The GRAN Experiment is designed to prove a world-wide search and rescue (SAR) system utilizing Omega navigation system signals and geo-synchronous satellites. In order to develop a SAR system, the original NASA Omega Position Locating Equipment (OPLE) experiments have been expanded by the Naval Air Test Center, Patuxent River. Specifically, a fourth frequency (10.880 KHz) has been added experimentally to two Omega transmitters. This will increase line of position (LOP) ambiguities from 72 nautical miles to 360 nmi apart. Algorithms have been developed to resolve the 360 nmi ambiguities. During September and October 1974, two series of tests were conducted with Lincoln Experimental Satellite 6 (LES-6) to demonstrate the position locating potential of the four-frequency Omega concept. This paper presents the experiment design, results, and conclusions as they apply to the GRAN system.

INTRODUCTION

The Global Rescue Alarm Net (GRAN) was conceived as a worldwide search and rescue (SAR) system designed to provide real time distress alerting, identification and position location. The Omega Navigation System, presently under construction, will provide the information from which the distress site will be computed. The GRAN concept basically consists of portable battery powered search and rescue communicators (SARCOMs), appropriate frequency translators aboard earth synchronous satellites (SARSATS), and a network of three or more ground receiving stations (SARCENs) (figure 1). The GRAN concept has been under development for five years. It evolved as an application of the OMEGA Position Location Experiment (OPLE) performed in 1967 by the NASA Goddard Space Flight Center. In this experiment, raw OMEGA navigation signals were received at a remote test site, upconverted in frequency to VHF, and retransmitted to a synchronous satellite (ATS-1 and 3) for relay to a ground processing center where a geographic position was computed. This experiment demonstrated that OMEGA data could be relayed without distortion. (reference 1).

In 1969, the U. S. Naval Air Test Center at Patuxent River, Maryland, performed an OPLE test using a low power (less than 5W EIRP) UHF uplink. This series of experiments demonstrated
the feasibility of low power SARCOMs for retransmission of raw OMEGA data to earth-synchronous satellites (reference 8).

The OPLE experiments required a foreknowledge of the retransmission site to within 72 miles which is the ambiguous "lane" structure of the basic three frequency OMEGA system. For the GRAN application to search and rescue such foreknowledge cannot be assumed. Thus, it became necessary to devise a method for obtaining unambiguous position location from Omega in the absence of any foreknowledge of position.

Originally, OMEGA was proposed as a five frequency system with ambiguities arising approximately every 3600 miles. However, the U. S. Navy found little demand for the five frequency format. Instead, maritime users seemed willing to accept a three frequency system with its 72 mile ambiguities. This appeared to pose no special problems for ships which could "initialize" their Omega receivers at known geographic positions upon embarkation, and keep count of lanes as they slowly traversed the seas to their destinations. The U. S. Navy was satisfied to construct the less costly three frequency Omega system with its concomitant savings in individual receiver-processor units for shipboard use.

It is probable that that decision underestimated the potential user population for OMEGA, particularly air traffic. As of this writing at least one U. S. carrier is testing Omega receivers as a potential replacement for some on board inertial platforms which have demonstrated very high cost of acquisition and maintenance. For instance, many Boeing 747 passenger jets carry three inertial platforms. These remarks are offered to justify the GRAN efforts to expand the present three frequency Omega system to a four frequency system. These efforts are well within the scope of the original Omega concept, and the applications for an expanded Omega satisfy an unforeseen demand for a worldwide, reliable, inexpensive area navigation system.

The GRAN concept utilizes a four frequency OMEGA format with an additional signal at 10.880 KHz. The additional frequency was selected by Dr. J. A. Pierce of Harvard University, and has been added to two Omega transmitters for test purposes. The addition of the fourth frequency increases the lane width from 72 nmi to approximately 360 nmi, and permits use of the maximum likelihood estimator technique for resolution of position within the larger lane.

The location of the SARCOM in distress is accomplished in three steps:

1. Reception from one of three geo-synchronous satellites determines which 1/3 of the earth's surface contains the distress site.
2. A coarse lane estimate is then determined by one of two methods:

a. Signal-to-signal comparison of the relayed Omega can be used to reduce the area of interest to approximately 1000-2000 nmi.

b. Difference in time of arrival (TOA) of the Omega pulse envelope to determine a 360 nmi lane.

3. A maximum likelihood estimator, or walkup algorithm, refines this estimate to a correct 8 nmi lane and then further to a 1-2 nmi area.

The signal-to-signal comparison is based on the fact that the amplitude of very low frequency (VLF) signals decrease in strength approximately inversely with distance from the transmitter. A comparison of signals from Omega receivers potentially could be used as a coarse ranging function. Preliminary computations indicated an accuracy of ± 500 nmi at the baseline (between two Omega stations) and ± 750 nmi at the farthest location away from the baseline. Initial experiments to prove this concept were conducted by the Naval Air Test Center and Texas Instruments, Dallas, Texas, and are reported in reference (2). These experiments indicate that when the Omega transmitters are at full power (10 KW at 10.2 KHz) the signal-to-signal ratios may provide a coarse ranging function, but this function will not satisfy the GRAN requirements for a ± 180 nmi estimate to the increased lane width from the additional Omega frequency. The method of time of arrival (TOA) is more applicable to the GRAN needs than the signal-to-signal comparison.

