ION-THRUSTER PROPELLANT UTILIZATION

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SUMMARY

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INTRODUCTION

The mercury electron-bombardment ion thruster was introduced in 1960 (refs. 1 to 2). (Although ref. 1 was published in Nov. 1960, ref. 2 was actually written first.) Bombardment by electrons had, of course, been used to produce ions prior to 1960. The need in electric propulsion was for a copious source of ions, but with a low enough current density to permit the integration of the source with long-lived accelerators operating at exhaust velocities of interest for propulsion applications. The earlier electron-bombardment ion sources either produced too few ions to be of interest or

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produced too high an ion current density to be used with practical electric-propulsion accelerators (refs. 3 to 10). In addition, most of the earlier sources were developed for specific applications, so that the source itself was often of secondary interest and inadequate information was given for evaluation in other applications.

The performance of the early electron-bombardment thrusters showed advantages over the performance of other ion thrusters of that period (ref. 11). These advantages led to a substantial research program on the bombardment type of thruster (refs. 12 to 141). Propellants other than mercury have been investigated, but only cesium appears to be a practical alternative to mercury (refs. 142 to 156). Because the primary interest in space propulsion is for mercury propellant, and because there are fundamental differences in operation with cesium, the past work with mercury will be emphasized in the following historical review.

Historical Development

The most characteristic part of an electron-bombardment thruster is the ion chamber, which started as a simple cylinder having a nearly uniform magnetic field roughly parallel to its axis. Most of the later improvements have been associated with the magnetic-field shape. First, the field windings were designed to give a decreasing magnetic field in the downstream direction (ref. 12). This shape is usually referred to as a divergent field. The strength of the optimum magnetic field was found to vary inversely with thruster diameter, with the optimum in the range $1 \times 10^{-3}$ to $5 \times 10^{-3}$ tesla ($10$ to $50$ G) for a 10-centimeter-diameter thruster. An increase in magnetic-field strength was found to decrease ion-chamber losses at low values of field strength (ref. 12). The practical limit for magnetic-field strength was obtained when a further increase in field strength yielded a negligible decrease - or even an increase - in ion-chamber losses. More detailed investigations conducted later showed that ion-chamber noise increased with magnetic-field strength at high field-strength values (refs. 51 and 66), which indicated that collective or wave interactions were limiting electron containment at these higher field strengths. Iron pole pieces were added to increase the divergence of field lines in more recent designs (refs. 50 and 80). These pole pieces were originally incorporated as part of permanent-magnet designs (refs. 26 and 50) but have since become important tools for shaping the magnetic field. These pole pieces are therefore also employed on more recent thrusters that use electromagnets (refs. 95, 112, 119, and 141).

The foregoing constitutes the main line of magnetic-field configuration development, but some other concepts deserve mention. An Ioffe quadrupole magnetic field was adapted from fusion research (ref. 103) but gave no improvement in performance despite a decrease in plasma noise. The multipole "picket-fence" concept of plasma contain-
A more important, but still significant aspect of ion-chamber design is that of propellant introduction. The first approach was to introduce the propellant at one end of the ion chamber and to let it flow through to the accelerator system on the other end. An investigation of various propellant introduction locations then showed that introduction at the downstream end of the chamber (reverse feed) gave a substantial reduction in losses (ref. 37). The effects of magnetic-field shape and propellant introduction are interrelated, though, so that the amount of improvement possible by changing the propellant introduction mode is less for the more recent divergent-field configurations. In fact, for the SERT II configuration, little change was noted with introduction mode except for introduction near the cathode (ref. 80). Introduction near the cathode gave substantially poorer performance.

Considerable effort has also been expended on the development of ion-chamber theory. Most of the theory has been of only moderate utility, typically describing qualitative trends with poor quantitative agreement (refs. 2, 14, 19, 43, 44, 51, 52, and 85). A thorough evaluation of published ion-chamber theory has been made recently (ref. 124). As concluded in this evaluation, the most detailed description of plasma processes and loss mechanisms has been obtained from a combination of theory and extensive probing of the ion-chamber plasma (refs. 21, 74, 97, and 113). To date, almost all progress in ion-chamber performance has been the result of cut-and-try experimentation. Ion-chamber theory, though, is reaching a level such that this empirical pattern may not be followed in the future.

The specific area of interest for the investigation reported here is propellant utilization. Propellant utilization is defined for singly ionized atoms as the fraction of total propellant flow that is ionized and accelerated into the ion beam. The earliest ion chambers reached a propellant utilization of 0.8. Shortly thereafter a scale effect was observed in which utilization was found to increase in some general manner with thruster size (ref. 14). Except for one attempt to correlate utilization data with a simple residence-time parameter (ref. 43), there were no further general advances in understanding or improving utilization. Instead, the typical approach was to improve the utilization of a specific design at a particular operating condition by largely cut-and-try methods.

The main and neutralizer cathodes have been major lifetime problems of the mercury-bombardment thruster. The main cathode has received the bulk of the attention and is considered first. The first cathode type that was used was a refractory-metal wire or ribbon. Ion bombardment was found to limit this type of cathode to lifetimes of about 1000 hours, or less, in the ion-chamber environment (ref. 29). A greater thick-
ness will be more resistant to sputtering, but cathode thickness is limited by conduction losses to supports. If the conduction losses were limited by using a heavy refractory-metal emitting surface heated by a fine enclosed filament, sublimation of the enclosed filament limits lifetime. A wide variety of matrix and dispenser cathodes (impregnated with strontium and/or barium oxides) were investigated next (refs. 31, 42, 53, 62, and 90) with the maximum lifetime exceeding 5000 hours. An oxide-coated cathode in which most of the surface is protected against energetic ion bombardment was also investigated (ref. 78). A shortcoming of any cathode that depends on oxide for most or all of its emission, though, was brought out during the SERT II program. It is desirable from a reliability viewpoint to test the actual hardware to be flown before it is launched. A tested, but unlaunched, oxide cathode is difficult to keep from exposure to the atmosphere and subsequent deactivation. This difficulty was a critical factor in the SERT II decision to use a hollow cathode (ref. 90).

The mercury hollow cathode has an interesting history. A cesium plasma-bridge neutralizer was developed for the cesium electron-bombardment thruster (ref. 143). This neutralizer was a small-scale version of the autocathode used in the ionization chamber of the cesium thruster, and its electron emission was readily explained in terms of the low work function of a cesium coating. A similar design of neutralizer was then operated on a mercury-propellant thruster (ref. 45), where the high work function of mercury made the previous explanation of operation unsuitable. During the development of the mercury plasma-bridge neutralizer for SERT II, it became evident that the neutralizer cathode would easily operate at main cathode conditions. As mentioned earlier, the switch to the hollow cathode was then made on the basis of being able to ground test the actual flight hardware. A small amount of oxide is used in the hollow cathode, but it is buried inside the cathode and is used only to provide a few microamperes of starting current. With the oxide used in this manner, repeated exposure to the atmosphere has no significant adverse effects (ref. 71). Another hollow-cathode design, now called an "enclosed keeper" design, was also considered in the early development of mercury hollow cathodes (ref. 45). This type of hollow cathode has recently shown substantial reductions over more conventional hollow cathodes in the propellant-flow requirements for low-emission applications (ref. 125).

