STEADY-STATE AND STABILITY ANALYSIS
OF EXTERNALLY PRESSURIZED
GAS-LUBRICATED JOURNAL BEARINGS
WITH HERRINGBONE GROOVES

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**Key Words (Suggested by Author(s))**
- Gas-lubricated bearings
- Externally pressurized bearings
- Self-acting bearings
- Bearing stability
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SUMMARY

A small eccentricity analysis was performed to predict the load capacity and stability of an externally pressurized bearing with herringbone grooves. Numerical results were obtained for a range of feeding parameters, pressure ratios, groove lengths, and orifice recess volumes for compressibility numbers from 0 to 50. These results were obtained from the digital computer program which is presented in an appendix. Results showed that the addition of herringbone grooving to an externally pressurized bearing increases stability, but reduces load capacity at low compressibility numbers. A fully grooved bearing is more stable than a partially grooved bearing. Load capacity and stability decrease near the speed where the pressure due to the herringbone groove pumping equals the external supply pressure. Orifice recesses decrease stability, particularly at high compressibility numbers.

INTRODUCTION

Gas-lubricated bearings may be divided into two broad classifications: self-acting and externally pressurized. In a self-acting bearing, the film pressure which supports the load is developed by the relative motion of the bearing parts and is proportional to the fluid viscosity. When there is no motion, the load capacity is zero. In contrast, in an externally pressurized bearing, lubricant gas under pressure is supplied from an external source. Thus, this type of bearing can have a substantial load capacity even when it is stationary.

Because of the low viscosity of gases, self-acting gas-lubricated bearings will carry a much smaller load than oil-lubricated bearings. For the same reason, they are much more susceptible to self-excited instability, commonly known as fractional frequency whirl. A major part of the research in gas-lubricated bearings has been directed toward
development of bearing configurations that will operate stably. Some of these designs, for example, tilting pad bearings, achieve stability at the expense of steady-state load capacity. One type of self-acting bearing that has good stability and can also carry a higher load than a plain bearing is the herringbone grooved bearing (refs. 1 to 3). Externally pressurized bearings also have a higher load capacity than plain self-acting bearings and also are fairly stable (ref. 4).

The principal disadvantage of the externally pressurized bearing is the need for a continuous supply of pressurized gas. The herringbone bearing, on the other hand, needs no external supply, but has no load capacity at zero speed. The two bearing types could be combined; for example, a herringbone grooved rotor could be installed in an externally pressurized bearing. External pressurization could be used for a startup; upon reaching operating speed the external supply could be shut off, and the unit operated as a self-acting herringbone bearing. Alternatively, the external supply could be maintained; the inward pumping of the herringbone grooves would reduce the amount of gas needed from the external supply.

Previous analyses have evaluated the load capacity and stability of herringbone grooved bearings (refs. 1 and 2) and of externally pressurized bearings (refs. 4 to 6). Vohr and Chow determined the load capacity of herringbone grooved bearings in reference 1; their analysis was used to evaluate stability in reference 2. Experimental stability data for herringbone bearings were obtained in reference 3. The data showed that the analysis predicts the onset of instability consistently; however, actual instability occurred at somewhat lower speeds than predicted.

The load capacity of externally pressurized bearings was determined by Lund in reference 5. In a later report (ref. 6), Lund calculated the stability of externally pressurized bearings operating at finite eccentricities. Here he included the effect of orifice recess volume and attempted to account for there being a finite number of orifices, rather than the line source usually assumed. Reference 4 evaluated the stability of an unloaded externally pressurized bearing and included the effect of orifice recess volume as in reference 6.

All of these analyses are similar in that they use a small eccentricity perturbation and solve for the perturbed pressure using a separation of variables scheme. Thus it is easy, in principle, to combine the solutions to find the load capacity and stability of a herringbone bearing with external pressurization.

The objectives of this investigation are to determine analytically the steady-state and stability characteristics of externally pressurized herringbone grooved bearings. Various combinations of supply pressure, feeding parameter, orifice recess volume, and groove length will be explored.
ANALYSIS

The bearing configuration to be analyzed is shown in figure 1. It consists of a double row externally pressurized bearing with herringbone grooves. The grooves are shown on the rotor, but the analysis is unchanged if they are on the bearing. The herringbone grooves may be partial, as shown, or they may extend the full length of the bearing. For simplicity of presentation, it will be assumed that the rows of orifices are closer to the midplane of the bearing than are the herringbone grooves. This includes the limiting case of the orifice rows coinciding with the ends of the grooves. Extension to other cases is straightforward. It will be further assumed that the bearing is symmetric about the midplane. With this assumption, only half the bearing need be analyzed. Other assumptions are that the number of herringbone grooves is large (ref. 1) and that there are enough orifices so that each row may be approximated by a line source.

![Figure 1. - Externally pressurized herringbone bearing.](image)

The analysis of reference 1 applies, with the exception that the axial mass flow is no longer zero as it was in the herringbone bearing without orifices. Thus, the differential equations and boundary conditions must be modified to account for axial mass flow in the bearing and flow through the orifice.

To conveniently obtain solutions for steady whirling, which are needed for the stability analysis, a rotating coordinate system is introduced by
\[ \theta^* = \theta - \omega_p t \]  

where \( \omega_p \) is the frequency of steady circular whirling. Symbols are defined in appendix A. The differential equation to be solved (from ref. 1), is

\[
\frac{1}{R} \frac{\partial}{\partial \theta^*} \left[ \mathcal{M}_{\theta R} \sin \beta + (\mathcal{M}_{zg} - \mathcal{M}_{zr}) \alpha \cos \beta - \rho R \omega h_r \sin \beta \right] + \frac{\partial}{\partial z} \left[ \alpha \mathcal{M}_{zg} + (1 - \alpha) \mathcal{M}_{zr} \right] \sin \beta \\
+ (\omega - \omega_p) \frac{\partial}{\partial \theta^*} \left[ \rho \alpha h_g - \rho (1 - \alpha) h_r \right] \sin \beta = 0
\]

This and subsequent expressions were derived for the herringbone grooved section of the bearing, but may also be used for the smooth section by setting \( h_g = h_r \). The expressions for the mass flows \( \mathcal{M}_{\theta R}, \mathcal{M}_{zg}, \) and \( \mathcal{M}_{zr} \) are in appendix B. The procedure now is to approximate the film pressure according to

\[ p(\theta^*, z) \sim p_0(z) + \epsilon p_1(\theta^*, z) \]  

Equation (3) and the expressions for the mass flows from appendix B are substituted into equation (2). The resulting expression is considered an identity in the eccentricity ratio \( \epsilon \), and a separate equation written for each power of \( \epsilon \) which appears. Powers of \( \epsilon \) higher than 1 are neglected; thus, two equations result. The zero-order equation can be written

\[
\frac{d}{dz} \left[ \alpha \mathcal{M}_{zg0} + (1 - \alpha) \mathcal{M}_{zr0} \right] = 0
\]

This may be integrated once immediately to yield

\[
\alpha \mathcal{M}_{zg0} + (1 - \alpha) \mathcal{M}_{zr0} = \mathcal{M}_{z0} = \text{Constant}
\]

In terms of the dimensionless pressure \( P_0 = p_0 / p_a \) and dimensionless coordinate \( \zeta = z / L \), equation (5) for an isothermal bearing becomes

\[
P_0 \left[ \frac{dP_0}{d\zeta} - \frac{12 \mu \mathcal{T} \mathcal{M}_{z0} R}{C^3 p_a^2 \zeta^1} \right] = \text{Constant}
\]
The first-order equation is

\[
\frac{\partial^2 P_1}{\partial \zeta^2} + \left[ 2 \frac{dP_0}{d\zeta} - \mathscr{G}_p \right] \frac{\partial P_1}{\partial \zeta} + \mathscr{G}_3 P_0 \frac{\partial^2 P_1}{\partial \zeta^2} + \left[ \mathscr{G}_4 \frac{dP_0}{d\zeta} + \mathscr{G}_5 (\Lambda - \sigma) + \mathscr{G}_6 c \right] \frac{\partial P_1}{\partial \theta^*} + \mathscr{G}_7 P_0 \frac{\partial^2 P_1}{\partial \theta^* \partial \zeta} \\
+ \left[ \mathscr{G}_6 a \frac{dP_0}{d\zeta} + \mathscr{G}_6 b (\Lambda - \sigma) + \mathscr{G}_6 c \right] P_0 \sin \theta^* + \mathscr{G}_7 \frac{dP_0}{d\zeta} \cos \theta^* \\
+ \left[ \mathscr{G}_p - \frac{dP_0}{d\zeta} \right] \frac{dP_0}{d\zeta} \cdot \frac{1}{P_0} = 0
\]

(7)

where the \( \mathscr{G}'s \) are constants given in appendix B. They differ from the constants given in reference 1 because \( \frac{dP_0}{d\zeta} \) is not constant in a bearing with orifices. The constant \( \Lambda \) is the standard gas bearing compressibility number, and \( \sigma \) is a dimensionless representation of the whirl frequency.