The solution to determine the TOA of the pulse envelope can be approached in a number of ways. One approach that has been considered is outlined in figure 2. Four frequency Omega data from a recent test period has been stored on magnetic tape. This data would be digitally filtered to obtain the four individual Omega frequencies from each station. Reconstruction of the signal would then be accomplished using a third order hold technique. The reconstructed signal would then be sampled in quadrature and a technique developed by Mr. Eric Swanson of the Naval Electronics Laboratory Center (NELC), San Diego, (reference 3) would be used to construct a pulse envelope. The envelope for each frequency would then be cross correlated with a model of pulse rise and pulse decay to establish a relative time of arrival. The resulting pulse time of arrival estimate would then be averaged. The final result would be a TOA estimate with respect to the time reference, recorded on the data tapes, for each Omega station frequency. This approach will work only if amplitude information is available to determine the start of the signal. Since this amplitude
information is not available in our present system configuration, another approach also is being considered.

Instead of detecting pulse TOA via amplitude, a means for frequency detection is being explored. This can be accomplished by:

1. Fast Fourier Transform

   The application of this technique depends on the rise time of the pulse. If the signal is distorted enough in the rise time region by the automatic gain control (AGC) in the ground station, then the frequency may not be detected until the level period of the pulse, thus, diminishing the possible use of a fast fourier transform.

2. Coherent Detector

   This detector provides a translation of the carrier frequency to direct current. It does not destroy phase information nor does it destroy amplitude information. The coherent detection is efficient especially when signal-to-noise ratios are low. It has the disadvantage that pulse rise times may be distorted.

3. Zero-Crossings Detector

   Information contained in the zero-crossings of the waveform can be used to detect the presence of signal in noise. Of particular interest is the distance between the crossings of the waveform along the zero voltage axis. The variations in distance depend on whether signal plus noise is present, or noise alone. One possible form of this detection is a phase filter which is dependent on the frequency of the input signal and not its amplitude.

These are just a few of the possible avenues for solution of TOA estimation. Each is being evaluated to determine its adaptability to the needs of the GRAN system.

The final step in determining position location utilizes the maximum likelihood estimator derived by LCDR C. J. Waylan of the Naval Postgraduate School, Monterey, California (reference 6). His work was supported by the GRAN project and has been incorporated in the GRAN processing technique. This maximum likelihood estimator assumes that the correct major (360 nmi) lane has been identified. The estimation is then performed within this unambiguous lane by fixing the sum of the great circle distances from each of the Omega stations to the center of the lane of interest, and then varying one great circle distance over a range of values necessary to traverse all candidate lines of position (LOP) in the given lane.
This variation would be \( \pm 180 \) nmi on the baseline between the two stations (figure 3). The likelihood function varies with great circle distance (figure 4), and the number of local maxima in the unambiguous lane is determined by the values of the function and the number of Omega frequencies. The cyclic nature of the function shows the necessity for lane ambiguity resolution and yields LOP estimates which fall into three categories:

1. Estimates within 1-2 nmi or less of the correct LOP.

2. Estimates one half wavelength of the four Omega frequencies form the correct LOP (minor lane error).

3. Estimates farther from the correct LOP than the previous two (major lane error).

In the GRAN application at least three stations (two station pairs) would be used to obtain two LOP's. The intersection of these LOPs would yield a better position estimate of the SARCOM than the use of one LOP. The use of four stations (three station pairs) would pinpoint the 1-2 nmi distress area.

Data retransmission tests are presently being conducted at remote sites using LES-6 as the SARSAT link and two experimental four frequency Omega stations (Forestport and Trinidad). The data collected from each of the seven remote sites will be processed using both the maximum likelihood estimator and the walk-up technique developed by Professor Pierce (reference 4). Processing using the walk-up method, is being done at Texas Instruments, Inc., Dallas, Texas. These results will be compared with those of the maximum likelihood estimator as part of the analysis to help determine the adaptability of the estimator in the present configuration. Further analysis of the data will be done to determine the effect of using skywave correction factors in the calculations.

From the detailed analysis of the collected data it will be possible to determine the best position estimate, using the maximum likelihood estimator, based on a foreknowledge of the correct 360 nmi. Also, the best technique for arriving at a TOA estimate of this 360 mile lane in order to fit the GRAN system, will evolve from this collected data. Each of these pieces when added together, will equal a global search and rescue system with a position location ability of 1-2 nmi.
PRESUPPOSED AREA

PATH ON WHICH LIKELIHOOD FUNCTION EXAMINED

SAMPLE LOP

STATION ONE

STATION TWO

GEOMETRY FOR THE ESTIMATION PROBLEM
A TYPICAL LIKELIHOOD FUNCTION
REFERENCES


