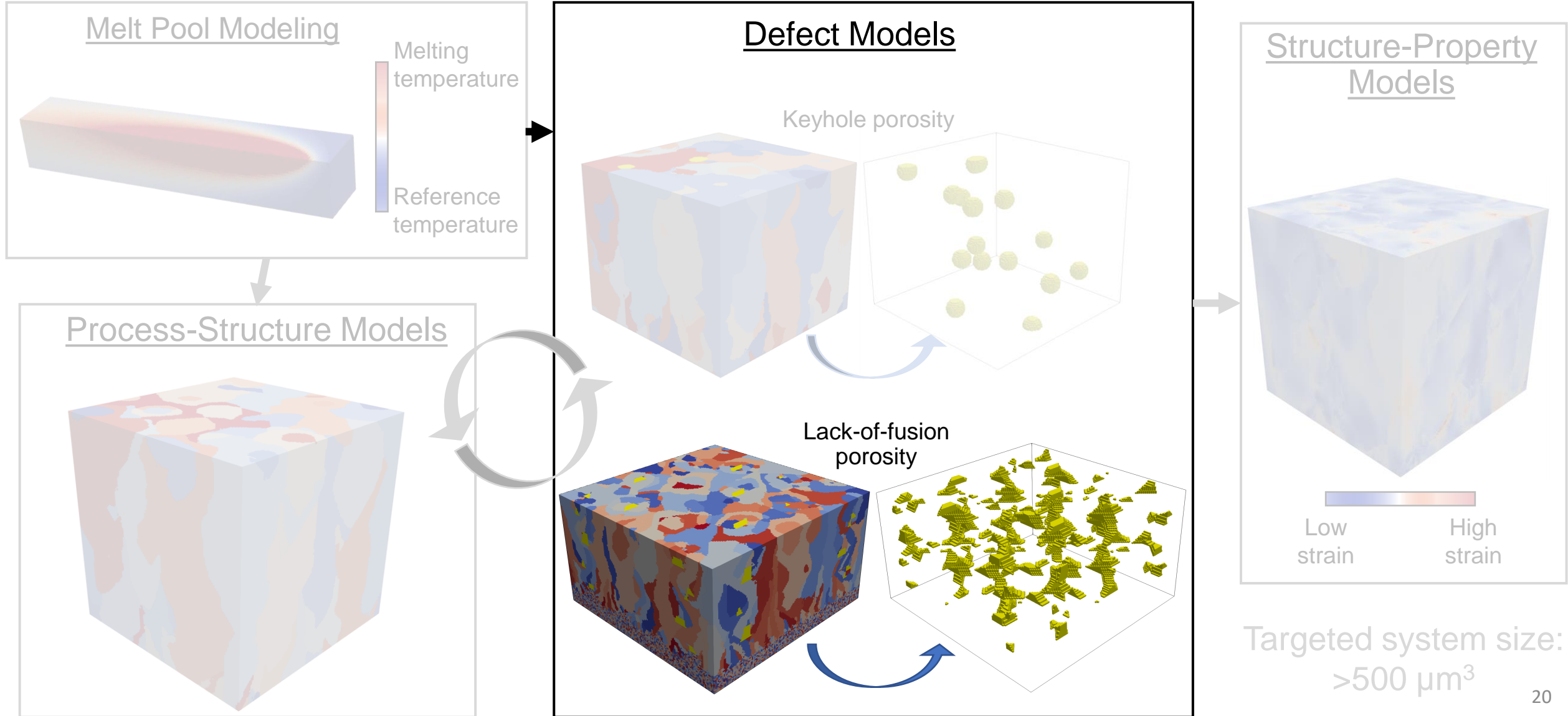
Sample pores and seed into simulation



PSP Models: Defect Models



PSP Models: Defect Models

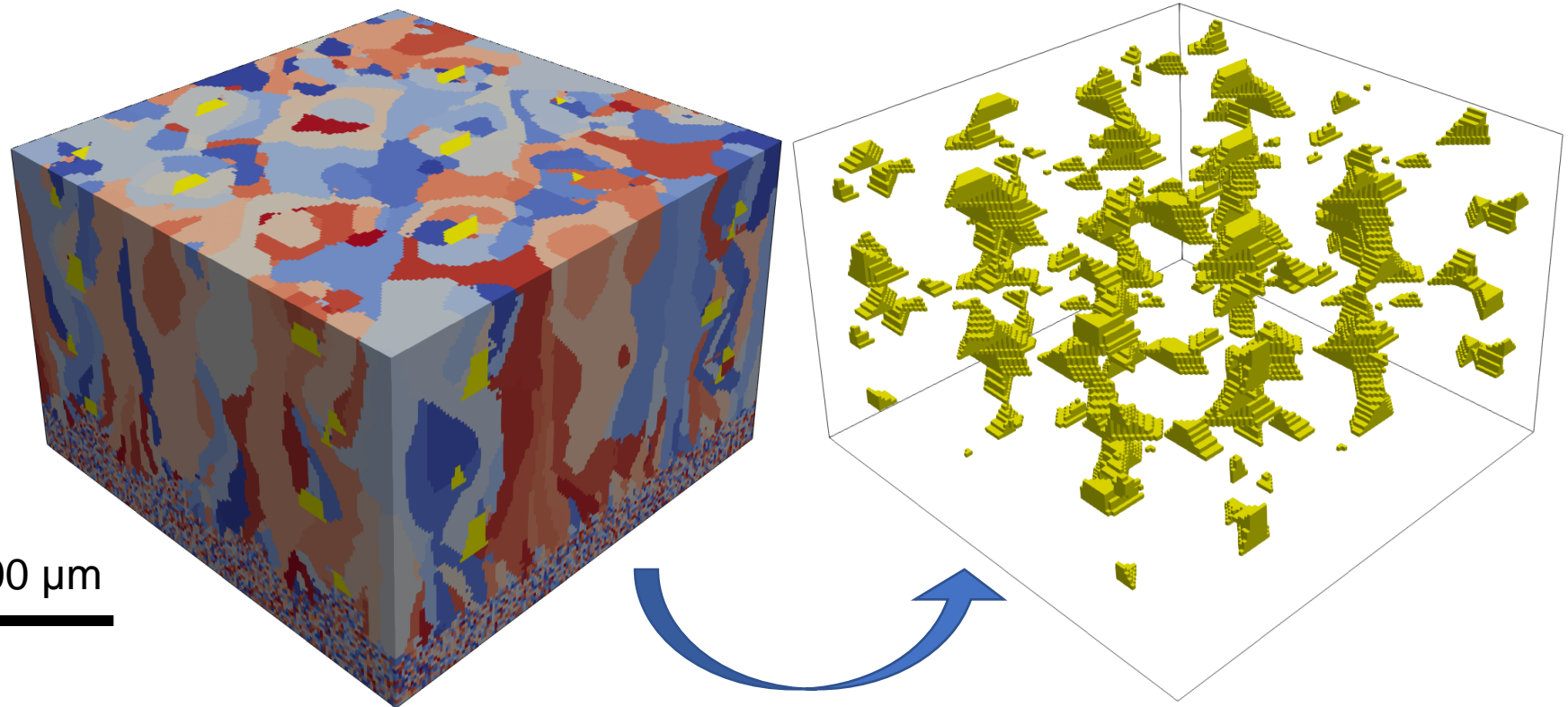


Defects Models: Lack-of-Fusion Porosity

- Lack-of-fusion porosity is semi-deterministic and geometry related
- Tang et al. derived a lack-of-fusion criteria based on the melt pool geometry and processing [5]

No porosity occurs if ...

$$\left(\frac{L}{D}\right)^2 + \left(\frac{H}{W}\right)^2 \leq 1$$



200 μm

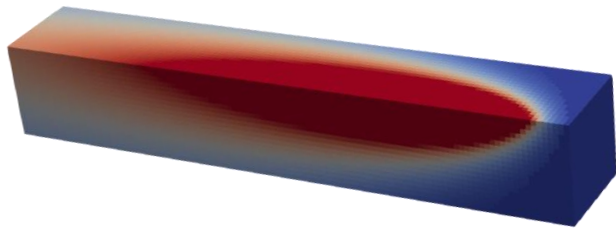
L : Layer thickness
 H : Hatch spacing
 W : Melt pool width
 D : Melt pool depth

[5] M. Tang et al., 2017

Defects Models: Lack-of-Fusion Porosity

