

# The Role of a Neutron Component in the Photospheric Emission of Long-Duration Gamma-Ray Burst Jets

NATHAN WALKER <sup>1</sup>, TYLER PARSOTAN <sup>2</sup>, AND DAVIDE LAZZATI <sup>1</sup>

<sup>1</sup>*Oregon State University*

*Department of Physics, 301 Weniger Hall, Oregon State University  
Corvallis, OR 97331, USA*

<sup>2</sup>*Astrophysics Science Division, NASA Goddard Space Flight Center, Greenbelt, MD 20771, USA*

## ABSTRACT

Long-duration gamma-ray bursts (LGRBs), thought to be produced during core-collapse supernovæ, may have a prominent neutron component in the outflow material. If present, neutrons can change how photons scatter in the outflow by reducing its opacity, thereby allowing the photons to decouple sooner than if there were no neutrons present. Understanding the details of this process could therefore allow us to probe the central engine of LGRBs, which is otherwise hidden. Here, we present results of the photospheric emission from an LGRB jet, using a combination of relativistic hydrodynamic simulations and radiative transfer post-processing using the Monte Carlo Radiation Transfer (MCRaT) code. We control the size of the neutron component in the jet material by varying the equilibrium electron fraction  $Y_e$ , and we find that the presence of neutrons in the GRB fireball affects the Band parameters  $\alpha$  and  $E_0$ , while the picture with the  $\beta$  parameter is less clear. In particular, the break energy  $E_0$  is shifted to higher energies. Additionally, we find that increasing the size of the neutron component also increases the total radiated energy of the outflow across multiple viewing angles. Our results not only shed light on LGRBs, but are also relevant to short-duration gamma-ray bursts associated with binary neutron star mergers, due to the likelihood of a prominent neutron component in such systems.

*Keywords:* Gamma-ray bursts(629) — Radiative transfer simulations(1967) — Hydrodynamical simulations (767)

## 1. INTRODUCTION

Our understanding of Gamma-Ray Bursts (GRBs) has evolved dramatically since their discovery in the late 1960's. First detected as short transient bursts of high energy photons (Klebesadel et al. 1973), observations of afterglows (Groot et al. 1998; Costa et al. 1997) and supernova counterparts (Galama et al. 1998; Hjorth et al. 2003; Woosley & Bloom 2006; Bloom et al. 1999) have facilitated a deeper understanding of these otherwise mysterious events. Long duration gamma-ray bursts (LGRBs) are now thought to occur during core-collapse supernovæ, a process in which stars more massive than about  $8M_\odot$  end their lives in a violent explosion, resulting in the formation of either a Black Hole (BH) or a Neutron Star (NS) (Woosley & Janka 2005). After the formation of either a BH or a NS, material from the preceding collapse can accrete around the compact object, providing a possible power source for an ensuing LGRB (e.g. Narayan et al. (2001)). Alternatively, a highly magnetized, fast spinning NS could power a rel-

ativistic outflow by tapping into its rotational energy (e.g., Bucciantini et al. 2012). Given the possibility of a NS as either an intermediate or a terminal stage of the supernova, there is a strong possibility of a neutron component in the accreting material, which can then be collimated into a relativistic jet and produce a LGRB.

In spite of this progress, one aspect of GRBs that still remains in contention is the nature of the prompt emission. In LGRBs, the prompt emission can last anywhere from a few seconds to a few minutes (Bloom et al. 1999; MacFadyen et al. 2001) and is characterized by bright, non-thermal spectra (Band et al. 1993). A leading model that explains this emission is the Synchrotron Shock Model (SSM). In this model, the jet expands and reaches the photosphere without producing noticeable radiation. After passing the photosphere, electrons in colliding internal shocks produce non-thermal radiation (Rees & Meszaros 1994). While this model naturally explains the characteristic non-thermal emission of GRBs and is able to fit the spectra of a number of bursts,

63 it may have difficulties in reproducing the peak width  
 64 of bursts (Beloborodov 2013). In addition, some burst  
 65 have spectra that are inconsistent with a simple model in  
 66 which electrons are accelerated impulsively and either do  
 67 not cool (the line-of-death problem, Preece et al. 1998)  
 68 or cool radiatively (Ghisellini et al. 2000). Finally, the  
 69 SSM model has difficulty reproducing the ensemble cor-  
 70 relations between properties of different bursts, such as  
 71 the Amati and the Yonetoku correlations (Amati et al.  
 72 2002; Yonetoku et al. 2004).

73 A viable alternative to the SSM is the so-called pho-  
 74 tospheric model (e.g. Beloborodov (2010a), Giannios &  
 75 Spruit (2007), Lazzati et al. (2009), Ryde et al. (2011),  
 76 Pe’er et al. (2006)). In this model, thermal radiation is  
 77 produced when the jet is hot and dense near the central  
 78 engine. As the jet propagates and expands the radi-  
 79 ation is shaped through its interaction with the expand-  
 80 ing outflow. Effects such as sub-photospheric dissipation  
 81 (Chhotray & Lazzati 2015; Parsotan et al. 2018; Ito et al.  
 82 2018) and multi-color blackbody emission (Pe’er & Ryde  
 83 2011) enable this model to account for a non-thermal  
 84 spectrum. Additionally, as the radiation scatters and  
 85 propagates with the outflow, it is imprinted with a sig-  
 86 nature of the history of the outflow that survives until  
 87 the radiation escapes at the photosphere (Vurm & Be-  
 88 loborodov 2016). Because of this, the composition and  
 89 dynamics of the jet material are of crucial importance  
 90 in shaping the observed prompt emission in the pho-  
 91 spheric model. An important test of the photospheric  
 92 model can then be to model the effect that different  
 93 compositions of the jet material can have on radiation.

94 Given the possibility of a neutron component in both  
 95 the compact mergers and supernovæ that are thought  
 96 to produce GRBs, a body of work has been produced  
 97 that explores the consequences of a neutron component  
 98 in GRB fireballs. This includes a detailed study on the  
 99 processes that shape the nuclear composition of the fire-  
 100 ball as it expands (Beloborodov 2003), the role neutrons  
 101 play in heating the jet through collisional processes (Be-  
 102 loborodov 2010b; Rossi et al. 2004), and that of the dy-  
 103 namics of shocks in the explosion (Derishev et al. 1999).  
 104 However, no work has been done on how neutrons di-  
 105 rectly shape the observed prompt emission of GRBs.  
 106 Therefore the role of a neutron component on the pho-  
 107 tosepheric emission of a LGRB is of particular interest,  
 108 and a good candidate to further test the photospheric  
 109 emission model.