Before leaving main cathodes, one more type should be mentioned, the liquid metal (LM) type (refs. 56, 64, and 95). The LM cathode is similar to the hollow cathode in that it can be exposed repeatedly to the atmosphere when used with mercury propellant. The LM cathode is a workable, long-lived alternative to the hollow cathode but appears to require more complex solutions to the feed and isolation problems (ref. 84). It should also be mentioned that the baffle used to control discharge voltage in the SERT II thruster with a hollow cathode had its origin in a similar baffle used in ion chambers with LM cathodes.
The first neutralizers used with bombardment thrusters were simple refractory-metal thermionic emitters that were immersed in the ion beams (refs. 1 and 23). Such neutralizers are satisfactory for short tests, such as the SERT I ballistic flight (ref. 39), but ion erosion prevents their use for long-duration applications. Thermionic cathodes have also been placed near the ion beam, but such placement has always been a compromise between ion impingement from the fringe of the ion beam and high losses due to poor coupling to the beam (ref. 55). The plasma-bridge neutralizer avoids this compromise by providing ions to neutralize the electron space charge (refs. 83, 86, 89, and 131). Thus, the plasma-bridge neutralizer can be located well out of the ion beam and still operate with small coupling losses.

The accelerator system that is presently used on most electron-bombardment thrusters consists of parallel plates with matching hexagonal arrays of holes and held in relative position by shadow-shielded ceramic insulators around the outside of the structure. Extensive experimental tests have been conducted on this type of accelerator system (refs. 13, 25, 41, and 61). Unlike ion-chamber theory, acceleratory theory has been well understood for a long time. The major cause of wear in a well-designed accelerator is charge-exchange erosion (ref. 22). The calculation of ion trajectories is well understood - although complicated and tedious. Because of the difficulty of making ion-trajectory calculations, early accelerator designs were created by empirical methods. The availability of electronic computers and ion-trajectory programs, though, has made the theoretical approach much easier to use (ref. 105).

Another type of accelerator system uses only one metal grid with a nonconducting coating on the side of the grid facing the ion chamber (refs. 54, 75, and 102). This composite accelerator is particularly sensitive to backspattered metal from the ion-beam target and has not yet reached the reliability and durability of more conventional accelerators. The composite accelerator originated from discussions at the Lewis Research Center of an early version of a radiofrequency ion thruster developed by LÖb (ref. 157). The thruster discussed had a conventional metallic accelerator, but there was an insulator in contact with the accelerator to take the place of the usual screen grid. This sharp departure from conventional electron-bombardment accelerator construction stimulated a series of experiments that ended in the construction of the first one-piece composite accelerators (ref. 54).

There is a significant interaction between the ion source and the accelerator system. One aspect is the effect of screen-grid - open-area fraction, with the largest open-area fraction giving the lowest ion-chamber loss (ref. 60). Another aspect is the relation between ion-beam current and the current capacity of the accelerator system. For a given beam current and total propellant flow rate, the ion-chamber losses are lowest for an accelerator system operated at a small fraction of its current capacity. This last aspect has been shown by varying the voltage of a single accelerator configuration (ref. 12) and by a more general correlation of similar configurations (ref. 87).
Other components and aspects of electron-bombardment thrusters that have been investigated are feed systems (refs. 15 and 46) isolators (refs. 34, 49, and 77), arcing (refs. 20 and 33), and controls (refs. 28, 35, 66, and 127). The effluents of the thruster have also been studied, first from the diagnostic viewpoint (refs. 38 and 45) and later from the viewpoint of interactions with the rest of the spacecraft (refs. 72, 104, 107, 122, 133, 135, and 140). Although the bulk of published electron-bombardment development has taken place in the United States, considerable work has also been done in Europe (refs. 63, 68, 81, 93, 98, 129, and 141).

Present Investigation

The objective of the present investigation is to determine the factors that control maximum utilization of propellant in an electron-bombardment thruster. The thrust in a space propulsion application is provided almost entirely from the ionized portion of the propellant. The un-ionized propellant thus constitutes a loss and should be minimized. The only previously published attempt to predict propellant utilization (ref. 43) used a residence-time approach for a neutral in the ion chamber. Although this approach gave the correct qualitative trends, quantitative agreement was poor. The objective of this investigation, then, includes obtaining a quantitative agreement better than that previously published. An analysis of maximum propellant utilization was published earlier as part of the investigation described in this report (ref. 136) and is the foundation for the theory which will be compared with experimental data.

The thruster selected for the experimental portion of the investigation was originally operated with a 20-centimeter-diameter accelerator system but was masked down to a 10-centimeter system for the work described in this report. This thruster permitted tests over a wide range of ion-chamber configurations, including ones with diameters larger than the accelerator system. An electromagnet was used instead of permanent magnets to permit a range of field strengths to be investigated. A strongly divergent magnetic field (with field-shaping pole pieces) was employed to be consistent with current design trends. Each ion-chamber configuration was operated over a wide range of propellant flow rates from near the lower limit for a sustained discharge to near the upper limit controlled by frequent electrical breakdowns. The thruster was operated in vacuum chambers located at Colorado State University and at the NASA Lewis Research Center. SI (mks) units are used throughout this report.
ION-CHAMBER THEORY

The operation and typical values of various operating parameters are presented in the first part of this section. The two propellant-utilization theories that are compared to the experimental data are also presented, as well as a discussion of the Bohm criterion and its use in this investigation.

Typical Operation

A schematic of an electron-bombardment thruster is shown in figure 1. Electrons are emitted by the ion-chamber cathode, which is maintained 30 to 40 volts negative of the anode. The emitted electrons are constrained by the magnetic field (not shown in fig. 1) until they collide with propellant atoms. The magnitude of the cyclotron radius for high-velocity emitted electrons is typically 0.1 to 0.5 of the ion-chamber radius.

![Figure 1. - Schematic diagram of electron-bombardment thruster with power supplies.](image-url)
Some of the ions produced by these collisions reach the right end of the ion chamber, where they are accelerated to form the ion beam. This ion beam is normally charge-density and current neutralized in space by electrons emitted by the neutralizer cathode. In this investigation no neutralizer was used. Instead, as is frequently done in ground tests, the secondary electrons from the ion-beam target were used to charge neutralize the ion beam. The low density and high velocity of the ions in the ion beams assure that only a negligible fraction of the ions recombines with electrons near the thruster.

Un-ionized propellant atoms also escape through the accelerator and are the loss of particular interest in this investigation. Thruster efficiency is defined as

$$\eta_T = \frac{F^2}{2mP}$$  \hspace{1cm} (1)

where $F$ is the thrust in newtons, $\dot{m}$ is the total propellant flow in kilograms per second, and $P$ is the power in watts. In terms of the propellant flow $\dot{m}_i$ that is ionized and ejected from the thruster and the propellant utilization $\eta_U(= \dot{m}_i/\dot{m})$, equation (1) can be rewritten as

$$\eta_T = \frac{\eta_U F^2}{2\dot{m}_i P}$$  \hspace{1cm} (2)

The thruster efficiency is thus proportional to propellant utilization, and an improvement in propellant utilization can be translated directly into improved thruster performance. The understanding that might make possible such a performance improvement is the objective of this investigation.

During typical operation the neutral density in the ion chamber corresponds to about $10^{-4}$ torr, or $\sim 10^{18}$ mercury atoms per cubic meter at a 500 K ion-chamber wall temperature. The ions are only about 10 percent as dense as the neutrals ($\sim 10^{17}/m^3$), and the electron density equals that of the ions (ref. 123). All of these densities are approximate mean values for the ion chamber as a whole when operated at design conditions. Special locations such as the vicinity of a hollow cathode could exhibit large departures from the values given. The electron energy distribution corresponds to roughly a 5-eV temperature, although there are significant departures from a Maxwellian distribution that are discussed later in this report. This approximately 5-eV temperature is the result of energy addition (directly or indirectly) by emitted electrons and energy loss by excitation and ionization.

The Debye shielding distance for a plasma in which most of the random energy is in the electron population ($T_e \gg T_i$) is
\[ l_D = 7.43 \times 10^3 \sqrt{\frac{T_e}{n_e}} \]  

where \( T_e \) is the electron temperature in eV, and \( n_e \) is the electron density in number per cubic meter. For typical ion-chamber conditions, equation (3) gives \( \sim 5 \times 10^{-3} \) centimeter. This small Debye shielding distance, when compared with the ion-chamber diameter of 10 centimeters, justifies the assumption of \( n_e = n_i \).

