

1    **Advancing Passive Microwave Retrievals of Precipitation using CloudSat**  
2    **and GPM Coincidences: Integration of Machine Learning with a Bayesian**

3                                    **Algorithm**

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10 ABSTRACT: Integration of machine learning with a classic Bayesian algorithm is investigated for  
11 passive microwave precipitation retrievals using coincidences from the Global Precipitation Mea-  
12 surement core satellite and the *CloudSat* Profiling Radar (CPR). Among several machine learning  
13 models, the eXtreme Gradient Boosting Decision Tree (XGBDT), equipped with a weighted cross  
14 entropy loss function, exhibits the highest accuracy in the detection of precipitation occurrence  
15 and phase with a true positive rate greater than 94 (98)% and a false positive rate smaller than 1  
16 (1)% for rainfall (snowfall) over land and oceans with no frozen surfaces. Bayesian retrievals in  
17 the embedding space of a fully connected multi-layer perception (MLP), equipped with a focal loss  
18 function, provide the most accurate estimates of the rates with a mean absolute error of less than  
19 1.80 (0.15)  $\text{mm hr}^{-1}$  for rainfall (snowfall). Mutual information analysis unravels that beyond the  
20 near-surface air temperature, the 37 and  $183 \pm 7(3)$  GHz are the most informative channels for phase  
21 detection over the ocean (land). The physical consistency of the retrievals and new explanations of  
22 the precipitation passive microwave signatures are provided through partial dependence analysis  
23 and annual comparison with the reanalysis data.

24 SIGNIFICANCE STATEMENT: The cloud profiling radar (CPR) onboard the CloudSat satellite  
25 provided information about light precipitation and snowfall on a quasi-global scale with unprece-  
26 dented accuracy for more than 15 years. This study examines how machine learning (ML) and its  
27 integration with classic Bayesian statistical approaches can learn from coincidences of CPR and  
28 the radiometer onboard the global precipitation measurement (GPM) core satellite to expand our  
29 algorithmic tools for a better understanding of precipitation global variability. New approaches  
30 are used to interpret the results of the ML model in connection with the underlying physics con-  
31 trolling the precipitation phase change processes and their microwave signatures. Comparisons  
32 with observationally constrained simulations from the Earth system models unravel where satellite  
33 observations can provide new insights or need further improvements. The outcome paves the  
34 way to expand our understanding of the impacts of climate change on snowfall patterns and the  
35 hydrologic water cycle.

## 36 1. Introduction

37 Precipitation is monitored remotely from space using passive and active spaceborne instruments  
38 in infrared and microwave regions of the electromagnetic spectrum. Microwaves can penetrate the  
39 raining clouds and interact with their microphysical properties (Wilheit et al. 1977; Olson 1989).  
40 Over the past few decades, the passive microwave (PMW) precipitation retrieval algorithms have  
41 advanced along different trajectories depending on the dynamics of surface emissivity over ocean  
42 and land.

43 Over radiometrically cold open oceans, with large-scale variability of surface emissivity, the  
44 scatter-free theory of radiative transfer (Wilheit et al. 1977) was used to connect precipitation rates  
45 to their emission and absorption properties in low-frequency channels below the oxygen absorption  
46 line at 60 GHz. Discrete dipole approximation of the raindrop scattering phase function (Liu and  
47 Curry 1992) was employed, and theoretically derived empirical regression equations were used  
48 (Kummerow and Giglio 1994; Petty 1994) to retrieve rainfall rates from observations by the Special  
49 Sensor Microwave/Imager (SSM/I). The regression approaches evolved into Bayesian retrieval  
50 algorithms (Kummerow et al. 1996, 2001; Petty and Li 2013; Kummerow et al. 2015, among  
51 others) that rely on offline libraries of a statistically representative number of simulated/observed

52 brightness temperatures (TB) for computationally efficient inversions of the radiative transfer  
53 equation.

54 Over highly emissive and radiometrically complex land surfaces, simulations of TBs of raining  
55 clouds have been challenging due to the uncertainties chiefly related to the quantification of the  
56 surface emissivity values. Consequently, the initial algorithms remained predominantly empirical  
57 and used thresholding (Grody 1991) and regression models (McCollum and Ferraro 2003) for  
58 relating the scattering signatures of precipitation to its rate, using 80–100 GHz channels (Gopalan  
59 et al. 2010), with often uncertain outcomes over snow-cover surfaces (Ebtehaj et al. 2016). In  
60 parallel to the improvement of active precipitation retrievals over land and oceans (Grecu et al.  
61 2016; Iguchi et al. 2000), Bayesian PMW algorithms used libraries of coincident observations  
62 from the precipitation radar and microwave imagers (Petty and Li 2013; Ebtehaj et al. 2015) and  
63 reported improved estimates over radiometrically complex surfaces.

64 Motivated by the launch of the CloudSat (Stephens et al. 2009) and the Global Precipitation  
65 Core Satellite (GPM) (Skofronick-Jackson et al. 2017), a body of research was devoted to studying  
66 the microwave propagation properties of snowing clouds (Bennartz and Bauer 2003; Skofronick-  
67 Jackson et al. 2004; Skofronick-Jackson and Johnson 2011) and characterizing the sensitivity of  
68 high-frequency channels to ice aloft and snowfall scattering. Radiative transfer modeling and  
69 ancillary forecast data were utilized to implement Bayesian algorithms for snowstorm retrievals  
70 using the Advanced Microwave Sounding Unit (AMSU) high-frequency TBs (Noh et al. 2006;  
71 Kim et al. 2008).

72 Liu and Seo (2013) demonstrated that snowfall high-frequency scattering could be masked by the  
73 emission of supercooled liquid water content in snowing clouds and called for empirical approaches  
74 that rely on coincident observations from CloudSat. Kongoli et al. (2003) utilized empirical  
75 thresholding of low and high-frequency AMSU channels for global snowfall retrievals over snow-  
76 free land surfaces. Hybrid algorithms were proposed (Kongoli et al. 2015; You et al. 2022) that  
77 used logistic regression and iterative inversion of a one-layer two-stream radiative transfer model  
78 (Meng et al. 2017) using the Advanced Technology Microwave Sounder (ATMS) data. Despite  
79 substantial progress, comparisons of satellite retrievals of high-latitude precipitation and reanalysis  
80 data (Munchak and Skofronick-Jackson 2013; Behrangi et al. 2016; You et al. 2023) uncovered  
81 that PMW satellite snowfall data are still highly uncertain, especially over radiometrically complex

82 ice sheets (Milani et al. 2018), snow-covered lands (Rahimi et al. 2022) and those areas affected  
83 by extreme moisture transport from large inland lakes (Milani et al. 2021).

84 Modern PMW retrieval algorithms have emerged to utilize machine learning (ML) advances  
85 (Tapiador et al. 2004). In one of the early attempts, Sanò et al. (2018) trained a shallow neural  
86 network for rainfall retrievals, using coincidences (Greco et al. 2016) of the GPM Microwave  
87 Imager (GMI) and the GPM dual-frequency precipitation radar (DPR). The algorithm was further  
88 expanded for snowfall retrievals using GMI and CloudSat coincidences based on a random forest  
89 (RF) (Rysman et al. 2018) and later on using an XGBDT for estimation of the rates (Rysman et al.  
90 2019). Similarly, Tang et al. (2018) proposed a fully connected neural network with two hidden  
91 layers and trained it, chiefly using coincidences of GMI, DPR, and CPR data, for high-latitude rain  
92 and snowfall retrievals.

93 Unlike pixel-level ML models, Goroooh et al. (2022) used a U-Net architecture (Ronneberger  
94 et al. 2015) for rainfall retrieval using both GPM and geostationary infrared spatial data. Orescanin  
95 et al. (2021) deployed a Residual Network (ResNet, He et al. 2016) to distinguish convective  
96 precipitation using the GMI-DPR coincidences. Pfreundschuh et al. (2022) expanded the Bayesian  
97 Goddard Profiling Algorithm (Kummerow et al. 2015) using quantile regression convolutional  
98 neural networks (Taylor 2000). More recently, a convolutional neural network (Bannai et al. 2023)  
99 was proposed that used a weighted average of cross entropy and mean squared error (mse) loss  
100 functions for one-step PMW precipitation retrievals using GPM and DPR coincidences.

101 This paper extends the previous research through the following contributions using the latest  
102 version of CloudSat and GPM satellite coincidences (Turk et al. 2021). (i) The paper presents a  
103 two-step PMW retrieval framework and examines it for precipitation occurrence and phase detection  
104 (step 1) and rate estimation (step 2). The phase determination does not rely on thresholding based  
105 on the near-surface air temperature and uses it as an input. (ii) Different pixel-level ML models  
106 including random forests (Breiman 2001), XGBDT (Chen and Guestrin 2016), and MLP are tested  
107 and compared. Although convolutional neural networks (CNNs) have shown some success with  
108 limited horizontal coverage in other studies (Amell et al. 2024), we excluded CNNs here due to  
109 the minimal spatial overlap in GMI-CPR coincidences, which further restricts the spatial context  
110 needed for CNNs to perform effectively in this framework. (iii) A new precipitation rate estimation  
111 framework is proposed by conducting Bayesian PMW retrievals in the embedding space of an MLP

112 that reduces the uncertainty of rate estimation beyond the deployed off-the-shelf ML algorithms  
113 using proper reflectivity ( $Z$ ) to rainfall rate ( $R$ ) or snowfall rate ( $S$ ) relationships. (iv) The causal  
114 relationships between TBs and precipitation occurrence and phase change are unveiled through  
115 explainable ML using mutual information (Peng et al. 2005) and partial dependence analyses  
116 (Hastie et al. 2009).

117 The paper is organized as follows. Section 2 describes the data, and the methodology is explained  
118 in Section 3. The results, findings, and discussions are presented in Section 4. Section 5 provides  
119 a summary and points out future research directions.

## 120 2. Data sets

### 121 a. Satellite coincidences and ancillary data

122 This study uses the latest version of near-coincident GMI brightness temperatures with CPR  
123 (DPR) active retrievals (2B-CSATGPM) from March 2014 to August 2019 (January 2021 to  
124 December 2022) – the last date reported by the CloudSat data processing center (personal com-  
125 munication with Dr. J. Turk at Jet Propulsion Laboratory, Turk et al. 2021) as well as the ERA5  
126 reanalysis data (Hersbach et al. 2018). The precipitation products and land surface types from  
127 the Goddard Profiling Algorithm (GPROF, Kummerow et al. 2015, V07) are also used for cross-  
128 comparisons and assessments. It should be noted that the surface type used by GPROF is carried  
129 within the GPM-CloudSat dataset.

