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AS LOW-ENERGY PHOTON SPECTROMETERS

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NATIONAL AERONAUTICS AND SPACE ADMINISTRATION

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SUMMARY

Lithium-drifted silicon detectors were fabricated from 10 000 ohm-centimeter, p-type silicon and were tested for use as low-energy photon spectrometers. Three X-ray and gamma-ray sources (Am$^{241}$, Co$^{57}$, Cd$^{109}$) were used to determine the energy resolution. At 77°K and less than 10$^{-5}$ torr (1.33 mN/m$^2$) the detector resolution varied from 0.82 keV (full width half maximum (FWHM)) at a photon energy of 22.10 keV to 1.04 keV (FWHM) at 122.05 keV with detector-amplifier noise (measured with a pulse generator) almost constant at 0.75 keV (FWHM). From these measurements an intrinsic detector resolution corresponding to a Fano factor of 0.205 was calculated.

INTRODUCTION

The use of solid-state semiconductor detectors in nuclear physics is widespread (refs. 1 to 3). These devices have rapidly progressed from the experimental state to the development level and now enjoy a position of prominence in nearly all recent experiments in low-energy spectroscopy.

In 1960 Pell (ref. 4) demonstrated the possibility of producing a large volume of intrinsic silicon by first diffusing lithium metal into p-type silicon and then drifting the lithium ions through the material. This discovery initiated a surge of activity to develop large diodes with better energy resolution and stopping power than could be obtained from p-n junction detectors in use at that time. Within 2 years the techniques for producing good detectors with depletion regions greater than 5 mm deep were well established for 50 to 100 Ω-cm, p-type silicon (ref. 5). Diodes with 6.5 keV resolution at full width half maximum (FWHM) for Cs$^{137}$ conversion electrons (625 keV and 655 keV energy) and the same resolution for Pb$^{207}$ X-rays (74 keV and 90 keV) were discussed in reference 5. By 1964, lithium-drifted silicon detectors had been reported with 3 to 4 keV resolution for the same energies (ref. 6). At this time, it appeared that the energy resolution of silicon detectors would be limited by noise in the amplifying systems.

The advent of the field effect transistor (FET) and its applicability to low-noise, charge-sensitive preamplifiers (ref. 7) opened a new phase in the development of
solid-state radiation-detection systems. The degree of success is indicated in more recent publications by Elad and Nakamura (refs. 8 to 10) where 1.5 keV (FWHM) resolution is reported on the 89.4 keV electron line of U$^{237}$ and by Harris and Shuler (ref. 11) where it is reported less than 0.5 keV (FWHM) resolution for 6.4 keV photons of Am$^{241}$.

The development of lithium-drifted germanium detectors has paralleled that of silicon devices. However, perhaps more effort has gone into producing germanium detectors mainly because of the high mobility of lithium ions at room temperature in germanium which increases the complexity of the fabrication process. Nevertheless Tavendale (ref. 12) reported in 1964 3.1 keV (FWHM) resolution on the 122 keV gamma ray from Co$^{57}$. Recently Elad and Nakamura (ref. 10) have obtained 0.8 keV (FWHM) resolution on the Co$^{57}$ gamma rays.

The present report is concerned with the performance of lithium-drifted silicon detectors developed at the Langley Research Center for use as low-energy gamma- and X-ray spectrometers. The advantages and limitations of such devices are indicated in comparison with germanium detectors. The results presented herein are based on measurements made in mid-1966 on detectors produced in the first quarter of that year.

SYMBOLS

A \hspace{1cm} \text{atomic weight} \\
E \hspace{1cm} \text{photon energy, keV} \\
F \hspace{1cm} \text{Fano factor} \\
I \hspace{1cm} \text{photon flux at distance } x \\
mc^2 \hspace{1cm} \text{rest mass energy of electron, 0.511 MeV} \\
N \hspace{1cm} \text{number of atoms/cm}^3 \\
W \hspace{1cm} \text{line width, same as FWHM} \\
x \hspace{1cm} \text{distance in detector} \\
Z \hspace{1cm} \text{atomic number} \\
\varepsilon \hspace{1cm} \text{energy required to produce one electron-hole pair} \\
\sigma \hspace{1cm} \text{standard deviation for normal distribution} \\
2
The absorption and attenuation of electromagnetic radiation in a detector follow the exponential power law:

\[ I = I_0 e^{-\mu x} \]
where $I_0$ is the incident photon flux, $I$ is the photon flux at a distance $x$ from the irradiated surface, and $\mu$ is the total attenuation coefficient which is a function of the atomic number of the detector and the incident photon energy. The total attenuation coefficient is a sum of three coefficients associated with photon interactions in matter:

$$\mu = \mu_{\text{photo}} + \mu_{\text{compt}} + \mu_{\text{pair}}$$

where the symbols denote absorption by the photoelectric effect, Compton scattering, and pair production, respectively. The attenuation coefficients for these three interactions have the following dependence on atomic number of the detector and photon energy (ref. 13):