- By using a thermal model to calculate temperature field and calculating the melt pool geometry, a user can determine if porosity will occur
- If occurrence is likely, can track in process-structure model using distinct phases for melted vs. unmelted material

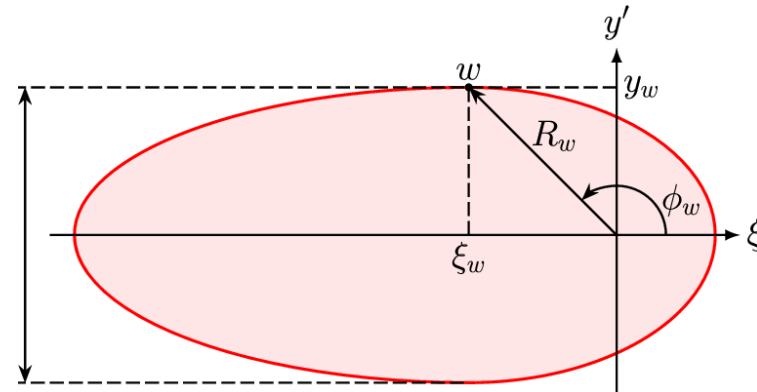
Melt pool from analytical thermal model (Rosenthal equation)



$$T = T_0 + \frac{Q}{2\pi rk} \exp\left(-\frac{v(\xi + r)}{2\alpha}\right)$$

Melt pool geometry relationship

$$W, D = f(\text{Processing}, \text{Material})$$

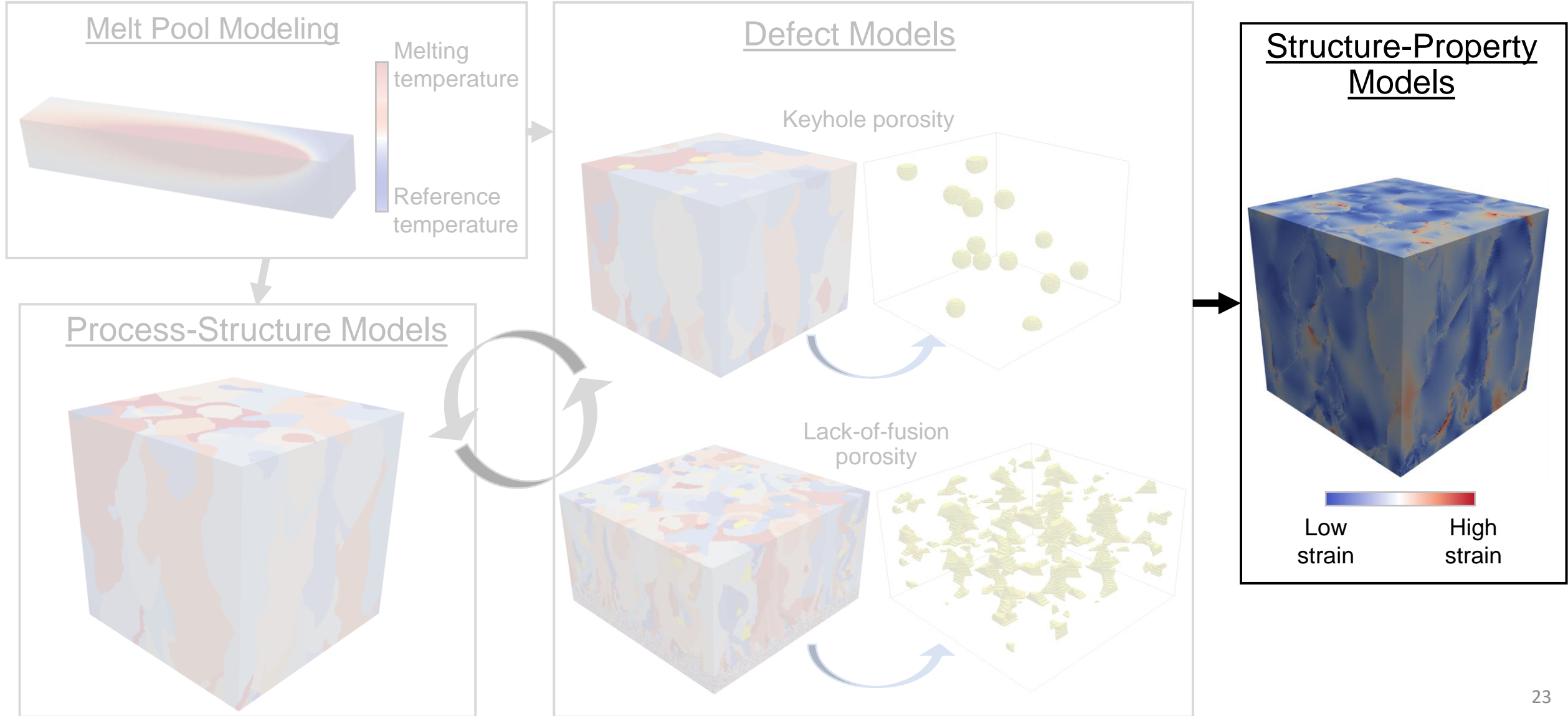


$$\left(\frac{L}{D}\right)^2 + \left(\frac{H}{W}\right)^2 \leq 1$$

Lack-of-fusion criteria

Adapted from J.D. Pribe et al., 2023 [6]