130 The CPR near surface snowfall data are from the latest level-II products including the 2C-  
131 PRECIP-COLUMN (Haynes et al. 2009) and the 2C-SNOW-PROFILE (Wood et al. 2013, 2014)  
132 that contain the information related to precipitation phase and snowfall rate, respectively. To avoid  
133 ground-clutter contamination, the near-surface rates within radar bins above the oceans (land) at  
134 720 m (1200 m) height (Kulie et al. 2010) are used. Note that overland rainfall retrievals are  
135 unavailable for CloudSat products. Even though the CPR-based snowfall retrievals are central to  
136 the goal of the paper, for the sake of completeness, the near-surface rainfall data from 2A-DPR Ku-  
137 band product (Iguchi et al. 2018), based on blind zone extrapolations (Hirose et al. 2021; Shimizu  
138 et al. 2023), are used to train the algorithm and present the results for a multiclass precipitation  
139 phase detection. Note that the DPR precipitation phase is determined via a combination of the  
140 bright band detection algorithm evaluation of the atmospheric temperature profile (Iguchi et al.

141 2018). Meanwhile, CloudSat 2C-PRECIP-COLUMN uses the estimated height of the melting  
142 layer from the European Centre for Medium-Range Weather Forecasts (ECMWF) reanalysis and  
143 models for expected snow particle melting to distinguish snow from rain (Wood et al. 2014).

144 It is worth noting that, unlike the CPR, research suggested that DPR is not sufficiently sensitive in  
145 capturing backscattering signatures of light precipitation (Liu 2008; Hamada and Takayabu 2016)  
146 with rates less than  $0.2\text{--}0.5\text{ mm hr}^{-1}$  (Skofronick-Jackson et al. 2013; You et al. 2017; Casella et al.  
147 2017). At the same time, it is essential to highlight that for intense storms, the CPR reflectivity  
148 tends to saturate near 20 dBZ as the size of the hydrometeors approaches the wavelength (Matrosov  
149 and Battaglia 2009; Liu 2008). This saturation often increases the uncertainty of the retrievals as  
150 the precipitation intensity grows (Lécuyer and Stephens 2002; Tang et al. 2017).

#### 151 *b. Training and validation data sets*

152 We use imbalanced data for training, validation, and testing based on the available coincidences.  
153 The dataset for training and validation was randomly permuted and split into 70% for training and  
154 30% for validation. The test set was constructed using independent data from the final year of each  
155 overlap period, with January 2021 to December 2021 for GMI-DPR and July 2018 to August 2019  
156 for GPM-CloudSat. To construct our training and testing data sets, we confine our considerations  
157 to the GMI and DPR (CPR) rainfall (snowfall and clear sky) coincidences. For snowfall data,  
158 we utilize DPR data only for heavy rates where CPR is likely to saturate with reflectivity values  
159 greater than 15–20 dBZ (Matrosov and Battaglia 2009). Using Z-S relationship by Liu (2008), this  
160 reflectivity range translates into  $2.2\text{--}5.6\text{ mm hr}^{-1}$ . To alleviate this issue, we use DPR snowfall  
161 when CPR snow rates are  $\geq 4\text{ mm hr}^{-1}$ , constituting only a small fraction of data points.

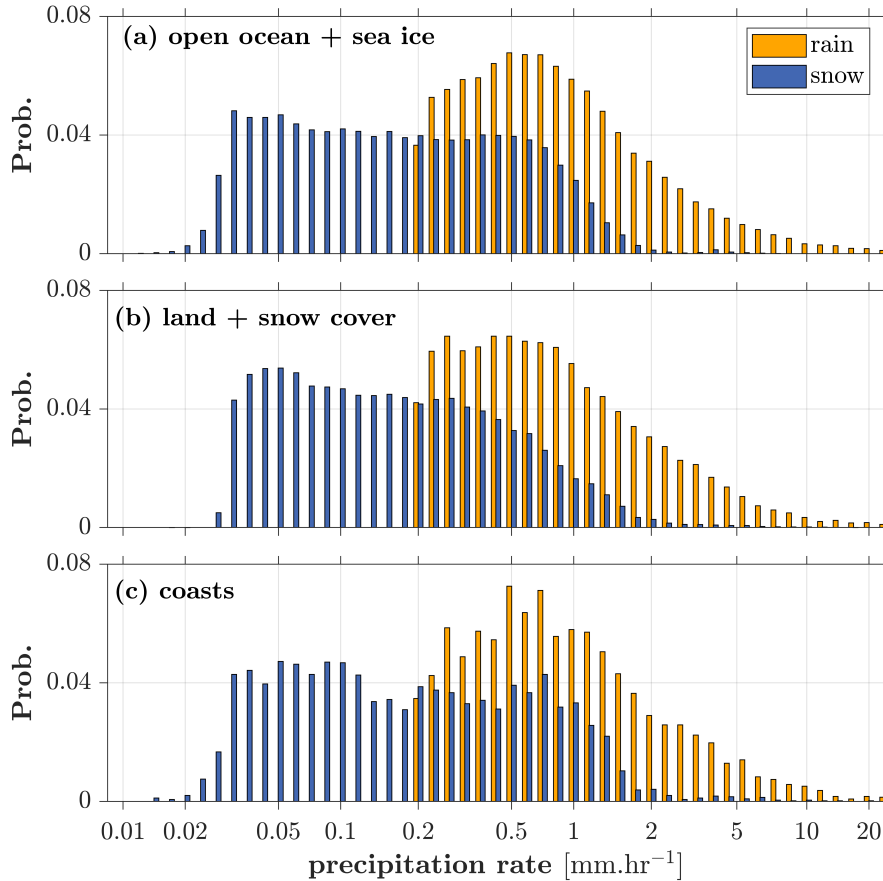
162 The training data is augmented by the ERA5 2-m air temperature (T2m), water vapor path (WVP),  
163 cloud liquid (LWP), and ice (IWP) water paths as well as convective available potential energy  
164 (CAPE). The data are stratified only based on five different surface types including open oceans,  
165 sea ice, land surfaces with no snow, snow cover, and coastal zones through agglomerating the  
166 dynamic surface types provided by the Goddard Profiling Algorithm (GPROF, Kummerow 2016).

167 The number of coincidences differs over the surface types due to their spatial extent and satellite  
168 coverage. We use an imbalanced representation of rain, snow, and clear sky classes across each  
169 surface type to train the ML classification algorithms to ensure unbiased retrievals. A summary

Surface type	Ocean	Land	Coast	Sea ice	Snow cover
# imbalanced samples	3.4E+6	1.8E+6	5E+5	4.1E+5	3.3E+5

176 TABLE 1. The total number of imbalanced data points over five different surface types used for training and  
 177 testing.

170 of the number of available coincidences is reported in Tab. 1. Probability histograms of the  
 171 training data are also shown over three grouped surface types in Fig. 1. The DPR rainfall rates are  
 172 positively skewed over all surfaces with a global mean of around  $1.7 \text{ mm hr}^{-1}$ . The distribution of  
 173 CPR snowfall rates is much wider than the DPR rainfall distribution and has a significantly smaller  
 174 global mean value  $\sim 0.3 \text{ mm hr}^{-1}$ . While the tail of the rainfall distributions extends to almost  
 175  $20 \text{ mm hr}^{-1}$ , the bulk of the snowfall density is accumulated below  $2 \text{ mm hr}^{-1}$ .



178 FIG. 1. Probability histograms of the rainfall and snowfall data over three grouped surface types as explained  
 179 in the text.

### 180 3. Methodology

#### 181 a. Retrieval algorithm

182 In the first phase of the algorithm, a classification model detects the occurrence and phase of  
183 precipitation, given pixel-level inputs of TBs and the ERA5 physical precipitation drivers. In the  
184 second step, a regression model estimates the rate of precipitating pixels. We take a two-step  
185 approach mainly because optimal classification and regression loss functions can be deployed  
186 separately. The regression network with a regression loss function often leads to a lower detection  
187 accuracy than those equipped with classification loss functions. Moreover, a two-step paradigm  
188 allows phase detection and does not require thresholding using near-surface air temperature values.  
189 Thus the algorithm can be trained for different snowfall and rainfall Z-S, and Z-R relationships.

190 As previously explained, for the phase detection, over each surface type, a set of classic machine  
191 learning algorithms are examined including  $k$ -nearest neighbors ( $k$ NN, [Cover and Hart 1967](#)),  
192 random forest (RF, [Breiman 2001](#)), XGBDT ([Chen and Guestrin 2016](#)), and a deep multi-layer  
193 perception (MLP) ([Atkinson and Tatnall 1997](#)). For the estimation step, we implement a Bayesian  
194 algorithm called the shrunken locally linear embedding algorithm for retrieval of precipitation  
195 (ShARP, [Ebtehaj et al. 2015](#)) in the feature of an MLP.

#### 196 1) DETECTION STEP

197 We employ the same procedure for using the  $k$ -nearest neighbor for PMW precipitation retrievals  
198 in a Bayesian setting as explained in ([Ebtehaj et al. 2015, 2020](#)) with the number of nearest  
199 neighbors ranging from 10–30. All machine learning models in the detection step are trained  
200 based on the weighted cross entropy ([Wang et al. 2020](#)). The weighted cross entropy loss accounts  
201 for the effects of imbalanced labels as the number of rain and snowfall labels is much smaller than  
202 the clear sky cases. This loss function for a multi-class classification can be expressed as follows:

$$\mathcal{L}(\mathbf{x}_i, \boldsymbol{\theta}) = - \sum_{i=1}^N \alpha_i y_i(\mathbf{x}_i) \log \hat{y}_i(\mathbf{x}_i), \quad (1)$$

203 where  $\alpha_i$  is the imbalance parameter,  $y_i$  is the one-hot encoding of the labels of input features  $\mathbf{x}_i$ ,  
204  $\hat{y}_i$  is the ML predicted probability of  $y_i$ , and  $\boldsymbol{\theta}$  denotes the trainable parameters of the ML. Since

205 the training set is imbalanced towards clear-sky data points, improved detection is expected when  
206  $\alpha_i > 1$  is assigned for rain and snowfall classes.

