ANALYTICAL DESIGN
OF SENSORS FOR MEASURING
ATMOSPHERIC TEMPERATURE DURING
TERMINAL PHASE OF PLANETARY ENTRY

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# 16. Abstract
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The results of the parametric study show that inaccurate knowledge of the recovery temperature ratio is the potential source of the greatest error for the sensor designed for the PAET-Earth mission with deployment at Mach number 2. The effects of radiation are negligible for this particular mission. For deployment at Mach number 3, the sensor does not track recovery temperature as well because the temperatures are high and changing rapidly with time. If the sensor wire designed for PAET were shortened by a factor of 2, errors induced by conduction effects would increase by about 2° K. However, if this short sensor were used for the Viking-Mars mission, errors of the order of 50° K would result. Thus, it cannot be assumed that a sensor designed for one mission will be adequate for another.

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**NOMENCLATURE**

- $a$: speed of sound, m/sec
- $A$: cross-sectional area of sensor wire, m$^2$
- $c_P$: specific heat, J/kg °K
- $C$: circumference of sensor wire, m
- $c_P$: pressure coefficient, $\frac{p_L - p_\infty}{q_\infty}$, dimensionless
- $D$: diameter of sensor wire, m
- $F_P$: view factor for planetary radiation, dimensionless
- $F_S$: view factor for solar radiation, dimensionless
- $F_V$: view factor for vehicle-emitted radiation, dimensionless
- $h_C$: convective heat-transfer coefficient, W/m$^2$ °K
- $k$: thermal conductivity, W/m °K
- $L$: length of sensor wire, m
- $m$: parameter defined by equation (15), per m
- $M$: Mach number, $\frac{V}{a}$, dimensionless
- $Nu$: Nusselt number, $\frac{h_C D}{k a}$, dimensionless
- $p$: pressure, N/m$^2$
- $q$: dynamic pressure, $\frac{\rho V^2}{2}$, N/m$^2$
- $Q$: heat-transfer rate, W/m$^2$
- $R$: gas constant for a particular gas, J/kg °K
- $Re$: Reynolds number, $\frac{\rho V D}{\mu}$, dimensionless
- $RTR$: recovery temperature ratio, $\frac{T_R}{T_t}$, dimensionless
- $S$: solar constant, W/m$^2$
\[ \frac{S}{R_B} \] \quad \text{ratio of length measured along forebody surface, from axis of vehicle, to maximum radius of forebody}

t \quad \text{time, sec}

T \quad \text{temperature, } ^\circ \text{K}

V \quad \text{speed, m/sec}

x \quad \text{distance along sensor wire, m}

\alpha \quad \text{absorptance of sensor wire for radiation emitted by a particular source, dimensionless}

\gamma \quad \text{ratio of specific heats, } \frac{c_P}{c_v}, \text{ dimensionless}

\epsilon \quad \text{emittance of a particular source of radiant energy, dimensionless}

\mu \quad \text{dynamic viscosity, N sec/m}^2

\rho \quad \text{density, kg/m}^3

\sigma \quad \text{Stefan-Boltzmann constant, } \text{W/m}^2 \, ^\circ \text{K}^4

\tau \quad \text{time constant, sec}

\text{Subscripts and Special Notation}

\begin{align*}
a & \quad \text{atmosphere} \\
c & \quad \text{convection} \\
L & \quad \text{local} \\
p & \quad \text{planet} \\
R & \quad \text{recovery} \\
s & \quad \text{sensor} \\
S & \quad \text{Sun} \\
t & \quad \text{total} \\
v & \quad \text{vehicle} \\
iv & \quad \text{iv} \end{align*}
$(x, t)$ location $x$ on sensor wire at time $t$

$\infty$ free stream
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SUMMARY

An analytical study was conducted to develop a sensor for measuring the temperature of a planetary atmosphere from an entry vehicle traveling at supersonic speeds and having a detached shock. Such a sensor has been used in the Planetary Atmosphere Experiments Test Probe (PAET) mission and is planned for the Viking-Mars mission. The study specifically considered butt-welded thermocouple sensors stretched between two support posts; however, the factors considered are sufficiently general to apply to other sensors as well. This study included: (1) an investigation of the relation between sensor-measured temperature and free-stream conditions; (2) an evaluation of the effects of the extraneous sources of heat; (3) the development of a computer program for evaluating sensor response during entry; and (4) a parametric study of sensor design characteristics.

The results of the parametric study show that inaccurate knowledge of the recovery temperature ratio is the potential source of the greatest error for the sensor designed for the PAET-Earth mission with deployment at Mach number 2. The effects of radiation are negligible for this particular mission. For deployment at Mach number 3, the sensor does not track recovery temperature as well because the temperatures are high and changing rapidly with time. If the sensor wire designed for PAET were shortened by a factor of 2, errors induced by conduction effects would increase by about 2° K. However, if this short sensor were used for the Viking-Mars mission, errors of the order of 50° K would result. Thus, it cannot be assumed that a sensor designed for one mission will be adequate for another.

