

Cryogenic Flow Boiling Parabolic Flight Experiment and Universal Correlations for Cryogenes

November 14, 2023

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Graduate Students

Issam Mudawar

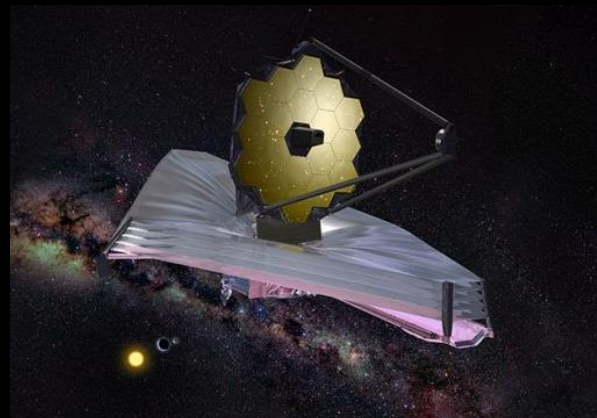
Betty Ruth & Milton B. Hollander Family Professor of Mechanical Engineering

Purdue University Boiling & Two-Phase Flow Laboratory (PU-BTPFL)
Mechanical Engineering Building, 585 Purdue Mall
West Lafayette, IN 47907

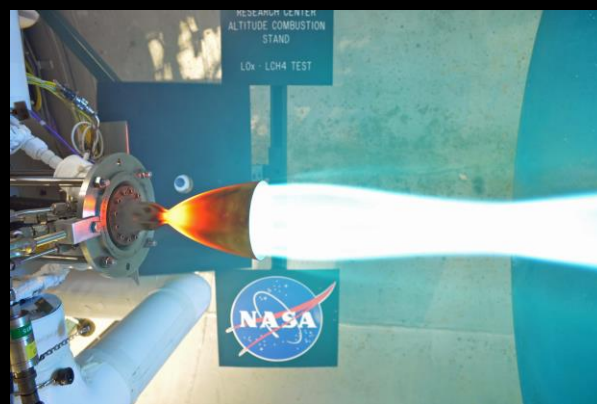
Jason Hartwig

Research Aerospace Engineer

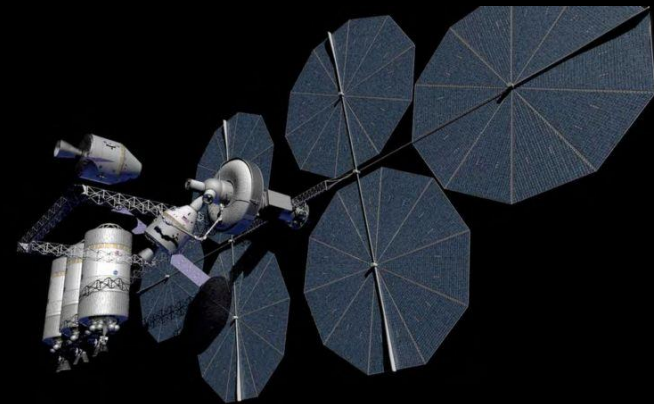
NASA Glenn Research Center, Fluids and Cryogenics Branch
21000 Brookpark Road
Cleveland, OH 44135



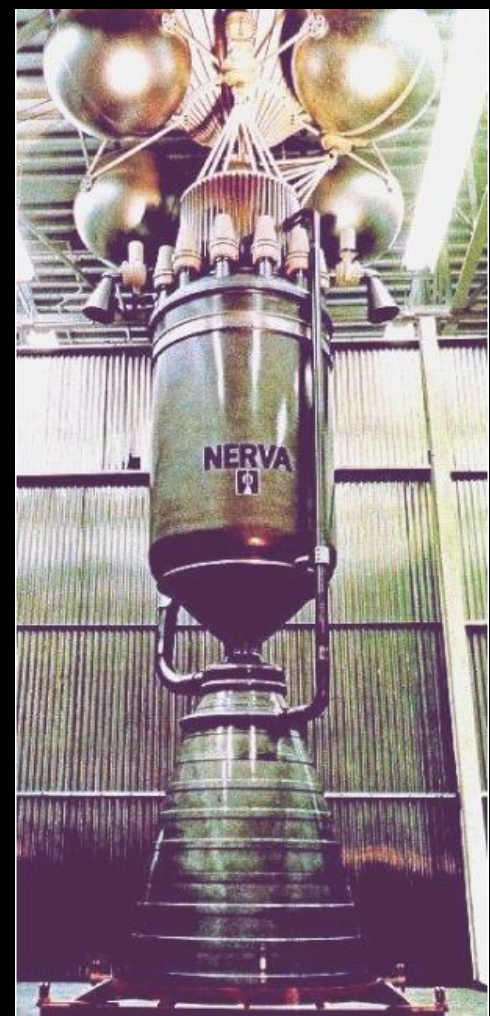
James Webb
Space Telescope
(LHe)



Propulsion and Cryogenics
Advanced Development
(PCAD) Project
(LOX/LCH₄)

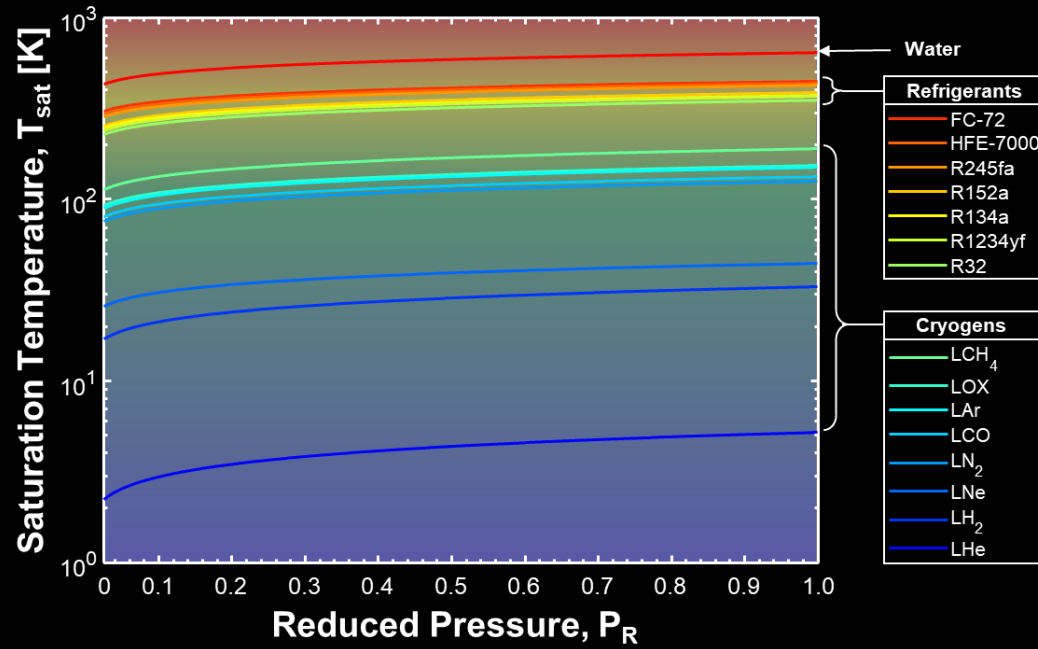


Orbital Refueling

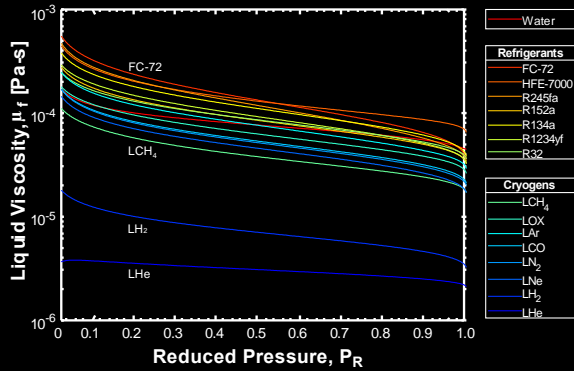


Nuclear Thermal
Propulsion Systems
(LH₂)

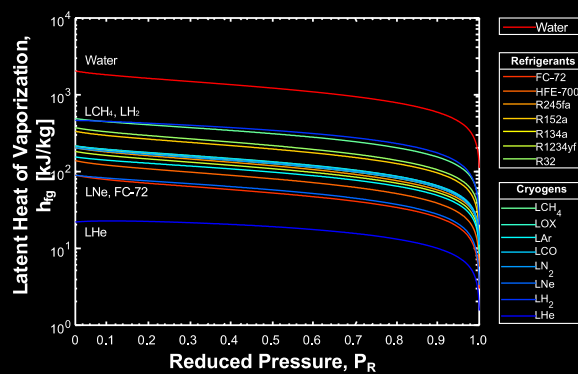
Very low saturation temperature



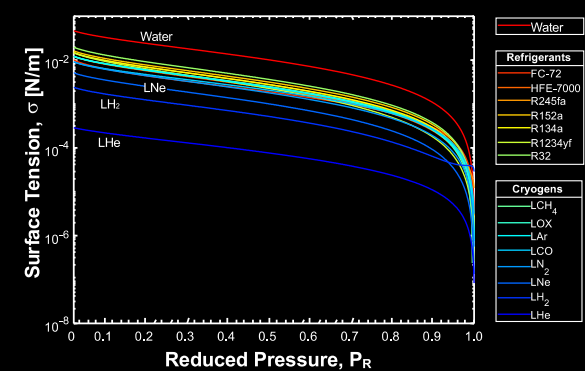
Low liquid viscosity



Low latent heat of vaporization



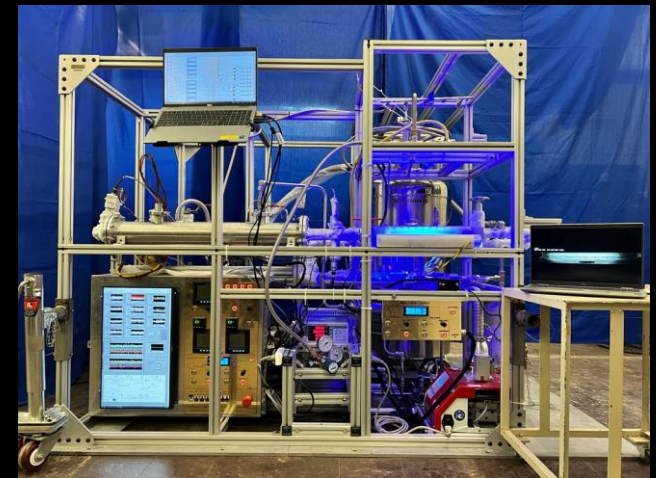
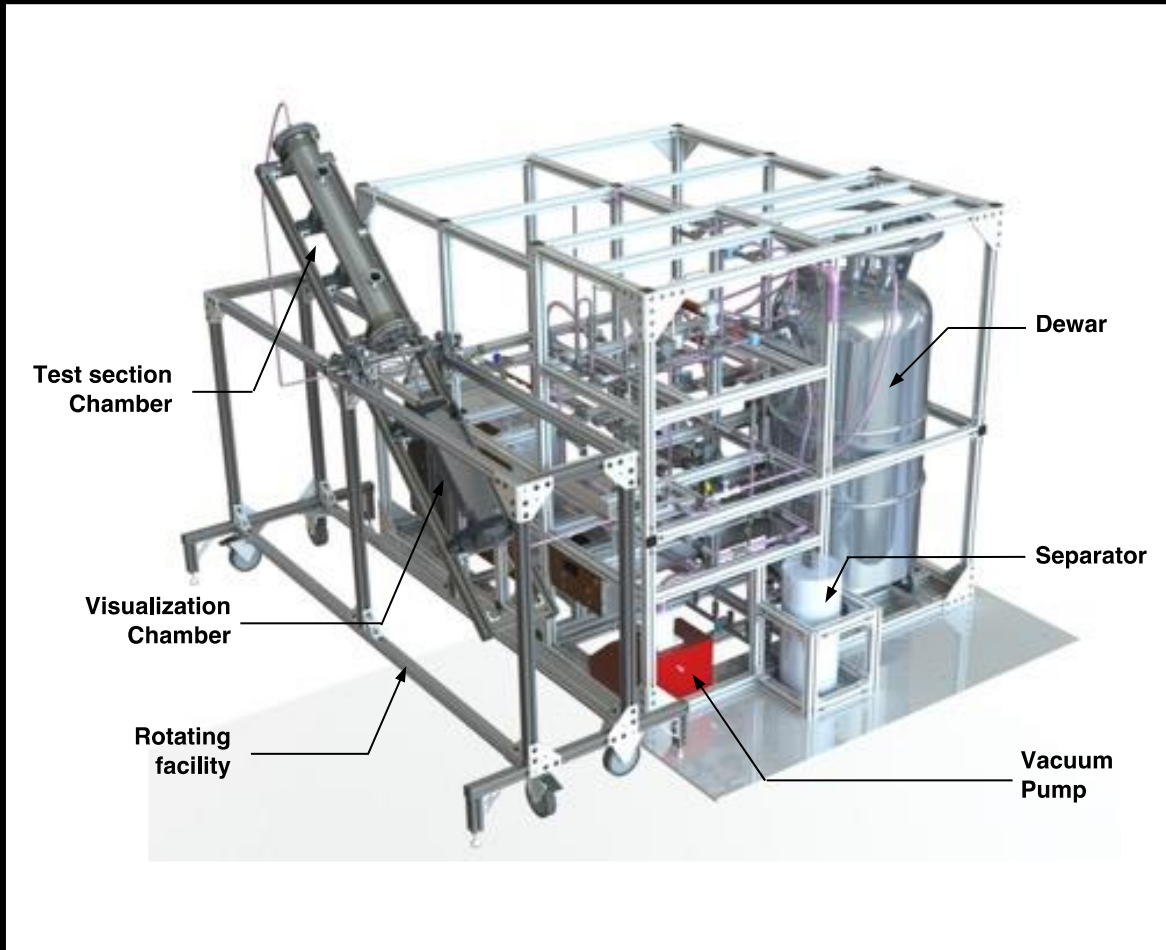
Low surface tension



