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RESEARCH INVESTIGATION DIRECTED TOWARD EXTENDING THE USEFUL RANGE OF THE ELECTROMAGNETIC SPECTRUM

Sven R. Hartmann, et al

Columbia Radiation Laboratory

Prepared for:

Office of Naval Research
Air Force Office of Scientific Research
Army Electronics Command
National Aeronautics and Space Administration
National Science Foundation

30 June 1974
A powerful new spectroscopic technique, cascade level anticrossing spectroscopy, has been developed and used to determine the complete hyperfine Hamiltonian of the $^4D$ state of rubidium. The anomalous magnetic hyperfine structure of this state is due to an anisotropic core polarization which has both a contact and a spin-dipole component. The spin-dipole component is so large that the sign of the net spin-dipole interaction is reversed with respect to the sign expected for the direct interaction between the nucleus and the valence electron. This is the first instance of a negative spin-dipole interaction ever discovered, and it may help in the formation of a satisfactory theory for the anomalous magnetic interactions in the $^4D$ states of alkali atoms.

A number of new hyperfine interaction constants have been measured for $S$, $P$, $D$, and $F$ states of the alkali atoms.

We have succeeded in obtaining narrow optical pumping signals in alkali vapors at vapor densities much higher than those previously attained, demonstrating the existence of a hitherto unsuspected high density optical pumping regime in which the Zeeman resonance frequency is shifted downward by a large factor and spin-exchange broadening vanishes. This new regime opens the way to miniature
Metastable atoms and ions
Metastable autoionizing atoms
Level-crossing spectroscopy
Optical double-resonance spectroscopy
Collision phenomena
Electron-impact excitation of atoms
Intensity modulation of light
Molecular beam maser spectroscopy
Hyperfine spectroscopy
Carbon monoxide Galaxy survey
Millimeter-wave radio astronomy
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optically pumped devices, such as magnetometers, and affords impor-
tant new possibilities for investigating basic interactions in dense
alkali vapors.

Nuclear magnetic resonance signals from diatomic alkali molecules
have been observed in optically pumped cesium and rubidium vapors.
Some important rate constants have been deduced from the observed
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Hyperfine structure in the rotational spectrum of the heterocyclic
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tudes two to three orders of magnitude smaller than in CaWO4:Nd3+.
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Using the Cr-Al interaction parameters determined from PENDOR studies
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field dependence of the exponential decay of the photon echo, and
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We have measured electron-spin echo-modulation behavior associated
with the 3/2 → 1/2 transition of the 4A2 ground state of ruby.

Stimulated Raman scattering and four-wave parametric mixing has been
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presence of SRS, the laser-beam divergence increases to 1.23 mrad.
Generated Stokes energy appeared to be a function of thallium vapor
pressure. The energy of the dye laser anti-Stokes pulse versus the
product of the laser and Stokes energies is 0.96 ± 0.02.
13. ABSTRACT (cont'd)

We have studied two of the cascading single-photon fluorescences from cesium gas excited by two-photon absorption. The fluorescent pulsewidth is two to four times that of the laser at low incident power levels.

After reanalyzing published experimental data regarding the relaxation behavior of two- and three-pulse electron-spin echoes in dilute systems, we find excellent agreement with our recently published theory of spectral diffusion decay.

We have confirmed that the superradiant condition is unstable by both a theoretical mode analysis and straightforward numerical computation.

We have found a clear singularity in the temperature coefficient of viscosity for He\textsuperscript{4} at the superfluid transitions (T\textsubscript{c}). The reduced viscosity difference $\Delta \eta/\eta$ depends on the reduced temperature difference $\xi = 2/3$ below T\textsubscript{c}, and $x = 0.9$ to 1.1 above T\textsubscript{c}. An experiment to detect the quantized rotation of superfluid helium by a thermal modulation technique is underway, and an apparatus to study mechanical properties of superfluid He\textsuperscript{3} is nearing completion.
Physical research in fields in which microwave frequency techniques are employed; the development of microwave electronic and circuit devices.

The research reported in this document was made possible through support extended the Columbia Radiation Laboratory, Columbia University, by the Joint Services Electronics Program (U. S. Army Electronics Command and U. S. Army Research Office, Office of Naval Research, and the Air Force Office of Scientific Research) under Contract DAAB07-69-C-0383.

Submitted by: S. R. HARTMANN and W. HAPPER, Co-Directors

Coordinated by: A. Owen, Editor

COLUMBIA UNIVERSITY
Division of Government-Aided Research

New York, N. Y. 10027

June 30, 1974

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The names of the authors are arranged alphabetically.
PUBLICATIONS AND REPORTS

Publications


1. Present Address: Bell Telephone Laboratories, Inc., Holmdel, New Jersey 07733.


3. Present Address: Department of Physics, University of British Columbia, Vancouver, Canada.


5. Present Address: Department of Physics, Chalmers University of Technology, Goteborg, Sweden.


8. Present Address: Department of Physics, City College of the CUNY, New York, New York 1003.


Papers by CRL Staff Members Presented at Scientific Meetings


S. R. Hartmann and P. Hu, "Theory and Support for an Uncorrelated Sudden-Jump Model of Spectral Diffusion Decay."


Lectures

S. Chandra, "Photon Echoes and PENDOR," Seminar, Department of Physics, Fordham University, Bronx, New York, April 25, 1974.


P. Thaddeus, "The Unidentified Interstellar Molecules," Colloquium, Department of Physics, University of Texas, Austin, Texas, January 22, 1974; id., Colloquium, Department of Physics, University of Texas, Dallas, Texas,


Radiation Laboratory Seminars

Meetings are held weekly at Columbia University, New York, New York, during the academic year and are open to all members of the Physics Department. Guest speakers are invited to discuss work in the general area of the research in the Columbia Radiation Laboratory.


D. Klepner, Massachusetts Institute of Technology, "Magnetic Interactions in Alkali-Rare-Gas Molecules," March 1, 1974.


I. Lowe, University of Pittsburgh, "A New Method for Measuring Short Time Behavior of Free Induction Decay with Applications to CaF$_2$ and NH$_4$Cl," April 5, 1974.


A powerful new spectroscopic technique, cascade level anticrossing spectroscopy, has been developed and used to determine the complete hyperfine Hamiltonian of the 4p state of rubidium. The anomalous magnetic hyperfine structure of this state is due to an anisotropic core polarization which has both a contact and a spin-dipole component. The spin-dipole component is so large that the sign of the net spin-dipole interaction is reversed with respect to the sign expected for the direct interaction between the nucleus and the valence electron. This is the first instance of a negative spin-dipole interaction ever discovered, and it may help in the formation of a satisfactory theory for the anomalous magnetic interactions in the D states of alkali atoms.

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I. ATOMIC PHYSICS

A. HYPERFINE STRUCTURE OF EXCITED S STATES OF POTASSIUM, RUBIDIUM, AND CESIUM*

(R. Gupta, W. Happer, L. Lam, S. Svanberg)

We have completed measurements of the hyperfine structure (hfs) of the first and second excited S states of K$^{39}$ and K$^{41}$, and of the first, second, and third excited states of Rb$^{85}$, Rb$^{87}$, and Cs$^{133}$. These systematic measurements of the hfs of several excited S states of each alkali metal have revealed some very interesting properties of these states. These measurements have been performed by the method of cascade radio-frequency spectroscopy, a technique developed in this Laboratory. This method of reaching the optically inaccessible states has been described in detail in the previous Progress Report, and is also illustrated in Fig. 1.

The results of our measurements are shown in Table I. For completeness, we have included in Table I the well-known ground-state hfs constants of the alkali metal atoms. We have also included the hfs value$^{(2)}$ for the $4^2S_{1/2}$ state of sodium (see p. 10 below). Recently, Rosén and Lindgren$^{(3)}$ calculated hfs-coupling constants using restricted self-consistent field methods for the sequences of 3 and P states of alkali metal atoms. Also, Norcross$^{(4)}$ has calculated the A values for the 6, 7, 8, and 9 S states of cesium using a semiempirical model potential. Both of these calculations, as well as the results obtained from the semiempirical formula for S states, allow us to compare our experimental values with the theoretical A values for sequences of S states. Some interesting conclusions can be drawn from these comparisons.

Columns 4 through 10 of the table list some of the theoretical
Fig. 1. Schematic illustration of the method of cascade radio-frequency spectroscopy. The polarized P states are created by excitation with circularly polarized resonance light. The excited S states are populated and polarized by the spontaneous decay of these P states. The polarization of the excited S states is monitored by observing the circular polarization of the fluorescent light. Rf resonances in these states are observed as a decrease in the polarization of the fluorescent light.
### TABLE I. Experimental and theoretical values of the hyperfine structure coupling constant A.

<table>
<thead>
<tr>
<th>Isotopo</th>
<th>State</th>
<th>( A_{\text{exp}} ) (MHz)</th>
<th>( A_{\text{HF}} ) (b)</th>
<th>( A_{\text{CSHFS}} ) (b)</th>
<th>( A_{\text{RHF} + \text{CP}} ) (c)</th>
<th>( A_{\text{RHF} + \text{ACP}} ) (b)</th>
<th>( A_{\text{SIMP}} ) (a)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Na(^{23})</td>
<td>( 3^2S_{1/2} )</td>
<td>705.0</td>
<td>995.4</td>
<td>631.1</td>
<td>840.67</td>
<td>814.1</td>
<td>777.54</td>
</tr>
<tr>
<td></td>
<td>( 4^2S_{1/2} )</td>
<td>202(3) (a)</td>
<td>228.45</td>
<td>151.8</td>
<td>198.9</td>
<td>198.9</td>
<td>187.79</td>
</tr>
<tr>
<td>K(^{39})</td>
<td>( 4^2S_{1/2} )</td>
<td>230.85</td>
<td>246.3</td>
<td>150.9</td>
<td>222.0</td>
<td>196.6</td>
<td>184.49</td>
</tr>
<tr>
<td></td>
<td>( 5^2S_{1/2} )</td>
<td>55.50(60)</td>
<td>59.98</td>
<td>39.76</td>
<td>56.57</td>
<td>53.42</td>
<td>29.36</td>
</tr>
<tr>
<td></td>
<td>( 6^2S_{1/2} )</td>
<td>21.81(10)</td>
<td>23.62</td>
<td>16.15</td>
<td>22.38</td>
<td>21.72</td>
<td>11.94</td>
</tr>
<tr>
<td>K(^{41})</td>
<td>( 4^2S_{1/2} )</td>
<td>127.00</td>
<td>136.0</td>
<td>82.94</td>
<td>122.0</td>
<td>108.1</td>
<td>101.40</td>
</tr>
<tr>
<td></td>
<td>( 5^2S_{1/2} )</td>
<td>20.75(75)</td>
<td>32.85</td>
<td>21.85</td>
<td>31.09</td>
<td>29.36</td>
<td>11.94</td>
</tr>
<tr>
<td></td>
<td>( 6^2S_{1/2} )</td>
<td>12.03(40)</td>
<td>12.99</td>
<td>8.076</td>
<td>12.30</td>
<td>11.94</td>
<td>11.94</td>
</tr>
<tr>
<td>Rb(^{85})</td>
<td>( 5^2S_{1/2} )</td>
<td>1011.9</td>
<td>1084.8</td>
<td>660.6</td>
<td>1003</td>
<td>856.9</td>
<td>793.54</td>
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<tr>
<td></td>
<td>( 6^2S_{1/2} )</td>
<td>239.3(1.2)</td>
<td>261.6</td>
<td>176.1</td>
<td>254.5</td>
<td>237.5</td>
<td>216.9</td>
</tr>
<tr>
<td></td>
<td>( 7^2S_{1/2} )</td>
<td>94.93(59)</td>
<td>103.9</td>
<td>71.23</td>
<td>101.3</td>
<td>97.58</td>
<td>49.25</td>
</tr>
<tr>
<td></td>
<td>( 8^2S_{1/2} )</td>
<td>45.5(2.0)</td>
<td>51.6</td>
<td>36.15</td>
<td>50.78</td>
<td>49.25</td>
<td>31.09</td>
</tr>
<tr>
<td>Rb(^{87})</td>
<td>( 5^2S_{1/2} )</td>
<td>3417.3</td>
<td>3675.6</td>
<td>2266</td>
<td>3300</td>
<td>2904</td>
<td>2689.4</td>
</tr>
<tr>
<td></td>
<td>( 6^2S_{1/2} )</td>
<td>809.1(5.0)</td>
<td>885.6</td>
<td>596.7</td>
<td>862.5</td>
<td>804.0</td>
<td>2703.4</td>
</tr>
<tr>
<td></td>
<td>( 7^2S_{1/2} )</td>
<td>318.1(3.2)</td>
<td>351.6</td>
<td>241.4</td>
<td>343.4</td>
<td>330.7</td>
<td>2703.4</td>
</tr>
<tr>
<td></td>
<td>( 8^2S_{1/2} )</td>
<td>158.0(3.0)</td>
<td>174.9</td>
<td>122.5</td>
<td>172.3</td>
<td>166.9</td>
<td>216.9</td>
</tr>
<tr>
<td>Cs(^{133})</td>
<td>( 6^2S_{1/2} )</td>
<td>2298.1</td>
<td>2342.3</td>
<td>1519</td>
<td>2209</td>
<td>1763</td>
<td>1854.3</td>
</tr>
<tr>
<td></td>
<td>( 7^2S_{1/2} )</td>
<td>346.3(3.0)</td>
<td>570.8</td>
<td>412.5</td>
<td>551.7</td>
<td>516.0</td>
<td>579.8</td>
</tr>
<tr>
<td></td>
<td>( 6^2S_{1/2} )</td>
<td>218.9(1.6)</td>
<td>230.5</td>
<td>172.1</td>
<td>239.3</td>
<td>218.1</td>
<td>231.9</td>
</tr>
<tr>
<td></td>
<td>( 5^2S_{1/2} )</td>
<td>109.5(2.0)</td>
<td>115.8</td>
<td>87.55</td>
<td>120.9</td>
<td>112.0</td>
<td>116.3</td>
</tr>
</tbody>
</table>

(b) A. Rosen and I. Lindgren, Physica Scripta 6, 109 (1972).
Fig. 2. A pictorial representation of our experimental results and some of the theoretical values of the hyperfine interaction constant $A$. Ratios of the experimental and theoretical values of $A$ have been plotted against the principal quantum numbers of the states. The symbol SE represents the results of the semiempirical formula, while RHS, RHF, and ROHFS represent the relativistic Hartree-Slater, Hartree-Fock, and optimized Hartree-Fock-Slater schemes, respectively. The symbol RHF-CP is the results of the relativistic Hartree-Fock method, including core-polarization effects, while RHF-RCP represents RHF-CP results corrected for relativistic effects in the core polarization term. The symbol BG is the results of the Brueckner-Goldstone manybody perturbation theory, while S-EMP stands for the results of a semiempirical model potential.
A values. Column 4 gives the values of the magnetic dipole-coupling constants calculated from the semiempirical formula (5)

\[ A = \frac{8}{3} \frac{\alpha^2}{n_0^3} \frac{Z g_I}{g_I} \left( 1 - \frac{dg}{dn} \right) F_r(j, Z)(1 - \epsilon)(1 - \delta). \]  

(1)

Here, \( n_0 \) is the effective principal quantum number of the state, \( \sigma \) is the Rydberg correction, \( F_r(j, Z) \) is the relativistic correction, and \( \epsilon \) and \( \delta \) are the corrections required by the distribution effects over the nuclear volume, respectively. All other symbols in Eq. (1) have their usual meaning. Both the effective quantum number \( n_0 \) and the quantity \( (dg/dn) \) are deduced from the measured binding energies of the atomic states. (6) We have used the values of the correction terms \( F_r(j, Z) \), \( \epsilon \), and \( \delta \) listed in Kopfermann. (7) Columns 5, 6, and 7 of Table I give the \( A \) values calculated by Rosén and Lindgren using relativistic Hartree-Fock, Hartree-Slater, and optimized Hartree-Fock-Slater schemes, respectively. Column 8 shows the \( A \) values calculated by Tterlikkis et al. (8) They have taken into account both the core polarization and the relativistic effects, the former by a moment-perturbation procedure and the latter by a relativistic Hartree-Fock method. These calculations have been done only for the ground state of the alkali metal atoms. The ground-state hfs of sodium has also been calculated by Lee et al., (9) using the Brueckner-Goldstone manybody perturbation theory (also shown in column 8). Tterlikkis' calculation does not take into account the relativistic effects in the core-polarization term itself. Rosén and Lindgren have applied a relativistic correction to Tterlikkis' core-polarization term, and the resulting \( A \) values are shown in column 9. The results of Norcross' (10) calculations using a semiempirical model potential are shown in column 10. In this calculation, two parameters in the model potential were chosen such that the spectroscopic term values of the \( 6^2S \) and the \( 6^2P \) states of Cs agree with those calculated using this potential. A graphical summary of the results of various calculations is shown in Fig. 2. The ratio of the theo-
Theoretical and experimental A values have been plotted against the principal quantum numbers for various states. Referring to Fig. 2, we can make the following observations:

The values of A calculated by the semiempirical formula always lie higher than the experimental values. If Rosén and Lindgren's relativistic correction factors are used instead of those of Kopfermann, the theoretical A values will be even higher; i.e. the disagreement between the theoretical and experimental values will increase. Considering the simplicity and generality of the semiempirical formula, we find that the agreement with the experimental values that this formula provides (to within about 10%) is remarkable.

Of the restricted self-consistent field methods, the relativistic Hartree-Slater scheme gives the best agreement with the experimental A values, and the overall agreement is very good. It is worth noting that Rosén and Lindgren have not explicitly taken the core polarization into account, as their principal aim was to calculate new and more accurate relativistic correction factors for $^2S$ and $^2P$ states. Inclusion of core polarization explicitly will perhaps move all these theoretical hfs values somewhat higher. It is interesting that the ratio $\frac{A_{\text{theo}}}{A_{\text{exp}}}$ systematically increases with increasing principal quantum number for all alkali-metal atoms that we have investigated and for all three schemes that Rosén and Lindgren have used. They have also calculated electron-binding energies by using the relativistic Hartree-Fock, Hartree-Slater, and the optimized Hartree-Slater schemes. We find that the ratios of the theoretical and experimental binding energies have exactly the same trend with the principal quantum number $n$ as do the ratios of the theoretical and experimental hfs coupling constants $A$.

Teterlikis' A values for the ground state, calculated by the relativistic Hartree-Fock method and including core-polarization effects, are small compared to the experimental values. If the relativistic correction is applied to the core-polarization term, the resulting A values are seen to agree better with the experimental values. Lee's A value for the ground state of sodium, calculated by the Brueckner-Goldstone manybody perturbation theory, agrees very
well with the experiment. This may indicate that electron correlation effects are quite important for $S$ state hyperfine structure. An obvious question, however, is how well similar Brueckner-Goldstone calculations would work for the higher $S$ states of sodium and for the $S$ states of the other alkali atoms. Would the inclusion of electron-correlation effects remove the striking increase in $A_{\text{theo}}/A_{\text{exp}}$ with principal quantum number?

The results of Norcross' calculations for the $S$ states of Cs using a semiempirical model potential agree very well with the experimental values. It is remarkable that the ratio of Norcross' values to the experimental values is nearly independent of the principal quantum number, in striking contrast to the results of the self-consistent field calculations.

