ENERGY DISTRIBUTION FUNCTIONS
OF KILOVOLT IONS PARALLEL AND
PERPENDICULAR TO THE MAGNETIC FIELD
OF A MODIFIED PENNING DISCHARGE

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NATIONAL AERONAUTICS AND SPACE ADMINISTRATION • WASHINGTON, D. C. • FEBRUARY 1973
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SUMMARY

The distribution function of ion energy parallel to the magnetic field of a modified Penning discharge has been measured with a retarding potential energy analyzer. These ions escaped through one of the throats of the magnetic mirror geometry. Simultaneous measurements of the ion energy distribution function perpendicular to the magnetic field have been made with a charge-exchange neutral detector. The ion energy distribution functions are approximately Maxwellian, and the parallel and perpendicular kinetic temperatures are equal within experimental error. These results suggest that turbulent processes previously observed in this discharge Maxwellianize the velocity distribution along a radius in velocity space and cause an isotropic energy distribution. The kinetic temperatures observed are of the order of kilovolts, and the tails of the ion energy distribution functions are Maxwellian for up to a factor of 7 e-folds in energy. When the distributions depart from Maxwellian, they are enhanced above the Maxwellian tail. Above densities of about $10^{10}$ particles per cubic centimeter, this enhancement appears to be the result of a second, higher temperature Maxwellian distribution. At these high particle energies, only the ions perpendicular to the magnetic field lines were investigated.

INTRODUCTION

Previous investigations of a modified Penning discharge (ref. 1) revealed ions with approximately Maxwellian velocity distributions and kilovolt kinetic temperatures. The diagnostic instrument used to measure the energy distribution of ions parallel to the magnetic field lines was a retarding potential analyzer, located outside one of the mag-
netic mirrors. The data reduction procedures and experimental results from an extensive series of measurements with the retarding potential energy analyzer have been reported elsewhere (ref. 2).

In view of the possible application of the modified Penning discharge to a steady-state plasma heating scheme for fusion research, it is desirable to confirm independently the high ion kinetic temperatures and Maxwellian velocity distribution observed in the ions lost along the magnetic-field lines. This report describes an investigation in which the parallel and perpendicular ion energy distribution functions were simultaneously measured for 163 experimental runs taken under a range of operating conditions. Such simultaneous measurements have not been reported in the literature of Penning discharges, although Konstantinov, Myskin, Sorokin, and Tsel'nik (ref. 3) have measured the energy of charge-exchange neutrals from the midplane of a modified Penning discharge. In the investigation described in this report, a charge-exchange neutral detector was used to measure the perpendicular ion energy, while simultaneous observations of the parallel ion energy were made with the retarding potential energy analyzer.

Characteristics of Modified Penning Discharge

The operating characteristics of the discharge have been described in references 1 and 4; a detailed description of the superconducting magnet facility in which the discharge is operated is described in reference 5; and some of the physical processes responsible for ion heating are discussed in reference 6. An isometric cutaway drawing of the experimental configuration is shown in figure 1. The plasma is approximately 15 centimeters in diameter at the midplane. The magnetic field consists of a magnetic mirror with a 2.62:1 mirror ratio generated by two superconducting coils, the Dewars of which are approximately 18 centimeters in diameter at the magnetic mirror throats. The magnet system shown in figure 1 is located in a vacuum tank 1 meter in diameter and approximately 2 meters long and gives very good experimental and visual access to the experimental volume. The parallel Dewars on either side of the experimental volume are at liquid-nitrogen temperature. The anode ring is operated at positive potentials up to 35 kilovolts with respect to the walls of the vacuum tank, and the electrical circuit to the power supply is completed by ions which impinge on the grounded tank walls.

