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OUTDOOR FLAT-PLATE COLLECTOR PERFORMANCE PREDICTION FROM SOLAR SIMULATOR TEST DATA

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ABSTRACT

This paper describes how collector performance data obtained from tests with a simulator can be modified for real-life conditions. The approach taken is to correct the performance data obtained with the simulator for the variable conditions of ambient temperature, wind, incident angle, flow rate, etc., that are encountered in outdoor conditions. Modification of simulator data is accomplished by combining experiment with theory. The technique is demonstrated by application to a spectrally selective and a nonselective type of collector. This kind of modified simulator collector performance data should be valuable in solar systems analysis and for collector performance ranking based on all-day calculated conditions.

INTRODUCTION

An area presently being investigated by the NASA-LRC in its efforts to aid in the utilization of alternate energy sources is the use of solar energy for the heating and cooling of buildings. An important part of this effort is the investigation of flat-plate collectors which have the potential to be efficient, economical, and reliable. Efficient collectors will be an important consideration in the realization of effective solar cooling systems. The approach being taken at the Lewis Research Center for determining collector performance is to test collectors under simulated (indoor) and actual (outdoor) conditions.

Indoor testing of collectors with a solar simulator has permitted ranking of collectors on the basis of performance\(^1\) and a determination of the key parameters affecting collector performance\(^2\). The solar simulator approach has been extremely effective in evaluating collector performance on a relative basis. The questions which need answering are: (1) How good are the simulator results when compared to actual conditions? (2) Since the performance data is determined under standard conditions of wind, ambient temperature and flow rate, what corrections are needed for actual conditions other than the standard?

If it can be shown that the simulator does indeed do a good job of simulating actual conditions and that the results can be corrected for conditions other than those of the simulator tests, then the simulator results can be used in the design and analysis of solar heating and cooling systems. The application of simulator data to outdoor conditions would also permit performance ranking to be based on all-day performance calculations. The objective of this paper is to present evidence of the simulation ability of the indoor collector test approach, and to demonstrate how collector performance from the simulator can be modified to account for variable outdoor conditions.

SOLAR SIMULATOR

Experimental Facility

A drawing of the facility is presented in Fig. 1. The primary components of the facility are the energy source (solar simulator), the liquid flow loop, and the instrumentation and data acquisition equipment. A summary of information describing the facility is presented in Table I. More detail on the manner of testing, instrumentation, etc., may be found in Refs. 1, 2 and 3.

Solar Simulator

The basic rational for the use of a solar simulator for the testing of solar collectors was given in Ref. 4. This approach allows for controlled conditions that make it possible to properly compare the performance of different collector types. The simulator shown in Fig. 1 consists of 143 tungsten-halogen 300-watt lamps placed in a modular array with Fresnel lenses placed at the focal distance so as to collimate the radiation.

A comparison of spectral characteristics of the simulator output with air mass-2 sunlight is given in Table II. Table II demonstrates that the solar simulator does an excellent job of simulating the sun's radiation in this application. The fact that the spectral qualities of the simulator come close to actual sunshine is a key requirement in using the indoor approach to simulate actual conditions. For more detail information on the spectral qualities of the simulator and other information see Ref. 3.

Correlative Method

The experimental efficiency calculated by the use of

\[
\eta = \frac{G_p(T_o - T_i)}{\dot{q}_{DR}}
\]

is calculated in a manner corresponding to the following basic collector equations.

\[
\eta = \frac{\alpha r - U_L(T_f - T_a)}{q_{DR}}
\]  
\[
\eta = F'\left[\alpha r - U_L(T_f - T_a)\right]/q_{DR}
\]  

Examples of how these equations can be used in conjunction with the experimental data were given in Refs. 1, 2 and 4. The performance curves from Ref. 2 for a black-nickel two-glass collector and a black paint two-glass collector are given in Figs. 2(a) to (c) and 3(a) to (c), respectively. We see from Eqs. (2-4) and Figs. 2 and 3 that depending on how we plot the basic performance we can
obtain information on the basic parameters affecting collector performance \((aT, F', FR, \text{and } UL)\) and have an approach by which to obtain basic correlating equations. The correlating equations for the data of Figs. 2 and 3 have the basic form of

\[ n = a_\phi - b_\phi - C_\phi \psi^2 \]  
\[ n = a_\psi - b_\psi - C_\psi \varphi^2 \]  
\[ n = a_0 - b_0 - C_0 \delta^2 \]  

where \(\phi = (T_p - T_a)/q_{DR}\)  
\(\varphi = (T_f - T_a)/q_{DR}\)  
and \(\delta = (T_1 - T_o)/q_{DR}\)

Comparing Eqs. (5-7) with the corresponding Eqs. (2, 3 and 4), we see the following relationships:

\[ (aT)_B = a_0 \]  
\[ (F'aT)_B = a_0 \]  
\[ (FRaT)_B = s_0 \]  
\[ (ULs) = b_\psi + C_0 \]  
\[ (F'UL)_B = b_\psi + C_\psi \]  
\[ (FRUL)_B = b_0 + C_0 \]  

These relationships will form the basis later for modifying the basic correlation Eqs. (5-7) to environmental conditions other than those used in obtaining these equations (conditions of Table I).