110 In this paper, we use the MCRaT radiative transfer  
 111 code and the ProcessMCRaT python package (Lazzati  
 112 2016; Parsotan & Lazzati 2018; Parsotan et al. 2018;  
 113 Parsotan & Lazzati 2021) to scatter photons through  
 114 a 2D relativistic hydrodynamic (RHD) simulation of a

115 LGRB jet (Morsony et al. 2007; Lazzati et al. 2013), and  
 116 produce mock observables. We control the relative size  
 117 of the neutron component in the jet material by vary-  
 118 ing the equilibrium proton-to-nucleon ration  $Y_e$ . This  
 119 paper is organized as follows: in Section 2 we summa-  
 120 rize how the MCRaT code scatters photons and describe  
 121 how we take into account a neutron component in the  
 122 jet; in Section 3 we present results of spectra obtained  
 123 by varying  $Y_e$ ; and in Section 4 we discuss our results  
 124 and their implications.

## 125 2. COMPUTATIONAL METHODS

### 126 2.1. The MCRaT Code

127 We use the MCRaT radiative transfer code to indi-  
 128 vidually Compton-scatter a set of photons injected into  
 129 a RHD simulation of a LGRB jet. In this section we  
 130 summarize the MCRaT algorithm. Further details on  
 131 the original algorithm can be found in Lazzati (2016),  
 132 with improvements found in Parsotan & Lazzati (2018).

133 MCRaT begins by injecting photons into the output  
 134 of a RHD simulation. During this injection process,  
 135 MCRaT selects which RHD cells to inject photons into  
 136 based on a set of user-defined parameters: the injection  
 137 radius  $R_{inj}$  and the angular interval  $\delta\theta$ , defined with re-  
 138 spect to the jet axis. All cells within the interval  $\delta\theta$  and  
 139 with a radius between  $R_{inj} \pm \frac{1}{2} c\delta t$  are selected, where  
 140  $c$  is the speed of light and  $\delta t$  is the time interval of the  
 141 selected RHD frame. Once the injection frames are se-  
 142 lected, MCRaT determines the four-momentum of the  
 143 injected photons in each cell by sampling a thermal dis-  
 144 tribution centered at the local co-moving temperature,

$$145 T'_i = \left( \frac{3p_i}{a} \right)^{\frac{1}{4}}, \quad (1)$$

146 where  $p_i$  is the pressure of the fluid and  $a$  is the radi-  
 147 ation density constant. The injected photons are then  
 148 weighted according to (Parsotan et al. 2018)

$$149 dN_i = \frac{\xi T_i'^3 \Gamma_i}{w} dV_i, \quad (2)$$

150 where  $dN_i$  is the expected number of photons in the  
 151  $i^{th}$  RHD cell,  $\xi$  is the photon number density coefficient  
 152 from  $n_\gamma = \xi T^3$  ( $\xi = 20.29$  for a Planck spectrum and  
 153  $\xi = 8.44$  for a Wein spectrum),  $T'_i$  is the comoving fluid  
 154 temperature,  $\Gamma_i$  is the bulk Lorentz factor,  $dV_i$  is the vol-  
 155 ume element of the RHD cell, and  $w$  is the weight of the  
 156 injected photons. MCRaT calculates the expected num-  
 157 ber of photons in each cell via Equation 2, and draws a  
 158 photon number from a Poisson distribution with a mean  
 159 given by the expected number of photons. MCRaT then  
 160 sums over the photon numbers in each cell, and if the

total number of injected photons so obtained lies outside the user-specified range, the weights are adjusted and the process of calculating the expected number of photons via Equation 2 repeats. The final weights are those that result in a total number of injected photons that lies within the user-defined range.

Once the injected photon properties are determined, MCRaT scatters each photon according to the properties of the RHD simulation. To begin with, each photon is assigned a mean-free path according to Abramowicz et al. (1991)

$$\lambda_i = \frac{dr}{d\tau_T} = \frac{1}{\sigma_T n'_i \Gamma_i (1 - \beta_i \cos \theta_{fl,i})}, \quad (3)$$

where  $\sigma_T$  is the Thomson cross section,  $n'_i$  is the co-moving lepton number density,  $\beta_i$  is the fluid velocity in units of  $c$ , and  $\theta_{fl,i}$  is the angle between the fluid velocity and the photon velocity. A random scattering time for each photon is drawn from the distribution

$$P_i(t) \propto e^{-\frac{c}{\lambda_i} t}, \quad (4)$$

and if the smallest of those scattering times is within the time interval of the given hydrodynamical simulation frame, the positions of the photons are all updated by allowing them to travel at the speed of light for the smallest scattering time obtained via Equation 4. Once all photons are updated to a new position in a frame, the photon with the shortest scattering time is scattered with an electron drawn from either a Maxwell-Boltzmann or a Maxwell-Jüttner distribution at the local fluid temperature, with a direction drawn from a random distribution. If the smallest scattering times obtained from equation 4 lies outside the given RHD frame time interval, MCRaT allows the photons to propagate at the speed of light, without scattering, for an amount of time equal to the remaining time in the current RHD frame. Then, MCRaT loads a new simulation frame and the photon mean free paths are all calculated again. This process of calculating photon properties and scattering with electrons is repeated for all the injected photons as they propagate and scatter through all of the provided RHD simulation frames.

## 2.2. Mock Observations

When all the injected photons have been diffused beyond the photosphere we use the ProcessMCRaT package (Parsotan & Lazzati 2022) to conduct mock observations. This software allows for the injected photons to continue propagating unimpeded out to a virtual detector placed at a user-defined radius. To mimic a real observation in which the viewing geometry is unique

we count only photons within a given acceptance range around the angle to the observer. The energies of photons are obtained from the time component of the four-momentum at the end of the simulation, and the detection time is calculated as

$$t_d = t_p + t_{real} - t_j, \quad (5)$$

where  $t_{real}$  is the simulation time at the frame used for an observation,  $t_p$  is the photon detection time, and  $t_j = r_d/c$  is the time it takes for a photon that was emitted at the instant the jet was launched to propagate to the detector.

In the following, all light curves and spectra are obtained by placing the virtual detector at a radius of  $r_d = 2.5 \times 10^{13}$  cm, which corresponds to approximately the edge of the RHD simulation. When the photons haven't yet reached the last frame we find the positions of all the photons at the corresponding RHD simulation time and place a detector slightly beyond that point.

After conducting a mock observation, we can bin the photon arrival times to calculate light curves,

$$L_t = \frac{1}{\Delta\Omega \Delta t_{bin}} \sum_i w_i E_i, \quad (6)$$

where  $E_i$  is the energy of each photon,  $\Delta t_{bin}$  is the time bin, and  $\Delta\Omega = 2\pi[\cos(\theta_v - \Delta\theta/2) - \cos(\theta_v + \Delta\theta/2)]$  is the solid angle the detector occupies, with  $\Delta\theta$  being the angular acceptance range centered around  $\theta_v$ . We also bin the photon energies to calculate spectra via

$$\frac{dN_e(E)}{dE dt} = \frac{1}{\Delta E_{bin} \Delta\Omega \Delta t} \sum_i w_i, \quad (7)$$

where all the terms are the same as in Equation 6 except  $\Delta E_{bin}$  and  $\Delta t$ , which are the energy bin width and the time interval over which photons were detected, respectively.

