THE EFFECT OF WINGLETS
ON THE STATIC AERODYNAMIC
STABILITY CHARACTERISTICS
OF A REPRESENTATIVE
SECOND GENERATION
JET TRANSPORT MODEL

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The winglet configuration showed slight increases over the baseline wing in static longitudinal and lateral aerodynamic stability throughout the test Mach number range for a model design lift coefficient of 0.53. Reynolds number variation had very little effect on stability.
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SUMMARY

This investigation was made to determine the effects of winglets on the static aero-
dynamic stability characteristics of a full-span representative second generation jet
transport model without tails. Two configurations were tested: a baseline wing and a
version of the same wing fitted with winglets. The longitudinal aerodynamic character-
istics were determined through an angle-of-attack range from -1° to 10° at an angle of
sideslip of 0° for Mach numbers of 0.750, 0.800, and 0.825. The lateral aerodynamic
characteristics were determined through the same angle-of-attack range at fixed side-
slip angles of 2.5° and 5°. Both configurations were investigated at Reynolds num-
bers of \(13 \times 10^6\) per meter (\(4 \times 10^6\) per foot) and approximately \(20 \times 10^6\) per meter
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The winglet configuration showed slight increases over the baseline wing in static
longitudinal and lateral aerodynamic stability throughout the Mach number range for a
model design lift coefficient of 0.53. Reynolds number variation had very little effect on
stability.

INTRODUCTION

Winglets, described in reference 1, are intended to provide reductions in drag coef-
ficient for near-cruise conditions substantially greater than those obtained with simple
wing-tip extensions which impose the same bending increments on the wing structure.
The National Aeronautics and Space Administration has been conducting extensive experi-
mental investigations of the effects of winglets for jet transport wings at high subsonic
Mach numbers.

This investigation was conducted to determine the effects of winglets on the lateral-
directional and longitudinal aerodynamic stability characteristics of a full-span transport
model without tails for cruise Mach numbers of 0.750, 0.800, and 0.825. To observe the
sensitivity of the model stability parameters to Reynolds number, tests were conducted at
two different Reynolds numbers: $13 \times 10^6$ per meter ($4 \times 10^6$ per foot) and approximately $20 \times 10^6$ per meter ($6 \times 10^6$ per foot). This stability analysis, presented at a wing-body lift coefficient of 0.53, corresponds to the somewhat lower overall cruise lift coefficient of a typical transport aircraft having a downward-loaded horizontal tail.

The nature of this investigation necessitated a strain-gage balance capable of measuring large forces and moments. Unfortunately, the relatively large axial-force beam of this balance was insufficiently accurate to measure the small increments of drag involved in this investigation. Even if it were possible to measure these drag increments, the test Reynolds numbers of the winglets (approximately $0.4 \times 10^6$ and $0.6 \times 10^6$ based on average chord, for the upper winglet) are so low that the winglets experience disproportionately large skin-friction drag levels. For these reasons, accurate absolute values of drag are unobtainable; therefore, drag data are not given in this report. (Drag data are presented in ref. 2.)

**SYMBOLS**

The results presented in this report are referred to the stability-axis system for the longitudinal aerodynamic characteristics and to the body-axis system for the lateral-directional aerodynamic characteristics. Force and moment data have been reduced to conventional coefficient form based on the geometry of the baseline wing planform. Moments are referenced to the quarter-chord point of the mean aerodynamic chord of the baseline wing (fig. 1). All dimensional values are given in both the International System of Units (SI) (ref. 3) and U.S. Customary Units; however, all measurements and calculations were made in U.S. Customary Units.

Coefficients and symbols used herein are defined as follows:

- $b$  
  wing span, 114.45 cm (45.06 in.)

- $C_L$  
  lift coefficient, \( \frac{\text{Lift}}{qS} \)

- $C_{L\alpha}$  
  lift-curve slope per degree, \( \frac{\partial C_L}{\partial \alpha} \)

- $C_l$  
  rolling-moment coefficient \( (C_l \text{ on computer-drawn figures}) \), \( \frac{\text{Rolling moment}}{qSb} \)

- $C_{l\beta}$  
  rate of change of rolling-moment coefficient with sideslip angle (effective-dihedral parameter) \( \frac{\Delta C_l}{\Delta \beta} \), per degree