Another check of the simulator’s spectrum as compared to that of the sun’s is to calculate the experimental value of absorptivity for a wavelength sensitive surface such as black nickel. Using Eq. (8) and the measured value of glass transmittance, we can calculate the value of the absorptivity determined with the simulator and compare it with the value obtained with a spectrophotometer. The comparison shown in Table III gives further evidence of the simulator’s ability to simulate the spectrum of the sun.

**Indoor vs. Outdoor Data**

Collectors of the same type and design as those of Figs. 2 and 3 were tested under contract to NASA-LeRC by the Honeywell Corporation in Minneapolis, Minnesota. A black-nickel two-glass and a black-paint two-glass collectors were tested both indoors under simulated conditions and outdoors. The solar simulator used by Honeywell is a copy of the NASA-LeRC solar simulator. The results of the indoor tests with the two collector types were used to predict the outdoor tests of these same collectors. A comparison of the indoor and outdoor tests is given in Fig. 4. The time previous to the steady state arrow of 1800 F shown in Fig. 4 was a period in which the collector and the rest of the system was warming up. This period can be considered a total test system transient. This period, as shown in Fig. 4, existed for about 1 hour. Another collector transient period occurred from 12 p.m. to 1 p.m. due to a condition in which the incident flux decreased. The use of the steady state simulator results are not expected to be completely applicable during a transient period due to the collector heat capacity. The effect of this is a lag between the calculated and experimental energy collected (useful solar flux, \(q_0\)). This paper does not consider transient effects. However, for collectors of small heat capacity these transient effects will have little effect on all day collector performance. This transient effect needs to be considered in the dynamic analysis of solar systems. It appears from Fig. 4 that the steady-state collector results obtained with the solar simulator does a good job of predicting the steady-state outdoor tests.

**Method Of Modifying Simulator Data**

The first step in establishing modified versions of the simulator data is to rework the correlation Eqs. (5-7) into a modified form. The three parameters requiring modification so that variable conditions may be comprehended are the flow factor \((FR)\), the overall heat loss coefficient \((UL)\) and the product of transmittance and absorptance \((aT)\). Correction factors related to the simulator values of \(FR, UL\) and \(aT\) are as follows:

\[ K_{FR} = FR/FR_s \]  
\[ K_{UL} = UL/UL_s \]  
\[ K_{aT} = aT/(aT)_s \]  

Combining Eqs. (14-16) with Eqs. (10,13 and 7) results in a modified version that can be utilized for performance predictions for the direct component of solar energy.

\[ n = K_{FR} K_{UL} K_{aT} \left[ K_{FR} a_0 - K_{UL} (b_\delta + C_0 \delta^2) \right] \]

The method of determining the correction factors \((K_{UL}, K_{FR}\) and \(K_{aT}\)) follows.

**Heat Loss Modification (\(K_{UL}\))**

Use of theory leads to an approach for modifying the overall heat loss coefficient \((UL)\) determined experimentally in the simulator facility. The overall heat loss coefficient has three components as represented by the following equation

\[ UL = UL_c + UL_R + UL_e c/\rho A_p/A_c \]

The rear conduction loss coefficient \((UL_R)\) is easily calculated by

\[ h_L/\delta \]  

and for the edge loss coefficient the value given by Whillier (3) is appropriate.
For the cover heat loss coefficient \( U_{L,c} \), a solution of the following equation is necessary:

\[
U_{L,c} = 0.08 \quad (20)
\]

Absorber Plate To 1st Cover

\[
q_{L,c} = \frac{c}{(T_p - T_{B1})^n} + \frac{\sigma}{(1/c_p)^{1/3} + (1/c_v)^{1/3}} \left( T_p - T_{B1} \right) \quad (21)
\]

1st Cover To 2nd Cover

\[
q_{L,c} = \frac{c}{(T_{B1} - T_{B2})^n} \quad (22)
\]

2nd Cover To Environment

\[
q_{L,c} = h_0\left( T_{B2} - T_a \right) + \frac{\sigma}{(T_{B2}^4 - T_{sky}^4)} \quad (23)
\]

\[
U_{L,c} = q_{L,c}/(T_p - T_a) \quad (24)
\]

The only additional information required for the solution of Eqs. (18-24) is knowledge of the coefficients \( C \) and \( n \) related to convective heat loss. For obtaining this information the equations relating the heat transfer by natural convection are applicable. The following is a summary of possible candidates for predicting heat loss due to natural convection:

De Craaf and Van Der Held(6) made a systematic experimental investigation of heat transfer in enclosed plane air layers in horizontal, oblique and vertical positions. The following equations were deduced:

