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Produced by the NASA Center for Aerospace Information (CASI)
AN EXPERIMENTAL STUDY OF THE
NOISE FIELD RESULTING FROM GROUND TESTING A
NUCLEAR ROCKET ENGINE

NERVA Program Contract SNP-1
NUCLEAR ROCKET OPERATIONS
December 1969

CLASSIFICATION CATEGORY

UNCLASSIFIED

WR Thompson 11/1/69
CLASSIFYING OFFICER DATE

AEROJET-GENERAL CORPORATION
A SUBSIDIARY OF THE GENERAL ELEMS & RUBBER COMPANY

SECRET

ELECTRONIC DATA SYSTEMS

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ABSTRACT

The experimental engine cold flow (EECF) tests were conducted in April 1968 in Engine Test Stand No. 1 (ETS-1) at the Nuclear Rocket Development Station (NRDS) in Nevada. Posttest inspection of ETS-1 showed evidence of damage that was caused by acoustic forces. Because the duct effluent from EECF tests had relatively low kinetic energy, it was apparent that the jet noise anticipated during later high-power engine tests could reach destructive levels.

To determine the magnitude and extent of the noise field resulting from ground tests of the rocket engine, Aerojet-General Corporation began a comprehensive investigation to identify the factors necessary to define the acoustics. The investigation was divided into four steps: (1) analytical predictions of the acoustic environment, (2) scale-model tests to clarify the empirical factors required for analysis, (3) improvement of the facility components as required, and (4) acoustic measurements of the sound pressures during power tests (up to and including the full-power test and comparison of measured data with predictions). This report describes the fourth step in detail and summarizes the entire investigation. The experimental information, theoretical results, and full-scale test data are expected to be of value to other investigators in the field of acoustics.

The ground-test facility for the nuclear rocket requires an engine test compartment (ETC) that will enclose the engine and a nuclear exhaust system (NES) to convey the heated hydrogen propellant (primary fluid) away from the engine and ETS-1. Typically, the ETC is purged with a small amount of nitrogen gas. Further purging and low mass back pressure are provided by introducing a large flow of high-temperature steam (secondary fluid) into the NES. The resulting mixture of gases burns along the surface of the plume at a rate that is controlled by the diffusion of ambient oxygen into the hydrogen-rich jet.

The results of 16 tests are reported. The gases used were principally hydrogen, steam, and nitrogen. Mixtures of these gases, at various velocities and temperatures, were expelled from the duct that terminated in a 45-degree elbow to give an upward direction to the gas jet. Four external sound-measuring microphones were used in the study; one was in the far field 400 ft from the source, and three were in the near field at critical points on the sheet metal portion of ETS-1. All acoustic data were processed for spectral evaluation. There is a low frequency contribution that appears to result from the combustion process. Jet conversion efficiency, limits of combustion, and frequency-spectra results are reported. Oscillatory combustion was considered possible, but no evidence of its occurrence was obtained. The spectral shape is similar to the jet-noise spectra for rockets and turbojet engines as reported in published literature.

The measured-sound pressure levels for the duct-vault inerting wall and the weather doors at ETS-1 agree quite well with the calculated values; the actual levels are about 1 db lower than those that were predicted. The tabulated results of the measurements, a sketch of the duct model and test stand, a photograph of the exhaust plume, schematics of the data-processing system, spectral-density profiles, and the relation of sound to mechanical power are included. Also included is a suggested method of analysis when a substantial combustion contribution is expected. Statistical analysis of the acoustic power shows that the variation in acoustic efficiency is reduced if a thermomechanical theoretical model is utilized rather than the conventional theoretical model of a noise-radiating jet.
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1. **INTRODUCTION**

Testing of the experimental cold flow engine (XECF) in ETS-1 resulted in slight damage to the corrugated aluminum sheet metal of the duct-vault inerting wall. Screws that hold the sheet metal to the frame had backed out in some places while in other locations the sheet metal had torn loose around the screws. This damage, though slight, occurred at sound pressure levels, flow rates, and gas temperatures that were substantially less than those anticipated for full-power engine testing. Various causes for the damage were suggested: jet noise, combustion overpressures, heat radiation, and static pressure differentials. A comprehensive investigation of the damaged area indicated that sound pressure waves generated by the duct effluent with the unsteady combustion of the duct effluent hydrogen during certain portions of the test were primarily responsible for the damage. A photograph of the wall was taken after this test series and is shown in Figure 1.

To determine the extent of the noise field resulting from the testing of a nuclear rocket engine, Aerojet-General Corporation in July 1968 began an extensive program to identify the factors necessary to define the acoustics by using scale-model experiments and taking acoustic measurements during tests of the nuclear rocket engine while it is operating at various reactor power levels. This report describes the results of the full-scale power tests, including the full-power run conducted in ETS-I on June 11, 1969. The results of the scale-model tests were previously described(1).²

During consultations with SNPO and a group experienced in acoustic problems (Paul S. Venniksen and Associates, LASL, and Marshall Space Flight Center) an approach was formulated to set the objectives for the investigation and these are:

²Numbers in parentheses refer to references
1. Define the acoustic field near the duct.
2. Identify problem areas in ETS-1 during partial-power runs.
3. Modify the theoretical model and state-of-the-art methods if necessary.
4. Identify and investigate evidence of oscillatory combustion.

A survey of related experience applicable to this problem was conducted. The acoustic field for a nuclear-rocket nozzle exhausting directly to the atmosphere (XIVI B) was studied by Manhart et al.\(^2\); in this case the high-temperature exhaust gases from the nozzle were directed vertically upwards with an exit velocity of 5000 to 20,000 ft/sec. The mass-flow rate (helium and hydrogen) varied from 35 to 85 lb/sec. However, the XES duct cools and dilutes the nozzle hydrogen with steam and discharges it to the atmosphere with a flow direction approximately 40° to the horizontal and with a velocity that varies from 200 to 6000 ft/sec. The two nuclear-exhaust systems are thus basically dissimilar.

Acoustic data on subsonic jets, with and without combustion, have been compiled by Lighthill\(^3\), and Washburn and Fenstermacher\(^4\). However, the jets involved were much smaller than the XES duct and combustion was either stable or non-existent. Hayes and Lamford\(^5\) and Overton\(^6\) compiled data on the noise produced by rocket engines firing at thrust levels from 1000 to 1,000,000 lb. Grande\(^7\) considered the effect of directivity on scaling hot and cold jets as well as the characteristics of the noise spectra and the total acoustic power. A comprehensive summary of directivity functions for subsonic jets (air and turbojet exhaust), as well as supersonic jets, was compiled by Howe\(^8\). Study of the cited and other available references, however, indicates a lack of information on the parameters that are important to the determination of the pressures on the test stand such as the effect of mixing steam and hydrogen, velocity distribution in the exit plane, and limits of combustion stability; further, data from different sources disagree by as much as 10 dB. The data obtained during this investigation are thus unique in a number of ways. These include the flow-jet angle, variations in the effluent-gas-mixture ratio, and the near-field environment.