207 We use an exhaustive grid search approach (Bergstra and Bengio 2012) for the hyperparameter  
208 tuning of the ML models. In particular, the RF and XGBDT are tuned for the number of estimators  
209 (i.e., 100–300), maximum tree depth (i.e., 15–30), and minimum sample split number (i.e., 2–10).  
210 Additionally, the learning rate, ranging from 0.01 to 0.3, is optimized for XGBDT. The architecture  
211 of the MLP for detection features six layers with Rectified Linear Units (ReLU) and a 15% dropout  
212 which is trained using the Adam algorithm (Kingma and Ba 2014). The batch size (i.e., 1024),  
213 the initial learning rate (i.e., 0.001), and the number of neurons (i.e., 50) are optimized through a  
214 random grid search approach.

215 The optimal imbalance weights  $\alpha_i$  are obtained through additional exhaustive hyperparameter  
216 tuning based on the maximization of the F1-score. Conceptually, larger values of  $\alpha$  increase the  
217 true positive rate (TPR) or recall  $TP/(TP+FN)$  but decrease precision  $TP/(TP+FP)$ , where TP, FN,  
218 and FP are the true positives, false negatives, and false positives. Selecting an appropriate  $\alpha$  to  
219 maximize the F1-score (i.e., the harmonic mean of the precision and recall) ensures a balance  
220 between precision and recall. Our analysis shows that the effects for different choices of  $\alpha$  in the  
221 F1-score are uniform across the used ML models and land surface types. We conducted several  
222 hyperparameter tuning experiments and assigned optimal weights of 5 (snowfall), 2 (rainfall), and  
223 1 (clear sky) in Eq. 1.

## 224 2) ESTIMATION STEP

225 For using the ML models in the estimation step, we only change their penalty functions to a  
226 least-squares regression loss function and train them based on active retrievals using proper  $Z-R$   
227 and  $Z-S$  relationships. As will be shown later, in the detection phase, XGBDT and MLP provide  
228 comparable results; however, the former indicates marginally superior performance, especially for  
229 surface types with a smaller number of samples (e.g., sea ice). In the estimation phase, we realized  
230 that on average, the mean-squared of the MLP is greater than XGBDT appreciably for rainfall and  
231 snowfall over different land surface types. We conjecture that the training sample size is the main  
232 contributing factor, as neural networks often need a large sample size, especially for imbalanced  
233 data with skewed distribution. This is consistent with recent research showing that for tabular

234 or pixel-level data, the gradient-boosting decision trees provide state-of-the-art results beyond the  
 235 most advanced deep learning methods (Borisov et al. 2024). However, as will be presented later,  
 236 a classic Bayesian algorithm in the embedding space of the MLP can provide the most accurate  
 237 estimation of precipitation rates over most of the surface classes.

238 To that end, the Bayesian Shrunken locally linear embedding Algorithm for Retrieval of Precip-  
 239 itation (Ebtehaj et al. 2015) is implemented in the embedding space of the MLP, hereafter called  
 240 ShARP<sup>ML</sup>. This model comprises four fully connected layers, each containing 75 neurons and  
 241 utilizing the ReLU activation function. We discretize the precipitation rates and recast the rate es-  
 242 timation into a multi-class classification problem. This formalism enables the network to learn the  
 243 features associated with the entire probability distribution of precipitation rather than those that can  
 244 be encoded solely through a least-squares minimization. However, the defined precipitation rate  
 245 classes are significantly imbalanced due to the positive skewness of the precipitation distribution  
 246 and a continuous retrieval is infeasible.

247 To alleviate the class imbalance problem, we use the focal loss,  $F_L(p, q) =$   
 248  $-\sum_{x \in X} \eta(x) [1 - q_X(x)]^\gamma p_X(x) \log q_X(x)$ , in which  $p_X(x)$  and  $q_X(x)$  are distributions of observed  
 249 and predicted class probabilities, respectively. This loss function modifies the cross-entropy in two  
 250 ways. First, the parameter  $\eta$  balances the weights of the loss associated with each class, which  
 251 is set to the inverse of the frequency of the within-class sample size. Second, as the modulating  
 252 factor  $\gamma > 0$  increases, it amplifies the impacts of low-probability classes in the total loss with  
 253 recommended values of  $\gamma = 2$  to 5. Here  $\eta$  is chosen based on the frequency of the different classes  
 254 and the  $\gamma = 2$ .

255 The pre-trained network maps the inputs onto a lower-dimensional embedding space that feeds  
 256 the Bayesian retrieval algorithm for obtaining continuous retrievals. By the embedding space,  
 257 here we mean the outputs of the last fully connected  $(l - 1)^{\text{th}}$  layer of the pre-trained MLP that is  
 258  $\mathbf{z} = \mathcal{F}^{l-1}(\mathbf{x}) \in \mathbb{R}^{n_f}$ , where  $n_f = 10$  represents the number of neurons in the last layer and  $\mathbf{x} \in \mathbb{R}^{18}$   
 259 represents the dimension of inputs consisting 13 TB channels and 5 ERA5 variables.

260 In particular, let us assume that  $M$  vectors of input predictors  $\mathbf{x}_i \in \mathbb{R}^n$  and their corresponding  
 261 precipitation rates  $\mathbf{r}_i$  are collected in a database  $\mathcal{B} = \{(\mathbf{x}_i, \mathbf{r}_i)\}_{i=1}^M$ , which is transformed into the  
 262 embedding space as  $\mathcal{B}_f = \{(\mathbf{z}_i, \mathbf{r}_i)\}_{i=1}^M$  – using the pre-trained MLP. For a given observed predictor  
 263  $\mathbf{x}_j^o$ , we can obtain its counterpart in the embedding space,  $\mathbf{z}_j^o = \mathcal{F}^{l-1}(\mathbf{x}_j^o) \in \mathbb{R}^{n_f}$  and then use

264 the Bayesian model to retrieve the precipitation rate. Specifically, for each  $\mathbf{z}_j^o$ , its  $k$ -nearest-  
 265 neighbors  $\{\mathbf{z}_k\}_{k=1}^K$  and their corresponding rates  $\{\mathbf{r}_k\}_{k=1}^K$  are isolated in  $\mathcal{B}_f$  to retrieve the rate as  
 266  $\hat{\mathbf{r}}_j = \sum_{k=1}^K w_k \mathbf{r}_k$ .

267 To calculate the weights  $w_k$ , we employ a ridge regression:  $\|\mathbf{z}_j^o - \mathbf{Z}_k \mathbf{w}\|_2^2 + \lambda \|\mathbf{w}\|_2^2$  such that  
 268  $\sum_k w_k = 1$ ,  $w_k > 0$ . Here,  $\|\cdot\|_2^2$  is the 2-norm,  $\mathbf{Z}_k \in \mathbb{R}^{n_f \times K}$  denotes a matrix containing  $\{\mathbf{z}_k\}_{k=1}^K$  in  
 269 its column space,  $\mathbf{w} \in \mathbb{R}^K$  is a vector representation of weights, and  $\lambda > 0$  represents a regularization  
 270 parameter, which is set to 0.01 through cross-validation. One of the important features of the  
 271 ShARPM<sup>L</sup> is that the statistics (e.g., variance, quantiles) of  $\{\mathbf{r}_k\}_{k=1}^K$  can provide an uncertainty  
 272 bound around  $\hat{\mathbf{r}}_j$ .

### 273 *b. Explainable machine learning*

274 Two key questions often emerge for ML-based PMW retrieval of precipitation. What are the  
 275 most important predictors? Can ML capture the expected underlying governing physical laws?  
 276 To shed light on these questions, we employ the maximum relevance and minimum redundancy  
 277 (MRMR, [Peng et al. 2005](#)) and the partial dependence (PD) analysis ([Hastie et al. 2009](#)).

#### 278 1) MINIMUM REDUNDANCY AND MAXIMUM RELEVANCE

279 The MRMR method uses mutual information to identify the most informative and the least  
 280 redundant features among the predictors irrespective of the ML algorithm. Specifically, it finds an  
 281 optimal set of predictors  $\mathcal{S}$  that maximizes the relevance  $A_{\mathcal{S}} = 1/|\mathcal{S}| \sum_{x \in \mathcal{S}} I(x, y)$  to the response  
 282 variable with minimum internal redundancies  $B_{\mathcal{S}} = 1/|\mathcal{S}|^2 \sum_{x, z \in \mathcal{S}} I(x, z)$ , where  $I(\cdot, \cdot)$  is the mutual  
 283 information and  $|\mathcal{S}|$  denotes the cardinality of  $\mathcal{S}$ . The MRMR method computes the Mutual  
 284 Information Quotient (MIQ) for each predictor outside the selected set  $\mathcal{S}^c$ , by maximizing the ratio  
 285 of its relevance to the response variable over the average redundancy with the selected features.

286 This is mathematically expressed as  $\max_{x \in \mathcal{S}^c} MIQ_x = \max_{x \in \mathcal{S}^c} \frac{I(x, y)}{\frac{1}{|\mathcal{S}|} \sum_{z \in \mathcal{S}} I(x, z)}$ .

#### 287 2) PARTIAL DEPENDENCE ANALYSIS

288 The PD analysis offers interpretability of the relationship between the input predictors  $\mathbf{x}_i$  and  
 289 the response of an ML model  $f(\cdot)$ . To that end, for a set of  $m$  predictors  $\mathbf{X} = \{\mathbf{x}_i\}_{i=1}^m$ , the  
 290 approach computes the dependency of a response to  $\mathbf{x}_i$  by marginalizing over the complement

291 set  $\mathbf{X}^{C_i} = \mathbf{X} - \{\mathbf{x}_i\}$  as  $g(\mathbf{x}_i) = \int f(\mathbf{x}_i, \mathbf{X}^{C_i}) p_C(\mathbf{X}^{C_i}) d\mathbf{X}^{C_i}$ , where  $p_C(\mathbf{X}^{C_i})$  denotes the probability  
292 distribution of  $\mathbf{X}^{C_i}$ .