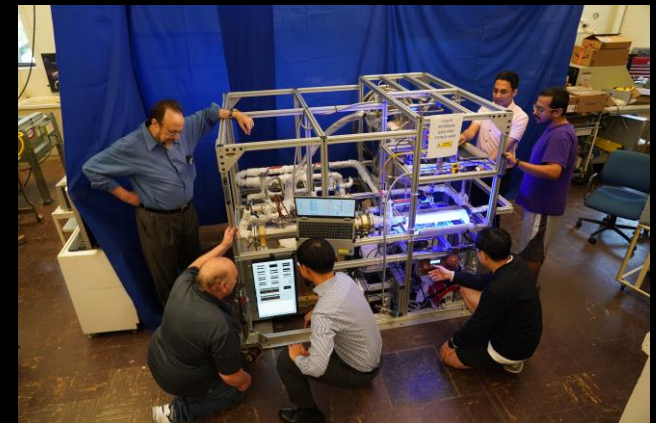
PU-BTPFL Cryo Projects

PU-BTPFL CRYO Projects		
#	Project Title	Project Duration
1.	Cryo Heated tube flow boiling I → <i>Parabolic flight (5 flight days)</i>	<i>Jan. 2021 – Jan. 2023</i>
2.	Cryo Heated tube flow boiling II → <i>Flight Extension (4 flight days)</i>	<i>Oct. 2023 – Oct. 2024</i>
3.	Cryo Pool boiling → <i>Ground Exp.</i>	<i>June. 2023 – Nov. 2023</i>
4.	Cryo Spray cooling → <i>Ground Exp.</i>	<i>Mar. 2023 – Mar. 2025</i>
5.	Cryo Spray cooling – Flight Exp → <i>Parabolic flight (5 flight days)</i>	<i>Mar. 2023 – Mar. 2025</i>

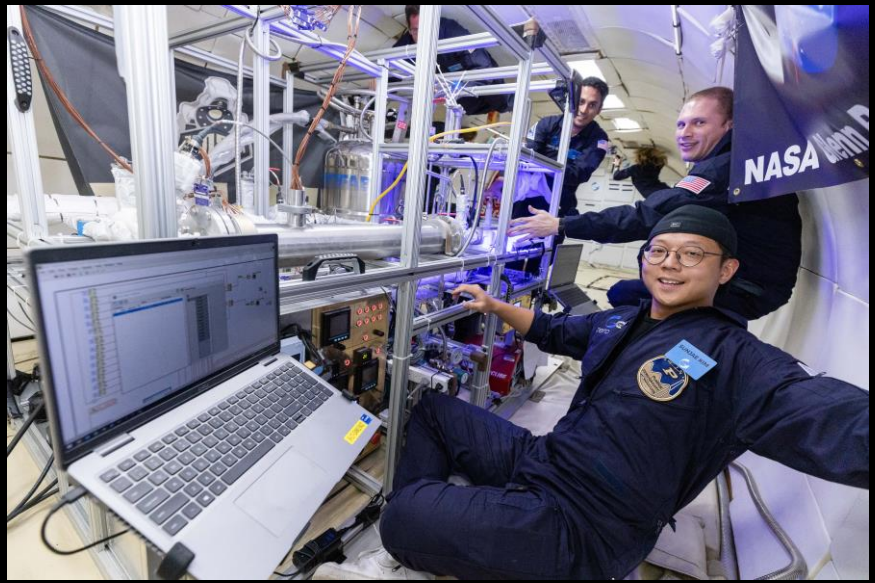
CAD of Test Rig with Rotating Platform



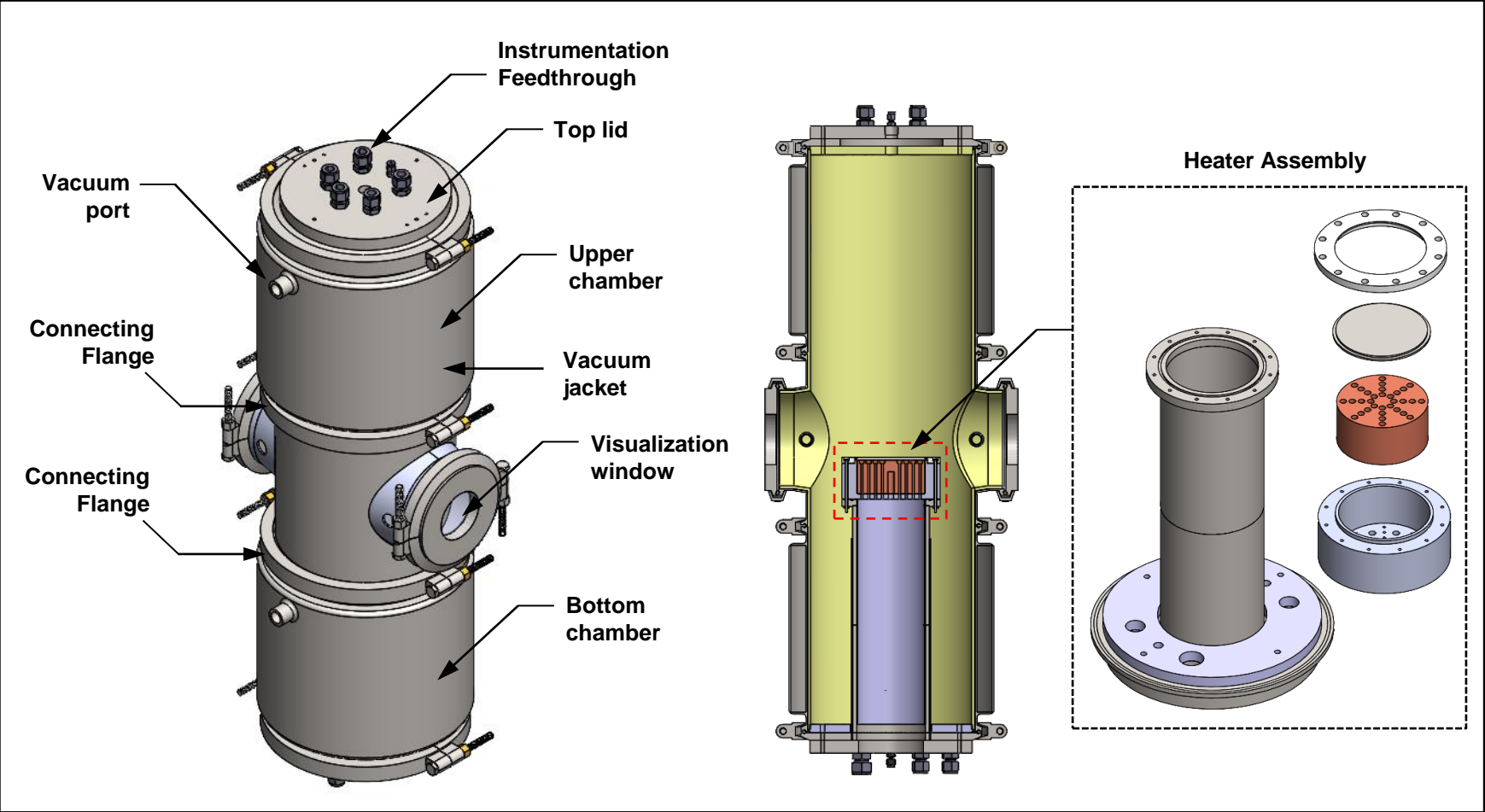
Constructed Flight Rig







Pressure Chamber Design

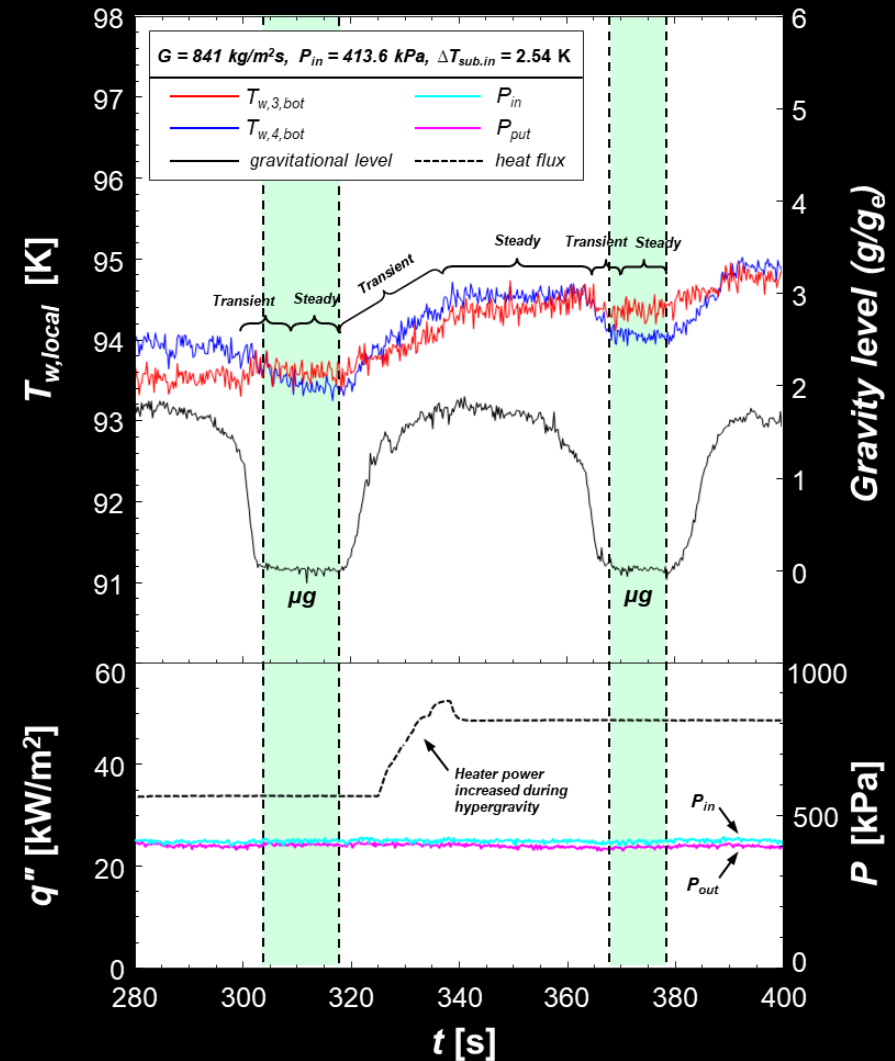
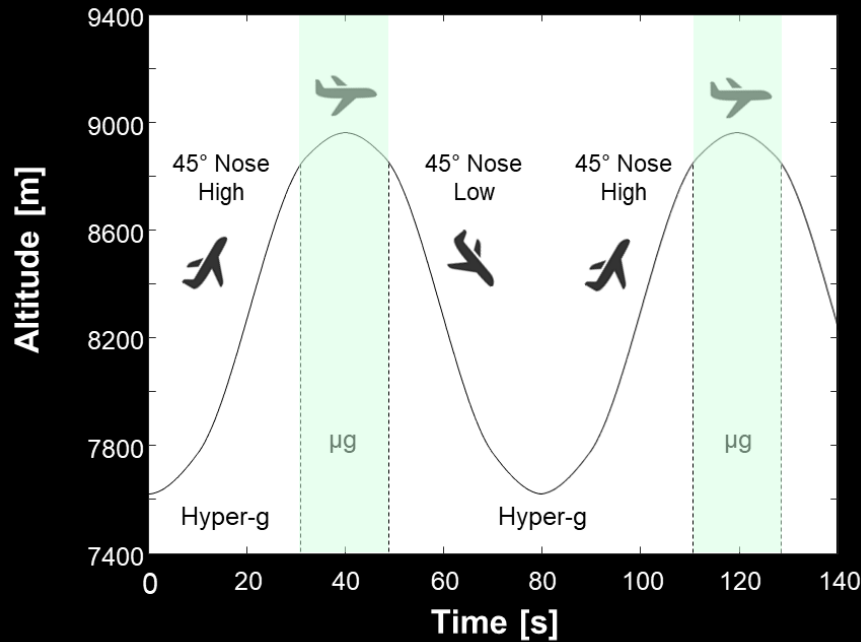