The experimental investigation consisted of 163 runs taken with deuterium gas. The maximum value of the magnetic field was 1 tesla at the magnetic mirror throats and 0.38 tesla at the midplane, in the vicinity of the anode rings. From previous measurements taken with a Langmuir probe at the throat of the mirror (ref. 6), the electron temperature is known to be approximately 50 eV, within a factor of 2, in this plasma.
Figure 1. - Isometric cutaway drawing of modified Penning discharge and superconducting magnetic mirror facility. Approximate locations of retarding potential energy analyzer and of fast neutral energy analyzer are shown schematically.
This is as much as an order of magnitude below the ion temperature at the same operating conditions. Any atomic deuterium generated in the plasma volume has ample opportunity to recombine on the walls before it can return to the experimental volume, as a result of the long mean free paths for binary collision processes. Because of the rather large vacuum-tank wall area and the cold liquid-nitrogen surfaces on either side of the plasma volume, it is unlikely that a significant population of atomic deuterium can exist in the plasma. For this reason it was assumed that the neutral background gas consisted of molecular deuterium gas. The principal ionized species within the plasma was taken to be ionized deuterium atoms $D^+$. It is believed that $D^+$ dominated the plasma because investigation of the spectrum of electrostatic potential fluctuations yielded a peak at the ion cyclotron frequency of $D^+$ (when such a peak could be observed), and peaks were absent or much fainter by comparison at the ion cyclotron frequency appropriate to ionized molecular deuterium $D_2^+$.

The 163 experimental runs spanned a range of the positive anode voltage from 5 to 35 kilovolts and neutral background pressures $p_0$ from $3.9 \times 10^{-5}$ to $12.0 \times 10^{-5}$ torr, where the neutral deuterium pressure has been corrected for the gage factor of this apparatus. It was estimated from previous work (ref. 6) that the ion density at the mid-plane of the modified Penning discharge ranged from approximately $10^9$ to $6 \times 10^{10}$ particles per cubic centimeter in this investigation.

**Diagnostic Instruments**

The ion energy distribution function was measured by two nonperturbing diagnostic techniques, one parallel to the magnetic-field lines, and the other perpendicular to the magnetic-field lines. In figure 2(a) is a schematic drawing of the retarding potential energy analyzer used to measure the parallel distribution function of ions leaving the plasma through the magnetic mirror throat. The analyzer was located approximately 20 centimeters outside the magnetic mirror throat and 10 centimeters from the magnetic axis. The analyzer was parallel to the local magnetic-field line and measured the parallel component of the ion energy. The raw data, taken on an X, Y-recorder, represented an integrated ion energy distribution function. A computer program determined, by iteration, the integrated Maxwellian distribution which best fit the raw data, in the sense of minimizing the mean square error between the logarithms of the best-fitting distribution and of the raw data. Using the logarithm of the value of the data point rather than the actual value of the data point tended to give approximately equal weight to all portions of the data curves. By comparing the best-fitting computer solution to the raw data, one may assess the extent to which the raw data are Maxwellian by observing the extent to which the best-fitting curve is also a good fit. The principal source of error for this application of the retarding potential energy analyzer is in the iterative procedure used.
(a) Retarding potential energy analyzer, located approximately 4 centimeters from plasma axis and 20 centimeters outside magnetic mirror throat.

(b) Schematic drawing of charge-exchange neutral detector. Line of sight of the detector was tangent to sheath between plasma and anode ring approximately 6 centimeters below magnetic axis.

Figure 2. Apparatus for measurement of parallel and perpendicular ion energy distribution functions.
to reduce the data, which sometimes does not converge to the proper kinetic tempera-
ture. (This was determined by obtaining a best fit to "pseudodata," an integrated Max-
wellian of specified kinetic temperature.) These convergence problems give rise to
errors in the parallel-ion kinetic temperature which may be as high as 20 percent. The
analytical theory, error analysis, and experimental application of the retarding poten-
tial energy analyzer are discussed in reference 2.