**Photoelectric effect:**

$$\mu_{\text{photo}} \sim NZ^5/E^{3.5}$$

**Compton scattering:**

$$\mu_{\text{compt}} \sim \frac{NZ}{E_\gamma} \left[ \ln \left( \frac{2E_\gamma/mc^2}{1/2} \right) \right] \quad \text{for} \quad E_\gamma > 1 \text{ MeV}$$

**Pair production:**

$$\mu_{\text{pair}} \sim \begin{cases} NZ^2(E_\gamma - 2mc^2) & \text{near threshold} \\ NZ^2 \ln E_\gamma & \text{at higher energies} \end{cases}$$

The attenuation coefficients (ref. 14) for silicon at photon energies from $10^{-2}$ MeV to 10 MeV are plotted in figure 1. The total attenuation coefficient for germanium is presented for comparison. For silicon the attenuation process below 0.05 MeV is dominated by the photoelectric effect; between 0.05 MeV and 10 MeV, Compton scattering predominates.

**Comparison of the Properties of Silicon and Germanium**

Although the absorption of photons by a detector is dependent on the atomic number of the detector material and the incident photon energy, these are only two considerations in choosing a detector for low-energy spectroscopy. In the following discussion the advantages and disadvantages of silicon and germanium detectors for photon spectroscopy below 150 keV are outlined.

The use of lithium-drifted silicon detectors for photon spectroscopy below 100 keV has several advantages. First, silicon detectors can be made with less than 0.5 g/m² dead layer on the entrance window, which allows detection of photons of less than 6 keV energy. The excellent resolution of silicon detectors below 50 keV is possible for several
reasons; the main one is the availability of good quality silicon which permits fabrication
of excellent diodes that exhibit almost no energy degradation due to charge trapping by
crystal defects. At 77° K some diodes have estimated leakage currents less than 10⁻¹¹
amperes at 500 volts bias. This extremely low current creates a minimum of electrical
noise in the amplifying system and consequently increases the energy resolution.

An important practical advantage of silicon devices is their mechanical and thermal
ruggedness. Detectors used for this report have been repeatedly cycled between 77° K
and 300° K without degradation in resolution or surface properties. This feature greatly
facilitates their use and is very convenient in testing new detector-preamplifier configu-
rations. Also, these detectors can be stored at room ambient conditions for extended
periods without changes in detector characteristics. The one main disadvantage of sili-
con detectors is the low atomic number (Z = 14) and density which limits their detection
efficiency.

Lithium-drifted germanium detectors have several physical properties which make
them the ideal choice for photon spectroscopy. Their main advantages over silicon are
higher atomic number (Z = 32), lower value of energy for the creation of electron-hole
pairs, and greater probability of both electrons and holes. Since the photoelectric atten-
uation varies as \( Z^5 \), germanium is approximately \( \frac{32^5}{14} \) more efficient for photon detec-
tion than silicon. The greater mobility of both electron and holes in germanium permits
faster charge collection and hence greater count rates than in silicon for the same size
devices. The lower value of energy for the creation of electron-hole pairs in germanium
causes less statistical fluctuation and hence less energy broadening than in silicon.

Although germanium would appear to be the best choice for a low-energy detector,
there are several disadvantages and difficulties associated with these devices. The most
pertinent is the availability of good germanium crystals. Most commercially obtainable
ingots have large defect concentrations which adversely affect detector performance in
that the defects act as trapping sites for charge carriers which tend to degrade the energy
resolution and to produce a skewing on the low-energy side of photon peaks.

The fabrication of germanium detectors is complicated and time consuming. Ger-
manium crystals are quite brittle and can crack under relatively slight mechanical or
thermal stresses. Furthermore, the 0.67 eV band gap requires the use of low tempera-
tures in order to reduce the current flow and resistive heating in the fabrication process.
As a consequence, the lithium ion mobility is kept low, and long drifting times are
required. After fabrication, detectors must be stored at dry-ice temperatures or below
in order to prevent redistribution of lithium ion concentration as noted previously. Also,
for maximum performance, germanium detectors must be used at liquid nitrogen tempera-
ture in order to suppress thermal creation of electron-hole pairs.
At the present time, all germanium detectors suffer from a relatively thick surface
dead layer that attenuates photons below 20 keV and produces a nonlinearity in energy
measurements up to 35 to 40 keV. For measurements above 100 keV these problems
are negligible and such detectors can give excellent energy resolution. Figure 2 shows
a comparison between the intrinsic resolution of silicon and germanium detectors. Data
for this figure were taken from reference 11 for silicon and reference 15 for germanium.