PSP Models: Structure-Property Models



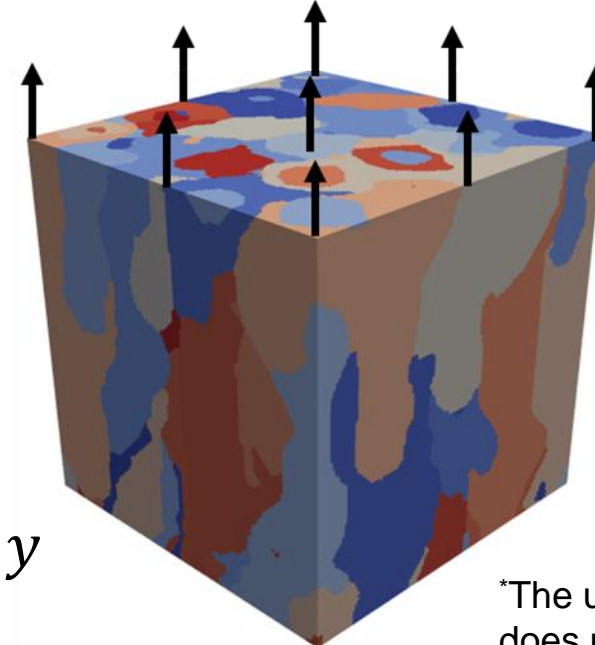
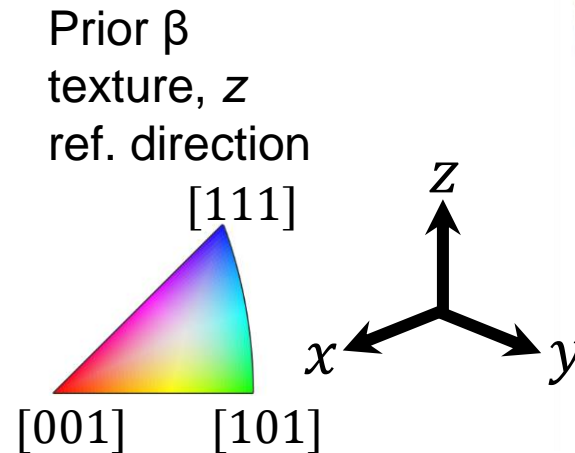
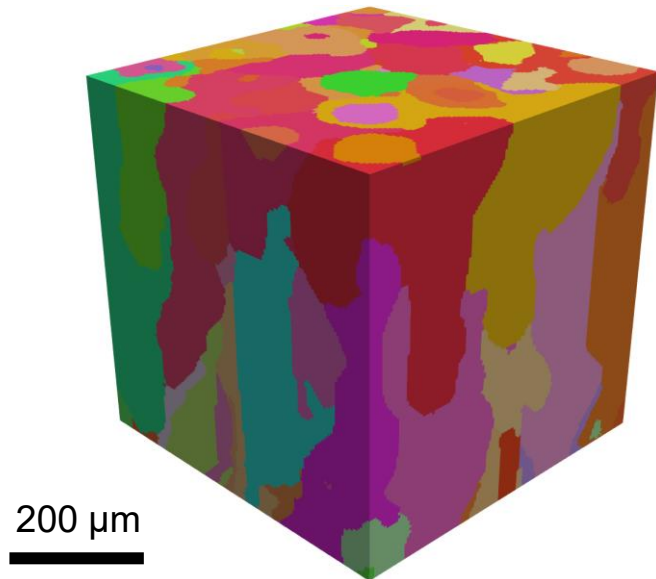
Structure-Property: Crystal Plasticity

- **Elasto-Viscoplastic Fast Fourier Transform (EVP-FFT) [7]***
- **Advantages**
 - Speed improvements over crystal plasticity finite element methods
 - Shares voxel-based microstructure representation with SPPARKS

Section adapted from J.D. Pribe et al., 2023 [6]

One of 12 possible α variants randomly selected for each grain

0.6% applied strain in build direction; periodic boundary conditions on sides of domain



J.D. Pribe et al., 2023 [6]



*The use of specific software names does not imply an endorsement by the U.S. Government or NASA.