INTRODUCTION

An atmospheric temperature sensor was selected as one of the instruments to be flown aboard the Planetary Atmosphere Experiments Test (PAET) vehicle. This vehicle was to enter the Earth's atmosphere at a velocity of 7000 m/sec with the mission of evaluating techniques for measuring atmospheric composition and structure. The temperature sensor was to provide a measurement of free-stream ambient temperature, as a function of altitude in the terminal phases of entry, to an accuracy of 10° K or better. The sensor was to be deployed when the vehicle had slowed, because of drag to about Mach number 2 or 3, after which it was to remain operational until impact. The sensor was positioned on the front face, near the base of the vehicle forebody, and extended beyond the boundary layer but behind the main shock wave.
The sensor selected was a butt-welded thermocouple stretched between two support posts. Its advantages are (1) the wire diameter can be specified to yield a tailormade time response for a specific mission (wires as small as 0.025-mm dia could be used), (2) the temperature at the butt-weld junction can be made independent of support-post temperature by the use of sufficiently long wires, (3) metals usually have a higher reflectance for solar and infrared radiation than do other materials, thus reducing solar and infrared inputs; and (4) the cylindrical configuration of a rolled butt-welded joint is a configuration for which there is much heat-transfer data in the literature.

An analytical study was undertaken as a basis for the design of a butt-welded thermocouple sensor that would yield reliable data. This study included: (1) an investigation of the relation between sensor-measured temperature and free-stream conditions; (2) an evaluation of the effects of extraneous sources of heat; (3) development of a computer program for evaluating sensor response during entry; and (4) a parametric study of sensor design characteristics.

This paper documents the analytical study and illustrates its value. The factors considered and the computer program used are sufficiently general to apply to similar missions. Numerical examples pertain to possible Earth or Mars missions; PAET was to be tested first in the Earth’s atmosphere, and a similar temperature sensor is planned for the Viking-Mars mission.

FACTORS INFLUENCING MEASUREMENT

The measurement of free-stream ambient temperature with a sensor located behind a shock wave is a complex problem. The ambient temperature must be determined indirectly from a measurement of total temperature, which for reference is defined in equation (1) for a gas with constant ratio of specific heat $\gamma$. In the absence of radiation, total temperature is constant across a shock, and therefore the value at the sensor location is the same as in the free stream. Density and velocity vary with position behind a shock, however, and these influence sensor response time and efficiency of conversion of kinetic energy of the gas to thermal energy at the sensor. Thus, it is necessary to know the flow characteristics at the sensor location.

Another problem is that of extraneous heat sources, which can render a measurement meaningless: the Sun, planetary and vehicle infrared radiation, infrared emission of the sensor itself, and conduction through support leads. The importance of these heat sources can be evaluated only by comparing their heat inputs with that from the air stream, and their implications for sensor performance will vary with the particular mission.

In this section, factors that influence measurement are discussed in some detail.
and incorporated into an energy equation for relating free-stream ambient temperature to sensor response. This discussion is general, but numerical values are presented that pertain to butt-welded thermocouple sensors and Earth and Mars missions. The sensor designed and constructed for PAET is shown in figure 1; the direction of flow is perpendicular to the plane of the page. For redundancy, this particular sensor contains three thermocouples mounted in parallel; for analysis, only one wire need be considered. Figure 2 illustrates the blunt-body PAET vehicle and its detached shock wave. This is a shadowgraph of a PAET model in a ballistic range at a Mach number of 3.\(^1\)

Tables 1 and 2 give trajectory and planetary data for the PAET and Mars missions.

**Total Temperature**

Total temperature is the measurement from which free-stream ambient temperature can be deduced. The relation is

\[
T_t = T_\infty \left(1 + \frac{\gamma - 1}{2} M_\infty^2 \right)
\]

The term on the right is the sum of ambient temperature and the temperature increment contributed by kinetic energy of the gas molecules relative to the vehicle. An important consequence of this equation is that a vehicle undergoing rapid deceleration from high Mach numbers will encounter large and rapid changes in total temperature. This is illustrated in figure 3 for Earth and Mars missions. The measurement problem includes the accurate tracking of this rapidly varying total temperature (41° K/sec at \(M = 2\) for PAET).

In the design of the sensor, the free-stream ambient temperature profile and vehicle Mach number are assumed to be known; the total temperature versus time is

\[\text{Figure 2.} \quad \text{Blunt-body PAET vehicle and detached shock wave.}\]

\[\text{Figure 3.} \quad \text{Total temperature versus time for PAET and Viking missions.}\]

\(^1\)Provided by courtesy of Mr. Robert I. Sammonds, Hypersonic Free Flight Branch, Ames Research Center, NASA.
computed from equation (1), and the response of a candidate sensor to that imposed temperature variation is sought.

Flow Conditions at Sensor Location

Values of Mach and Reynolds numbers at the location of the sensor influence the speed and efficiency of sensor response. In the following, variables necessary to evaluate these numbers are defined in terms of free-stream conditions. The definitions were obtained or deduced from reference 1.

