

AUTOMATIC VEHICLE MONITORING SYSTEMS STUDY Report of Phase 0

Vol. 2. Problem Definition and Derivation of AVM System Selection Techniques

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PREFACE

This document on Automatic Vehicle Monitoring Systems presents the results of work supported by the National Science Foundation. It was sponsored under an interagency agreement with the National Aeronautics and Space Administration through Contract NAS 7-100. Points of view and opinions stated in this document are those of the authors and do not necessarily represent the official position of the sponsoring agency.

FOREWORD

This report was prepared for distribution to public safety planners for the purpose of providing them with a compact source of information regarding improvements in efficiency and cost benefits obtainable with various classes of operational and proposed automatic vehicle monitoring (AVM) systems. An AVM system can contribute to emergency patrol effectiveness by reducing response times and by enhancing officer safety as well as by providing essential administrative control and public relations information. This complete report and the Executive Summary (Vol. 1) were prepared by the Jet Propulsion Laboratory of the California Institute of Technology using the results of studies sponsored by the National Science Foundation.

Special computer programs are described which can simulate and synthesize AVM systems tailored to the needs of small, medium and large urban areas. These analyses can be applied by state and local law enforcement agencies and by emergency vehicle operators to help decide on what degree and type of automation will best suit their individual performance requirements and also the possible reduction in the number of vehicles needed which could substantially reduce operating expenses.

G. R. Hansen

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Lieut Robert Zippel	Anaheim
Capt. Daniel Sullivan, Sgt. Howard Ebersole, Ofc Louis Lozano	Los Angeles
Lieut James Lance	Long Beach
Chief Raymond McLean	Montclair
Lieut Allen Stoen	Monterey Park
Ofc. Luke Villareal	Pasadena
Lieut. Robert L. Walker, Sgt. Robert E. Ristau	San Diego

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Chief David Michel	Anaheim
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Chief William Mooney	Long Beach
Chief Raymond McLean	Montclair
Chief Raymond Warner (dec)	Monterey Park
Chief Robert McGowan	Pasadena
Chief Raymond Hoobler (ret)	San Diego

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ABSTRACT

A set of planning guidelines is presented to help law enforcement agencies and vehicle fleet operators decide which automatic vehicle monitoring (AVM) system could best meet their performance requirements. Improvements in emergency response times and resultant cost benefits obtainable with various operational and planned AVM systems may be synthesized and simulated by means of special computer programs for model city parameters applicable to small, medium and large urban areas. Design characteristics of various AVM systems and the implementation requirements are illustrated and costed for the vehicles, the fixed sites and the base equipments. Vehicle location accuracies for different RF links and polling intervals are analyzed. Actual applications and coverage data are tabulated for seven cities whose police departments actively cooperated in the JPL study. Volume 1 of this Report is the Executive Summary. Volume 2 contains the results of systems analyses.

G. R. Hansen

AUTOMATIC VEHICLE MONITORING SYSTEMS STUDY

EXECUTIVE SUMMARY

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AUTOMATIC VEHICLE MONITORING SYSTEMS

George R. Hansen

I. INTRODUCTION

In this report, the results of the first phase of a three-phase program to aggregate existing information on Automatic Vehicle Monitoring (AVM) Systems are presented in terms of performance, urban characteristics, operating modes, and cost in a way that will assist prospective AVM User Agencies to make valid comparisons and selections from among the many competing AVM techniques and AVM Systems. This phase (Phase 0) of the study was performed by the Jet Propulsion Laboratory (JPL) for the National Science Foundation (NSF). As originally conceived by NSF and JPL, the AVM Systems study program would include the following three phases:

- Phase 0 Problem Definition and Derivation of AVM System Selection Techniques (in this Report)
- Phase I Critical Research and Verification of the Efficacy of AVM System Selection Techniques Through Computerized System Simulation.
- Phase II Proof of Concept Experiment Demonstrating the Efficacy of Selected AVM Systems in Urban Environments.

In brief, the Phase 0 research was concentrated in three areas: (1) Compilation of a broad information base on AVM technology and urban characteristics, (2) adaptation of computerized analytical techniques needed in the AVM System selection process and in cost benefit trade-offs, and (3) application of AVM System selection process by manual iteration to small, medium and large model cities.

Frequent reference is made in this Report to "AVM techniques" and "AVM Systems". The term "AVM technique" is used to denote the technology required to acquire a fix on a vehicle, while "AVM System" is used to denote the integration of all functional elements required to locate and keep track of vehicles in some automated fashion.

II. SUMMARY OF AVM SYSTEMS STUDY RESULTS

A. WORK ACCOMPLISHED IN PHASE 0

A broad range of information concerning automatic vehicle monitoring (AVM) was compiled from the existing literature, including: (1) Various vehicle location sensing techniques, (2) all functional elements of the total AVM system, and (3) various sized cities with representative geography, topology, demography and urbanology. The information obtained from the literature was supplemented by data obtained directly from police department representatives of seven Southern California cities that participated in the User Group Advisory Committee (UGAC).

Several computerized analytical techniques were developed. City models representative of those characteristics that affect AVM selection were developed for use in the general cost benefit solutions. An analytical technique for predicting vehicle polling rates achievable for the various location sensing techniques in a full AVM system configuration was also developed. Algorithms were developed to estimate the accuracies achievable by a large variety of AVM systems using the probabalistic distributions for three independent variables: (1) vehicle speed, (2) inherent accuracies of location sensing techniques, and (3) vehicle polling intervals.

