ZERO-GRAVITY VENTING OF THREE REFRIGERANTS

by Thomas L. Labus, John C. Aydelott, and Geraldine E. Amling

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An experimental investigation of venting cylindrical containers partially filled with initially saturated liquids under zero-gravity conditions was conducted in the NASA Lewis Research Center 5-second zero-gravity facility. The effect of interfacial mass transfer on the ullage pressure response during venting was analytically determined, based on a conduction analysis applied to an infinitely planer (flat) liquid-vapor interface. This pressure response was compared with both the experimental results and an adiabatic decompression computation.
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SUMMARY

An experimental investigation of venting cylindrical containers partially filled with initially saturated liquids under zero-gravity conditions was conducted in the NASA Lewis Research Center 5-second zero-gravity facility. The test fluids possessed a near 0° contact angle on the cylindrical container surface resulting in a hemispherical liquid-vapor interface shape in zero gravity. The effect of interfacial mass transfer on the ullage pressure response during venting was analytically determined. This pressure response was compared with both the experimental pressure response and the pressure response based on an adiabatic decompression computation. The results showed that interfacial mass transfer, based on a conduction analysis applied to an infinitely planar (flat) liquid-vapor interface, in a lumped system analysis is significant in determining the ullage pressure response. The pressure response computations from adiabatic decompression consistently yielded too large a predicted ullage pressure decrease. Inclusion of the interfacial mass transfer effects resulted in approximately a 30-percent improvement in the predicted pressure response.

INTRODUCTION

The use of high-energy liquid propellants in our space program has led to a need for information concerning the thermodynamic behavior of cryogenic fluids in tanks which are vented or depressurized in space. The task of venting in low gravity has been successfully accomplished during a number of past missions with venting systems that rely exclusively on auxiliary thrusters to actively position the liquid propellant away from the tank vent.

Short-term venting has been employed by the Saturn S-IV-B (ref. 1) and the Centaur (ref. 2) vehicles in near-Earth orbit. The methods of pressure control include using the vented propellant vapor to provide adequate acceleration to keep the liquid propellant settled at the end of the tank opposite the vent or using auxiliary chemical rockets to
provide a reorientation maneuver to "collect" the liquid propellant at the end of the tank away from the vent. The low-level acceleration criteria for controlling the liquids are based on studies conducted in the zero-gravity drop tower (ref. 3).

The problems of long-term space missions such as interplanetary flights, deep space probes, and orbital storage systems more acutely point up the need for basic understanding in the area of zero- and low-gravity venting. The short-term cryogenic storage requirements of the Saturn and Centaur vehicles yield optimum weight system designs when the cryogenic boiloff is sacrificed in lieu of additional insulation. For long-term storage of cryogenics, insulation systems will be improved such that the vented propel-lant vapor will not be sufficient to supply propellant settling, and the use of auxiliary thrusters will place too large a weight penalty on the vehicle. Unless a device such as a liquid propellant thermal conditioning system (ref. 4) is employed, propellant control becomes mandatory. However, the application of a thermal conditioning system may add excessive weight penalties and complexity.

If some type of internal surface tension devices are included in the propellant tank to maintain liquid-vapor interface control, it would appear that venting during long-term space missions could be considered on a continuous basis. If the vent rate is very low, pressure control may be accomplished without disturbing the liquid bulk since liquid-vapor interface evaporation alone will supply the required vapor for venting. The objective of this study is to predict the pressure response of a saturated liquid-vapor system when undergoing a venting or depressurization process in zero gravity (weightless-ness) at low vent rates.

A venting analysis was formulated based on lumping the continuity and energy equations governing the vapor space. The analysis is not limited to any particular tank shape or contained liquid.

The analysis includes interfacial mass transfer based on an infinitely planer (flat surface) conduction analysis (refs. 5 and 6). Interfacial mass transfer is often neglected for rapid venting, but for low vent rates the effect of interface mass transfer on the pressure response is significant. The pressure response for rapid venting is usually based on the adiabatic decompression venting model.

The pressure responses determined from the venting model which includes inter-face mass transfer are compared with the results from the adiabatic decompression venting model and the pressure responses obtained from short duration (5 sec nominally) drop tower tests conducted at the Lewis zero-gravity facility. Some qualitative informa-tion concerning bulk boiling similar to that obtained in reference 7 is also presented.

The work presented herein is concerned primarily with low vent rates in contrast to reference 8 in which larger vent rates (more than one ullage/sec) were of interest. Reference 8 presents experimental zero-gravity data for both refrigerant Freon 11 and liquid hydrogen. The test fluids used for this study include the refrigerants Freon 11
(R11), octofluorocyclobutane (RC318), and n-butane (R600). These fluids were chosen because they provide a range of heat-transfer properties and are saturated at room temperature and pressures only slightly above atmospheric.

SYMBOLS

A \hspace{1cm} \text{area, m}^2
\hline
C_D \hspace{1cm} \text{discharge coefficient}
\hline
C_V \hspace{1cm} \text{specific heat at constant volume, J/(kg)(K)}
\hline
F_1, F_2 \hspace{1cm} \text{functions}
\hline
h \hspace{1cm} \text{specific enthalpy, J/kg}
\hline
h_{fg} \hspace{1cm} \text{heat of vaporization, J/kg}
\hline
K \hspace{1cm} \text{thermal conductivity, W/(m)(K)}
\hline
M \hspace{1cm} \text{mass, kg}
\hline
\vec{n} \hspace{1cm} \text{unit normal vector}
\hline
P \hspace{1cm} \text{pressure, N/m}^2
\hline
Q \hspace{1cm} \text{volumetric flow rate, m}^3/\text{sec}
\hline
q \hspace{1cm} \text{heat flux, W/m}^2
\hline
R \hspace{1cm} \text{gas constant, (m)(N)/(kg)(K)}
\hline
T \hspace{1cm} \text{temperature, K}
\hline
t \hspace{1cm} \text{time, sec}
\hline
U \hspace{1cm} \text{internal energy, J}
\hline
u \hspace{1cm} \text{specific internal energy, J/kg}
\hline
V \hspace{1cm} \text{volume, m}^3
\hline
v \hspace{1cm} \text{velocity, m/sec}
\hline
\alpha \hspace{1cm} \text{thermal diffusivity, m}^2/\text{sec}
\hline
\gamma \hspace{1cm} \text{ratio of specific heats}
\hline
\rho \hspace{1cm} \text{density, kg/m}^3
\hline
\xi(\bar{x}) \hspace{1cm} \text{parameter}
The Lewis zero-gravity facility was used to obtain the experimental data for this investigation. A complete description of the facility, the experiment package, and procedures for conducting the tests can be found in appendix A. The venting tests were conducted with right-circular cylindrical containers having flat ends as shown in figure 1. These test containers were fabricated from acrylic plastic.