As a result of the studies and analyses performed prior to power tests in ETS-1, a theoretical model was developed, acoustic and structural studies were completed, and a structurally improved wall was designed and installed. A photograph of this wall is shown in Figure 2.
II. DESCRIPTION OF TEST FACILITIES

A. DUCT

The NES duct at NRDS consists of a supersonic diffuser, 90° subsonic turning elbow, steam ejector, mixing section, and a 45° discharge elbow as shown in Figure 3. The stand is equipped with transducers to measure engine, steam-ejector, control, safety, and environmental parameters. Measurements of the gas and steam flow rates, pressures, and temperatures are performed at eight locations in the facility and four in the FTC. These measurements are necessary to identify the duct-exit gas conditions.

B. GAS SUPPLY

Hydrogen gas in the duct is provided by the engine at flow rates to 80 lb/sec. Steam (the ejector fluid) is provided from combustion of oxygen and propane further quenched with water. The term steam is used herein to conform to standard practice, but the fluid is not entirely steam, having a molecular weight of about 19 lb/lb mol. The upper temperature limit of hydrogen in the engine is 4100°F, and that of the steam generator products is 1660°F.

The engine and facility control consoles are located in a blockhouse adjacent to ETS-1. Flow rates and all other parameters are controlled through these consoles.

C. MICROPHONE SYSTEM, CALIBRATIONS AND TAPE RECORDERS

Four Kaman Nuclear Model KM1800-1 microphones were used in the study. Three, designated near field, were positioned at location numbers 113, 115, and 116 as shown in Figure 4. One, designated far field, was positioned
Figure 3 - NGS Duct

50' 10"

Figure 4 - Instrumentation Location, Acoustic Tests
at location number 114. All four contained identical transducers, which could measure static and dynamic pressures from 85 to 180 db at 0.0002 dynes/cm² at frequencies from 0 to 20,000 Hz. An isometric sketch of the facility is shown in Figure 5. Preamplifiers were provided because of the long cables required. All microphones were supported by rubber shock-absorbing mountings to insure isolation from the support. A typical microphone is shown in Figure 6.

The sound pressure signals were amplified on facility amplifiers and recorded on magnetic tape. A schematic of the data system is shown in Figure 7. The final data playback was performed after the test on a Bruel and Kjaer system for presentation either as overall or octave-band sound pressure or in terms of frequency-spectrum pressure levels.

The tape playback unit was a Honeywell 7600. The signal from the tape was processed on a Bruel and Kjaer 2000 Spectrometer, a true RMS Level Voltage Recorder was utilized for the overall sound pressure-level studies. For calibration, electrical and sound-wave signals were available. Electrical calibration was rejected as a primary calibration source for the microphones because of the inability to calibrate the most questionable component in the system, the microphone itself. A General Radio Sound Level Calibrator, Type 1562-A, was selected for the sound source as a calibration standard.

The decibel is a dimensionless unit used to express a logarithmic ratio between a measured quantity and a reference quantity. For example, sound pressure level (SPL) in decibels = 20 log (P₁/P₀) where P₁ = measured rms pressure in dynes/cm² and P₀ = reference pressure of 0.0002 dynes/cm². This is conveniently written as SPL, db at 0.0002 dynes/cm².
Figure 6 - Microphone and Adapter

Figure 7 - Schematic of the Acoustic Data-Reduction System
III. SCOPE OF DATA OBTAINED

A. EXPERIMENTAL PROCEDURE

The XE tests for which acoustic data were analyzed had the following objectives:

Test No. EP-2A - Transient-flow bootstrap tests
Test No. EP-3 - Steady-flow intermediate power
Test No. EP-5C - Steady-flow full power
Test No. EP-6A - Transient-flow start-up tests
Test No. EP-9A - Steady-flow high-Ip tests

The complete range of test variables is:

**Engine Gas**
- Species: Hydrogen
- Flow Rate, lb/sec: 0 to 80
- Temperature, °R: to 4100°R

**Ejector Gas**
- Species: Mostly steam
- Flow Rate, lb/sec: 120 to 160
- Temperature, °R: 540 to 1600

**Duct Geometry**
- Exit diameter, ft: 4.33
- Exit Angle, degrees: 45

A more complete listing of the tests conducted and the flow conditions is given in Table 1.