**Boundary conditions.** - At the ends of the bearing

\[ P_0 = 1 \]

and

\[ P_1 = 0 \]  

(8)

At the bearing midplane, by symmetry,

\[ \frac{dP_0}{d\zeta} = \frac{\partial P_1}{\partial \zeta} = 0 \]  

(9)

Pressures \( P_0 \) and \( P_1 \) are continuous throughout the bearing film, but there will be discontinuities in the derivatives \( \frac{dP_0}{d\zeta} \) and \( \frac{\partial P_1}{\partial \zeta} \). These are caused at \( \zeta = \zeta_g \), by the end of the herringbone groove pattern, and at \( \zeta = \zeta_f \), by the gas flow through the orifices.

Since, in differential equation (6) for \( P_0 \), \( \frac{dP_0}{d\zeta} \) is the highest order derivative, the discontinuity in \( \frac{dP_0}{d\zeta} \) at \( \zeta = \zeta_g \) need not be found explicitly. The discontinuity in \( \frac{\partial P_1}{\partial \zeta} \) at \( \zeta = \zeta_g \) may be determined by noting that \( M_{z1} = \alpha M_{zg1} + (1 - \alpha) M_{zr1} \) is continuous at this point. The perturbed mass flows \( M_{zg1} \) and \( M_{zr1} \) may be found by differentiating the expressions for \( M_{zg} \) and \( M_{zr} \) (appendix B) with respect to \( \epsilon \) and
then setting $\epsilon = 0$, for example, $M_{zg1} = \partial M_{zg}/\partial \epsilon \bigg|_{\epsilon = 0}$. The result for $\partial P_1/\partial \xi$ is

$$\frac{\partial P_1}{\partial \xi} \bigg|_{\xi = \zeta_g^+} = M_{zg0} \frac{12\mu A TL}{P_0 c^3 p_a} \zeta_m \cos \theta^* + \xi_1 \frac{L}{R} \left[ \zeta_m \cos \theta^* + \frac{1}{2} \zeta_3 \frac{\partial P_1}{\partial \theta^*} + \frac{\partial P_1}{\partial \xi} \bigg|_{\xi = \zeta_g^-} \right]$$

(10)

in which $\zeta_g^+$ denotes a value of $\zeta$ infinitesimally greater than $\zeta_g$. The expression for $\zeta_m$, as well as for the other $\zeta$'s, is in appendix B.

At the orifices, conditions are similar to those in an ungrooved externally pressurized bearing, analyzed in reference 5. One important difference is that, in an externally pressurized herringbone bearing, the gas flow through the orifices can be in either direction, depending on the supply pressure and the pumping in the herringbone grooves. Boundary conditions on pressure are found by balancing the gas flow through the orifices with that through the bearing film. The results are

$$m_0 = -\frac{DP_0 c}{L \Lambda_t} \frac{dP_0}{d\xi} \bigg|_{\xi = \zeta_f^-}$$

(11)

and

$$P_0 c \left[ \frac{\partial P_1}{\partial \xi} \bigg|_{\xi = \zeta_f^-} - \frac{\partial P_1}{\partial \xi} \bigg|_{\xi = \zeta_f^+} \right] = -m_0 \Lambda_t \frac{L}{D} \frac{P_1 c}{m_0 P_s} \frac{\partial m}{\partial (P c / P_s)} \bigg|_{\epsilon = 0}$$

$$= -\frac{3 + 2\delta^2}{1 + \delta^2} \cos \theta^* - \frac{P_1 c}{P_0 c} + 2P_0 c \psi \frac{L}{D} \frac{\partial P_1 c}{\partial \theta^*}$$

(12)

The dimensionless mass flow $m$ is given by the usual orifice flow equations, with inherent compensation effects accounted for as in reference 6.

$$m = M_z \frac{4R \sqrt{AT} \left[ 1 + \left( \frac{\delta C}{h_r} \right)^2 \right]}{Na^2 p_a}$$

(13)
The flow when the bearing is concentric, $m_0$, is obtained by using the concentric values $P_c = P_{0c}$ and $h_r = C$ in equations (13) and (14). The feeding parameter $\Lambda_t$ (eqs. (11) and (12)) is defined by

$$\Lambda_t = \frac{6\mu N_a^2 \sqrt{\pi T}}{p_a C^3 \sqrt{1 + \delta^2}}$$

and $\psi_1$ (in eq. (12)) by

$$\psi_1 = \frac{NV}{\pi DLC} \cdot \frac{L}{P_{0c}D} = \frac{vL}{P_{0c}D}$$

**Solution of differential equations.** - The constant in equation (6) is determined by the gas flow through the orifices. From equation (13), with $\epsilon = 0$,

$$m_{0z} = \frac{N_a^2 p_a m_0}{4R \sqrt{\pi T} \sqrt{1 + \delta^2}}$$

Combination of equations (15) and (17) with equation (6) gives
This differential equation contains two unknowns: the pressure \( P_0 \) and the mass flow \( m_0 \). The procedure for determining \( P_0 \) and \( m_0 \) is (1) assume a value for \( m_0 \), (2) integrate equation (18) from \( \zeta = 0 \) to \( \zeta = \zeta_f \), using a forward integration scheme such as Runge-Kutta (for \( \zeta > \zeta_f \), \( m_0 = 0 \) and \( P_0 = P_{0c} \)), (3) calculate a new value of \( m_0 \) from the value of \( P_0 = P_0(\zeta_f) \) just found, and (4) compare with the previous \( m_0 \); if different, repeat steps 2 to 4 until convergence is obtained.

Differential equation (7) for \( P_1 \) may be solved (as in ref. 2) by assuming that \( P_1 \) is represented by

\[
P_1 = \rho e^{\left[ G(\zeta) e^{i\theta G} \right]} \tag{19}
\]

When this is substituted into equation (7) there results

\[
\frac{d^2 G}{d\zeta^2} + \left( 2 \frac{dP_0}{d\zeta} - \varphi + \varphi \right) \frac{dG}{d\zeta} + \frac{dG}{d\zeta} + \left[ \varphi + \frac{dP_0}{d\zeta} \left( \lambda - \sigma \right) \right] \frac{dG}{d\zeta} + \frac{1}{P_0} \left( \varphi - \frac{dP_0}{d\zeta} \right) - \frac{dP_0}{d\zeta} = 0 \tag{20}
\]

Boundary conditions for \( P_1 \) in equations (8), (9), (10), and (12) transform into the following boundary conditions for \( G \)

\[
G = 0 \quad \text{at} \quad \zeta = 0 \tag{21}
\]

\[
\frac{dG}{d\zeta} = 0 \quad \text{at} \quad \zeta = \frac{1}{2} \tag{22}
\]

\[
\frac{dG}{d\zeta} \bigg|_{\zeta = \zeta_f} = \frac{\lambda m_0 L e^m}{2 P_0 R} + \varphi \frac{L}{R} \left( \frac{\varphi + \frac{1}{2} \varphi}{2} \right) \left| \zeta = \zeta_g \right. + \frac{dG}{d\zeta} \bigg|_{\zeta = \zeta_g} \tag{23}
\]

\[
\frac{dG}{d\zeta} \bigg|_{\zeta = \zeta_f} = \frac{dG}{d\zeta} \bigg|_{\zeta = \zeta_f} - \frac{L}{G} \left( \frac{\psi_0 + \frac{m_0 \lambda}{2 P_0 c}}{2 P_0 R} + i \sigma \psi_1 \right) + \frac{1.5 + \delta^2}{1 + \delta^2} \frac{m_0 \lambda}{P_0 c R} \tag{24}
\]
The perturbed pressure $P_1$ may now be determined by solving differential equation (20) numerically by the method detailed in reference 4.

**Determination of load and stability.** - The radial and tangential components of the bearing load are found by integrating the film pressure over the bearing area.

$$\begin{bmatrix} F_r \\ F_t \end{bmatrix} = \int_0^L \int_0^{2\pi} p_a P \begin{bmatrix} -\cos \theta^* \\ \sin \theta^* \end{bmatrix} R \, d\theta^* \, dz$$

Substitution of equations (3) and (19) for $P$ and performance of the $\theta^*$ integration yields, in dimensionless variables,

$$\begin{bmatrix} f_r \\ f_t \end{bmatrix} = -\pi \begin{bmatrix} \lambda \phi \\ \lambda \mu \end{bmatrix} \int_0^{1/2} G \, d\xi$$  \hspace{1cm} (25)

The dimensionless forces in equation (25) are defined by

$$\begin{bmatrix} f_r \\ f_t \end{bmatrix} = \begin{bmatrix} \frac{F_r}{\epsilon p_a LD} \\ \frac{F_t}{\epsilon p_a LD} \end{bmatrix}$$  \hspace{1cm} (26)

The resultant bearing load $\overline{W}$ and attitude angle $\varphi$ may now be calculated.

$$\overline{W} = \frac{W}{\epsilon p_a LD} = \left( f_r^2 + f_t^2 \right)^{1/2}$$  \hspace{1cm} (27)

$$\varphi = \tan^{-1} \left( \frac{f_t}{f_r} \right)$$  \hspace{1cm} (28)

Figure 2 illustrates the relations among these quantities.