The liquids employed in the tests were refrigerant 11 (CCl₃F), refrigerant C318 (C₄F₈), and refrigerant 600 (CH₃CH₂CH₂CH₃). Refrigerant 600 is commonly known as n-butane and refrigerant 11 is commonly known as Freon 11 or Genetron 11. The pertinent thermodynamic properties for all these fluids, such as enthalpy, specific volume, and entropy, can be found in standard refrigeration tables (ref. 9). All three of these fluids were found to exhibit a nearly 0° static contact angle on the test container surface, and are, therefore, representative of typical liquid propellants. The area of the liquid surface (5.57×10⁻³ m²) is simply the area of a hemisphere having a radius equal to that of the tank since the venting sequence occurs during weightlessness. The tank pressure and the temperature in the vicinity of the liquid-vapor interface were monitored continuously before the drop test to ensure reaching nearly saturated conditions. The tank pressure was recorded during the drop test along with high-speed motion pictures. After releasing an experiment package, a maximum of 1.9 seconds was allowed for the liquid to achieve the hemispherical zero-gravity interface configuration; the timers then activated the vent sequence for approximately 3 seconds.
ANALYSIS

Adiabatic Decompression Venting Model

The pressure reduction of a tank containing only a perfect gas during the adiabatic withdrawal of that gas is calculated in order to make comparisons with a venting model which includes interfacial mass transfer. Conservation of mass is applied in the following manner: The rate of decrease of mass in the tank is set equal to the withdrawal rate where the volumetric withdrawal rate $Q$ is assumed constant. When proceeding along the lines of the analysis presented in appendix B, substituting equation (B16), which is

$$\frac{P_1 T_2}{P_2 T_1} = e^{\frac{Q t}{V_v}}$$

into equation (B11), which is

$$\frac{T_2}{T_1} = e^{-\frac{Q R t}{V_v} C_V}$$

leads to the following expression for the pressure reduction during an adiabatic decompression:

$$\frac{P_2}{P_1} = e^{-\gamma \frac{Q t}{V_v}}$$

Interface Mass Transfer Venting Model

At time zero, the venting process is assumed to start with initially saturated vapor exiting through the vent to a vacuum. A schematic of the venting system at various instances of time is shown in figure 2. The initial thermodynamic state of the vapor and liquid are known (saturated conditions). The pressure decrease within the container during venting causes mass to be transferred across the liquid-vapor interface. As venting continues, it is assumed that only vapor passes through the vent line. The analysis is based on a flat interface shape. However, in order to compare the model with the experimental data the area of the hemispherical surface is used for the analysis.

The overall system is divided into two separate control volumes - the vapor and the liquid regions. The vapor region consists of the region above the liquid surface, and its
volume is a function of the liquid height. The vented vapor \( M_0 \) is taken from this region. The mass transfer terms associated with the vapor region are shown in figure 3. As the liquid evaporates during a pressure reduction, some mass \( M_s \) is transferred to the vapor region causing the volume of the liquid region (see fig. 4) to vary slightly with time. It is assumed that no boiling occurs within the bulk liquid.

**Derivation of Venting Equations**

In applying the continuity and energy conservation equations, the volume \( V \), which appears in the equations, is fixed since actual volume variations due to mass transfer will be small. The continuity equation is

\[
\int_V \frac{\partial \rho}{\partial t} \, dV + \int_A \rho \mathbf{v} \cdot \mathbf{n} \, dA = 0
\]  

(2)

\[
\frac{d}{dt} \int_V \rho \, dV = - \int_A \rho \mathbf{v} \cdot \mathbf{n} \, dA
\]  

(3)

For the vapor region, equation (3) becomes

\[
\frac{dM_v}{dt} = \dot{M}_s - \dot{M}_o
\]  

(4)

For the liquid region,

\[
\frac{dM_l}{dt} = -\dot{M}_s
\]  

(5)

If the internal energy is assumed to be only a function of time, the energy equation in integral form is

\[
\frac{d}{dt} \int_V \rho u \, dV + \int_A \rho u \mathbf{v} \cdot \mathbf{n} \, dA = - \int_A P \mathbf{v} \cdot \mathbf{n} \, dA - \int_A \mathbf{q} \cdot \mathbf{n} \, dA
\]  

(6)
Using the relation

$$h = u + \frac{P}{\rho}$$  

(7)

in equation (6) yields the following form of the energy equation with $\bar{q} = 0$ (valid only for short test times):

$$\frac{d}{dt} \int_V \rho h dV - \frac{d}{dt} \int_V P dV = - \int_A \rho \vec{v} \cdot \vec{n} dA - \int_A \bar{q} \cdot \vec{n} dA$$  

(8)

For the vapor region, equation (8) becomes

$$\frac{d}{dt} (M_{vh} h_v) - V_v \frac{dP_2}{dt} = M_s h_v, s - M_0 h_v$$  

(9)

For the liquid region,

$$\frac{d}{dt} (M_l h_l) - V_l \frac{dP_2}{dt} = -M_s h_l, s$$  

(10)

For the bulk liquid region, it is assumed that the initial and final temperatures during venting are identical and equal to $T_1$. The temperature at the liquid-vapor interface is $T_{2, \text{sat}}$, which is the saturation temperature corresponding to the ullage pressure $P_2$. The addition of equations (9) and (10), which is not independent of the mass transferred across the liquid-vapor interface, yields the product of the interface mass transfer rate and the latent heat of vaporization $M_s h_{fg}$. The temperature of the vapor is also assumed to be $T_{2, \text{sat}}$, which is the saturation temperature corresponding to the ullage pressure. Since the mass transferred across the liquid-vapor interface enters at the saturation temperature, an adiabatic decompression computation was performed to show that the vapor initially in the control volume remains nearly saturated during a pressure reduction. This analysis was performed for the three fluids employed, and a sample calculation is contained in appendix C. The enthalpy of the vapor $h_v$ is to be evaluated at the saturated conditions. Since the vapor region is of primary interest, the governing equations of the vapor region are rewritten as follows:
Continuity vapor:

\[ \frac{dM_v}{dt} = \dot{M}_s - \dot{M}_o \]  

(11)

Energy conservation vapor:

\[ \frac{d}{dt}(M_v h_v) - V_v \frac{dP_2}{dt} = h_v (\dot{M}_s - \dot{M}_o) \]  

(12)

Expressions for the mass transfer terms which appear in equations (11) and (12) are now examined in detail.