<table>
<thead>
<tr>
<th>Date</th>
<th>Test</th>
<th>Time sec</th>
<th>Engine Temp, °F</th>
<th>Gas Temp, °F</th>
<th>Steam Temp, °F</th>
<th>Flow, LFM</th>
<th>Steam Flow, LFM</th>
<th>Diluent Cases</th>
</tr>
</thead>
<tbody>
<tr>
<td>3/20</td>
<td>2A</td>
<td>29270</td>
<td>500</td>
<td>0</td>
<td>1100</td>
<td>3</td>
<td>1138</td>
<td>N2</td>
</tr>
<tr>
<td>3/20</td>
<td>2A</td>
<td>49350</td>
<td>500</td>
<td>0</td>
<td>1150</td>
<td>3</td>
<td>1137</td>
<td>N2</td>
</tr>
<tr>
<td>3/20</td>
<td>2A</td>
<td>49450</td>
<td>1280</td>
<td>16</td>
<td>1200</td>
<td>3</td>
<td>1200</td>
<td>N2</td>
</tr>
<tr>
<td>3/21</td>
<td>2A</td>
<td>69478</td>
<td>1350</td>
<td>21</td>
<td>1200</td>
<td>3</td>
<td>1200</td>
<td>N2</td>
</tr>
<tr>
<td>4/16</td>
<td>3</td>
<td>54625</td>
<td>530</td>
<td>1</td>
<td>1130</td>
<td>3</td>
<td>134</td>
<td>N2</td>
</tr>
<tr>
<td>4/16</td>
<td>3</td>
<td>54900</td>
<td>3050</td>
<td>38</td>
<td>1360</td>
<td>3</td>
<td>134</td>
<td>N2</td>
</tr>
<tr>
<td>4/16</td>
<td>3</td>
<td>54990</td>
<td>2350</td>
<td>33</td>
<td>1360</td>
<td>3</td>
<td>134</td>
<td>N2</td>
</tr>
<tr>
<td>5/16</td>
<td>3</td>
<td>55250</td>
<td>1050</td>
<td>2</td>
<td>1390</td>
<td>3</td>
<td>133</td>
<td>N2</td>
</tr>
<tr>
<td>6/11</td>
<td>5C</td>
<td>38500</td>
<td>540</td>
<td>3</td>
<td>1350</td>
<td>3</td>
<td>139</td>
<td>N2</td>
</tr>
<tr>
<td>6/11</td>
<td>5C</td>
<td>38800</td>
<td>2380</td>
<td>44</td>
<td>1360</td>
<td>3</td>
<td>140</td>
<td>N2</td>
</tr>
<tr>
<td>6/11</td>
<td>5C</td>
<td>38930</td>
<td>4100</td>
<td>71</td>
<td>1360</td>
<td>3</td>
<td>142</td>
<td>N2</td>
</tr>
<tr>
<td>6/11</td>
<td>5C</td>
<td>39200</td>
<td>1960</td>
<td>29</td>
<td>1340</td>
<td>3</td>
<td>142</td>
<td>N2</td>
</tr>
<tr>
<td>7/10</td>
<td>6A</td>
<td>44320</td>
<td>500</td>
<td>0</td>
<td>1280</td>
<td>2</td>
<td>153</td>
<td>N2</td>
</tr>
<tr>
<td>7/10</td>
<td>6A</td>
<td>44520</td>
<td>1700</td>
<td>24</td>
<td>1290</td>
<td>2</td>
<td>158</td>
<td>N2</td>
</tr>
<tr>
<td>8/28</td>
<td>9</td>
<td>59200</td>
<td>206</td>
<td>0</td>
<td>1350</td>
<td>3</td>
<td>132</td>
<td>N2</td>
</tr>
<tr>
<td>8/28</td>
<td>9</td>
<td>59810</td>
<td>3990</td>
<td>38</td>
<td>1370</td>
<td>3</td>
<td>135</td>
<td>N2</td>
</tr>
</tbody>
</table>
Prior to tests, the microphones were returned to the factory for
a complete re-calibration from 0 to 10,000 Hz and 60 to 180 db frequency range
and sound pressure level. Prior to each test, the test-operation procedure
required a pretest calibration from 100 to 160 db at 1000 Hz for each microphone.
However, lateness of the hour or equipment demands sometimes forced deviations
from this procedure. Calibration history is presented in Table 2. This
procedure was restricted to the sound-pressure measurements as other instruments
are inherently more reliable and are calibrated by facility personnel on a
periodic basis. Because the validity of the test results is limited not only
by the microphones, but also to their associated amplifiers, pre-amplifiers, tape
recorders, and cable, special attention was directed to the secondary components.
The overall response of the system was determined by experiment to be quite flat
from 1 to 20K Hz for all microphones. The data shown in Table 3, indicates that
the microphones limit the system response.

B. METHOD OF CALCULATION OF FLOW PARAMETERS

The results of the tests and the conclusions drawn are based on
the gas flow conditions at the duct exit and the resulting sound pressure levels;
however, only the sound pressure levels were directly measured. The other
quantities are calculated from measured pressures, temperatures, etc. To
enable other investigators to make use of the data independently at some later
date, a summary of the method of calculation of the gas-mass flow rate, jet-
mechanical power, and gas-effluent exit velocity is described fully in Appendix
A(1). A summary of duct exit conditions so calculated is presented in Table 4.

C. METHOD OF CALCULATION OF ACOUSTIC EFFICIENCIES

Sound pressure levels were measured using microphones, and jet
powers were calculated as given by the formulas in Appendix B(1). The expression
for the mechanical-to-total acoustic power conversion efficiency was
obtained from the measured-sound pressure level*, the calculated jet mechanical

*Both far and near field values were utilized in the calculation of acoustic
power and acoustic efficiencies.
TABLE 4
Duct Exit Flow Parameters for XE Tests

<table>
<thead>
<tr>
<th>Parameter</th>
<th>XE HA</th>
<th>XE HB</th>
<th>XE HC</th>
<th>XE HD</th>
<th>XE HE</th>
<th>XE HF</th>
<th>XE HG</th>
<th>XE HH</th>
</tr>
</thead>
<tbody>
<tr>
<td>Duct Exit Flow</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Time, sec</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Free Stream, gpm</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Temperature, °C</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Flow Rate, gpm</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Velocity, %</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Mass Flow, lb/min</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

*Indicates values of engine and turbine tests and point for XE test, where specified.

From Microphone to Spectral Response

Sensitivity, microv. per sec

Frequency Response

Decibels

<table>
<thead>
<tr>
<th>Frequency, Hz</th>
<th>0</th>
<th>10</th>
<th>20</th>
<th>30</th>
<th>40</th>
<th>50</th>
<th>60</th>
<th>70</th>
</tr>
</thead>
<tbody>
<tr>
<td>Response, dB</td>
<td>0</td>
<td>10</td>
<td>20</td>
<td>30</td>
<td>40</td>
<td>50</td>
<td>60</td>
<td>70</td>
</tr>
</tbody>
</table>

*Indicates values of engine and turbine tests and point for XE test, where specified.
Another ideal model of the acoustic process, the thermal-mechanical model, is applicable only to burning jets. This visualizes all acoustic power as emanating from two component power terms and is calculable as the sum of each taken separately. These component terms are each assumed proportional to the jet mechanical power and the jet thermal power. By this model,

\[ OAPW = \eta_{TH} \times W_{JET} + \eta_{M} \times W_{JET} \]  

Equations (1) and (2) are combined to show the relationship between the three efficiencies.

\[ \eta = \eta_{TH} \times W_{JET}/W_{JET} + \eta_{M} \]  

Equation (3) shows that if the jet power terms or their ratio and the thermal efficiency are constant, a change in the mechanical-to-acoustic power conversion efficiency produces a corresponding change in the total acoustic power conversion efficiency.

3. Discussion

Equation (1) is obtained from the application of acoustic principles to the first model described and equation (2) similarly is obtained from the second model. From a scientific viewpoint the second model appears to offer the best approach, that is, the two component efficiencies should be closer to constant values for a given change in gas mixture ratio than is the total acoustic efficiency.

D. ACOUSTIC SPECTRAL DISTRIBUTION \( \Phi \)

For each test, one reel of tape was used to record all pre and post calibrations as well as the data signals. Calibration provided a means of determining the amplitude and frequency response of each data-analysis
channel. Comparison of the pre and post calibration signal gave assurance that the sensitivity of each channel did not change during the test.

Overall acoustic efficiency was determined as described above, assuming a value for the directivity index. Figure 4 shows that not enough microphones were available to reliably determine sound power levels without prior knowledge of directivity index. Spectral distribution was determined from octave-band plots using the Bruel and Kjaer Graphic Level Recorder Type 2305.