Local Mach number can be written:

\[ M_L = \left\{ \left[ \frac{1 + \frac{\gamma - 1}{2} M_\infty^2}{\gamma - 1} \right] \frac{p_{t,L}/p_{t,\infty}}{p_L/p_\infty} \right\}^{1/2} \]  

(2)

where

\[ \frac{p_L}{p_\infty} = 1 + C_p \left( \frac{\gamma}{2} \right) M_\infty^2 \]  

(3)

For \( M_\infty < 1 \)

\[ \frac{p_{t,L}}{p_{t,\infty}} = 1 \]  

(4)

and for \( M_\infty \geq 1 \)

\[ \frac{p_{t,L}}{p_{t,\infty}} = \frac{\gamma + 1}{\gamma - 1} \left[ \frac{\gamma}{2} M_\infty^2 - (\gamma - 1) \right] \]  

(5)

The ratio \( p_L/p_\infty \) depends on vehicle configuration and, for detached shock waves, is not easily or accurately computed. The work presented in this paper for the PAET mission is based upon experimental evaluations of the pressure coefficient \( C_p \) as defined by equation (3). Approximate values may be obtained from modified Newtonian theory: \( C_p = C_{p,t} \cos^2 \theta \), where

\[ C_{p,t} = \frac{[(p_{t,L}/p_{t,\infty}) - 1]/(q_{t,\infty}/p_{t,\infty})}{\tan \theta} \]  

Knowledge of local Mach number permits local temperature to be evaluated. The derivation follows from equation (1) and the constancy of total temperature in subsonic flow and across a shock

\[ T_L = \frac{1 + \frac{\gamma - 1}{2} M_\infty^2}{1 + \frac{\gamma - 1}{2} M_L^2} T_\infty \]  

(6)

Equations (2) and (6) can be used to evaluate local velocity and density:

\[ V_L = M_L a_L = M_L \sqrt{\gamma R T_L} \]  

(7)

\[ \rho_L = \frac{p_L}{R T_L} \]  

(8)
Conversion of Kinetic Energy at the Sensor

Total temperature has two components: the local ambient temperature and the contribution of local kinetic energy of the gas stream. Not all the kinetic energy is converted to heat at the sensor, and thus even under steady-state conditions a sensor will not record true total temperature. This incomplete conversion also implies that the effective temperature for driving a sensor is less than total temperature. The effective temperature for driving heat into a sensor—the temperature it attains when convective heat transfer goes to zero—is termed recovery temperature.

The magnitude of recovery temperature is influenced by sensor shape, size, orientation, Mach number, flow regime (continuum, slip, or free molecule), and, in some cases, the support-post configuration as it affects the flow of gas. Thus, for highest accuracy, a specific sensor should ultimately be evaluated in a wind tunnel under conditions representative of those in which it will be used. For design purposes, however, data reported in the literature can suffice. A good summary of data for cylindrical wires, which rolled butt-welded thermocouples approximate, is given by Baldwin et al. (ref. 2), who concluded that for transverse cylinders in continuum and slip flow, recovery temperature depends primarily on local Mach number and is almost entirely free of Reynolds number dependence for at least $30,000 > Re > 0.10$. This range is compatible with the Earth and Mars missions and possible sensors.

For reference, plots of the ratio of recovery temperature to total temperature

$$RTR = \frac{T_R}{T_t}$$

are given in figure 4 as a function of Mach number ($M \leq 1$). These data pertain to transverse cylinders in continuum slip flow; the data were summarized by Baldwin et al. (ref. 2) from refs. 3 and 4. The Mach number range 0 to 1 is presented here because the flow behind the PAET bow wave at the sensor location is subsonic.

![Figure 4: Values of recovery temperature ratio versus Mach number reported in the literature for Reynolds numbers greater than 250 and for continuum flow.](image)

Heat Transfer Rate to Sensor

The rate at which heat is transferred from an air stream to a sensor can be expressed by

$$Q_c = h_c(T_R - T_s)C \, dx$$

where $h_c$ is the convective heat-transfer coefficient, $C \, dx$ is surface area of sensor, $T_R$ is local recovery temperature, and $T_s$ is sensor temperature. The convective heat-transfer coefficient is a function of sensor shape and size and local flow conditions. Its value is generally presented on a dimensionless plot of Nusselt number versus Reynolds number with Mach number as parameter for a specific sensor shape. The dimensionless plot of reference 2 for transverse cylinders is reproduced in figure 5.
The convective heat-transfer coefficient $h_c$ directly influences speed of sensor response. The relation between time constant and $h_c$ is

$$\tau = \frac{\rho c_p D}{4 h_c} \quad (11)$$

where $\tau$ is the time in which a freely suspended sensor would respond by $1 - e^{-1}$, or 63.2 percent, to a step change in recovery temperature; $\rho$ is sensor density; $c_p$ is sensor specific heat; and $D$ is sensor diameter.