Although the ion density is normally much less than the neutral density in the ion chamber (ref. 97), far more ions than neutrals leave through the accelerator system. This apparent discrepancy is due to the difference in velocities for these two species in the ion chamber. The neutral velocity distribution is essentially Maxwellian and is controlled by the wall temperature. The average magnitude of neutral velocity \( \left( \bar{V}_o = \sqrt{8kT/nm} \right) \) is 230 meters per second for a typical wall temperature of 500 K. The loss rate of neutrals \( \dot{N}_o \) can be calculated from

\[ \dot{N}_o = \frac{n_o \bar{V}_o A_o}{4} \]  

where \( n_o \) is the neutral density in the ion chamber, and \( A_o \) is the equivalent sharp-edged orifice area of the accelerator system. The ions, on the other hand, have a directed velocity towards the boundaries of the ion chamber, including the accelerator system. This directed velocity is given by Bohm's criterion for a stable sheath (ref. 158),

\[ v_i \approx \sqrt{\frac{q_i T_e}{m_i}} \]  

where \( q_i \) and \( m_i \) are the charge and mass of the ions. Expression (5) is equivalent to the ions having a minimum energy equal to one-half that of an electron at the most probable velocity \( \left( v_{mp} = \sqrt{2kT/m} \right) \). Expression (5) indicates a range of ion velocity is possible. In practice, though, an equality is generally assumed. This use of an equality is discussed later in this section. There are corrections that can be given to the minimum velocity of expression (5). One correction that has been made is due to the departure of electrons from a Maxwellian distribution (ref. 123). Another more difficult correction, that apparently has been done only in a simplified form (ref. 159), includes the effect of ions coming from different regions at different potentials, and thus having a range of ion velocities. To apply the first of these corrections to the investigation of this report requires a completeness of probe data that has seldom been attained. To
apply the second would require laborious detailed calculations based on such complete probe data. Because of the directed nature of this Bohm velocity, the relation for loss rate of ions is essentially

\[ \dot{N}_i = n_i v_i A_i \]  

(6)

where \( n_i \) is the ion density, and \( A_i \) is the boundary area involved in ion loss. (The area \( A_i \) is usually several times larger than the neutral-loss area \( A_o \) used in eq. (4).) For an electron temperature of 5 eV, the Bohm velocity for singly charged mercury ions is \( 1.55 \times 10^3 \) meters per second. With this velocity, equation (6) indicates a loss rate of ions about a factor of 10 greater than that for neutrals (eq. (4)). The low fraction of ionization in the ion chamber is thus quite compatible with a high fraction of ions in the particles escaping through the accelerator system.

The ion-chamber plasma is assumed in the foregoing to have all path lengths long compared to ion-chamber dimensions. The mean-free-path length for electrons colliding with neutrals or for energetic electrons colliding with slower background electrons is given by

\[ l = \frac{1}{n \sigma} \]  

(7)

where \( n \) is the density of the target species, and \( \sigma \) is the cross section of the process. The path length for the total collision cross section of electrons with neutrals is about 1 to 3 meters for an electron energy range of 5 to 40 eV. The large magnitude of this path length compared with ion-chamber size is the reason for using a magnetic field to conserve electrons. The magnetic field is weak enough (~10^-3 T, or ~10 G), though, that the ion trajectories are essentially unaffected.

The cross section for excitation or ionization by 30- to 40-eV electrons is about \( 5 \times 10^{-20} \) square meter (refs. 160 and 161), which gives a path length of about 20 meters. The electron-electron coulomb-collision cross section (90° collision) for 30- to 40-eV electrons and a \( \sim 10^{17} \)-per-cubic-meter background electron density is also about \( 5 \times 10^{-20} \) square meter (ref. 162), but the electron density is lower than the neutral density so that the path length for this process is about 200 meters. Thus, the probability of energy loss due to excitation and ionization for a 30- to 40-eV electron is much greater than that due to coulomb collisions with back-ground electrons. The population of these energetic electrons, then, is determined by cathode emission rather than a Maxwellian "tail." As a rough approximation perhaps 10 percent of the electrons are usually found to be energetic "primaries," while the rest make up an essentially Max-
wellian distribution. The primary electrons have been found to produce about half the ions in the ion chamber, while the Maxwellian "tail" produces the rest (ref. 123). This division of ion production is for normal operation and will be a subject of discussion for conditions of maximum utilization.

Metastable states are often important in mercury discharges. Because of the low pressure of the discharge, though, metastable states are not important for ion production in a bombardment ion thruster.

Residence-Time Approach

The residence-time approach described in this section was published in 1965 (ref. 43). It assumes a cylindrical ion chamber with an accelerator system covering one end of the cylinder and with uniform conditions throughout the chamber. The differential equation for probability of ionization $p_i$ is

$$dp_i = v_e \sigma t_o (1 - p_i) dn_e$$

where $\sigma$ is the ionization cross section, $t_o$ is the residence time for a neutral (in the absence of ionization) in the volume of interest for production of beam ions, and $n_e$ and $v_e$ are the density and velocity of the ionizing electrons. The probability $p_i$ can be integrated from 0 to $\eta_U$, while the electron density is integrated from 0 to $n_e$. This gives propellant utilization $\eta_U$ as

$$\eta_U = 1 - \exp(-n_e v_e \sigma t_o)$$

Thus $n_e v_e \sigma t_o$ can be used as a correlating parameter for propellant utilization. The variables used in this parameter, though, are not particularly convenient. More accessible variables will therefore be substituted. The mean electron energy can be assumed proportional to the ionization potential $\varphi_i$, inasmuch as the electron energy is normally controlled by excitation of ground-state neutrals, and the excitation energy of ground-state neutrals is roughly proportional to $\varphi_i$. Thus, the electron velocity is

$$v_e \propto \varphi_i^{1/2}$$

1This is one of the important differences between cesium and mercury electron-bombardment thrusters. The electron-electron coulomb-collision cross section varies inversely as the square of electron energy. The much lower discharge voltages used with cesium thus result in very rapid randomization of emitted electrons, with no distinct primary electron group.
The electron density can be expressed in terms of the ion density upstream of the accelerator, which in turn can be expressed in terms of the ion-beam current density \( j_i \) and the Bohm critical velocity. With these assumptions, one finds

\[
n_e \propto \frac{j_i w^{1/2}}{\varphi_i^{1/2}}
\]

where \( w \) is the atomic weight of the propellant. The residence time is a function of neutral velocity \( (v_0 \propto w^{-1/2}) \) and ion-chamber length \( l \), so that

\[
t_0 \propto l w^{1/2}
\]

From the last three relations, the correlating parameters can be written as

\[
n e v e \sigma t_0 \propto j_i l \sigma w \propto j_i l
\]

(The last step results from the propellant being restricted to mercury in this investigation.) Equation (9) can therefore be written as

\[
\eta_U = 1 - \exp(-K j_i l)
\]

where \( K \) is a constant that can be evaluated from the previously published analysis (ref. 43) as 5.2.

For equation (14) to correlate the performance of different thrusters, various conditions (such as ion-chamber wall temperature and fraction blockage of the accelerator system) must be nearly the same for different thrusters. In particular, the use of a 20-centimeter chamber diameter with a 10-centimeter accelerator system is a sharp departure from the conditions assumed for this equation. In fact, only the 10-centimeter chamber data presented in this report are suitable for comparison with equation (14). Inasmuch as these last mentioned data will still be found to correlate poorly with equation (14), there will be no need to modify that equation for the 20-centimeter-chamber data.