E. EXHAUST VELOCITY

The exhaust velocity was calculated from an approximate one-dimensional model using the area normal to the duct centerline as the flow area and assuming the duct effluent to be perfectly mixed at the exit plane. Mixing is an important consideration as the duct downstream of the steam-ejector nozzles consisted of a straight mixing section only 5 diameters in length, followed by a 45-degree elbow. The jet direction was always assumed to be 38 degrees with the horizontal. This angle was determined from photographs of the plume from many previous model tests, taken when the exit Mach number was near unity. The actual situation is probably more complicated than this approximate model; the exit velocity profile is skewed and the flow area is reduced by the rotation in the elbow.

IV. EXPERIMENTAL PROCEDURE

Gaseous hydrogen, steam, and miscellaneous other gases in trace amounts over a wide range of mixtures were expelled at large kinetic energies. Because of the difficulty of obtaining exactly the predicted exit velocity for any given test, i.e., the gas flow and temperature could not be regulated exactly, the microphone system ranges were selected for each test on the basis of both experience and theoretical calculations.

The KE tests were conducted both at night and during the day. If the test could not be completed during daylight it was completed during the night. Motion pictures and still photographs were taken. Figure 8 shows a photograph of the exhaust plume at a time when the plume composition was 100% steam. For convenience the arrowhead shown in the photograph is about 10C ft away from ETS-1.

The method of determining the mechanical/thermal-to-acoustic power conversion efficiencies for burning jets used in this investigation was to consider the sound pressure spectrum as composed of a typical nonburning gas jet component plus an additional contribution in the lower frequencies caused by combustion. Because the portion ascribed to jet noise and the mechanical power was known, the mechanical-to-acoustic power conversion efficiency was determined for a number of tests and then averaged. This average was then assumed fixed for all tests, and equation (2) was solved to obtain the thermal-to-acoustic power conversion efficiency.

The test data could also be utilized to obtain new correlations for both acoustic efficiency and directivity index. This investigation would, however, involve time consuming trial-and-error cross-correlation studies because of the limited number of microphones and the sensitivity of the result to an assumed directivity index.
A. MICROPHONE LOCATIONS

The locations of the microphones are summarized below:

<table>
<thead>
<tr>
<th>Microphone Number</th>
<th>Location*</th>
<th>Coordinates</th>
<th>Distance**</th>
<th>Angle***</th>
</tr>
</thead>
<tbody>
<tr>
<td>113</td>
<td>N</td>
<td>X ft: 0</td>
<td>Y ft: 25.5</td>
<td>Z ft: 23.1</td>
</tr>
<tr>
<td>114</td>
<td>F</td>
<td>X ft: 283</td>
<td>Y ft: 60.5</td>
<td>Z ft: 306.3</td>
</tr>
<tr>
<td>115</td>
<td>N</td>
<td>X ft: -23.3</td>
<td>Y ft: 0</td>
<td>Z ft: 115.7</td>
</tr>
<tr>
<td>116</td>
<td>N</td>
<td>X ft: 13.5</td>
<td>Y ft: 6.1</td>
<td>Z ft: 32.2</td>
</tr>
</tbody>
</table>

* N denotes near field, F denotes far field.
** Measured from the microphone to the calculated center of sound.
*** Center of sound location estimated for duct-exit conditions of Test 5C, Table 1, CRT 38930 sec.
**** Measured from the forward end of a fictitious rocket having the same exhaust-jet direction.

A complete derivation of the equations and a list of the assumptions is included in Appendix B(1).

B. CONTRIBUTION OF HYDROGEN COMBUSTION TO THE SOUND PRESSURE

Tests with steam only, and with steam and varying quantities of hot or cold hydrogen were conducted to permit an indirect calculation of the contributions of hydrogen combustion to the overall noise. The conclusions of previous investigations have varied on the significance of this contribution; this is caused by the fact that all the important parameters for burning noise are not measured or calculated in a typical rocket firing. It would be expected that the Froude number, the heat of combustion of the fuel,
extent of dilution with non-combustibles (i.e., the mol fraction of inert gases), and the duct-exit Mach number are the important parameters.

The combustion contribution was determined by extrapolation of non-burning sound pressure levels from these and other relevant tests and comparison with sound pressure levels when there was combustion at the same mechanical power levels. Figure 8 illustrates the relative scale of the plume and duct size. This photograph was taken several years ago of a steam-only jet to study the duct performance. The June meteorological data for the run days are included in Table 5.

Prior to testing, the sound recording equipment was calibrated as described whereas the gas flow, pressure and temperature measuring equipment were calibrated with a series of electrical calibrations at 20, 40, 60, and 80 percent of full scale. Cameras were operated for a few seconds to determine if the film transport mechanisms were operating as required. Following each test all calibrations were repeated, if time permitted.

Each test was initiated by a pre-operational phase during which data systems, communications, valves, emergency systems, etc., were checked. The steam generators were then started and the engine tests followed. The NES was then shutdown and emergency systems secured. Calibration of the data system followed each test. Instrument ranges are presented in Table 5.
TABLE 5 (continued)
Local Climatological Data

<table>
<thead>
<tr>
<th>OBSERVATIONS AT 12-HOUR INTERVALS</th>
</tr>
</thead>
<tbody>
<tr>
<td>Date</td>
</tr>
<tr>
<td>------</td>
</tr>
<tr>
<td></td>
</tr>
</tbody>
</table>

V. RESULTS OF DATA ANALYSIS

The recorded data were of necessity not in final form. For example, gas pressure was recorded on magnetic tapes and oscillographs as percent of full scale, and sound pressure was recorded on magnetic tape. These raw data were reduced to meaningful engineering units after each test. The following parameters were calculated: gas flow rate, molecular weight, temperature, velocity and Mach number, sound pressure and frequency, and heat radiation from the plume, by using the methods described in Appendices of Reference (1).

A. FLOW PARAMETERS

The flow parameters that were determined for each test, or at selected times during a given test when the test involved a flow ramp, are given above (see also Tables 1 and 4).

B. ACOUSTIC EFFICIENCY

One generally accepted method of predicting sound pressure levels for jets is to determine the jet mechanical power, estimate the acoustic power-conversion efficiency, and then calculate the sound pressure level. This method is successful because the efficiency changes less than any of the other jet parameters. The theoretical model that is the basis for this method is designated herein as the mechanical model. It has the disadvantage in that it ignores the contribution of burning to the noise. Another method, which is more complex, is to determine the jet mechanical and thermal power, estimate the mechanical and thermal power-conversion efficiency and then calculate the sound pressure level. The corresponding designation is "Thermal mechanical model."