### Extraneous Heat Sources

A sensor of the type considered here cannot distinguish among the heating effects of different sources. Thus, the effects of solar heating are indistinguishable from those of convective heating caused by the gas stream. To ensure that a measurement pertains only to the air stream, effects of all other sources of heat should be evaluated to make certain they are negligible. Sources of heat can be categorized as: (1) radiant sources, which include the Sun, planet, and vehicle; (2) radiant self-emission of the sensor, and (3) conduction through support leads.

The solar heating effects on a sensor can be expressed

$$Q_S = \alpha_S F_S S C \, dx$$

where $\alpha_S$ is the absorptance of the sensor for sunlight, $F_S$ is the view factor or effective portion of sensor exposed to the flux of one solar constant, $S$ is the solar constant at the planet, and $C \, dx$ is surface area of the sensor. For a sensor exposed broadside to sunlight, $F_S$ equals $1/\pi$; view factors are further described in reference 5. Analogously, the heating rates of a sensor due to planetary or vehicle infrared radiation are

$$Q_p = \alpha_p F_p \sigma T_p^4 \, C \, dx$$

and

$$Q_v = \alpha_v F_v \sigma T_v^4 \, C \, dx$$

where $T_p$ and $T_v$ are the temperatures of planet and vehicle. Sensor self-emission is defined as $\varepsilon_s \sigma T_s^4 \, C \, dx$, where $T_s$ is the temperature and $\varepsilon_s$ is the emittance of the sensor.

Conduction effects are caused by the relatively massive support posts that do not rapidly track total temperature. Thus, heat is conducted from the center of the thermocouple wires to the support posts. As a first approximation, conduction effects may be made negligible by means of a formula for the steady-state temperature distribution in a wire anchored at both ends (ref. 6). This formula states that the temperature error at the center of the wire equals the difference between
recovery temperature and support-post temperature divided by \cosh m_L/2, where \( L \) is the length of wire and \( m \) is defined by

\[
m = \sqrt{h_c C / k A}
\]

(15)

In this equation, \( h_c \) is the convective heat-transfer coefficient, \( C \) is the circumference of the wire, \( k \) is thermal conductivity of the wire, and \( A \) is the cross-sectional area of the wire. Equation (15) can be used in designing the wire sufficiently long to make the temperature error negligible.

**ENERGY EQUATION AND COMPUTER SOLUTION**

The factors that influence measurement were incorporated into an energy equation for relating free-stream ambient temperature to sensor response, and the equation was numerically solved by computer. To use the resulting computer program for design purposes, one would insert (1) vehicle trajectory data, (2) a probable atmospheric temperature profile and thermophysical data, and (3) details of sensor design into the program to determine sensor-measured temperature as a function of time. Any of the values can be altered to find the effect on sensor response.

**Energy Equation**

The energy equation pertains to a wire stretched between two support posts, and is a balance of heat terms on incremental lengths of wire \( dx \) as shown in figure 6. The equation considers (1) heat transferred from the air stream, (2) heat conducted along the wire, (3) absorbed sunlight, (4) absorbed infrared radiation from the planet, (5) absorbed infrared radiation from the entry vehicle, (6) sensor-emitted infrared radiation, and (7) changes in heat storage of the sensor. It can be written

\[
\text{(convection + conduction + solar + planet + vehicle)}_{\text{input}} = \Delta T_s (\text{heat storage} + (\text{self emission + conduction})_{\text{output}})
\]

That is,

\[
h_c (T_R - T_s) C \ dx - k A \frac{\partial T_s}{\partial x} + (\alpha_S F_S S + \alpha_p F_p \sigma T_p^4 + \alpha_v F_v \sigma T_v^4) C \ dx
\]

\[
= \rho c_p A \frac{\partial T_s}{\partial t} \ dx + e \sigma T_s^4 C \ dx - k A \left( \frac{\partial T_s}{\partial x} + \frac{\partial^2 T_s}{\partial x^2} \right) dx
\]

(16)

where \( T_s \) is sensor temperature, and \( \rho, c_p, A, \) and \( C \) are sensor density, specific heat, cross-sectional area, and circumference, respectively. Recovery temperature, \( T_R \), is defined by equation (9) and is obtained from a plot such as figure 4. The solar, planet, and vehicle radiation terms are defined in equations (12) through (14). The heat-transfer coefficient \( h_c \) is obtained from a dimensionless plot,
such as figure 5, of Nusselt number versus Reynolds number with Mach number as parameter. Equations (2) through (8) provide means of evaluating these dimensionless numbers. Viscosity or thermal conductivity are evaluated at total temperature where needed.

The sensor wire was subdivided into many incremental lengths $dx$ (fig. 6), and the energy equation was solved for each length, but subject to defined boundary temperatures at the support posts.