The charge-exchange neutral detector used in these investigations is a geometric
duplicate of that developed at Fontenay-aux-Roses (ref. 7). The particle detector elec-
tronic system was developed at the NASA Lewis Research Center. A schematic showing
this instrument and its location with respect to the plasma is presented in figure 2(b).
The retarding potential energy analyzer and the neutral detector were positioned to
sample the anode sheath, approximately 1 centimeter from the inner circumference of
the anode ring. Fast ions in the sheath between the plasma and the anode ring charge
exchange on the background of neutral molecular deuterium gas, and the resulting fast
deuterium atoms then move along straight lines to the walls of the vacuum vessel. In
the neutral detector, some of the fast neutrals pass through a series of slits and are
reionized by a nitrogen gas cell, which is maintained at pressures of approximately
0.10 torr. The reionized fast particles then pass through additional focusing slits into
a set of 90° electrostatic deflector plates. The energy of the ions which may pass
through the 90° deflector plates is determined by the potential applied across them. By
changing the voltage applied between the deflector plates, one may sweep out the energy
distribution function of the reionized particles. The ions are passed through a second
series of slits and impinge on a photomultiplier detector, which counts individual par-
ticles.

The particle flux at the photomultiplier is only indirectly related to the ion distribu-
tion function inside the confined plasma. To obtain the original ion distribution function,
one must correct for the charge-exchange process of atomic deuterium ions on molecu-
lar deuterium,

\[ \text{D}^+ + \text{D}_2 \rightarrow \text{D}_2^+ + \text{D}^0 \]

One must also correct for the reionization cross section in the nitrogen gas cell and for
the energy resolution of the electrostatic analyzer. The flux \( I(V) \) of individual particles
reaching the photomultiplier (see the appendix) may be written

\[ I(V) = C_0 n_a n_n \sigma_x (V) v_1 f(V) k(V) g_a (V) \]  \hspace{1cm} (1)

where \( V \) is the ion energy in electron volts, \( C_0 \) is a geometrical and dimensional con-
stant, \( f(V) \) is the desired ion energy distribution, \( k(V) \) is the reionization probability of
atomic deuterium in a nitrogen gas cell, and \( G_a(V) \) is a correction for the energy resolution of the analyzer and results from the fact that the relative energy resolution \( dV/V \) is independent of energy. Thus, the energy resolution involves correction by a factor

\[
G_a(V) \sim V
\]

The factor \( n_1n_0\sigma_x(V)v_i \) is the number of charge-exchange reactions per cubic centimeter per second in the volume sampled by the analyzer, \( n_1 \) and \( n_0 \) are the ion and neutral number density, respectively, and \( v_i \) is the deuterium ion velocity. The charge-exchange cross section \( \sigma_x(V) \) is available in reference 8 and is known from 70 eV \( \leq V \leq 200 \) keV. The correction factor \( k(V) \) for the nitrogen gas cell is known for energies over the range 2 \( \leq V \leq 100 \) keV and is

\[
k(V) \sim V^{0.56}
\]

over this range (refs. 7 and 8).

One may convert the raw data for \( I(V) \) to the distribution function of ion energy in the plasma \( f(V) \) by using equations (1) to (3) to obtain

\[
f(V) = \frac{C_1I(V)}{V^{2.06}\sigma_x(V)}
\]

where \( C_1 \) is a constant for the apparatus. The ion energy distribution function obtained from equation (4) was used as input to a computer program which obtained a Maxwellian distribution with a least-squares best fit to the experimentally determined ion energy distribution \( f(V) \). Because the correction factor \( k(V) \) was not known for nitrogen gas below 2 kilovolts, raw data below 2 kilovolts were not utilized in obtaining the best-fitting Maxwellian distribution. The principal error in applying the neutral detector arose from establishing the zero level and rounding off errors in reading the raw data. These errors, combined with uncertainties in the charge-exchange cross sections, may have introduced an error of as much as 10 percent in determining the perpendicular ion kinetic temperature.

**EXPERIMENTAL RESULTS**

In figure 3 is shown a characteristic example of data which were taken simultaneously with the retarding potential energy analyzer and the charge-exchange neutral detector. The anode voltage was 8 kilovolts, and the neutral background gas pressure was
5.2×10⁻⁵ torr of deuterium. Figure 3(a) is the energy distribution function measured with the charge-exchange neutral detector, corrected with equation (4), and plotted as a function of energy on a semilogarithmic graph. The corrected raw data are indicated by the round symbols, and the Maxwellian distribution which best fits these raw data is indicated by the triangular symbols. In figure 3(b) is shown the integrated energy distribution function measured with the retarding potential energy analyzer. The round
symbols are the corrected raw data, and the triangular symbols are the best-fitting integrated Maxwellian distribution. Figure 3(a) gives a perpendicular component of the ion kinetic temperature, \( V_\perp = 620 \text{ eV} \), and figure 3(b) a best-fitting parallel kinetic temperature, \( V_\parallel = 559 \text{ eV} \). It is characteristic in figure 3 that both the parallel and perpendicular ion energy distribution functions are approximately Maxwellian, that the Maxwellian tail of the neutral detector data extends over approximately seven \( e \)-folding lengths in energy, and that the parallel and perpendicular ion energies are approximately equal within the scatter in the data of the two diagnostic methods employed.