APPARATUS

Electronic System

The electronic system, detector mount, and cryogenic system used to obtain the
results reported herein are the same as those described by Harris and Shuler (ref. 11).
The first stage of a commercial charge-sensitive preamplifier was modified and physi­
cally separated from the later stages by approximately 8 cm to permit cooling of the FET.
The detector was direct-coupled to a selected type 2N3823 FET, as shown in figure 3.
This modification did not significantly affect the characteristics of the preamplifier with
respect to rise and decay times, but the noise contribution from the preamplifier was
reduced from 1.56 keV (FWHM) to 0.89 keV (FWHM) for zero external capacitance at room
temperature. The best noise figure obtained by cooling the front end was 0.63 keV for
zero external capacitance.

Signals from the preamplifier were fed to a pulse-shaping amplifier and then to a
pulse-height analyzer which had a 3200-channel analog-to-digital converter and a 1600-
channel memory. The energy calibration of this system was 0.043 keV/channel for mea­

urements reported herein. The differential and integral linearity was less than 2 percent
and 0.1 percent, respectively, over the top 98 percent of the channels. Single differentia­
tion of 6.4 μs and integration of 3.2 μs were found to be the optimum time constant settings
for the amplifier.

Detector Characteristics

All detectors used in the measurements were fabricated with techniques developed at
the Langley Research Center. These devices were produced from 10 kΩ-cm, p-type, boron
doped, float zone purified material. The minority carrier lifetime was greater than 1 ms
and the dislocation density as stated by the manufacturer was less than 30 000/cm^2. The
wafers were 3 mm thick and 1.8 cm in diameter and cut parallel to the (1,1,1) direction.

From a group of 20 wafers, all cut from the same ingot, six detectors were produced
which were considered for use as spectrometers. These detectors have been used periodi­
cally over a period of 1 year without any noticeable deterioration in resolution, with the
exception that difficulty was encountered in a deterioration of some rear contacts made by
aluminum vacuum deposition. Maximum detector performance can be restored simply by removing the old contact, cleaning the surface, and depositing a new contact. No problems have been noted with the front side and its gold contact. In fact, several detectors were tested with the gold removed from the front sides. No serious degradation in the resolution was noted in such tests.

In figure 4 a cross section of a typical detector is shown and detector characteristics are given. For a description of the detector holder and preamplifier configuration, see reference 11.

RESULTS AND DISCUSSION

Low-Energy Photon Measurements

Three low-intensity X-ray and gamma-ray sources (Am$^{241}$, Cd$^{109}$, and Co$^{57}$) were used to measure the energy resolution of the spectrometer system. As previously noted the system noise at zero external capacitance, as measured by using a precision pulse generator, was 0.63 keV (FWHM).

Photons from the sources were incident on the detector after passing through a 0.25-mm-thick aluminum window in the vacuum system. This window effectively absorbed all photons below 10 keV and probably caused some energy spread in the measurements. No attempt was made to measure this possible error because it was feared that the radiation sources used would outgas and contaminate the cryogenic system if placed inside the vacuum. The spectra shown in figures 5 to 7 were taken with the detectors cooled to 77°C and the system pressure at less than 10$^{-5}$ torr (1.33 mN/m$^2$).

The system resolution varied from 0.82 keV (FWHM) at 22.10 keV (fig. 6) to 1.04 keV (FWHM) at 122.05 keV (fig. 7) with the system noise constant at 0.75 keV (FWHM). This system resolution is sufficient to resolve photon peaks differing in energy by more than 1 keV.

In the next section the intrinsic resolution of the detectors is calculated and a discussion is presented of the importance of statistical fluctuations that occur in the conversion of photon energy to electron-hole pairs in the detector.