Experimental Results

1. Microgravity LN₂ Flow Boiling

Transient dynamics of measured parameters

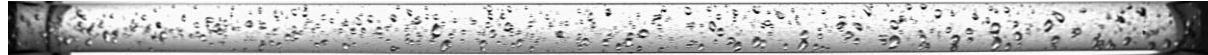
Parabolic flight projectile



$G = 400 \text{ kg/m}^2\text{s}$, $P_{in} = 689.5 \text{ kPa}$, $\Delta T_{sub,in} = 5.39 \text{ K}$, CHF = N/A

q'' [kW/m²]

2.76



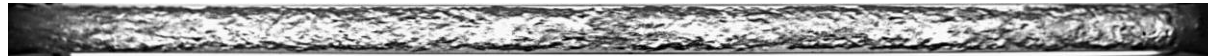
4.21



5.59



11.26



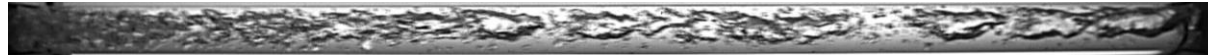
$G = 743 \text{ kg/m}^2\text{s}$, $P_{in} = 482.6 \text{ kPa}$, $\Delta T_{sub,in} = 3.61 \text{ K}$, CHF = N/A

q'' [kW/m²]

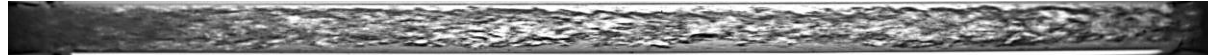
8.46



16.83



28.11



44.78



61.58



$G = 1322 \text{ kg/m}^2\text{s}$, $P_{in} = 620.5 \text{ kPa}$, $\Delta T_{sub,in} = 4.62 \text{ K}$, CHF = N/A

q'' [kW/m²]

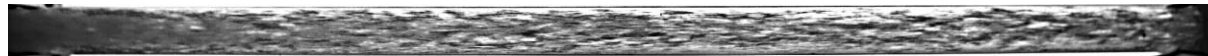
17.53



28.09



38.73



50.02



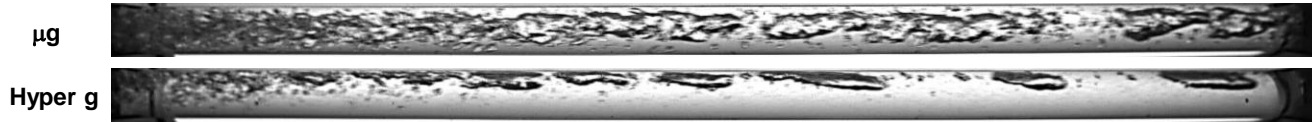
67.36



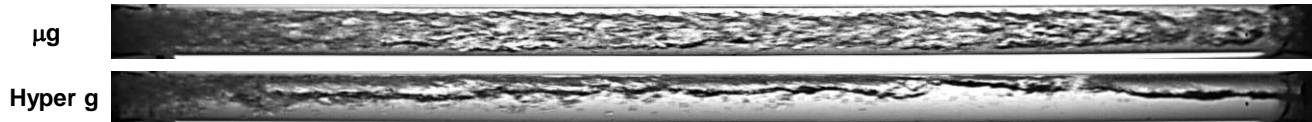
Effect of gravity on interfacial flow pattern

$G = 743 \text{ kg/m}^2\text{s}$, $P_{in} = 482.6 \text{ kPa}$, $\Delta T_{sub,in} = 3.61 \text{ K}$, $CHF = \text{N/A}$

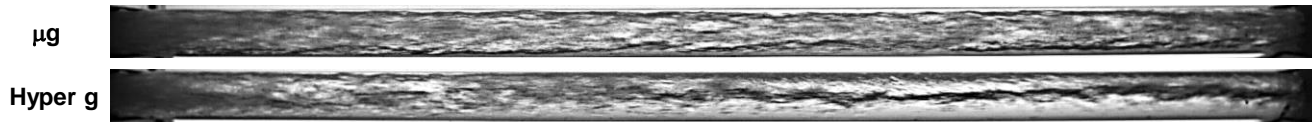
$q'' = 16.83 \text{ kW/m}^2$



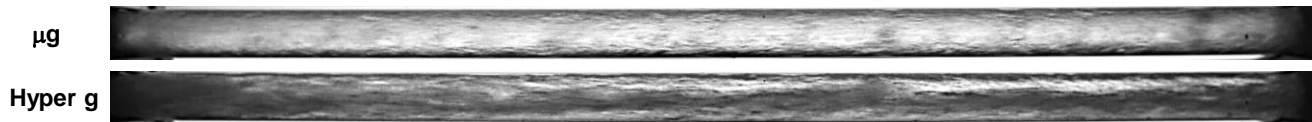
$q'' = 28.11 \text{ kW/m}^2$



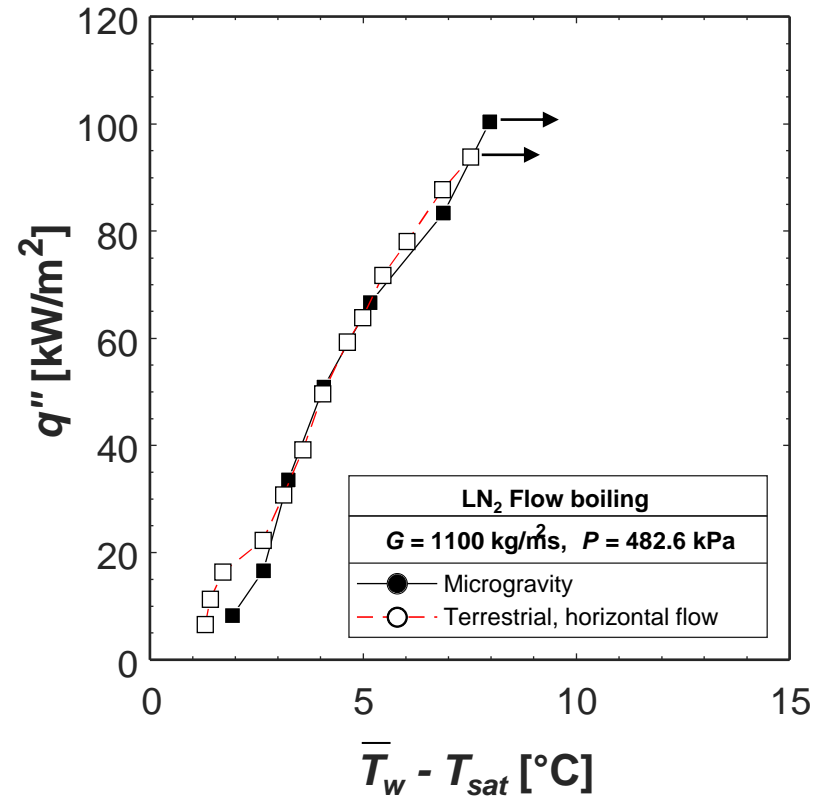
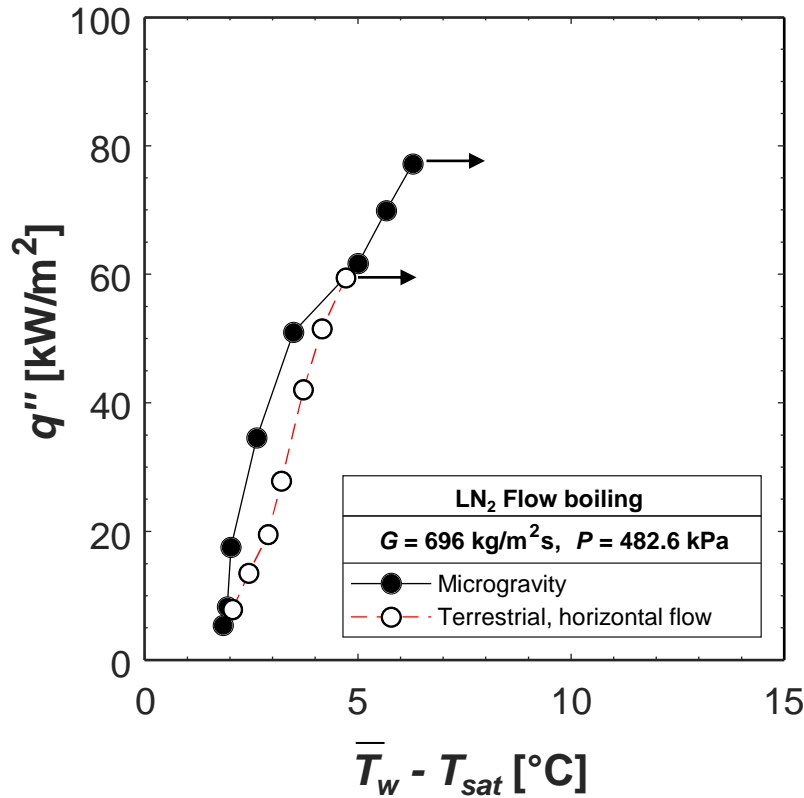
$q'' = 44.78 \text{ kW/m}^2$



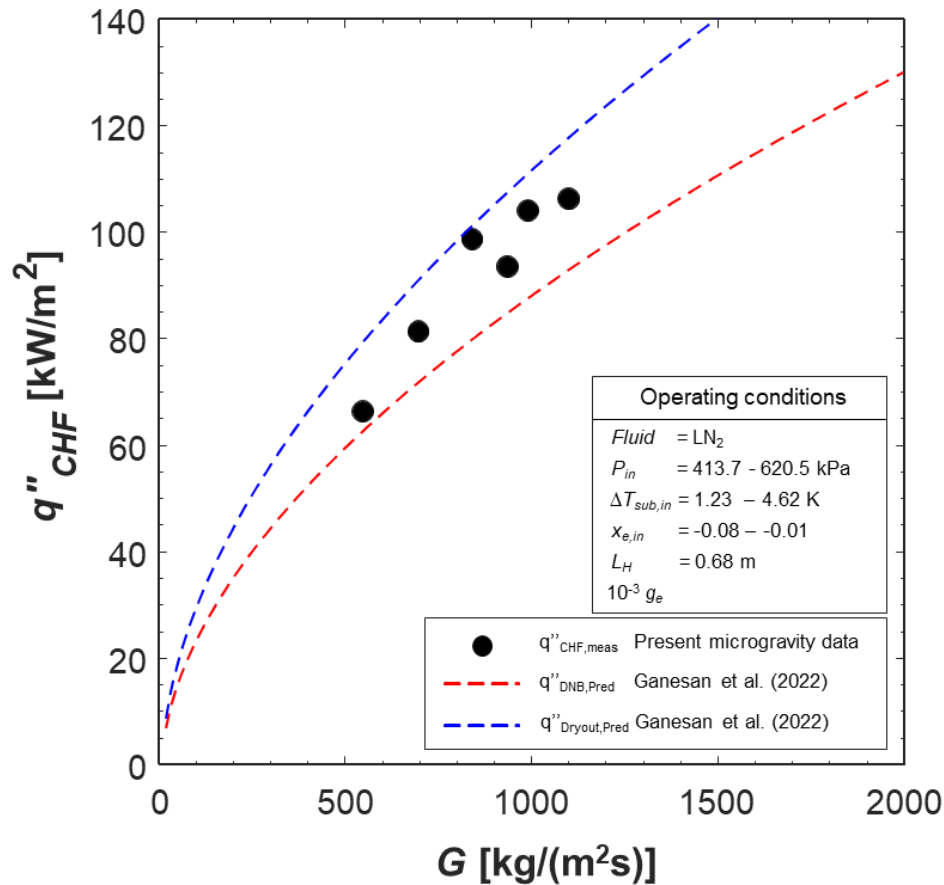
$q'' = 61.58 \text{ kW/m}^2$



Effect of gravity on boiling curve



- Lower wall superheat in low heat flux range in microgravity due to flow symmetry
- Merging of boiling curves at high mass velocity due to dominating effect of flow inertia over gravity
- Larger CHF in microgravity compared to 1- g_e horizontal flow; due to symmetrical flow pattern in μg