**Primary-Electron-Region Approach**

This analysis is directed at a condition of high propellant utilization and is concerned for the most part with primary electrons. The primary electrons do not occupy
the entire ion chamber, but instead are concentrated in only a portion of the volume. This portion is essentially restricted to the volume enclosed by the accelerator system and magnetic-field lines that intersect the anode. The reason for this restriction of primary electrons to a small volume is that the small plasma sheath on the anode does not reflect energetic electrons that can reach it. The existence of a primary-electron region is experimentally evident when detailed probe data are available (ref. 123). At the high-utilization condition of interest in this analysis, a high fraction of primary electrons is expected. The high fraction of primary electrons is in turn expected to result in primaries causing the bulk of ionizations. The expectation of a high fraction of primaries is supported by probe data.

Early bombardment-thruster designs typically had an extensive volume occupied by primary electrons, as indicated in figure 2. Because the region occupied by primary electrons in this design extends the full length of the ion chamber, a change in ion-chamber length will clearly affect the primary electrons. The primary-electron region indicated in figure 2 is, of course, somewhat idealized. The finite cyclotron radius of primary electrons leads to a boundary with finite thickness instead of the line thickness of a limiting magnetic-field line, as indicated in figure 2. With recent divergent-field designs, however, the primary-electron region is localized near the screen. For the thruster under investigation in this report, the primary-electron region is indicated in figure 3. As shown in figure 3, the primary-electron region is independent of chamber geometry unless the chamber is made very short.

The density of primary electrons increases with discharge current. For a rough approximation, then, the limiting condition of all electrons being primaries can be assumed for maximum utilization. Consider first the total ion production rate $\dot{N}$ from primary electrons. When mean values are used for the primary-electron region,

$$\dot{N} = n_p v_p n_0 \sigma V_p$$

where $n_p$ and $v_p$ are the primary-electron density and velocity, $n_0$ and $\sigma$ are the neutral density and ionization cross section, and $V_p$ is the volume of the primary-electron region. For the total loss rate of ions from this region,

$$\dot{N} = n_i v_i A_p$$

where $n_i$ and $v_i$ are the ion density and velocity toward the outer boundary of the primary-electron region, and $A_p$ is the area of this outer boundary. The ion velocity toward the outer boundary can be estimated from the Bohm criterion for a stable sheath given in expression (5), in which a Maxwellian electron distribution is assumed. The limiting condition of all electrons being primaries would probably depart from a Maxwellian distribution, but expression (5) should still approximate the sheath stability limit.
Figure 2 - Primary-electron region (shown by crosshatching) of early bombardment thruster.

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Figure 3 - Primary-electron region (shown by crosshatching) of divergent-field thruster used in this investigation.
For the limiting condition of all electrons being primaries and the mean energy used for $T_e$, the minimum ion velocity from expression (5) is

$$v_i = v_p \sqrt{\frac{m_e}{2m_i}} \quad (17)$$

As mentioned earlier, the Debye shielding distance is very small. For the primary-electron region, then, with all electrons in this region assumed to be primaries,

$$n_p = n_i \quad (18)$$

With the substitution of equations (17) and (18) into (16) and the equating of ion loss and production rates (eqs. (15) and (16)), one finds

$$n_o = \frac{\sqrt{m_e/2m_i}}{\sigma(V_p/A_p)} \quad (19)$$

With mercury used for $m_i$, and $5 \times 10^{-20}$ square meter used for the ionization cross section $\sigma$ (40-eV electrons), this becomes

$$n_o = \frac{2.34 \times 10^{16}}{V_p/A_p} \quad (20)$$

A constant neutral density upstream of the accelerator system implies a constant loss of neutrals at maximum propellant utilization regardless of the total mass flow.

The preceding part of this approach (eqs. (15) to (20)) has been published previously (ref. 136). The following extension has been made in an attempt to approximate more closely the effects of a non-Maxwellian electron distribution. This extension includes the effects of both primary and Maxwellian electrons.

A modified Bohm criterion has been derived by Masek to give the combined effect of monoenergetic primary and Maxwellian electron populations (refs. 97 and 123). This modified Bohm criterion can be written (at the minimum ion energy) as

$$v_i = v_m \sqrt{\frac{m_e(n_p + n_m)}{2m_in_m}} \quad (21)$$

15
where \( v_m \) is the most probable Maxwellian electron velocity \((v_{mp} = \sqrt{2kT/m})\), and \( n_p \) and \( n_m \) are the primary and Maxwellian electron densities. Equation (21) can be rewritten as

\[
v_1 = v_p \sqrt{\frac{m_e}{2m_i}} \sqrt{\frac{T_m}{\varepsilon_p}} \sqrt{1 + \frac{n_p}{n_m}}
\]  
(22)

where \( v_p \) is the primary-electron velocity, and \( T_m \) and \( \varepsilon_p \) are the Maxwellian electron temperature and primary-electron energies, both in eV. Equation (18) can be rewritten in terms of primary and Maxwellian electron populations as

\[
n_i = n_p \left(1 + \frac{n_p}{n_m}\right)
\]  
(23)

Substitution of equations (22) and (23) into the loss-rate equation (eq. (16)) yields

\[
N = n_p v_p \sqrt{\frac{m_e}{2m_i}} \sqrt{\frac{T_m}{\varepsilon_p}} \frac{(1 + n_p/n_m)^{3/2}}{n_p/n_m} A_p
\]  
(24)

Equation (15) can be used again for the production-rate equation. Equating the loss and production rates,

\[
n_o = \frac{\sqrt{m_e/2m_i}}{\sigma(V_p/A_p)} \sqrt{\frac{T_m}{\varepsilon_p}} \frac{(1 + n_p/n_m)^{3/2}}{n_p/n_m}
\]  
(25)

The mass of a mercury ion can be assumed for \( m_i \), and \( 5 \times 10^{-20} \) square meter can be used for \( \sigma \). A value of 5 eV is reasonable for \( T_m \), while \( \sim 40 \) eV would be expected for \( \varepsilon_p \) in a 40-volt discharge (used throughout this investigation). Equation (25) can then be written as

\[
n_o = 0.827 \times 10^{16} \left(1 + \frac{n_p}{n_m}\right)^{3/2}
\]  
(26)

The variation of \( n_o(V_p/A_p) \) as a function of \( n_p/n_m \) was obtained from equation (26) and plotted in figure 4. The value of \( n_o(V_p/A_p) \) from equation (26) is seen to be higher than
Figure 4. Variation of neutral-density parameter with primary-to-Maxwellian density ratio – from equation (26). Primary energy, 40 eV; Maxwellian temperature, 5 eV.
the same value from equation (20) for all $n_p/n_m < 1$. Because of its inclusion of non-Maxwellian electron-distribution effects, equation (26) is thought to be more accurate than equation (20).

**Use of Bohm Criterion**

The Bohm criterion plays an important role in the preceding analysis. Some additional comments on the use of this criterion therefore appear to be appropriate. The original relation given for this criterion of sheath stability was (ref. 158)

$$v_i \geq \sqrt{\frac{q_i T_e}{m_i}}$$

(27)

**Figure 5.** - Form of potential solutions for low-density plasma.
That is, the directed velocity of (cold) ions toward a collisionless sheath must be equal to, or greater than, the critical value of \( \sqrt{q_i T_e / m_i} \). In making ion-flux calculations for a sheath, however, it is customary to assume a simple equality. Perhaps the best justification for such an assumption is that it gives results in agreement with experiment (refs. 97 and 123). Another assumption in the preceding analysis is the use of the Bohm criterion at the upstream boundary of the primary-electron region. This boundary is not a sheath in the ordinary sense. It is, instead, a boundary that separates the primary-electron region with its high ion production rate from the rest of the ion chamber with a much lower ion production rate. This assumed difference in ion production rate is supported in the RESULTS AND DISCUSSION section by Langmuir probe data.