For \( \theta_T = 0^\circ \):

\[
\begin{align*}
\text{Nu}_L &= 1 \quad \text{Gr}_L < 2 \times 10^3 \\
\text{Nu}_L &= 0.0507 \quad \text{Gr}_L < 5 \times 10^4 \\
\text{Nu}_L &= 3.8 \quad 5 \times 10^4 < \text{Gr}_L < 2 \times 10^5 \\
\text{Nu}_L &= 0.0426 \quad \text{Gr}_L < 2 \times 10^5
\end{align*}
\]

For \( \theta_T = 20^\circ \):

\[
\begin{align*}
\text{Nu}_L &= 1 \quad \text{Gr}_L < 2 \times 10^3 \\
\text{Nu}_L &= 0.0507 \quad 2 \times 10^3 < \text{Gr}_L < 3 \times 10^4 \\
\text{Nu}_L &= 3.6 \quad 4 \times 10^4 < \text{Gr}_L < 5 \times 10^5 \\
\text{Nu}_L &= 0.0402 \quad \text{Gr}_L < 2 \times 10^5
\end{align*}
\]

For \( \theta_T = 30^\circ \):

\[
\begin{align*}
\text{Nu}_L &= 1 \quad \text{Gr}_L < 3 \times 10^3 \\
\text{Nu}_L &= 0.0588 \quad 3 \times 10^3 < \text{Gr}_L < 5 \times 10^4 \\
\text{Nu}_L &= 0.039 \quad \text{Gr}_L > 2 \times 10^5
\end{align*}
\]

For \( \theta_T = 45^\circ \):

\[
\begin{align*}
\text{Nu}_L &= 1 \quad \text{Gr}_L < 4 \times 10^3 \\
\text{Nu}_L &= 0.0503 \quad 4 \times 10^3 < \text{Gr}_L < 5 \times 10^4 \\
\text{Nu}_L &= 0.0372 \quad \text{Gr}_L > 2 \times 10^5
\end{align*}
\]

For \( \theta_T = 60^\circ \):

\[
\begin{align*}
\text{Nu}_L &= 1 \quad \text{Gr}_L < 6 \times 10^3 \\
\text{Nu}_L &= 0.0431 \quad 5 \times 10^3 < \text{Gr}_L < 5 \times 10^4 \\
\text{Nu}_L &= 0.0354 \quad \text{Gr}_L > 2 \times 10^5
\end{align*}
\]

For \( \theta_T = 70^\circ \):

\[
\begin{align*}
\text{Nu}_L &= 1 \quad \text{Gr}_L < 7 \times 10^3 \\
\text{Nu}_L &= 0.0384 \quad 10^4 < \text{Gr}_L < 8 \times 10^4 \\
\text{Nu}_L &= 0.0342 \quad \text{Gr}_L > 2 \times 10^5
\end{align*}
\]

For \( \theta_T = 90^\circ \):

\[
\begin{align*}
\text{Nu}_L &= 1 \quad \text{Gr}_L < 7 \times 10^3 \\
\text{Nu}_L &= 0.0384 \quad 10^4 < \text{Gr}_L < 8 \times 10^4 \\
\text{Nu}_L &= 0.0317 \quad \text{Gr}_L > 2 \times 10^5
\end{align*}
\]

De Craaf and Van Der Held concluded from their results that the \( \text{Nu}_L \) depends only on inclination when the air motion is turbulent and one may freely interpolate between horizontal and vertical positions only if \( \text{Gr}_L > 10^5 \). Between 20° and 70°, interpolation can be made if \( 5 \times 10^3 < \text{Gr}_L < 6 \times 10^4 \).

Tabor(7) recommended the results of his correlation using the 1954 Housing and Home Finance Agency Report 32 which in dimensionless form may be written in generalized form as
For $\theta = 0^\circ$:

$$\text{Nu}_L = 0.152 \cdot \text{Gr}_L^{0.281} \quad 10^4 < \text{Gr}_L < 10^7$$

(48)

For $\theta = 45^\circ$:

$$\text{Nu}_L = 0.0923 \cdot \text{Gr}_L^{0.310} \quad 10^4 < \text{Gr}_L < 10^7$$

(49)

For $\theta = 90^\circ$:

$$\text{Nu}_L = 0.0326 \cdot \text{Gr}_L^{0.381} \quad 1.5 \times 10^6 < \text{Gr}_L < 1.5 \times 10^8$$

(50)

$$\text{Nu}_L = 0.0616 \cdot \text{Gr}_L^{0.327} \quad 1.5 \times 10^7 < \text{Gr}_L < 10^7$$

(51)

A subsequent experimental work using fluids whose Prandtl number varied over a very wider range of values was the work of Dropkin and Somerovalles (8)

For $\theta = 0^\circ$:

$$\text{Nu}_L = 0.069 \cdot \text{Ra}_L^{1/3} \cdot \text{Pr}^{0.074} \quad 1.5 \times 10^3 < \text{Ra}_L < 7.5 \times 10^5$$

(52)

For $\theta = 30^\circ$:

$$\text{Nu}_L = 0.065 \cdot \text{Ra}_L^{1/3} \cdot \text{Pr}^{0.074} \quad 1.5 \times 10^3 < \text{Ra}_L < 7.5 \times 10^5$$