Measured μg CHF

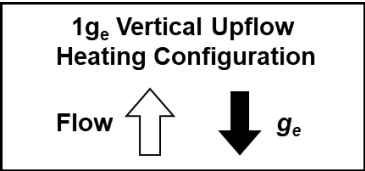
- CHF Mechanism : annular liquid dryout
- CHF increases with G
- CHF tend to level-off as G increases
- Requires more μg CHF for high G

Predictions by CHF correlations

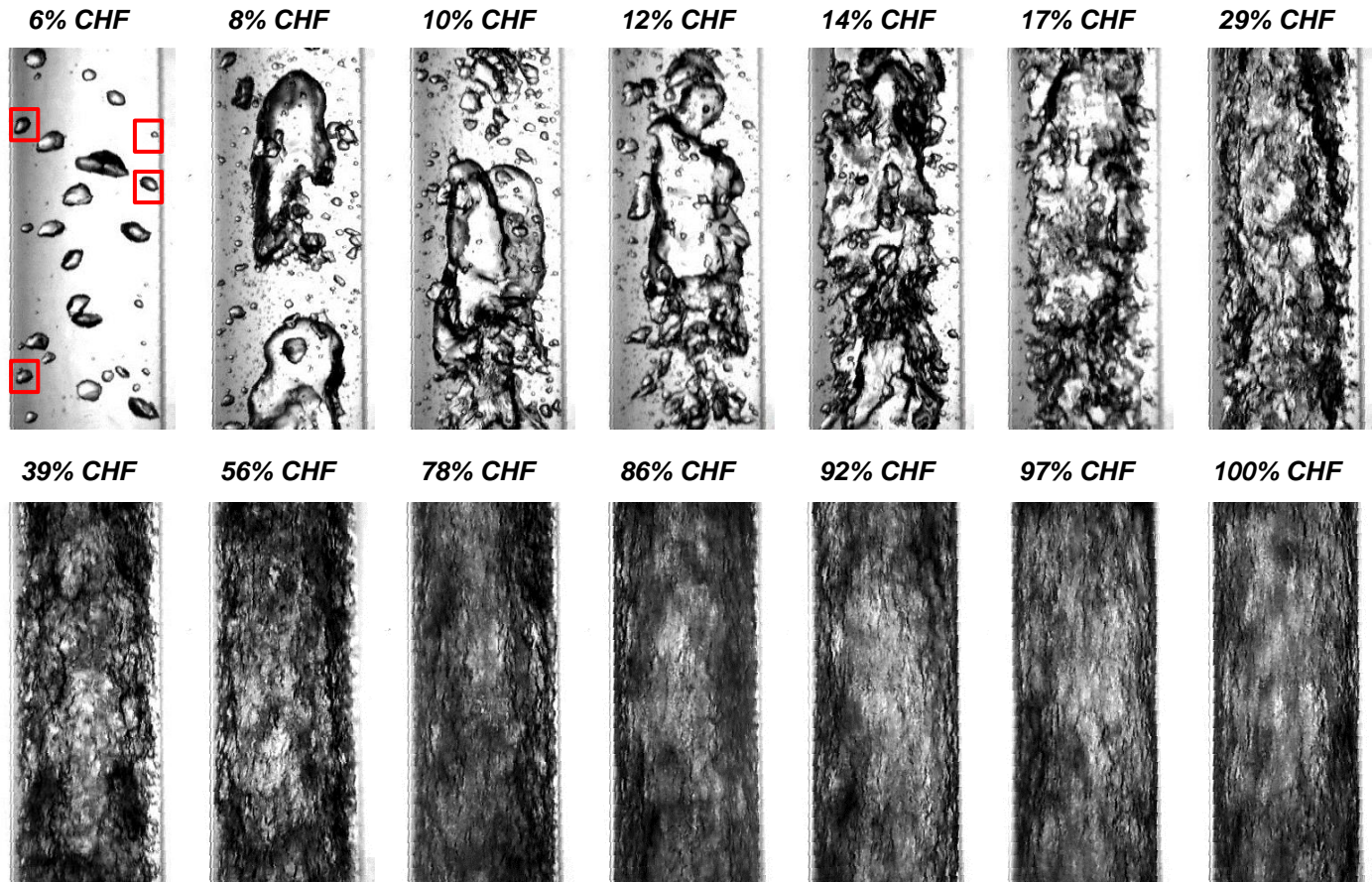
- CHF correlation by Ganesan et al. (2022)
- Dryout & DNB correlations
- μg CHF is predicted with decent accuracy

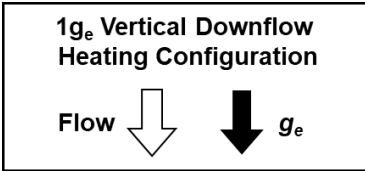
Experimental Results

2. Terrestrial LN₂ Flow Boiling

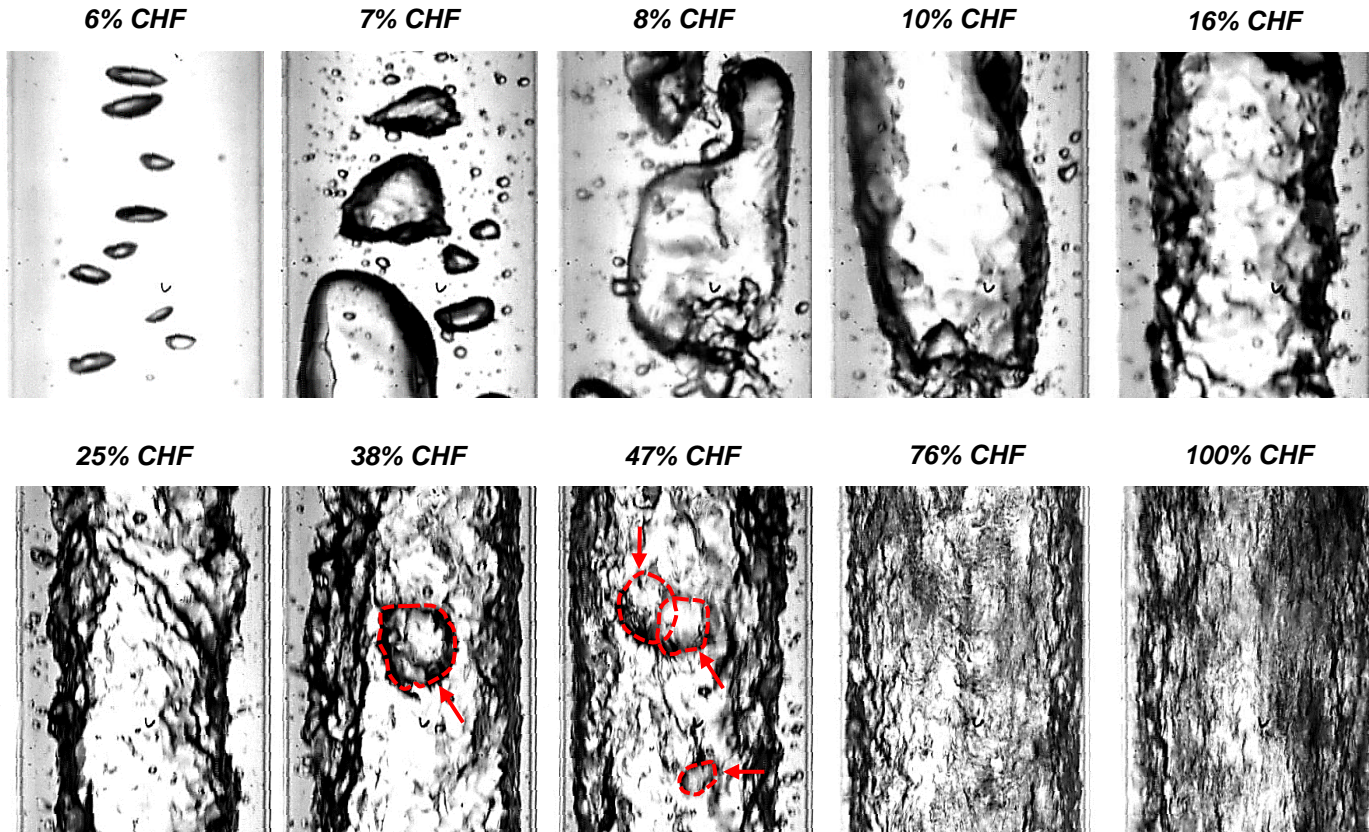


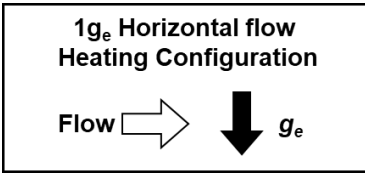
$G = 576.8 \text{ kg/m}^2\text{s}$, $P_{in} = 628.8 \text{ kPa}$, $\Delta T_{sub.in} = 2.28 \text{ K}$, $CHF = 99.58 \text{ kW/m}^2$