The mass flow rate through the vent \( \dot{M}_o \) is determined by using the classical choked flow analysis. Since the vented gas goes directly into a vacuum, the choked flow assumption is valid and the mass flow rate is a function of upstream thermodynamic properties and an experimentally determined discharge coefficient (see table I). As discussed previously, the ullage pressure is a time-dependent quantity. Therefore, it follows that the vent mass flow rate will vary with time.

Analytical expression for \( \dot{M}_s \). A conduction analysis by Thomas and Morse (ref. 6) was applied to the interfacial mass transfer process occurring during depressurization for an infinitely planer (liquid-vapor) interface. The following expression was obtained from this analysis for the mass transfer rate:

\[ \dot{M}_s = A_s \rho_l \left( \frac{\alpha_l}{t} \right)^{1/2} | \xi_l(\overline{x}) | \]  

(13)

where \( \xi_l(\overline{x}) \) satisfies the transcendental equation

\[ \sqrt{\pi \alpha_v \rho_l h_v} \xi_l(\overline{x}) = \frac{K_v(T_2, \text{sat} - T_2, v)}{\sqrt{\alpha_v}} \exp \left\{ \left( \frac{\alpha_l}{\alpha_v} \right) \left[ \frac{(\rho_l)}{(\rho_v)} \xi_l(\overline{x}) \right] \right\} \]  

\[ + \frac{K_l(T_2, \text{sat} - T_1)}{\sqrt{\alpha_l} \left[ 1 + \text{erf} \frac{\xi_l(\overline{x})}{\sqrt{\alpha_v}} \right]} \]  

(14)
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<th>Nozzle diameter, m</th>
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where $T_1$ is the liquid temperature, $T_{2, \text{sat}}$ the liquid-vapor interface temperature, and $T_{2,v}$ the vapor temperature. Thomas and Morse show that if the expression for $\xi_l(x)$ is solved explicitly for $\xi_l(x)$ by expanding both the error functions and exponentials for small $\xi_l(x)$ one obtains

$$
\xi_l(x) = \frac{K_l(T_{2, \text{sat}} - T_1) + K_v(T_{2, \text{sat}} - T_{2,v})}{\sqrt{\alpha_l} + \sqrt{\alpha_v}}
$$

$$
\sqrt{\pi \alpha_l} \rho_l h_{fg} - \frac{2K_v(T_{2, \text{sat}} - T_{2,v})}{\sqrt{\pi \alpha_v}} \frac{\rho_l}{\rho_v} \sqrt{\alpha_l} + \frac{2K_l(T_{2, \text{sat}} - T_1)}{\sqrt{\pi \alpha_l}}
$$

Now let $T_{2, \text{sat}} = T_{2,v}$ (as per our stated assumption and appendix C verification):

$$
\xi_l(x) = \frac{\sqrt{\pi K_l(T_{2, \text{sat}} - T_1)}}{\pi \alpha_l \rho_l h_{fg} + 2K_l(T_{2, \text{sat}} - T_1)}
$$

Let

$$
F_1 = \pi \alpha_l \rho_l h_{fg}
$$

and

$$
F_2 = 2K_l(T_{2, \text{sat}} - T_1)
$$

### TABLE II. - TYPICAL PROPERTIES FOR TEST FLUIDS AT 297 K

<table>
<thead>
<tr>
<th>Refrigerant</th>
<th>Thermal conductivity of liquid, $K_l$, W/(m)(K)</th>
<th>Liquid density, $\rho_l$, kg/m$^3$</th>
<th>Thermal diffusivity of liquid, $\alpha_l$, m$^2$/sec</th>
<th>Heat of vaporization, $h_{fg}$, J/kg</th>
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</table>
Typical values of \( F_1 \) and \( F_2 \) and hence the ratio \( F_2/F_1 \) are now computed. This computation was based on the largest temperature change of the tests that were performed for each fluid. The resulting values of \( F_2/F_1 \) were 0.071 for R11, 0.150 for RC318, and 0.157 for R600 (table II). Hence, the largest error in neglecting \( F_2 \) with respect to \( F_1 \) is 16 percent. Therefore,

\[
\tilde{\xi}_l(x) \approx \frac{K_l(T_{2,\text{sat}} - T_1)}{\sqrt{\pi} \alpha_l \rho_l h_{fg}}
\]

Equation (19) can be substituted into equation (13) to obtain the following approximate solution for the interface mass transfer rate:

\[
\dot{M}_s \approx \frac{A_s K_l(T_1 - T_{2,\text{sat}})}{\sqrt{\pi} h_{fg}} \sqrt{\frac{1}{\alpha_l t}}
\]

By definition

\[
K_l = \alpha_l C_p \rho_l
\]

Therefore,

\[
\dot{M}_s \approx \frac{A_s \rho_l C_p \rho_l(T_1 - T_{2,\text{sat}})}{\sqrt{\pi} h_{fg}} \sqrt{\frac{\alpha_l}{t}}
\]

When combined with the appropriate initial and boundary conditions, equations (11), (12), and (22) provide a complete thermodynamic description of the vapor space. These equations, along with equation (1) which gives the pressure reduction during an adiabatic decompression, were solved using a computer program (appendix D) which employed a calculation procedure using 60 time intervals. A comparison of the solutions to these equations with experimental data is presented in the RESULTS AND DISCUSSION section.
RESULTS AND DISCUSSION

Pressure Decay Characteristics

During space missions involving the use of cryogenic liquids, the maximum allowable tank pressure and the thermal environment dictate such items as venting times and insulation requirements. Consequently, the pressure response of the tank ullage during a venting sequence in space is an important parameter to be considered. A typical ullage pressure response for RC318 during one of the experimental tests is shown in figure 5. As previously mentioned in the APPARATUS AND PROCEDURE section, the experiment tank contents were allowed sufficient time to reach a saturated equilibrium condition corresponding to the ambient temperature in the test facility. The initial pressure for the test shown in figure 5 is $29 \times 10^4$ newtons per square meter. A time duration of 1.9 seconds was then allowed during free-fall so that the liquid-vapor interface could attain a hemispherical equilibrium configuration. Note that the tank pressure remains constant during this time period as expected. At 1.9 seconds after the initiation of the test, the vent was opened and vapor passed through the vent line for a period of 3 seconds. The final ullage pressure reached $13 \times 10^4$ newtons per square meter as seen in figure 5.