**Numerical Solution**

For the numerical solution of the one-dimensional energy equation (16), we first rearrange the equation into the form

$$ \frac{\partial T_S}{\partial t} + a(x) \frac{\partial^2 T_S}{\partial x^2} + b(x,t,T_S)T_S = c(t) \quad (17) $$

where

$$ a(x) = \frac{k(x)}{\rho c_p} > 0 $$

$$ b(x,t,T_S) = \frac{C[h_c(t) + \epsilon \sigma T_S^3]}{\rho c_p A} $$

$$ c(t) = \frac{C \{ h_c(t)T_R(t) + \alpha_S F_S S + \alpha_p F_p \sigma [T_p(t)]^4 + \alpha_v F_v \sigma [T_v(t)]^4 \}}{\rho c_p A} $$

and

$$ T_S = T_S(x,t) $$

The parabolic partial differential equation (17) is quasilinear, since the coefficient $b$ of the nonlinear term is not a function of the derivatives of the dependent variable $T_S$. The solution of this equation is uniquely determined in the semi-infinite strip $R$: $\{0 \leq x \leq L; \ t \geq 0\}$ by specifying the initial and boundary conditions:

$$ T_S(x,0) = f(x) \quad 0 \leq x \leq L $$
$$ T_S(0,t) = g_0(t) \quad t > 0 $$
$$ T_S(L,t) = g_1(t) \quad t > 0 $$ \quad (18)

The analytic solution of the initial boundary-value problem, equations (17) and (18), would specify $T_S$ and its necessary derivatives as continuous functions of the two independent variables $x$ and $t$. A set of mesh points $\{(x_j, t_n): \ x_j = j(\Delta x) \text{ where } j = 0, 1, \ldots, J + 1 \text{ and } \Delta x = L/(J + 1); \ t_n = n(\Delta t), \ n = 0, 1, \ldots \}$ is introduced on the strip $R$. The numerical solution is obtained by replacing the continuous variables by discrete variables at each mesh point $(x_j, t_n)$. 
The Crank-Nicholson finite-difference scheme is used in finding the numerical solution of equations (17) and (18). A description of this scheme, including restrictions for convergence and stability, and an error analysis, are given in reference 7. When the Crank-Nicholson procedure is applied, functions are evaluated at the point \((x_j, t_{n+1/2})\), which is halfway between the known temperature time level \(n\) and the unknown temperature time level \((n + 1)\). For subsequent notational convenience, let \(\phi(x_j, t_n) = \phi_{j, n}\) and \(T_s(x_j, t_n) = T_{s, n}\).

The Crank-Nicholson analogs to the continuous functions are

\[
T_{j, n+1/2} \approx \frac{1}{2} \left( T_{j, n+1} + T_{j, n} \right) \tag{19}
\]

\[
\left( \frac{\partial T}{\partial t} \right)_{j, n+1/2} \approx \frac{1}{\Delta t} \left( T_{j, n+1} - T_{j, n} \right) \tag{20}
\]

\[
\left( \frac{\partial^2 T}{\partial x^2} \right)_{j, n+1/2} \approx \frac{1}{2(\Delta x)^2} \left[ \left( T_{j+1, n+1} - 2T_{j, n+1} + T_{j-1, n+1} \right) \right.
\]
\[
\left. + \left( T_{j+1, n} - 2T_{j, n} + T_{j-1, n} \right) \right] \tag{21}
\]

Substituting equations (19) through (21) into equation (17) and rearranging transforms equation (17) for the time level \((n + 1/2)\) into a system of algebraic equations

\[-u_j T_{j-1, n+1} + v_j, n+1/2 T_{j, n+1} - u_j T_{j+1, n+1} = S_{j, n+1/2} \quad 1 \leq j \leq J \tag{22}\]

where

\[u_j = \frac{\lambda}{2} a_j\]

\[v_j, n+1/2 = 1 + \lambda a_j + \frac{\Delta t}{2} b_j, n+1/2\]

and

\[S_{j, n+1/2} = u_j T_{j-1, n} + (2 - v_j, n+1/2) T_{j, n} + u_j T_{j+1, n} + (\Delta t)c_j\]

The boundary conditions given in equation (18) can be written as

\[T_{0, n+1} = g_0(t_{n+1}) \quad n \geq 0\]

\[T_{J+1, n+1} = g_1(t_{n+1})\]

Equations (22) and (23) form a system of equations in which the coefficient matrix is tridiagonal. The system is readily solved by using the line-inversion algorithm of reference 8, in which the quantities
and
\[
\begin{align*}
    d_j &= \frac{u_j}{v_j} \frac{u_j}{n+1} - u_j d_{j-1} \\
    e_j &= \frac{S_j^* + u_j e_{j-1}}{v_j} \frac{n+1}{n+2} - u_j d_{j-1}
\end{align*}
\]
are computed, where \(d_0 = e_0 = 0;\)

\[
S_1^* = S_0^* + u_1 T_{0,n+1}; S,j^* = S_j^* + u_j T_{j,n+1}
\]

and

\[
S_j^* = S_j^* + u_j T_{j+1,n+1}
\]

The temperature solution for the time level \((n + 1)\) is obtained by backward substitution formulas:

\[
\begin{align*}
    T_{j,n+1} &= e_j \\
    T_{j,n+1} &= d_j T_{j+1,n+1} + e_j
\end{align*}
\]

In figure 7, the centering point for the difference equations is indicated by +. The circles in the stencil represent the mesh points where the temperature values are determined.