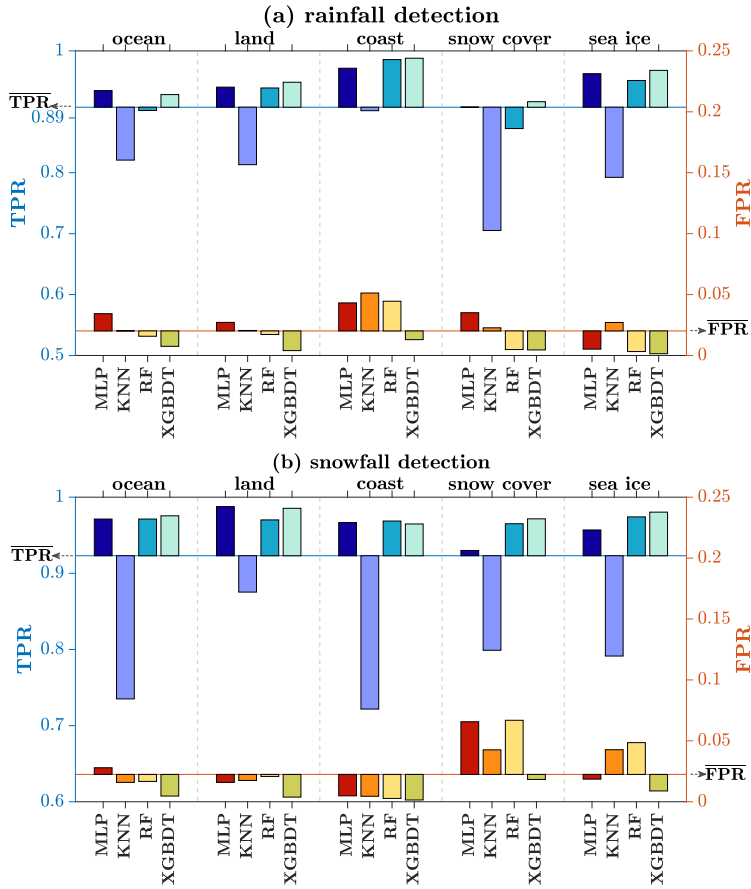
## 293 4. Results and Discussion

294 The results are shown and discussed in four steps. First, we show the performance metrics of  
295 classification and estimation steps for the testing data sets. Second, the results of explainable ML  
296 are presented. Third, orbital retrievals of a few snowstorms over Greenland and the North Atlantic  
297 Ocean are presented. Lastly, we provide the annual retrievals for all GMI orbits in the year 2022  
298 and compare them with the current official GPM product and ERA5 reanalysis data. We need  
299 to emphasize that the comparisons with the GPROF product are subjective as the algorithms are  
300 different and use fundamentally different training data sets.

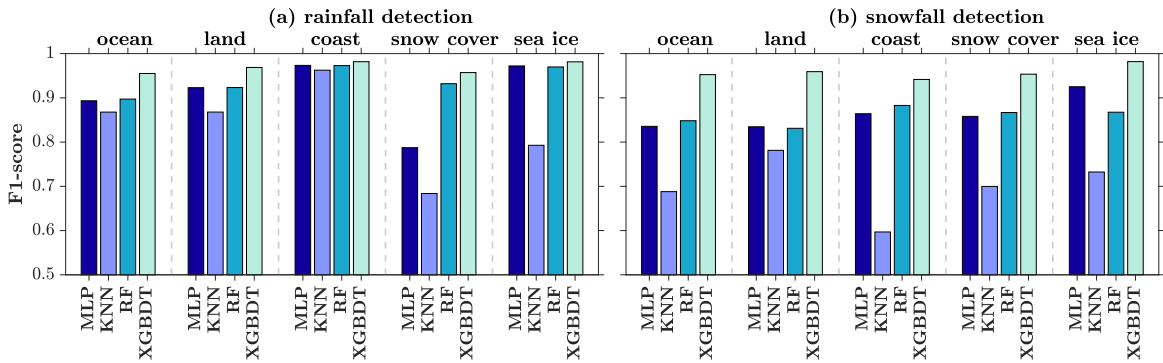
### 304 a. Detection quality metrics

305 Figure 2 shows the TPR (TPR = TP/TP+FN) and false positive rates (FPR = FP/FP+TN) over  
306 different surface types, where TN denotes true negatives. The  $k$ NN has the lowest performance  
307 for rainfall detection (Fig. 2a), across all land surface types. Typically, when the training sample  
308 size is sufficiently large, the MLP slightly outperforms the decision trees; however, based on the  
309 available training sample sizes, the XGBDT exhibits the highest overall performance across most  
310 surface types. Specifically, the TPR in rainfall detection over the ocean (land) is around 94 (95)%  
311 for MLP and XGBDT (Fig. 2a). However, the XGBDT reduces the false alarm rate from around 3  
312 (2)% in MLP over the ocean (land) to around 1%. Over the coasts, both decision tree-based models  
313 outperform the MLP with higher (lower) TPR (FPR) values of 2–3 (1–3)%.

314 For the snowfall detection (Fig. 2b), the  $k$ NN shows the lowest TPR over all surface types. The  
315 XGBDT performs the best consistently almost over all surface types, except coastal regions, with  
316 a TPR greater than 95% and an FPR below 2%. Overall, the mean TPR values among different  
317 ML models are larger for snowfall than rainfall detection by almost 5%, while the FPR values  
318 are approximately the same. Additionally, we compare the F1-score of all ML approaches. Once  
319 again, XGBDT consistently shows the highest F1-score across all land surface and precipitation  
320 types as shown in Fig. 3. Therefore, we use XGBDT for the detection step.



301 FIG. 2. The true (TPR) and false positive rate (FPR) of rainfall (top) and snowfall (bottom) detection using four  
 302 different ML classification models over different surface types, where the  $\overline{\text{TPR}}$  and  $\overline{\text{FPR}}$  represent the average  
 303 values across all models.



321 FIG. 3. F1-score of rainfall (left) and snowfall (right) detection using four different ML classification models  
 322 over different surface types.

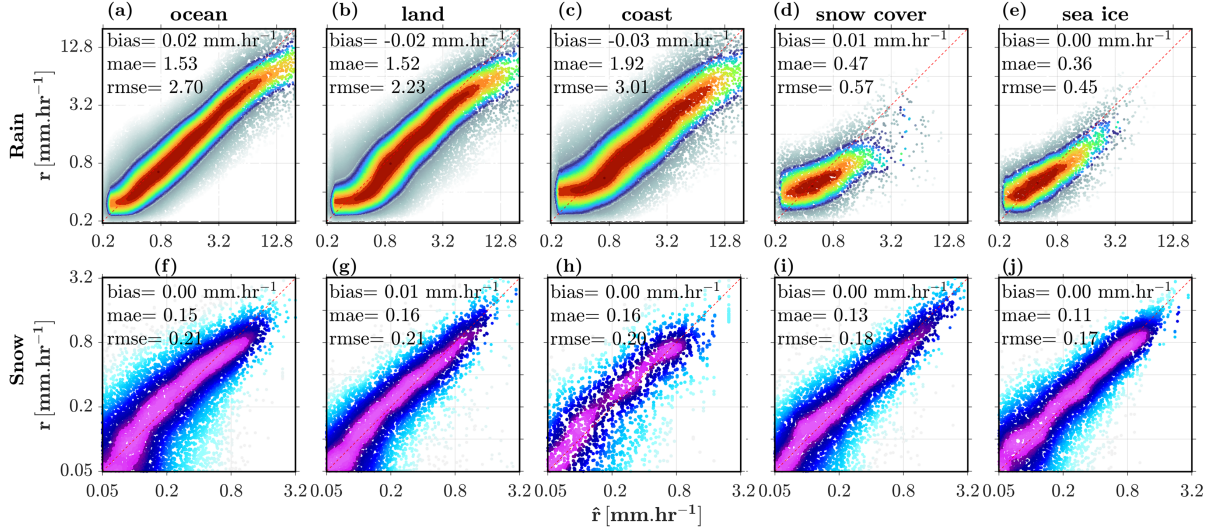
343 TABLE 2. Conditional root mean square error (rmse,  $\text{mmhr}^{-1}$ ) of ShARP<sup>ML</sup> and XGBDT for estimation of  
 344 precipitation rate, given the occurrence and phase are determined in the detection step.

			Surface Type				
			ocean	land	coast	snow cover	sea ice
rain	rmse	ShARP <sup>ML</sup>	2.70	2.23	3.01	0.57	0.45
		SHARP	3.20	2.82	3.15	0.65	0.44
		XGBDT	2.90	2.92	3.10	0.58	0.43
snow	rmse	ShARP <sup>ML</sup>	0.21	0.21	0.20	0.18	0.17
		SHARP	0.26	0.28	0.32	0.24	0.24
		XGBDT	0.32	0.36	0.31	0.19	0.16

323 A comparison of the results with some previous works is not straightforward because of the lack  
 324 of non-uniform training and testing data sets. For example, the training data in (Pfreundschuh  
 325 et al. 2022) differ notably as they utilized ERA5 precipitation over sea ice, compensating for  
 326 limitations in DPR-based reference retrievals. Additionally, collocations of ground-based radar  
 327 data were employed over snow-covered surfaces in their analysis. The All-Surface Snow Water  
 328 Path Retrieval Algorithm (SLALOM, Rysman et al. 2018) used the random forest and trained it  
 329 using an older version of GMI-CPR coincidences (Turk et al. 2021). The highest values of 83%  
 330 (TPR) and 12% (FPR) were reported over land, open sea, and sea ice. The reported improvements  
 331 can be attributed to the following reasons. (i) The latest version of CPR and GMI coincidences  
 332 include more crossings than the older version. (ii) The XGBDT is used rather than RF, which uses  
 333 a different parameterization. (iii) We are using weighted cross-entropy loss to formally account for  
 334 the imbalanced nature of the training and testing data sets.