Preliminary analyses were performed to determine first-order cost estimates for AVM Systems as a function of the various vehicle location sensing techniques when used in small, medium and large cities. Preliminary analyses of the accuracies achievable with various AVM systems were also performed. Various AVM system configuration options were developed, and promising options were examined for possible cost benefits to seven UGAC cities.

B. PRELIMINARY CONCLUSIONS

1. AVM Class should indicate effects on urban environment. From the viewpoint of the prospective AVM system user, the traditional classifications of vehicle locating systems (i. e., piloting, deadreckoning, triangulation, trilateration, and proximity) do not necessarily reflect the impact of an AVM installation on the local urban scene. It is believed that the prospective user's needs would be better met if vehicle monitoring classifications were based on system element types and functions as follows:

Class 0	Manual Monitoring. No AVM
Class I	AVM. No modification to the urban environment. (existing RF links)
Class II	AVM. Autonomous signposts throughout urban area
Class III	AVM. Sparsely distributed special RF sites
Class IV	AVM. Monitored signposts throughout urban area

2. AVM cost benefits obtainable by medium and large cities. The preliminary cost analysis indicates that the cost benefit break-even point occurs for a medium sized city with an area of about 100 km^2 (40 mi^2) and with roughly 50 vehicles. In other words, cities larger in size could expect a positive and increasing benefit with size, up to a certain point. Conversely, cities below this medium size probably would not realize any cost benefit. This conclusion was based on 5-year estimates of AVM system costs and savings.

3. No cost benefits derived from monitored signpost systems. None of the Class IV systems produced a cost benefit for the cities studied, generally because the rental rates on telephone lines raise the equipment costs excessively.

4. AVM System accuracies greater than technique accuracies. In general, the 95% total system accuracy can be expected to be significantly greater than the inherent accuracy of the location sensing technique. Usually the system accuracy is no less than three times the inherent technique accuracy.

5. Vehicle polling intervals determine AVM system accuracies. It appears that the polling interval will dominate system accuracy and that the polling interval can only be shortened at the expense of RF resources dedicated to AVM purposes. Because of the present and predicted future demand on RF resources, this is one area that demands optimization.

6. Critical research required for verification of selection technique. The results of the first phase of the AVM study effort should be used with caution and should not be construed as specific recommendations at this point. The second phase of the analytical work should be completed to verify the results of the first phase.

C. PROGRAM RECOMMENDATIONS

1. It is recommended that the second phase (Phase I) of the AVM Systems study proceed.

2. It is further recommended that mission agencies such as the Law Enforcement Assistance Administration (LEAA) and/or the Department of Transportation (DOT) sponsor the Proof of Concept Experiment, or third phase. The tests presently planned jointly by the city of Los Angeles and DOT could effectively serve this purpose. This could be accomplished by closely coordinating the analytical techniques developed in this study with the Los Angeles Police Department, the Southern California Rapid Transit District, LEAA and DOT and making the analytical tools available to the city for use in the design of the experiment.

III. CLASSES OF AVM SYSTEMS

A. CLASSIFICATION RATIONALE

Traditionally, AVM systems have been classified in the literature according to the method used to locate the vehicle within an urban area. Recognizing that all AVM systems have certain elements in common and that some systems have unique elements, an alternate classification scheme was developed for the purpose of this study. This classification not only implies the type of AVM system but also suggests the physical impact that the system elements and functions will have on the local urban environment. The following groupings of system elements suggested the classification scheme:

Functional Elements Common to All AVM Systems

- (1) Existing communications system.
- (2) Vehicle polling subsystem.
- (3) Landline data links.
- (4) Telemetry data/polling handler.
- (5) Telemetry link (common to most).
- (6) In-vehicle equipment, such as data processor, telemetry data encoder, polling processor, and signpost sensor
- (7) Vehicle location computer.
- (8) Information display subsystem.

Functional Elements Unique to Specific AVM Systems

- (9) Autonomous signposts; signpost sensor in vehicle (Class II).
- (10) Fixed synchronized RF transmitter sites (Class III).
- (11) Monitored signposts, vehicle sensor on signpost (Class IV).

A discussion of each of these AVM functional elements follows:

1. Existing communications system. As a practical consideration, AVM systems will probably be integrated with the existing voice communication and vehicle polling RF links, especially for the telemetered location data between the vehicle and the dispatch center.

2. Vehicle polling subsystem. This interrogation device or procedure enables the vehicle location computer (VLC), described in Element 7, to know which vehicle corresponds to which set of location data. Polling may be either an operating procedure or an active element that allows the dispatcher to obtain locations of specific vehicles.

3. Landline data link. This data link is a landline supplying data to the VLC (Element 7). It may either be relatively short, leading from the telemetry data/polling handler (Element 4) to the VLC, or it may be quite extensive, collecting data from monitored signposts throughout the covered urban area, or it may be somewhere in between these in its extent, bringing data from a relatively small number of fixed RF sites.

4. Telemetry data/polling handler. This device is included because AVM systems deal with data that are different (e. g., digital) in character from that used by the dispatcher in voice communication with the vehicles. Furthermore, if the vehicle polling subsystem (Element 2) provides for selective polling, then there are likely to be corresponding additional requirements on the communication system.

5. Telemetry link. Since it is tacitly assumed that the AVM system will not restrict the mobility of the fleet vehicles, some kind of communication-at-a-distance is essential. In some systems, the telemetry link is assumed to share or be in addition to the RF link now used for voice communications. In other systems the telemetry path might be between the vehicles and sparsely distributed synchronized RF sites. In still other AVM systems, the telemetry path may be relatively short, being only from the vehicles to signposts distributed throughout the urban area. In that case, the transmission medium could conceivably be sonic, optical, or even magnetic, instead of radio.