We fit the Band function (Band et al. 1993),

$$N_E(E) = A \left( \frac{E}{100\text{keV}} \right)^\alpha \exp(-E/E_0), \quad (8)$$

$$E \leq (\alpha - \beta)E_0$$

$$A \left[ \frac{(\alpha - \beta)E_0}{100\text{keV}} \right]^{\alpha - \beta} \exp(\beta - \alpha) \left( \frac{E}{100\text{keV}} \right)^\beta$$

$$E \geq (\alpha - \beta)E_0.$$

to spectra obtained from equation 7. In equation 8,  $\alpha$  and  $\beta$  are the low and high energy slopes, respectively,  $E_0$  is the break energy, and  $A$  is related to normalization.

245 The spectral peak is defined with respect to the spectral  
246 parameters in equation 8 as  $E_{pk} = (2 + \alpha) E_0$ .

247 In order for the calculated spectra and light curves to  
248 correspond to what an observer would see, the optical  
249 depth must reach a value  $\tau \sim 1$ . We calculate the optical  
250 depth (Parsotan et al. 2018) as:

$$251 \quad \tau_i^n = \sum_{j=i}^L \langle N \rangle_j^n, \quad (9)$$

252 where  $L$  is the last frame of the RHD simulation and  
253  $n$  refers to a group of photons located initially in the  
254  $i^{th}$  frame, at some average position  $R_i$ . The sum over  
255 the RHD frame number  $j$  goes from the  $i^{th}$  frame to  
256 the last, with  $\langle N \rangle_j^n$  being the average number of scat-  
257 terings that the  $n^{th}$  group of photons experienced in the  
258  $j^{th}$  frame. Equation (9) essentially counts the number  
259 of scatterings each photon undergoes starting from the  
260  $i^{th}$  frame and we calculate it by tracking the number  
261 of scatterings that individual photons undergo, starting  
262 immediately after they are injected. We similarly calcu-  
263 late the average energy of individual photons by tracking  
264 their energy throughout the MCRaT simulation.

265 A group of photons is uncoupled from the jet if the  
266 average number of scatterings per photon starting from  
267 the  $i^{th}$  RHD frame is  $\lesssim 1$ , corresponding to the pho-  
268 tosphere condition of  $\tau \sim 1$ . Since this is computed  
269 separately for separate groups of photons it allows for  
270 the fact that photons in different parts of the jet and  
271 cocoon may uncouple at different times.

### 272 2.3. A Neutron Component in the Fireball

273 The MCRaT code reads in hydrodynamical data and  
274 determines the energy of injected photons via the hy-  
275 drodynamical pressure (Equation 1), and their mean  
276 free paths via the hydrodynamical density and veloc-  
277 ity (Equation 3). Normally it is assumed that the total  
278 mass of the hydrodynamical simulation is attributed  
279 to protons (with a negligible contribution by electrons),  
280 and the lepton number density is therefore calculated by  
281 dividing the hydrodynamical density by the mass of the  
282 proton. This picture changes when we include neutrons  
283 in our radiative transfer simulations.

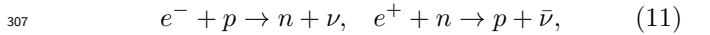
284 To simulate the role of a neutron component in the  
285 fireball, we use the proton-to-nucleon ratio,  $Y_e$ , defined  
286 through the charge neutrality condition (Beloborodov  
287 2003)

$$288 \quad n_- - n_+ = Y_e \frac{\rho}{m_p}, \quad (10)$$

289 where  $n_{\pm}$  are the  $e^{\pm}$  number densities. In the ab-  
290 sence of  $e^{\pm}$  pairs,  $Y_e$  is just the electron-to-nucleon ra-  
291 tio and describes how many electrons there must be in

292 a plasma in order to preserve charge neutrality. The  
293 density  $\rho$  in Equation 10 can in general consist of both  
294 protons and neutrons, and when both are taken into  
295 account the result is the equilibrium electron fraction  
296  $Y_e = n_p / (n_p + n_n)$ . Therefore, increasing the fraction of  
297 neutrons in the fireball decreases the electron-to-nucleon  
298 ratio, which in turn leaves fewer electrons with which to  
299 scatter photons. When calculating photon mean free  
300 paths via Equation 3, we can then scale the lepton den-  
301 sity by  $Y_e$ . A larger neutron component reduces the  
302 lepton density of the jet.

303 A neutron component can in principle also change the  
304 hydrodynamical behavior of the plasma. When the jet  
305 is still near the central engine it is hot and dense enough  
306 that the charged current reactions,



308 establish an equilibrium  $Y_e$ . While these conditions will  
309 change as the jet expands, it has been shown that, fur-  
310 ther from the central engine, neutrons and ions can stay  
311 coupled through the acceleration stage as long as the jet  
312 has relatively high baryon loading (Beloborodov 2003).  
313 In the same work it was also found that fireballs from  
314 neutron rich central engines are likely to remain neutron  
315 rich. We therefore do not consider the hydrodynamical  
316 effects of neutrons decoupling from protons, and we  
317 likewise keep the value of  $Y_e$  constant throughout our  
318 MCRaT simulations. Since the baryons are treated as  
319 being in equilibrium we leave the pressure and velocity  
320 variables from the RHD simulation unchanged, and we  
321 scale the fluid density by the equilibrium electron frac-  
322 tion  $Y_e$ :  $\rho \rightarrow Y_e \rho$ .

323 While we use a constant value of  $Y_e$  for each MCRaT  
324 simulation we run, the RHD simulation is in fact com-  
325 prised of material ejected from the central engine, a stel-  
326 lar envelope through which the jet must escape, and a  
327 radial power law as the jet propagates into the inter-  
328 stellar medium. All of this materials could, in principle,  
329 have a different composition. In light of this, a constant  
330 value of  $Y_e$  applied to the entire RHD domain is just  
331 an approximation. To ensure that such approximation  
332 gives reliable results, we restrict this study to the region  
333 near the jet axis by injecting photons only within the  
334 first  $3^\circ$  relative to the jet axis, where the jet material  
335 has a high temperature and Lorentz factor. The role  
336 of mixing between materials with different  $Y_e$  will be  
337 explored in a future work.

## 338 3. RESULTS

339 In this paper we used the FLASH version 2.5 2D RHD  
340 simulation in Lazzati et al. (2013) that is based on a  
341 16TI progenitor (Woosley & Heger 2006) in which a jet

with initial Lorentz factor of 5 and an opening angle of  $10^\circ$  is injected into the 16TI progenitor for 100 s and propagates out to the photosphere at  $\sim 10^{13}$  cm. The 16TI simulation in Lazzati et al. (2013) was performed on an adaptive mesh grid with a maximum resolution of  $4 \times 10^6$  cm and output files were saved every  $\delta t = 0.2$  s. For our MCRaT simulations to converge according to Arita-Escalante et al. (2023), injected photons should travel through multiple RHD cells in each frame. This can be quantified through the light crossing ratio, defined as  $c\delta t/\delta r$  which, with the spatial and temporal resolutions from the 16TI simulation used here, results in a light crossing ratio as large as  $\sim 1500$ .