(53)

For $\theta = 45^\circ$:

$$\text{Nu}_L = 0.059 \cdot \text{Ra}_L^{1/3} \cdot \text{Pr}^{0.074} \quad 1.5 \times 10^5 < \text{Ra}_L < 2.5 \times 10^7$$

(54)

For $\theta = 60^\circ$:

$$\text{Nu}_L = 0.057 \cdot \text{Ra}_L^{1/3} \cdot \text{Pr}^{0.074} \quad 1.5 \times 10^5 < \text{Ra}_L < 2.5 \times 10^7$$

(55)

For $\theta = 90^\circ$:

$$\text{Nu}_L = 0.049 \cdot \text{Ra}_L^{1/3} \cdot \text{Pr}^{0.074} \quad 5 \times 10^4 < \text{Ra}_L < 2.5 \times 10^8$$

(56)

The above equations may be put into a form first used by Hottel and Woertz (9),

$$q = C(T - T_B)^n$$

(57)

The constant $C$ in Eq. (57) is a function of temperature and angle of tilt and the value of $n$ depends on whether the fluid between the walls is in laminar or turbulent condition. Using the above equations for natural convection heat loss, values of $C$ and $n$ were calculated for a black nickel two-glass and a black paint two-glass collector, both of which had a gap distance for free convection of 1 1/4 in. The results of these calculations are shown as Table IV. Also shown in Table IV are the values of $C$ and $n$ suggested by Whillier (5). Use of Table IV with Eqs. (21-24) results in theoretical values of the cover heat loss coefficient ($U_{LC}$), which can be compared to the simulator determined heat loss coefficients. The simulator cover heat loss coefficient was determined with Eqs. (18-20) by using the values of the experimental overall heat loss coefficient and the collector back and edge loss coefficient. The experimental overall heat loss coefficient was calculated using Eq. (21) with an average flux of 250 BTU/hr ft$^2$. The edge and rear collector losses were approximately 15% of the total loss in the case of the black paint two-glass collector and 21% for the black nickel two-glass collector. The comparison between the theoretical and experimental cover heat loss coefficients are shown in Fig. 5. Figure 5 appears to indicate that the experimental heat loss is larger than predicted from theory. The difference between theory and experiment is especially dramatic in the case of the selective black nickel collector where the majority of the heat loss is by free convection.

It appears that the convection loss equation suggested by Whillier comes closest to the experimental findings. However, the exponent (n) suggested by Whillier does not satisfy the turbulent conditions (as indicated by Gr) encountered in the two collectors tested. Duffle and Beckman (10) recommend the Home Finance equations. Since these equations do about as well as Whillier's and have an exponent (n) consistent with the Gr no, they will be used for modification of the experimental values of heat loss. Simply, the values of $C$ in the Home Finance equation are corrected so that the theoretical values of the cover heat loss coefficient ($U_{LC}$) is equal to the experimental value of the cover heat loss coefficient. Using these "experimental" values of $C$ in Eqs. (21-24), we have a means by which we can calculate the effect of ambient temperature (Fig. 6), sky temperature (Fig. 7(a) and 7(b) and wind (Fig. 8). Figure 6 shows that the effect of ambient temperature on the heat loss coefficient is most pronounced at the lower plate temperatures for the black nickel two-glass collector. This effect could be explained by the low radiation heat loss component of the black nickel collector causing a cooler glass condition. A glass temperature which is lower than one would get at high plate temperature or high plate emittance increases the convection losses and thus increasing the heat loss coefficient. Increased convection losses at lower plate temperatures is a possible explanation of the curve forms shown in Fig. 7. It can be seen from Fig. 8 that the effect of wind on the heat loss coefficient is to increase it, as expected, but for wind speeds greater than the simulator wind speed, the increase in heat loss due to wind speed is small.

In general, once we have fixed on a value of $C$ using the experimental data we can calculate the cover heat loss coefficient at different conditions.

$$U_{LC} = f(T_p, T_{sky}, T_0, T_B)$$

(58)

Use of Eqs. (18-20) permits a calculation of the overall heat loss coefficient:

$$U_L = f(T_p, T_{sky}, T_0, T_B)$$

(59)
The simulator results may be expressed:

\[ U_{L_s} = f(T_a = \text{const.}, T_{sky} = \text{const.}, T_p = \text{const.}) \]  

(60)

The heat loss modifying factor (Eq. (15)) is obtained from Eqs. (59) and (60).

Since the simulator results are obtained at a fixed tilt angle, a way is needed to modify the experimental value of \( C \). The present collector experiments were run at a tilt angle of 57°.