- $C_m$  
  pitching-moment coefficient, \( \frac{\text{Pitching moment}}{qSc} \)
\[ C_{m_{CL}} \] longitudinal stability derivative, \( \frac{\partial C_m}{\partial C_L} \)

\[ C_{m,0} \] pitching-moment coefficient at zero lift

\[ C_n \] yawing-moment coefficient, \( \frac{\text{Yawing moment}}{qSb} \)

\[ C_{n\beta} \] rate of change of yawing-moment coefficient with sideslip angle (directional-stability parameter) \( \frac{\Delta C_n}{\Delta \beta} \), per degree

\[ C_Y \] side-force coefficient, \( \frac{\text{Side force}}{qS} \)

\[ C_{Y\beta} \] rate of change of side-force coefficient with sideslip angle (side-force parameter) \( \frac{\Delta C_Y}{\Delta \beta} \), per degree

\( c \) local streamwise chord of wing

\( c^* \) mean aerodynamic chord of baseline reference wing panel, 18.06 cm (7.11 in.)

\( M \) free-stream Mach number

\( q \) free-stream dynamic pressure, N/m\(^2\) (psf)

\( R \) Reynolds number per unit length, per m (per ft)

\( S \) baseline wing planform reference area, 0.1884 m\(^2\) (2.028 ft\(^2\))

\( \alpha \) angle of attack, deg

\( \beta \) angle of sideslip, deg

\( \Delta \) values obtained by interpolation

\( \sigma \) values obtained by linear regression

**APPARATUS AND PROCEDURES**

**Model Description**

A full-span, sting-mounted transport model without tails was used in this investigation (fig. 1). The model has a relatively wide cylindrical fuselage similar to present
second generation jet transports and a conventional low wing with $3^\circ$ of incidence and $6^\circ 40'$ of twist (washout) distributed nonlinearly between the root and tip chords. The wing has an aspect ratio of 6.95, a taper ratio of 0.299, and $35^\circ$ of sweep at the quarter chord. The thickness ratio of the wing varies from 0.124 at the wing-fuselage juncture to 0.09 at midsemispan; this ratio then remains a constant 0.09 out to the tip.

A variation of this baseline configuration was also tested. The outboard 1.91 cm (0.75 in.) of the wing was removed and two winglets were installed on each wing tip. The two winglets, one large inclined upward and one small inclined downward, have trapezoidal planforms with a supercritical airfoil section (fig. 1).

The total winglet area represents 2.75 percent of the total wing area. The trailing edges of the upper winglets and the wing tips were flush mounted with the winglets canted outboard $15^\circ$ from vertical ($75^\circ$ dihedral) and toed-out $2^\circ$ relative to the fuselage center line.

Similarly, the leading edges of the lower winglets and the wing tips were also flush mounted with the winglets canted outboard $40^\circ$ from vertical ($50^\circ$ anhedral) and toed-in $5^\circ$ relative to the fuselage center line.

Test Facility

The investigation was conducted in the Langley 8-foot transonic pressure tunnel, a continuous, single-return tunnel with a slotted, rectangular test section. The longitudinal slots in the floor and ceiling of the test section reduce wall interference effects and allow relatively large models to be tested through the subsonic speed range. Available controls permit independent variation of Mach number, stagnation pressure and temperature, and dewpoint. A more detailed description of the tunnel is found in reference 4.

Test Conditions

Measurements were taken at Mach numbers of 0.750, 0.800, and 0.825 for an angle-of-attack range of $-1^\circ$ to $10^\circ$ and nominal sideslip angles of $0^\circ$, $2.5^\circ$, and $5^\circ$. The Reynolds numbers and dynamic pressures at which the data were taken are presented in table I. Stagnation temperature was maintained at 322 K ($120^\circ$ F) and the air was dried until the dewpoint was sufficiently low to prevent condensation effects.

Boundary-Layer Transition

For all test Mach numbers, boundary-layer transition strips were sized and located by using the techniques discussed in references 5 and 6 to simulate the boundary-layer and shock-induced separation characteristics at a typical full-scale transport Reynolds number of $40 \times 10^6$. 
A boundary-layer transition strip of No. 180 carborundum grains (set in a plastic adhesive) was applied to the fuselage 3.81 cm (1.50 in.) aft of the nose. On the winglets, transition strips of No. 220 carborundum grains were applied 0.25 cm (0.10 in.) from the leading edge of each upper surface and at 40 percent of the streamwise chord on each lower surface. The transition strips on the upper surface of the winglets were located forward in order to eliminate interaction of a shock wave and the laminar flow (based on previous experience with this model). (The transition pattern on the wing is shown in fig. 2. All transition strips were 0.16 cm (0.06 in.) wide.)