Our methods are similar to Parsotan et al. (2018), with a key difference being that we inject  $\sim 2 \times 10^5$  photons for  $\sim 50$  s of a non-variable jet, which excludes only a constant, low luminosity portion of the lightcurve that is not observed in nature. We also restrict photon injection to the first  $3^\circ$  of the jet as outlined in Section 2. We then adopt a viewing angle of  $\theta_v < 3^\circ$  when conducting mock observations. For the electron-to-nucleon ratio we use the values  $Y_e = 1, 0.7, 0.4,$  and  $0.1$  to cover the cases of a small to large neutron component.

Figure 1 shows lightcurves obtained at a viewing angle of  $\theta_v = 1^\circ$  alongside the time-resolved best fit parameters  $\alpha$  and  $\beta$  for the Band function (equation 8), in addition to the peak energy  $E_{pk} = (2 + \alpha)E_0$ , for all 4 values of  $Y_e$ . Our lightcurve from the  $Y_e = 1$  simulation agrees well with past MCRaT results based on similar 16TI simulations (Lazzati 2016; Parsotan & Lazzati 2021), and all lightcurves show a characteristic small peak at  $\sim 8$  s, with a brighter peak at  $\sim 30$  s. As  $Y_e$  is increased, the second peak dims noticeably as evident in panel (d) of Figure 1, where the first peak is brighter than the second.

In Figure 2 we show time-integrated spectra obtained from photons in the  $Y_e = 0.1$  and  $Y_e = 1$  MCRaT simulations that have reached the final RHD frame. Both spectra in figure 2 were integrated from 0 to 40 s, corresponding to the first two peaks seen in figure 1. As with Figure 1, our spectra with  $Y_e = 1$  agrees well with past results. Here, as  $Y_e$  is decreased, the peak energy shifts to higher frequencies as seen by the dotted lines in Figure 2. We will look at how  $Y_e$  affects other spectral parameters below.

Figure 3 shows a corner plot for a Band function fit to the  $Y_e = 0.1$  spectrum. While spectral parameters in figures 1 and 2 were obtained via a non-linear least squares fitting algorithm available in ProcessMCRaT, those in Figure 3 were obtained by fitting a Band function to our MCRaT data with a Markov Chain Monte Carlo algorithm via emcee (Foreman-Mackey

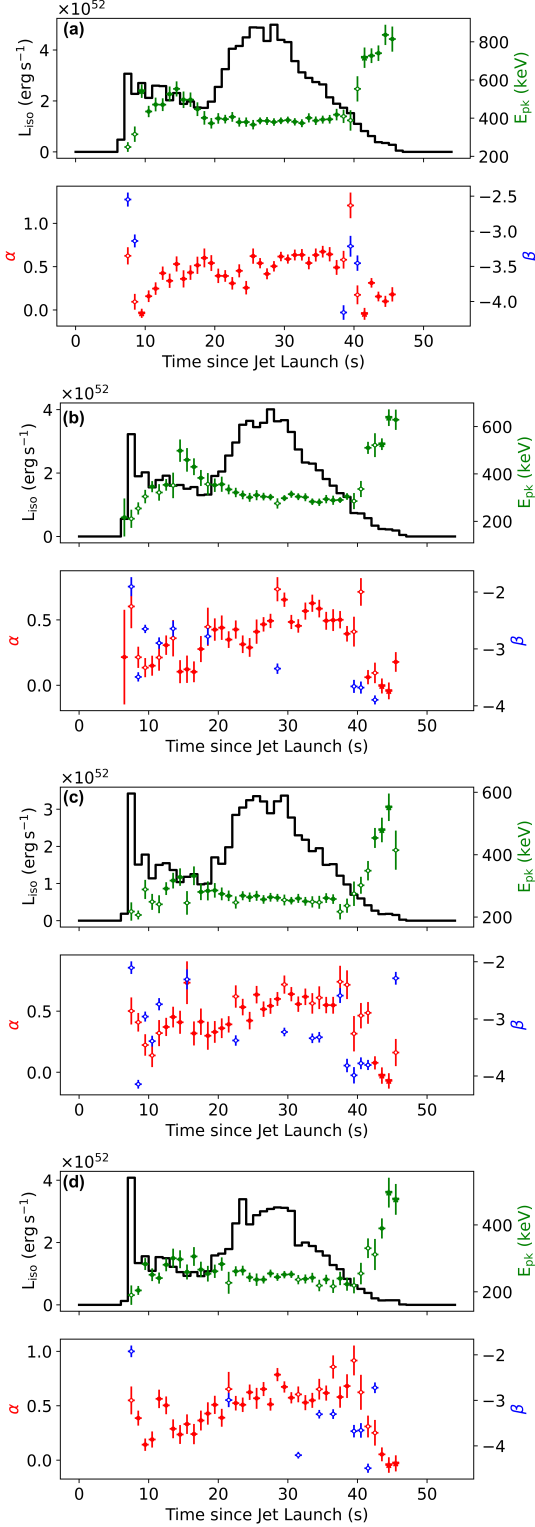
et al. 2013). The parameters in Figure 3 are different from those seen in Figure 2 due to the different methodologies used to obtain them. Figure 3 shows a clear correlation between  $E_0$  and  $\alpha$ , while the other pairs of parameters have no notable correlations. This strong correlation between  $\alpha$  and  $E_0$  plays a part in the evolution of Band function parameters for all four of the MCRaT simulations in this work.

It is also illuminating to analyze the behaviour of the Band Function parameters as the radiation propagates with and through the outflow material. We do this by conducting a mock observation and calculating spectra for multiple intermediate times throughout the MCRaT simulation. At each of these times, the injected photons have scattered through only a portion of the RHD simulation, and thus have some average distance from the central engine. This distance increases as the photons propagate with the outflow until they near the photosphere. For these observations, the position of the detector is determined by the positions of the photons at a given frame. The Band function is fit to the spectrum at each time, and Figure 4 shows how the Band function parameters  $\alpha$ ,  $\beta$ , and  $E_0$  vary as a function of the photons' average distance from the central engine for all values of  $Y_e$  we consider. As with Figure 2, all parameters come from time-integrated spectra.