Detector Resolution and the Fano Factor

For each charged particle or photon which loses all its kinetic energy $E$ within a solid-state detector, there is an average number $N$ of electron-hole pairs produced in the device. These charges are swept from the detector volume by the electric field produced by the applied voltage, and then into an amplifying system. If the number of electron-hole pairs varies greatly from the average for each particle or photon of the same energy $E$ detected, then the output from the amplifying system will reflect these
variations, which decrease the total energy resolution of the system. For the best energy resolution the variations about the average number of pairs must be a minimum. In principle this minimum variation is defined by Poisson statistics. For example, consider a 36.6 keV particle or photon incident on a silicon detector. The number of electron-hole pairs created is determined by the average energy expended to produce one pair and the particle energy; that is,

\[ N = \frac{E}{\epsilon} \]

where \( \epsilon = 3.66 \text{ eV} \) (for silicon). Hence, the average number of pairs produced would be

\[ N = \frac{36.6 \text{ keV}}{3.66 \text{ eV}} = 10^4 \text{ pairs} \]

If the creation of each electron-hole pair is independent of all others, then Poisson statistics predicts a standard deviation about the average number \( N \) of \( \sqrt{N} \) or

\[ \sigma = \sqrt{N} = 10^2 \]

For large \( N \), the difference between a Poisson distribution and a normal or Gaussian distribution is negligible. Thus, this number is converted to FWHM in energy terms by the relation

\[ \text{FWHM} = 2.355\sigma \epsilon = 2.355\epsilon \sqrt{\frac{E}{\epsilon}} \text{ keV} \]

where the constant 2.355 is the conversion ratio between FWHM and the standard deviation \( \sigma \) of a normal distribution. Hence,

\[ \text{FWHM} = 0.928 \text{ keV} \]

is the best resolution possible for a 36.6 keV particle based on statistics. Experimentally the situation is quite different. For example, the detectors used in this report exhibit resolution better than 0.420 keV at this energy. This improved resolution is only possible if the fluctuations about the mean number of electron-hole pairs at a given energy are much less than that predicted by Poisson statistics which, in turn, implies a high degree of correlation between electron-hole pair creation events.

Fano (ref. 15) was the first to point out that such a correlation should exist for particles which lose all their energy in a gaseous detector such as an ionization chamber or proportional counter. The degree of correlation is indicated by a factor \( F \) which is the experimental deviation from the mean number of pairs expected from a Poisson distribution. This Fano factor \( F \) is usually given by

\[ F = \frac{(\text{FWHM})^2}{(2.355)^2 \epsilon E} \]
where FWHM is the detector resolution. A Fano factor of 1 would imply no correlation, that is, Poisson statistics. A Fano factor of 0 would indicate perfect correlation of events; that is, every particle of a given energy would produce the same number of electron-hole pairs and thus the detector resolution would be perfect. Figure 8 demonstrates how the Fano factor affects the resolution of two hypothetical spectrometer systems used to measure closely spaced low-energy photons. All conditions, based on actual spectrometer systems (ref. 11), are assumed to be identical except that detector A has $F = 1$ and detector B has $F = 0.2$. The data used are summarized as follows:

<table>
<thead>
<tr>
<th>Photon energy, keV</th>
<th>Relative intensity</th>
<th>Detector resolution, FWHM, keV</th>
<th>System resolution, FWHM, keV</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Detector A</td>
<td>Detector B</td>
</tr>
<tr>
<td>$E_1 = 21.50$</td>
<td>1</td>
<td>0.660</td>
<td>0.295</td>
</tr>
<tr>
<td>$E_2 = 22.00$</td>
<td>3</td>
<td>.668</td>
<td>.299</td>
</tr>
<tr>
<td>$E_3 = 22.50$</td>
<td>2</td>
<td>.676</td>
<td>.304</td>
</tr>
</tbody>
</table>

$F = 1.0$ for detector A, $F = 0.20$ for detector B; 
Electronic noise = 0.500 keV (FWHM) for both systems.

The spectrum from system A (for which $F = 1$) gives an indication of multiple peaks and almost no information on the relative intensities. To extract meaningful information from such a curve it must be decomposed to its component parts by a Gaussian curve fitting routine. Such a procedure generally required a computer because of the large number of computations needed to obtain the best fit. Furthermore, the proximity of a high-intensity peak increases the uncertainty in the computed value of the centroid of a smaller peak.

The three photon peaks are clearly resolved by system B ($F = 0.2$). There is no ambiguity in either the energy or intensities. Such a system could detect the presence of two photon sources of equal intensity which differ in energy by 200 eV or less.

The spectra shown in figures 5 to 7 were taken with a detector having a Fano factor of 0.205 (fig. 8) and a pulse-height analyzer and amplifier system which gave a noise contribution of about 0.75 keV, which was almost three times greater than the detector energy spread. Thus, in the measurements shown here, the amplifying system, not the detector, was the limiting factor.