6. In-vehicle equipment. Depending on the AVM system, some or all of the four following devices may be carried in the vehicle.

a. Vehicle data processor. This device receives raw vehicle location data either from the officer or from signpost sensors. It does whatever data processing is done on-board, then adds the vehicle identification data, and passes this information along to the telemetry data encoder, described next.

b. Vehicle telemetry data encoder. This device puts the vehicle location data supplied by the vehicle data processor into the telemetry link (Element 5).

c. Vehicle polling processor. This device enables the vehicle to respond properly when polled, and may range in complexity from a clock to an RF signal decoder.

d. Signpost sensor. Where the densely distributed autonomous signpost concept is used (Class II), the signpost sensor must be carried in the vehicle. This sensor is required to read the signpost ID/location. Location data may be acquired by coded optical, infrared, sonic, or magnetic means besides radio.

7. Vehicle location computer (VLC). This device transforms the vehicle location data into location points or coordinates for use by the information display subsystem (Element 8). It also informs the display subsystem as to the identity of the vehicle to which the location data belongs. The VLC may also interface with the Computer-Aided Dispatch System.

8. Information display subsystem. This device indicates to the dispatcher where the vehicles are currently located (or were when last polled). It may also identify the vehicle's status. As in the case of manual aids used for vehicle location in Class 0, the possible range of complexity and sophistication may range from a simple printer to an elaborate electro-optical device supported by a computer. It should be noted that the display subsystem is virtually independent of the location technique used.

9. Autonomous signposts used in Class II AVM. Each autonomous wayside or buried signpost has a location ID and must be recognizable and readable by the signpost sensor in the vehicle. The signpost telemetry link to the vehicle may be by radio, pulsed light, infrared, sonic, or magnetic means.

10. Fixed synchronized RF transmitter sites used in Class III AVM. These RF sites are a relatively small number of special-purpose transmitters which broadcast synchronized signals that can be used to determine the locations of receivers on vehicles by means of navigation techniques. The characteristics of these signals could be FM phase, pulse, or noise correlation. Some of these sites may also receive retransmitted signals from the monitored vehicles.

11. Monitored signposts used in Class IV AVM. Each monitored wayside or buried signpost requires a vehicle sensor that will transmit the vehicle's ID data received and also identify its own location to the central collection station. These signposts may sense vehicle motion, or they may detect pulsed light, infrared, or ultrasonic signals or receive RF signals through buried antennas.

B. AVM CLASS DESCRIPTIONS

The vehicle location system classes, based on their physical impact on the urban environment, are shown in the following list and are described in greater detail in subsequent paragraphs and accompanying figures. For reference, the traditional vehicle location classifications are noted as indentures.

- (1) Class 0 Manual Monitoring. No AVM
 - (a) Piloting
- (2) Class I AVM. No Modification to Urban Environment (Existing RF Links)
 - (a) Officer Update
 - (b) Dead Reckoning
 - (c) Navigation (Using Existing RF Beacons)
- (3) Class II AVM. Autonomous Signposts Throughout Urban Area

- (4) Class III AVM. Sparsely Distributed Special RF Sites
 - (a) Triangulation
 - (b) Trilateration
- (5) Class IV AVM. Monitored Signposts Throughout Urban Area
 - (a) Vehicle Proximity

1. Class 0 Manual Monitoring; No AVM. This baseline (piloting) class is included in the listing of vehicle location techniques purely for comparative purposes. In Class 0, the location monitoring methods (Figure 1) range from those relying solely on the dispatcher's memory, through manually updated mechanical and visual aids, to keyboard-updated computer displays which keep current each vehicle's location and status based on verbal or digital communications between dispatcher and vehicle.

2. Class I AVM with no modifications to urban environment. All AVM systems require the installation of certain equipment in the command center to accomplish the automation of vehicle monitoring. All AVM systems also require the installation of some device in or on the monitored vehicles. But systems in Class I require nothing further, though they perform utilize RF resources.