The data obtained in these tests have been evaluated by calculating the jet mechanical power, overall acoustic power level, acoustic power-conversion efficiency, jet thermal power, and mechanical and thermal
power-conversion efficiencies. The results of this analysis are listed below. All test times were selected from runs when the flow of hydrogen gas was significant, i.e., the plane shape and velocity were momentum rather than buoyancy controlled.

The acoustic conversion efficiencies were calculated from the measured sound pressure levels for all scale-model and XE tests. The results of the analysis for typical cases of both test series are shown below:

### ACoustic Conversion Efficiencies, Selected Scale-Model Tests

<table>
<thead>
<tr>
<th>Test No.</th>
<th>A2</th>
<th>A2</th>
<th>A5</th>
<th>A5</th>
<th>A6</th>
<th>A6</th>
<th>A11</th>
<th>A11</th>
</tr>
</thead>
<tbody>
<tr>
<td>MicropHONE(s)</td>
<td>5</td>
<td>11</td>
<td>5</td>
<td>11</td>
<td>11</td>
<td>11</td>
<td>11</td>
<td>11</td>
</tr>
<tr>
<td>Time, sec</td>
<td>10</td>
<td>10</td>
<td>9</td>
<td>9</td>
<td>67</td>
<td>92</td>
<td>92</td>
<td>108</td>
</tr>
<tr>
<td>Sound, megawatts</td>
<td>2.03</td>
<td>2.03</td>
<td>2.79</td>
<td>2.79</td>
<td>1.204</td>
<td>1.204</td>
<td>0.660</td>
<td>0.207</td>
</tr>
<tr>
<td>OAP, kilowatts</td>
<td>8.12</td>
<td>11.17</td>
<td>10.32</td>
<td>9.49</td>
<td>4.70</td>
<td>5.56</td>
<td>2.94</td>
<td>0.869</td>
</tr>
<tr>
<td>OAP, db re 10^(-13) watt</td>
<td>150.3</td>
<td>170.2</td>
<td>197.2</td>
<td>197.7</td>
<td>166.6</td>
<td>167.4</td>
<td>167.4</td>
<td>169.4</td>
</tr>
<tr>
<td>n</td>
<td>0.40</td>
<td>0.58</td>
<td>0.37</td>
<td>0.37</td>
<td>0.39</td>
<td>0.46</td>
<td>0.46</td>
<td>0.42</td>
</tr>
<tr>
<td>nM, %</td>
<td>0.20</td>
<td>0.20</td>
<td>0.20</td>
<td>0.20</td>
<td>0.20</td>
<td>0.20</td>
<td>0.20</td>
<td>0.20</td>
</tr>
<tr>
<td>nTH, %</td>
<td>.0023</td>
<td>.0027</td>
<td>.0022</td>
<td>.0017</td>
<td>.0013</td>
<td>.0024</td>
<td>.0013</td>
<td>.0013</td>
</tr>
</tbody>
</table>

The average value of \( n \) for all scale-model tests is 0.43% with a standard deviation of 0.076%. Similarly, the average value of \( nH \) and its standard deviation are 0.0023 and 0.00099%, respectively. A constant value of 0.20% for \( nM \) was assumed for all scale-model tests based on the data of Manhars(2).

### ACoustic Conversion Efficiencies, Selected Engine Tests (XE)

<table>
<thead>
<tr>
<th>Test No.</th>
<th>1</th>
<th>3</th>
<th>5C</th>
<th>5C</th>
<th>5C</th>
<th>6A</th>
</tr>
</thead>
<tbody>
<tr>
<td>Time, sec</td>
<td>54625</td>
<td>54900</td>
<td>38000</td>
<td>38930</td>
<td>39200</td>
<td>44320</td>
</tr>
<tr>
<td>Sound, megawatts</td>
<td>0.714</td>
<td>16.8</td>
<td>30.3</td>
<td>191</td>
<td>10.3</td>
<td>0.843</td>
</tr>
<tr>
<td>OAP, kilowatts</td>
<td>6.03</td>
<td>111.5</td>
<td>201</td>
<td>1077</td>
<td>105.9</td>
<td>5.37</td>
</tr>
<tr>
<td>OAP, db re 10^(-13) watt</td>
<td>167.8</td>
<td>180.4</td>
<td>183.0</td>
<td>190.3</td>
<td>180.2</td>
<td>167.3</td>
</tr>
<tr>
<td>n, %</td>
<td>0.844</td>
<td>0.66</td>
<td>0.66</td>
<td>0.56</td>
<td>0.99</td>
<td>0.64</td>
</tr>
<tr>
<td>nM, %</td>
<td>0.18</td>
<td>0.33</td>
<td>0.42</td>
<td>0.50</td>
<td>0.55</td>
<td>0.38</td>
</tr>
<tr>
<td>nTH, %</td>
<td>0.0023</td>
<td>0.0023</td>
<td>0.0023</td>
<td>0.0023</td>
<td>0.0023</td>
<td>0.0023</td>
</tr>
</tbody>
</table>

For all tests, the average values of \( n \) and \( nM \) are 0.73 and 0.32%, respectively, with standard deviations of 0.254 and 0.181%. The heating value of hydrogen was taken as 60,000 Btu/lb.

1. **Comparison of Acoustic Models**

Two theoretical models have been described and the corresponding results of the data analysis presented. The results are summarized below:

### COMPARISON OF ACOUSTIC MODELS

<table>
<thead>
<tr>
<th>Test Series</th>
<th>Engine series (XE)</th>
<th>n, %</th>
<th>nH, %</th>
<th>nTH, %</th>
<th>nM, %</th>
</tr>
</thead>
<tbody>
<tr>
<td>Scale Model (1)</td>
<td>Steam + CH_2</td>
<td>0.73</td>
<td>0.0023</td>
<td>0.32</td>
<td></td>
</tr>
<tr>
<td>Scale Model (1)</td>
<td>CH_4</td>
<td>0.43</td>
<td>0.0023</td>
<td>0.20</td>
<td></td>
</tr>
<tr>
<td>Scale Model (1)</td>
<td>CH_3</td>
<td>0.50</td>
<td>-------</td>
<td>-------</td>
<td></td>
</tr>
</tbody>
</table>

The calculated standard deviations from experiments for the mechanical and thermal-mechanical models are 0.254 and 0.181%, respectively. This indicates that the acoustic prediction should be improved if the second theoretical model is used, i.e., the contribution of the burning hydrogen to the noise is considered as an additive term to the mechanical contribution.
Evaluation of the test results also indicates that for a duct using hydrogen gas mixtures, a thermal-to-acoustic power conversion efficiency of 0.00232, as calculated by Ortega(10), would appear to be a valid number. The calculated mechanical-to-total acoustic power-conversion efficiency is in substantial agreement with the results of other investigations such as that done by Manhart(1). 