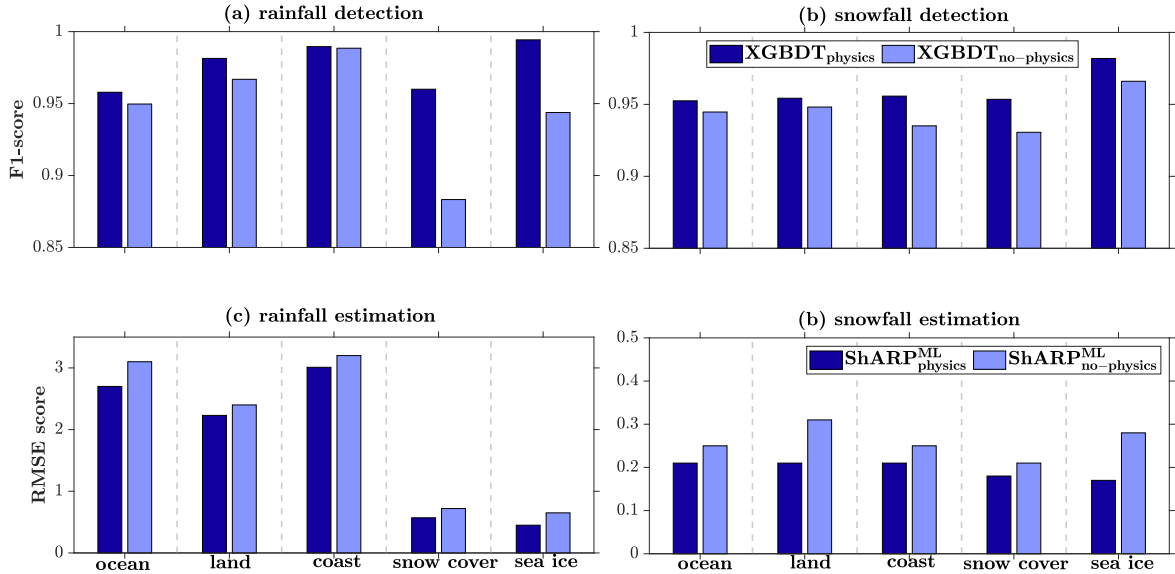
335 *b. Estimation quality metrics*

336 Table 2 compares the performance of ShARP<sup>ML</sup> and XGBDT in the estimation step in terms of  
 337 the conditional root mean square error (rmse,  $\text{mmhr}^{-1}$ ), given that the precipitation occurs. The  
 338 two models have comparable skills; however, ShARP<sup>ML</sup> outperforms the XGBDT over the oceans  
 339 and land. Conversely, over coastal, snow cover, and sea ice surfaces with relatively small training  
 340 sample sizes; the XGBDT is still marginally the best choice. Additionally, Table 2 presents the  
 341 performance of the original SHARP algorithm (Ebtehaj et al. 2015) showing lower skills compared  
 342 to the ShARP<sup>ML</sup> model.



345 FIG. 4. Density scatter plots of conditional retrievals of rainfall (a–e) and snowfall (f–j) rates by the ShARPM<sup>L</sup>  
 346 for the test data. The quality metrics are biases, root mean square errors (rmse), and mean absolute errors  
 347 (mae). The scatter plots are normalized column-wise for improved visualization and the color of the scatter plots  
 348 captures the relative density of the points from blue to red (rainfall) rain and magenta (snowfall).

349 The ShARPM<sup>L</sup> results, with  $K = 20$  nearest neighbors, are presented in Fig. 4 for both rainfall (top  
 350 row) and snowfall (bottom row) test data, given that the precipitation and its phase are detected.  
 351 The bias is relatively under control and is larger for rainfall than snowfall. The light (heavy)  
 352 rainfall rates are overestimated (underestimated), especially over those surface types with limited  
 353 sample sizes. This is a generic pattern when an unbiased estimator attempts to retrieve data with a  
 354 positively skewed distribution. This gives rise to small negative biases as the algorithm struggles  
 355 to retrieve the heavy rainfall rates, especially over surface types with limited training samples.  
 356 The rmse values of conditional retrievals and their gaps with their mean absolute error (mae)  
 357 counterparts are larger for rainfall than snowfall over most land cover types, due to the heavier tail  
 358 probability distribution of rainfall. The mean mae values of rainfall (snowfall) amongst all land  
 359 surface types is around 1.15 (0.14) mm hr<sup>-1</sup>. The largest rmse is related to rainfall retrievals over  
 360 coastal areas and snowfall over land and oceans. The large rmse can be attributed to the small  
 361 sample size for the coastal rainfall. At the same time, the heaviest convective rainfall (snowfall)  
 362 occurs over land (oceans) and contributes to the observed elevated error statistics.



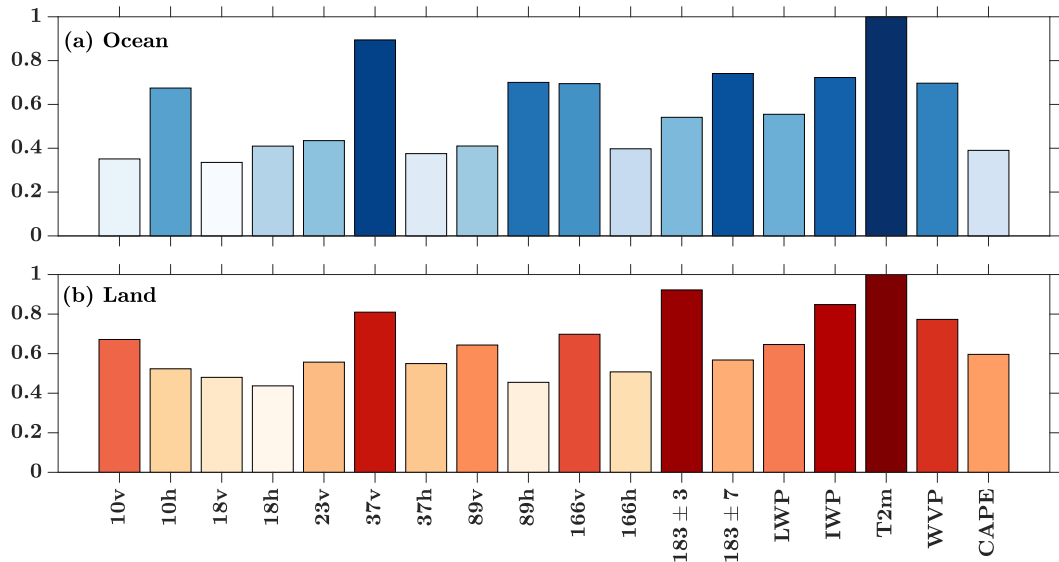
373 FIG. 5. The effects of ERA5 physical variables on detection (a–b), and estimation (c–d) performance of final  
 374 retrieval models.

363 *c. Impacts of the Reanalysis Physical Variables*

364 Figure 5 highlights the effect of incorporating physical variables from ERA5 on the detection  
 365 and estimation capabilities of XGBDT and ShARP<sup>ML</sup> models across various surface types. As is  
 366 evident, the F1-score increases across all land surface types for both rain and snowfall detection.  
 367 This increase seems marginal and less than 2% over ocean and land for both rain and snow. However,  
 368 we need to recall that each GMI orbit consists of  $221 \times 2961$  number of pixels. Therefore, on an  
 369 annual basis, only a 1% improvement in the F1-score translates into more than 10 million pixel-  
 370 level events, considering 30% of each orbit is precipitating. The impact on the rmse values is also  
 371 significant. On average, the rmse values decrease by 15 (9)% over ocean (land) for rainfall and 14  
 372 (33)% for snowfall.

375 *d. Interpreting the ML results*

376 For brevity, we confine our considerations to the data points collected only over ocean and land  
 377 surface types to investigate mutual information of the inputs with precipitation occurrence and  
 378 phase change and the consistency of the detection module with the underlying physical causalities.



385 FIG. 6. Mutual Information Quotient (MIQ) derived from Minimum Redundancy Maximum Relevance  
 386 (MRMR) analysis for inputs used in precipitation and its phase detection over the ocean (a) and land (b). Darker  
 387 shades represent higher MIQ values, indicating greater importance of the corresponding features.

### 379 1) MRMR

380 The results of MRMR analysis (Fig. 6) show that, amongst the input variables, the 2-m air  
 381 temperature is the most important one for the classification of the atmosphere into a clear, raining,  
 382 and snowing atmosphere both over land and ocean, which is simply consistent with our physical  
 383 understanding of precipitation phase change. The other two most important inputs are the liquid  
 384 water and the water vapor channels at 37v and 183 GHz followed by ice scattering at 166v GHz.

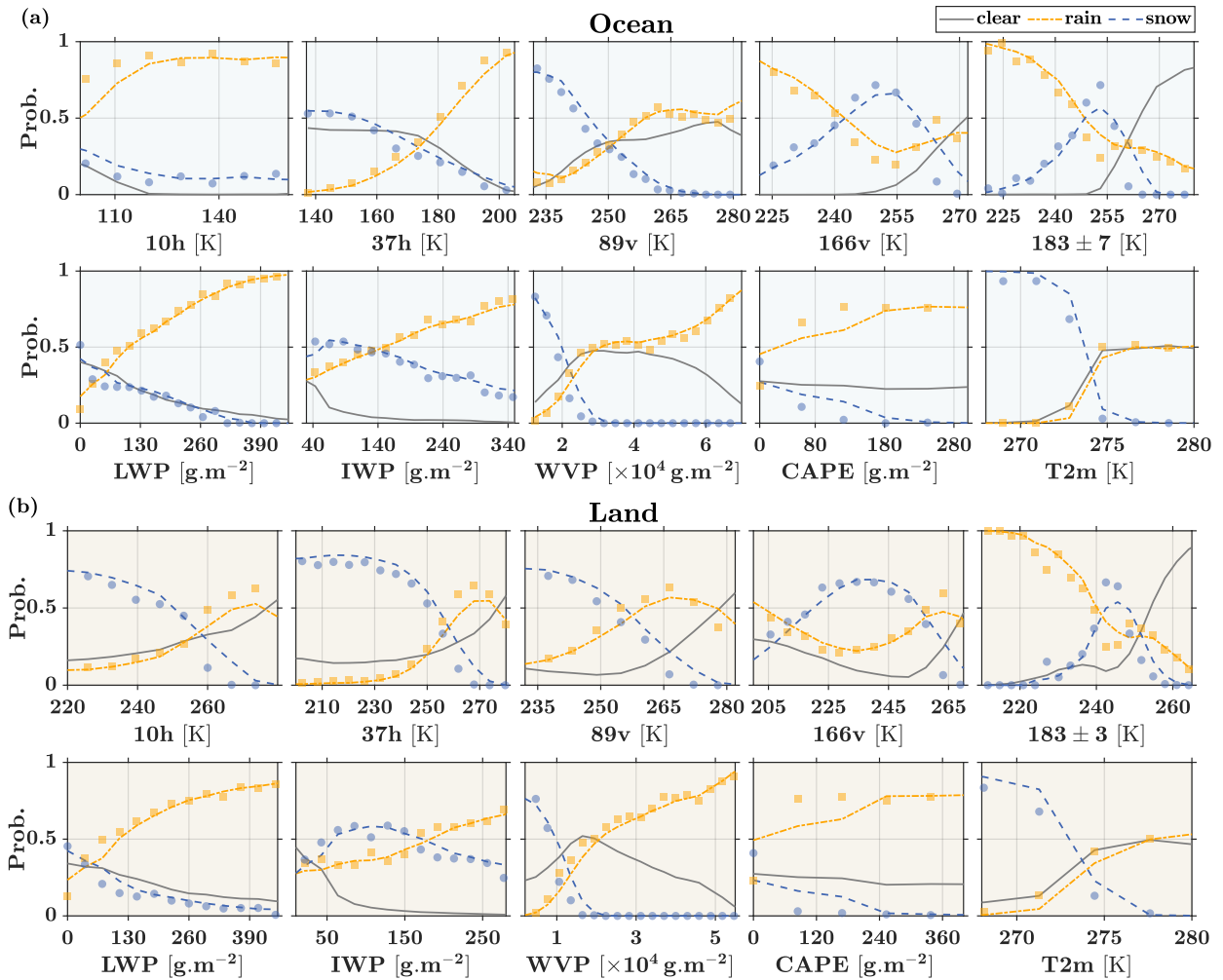
388 It is well understood that the total columnar atmospheric liquid water content increases the  
 389 absorption at 37 GHz. This channel has been widely used for rain and cloud liquid water retrievals  
 390 over oceans (O'Dell et al. 2008). The overland MRMR importance of 37v is surprising as it  
 391 does not capture a strong emission/scattering signal of liquid water particles over highly emissive  
 392 surfaces. The importance of this channel might be interpreted in light of its relationship with  
 393 land surface temperature (Holmes et al. 2009). The MRMR analysis is performed separately on  
 394 snow-clear, rain-clear, and snow-rain label cases for testing this conjecture. The results (not shown  
 395 here), revealed that when considering only snow-clear and rain-clear labels, the MRMR score drops  
 396 from 0.8 to 0.4. In other words, the 37v channel provides no relevant information on precipitation