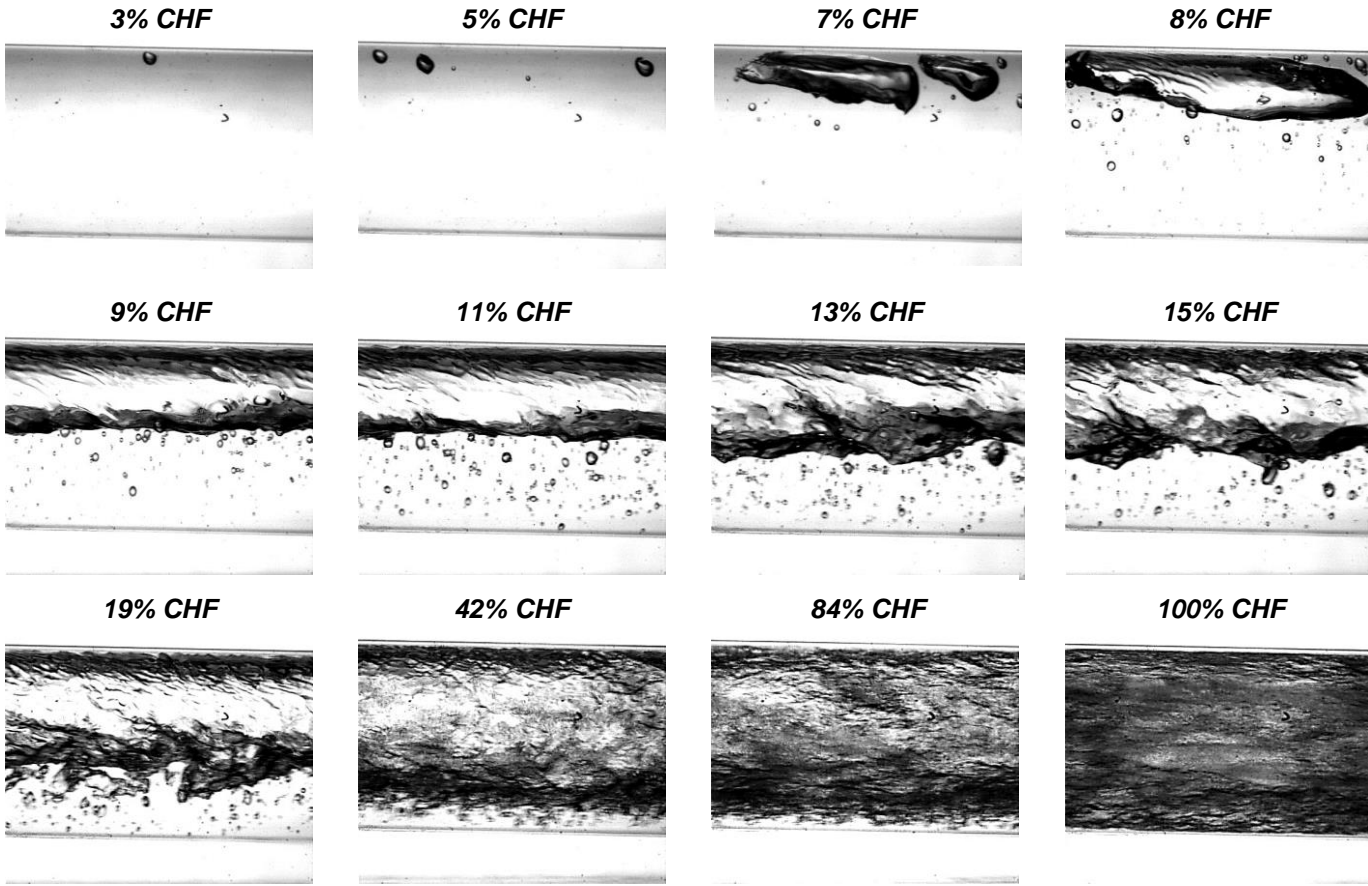


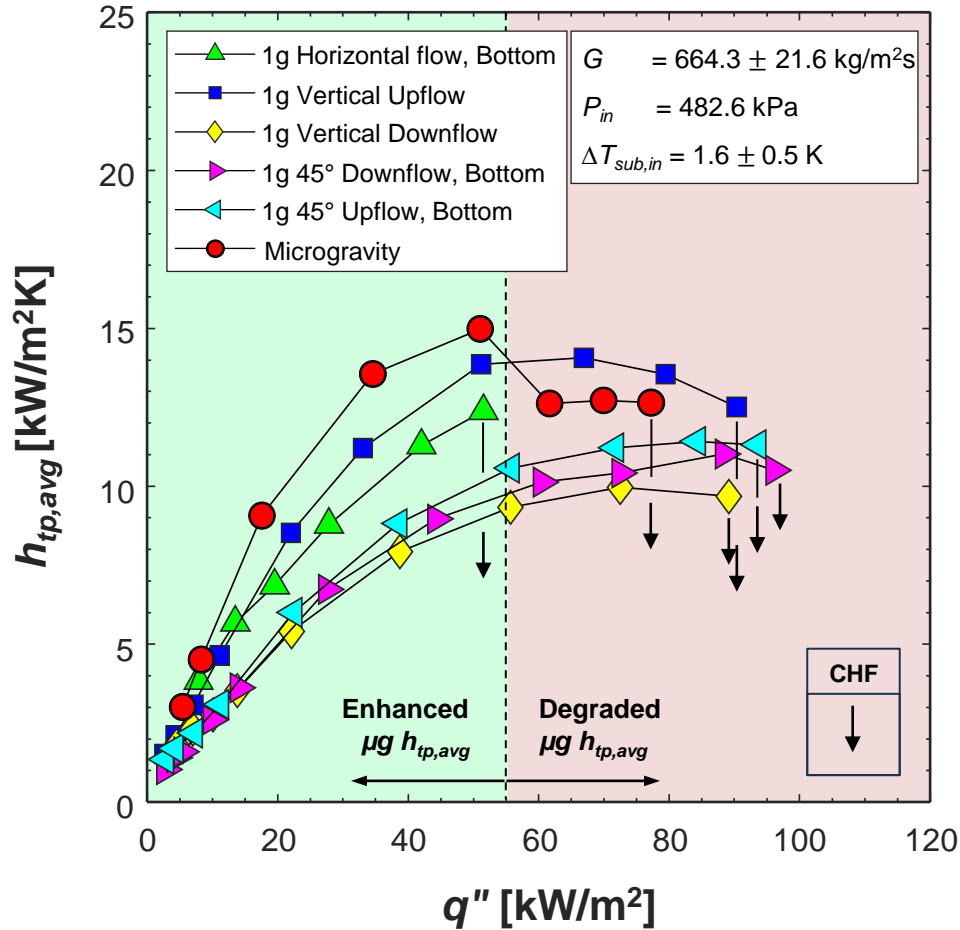
$G = 511.1 \text{ kg/m}^2\text{s}$, $P_{in} = 458.5 \text{ kPa}$, $\Delta T_{sub.in} = 0.95 \text{ K}$, $CHF = 87.75 \text{ kW/m}^2$





$G = 544.9 \text{ kg/m}^2\text{s}$, $P_{in} = 356.6 \text{ kPa}$, $\Delta T_{sub.in} = 1.89 \text{ K}$, $CHF = 91.67 \text{ kW/m}^2$





$$h_{nb} = h_{pb} * S$$

$$h_{pb} = f(q'') : \text{As } q'' \uparrow h_{pb} \uparrow$$

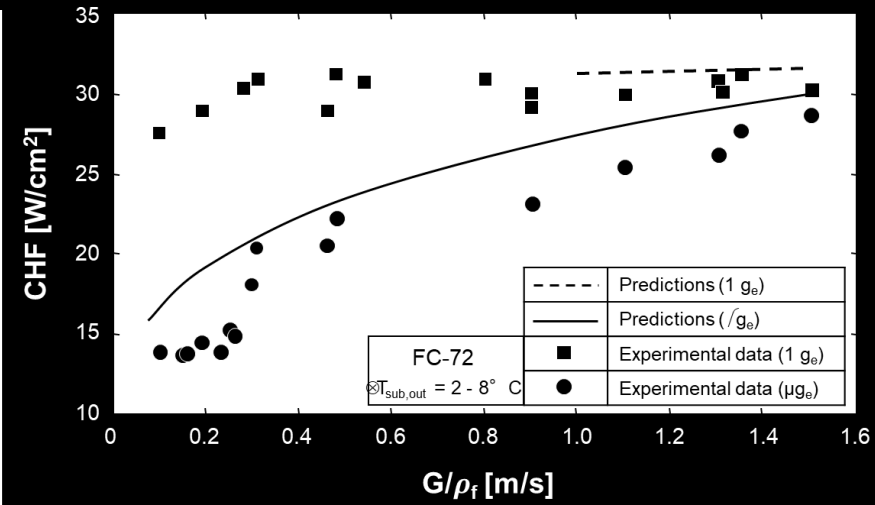
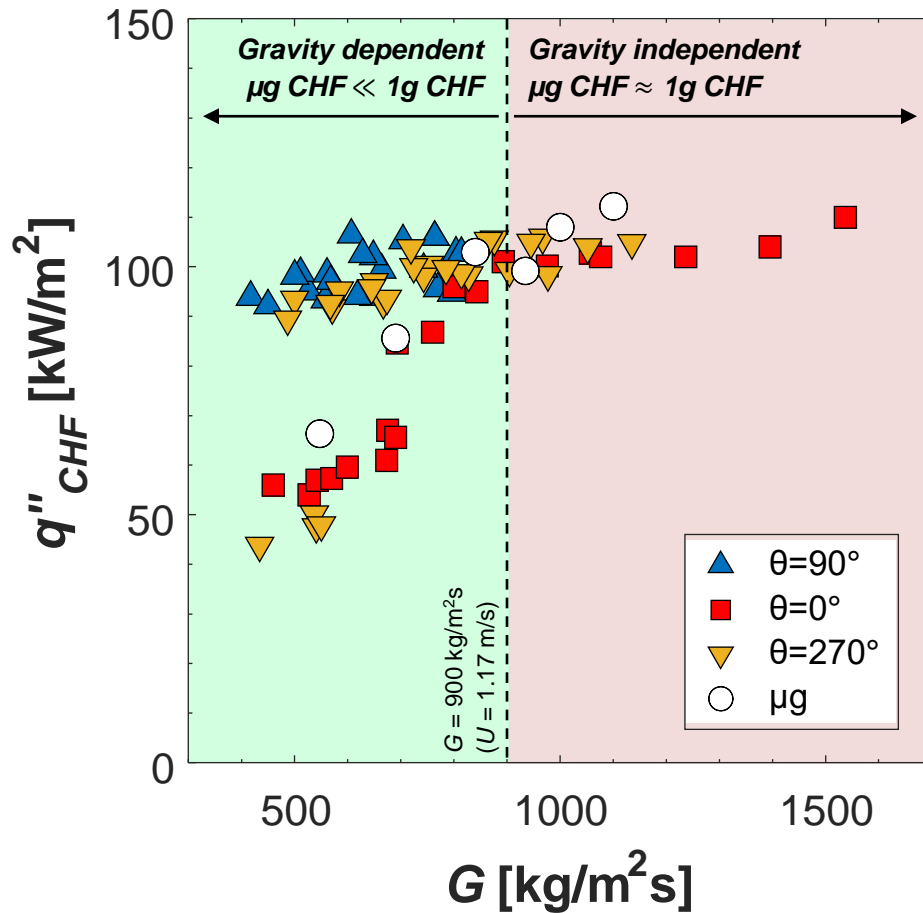
$$S = f(G, x_e) : \text{As } q'' \uparrow x_e \uparrow S \uparrow$$

HTC trend by flow orientation

- $\mu g > \text{vertical up} > \text{horizontal} > \text{vertical down}$
- 45 inclined orientations very similar to each other

HTC trend by q''

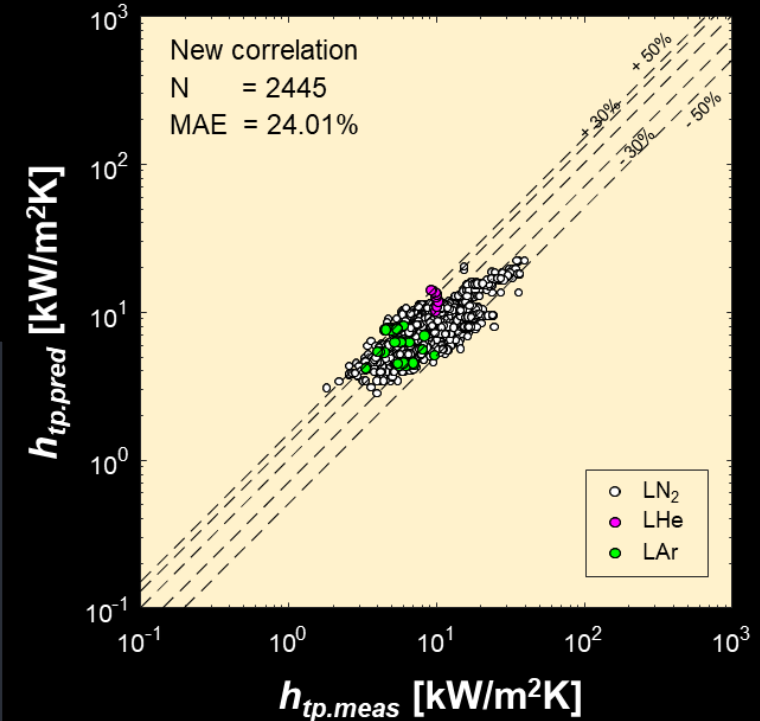
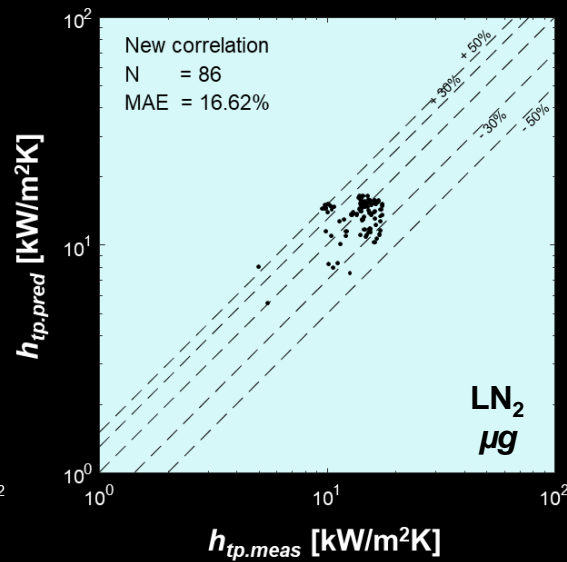
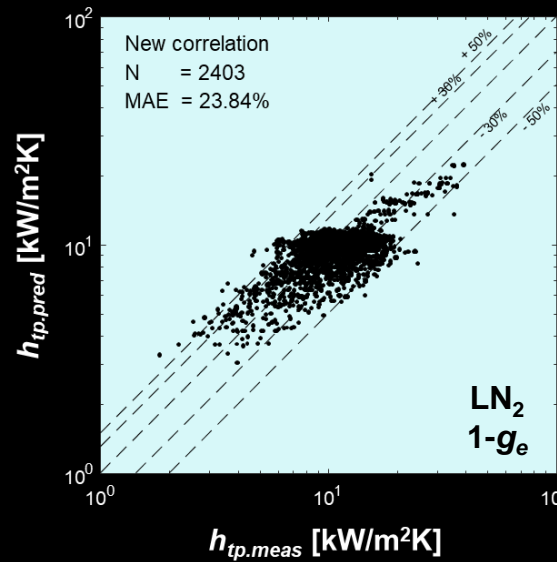
- Steep increase of HTC from low q'' to medium q''
 - *Nucleate Boiling Dominant*
 - *PDB to FDB to Saturated Boiling*
- Sustaining HTC over high q'' range
 - *Suppression of N.B.*
 - *Aggressive bubble departure leading to increased mixing and turbulence effect causing decreased wall superheat*



CHF trend

- Increasing CHF with increasing G
 - Effect of flow inertia
 - Stagnation at high G
- Body force effect on CHF
 - Microgravity CHF \ll 1g vertical upflow CHF
 - Microgravity CHF \approx 1g horizontal CHF
 - Stronger gravity influence at low G
 - Gravity independent at G higher than $900 \text{ kg/m}^2\text{s}$