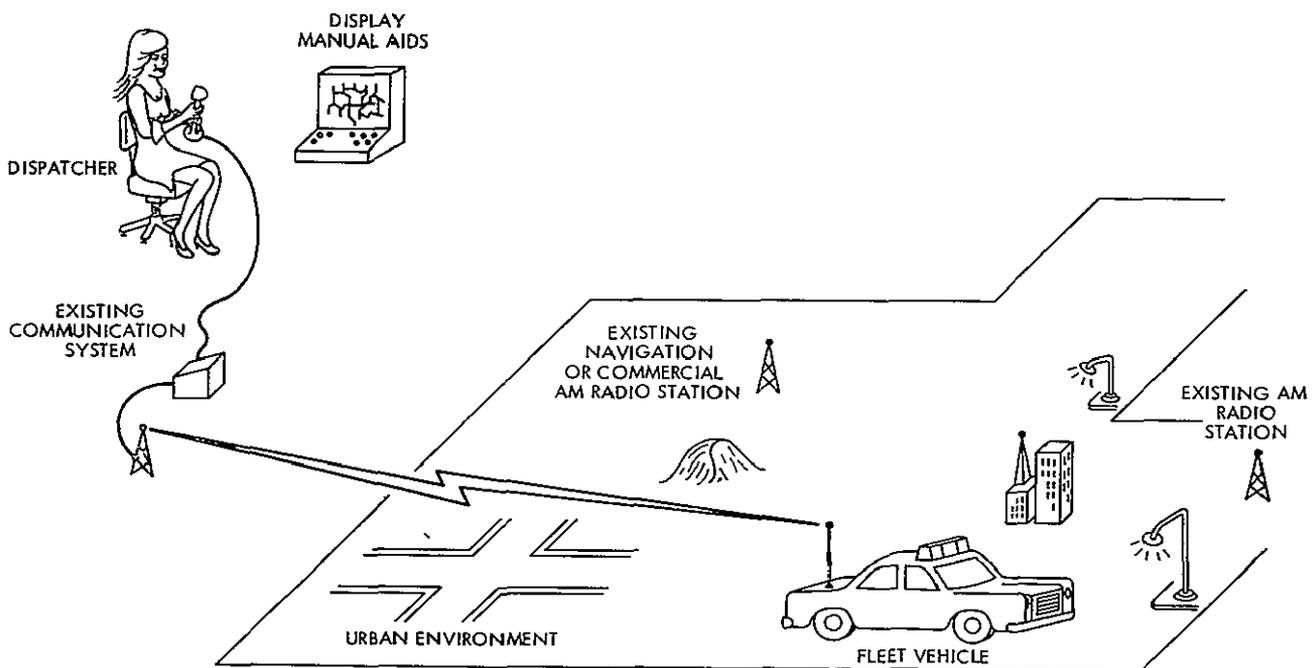


Figure 1. Class 0 Manual Monitoring, No AVM

A typical Class I AVM configuration is shown in Figure 2. Each AVM command center must contain a display subsystem, a vehicle location computer, a vehicle polling subsystem, and a telemetry data/polling handler, which are described in Section IV. Each vehicle requires location sensors, a data processor, a telemetry data encoder, and a polling processor. Class I AVM systems are based upon a variety of location techniques and algorithms which include the following: (a) Officer update techniques, in which the functions of the vehicle's sensors and its data processor are performed by an occupant of the vehicle. (b) Deadreckoning systems are included if the requisite updating does not require the installation of fixed location reference equipment in the environment. (c) If the AVM systems use existing navigation beacons or AM broadcasting stations, they are also included in Class I because the required stations are assumed to be part of the urban environment.

3. Class II AVM with autonomous signposts throughout urban areas.

The defining characteristic of Class II AVM systems is the installation of autonomous signposts in strategic wayside or buried locations at intersections throughout the covered urban area. These location reference sites are autonomous in that they communicate their identity only to the vehicles and not to the command center.

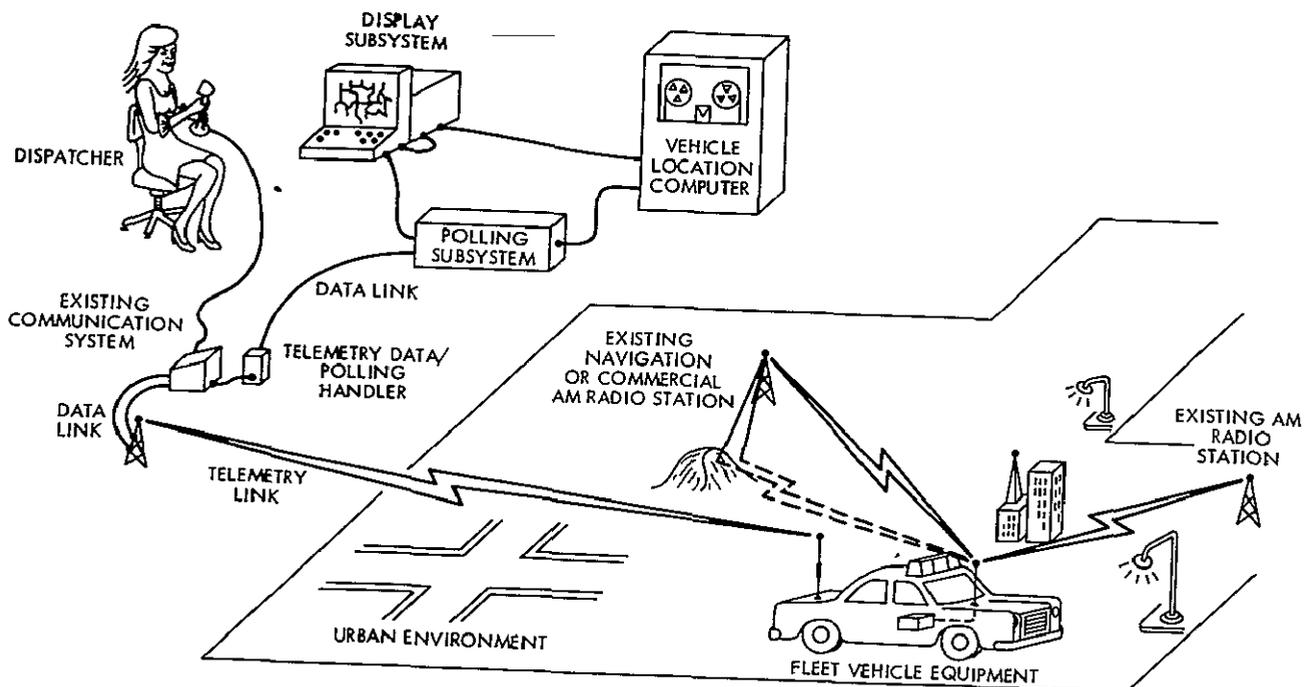


Figure 2. Class I AVM; No Modifications to Urban Physical Environment

The location information provided by the signposts to the vehicle may be either an identification code or the geographic coordinates of the location. Since the vehicle location accuracy provided by systems in Class II is dependent upon signpost spacing, greater accuracy can be achieved in critical areas by locally increasing the signpost density to one per intersection or per lane. A typical Class II system configuration is shown in Figure 3. Signpost systems can be "pure", in that all location information is derived from the fact that a monitored vehicle is (or was) near a signpost; or they can be "hybridized", with the fact of signpost proximity used either to augment, calibrate, or reinitialize the determination of vehicle locations obtained by other means, such as odometers. If a hybrid system does not require a data link in the environment, it is placed in Class II. If the hybrid system requires a data link from the signposts but no special-purpose fixed RF sites, it belongs in Class IV. If it has both a data link in the field and special-purpose fixed sites, it is in Class III.