When the bearing is operating stably, the frequency number $\sigma$ is zero. To determine the threshold of instability, $\sigma$ is varied until $f_t = 0$ (ref. 7). The bearing neutral stability condition is then found by equating the centrifugal force, due to the whirling bearing mass, to the radial bearing force.
The subscript \( n \) denotes the condition where \( f_t = 0 \).

A dimensionless bearing mass may be defined by

\[
\overline{M} = \frac{M_{pa}}{2L_{\mu}^2} \left( \frac{C}{R} \right)^5
\]  

In terms of previously calculated quantities, \( \overline{M} \) for the neutral stability condition is given by

\[
\overline{M}_n = \frac{144 f_{rn}}{\sigma^2}
\]  

Reference 7 shows that \( \overline{M}_n \) is an upper limit of \( \overline{M} \) for stability if the quantity \( \partial f_t / \partial \sigma \) is negative at \( \sigma = \sigma_n \); conversely, \( \overline{M}_n \) is a lower limit for stability if \( \partial f_t / \partial \sigma \) is positive at \( \sigma = \sigma_n \).

RESULTS AND DISCUSSION

The analysis of the preceding section has been used to obtain steady-state and stability information for a number of externally pressurized herringbone bearing configura-
tions. Results were obtained using the computer program presented in appendix C. The computer program was checked by running cases for a plain externally pressurized bearing (without grooves) and a herringbone grooved bearing (without orifices). Results for the test cases agreed well with those of reference 1 and 4.

Because of the large number of parameters that may vary in a bearing, the effects of all of them were not investigated. Rather, a number of the parameters were fixed. The basic bearing chosen for study has a length to diameter ratio of 1 with a single row of orifices at the bearing midplane. No inherent compensation effects were included. The herringbone groove angle \( \beta \) is 30°; the groove width fraction \( \alpha \), 0.5; and the groove clearance to land clearance ratio \( H \), 2.1. These values approximate the optima found in reference 1 for maximizing the radial load component. Three groove length fractions \( L_g/L \) were investigated: 0 (ungrooved), 0.5, and 1 (fully grooved). The feeding parameter \( \Lambda_t \) was varied from 0 (no orifices) to 4, and the supply pressure ratio from 1 to 5. Any other configurations of interest can be easily investigated using the computer program in appendix C.

Steady State Results

Figure 3 shows the effect of the feeding parameter \( \Lambda_t \) on load capacity. Figure 3(a) is for a pressure ratio \( P_s \) of 1, which means the bearing is actually unpressurized. For this case, the load capacity \( \bar{W} \) is greatest when there are no orifices \( (\Lambda_t = 0) \); \( \bar{W} \) decreases with increasing \( \Lambda_t \). A partially grooved bearing will carry a higher load than a fully grooved bearing. The ungrooved bearing is not shown for this case; it is unsuitable for most uses because it is unstable when not loaded.

Figure 3(b), for a pressure ratio of 2, shows that at low values of \( \Lambda \) (less than about 5) the load capacity now increases with increasing feeding parameter \( \Lambda_t \). At higher \( \Lambda \)'s the order is reversed for the grooved bearings. That is, load capacity decreases with increasing \( \Lambda_t \), as was the case for the unpressurized bearing. The load capacity of the partially grooved bearing again exceeds that of the fully grooved bearing. For \( \Lambda \) less than 13 to 33 (depending on feeding parameter) the ungrooved bearing has the highest load capacity. At higher \( \Lambda \), the load curves for the ungrooved bearings level off, while those for the grooved bearings continue to rise. This, of course, is because of the increasing self-pressurization by the inward pumping herringbone grooves.

The load curves for the grooved bearings show an interesting phenomenon in that they have a pronounced depression at an intermediate value of \( \Lambda \). This depression occurs when the pumping of the herringbone grooves raises the pressure on the bearing side of the orifices to the pressure that is supplied externally. Near this point, the derivative of mass flow with respect to bearing orifice pressure \( P_c \) becomes very large.
Figure 3. - Effect of feeding parameter $\Lambda_1$ on load. Length to diameter ratio, $l_1$; orifice location parameter $L_y/L_1$; groove angle, 30°; groove width fraction, 0.5; groove to land clearance ratio, 2.1.
That is, a very small change in $P_c$ causes a large change in orifice flow. Consequently, the bearing is not as well compensated and the stiffness is reduced.

It should be pointed out that for an actual bearing the loss of load capacity will not be as great as predicted by figure 3(b). This is because the difference $\Delta m/\Delta(P_c/P_s)$ for finite $\Delta(P_c/P_s)$ does not approach the infinite value of the derivative $\partial m/\partial(P_c/P_s)$. Also, the orifice flow equations (14) neglect viscous effects. These become significant at low flow rates and reduce the value of $\partial m/\partial(P_c/P_s)$ near $P_c = P_s$.

Load curves for a pressure ratio of 5 are plotted in figure 3(c). The trends of figures 3(a) and (b) are continued here. Load capacity increases with increasing $\Lambda_t$ out to the highest compressibility number plotted. No depressions occur in the curves (as in fig. 3(b)), because the $\Lambda$ value where $P_c = P_s$ is beyond the boundary of the figure.

Figures 3(b) and (c) show that the addition of grooves to an externally pressurized bearing lowers the load capacity at low compressibility numbers, but at higher $\Lambda$ the load can be increased. The compressibility number, where the load capacity of the grooved bearing first becomes greater than that of the ungrooved bearing, varies with the pressure ratio, length of grooves, and feeding parameter.

The effect of pressure ratio on load is shown in figure 4. Load capacity generally increases with pressure ratio. The load capacity for $P_s = 2$ is little different than for $P_s = 1$ (unpressurized), particularly at higher compressibility numbers. Near the value of $\Lambda$ where $P_c = P_s$ (depression in load curve), the load capacity for $P_s = 2$ can drop below that for $P_s = 1$. Increasing the pressure ratio to 5 results in a relatively large increase in load capacity, particularly at low compressibility numbers and large feeding parameters.

Attitude angles are plotted in figure 5 for a pressure ratio of 2. Except at quite low compressibility numbers ($\Lambda < 5$), attitude angles are smaller for smaller values of the feeding parameter $\Lambda_t$. The grooved bearings (figs. 5(b) and (c)) exhibit behavior generally similar to an ungrooved externally pressurized bearing, with two exceptions. At zero speed ($\Lambda = 0$) the grooved bearings have a small attitude angle, which may be positive or negative, depending on the length of the grooves. In addition, when the pumping of the herringbone grooves increases the pressure $P_c$ to near the supply pressure $P_s$, the attitude angle rises rapidly. This corresponds to the drop in load capacity mentioned earlier. A comparison of figures 5(a) to (c) shows that attitude angle decreases with increasing groove length, except at high compressibility numbers ($\Lambda > 35$), where the bearing with half-length grooves has a lower attitude angle than either the fully grooved or ungrooved bearing.

Because the herringbone grooves act as a pump, the gas pressure in the bearing increases with increasing compressibility number. Figure 6 shows the pressure at the center of the bearing, $P_{oc}$, for three values of the feeding parameter $\Lambda_t$, at an external
Figure 5. - Effect of feeding parameter on attitude angle. Pressure ratio $P_C/P_S$, length to diameter ratio, $L_g/L$, orifice location parameter $L_y/L$, groove angle, $30^\circ$; groove width fraction, 0.5; groove to land clearance ratio, 2.1.

Figure 6. - Pressure at center of bearing. Pressure ratio, $P_C/P_S$, length to diameter ratio, $L_g/L$, orifice location parameter $L_y/L$, groove angle, $30^\circ$; groove width fraction, 0.5; groove to land clearance ratio, 2.1.
supply pressure ratio of 2. As expected, larger values of $\Lambda_t$ decrease the rate of change of $P_{oc}$ with $\Lambda$. This is because a larger $\Lambda_t$ means the bearing is more open to the external supply. The fully grooved bearing's pressure changes more rapidly than does the partially grooved, since pumping is proportional to groove length. Pressure does not change with compressibility number in the ungrooved bearings; to avoid confusion, these curves have not been extended to $\Lambda = 0$. The solid lines, for $\Lambda_t = 0$, indicate the pressure in a bearing with no orifices; they are, of course, valid for any supply pressure.