In summary, comparison of our measured values with various theoretical values shows that, although many creditable attempts have been made to calculate the $S$ state hfs intervals of alkali atoms, no really precise theory seems to exist yet.

This project is now complete. Higher excited $S$ states are now being investigated by dye-laser spectroscopy, as described in Part G of this Section.

*This research was also supported by the Air Force Office of Scientific Research under Grant AFOSR-72-2180.

(1) CRL Progress Report, June 30, 1973, p. 3.
(7) H. Kopfermann, op. cit., p. 132 and 136.
B. HYPERFINE STRUCTURE OF EXCITED S STATES OF SODIUM*
(R. Gupta, W. Happr, K. Liao)

The measurement of the hyperfine structure of the 4S 1/2 state of Na 23 by cascade radio-frequency spectroscopy has been completed, and the results have been published.\(^{(1)}\)

One of our experimental resonance curves is shown in Fig. 3. This resonance results from the \(m_F = -2 \rightarrow m_F = -1, \Delta F = 0\) transition at about 147.5 MHz in an external field of about 117 G. At the peak of the resonance, the polarization of the fluorescent light decreases by about 10%. Figure 4 shows a similar resonance at 231.5 GHz field strength. This resonance also comes from the \(m_F = -2 \rightarrow m_F, \Delta F = 0\) transition, but the rf field has a frequency of about 405 MHz. The sharp dip at the low-field side of the 4 2 S 1/2 resonance results from a 4 2 P 3/2 state resonance. Unfortunately, a transition in the 3 2 P 3/2 state accidentally overlaps the 4 2 S 1/2 state transition at this field. Although the 3 2 P 3/2 resonance should be very weak and very broad, as the lifetime of this state is only 16 nsec, we are not sure that the 3 2 P 3/2 resonance does not slightly affect the observed position of the 4 2 S 1/2 state resonance. For this reason, we have used only the data for the 147-MHz transition frequency to deduce our final results. The 405-MHz resonance, however, serves to confirm our identification of the 4 2 S 1/2 resonance. For about 25 curves of the type shown in Fig. 3, we have deduced the hfs of the 4 2 S 1/2 state from the magnetic field at which these resonances are seen. We find, for the magnetic dipole coupling constant, a value of

\[
A(4^2S_{1/2}) = 202 \pm 3 \text{ MHz.}
\]

*This research was also supported by the Air Force Office of Scientific Research under Grant AFOSR-72-2180.
Fig. 3. Rf resonance curve for the $m_r = -2 - m_p = -1, \Delta F = 0$ transition in the $4^2S_{1/2}$ state of Na$^{23}$. The transition frequency is 147.8 MHz. This curve represents ~3 hr of signal averaging.
Fig. 4. Rf resonance curve due to the $m_F = -2 \rightarrow m_F = -1$, 
$\Delta F = 0$ transition at 405-MHz frequency in the 
$42S_{1/2}$ state of Na$_{23}$. 

$\nu = 405 \text{ MHz}$
C. HYPERFINE STRUCTURE OF EXCITED D\textsubscript{5/2} AND D\textsubscript{3/2} STATES OF ALKALI ATOMS\textsuperscript{*}

(R. Gupta, W. Happer, C. Tai)

We have measured the hyperfine structures of some of the excited D states of rubidium and cesium. A compilation of these results appears in Table II. The double-resonance data are obtained from the results of several repeated measurements, and the quoted error bars represent three standard deviations in the statistical spread of the results plus an allowance for possible systematic errors, such as errors in the magnetic-field calibration, etc. The hyperfine structure of the \(8\text{P}_{1/2}\) state of cesium was also measured and is given in Table II. The methods we used to investigate the hfs of the D states are cascade-double-resonance, cascade-level-crossing, and cascade-decoupling spectroscopy. These were all discussed in last year's Progress Report.\textsuperscript{(1)} Additional experimental results of this work are given in Figs. 5-13.

This year we have developed a new and powerful method to determine the sign of the hfs constant. In the measurement of the hyperfine constant of the Cs 6D\textsubscript{3/2} state, we excite the ground-state atoms into the \(8\text{P}_{1/2}\) state with circularly polarized helium 3888-Å light; we then get polarized D state atoms by the spontaneous decay of the atoms in the \(8\text{S}_{1/2}\) state from Fig. 14. From Fig. 14, we see that we can approximate the excitation process by white light excitation from the ground-state \(F = 4\) sublevel alone. After simple calculation, at a magnetic field low for the ground state but high for the associated excited states, we find out that, with helium \(\sigma^+\) exciting light, the cesium \(8\text{P}_{1/2}\) state is polarized, with the \(m_J = -1/2\) sublevels unpopulated and the population of the \(m_J = +1/2\) sublevels proportional to \((I + 1/2 + m_J)\). If rf transitions are induced between the sublevels, the resonance signals corresponding to sublevels with different \(m_J\)
### TABLE II. Hyperfine coupling constants $A$ measured in this work.

<table>
<thead>
<tr>
<th>Element</th>
<th>State</th>
<th>Method</th>
<th>Measured $A$ (in MHz)</th>
<th>Calculated $A$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rb$^{87}$</td>
<td>$5^2D_{3/2}$</td>
<td>Double-resonance and decoupling</td>
<td>14.43 ± 0.12</td>
<td>13.57</td>
</tr>
<tr>
<td>Rb$^{85}$</td>
<td>$5^2D_{5/2}$</td>
<td>Double-resonance and decoupling</td>
<td>-7.44 ± 0.06</td>
<td>5.81</td>
</tr>
<tr>
<td>Cs$^{133}$</td>
<td>$6^2D_{3/2}$</td>
<td>Level-crossing and decoupling</td>
<td>16.5 ± 0.3</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$6^2D_{3/2}$</td>
<td>Double-resonance and decoupling</td>
<td>16.38 ± 0.05</td>
<td>9.4</td>
</tr>
<tr>
<td></td>
<td>$6^2D_{5/2}$</td>
<td>Decoupling</td>
<td>-3.0 ± 1.0</td>
<td>4.0</td>
</tr>
<tr>
<td></td>
<td>$8^2P_{1/2}$</td>
<td>Decoupling and double-resonance</td>
<td>42.97 ± 0.10</td>
<td></td>
</tr>
</tbody>
</table>
Fig. 5. Observed radio-frequency resonances in Cs$^{133}$. The symbols $\alpha$ and $\beta$ refer to rf resonances in the $8p_{1/2}$ and $6d_{1/2}$ states, respectively. One division on the ordinate corresponds to about a 5% change in the polarization of $\sigma^-$ light and an 8% change in the $\sigma^+$ light.
Fig. 6. Observed radio-frequency resonances of Rb$^{87}$ $5D_{3/2}$ states with Rb$^{87}$ lamp. The resonance at highest H-field is an $8P_{1/2}$ resonance. Radio frequency is 403 MHz.
Fig. 7. Observed radio-frequency resonances of $\text{Rb}^{87} 5D_{5/2}$ states.
Fig. 8. Observed radio-frequency resonances of Rb$^{85}$ 5D$_{5/2}$ states. Radio frequency is 403 MHz.
Fig. 9. Observed radio-frequency resonances of Rb$^{85}$ $5D_{3/2}$ states. Radio frequency is 403 MHz.
Fig. 10. Observed radio-frequency resonances of Rb\(^{87}\) 5D states with Rb\(^{85}\) lamp. The letters A, B, C, and D refer to radio-frequency resonances in the 7P\(_{3/2}\), 5D\(_{5/2}\), 5D\(_{3/2}\), and 7P\(_{1/2}\) states, respectively.
Fig. 11. Cascade-decoupling data for the $5D_{5/2}$ states of Rb$^{85}$. The points are experimental data. The solid lines are calculated from the hyperfine structure parameters indicated in the figure. These data determine the sign and the approximate magnitude of the D state $A$ value.
Fig. 12. Cascade-decoupling data for the $5D_{3/2}$ states of Rb$^{85}$. The points are experimental data. The solid lines are calculated from the hyperfine structure parameters indicated in the figure. These data determine the sign and the approximate magnitude of the D state A value.
Fig. 13. Decoupling of Rb$^{87}$ 5D$_{5/2}$ states with exciting light linearly polarized in the direction of the magnetic field.
Fig. 14. Helium and cesium lineshapes. (From P. Rabinowitz and S. Jacobs, Quantum Electronics, Proceedings of the Third International Congress, 1963 Paris Conference.)
Fig. 15. Process of cascade double resonance of the 8P_{1/2} state of Cs$^{133}$; the Cs cell is excited with circularly polarized light from a helium lamp. The magnetic field is ~700 gauss. The relative amplitude of the resonance signals can be used to determine the sign of the A values of the P and S states.
Fig. 16. Plot of measured $A$ values of cesium D states vs (binding energy)$^{3/2}$. 
Fig. 17. Plot of measured $A$ values of Rb$^{87}$ D states vs (binding energy)$^{3/2}$.  

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<table>
<thead>
<tr>
<th>Atom</th>
<th>State</th>
<th>A</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rb$^{87}$</td>
<td>4 $D_{5/2}$</td>
<td>(-) 16.9 (6)</td>
</tr>
<tr>
<td></td>
<td>6 $D_{3/2}$</td>
<td>(?) 7.72 (20)</td>
</tr>
<tr>
<td></td>
<td>6 $D_{5/2}$</td>
<td>(?) 3.6 (7)</td>
</tr>
<tr>
<td></td>
<td>7 $D_{3/2}$</td>
<td>(?) 4.52 (3)</td>
</tr>
<tr>
<td></td>
<td>7 $D_{5/2}$</td>
<td>(?) 2.2 (5)</td>
</tr>
<tr>
<td></td>
<td>8 $D_{3/2}$</td>
<td>(?) 2.85 (3)</td>
</tr>
<tr>
<td></td>
<td>8 $D_{5/2}$</td>
<td>(?) 1.2 (2)</td>
</tr>
<tr>
<td></td>
<td>8 $^2D_{3/2}$</td>
<td>(?) 3.98 (12)</td>
</tr>
<tr>
<td></td>
<td>8 $^2D_{5/2}$</td>
<td>(?) 0.9 (4)</td>
</tr>
<tr>
<td></td>
<td>9 $^2D_{3/2}$</td>
<td>(?) 2.37 (3)</td>
</tr>
<tr>
<td></td>
<td>9 $D_{5/2}$</td>
<td>(?) 0.3 (2)</td>
</tr>
<tr>
<td></td>
<td>10 $D_{3/2}$</td>
<td>(?) 1.52 (3)</td>
</tr>
<tr>
<td></td>
<td>10 $D_{5/2}$</td>
<td>(?) 0.4 (2)</td>
</tr>
</tbody>
</table>

(a) L. Lam (private communication); S. Svanberg, *Proceedings, Laser Spectroscopy Conference, Vail, Colorado, 1973.*
will have different amplitudes. If we sweep the rf frequency while keeping the magnetic field fixed, we get a resonance pattern as shown in Fig. 15. The relative amplitude determines the sign of the hfs constant. In the case of cascade excitation, since the nuclear polarization is not changed at all by spontaneous decay at high field, the nuclear polarization will be the same throughout the cascade process. Thus we can determine the sign of the hfs constant of the D state by this method. The whole process is illustrated in Fig. 15.

The experimental results of double-resonance experiments with narrow band excitation are shown in Figs. 5 and 10. The sign of the hfs constants determined by this method is consistent with that given by the method of cascade decoupling, discussed previously, and no complicated computer calculation is needed in this method.

We have compared our results with some of the recently measured hfs of other excited D states of rubidium and cesium. A compilation of these results is shown in Table III. A plot of the measured value of A versus the ionization energy, $\varepsilon_n$, raised to the 3/2 power, is given in Figs. 16 and 17. The number n is the principal quantum number. Note that the sign of the hyperfine constants of the first, third, and higher D states are not fully determined. The fact that all the points lie in a straight line might indicate that all the D$_{5/2}$ hyperfine states are inverted and all the D$_{3/2}$ states are normal. The hyperfine structures of the excited D states of Rb and Cs depend on n only through the simple $(\varepsilon_n)^{3/2}$ relation, contrasting with the fine structures that do not scale according to this function. This completes our investigation of the hyperfine structure of the second excited D$_{5/2}$ and D$_{3/2}$ states of Rb and Cs.

*This research was also supported by the Air Force Office of Scientific Research under Grant AFOSR-72-7180.

(1) CRL Progress Report, June 30, 1973, p. 10.
Fig. 18. Rb$^{85}$ cascade decoupling curve compared with fitted theoretical curves for $A(4^2D_{5/2}) = +5$ MHz and $-5$ MHz. The cascade scheme is shown in the upper right corner.
D. HYPERFINE STRUCTURE OF THE FIRST EXCITED S AND D STATES OF ALKALI ATOMS

(R. Gupta, W. Happer, L. Lam)

We have already measured and reported the absolute magnitude of the magnetic dipole hfs constants for the \( \text{4}^2\text{D}_{5/2} \) states of Rb. We have determined the sign by measuring the change in the polarization of the fluorescence as the atoms decouple under increasing magnetic field. The data are shown with the theoretical curves in Fig. 18. Agreement between the experimental and theoretical curves is not good, although the curve for a negative value has the same general structure as the experimental curve. The discrepancy may result from inaccuracy in the theoretical branching ratios and imperfection of the circular polarizers and analyzers. We independently measured the relative rf-resonance signal amplitudes with nonwhite excitation (see Part C of this Section). Results for Rb\(^{85}\) and Rb\(^{87}\) are shown in Figs. 19 and 20, respectively. The change in the relative amplitude of the rf resonances is prominent for Rb\(^{85}\) and is clearly in opposite directions for the \( \text{4}^2\text{D}_{5/2} \) and \( \text{6}^2\text{P}_{3/2} \) states. Since the hfs of the \( \text{6}^2\text{P}_{3/2} \) state is known to be normal, this suggests that the hfs of the \( \text{4}^2\text{D}_{5/2} \) is inverted.

We have also performed cascade rf spectroscopy on the \( \text{4}^2\text{D}_{3/2} \) states of Rb\(^{85}\) and Rb\(^{87}\); the results are shown in Fig. 21. The \( \text{4}^2\text{D}_{3/2} \) resonances are not of equal magnitude, and some of the smaller resonances cannot be resolved from the noise because of the recoupling of the electronic (\( J \)) and nuclear (\( I \)) spins in the fluorescing \( \text{5}^2\text{P}_{1/2} \) state. The fact that the \( m_I = -I + 1/2 \) group of resonances is small indicates that the magnetic dipole hfs constant for the \( \text{4}^2\text{D}_{3/2} \) state of Rb is positive. The \( A \) values we obtained from the data, +7.3(5) MHz for Rb\(^{85}\) and +25.1(6) for Rb\(^{87}\), are significantly smaller than those extrapolated from the higher-lying \( \text{2}^2\text{D}_{3/2} \) state. Values for the coupling constants of both \( \text{4}^2\text{D} \) states are given in Table IV. The hfs measurements of the first excited S states of K, Rb, and Cs have been completed, and results are discussed in Part A of this.
Fig. 19. The $6^2P_{3/2}$ and $4^2D_{5/2}$ rf resonances with an Rb$^{85}$ cell excited by an Rb$^{85}$ lamp. The $4^2D_{5/2}$ resonances are not resolved here. The relative amplitudes of the $P_{3/2}$ and $D_{5/2}$ resonances change in opposite directions as excitation changes from $\sigma_+$ to $\sigma_-$. 

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Fig. 20. The $^6\text{P}_{3/2}$ (A, B, C, F) and $^4\text{D}_{5/2}$ (D, E, G, H) rf resonances with an Rb$^{87}$ cell excited by an Rb$^{85}$ lamp.
Fig. 21. a) The $^2\text{D}_{3/2}$ rf resonances of Rb$^{85}$ shown with three $^2\text{P}_{1/2}$ resonances, A, C, and E. Point C overlaps with some of the $^2\text{P}_{1/2}$ resonances, while B and D are identified $^2\text{D}_{3/2}$ resonances.

b) Rb$^{87}$ $^2\text{D}_{3/2}$ rf resonances.
TABLE IV. Magnetic dipole hyperfine coupling constants of the $^{42}D$ states of rubidium.

<table>
<thead>
<tr>
<th></th>
<th>$\text{Rb}^{85}$</th>
<th>$\text{Rb}^{87}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$^{42}D_{3/2}$</td>
<td>$+7.3(5)$ MHz</td>
<td>$+25.1(6)$ MHz</td>
</tr>
<tr>
<td>$^{42}D_{5/2}$</td>
<td>$-5.2(3)$ MHz</td>
<td>$-16.9(6)$ MHz</td>
</tr>
</tbody>
</table>
Section.

**Program for the next interval:** We will measure the hfs of the $^5D_{3/2}$ and $^5D_{5/2}$ states of cesium.

*This research was also supported by the Air Force Office of Scientific Research under Grant AFOSR-72-2180.


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**E. CASCADE LEVEL ANTICROSSING SIGNALS**

(R. Gupta, W. Happer, K. Liao)

We have developed a cascade level anticrossing technique which can be used to measure the fine structures and to determine the complete hyperfine Hamiltonians of the states of atoms. In this method, two fine structure sublevels of an atom are excited at different rates by cascading from a higher state. In the absence of hyperfine structure, the fine structure levels can be made to "cross" by tuning them to the same energy with an external magnetic field. However, if hyperfine structure is present, each fine structure sublevel is split into $(2I + 1)$ hyperfine sublevels ($I$ is the nuclear spin), and those sublevels which have the same total magnetic quantum number $m_F = m_J + m_I$ may be prevented from crossing by the hyperfine interactions. Instead of crossing, the levels repel one another, and the wavefunctions of the two substates interchange their identities as the magnetic field strength is swept through the region of closest approach. This state mixing will equalize the population differences between these two particular sublevels. During one more cascading process, the dipole selection rules allow us to monitor the fluorescence which comes only from one of the two sublevels involved. Any changes in the detected fluorescence can be used to deduce the information about fine and hyperfine structures of the state. The $4D$ state of the rubidium alkali atom, due to its anomalously small fine structure splitting, serves as a good example to demonstrate our new
method.

Figure 22 shows the energy-level scheme of the relevant states of the rubidium atom and the Zeeman splittings of the fine structure levels of $4^2D$ state in a magnetic field. The Rb$^{85}$ (or Rb$^{87}$) atoms in the $5S_{1/2}$ ground states are excited to $6P$ states by the $\sigma$-polarized light of the second resonance lines of Rb$^{87}$ atoms in a microwave lamp. In the high field region where the nuclear-spin angular momentum, $I$, and the electronic-spin angular momentum, $J$, are decoupled, the magnetic sublevels of the $6P$ state that have higher $m_J$ values are more strongly populated than those of lower $m_J$ values. This follows from considerations of the lamp profile and the atomic absorption profile, and also from the selection rules for excitation by $\sigma$-polarized light. After spontaneous decay, the major part of this population imbalance is carried over to the $4D$ state. Now, application of an external magnetic field at about 3800 gauss will cause crossing of the $J = 3/2, m_J = 1/2$ and $J = 5/2, m_J = 5/2$ fine structure levels of the $4D$ term. Figure 23 shows the eight hyperfine structure levels of Rb$^{87}$ that are involved in this crossing. The static perturbation which couples the levels and causes them to "anticross" is provided in this case by the electric quadrupole interaction between the nucleus and the electrons. Coupling occurs between pairs of levels having the same value of $m_F = m_J + m_I$, but different values of $m_I$. This coupling mixes the wavefunctions of the hyperfine sublevels and equalizes the population imbalance between them.