C. OVERALL SOUND PRESSURE LEVEL

The most important information obtained from this or any similar test series is the overall sound pressure level (OASPL) because the structural integrity of the inserting wall is influenced by this parameter. Because jet noise is broadband in character, it is not necessary to analyze the noise in any great detail; overall sound pressure levels and octave-band analysis, described later, are adequate. The overall sound pressure levels were determined by tape playback on a Bruel and Kjaer analyzer. Pretest and posttest calibrations were utilized to range the analyzer and to assure that calibration did not change during the test. Figure 9 shows typical overall sound pressure levels prior to full-power test X. Note that the duration of the test is important as the jet takes a finite time to reach steady-state.

Figure 10 shows the overall sound pressure levels at microphone 113 during full-power test S. The evaluation of differences in noise levels requires consideration of related performance parameters such as mechanical power, nozzle diameter, mass flow, velocity, density, directivity, and combustion level. Figures 11, 12, and 13 show similar data for microphones 114, 115, and 116.

Sound pressure levels were determined for each microphone 16 times during the tests. The results of this study are presented in Table 6. The ranges of all the instruments were limited so a procedure was utilized to prepare for each test; rough-order-of-magnitude sound pressure levels were predicted and the results used for rangiing the instruments.

Figure 9 - Overall sound Pressure Level, Microphone 116

31
Figure 10 - Sound Spectra for Microphone 113

Figure 11 - Sound Spectra for Microphone 114
Figure 12 - Sound Spectra for Microphone 115

Figure 13 - Sound Spectra for Microphone 116
TABLE 6
SOUND PRESSURE LEVELS
(dB re .0002 dynes/cm²)

<table>
<thead>
<tr>
<th>Test No.</th>
<th>Time sec.</th>
<th>Microphone Number</th>
<th>HN</th>
<th>113</th>
<th>114</th>
<th>115</th>
<th>116</th>
</tr>
</thead>
<tbody>
<tr>
<td>2A</td>
<td>49270</td>
<td></td>
<td></td>
<td>134.5</td>
<td>112.5</td>
<td>114.4</td>
<td>125.5</td>
</tr>
<tr>
<td>2A</td>
<td>49350</td>
<td></td>
<td></td>
<td>134.5</td>
<td>112.5</td>
<td>114.5</td>
<td>125.7</td>
</tr>
<tr>
<td>2A</td>
<td>49450</td>
<td></td>
<td></td>
<td>140.0</td>
<td>118.5</td>
<td>121.5</td>
<td>139.5</td>
</tr>
<tr>
<td>2A</td>
<td>49470</td>
<td></td>
<td></td>
<td>142.0</td>
<td>121.0</td>
<td>120.0</td>
<td>144.0</td>
</tr>
<tr>
<td>3</td>
<td>34625</td>
<td></td>
<td></td>
<td>132.0</td>
<td>109.5</td>
<td>*</td>
<td>136.5</td>
</tr>
<tr>
<td>3</td>
<td>54900</td>
<td></td>
<td></td>
<td>151.5</td>
<td>123.0</td>
<td>*</td>
<td>149.6</td>
</tr>
<tr>
<td>3</td>
<td>54990</td>
<td></td>
<td></td>
<td>147.0</td>
<td>118.5</td>
<td>*</td>
<td>144.6</td>
</tr>
<tr>
<td>3</td>
<td>55250</td>
<td></td>
<td></td>
<td>140.5</td>
<td>112.5</td>
<td>*</td>
<td>148.0</td>
</tr>
<tr>
<td>5C</td>
<td>38500</td>
<td></td>
<td></td>
<td>137.0</td>
<td>112.0</td>
<td>116.0</td>
<td>138.0</td>
</tr>
<tr>
<td>5C</td>
<td>38800</td>
<td></td>
<td></td>
<td>150.5</td>
<td>125.0</td>
<td>131.0</td>
<td>148.5</td>
</tr>
<tr>
<td>5C</td>
<td>38930</td>
<td></td>
<td></td>
<td>158.0</td>
<td>132.4</td>
<td>142.0</td>
<td>156.2</td>
</tr>
<tr>
<td>5C</td>
<td>39200</td>
<td></td>
<td></td>
<td>146.5</td>
<td>*</td>
<td>*</td>
<td>144.5</td>
</tr>
<tr>
<td>5C</td>
<td>44320</td>
<td></td>
<td></td>
<td>132.5</td>
<td>108.5</td>
<td>*</td>
<td>135.0</td>
</tr>
<tr>
<td>6A</td>
<td>44520</td>
<td></td>
<td></td>
<td>142.5</td>
<td>116.5</td>
<td>*</td>
<td>140.5</td>
</tr>
<tr>
<td>9</td>
<td>59200</td>
<td></td>
<td></td>
<td>134.5</td>
<td>112.0</td>
<td>114.0</td>
<td>135.0</td>
</tr>
<tr>
<td>9</td>
<td>39810</td>
<td></td>
<td></td>
<td>148.0</td>
<td>126.5</td>
<td>126.5</td>
<td>148.5</td>
</tr>
</tbody>
</table>

*Electrical failure

D. SPECTRAL DATA

Sound spectra are important characteristics of this or any noise source. For example, in structural analysis of the subject wall, the wall as an entity will have a resonant frequency, the wall frame will probably have a different resonant frequency, and each panel will have its own resonant frequency that may be different than that of adjacent panels. A given amount of energy at low, midrange, and high frequencies will have markedly different effects in terms of exciting the structure. The data process for obtaining spectra is described below.

All acoustic tapes were processed through the Bruel and Kjaer Graphic Level Indicator to obtain OASPL (Octave-Band Sound Pressure Levels). The bands chosen for analysis were 12.5, 25, 50, 100, 200, 400, 800, 1600, 3150, 6300, and 12,500 Hz*. This narrow-band analysis was done by using Bruel and Kjaer octave-band filters that have a relatively sharp cutoff, 13 dB per 1/3 octave. The results of the study for typical test conditions are shown in Figures 10 through 13. Note that there is a peak from about 100 to 400 Hz band. This pattern is typical of jet noise from rockets and large turbojet engines.

Experience gained from the scale-model tests showed that when the jet had a large thermal-energy content (amount of burning hydrogen) there were peaks at about 100 and 1600 Hz. It was suggested that the bi-modal spectra was caused by a large energy noise contribution at 1600 Hz by jet turbulence.