Using the variation of \( C \) with respect to tilt angle according to the equation for BeGraaf and Van Der Field we have:

\[ C_0 \to -k 6.38 \times 10^{-4} (aT - 57) + C_{0,57} (\text{exp}) \]  

(61)

where

\[ k = \frac{C_{0,57} (\text{exp})}{C_{0,57} (\text{theory})} \]  

(62)

Figure 9 shows the effect of tilt angle by utilizing Eq. (61) with the basic theoretical equations. Figure 9 suggests that tilt angle has a 10-20% effect over the entire range of tilt range or about a 1-2% per tilt angle degrees.

Incident Angle Modification (\( K_{\alpha T} \))

The modification for the variation of the product of absorptance and transmittance (\( \alpha T \)) may be obtained from curves of transmittance and absorptance versus incident angle. To determine the modifying factor (\( K_{\alpha T} \)) one simply uses the following relationship:

\[ K_{\alpha T} = \frac{(\alpha T)_{\theta_1}}{(\alpha T)_{\theta_1 = 0}} = \frac{(\alpha T)_{\theta_1}}{(\alpha T)_{\theta_0}} \]  

(63)

Equation (63) is an incident angle modifier for the simulator results obtained at zero incident angle. Calculated results of this modifier for the black-nickel two-glass and black-paint two-glass collector are shown in Fig. 10. The calculations of Fig. 10 are based on theoretical transmission curves for glass and the reflectivity measurements for a non-selective black paint and a selective black nickel coating.

A correlation for the product of \( \alpha T \) was suggested by Souka and Safrut(12). This correlation has the following general form

\[ \alpha T = a - b/\cos \theta_1 \quad \theta_1 < \pi/2 \]  

(64)

Use of Eq. (64) allows the following expression for the incident angle modifier.

\[ K_{\alpha T} = 1.0 - b/\cos \theta_1 - 1 \]  

(65)

The results of Fig. 10 for the black paint two-glass collector are plotted in the manner of Eq. (65) in Fig. 11. For the range of incident angles of interest in determining collector performance, Fig. 11 demonstrates the validity of Eq. (65). The constant (b0) of Eq. (65) should be a function of the number of collector covers, the absorber surface and the internal physical structure of the collector.

Another way to determine the incident angle modifying factor is to use the Lewis simulator facility, since this facility permits a determination of collector performance at different incident angles. The approach is to determine collector performance at an inlet temperature (Tf) equal to the ambient temperature (Ta). According to Eq. (4) the effect of this procedure is to relate the collector efficiency to the product of the absorptance and transmittance.

\[ n = F_R \alpha T \]  

(66)

By performing the above procedure at different incident angles and realizing that the flow factor (F_R) is independent of incident angle, one is able to determine the incident angle modifier according to Eq. (63). Examples of the results of this procedure for two selective surfaces are given in Fig. 11. The experimental points in Fig. 11 for the two selectively coated collectors tested appear to follow the calculated line for the black-paint two-glass collector.

Flow Factor Modifier (\( F_R \))

To assess the effect of flow rate on performance, the equation derived by Whillier(5) is applicable.

\[ F_R = F'_1 (G_{CP}) / (F'UL) (1 - a) \]  

(67)

Where the plate efficiency factor for the type of collectors being used as examples in this paper can be represented by

\[ F'_1 = 1 / (1 + b/\eta_f) \]  

(68)

Since the value of \( b \) is essentially equal to one, the plate efficiency factor determined from the simulator results (F') can be corrected for different flow rates and heat loss as follows:

\[ F' = F'_1 \eta / \eta_f \]  

(69)

where

\[ \eta = 1 / \left( \frac{aU}{h_f} \right) + 1 \]

and \( a \) is determined from the simulator values of \( F'_1, U_L \) and \( h_f \). The collectors of this paper have a value of the plate efficiency factor of 0.97 for the conditions stated in Figs. 2 and 3(2). For these collectors Eq. (69) would be

\[ F' = 0.97 \eta / \eta_f \]  

(70)

Use of Eq. (67) allows a calculation of the flow factor as follows:
The collector tilt angle is 65.0° and the flow rate the same as employed in the tests with the simulator facility (10 lb/hr ft^2). Using the methods described above a determination is made of the heat loss modifier (KUL), incident angle modifier (KαT, fig. 10), diffuse energy modifier (KDF) and the direct energy modifier (KDR). Table V lists these modifiers and the required collector performance constants obtained from the simulator tests. The value of KT for the use in Eq. (72) can be determined from the following equation derived in Appendix A

\[
\alpha T = \alpha T_0 = 0.914 T_a \text{ (Absolute temp.)} \quad (74)
\]

Table V shows that the results for heating (T_1 = 120°F) for the day chosen give n-2 day efficiencies of 39.7% and 32.5% for the black-nickel two-glass and black-paint two-glass collectors, respectively. The heat loss modifier for the black-nickel collector was significantly larger than for the black-paint collector. One possible reason for this difference is the lower glass temperatures for the black-nickel collector due to a smaller radiation component. A lower glass temperature will increase convection losses. This effect can better be seen in Figs. 6 and 7 where a condition of low-plate temperature or low-plate emissivity (black-nickel collector) gives a higher differential of the heat loss coefficient between the calculated value and the simulator test value. When the radiation component becomes significant (high T_p) the effect of ambient temperature and sky temperature on the heat loss modifier becomes smaller.