Because the fine structure sublevel with $m_J = 5/2$ of the $^2D_{5/2}$ state remains a pure $^2D_{5/2}$ state in high magnetic fields, atoms in this sublevel cannot decay to a $^2P_{1/2}$ state because of the dipole selection rule $\Delta m_J = 0, \pm 1$. However, in the neighborhood of 3800 gauss, the electric quadrupole interaction can cause the electrons to jump from the state with $m_J = 1/2$ while the magnetic quantum number of the nucleus changes from $m_I$ to $(m_I + 2)$ to conserve angular momentum. Since the initial and final levels are "crossed," no energy has to be supplied and the static quadrupole interaction is adequate to cause the transition, provided that the quadrupole interaction energy is greater than the natural width, $\gamma/\tau$, of the crossing.
Fig. 22.  

a) The energy-level scheme of the relevant states in this work; 

b) Zeeman splittings of the fine structure levels in the $4^2D$ state of Rb in a magnetic field.
Fig. 23. The hyperfine levels involved at the 3800-G crossing in the $4^2D$ state of Rb$^{87}$. Circles indicate the positions of the anticrossings.
Fig. 24. Typical anticrossing signal recordings with $\sigma$ exciting light. ($\text{Rb}^{87}$ resonance line has been used in both cases.) The magnitude of the anticrossing signals depends, among other things, on the polarization and the line profile of the exciting light.
levels (τ is the radiative lifetime of the 4D state atoms). When an atom has jumped from the \( m_J = 5/2 \) to the \( m_J = 1/2 \) sublevel, it is free to decay to the lower \( \text{P}_{1/2} \) state, and the anticrossing should therefore be detectable as an increase in the fluorescence from the \( \text{P}_{1/2} \) state. In the case of \( \text{Rb}^{85} \) there are four such anticrossings corresponding to the \( \Delta m_J = 2 \) crossing between the \( m_J = 5/2 \) and \( m_J = 1/2 \) fine structure levels of the \( 4^2 \text{D} \) state. In \( \text{Rb}^{87} \) there are only two anticrossings in the same region. Because the cascading steps wash out the transverse coherence of the excited atom, no level-crossing signals will be present to distort the anticrossing signals.

We modulate the magnetic field as the main field sweeps through the interesting region. A phase-sensitive lock-in technique is used in the detection process to suppress the background noise. We also use an NMR gaussmeter to measure the field very accurately.

Our preliminary experimental data for \( \text{Rb}^{85} \) and \( \text{Rb}^{87} \) are shown in Fig. 24. Some expected resonances are small, mainly because the overlapping of the profiles between the exciting light and the absorption spectrum of the atoms is rather poor. Since the lamp is located in a fringing field of less than a few gauss, while the atoms are sitting in the very high applied field, some exciting transitions may be only partially induced by the spectral distribution of our lamp. The data were taken with a sufficiently short time constant in the detector circuit and with a slow sweep rate of the magnetic field to avoid significant broadening from these sources. The modulation broadening has also been eliminated. We deduce our electric quadrupole interaction from the distance from peak to peak of the modulated signal and the lifetime of the \( 4 \text{D} \) state of the rubidium atom. Our preliminary results are:

Hyperfine electric quadrupole interaction

\[
B_L (\text{Rb}^{85}) = 6(3) \text{ MHz}; \\
B_L (\text{Rb}^{87}) = 3(2) \text{ MHz};
\]

Fine structure splitting = 13360(5) MHz.
We may obviously extend this method to measure the fine and hyperfine interactions of other states of alkali atoms. For example, if we apply a two-step excitation technique by using a cw tunable dye-laser to excite D states and then let them cascade down to F, or even G, states, the fine and hyperfine interactions of these states can be measured. Furthermore, if we put the results from these measurements together with the hyperfine interaction measurements from cascade radio-frequency spectroscopy, then for various interaction terms we can deduce core-polarization interactions and \( \langle 1/r^3 \rangle \), values that are of particular interest in understanding atomic structures.

Program for the next interval: We will continue to make further measurements on this crossing and some other crossings at higher field region.

*This research was also supported by the Air Force Office of Scientific Research under Grant AFOSR-72-2180.


F. TUNABLE DYE-LASER SPECTROSCOPY OF HIGHLY EXCITED STATES IN ALKALI ATOMS: I. D STATES*
(R. Gupta, W. Happer, P. Tsekeris)

We have continued the measurement of the hyperfine interaction constants (magnetic dipole and electric quadrupole constants) of the highly excited \( ^2D \) states in \( \text{Rb}^{87} \) and \( \text{Cs}^{133} \) by the two-step excitation method. In the first step of this process we excited the alkali atoms from the ground \( ^2S_{1/2} \) state to the first excited \( ^2P \) state, using the \( D_1 \) or \( D_2 \) resonance line from a powerful rf-discharge lamp; in the second step we excite the atoms from the \( ^2P \) state to the appropriate \( ^2D \) states using light from a tunable dye laser. We observe the polarization of the light which is emitted when atoms in the \( ^2D \) states decay to lower states; and, making use of the level-crossing and optical double-resonance methods, we measure the hyperfine interaction constants.
TABLE V. Experimentally determined values for the hyperfine interaction constants of the highly excited $^2D$ states of Rb$^{87}$ and Cs$^{133}$.

<table>
<thead>
<tr>
<th>Element</th>
<th>State</th>
<th>$a$ (absolute value) (MHz)</th>
<th>$b$ (absolute value) (MHz)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rb$^{87}$</td>
<td>$^3^2D_{3/2}$</td>
<td>7.84(5)</td>
<td>0.53(6)</td>
</tr>
<tr>
<td></td>
<td>$^7^2D_{3/2}$</td>
<td>4.53(3)</td>
<td>0.26(4)</td>
</tr>
<tr>
<td></td>
<td>$^7^2D_{5/2}$</td>
<td>2.2 (5)</td>
<td></td>
</tr>
<tr>
<td>Cs$^{133}$</td>
<td>$^9^2D_{3/2}$</td>
<td>2.73(3)</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$^{10^2D}_{3/2}$</td>
<td>1.52(3)</td>
<td></td>
</tr>
</tbody>
</table>
We have repeated the measurements for the 6 and $^2\text{D}_{3/2}$ states of Rb$^{87}$ and the $^2\text{D}_{3/2}$ of Cs$^{133}$, and we have also measured the $^{10}\text{D}_{3/2}$ state of Cs$^{133}$. We have increased the precision of the measured hyperfine constants as shown in Table V.

The above experimental methods give us the absolute value of the hyperfine structure coupling constants. It is interesting to determine the algebraic sign of these constants, especially since experiments in the low-lying $^2\text{D}_{5/2}$ states give inverted signs. We have therefore performed magnetic decoupling experiments to determine these signs. In the second step of the excitation process we use $\sigma^+$ or $\sigma^-$ laser light. As the $^2\text{D}$ state decays to a lower $^2\text{P}$ state and finally to the ground $^2\text{S}$ state, we observe the polarization of the emitted light in this final step as a function of the magnetic field. The shape of the decoupling curve depends on the sign of the coupling constants. The experimental data are compared with computer-calculated curves, but unfortunately the shape of these curves depends critically on the spectral profile of the exciting laser light. Because of our lack of knowledge of the precise mode structure of the laser light, we have not yet succeeded in determining the signs of the magnetic dipole coupling constants. However, we have recently acquired a spectrum analyzer, which should now enable us to successfully apply the decoupling method.

We have also tried to find the signs of these coupling constants in Rb$^{87}$ by exciting the atoms first with $\sigma^+$ or $\sigma^-$ light from an Rb$^{85}$ rf lamp and then with $\pi$-laser light to the $^2\text{D}_{3/2, 5/2}$ states. We predict that this arrangement can create nuclear polarization in the $^2\text{D}$ states which would lead to asymmetry in the optical double-resonance signal. However, we have failed to see a definite indication of this asymmetry. We suspect that collisions and radiation trapping in the first $^2\text{P}$ state destroy its polarization.

*This research was also supported by the Air Force Office of Scientific Research under Grant AFOSR-72-2180.

G. TUNABLE DYE-LASER SPECTROSCOPY OF HIGHLY EXCITED STATES IN ALKALI ATOMS: II. S STATES*  
(R. Gupta, W. Happer, P. Tsekeris)

Extensive measurements of the hyperfine structure of the excited S states of alkali atoms, which have recently been carried out in this Laboratory, have revealed some very interesting properties of these states (see Part A of this Section). It is therefore desirable to extend these measurements to the highly excited S states. The measurements described in Part A, performed by the method of cascade radio-frequency spectroscopy, have been confined to the first two or three excited states. It is difficult to achieve significant population of the highly excited S states by the method of cascade excitation, since the oscillator strengths for highly excited P states are very low. We have, therefore, used a two-step excitation method (similar to the one used for D states described in Part F) to populate the highly excited S states. Cesium atoms are excited to their first excited P state ($6^2P_{3/2,1/2}$) by resonance light from an rf lamp. Atoms in the $6^2P_{3/2}$ are excited to the $11^2S_{1/2}$ state by dye-laser radiation of the 5746-Å fluorescent light. Our typical data are shown in Fig. 25. We obtain, for the magnetic dipole coupling constant, a value of $A (11^2S_{1/2}, \text{Cs}^{133}) = 39.4(2) \text{ MHz}$.

Program for the next interval: We will extend these measurements to other highly excited S states in Cs and Rb.

*This research was also supported by the Air Force Office of Scientific Research under Grant AFOSR-72-2180.

H. TUNABLE DYE-LASER SPECTROSCOPY OF HIGHLY EXCITED STATES IN ALKALI ATOMS: III. F STATES*  
(J. Farley, W. Happer)

Recent work at the Columbia Radiation Laboratory has resulted in the development of the stepwise excitation method. We excite alkali atoms to P states with a conventional rf lamp, then to a D state with
Fig. 25. Radio-frequency resonance due to transitions between $F = 4$, $m = -4$ and $m_f = -3$ sublevels of the $11s^1S_{1/2}$ state of Cs$^{133}$. The transition frequency is $\Delta \nu = 147.9$ MHz.
a tunable dye laser. In our work, the D state decays to an F state, and we observe the subsequent fluorescence (see Fig. 26).

Using optical double resonance (ODR) spectroscopy, we obtained rough upper limits of the absolute value of the magnetic dipole coupling constant, \( a \), for the \( 5F_{7/2} \) and \( 5F_{5/2} \) states of Cs\(^{133}\). By using a least-squares fit of one set of experimental decoupling data with computer-generated curves, we have obtained a better value for the quantity \( a \) of the \( 6F_{7/2} \) state of Cs\(^{133}\):

\[
a = 0.05 \pm 0.17 \text{ MHz.}
\]

The fine structure intervals of the Rb \( 4F \), \( 5F \), and \( 6F \) states are very poorly known. Since they are listed as \(-0.01 \text{ cm}^{-1}\) with no error given, the uncertainty may be nearly 100%. Moreover, they are inverted and hence of special interest.

In the investigation of the Rb \( 5F \) state with ODR, \( 7950-\text{Å} \) light from the \( 5S_{1/2} \rightarrow 5P_{1/2} \) line of the rf lamp excites Rb atoms in the sample to the \( 5P_{1/2} \) state, after which laser light at \( 5649 \text{ Å} \) excites the atoms to the \( 7D_{3/2} \) state. After a spontaneous unobserved decay to the \( 5F_{5/2} \), and then to the \( 5D_{3/2} \), level, the observed decay back to the \( 5P_{1/2} \) state occurs at \( 7621 \text{ Å} \).

The direction of polarization of the laser light lies parallel to the magnetic field. Hence only \( \Delta m = 0 \) transitions are possible. Consequently, the F sublevels with high \( |m_J| \) values are less populated than if the populations were statistical. When we apply an rf magnetic field to equalize the populations of a pair of sublevels, the fluorescent light has a more isotropic distribution. Our phototube, situated directly along the magnetic field from the sample, does not register \( \pi \) fluorescence. Hence we see an increase in fluorescent intensity at resonance.

We can calculate the theoretical position of the resonances for a given fine structure interval using the Breit-Rabi formula. From the observed positions of the resonances we deduce the fine structure interval. Similar considerations apply to the \( 4F \) fine structure.
Fig. 26. Level diagram of the relevant states.
When new dyes or new solvents for the old dye are able to extend the wavelength range of the laser, we will study the 6F state of Rb.

Another program will utilize the fact that the 5D$_{3/2}$ and 5D$_{5/2}$ states of Cs$^{133}$ are very long-lived (calculated lifetime of 960 nsec for the 5D$_{3/2}$ state and 1400 nsec for the 5D$_{5/2}$ state). Since atoms can decay into the 5D from the 5P states we can then use the 5D states as platforms for reaching highly excited F states with laser excitation. Since we would be exciting the F states directly (instead of using cascade excitation), we could perform level-crossing as well as ODR and decoupling experiments. The only problem is that we would detect almost the same wavelength (to within 50 Å) as the laser light. Normally this would mean that the laser background swamps the fluorescent signal, but we might overcome this if we increased the population of the 5D state by using lamps with elliptical reflectors, which have proven successful in other experiments.

*This research was also supported by the Air Force Office of Scientific Research under Grant AFOSR-72-2180.

I. HYPERFINE STRUCTURE OF THE $3^3S_1$ STATE OF He$^3$*

(W. Happer, A. Tam, H. Tang)

Because of changes in personnel, we have postponed work on this project.

*This research was also supported by the Air Force Office of Scientific Research under Grant AFOSR-72-2180.

J. STEPWISE EXCITATION AND LEVEL-CROSSING SPECTROSCOPY OF THE TRIPLET D STATE FINE STRUCTURE OF He$^4$*

(W. Happer, A. Tam)

Fine and hyperfine structures of helium are of fundamental interest, as helium is the only multielectron system that can be treated theoretically with high precision, and accurate experimental
Fig. 27. Stepwise excitation scheme.
determination of the structures is needed to assess a theoretical calculation. This comparison is nontrivial, as different calculations using different wavefunctions and different approximations may predict very different structures or other properties of the excited states of helium. As an example, the existence of a large degree of singlet-triplet mixing in F states of helium has been established qualitatively by several electron-excitation experiments,\(^{(1)}\) and various recent calculations\(^{(2,3)}\) handling this problem predict vastly different degrees of singlet-triplet mixing and fine structures in the D, F, G,... states of He\(^4\). (The S states are nonmixed, and the P states are essentially so.) Checking with experimentally determined fine structures in the \(^3\)D states of He\(^4\) would help us to evaluate the reliability of each calculation. Of course, experimental determinations of the fine structures in the F states are more useful for this comparison, but such determinations are difficult to achieve, as resonance lines involving F states are in the far-infrared region. We should note that the understanding of this singlet-triplet mixing in helium is essential to evaluate quantitively much applied research; e.g., studies of populations in a helium or helium-mixture plasma and their laser applications.

Some experimental studies on the \(^3\)D state fine structures of He\(^4\) have previously been done by optical spectroscopy,\(^{(4)}\) electron-bombardment level-crossing spectroscopy,\(^{(5)}\) ion-bombardment level-crossing spectroscopy,\(^{(6)}\) and beam-foil quantum beats.\(^{(7)}\) We have developed a new method to study the \(^3\)D fine structures: use of a two-step optical excitation from the metastable \(^2\)S state and level-crossing spectroscopy.\(^{(8)}\) This method is capable of achieving higher accuracy than all the other methods mentioned above and is less sensitive to systematic errors than the electron-bombardment method, as electron trajectories are seriously affected by the magnetic field applied for level crossing. The stepwise excitation is represented schematically in Fig. 27. We have obtained preliminary results for the fine structures of the \(^3\)D and \(^4\)D states. These are tabulated in Table VI, and Table VII also gives comparisons with other experiments and theory.
<table>
<thead>
<tr>
<th></th>
<th>$3^3D_1 - 3^3D_3$</th>
<th>$3^3D_2 - 3^3D_2$</th>
<th>$4^3D_1 - 4^3D_2$</th>
<th>$4^3D_2 - 4^3D_3$</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Present work</strong> (preliminary)**</td>
<td>1400.7 ± 0.5</td>
<td>76 ± 1</td>
<td>590.8 ± 0.5</td>
<td>36 ± 1</td>
</tr>
<tr>
<td><strong>Optical spectroscopy (a)</strong></td>
<td>1448 ± 30</td>
<td>90 ± 24</td>
<td>518 ± 30</td>
<td>54 ± 30</td>
</tr>
<tr>
<td><strong>Electron bombardment (b)</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>(1969)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Ion bombardment (c)</strong></td>
<td>1399.9 ± 1.1</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>(1968)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Beam-foil quantum beat (d)</strong></td>
<td>1420 ± 25</td>
<td>71 ± 2</td>
<td>576 ± 30</td>
<td>40 ± 5</td>
</tr>
<tr>
<td>(1972)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>


(d) H. G. Berry, J. L. Subtil, and M. Carre, J. Physique 33, 947 (1972).
**TABLE VII.** Theoretically determined fine structure intervals of triplet D states of He$^4$.

<table>
<thead>
<tr>
<th></th>
<th>$3^3D_1 - 3^3D_3$</th>
<th>$3^3D_2 - 3^3D_3$</th>
<th>$4^3D_1 - 4^3D_3$</th>
<th>$4^3D_2 - 4^3D_3$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Prish and Mires$^{(a)}$ (1972)</td>
<td>1473</td>
<td>126</td>
<td>633</td>
<td>60</td>
</tr>
<tr>
<td>Van den Eynde et al.$^{(b,c)}$ (1972)</td>
<td>1414</td>
<td>85.8</td>
<td>500</td>
<td>41.8</td>
</tr>
<tr>
<td>Moser et al.$^{(c,d)}$ (1964, 1968)</td>
<td>1409</td>
<td>83.8</td>
<td>598</td>
<td>41.1</td>
</tr>
<tr>
<td>Bethe and Salpeter$^{(e)}$ (1957)</td>
<td>1390</td>
<td>92.5</td>
<td>587</td>
<td>39.1</td>
</tr>
<tr>
<td>Araki$^{(f)}$ (1937)</td>
<td>1353</td>
<td>75</td>
<td>567</td>
<td>28.5</td>
</tr>
</tbody>
</table>

(c) Fine structure given only implicitly by these workers.
We can see from the tables that good agreement between experiment and theory is still lacking. We hope that accurate experimental determinations of the fine structures will stimulate some better theoretical calculations which hopefully would also give us a better understanding of the degree of singlet-triplet mixings in helium.

Further refinement and extension of our triplet D state measurements is underway.

*This research was also supported by the Air Force Office of Scientific Research under Grant AFOSR-72-2180.


K. FORBIDDEN TRANSITION RATES IN HELIUM*
(W. Happer, H. Tang)

Due to changes in personnel this research has been terminated.

*This research was also supported by the Air Force Office of Scientific Research under Grant AFOSR-72-2180.