*Because the contribution of the last two bands was insignificant, these were later eliminated from the study.
and another at 100 Hz by combustion. However, it appears that there is no such bi-modal shape to the spectra here. The explanation suggested is that the combustion noise spectra is not sensitive to jet diameter but that the turbulence noise is. The turbulence energy is now in the 100 to 400 Hz band, and so the spectra show only a typical broadband noise resulting from both noise energy sources acting simultaneously.

Four large propane igniters were provided at the end of the NEP duct to flare the hydrogen. All of the hydrogen plumes burned vigorously.

Figures 14 through 18 show the measured octave-band pressure levels for tests 2A, 3, 5C, 6A, and 9. Note the broadband nature of the noise. The average sound pressure level over the range of frequencies of interest is only slightly less than the maximum.

The octave-band sound pressure spectra for air jet indicate about 9 dB/octave roll-off below the frequency at which the sound-pressure peaks and about 4 dB/octave above this frequency, whereas for chemical rocket jets the equivalent values are about 4 and 2 dB respectively. Air-jet and helium-jet spectra are similar to the right-hand half of the hydrogen-jet spectra. Examination of the noise spectra from these tests shows a roll-off of about 5 and 2.5 dB/octave respectively. This agrees with data for chemical rockets.

E. NEAR AND FAR FIELD LIMITS

A preliminary estimate was made of the acoustic spectrum to determine the limits of the acoustic near and far fields for the jet tests. It was determined that a distance of 200 ft would be sufficient to locate the microphones within the far field. Therefore, the far-field microphone was located more than 300 ft away from the sound center to ensure that far-field results would be obtained. Microphones 113, 115, and 116 were intended to obtain specific design data in the near field and were located near the jet source on the critical components of the stand.
Figure 15 - Octave-Band Pressure Level, Test EP-3

Figure 16 - Octave-Band Pressure Level, Test EP-5C
Figure 17 - Octave-Band Pressure Level, Test EP-6A

Figure 18 - Octave-Band Pressure Level, Test EP-9
F. PROBABLE ACCURACY

The SPL (Sound Pressure Levels) and PWL (Sound Power Levels) presented in this report are subject to the following errors: electrical, visual, calibration, atmospheric, data reduction, and data processing. These are estimated to be as follows:

- Electrical noise: ± 0.2 db
- Visual reading: ± 1.0 db
- Data processing: ± 0.5 db
- Acoustical calibration: ± 0.1 db
- Round-off error: ± 0.5 db

The probable error is therefore,

\[ \pm \sqrt{0.04 + 1.0 + 0.25 + 0.01 + 0.25} \]
\[ = \pm \sqrt{1.55} \]
\[ = \pm 1.25 \text{ db} \]

This figure is accurate above 0.1 Hz; below that the response of the microphones falls off rapidly.

G. COMPARISON WITH THE NOISE FIELDS OF OTHER JETS

The noise fields of other jets have been extensively studied. Because of the relatively large size of the duct exit and the high velocity, most of the relevant data is limited to rocket jets. Figure 19 shows the relationships between sound power and mechanical power for this and similar studies. The data shown for nuclear rockets are taken from Manhart(10), data for chemical rockets are taken from Cole(12) and others as noted.

The eighth power law of Lighthill(13), which gives such a good correlation for small, subsonic, cold-air jets, does not appear applicable for
large jets with high-velocity gases. The number of important parameters is probably much greater than those of a cold-air jet; gases of radically different molecular weight are mixing, the acoustic velocity in the jet is not the same as in the atmosphere, and the gas does not follow the 45 degree turn of the pipe elbow at the exit but turns only a fraction of that amount, to name only a few effects.

The mechanical power level of the jet when the engine is operating at design is about 400 times that at zero power. Because steam is flowing, regardless of the engine power, at about 130 lb/sec, the ratio is not infinite. The difference in efficiency was only 26%. This indicates a nearly constant efficiency in conversion of mechanical power to sound power over a wide range of output power. This trend was demonstrated to extend over a range of jet mechanical power from $10^3$ to $10^5$ watts. Other investigators have confirmed this trend.

VI. COMBUSTION STUDIES

The noise that is emitted by a flame is well known to anyone who has witnessed a large forest or petroleum fire. However, the chemical compositions that will sustain combustion must be uniquely determined for each new situation. Additional noise can be expected when oscillatory combustion is present as in the familiar singing flame phenomenon. Available literature was evaluated for application to combustion studies. It appears that the field of combustion noise from flames is large and growing; essentially all of this work, however, is devoted to combustion chambers in some form and is not germane to the free, turbulent, diffusion flames typical of the experiments in this program. In view of the lack of applicable literature, combustion studies were made an important part of this investigation.

Test data were obtained with hydrogen-in-duct effluent ranging from 5 to 8/ mol percent. One useful side result of the test series is that predictions regarding the dynamic lower flammability limit of about 22 mol percent were confirmed.

A. CONTRIBUTION OF BURNING TO NOISE

The overall acoustic conversion efficiencies of the earlier scale-model tests were calculated by using the equations presented earlier. Typical results are shown below:

ACOUSTIC CONVERSION EFFICIENCY, GAS JETS WITH NO BURNING
(Nitrogen Gas with a Small Amount of Hydrogen Gas)

<table>
<thead>
<tr>
<th>Test No.</th>
<th>A10</th>
<th>A11</th>
<th>A12</th>
<th>A14</th>
<th>A16</th>
</tr>
</thead>
<tbody>
<tr>
<td>Time, sec</td>
<td>32</td>
<td>8</td>
<td>18</td>
<td>12</td>
<td>30</td>
</tr>
<tr>
<td>Average Acoustic Conversion Efficiency</td>
<td>0.39</td>
<td>0.36</td>
<td>0.31</td>
<td>0.33</td>
<td>0.46</td>
</tr>
<tr>
<td>Duct Gas Temperature °R</td>
<td>1347</td>
<td>1065</td>
<td>1066</td>
<td>1058</td>
<td>647</td>
</tr>
<tr>
<td>Average efficiency of all tests is 0.39%</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Note: Extracted without change from Reference (1).
When this average is compared with that of burning hydrogen jets it can be seen that the overall noise of the combusting system is slightly greater than for the noncombusting jet for the same mechanical jet power. The contribution of burning to noise was shown to be much more evident in the frequency analysis, and it was concluded that the effect of combustion is additive and is confined to the low frequencies, 100 and 200 Hz band.

The results of this test series tend to confirm the conclusions presented in the scale-model test report.\(^{(1)}\) The overall contribution to noise when the mechanical jet power is the same jet power (based on heating value) are similar in calculable but generally not significant. The contribution is confined to the low frequencies, 50 to 200 Hz band.