The gas mass flow through the bearing appears in figure 7 for the same bearing conditions as in figure 6. There are additional curves for $\Lambda_t = 1$. For $\Lambda_t = 0$, the mass flow is always 0. A negative value of $m_0$ indicates the gas flow is from the pressurized
supply to the bearing, whereas positive \( m_0 \) indicates the bearing is pumping gas into the pressurized supply.

The mass flow curves are arranged in the same order as the bearing pressure curves of figure 6. Note that the magnitude of the dimensionless flow \( m_0 \) decreases as the feeding parameter increases. This is due to the way mass flow is made dimensionless. At zero speed \( (\Lambda = 0) \), gas consumption increases with increasing length of grooves. This is because a grooved portion of a bearing has a larger flow area, and thus offers less resistance than an ungrooved portion.

**Stability Results**

In order to keep the figures presented to a reasonable number, stability information will not be given for all combinations of groove length, pressure ratio, feeding parameter, and orifice recess volume which were investigated. Instead, the basic bearing mentioned at the beginning of this section will be further defined, and results presented for variations of each of the preceding four parameters from their basic values. These basic values are \( L_g/L = 1, P_s = 2, \Lambda_t = 2, \text{ and } v = 0. \)

Figure 8 shows the variation of stability with compressibility number, with groove length as a parameter. Stability, as measured by the dimensionless mass \( \overline{M} \), generally decreases with increasing \( \Lambda \), and increases with groove length. Above a compressibility number of 15, the stability of the fully grooved bearing increases sharply and becomes much greater than that of either the half-grooved or ungrooved bearing.

The stability curves of the fully grooved and half-grooved bearings have distinct depressions near \( \Lambda = 14 \) and \( \Lambda = 27 \), respectively. These depressions correspond to the depressions in the load curves of figures 3(b) and 4(b). As was discussed regarding the load capacity curves, the drop in stability in an actual bearing whirling with a finite eccentricity would probably not be as drastic as figure 8 predicts. With an actual bearing, problems with this low stability region can probably be avoided by passing through the region rapidly, either by accelerating the bearing rotor or changing the supply pressure.

Near a compressibility number of 38, the stability curve for the half-grooved bearing becomes very steep, in effect imposing an upper speed limit even for very small values of \( \overline{M} \). This limit generally occurred between compressibility numbers of 20 and 40 in the half-grooved bearings. A similar limit was not observed for fully grooved or ungrooved bearings within the range of compressibility numbers investigated.

The effect of the feeding parameter \( \Lambda_t \) on stability is shown by figure 9. At low compressibility numbers \( (\Lambda < 5) \), higher feeding parameters give greater stability. Near \( \Lambda = 14 \), where the herringbone pumping pressure becomes equal to the supply
Figure 8. - Effect of groove length on stability. Pressure ratio $P_s$, 2; feeding parameter, 2; orifice recess volume ratio, 0; length to diameter ratio, 1; orifice location parameter $L_d/L_1$; groove angle, 30°; groove width fraction, 0.5; groove to land clearance ratio, 2.1.

Figure 9. - Effect of feeding parameter on stability. Pressure ratio $P_s$, 2; groove length ratio $L_d/L_1$, 1; orifice recess volume ratio, 0; length to diameter ratio, 1; orifice location parameter $L_d/L_1$, 1; groove angle, 30°; groove width fraction, 0.5; groove to land clearance ratio, 2.1.
pressure, the order is reversed, with the no-orifice bearing \( \Lambda_t = 0 \) most stable. At high \( \Lambda (>20) \), there is no clear trend. The greatest stability is offered by \( \Lambda_t = 2 \), and the least by \( \Lambda_t = 4 \).

Figure 10 shows the effect on stability of a variation in supply pressure ratio. Included in this figure is the curve for \( \Lambda_t = 0 \); the remainder of the curves are for \( \Lambda_t = 2 \). For low compressibility numbers \( \Lambda < 10 \), \( P_s = 5 \) provides the greatest stability; the curve is beyond the maximum ordinate of the figure. Stability decreases with decreasing pressure ratio. The plain herringbone bearing \( \Lambda_t = 0 \) is between \( P_s = 1 \) and \( P_s = 2 \) (\( P_s = 1 \) denotes a bearing whose supply lines are open to the atmosphere). For compressibility numbers between 10 and 20 there is no clear optimum, as the curves rise and fall. At high \( \Lambda \), pressure ratios of 1 and 2 are more stable than \( P_s = 5 \) or the no-orifice bearing. The figure shows that the addition of orifices to a herringbone bearing, without pressurization, lowers the stability at low compressibility numbers, but can increase the stability at high \( \Lambda \).

The decrease in stability due to a small orifice recess is shown in figure 11. For
compressibility numbers less than 14 there is only a small loss of stability. At higher \( \Lambda \), however, the stability for a recess volume ratio of 0.2 continuously decreases, while the stability for \( v = 0 \) increases from \( \Lambda = 14 \) to a maximum at \( \Lambda = 40 \) before decreasing. This behavior at higher compressibility numbers is typical of the effect of recess volume on the bearing configurations studied.

**Multibranch curves.** - For all cases of finite recess volume in grooved bearings, there was more than one neutral stability condition found at the higher compressibility numbers. That is, for a given \( \Lambda \), there was more than one whirl frequency which yielded \( f_L = 0 \). Figure 12 illustrates this for a feeding parameter of 2, pressure ratio of 5, and recess volume ratio of 0.2. The controlling curve will be the lowest; this will give the maximum value of \( \bar{M} \) at which the bearing will be stable. Therefore, in using the analysis to determine stability, one must use some caution to be certain the smallest value of \( \bar{M}_n \) has been found.
SUMMARY OF RESULTS

A small eccentricity analysis was performed to determine the steady-state and stability characteristics of externally pressurized bearings with herringbone grooves. Compressibility numbers from 0 to 50 were investigated. The following results were obtained for a bearing with a single row of orifices and a length to diameter ratio of 1:

1. The addition of herringbone grooves to an externally pressurized bearing increases the stability of the bearing. Grooving reduces load capacity at low compressibility numbers but increases load capacity at high compressibility numbers.

2. The fully grooved bearing is generally more stable than the partially grooved bearing. This is especially true at high compressibility numbers. However, the partially grooved bearing has a higher load capacity.

3. At low compressibility numbers, stability increases with increasing supply pressure and feeding parameter. At high compressibility numbers, there is no clear relation of stability with feeding parameter and supply pressure.
4. Load capacity and stability decrease, and the attitude angle increases near the speed where the pressure due to the herringbone groove pumping equals the external supply pressure. This at least partly due to assumptions in the analysis.

5. Orifice recesses decrease stability. The effect is marked at high compressibility numbers. When there are orifice recesses, more than one neutral stability condition can exist at high compressibility numbers. The controlling condition is that which gives the lowest dimensionless mass for neutral stability.

Lewis Research Center,  
National Aeronautics and Space Administration,  
Cleveland, Ohio, March 30, 1970,  
129-03.
APPENDIX A

SYMBOLS

\(a\) orifice radius

\(C\) ridge clearance at zero eccentricity

\(\epsilon\) coefficient (see appendix B)

\(D\) bearing diameter

\(d\) orifice recess diameter

\(e\) journal eccentricity

\(F\) bearing load component

\(f\) dimensionless load component, \(F/\epsilon p_aLD\)

\(G\) dimensionless complex function of \(\zeta\)

\(H\) ratio of ridge clearance to groove clearance when bearing is concentric, \((h_g/h_r)_0\)

\(h_g\) local film thickness over groove, \(C(H + \epsilon \cos \theta^*)\)

\(h_r\) local film thickness over ridge, \(C(1 + \epsilon \cos \theta^*)\)

\(\text{Im}\) imaginary part of expression

\(i\) \(\sqrt{-1}\)

\(k\) specific heat ratio

\(L\) bearing length

\(L_f\) length of bearing outboard of orifices

\(L_g\) total axial length of grooves

\(M\) rotor mass per bearing

\(\mathcal{M}\) lubricant flow per unit length

\(\bar{M}\) dimensionless rotor mass, \((MP_a/2L\mu^2)(C/R)^5\)

\(\bar{M}_2\) dimensionless rotor mass, \(MC\omega^2/p_aLD\)

\(m\) dimensionless lubricant flow rate, \(4\alpha\zeta R \sqrt{RT} \sqrt{1 + \delta^2}/Na^2 p_a\)

\(N\) number of orifices per bearing

\(P\) dimensionless pressure, \(p/p_a\)

\(p\) pressure

\(p_a\) atmospheric pressure

\(R\) bearing radius

\(\alpha\) gas constant

\(\Re\) real part of expression

\(T\) absolute temperature

\(t\) time

\(U_g\) surface speed of grooved member

\(U_p\) surface speed of smooth member

\(V\) orifice recess volume

\(v\) orifice recess volume ratio, \(NV/\pi DLC\)

\(W\) total bearing load

\(\bar{W}\) dimensionless load, \(W/\epsilon p_a LD\)