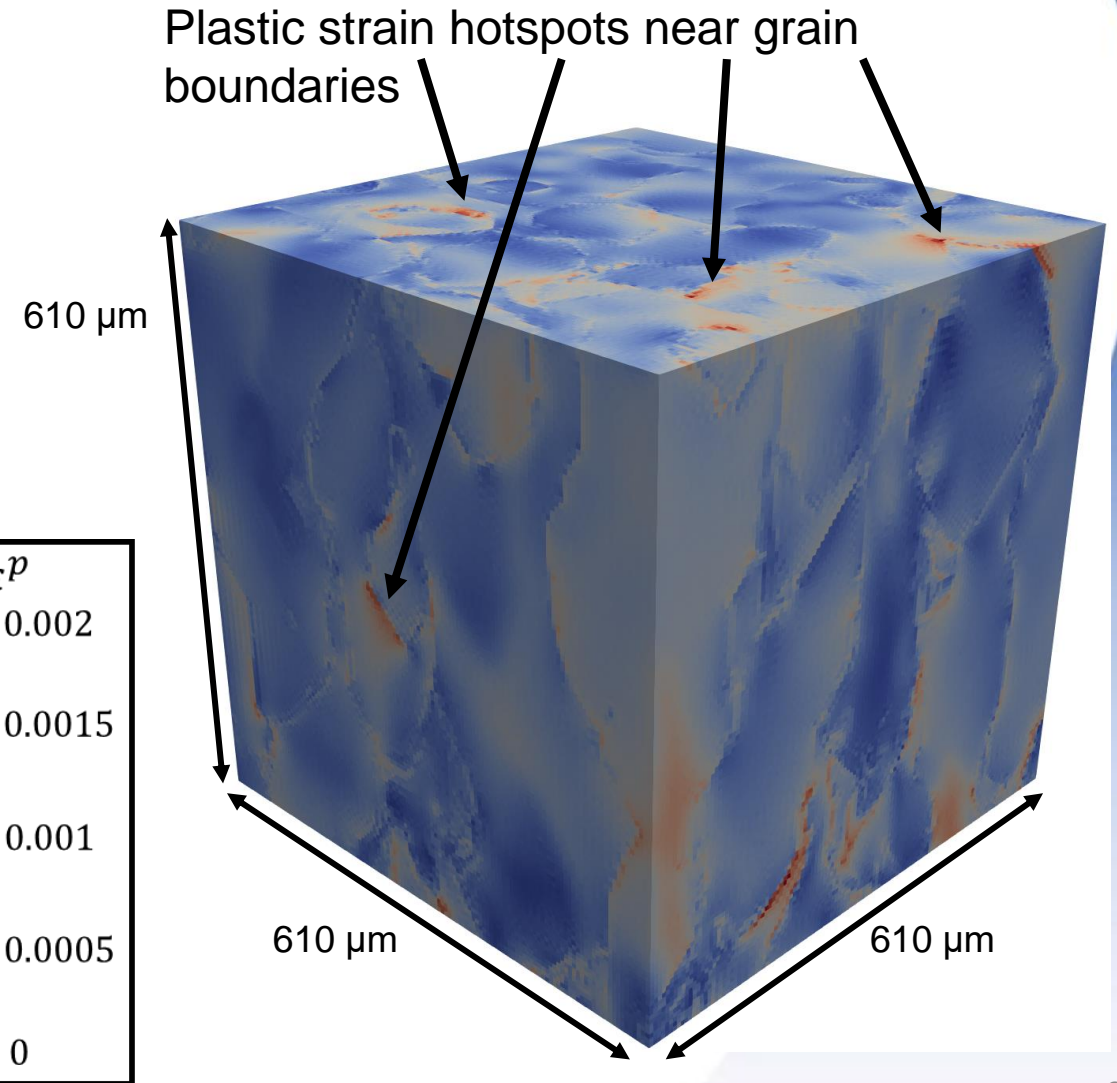
Structure-Property: Micromechanical Fields

- Goal: estimate distributions of fatigue indicator parameters (FIPs)

- Here: equivalent plastic strain

$$\varepsilon^p = \int \dot{\varepsilon}^p dt \quad \dot{\varepsilon}^p = \sqrt{\frac{2}{3} \dot{\varepsilon}^p : \dot{\varepsilon}^p}$$

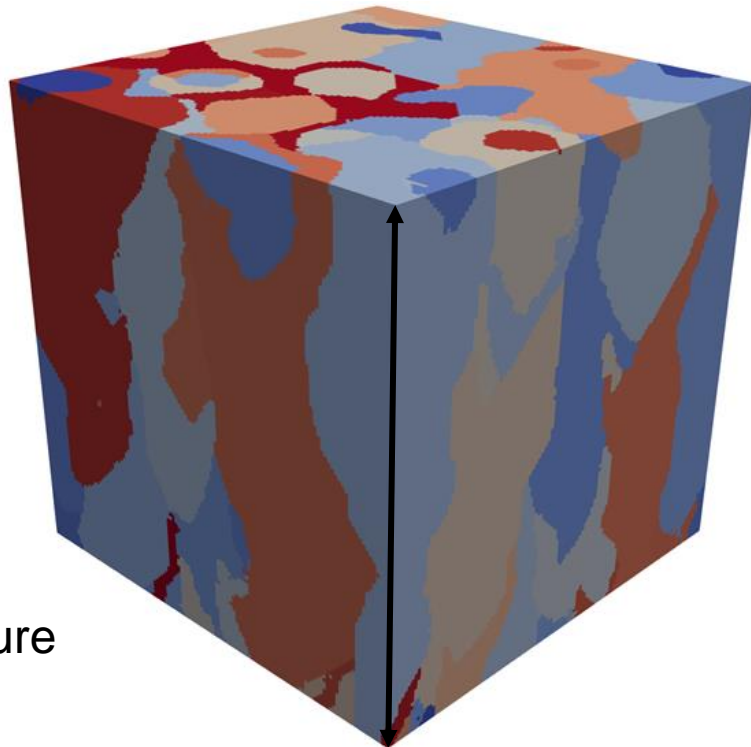
- Value assigned to each grain by volume averaging near hotspots



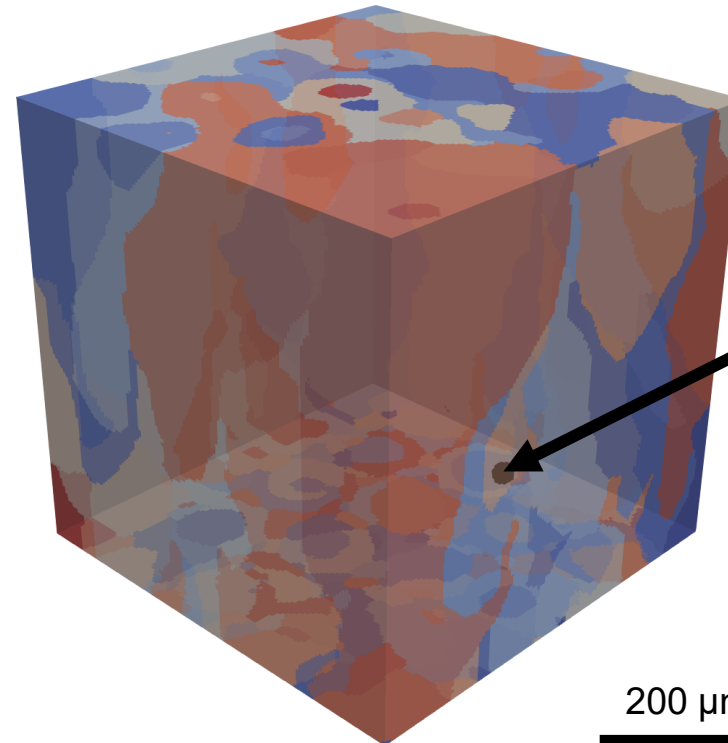
$\dot{\varepsilon}^p$: plastic strain rate tensor

Microstructures with and without porosity

- Compare simulations with no porosity and with one 30- μm -diameter pore per simulation (~99.995% dense)
- Motivation: operating near the keyhole boundary could induce process-escape pores
 - Here: 370 W laser power, 1.2 m/s scan speed [8]; MAP estimates for thermophysical parameters