4. Class III AVM with sparsely distributed special RF sites. This AVM class includes those systems that require the installation of a relatively small number of special purpose fixed RF sites, where a "fixed site" either broadcasts or receives over a relatively large urban area with a radius of 5 to 11 km (3 to 7 miles).

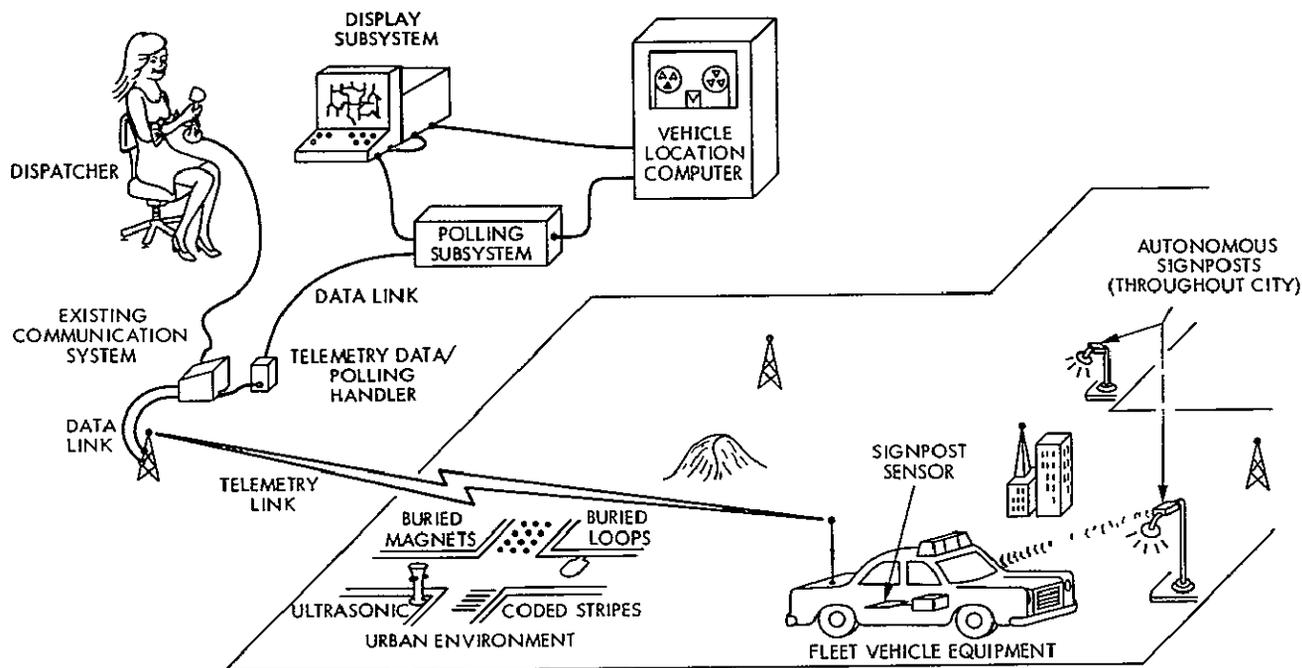


Figure 3. Class II AVM, Autonomous Signposts Throughout Urban Area

Data links in the environment are required to maintain synchronization for triangulation or trilateration purposes. Since the number of fixed sites is relatively small, these data synchronization links could be microwave rather than landline. Figure 4 shows a typical Class III configuration. It is optional only in Class III systems whether the telemetry link from the vehicle be along the existing communication system or through the special-purpose RF sites. In either case, RF resources are utilized for that link.

5. Class IV AVM with monitored signposts throughout urban area.

Systems in this class contain monitored signposts installed in strategic wayside or buried locations throughout the covered urban area for the purpose of sensing the proximity and identity of signals transmitted from vehicles. A Class IV data link does not share the use of RF resources with the existing communication system but uses telephone lines, which may make this class of AVM systems very attractive for some applications. A typical Class IV system configuration is shown in Figure 5.