\(z\) axial coordinate measured from end of bearing

\(z_f\) distance from end of bearing to first row of orifices

\(z_g\) \(L_g/2\)

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\[ \alpha \] ratio of groove width to width of groove-ridge pair

\[ \alpha_d \] orifice discharge coefficient

\[ \beta \] groove angle (fig. 1)

\[ \delta \] inherent compensation factor, \( a^2/dC \)

\[ \epsilon \] eccentricity ratio, \( e/C \)

\[ \zeta \] dimensionless axial coordinate, \( z/L \)

\[ \zeta_f \] \( z_f/L \)

\[ \zeta_g \] \( z_g/L \)

\[ \theta \] angular coordinate

\[ \theta^* \] rotating angular coordinate, \( \theta - \omega_p t \)

\[ \Lambda \] bearing compressibility number, \( 6\mu\omega R^2/p_a C^2 \)

\[ \Lambda_s \] \( \Lambda(L/R) \) if smooth member is rotating; \( -\Lambda(L/R) \) if grooved member is rotating

\[ \Lambda_t \] feeding parameter, \( 6\mu N_a^2 \sqrt{\omega T/p_a C^3} \sqrt{1 + \delta^2} \)

\[ \mu \] lubricant dynamic viscosity

\[ \rho \] local lubricant density

\[ \sigma \] frequency number, \( 12\mu\omega R^2/p_a C^2 \)

\[ \varphi \] attitude angle

\[ \psi_0 \] \( -(\lambda_t/2P_{0c}) [\partial m/\partial (P_c/P_s)] \big|_{\epsilon=0} \)

\[ \psi_1 \] \( NV/\pi D^2 CP_{0c} \)

\[ \omega \] rotational speed

\[ \omega_p \] whirl frequency

**Subscripts:**

- \( c \) condition immediately downstream of orifice
- \( g \) groove region
- \( n \) condition at which \( f_t = 0 \)
- \( r \) radial; ridge region
- \( s \) condition upstream of orifice
- \( t \) tangential
- \( z \) axial direction
- \( \theta \) circumferential direction
- \( 0 \) zero eccentricity
- \( 1 \) perturbed quantity

**Superscripts:**

- \(+\) value of coordinate infinitesimally greater than base value
- \(-\) value of coordinate infinitesimally less than base value
APPENDIX B

EXPRESSIONS FOR BEARING MASS FLOW AND DIFFERENTIAL EQUATION COEFFICIENTS

Mass Flow Expressions Used in Equation (2) (from ref. 1)

\[
\mathcal{M}_z = \frac{\rho}{12\mu} \frac{h_g^3}{\alpha h_r^3 + (1 - \alpha)h_g^3} \left\{ (1 - \alpha)(h_g^3 - h_r^3) \sin \beta \cos \frac{1}{R} \frac{\partial P}{\partial \theta} \right. \\
+ \left[ h_r^3 + (1 - \alpha)(h_g^3 - h_r^3) \sin^2 \beta \right] \frac{\partial P}{\partial z} - 6\mu(1 - \alpha)(U_p - U_g)(h_g - h_r) \sin \beta \cos \beta \}
\]

\[
\mathcal{M}_r = \frac{\rho}{12\mu} \frac{h_r^3}{\alpha h_r^3 + (1 - \alpha)h_g^3} \left\{ \alpha(h_g^3 - h_r^3) \sin \beta \cos \frac{1}{R} \frac{\partial P}{\partial \theta} \right. \\
+ \left[ h_g^3 - \alpha(h_g^3 - h_r^3) \sin^2 \beta \right] \frac{\partial P}{\partial z} + 6\mu\alpha(U_p - U_g)(h_g - h_r) \sin \beta \cos \beta \}
\]

\[
\mathcal{M}_\theta = \frac{\rho}{12\mu} \frac{h_r^3}{\alpha h_r^3 + (1 - \alpha)h_g^3} \left\{ \left[ h_g^3 - \alpha(h_g^3 - h_r^3) \cos^2 \beta \right] \frac{1}{R} \frac{\partial P}{\partial \theta} - \alpha(h_g^3 - h_r^3) \sin \beta \cos \beta \frac{\partial P}{\partial z} - 6\mu\alpha(U_p - U_g)(h_g - h_r) \sin^2 \beta \right. \\
+ \left. \frac{\rho h_r}{2} (U_p + U_g) \}
\]

Differential Equation Coefficients

\[
\varphi_1 = \frac{H^3 + \alpha(1 - \alpha)(H^3 - 1)^2 \sin^2 \beta}{\alpha + (1 - \alpha)H^3}
\]
\[ \mathcal{E}_p = \frac{\alpha(1 - \alpha)(H^3 - 1)(H - 1) \sin \beta \cos \beta \Lambda_s}{H^3 + \alpha(1 - \alpha)(H^3 - 1)^2 \sin^2 \beta} \]
\[ \mathcal{E}_3 = \frac{2\alpha(1 - \alpha)(H^3 - 1)^2 \sin \beta \cos \beta L}{H^3 + \alpha(1 - \alpha)(H^3 - 1)^2 \sin^2 \beta} \]
\[ \mathcal{E}_{4a} = \mathcal{E}_3 \]
\[ \mathcal{E}_{4b} = -\frac{(\alpha H + 1 - \alpha)[\alpha + (1 - \alpha)H^3]}{H^3 + \alpha(1 - \alpha)(H^3 - 1)^2 \sin^2 \beta} \left( \frac{L}{R} \right)^2 \]
\[ \mathcal{E}_{4c} = \frac{\alpha(1 - \alpha)(H^3 - 1)(H - 1)\Lambda_s \sin^2 \beta}{L} \]
\[ \mathcal{E}_5 = \frac{H^3 + \alpha(1 - \alpha)(H^3 - 1)^2 \cos^2 \beta \left( \frac{L}{R} \right)^2}{H^3 + \alpha(1 - \alpha)(H^3 - 1)^2 \sin^2 \beta} \]
\[ \mathcal{E}_{6a} = \frac{3\alpha(1 - \alpha)(H^3 - 1)(H - 1) \sin \beta \cos \beta \left[ \alpha(H^2 - H - 1) - (1 - \alpha)H^2(H^2 + H - 1) \right]}{L} \]
\[ \left[ H^3 + \alpha(1 - \alpha)(H^3 - 1)^2 \sin^2 \beta \right] \left[ \alpha + (1 - \alpha)H^3 \right] \]
\[ \mathcal{E}_{6b} = \frac{\left[ \alpha + (1 - \alpha)H^3 \right]}{H^3 + \alpha(1 - \alpha)(H^3 - 1)^2 \sin^2 \beta} \left( \frac{L}{R} \right)^2 \]
\[ \mathcal{E}_{6c} = \frac{3\alpha(1 - \alpha)(H - 1)^2H^2\Lambda_s \sin^2 \beta}{\left[ H^3 + \alpha(1 - \alpha)(H^3 - 1)^2 \sin^2 \beta \right] \left[ \alpha + (1 - \alpha)H^3 \right]} \]
\[ \mathcal{E}_7 = \frac{3\alpha(1 - \alpha)(H - 1)(H^2 - 1)\Lambda_s \sin \beta \cos \beta \left[ H^2(H^2 + 1) + \alpha(1 - \alpha)(H^3 - 1)^2 \sin^2 \beta \right]}{L} \]
\[ \left[ H^3 + \alpha(1 - \alpha)(H^3 - 1)^2 \sin^2 \beta \right]^2 \]


\[ e_m = \frac{3\alpha H^2(H - 1)}{[H^3 + \alpha(1 - \alpha)(H^3 - 1)^2 \sin^2 \beta]^2} \left[ 1 + (1 - \alpha)(H^3 - 1)^2 \sin^2 \beta \right] \]

In the ungrooved portion of the bearing, these coefficients become

\[ e_p = 0 \]
\[ e_3 = 0 \]
\[ e_{4a} = 0 \]
\[ e_{4b} = -\left(\frac{L}{R}\right)^2 \]
\[ e_{4c} = 0 \]
\[ e_5 = \left(\frac{L}{R}\right)^2 \]
\[ e_{6a} = 0 \]
\[ e_{6b} = \left(\frac{L}{R}\right)^2 \]
\[ e_{6c} = 0 \]
\[ e_7 = 0 \]
APPENDIX C

COMPUTER PROGRAM FOR ANALYSIS OF EXTERNALLY PRESSURIZED
HERRINGBONE GROOVED GAS-LUBRICATED JOURNAL BEARING

The program for determining steady-state and stability characteristics of the externally pressurized herringbone bearing is written in FORTRAN IV, version 13, for use on the IBM 7094-II digital computer at Lewis Research Center. Minor modifications may be necessary to allow the program to be used with other computing systems.