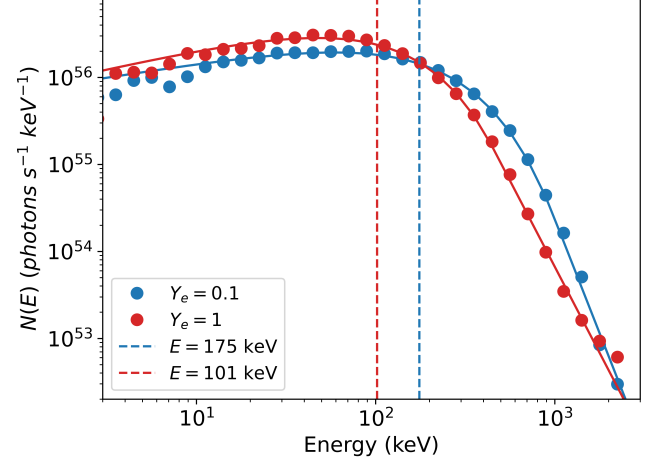
Panels (a) and (c) in Figure 4 clearly show the imprint of a neutron component on the spectral parameters of LGRBs. All four of our MCRaT simulations start off hot near the central engine and gradually cool as the photons and outflow propagate. Simulations with a smaller neutron component cool down more, resulting in lower peak energies. Since  $E_0$  and  $\alpha$  are correlated (e.g. Figure 3), the low energy slope  $\alpha$  mirrors this behavior, with simulations having larger neutron components displaying smaller values for  $\alpha$ . Panel (b), however, shows no clear trend.

Figure 5 shows the average photon energy as a function of their distance from the central engine. Figure 6 similarly shows how the optical depth (equation 9) of the injected photons. In figures 5 and 6, the photon energy and number of scatterings for each photon are, respectively, calculated for every individual photons starting immediately when they're injected near the central engine.

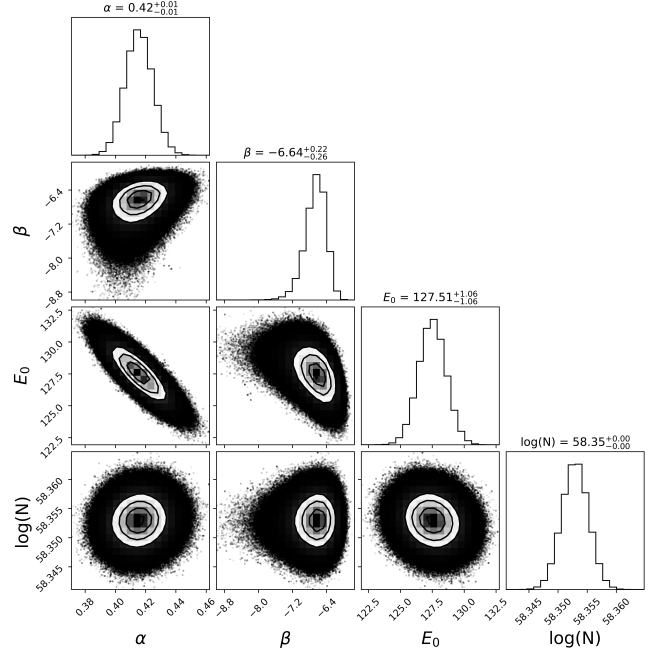
As stated in the Methods section, for the spectra and lightcurves from MCRaT to correspond what an observer would see from an actual burst, the photons have to decouple from the jet material. Figure 6 shows this directly. All four MCRaT simulations considered here start off with photons that have an optical depth of  $10^3 - 10^4$ . As the photons scatter and propagate with



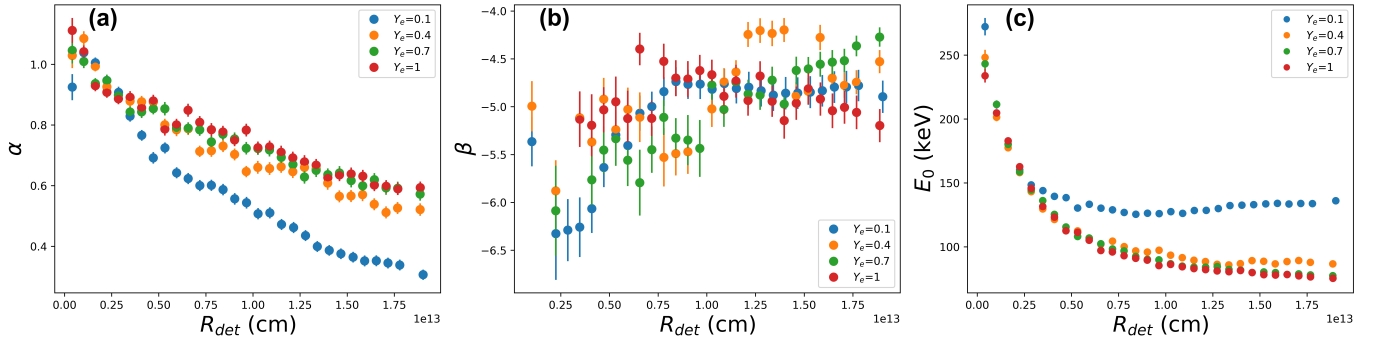
**Figure 1.** Light curves and time resolved best fit parameters of the 4 MCRaT simulations: (a.)  $Y_e = 0.1$ , (b.)  $Y_e = 0.4$ , (c.)  $Y_e = 0.7$ , (d.)  $Y_e = 1$ . The best fit parameter  $\alpha$  is shown in red,  $\beta$  is shown in blue, and  $E_{pk}$  is shown in green.  $\beta$  is not shown when a comptonized function provides a better fit than the Band function



**Figure 2.** Time-integrated spectra for MCRaT simulations with  $Y_e = 1$ , shown in red, and  $Y_e = 0.1$ , shown in blue. In both cases circles show data points and the solid lines show the best fit Band functions. The vertical dashed lines show the break energies,  $E_0$ , for both simulations. Both spectra were calculated using photons collected over the the first 40 s of the lightcurves in figure 1.



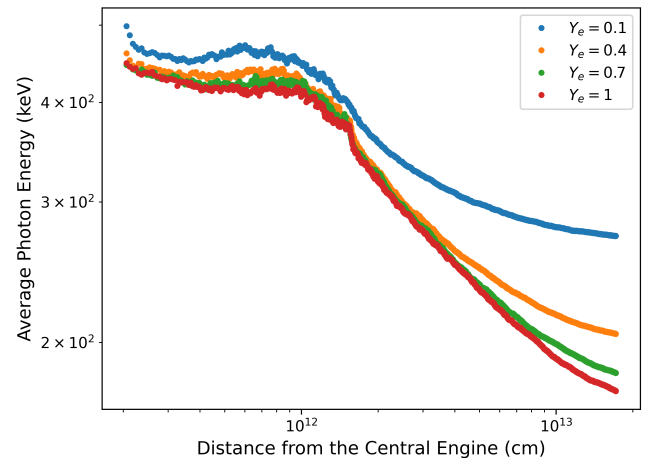
**Figure 3.** Corner plot resulting from fitting the Band function to the spectrum from the  $Y_e = 0.1$  simulation with a Markov-Chain Monte Carlo algorithm. The four parameters are the low energy slope  $\alpha$ , the high energy slope  $\beta$ , the break energy  $E_0$ , and the normalization parameter  $N$ . This clearly shows a tight correlation between  $E_0$  and  $\alpha$ , with less prominent correlations between all other parameters.