In table I, the test parameters for the 16 no-boiling zero-gravity tests conducted during this program are shown. Note that test 10 is the typical test whose pressure characteristics are shown in figure 5.

Comparison of Experiment With Theory

As a direct result of one of the assumptions made in the analyses, namely, that the vapor remains saturated during a depressurization or venting sequence, the mass conservation equation (eq. (11)) and the energy conservation equation (eq. (12)) remain uncoupled. Hence, the solution to either equation along with the corresponding expressions for the vent mass flow rate and interface mass transfer, using the proper boundary and initial conditions, results in identical solutions. Computer programs were run with each separately and yielded similar results. The test conditions and the results from the computer program are contained in table I. The final ullage pressure, based on the interface mass transfer venting model, is under the column labeled "Final analytical ullage pressure." The tabulated results for the final ullage pressure based on the adiabatic decompression venting model are under the column labeled "Final adiabatic ullage pressure." In all cases the adiabatic calculation yielded a lower final ullage pressure than for the venting model calculation which included interfacial mass.
transfer. The difference is due to the fact that the addition of mass from the interface into the vapor space would not allow the tank pressure to decrease as rapidly. In all tests, for both the adiabatic decompression and the venting model calculation including mass transfer, the computed final ullage pressures were lower than the corresponding experimental values.

A graphical comparison of the three previously mentioned pressure drops nondimensionalized in terms of the initial pressure ($\Delta P/P_1$) is presented as a function of the reduced flow rate ($Q/V_{v_1}$) in figures 6 to 8. The reduced flow rate is the average volumetric flow rate divided by the initial vapor volume. (These two parameters are also tabulated in table I). Figure 6 presents the results for refrigerant 11, figure 7 presents the results for refrigerant C318, and figure 8 presents the results for refrigerant 600. The experimental and analytical data points contained on these three curves are for the 0.06 meter diameter cylindrical tank having a nominal 33 percent by volume initial filling of liquid.

Figures 6 to 8 indicate that the analysis which includes interfacial mass transfer shows approximately 25 to 35 percent improvement with respect to the final ullage pressure prediction in comparison with the adiabatic computation. However, there still exists a significant gap between experiment and theory.

The inclusion of the term $F_2$ in equation (16) would lead to larger interfacial mass transfer rates since the final temperature ($T_{2,\text{sat}}$) is always less than the initial temperature ($T_1$). Since the discrepancy between experiment and analysis is the result of an insufficient amount of interfacial mass transfer, inclusion of the term $F_2$ would result in an improvement. However, this was earlier judged to be a minor effect. Of major importance is the fact that an infinitely planer conduction analysis attributable to Thomas and Morse (ref. 6) was employed. This, in effect, neglects heat conduction from the side walls. Since the liquid-vapor interface was hemispherical in shape there exists a very large temperature gradient and, hence, significant heat-transfer rate through the thin liquid surface on the walls in the neighborhood of the leading edge. It would appear that an improvement in the analysis that included both curved interfaces and finite walls would yield higher mass transfer rates and, thus, lead to a much better agreement between analysis and experiment.

Another factor which could contribute to increasing the interfacial mass transfer is the liquid motion caused by the initial change from a normal-gravity to a zero-gravity configuration and as a response to the venting disturbance. However, it would probably be impossible to incorporate this effect into a venting model analysis.
Any complete study of venting under any gravitational conditions should include the possibility of boiling occurring within the liquid bulk. The analysis which appears in this report does not apply to situations in which bulk boiling occurs. Hence, all the data points which appear in table I are for cases wherein no bulk boiling was observed. The problem of predicting the inception of bulk boiling is presently without solution. Certainly the inception point would depend on the tank surface conditions which determine the size and distribution of nucleation sites and also the properties of the particular fluid. While the intent of this report was not geared directly toward a discussion of the prediction of the aforementioned phenomenon, it did arise in one test case.

The photographic sequence for test 10 (refrigerant C318) is shown in figure 9. Note that the average vent rate for this particular test was $\frac{Q}{V_v} = 0.5$ ullage volume per second. In this test no bulk boiling occurred. However, as seen in figure 10, for an average vent rate of 1.0 ullage volume per second, for RC318, extensive bulk boiling occurs. The liquid-vapor interface is pushed toward the vent as a result of the growth of two rather large vapor bubbles. These vapor bubbles do not break the liquid-vapor interface and cause large surface disturbances as the vent sequence continues. The venting model analysis cannot be applied to test cases where bulk boiling occurs since the liquid-vapor interface area is not only varying with time but would also be impossible to predict.

CONCLUDING REMARKS

An experimental investigation of venting cylindrical containers partially filled with initially saturated liquids under zero-gravity conditions was conducted in the NASA Lewis Research Center 5-second zero-gravity facility. The test fluids, refrigerants 11, C318, and 600, all possessed a near-zero contact angle on the container surface resulting in a hemispherical liquid-vapor interface shape in zero gravity. The experimental pressure responses were compared with pressure responses predicted by an adiabatic decompression venting model and a lumped system venting model which includes interfacial mass transfer.

For the tests which exhibited no bulk boiling the adiabatic decompression venting model predicted too large a pressure reduction by nearly a factor of two. The addition of the effects of interfacial mass transfer to a lumped system venting model, based on a conduction analysis for an infinitely planer (flat) surface, resulted in approximately a 30-percent improvement in the determination of the ullage pressure response when compared to the adiabatic decompression venting model.
It is the authors' belief that the container walls act as a heat source and cause additional liquid evaporation thus reducing the experimental pressure decay. In order to improve the agreement between experimental and analytical venting system results, the infinitely planar surface analytical approach presented in this report would have to be modified to account not only for the container walls but also the curvature of the liquid-vapor interface.

Lewis Research Center,
National Aeronautics and Space Administration,
Cleveland, Ohio, August 14, 1973,
909-72.
APPENDIX A

APPARATUS AND PROCEDURE

Test Facility

The experiment data for this study were obtained in the 5- to 10-second zero-gravity facility at the Lewis Research Center. A schematic diagram of this facility is shown in figure 11. The facility consists of a concrete-lined 8.5-meter-diameter shaft that extends 155 meters below ground level. A steel vacuum chamber, 6.1 meters in diameter and 143 meters high, it contained within the concrete shaft. The pressure in this vacuum chamber is reduced to 13.3 newtons per square meter by utilizing the Center's wind tunnel exhaust system and an exhauster system located in the facility.