L. LIFETIME MEASUREMENTS OF OPTICALLY INACCESSIBLE EXCITED STATES*
(R. Gupta, W. Happer, C. Tai)

We are continuing our measurements of the lifetimes of the optically inaccessible excited states. Table VIII gives a compilation of
Fig. 28. $^{87}$Rb $5D_{3/2}$ state Hanle-effect data fitted with $\tau(D_{3/2}) = 210$ nsec.
Fig. 29. Cesium 6D$_{3/2}$ Hanle effect; $\gamma = 50$ nsec.
the experimental results, while experimental data together with a least-squares fit are shown in Figs. 28 and 29. A compilation of the P state hfs and lifetime data which we used in the calculation of the Hanle-type curves is shown in Table IX. We used the cascade-Hanle method discussed in last year's Progress Report(1) to investigate the lifetimes of these states.

TABLE VIII. D state lifetimes.

<table>
<thead>
<tr>
<th>Atom</th>
<th>State</th>
<th>Calculated(a) τ (nsec)</th>
<th>Measured τ (nsec)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Kr 87</td>
<td>5D_{3/2}</td>
<td>241</td>
<td>205 ± 40</td>
</tr>
<tr>
<td>Cs 133</td>
<td>6D_{3/2}</td>
<td>64.5</td>
<td>57 ± 15</td>
</tr>
</tbody>
</table>


The comparatively large error bar associated with our results arises partly from the uncertainty in the lifetimes of the P states.

Program for next interval: We will continue to collect and analyze Hanle-effect data on other S and D states of alkali atoms.

*This research was also supported by the Air Force Office of Scientific Research under Grant AFOSR-72-2180.


M. LIGHT SHIFTS OF ZEEMAN RESONANCES IN OPTICALLY PUMPED ATOMIC VAPORS*
(W. Happer, S. Svanberg)

A relatively simple perturbation method to calculate light shifts of the Zeeman resonance frequencies of atoms has been developed, and the results are summarized in The Physical Review. This work is now complete.

*This research was also supported by the Air Force Office of
<table>
<thead>
<tr>
<th>Atom</th>
<th>I</th>
<th>$\mu_I$ (a)</th>
<th>State</th>
<th>A (MHz)</th>
<th>B (MHz)</th>
<th>Lifetime (nsec)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rb$^{85}$</td>
<td>5/2</td>
<td>1.3527</td>
<td>$7^2P_{1/2}$</td>
<td>17.65(2) (b)</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>$7^2P_{3/2}$</td>
<td>3.71(1) (c)</td>
<td>3.68(10) (d)</td>
<td>240 ± 20(e)</td>
</tr>
<tr>
<td>Rb$^{87}$</td>
<td>3/2</td>
<td>2.7506</td>
<td>$7^2P_{1/2}$</td>
<td>59.92</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>$7^2P_{3/2}$</td>
<td>6.75(3) (g)</td>
<td>0.96(6) (h)</td>
<td>330 ± 30(j)</td>
</tr>
<tr>
<td>Cs$^{133}$</td>
<td>7/2</td>
<td>2.579</td>
<td>$8^2P_{1/2}$</td>
<td>42.97(10) (i)</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>$8^2P_{3/2}$</td>
<td>7.626(5) (k)</td>
<td>-0.049(42) (l)</td>
<td></td>
</tr>
</tbody>
</table>

(d) Ibid., p. 101.
(e) Ibid., p. 101.
(h) Ibid., p. 470.
(l) Ibid., p. 119.
N. SPIN-EXCHANGE SHIFT AND NARROWING OF MAGNETIC RESONANCE LINES IN ALKALI VAPORS*
(W. Happer, G. Moe, H. Tang)

In our previous Progress Report\(^{(1)}\) we presented some preliminary results of an experiment to study the effects of very rapid spin-exchange collision rates on the magnetic resonance lines of an alkali vapor. In this Report we present some data obtained during the past interval which conclusively demonstrate that when the spin-exchange collision rate greatly exceeds the unperturbed Larmor frequency of the alkali vapor, the magnetic resonance frequency decreases dramatically, while the spin-exchange broadening of the resonance line vanishes. We were able to observe magnetic resonance lines with 200-Hz widths at atomic densities of greater than \(10^{14} \text{ cm}^{-3}\). These results point out the possibilities of constructing miniaturized optically pumped devices such as magnetometers. Smaller devices would require higher atomic densities to achieve the required optical density, and up to now spin-exchange broadening of the magnetic resonance lines has placed an upper limit on the atomic densities one can use, and, therefore, on the smallness of the device. We are presently studying the feasibility of constructing optically pumped devices as much as 1000 times smaller than usual.

To review the theory of spin-exchange shifts and narrowing we refer to Eqs. (9) through (12) in the previous Report, which we rewrite here as

\[
\frac{d}{dt} \langle S_+ \rangle = - \left( A + \frac{i \omega_0}{[I]} \right) \langle S_+ \rangle + \left( B + \frac{2 \gamma}{[I]^2} + \frac{i \omega_0}{[I]} \right) \langle I_+ \rangle, \tag{1}
\]

\[
\frac{d}{dt} \langle I_+ \rangle = \left( A + \frac{4 i \omega_0 I(I + 1)}{[I]} \right) \langle S_+ \rangle - \left( B + \frac{2 \gamma}{[I]^2} + \frac{i \omega_0}{[I]} \right) \langle I_+ \rangle, \tag{2}
\]
where

\[ A = \frac{1}{T} \frac{8I(I+1)}{3[I]^2}, \]  

(3)

\[ B = \frac{1}{T} \frac{2}{[I]^2}, \]  

(4)

and

\[ [I] = (2I + 1). \]  

(5)

Here, \( I \) is the nuclear spin of the alkali atom, \( T \) is the mean time between spin-exchange collisions, \( \omega_o \) is the unperturbed Larmor frequency [\( \omega_o = 2\omega_o H/(2I + 1) \hbar \)], and \( \gamma \) is the electronic spin-depolarization rate due to buffer gas and wall collision. Equations (1) and (2) are a set of linearized coupled equations describing the motions of the electronic and nuclear spins, and they are written here for the transverse components \( \langle S^z \rangle \) and \( \langle I^z \rangle \) which rotate about the \( z \)-axis in the right-hand sense. These equations can be obtained from the density matrix of the atoms in the vapor. For a derivation of the density matrix of atoms undergoing spin-exchange collisions, one can refer to the works of Grossetête(2) and Gibbs.(3) In deriving Eqs. (1) and (2), we assumed weak polarization and the absence of hyperfine structure coherence. The eigensolutions of Eqs. (1) and (2) are of the form

\[ \langle S^z \rangle = a \exp(\lambda t), \]

and

\[ \langle I^z \rangle = b \exp(\lambda t) \]

with eigenvalues

\[ \lambda_{\pm} = -\frac{1}{2} \left( A + B + \gamma + \frac{2\gamma}{[I]^2} \right) \pm \frac{1}{4} \left( A + B + \gamma + \frac{2\gamma}{[I]^2} \right)^2 \]

\[ - 4\gamma \left( A + B + \frac{2\gamma}{[I]^2} \right) + \frac{4i\omega_o}{[I]} \left( \gamma + [I]^2 B \right) - 4\omega_o^2 \right)^{1/2} \]

\[ = -\Gamma_{\pm} \pm i\omega. \]

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The imaginary parts of the eigenvalues can be interpreted as precession frequencies, while the real parts can be interpreted as damping rates. The positive precession frequency would correspond to a resonance of the upper Zeeman multiplet while the negative precession frequency would correspond to a resonance of the lower Zeeman multiplet. If one applied a linearly polarized oscillating field, one would then observe both resonances. The two damping rates determine the widths of the two resonances. Figure 30 shows a plot of the two damping rates and the magnitude of the resonance frequency as a function of the spin-exchange collision rate for the case of Rb$^{85}(I = 5/2)$. We see that the positive frequency damping rate first increases, reaches a maximum, and then decreases with increasing spin-exchange rate, eventually going to a limiting value determined by $\gamma$. The negative frequency damping rate is seen to always increase with increasing spin-exchange rate. This means that at high spin-exchange rates, the negative frequency resonance is "broadened out of existence," and only the positive frequency resonance can be observed. The magnitude of the resonance frequency is seen to start out at the unperturbed Larmor frequency. As the spin-exchange collision rate increases, the resonance frequency drops rapidly and eventually goes to the high density limit as given by Eq. (8) of the last Report. The magnetic resonance signal one observes when applying an oscillating magnetic field is proportional to the longitudinal torque on the spins due to the applied field. For an applied field of the form

$$\vec{H} = H_1(\cos wt \hat{e}_x + \sin wt \hat{e}_y),$$

the longitudinal torque, $T_\parallel$, can be written as

$$T_\parallel = \frac{2\mu_0 H_1}{h} [I] \text{Im exp } -iwt \langle S_+ \rangle.$$  \hspace{1cm} (9)

The magnetic resonance lineshapes using Eq. (9) are plotted in Fig. 31 as a function of temperature for the case of Rb$^{85}$. In computing these
Fig. 30. Theoretical plot of the damping rates $\Gamma_+$ and $\Gamma_-$ for the positive and negative frequency resonances and the observed Larmor frequency $\omega$ vs the spin-exchange rate $1/T$ for the case of Rb$^{85}$, which has nuclear spin $I = 5/2$. The above quantities have been normalized with respect to the Larmor frequency without spin exchange, $\omega_0$. 

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Fig. 31. Theoretical magnetic resonance lineshapes for different values of the spin-exchange rate $1/T_e$, showing the effects of spin-exchange frequency shift and narrowing.
theoretical lineshapes we have used the spin-exchange collision con-
stant \( \nu_0 \) for Rb\(^{65} \) measured by Gibbs and Hull\(^4\) to compute the ato-
mic density \( N \), which corresponds to a certain spin-exchange collision
rate \( (1/T = N\nu_0) \); then the Rb vapor pressure versus temperature data
of Killian\(^5\) were used to deduce the vapor temperature corresponding
to a certain spin-exchange collision rate. We can see from these
theoretical lineshapes that as the vapor temperature is initially
increased, both the positive and negative frequency resonance lines
broaden, with the negative frequency resonance being the broader of
the two. While the negative frequency resonance continues to broaden
with temperature until it can no longer be observed, the positive
frequency resonance reaches a maximum width and then becomes narrower
with increasing temperature. Furthermore, the positive frequency
resonance has shifted to a much lower frequency at high temperatures.
At intermediate temperatures, the theoretical lineshape is seen to
be quite asymmetric.

The experimental apparatus is shown in Fig. 26 of the previous
Report. Since according to the theory, the narrowing and shift be-
come prominent only when the spin-exchange collision rate is comparable
to or exceeds the magnetic resonance frequency, it is advantageous
to work at as low a frequency as possible. Therefore, a set of two
concentric cylindrical \( \mu \)-metal shields were used to shield out the
earth’s field as well as other stray fields in the laboratory. The
static magnetic field was applied by means of a coaxial solenoid
inside the shields. The shields also served to make the fields inside
the solenoid more uniform, thus greatly reducing the broadening of the
resonance lines due to field inhomogeneities.\(^6\) The rest of the
apparatus is rather conventional optical pumping apparatus, except
for the resonance cell. In order to reduce the optical thickness of
the vapor at high temperatures, very thin resonance cells were used.
The Pyrex cells were 2 in. in diameter and about 1 mm thick. In order
to ensure a long diffusion time for the atoms in the cell, high buf-
fer gas pressures were used (\~2000 torr of He at 300°C). Fortunately,
the high buffer gas pressure also greatly broadened the optical absorp-
tion line,\(^7\) thus further reducing the optical thickness of the vapor.
The cells were made by first distilling the alkali metal into the cell; then the vacuum system was filled with about 700 torr of He gas, and the cell was cooled to liquid nitrogen temperatures before it was sealed off. Using cells made in this way, we were able to detect optical pumping signals in Cs\(^{133}\) vapor up to a density of about \(6 \times 10^{14} \text{ cm}^{-3}\). Plots of resonance frequency and linewidths versus temperature for Rb\(^{85}\) and Cs\(^{133}\) vapors are shown in Fig. 32. The points represent the experimental data, while the lines represent the theory. The theoretical curves were computed using the spin-exchange constant of Gibbs and Hull\(^{(8)}\) and the vapor pressure versus temperature data of Killian.\(^{(9)}\) The value of the spin-exchange constant has an experimental uncertainty of about 10%, while the uncertainty in the vapor pressure is unknown. We note that Cs\(^{133}\), because of its higher nuclear spin (I = 7/2), exhibits a larger shift in resonance frequency between its low and high density values.

The noise in the data resulted principally from magnetic noise in the laboratory. Although the \(\mu\)-metal shields greatly reduced this noise, it was still the dominant noise in our experiment. The experimental magnetic resonance lines of Rb\(^{85}\) vapor are shown in Fig. 33. Again, the noise mainly arises from magnetic noise. In the experiment, a linearly oscillating magnetic field was used so that the magnetic resonance signal observed is the sum of a large positive frequency signal and a small negative frequency signal.

At low temperatures we start out with a symmetric lineshape which becomes broader as the temperature is increased. This broadening reaches a maximum and begins to decrease with temperature in the high temperature regime. The size of the signal is decreased at high temperatures owing to the vapor becoming optically thick. The lineshape becomes quite asymmetric at intermediate temperatures, while remaining symmetric in both the low and high temperature regimes, which is in agreement with the theory. The frequency at the peak of the line, which started out at about 1 kHz, has shifted to about 500 Hz at 170°C, also in agreement with the theory.

Since the spin-exchange rate must be greater than the magnetic resonance frequency for the frequency shift and narrowing to become
Fig. 32. Magnetic resonance frequency, \( \nu \), and half width at half maximum, \( \Delta \nu \), of the magnetic resonance line in Rb\(^{85}\) and Cs\(^{133}\) vs the cell temperature.
Fig. 33. Experimental magnetic resonance lines of Rb$^{85}$ vapor for different temperatures, showing the effects of spin-exchange frequency shift and narrowing.
appreciable, it is desirable to greatly increase the Cs-vapor density in order to allow operation in stronger magnetic fields. To observe optical pumping signals at higher densities, however, some means must be found to decrease the optical thickness of the vapor. The quality of the observed signal decreased rapidly with increasing vapor density when more than approximately 50% of the light is absorbed. In addition, when the optical thickness becomes very great, the photons are absorbed and reemitted many times, thus depolarizing the vapor.

One possible way to circumvent this difficulty is to pump the vapor with light that is less strongly absorbed than the D\textsubscript{1} line normally used, which excites the Cs atoms, for example, from the 6\textsuperscript{2}S\textsubscript{1/2} ground state to the 6\textsuperscript{2}P\textsubscript{1/2} first excited state. The transition to the 8\textsuperscript{2}P\textsubscript{1/2} third P state in Cs has an oscillator strength smaller than the D\textsubscript{1} line by a factor of approximately 300.\textsuperscript{(10)} There is a fortunate coincidence between this transition and the 3888-Å line in helium, and since an intense helium lamp was already available in the Laboratory, we attempted to optically pump Cs with the helium lamp, even though preliminary calculations showed the signal-to-noise ratio that would be obtained would be quite marginal. While pumping with the He lamp was envisioned as a simple, quick means of obtaining optical pumping signals at densities intermediate (on the order of 10\textsuperscript{16} atoms/cm\textsuperscript{3}) between those previously obtained and our ultimate objective (~10\textsuperscript{18} cm\textsuperscript{3}), we discovered this to be an unexpectedly complicated system.

Once excited to the 8\textsuperscript{2}P\textsubscript{1/2} state, the Cs atoms have, at a vapor density of 10\textsuperscript{16} atoms/cm\textsuperscript{3}, a high probability of colliding with ground-state Cs atoms and undergoing nonradiative deexcitation, probably largely by forming Cs\textsubscript{2}+ molecules by the process of associative ionization.\textsuperscript{(11)} The Cs\textsubscript{2}+ molecules thus formed are likely to recombine with an electron in the process of dissociative recombination,\textsuperscript{(12)} apparently dissociating into two excited Cs atoms in the 6P first excited state. By this means, as well as by direct cascade fluorescence from the 8\textsuperscript{2}P\textsubscript{1/2} state, most of the energy incident as 3888-Å photons is subsequently reemitted in the form of the 6P → 6S D-line photons we were trying to avoid. These photons are strongly trapped, and they depolarize the vapor. We at-
tempted to quench this fluorescence by using nitrogen as a buffer gas, but this introduced an additional complication because nitrogen reacts with the Cs to form an azide, CsN₃. While we believe the CsN₃ is sufficiently dissociated at 300°C to provide an adequate buffer gas pressure, it is possible that CsN₃ molecules could also be present, providing a relaxation mechanism via spin exchange. At any rate, our attempt to pump Cs with the He lamp was unsuccessful, but the lack of success almost certainly resulted from the complicated phenomena involved and not from any fundamental problem with the spin-exchange narrowing mechanism itself.

A second method for decreasing the optical thickness of the vapor is to use much higher buffer gas pressure to obtain large collision broadening of the optical absorption profile. We are currently evaluating methods for constructing very small Cs-absorption cells with buffer gas pressures up to 100 atm. Since collision broadening proceeds at a rate of approximately 1 Å/atm in argon, for example, this will result in absorption linewidths on the order of 100 Å. This should allow us to pump Cs vapors at very high densities with a GaAs injection laser. This would be a major step in the direction of miniaturization, cheap, optically pumped devices of great potential usefulness.

*This research was also supported by the Air Force Office of Scientific Research under Grants AFOSR-72-2180 and AFOSR-74-2685.

(1) CRL Progress Report, June 30, 1973, p. 34.
(2) F. Grossetête, J. Physique 25, 383 (1965); F. Grosstête, J. Physique 29, 456 (1968).
(5) T. J. Killian, Phys. Rev. 27, 578 (1926).
(9) T. J. Killian, op. cit., p. 578.
0. NUCLEAR MAGNETIC RESONANCE OF DIATOMIC ALKALI MOLECULES IN OPTICALLY PUMPED ALKALI VAPORS

(R. Gupta, W. Happer, G. Moe, W. Park)

We have observed nuclear magnetic resonance signals which originate in diatomic alkali molecules in optically pumped cesium and rubidium vapors. Although the molecular number density is a small fraction of the atomic number density (~5 × 10^-4 at 350°K), the rate of transfer of angular momentum between the atoms and molecules is still sufficient for the Cs_2 molecules to have an appreciable influence on the atomic spin polarization. Good signals are therefore observable. The behavior of the molecules is strongly affected by the temperature and buffer gas pressure, and these experiments afford a unique and simple way to observe simple gas-phase chemical reaction rates for a system in thermal equilibrium. These seem to be the first measurement of the formation and breakup rates of alkali molecules. The molecules also represent a new factor that must be taken into consideration when designing miniature optically pumped devices for operation at high temperature (see Part N of this Section).

Our data were obtained with the apparatus sketched in Fig. 34. We distilled cesium metal into cylindrical Pyrex absorption cells, 5 cm in diameter and 1 cm in height. We then introduced various amounts of inert gas into these cells and measured the room-temperature (~22°C) pressure before seal-off. The cells were placed in an oven, which controlled the temperature and hence the pressure of the saturated cesium vapor. The cells were optically pumped with circularly polarized D_1 (8943-Å) resonance radiation from a cesium lamp, and we monitored the transmitted pumping light with a photomultiplier.
Fig. 34. Schematic diagram of the experimental arrangement and sketches of typical data.
Fig. 35. Relaxation time of nuclear spins in Cs$_2$ as a function of temperature and the pressure of buffer gas. The curves are the fit to the data based on the rate constants given in the text.
tube. We applied a large rf field with a peak amplitude of as much as 10 G and a frequency of 55 kHz to the cells. The rf field was square-wave modulated on and off at 13 Hz, and the synchronous component of the transmitted light intensity was detected with a lock-in amplifier and displayed on a chart recorder.