Fully-dense
microstructure



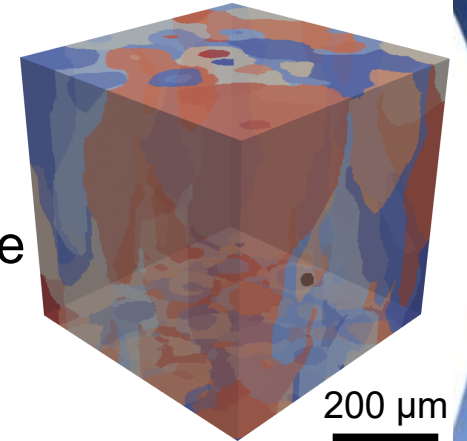
Microstructure with
one pore, inserted
stochastically during
process-structure
simulation

200 μm

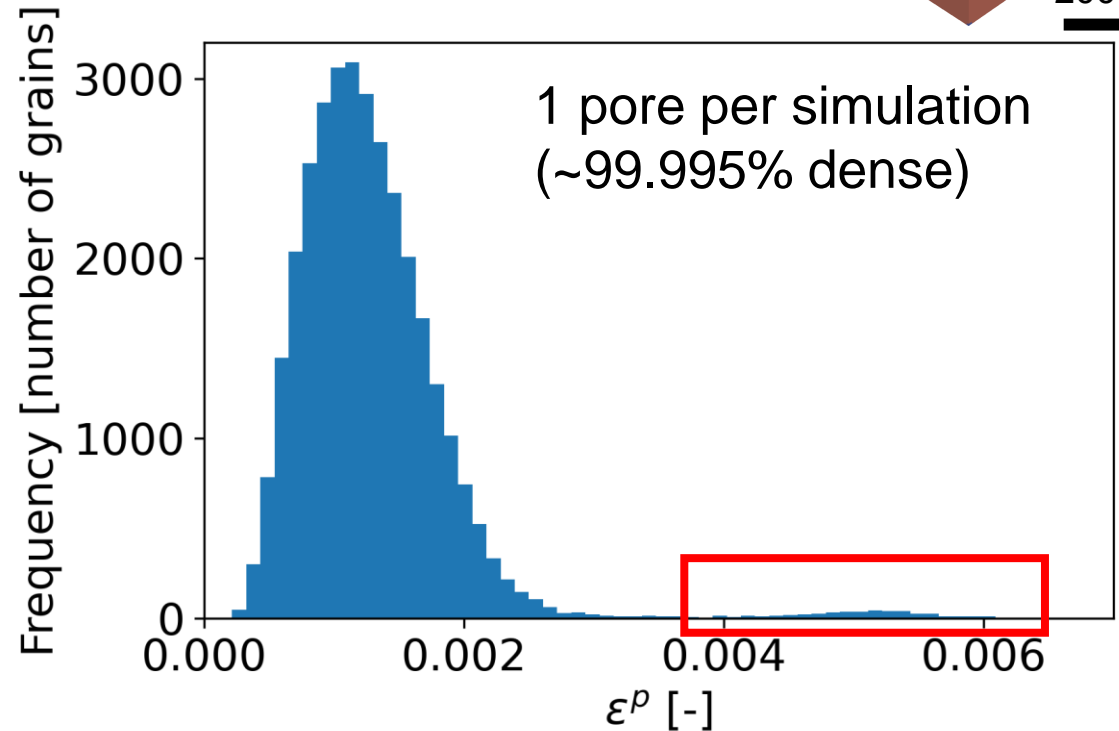
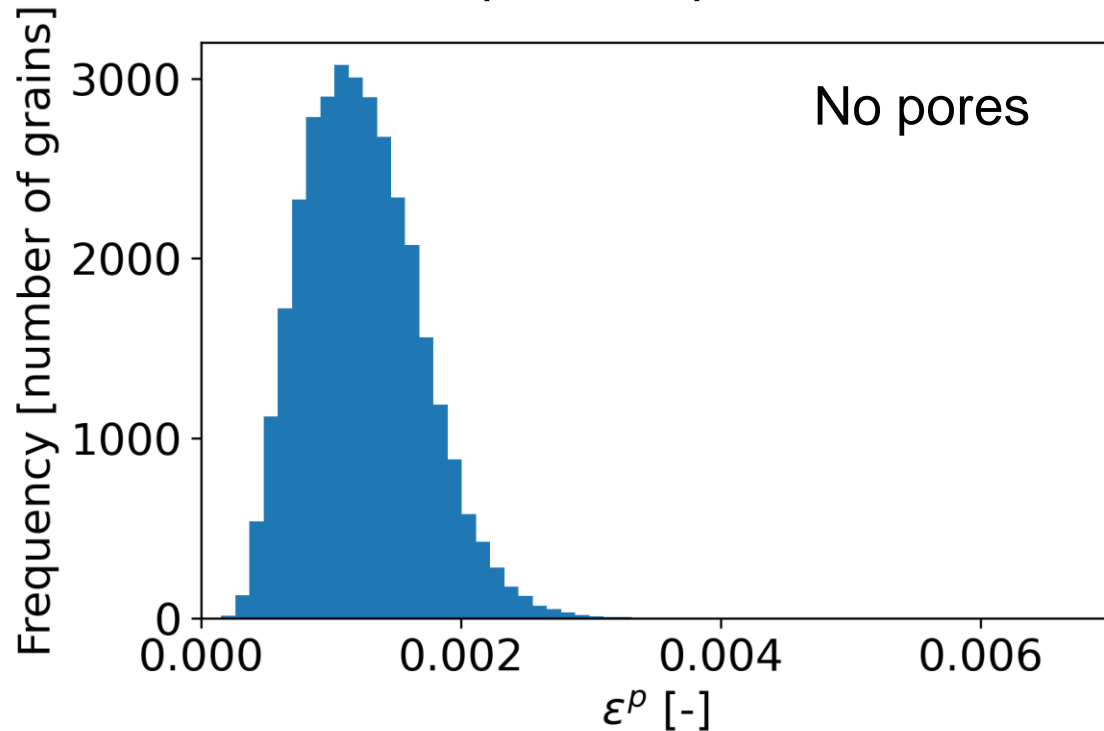
Microstructures with and without porosity

- 200 simulations with one 30- μm keyhole pore per simulation
- Overall distribution of plastic strain is similar
- **But extreme values are shifted!**