**Figure 4.** Evolution of the Band function parameters for spectra computed from each value of  $Y_e$ : (a) the low energy slope  $\alpha$ ; (b) the high energy slope  $\beta$ ; and (c) the break energy  $E_0$ . Each data point represents a parameter obtained from a mock observation conducted at various intermediate steps throughout the MCRaT simulation. At each step, the injected photons have some average position and a detector was placed slightly beyond that point, denoted  $R_{det}$ . As the simulation progresses, the position of the detector moves further away from the central engine and the Band function parameters approach their final values near the photosphere. Panels (a) and (c) show clear patterns for  $\alpha$  and  $E_0$ , respectively. Spectra obtained for all four values of  $Y_e$  start off hot, having a high  $E_0$ , and gradually cool as the MCRaT simulations progress.  $E_0$  obtained from the  $Y_e = 0.1$  simulation levels off sooner than for the other simulations, and so maintains a hotter spectra. This behavior is mirrored in panel (a), with  $\alpha$  reaching a smaller value for  $Y_e = 0.1$  than for other simulations. Panel (b) shows no discernible pattern for  $\beta$ .

448 the outflow, their optical depth slowly decreases until it  
 449 reaches a sharp decay at  $\sim 1.8 \times 10^{13}$  cm. While the  
 450 photons in all of our MCRaT simulations reach  $\tau = 1$ ,  
 451 some only do so at this sharp drop. This rapid decay is  
 452 due to the sum in Equation 9 only going to the last RHD  
 453 simulation frame, instead of all the way out to infinity.  
 454 The fact that our MCRaT simulations with  $Y_e = 0.7$   
 455 and  $Y_e = 1$  only reach an optical depth of 1 when this  
 456 artificial drop occurs is indicative of the fact that the  
 457 photons in these simulations are still relatively coupled  
 458 to the outflow. A proxy for this can be seen in Figure  
 459 5, which shows the same cooling behavior as panel (c)  
 460 in Figure 4, with photon energies beginning to level off  
 461 as they approach the photosphere. In particular, it also  
 462 shows that the photon energy for the simulation with  
 463  $Y_e = 0.1$  has nearly leveled off while the energies for  
 464 the other three simulations are still actively decreasing,  
 465 indicating that the photons are still scattering with the  
 466 outflow.

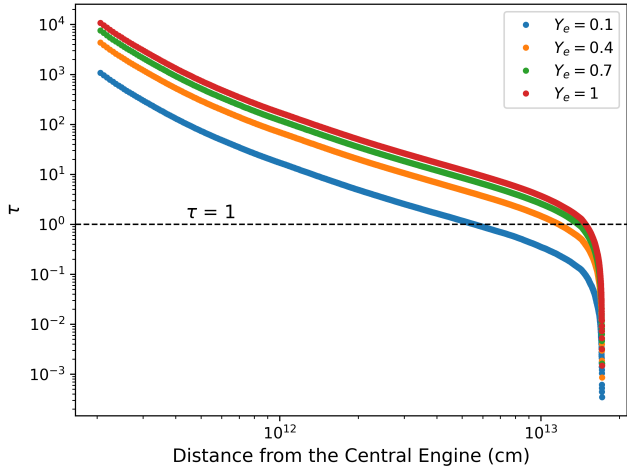
467 In past works, MCRaT has had successes in repro-  
 468 ducing various observational correlations of GRBs (Par-  
 469 sotan et al. 2018). Figure 7 shows the Amati and Yo-  
 470 netoku correlations for the four simulations considered  
 471 here, with viewing angles of  $\theta_v = 1^\circ, 2^\circ, 3^\circ$ . The Am-  
 472 ati relation in panel (a) shows two sets of points, one  
 473 set corresponding to calculations using photons from the  
 474 first 20 s of the lightcurves in Figure 1 (shown in solid  
 475 colors), while the other set uses photons from the first  
 476 40 s (shown in faded colors). Panel (b) shows the Yo-  
 477 netoku relation for photons obtained only during the first  
 478 40 s. Here, we see that our simulations agree well with  
 479 the Yonetoku relation, regardless of  $Y_e$  or which portion



**Figure 5.** Average photon energy computed as a function of distance from the central engine. Injected photons in all four of our simulations start off with similar energy and as the photons propagate further from the central engine photons in simulations with lower values of  $Y_e$  begin to decouple from the jet sooner, resulting in higher energies for those simulations. The energy from the  $Y_e = 0.1$  is nearly constant after  $R \sim 10^{13}$  cm, while the rest appear to be somewhat coupled to the jet by the time the photons reach the last RHD simulation frame at  $R \sim 10^{13}$  cm.

480 of the lightcurve we use. With the Amati relation, we  
 481 find that there is some strain when using photons from  
 482 all 40 s, which is similar to results from Parsotan & Laz-  
 483 zati (2018). However, we can recover the relation if we  
 484 restrict ourselves to photons from the first 20 s.

485 This is not an entirely new result, since MCRaT anal-  
 486 ysis of a similar simulation with a short-lived engine  
 487 (Parsotan et al. 2018) yielded analogous results. Quali-



**Figure 6.** Optical depth (Equation 9) for all four of our MCRaT simulations. Scatterings for each photon are counted, starting when they’re injected near the central engine, and accumulate as they propagate out to the photosphere. Initially,  $\tau \sim 10^3 - 10^4$  which is high enough to ensure that the photons are described by a Planck spectrum. There is a significant drop in  $\tau$  at  $\sim 1.8 \times 10^{13}$  cm, which corresponds to the average photon position in the last RHD frame. Photons that are fully decoupled from the outflow have an optical depth of  $\tau \sim 1$ , and the MCRaT simulations with  $Y_e = 0.1$  and  $Y_e = 0.4$  reach this value before the drop. The MCRaT simulations with  $Y_e = 0.7$  and  $Y_e = 1$ , however, reach this value right at the edge of the drop, indicating that these simulations are still somewhat coupled to the outflow.

tatively, it is also expected that shortening the duration of the engine reduces the total burst energy (moving points to the left in the Amati plane) with only a relatively small effect on the peak photon energy, likely in the upward direction since bursts tend to have harder spectra in their early phases.

Figure 8 shows the Golenetskii relation for all values of  $Y_e$ . Each point is calculated by finding the luminosity and time resolved  $E_{pk}$  over 1 s time bins for the first 20 s of the lightcurves in Figure 1. As with the Yonetoku relation, we find good agreement with observations without any restrictions on  $Y_e$  or photons. Moreover, we find that simulations with a larger neutron component tend to push peak energies and luminosities into better agreement with all three observational correlations.