In figure 4 is a second example of the perpendicular and parallel ion energy spectra, under conditions which yielded kinetic temperatures of nearly 2 kilovolts. The operating conditions were an anode voltage of 35 kilovolts, and a neutral background gas pressure of \( 4.3 \times 10^{-5} \) torr of deuterium. In figure 4(a) is the neutral detector spectrum with a best-fitting perpendicular kinetic temperature of \( V_\perp = 1942 \text{ eV} \). In figure 4(b) is the retarding potential data, with a best-fitting parallel kinetic temperature of \( V_\parallel = 1705 \text{ eV} \). The knee in the latter data indicates that the magnetic-field line on which the retarding potential analyzer was located was floating at a positive potential of \( V_f = 2200 \) volts, an unusually high value for this experiment, but only 6 percent of the applied anode voltage. Figures 3 and 4 are characteristic in that it was possible, because of instrument limitations, to take valid data at higher energies with the neutral detector than with the retarding potential energy analyzer.

Ion energy distributions analogous to those shown in figures 3 and 4 were obtained for all 163 runs. Temperatures obtained from the best-fitting Maxwellian distributions are shown in figure 5. On the small number of occasions for which a two-temperature Maxwellian distribution was observed with the neutral detector, the lower of the two kinetic temperatures was plotted in figure 5. On the abscissa is the kinetic temperature derived from the parallel component of ion energy, measured with the retarding potential energy analyzer. On the ordinate is the kinetic temperature derived from the perpendicular component of ion energy measured with the charge-exchange neutral detector. There is approximate agreement of the parallel and perpendicular components of the ion kinetic temperature over the range of data taken.

The agreement of \( V_\perp \) with \( V_\parallel \) and the degree of data spread may be estimated by fitting the data in figure 5 to the relation

\[
V_\perp = C_2 V_\parallel
\]  

and obtaining the median and relative standard deviation of \( C_2 \). In figure 6, the cumulative probability of \( C_2 \) for 163 runs is plotted on probability coordinates. The author's best estimate of the Gaussian distribution to the data is indicated by the straight line.
The median value of \( C_2 \), \( \bar{C}_2 \), is the intersection of the best-fitting straight line with the 50 percent line,

\[ \bar{C}_2 = 1.04 \]  

which implies that the perpendicular energy is slightly higher than the parallel energy. The relative standard deviation of the data population, the horizontal distance between the intersection of the best-fitting straight line with the median and the one standard deviation lines, was approximately

\[ \Delta C_2 = \frac{\delta(C_2)}{C_2} = 0.26 \]  

Thus, the parallel and perpendicular ion kinetic temperatures are equal to within the estimated experimental error. The parameter \( C_2 \) was plotted as a function of the independent variables (anode voltage and neutral gas pressure) for the 163 runs, and no systematic trend of \( C_2 \) was observed. The same physical process which is responsible for making \( C_2 \) a fixed constant apparently operates over the entire range of parameters investigated.

Two general types of anomalous ion energy distributions were observed in the perpendicular ion energy distribution function. Both were characterized by an increase of
the observed distribution function above the best-fitting Maxwellian value in the tail of the distribution. This enhancement of the Maxwellian tail assumed two forms. One of these was a two-temperature Maxwellian distribution, in which the Maxwellian tail was dominated by a hotter component of lower density that gave the type of ion energy distribution function illustrated in figure 7. Two-temperature distributions were observed only at plasma densities above approximately $10^{10}$ particles per cubic centimeter. This two-temperature Maxwellian distribution apparently results from the analyzer sampling two separate regions with different ion kinetic temperatures.