Program Input

Two variables are set within the program: \( k \), the specific heat ratio of the lubricant gas, and RKEP, an accuracy parameter. As the program operates, the step size in the Runge-Kutta differential equation solver is successively halved until the magnitude of the bearing load \( W \) varies by less than RKEP times \( W \).

The remainder of the information needed by the program is read from punched cards. A triad of cards shows each configuration to be analyzed. The first gives geometric and operating parameters; the second contains the array of bearing numbers \( \Lambda \) to be used (up to 19 values); and the third gives initial estimates of the frequency number \( \sigma \), one for each \( \Lambda \) value. Specific formats follow.

Geometric configuration card: Format (13F6.0). - Succeeding eight-column fields contain, in real format (with decimal point): \( \beta, \alpha, H, L/D, L_{g}/L, SGN, L_{f}/L, \Lambda_{t}, P_{S} \), \( v, \sigma_{d} \), and \( 1 + \delta^{2} \). \( SGN \) is +1.0 if the smooth member of the bearing is rotating, and -1.0 if the grooved member is rotating.

Bearing number array card: Format (14, 19F4.1). - First four-column field: the number of \( \Lambda \)'s in the array, integer format, right adjusted. Succeeding four-column fields: the values of \( \Lambda \) for which calculations are desired, real format (with decimal point). Positive \( \Lambda \) means the program will search for a root of \( f_{t} = 0 \) such that \( \partial f_{t} / \partial \sigma < 0 \). The reverse is true if \( \Lambda \) is negative.

Frequency number estimate card: Format (4X, 19F4.0). - First four-column field is not read. Succeeding four-column fields contain, in real format (with decimal point), the initial estimate of frequency number \( \sigma \), one value for each \( \Lambda \).

Any number of geometric configurations may be examined in one run of the program. Sample program input on a FORTRAN coding sheet appears as figure 13.

The first card is a geometric configuration card which indicates that \( \beta = 30^{\circ} \), \( \alpha = 0.5, H = 2.1, L/D = 1, L_{g}/L = 1, SGN = -1, L_{f}/L = 1, \Lambda_{t} = 2, P_{S} = 2, v = 0, \sigma_{d} = 0, \) and \( 1 + \delta^{2} = 1 \). The second card, the \( \Lambda \) array, indicates there are 13 \( \Lambda \) values ranging
from 0 to 50. The third card is the \( \sigma \) estimate card, showing initial estimates of \( \sigma \), which correspond to the \( \Lambda \) array. Any number of these sets of three cards may be used.

When the orifice discharge coefficient is specified as zero on the geometric configuration card, the actual value used is computed as a function of the pressure ratio across the orifice, using the information in reference 2. If a nonzero \( \sigma_d \) is specified, that value is used.

**Program Output**

Output consists of two sheets for each configuration: A working sheet and a calculation summary sheet.

The working sheet shows the geometric and operating parameters, trial values for determination of the pressure downstream of the orifices, final value of orifice downstream pressure, \( \psi_0 \), \( \psi_1 \), and RKEP. For each \( \Lambda \) in the array and for each trial value of \( \sigma \) there appear \( \Lambda, f_r, f_t, W/(\varepsilon p_a LD), \varphi, \bar{M}_a \), final Runge-Kutta step size, \( M \), \( \omega_p/\omega \), \( \sigma \), and a coefficient applied to \( \psi_0 \) in equation (24). This coefficient, in refer-
ence 4, was taken as 1 when \( \sigma \) was 0, and 0 otherwise. In the present work it is always 1. A sample working sheet appears as figure 14. The data appearing thereon were generated from the values shown in the sample input.

The calculation summary sheet again shows the geometric and operating parameters, and, for each \( \Lambda \) of the \( \Lambda \) array, \( W/(e_pLD) \), \( \varphi \), \( \omega_p/\omega \), \( \sigma_n \), \( \bar{M}_n \), \( \bar{M}_n \), \( P_c \), \( \partial f/\partial \sigma \), \( m_0 \), \( \sigma_d \) (actual value used), and the \( \psi_0 \) coefficient. Figure 15 shows an example of a summary sheet. Again, the data correspond to those of the sample input. Program execution time for the sample input was 20 seconds.
### Table 1:

**Externally Pressurized Herringbone Bearing -- Grooved Member Rotating**

<table>
<thead>
<tr>
<th>L/D</th>
<th>L/L</th>
<th>LAMBDA</th>
<th>T</th>
<th>I*DELTA**Z</th>
<th>K=CP/CV</th>
<th>ORIF COEF</th>
<th>REC_VOL</th>
<th>VC</th>
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<td>1.000</td>
<td>2.000</td>
<td>1.000</td>
<td>1.400</td>
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<td>0</td>
<td></td>
<td></td>
</tr>
<tr>
<td>FS/PA</td>
<td>BETA</td>
<td>ALFA</td>
<td>H</td>
<td>LG/L</td>
<td>RKEP</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
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<td>30.00</td>
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<td>2.100</td>
<td>1.000</td>
<td>0.500E-02</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

<table>
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<th>BRG LOAD W/EPALU</th>
<th>ATT ANGLE PHI</th>
<th>WHIRL RATIO WP/OMEGA</th>
<th>VIB NR SIGMA</th>
<th>STABILITY PARAMETERS MKR2/PALD</th>
<th>MRC5/2LR5MU2</th>
<th>PC/PA</th>
<th>DIFVT DISIGMA</th>
<th>MASS FLOW PG</th>
<th>ORIFICE COEF AO</th>
<th>PSD COEF</th>
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<td>1.000</td>
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<td>0.589E-04</td>
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<td>0.328</td>
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<td>0.531</td>
<td>1.326</td>
<td>-0.83E-01</td>
<td>-0.889</td>
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<td>-0.874</td>
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<td>11.55</td>
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<td>0.340</td>
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<td>9.778</td>
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</table>