The unknown temperature \(T_{j,n+1}\) required to calculate \(b_j,n+1/2\) in equation (22) is initially predicted to be equal to \(T_{j,n}\) and the solution \(T_{j,n+1}\) is obtained as described above. The value \(T_{j,n+1/2}\) is corrected by averaging \(T_{j,n}\) and \(T_{j,n+1}\), and a new iterated solution \(T_{j,n+1}\) is found. This process of iterating over a time step is continued until the relative error of two successive solutions is within a prescribed tolerance.

The restriction on the time increment (ref. 7) for convergence and stability of the Crank-Nicholson finite difference scheme is

\[
\Delta t \leq \frac{2(\Delta x)^2}{2a(x) + (\Delta x)^2 b(x,t,T\bar{s})}
\]

Keller (ref. 7) also shows that for a linear analog the error \(e_j,n\) between the true solution and the approximate solution obtained using the Crank-Nicholson method has a second-order bound

\[
|e_j,n| \leq o((\Delta x)^2) + o((\Delta t)^2)
\]

The numerical method was coded in Fortran IV(G) using the IBM 360/67 at Ames Research Center.
PARAMETRIC STUDY

The computer program was used to evaluate the effects of various parameters on the response of a sensor mounted on the PAET or Viking vehicles and flown in proposed Earth and Mars trajectories (tables 1 and 2). The method was to vary the value of one parameter at a time and observe the effects on the sensor time-temperature history. The effects of (1) sensor diameter, (2) sensor length, (3) sensor thermal conductivity, (4) recovery temperature ratio, (5) solar radiation, (6) vehicle-emitted infrared radiation, and (7) time of deployment were studied.

The sensor consisted of a butt-welded chromel-alumel thermocouple wire suspended between two support posts (fig. 1). The physical appearance of the weld was that of a continuous piece of wire. The wire was 0.0127 cm (0.005 in.) in diameter, and 1.4 cm long. The chromel end of the wire was spot-welded to a chromel support post, and the alumel was welded to an alumel post. The remainder of the electrical circuit was not specifically considered, but was assumed to be standard thermocouple measuring circuit. The sensor was mounted near the outer edge of the forebody, $S/R_B = 0.985$ for PAET and 0.925 for Viking, and was oriented normal to the air flow. It was assumed to be housed inside the entry vehicle until a predetermined Mach number was reached, at which time it was deployed beyond the boundary layer.

PAET-Earth Mission

The Earth-entry computer solutions were initiated, with one exception, when the entry vehicle had slowed to a Mach number of 2. The sensor on PAET was to be deployed at this Mach number. The values assigned to the various parameters in the computer solutions are given in table 3. In addition to these, (1) recovery temperature ratios were obtained from Scadron and Warshawsky’s data (ref. 4), plotted in figure 4; (2) heat-transfer coefficients were obtained from figure 5; (3) pressure coefficients, $C_p$, were obtained from experimental data, figure 8; (4) support-post temperatures were obtained from a computer solution of freely supported posts at flow conditions corresponding to the sensor location, figure 9; and (5) surface temperatures of the vehicle forebody, which radiates to the sensor, were obtained from predictions, figure 10.
Figure 10. – Forebody temperature, near the sensor, versus time.

The time response of the 0.0127-cm-dia sensor to be flown on PAET is illustrated in figure 11(a). The response curve corresponds to computer run 1 in table 3, and represents the nominally expected values of the various parameters. This figure is a plot of sensor temperature versus time, with time beginning at the instant of deployment and continuing to 30 sec. This time span is considered illustrative of the problems of measurement. In actual flight, measurements will be made over a longer time. The dashed curve represents recovery temperature, which is the temperature directly available for driving convective heat into the sensor.

The sensor temperature is seen to increase rapidly after deployment, where its initial temperature is 300° K, and in 0.4 sec reaches recovery temperature. Thereafter, however, the sensor lags this temperature because of its own thermal mass and because vehicle deceleration causes the recovery temperature to fall rapidly. At \( t = 1 \) sec, the difference between sensor and recovery temperatures is 6° K; at \( t = 6 \) sec, 3° K; and at \( t = 30 \) sec, less than 1° K. Thus the maximum difference occurs at about 1 sec, and thereafter continually decreases with time. The useful measurement period begins at \( t = 0.4 \) sec, when \( M_\infty = 1.92 \) and the altitude is 30.2 km.

Figure 11(a) also illustrates the effect of sensor diameter on response. The curve labeled \( D/5 \) is for a 0.00254-cm (0.001-in.)-dia sensor, and the one labeled \( 2D \) is for a 0.0254-cm (0.010-in.)-dia sensor. These correspond to computer runs 2 and 3 in table 3. The smaller sensor has a decided advantage in speed of response and overall accuracy. It reaches recovery temperature in about 0.1 sec, and thereafter its temperature difference with respect to recovery temperature is less than 1.5° K. The larger sensor has a very slow time response, requiring almost 0.8 sec to reach
recovery temperature. It has a maximum difference of $10^\circ$ K, and this only slowly decreases with time. The reasons the intermediate size sensor was selected for the PAET mission are that its time response was adequate for objectives, and that it was considerably more rugged, for handling purposes, than the smaller one.