The fluorescent-oil film flow visualization technique described in reference 7 was employed to verify the presence of laminar flow ahead of the transition strip.

Measurements

Force and moment data were obtained by use of a six-component electrical strain-gage balance housed within the fuselage cavity. Drag data, for the reasons previously stated, are not presented. Angle of attack was measured by an accelerometer that was also housed within the fuselage. Static pressures were measured in the model along the sting cavity by using differential-pressure transducers referenced to free-stream static pressures.

Corrections

The angle of attack of the model was corrected for flow angularity in the tunnel test section. This correction was obtained from upright and inverted tests of the baseline wing configuration. The lift and pitching-moment coefficients have been adjusted to correspond to the condition of free-stream static pressure in the sting cavity. Blockage and interference effects were negligible; therefore, no corrections to the data have been made for these factors.

PRESENTATION OF RESULTS

The results of this investigation are presented in the following figures:

<table>
<thead>
<tr>
<th>Figure</th>
</tr>
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<tbody>
<tr>
<td>Variation of pitching-moment coefficient and angle of attack with lift coefficient</td>
</tr>
<tr>
<td>Summary of static longitudinal aerodynamic characteristics. ( \beta = 0^\circ )</td>
</tr>
<tr>
<td>Variation of rolling-moment, yawing-moment, and side-force coefficients with lift coefficient</td>
</tr>
<tr>
<td>Summary of static lateral aerodynamic characteristics at ( C_L = 0.53 )</td>
</tr>
</tbody>
</table>
DISCUSSION

Longitudinal Aerodynamic Characteristics

The static longitudinal aerodynamic characteristics of the model with and without winglets are presented in figure 3 and summarized in figure 4 for the two test Reynolds numbers.

Although the actual variation of absolute values of $C_m$ at all test conditions (fig. 3) is nearly negligible, the winglets do provide small increases in longitudinal stability (fig. 4). These increases are shown by more negative $C_{ml}$ values. (Note that the $C_{ml}$ values become increasingly negative with Mach number and that the difference between the curves for winglets on and off remains fairly constant over the test Mach number range.) This increased stability trend is offset somewhat by an increasing zero-lift pitching-moment coefficient. A very slight positive effect on the longitudinal stability characteristics due to increased Reynolds number is shown.

Lateral Aerodynamic Characteristics

A summary of the static lateral-directional aerodynamic characteristics of the model is presented in figure 6. Although the absolute values of these stability parameters are small (as in the longitudinal case), the winglets do have a slight positive effect on each of the lateral-directional stability parameter levels. Although the actual winglet Reynolds numbers are small, a slight positive effect is again shown on the stability parameters at the higher test Reynolds numbers.

CONCLUDING REMARKS

An investigation was made at Mach numbers of 0.750, 0.800, and 0.825 of the static longitudinal and lateral aerodynamic characteristics of a tailless full-span representative transport model with and without winglets.

Winglets were initially proposed to be retrofitted to existing aircraft to reduce induced drag. The results of this investigation showed that no adverse stability penalties could be attributed to the addition of winglets; in fact, the winglets actually showed small positive increases in both lateral and longitudinal stability over the baseline configuration.

Although the winglet Reynolds numbers were quite low, there was a very slight positive effect on the stability parameters at the higher test Reynolds number. Experience suggests that the stability benefits exhibited by winglets will continue to increase with further increases in Reynolds number.
Increases in the directional stability of an aircraft utilizing winglets presented the possibility of reducing the vertical tail surface, with a resulting decrease in drag.