The ground-level service building has, as its major elements, a shop area, a control room, and a clean room. Assembling, servicing, and balancing the experiment vehicle are accomplished in the shop area. Tests are conducted from the control room (see fig. 12) which contains the exhauster control system, the experiment vehicle pre-drop checkout and control system, and the data retrieval system. Those components of the experiment which are in contact with the test fluid are prepared in the facility's class 10,000 clean room. The major elements of the clean room are an ultrasonic cleaning system (fig. 13(a)) and a class 100 laminar-flow station (fig. 13(b)) for preparing those experiments requiring more than normal cleanliness.

Mode of operation. - The zero-gravity facility has two modes of operation. One is to allow the experiment vehicle to free-fall from the top of the vacuum chamber, which results in nominally 5 seconds of free-fall time. The second mode is to project the experiment vehicle upwards from the bottom of the vacuum chamber by a high pressure pneumatic accelerator located on the vertical axis of the chamber. The total up-and-down trajectory of the experiment vehicle results in nominally 10 seconds of free-fall time. The 5-second mode of operation was used for this experimental study.

In either mode of operation, the experiment vehicle falls freely; that is, no guide wires, electrical lines, and so forth are connected to the vehicle. Therefore, the only force (aside from gravity) acting on the freely falling experiment vehicle is due to residual air drag. This results in an equivalent gravitational acceleration acting on the experiment which is estimated to be of the order of $10^{-5}$ g maximum.

Recovery system. - After the experiment vehicle has traversed the total length of the vacuum chamber, it is decelerated in a 3.6-meter-diameter, 6.1-meter-deep container which is located on the vertical axis of the chamber and filled with small pellets of expanded polystyrene. The deceleration rate (averaging 32 g's) is controlled by the flow of pellets through the area between the experiment vehicle and the wall of the
deceleration container. This deceleration container is mounted on a cart which can be retracted prior to utilizing the 10-second mode of operation. In this mode of operation, the cart is deployed after the experiment vehicle is projected upward by the pneumatic accelerator. The deceleration container mounted on the cart is shown in figure 14.

Experiment Vehicle

The experiment vehicle consisted of two basic sections (see fig. 15). The experiment section is contained in the cylindrical midsection and the telemetry section is contained in the top fairing.

Experiment. - The experiment section consisted of the test container tray (see fig. 16) plus electrical power and control system equipment mounted in the cylindrical section of the experiment vehicle. The test container tray includes the test container, camera, and lighting and timing systems. The vent system which included a solenoid valve and various sized nozzles and orifices was mounted above the test container. The solenoid valve opened during the test drop and vapor was vented either to the low pressure test chamber or to a collection tank also at a low pressure. The ensuing venting procedure was recorded by a high-speed motion picture camera. Elapsed time was obtained from a digital clock.

Telemetry system. - The on-board telemetry system is an FM/FM system with 18 continuous channels. During a test drop, telemetry is used to continuously record the output from two low-gravity accelerometers and the tank pressure. The initial temperature in the vicinity of the liquid-vapor interface is also obtained from the recording system, but the temperature data obtained during the test was not used due to the questionable response time of the transducer. The accuracy of all temperatures quoted in this report is conservatively estimated to be ±1.5°, while the accuracy of all pressures is estimated to be ±1 newton per square centimeter.

Test Procedure

Cleaning, filling, and hermetic sealing the test containers were conducted in the zero gravity facility's clean room (fig. 13). Contamination of the liquid and cylinder, which could alter the surface tension and contact angle, was carefully avoided. The test cylinders were cleaned ultrasonically in a detergent-water solution, rinsed with a distilled-water-methanol solution, and dried in a warm air dryer. The test cylinders were rinsed with the test liquid, filled to the desired liquid depth, and sealed to prevent contamination. They were then mounted on the test container tray. During the test, a predetermined time increment was allowed (1.9 sec maximum) so that the liquid-vapor
interface could approach its low-gravity equilibrium shape. After the formation time, the solenoid valve was opened and the vapor vented to vacuum for 3 seconds.

Electrical timers on the experiment vehicle are set to control the initiation and duration of all functions programmed during the drop. The experiment vehicle is balanced about its vertical axis to ensure an accurate drop trajectory.

The vehicle is then positioned at the top of the vacuum chamber as shown in figure 17. It is suspended by the support shaft on a hinged-plate release mechanism. During vacuum chamber pumpdown and prior to release, monitoring of experiment vehicle systems is accomplished through an umbilical cable attached to the top of the support shaft. Electrical power is supplied from ground equipment. The system is then switched to internal power a few minutes before release. The umbilical cable is remotely pulled from the support shaft 0.5 second prior to release. The vehicle is released by pneumatically shearing a bolt that holds the hinged plate in the closed position. No measurable disturbances are imparted to the experiment vehicle by this release procedure.

The total free-fall test time obtained in this mode of operation is 5.16 seconds. During the test drop, the vehicle's trajectory and deceleration are monitored in closed-circuit television. Following the test drop, the vacuum chamber is vented to the atmosphere and the experiment vehicle is returned to ground level.
APPENDIX B

ADIABATIC DECOMPRESSION VENTING MODEL

A container of gas at some high pressure is assumed. At time zero, a valve is opened allowing the gas to escape. The temperature and pressure dependence with time will be examined. An adiabatic process is assumed \((q = 0)\) so that the rate of change of internal energy is equal to the rate of energy removal:

\[
\frac{dU}{dt} = \frac{dM}{dt} (h) \quad (B1)
\]

where

\[
U = Mu = MCVT \quad (B2)
\]

and

\[
h = u + RT \quad (B3)
\]

Expanding equation (B2) gives

\[
\frac{dU}{dt} = \left( \frac{\partial U}{\partial t} \right) \left( \frac{dT}{dt} \right) + \left( \frac{\partial U}{\partial M} \right) \left( \frac{dM}{dt} \right) \quad (B4)
\]

and

\[
\frac{dU}{dt} = MCVT \left( \frac{dT}{dt} \right) + u \left( \frac{dM}{dt} \right) \quad (B5)
\]

When equation (B1) is used, equation (B5) becomes

\[
h \frac{dM}{dt} = MCVT \left( \frac{dT}{dt} \right) + u \left( \frac{dM}{dt} \right) \quad (B6)
\]