To see the effect of localizing the ion production region, consider figure 5. In figure 5(a) the ion production extends throughout the region between two walls and shows the customary gradual transition from plasma to sheath. In figure 5(b) the ion production has been localized to a central portion of this region. The solution shown in figure 5(b) has been obtained analytically (ref. 163). The ions were found in this analysis to have close to the critical velocity of \( \sqrt{q_i T_e / m_i} \) throughout the two regions of nearly uniform potential shown in figure 5(b). From figure 5(b), then, one would expect the Bohm criterion to apply to the boundary of the primary-electron region as long as the bulk of ion production takes place in this region.

APPARATUS

The mercury propellant thruster used in this investigation is shown in figure 6. The magnetic field is determined by a ring-shaped soft-iron pole piece near the accelerator and a cylindrical soft-iron pole piece near the cathode. These pole pieces are connected by four soft-iron paths (each about 3.2 by 12.7 mm, in cross section) on which the field windings are mounted. The cylindrical pole piece has about the same cross section as the total of the four paths and also has a field winding for most of its length. There were about 5.3 turns per centimeter for all of the field windings. The construction of the four soft-iron paths permitted axial motion of the cylindrical pole piece for initial optimization. Thereafter, the cylindrical pole piece was held fixed. The data presented in this report were obtained with the central pole piece 3.5 centimeter from the screen grid. This axial location gave good performance over a wide range of utilization. Experimental data were taken at various magnetic-field currents, but most of the data were obtained at a current of 1 ampere. At this current the typical magnetic field in the ion chamber (assumed to be midway between probes A and B in fig. 7) was about \( 3 \times 10^{-3} \) tesla (30 G). This field was somewhat nonlinear with current and rose to about \( 5 \times 10^{-3} \) and \( 9 \times 10^{-3} \) tesla for currents of 2 and 5 amperes.
A screen with 71 percent open area was used to reduce ion recombination on the screen. Only holes completely within a 10-centimeter-diameter circle were used to accelerate ions, and there were 429 such holes in the accelerator design used. The screen-accelerator spacing was 2 to 2.5 millimeters over the beam area. A tungsten wire cathode was used to avoid both (1) the uncertainty in propellant utilization that can occur when an oxide cathode is inadvertently overheated, and (2) the effect of localized propellant concentration associated with a hollow cathode.

Ion-chamber probes were made by using 0.75-millimeter tantalum wire inside aluminum oxide tubes with an outside diameter of 1.6 millimeters. The locations of the probes are shown in figure 7. The two probes closest to the accelerator (A and B in fig. 7) were constructed with 0.75 millimeter of tantalum wire extending beyond the aluminum oxide. Probe C, because of the lower plasma density in that location, was constructed with a 1.5-millimeter extension. Probe location selections were made.
based on published probe surveys (refs. 85 and 97). Probe A intersected a magnetic-field line near the edge of the cathode and was thought to be representative of the primary-electron region. Probe B intersected a magnetic-field line at the boundary of the primary-electron region, while probe C was well removed from that region. Quartz tubes were used for one set of probe data in an attempt to extend the range of the probe data to higher propellant mass flows by reducing outgassing. Tantalum wires of 0.5-millimeter diameter (in holes of approximately the same diameter) were mounted flush with the ends of the quartz tubes in this set.

The thruster was first operated in a 1.2-meter-diameter, 4.8-meter-long Space Propulsion Research Facility located at Colorado State University. Most of the data, including all the probe data, were obtained during later operation in a 1.5-meter-diameter, 4.2-meter-long vacuum chamber at the NASA Lewis Research Center. Sketches of these two facilities are shown in figure 8. Both facilities used liquid-nitrogen-cooled liners and oil-diffusion pumps to attain pressures in the $10^{-6}$ torr range. In both cases the thruster was mounted in the bell jar shown at the left end of the facility. Existing power supplies were used for the various thruster functions at both facilities,
Figure 8. - Vacuum facilities used in this investigation.
and the propellant flow at both locations was measured by timing the drop of a mercury column in a calibrated glass tube.

The meters used in voltage and current measurements are accurate within ±2 percent of full scale. Typical part-scale measurements should therefore be within ±1 percent. Because of the electrical transients that occur in other circuits when the accelerator system arcs, frequent calibration is necessary. The glass propellant-flow tube has a bore variation of 2 to 3 percent. This variation, together with a maximum of about 1 percent uncertainty in column-height measurement, determines the accuracy of the mercury-flow measurement.

PROCEDURE

The thruster used was unusual in that a thruster body suitable for a 20-centimeter-diameter accelerator system was used with only a 10-centimeter system. Because of this thruster design, the ratio of thruster mass to discharge power was large. This large mass resulted in the slow starting transient shown in figure 9. The 0.5-ampere discharge was started at time zero in figure 9. The high voltages were applied 2 minutes after the discharge was started, but did not reach the values of 3000 and -1500 volts until 12 minutes after the discharge was started. Condensation of propellant was assumed to have taken place on internal thruster surfaces before the thruster discharge was started. Evaporation after the ion-chamber discharge was started would then account for the rapid rise and large peak in ion-beam current. Equilibrium operation was attained when the condensed propellant was all evaporated, which apparently took about 1$\frac{1}{2}$ hours. The bumps in the descending curve of figure 9 were typical and apparently resulted from different parts of the thruster becoming warm enough to vaporize the condensed propellant at different times.

There was also a short-term transient effect whenever discharge conditions were changed. This effect was found after the initial warmup and was presumably due to the large ratio of internal surface area to beam area. Because of the adsorption of propellant on these surfaces at pressures of the order of $10^{-4}$ torr, a few minutes were required to reach equilibrium when the ion-beam current was changed. The associated transient effect is shown in figure 10, where a hysteresis loop is shown that was obtained by rapidly changing the discharge current (one data point per min). Some data in the first paper of this investigation (ref. 136) were taken without sufficient operation at each condition to avoid this effect. For the data presented here the thruster was operated for at least 5 minutes at any conditions that involved a substantial change in beam current from the previous operation point.

A transient thermal effect was also evident in the propellant flow measurement. A mass flow was set by holding the vaporizer constant (±10°C) at some temperature. The
Figure 9. - Starting transient for discharge (anode) current of 0.5 A and total propellant flow of 78 mA equiv.

Figure 10. - Short-term transient (1 min between data points) for total propellant flow of 74 mA equiv.
flow was then determined by measuring the drop in height of a mercury column and the
time required for this drop. To assure an accurate measurement of this column drop
despite meniscus effects in an approximately 1-millimeter bore, a drop of about 4 cen-
timeter or more was used at any vaporizer temperature. To obtain reproducible read-
ings after any change in vaporizer temperature, though, a wait of about 15 minutes was
found necessary.

All steady-state operation was at an anode potential of 3000 volts and an accelerator
grid potential of -1500 volts, with both measured relative to the vacuum facility. The
acceleration potential difference of 4500 volts was sufficient to handle ion-beam currents
of at least 150 milliamperes without any substantial rise in impingement. No neutrali-
zer was used, and charge-density neutralization of the ion beam was obtained by second-
ary electrons from ions striking the various portions of the facility.

The discharge chamber was operated at a potential difference of 40 volts for all data
presented herein. A range of cathode emissions was obtained for each of several mass
flow rates. The cathode emission was limited on the high end of the range by extinguis-
ishing the discharge, reaching the space-charge emission limit of the cathode, or simply
approaching the heater power limit of the cathode. The space-charge limit on emission
is reached when an increase in heater power results in little or no increase in emission.
A check point of one of the initial points was usually taken after covering a range of
emission currents. This procedure provided a spot check on constancy of other vari-
ables while emission-range data were obtained.

Propellant flows were limited on the low end by inability to sustain a discharge at
40 volts and at the high end by repeated electrical breakdowns between the screen and
accelerator grids. This range of propellant flow (and emission) was investigated with
each of the ion-chamber configurations.