397 occurrence. At the same time, when only considering the snow-rain labels, the score increases to  
398 0.9, indicating that this channel provides a significant discriminative power for precipitation phase  
399 detection. Now the question is why the water vapor channel 183 GHz provides more relevant  
400 mutual information with precipitation phase change than the known ice scattering channels at 89  
401 and 166 GHz (Bennartz and Petty 2001; Bennartz and Bauer 2003). Findings by You et al. (2017)  
402 can provide an explanation.

403 In summary, the precipitation phase detection accuracy depends on the discriminative power of  
404 the channel in separating the high-frequency scattering signals of snowfall from the surface under  
405 the masking effects of water vapor emission. It was found that the  $183\pm 3$  channel is the most  
406 sensitive channel to ice scattering in a relatively dry atmosphere while it remains fully agnostic  
407 to the land surface emissivity changes. As the water vapor increases to a moderate level, channel  
408  $183\pm 7$  becomes more sensitive to ice and snowfall scattering than other channels. However, in  
409 a very moist atmosphere with a relatively large amount of water vapor, the sensitivity of 166v to  
410 the surface emissivity drops markedly and the channel becomes more effective in capturing the ice  
411 and snowfall scattering. The MRMR results show that over the ocean, where the atmosphere is  
412 expected to be relatively wetter than land, the  $183\pm 7$  channel provides higher mutual information  
413 with the precipitation type than  $183\pm 3$  and vice versa. The 166v channel is the next most important  
414 high-frequency channel for precipitation phase detection over land and ocean.

## 415 2) PARTIAL DEPENDENCE ANALYSES

419 Figure. 7 shows the partial dependence plots for the detection step (solid lines) and conditional  
420 observational probabilities (markers) for a few selected input variables using the test data. Over  
421 the ocean, as the 10h and 37h channels warm up, the probability of rainfall occurrence increases,  
422 explaining that the ML captures the raindrop and cloud liquid water emission signals for rainfall  
423 detection. The 10h GHz channel appears to provide specificity for rainfall detection with a  
424 probability greater than 0.5 across the analyzed range. Since the probabilities are almost the same  
425 for clear-sky and snowfall events, this channel does not provide any information for the snowfall  
426 detection, expectedly. While the probability increases monotonically with the temperature at 37h  
427 GHz, the PD analysis indicates that this channel is only effective for rainfall detection when the  
428 TBs are greater than 180 K.



416 FIG. 7. Partial dependence analysis of the detection step using XGBDT for the test data over the ocean (top  
 417 two rows) and land (bottom two rows). The analysis is confined to each bin to avoid sampling the low-probability  
 418 regions of the joint distribution.

429 Among the scattering channels over the ocean, 89v shows high specificity in surface snowfall  
 430 detection for TBs smaller than 250 K with no substantial information about rainfall detection.  
 431 However, surprisingly, the 166v ( $183 \pm 7$ ) channel with cold TBs below 240 (245) K is chiefly  
 432 associated with high rainfall class probabilities and seems important only for snowfall detection  
 433 over the range 240–265 (245–260) K with no discriminative power over warmer values. The  
 434 results unravel that the coldest TBs in 89 (166) GHz are associated with snowfall (rainfall).  
 435 One reason is that the 89 GHz channel responds to near-surface snowfall scattering; however,

436 higher frequencies capture the ice-aloft scattering (Skofronick-Jackson and Johnson 2011) that can  
437 statistically represent frequent heavy rainfall events in tall clouds with melting layers.

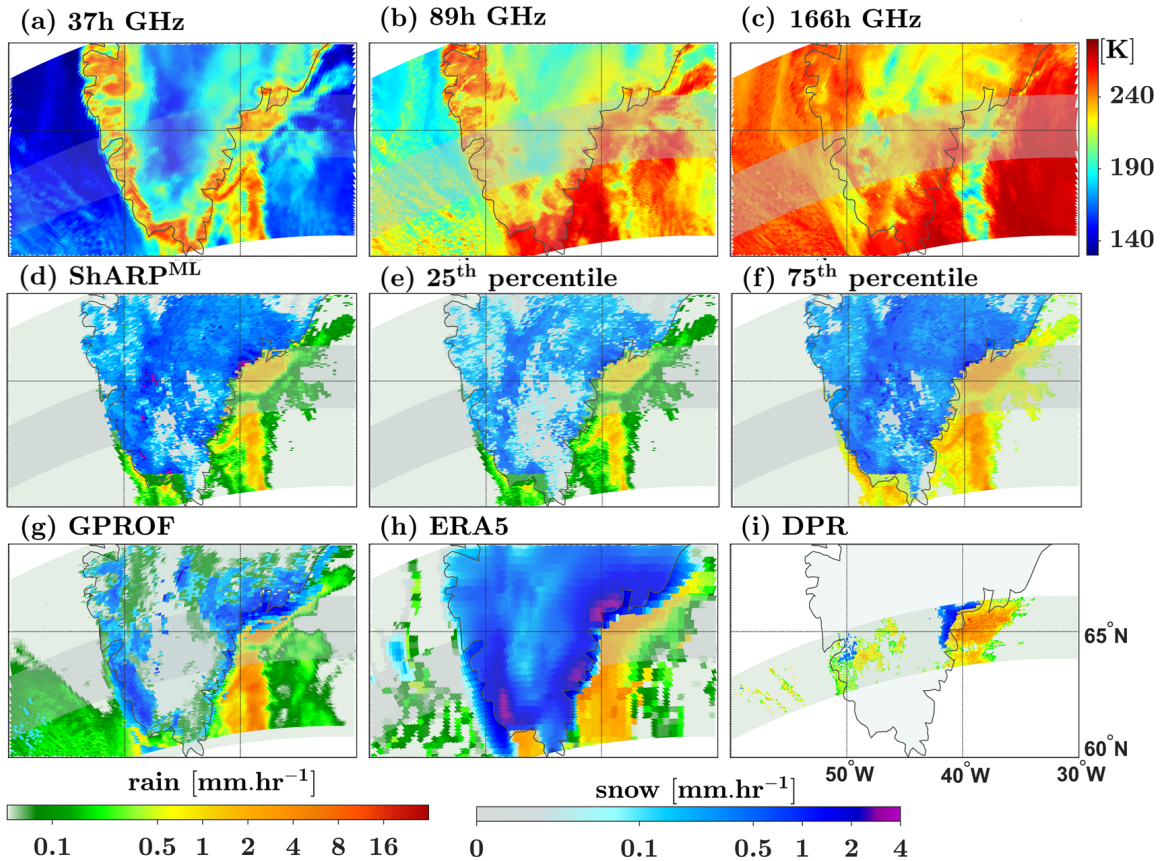
438 As the cloud IWP and LWP increase and the atmosphere becomes wetter over oceans, the ML  
439 produces higher rainfall class probability, and the surface snowfall is largely associated with drier  
440 atmospheric conditions. The PD of precipitation classes with CAPE is also consistent with the  
441 fact that rainfall events are more associated with strong convective activities than snowfall. The  
442 PD analysis of the 2-m air temperatures is striking and demonstrates how the used ML model can  
443 consistently capture the phase change of surface precipitation as a function of temperature.

444 Overland, the cold 10h and 37h TBs are associated with surface snowfall and do not provide  
445 any specificity for rainfall detection. These high snowfall class probabilities represent surrogate  
446 dependencies with the surface temperature and are unrelated to any scattering signatures, as  
447 discussed previously. The response patterns for high-frequency channels are similar to those over  
448 the ocean; however, these channels seem to provide more discriminative power, especially at 89  
449 GHz.

### 450 3) ORBITAL RETRIEVALS

451 Figure 8 shows the result of ShARP<sup>ML</sup> for GMI orbit #3080 over Greenland on September  
452 13, 2014. Precipitation retrieval over an ice sheet is challenging because fewer active/passive  
453 coincidences exist over this specific surface type. Moreover, over a low emissive snow-covered  
454 ice, snowfall high-frequency scattering signatures can be weak and masked by supercooled cloud  
455 liquid water content.