The rate of change of mass leaving the container can be expressed in terms of the volumetric flow rate \(Q\) as follows:
when \( Q \) is assumed to be a constant in time. Substituting equation (B7) into equation (B6) gives

\[
- \frac{PQ}{RT} (u + RT) = MC_V \left( \frac{dT}{dt} \right) - \frac{PQ}{RT} u
\]

which becomes after some simplification

\[
\frac{dT}{T} = - \frac{Q}{V_v C_V} R \frac{dt}{dt}
\]

Integrating gives

\[
\int_{T_1}^{T_2} \frac{dT}{T} = - \frac{Q}{V_v C_V} R \int_{t_1}^{t_2} dt
\]

The solution of the previous equation is

\[
T_2 = T_1 e^{-\frac{QRt}{V_v C_V}}
\]

Now the time dependence of the ullage pressure is derived by employing conservation of mass. The rate of decrease of mass in the container equals the withdrawal rate which the volumetric removal rate is assumed constant. The rate of change of mass leaving the container is expressed in terms of \( Q \) by equation (B6) and \( M \), of course, is related to the other thermodynamic variables through the perfect gas law

\[
M = \frac{PV_v}{RT}
\]

Therefore, expanding equation (B12) gives

\[
\frac{dM}{dt} = \left( \frac{\partial M}{\partial P} \right) \left( \frac{dP}{dt} \right) + \left( \frac{\partial M}{\partial T} \right) \left( \frac{dT}{dt} \right)
\]
Using previous relations in equation (B12) gives

\[
\frac{PQ}{RT} = \frac{V_v}{RT} \left( \frac{dP}{dt} \right) - \frac{PV_v}{RT^2} \left( \frac{dT}{dt} \right)
\]  \hspace{1cm} (B14)

Rewriting equation (B14) gives

\[
\frac{Q}{V_v} \frac{dt}{dt} = -\frac{dP}{P} + \frac{dT}{T}
\]  \hspace{1cm} (B15)

Integration yields

\[
\frac{P_1 T_2}{P_2 T_1} = e^{\frac{Q t}{V_v}}
\]  \hspace{1cm} (B16)
APPENDIX C

EXAMINATION OF ASSUMPTION OF SATURATED VAPOR

The procedure used to check the validity of the assumption of the vapor temperature remaining saturated was to calculate $T_2/T_1$ from equation (B11). To accomplish this, typical values of $Q$, $V_v$, and $t$ were chosen (table III). The value of $T_2/T_1$ thus found was substituted into equation (B16), and equation (B16) was solved for $P_2/P_1$. Finally, the saturation pressure corresponding to $T_2$ is compared with the value of $P_2$ computed by means of equation (B16). Using these typical values in equation (B11) yields $T_2/T_1 = 0.945$. Therefore, $T_2$ equals 278.5 K, which corresponds to a saturation pressure of $5.07 \times 10^4$ newtons per square meter. The ratio $P_2/P_1$ calculated from equation (B16) is found to be 0.563. Hence, $P_2 = 4.94 \times 10^4$ newtons per square meter. Therefore, the assumption of saturated vapor throughout the venting sequence appears reasonable.

### TABLE III. - TYPICAL FLUID PROPERTIES AND EXPERIMENTAL VALUES FROM TEST 2

<table>
<thead>
<tr>
<th>Fluid properties</th>
<th>Refrigerant 11</th>
</tr>
</thead>
<tbody>
<tr>
<td>Liquid</td>
<td></td>
</tr>
<tr>
<td>Specific heat at constant volume, $C_v$, J/(kg)(K)</td>
<td>528</td>
</tr>
<tr>
<td>Gas constant, $R$, J/(kg)(K)</td>
<td>58.6</td>
</tr>
<tr>
<td>Time, $t$, sec</td>
<td>3</td>
</tr>
<tr>
<td>Volume of vapor, $V_v$, m³</td>
<td>$2.01 \times 10^{-4}$</td>
</tr>
<tr>
<td>Average volumetric flow rate, $Q$, m³/sec</td>
<td>$0.342 \times 10^{-4}$</td>
</tr>
<tr>
<td>Temperature, $T$, K</td>
<td>294.7</td>
</tr>
<tr>
<td>Initial pressure, $P_1$, N/m²</td>
<td>$8.79 \times 10^4$</td>
</tr>
</tbody>
</table>
APPENDIX D

COMPUTER PROGRAM

The computer program used for numerically solving equations (11), (12), and (22) consists of a main program and four subroutines. The subroutines DD, CURVE, DERIV, and RKGS make available the Runge-Kutta method for the numerical solution of an ordinary first-order differential equation with nonconstant coefficients, the independent variable in all cases being time. A calculation procedure was employed which divided the 3-second test time into 60 intervals in order to improve the accuracy of the computations. Also included in the computer program was the solution of equation (1) which yields the pressure decrease based on the adiabatic decompression venting model. This appendix includes a dictionary of the FORTRAN symbols used, the program listing, and a complete input/output list for one test. A typical flow chart is shown in figure 18. All of the data were analyzed using the computer program with only slight variations due to the different sources and formats of the thermodynamic properties for the three fluids.

Dictionary of FORTRAN Symbols

<table>
<thead>
<tr>
<th>FORTRAN symbol</th>
<th>Engineering symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>AT</td>
<td>A</td>
<td>area of vent nozzle at throat</td>
</tr>
<tr>
<td>AS</td>
<td>A_s</td>
<td>liquid-vapor surface area</td>
</tr>
<tr>
<td>CD</td>
<td>C_D</td>
<td>discharge coefficient</td>
</tr>
<tr>
<td>CPL</td>
<td>C_p,l</td>
<td>specific heat of liquid</td>
</tr>
<tr>
<td>GO</td>
<td>G_o</td>
<td>acceleration due to gravity</td>
</tr>
<tr>
<td>H</td>
<td>h</td>
<td>specific enthalpy</td>
</tr>
<tr>
<td>HFG</td>
<td>h_{fg}</td>
<td>heat of vaporization</td>
</tr>
<tr>
<td>K</td>
<td>K</td>
<td>thermal conductivity</td>
</tr>
<tr>
<td>MV</td>
<td>M_v</td>
<td>mass flow rate of vented vapor</td>
</tr>
<tr>
<td>MMT</td>
<td>M_s</td>
<td>mass flow rate across liquid-vapor surface</td>
</tr>
<tr>
<td>P2, Y(1)</td>
<td>P_2, Y(1)</td>
<td>ullage pressure based on venting model</td>
</tr>
<tr>
<td>Q</td>
<td>Q</td>
<td>volumetric flow rate</td>
</tr>
</tbody>
</table>
FORTRAN symbol | Engineering symbol |
--- | --- |
T, X | t | time |
T1 | T, 1 | initial ullage temperature |
T2 | T, 2 | saturation temperature corresponding to \( P_2 \) |
VV | V | volume |
Y3 | \( P_2 \) | ullage pressure based on adiabatic decompression |
ALPHAL | \( \alpha_L \) | liquid thermal diffusivity |
RHOL | \( \rho_L \) | liquid density |
RHOV, Y(2) | \( \rho_v \) | vapor density |