Universal Correlations



IF $PR < 0.41$

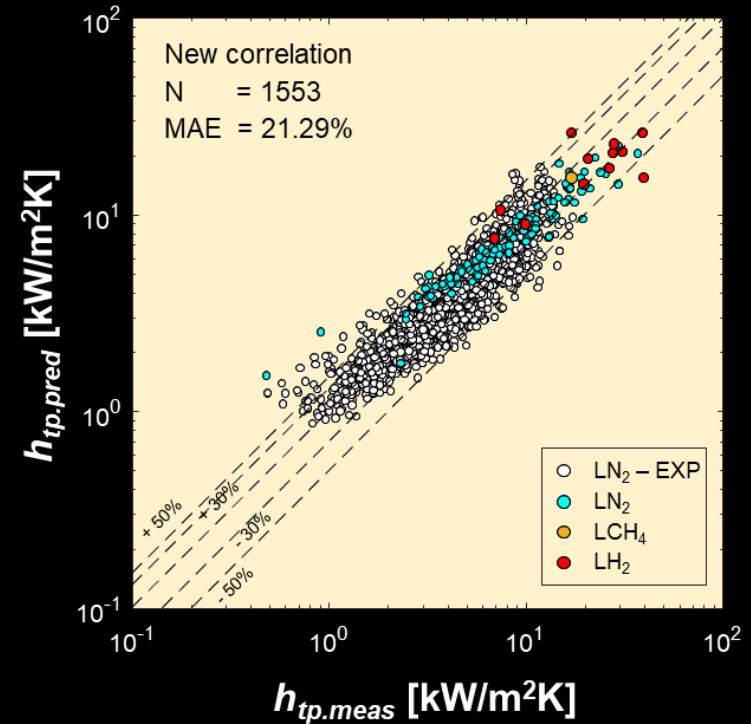
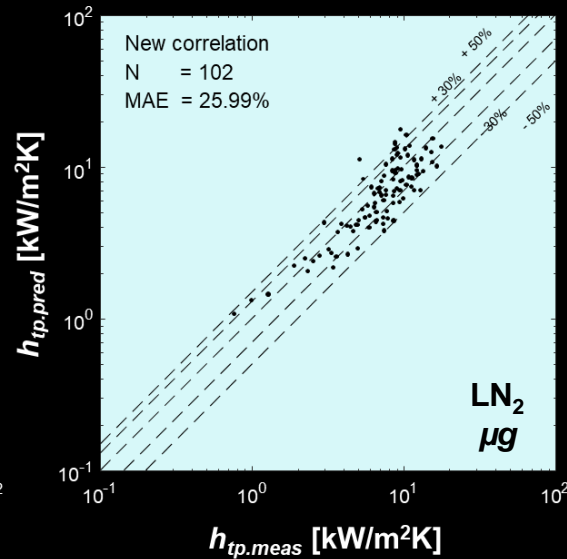
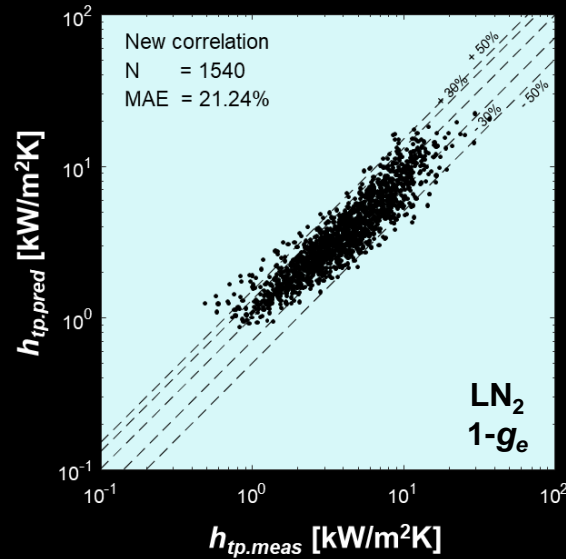
$$h_{NB} = h_{PB} \cdot \left[1.36 \cdot \tanh\left(\frac{g_e}{g}\right) \right] \cdot \left[\frac{1}{1 + 10^3 \cdot \exp(Bo^2 We)} \right]^{0.475}$$

IF $PR \geq 0.41$

$$h_{NB} = h_{PB} \cdot \left[1.2 \cdot \tanh\left(\frac{g_e}{g}\right) \right]$$

$$h_{CB} = h_{sp} \cdot 7 \cdot \left(\frac{1}{X_{tt}}\right)^{0.39} \cdot \left(\frac{\rho_f}{\rho_g}\right)^{-0.34}$$

$$h_{tp} = [h_{NB}^2 + h_{CB}^2]^{1/2}$$



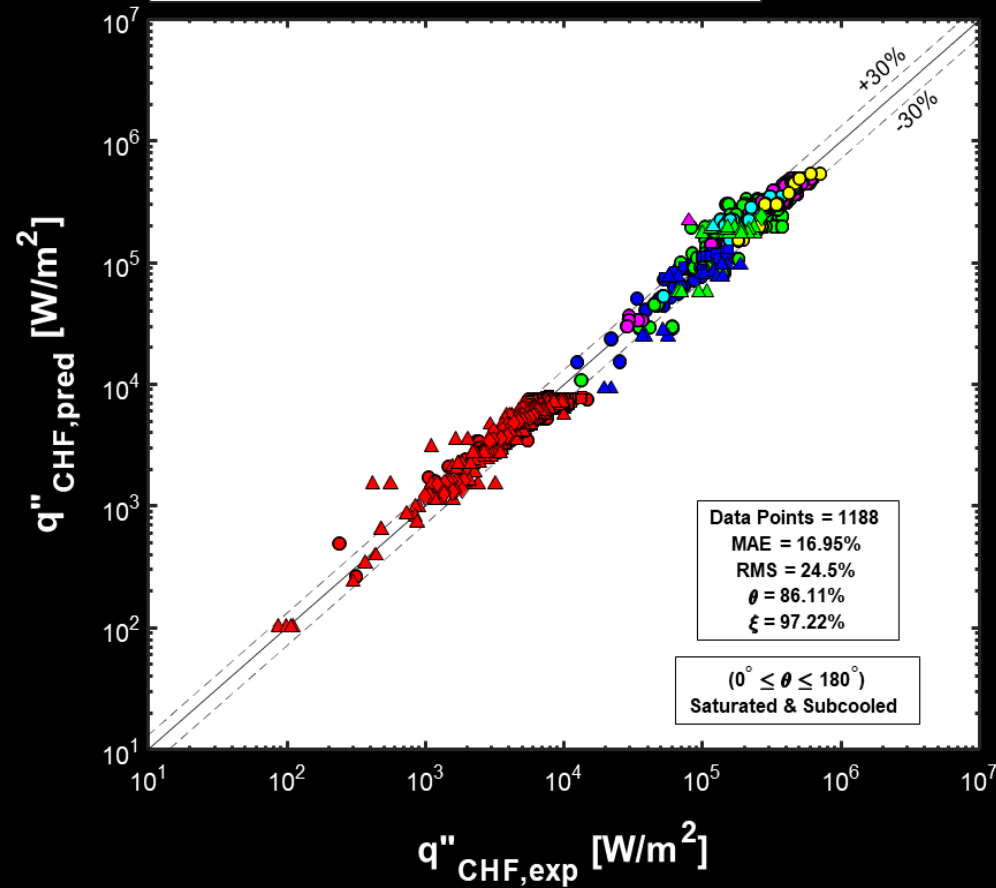
$$\frac{h_{tp}}{h_{sp}} = 6.58Bo^{0.68}(0.1 + Ja^{**})^{-1.3} \left(\frac{\rho_g}{\rho_f}\right)^{-0.4} Pr_f^{0.46} \left(\frac{\bar{M}_{LN_2}}{\bar{M}}\right)^{0.42}$$

$$h_{sp} = \frac{(4f_{sp}/8)(Re_{f0,D} - 1000)Pr_f}{1 + 12.7(4f_{sp}/8)^{0.5}(Pr_f^{2/3} - 1)} \cdot \left(\frac{k_f}{D}\right)$$

↑
Gnielinski correlation

$$q''_{CHF} = \left[0.16 - 0.104 \left(\frac{P}{P_c} \right)^{10} \right] \times \left[1 - 0.004 \left(\frac{P}{P_c} \right) \theta \right] \left| \cos \left(\left(\frac{88}{180} \theta \right) \right) \right|^{0.364} \times \left[1 + 0.16 \left(\frac{c_{p,f} \Delta T_{sub}}{h_{fg}} \right) \right] \times \left[\rho_g h_{fg} \left(\frac{\sigma(\rho_f - \rho_g)}{\rho_g^2} \right)^{0.25} \right]$$

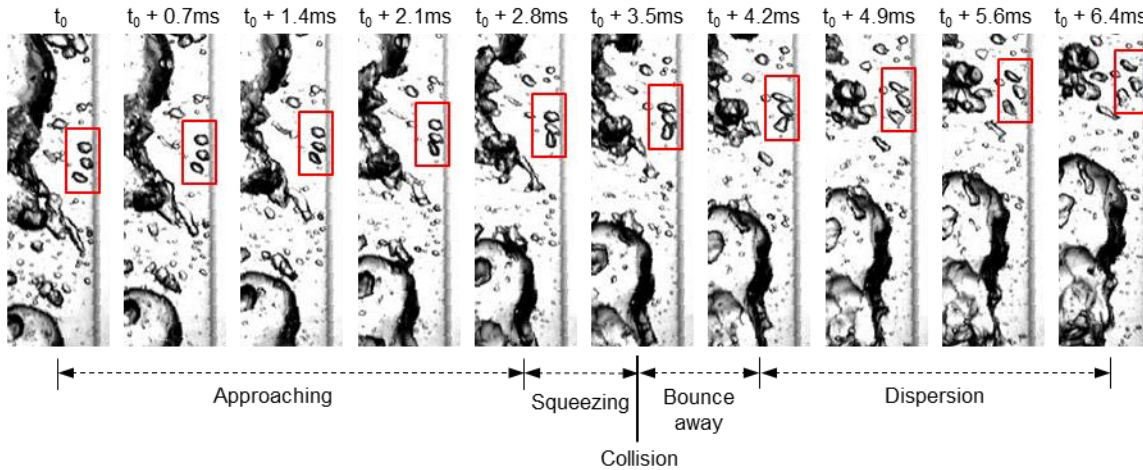
- LHe I ($\Delta T_{sub} = 0 \text{ K} \ \& \ \theta = 0^\circ$) ▲ LHe I ($\Delta T_{sub} = 0 \text{ K} \ \& \ 0 < \theta \leq 180^\circ$)
- LH₂ ($\Delta T_{sub} = 0 \text{ K} \ \& \ \theta = 0^\circ$) ▲ LH₂ ($\Delta T_{sub} = 0 \text{ K} \ \& \ 0 < \theta \leq 180^\circ$)
- LN₂ ($\Delta T_{sub} = 0 \text{ K} \ \& \ \theta = 0^\circ$) ▲ LN₂ ($\Delta T_{sub} = 0 \text{ K} \ \& \ 0 < \theta \leq 180^\circ$)
- LO₂ ($\Delta T_{sub} = 0 \text{ K} \ \& \ \theta = 0^\circ$) ▲ LO₂ ($\Delta T_{sub} = 0 \text{ K} \ \& \ 0 < \theta \leq 180^\circ$)
- LAr ($\Delta T_{sub} = 0 \text{ K} \ \& \ \theta = 0^\circ$) ▲ LAr ($\Delta T_{sub} = 0 \text{ K} \ \& \ 0 < \theta \leq 180^\circ$)
- LCH₄ ($\Delta T_{sub} = 0 \text{ K} \ \& \ \theta = 0^\circ$) ◆ LHe I ($\Delta T_{sub} > 0 \text{ K} \ \& \ 0 < \theta \leq 180^\circ$)
- LHe I ($\Delta T_{sub} > 0 \text{ K} \ \& \ \theta = 0^\circ$) ◆ LN₂ ($\Delta T_{sub} > 0 \text{ K} \ \& \ 0 < \theta \leq 180^\circ$)
- LH₂ ($\Delta T_{sub} > 0 \ \& \ \theta = 0^\circ$)



CFD Predictions

Bubble Collision Dispersion (EXP)

$G = 576.8 \text{ kg/m}^2\text{s}$, $P_{in} = 628.8 \text{ kPa}$, $\Delta T_{sub.in} = 2.28 \text{ K}$, $q'' = 7.97 \text{ kW/m}^2$



$$F^{BCD} = - \left(K \frac{\rho_f u_t^2}{2\alpha_{max}^{2/3}} \right) f(\alpha) \nabla \alpha$$

$$f(\alpha) = \alpha_g^{2/3} \left[1 - \left(\frac{\alpha_g}{\alpha_{max}} \right) \right]$$