The Fano factor for the detector used here was calculated from the 26.36 keV and 59.57 keV lines of Am$^{241}$, 22.10 keV line of Cd$^{109}$, and the 122.05 keV line of Co$^{57}$. The detector resolution (FWHM) was 0.331 keV at a photon energy 22.10 keV, 0.326 keV at 26.36 keV, 0.474 keV at 59.57 keV, and 0.720 keV at 122.05 keV. Figure 9 shows detector resolution squared $(\text{FWHM})^2$ plotted as a function of photon energy with $F$ as a
A Fano factor of 0.205 ± 0.012 was obtained from a least-squares fit to the data points. The uncertainty in $F$ is one standard deviation. The error bars in figure 9 are based on the following assumptions:

1. A peak of 20 channels full width at half maximum and an integrated area of approximately $10^4$ counts can be measured to ±0.25 channel.

2. The differential nonlinearity of the pulse-height analyzer should introduce an error of no more than ±2 percent in the observed width; for 20 channels this error is ±0.4 channel.

3. The pulse-height analyzer integral nonlinearity of 0.1 percent full scale could introduce an error in the peak width of not more than 0.025 channel for a 20 channel width.

4. These errors are independent, hence the uncertainty in peak width is given by

$$W = \left[ (0.25 \text{ ch})^2 + (0.4 \text{ ch})^2 + (0.025 \text{ ch})^2 \right]^{1/2}$$

$$= \pm 0.472 \text{ ch}$$

$$= \pm 0.472 \text{ ch}/20 \text{ ch} = \pm 0.0236 \text{ ch/ch}$$

$$= \pm 0.0010 \text{ keV/ch}$$

5. Since the square of the detector resolution is given by

$$W_{\text{det}}^2 = W_{\text{photon}}^2 - W_{\text{pulser}}^2$$

the extremes between values of $W_{\text{photon}}$ and $W_{\text{pulser}}$, by using the estimated uncertainty in energy per channel, represent a reasonable maximum error for $W_{\text{det}}^2$. The symbol $W_{\text{det}}$ represents FWHM of detector, $W_{\text{photon}}$ represents FWHM of observed photon peak, and $W_{\text{pulser}}$ represents FWHM of pulser peak.

A Fano factor of 0.205 compares favorably with a Fano factor of 0.26, calculated from data in reference 11 for a silicon detector, and with a Fano factor of 0.166 reported for germanium detectors in reference 16.
CONCLUDING REMARKS

The data presented demonstrate that lithium-drifted silicon detectors can be fabricated with excellent resolution in the energy range below 50 keV. Intrinsic detector resolutions of 0.331 keV at 22.10 keV, 0.326 keV at 26.36 keV, 0.474 at 59.57 keV, and 0.720 keV at 122.05 keV were measured. These measurements were used to calculate a Fano factor of 0.205 which is the lowest value reported to date for silicon. With this detector resolution, the overall resolution of the measurements is presently limited by the noise levels generated in the associated electronic systems.

Langley Research Center,
National Aeronautics and Space Administration,
Langley Station, Hampton, Va., December 18, 1968,
124-09-11-03-23.
REFERENCES


Figure 1.- Attenuation coefficients for silicon and germanium. (From ref. 14.)
Figure 2. Comparison between the intrinsic resolution of silicon and germanium detectors. Data for silicon are from reference 11; data for germanium, from reference 15.
Figure 3: Detector-preamplifier first-stage configuration.
Detector characteristics:

Silicon: p-type, boron doped, float zoned, (1,1,1) orientation

Resistivity: 10,000 $\Omega\cdot$cm (10 $k\Omega\cdot$cm)

Minority carrier life-time $\geq$ 1 ms

Dislocation density: $< 30,000$ EPD/cm$^2$

Leakage current at 77°K $\approx 10^{-11}$A at 500 V

Capacitance $\approx 10$ pF

Active area: 25 to 50 mm$^2$

Figure 4: Detector characteristics.
Figure 5.- X-ray spectrum of Am$^{241}$. Si(Li) detector at 77° K and 490 V bias; energy resolution, 0.043 keV/ch.
Figure 6.- X-ray spectrum of Cd$^{109}$ SiLi detector at 77$^0$ K and 490 V bias; energy resolution, 0.043 keV/ch.
Figure 7.- Gamma rays of Co$^{57}$. Si(Li) detector at 77 K and 490 V bias; energy resolution, 0.043 keV/ch.
Detector A
F = 1.0

Detector B
F = 0.2

Figure 8.- Effect of Fano factor on resolution.
Figure 9: Fano factor for Si(Li) detectors. \((\text{FWHM})^2 = (2.359)^2 \times \epsilon \times E.\)