Figure 15. - Calculation summary sheet.
C SMALL ECCENTRICITY STABILITY ANALYSIS FOR HERRINGBONE BEARING WITH ORIFICES
D DIMENSION SLAM(20),SN(20),SPE(20),SM(20),SSIG(20)
D DIMENSION ASM(20),SD(20),SPC(20),SMU(20),SAD(20),SPS(20)
D COMMON /CYH/ DP,UC,DG,DS
D COMMON /PCG/ PK,K,SK1,SK2,VARA,AD
D COMMON /CHR/ CG,UC,C
D COMMON /HLM/ GM,CG,GC,GZ3A,GZ3B,GZ3C,GZ3D,S
D COMMON /HLS/ LAMDA,PSD,PS1,CM,SMA,CMC,N,PHI,WR,RKEP,Q,L,PC,C4A,B,C4C
D COMMON /CHR/ CG,20,Z3,ZD
D REAL LS,LG,LO,LT,MU,L(2),K,LS,LAMDA
D COMPLEX IC3A,IC4A,IC4W,IC5A,IC5W,IC6A,IC6W,IC6W
D COMPLEX Y(2),A(2),Z(2),XF,CDX,CG,D3
D LOGICAL VARA,FIRST
D EXTERNAL F1
D ALPHAP = .84276 + (.06451 + (-.75195 + .43415*P)*P)*P
D EPS = 1.E-4
D EPSW = 1.E-3
D K = 1.4
D SK1 = SQRT (2.*K/(K+1.))* (2.1/(K+1.))* (1./ (K-1.))
D SK2 = SQRT (2.*K/(K-1.))
D PR3 = (2.1/(K+1.))* (K/(K-1.))
D RKEP = .005
D READ (5,5) BETAD,ALFA,H,CL,LC,SN,LS,LT,PS,VC,AD,DL
D F4,5MAT (13F6.0)
D C BETAD = GROOVE ANGLE, DEGREES, ALFA = GROOVE WIDTH FRACTION, H = GROUJVF
D C CLEARANCE/LAND CLEARANCE, CL = L/D, LS = GROOVE LENGTH FRACTION LG/L
D C SG = +1.0 FOR SMOOTH MEMBER ROTATING, -1.0 FOR GROOVED MEMBER ROTATING
D C LO=FRACME OF LENGTH OUTBOARD OF ORIFICES, LT=LAMBDAT, PS=PRESSURE RATIO
D C ORICETRESS VOLUME RATIO, ALF=ORIFICE COEFFICIENT, DL=1+DELT**2
D C LG=1 DENOTES FULLY GROOVED BEARING, LG=0 DENOTES SINGLE ROW OF ORIFICES
D IF (LG=.EQ.0.) SG = 0.
D VARA = .FALSE.
D IF (AD.EQ.0.) VARA = .TRUE.
D READ (5,1) IS, (SLAM(I), I = 1, IS)
D F3,4MAT (14,19F4.1)
D READ (5,2) (SSIG(I), I = 1, IS)
D F4,5MAT (14,19F4.0)
D F4,5MAT (1,1)I/8X,65H SMALL ECCENTRICITY ANALYSIS FOR HERRINGBONE BEARING
D WITH ORIFICES
D PCB = PS*PCR
D BETA = SG (BETAD/57.2957/96, SG)
D L = 2.*CL
D SI = SIN (3*BETA)
D CJ = COS (3*BETA)
D ALFI = 1.-ALFA
D H2 = H*H
D H3 = H2*H
D DN = ALFA*ALFI*H3
D H32 = (H3-1.)*H2
D AA = ALFA*ALFI
D AS = AA*S1*S1
D ASC = AA*SI*CJ
D D3 = H3+AS*H32
D H31 = (H3-1.)*(H-H3)
D C1 = D2/(DN*DL)
D WRITE (6, 707)
701701 FORMAT (1HI/15X,45HEXERNALLY PRESSURIZED HERRINGBONE BEARING -- )
91  IF (SG4) 9, 90, 91
91  WRITE (6,808)
808  FORMAT (1HI+ 60X, 22+SMOOTH MEMBER ROTATING )
90  GO TO 902
90  WRITE (6,890)
890  FORMAT (1HI+ 60X,17+UNGROOVED BEARING )
90  GO TO 902
9  WRITE (6,909)
909  FORMAT (1HI+ 60X, 23+GROOVED MEMBER ROTATING )
902  WRITE (6,909)
6  FJRMT (6HL BETA 7X,4+ALFA 8X,20LH 9X,3HL/D 7X,6HL(J)/L 5X,6HL(J)/I-
1 4X,8HLAMDBA T 4X,5HPS/PA 8X,2+VC 6X,8HOKF. C3EF 4X,5H1+D**2 5X,
2 7HK=CP/CV )
6  IF (*NUT,VARA) WRITE (6,61) BETAD,ALFA,H,CL,LG,LU,LT,PS,VC,AL,DL,<
61  FJRMT (12G11.3)
6  IF (VARA) WRITE (6,62) BETAD,ALFA,H,CL,LG,LU,LT,PS,VC, AL,DL,<
62  FJRMT (9G11.3, dHVARAble 3X 2511.3)
ZG = LG/2,
ZD = LG/2,
CZA = 2.*
ICZA = (0.,2.)*ASC*H32/D2*L
IC4A = L3A
IC5A = (H3 + AA*CG*CG*H32)/D2*L
IC6A = (0.,3.)*ASC*H31*(ALFA*(H2+H-1.)) - ALFI*12*(H2+H-1.))/D2/D4*L
C6B = L/C1
C4B = -C6B*(ALFI + ALFA*H)
C5S = L*L
DPT = 3./UN/J2*ALFA*12*(H1.)*1. + ALFI*(H3-1.)*SI*SI*(2.*ALFA
1. + ALFI*(H3+1.))
DG = IC3A*C1*L/2.
DGP = C1*L
DO 300 I=1,IS
SDS = SIGN (1.+, SLAM(I))
SLAM(I) = ABS (SLAM(I))
LAMBDA = SLAM(I)
6  IF (LAMBDA.EQ.0. AND. (PS.EQ.1. OR. LT.EQ.J.)) GO TO 333
6  IF (LAMBDA.EQ.0. AND. (PS.EQ.1. OR. LT.EQ.J.)) GO TO 333
6  IF (LG.EQ.0. AND. I.GT.1) GO TO 27
LS = SGNS*L*LAMBDAL
CP = ASC*H31*LS/32
WRITE (6,8) LAMBDAL
8  FJRMT (17HLSOLUTION FOR PUC 8X 7HLAMBDAL= 61.371)
HLM = 0.
HLM2 = 0.
MO = 0.
PC = 1. + CG*ZG
6  IF (LT.EQ.0.) GO TO 25
PC = AMAX1 (PC, SQRT(PS))
XF = ZG
CDX = LG/32.
DJI 20 J = 1, 10
6  IF (*NUT,VARA) GO TO 15
P = PC/PS
6  IF (P.GT.1.) P = 1./P
AL = ALPHA(P)
33
<table>
<thead>
<tr>
<th>Line</th>
<th>Code</th>
</tr>
</thead>
<tbody>
<tr>
<td>22</td>
<td>IF (ZG .EQ. 0.), GO TO 23</td>
</tr>
<tr>
<td>23</td>
<td>ZG = ZG - (1. - PC<em>PC) / HLM2/2.</em></td>
</tr>
<tr>
<td>24</td>
<td>IF (PC .LT. PCA*.AND.*PCI.LT.PCA) PCI = SQRT(1. - 2.<em>HLM2</em>Z0)</td>
</tr>
<tr>
<td>81</td>
<td>Y(2) = 1.</td>
</tr>
<tr>
<td>92</td>
<td>CALL RKGC (F1, Y, XF, CJX, A, B, Z)</td>
</tr>
<tr>
<td>25</td>
<td>PS = -LT/2.*UMO/PC</td>
</tr>
<tr>
<td>26</td>
<td>F3MAT (0HK PG G10.3,5*PC/PS G10.3,6H PSO G10.3,6H PSI LG G10.3,32H RKDCX REDUCED UNTIL ERROR .LE. G10.3)</td>
</tr>
<tr>
<td>27</td>
<td>SPC(I) = PC</td>
</tr>
</tbody>
</table>

**Note:** The code appears to be a segment of a larger program, possibly related to numerical or scientific computations, but the context is not provided in the image.
WRITE (6, 140)
140 FORMAT (BHK LAMBDA A 4X, 5HFR/EPALD 3X, 8HF/EPALD 4X, 7H/EPALD) 2X,
14X 3HPHI 4X 9HMCW2/PAUJ 7X 4HRKDX 5X 12HMPC5/2LE5MJ2 1X
2 11HHHRRL RATIO L1 12HVIS NR SIGMA 2X 8EPS(I) COEF)
FIRST = .TRUE.
CALL Hyst (0, G1J)
FIRST = .FALSE.
IF (LAMBDA.EQ.0.) SIG0 = .25
SW(I) = W
SPHI(I) = PHI
CALL Hyst (SIG1, G1I)
SIG = SIG1
IF (ABS(SIG1/3I0).LE.EPSW) GO TO 299
DS1 = SDS*SIGN (DS, 3I1)
SIG2 = SIG1
DO 150 J = 1, 20
SIG2 = SIG2 + DS1
CALL Hyst (SIG2, G12)
SIG = SIG2
IF (ABS(SIG2/3I0).LE.EPSW) GO TO 299
DS2 = SDS*SIGN (DS, 3I2)
IF (DS2 - DS1) 220, 210, 220
210 SIG1 = SIG2
150 G11 = G12
GO TO 299
220 DO 235 J = 1, 10
SIG = (G12*SIG1 - G1I*SIG2)/(G12 - G1I)
SD(I) = (G12 - G1I)/(SIG2 - SIG1)
CALL Hyst (SIG, GI)
IF (ABS(SIGI/G1I).LE.EPSW) GO TO 299
IF (ABS(SIG2/G1I).GT.ABS(SIGI)) GO TO 230
G11 = G12
SIG1 = SIG2
230 G12 = GI
235 SIG2 = SIG
299 SW3(I) = W3
ACM(I) = CMA
SCM(I) = CMC
SSSIG(I) = SIG
SPS(I) = CPS
300 CONTINUE
WRITE (6, 707)
IF (SGN.LT.0.) WRITE (6, 909)
IF (SGN.EQ.0.) WRITE (6, 390)
IF (SGN.GT.0.) WRITE (6, 808)
WRITE (6, 600) CL, LG, LT, DJ, K
600 FORMAT (1HL 8X, 3HLD/8X, 4HL/D 6X, 8FLAMBDA A 5X, 13H1*DELTA**2 3X,
1 7HCP/CV 4X, 9HORIF COEF 2X, 1OHREC.*VOL.*VC /5X, 5G12.3)
IF (.NOT. VARA) WRITE (6, 601) AO, VC
601 FORMAT (1H+ 64X 2G12.3)
IF (VARA) WRITE (6, 602) VC
602 FORMAT (1H+ 65X dMVARIABLE G15.3)
WRITE (6, 603) PS,BETA,ALFA,H,LG,RKEP
603 FORMAT (8X 5HPS/PA 7X 4HBE 8X 4HALFA 11X 1MH 13X 4HLG/L 8X
1 4HRKDEP/5X 7G12.3)
WRITE (6, 325) (SLAM(I), SW(I), SPHI(I), SW3(I), SISIG(I), ACM(I), SC4(I),
1 SPC(I), SD(I), SMJ(I), SD(I), SPS(I), I = 1, IS)
329  FORMAT (/1HL 3X,6IBKG NK 3X,8IBKG LOAD 2X,22HAFIT ANGLE 4HIRM  KAI
1DJ 2X,6W1B NR 3X,264StABILITY PARAMETERS 1DX 5HDF16(F1) 6X 4HMURW
2 4X THDORIFIGE 5X 3HPSO /
1 4X 6HHLAMBDA 4X 7HWP/EPALCJ 5X 34PHI 6X 8HWP/OMEGA 4X 5HSIGMA 4X
2 30HMCGW2/PALD MPC75/ZLR5MU2 PC/PA 4X 8HD(SIGMA) 3X 7HFLWU MUJ
3 2X 7HCGEF AO 5X 4HCGEF /
4 (/$3X 2010.3,611.3,512.3,3210.0,2312.3,69.2,511.3,610.3,F5.3))
GO TO 3
END