One factor which the performance calculations do not at present consider is the effect of aging and the effect of dust, etc., on collector performance. It should be possible to experimentally determine modifiers that will correct for such an effect. These experimentally determined modifiers can be incorporated into Eq. (72).

**CONCLUSION**

A method is presented for the modification of solar simulator results for conditions encountered outdoors. The modified performance equation is:

\[
n = K_{FR} [K_{αT} K_{DR} a + K_{DF} \alpha T - K_{UL} b_0 \theta + C_0 0] \quad (73)
\]

with

\[
\theta = (T_1 - T_a)/q_T
\]

Equation (73) is the collector efficiency equation which can be utilized for outdoor performance prediction. A sample calculation is made to demonstrate the use of Eq. (73).

**Sample Calculation**

Basic solar and weather information (q_l, T_a, wind, q_{DF}, q_{DR}, q_T) is the input needed to modify the simulator data for outdoor conditions.

For the purpose of a sample calculation the Blue Hill, Mass. solar data of Dec. 20, 1955, is used. It is assumed that the wind speed was the same as in the simulator facility (7 mi/hr). The effective sky temperature for radiation is calculated with the following equation of Ward (11).
APPENDIX A

Determination Of Product Of Absorptivity And Transmittance For Diffuse Radiation ($\alpha T$)

The product of absorptivity and transmittance for diffuse radiation can be shown to be expressed as follows:

$$\alpha T = 2 \int_0^{\pi/2} \alpha \sin \theta_1 d\theta_1$$  
(A-1)

From Eq. (65) the following is obtained

$$\alpha T = (\alpha T)_{\theta_1=0} \left[ 1 - b_0 \left( \frac{1}{\cos \theta_1} - 1.0 \right) \right]$$  
(A-2)

Combining Eqs. (A-1) and (A-2) and integrating results in

$$\alpha T = (\alpha T)_{\theta_1=0} \left[ 1 - b_0 \right]$$  
(A-3)

Comparing Eq. (A-3) with Eq. (65) results in the following identity

$$\frac{\alpha T}{\alpha T_{\theta_1=0}} = \frac{K_{\theta_1=0}}{K_{\theta_1=60^\circ}}$$  
(A-4)

Therefore the product of absorptivity and transmittance for diffuse radiation ($\alpha T$) may be determined as follows:

$$\alpha T = (\alpha T)_{\theta_1=0} \left( \frac{K_{\theta_1=60^\circ}}{K_{\theta_1=0}} \right)$$  
(A-5)

**SYMBOLS**

- $A_c$: collector area, $\text{ft}^2$
- $A_p$: area associated with collector perimeter, $\text{ft}^2$
- $C$: constant
- $C_p$: heat capacity, $\text{BTu/lbm \ OP}$
- $F_R$: collector flow efficiency factor, dimensionless
- $F'_R$: collector plate efficiency factor, dimensionless
- $g$: acceleration due to gravity, 32.17 $\text{ft/sec}^2$
- $G_{R_L}$: glass number based on $L_1$, dimensionless
- $G$: flow per unit of absorber area $\text{lb/hr ft}^2$
- $h_o$: wind coefficient $\text{BTu/hr ft}^2 \text{ OP}$
- $h_f$: heat transfer coefficient $\text{BTu/hr ft}^2 \text{ OP}$
- $k$: thermal conductivity $\text{BTu/hr ft} \text{ OP}$
- $L$: distance between cover plates, $\text{ft}$
- $m,n$: exponents, dimensionless
- $N_R$: Nusselt number based on $L_1$, dimensionless
- $P_R$: Prandtl number, dimensionless
- $q$: energy flux, $\text{BTu/hr ft}^2$
- $q_L$: energy loss, $\text{BTu/hr ft}^2$
- $R_{R_L}$: Rayleigh number based on $L_1$, dimensionless
- $T$: temperature $\text{OP}$
- $T_0$: outlet temperature $\text{OP}$
- $T_1$: inlet temperature $\text{OP}$
- $U_L$: overall heat loss coefficient, $\text{BTu/hr ft} \text{ OP}$
- $\alpha$: coating absorptivity, dimensionless
- $\alpha T$: absorptivity transmittance product for diffuse radiation
- $\delta$: insulation thickness, $\text{in}$.
- $c$: emissivity of coating
- $\eta$: collector efficiency, dimensionless
- $\theta_1$: incident angle of radiation
- $\theta_T$: collector tilt angle
- $\sigma$: Stefan-Boltzmann constant, $\text{BTu/hr ft}^2 \text{ OP}^4$
- $\tau$: transmittance

**Subscripts**

- $a$: ambient
- $c$: cover
- $DF$: diffuse in the plane of the collector
- $DR$: direct in the plane of the collector
- $e$: edge
- $f$: fluid
- $G_1$: inner glass
- $G_2$: outer glass
- $L$: based on thickness of gas layer
- $I$: insulation
- $P$: plate
- $R$: rear
- $s$: simulator
- $T$: total
- $u$: useful