Example
microstructure



Equivalent plastic strain for all grains across 200 simulations



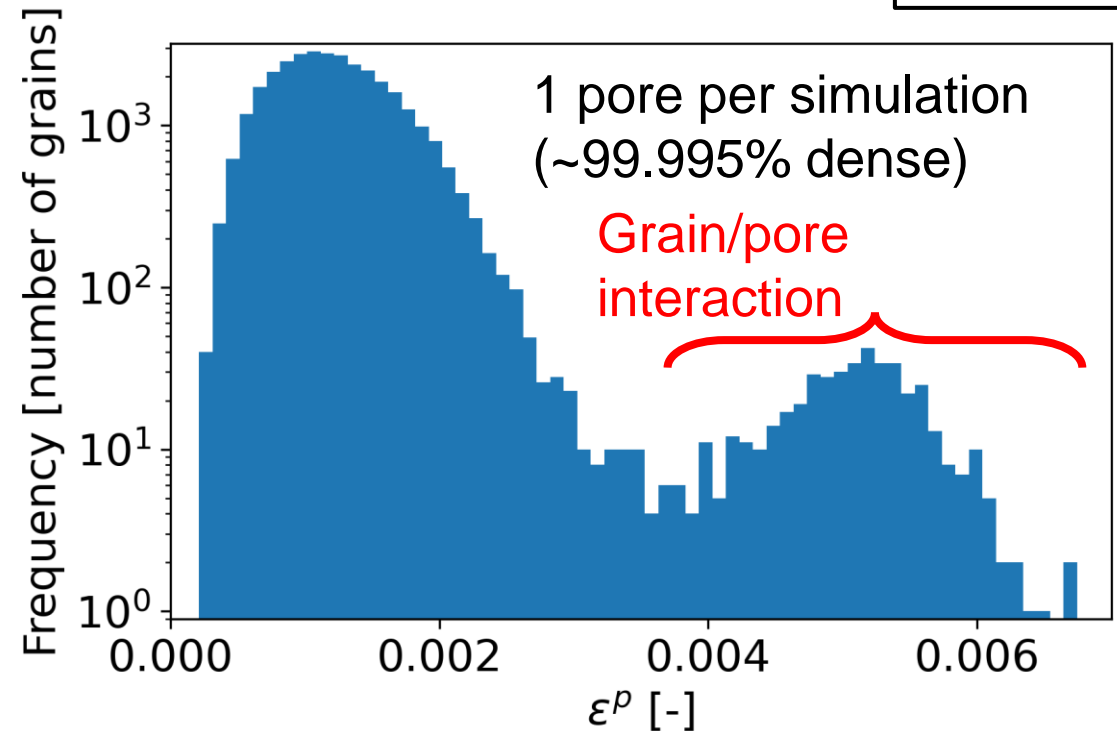
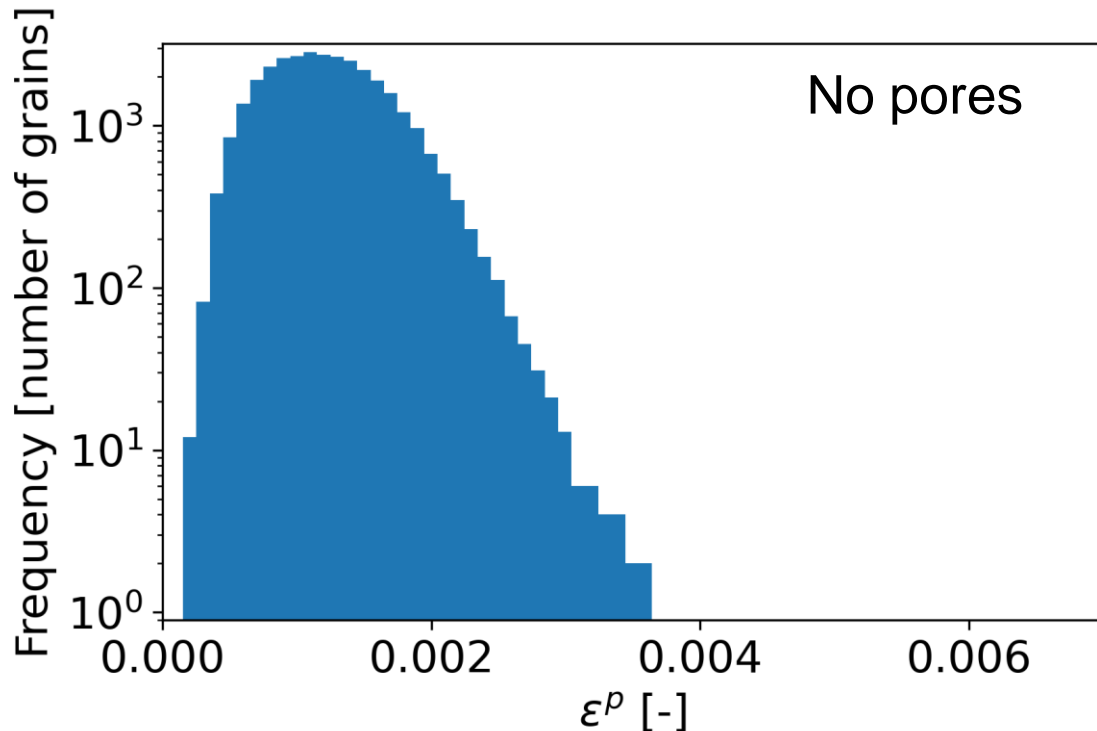
Microstructures with and without porosity

- 200 simulations with one 30- μm keyhole pore per simulation
- Overall distribution of plastic strain is similar
- **But extreme values are shifted!**
 - **Bimodal distribution starts to develop**