![Graph](image)

Figure 7. - Example of two-temperature Maxwellian distribution observed with neutral detector at ion number densities above about $10^{10}$ per cubic centimeter. Anode voltage, 10 kilovolts; background pressure, $7.8 \times 10^{-5}$ torr of deuterium gas.

Two-temperature Maxwellian distributions may also occur as a result of a population of hot impurities superimposed on the distribution function of the principal species. Such impurities, with each species having a distinct ion temperature, have been described by Stirling (ref. 9). This explanation is unsatisfactory for the present experiment, however, since observation of the Penning discharge plasma with a bench spectrometer revealed no detectable impurity lines. Ion energy distributions similar to figure 7 have been reported by Artsimovich (ref. 10) in connection with the Tokamak series of experiments. Artsimovich reported that two-temperature Maxwellian distributions occurred in the Tokamak at number densities below $10^{12}$ particles per cubic centimeter.
A second anomalous departure from the Maxwellian distribution was observed in approximately a dozen cases, at higher neutral gas pressures. This departure is illustrated in figure 8 and shows an ion energy distribution function with a bump on the Maxwellian tail at an energy which roughly corresponds to the voltage applied to the anode ring. Such a distribution function may be due to physical processes in the weak plasma penumbra which surrounds the modified Penning discharge.

![Corrected raw data Best-fitting Maxwellian with V⊥ = 936 eV](image)

**Figure 8.** Example of ion energy distribution function, measured with neutral detector, with a bump on the Maxwellian tail. Anode voltage, 11 kilovolts; background pressure, 1.2x10⁻⁴ torr of deuterium gas.

**DISCUSSION OF RESULTS**

The present investigation has demonstrated generally good agreement between the parallel and perpendicular kinetic temperatures observed with nonperturbing diagnostics in a modified Penning discharge. These observations provide an independent confirmation of the results reported in reference 2, in which a sophisticated data reduction procedure was applied to raw data obtained from the modified Penning discharge with a retarding potential energy analyzer. The Maxwellian ion energy distributions observed in the distribution functions parallel and perpendicular to the magnetic field are consistent with a model in which the turbulent processes described in reference 4 tend to Maxwellianize the distribution function along a radius in velocity space in such a way that the ion energy is also isotropic in velocity space.

The modified Penning discharge has been shown to be capable of generating a steady-state plasma of kilovolt ion energies with an energy distribution function that is...
Maxwellian and virtually isotropic in velocity space. The modified Penning discharge may therefore be of interest in controlled fusion experiments, particularly in those toroidal systems in which one desires to create an approximately isotropic distribution of hot ions.

R. P. G. Valckx and A. Bariaud of Fontenay-aux-Roses provided useful conversations and assistance with the construction of the fast neutral energy analyzer.

Lewis Research Center,
National Aeronautics and Space Administration,
Cleveland, Ohio, November 3, 1972,
503-10.
APPENDIX - SYMBOLS

B  magnetic-field strength, T

C₀  constant appearing in eq. (1)

C₁  constant appearing in eq. (4)

C₂  constant appearing in eq. (5)

C̄₂  median value of C₂

ΔC₂  defined by eq. (7)

δC₂  standard deviation of C₂

σᵣ  electric field strength, V/m

f(V)  distribution function of ions in plasma

Gₐ(V)  correction for energy resolution of analyzer

I(V)  particle flux

k(V)  reionization probability in neutral gas cell

nᵢ  ion number density, particles/m³

n₀  neutral particle density, particles/m³

V  ion energy, eV

V⊥  perpendicular component of ion energy

V∥  parallel component of ion energy

vᵢ  ion velocity in plasma

σₓ(V)  charge-exchange cross section in plasma
REFERENCES


"The aeronautical and space activities of the United States shall be conducted so as to contribute ... to the expansion of human knowledge of phenomena in the atmosphere and space. The Administration shall provide for the widest practicable and appropriate dissemination of information concerning its activities and the results thereof."

— National Aeronautics and Space Act of 1958

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