Figure 34 shows signals of the type recorded when a static magnetic field $H_0$ was swept from zero to several hundred gauss. The large signal near zero magnetic field presumably resulted from magnetic resonance of the cesium atoms, although the rf-field amplitude was so large and the frequency so low that the conventional Bloch solutions for the magnetic resonance lineshape clearly need some revision to apply to our conditions. At a field of about 100 G we usually observed a second resonance. The high field resonance arises from nuclear magnetic resonance in molecules. A typical recording of the molecular signal is sketched in Fig. 34.

The mechanism for detection of the nmr signals in our work is very similar to that of Dehmelt's original spin-exchange work, and we shall limit ourselves to a qualitative description of the process. The reactions (1) and (6), to be described below, can be expected to conserve both the electronic and nuclear spins of the cesium atoms and molecules. If these reactions proceed at a sufficiently rapid rate, the spin angular momentum of the molecules will be tightly coupled to the spin angular momentum of the atoms, and saturation of the nuclear spin polarization of the molecules with an rf field will also diminish the atomic spin polarization, which is monitored by the transmitted pumping light.

By obtaining magnetic resonance curves for a series of rf powers and extrapolating to zero rf power to determine the residual width $\Gamma$, which is the inverse of the transverse relaxation time $\tau$ of the nuclear spins, we were able to obtain the data summarized in Fig. 35 for the temperature of the saturated cesium vapor. The most striking feature of the data of Fig. 35 is the decrease of the relaxation time with increasing pressure and increasing temperature. This behavior can be understood most simply by assuming that the molecules are being broken up into atoms by the reaction
Cs₂ + Ne → Cs + Cs + Ne.  \( \text{(1)} \)

Of course, the inverse of Eq. (1), the three-body association of cesium atoms into molecules, must also occur. Since the mean thermal energy of the neon atoms (~0.03 eV) is much smaller than the dissociation energy(2)(0.396 eV) of the cesium molecules, one would expect that only a small fraction of the collisions between Cs₂ and the buffer gas atoms would lead to molecular dissociation. One would also expect the rate for the process (1) to be strongly temperature dependent, and to be characterized by an activation energy on the order of the molecular dissociation energy. Indeed, we find that the high-pressure data of Fig. 35 can be fit very well if we assume that the rate for the process (1) is

\[
\frac{1}{\tau_g} = \langle v_0 \rangle_g \exp\left(-\frac{4520}{T}\right)[Ne], \tag{2}
\]

where \( T \) is the absolute temperature, \([Ne]\) is the number density of neon atoms, and the rate constant is

\[
\langle v_0 \rangle_g = 2 \times 10^{-10} \text{ cm}^3 \text{ sec}^{-1}. \tag{3}
\]

The characteristic temperature, 4520°CK, corresponds to an activation energy of 0.39 eV, which agrees very well with the 0.396-eV dissociation energy(3) of Cs₂.

Another important experimental fact is the absence of any hyperfine structure of the nmr signals. The diatomic alkali molecules are known to have a fairly large hyperfine structure due to the electrostatic interaction between the nuclear quadrupole moment Q and the electric field gradient q produced by the atomic electrons. Logan, Cote, and Kusch(4) find \( eqQ/h = 230 \text{ kHz} \) for \(^{133}\text{Cs}_2\) and \( eqQ/h = -1100 \text{ kHz} \) for \(^{85}\text{Rb}_2\). Because of the rapid reorientation of the rotational angular momentum J of the molecule due to collisions with the buffer gas atoms, there should be a pronounced motional narrowing of the hfs, and the quadrupole interaction should manifest itself by causing the
nuclear spins to relax at a rate \(5\)

\[
\frac{1}{\tau_Q} = \frac{3}{40} \frac{2I + 3}{I^2(2I - 1)} \left( \frac{eQ}{h} \right)^{1/2} \tau_J,
\]

where \(I\) is the nuclear spin, and \(\tau_J\) is the characteristic time for reorientation of \(J\). We expect \((\tau_J)^{-1}\) to be proportional to the buffer gas pressure, i.e.

\[
\frac{1}{\tau_J} = \langle \nu \sigma \rangle J [\text{Ne}].
\]

In contrast to molecular breakup [Eq. (1)], for which the electronic and nuclear spins should be conserved, the quadrupolar relaxation of Eq. (4) represents a loss of nuclear spin angular momentum to translational and rotational angular momentum of the molecules and buffer gas atoms. Because of the factor \(\tau_J\) in Eq. (4), we expect the quadrupolar relaxation rate to vary inversely as the buffer gas pressure. The diffusion rate of the molecules to the cell walls also varies inversely with the pressure. However, the diffusion rates at one atmosphere should not exceed 3 sec \(^{-1}\), and the diffusion rates were therefore too small to have had a noticeable influence on the rates measured in this work.

Before concluding our discussion of quadrupolar relaxation, let us note that a third process, chemical exchange, may also contribute to the nmr linewidth:

\[
\text{Cs}(1)\text{Cs}(2) + \text{Cs}(3) \rightarrow \text{Cs}(1) + \text{Cs}(2)\text{Cs}(3).
\]

Although chemical exchange is known to occur at a very slow rate in hydrogen and deuterium, \(6\) recent experiments by Whitehead and Grice \(7\) indicate that the chemical exchange rates in the alkali atoms are quite fast, and thermal energy cross sections for the Process (6) are on the order of \(10^{-14} \text{ cm}^2\). Although we expect that chemical exchange will conserve the electronic and nuclear spins of the reactants
in Eq. (6), the exchange collisions will contribute an amount $1/\tau_{ce}$ to the relaxation rate of the nuclear spins of the molecules:

$$\frac{1}{\tau_{ce}} = \langle v_0 \rangle_{ce} [Cs].$$

(7)

Here $\langle v_0 \rangle_{ce}$ is the rate constant, and [Cs] is the number density of cesium atoms. (8)

The accuracy of our data is too poor to allow us to make a very accurate determination of the relaxation rates due to chemical exchange and molecular hfs. However, from the data of Fig. 36 it is clear that something in addition to molecular breakup is limiting the relaxation time, since the relaxation time at lower pressures is too short to be explained solely by Eq. (2). We can obtain a fairly good fit to the data of Fig. 35 by choosing the rate constant for chemical exchange on the order of $\langle v_0 \rangle_{ce} \approx 10^{-10} \text{ cm}^3 \text{ sec}^{-1}$. (8)

The quadrupolar relaxation rate is then

$$\frac{1}{\tau_Q} = 7 \times 10^{20} [\text{Ne}]^{-1} \text{ cm}^{-3} \text{ sec}^{-1},$$

(9)

which together with Eqs. (4) and (5) and the measured values (9) of eqQ/h, yields a rate constant for relaxation of the rotational angular momentum of the molecules

$$\langle v_0 \rangle_J = 3 \times 10^{-11} \text{ cm}^3 \text{ sec}^{-1}.$$  

(10)

We note that the rate constant for the randomization of $J$ corresponds to a mean cross section on the order of $10^{-15} \text{ cm}^2$, while the cross section for relaxation due to chemical exchange would be on the order of $10^{-14} \text{ cm}^2$. Although the numbers of Eqs. (8), (9), and (10) are physically reasonable, they can only be considered as order-of-magnitude estimates at this time because our data have been taken over such a limited range of temperature and pressure.
We have also observed good nmr signals for Cs$^{133}$ in helium and argon buffer gases, and some measured relaxation rates for Cs in 338-torr helium buffer gas are shown in Fig. 35. The rates for breakup reactions such as Eq. (1) do not appear to be very sensitive to the nature of the inert gas.

*This research was also supported by the Air Force Office of Scientific Research under Grant AFOSR-72-2180.

(3) Ibid., p. 181.
(9) R. A. Logan et al., op. cit., p. 280.
II. PHYSICS OF MOLECULES

A. MICROWAVE SPECTROSCOPY*
(S. Green, R. Nerf, P. Thaddeus, K. D. Tucker)

1. Pressure Broadening

The program of millimeter microwave pressure-broadening measurements on molecules of astrophysical interest is continuing. These measurements are part of a joint theoretical-experimental approach to the study of rotational excitation of molecules. The intermolecular potential, which determines collisional excitation, can neither be measured directly, nor calculated with complete confidence. However, collision cross sections obtained from pressure broadening can be used to fix some of the parameters of the potential, and so allow calculation of excitation rates.

At present, preliminary data have been taken on broadening of carbon monoxide by CO, H$_2$, D$_2$, and He. Measurements have been made at both room temperatures and liquid nitrogen temperatures, and will shortly be extended to dry-ice temperatures. During the next few months work on this molecule will be completed.

Studies have also begun on hydrogen cyanide at room and dry-ice temperatures. This molecule is a more difficult subject than molecules previously studied because of hyperfine structure in the observed transition; the J = 0 → 1 line consists of three components separated by 1-2 MHz. Since this splitting is neither large with respect to the Doppler widths of the lines, nor small with respect to the widest line the spectrometer can measure, the analysis of the observed spectrum is quite complex. It is also possible that interference effects may exist in the overlapping spectra. To facilitate the re-
duction of the HCN data, the spectrometer has been modified to allow output on digital magnetic tape. Nonlinear least-squares fitting techniques are then used to obtain the lineshape parameters from the observed spectra.

2. Spectroscopy

Recently a quartet of unidentified interstellar lines was discovered near 87.3 GHz; the observations strongly hinted that at least three, and possibly all four, of the lines were caused by the same molecule. As part of a systematic attempt to identify the source of the lines, the spectra of some twenty molecules were investigated in the neighborhood of the unknown lines. The molecules so studied can be characterized as simple enough to occur in the interstellar medium, and complex enough to prohibit the calculation of their spectra to the requisite accuracy. None of the molecules investigated could reasonably account for more than one of the unknown lines. The failure of the laboratory investigations to identify the unknown molecule prompted further theoretical studies. We evaluated a number of free radicals whose molecular constants were only poorly known. These investigations showed that all four of the unknown lines were from the ethynyl radical C_2H, which has never been observed in the gas phase in the laboratory.

*This research was also supported by the National Aeronautics and Space Administration under Grant NGR-33-008-191, Scope T.

B. MOLECULAR BEAM MASER SPECTROSCOPY*

(L. Gaines, P. Thaddeus, G. Tomasevich, K. Tucker)

We have completed our program to measure the hyperfine structure of the normal isotopic species of the organic ring molecule pyrrole, C_4H_5N, by studying rotational transitions of the type J_{JO} \rightarrow J_{J1} in our high resolution maser spectrometer (see Table X). The J = 1 through 4 and J = 10 spectra determined the hyperfine parameters, which correctly predicted the J = 9 manifold (see Figs. 36 and 37.
<table>
<thead>
<tr>
<th>J</th>
<th>F_N</th>
<th>F'_N</th>
<th>\nu</th>
</tr>
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<tr>
<td>1</td>
<td>2</td>
<td>2</td>
<td>4469447.399 ± 0.014</td>
</tr>
<tr>
<td>2</td>
<td>2</td>
<td>1</td>
<td>4341698.974 ± 0.006</td>
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<td>2</td>
<td>3</td>
<td>4341945.132</td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>2</td>
<td>4342399.876</td>
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<td>3</td>
<td>3</td>
<td>4342816.467</td>
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<td></td>
<td>1</td>
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<td>4158258.922</td>
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<td>3921627.390 ± 0.006</td>
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<td>3</td>
<td>3921778.402</td>
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<td>8 → 8</td>
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<td>2303432.383 ± 0.030</td>
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<td>9</td>
<td>9 → 9</td>
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<td>10 → 10</td>
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<tr>
<td></td>
<td>9 → 10</td>
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<td>1973084.456 ± 0.008</td>
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<tr>
<td>10</td>
<td>10 → 10</td>
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<td></td>
</tr>
<tr>
<td>11 → 11</td>
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TABLE XI. Molecular hyperfine parameters of pyrrole and furan, and internuclear distances of pyrrole.

<table>
<thead>
<tr>
<th>Atom</th>
<th>Parameter (Hz)</th>
<th>Pyrrole</th>
<th>Furan</th>
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<tr>
<td></td>
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<td></td>
<td></td>
</tr>
<tr>
<td>H 1 or 2</td>
<td>M&lt;sub&gt;aa&lt;/sub&gt;</td>
<td>-590 ± 14</td>
<td>-537 ± 3</td>
</tr>
<tr>
<td></td>
<td>M&lt;sub&gt;bb&lt;/sub&gt;</td>
<td>686 ± 13</td>
<td>611 ± 5</td>
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<td></td>
<td>M&lt;sub&gt;cc&lt;/sub&gt;</td>
<td>-428 ± 111</td>
<td>-548 ± 13</td>
</tr>
<tr>
<td>H 3 or 4</td>
<td>M&lt;sub&gt;aa&lt;/sub&gt;</td>
<td>347 ± 14</td>
<td>253 ± 4</td>
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<td>M&lt;sub&gt;bb&lt;/sub&gt;</td>
<td>-137 ± 14</td>
<td>-189 ± 5</td>
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<td>M&lt;sub&gt;cc&lt;/sub&gt;</td>
<td>-486 ± 101</td>
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<td>H 5</td>
<td>M&lt;sub&gt;aa&lt;/sub&gt;</td>
<td>852 ± 14</td>
<td></td>
</tr>
<tr>
<td></td>
<td>M&lt;sub&gt;bb&lt;/sub&gt;</td>
<td>-870 ± 16</td>
<td></td>
</tr>
<tr>
<td></td>
<td>M&lt;sub&gt;cc&lt;/sub&gt;</td>
<td>143 ± 104</td>
<td></td>
</tr>
<tr>
<td>N</td>
<td>M&lt;sub&gt;aa&lt;/sub&gt;</td>
<td>1319 ± 7</td>
<td></td>
</tr>
<tr>
<td></td>
<td>M&lt;sub&gt;bb&lt;/sub&gt;</td>
<td>889 ± 7</td>
<td></td>
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<tr>
<td></td>
<td>M&lt;sub&gt;cc&lt;/sub&gt;</td>
<td>-405 ± 25</td>
<td></td>
</tr>
<tr>
<td></td>
<td>eQq&lt;sub&gt;aa&lt;/sub&gt;</td>
<td>1405532 ± 29</td>
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<tr>
<td></td>
<td>eQq&lt;sub&gt;bb&lt;/sub&gt;</td>
<td>1294109 ± 60</td>
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Pyrrole Internuclear Distances (Å) This work Rotational Analysis<sup>(a)</sup>

<p>| | | | |</p>
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<tbody>
<tr>
<td>a&lt;sub&gt;13&lt;/sub&gt;</td>
<td>2.591 ± 0.007</td>
<td>2.6055 ± 0.008</td>
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<td>a&lt;sub&gt;1&lt;/sub&gt;</td>
<td>1.404 ± 0.010</td>
<td>1.362 ± 0.008</td>
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<td>a&lt;sub&gt;56&lt;/sub&gt;</td>
<td>1.040 ± 0.002</td>
<td>0.996 ± 0.004</td>
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<tr>
<td>b&lt;sub&gt;12&lt;/sub&gt;</td>
<td>4.195 ± 0.011</td>
<td>4.210 ± 0.008</td>
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<td>b&lt;sub&gt;34&lt;/sub&gt;</td>
<td>2.712 ± 0.007</td>
<td>2.716 ± 0.008</td>
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Fig. 36. Representative pyrrole spectra. Upper trace is experimental spectrum with best-fit theoretical below.
Fig. 37. Preliminary pyridine spectra. Experimental spectra above prediction from pyrrole constants.
Fig. 38. Molecular structures of furan, pyrrole, and pyridine.
for representative spectra).

The nitrogen quadrupole interaction dominates the hyperfine structure for pyrrole and splits the spectra into widely spaced manifolds which can be labeled by the quantum numbers $F_N = I_N + J$. Since it is so large, the quadrupole interaction is fitted separately. The spin-spin interaction determines the width of each manifold (~20KHz) with the spin-rotation tensor elements (three for each type of proton) which determine the pyrrole hfs. The results of a 14-parameter least-squares fit are shown in Table XI.

We can compare the pyrrole results to those for the similar ring molecule furan, $C_4H_4O$, which was previously studied in this laboratory. The similarity in spin-rotation tensor elements for the corresponding protons in the two molecules is striking. This implies that the molecular electron distribution at these sites is barely changed by the substitution of N for the O in the ring. We are now studying another similar ring, pyridine, $C_5H_5N$, to further understand the effects of small changes in ring atoms on the hfs. (See Fig. 38 for a comparison of molecular structures.) Table XII below gives our measured values for the transition frequencies.

**TABLE XII. Observed pyridine transition frequencies.**

<table>
<thead>
<tr>
<th>$J = 3$ ($3_{30} \rightarrow 3_{31}$)</th>
<th>$\nu$ (KHz)</th>
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<tr>
<td>$F_N = 3 \rightarrow 3$</td>
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<td>4 → 4</td>
<td>2320636 ± 1</td>
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<tr>
<td>2 → 2</td>
<td>2320844 ± 1</td>
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</table>

<table>
<thead>
<tr>
<th>$J = 10$ ($10_{9,1} \rightarrow 10_{9,2}$)</th>
<th>$\nu$ (KHz)</th>
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<td>$F_N = 9 \rightarrow 9$</td>
<td>3524251.4 ± 0.5</td>
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<td>11 → 11</td>
<td>3524191.6 ± 0.5</td>
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<td>10 → 10</td>
<td>3523584.7 ± 0.5</td>
</tr>
</tbody>
</table>

We are also attempting to study the hyperfine structures of $H_2C^{17}O$, which has recently been observed in the interstellar medium.

*This research was also supported by the National Aeronautics and Space Administration under Grant NGR-33-008-191, Scope T.
Fig. 39. Front-end box block diagram.
C. CARBON MONOXIDE SKY SURVEY*
(G. Chin, H. Cong, P. Thaddeus)

One of the most exciting projects in molecular astronomy today is a Galactic survey in the CO region of the microwave spectrum (2.6 mm, 115 GHz). The 21-cm survey of atomic hydrogen has heretofore provided the only information we have of detailed Galactic structure. A small 4-ft radio telescope operating in the millimeter region will have the same angular resolution as the largest 21-cm telescope. The CO sky survey will not only complement the 21-cm survey but will provide greater information on the denser region of the Galaxy which the 21-cm telescope cannot give.

Construction of the millimeter-wave telescope is essentially completed. The 48-in aperture Cassegrain with a primary focal ratio of 0.375 has been delivered and mated to an alt-azimuth fork mount. The primary parabolic reflector was numerically machined out of a lightweight aluminum casting to an rms accuracy of 0.001 in. The receiver, which consists of a Schottky-barrier mixer, followed by an IF parametric amplifier at 1400 MHz and then a conventional 1400-MHz receiver, is also essentially completed (see Fig. 39). The 40-channel filter bank with 2.5-km/sec (1-MHz) spectral resolution and the analog-signal multiplexer has been built and tested satisfactorily.