**PROGRAM LISTING**

```fortran
EXTERNAL DD
COMMON P2, MV, Q, Y3, AT, AS, CPL, ALPHAL, VV, RHOL, T1, CD, GO, KODE
DIMENSION Y(2), DY(2), TITLE(12)
REAL MV
2 READ(5,102) (TITLE(I), I=1,12)
READ(5,103) P2, RHOV, AT, AS, CPL, ALPHAL, VV, RHOL, T1, CD, GO
C KODE=1  MMT CALCULATED  KODE=0  MMT=0.0
KODE=0
DO 3 II=1,2
C INITIALIZE T = X
X=0.0001
C INITIALIZE P2 = Y(1)
Y(1)=P2
C INITIALIZE RHOV = Y(2)
Y(2)=RHOV
P2I=Y(1)
WRITE(6,100)
WRITE(6,103) (TITLE(I), I=1,12)
WRITE(6,104)
WRITE(6,107) P2, RHOV, AT, AS, CPL, ALPHAL, VV, RHOL, T1, CD, GO, KODE
WRITE (6,104)
WRITE(6,106)
DO 1 I=1,60
XF=X+0.05
CALL RKGS (X, XF, H, .1E-3, Y, DY, 2, DD)
WRITE(6,101) X, Y(1), MV, Q, Y3
1 CONTINUE
KODE=KODE+1
3 CONTINUE
GO TO 2
100 FORMAT(120H1ZERO GRAVITY VENTING MASS BALANCE AND ENERGY BALANCE)
101 FORMAT(10X,5G15.6)
102 FORMAT(12A6)
103 FORMAT(1HK, 12A6)
```
SUBROUTINE DD (X,Y,DY)
C HOMOGENEOUS DIFFERENTIAL EQUATION OF THE FIRST ORDER USING RUNGE-KUTTA SOLUTION
COMMON P21,MV,Y3,AT,AS,CPL,ALPHAL,RHOL,T1,CD,GO,KODE
COEFF6(5),COEFF7(5),COEFF8(5),T(100),P2A(100),Y(2),DY(2)
C R600 COEFFICIENTS
C CURVE 1  RHOV VS. P
DATA (COEFF1(I),I=1,5)/0.12715492E-01,0.1D550608E-01,0.11994321E-03,
-4.6139911E-06,0.72537941E-38/ 
C CURVE 2  T2 VS. P
DATA (COEFF2(I),I=1,5)/-45.905340,7.8234674,-0.22653183E-02,
1.3825971E-02,-0.25415846E-04/ 
C CURVE 3  H2 VS. P
DATA (COEFF3(I),I=1,5)/-633.910022.4116720,-0.65913194E-01,
1.0513420E-02,0.65971124E-05/ 
C CURVE 4  HFG VS. P
DATA (COEFF4(I),I=1,5)/180.66624,-1.5806674,0.49739617E-01,
-0.93911366E-03,0.67298545E-05/ 
C CURVE 5  K VS. P
DATA (COEFF5(I),I=1,5)/-0.36075050E-03,4.9051085,-0.34892180E-01,
1.71910064E-03,-0.59942675E-05/ 
REAL MMT,MV,K
SQRTPI=1.772438
C COMPUTE MMT - USE THERMODYNAMIC CHARTS TO OBTAIN T2, AND HFG
P2=Y(1)
CALL CURVE(COEFF2,P2,T2)
CALL CURVE(COEFF4,P2,HFG)
MMT=0.0
IF(KODE.EQ.0) GO TO 1
MMT=AS*RHOL*CPL*(T1-T2)*SQRT(ALPHAL/X)/(SQRTPI*HFG*60.)
1 CONTINUE
CALL CURVE (COEFF5,P2,K)
MV=CD*AT*K
C COMPUTE DP2/DT USE THERMODYNAMIC CHARTS TO OBTAIN RHOV, RHOPV, AND H2P
CALL CURVE(COEFF1,P2,R40V)
CALL CURVE(COEFF3,P2,H2)
CALL DERIV(COEFF1,P2,H40VP)
CALL DERIV(COEFF3,P2,H2P)
DY(2)=((MMT-MV)/VV)
DY(1)=DY(2)/RHOPV
Q=MV/Y(2)
Y3=P2*I*EXP(-Q*X*1.11/VV)
RETURN
END
SUBROUTINE CURVE(COEFF, X, Y)
DIMENSION COEFF(5)
Y = COEFF(1) + X * (COEFF(2) + X * (COEFF(3) + X * (COEFF(4) + X * COEFF(5))))
RETURN
END

SUBROUTINE DERIV(COEFF, X, DYDX)
DIMENSION COEFF(5)
DYDX = COEFF(2) + X * (2.0 * COEFF(3) + X * (3.0 * COEFF(4) + X * 4.0 * COEFF(5)))
RETURN
END

PARAMETERS

XO INITIAL VALUE FOR X, RETURNED AS XF NORMALLY
XF FINAL VALUE FOR X
HH NORMALLY RETURNED AS STEP SIZE USED NEAR XF
RETURNED AS 0 IF MORE THAN 25 HALVINGS
ERR UPPER ERROR BOUND, USED TO CONTROL STEP SIZE
Y DEPENDENT VARIABLES, SET TO INITIAL VALUES,
RETURNED AT X=XF NORMALLY
DERY DERIVATIVES DY/DX
NDIM1 NUMBER OF EQUATIONS IN SYSTEM
FCT EXTERNAL SUBROUTINE WHICH CALCULATES DERIVATIVES
CALL IS CALL FCT(X, Y, DER Y)