The role of the neutron component in our simulations can be summarized by plotting spectral parameters as a function of  $Y_e$ . Panel (a) in Figure 9 shows how the Band parameters  $\alpha$  and  $E_0$  depend on  $Y_e$ , with best-fit power laws shown as dashed and dash-dotted lines.  $\beta$  is not shown due to the lack of a clear pattern in Figure 4. Neither  $\alpha$  nor  $E_0$  change very much when  $Y_e$  is near 1. However, as the size of the neutron component increases, corresponding to our simulations with  $Y_e = 0.4$

and  $Y_e = 0.1$ , the spectral parameters begin to change more dramatically. This is consistent with Figures 5 and 6 showing that simulations with a small neutron component are still somewhat coupled to the outflow. Had the injected photons been able to scatter for longer, it is likely changes would be more consistent across the range of  $Y_e$  considered here. Furthermore, the nearly symmetric slopes of trend lines in panel (a) are consistent with the strong correlation between  $\alpha$  and  $E_0$  on display in Figure 3. Additionally, as suggested by Figures 7 and 8, panel (b) in Figure 9 shows that the radiative efficiency increases as the size of the neutron component is increased, and that this effect isn’t dependent on viewing angle for the range considered here.

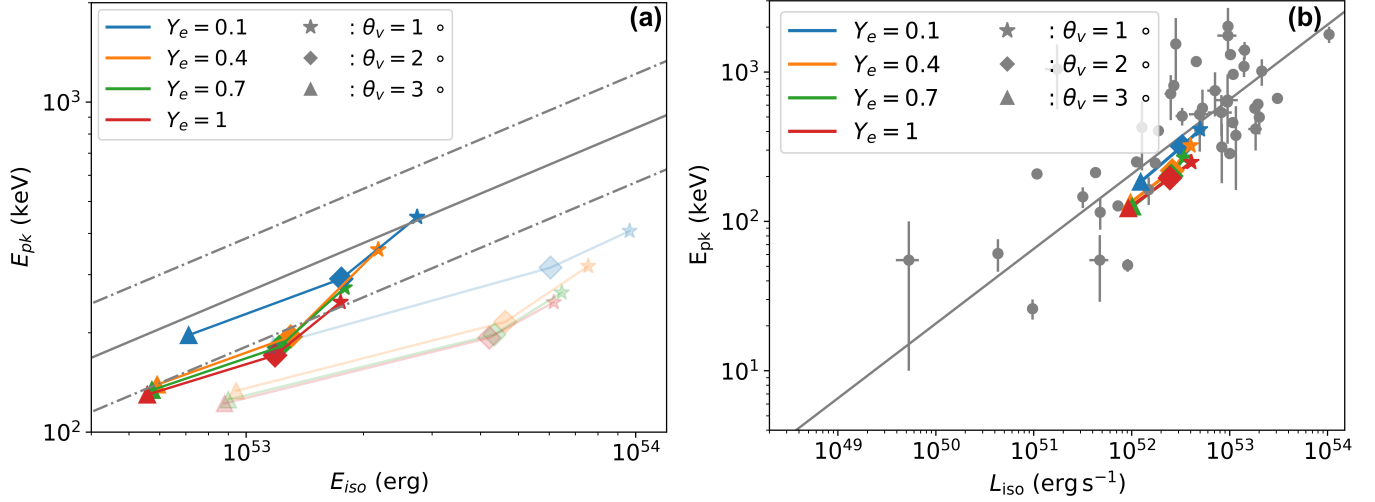
#### 4. SUMMARY AND DISCUSSION

In this paper we present results from a series of MCRaT radiative transfer simulations that probe the role that a neutron component in the outflow has on the radiation produced in a LGRB. Varying the density of the input RHD simulation controls the size of the neutron component via the lepton density in Equation 3, which in turn changes how the photons interact with the outflow until they reach the photosphere.

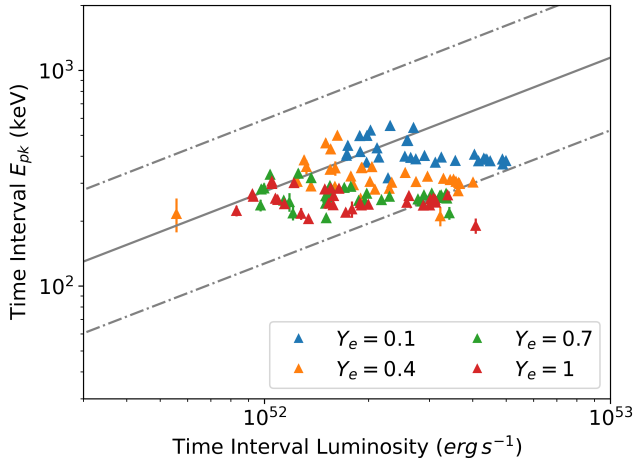
Observables, such as spectra and lightcurves, can be produced with the results of our MCRaT simulations. Our  $Y_e = 1$  lightcurve, and the associated time-resolved spectral parameters, show good agreement with past works using similar 16TI RHD simulations (e.g. Parson et al. 2021). We likewise find good agreement between our  $Y_e = 1$  time-integrated spectra and those seen in the same paper.

We find clear patterns in the spectral parameters as we vary  $Y_e$ . In particular, the break energy  $E_0$  (and thus the corresponding peak energy  $E_{pk} = [2 + \alpha]E_0$ ) is shifted to higher energies as  $Y_e$  decreases (and the size of the neutron component increases). A power-law fit to  $E_0$  as a function of  $Y_e^{-1}$  ( $E_0 \propto Y_e^\zeta$ ) yields an index  $\zeta = -0.26$ . This behavior is consistent with how the radiation in each of our MCRaT simulations decouple from the outflow. Our simulations with  $Y_e = 1$  and  $Y_e = 0.7$  are still relatively coupled to electrons in the outflow and so the photons are still appreciably cooling when they reach the last frame of the RHD simulation, resulting in a relatively weak power-law index. We also find that  $\alpha$  obtained from simulations with a smaller  $Y_e$  is consistent with a less thermal spectrum than when  $Y_e$  is larger, and that this behavior is likely due to a strong correlation between  $E_0$  and  $\alpha$ . This is supported corresponding power law for  $\alpha(Y_e^{-1})$ , which is 0.297. In contrast to the other parameters,  $\beta$  has no clear trend, possibly due to the fact that the high en-





**Figure 7.** a.) Amati and b.) Yonetoku correlations for all four values of  $Y_e$ . To obtain multiple observations for each simulation, we conduct a mock observation at three different viewing angles. In each figure, different shapes denote viewing angles and different colors denote different values of  $Y_e$ . In a.), the solid gray line shows the Amati Relationship from Tsutsui et al. (2009), with the dotted gray line showing the  $1\sigma$  confidence intervals. The faded colors show data obtained from the first 40 s of the lightcurves in Figure 1, while the solid colors show only the first 20 s. In b.), the gray dots show observational data of GRBs from Nava et al. (2012), with the solid gray line showing the line of best fit. All MCRaT simulations follow the Yonetoku relation, with lower values of  $Y_e$  corresponding to higher  $E_{pk}$ ,  $E_{iso}$ , and  $L_{iso}$ . Similarly to past work with MCRaT, there is some strain with the Amati relation, but this strain is removed when only considering photons from the first 20 s of the jet, when it is experiencing more shocks. Simulations with more neutrons fit both relations better, regardless of which portion of the lightcurve we consider.