The Nova minicomputer which controls the telescope pointing as well as the data acquisition with its complement of peripheral equipment and interfaces is operating satisfactorily (see Fig. 40). The telescope position is sent to the computer by digital shaft-encoders, and position errors are corrected by the computer pulsing digital stepping motors. The computer can control the tracking of the telescope within the shaft-encoder resolution, which is 40 arc-sec. The angular resolution of the telescope at 2.6 mm is about 8 arc-min. The Nova computer is operating in a multiprogram mode in which every 50 msec the computer is interrupted in its keyboard task
Fig. 40. Block diagram for telescope system.
to strip 40 channels of data and update the telescope position. A 
Clocks and Timing Unit (CTU) routes the digital and analog signals 
to the computer and provides the local sidereal time for position 
updating. For the Nova computer a powerful interactive programming 
language has been written which allows for flexible modes of teles­
scope operation as well as for powerful calculations using a hard­
wired Floating Point Unit.

A 12-ft astrodome has been built on the roof of Pupin Hall to 
house the millimeter telescope. The dome is equipped with heaters 
and an air conditioner to provide a thermally stable operating en­
vironment. Observations are made through a thin nylon radome. The 
control room, containing the circuitry, is inside Pupin.

The telescope has been assembled in the Laboratory and is 
operating as designed. Assembly of the entire system at Pupin will 
take place in mid-June, 1974, after a final noise test on the re­
ceiver.

*This research was also supported by the National Aeronautics 
and Space Administration under Grant NGR-33-008-191, Scope T.
III. RESONANCE PHYSICS

A. PHOTON ECHOES IN NEODYMIUM$^{3+}$

(S. Chandra, Y. Chen, S. R. Hartmann)

Last year we reported the first observation of photon echoes for the $^4I_{9/2} \rightarrow ^4F_{3/2}$ transition of Nd$^{3+}$ in CaWO$_4$. We described the temperature dependence and magnetic field behavior of the echo. Since then we have succeeded in detecting echoes for the same transition in two other crystals: LaF$_3$:Nd$^{3+}$ and YAG:Nd$^{3+}$. Below we present a comparative study of the echo behavior in the three crystals.

In all three crystals, the ground state, $^4I_{9/2}$, is split into five Kramer's doublets ($Z_1 - Z_5$), and the $^4F_{3/2}$ state into two doublets ($R_1$ and $R_2$) as shown in Fig. 41. The echoes were excited between the $Z_1$ and $R_1$ levels. Our samples were: LaF$_3$:Nd$^{3+}$ (0.1 atom %), with transition frequencies corresponding to 8626 Å, 8767 Å, and 8749 Å, respectively. The experimental arrangement was similar to that described in last year's Progress Report, (1) except that the excitation laser pulses were collinear, and consequently the echoes were also emitted collinearly. A three-stage Kerr-cell optical shutter prevented the photomultiplier detector from saturating. The laser E-field was vertical. The LaF$_4$ and CaWO$_4$ samples were oriented with the c-axis perpendicular to both the E-vector and the direction of propagation to maximize the echo signal. The sample temperature was varied between 3° and 20° K, and a magnetic field variable up to 3 kG was applied along the c-axis. The shot-to-shot signal fluctuation was typically a factor of two.

The photon-echo amplitude in each crystal depended on both magnetic field and sample temperature. The echoes were larger in CaWO$_4$. They were typically two orders of magnitude smaller in LaF$_3$ and three
Fig. 41. The $^4I_{9/2}$ and $^4F_{3/2}$ energy levels of Nd$^{3+}$ in the three crystals.
Fig. 42. Temperature dependence of photon echoes in Nd$^{3+}$ in the three crystals.
orders smaller in YAC. Photon echoes in YAG, although considerably more difficult to observe than in the other two crystals, were still easily observed. There is a threshold temperature above which the echo amplitude at fixed excitation-pulse separation decreases rapidly (Fig. 41). This behavior was unaffected by the magnitude of the applied magnetic field. The threshold temperature for an excitation-pulse separation of 64 nsec was \( \sim 5^\circ K \) for LaF\(_3\), \( \sim 8^\circ K \) for CaWO\(_4\), and \( \sim 13^\circ K \) for YAG. We attribute this sharp decay to phonon-induced relaxations of the Orbach and Raman type. For either mechanism the most important contribution comes from levels closest to the echo levels \( Z_1 \) and \( R_1 \), viz. \( Z_2 \) and/or \( R_2 \). The Orbach relaxation rate behaves as \( \sim \Delta^3 \exp(-\Delta/kT) \), while the Raman relaxation rate follows \( \sim \Delta^4 T^{-\nu} \), where \( \Delta \) is the energy separation between \( R_1 \) and \( R_2 \) or between \( Z_1 \) and \( Z_2 \). We note that the ordering of the observed threshold temperatures follows that of \( \Delta \) (see Fig. 41 for values of \( \Delta \)). Our experimental data do not allow us to determine which of the two relaxation mechanisms is responsible for the echo decay. We think that it is probably the Orbach-type process that dominates the relaxation. We arrived at this conclusion by some theoretical considerations based on spin-lattice relaxation data of electron-spin-resonance experiments.

The solid lines in Fig. 42 are drawn for the following relaxation-time constants:

- **LaF\(_3\):Nd\(^{3+}\)**: \( \tau_{10} = 1.5 \times 10^{12} \left[ \exp(-65/T) + \exp(-60.5/T) \right]^{-1} \) sec;
- **CaWO\(_4\):Nd\(^{3+}\)**: \( \tau_{10} = 3 \times 10^{-12} \exp(91/T) \) sec;
- **YAG:Nd\(^{3+}\)**: \( \tau_{10} = 14 \times 10^{-12} \exp(121/T) \) sec.

The dashed curve is a fit for YAG with a Raman process.

The magnetic field dependence of photon echoes was studied for fields up to 3 kG. For pulse separations up to 300 nsec in CaWO\(_4\):Nd\(^{3+}\), the echo signal increased monotonically with the applied field for the initial few hundred gauss and thereafter became constant. Figure 43 shows the echo behavior in LaF\(_3\):Nd\(^{3+}\) for various pulse separations. Figure 44 gives a comparison of the echo behavior in the three crystals.
Fig. 43. Photon-echo signal in LaF$_3$:Nd$^{3+}$ (0.1 atom %) as a function of applied magnetic field for indicated fixed pulse separations. The solid error bars represent standard deviations. Dashed vertical bars are drawn for single shots.
LaF$_3$: Nd$^{3+}$

97ns

Fig. 44. Contrasting magnetic field behavior of photon echoes in the three host crystals. Nuclear magnetic superhyperfine interactions are believed responsible for the modulations.
for a fixed pulse separation of 97 nsec. We attribute the difference in the magnetic behavior of the echo to the difference in the magnetic interaction of the Nd\(^{3+}\) atoms with neighboring paramagnetic nuclei present in the crystals.\(^{(2)}\) In CaWO\(_4\) only 14% of the tungsten nuclei are magnetic and only weakly so (\(g_n/\pi = 0.175\) MHz/kG). We therefore do not expect any modulation of the echo since we have \(g_nHt \ll \pi\)
(where \(H = 3\) kG and \(t = 97\) nsec pulse separation). This is in agreement with our observation. For both LaF\(_3\):Nd\(^{3+}\) and YAG:Nd\(^{3+}\) we expect and observe modulation effects. In LaF\(_3\) there are eleven \(F\) nuclei (\(g_n/4\pi = 4.0\) MHz/kG) within 3 Å of the Nd\(^{3+}\) ion. In YAG the ten nearest \(Al\) nuclei (\(g_n/2\pi = 1.1\) MHz/kG) are within 4 Å of the Nd\(^{3+}\) ion.

*This research was also supported by the National Science Foundation under Grant NSF-GH-38503X.

(1) CRL Progress Report, June 30, 1973, p. 68.

B. PHOTON-ECHO RESONANCE IN RUBY\(^*\)
(S. R. Hartmann, P. Liao, S. Meth)

We are continuing our investigation of photon echoes in ruby using the gated cw system described in the previous Progress Report.\(^{(1)}\) We are using the more powerful laser pump, and are presently mounting the entire experiment on a vibration-isolation system to reduce vibrations and increase the echo signal.

1. Modifications in Equipment

The gated cw system is shown in Fig. 45. The Spectra Physics Model 170 Argon-Ion Laser is capable of producing 6 W at 5145 Å; however, we have been able to generate as much as 9 W for short periods. The remaining optical apparatus has not been changed from that described in the previous Report.

We have completely automated the photon-echo experiment by using a unique echo multipulser designed and built in the CRL electronics shop. When triggered, this device produces a series of clock pulses whose time separation is controlled by a 10-turn potentiometer. The
Fig. 45. Optical arrangement of photon-echo experiment.
Experimental timing sequence is triggered by these clock pulses, with the first and second pulses triggering the first and second laser pulses, respectively. The sample Pockel's cells are closed during the laser pulses to prevent saturation of the photomultiplier tube, and the third clock pulse triggers the cells to open just prior to the arrival of the echo. This clock pulse also initiates the timing sequence for the data-acquisition electronics. We have replaced the boxcar integrator with an integrated circuit Analog Devices SHA-5 sample-and-hold.

When the experiment is operating, the PDP-8/e computer controls the multipulser potentiometer, varying the pulse separation in a manner programmed by the experimenter. Thus, in about 30 min we can acquire data corresponding to a sweep of pulse separation from 200 nsec to 6 μsec, in increments of 100 nsec. This corresponds to a decrease in data-taking time by a factor of at least five over manual operation.

We had been able to produce a fairly stable, nonspiking cw ruby beam with argon pumping power as high as 4.2 W. At higher power, we were unable to eliminate the ruby spiking due to vibrations of the ruby-laser rod with respect to the argon beam. We also had an extremely small laser spot size (~100-μ diameter) at the sample. If, between the two laser pulses, the beam moves with respect to the sample, the two spots will not overlap completely, resulting in a decrease of the echo signal. To reduce these problems, we have used a 4-ft by 10-ft, 3600-lb cast iron, ribbed optical table, mounted on a Jodon Engineering Vibration-Isolation System. This system of pneumatic legs reduces by a factor of 50 the transmission of floor vibrations to the table at 10 Hz, the resonant frequency of the laboratory floor. We are in the process of mounting the entire experiment on the table. We have already mounted the ruby laser and pump and have obtained a nonspiking cw ruby beam at 6-W pump power. No spiking was observed to 8-W pump power, but the 170 Laser cannot sustain such high powers for very long periods. This should increase the ruby output over that of the old system by 50%. We hope with the new system to be able to measure photon echoes across at least three orders of magnitude in pulse separation, and

98
six orders of magnitude in echo intensity.

2. Photon-Echo Modulation

The photon echo is the optical analog of Hahn's spin echo.\(^{(2)}\) Two resonant pulses of light, separated by a time \(\tau\), pass through the sample. These pulses act as the 90° and 180° pulses of the spin-echo pulse sequence, so that at a time \(\tau\) after the second pulse, the sample radiates the photon echo. As in the case of spin echoes, the formation of the photon echo is sensitive to changes in the local field at the echo-atom site and hence to interactions with other atoms and nuclei. The interaction of the chromium atoms in ruby with neighboring aluminum nuclei causes a marked modulation of echo intensity with respect to pulse separation similar to that observed in electron-spin echoes.\(^{(3)}\)

Recent photon-echo nuclear double-resonance (PENDOR) studies have allowed the determination of Cr-Al interaction parameters associated with the excited state.\(^{(4)}\) These parameters, together with those determined for the ground state from spin-echo ENDOR experiments,\(^{(5)}\) allow the calculation of photon-echo behavior in a manner similar to that used for spin-echo behavior.\(^{(6)}\) The results of these calculations are shown in Figs. 46 and 47, along with corresponding experimental data taken with the automated, gated cw system.

The data of Fig. 46 correspond to conditions that were measured previously: the magnetic field is applied at a slight angle with respect to the optic axis of the crystal. Our data agree with the data published earlier in the short time regime\(^{(7)}\) but extend also to longer pulse separations. The solid curve, which corresponds to the theory, does not include the overall exponential decay of the photon-echo envelope. The comparison of theory with experiment appears to be excellent. We expect to extend the pulse separation as far out as 20 µsec or longer in the near future and thereby study the interesting oscillatory behavior exhibited by the echo.

Figure 47 shows the photon-echo modulation for the magnetic field applied parallel to the optic axis for the \(E(2E)(1/2) \rightarrow 4A_2(1/2)\) transition. The theoretical calculations were multiplied by an exponential
Fig. 46. Off-axis photon-echo modulation.
Fig. 47. On-axis photon-echo modulation.
Fig. 48. a) Typical photon-echo exponential decay. b) Same data plotted vs $t^{1/2}$. 
TABLE XIII. Results of least-squares fit to the function $S = A \exp(Br^N)$ of photon-echo exponential decay.

<table>
<thead>
<tr>
<th>Cr$^{3+}$ (%)</th>
<th>Date of Experiment</th>
<th>H(kG)</th>
<th>N</th>
<th>Error(±)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.037</td>
<td>3/27/73</td>
<td>5.0</td>
<td>0.95</td>
<td>0.65</td>
</tr>
<tr>
<td>0.02</td>
<td>7/26/73</td>
<td>3.0</td>
<td>0.97</td>
<td>0.32</td>
</tr>
<tr>
<td>0.17</td>
<td>7/30/73</td>
<td>3.0</td>
<td>1.34</td>
<td>2.21</td>
</tr>
<tr>
<td>0.17</td>
<td>7/31/73</td>
<td>3.0</td>
<td>1.40</td>
<td>0.75</td>
</tr>
<tr>
<td>0.02</td>
<td>7/26/73</td>
<td>5.0</td>
<td>0.82</td>
<td>0.26</td>
</tr>
<tr>
<td>0.037</td>
<td>3/26/73</td>
<td>0.75</td>
<td>1.80</td>
<td>1.75</td>
</tr>
<tr>
<td>0.037</td>
<td>3/26/73</td>
<td>0.75</td>
<td>1.43</td>
<td>1.17</td>
</tr>
<tr>
<td>0.037</td>
<td>3/27/73</td>
<td>0.5</td>
<td>1.66</td>
<td>1.86</td>
</tr>
<tr>
<td>0.02</td>
<td>3/27/73</td>
<td>1.0</td>
<td>0.65</td>
<td>0.76</td>
</tr>
<tr>
<td>0.02</td>
<td>7/26/73</td>
<td>0.5</td>
<td>0.74</td>
<td>0.67</td>
</tr>
<tr>
<td>0.02</td>
<td>7/26/73</td>
<td>0.75</td>
<td>0.31</td>
<td>0.55</td>
</tr>
<tr>
<td>0.02</td>
<td>7/26/73</td>
<td>1.0</td>
<td>0.77</td>
<td>0.39</td>
</tr>
<tr>
<td>0.005</td>
<td>9/6/73</td>
<td>5.0</td>
<td>0.81</td>
<td>0.12</td>
</tr>
<tr>
<td>0.035</td>
<td>6/6/73</td>
<td>1.95</td>
<td>0.86</td>
<td>0.37</td>
</tr>
</tbody>
</table>
decay factor, whose decay time was estimated from the data. At lower fields, the depth of the modulation is quite substantial. The agreement between theory and experiment is generally fair, but poor when compared to spin-echo modulation results.

3. Concentration-Dependent Relaxation

We have measured the concentration and field dependence of the exponential decay of the photon echo for a large number of concentrations and fields, and all the decays appear as a simple exponential. In Fig. 48a we plot the echo intensity versus t for a 0.005% Cr$^+$ sample at 5 kG. The decay appears to be a simple exponential when compared to Fig. 48b, which is a plot of the same data against $t^{1/2}$. One should note the difficulty in distinguishing between $\exp(at^{1/2})$, which is the decay observed by Compaan, and $\exp(-bn)$ as we have observed in the limit of high fields.

To indicate the difficulties involved, we performed a least-squares fit to the function $S = A \exp(-bt^N)$ for approximately 20 different decays. The data in Fig. 48 show the most points and would be expected to yield the most accurate result. The numerical analysis yielded the result $N = 0.81 \pm 0.12$, which seems to favor the simple exponential decay. Some of the other results are given in Table XIII. It appears that the standard deviations are sufficiently large to admit either $N = 1/2$ or $N = 1$ as possible solutions. We hope to alleviate this ambiguity with the new experimental setup, when we extend pulse separations beyond the present two decades. We should then obtain more datapoints per curve and more accurate results.

A description of recent photon-echo experiments is being prepared for publication, and experiments will continue in photon-echo exponential decay and photon-echo modulation.

*This research was also supported by the National Science Foundation under Grant NSF-GH-38503X.

(1) CRL Progress Report, June 30, 1973, p. 72.
(2) E. L. Hahn, Phys. Rev. 80, 580 (1950).

**C. ECHO BEHAVIOR IN RUBY**

(P. Fu, S. R. Hartmann)

We have extended the range of pulse separation for which electron-spin echoes at 9.31 GHz in the $^4A_2$ ground state of ruby can be observed. We have measured echoes of $+1/2$ and $-1/2$ Zeeman levels in a magnetic field of approximately 3.3 kG, and $+3/2$ and $+1/2$ Zeeman levels in a field of approximately 7.5 kG. Echoes of the Zeeman $+1/2 \rightarrow +3/2$ transition in a magnetic field of about 0.785 kG have not been observed because of the very weak echo amplitude, which is a factor of $\sim 10^3$ smaller than that associated with the $+1/2 \rightarrow -1/2$ Zeeman transition. The range of pulse separation is 0.5 to 7.0 $\mu$sec for the $+1/2 \rightarrow -1/2$ transition and 0.5 to 16.4 $\mu$sec for the $+3/2 \rightarrow +1/2$ transition. Because the echo amplitude decays as the time separation between the exciting microwave pulses is increased, we observed the echoes by signal averaging. The echo was fed to an analog-to-digital converter whose digital output was interfaced into a PDP8/e computer. The time separation between the microwave pulses was controlled by computer and measured by a frequency counter. The optical axis of the ruby crystal was aligned parallel to the dc magnetic field. The $Cr_2O_3$ concentration was 0.005% by weight. We pumped the helium to increase the signal-to-noise ratio and measured the echoes at a temperature of $\sim 2^\circ$K.

Using the following spin Hamiltonian, we calculate the spin-echo amplitude as a function of pulse separation:

$$
\chi = g_s H S_z + D [S_z^2 - \frac{1}{3} S(S+1)] + \sum_j \left[ -\Delta_j H_{iz}^j \right] + S_z \sum_j \left[ (A+B_z^j) I_z^j \right]
$$

105
Fig. 49. Echo-envelope modulation at 9.31 GHz, 7.5 kG, for a pulse-separation range of 0.5 to 6 μsec.
Fig. 50. Echo-envelope modulation at 9.31 GHz, 7.5 kG, for a pulse-separation range of 6 to 12 μsec.
Fig. 51. Echo-envelope modulation at 9.31 GHz, 7.5 kG, for a pulse-separation range of 12 to >16 μsec.
\[ + B_j^1 I_1^{j1} + \theta^j \exp(-i\theta_1 I_2^j) \exp(-i\theta_2 I_1^j) \exp(-i\theta_3 I_z^j) \]
\[ \times [I_z^j I_2^j + \eta \left( I_1^j I_2^j - I_2^j I_1^j \right)] \exp(i\theta_3 I_z^j) \exp(i\theta_2 I_1^j) \]
\[ \times \exp(i\theta_1 I_2^j) \]

where \( A_j^j, B_j^j, B_t^j, \theta^j, \theta_1, \theta_2, \theta_3, \) and \( \eta \) are the hyperfine interaction constants of neighboring aluminum neighbors. These parameters were measured using the technique of echo ENDOR.\(^{(2)}\) The subscripts 1 and 2 refer to the direction in the transverse plane parallel to and perpendicular to the transverse component of the local field at the aluminum neighbor site, respectively.