The effects of varying the length and thermal conductivity of the sensor are illustrated in figure 11(b). Three lengths of wire — corresponding to $L$, $L/2$, and $2L$ — and the case of zero thermal conductivity were considered. The purpose of these studies was to evaluate how closely the various lengths of wire correspond to the ideal situation of an infinitely long wire, or zero thermal conductivity. Thus, in this figure, the zero thermal conductivity case is considered ideal. At about 0.4 sec after deployment, the difference between the ideal case and the other sensors is a maximum. The maximum difference is about $8^\circ$ K and depends on sensor length. The reason for these large temperature differences is that the wire rapidly responds to the high recovery temperature, but the more massive support posts do not respond so fast, with the consequent loss of heat by conduction to the support posts. Fortuitously, however, the $L/2$ sensor would fall closer to true recovery temperature for relatively early times. At later times, the temperature of the $L = 1.4$-cm sensor is effectively that of an infinitely long sensor wire.

The effects of solar, vehicle-emitted, and sensor-emitted radiation on the accuracy of measurement are illustrated in figure 11(c). Each radiation level was assigned a value of zero, corresponding to computer runs 7, 8, and 9 in table 3, and these were compared with the response curve for the nominally expected radiation levels (computer run 1). The responses for zero values of solar and sensor-emitted radiation were so nearly identical to those
for the nominally expected levels that for the most part these curves are shown as one. The relation of one to the other is shown slightly exploded at about 0.4 sec where the small differences start to appear (the actual total spread of the four curves at \( t = 0.4 \) sec was found to be only 1.6° K). The largest error was for the case of zero vehicle radiation, but even this error was less than about 1° K. It can be concluded that for the PAET mission, and deployment at Mach number 2, the influence of radiation on measurement is negligible.

Figure 11(d) illustrates the effects of varying recovery temperature ratio. The cases of \( RTR = 1 \) (computer run 10) were compared with those for \( RTR \) from figure 4, ref. 4 (computer run 1). The effect is quite large, amounting to the order of 10° K, and only slowly decreases with time. The reason for this behavior can be deduced from figures 4 and 12. Figure 12 shows that local Mach number (at the sensor location behind the shock) is fairly constant but does slowly decrease with time. When the free-stream Mach number is 1 or 2, the local Mach number is only about 0.65. It can be seen from figure 4, that at Mach 0.65, \( RTR \sim 0.975 \). Thus, the difference between the two response curves at early times after deployment amounts to about 0.025 of total temperature, or approximately 10° K. Since local Mach number decreases only slowly with time, the temperature error too will decrease only slowly. Consequently, it is important to accurately know the value of the recovery temperature ratio.

The corresponding computer runs for deployment of the sensor at Mach number 3 during the PAET-Earth mission are illustrated in figures 13(a)-(d), which have a time scale going to 4 sec after deployment. Note that the Mach number decreases to 2 at about \( t = 3 \) sec. These figures illustrate that error of measurement in the first 3 sec
would be twice that for the Mach 2 deployment. The basic reason is that total and recovery temperatures are higher, and changing much more rapidly than at Mach number 2 (fig. 3), which influences the ability of the sensor to track the change. It can be seen that the difference between recovery temperature and sensor temperature for the 0.0127-cm wire, at a time of 1 sec, is about 12° K. For the 2D case, the error approaches 22° K. The influence of sensor length is more critical than before because of the increased temperature difference between the center of the sensor wire and support posts. Errors of the order 7° K result. The effects of radiation are again small, but larger than for Mach 2. The corresponding comparison of recovery temperature ratios produces an error of about 0.025 total temperature, or about 14° K. Thus the tracking ability of the sensor is degraded above Mach number 2.

Viking-Mars Mission

An abbreviated form of the computer program was used for the Viking-Mars study. First, local Reynolds numbers at the sensor location were input to the computer (fig. 14); these numbers were used because experimental values of pressure coefficient $C_p$ were not available, but Reynolds numbers were available from a flow-field study. Second, Mach number effects on heat-transfer coefficients (fig. 5) were neglected, and all values were computed at an arbitrary Mach number of 0.65. (It will be recalled that flow at the sensor location is always subsonic.) Third, Mach number effects on recovery temperature ratios (fig. 4) were neglected, and all ratios were arbitrarily taken as 1.0. Fourth, the temperatures of the support posts were assumed to be constant. The values assigned to the various parameters are listed in table 4; the temperature of the vehicle
forebody, which radiates to the sensor, is illustrated in figure 10. The sensor Reynolds numbers, local Mach number, heat-shield temperatures, and other parameters of the flow for these calculations were provided by Mr. H. C. Norman of Martin Marietta Corporation from results obtained with a flow-field computer program.