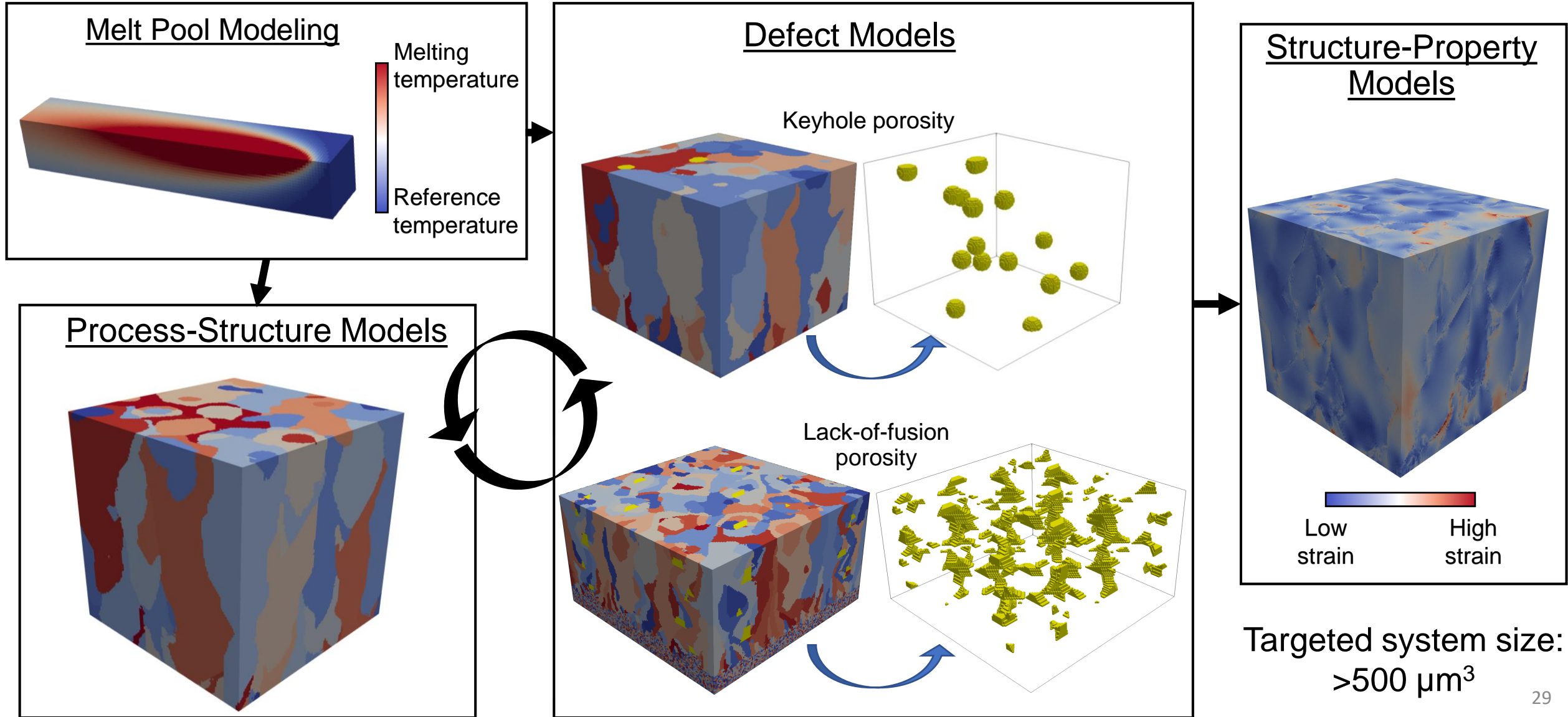
J.D. Pribe et al., 2023 [6]



Equivalent plastic strain for all grains across 200 simulations, log scale



PSP Models: Revisiting Our Complete Approach





Revisiting Initial Questions



With continued maturity, it is hoped that PSP models will support next-generation, computational-materials augmented qualification and certification approaches

Acknowledgements and References



This work was supported by the NASA Aeronautics Research Mission Directorate (ARMD) Transformational Tools and Technologies (TTT) project, and the NASA Langley Research Center Internal Research and Development Program

- [1] Rodgers, T.M. et al. "Simulation of powder bed metal additive manufacturing microstructures with coupled finite difference-Monte Carlo method," *Additive Manufacturing* 41 (2021): 101953
- [2] Pauza, J.G. et al., "Computer simulation of microstructure development in powder-bed additive manufacturing with crystallographic texture." *Modelling and Simulation in Materials Science and Engineering* 29.5 (2021): 055019
- [3] Richter, B. et al., "Integrated Monte Carlo microstructure and analytical temperature simulations of additive manufacturing," Additive Manufacturing Benchmark 2022 Conference (2022), Bethesda, MD
- [4] Gan, Z. et al., "Universal scaling laws of keyhole stability and porosity in 3D printing of metals," *Nature Communications* 12.1 (2021): 2379
- [5] Tang, M. et al., "Prediction of lack-of-fusion porosity for powder bed fusion," *Additive Manufacturing*, 14 (2017): 39-48
- [6] Pribe, J.D. et al., "A Process-Structure-Property Simulation Framework for Quantifying Uncertainty in Additive Manufacturing: Application to Fatigue in Ti-6Al-4V," *Integrating Materials and Manufacturing Innovation* (2023): 1-20.
- [7] Lebensohn, R.A. et al., "An elasto-viscoplastic formulation based on fast Fourier transforms for the prediction of micromechanical fields in polycrystalline materials," *International Journal of Plasticity* 32.33 (2012): 59-69
- [8] Gordon, J.V., "Defect structure process maps for laser powder bed fusion additive manufacturing," *Additive Manufacturing* 36 (2020): 101552

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J.D. Pribe et al., 2023 [6]





Structure-property: Crystal plasticity

- **Elasto-Viscoplastic Fast Fourier Transform (EVP-FFT) [7]**
- **Advantages**
 - Speed improvements over crystal plasticity finite element methods
 - Shares voxel-based microstructure representation with SPPARKS

Flow rule:
$$\dot{\boldsymbol{\varepsilon}}^p = \dot{\gamma}_0 \sum_{s=1}^{N_s} \mathbf{m}^s \left(\frac{|\mathbf{m}^s : \boldsymbol{\sigma}|}{\tau^s} \right)^n \text{sgn}(\mathbf{m}^s : \boldsymbol{\sigma})$$

Voce hardening:
$$\tau^s = \tau_0 + (\tau_1 + \theta_1 \Gamma) \left[1 - \exp\left(-\frac{\theta_0}{\tau_1} \Gamma\right) \right]$$

$$\Gamma = \sum_{s=1}^{N_s} \int \dot{\gamma}^s dt$$

Implicit time discretization:
$$\boldsymbol{\sigma} = \mathbf{C} : (\boldsymbol{\varepsilon}_{t+\Delta t} - \boldsymbol{\varepsilon}_t^p - \dot{\boldsymbol{\varepsilon}}^p_{t+\Delta t} \Delta t)$$