**Figure 8.** Golenetskii relation for all values of  $Y_e$  over the first 40 s of each burst. Each value of  $Y_e$  is denoted by a different color, and each point is calculated by binning the lightcurves shown in Figure 1 into 1 s bins and calculating the time resolved  $E_{pk}$  for each bin. The gray solid indicates the Golenetskii relation from Lu et al. (2012), with the dotted gray lines representing the  $2\sigma$  intervals. Every simulation shows good agreement with the Golenetskii relation, with smaller values of  $Y_e$  corresponding to higher values of  $E_{pk}$  and Luminosity, similar to Figure 7

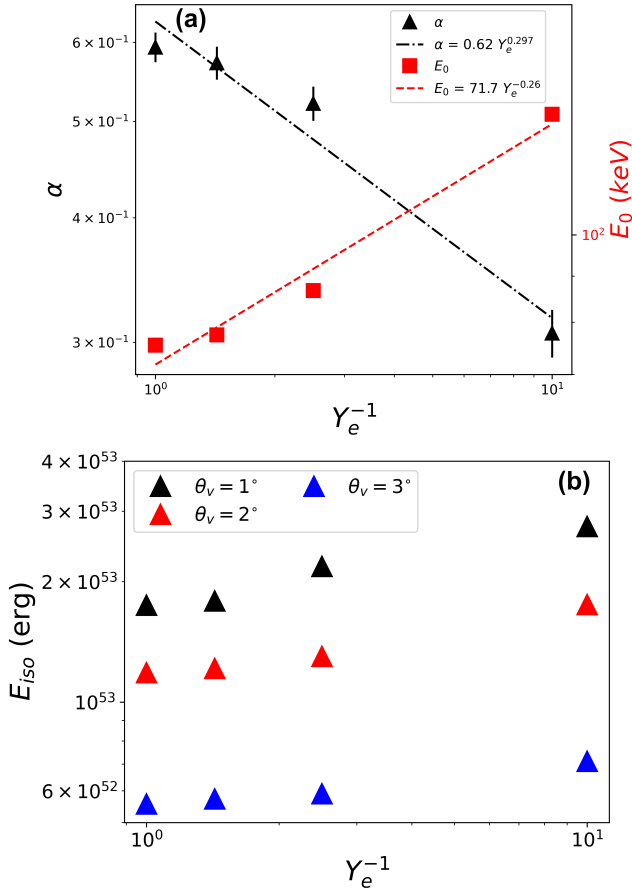
563 ergy tail of the spectrum forms relatively close to the

564 photosphere compared to the lower frequency parts of the  
565 spectrum, which are characterized by  $\alpha$  and  $E_0$ .

566 We also show how radiation evolves from the injected  
567 blackbody to the observed Band-type spectra by con-  
568 ducting mock observations, and calculating spectra, us-  
569 ing photons before they have finished scattering through  
570 the final RHD simulation frame. This shows that all  
571 parameters start off more or less equal across all our  
572 simulations, and at some point they begin to diverge  
573 until they settle to their final values near the photo-  
574 sphere. In particular,  $E_0$  starts off relatively high and  
575 decreases gradually as the injected photons propagate  
576 through and with the outflow. The low frequency index  
577  $\alpha$  mirrors this behavior, probably due to their strong  
578 correlation.

579 Similar behaviour is observed when we track the op-  
580 tical depth and average energy of the injected photons,  
581 beginning immediately after injection until they finish  
582 scattering. Both quantities start out high, indicating  
583 that that the photons are injected into a hot and dense  
584 outflow, and so are well-described by the blackbody  
585 spectrum. We see a gradual decoupling of the photons  
586 from the outflow, which mirrors the behaviour of the  
587 spectral parameters.

588 Finally, we check our simulations against the observa-  
589 tional correlations of Amati, Yonetoku, and Golenetskii  
590 (Amati et al. 2002; Yonetoku et al. 2004; Golenetskii



**Figure 9.** The  $Y_e$  effect on (a) the Band function parameters  $\alpha$  and  $E_0$ , and on (b) total radiated energy. The x-axis in both panels shows  $Y_e^{-1}$  so the size of the neutron component increases to the right. In (a), the red squares show the break energy  $E_0$  and the black triangles show the low energy slope  $\alpha$ , with the dashed and dashed-dotted lines showing the best fit trend lines for  $E_0$  and  $\alpha$ , respectively. The break energy  $E_0$  clearly increases as the neutron component gets larger, and  $\alpha$  clearly decreases nearly symmetrically as evidenced by the  $E_0$  slope of -0.26 and the  $\alpha$  slope of 0.297. The low energy slope  $\beta$  is not shown due to a lack of a clear pattern in Figure 4. In (b) the different colors show the isotropic energy from mock observations conducted at different viewing angles. As the neutron component is increased, the total radiated energy is increased across multiple viewing angles.

et al. 1983), and find good agreement with all three, regardless of  $Y_e$ . This agrees well with past work with MCRaT (Parsotan et al. 2018). However, given the maximum injection angle of  $3^\circ$ , we are limited to the number of observations we can make. Interestingly, while all of our simulations fit these correlations nicely, those with a larger neutron component tend to lie closer

to the trend lines than those with a smaller neutron component.

Generally, these results are very promising as they provide a mechanism for increasing the peak energy predicted by photospheric models of GRB prompt emission. While there is no consensus on the neutron content of GRB outflows, their presence in both core collapse supernovae and binary neutron star mergers suggests that peak energies are at least somewhat higher than seen in past works with MCRaT. The corresponding increase in total radiated energy (which is inevitable since the number of photons is conserved in a pure scattering process) increases radiative efficiency and brings the MCRaT predictions to better agreement with observational correlations. Both of these results can be interpreted by considering a baryon-loaded LGRB outflow: when the outflow is produced near the central engine, it is hot and dense and thus produces blackbody radiation. The outflow is subsequently heated via shocks as it bores its way through the stellar envelope. Eventually the outflow will clear the envelope and begin to cool while its internal energy is converted to bulk kinetic energy. Thus, the initially hot blackbody radiation also cools as it gradually decouples from the matter component of the outflow. When there is a neutron component in the outflow, radiation will decouple sooner and will thus carry with it a signature of the outflow from when it had converted less of its internal energy into bulk kinetic energy, thereby resulting in the observed increase in radiative efficiency. An important consideration of the material component of GRB outflows, not treated here, is that of mixing. The jet, cocoon, and stellar envelope could all have different neutron components, and mixing between these could thus modify observables. This effect would likely be more prominent at larger viewing angles where mixing is more prominent. Furthermore, the methods discussed here could naturally be extended to sGRB simulations emerging from binary neutron star mergers. Both of these considerations will be explored in future works.

N. W. and D.L. acknowledge support from NSF grant AST-1907955

*Facilities:* Resources supporting this work were provided by the NASA High-End Computing (HEC) Program through the NASA Advanced Supercomputing (NAS) Division at Ames Research Center.

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