$IBFGC HYDST

SUBROUTINE HYST (SIGMA, GI)
CJMON /CF/ HLM,CP,E0,EA2,CC2,B,CH1,IC1A,IC2A,IC4W,IC5W,IC6A,IC5A,IC6W,
CJMON /CS/ LAMBDA,PSU,PS1,CMA,CMA,CMA,PHI,WR,REPD,W,IE,IL,L,PC,C4B,C4C
1 CS6B,CS6C,FRSTI,GIZ,PSU
CJMON /CTR/ CMA,IO,IO,IO,
REAL LAMBDA,L
COMPLEX AA,AB,BA,BA,CA,CA,CG,CG,CG
COMPLEX IC3A,IC4A,IC4W,IC5W,IC6A,IC5A,IC6W
LOGICAL FIRST
IF (FIRST,WR,SIGMA,NE0) GO TO 10
GI = GIZ
WR = 10000.
IF (LAMBDA,NE0) WR = 0.
CMA = 0.
CMA = 0.
RETURN
10 CPS = 1.
CG = PSI*PS1 + Q + (0,0,0)*SIGMA*PS1
PSU=0 MEANS ORIFICE MASS FLOW DOES NOT VARY WITH THETA
DX = 0.25
TOX = 0.
WR=LAMBDA - SIGMA
IC4W = (0,0,0)*(C4B*WR + C4C)
IC6W = (0,0,0)*(C6B*WR + C6C)
ICS6W = (0,0,0)*(CS5*WR
ICS6W = -ICS6W
DJ = 1.0 N = 1.8
BA = 0.
BB = (-1,-1,-1)
CALL RKLP (BA,DX,AA,CA)
CALL RKLP (BB,DX,AB,CB)
CA = -2.14159265*(AB*CA - AA*CB)/(AB - AA)
IF (CAB*(TOX/CA-1) > LE, RKEP) GO TO 12
DX = 0.5*DX

36
TDX = CA
RDX=DX
GR = REAL (CA)
GI = AIMAG (CA)
IF (FIRST) GIZ = GI
W = CABS(CA)
PH1 = ATAN2 (GI,GR)*57.2957796
WR = 1000.
CMC = 0.
IF (SIGMA .NE. 0.) CMC = 144.*GR/SIGMA**2
CMA = CMC*LAMBDA**2/30.
IF (LAMBDA .NE. 0.) WR = .5*SIGMA/LAMBDA
WRITE (6,145) LAMBDA,GR,GI,W,PH1,CMA,RDX,CMC,WR,SIGMA,CPS
145 FORMAT (3G11.3, 3I2.4,3I1.3,6I2.4,2G13.4,3G12.4)
RETURN
END

**IBFC FNC**

FUNCTION FMD (PC,PS,DM0)
COMMON /CFM/ PCK,K,SK1,SK2,VARA,AO
COMMON /CHK/CC,UC,C(2)
REAL K
LOGICAL VARA
DALPH (Y) = .06491 + (-2.*.76195 + 3.*.43415*Y)*Y
IF (PC .GT. PS) GO TO 20
PCS = PC/PS
AD = DALPH (PCS)
PM = -PS
GO TO 30
20 PCS = PS/PC
AD = -PCS*PCS*DALPH (PCS)
PM = PC
30 IF (PCS .GT. PCR) GO TO 40
FMD = PM*SK1
DMO = 0.
IF (PC .GT. PS) DMO = PS*SK1
IF (VARA) DMO = DMO + FMO*AD/AD
C(1) = CC
RETURN
40 PK = PCS**((L./K))
PSQ = SQRT (1.-PCS/PK)
FMO = PM*SK2*PK*PSQ
IF (PS .GT. PK) DMO = -PS*SK2*(PK/PCS-(K+1.)/2.)/PSQ/K
IF (PS .LT. PK) DMO = PS*SK2*(K-1.)/K*(PK-PCS/2.)/PSQ
IF (PS .EQ. PK) DMO = 1.E10
IF (VARA) DMO = DMO + FMO*AD/AD
C(1)=UC
RETURN
END
$IBFTC BD

BLOCK DATA
COMMON /LH/CC, UC, C(2)
DATA CC, UC, C(2) / LH, 44 HCHOKED /
END

$IBFTC RKLPS

SUBROUTINE RKLPS (G0, DX, AD, CD)
COMMON /Y4/ DP, UC, DS, DGP
COMMON /CHR/ CD, QD, D3, ZU
COMPLEX Y(5), A(5), B(5), G0, AD, CD, D3, XF, CDX
COMPLEX DG
EXTERNAL F2, F3, F4
Y(1) = 0.
Y(2) = 1.
Y(3) = 0.
Y(4) = G0
Y(5) = 0.
IF (ZG, EQ, 0.) GO TO 10
XF = ZG
CDX = ZG/AMAX0(1+X(1)), 1)
CALL RKGC (F2, Y, XF, CDX, A, B, 5)
Y(4) = DP/ Y(2) + QD + DG*Y(3) + DS*Y(4)
10 IF (ZG, EQ, ZG) GO TO 15
XF = ZG
CDX = (ZG-ZG)/AMAX0(1+X(1)), 1)
CALL RKGC (F3, Y, XF, CDX, A, B, 5)
Y(4) = Y(4) - QD - D3*Y(3)
15 IF (ZG, EQ, 5) GO TO 20
XF = .5
CDX = (1.5-ZG)/AMAX0(1+X(1)), 1)
CALL RKGC (F4, Y, XF, CDX, A, B, 5)
20 AD = Y(4)
CD = Y(5)
RETURN
END
$IBFTC FF

SUBROUTINE F1 (Y, YP)
COMMON /CFF/ HLM, CP, C2A, C2B, IC3A, IC4A, IC4W, IC54W, IC6A, IC6W, IC56W,
1 C5A, C7A, CD3, HLM2, C55
COMPLEX IC3A, IC4A, IC4W, IC54W, IC6A, IC6W, IC56W, Y(1), YP(1)
C SUBROUTINE F3R >>
YP(1) = 1.
YP(2) = CP- HLM/4/Y(2)
RETURN
ENTRY F2 (Y, YP)
C SUBROUTINE F3R G IN GROUVED REGION
YP(2) = CP - HLM4/Y(2)
YP(4) = -((C2A*YP(2)+C2B)/Y(2)+IC3A)*Y(4) - ((
1 IC4A*YP(2)+IC4W + 1-YP(2)+C6B!*YP(2)/Y(2))/Y(2) - C5A)*Y(3)
2 + IC6A*YP(2)+IC6W
GJ TO 10
ENTRY F3 (Y, YP)
C SUBROUTINE F3R G IN SMOOTH REGION
YP(2) = -HLM2/Y(2)
YP(4) = -C2A*YP(2)*Y(4)/Y(2) - ((IC54W - YP(2))*YP(2)
1 /Y(2))/Y(2) - C55)*Y(3) + IC56W
GU TO 10
ENTRY F4 (Y, YP)
C SUBROUTINE F3R G IN REGION INBOARD OF ORIFICES
YP(2) = 0.
YP(4) = IC55 - IC54W/Y(2))*Y(3) + IC56W
10 YP(1) = 1.
YP(3) = Y(4)
YP(5) = Y(3)
RETURN
END

$IBFTC KKGHC

SUBROUTINE KKGHC (DERIV, Y, XFINAL, DELTA, Q, YP, N)
C RUNGE-KUTTA-GILL INTEGRATION OF N-1 COMPLEX FUNCTIONS OF COMPLEX
C ARGUMENT Y(1) FROM Y(1) INITIAL TO XFINAL
DIMENSION A(4), B(4), C(4)
COMPLEX Y(1), Q(1), YP(1), XFINAL, DELTA, T
DATA A/5., 292893219, 1.7010578, .15656557, B/2., 1., 1., 2.,
1 C/5., 292893219, 1.7010578, .5/
KK = CABS((XFINAL-Y(1))/DELTA) + .01
IF (KK LE .0) GU TO 20
DO 5 I = 1, N
5 Q(I) = 0.
DO 10 K = 1, KK
DO 10 J = 1, 4
CALL DERIV(Y, YP)
DO 10 L=1,N
T=A(J)*(YP(L)-B(J)*Q(I))
10 Y(I)=Y(I)+DELTA*T
Q(I)=Q(I)+3.*T-C(J)*YP(1)
20 RETURN
END
REFERENCES


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