The ion-chamber configurations were limited to three different lengths (7.2, 10.8,
and 14.4 cm) with a 10-centimeter diameter and two different lengths (9.4 and 14.4 cm)
with the larger 20-centimeter diameter. These configurations provided a range of about
4:1 for ion-chamber wall area and about 8:1 for volume. The propellant introduction to
the ion chamber was controlled by baffles of polyimide sheet. Most of the data were ob-
tained in the usual mode of straight-through flow from one end of the ion chamber to the
accelerator on the other end. This mode is called "forward feed." For comparison,

---

2 The current to the accelerator is usually called "impingement" in mercury
thruster work, because a low secondary-electron emission (10 percent or less) is the
only difference between the charge carried by ions striking the accelerator and the
measured current. In cesium thruster work it is customary to refer to this current as a
"drain." This is because a cesium coating on a hot accelerator electrode can result in
electron emission currents much greater than the ion impingement current.
one configuration was operated with "reverse feed," where the propellant was introduced through the gap between the ring-shaped pole piece and the anode.

Most of the data were obtained at a magnetic-field current of 1 ampere, which provided a compromise between good performance at high mass flow and ability to operate at low mass flow. Some data were also obtained at higher fields, though, for comparison.

Ion-chamber probe runs were made after runs of the same configuration without probes. This procedure permitted the time-consuming probe data to be obtained at a few preselected operating conditions, instead of determining the range of operation at the same time as obtaining the probe data. It also permitted a check on overheating of the probe insulation through the effect of the resultant outgassing on beam current and comparison with ion-chamber performance obtained without probes. Early runs showed that the probes became coated with a conducting layer after 2 to 3 days of operation, which led to erroneous probe data. To avoid this problem, probe insulators were discarded after 1 day of operation (in addition to being checked with an ohmmeter after each run to verify that there was no conducting layer). The use of aluminum oxide tubes led to a propellant-flow limitation where (at high discharge power) outgassing occurred because of overheating. In an attempt to extend the probe data to higher flows, the aluminum oxide tubes were replaced with quartz tubes. Although this substitution avoided the outgassing problem, the higher cathode sputtering at higher flows led to more rapid coating of the probe insulators with conducting layers. Thus, no significant extension of the probe data was obtained by this substitution. This probe limitation is apparently avoided with oxide-coated and hollow cathodes, inasmuch as probe data have been obtained at higher neutral flows with these cathodes (refs. 21, 74, 97, and 113).

In addition to the data checks described, the effects of multiple ionization and neutral backflow from the vacuum facility were also considered, though not included. A study of multiple ionization has shown that the ion-chamber discharge voltage and the cross sections for single and double ionization can be used to predict the fraction of doubly ionized atoms (ref. 16). The cross section for single ionization by a 40-eV electron is about $5 \times 10^{-20}$ square meter, while the cross section for double ionization by an electron of that energy is about $1 \times 10^{-21}$ square meter (refs. 160 and 161). The fraction of doubly ionized atoms should therefore be about 0.02. The appearance potential for triply ionized mercury is over 63 eV; hence, no triply ionized atoms would be expected. The reasons for this experimental result are that most beam ions come from collisions of primary electrons, and that these ions leave the ion chamber so rapidly after being ionized that there is little probability of additional ionizations taking place while they are leaving. Hollow cathode thrusters, which have a substantial potential difference across the baffle system, would be expected to have a smaller fraction of doubly ionized atoms for the same discharge voltage.
In order to calculate the backflow of neutrals into the ion chamber from the vacuum facility, a typical ion-gage reading of approximately $3 \times 10^{-6}$ torr can be used. Most of the indicated reading should be due to propellant atoms during thruster operation, and the calibration factor (gage reading divided by actual pressure) is about 3 for mercury. A particle density of approximately $2 \times 10^{16}$ per cubic meter would therefore be expected. A temperature of 300 K should be a conservative mean for the liquid-nitrogen-cooled tubes, the warmer baffles extending from these tubes, the room temperature end walls of the tank, and an ion-beam target that is warmer than room temperature. This density and temperature, together with an estimated effective backflow orifice area of 0.00196 square meter, permit calculation of the backflow. This backflow, if singly ionized, is equivalent to only approximately 0.3 milliampere.

The theory of plasma probes and their use in ion thrusters has been adequately described in literature (refs. 21 and 41) and is repeated here only in summary form. The basic assumption generally used in analyzing ion-chamber probe data is that the electron distribution is composed of monoenergetic primaries superimposed on a Maxwellian background population. This assumption leads to primary and Maxwellian probe currents of

$$J_p = n_p q A \sqrt{\frac{2q \Theta_p}{m_e}} \left(1 + \frac{V}{\Theta_p}\right)$$  \hspace{1cm} (28)

$$J_m = n_m q A \sqrt{q T_m / 2\pi m_e} \exp(V/T_m)$$  \hspace{1cm} (29)

where $n_p$ and $n_m$ are the densities of primary and Maxwellian electrons, $q$ and $m_e$ are the charge and mass of an electron, $\Theta_p$ and $T_m$ are the energy of the primary electrons and temperature of Maxwellian electrons in eV, and $V$ is the probe potential relative to the plasma potential in volts. The range of interest for the probe potential is $-\Theta_p \leq V \leq 0$. For the usual case of $\Theta_p \gg T_m$, a probe potential $V$ approaching $-\Theta_p$ will yield only a linear variation of primary-electron current with probe potential (eq. (28)). This region of nearly linear variation is shown in the plot of sample probe data in figure 11(a) and is approximated by the dotted line. Note that the linear region

$\text{An unpublished analysis by W. R. Kerslake indicated an effective flow factor of about 0.5 for the open area of a SERT II accelerator grid. The thruster used in this study had the same screen and accelerator grid thicknesses and hole diameters and thus should have the same flow factor. The accelerator open area was 50 percent of a 10-cm-diameter beam, so that this factor of 0.5 resulted in an effective sharp-edged orifice area of 0.00196 m}^2.$
Figure 11. - Typical Langmuir probe characteristics.
is actually somewhat curved. This curvature is due to the non-Maxwellian electrons actually having an energy distribution instead of being monoenergetic. The assumption of monoenergetic primaries, though, greatly simplifies the data analysis without departing from a reasonable approximation of the actual probe data. The contribution of the primaries (as approximated by the dotted line) can be subtracted from the measured probe currents to give a corrected current. The uncorrected and corrected probe currents are both shown in the semilogarithmic plot of figure 11(b). It is evident that the lower portion of the corrected curve closely approximates the straight line expected for a Maxwellian distribution. The upper portion of the corrected curve is ideally a horizontal line that indicates the plasma density, and the intersection of the two straight-line segments indicates the plasma potential. In practice, though, a probe potential above plasma potential leads to an enlarged plasma sheath around the probe, so that large positive voltages actually extract electrons from an area larger than the probe surface area. The plasma potential is ideally formed at the intersection of two precise straight-line segments. There is usually some noise in the ion chamber, and the superposition of curves that results while taking steady-state data is the reason customarily given for the rounding that occurs in this region (ref. 164).

RESULTS AND DISCUSSION

The ion-chamber performance data that were obtained without probes are presented first. Then, data for maximum propellant utilization are plotted and compared to the two theories presented earlier. Next, the ion-chamber probe data are presented and used to make a more detailed evaluation of the primary-electron-region approach to maximum propellant utilization. Last, a comparison is made with SERT-II throttling data.

Ion-Chamber Performance

The performance data for five basic ion-chamber configurations are shown in figure 12. Most of the data were obtained with a magnetic-field current of 1 ampere, as indicated earlier. Some of the data, though, were obtained at higher magnetic-field currents and are also included in figure 12. In addition, data for one configuration are included for operation with reverse feed, as opposed to the usual forward feed.