SUBROUTINE RKGS(XO, XF, HH, ERROR, Y, DERY, NDIM1, FCT)
DIMENSION Y(1), DERY(1)
DIMENSION AUX(7, 20), A(4), B(4)
DATA A / .5, .29289322, 1.7071068, .16666667/
DATA B / 2., 1., 1., 2. /
NDIM = NDIM1
ERR = ERROR
X = XO
XEND = XF
H = (XEND - X) * .0625
IHLF = -1
CALL FCT(X, Y, DERY)

PREPARATIONS OF FIRST RUNGE-KUTTA STEP
DO 3 I = 1, NDIM
   AUX(1, I) = Y(I)
   AUX(2, I) = DERY(I)
   AUX(3, I) = 0.
3   AUX(6, I) = 0.
   H = H + H
   IHLF = -1
ISTEP=0
IEND=0

START OF A RUNGE-KUTTA STEP
4 IF((X+H-XEND)*H)7,6,5
GONE PAST, ADJUST H, SET IEND
5 HH = H
H = XEND - X
IEND = 1
GO TO 7
ON OR WITHIN TOLERANCE, SET IEND
6 IEND = 1
HH = H

KEEP GOING
7 ITEST = 0
9 ISTEP = ISTEP + 1

START OF INNERMOST RUNGE-KUTTA LOOP
J = 1
10 AJ = A(J)
BJ = B(J)
CJ = AJ
IF(J.EQ.4) CJ = .5
DO 11 I = 1, NDIM
R1 = H*DERY(I)
R2 = AJ*(R1-BJ*AUX(6,I))
Y(I) = Y(I) + R2
R2 = R2 + R2 + R2
II
AUX(6,I) = AUX(6,I) + R2 - CJ*R1
IF(J.EQ.4)12,15,15
12 J = J + 1
IF(J.EQ.3)13,14,13
13 X = X + .5*H
14 CALL FCT(X,Y,DERY)
GOTO 13
END OF INNERMOST RUNGE-KUTTA LOOP

TEST OF ACCURACY
15 IF(ITEST)16,16,20
IN CASE ITEST=0 THERE IS NO POSSIBILITY FOR TESTING OF ACCURACY
16 DO 17 I = 1, NDIM
17 AUX(4,I) = Y(I)
ITEST = 1
ISTEP = ISTEP + ISTEP - 2
18 IMHLF = IMHLF + 1
X = X - H
H = .5*H
DO 19 I = 1, NDIM
Y(I) = AUX(1,I)
DERY(I) = AUX(2,I)
19 AUX(6,I) = AUX(3,I)
GOTO 9

IN CASE ITEST=1 TESTING OF ACCURACY IS POSSIBLE
IMOD=ISTEP/2
IF((ISTEP-IMOD-IMOD)21,23,21
CALL FCC(X,Y,DERY)
DO 22 I=I,NDIM
AUX(5,I)=Y(I)
AUX(7,I)=DERY(I)
SOTO 9
COMPUTATION OF TEST VALUE DELT
DELTA=0.
DO 24 I=I,NDIM
DELT=DELT+ABS(AUX(4,I)-Y(I))
IF(DELT.LE.ERR) GO TO 28
ERROR IS TOO GREAT
IF(IHLF.GT.25) GO TO 38
DO 27 I=I,NDIM
AUX(4,I)=AUX(5,I)
ISTEP=ISTEP+ISTEP-4
X=X-H
IEND=3
GOTO 18
RESULT VALUES ARE GOOD
CALL FCC(X,Y,DERY)
DO 29 I=I,NDIM
AUX(1,I)=Y(I)
AUX(2,I)=DERY(I)
AUX(3,I)=AUX(6,I)
Y(I)=AUX(5,I)
AUX(4,I)=AUX(7,I)
DO 31 I=I,NDIM
Y(I)=AUX(1,I)
AUX(4,I)=AUX(2,I)
IF(IEND)32,32,39
INCREMENT GETS DOUBLED
IHLF=IHLF-1
ISTEP=ISTEP/2
H=H+H
IF(IHLF)4,33,33
IMOD=ISTEP/2
IF((ISTEP-IMOD-IMOD)4,34,4
IF(DELT.GT.02*ERR) GO TO 4
IHLF=IHLF - 1
ISTEP=ISTEP/2
H=H+H
GOTO 4
38 HH = O.
GO TO 40
39 XO = X
40 RETURN
REFERENCES


Figure 1. - Schematic drawing of typical test container showing interface position during zero gravity venting.

Figure 2. - Schematic drawing of interface mass transfer venting model.

Figure 3. - Vapor region control volume.

Figure 4. - Liquid region control volume.
Initiation of vent, \( t_1 \)
Termination of vent, \( t_f \)

Figure 5. - Tank pressure response during representative data run. Test fluid, refrigerant C318; nozzle diameter, 0.132 centimeter; average vent rate, 0.5 ullage volume per second.

Figure 6. - Effect of volumetric flow rate on pressure drop for refrigerant 11.

Figure 7. - Effect of volumetric flow rate on pressure drop for refrigerant C318.

Figure 8. - Effect of volumetric flow rate on pressure drop for refrigerant 600.
(a) Normal gravity initial condition. Time from initiation of test, 0 second.

(b) Formation of zero-gravity equilibrium interface. Venting begins, time from initiation of test, 1.90 seconds.

(c) Venting occurring. Time from initiation of test, 4.00 seconds.

(d) Configuration prior to termination of test. No venting; time from initiation of test, 5.16 seconds.

Figure 9. - Typical test in which no bulk boiling occurs. Test fluid, refrigerant C318; nozzle diameter, 0.132 centimeter; initial ullage pressure, \(2.9 \times 10^5\) newtons per square meter; average vent rate, 0.5 ullage volume per second.
Figure 10. - Occurrence of bulk boiling in zero-gravity. Test fluid, refrigerant C318, nozzle diameter, 0.193 centimeter; initial ullage pressure, $2.76 \times 10^5$ newtons per square meter; average vent rate, 1.0 ullage volume per second.
Figure 11. - Schematic diagram of 5- to 10-second zero-gravity facility.
Figure 12. - Control room.

(a) Ultrasonic cleaning system.

Figure 13. - Facility clean room.
(b) Laminar flow work station.

Figure 13. - Concluded.

Figure 14. - Deceleration system.
Figure 15. - Experiment vehicle.

Figure 16. - Experiment assembly tray.
Figure 17. - Vehicle position prior to release.

Figure 18. - Computer program flow chart.