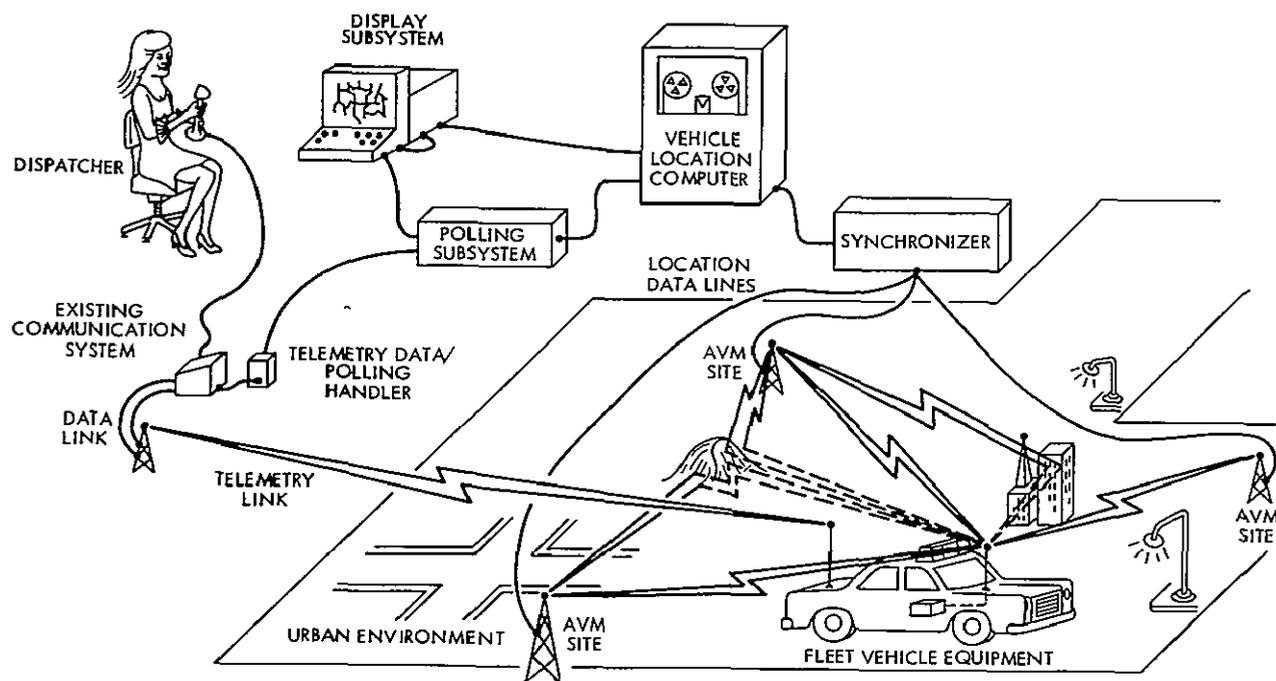


Figure 4. Class III AVM; Sparsely Distributed Special RF Sites

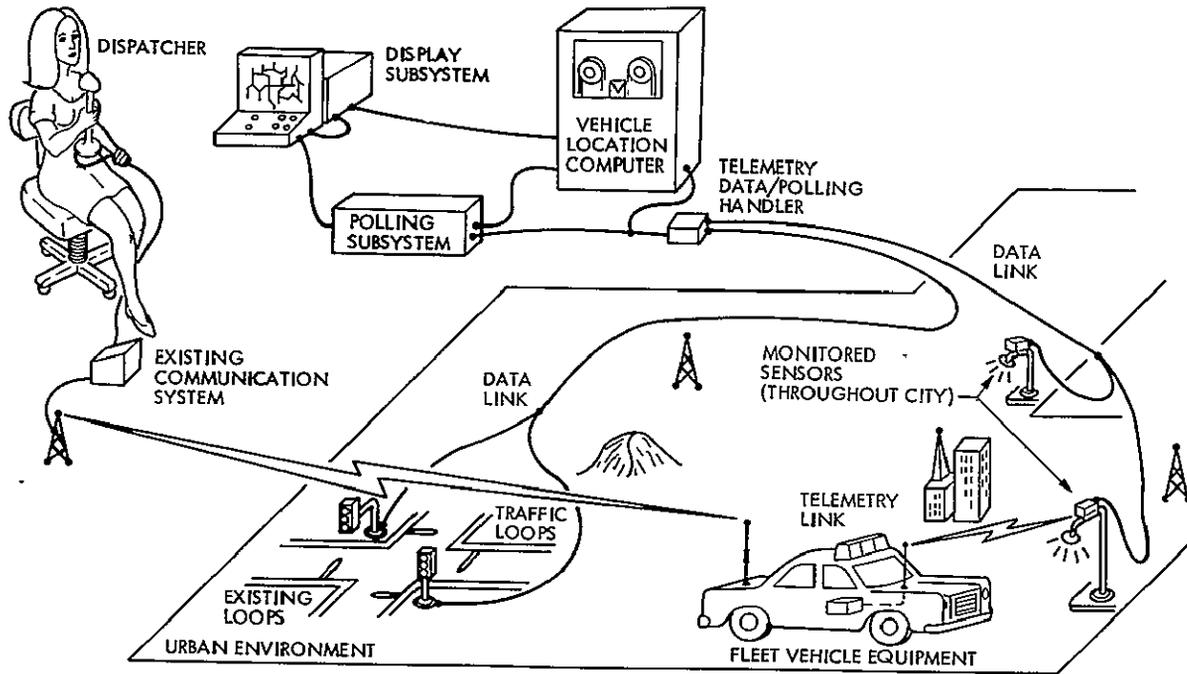


Figure 5. Class IV AVM, Monitored Signposts Throughout Urban Area

IV. VEHICLE LOCATION TECHNOLOGIES AND COSTS

A. PROVED AVM TECHNIQUES

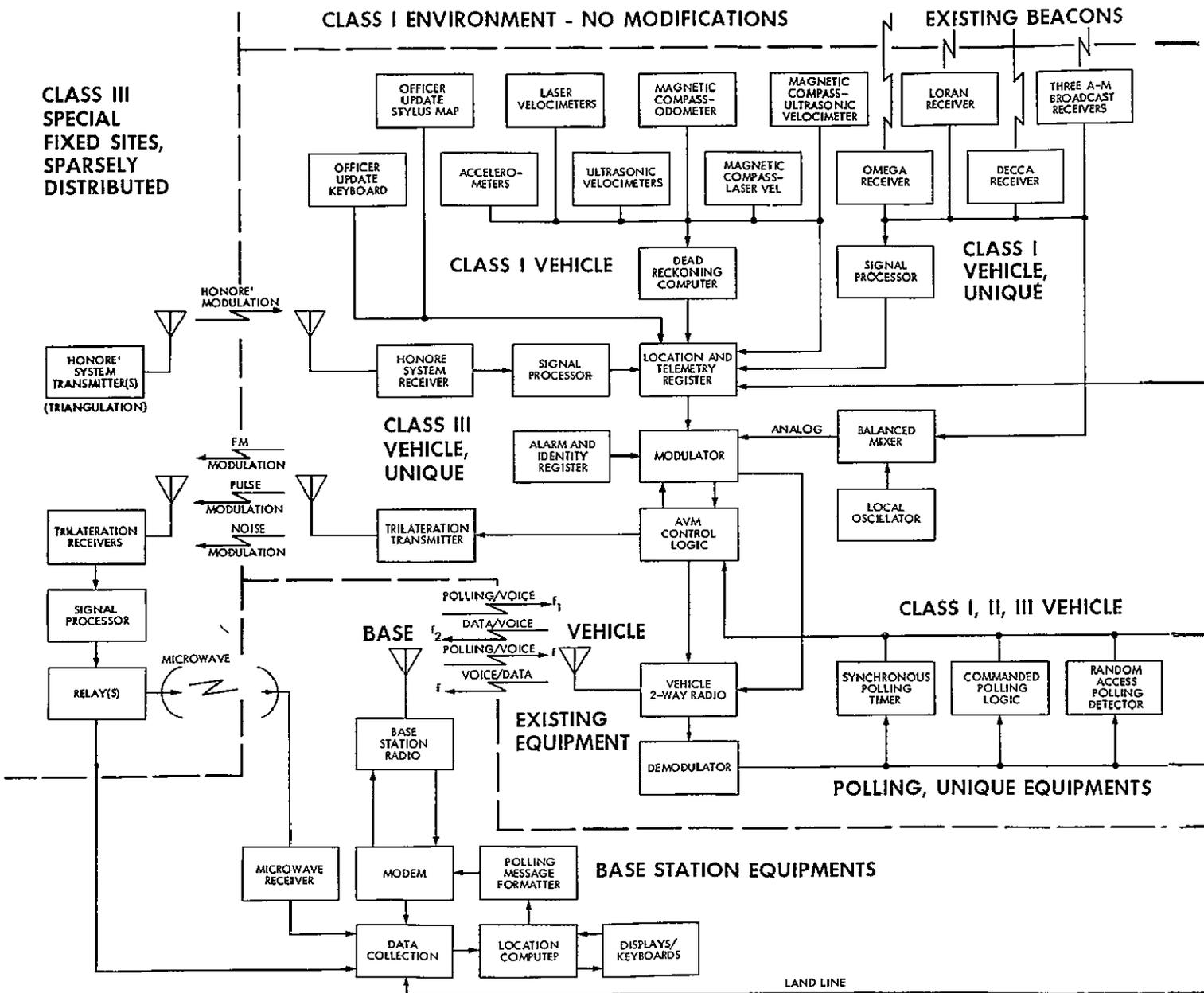
This section contains a narrative description and a compilation of the cost and performance parameters of operational or proved techniques used for automatic vehicle monitoring (AVM). Schemes primarily intended for vehicle identification, such as those used in rail freight or extensions of point-of-sale methods are not included. In this report, the vehicle monitoring techniques are categorized into five broad classes, based on system element types and functions: Class 0, Manual Monitoring, no augmentation of location information; Class I AVM, no additions to the urban environment; Class II AVM, densely distributed autonomous signposts; Class III AVM, sparsely distributed special transmitting/receiving fixed RF sites; and Class IV AVM, densely distributed monitored signposts. In Table 1, the proved vehicle location methods are listed by AVM Class along with estimated costs (as of 1974) for unique system-required equipments installed in each vehicle and at each signpost or special fixed site.

1. Functional diagram correlating various AVM techniques. In order to make equipment and cost comparisons, a functional block diagram combining the elements that make up all of the AVM techniques was generated. This block diagram (Figure 6) demonstrates the equipment and functional commonality among the various techniques. In most techniques, the functional elements can also be physically identical, such as the location/vehicle ID/status register. Variations in costing such elements are due to other factors, such as achievable location precision, fleet size, and amount of status telemetry desired which all affect register length but are technique independent.

Figure 6 illustrates the numerous optional methods available for performing the vehicle location function which make AVM system comparisons difficult. For example, the various Class I techniques can either process the location data on the vehicle or transmit the raw data to the base station. In the Class III techniques, the vehicles may be polled either through the normal 2-way radio or through a special telemetry link used for vehicle location purposes.