The shapes of the performance curves shown in figure 12 are typical of electron-bombardment thrusters. Each curve has a relatively flat portion below the "knee." The location of the knee and the nearly vertical portion above the knee depend on propellant flow rate. The curves of figure 12 can be used to show the relative importance of
(a) Forward feed, 1-A magnet, 10-cm diameter, 7.2-cm length.

(b) Forward feed, 1-A magnet, 10-cm diameter, 10.8-cm length.

Figure 12. - Ion-chamber performance.
(c) Forward feed, 1-A magnet, 10-cm diameter, 14.4-cm length.

(d) Forward feed, 1-A magnet, 20-cm diameter, 94-cm length.

Figure 12. - Continued.
(e) Forward feed, 1-A magnet, 20-cm diameter, 14.4-cm length.

(f) Reverse feed, 1-A magnet, 10-cm diameter, 7.2-cm length.

Figure 12. - Continued.
(g) Forward feed, 2-A magnet, 10-cm diameter, 7.2-cm length.

(h) Forward feed, 2-A magnet, 20-cm diameter, 9.4-cm length.

Figure 12. - Continued.
(i) Reverse feed, 2-A magnet, 10-cm diameter, 7.2-cm length.

(j) Forward feed, 5-A magnet, 20-cm diameter, 9.4-cm length.

(k) Reverse feed, 5-A magnet, 10-cm diameter, 7.2-cm length.

Figure 12. - Concluded.
the various parameters that were varied. Comparisons of performance for the nearly vertical portions of the curves are adequately covered by subsequent parts of this section. Some comparison of the nearly horizontal portions below the "knee" is also of interest, however, and is covered here. Data for the five different configurations are plotted in figure 13. The neutral flows for these data are equivalent to a current range from 142 to 166 milliamperes (the current that would be measured if each propellant atom carried one electronic charge). This small variation has little effect on the performance below the knee, so that performance in this region can be compared directly. The variation between configurations is small below the knee - only some ±15 percent. In addition, there is no clear trend with ion-chamber volume or surface area. One can conclude that variations in ion-chamber configuration outside of the primary-electron region have no substantial effect on performance below the knee. Comments by Poeschel, Ward, and Knauer (ref. 113) indicate that knowledgeable workers in the ion-thruster field would expect such a result. Also, a ±15 percent variation can be sufficient to meet, or not meet, specific performance goals, and thus may appear quite important.

One might expect a discharge-loss sensitivity to changes in the primary-electron region. This expectation is borne out by the lower losses found at higher magnetic-field currents. The higher magnetic field decreases the losses, of course, by making it more difficult for the high-velocity primaries to reach the anode. The use of reverse feed gives a small further decrease in losses, presumably through a change towards a slightly more uniform distribution of ion production in the primary-electron region. Double-valued ion-chamber performance data were not found, except possibly for a small region at high utilization with high magnetic-field currents. An intermittent short was found in the magnetic-field winding, and the extended double-valued performance data described in an earlier publication (ref. 136) were not encountered after this short was fixed.

**Maximum Propellant Utilization**

The widest range of operation was obtained at a magnetic-field current of 1 ampere. For this field current, though, no clear-cut maximum utilization was found (see figs. 12(a) to (f)). Instead, the utilization above the knee increased slowly with increasing losses. As a somewhat arbitrary choice, the utilization at an ion-chamber loss of 1000 eV per ion was used as a maximum. The use of some other high level of loss would have had no effect on the qualitative results presented and little effect on the quantitative results. Operation at higher magnetic-field strength gave nearly vertical lines for operation above the knee, so a similar arbitrary choice was not needed. For consistency, though, the same 1000-eV-per-ion definition was used.
Figure 13 - Comparison of performance for different ion-chamber configurations. Forward feed, 1-A magnet.

Figure 14 - Maximum-utilization data for 10-cm-diameter ion chambers plotted against residence-time parameter. Forward feed, 1-A magnet.
Having arrived at a definition of maximum utilization, it is now of interest to compare maximum-utilization data with the predictions of the previous analyses. Maximum-utilization data are plotted in figure 14 against the product $J_i l$ (ion-beam current times chamber length) for the three forward-feed 10-centimeter-diameter configurations at 1 ampere magnetic field. The product $J_i l$ is proportional to the residence-time correlation parameter $K_{ji} l$ in equation (14). The data for the three configurations were not correlated by the parameter $J_i l$, inasmuch as the short-chamber data appear to be shifted to the left, and those of the long chamber shifted to the right. Indeed, for the data in figure 14, it is clear that $J_1$ alone would have been a better correlation parameter than $J_i l$. This result should be expected for the highly divergent-field design used in these three configurations, where the primary-electron region is located close to the accelerator system. Older thruster designs, in which the primary-electron region extended the length of the ion chamber, were more suited to the residence-time approach.

Maximum-utilization data are plotted against total propellant mass flow in figure 15(a) for five forward-feed configurations operated at a magnetic-field current of 1 ampere. The un-ionized propellant mass flow was calculated for the data in figure 15(a) and plotted in figure 15(b). This calculation is defined by

$$J_0 \bigg|_{\text{un-ionized}} = (1 - \eta U, \text{max}) J_0 \bigg|_{\text{total}}$$

(30)

From figure 15(b), the maximum-utilization data correspond to a constant un-ionized loss rate equivalent to 52 milliamperes, ±8 percent. This result has considerably less scatter than the previously published maximum-utilization data (ref. 136). The reduced scatter is felt to be due to improved experimental techniques, particularly those techniques associated with the long time constants of the thruster used.

A difference between figure 15 and the results of the earlier portion of this investigation (ref. 136) is the agreement between data with 10- and 20-centimeter chamber diameters. There was poor agreement between data for these two diameters in the earlier results, and the lack of agreement was felt to be due to poor similarity for the region where primary electrons reach the anode. The short 10-centimeter-diameter section of the anode (in the 20-cm-diameter chamber) was only 0.6 centimeter long for the earlier data of the large chamber. This length was increased to 2.5 centimeters for the data presented in this report (see fig. 5) to assure a dimension greater than a primary-electron cyclotron radius. The close agreement of data for the two chamber diameters in figure 15 indicates the reasoning given earlier (ref. 136) for the poor correlation was probably correct.

The effects of a higher magnetic field and reverse feed of propellant are shown in the maximum-utilization data of figure 16. Reverse feed gave slightly higher maximum utilization of propellant, but again indicated a nearly constant loss of un-ionized propel-
Figure 15. - Correlation of maximum utilization with total propellant flow rate. Forward feed, 1-A magnet.

lant, but again indicated a nearly constant loss of un-ionized propellant (about 6 to 14 percent lower than fig. 15). The data for the 2-ampere field current (forward feed) agreed more closely with the data shown in figure 15, but also showed a slightly lower loss of un-ionized propellant (0 to 10 percent lower).

The data for a magnet current of 5 amperes in figure 12 were not included in figure 15. At this high magnet current the discharge generally extinguished before a high emission could be reached. Also, a high impingement current was obtained well below the approximately 150-milliampere limit for lower magnet currents. This latter condition indicated a beam-current profile that was more peaked, presumably because the discharge was concentrated nearer the ion-chamber axis by the high magnetic field.
As a general conclusion, then, a highly divergent-field thruster shows a nearly constant loss of un-ionized propellant at maximum utilization. This result can be obtained from either equation (20) or equation (26) with the proper selection of constants. In agreement with either of these equations of the primary-electron-region approach, the changes outside of the primary-electron region have no significant effect on the loss of un-ionized propellant. Further, even changes that do affect the primary-electron region can have a small effect on this value of propellant loss if the magnetic-field shape is constant (which is substantially true of the 1- to 2-ampere range included in figs. 15 and 16).
Thorough Langmuir-probe surveys have been made of current divergent-field ion-chamber designs at certain selected operating conditions (refs. 97 and 113). The objective in obtaining the probe data of this investigation was not to duplicate the published ion-chamber surveys. Instead, the objective was to take a few selected probe locations and obtain data for a wide range of propellant flow rates and ion-chamber configurations. Probe A (fig. 7) was selected as a representative sample of the primary-electron region. Probe B was located on the "critical field line" that separates the primary-electron region from the rest of the chamber. (The name "critical field line" was apparently first used by King, Poeschel, and Ward, ref. 119.) Probe C was selected as a representative sample of the ion chamber outside of the primary-electron region.