The results of the \(+1/2 \rightarrow -1/2\) transition at 3.3 kG are the same as our previous measurements.\(^{(3)}\) The experimental curves of transition \(+3/2 \rightarrow +1/2\) at 7.5 kG are shown as the upper curves in Figs. 49, 50 and 51. The lower curves in the figures are the theoretical calculations, for which we assume an exponential decay with decay constant \( 1/T = 0.25 \mu \text{sec}^{-1} \) in order to approximate the effect of dephasing interactions not included in the Hamiltonian. Although the relative magnitudes of the peaks are not correct, the general features of the echo behavior agree extremely well.

Program for the next interval: We will measure the spin-echo modulation of ruby for the \(-1/2 \rightarrow -3/2\) and \(+1/2 \rightarrow -1/2\) transitions at 16.2 GHz. We will also set up the apparatus for the spectral-diffusion experiment.\(^{(4)}\)

*This research was also supported by the National Science Foundation under Grant NSF-GH-38503X.


(3) CRL Progress Report, June 30, 1973, p. 102.

D. RAMAN ECHOES*

(A. Flusberg, S. R. Hartmann, R. A. Weingarten)

Using an improved apparatus, we have studied several nonlinear processes in atomic thallium vapor. We are seeking to optimize parameters for the generation and detection of Raman echoes. Consequently, we have examined stimulated Raman scattering (SRS) and four-wave parametric mixing (FWM) in the thallium vapor.

Stimulated Raman scattering in thallium vapor is usually accompanied by self-focusing of the incident ruby-laser pulse. To overcome this, a 1/16-in aperture was placed in the oscillator of the ruby laser to restrict possible transverse laser-cavity modes. We measured the far field laser-intensity distribution of the system using a pinhole in the focal plane of a lens and a photodetector. The intensity distribution was approximately Gaussian with a half-width (at 1/e²) divergence of 0.66 mrad. Because of the small aperture in the laser oscillator, total laser power was reduced to 5 to 15 MW. Therefore, we used a 1-m focal length lens to focus the laser beam at the center of the thallium-vapor zone of the heat-pipe oven. In the presence of SRS, we measured the divergence of the laser beam leaving the oven and found that it had increased to 1.23 mrad. No evidence of self-focusing was observed.

The generated Stokes light was detected with fast and slow photodetectors. A typical Stokes pulseshape is shown in Fig. 52. The exciting laser pulse was basically smooth, although there was some modulation corresponding to the interference of different longitudinal modes of the laser oscillator. Fabry-Perot analysis of the laser pulse indicated that most of its energy was concentrated in one or two modes approximately 1 GHz apart. Stokes pulseshape modulations do not appear to correspond to any laser modulations.

Despite the presence of the modulations, the Stokes energy followed a fairly regular pattern as a function of thallium vapor pressure (see Fig. 53). The high density points correspond to a
Fig. 52. Stokes pulseshape at 90 torr thallium vapor pressure. Stokes energy = 1.2 mJ.
Fig. 53. Stokes energy output as a function of thallium vapor pressure at constant laser-pulse power.
saturation of the medium wherein an appreciable fraction of the thallium atoms are being excited by the SRS. The threshold near 40 torr is very sharp, as indicated in the figure.

The Raman-echo effect arises from the rephasing of a macroscopic excitation of the thallium atoms following their interaction with two laser-Stokes pulses. Each atom is driven into a superposition of the two lowest lying states, the $6^2P_{1/2}$ ground state and the $6^2P_{3/2}$ metastable state. Because these two states are not coupled by an electric dipole transition (as they are in the photon-echo experiment) the rephased excitation can be detected only by use of a third frequency, at the time of the echo, to induce dipole moments in the atomic ensemble. As a prelude to this, we examined the effect of the third frequency pulse, from a tunable dye laser, simultaneously incident on the vapor with a laser-Stokes pulse. In form, this interaction is very similar to four-wave mixing with the fourth wave, generated in the vapor, being the Stokes or anti-Stokes frequency of the dye-laser frequency.

The thallium vapor was contained in a 15-cm long quartz cell. The dye-laser anti-Stokes frequency was detected using a IP28 photomultiplier tube (see Fig. 54). Some integration in the detector and electronics can be assumed. Using a gated pulse stretcher to integrate the photomultiplier pulse, we obtain a measure of the energy contained in the dye-laser anti-Stokes pulse. In Fig. 55, we have plotted this value, normalized by the dye-laser energy, as a function of the product of the laser and Stokes energies. Although there are point-to-point fluctuations, the data fall very close to a straight line. A least-squares fit of the points yields for the slope a value of $0.96 \pm 0.02$ without consideration for experimental uncertainties.

The dye laser was tuned to be near the $6^2P_{3/2} \rightarrow 7^2S_{1/2} (5350-Å)$ transition to enhance the FWM process. The effect of varying the thallium vapor density in the quartz cell on the scattering is indicated in Fig. 56. The lowest density points indicate an $N^2$-dependence of the scattering, whereas a least-squares fit of all the points except the highest density point indicates a slope of 1.58. It is clear that the scattering as a function of density is turning over. This is an effect attributable to phase mismatch among the four waves inter-
Fig. 54. Dyne-laser anti-Stokes pulse as detected by photomultiplier (PM) and corresponding Stokes pulseshape (SP).
Fig. 55. Normalized dye-laser anti-Stokes signal as a function of the product of the laser and Stokes energies at constant vapor density.
Fig. 56. Normalized dye-laser anti-Stokes signal as a function of thallium vapor density.

\[(U_{DAS}/U_D) \propto N^\beta\]

\[\Delta k \approx 40 \text{cm}^{-1}\]
acting in the FWM process.

Program for the next interval: We believe that a better understanding of SRS in thallium vapor is essential. We are examining this process experimentally and theoretically to determine the optimum conditions in which to observe the Raman echo.

*This research was also supported by the National Science Foundation under Grant NSF-GH-38503X.


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E. COHERENCE EFFECTS IN TWO-PHOTON ABSORPTION

(Z. Friedlander, S. R. Hartmann)

We have increased by more than a factor of four the power-output capability of our temperature-tuned ruby laser and have carefully studied the dependence of the fluorescence from cesium gas excited by a two-photon absorption on the incident laser intensity over this extended power-output range. We have investigated two of the cascading single-photon fluorescences, namely the \( \text{9}_2^\text{D}_{5/2} \to \text{6}_2^\text{P}_{3/2} \) and the \( \text{7}_2^\text{P}_{3/2} \to \text{6}_2^\text{S}_{1/2} \) decays, following the \( \text{6}_2^\text{S}_{1/2} \to \text{9}_2^\text{D}_{5/2} \) two-photon excitation.

We obtain Q-switched laser pulses that are 8 nsec long and up to 100 MW/cm\(^2\) in intensity. The output wavelength can be tuned over the range 6934 Å to 6943 Å in steps of 0.05 Å to 0.01 Å by changing the temperature of the ruby. A given ruby temperature can be reproduced from shot to shot to within 0.05°C; this indicates a wavelength stability of better than 0.01 Å. We have previously determined that maximum fluorescent yield for the above transitions is obtained at a ruby temperature of \(-116.2 \pm 1.3^\circ\text{C}\), corresponding to a laser-output wavelength of 6935.76 ± 0.4 Å. This photon energy corresponds to one-half the \( \text{6}_2^\text{S}_{1/2} \to \text{9}_2^\text{D}_{5/2} \) energy interval in cesium, and we note that there is no level that can be reached from the ground \( \text{6}_2^\text{S}_{1/2} \) state with the absorption of a single photon of this
energy. Most of the experiments described below were performed with
the ruby at a temperature of -116.4°C.

Fabry-Perot pictures taken at 15- to 20-MW/cm² laser-output
intensity show several longitudinal modes lasing, with the average
width of the laser line being 0.075 cm⁻¹. The natural width of the
R₁ line in ruby at this temperature is 1.5 cm⁻¹. At higher power
levels more modes lase, with a corresponding increase in the frequen-
cy width of the laser line.

As in previous experiments, the unfocused laser light, filtered
by a long-pass #2-58 Corning glass filter, is incident on the 15-cm
Pyrex cell containing the cesium. The cell is kept in a temperature-
regulated oven at 200 ± 1.5°C, corresponding to a gas pressure of
0.1 torr and a density of 2.21 × 10¹⁵ atoms/cm³. The laser power
incident on the cesium cell is varied by means of neutral density
filters placed before the oven. The fluorescence is observed by
means of a 1P28V1 RCA photomultiplier tube, preceded by a copper
sulfate filter to eliminate the laser light, and an interference
filter appropriate for the wavelength being observed. Part of the
laser beam is split off before reaching the cesium cell and, appropria-
tely filtered, is incident on a Monsanto MD 1 diode. The photo-
multiplier tube and diode outputs are simultaneously displayed on a
dual-beam 555 Tektronix oscilloscope operating in the "add" mode.
Thus the laser pulse and the fluorescence pulse were photographed
together for every shot.

We have seen the 5846.58-Å 9D₅/₂ → 6P₇/₂ and the 4555.20-Å,
7P₃/₂ → 6S₁/₂ decays following the two-photon 6S₁/₂ → 9D₅/₂ absorp-
tion and have studied the dependence of the fluorescent intensity
and pulsewidth in both transitions on the incident laser intensity
and pulsewidth and on the density of the cesium. The radiative
lifetimes of the 9D₅/₂ and 7P₃/₂ levels in cesium are calculated
to be 200 nsec and 120 nsec respectively. The calculated mean life-
time between collisions for an ideal gas at 200°C and 0.1 torr is
1.27 \times 10^{-6} \text{ sec}, or about two orders of magnitude longer than our expected radiative lifetimes.

The 5846-Å fluorescence was studied at incident laser powers in the range 0 to 90 MW/cm$^2$. The laser pulsewidth (FWHM) varied between 9 and 10 nsec in this experiment. At 4-MW/cm$^2$ incident laser power we obtain fluorescent pulses 29 nsec long. In the 4- to 24-MW/cm$^2$ range we observe a dramatic decrease in the fluorescent pulsewidth from 29 to ~8 nsec, with most of the decrease occurring below 16-MW/cm$^2$ incident laser power. The fluorescent pulsewidth stays at 7 - 8 nsec for 24 - 90 MW/cm$^2$ incident laser power. The fluorescent pulsewidth is thus two to four times that of the laser at low incident power levels.

The fluorescent light intensity at 5846 Å varies linearly as the square of the input laser intensity, as we would expect for a second-order process; but its behavior divides itself into two regions, depending on the laser intensity. In the 0- to 42-MW/cm$^2$ incident laser-power range, which we shall call Region 1, the fluorescent intensity increases linearly as the square of the laser intensity with a slope of $1.7 \times 10^{-40}$ flr. photons/(laser photons)$^2$. This represents data taken over a range of ruby temperatures from -116.4°C to -117.9°C, and the results were consistently reproducible in experiments performed many months apart. Region 2 corresponds to high, never before attained, incident laser power levels that range from 42 to 90 MW/cm$^2$. The fluorescent intensity also varies linearly as the square of the incident laser intensity, but with a slope of only $3.7 \times 10^{-41}$ flr. photons/(laser photons)$^2$. Thus there is a leveling off of the fluorescent intensity yield at higher incident laser powers, as unusually short lifetimes are obtained.

The 4555-Å fluorescence corresponding to the 7$P_{3/2} \rightarrow 6S_{1/2}$ transition, or lower leg of the cascading single-photon transitions back to the ground state, was studied in a similar way for incident laser power in the range 0 to 72 MW/cm$^2$. Its behavior is different from
that of the 5846-Å fluorescence. The fluorescent pulsewidth increases only slightly, rather than decreasing at higher incident laser intensities. The duration of the fluorescent pulse for this transition is also an order of magnitude shorter than the calculated incoherent radiative lifetime. The fluorescent intensity vs laser-intensity-squared dependence also has two distinct regions of linear dependence, but the fluorescent intensity rises sharply, rather than leveling off, at high incident laser-power.

The incident laser intensity was varied between 0 and 7 MW/cm². The duration of the laser pulse was 7.5 to 9 nsec throughout this power range. We obtained fluorescent pulses 3 to 4 nsec in duration in the range of 0- to 14-MW/cm² incident laser power, with the pulsewidth increasing slightly to 4 to 5 nsec for incident laser power in the range 14 to 72 MW/cm². In the region of 0- to 12.2-MW/cm² incident laser power, the fluorescent intensity varies directly as the square of the laser intensity, with a slope of $1.6 \times 10^{-40}$ flr. photons/(laser photons)^2. At a threshold of 22.8-MW/cm² incident laser power the fluorescent yield increases by three orders of magnitude to a slope of $1.5 \times 10^{-37}$ flr. photons/(laser photons)^2. This linear dependence with the higher slope holds for the entire region 22.8- to 72-MW/cm² incident laser power. Note that the laser power threshold for the high yield of 4555-Å fluorescence is roughly the same as that for the production of the very short-lived, 8-nsec, 5846-Å fluorescence.

As previously reported, no fluorescence can be obtained when the ruby temperature is tuned above -114°C or below -121°C, or when the cesium cell is at room temperature. (The melting point of cesium is 28.5°C.) The fluorescent intensity drops sharply as the cesium temperature is decreased. The number density of the cesium atoms in the cell drops by about an order of magnitude for every 50°C decrease in temperature. Experiments are in progress to determine the exact nature of the dependence of the fluorescent intensity on the density.
of the cesium vapor. Theoretical study of the above experimental results is in progress, as are further experiments to study coherent effects in two-photon absorption.

F. FREQUENCYhifts IN RESONANT SYSTEMS*

(R. Friedberg, M. Friedlander, S. R. Hartmann)

We have completed construction of the experiment to measure the predicted shift in the resonance-transition frequency of atomic cesium. The tungsten-ribbon lamp housing is fitted with two collimator assemblies in order to use the light coming from both sides of the tungsten ribbon.

Each of the two cell-reservoir assemblies is housed in a two-section oven that will bake out the cell-reservoir assemblies prior to filling and control their temperatures during the experiment. Since the density of cesium in the absorption cell is the variable we wish to control, we must control separately the temperature of the absorption cell and that of the reservoir. We maintain the temperature of the reservoir lower than that of the cell so that the reservoir temperature determines the vapor pressure in the cell-reservoir assembly. We can then control the density in the cell by controlling the cell temperature. The temperature in the cell-reservoir assemblies is monitored by high output thermocouples and regulated by a four-channel proportional temperature controller with a stability of 0.005%.

We have obtained beam-splitting and beam-recombining optics which allow us to use for stabilization whichever of the cesium-resonance transitions is not being used for the experiment. Using an rf excited cesium lamp with this optical system, we are able to monitor the alignment and stability of both Fabry-Perot interferometers.
simultaneously during the experiment. We use a PDP-8/e computer interfaced to an analog-to-digital converter and to eight stepping motors (which rotate 10-turn potentiometers to control the parallelism and separation of the plates in the two Fabry-Perots) to lock the Fabry-Perots onto the cesium-resonance line.

We have aligned the exit-slit prism and have used it to separate the high and low frequency sides of the resonance lamp profile. Some initial parasitic light problems caused by the accidental equality of the prism apex angle and the bevel angle of the exit slit have been overcome.

The outputs of the two RCA 31034 photomultiplier tubes are clipped, using fast hot carrier diodes, to eliminate large noise spikes of unknown origin which are characteristic of this photomultiplier tube. This precaution prevents overloading of the lock-in amplifiers in their more sensitive ranges. The total power throughput of the system agrees with calculations based on the brightness of the tungsten lamp and the transmittance of the optical components.

The four signals of interest from the four lock-in amplifiers are monitored by the eight-channel analog-to-digital converter of the PDP-8/e computer (the same one used for Fabry-Perot stabilization). Fabry-Perot stabilization and signal averaging proceed simultaneously. We will measure the frequency shift in the near future.

*This research was also supported by the National Science Foundation under Grant NSF-GH-38503X.

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G. FREE-INDUCTION TWO- AND THREE-PULSE ECHO DEGRADATION DUE TO SPECTRAL DIFFUSION USING AN UNCORRELATED RANDOM-JUMP MODEL* (P. Fu, S. R. Hartmann, P. Hu)

As stated in last year's Progress Report, we have calculated the behavior of the free-induction, two-pulse echo, and three-pulse
echo signals using a sudden-jump model of spectral diffusion decay. The experimental situation has been unclear. Mims has measured the behavior of two-pulse and three-pulse echoes in CaWO₄ crystals doped with either Ce and Er or with Mn and Er. In both samples it is the flipping of the Er spins due to spin-lattice interactions (T₁ processes) which causes the spectral diffusion. His analysis of experimental results did not favor a sudden-jump model; however, he did not rule it out completely. He noted major discrepancies between his experimental and his calculated values of T₅M (the time it takes the signal to decay to 1/e of its original value) that make it impossible to decide conclusively in favor of any particular model.

We have reanalyzed the experimental data of Mims using our formulas, and we find rather good agreement with the sudden-jump model for those of his experiments in which either the Mn- or the Ce-echo signal is studied. On the other hand, we are unable to explain his experiment in which the Er-echo signal is studied.

For the two-pulse echo we found the echo amplitude to be given by
\[
E(2\tau) = \exp \left[-(\Delta \omega_{1/2}/W)K(2W\tau)\right],
\]
with
\[
K = z \left[\exp \left(\frac{-\tau}{\tau}\right)\right][I_1(z) + \left(\pi/2\right) [I_1(z)L_0(z) - L_1(z)I_0(z)]].
\]
In Eq. (1) the linewidth is given by
\[
\Delta \omega_{1/2} = \left(16\pi^2/9(3)^{1/2}\right)^{1/2} n \mu_a \mu_b^{-1},
\]
where \(\tau\) is the pulse separation time of the B spins, and \(n\) is their number density. The terms \(I_\nu(z)\) and \(L_\nu(z)\) are the modified Bessel and Struve functions of order \(\nu\). In the limit \(W\tau \ll 1\), \(E(2\tau)\) is given by
\[
E(2\tau) = \exp \left(-2W\Delta \omega_{1/2}\tau^2\right),
\]
while for \(W\tau \gg 1\), it is expressed as
\[
E(2\tau) = \exp \left[-2(1/\pi)^{1/2}W^{-1/2}\Delta \omega_{1/2}\tau^{1/2}\right].
\]
We plot in Fig. 57 the echo amplitude as a function of \(\Delta \omega_{1/2}\tau\) for several values of the parameter \(\eta = \Delta \omega_{1/2}/W\). Each curve in Fig. 57 starts out as a Gaussian. However, on the scale chosen, the initial Gaussian character for the curves with \(\eta = 2 \times 10^0, 2 \times 10^{-1}\) is not readily apparent, as it is confined to a small region near the origin. In fact the curve with \(\eta = 2 \times 10^0\) approximates a simple exponential, whereas the curve with \(\eta = 2 \times 10^{-1}\) first drops precipitately and exhibits approximately an \(\exp (-\tau^{1/2})\) behavior. One should note also that for a given value of \(\Delta \omega_{1/2}\tau\), the value of \(E(2\tau)\) is unity in the limit of very large or very small values of \(\eta\). It follows that the time \(T_M = 2\tau\), at which \(E(2\tau)/E(0) = 1/e\), has a minimum. This minimum occurs at \(\eta \approx 1\), i.e. \(W \approx \Delta \omega_{1/2}\). (8)

For the three-pulse echo we found
\[
E(2\tau + T) = \exp \left\{-(1/2)(\Delta \omega_{1/2}/W)\left[(1 - \exp -2WT)G(2W\tau)\right.ight.
\]
\[
+ (1 + \exp -2WT)K(2W\tau)]\right\},
\]
124
Fig. 57. The echo amplitude $E(2\tau)$ plotted as a function of $\Delta \omega_{1/2} \tau$ for several values of $\eta$. 