**Superscripts**

- $\overline{\text{average}}$

**REFERENCES**


Table I NASA Lewis solar simulator summary

Radiation source, 163 lamps, 300 W each
GE-type ELH, tungsten-halogen dichroic coating
12° Total divergence angle

Test area, 4 by 4 ft, maximum

Test condition limits,
Flux: 150 to 350 Btu/hr-ft²
Flow: up to 1 gal/min (30 lb/hr-ft²)
Inlet temp: 75°F to 210°F
Wind: 0 to 10 mph at 75°F

Table II Comparison of solar simulator and air-mass 2 performance

<table>
<thead>
<tr>
<th>Energy output percent</th>
<th>Air mass 2 sunlight</th>
<th>Simulator</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ultraviolet</td>
<td>2.7</td>
<td>0.3</td>
</tr>
<tr>
<td>Visible</td>
<td>44.4</td>
<td>48.4</td>
</tr>
<tr>
<td>Infrared</td>
<td>52.9</td>
<td>51.3</td>
</tr>
<tr>
<td>Absorptivity (selective surface)</td>
<td>0.90</td>
<td>0.90</td>
</tr>
<tr>
<td>Glass transmission</td>
<td>0.85</td>
<td>0.86</td>
</tr>
<tr>
<td>Al mirror reflectivity</td>
<td>0.86</td>
<td>0.88</td>
</tr>
<tr>
<td>Solar cell efficiency, percent</td>
<td>12.6</td>
<td>13.4</td>
</tr>
</tbody>
</table>

Table III Collector absorptivity

<table>
<thead>
<tr>
<th>Collector</th>
<th>( a_{\text{meas}} )</th>
<th>( a_{\text{cal}} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Black nickel collector</td>
<td>0.95</td>
<td>0.92</td>
</tr>
<tr>
<td>Black paint collector</td>
<td>0.95</td>
<td>0.93</td>
</tr>
</tbody>
</table>

\( a_{\text{cal}} \) calculated using experimental value of \( a_{\text{meas}} \).

Table IV Natural convection heat loss coefficients for 1 1/4 inch gap and 57° tilt angle

<table>
<thead>
<tr>
<th>Approach</th>
<th>( T_p = 100°F )</th>
<th>( T_p = 200°F )</th>
<th>( n )</th>
</tr>
</thead>
<tbody>
<tr>
<td>DeGraaf and Van Der Held</td>
<td>0.12</td>
<td>0.10</td>
<td>1.17</td>
</tr>
<tr>
<td>Housing and home finance</td>
<td>0.13</td>
<td>0.12</td>
<td>1.31</td>
</tr>
<tr>
<td>Dropkin and Somerscales</td>
<td>0.093</td>
<td>0.085</td>
<td>1.33</td>
</tr>
<tr>
<td>Whillier</td>
<td>0.18</td>
<td>0.18</td>
<td>1.25</td>
</tr>
</tbody>
</table>
### Table V All day performance calculations

Given: $\theta_T = 65^\circ$; $T_0 = -32^\circ$; $T_1 = 120^\circ$ [F]

<table>
<thead>
<tr>
<th>Time</th>
<th>$\theta_1$</th>
<th>$T_{oF}$</th>
<th>$a_T$</th>
<th>$K_D$</th>
<th>$q_T$</th>
<th>$\eta$</th>
<th>$q_U$</th>
</tr>
</thead>
<tbody>
<tr>
<td>7-8</td>
<td>57.4</td>
<td>8</td>
<td>0</td>
<td>1.0</td>
<td>2.4</td>
<td>------</td>
<td>------</td>
</tr>
<tr>
<td>8-9</td>
<td>43.9</td>
<td>7</td>
<td>0.92</td>
<td>0.08</td>
<td>106.6</td>
<td>------</td>
<td>------</td>
</tr>
<tr>
<td>9-10</td>
<td>30.3</td>
<td>6</td>
<td>0.94</td>
<td>0.06</td>
<td>222.5</td>
<td>78.7</td>
<td>------</td>
</tr>
<tr>
<td>10-11</td>
<td>16.5</td>
<td>7</td>
<td>0.94</td>
<td>0.06</td>
<td>290.8</td>
<td>132.1</td>
<td>------</td>
</tr>
<tr>
<td>11-12</td>
<td>2.8</td>
<td>9</td>
<td>1.0</td>
<td>0.05</td>
<td>323.9</td>
<td>159.5</td>
<td>------</td>
</tr>
<tr>
<td>12-1</td>
<td>11.1</td>
<td>9</td>
<td>0.94</td>
<td>0.06</td>
<td>323.8</td>
<td>158.2</td>
<td>------</td>
</tr>
<tr>
<td>1-2</td>
<td>24.8</td>
<td>10</td>
<td>0.97</td>
<td>0.05</td>
<td>302.6</td>
<td>140.5</td>
<td>------</td>
</tr>
<tr>
<td>2-3</td>
<td>52.1</td>
<td>9</td>
<td>0.93</td>
<td>0.07</td>
<td>231.5</td>
<td>84.2</td>
<td>------</td>
</tr>
<tr>
<td>3-4</td>
<td>52.8</td>
<td>9</td>
<td>0.93</td>
<td>0.07</td>
<td>152.1</td>
<td>21.7</td>
<td>------</td>
</tr>
<tr>
<td>Totals</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>1956.2</td>
<td>775.0</td>
<td>------</td>
</tr>
</tbody>
</table>