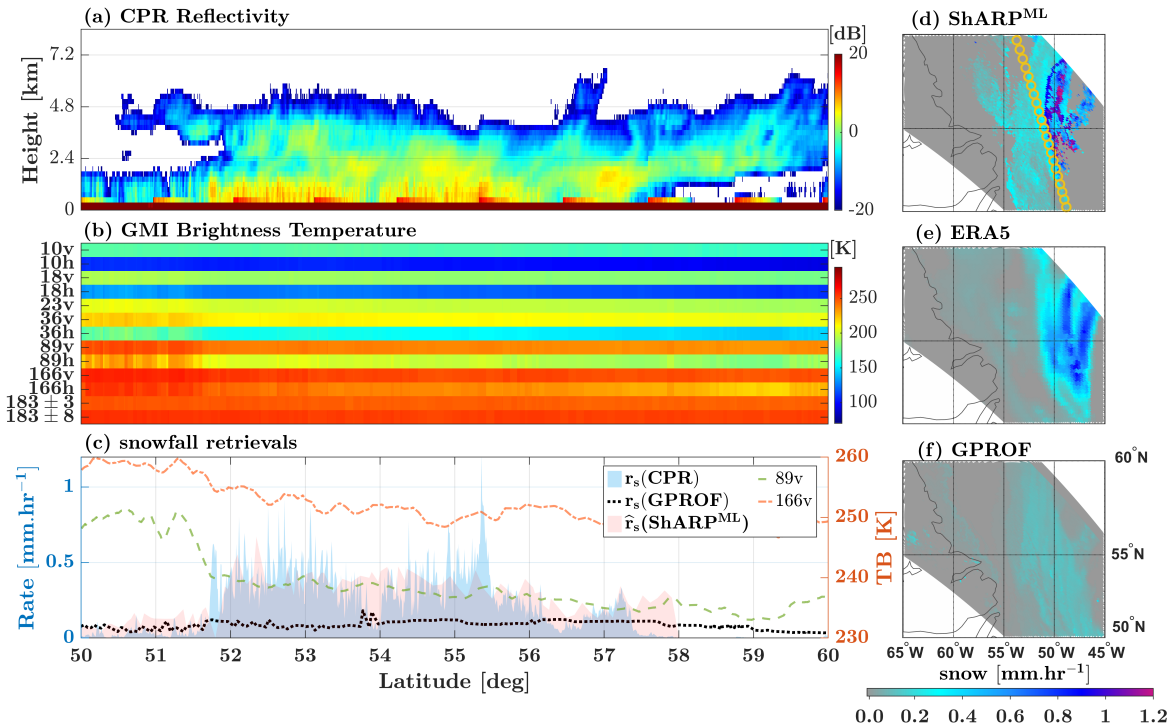
456 Visual inspection of the 37 GHz channel (Fig. 8a–c) indicates a warming signal and thus a  
457 potential rainfall event over the North Atlantic Ocean and Greenland Strait. This warm signal is  
458 accompanied by cooling in both 89 and 166 GHz – indicating ice aloft scattering and occurrence  
459 of a melting layer. A warming signal is observed at 37 GHz, over the ice-free southern and  
460 western coastlines, covered with sub-arctic and tundra climate regimes. Perceptual interpretation  
461 of high-frequency TBs is not straightforward due to the complexity of radiometric interactions of  
462 snow-covered ice with atmospheric signals – especially at surface sensitive 89 GHz. Nevertheless,  
463 a cooling signal, likely due to ice particles and falling snow, is visible over the southwest coastlines  
464 at 166 GHz.



465 FIG. 8. Brightness temperatures by GMI (a–c), precipitation retrievals by ShARP<sup>ML</sup> and its uncertainties (d–f)  
 466 and precipitation from GPROF, ERA5, and DPR (g–i) for orbit #3080 on September 13, 2014 over Greenland.

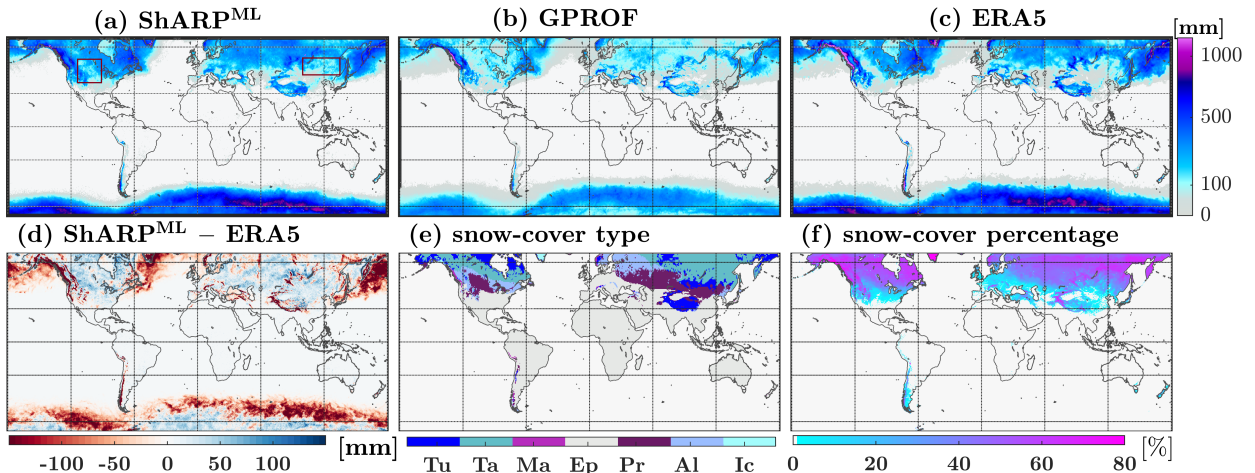
467 The precipitation retrievals and ERA5 data (Fig. 8d–i) indicate that as the storm moves over  
 468 the ice sheet, the phase of precipitation transitions from liquid to solid; however, they are notably  
 469 different in the middle of the ice sheet. The ShARP<sup>ML</sup>, which relies on CPR coincidences, shows a  
 470 notable snowstorm covering the ice sheet consistent with the ERA5 data (Fig. 8h), even though the  
 471 retrieved intensities are much lower. The retrieval quantiles indicate that the uncertainties are high  
 472 and the distribution of the retrievals is wide in the middle of the storm. It is important to recall  
 473 that ERA5 simulations represent a temporal interpolation between hourly simulations and are not  
 474 instantaneous.

480 We also retrieve the extent and rate of a snowstorm near the coast of the Labrador Peninsula  
 481 on January 3, 2019 – where CPR intersects the GMI orbit #27551 (Fig. 9). The narrow, sheared  
 482 columnar-like CPR reflectivity profile (Fig. 9a), distributed across this cross-section with values



475 FIG. 9. Passive retrievals of a snowstorm captured by GPM orbit #27551 over the Labrador Sea on the west  
 476 coast of Quebec in Canada on January 3, 2019. (a) The CPR reflectivity profile, (b) GMI TBs, (c) snowfall rates  
 477 from CPR ( $r_s$ , blue shaded area), ShARP<sup>ML</sup> ( $\hat{r}_s$ , red solid line), GPROF ( $r_s$ , black dotted line), and variation of  
 478 TBs at channels 89v (green dashed line) and 166v GHz (orange dashed line) over the CPR track. The spatial  
 479 representations are (d) ShARP<sup>ML</sup>, (e) ERA5, and (f) GPROF retrievals on the GMI swath.

483 exceeding 10 dBZ to almost 2 km above the surface, indicates the occurrence of a moderately  
 484 deep snowfall event. The TBs capture the scattering signatures from the shallow ice particles at 89  
 485 and 166 GHz (Fig. 9b), despite highly polarized surface emissivity over this intersection. These  
 486 channels become colder by more than 10–15 K, as CPR moves toward the storm’s northern edge  
 487 with higher snowfall rates. Consistent with these scattering signatures, the CPR retrieves sporadic  
 488 snowfall cells with a rate  $<1 \text{ mm hr}^{-1}$ , while both GPROF and ShARP<sup>ML</sup> retrieve lower rates than  
 489 CPR. The ERA5 simulations represent the occurrence of a cohesive snowstorm with a rate of less  
 490 than  $0.75 \text{ mm hr}^{-1}$ . Once again, we need to emphasize that there is a 15 min time lag between the  
 491 CPR and GMI coincidences, and ERA5 snowfall is temporally interpolated.



493 FIG. 10. Annual estimates of the total snowfall in 2022 at a 0.1-deg grid for (a) ShARP<sup>ML</sup>, (b) GPROF, (c)  
 494 ERA5, (d) the difference between ShARP<sup>ML</sup> and ERA5 with (e) the snow cover classes include tundra (Tu), taiga  
 495 (Ta), maritime (Ma), ephemeral (Ep), prairie (Pr), alpine (Al), and ice (Ic) as well as the (f) the annual MODIS  
 496 snow-cover percentage.

492 *e. Global Retrievals*

497 An estimate of total annual snowfall in 2022 for all data products is shown in Fig. 10 on a  
 498 0.1-deg grid. The results suggest that GPROF underestimates snowfall over oceans compared to  
 499 other retrievals consistent with previous findings (Skofronick-Jackson et al. 2019). The spatial  
 500 patterns between ShARP<sup>ML</sup> and ERA5 are in reasonable agreement over oceanic storm tracks in  
 501 the Southern Ocean, the Bering Sea, and the Labrador Sea. However, it appears that over relatively  
 502 ice-free (ice-covered) oceans, ShARP<sup>ML</sup> tends to underestimate (overestimate) ERA5. It is well  
 503 understood that the scattering signal of dry snow-covered sea ice can decrease the high-frequency  
 504 TBs (Ebtehaj and Kummerow 2017; Vahedizade et al. 2021) and lead to some overestimation.