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REFERENCES


TABLE I. - SUMMARY OF TEST CONDITIONS

<table>
<thead>
<tr>
<th></th>
<th>M</th>
<th>R per m</th>
<th>R per ft</th>
<th>q kN/m²</th>
<th>q psf</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.750</td>
<td>13.12 x 10⁶</td>
<td>4.00 x 10⁶</td>
<td>30.14</td>
<td>629.55</td>
<td></td>
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<tr>
<td></td>
<td>19.91 x 10⁶</td>
<td>6.07 x 10⁶</td>
<td>45.82</td>
<td>957.07</td>
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</tr>
<tr>
<td>0.800</td>
<td>13.12 x 10⁶</td>
<td>4.00 x 10⁶</td>
<td>31.58</td>
<td>659.51</td>
<td></td>
</tr>
<tr>
<td></td>
<td>20.57 x 10⁶</td>
<td>6.27 x 10⁶</td>
<td>49.96</td>
<td>1043.34</td>
<td></td>
</tr>
<tr>
<td>0.825</td>
<td>13.12 x 10⁶</td>
<td>4.00 x 10⁶</td>
<td>32.28</td>
<td>674.22</td>
<td></td>
</tr>
<tr>
<td></td>
<td>21.00 x 10⁶</td>
<td>6.40 x 10⁶</td>
<td>51.81</td>
<td>1082.04</td>
<td></td>
</tr>
</tbody>
</table>
Figure 1.- General arrangement of model. Dimensions are in cm (in.).
Figure 1.- Concluded.
Figure 2. - Location of wing transition strips. Dimensions are in cm (in.).
Figure 3.- Variation of pitching-moment coefficient and angle of attack with lift coefficient.

(a) $M = 0.750; \quad \beta = 0^\circ$. 
Figure 3.- Continued.

(b) $M = 0.800; \quad \beta = 0^0$. 

Figure 3.- Continued.
(c) $M = 0.825; \ \beta = 0^\circ$.

Figure 3. - Continued.
(d) $M = 0.750; \, \beta = 2.5^\circ$.

Figure 3.- Continued.
Figure 3. Continued. 

(e) \( M = 0.800; \ \beta = 2.5^\circ \).

Figure 3. - Continued.
(f) $M = 0.825; \quad \beta = 2.5^\circ$.

Figure 3. - Continued.
Figure 3.- Continued.

(g) $M = 0.750; \beta = 5^0$. 

Figure 3.- Continued.
(h) $M = 0.800; \ \beta = 5^\circ$.

Figure 3.- Continued.
Figure 3.- Concluded.

(i) $M = 0.825; \ \beta = 5^\circ$. 

Winglets | $R/\text{m}$ | $R/\text{ft}$
---|---|---
Off | $13.1 \times 10^6$ | $4.00 \times 10^6$
On | 13.1 | 4.00
Off | 21.0 | 6.40
On | 21.0 | 6.40
Figure 4.- Summary of static longitudinal aerodynamic characteristics.

(a) $R \approx 13 \times 10^6$ per meter ($4 \times 10^6$ per foot).

$\beta = 0^\circ$. 
Figure 4. - Concluded.

(b) $R \approx 20 \times 10^6$ per meter ($6 \times 10^6$ per foot).
Figure 5.- Variation of rolling-moment, yawing-moment, and side-force coefficients with lift coefficient.

(a) $M = 0.750; \; R \approx 13 \times 10^6$ per meter $(4 \times 10^6$ per foot).
(b) $M = 0.80; \ R \approx 13 \times 10^6$ per meter $(4 \times 10^6$ per foot).

Figure 5.- Continued.
(c) \( M = 0.825; \) \( R \approx 13 \times 10^6 \) per meter \( (4 \times 10^6 \) per foot).  

Figure 5.- Continued.
Figure 5. Continued.

\[ C_L \]
\[ C_n \]
\[ C_Y \]

(d) \( M = 0.750; \; R \approx 20 \times 10^6 \) per meter \( (6 \times 10^6 \) per foot).
(e) $M = 0.80; \ R \approx 20 \times 10^6 \text{ per meter} \ (6 \times 10^6 \text{ per foot})$.

Figure 5.- Continued.
(f) \( M = 0.825; \ R \approx 20 \times 10^6 \text{ per meter} \ (6 \times 10^6 \text{ per foot}).

Figure 5.- Concluded.
Figure 6.- Summary of static lateral aerodynamic characteristics. \( C_L = 0.53 \).

(a) \( R \approx 13 \times 10^6 \text{ per meter } (4 \times 10^6 \text{ per foot}) \).
Winglets

- Off
- On

\( C_{\beta} \)

\( C_{n\beta} \)

\( C_{\gamma\beta} \)

\( M \)

(b) \( R \approx 20 \times 10^6 \) per meter \((6 \times 10^6 \) per foot\).

Figure 6.- Concluded.