PARAMETER $\eta = \frac{\Delta \omega_{1/2}}{W}$ IS INDICATED.
with

\[ G(z) = z \exp(-z) \left[ I_0(z) + I_1(z) \right]. \]  

(4)

The function \( G(z) \) may be evaluated from the formula

\[ G(z) = zG'(z), \]

where \( G'(z) \) is plotted and tabulated in Ref. (2).

Mims has measured the two-pulse and three-pulse echo envelope for Ce in a CaWO\(_4\) sample doped with Er at 9.4 GHz and at several different temperatures. (9) Only the data taken at 2.2\(^\circ\)K is published, and these we have fit with our formulas, Eqs. (1) and (3), to obtain the results shown in Figs. 58 and 59. Since both two-pulse and three-pulse echo experiments were performed on the same sample at the same temperature, we have used the same values of \( \Delta \omega_{1/2} \) and \( W \) in fitting all the data. The fit is reasonably good.

The concentrations of the Ce and Er were \( 2 \times 10^{18} \) spins/cm\(^3\) and \( 2.5 \times 10^{18} \) spins/cm\(^3\), respectively. This leads to a value of \( \Delta \omega_{1/2} = 6.1 \times 10^6 \) sec\(^{-1}\), which is only a factor of two larger than that used in our fit. This is probably within the experimental error of the measured Er concentration.

The value of \( W \) can be obtained from \( T_1 \) by the relation \( W = 1/2T_1 \). Since the echo amplitude decay of the Ce spins was measured with the applied magnetic field normal to the c-axis, we have not used the value \( W = 6.3 \times 10^1 \) as would be obtained from Mims' measurement of \( T_1 \) for Er\(^{3+}\) in CaWO\(_4\). Instead we have used the data of Antipin et al., (10) who measured \( T_1 \) in Er-doped CaWO\(_4\) with \( H \) normal to the c-axis. Their measurements were made at 9.3 GHz and 36 GHz. Extrapolating their measurements to the 54.5-GHz measurement corresponding to the Er\(^{3+}\) splitting at which the Ce measurements were made, we find a value of \( W = 2.1 \times 10^3 \), which is close to the value \( W = 3.5 \times 10^3 \) used in our fit. We summarize the above data on \( \Delta \omega_{1/2} \) and \( W \) in Table XIV.

The only echo-envelope data shown for the CaWO\(_4\) sample doped with Mn and Er are for the two-pulse echo. Here we have obtained the
TABLE XIV. Values of $\Delta \omega_{1/2}$ and $W$ relevant to analysis of Ce-echo data in CaWO$_4$:Ce, Er.

<table>
<thead>
<tr>
<th></th>
<th>Mims (a)</th>
<th>Antipin et al. (b)</th>
<th>Our data</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\Delta \omega_{1/2}$</td>
<td>$6.1 \times 10^6$</td>
<td>$6.3 \times 10^1$</td>
<td>$2.1 \times 10^3$</td>
</tr>
<tr>
<td>$W$</td>
<td>$3 \times 10^6$</td>
<td>$3 \times 10^6$</td>
<td>$3 \times 10^6$</td>
</tr>
</tbody>
</table>


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TABLE XV. Values of $\Delta \omega_{1/2}$ and $W$ relevant to analysis of Mn-echo data in CaWO$_4$:Mn, Er.

<table>
<thead>
<tr>
<th></th>
<th>Mims (a)</th>
<th>Our data</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\Delta \omega_{1/2}$</td>
<td>$0.55 \times 10^6$</td>
<td>$0.55 \times 10^6$</td>
</tr>
<tr>
<td>$W$</td>
<td>$2.5 \times 10^6$</td>
<td>$2.3 \times 10^6$</td>
</tr>
</tbody>
</table>

Fig. 58. Two-pulse echo amplitude $E(2\tau)$ for Ce in (Ca, Ce, Er) WO$_4$ sample. The solid line is the theoretical fit using Eq. (1) with the parameters $W$ and $\Delta \omega_{1/2}$ shown in the figure. The data are those from Fig. 6, Ref. (3) renormalized for best fit.
Fig. 59. Three-pulse echo amplitude $E_s(2\tau+T)$ for Ce in the (Ca, Ce, Er) WO$_4$ sample for different values of $\tau$. The solid lines are the theoretical fits using our calculations with the parameters $W$ and $\Delta\omega_1/2$ shown in the figure. The data are those from Fig. 7, Ref. (3) renormalized for best fit.
fit with our Eq. (1) shown in Fig. 60. The concentrations of Mn and Er correspond to $3.0 \times 10^{16}$ spins/cm$^3$ and $1.1 \times 10^{18}$ spins/cm$^3$, respectively. This yields a value of $\Delta w_{1/2}$ of $0.55 \times 10^6$ sec$^{-1}$, which is exactly what we have used in our fit. For $W$ we have used the value $2.3 \times 10^6$ sec$^{-1}$, which is close to the value of $2.5 \times 10^6$ sec$^{-1}$ which we would obtain from the $T_1$ measurement of Mims. In this case the echo measurements were made with $H$ parallel to the $c$-axis so that Mims' measurements apply. Our value of $W$ is well within experimental error as it corresponds to a region of temperature $T$ where one must extrapolate measured data. We summarize the $\Delta w_{1/2}$ in Table XV.

If we had drawn Figs. 58 and 59 with respect to $\Delta w_{1/2} T$, rather than with respect to $\tau$, and if we had then chosen the scale of Fig. 57, the curves would have been modified only slightly. This follows because for Fig. 58 we have a value of $\Delta w_{1/2} \tau = 31.5 \pm 30$ at $\tau = 10.5 \mu$sec, whereas for Fig. 60 this value is $\Delta w \tau = 33 \pm 30$ at the corresponding endpoint $\tau = 60 \mu$sec. For Figs. 58 and 60 the values of $\eta$ are $8.6 \times 10^2$ and $2.4 \times 10^{-1}$, respectively, which places them in the context of Fig. 57. From Eq. (1) we can calculate

$$E(2\tau) = \exp (-2W\Delta w_{1/2} \tau^2), \quad \eta W \ll 1$$

and

$$E(2\tau) = \exp \left[-2(1/\eta)W^{-1/2} \Delta w_{1/2} \tau^{1/2}\right], \quad \eta W \gg 1.$$ 

The above values of $\eta$ do not quite correspond to the extreme limits characterized by these equations. In fact, Mims obtains a good fit using $E(2\tau) = \exp \left[(-2\tau/T_M)^x\right]$, with $x = 1.9$ and $x = 0.7$ for the data we have plotted in Figs. 58 and 60, respectively. (11) In the extreme limits these values would be $x = 2.0$ and $x = 0.5$.

It is important to note that in order to obtain the correct value of $T_M$ it is necessary to obtain data points for sufficiently small $\tau$. This is brought out dramatically in Fig. 60, where a simple extrapolation of the data points leads to a value of $T_M$ which is approximately a factor of three larger than it should be on the basis of the solid curve drawn in Fig. 60. Some of the $T_M$ values of
Fig. 60. Two-pulse echo amplitude for Mn$^{2+}$ in the (Ca, Mn, Er) WO$_4$ sample. The solid line is the theoretical fit using Eq. (1) with the parameters $W$ and $\Delta\omega_{1/2}$ shown in the figure. The data are those from Fig. 8, Ref. (3) renormalized for best fit.
Ref. (4) are therefore considerably different from what we would estimate on the basis of our formulas. In particular we would expect that the plot of $T_M$ as a function of $T$ given in Fig. 5 of Ref. (4) should be modified. A major effect on this plot would be to shift the minimum of $T_M$ [at $T \sim 4.5^\circ K$ according to Fig. 5, Ref. (4)] in the direction of higher temperatures. From the data of Antipin et al. (12), which enable us to estimate $W$ as a function of $T$, and from our formulas, we infer that $T_M$ should be a minimum at $\sim 6.5^\circ K$. This may correspond to a bigger shift than we can expect by reinterpreting $T_M$.

In contrast to the success we have had in fitting the Ce- and Mn-echo signal data, we have not been able to fit Mims' measurement of the two-pulse decay envelope corresponding to the Er-spin signal [Fig. 9, Ref. (4)]. These experiments were performed with the same CaWO$_4$ crystals used in the Ce-echo measurements. In order to obtain a fit we have had to use values of $W$ about two orders of magnitude larger than could be inferred by $T_1$ measurements. The problem is that the echo amplitude decays too fast. Mims has also noted the anomalously fast decay and has discussed several possible explanations for it.

From the rather good agreement between the echo data and our formulas using parameters whose value is close to that derived by independent considerations, we conclude that the sudden-jump model may very well be appropriate for resonance experiments applied to this material. More experimental work is clearly necessary. We have obtained a CaWO$_4$ crystal doped with Nd$^{3+}$ and will investigate the spectral diffusion behavior experimentally.

*This research was also supported by the National Science Foundation under Grant NSF-GH-38503X.

(1) CRL Progress Report, June 30, 1973, p. 115.
H. SUPERRADIANCE*

(R. Friedberg, S. R. Hartmann)

We have extended our work on superradiant stability (1,2) to pinpoint the conditions under which the superradiant condition is unstable.

The field of an oscillating dipole can be resolved into a real part (in phase with the dipole) and an imaginary part (90° behind). The reaction of the real part shifts the frequency, while that of the imaginary part damps the radiation.

For coherent spontaneous emission by a small sample into free space, Dicke and others have derived the equation \( \frac{d\varphi}{dt} = (1/2)N \tau_0^{-1} \sin \theta \) for the tipping angle \( \theta \), but the derivation assumes that the field is uniform throughout the sample. Since this is not true of the real component, which far exceeds the imaginary, we ask whether there is any system which should exhibit "Dicke decay."

It may be thought that nmr experiments have verified Dicke's equation for the small sample, but these experiments have not been done in free space. A tuned coil surrounds the sample and absorbs its energy before it has time to radiate. The sample is damped not by the imaginary component of its own field but by the real component, which the coil amplifies with a lag of 90°. We do not consider this an example of Dicke decay.
Certain ringlike arrangements of atoms in single file will produce reaction fields that are the same for all atoms because of circular symmetry. Such a system will exhibit true Dicke decay, but the arrangement seems unrealistic.

In a large sample, the real field can be neglected but the imaginary part is not uniform. Certain authors have nevertheless assumed that the atomic excitation density is uniform and have derived Dicke's equation for the large sample. Such derivations are incorrect, since a ray emitted coherently in a favored direction must gain intensity as it nears the exit face. The experiment performed at MIT indicated secondary peaks (ringing) in the emission intensity, in contradiction to Dicke's equation but in agreement with a one-dimensional Maxwell-Bloch analysis.

There remains the possibility that in small samples of particular shape, the nonuniformity of the real field, though large, does not destroy the coherence among parts of the sample because of subtle restoring effects. We have studied the sphere in detail. We expect it, starting from complete inversion, to follow Dicke's equation down to the Bloch equator and suddenly dephase.

Our analysis uses a linear approximation for the small departures from uniformity in the Bloch vector. The linearized equations admit proper solutions that predict oscillations of frequency $\sim (kR)^{-3} \cos \theta$ and amplitude $\sim (kR)^2 \sin \theta$, with characteristic spatial distribution. Near the equator certain modes become unstable because of the role played by the third Bloch component.

We have also divided the sphere into annular regions and followed their development by computer, taking no account of the foregoing concepts. This calculation has verified the existence of oscillations, the dependence of frequency and amplitude on $\theta$ and $kR$, and the dramatic loss of coherence at the equator.

*This research was also supported by the National Science Foundation under Grant NSF-GH-38503X.*

IV. MACROSCOPIC QUANTUM PHYSICS

A. QUANTIZED ROTATION AND VISCOSITY OF SUPERFLUID HELIUM
   (R. Biskeborn, R. Guernsey)

An analysis of the data from an experiment in which we measured the temperature dependence of the viscosity of liquid He$^4$ near the superfluid transition is in progress. The apparatus was similar to that described previously$^{(1)}$ with the following modifications: We replaced the linenedized Bakelite (Micarta) chamber with a copper sample chamber (a hollow cylinder 4.62 cm in diameter and 0.77 cm high) in order to simplify the geometry by eliminating the capillary fill tube, to increase the thermal contact between the helium boundary layer and the resistance thermometer, and to increase the strength of the cell. This permitted operation at higher differential pressures between the cell and the surrounding vacuum can (see Fig. 61). The new torsion pendulum was sufficiently sensitive to refine considerably the earlier work of Webeler and Allen,$^{(2)}$ who measured the damping on a piezoelectric crystal driven in a torsional mode. In this latter work, in order to provide reliable thermometry, the He$^4$ sample was doped with He$^3$ (0.5%) to suppress its lambda point relative to that of the superfluid bath. In the present work the good thermal contact between the resistance thermometer, which was mounted in a copper housing on the bottom of the cell and the helium sample, contained in the oscillating cell, resulted in reliable thermometry both above and below T$_\lambda$.

All of the lambda-point data were taken with the main bath (outside the vacuum can) either warming or cooling to produce drift rates of typically 80$^\circ\mu$K/min to 10$^\circ\mu$K/min in the cell via exchange gas contact through the can (at a pressure of typically 200$\mu$ Hg). The amplitude of oscillation of the pendulum, which is driven on resonance in
Fig. 61. Probe.
an electronic feedback loop described earlier,\(^{(3)}\) is proportional to the voltage on the coil [now attached to the bottom of the cell (see Fig. 61)]. Since the impedance of the coil on resonance is purely resistive and inversely proportional to the exponential decay constant of the pendulum, it is sufficient to monitor the (constant) coil voltage and (changing) current as a function of temperature to determine this constant, which is proportional to the square root of normal fluid density times the viscosity (after the background has been subtracted out).

In order to compute viscosity, the normal fluid density must be known. Taking the most recent work available\(^{(4)}\) we find from a preliminary analysis (see Figs. 62 and 63) that the formula

\[
\frac{\eta - \eta_\lambda}{\eta_\lambda} = A \left( \frac{T - T_\lambda}{T_\lambda} \right)^x
\]

gives \(x = 0.67\) and a value for \(A\) not in agreement with previous measurements\(^{(5)}\) (see Fig. 63). It is interesting to note that the superfluid fraction also varies as \([\frac{T - T_\lambda}{T_\lambda}]^{2/3}\) as a first approximation.\(^{(6)}\) The resolution is such that it is possible to resolve changes in viscosity of the order of 0.025% corresponding to temperature intervals of \(\approx 5^\circ \mu K\). The lambda point is identified by the abrupt change in slope in the damping itself to better than \(5^\circ \mu K\). For small (\(< 100 \mu K/\text{min}\)) rates the damping-temperature slope is essentially independent of drift rate.

Data have been taken over two decades in amplitude at 732.5-Hz oscillation frequency. The lowest of these results gives a peak angular velocity equal to one-half of the critical angular velocity \((\omega_c = 552 \mu \text{rad/sec})\) for the creation of one vortex in a steadily rotating cylinder of the same dimensions. No amplitude dependence was found. It is not yet known if the largest peak angular velocity is as large as any previously studied.

In order to make a direct comparison to the data of Ref. \(4\) we used a 0.5% mixture of \(\text{He}^3\) in \(\text{He}^4\). We found that the lambda point of the mixture was suppressed by \(7.75^\circ \mu K\), but that the viscosity was the
Fig. 62. Viscosity of He\textsuperscript{4} near $T_\lambda$. 

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Fig. 63. Critical exponents for the viscosity near $T_\lambda$. 

$|\Delta \eta/\eta_\lambda| = A|\epsilon|^x$
same. While in qualitative agreement with Ref. (2), our data give an exponent which is 26% lower. (7)

It has also been possible to record data over the temperature range from 1.2°K to 4.2°K. These data are now being analyzed. Previous measurements have indicated a discrepancy between oscillating and steady rotation measurements of viscosity between 1.2° and 1.5°K. We expect that the present research may help clarify this problem.

Program for the next interval: After completing the current analysis, we will attempt to understand the structure in the damping which we found with the Micarta cell. (8) We then hope to study the pressure dependence (up to perhaps 15 atm) of the exponent x cited above.

(1) CRL Progress Report, June 30, 1973, p. 129.
(3) CRL Progress Report, op. cit., p. 129.
(7) G. Ahlers, op. cit., p. 151.
(8) CRL Progress Report, op. cit. p. 129.

B. FACTORS DETERMINING THE FRACTION OF He-II IN THE SUPERFLUID STATE
(R. Guernsey, J. Kaplan)

In the last Progress Report (1) an experiment was described in which relative motion of the superfluid and its container might be sensed by thermal modulation of the sample. We have completed construction of the apparatus and have made the first trial run.

The results are encouraging: The random noise was reduced to less than 1 nV in a pendulum with a Q of 2000, and the heater could be run at more than 1/4 W in the steady state. The precision in measuring angular velocity of the superfluid should therefore be about 5 x 10⁻⁷ rad/sec. The rotation quantum interval for the superfluid
in this sample container should be about $400 \times 10^{-7}$ rad/sec.

In this first run, however, we were unable to study the superfluid motion because of a large additional coupling between the oscillating heat input and the pendulum. We have investigated this signal and suspect that it originates in the generation of sound or thermal expansion and contraction of the wires leading to the pendulum coil.

In the coming months we will attempt to eliminate the stray coupling and then proceed to study the quantized rotation of the superfluid.


C. EXPERIMENTS ON THE NEW PHASES OF LIQUID He$^3$

(A. Becker, R. Guernsey, R. J. McCoy, M. Steinback, C. S. Wu)

We are continuing an experimental program to measure both mechanical properties and the interaction of magnetic and mechanical properties in the anomalous phases, A and B, of liquid He$^3$. Our approach utilizes a high-Q torsion pendulum as described in last year's Progress Report. (1)

Our first experimental apparatus, an Andronikashvili-type cell to measure the superfluid fraction of He$^3$, is now almost finished. We have completed construction and pressure testing at 60 atm of the cell, which consists of 93 five-mil disks spaced three mils apart, the pressurization system and a capacitative pressure gauge; and the thermal parts, which include a vibration isolation link to the dilution refrigerator, a superconducting thermal link, and a CMN demagnetization refrigerator. We have completed and tested the electronics for the system, primarily a sensing and feedback apparatus which drives the pendulum and monitors its motion. We are in the final steps of incorporating this unit into the apparatus.

Program for the next interval: We will measure the superfluid density $\rho_s$ and normal viscosity $\eta_n$ of He$^3$ A and B, both with zero magnetic field and with applied axial and transverse magnetic fields.

(1) CRL Progress Report, June 30, 1973, p. 137.
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The facilities are available for the Columbia Radiation Laboratory.