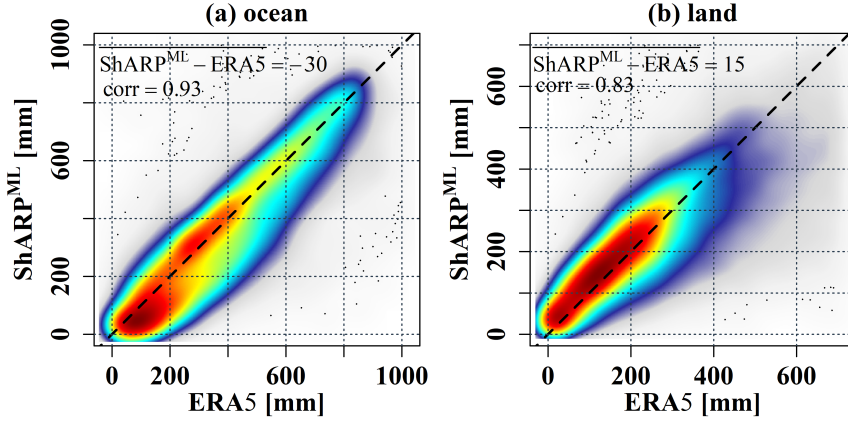
505 Notable differences are observed over terrestrial surfaces, especially in mountainous and low-land  
 506 snow- and ice-covered areas. To provide additional insights on these differences, the annual snow-  
 507 cover type (Sturm and Liston 2021) and fraction (Pagano and Durham 1993) from the Moderate  
 508 Resolution Imaging Spectroradiometer (MODIS) are also shown in Figs. 10e,f. Overall, visual  
 509 inspection indicates that ShARP<sup>ML</sup> is prone to overestimate ERA5 over lowlands and underestimate  
 510 it over mountainous regions and Greenland. The underestimation is more significant in GPROF  
 511 than ShARP<sup>ML</sup>, except over the Canadian Coast Mountains, where the orographic snowfall is the

512 dominant regime. However, compared to GPROF, the CPR-based retrievals are in better agreement  
513 with the reanalysis in other mountain ranges with predominantly orographic snowfall – such as the  
514 Norwegian mountains, the Himalayas, and the European and Japanese Alps. The underestimation  
515 of mountainous (orographic) snowfall is attributed to the fact that spaceborne retrievals can miss  
516 backscattered snowfall signatures over rough surfaces (Tang et al. 2017; Takbiri et al. 2019;  
517 Skofronick-Jackson et al. 2019). Moreover, due to the shallow nature of orographic snowfall, the  
518 snowfall passive scattering signatures can be markedly weak, especially over frequencies above  
519 150 GHz that capture upper-level ice scattering (Skofronick-Jackson and Johnson 2011).

520 Over the temperate grasslands, savannas, and shrublands biomes in the Eurasian Steppe, where  
521 relatively shallow Prairie and Tundra snow cover are expected, GPROF (ShARP<sup>ML</sup>) consistently  
522 underestimates (overestimates) ERA5. The climatological observations from the GlobSnow dataset  
523 (Takala et al. 2011) indicate that the mean annual snow depth varies from 200 (south) to 400 mm  
524 (north) in this ecoregion (Bormann et al. 2018), which seems to be consistent with the annual  
525 retrievals by ERA5 and ShARP<sup>ML</sup>. The MODIS snow-cover percentage data (Fig. 10f) indicates  
526 that perhaps ShARP<sup>ML</sup> is prone to overestimation over the Canadian Prairies and northeast China,  
527 marked with red boxes. These areas are often covered with seasonal shallow Prairie snow-cover  
528 type, which was recognized to manifest a similar scattering signal to snowfall (Rahimi et al. 2022)  
529 when the emerging vegetation is light and the snow depth is less than 15 cm.

530 The global snowfall retrievals of ShARP<sup>ML</sup> (Fig. 10) are shown versus the ERA5 data over  
531 ocean and land in Fig. 11. The two data sets are more correlated over the ocean than over land.  
532 The ShARP<sup>ML</sup> slightly underestimates (overestimates) the ERA5 over the ocean (land) by -30  
533 (15) mm year<sup>-1</sup>. The underestimation over oceans is largely accumulated where the total snowfall  
534 is less than 200 mm year<sup>-1</sup> while for the higher accumulation rates 200–400 mm year<sup>-1</sup>, satellite  
535 retrievals overestimate the reanalysis. On the contrary, the retrievals consistently overestimate  
536 ERA5 snowfall over land surfaces across a wide accumulation range of 0–400 mm year<sup>-1</sup> (Fig. 11b).

537 The terrestrial differences and correlation values are further stratified and reported in Tab. 3.  
538 Consistent with spatial differences (Fig. 10d), the largest overestimation (underestimation) is over  
539 prairie (maritime) 23 (-32) mm year<sup>-1</sup> snow types as well as ice-covered Greenland. The corre-  
540 lation between ShARP<sup>ML</sup> and ERA5 snowfall data varies across snow types. The retrievals over  
541 ephemeral snow show the least discrepancy and highest correlations, where the likelihood of scat-



530 FIG. 11. Density scatter plots of annual snowfall from ShARP<sup>ML</sup> and ERA5 (Fig. 10) over (a) ocean and (b)  
 531 land at a 0.1-deg grid. Hot (red) and cold (blue) colors denote the higher and lower densities of the available  
 532 data pairs. The corr denotes the correlation coefficient, and bias is reported in mm year<sup>-1</sup>.

549 TABLE 3. Mean difference and correlation of annual ShARP<sup>ML</sup> and ERA5 snowfall over different snow-cover  
 550 types as explained in Fig. 10.

Snow types	Tu	Ta	Ma	Ep	Pr	Al	Ic
ShARP <sup>ML</sup> - ERA5 [mm]	15	-3	-32	3	23	7	-25
Correlation Coef. (corr)	0.73	0.80	0.80	0.83	0.81	0.75	0.63

545 tering interference is minimal, as physically explained by [Rahimi et al. \(2022\)](#). High correlations  
 546 in maritime (0.80) environment suggest that ShARP<sup>ML</sup> and ERA5’s spatial patterns are close in  
 547 this regime despite the existing differences in the mean values. On the other hand, the lowest  
 548 correlation is over ice-covered surfaces.

551 Overall, the zonal mean of snowfall retrievals (Fig. 12) shows that ShARP<sup>ML</sup> and ERA5 retrievals  
 552 are in latitudinal agreements despite reported spatial heterogeneity and differences. Over oceans,  
 553 underestimation of ShARP<sup>ML</sup> increases over polar latitudes, probably due to additional complexities  
 554 of surface emissivity caused by heterogeneous sea ice variability in space and time. The agreement  
 555 is stronger in the Southern Ocean, which makes up, on average, 80% of total oceanic snowfall.  
 556 Over the Northern Hemispheric continents, there is a good agreement between zonal mean values,  
 557 especially at 30–40°N. In the Southern Hemisphere, a significant difference between satellite

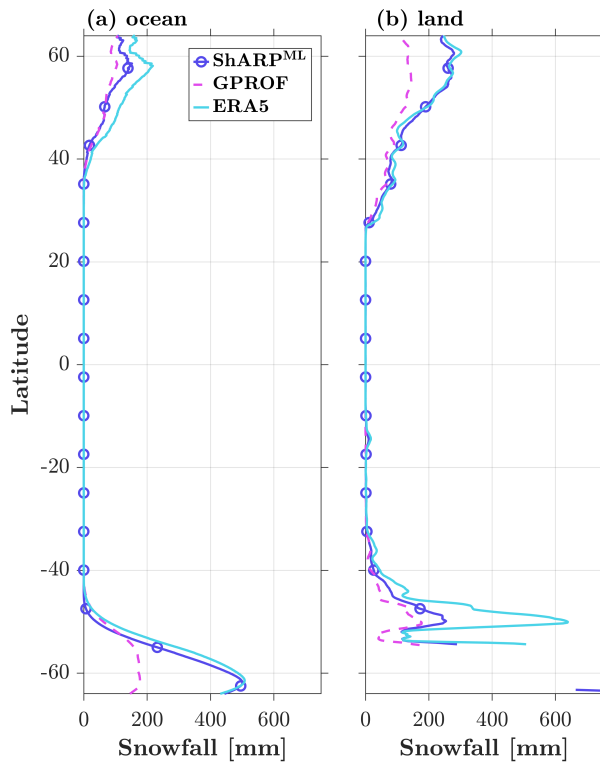


FIG. 12. Annual zonal mean of snowfall data over (a) ocean and (b) land obtained from Fig. 10.

558 retrievals and reanalysis data is observed over the Andes Mountains, perhaps indicating the lack of  
 559 signal in coincidences used for the algorithm training.

## 560 **5. Summary and Concluding Remarks**

561 The paper proposed and studied the performance of a PMW precipitation retrieval pipeline that  
562 learns from coincidences of passive/active observations from the Global Precipitation Measurement  
563 (GPM) core satellite and the W-band CloudSat Profiling Radar (CPR) as ancillary reanalysis  
564 drivers of precipitation. This architecture first detects the precipitation, determines its phase  
565 through the XGBDT algorithm with weighted cross-entropy, and then estimates its rate through  
566 a Bayesian retrieval approach in the embedding space of a fully connected MLP, equipped with  
567 a focal loss function. Consistent with the previous literature ([Rysman et al. 2018](#)), we found that  
568 gradient-boosted decision trees can outperform multi-layer perceptions based on learning from  
569 the available CPR-GMI coincidences. We provided evidence suggesting that Bayesian retrievals  
570 in the embedding space of an MLP provide competitive and even higher-quality retrievals than  
571 the examined classic MLs. The results highlight the importance of using proper loss functions  
572 that can formally account for the imbalanced nature of the precipitation types and their skewed  
573 distributions.

574 A few research directions can be envisaged. The overestimation in snowfall retrievals over  
575 regions with shallow prairie snow was attributed to the similarity of snowfall and snow-cover  
576 scattering signals and requires further investigation. Due to a limited number of CPR observations  
577 and microwave frequency channels, resolving this ill-posedness might need additional ancillary  
578 data related to the physical characteristics of snow cover (i.e., thickness, density, and liquid water  
579 content) as well as information on vegetation water content perhaps from the Soil Moisture Active  
580 and Passive Satellite data ([Kumawat et al. 2022](#); [Kumawat and Ebtehaj 2023, 2024](#)) over snow-  
581 covered surfaces.

582 The underestimation of snowfall in mountainous regions remains a challenge because of two  
583 main reasons. The sample size is small and lacks the backscattered signal of (shallow) orographic  
584 snowfall reflectivity due to increased surface roughness. Further constraining the retrievals using  
585 model simulations or reanalysis data might be inevitable when the scattering signal does not  
586 exist. Explainable machine learning can be further expanded to examine the signal strengths over  
587 complex terrains and the consistency of retrievals. Lastly, we need to emphasize that while visual  
588 comparisons with the GPROF product were provided, objective analysis will be needed to quantify

589 when, where, and to what extent the GMI-CPR coincidences can improve the retrievals globally,  
590 contingent upon the used algorithms.

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599 *Data availability statement.* The datasets utilized in this study are openly accessible to  
600 the public. The GPM dataset can be downloaded from NASA's Global Precipitation Mea-  
601 surement (GPM) website at <https://storm.pps.eosdis.nasa.gov/storm/data/Service.jsp?serviceName=Order>. The ERA5 dataset is available for download through the Copernicus  
602 Climate Data Store (CDS) at <https://cds.climate.copernicus.eu/cdsapp#!/dataset/reanalysis-era5-single-levels?tab=form>.

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