The ion-chamber probe data were obtained at several emission currents for each of several mass flows. Typical data from probe A are shown in figure 17 for one propellant mass flow. The density of Maxwellian electrons first increased with discharge, reached a maximum near the "knee" of the curve for ion-beam current, and then slowly decreased at higher discharge currents. The ratio of primary to Maxwellian electron densities increased continuously with discharge current throughout the range investigated. The electron temperature also increased with discharge current, but much less rapidly.

The probe data were cross plotted to determine ion-chamber parameters for 1000-eV-per-ion condition defined as maximum propellant utilization. For the data in figure 17 the value of 1000 eV per ion is reached at a discharge current of about 2.1 amperes. These cross-plotted values are presented in figure 18. The scatter in the data of figure 18 is to a large extent a measure of the uncertainties involved in obtaining and analyzing ion-chamber probe data. The overall uncertainty was estimated by Strickfaden and Geiler (ref. 21) as being about 30 percent, with most of the error associated with the straight-line assumption of primary-electron contribution. The frequent replacement of probes was necessary because of cathode sputtering and no doubt added to the total scatter. This sputtering problem could have been avoided by using a hollow or oxide cathode. A hollow cathode would have introduced a perturbation in neutral density and thus analytical uncertainty. An oxide cathode would be likely to affect utilization measurements at very high discharge losses through evaporation from ion bombardment.

The temperature of the Maxwellian electrons in the primary-electron region (probe A, fig. 18(a)) averaged about 5 eV, which agrees closely with values obtained previously at lower utilizations (ref. 123). This temperature drops slightly to about 4 eV at the critical field line and is only about 2.5 eV outside the primary-electron region.

The ratio of primary-to-Maxwellian electron densities averages about 0.4 for the primary-electron region (probe A, fig. 18(b)). This ratio drops to about 0.1 for the critical field line. Similar data are not shown for the ion chamber outside the primary-electron region.

40
Figure 17. - Typical variation of performance and probe data with discharge (anode) current. Probe A, 131 mA equiv.
Figure 18. - Ion-chamber probe data for maximum utilization. Symbols same as figures 15 and 16.
electron region (probe C) because the ratio was too low to measure accurately (≤0.02). It should be noted that the primary-to-Maxwellian density ratio in the primary-electron region is well above the ≤0.1 value found previously at more normal operating conditions. This high value is no doubt due to the 1000-eV-per-ion discharge losses associated with figure 18. One should also note that the electron parameters for this high discharge loss indicate that most of the ionization will take place in the primary-electron region, as assumed in the analysis. The mean energy of the primary electrons ranged from about 35 to 40 eV at probe A, ranged from 30 to 35 eV at probe B, and was less than 30 eV at probe C.

The data shown in figure 18 show no significant trends with propellant mass flow or ion-chamber surface area. The use of the constant values of 5 eV for Maxwellian-electron temperature and 0.4 for primary-to-Maxwellian density ratio appears justified for the primary-electron region values of equation (26). These values, together with a value of 0.011 meter for \( V_p/A_p \) (which can be obtained from a magnetic-field map such as shown in fig. 3), give a neutral density of \( 3.11 \times 10^{18} \) per cubic meter. This neutral density, equation (4), an equivalent sharp-edged orifice area of 0.00196 square meter, and an assumed wall temperature of 500 K result in a neutral loss rate equivalent to 56 milliamperes. This value is quite close to the experimentally determined value of 52 milliamperes (fig. 15). This close agreement is well within the possible error of the analytical model and constitutes an independent check on the analytical model.

**Comparison With SERT II Data**

It is of interest to compare the results of this investigation with published data. Probably the most documented thruster of divergent-field design is the one used on the SERT II flight (ref. 110). The SERT II throttling data (ref. 109) were reviewed and found to show the same nearly constant loss rate for un-ionized propellant that was found in this investigation. The comparison was not possible for the full throttling range above 250 eV per ion. But this value was high enough to be in the ''knee'' of the loss curve and thus be substantially proportional to maximum utilization as defined in this report. The un-ionized propellant loss was equivalent to a current range from 45 to 50 milliamperes for 250 eV per ion and a total propellant flow range of 2.5 to 1. (In a private communication with Byers has stated that fig. 6(b) of ref. 109 is incorrect. The utilization at 250 eV/ion and a beam current of 0.20 was close to 0.80.) The level of un-ionized pro-

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4The temperature enters as a square root in eq. (26), so that the possible variation of temperature indicated by fig. 18(a) would enter as less than a linear effect. In a similar manner, the possible variation of primary-to-Maxwellian density ratio would have less than a linear effect over the range of interest (see fig. 4).
pellant loss rate predicted from the theory of this investigation, however, was substan-
tially above the observed equivalent range of 45 to 50 milliamperes. An unusual aspect 
of SERT II ion-chamber operation (with the accelerator system used for the throttling 
data, ref. 109) was for formation of several-volt ridges in plasma potential near the 
anode (refs. 85 and 113). Although the cause of these potential ridges is not clear, their 
presence probably reduced radial ion losses in their vicinity. If one neglects the boundary 
area of the primary-electron region near these ridges, the calculated neutral loss 
becomes much closer to the experimental values. Also, the introduction of propellant 
through the hollow cathode (about one-third of the total propellant flow at SERT II design 
conditions) was a departure from the uniform conditions assumed for the theory derivation. 
Thus, although SERT II data are in good qualitative agreement with the theory of 
this investigation, it is apparently possible to obtain special plasma conditions that will 
affect the quantitative agreement of experimental data with the theory presented in this 
report. There is no evidence for reduced radial ion loss in the present investigation, 
inasmuch as probes A and B had an average potential difference of less than 1 volt.

CONCLUDING REMARKS

The most significant results of this investigation are the analyses of maximum prop-
pellant utilization and the experimental agreement that was obtained with these analyses. 
The significance of these results is in the implied ability to predict maximum utilization 
of new designs from the field shape, and the inverse ability to select field shapes that 
should give high utilization.

The results of this investigation can be expressed simply: the loss rate of un-
ionized propellant at maximum utilization is nearly a constant over a wide range of total 
propellant flow rate. The simplicity of this result permits rapid prediction of total flow-
rate effects from operation at one total flow rate.

In addition to the general design application, the results of this investigation are 
particularly significant for throttled operation of a fixed-configuration thruster. Because 
of variations in available power, many missions require considerable operation at less 
than maximum thrust. Further, to avoid either large power losses or large propellant 
losses, such part-thrust operation should be near the 'knee' of the ion-chamber loss 
curve. This knee will shift substantially in the same manner as maximum propellant 
utilization. Inasmuch as the un-ionized-propellant loss rate will be a larger fraction of 
total flow rate at part-throttle operation, one can expect the most difficult requirement 
for utilization to be at the lowest thrust level to be used. Without any configuration 
changes accompanying thrust reduction, then, a thruster with good part-thrust perfor-
ance would be expected to have very high utilization at full thrust. Good qualitative agreement of these results was found with published SERT II throttling data.

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Cleveland, Ohio, September 17, 1971,
113-26.

REFERENCES