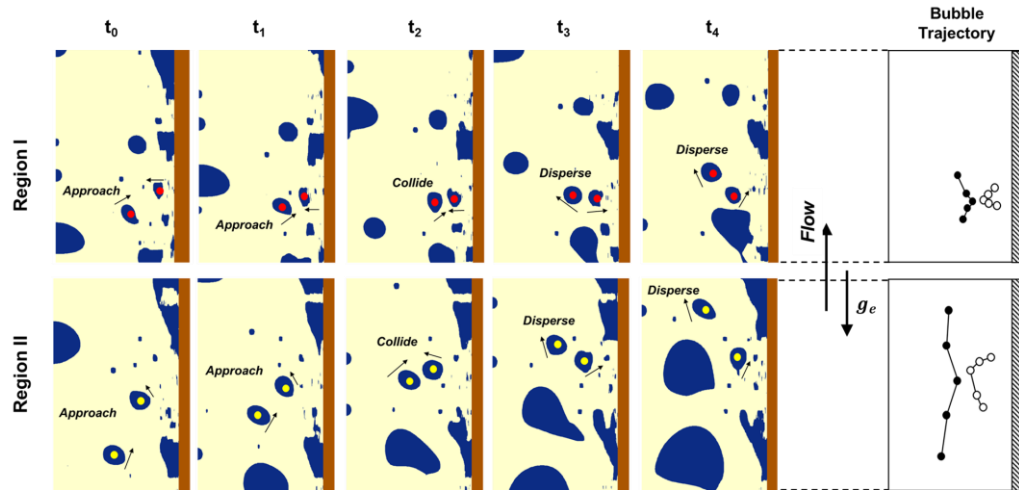
Bubble collision dispersion

- Reported by Sharma et al. (2017)
- Repelling force btw small bubbles
- Approach – Squeeze – Collision – Dispersion

User defined function (UDF)

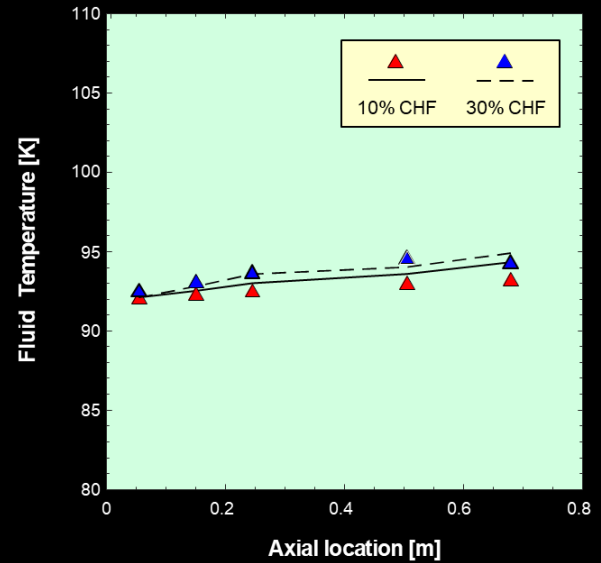
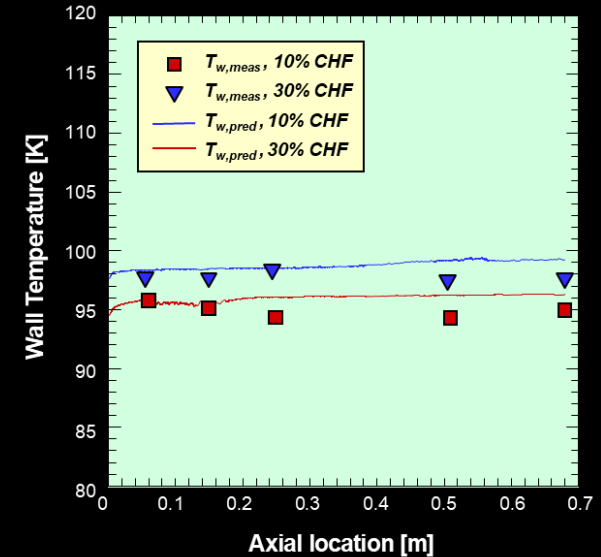
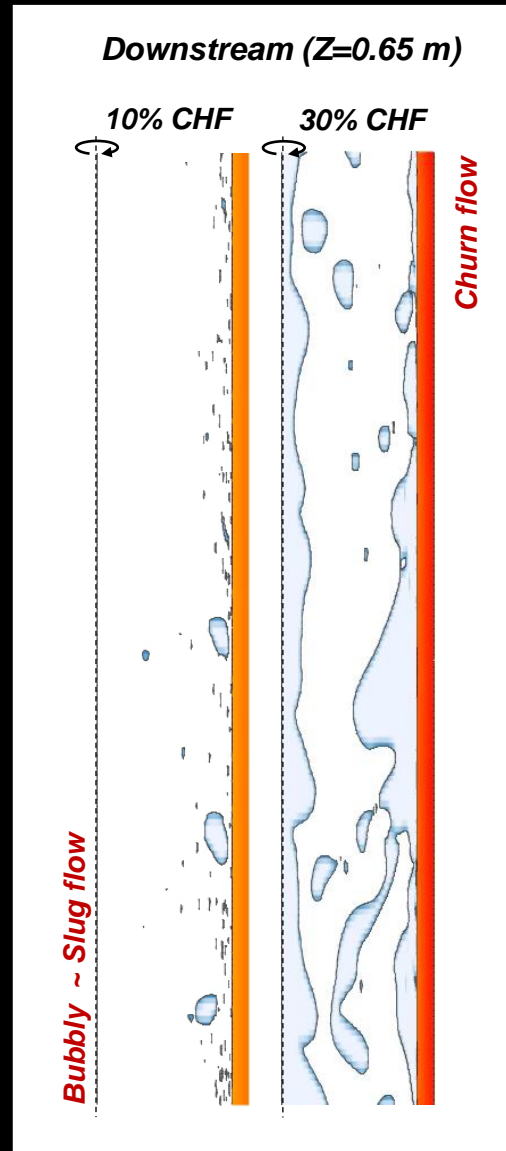
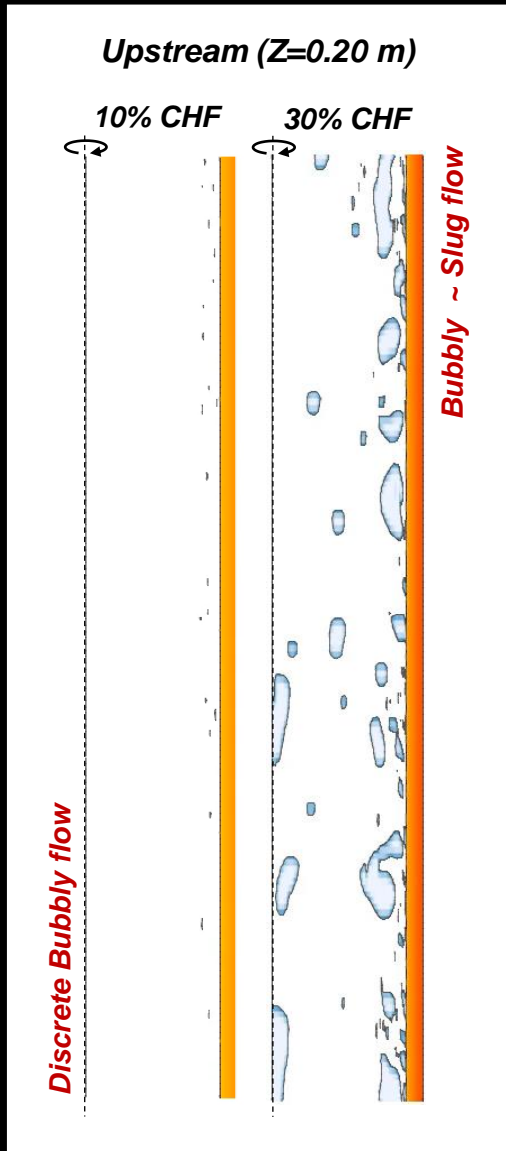
- Numerically formulated BCD function
- Coupling UDF with ANSYS Fluent
- Supplementing under-represented relative motion btw phases

CFD predictions



Predicted flow patterns

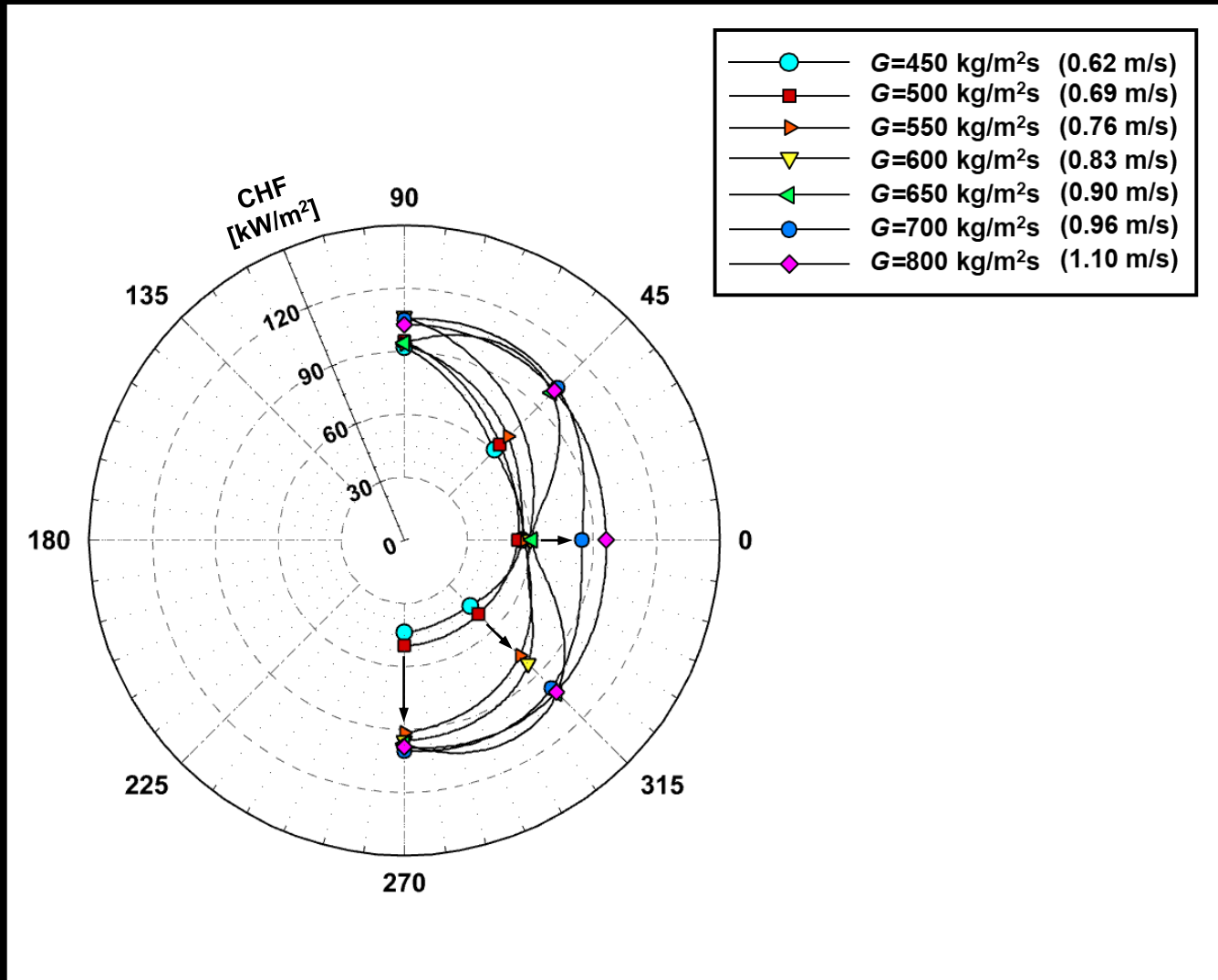
$G = 804 \text{ kg/m}^2\text{s}$, $P_{in} = 551.6 \text{ kPa}$, $\Delta T_{sub.in} = 3.24 \text{ K}$