The results of the parametric study are shown in figures 15(a)-(c) for deployment at Mach number 3. A 6-sec time span was selected as illustrative of the measurement problems. The response of a PAET sensor deployed during the Viking-Mars mission, is shown in figure 15(a); \( D = 0.0127 \text{ cm} \). It reaches the recovery temperature in about 1.5 sec and thereafter tracks it quite well, differing by only about 1° K. Conduction effects for the selected support-post temperature of 300° K are just sufficient to counterbalance the lag in the sensor temperature. The response of sensors having \( D/5 \) and \( 2D \) diameters is also shown. The \( D/5 \) sensor responds in less than 0.1 sec and thereafter tracks recovery temperature within 1° K. The \( 2D \) sensor, however, responds very slowly and after 3 sec has errors of the order of 12° K.

Figure 15(b) shows that the sensor selected for the PAET mission is not quite long enough to eliminate conduction effects for the Viking-Mars mission; if the sensor were shortened by a factor of 2, temperature errors of the order 45° K would result. Because of conduction effects, the sensor temperature will be influenced by the specific values of support-post temperatures.

The effect of radiation on measurement accuracy is shown in figure 15(c). Solar radiation has nominally no effect due to the long distance of Mars from the Sun. Sensor self-emission and vehicle forebody
radiation each produce errors of the order $1^\circ$ K, and in opposite directions, so these effects tend to cancel one another.

Deployment at Mach number 4 is illustrated in figures 16(a)-(c). The PAET sensor and the $D/5$ diameter sensor track recovery temperature quite well, but the $2D$ sensor has errors of the order $16^\circ$ K. The effect of sensor length is very prominent, and the $L/2$ sensor would produce errors of the order $60^\circ$ K. Figure 16(c) shows that the effect of sensor self-emission is about $4^\circ$ K.

Figure 15. — Concluded.

Figure 16. — Response of sensors deployed at $M_\infty = 4$ during Viking-Mars mission.
An analytical study, such as the one described here, must be conducted to define the behavior and evaluate the accuracy of an atmospheric recovery-temperature sensor to be used for specific atmospheric-measurement missions. The following mission-specific factors, shown to influence the sensor design and response were included in the analysis: the relation of free-stream conditions to local Mach and Reynolds numbers at the sensor location, the heat-transfer characteristics between the sensor and the atmosphere, and extraneous heat sources such as conduction and radiation. The computer program developed for this study should be valuable for analyzing the behavior of sensors for future missions.

For the sensor selected to be flown on PAET and deployed at Mach number 2, the potential source of greatest error is an inaccurate knowledge of the recovery temperature ratio. The effects of radiation are negligible, and the sensor was designed to minimize conduction effects. For deployment at a higher Mach number (3), the sensor does not track recovery temperature as well because the temperature is higher and changes more rapidly with time. At these higher temperatures, errors in the recovery temperature ratio also produce larger errors in the deduced ambient temperature. Deployment at Mach number 3 approximately doubles the measurement error (during the increased time of measurement).

If a sensor similar to that designed for PAET, but having only half the wire length, were used for the Viking-Mars mission, the resulting errors due just to conduction effects would be of the
order 45° to 60° K. Thus, one cannot assume that a sensor proved adequate for one mission will be adequate for another.

Ames Research Center
National Aeronautics and Space Administration
Moffett Field, California 94035, April 10, 1972

REFERENCES


BIBLIOGRAPHY


### TABLE 1 – TRAJECTORY AND PLANETARY DATA FOR PAET-EARTH MISSION

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### TABLE 2 – TRAJECTORY AND PLANETARY DATA FOR VIKING-MARS MISSION

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*1 Ballistic entry with entry velocity of 4,570 m/sec (15,200 ft/sec) ballistic coefficient of 47 kg/m² (0.3 slug/ft²), and an entry path angle 16° below the horizontal.*
## TABLE 3 – VALUES OF PARAMETERS USED IN COMPUTER PROGRAM FOR PAET-EARTH STUDY

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TABLE 4 – VALUES OF PARAMETERS USED IN COMPUTER PROGRAM FOR VIKING-MARS STUDY

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<td>Absorptance for vehicle radiation</td>
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<td></td>
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<td>Absorptance for planet radiation</td>
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<td>0.40</td>
<td>Absorptance for vehicle radiation</td>
<td>0.14</td>
<td>Absorptance for vehicle radiation</td>
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<tr>
<td></td>
<td>View factor for sunlight</td>
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<td></td>
<td>View factor for planet radiation</td>
<td>0.50</td>
<td>0</td>
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<td>View factor for vehicle radiation</td>
<td>0.50</td>
<td>View factor for vehicle radiation</td>
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<td></td>
<td>Specific heat, J/kg °K</td>
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<td>Thermal conductivity, chromel, W/m °K</td>
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<td>Thermal conductivity, alumel, W/m °K</td>
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<td></td>
<td>Density, kg/m³</td>
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<td>Support post temperature, °K</td>
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<td>0</td>
<td>300</td>
<td>Recovery temperature ratio</td>
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<td>Planet</td>
<td></td>
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<td></td>
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<td></td>
<td>Distance from Sun, AU</td>
<td>1.52</td>
<td>1</td>
<td>1.52</td>
<td>1</td>
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NASA-Langley, 1972 — 14 A-4412
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