$\dot{\gamma}_0$: reference strain rate

n : viscoplastic exponent

$\dot{\boldsymbol{\varepsilon}}^p$: plastic strain rate tensor

$\boldsymbol{\sigma}$: stress tensor

\mathbf{m}^s : Schmid tensor for slip system s

τ^s : critical resolved shear stress for slip system s

$\dot{\gamma}^s$: plastic shear strain on slip system s

$\tau_0, \tau_1, \theta_0, \theta_1$: Voce hardening law parameters

Γ : accumulated slip on all slip systems

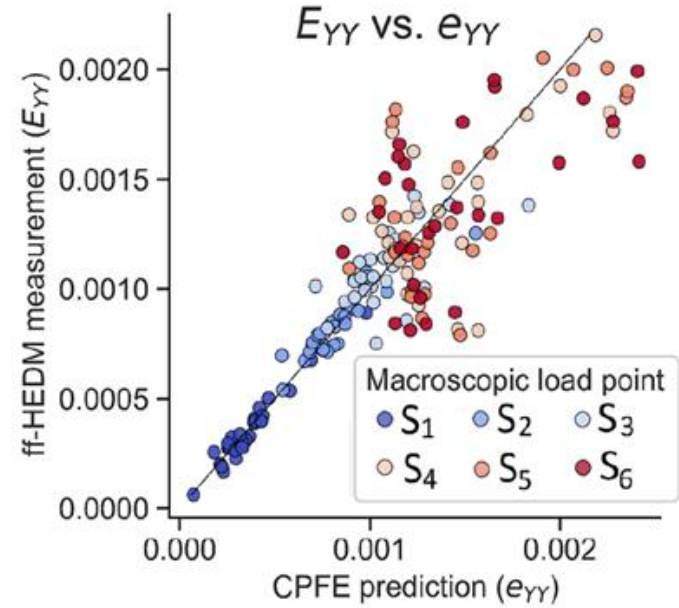
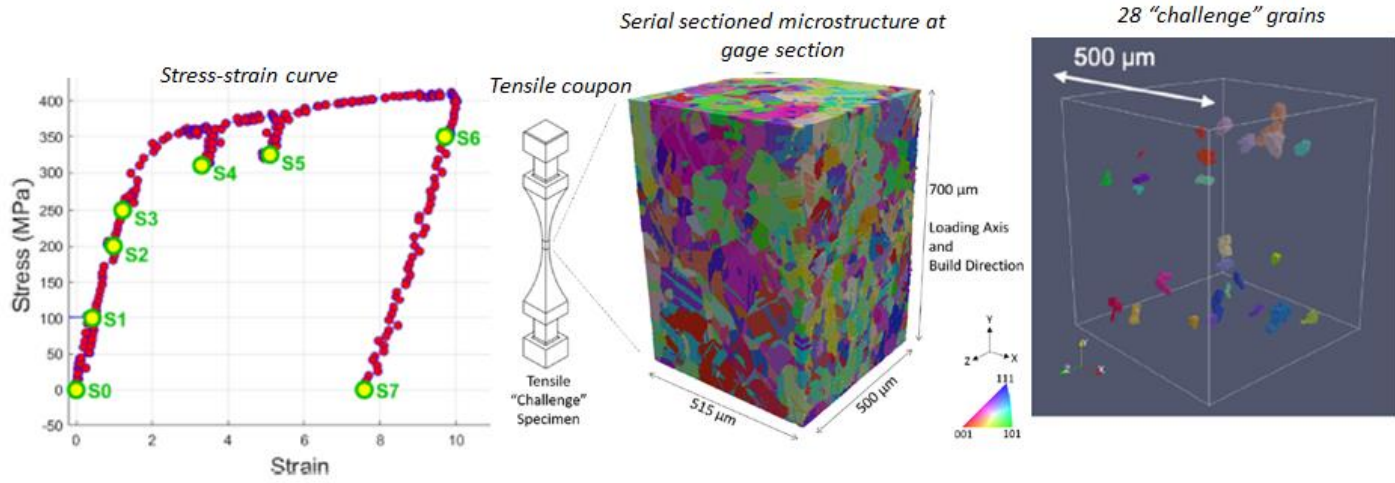
$t, \Delta t$: time, time step

\mathbf{C} : stiffness tensor

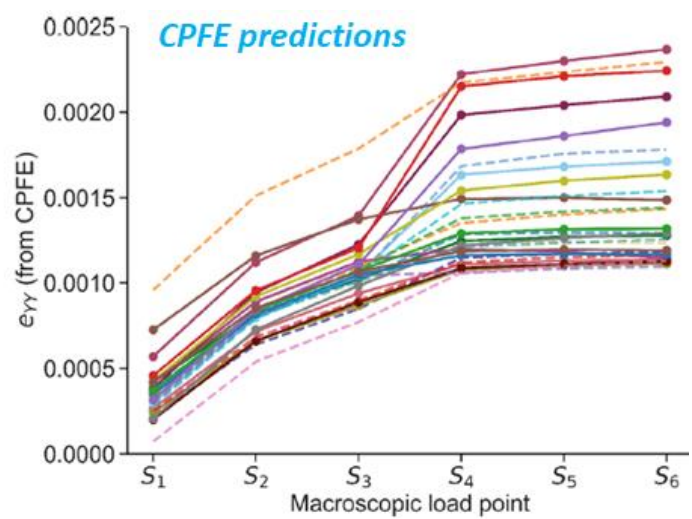
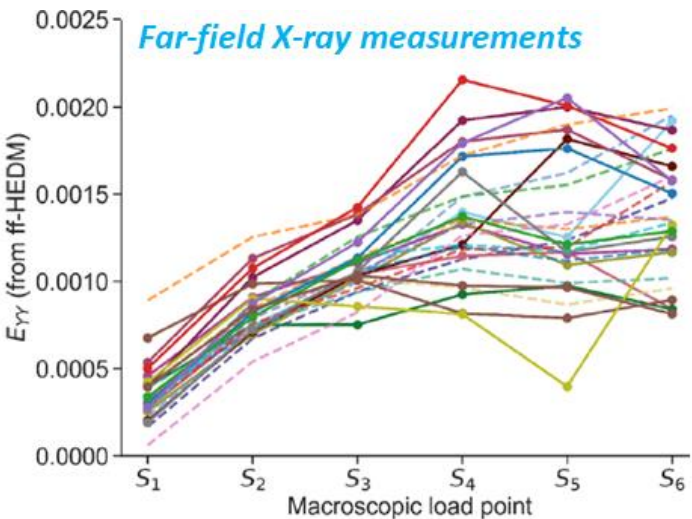
$\boldsymbol{\varepsilon}$: total strain tensor

$\boldsymbol{\varepsilon}^p$: plastic strain tensor

Structure-property: Validation



Challenge problem: Given the stress strain curve, serial-sectioned and reconstructed 3D microstructure, predict grain-average elastic strain tensor for 28 "challenge" grains at six different macroscopic load states, S1 through S6



Yeratapally, S. et al., "Effect of process-specific defects on the tensile and constant-amplitude fatigue behavior of as-built Ti-6Al-4V alloy produced by laser powder bed fusion process", Additive Manufacturing Benchmarks (AM-Bench), August 15-18, 2022, Bethesda, Maryland.