Black 2 glass: $a_0 = 0.728$; $b_0 = 0.705$; $\theta_T = 0.251$; $\alpha_T = 0.57$; $K_{UL} = 1.03$

<table>
<thead>
<tr>
<th>Time</th>
<th>$\theta_1$</th>
<th>$T_{oF}$</th>
<th>$a_T$</th>
<th>$K_D$</th>
<th>$q_T$</th>
<th>$\eta$</th>
<th>$q_U$</th>
</tr>
</thead>
<tbody>
<tr>
<td>7-8</td>
<td>57.4</td>
<td>8</td>
<td>0.95</td>
<td>1.0</td>
<td>2.4</td>
<td>------</td>
<td>------</td>
</tr>
<tr>
<td>8-9</td>
<td>43.9</td>
<td>7</td>
<td>0.92</td>
<td>0.08</td>
<td>106.6</td>
<td>------</td>
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</tr>
<tr>
<td>9-10</td>
<td>30.3</td>
<td>6</td>
<td>0.94</td>
<td>0.06</td>
<td>222.5</td>
<td>78.7</td>
<td>------</td>
</tr>
<tr>
<td>10-11</td>
<td>16.5</td>
<td>7</td>
<td>0.94</td>
<td>0.06</td>
<td>290.8</td>
<td>132.1</td>
<td>------</td>
</tr>
<tr>
<td>11-12</td>
<td>2.8</td>
<td>9</td>
<td>1.0</td>
<td>0.05</td>
<td>323.9</td>
<td>159.5</td>
<td>------</td>
</tr>
<tr>
<td>12-1</td>
<td>11.1</td>
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<td>0.94</td>
<td>0.06</td>
<td>323.8</td>
<td>158.2</td>
<td>------</td>
</tr>
<tr>
<td>1-2</td>
<td>24.8</td>
<td>10</td>
<td>0.97</td>
<td>0.05</td>
<td>302.6</td>
<td>140.5</td>
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<tr>
<td>2-3</td>
<td>52.1</td>
<td>9</td>
<td>0.93</td>
<td>0.07</td>
<td>231.5</td>
<td>84.2</td>
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<td>3-4</td>
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<td>0.93</td>
<td>0.07</td>
<td>152.1</td>
<td>21.7</td>
<td>------</td>
</tr>
<tr>
<td>Totals</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>1956.2</td>
<td>635.0</td>
<td>------</td>
</tr>
</tbody>
</table>

Black 2 glass: $a_0 = 0.713$; $b_0 = 0.504$; $\theta_T = 0.140$; $\alpha_T = 0.59$; $K_{UL} = 1.12$
Figure 1. - Indoor test facility.

Figure 2. - Collector performance correlation.

\[ \eta = \alpha - \frac{U(\theta_p - \theta_a)}{q_{DR}} \]

\[ \Phi = \frac{\theta_p - \theta_a}{q_{DR}} \left( \frac{\text{BTU}}{\text{HR FT}^2 \text{F}^{-1}} \right)^{-1} \]

(A) HONEYWELL/ERCO BL N1 2 GLASS.

ORIGINAL PAGE IS OF POOR QUALITY
Figure 2. - Continued.

(B) HONEYWELL/LeRC BLACK NI 2 GLASS.

\[ \eta = F \left[ \alpha \left( U_L \frac{(T_f - T_a)}{q_{DR}} \right) \right] \]

\[ \eta = F \left[ \alpha \left( U L \frac{(T_f - T_a)}{q_{DR}} \right) \right] \]

(C) HONEYWELL/LeRC BL NI 2 GLASS.

\[ \eta = F_R \left[ \alpha_T - \frac{U (T_f - T_a)}{q_{DR}} \right] \]

\[ \eta = F_R \left[ \alpha_T - \frac{U (T_f - T_a)}{q_{DR}} \right] \]
Figure 1 - Collector performance correlation.
Figure 4. - Outdoor vs. indoor (simulator) collector tests.

Figure 5. - Comparison of simulator results with analysis.
Figure 6 - Effect of ambient temperature on heat loss coefficient.

Figure 7 - Effect of sky temperature on heat loss coefficient.
Figure 8. - Effect of wind on heat loss coefficient.

Figure 9. - Effect of tilt angle on heat loss coefficient, $T_p = 160^\circ F$. 
Figure 10. - Calculated incident angle modifier.

Figure 11. - Correlation of incident angle modifier.