**B. OSCILLATORY COMBUSTION**

Oscillatory combustion has been observed in numerous experiments. The first attempt to explain it was by Lord Rayleigh\(^{(9)}\). In large-size installations these oscillations can be more than annoying - they can be destructive to equipment. At the present time it is difficult, if not impossible, to design a duct system to assure that oscillatory combustion will not occur. A list of the reasons would include:

1. The exact driving mechanisms are only partially understood.
2. Oscillations can occur in many different combinations.
3. The geometry of any real system is too complicated to model exactly.
4. The mathematics of analysis are primitive.

Because of this the results from each test were analyzed for evidence of oscillatory combustion. The test data (motion-picture film, magnetic tapes, personal observations, etc.) were studied for any indication of oscillatory combustion. No evidence of oscillatory combustion was found.

**VII. COMPARISON OF PREDICTED AND ACTUAL SOUND PRESSURE LEVELS**

The objective of this investigation (ETS-1 Modification No. 175) was to modify ETS-1 structures to be capable of withstanding the acoustic loads emanating from the combusting duct exhaust plume. Preliminary estimates of the plume-generated noise level indicated that walls designed to sustain these acoustic forces would be more than adequate in terms of all other design criteria; acoustics thus became the controlling design factor.

Accordingly, as soon as the preliminary results of the scale-model test program were available (Reference 1), these data with pertinent literature information were reviewed by representatives of Paul S. Veneklasen and Associates, LASL, MSFC, and Aerojet.* Because engine full-power testing was considered the most severe mode of operation, a priori prediction of 154 and 140 db OASPL was made for the centers of the duct-vault inverting wall and the upper heat shield respectively, thus establishing the acoustic design criteria for each wall.

Sound pressure levels at selected times are shown for the tests of interest in Table 6. Restricting discussion to test 5C, the full-power run, as imposing the highest acoustic loadings, the data show an OASPL of 158.0 db at the center of the duct-vault inverting wall just above the duct exit (Microphone HM 113) and 142.0 db at the center of the upper heat shield (Microphone HM 115). These measured values are 4 and 2 db higher than predicted. The possibility that this increase could be the result of experimental error, higher-than-anticipated jet-power energy, or near-field energy accentuation was evaluated and found insufficient to account for a discrepancy of this magnitude.

\*On 21 August 1968
After a review of the pretest estimate method and the test measurements from full-power run (5C), the most likely explanation of this discrepancy lies in an increase in the mechanical-acoustic conversion efficiency beyond that determined in scale-model testing. Whether this is caused by a change in duct effluent composition (hydrogen and nitrogen was used in scale-model flows and hydrogen and steam in the full-scale system) or to a scale-up effect that was not adequately modeled in the pretest-prediction method is open to conjecture. The mechanical conversion efficiency initially estimated from scale-model data was 0.20. The corresponding value calculated from the four microphone signals for the full-power run, suitably integrated, is 0.50%, a factor of 2.5. The agreement between microphone readings, which is sensitive to application of conventional principles to scaling as well as to estimates for the near field, far field, and wall and directivity effects, is within ±1 db of the initially estimated values. Sound pressure levels were estimated for the inverting wall and upper heat shield by using the pretest model but with a mechanical conversion efficiency of 0.50%. The results are shown in Figure 20.
VIII. RECOMMENDED PREDICTION METHOD

A major objective of the investigation was to develop an acoustic prediction method suitable for this application (high-energy gas jets, near-sonic gas velocities, both near and far field, and large amounts of free hydrogen in the duct gas). Accordingly, as soon as the preliminary results of the scale-model tests were complete, a preliminary model was developed. As engine test results became available, the theory was expanded and improved. The recommended prediction method is described below.

The jet kinetic power is calculated:

\[ \text{WKJET} = 0.676 \times \text{WJOT} \times \left( \frac{\text{VEKIT}}{2 \times \text{WJOT}} \right)^2 \]  

(4)

The jet thermal power is also calculated:

\[ \text{WJTH} = \text{WJOT} \times \text{HCB} \]  

(5)

The overall acoustic power and power level are obtained from a knowledge of the jet kinetic and thermal powers.

\[ \begin{align*} 
\text{OAPW} &= \text{WJTH} + \text{WKJET} \\
\text{OASPL} &= 130 + 10 \log (\text{OAPW})
\end{align*} \]  

(2)  

(6)

where \( \text{WJTH} \) and \( \text{WKJET} \) are estimated from scale model testing or relevant test data.

This completes the calculation of overall power level, the first part of the analysis. The spectral calculation follows:

The Strouhal number is estimated:

\[ \text{NSTR} = \text{FREQ} \times \text{DEEXIT}/\text{VEKIT} \]  

(7)

The power-spectrum level is estimated from the data of Refs. 1, 2, 3 or 6, and the octave-band power level from:

\[ \text{OBPL} = \text{OASPL} + \text{OAPWL} - 10 \log (\text{VEKIT}/\text{DEEXIT}) \]

\[ + 10 \log (\text{FREQ} \times \sqrt{2}) \]  

(8)

The directivity index, near field, and wall effects are estimated from scale-model data or relevant sources and the octave-band and overall sound pressure level calculated from:

\[ \begin{align*} 
\text{OBSPWL} &= \text{OBPL} - 10 \log (2 \pi \text{R}^2) + \text{DINDX} + \text{DNF} + \text{SMALL} \\
\text{OASPL} &= 10 \log \frac{M}{\Pi} \text{Antilog} \left(\frac{\text{OBSPWL}}{10}\right)
\end{align*} \]  

(9)  

(10)

This method is superior to conventional methods when large amounts of energy are released by combustion as \( \text{WJTH} \) and \( \text{WJTH} \) can be estimated separately and probably more accurately.

Nomenclature basis is as before, but with the following new symbols:

\( \text{DEEXIT} \) = Diameter of duct exit, ft
\( \text{DINDX} \) = Directional acoustic effect, \( \text{db re 0.0002 dynes/cm}^2 \)
\( \text{DNF} \) = Near field acoustic effect, \( \text{db re 0.0002 dynes/cm}^2 \)
\( \text{SMALL} \) = Wall acoustic effect, \( \text{db re 0.0002 dynes/cm}^2 \)
\( \text{FREQ} \) = Mean frequency, Hz
\( \text{E} \) = Conversion factor, \( \text{lbm ft/sec}^2 \text{ lbf} \)
\( \text{HCB} \) = Gross heat of combustion, \( \text{watt sec/lbm} \)
\( \text{OB} \) = A prefix indicating octave band
\( \text{NSTR} \) = Strouhal number
\( \text{PWL} \) = Acoustic power level, \( \text{db re 10}^{-13} \text{ watt} \)
\( R \) = Effective distance from the microphone to the effective center of sound, ft