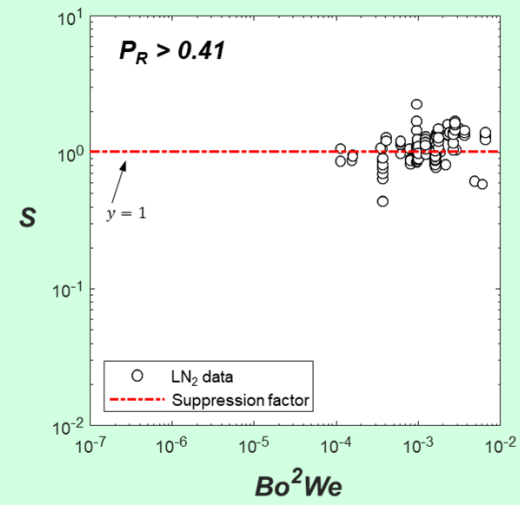
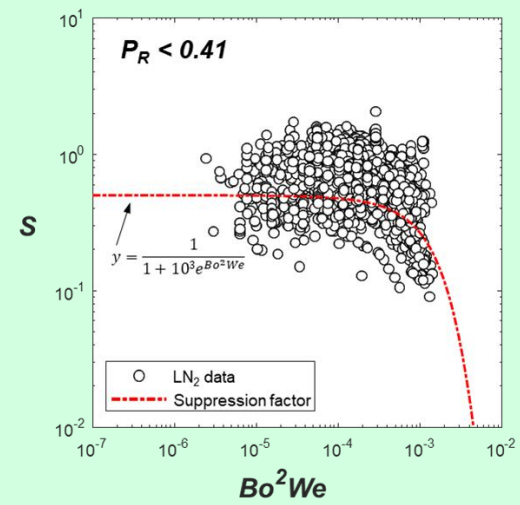
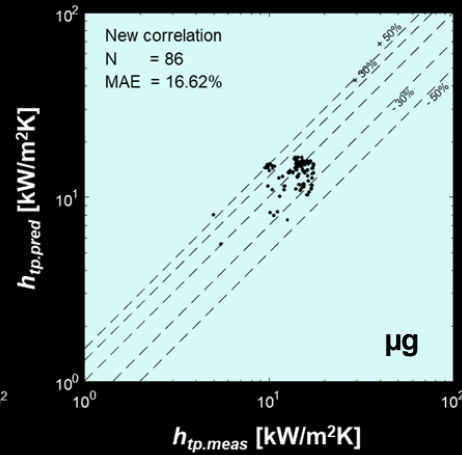
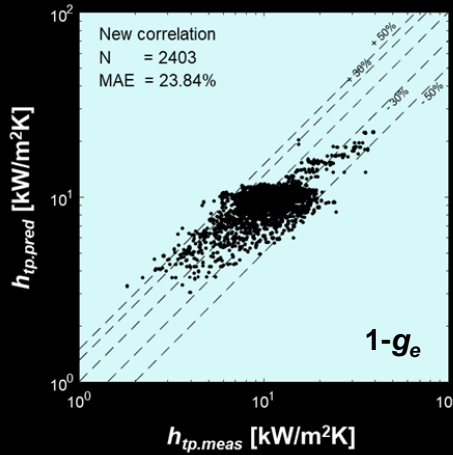




Thank you!

Supplement materials





Behavior of Suppression factor

IF $P_R < 0.41$

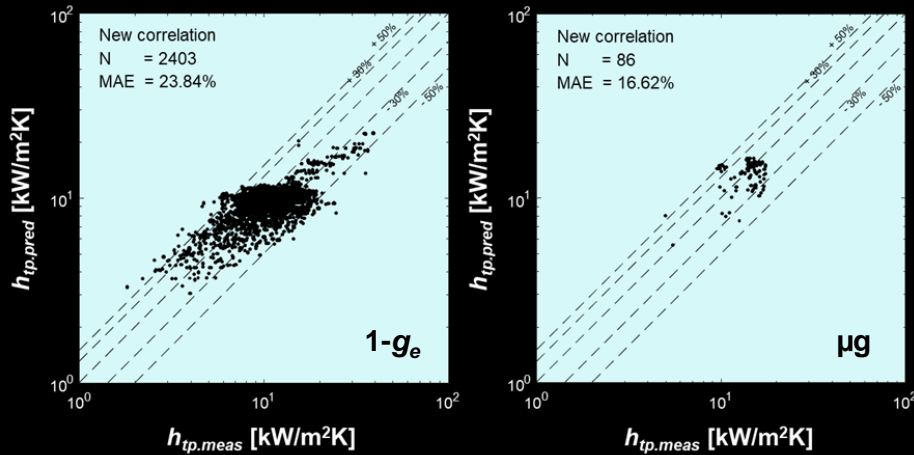
$$h_{NB} = h_{PB} \cdot \left[1.36 \cdot \tanh\left(\frac{g_e}{g}\right) \right] \cdot \left[\frac{1}{1 + 10^3 \cdot \exp(Bo^2We)} \right]^{0.475}$$

IF $P_R \geq 0.41$

$$h_{NB} = h_{PB} \cdot \left[1.2 \cdot \tanh\left(\frac{g_e}{g}\right) \right]$$

$$h_{CB} = h_{sp} \cdot 7 \cdot \left(\frac{1}{X_{tt}}\right)^{0.39} \cdot \left(\frac{\rho_f}{\rho_g}\right)^{-0.34}$$

$$h_{tp} = [h_{NB}^2 + h_{CB}^2]^{1/2}$$



IF $PR < 0.41$

$$h_{NB} = h_{PB} \cdot \left[1.36 \cdot \tanh\left(\frac{g_e}{g}\right) \right] \cdot \left[\frac{1}{1 + 10^3 \cdot \exp(Bo^2 We)} \right]^{0.475}$$

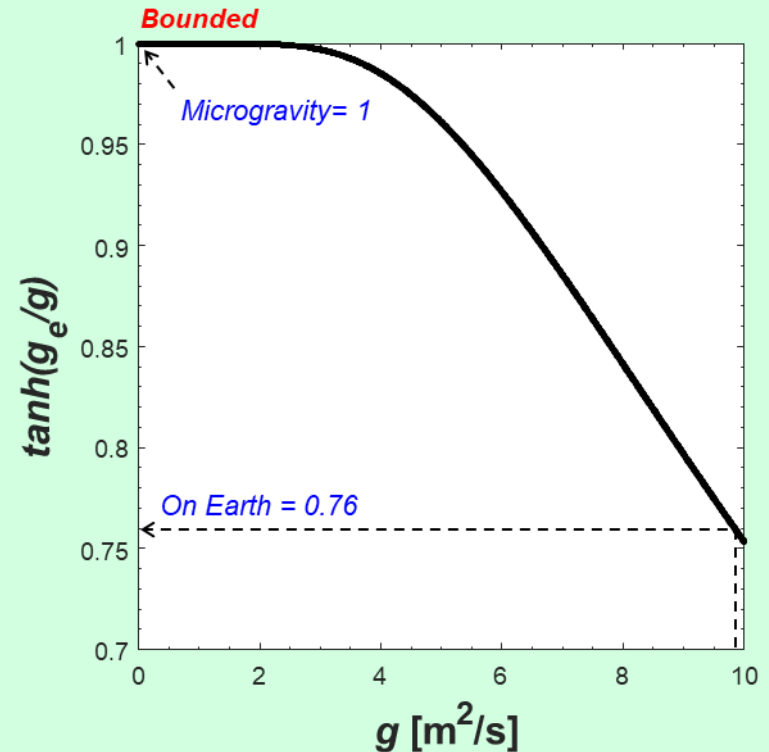
IF $PR \geq 0.41$

$$h_{NB} = h_{PB} \cdot \left[1.2 \cdot \tanh\left(\frac{g_e}{g}\right) \right]$$

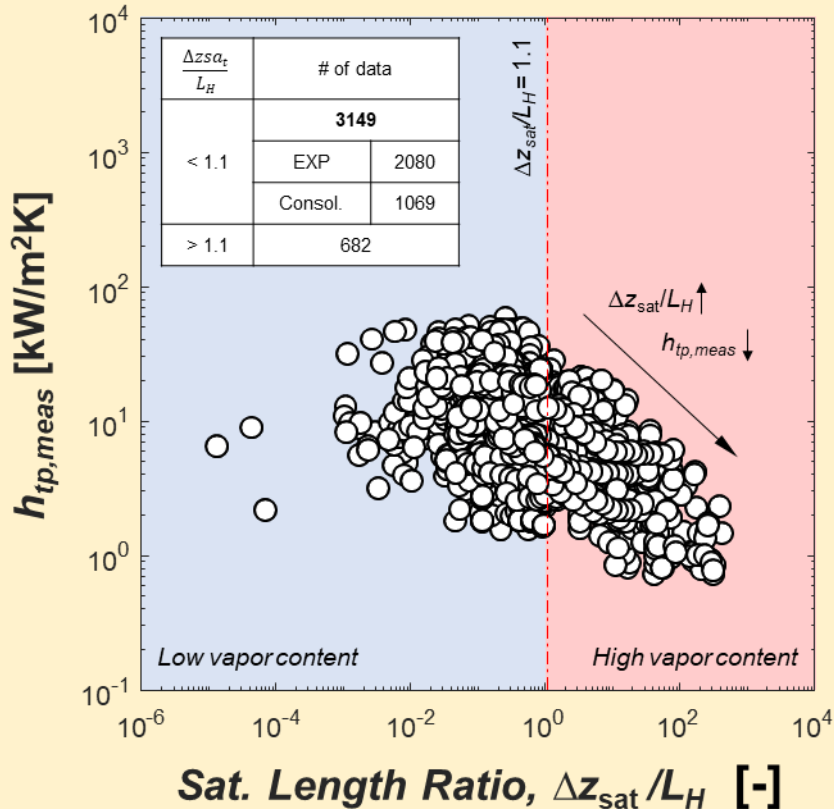
$$h_{CB} = h_{sp} \cdot 7 \cdot \left(\frac{1}{X_{tt}}\right)^{0.39} \cdot \left(\frac{\rho_f}{\rho_g}\right)^{-0.34}$$

$$h_{tp} = [h_{NB}^2 + h_{CB}^2]^{1/2}$$

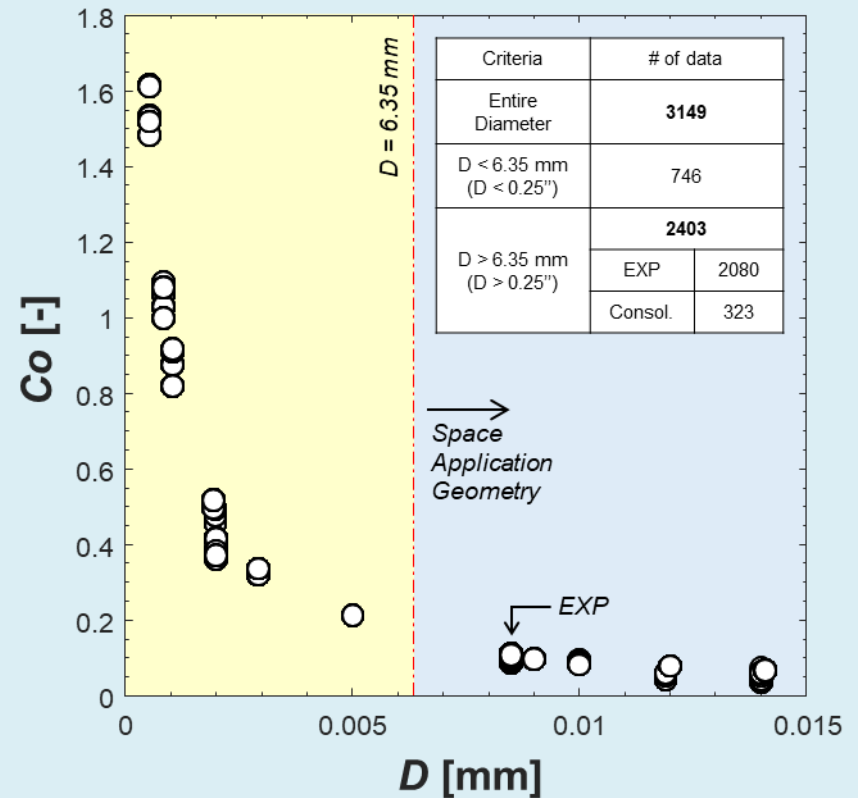
Behavior of Gravity parameter, $\tanh(g_e/g)$



Saturation Length Ratio,
 $\Delta Z_{sat}/L_H$



Tube Diameter,
 D



Bubble Dynamics

$$J = 1.44(1040) \cdot \left[\frac{\rho_f^2 \sigma}{\bar{M}^3} \right]^{1/2} \cdot \exp \left[\frac{-1.213(1024)\sigma^3}{T[\eta P_{sat} - P_f]^2} \right]$$

Rate of bubble formation is inversely proportional to molecular weight !!

Kinetic theory of gases

$$j_n = \left(\frac{1}{4} \right) \left(\frac{n}{V} \right) \left(\frac{8K_B T}{m\pi} \right)^{1/2}$$

Total rate of molecules passing through a plane surface per unit area, j_n , is inversely proportional to molecular weight !!

Heat transfer coefficient

$$q_i'' \approx (\bar{M})^{1/2} \cdot \exp \left(\frac{1.3}{\bar{M}^{0.5}} \right) \cdot (\bar{M})^{-1}$$

Heat transfer rate, q_i , inversely proportional to molecular weight !!

Target Question

What is the relation between h and M_w ?

Answer

Heat transfer coefficient, $\left(h_i = \frac{q_i}{\Delta T_i} \right)$, is inversely proportional to molecular weight !!