Table 1. AVM Classes, Systems and Costs of Functional Elements Installed

AVM Class and System	Element Costs, \$		AVM Class and System	Element Costs, \$	
	Vehicle	Fixed Site		Vehicle	Fixed Site
Class 0. Manual Monitoring No Augmentation of Vehicle Location Information			Class II Autonomous Signposts Throughout Urban Area		
Class I. No Modifications to Urban Environment (Existing RF Links)			(1) Active signposts	—	—
(1) Officer update systems	—	—	(a) Radio beacons	—	—
(a) Keyboard entry	120	0	Low frequency	145	165
(b) Stylus map	2535	0	Citizen band, VHF	145	145
(2) Dead reckoning systems	—	—	X-band beacon	160	275
(a) Two accelerometers	500	0	(b) Ultrasonic signposts	170	160
(b) Two velocimeters	—	—	(c) Optical, infrared	170	155
Laser, orthogonal	715	0	(d) Buried antennas	135	120
Laser/compass	805	0	(2) Passive signposts	—	—
Ultrasonic	485	0	(a) Buried Magnets	95	110
(c) Odometer/compass	—	—	(b) Reflective patterns	—	—
Magnetic compass	285	0	Coded on signposts	580	85
Gyro compass	—	0	Coded on roadway	135	125
(3) Navigation, existing beacons	—	—	(c) Buried resonant loops	135	95
(a) OMEGA systems	—	—	Class III. Sparsely Distributed Special RF Sites		
Differential	1580	0	(1) Trilateration systems	—	—
Relay OMEGA	455	0	(a) Phase TOA	—	—
(b) LORAN (A, C, or D)	—	—	Narrow-band	100	5,000
Differential	2680	0	Wide-band	2,965	11,000
Relay LORAN	505	0	(b) Pulse TOA	1,435	14,500
(c) DECCA System	1010	0	(c) Interferometer, noise	885	9,000
(d) AM Broadcast stations	365	0	(2) Triangulation systems	—	—
			(a) Rotating beams (HONORÉ)	—	—
			(b) Direction finding	50	27,500
			Class IV Monitored Signposts Throughout Urban Area		
			(1) Radio receivers	—	—
			(a) Wayside	135	260
			(b) Buried antennas	145	265
			(2) Ultrasonic receptors	185	280
			(3) Optical, infrared detectors	185	270



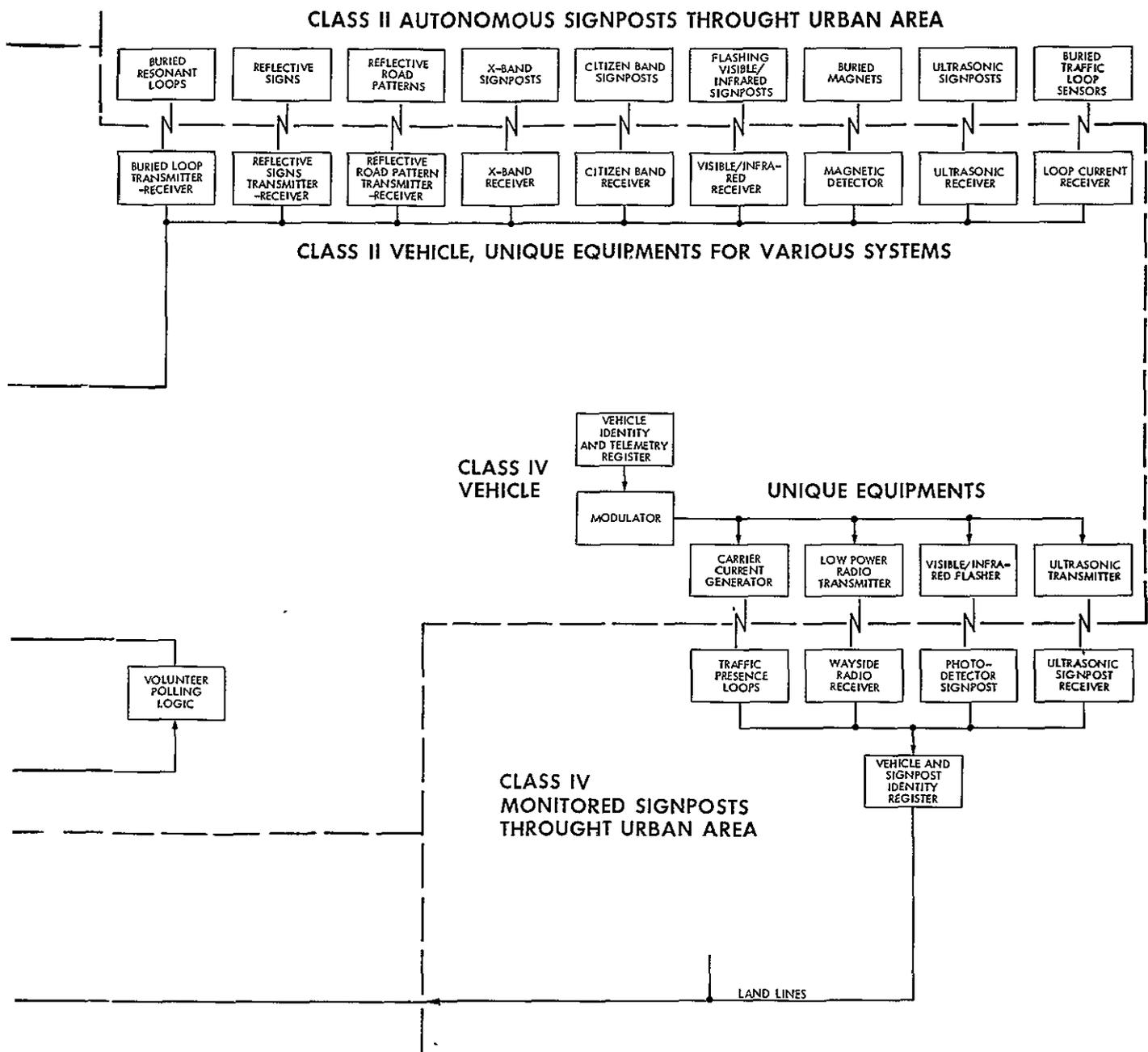


Figure 6. AVM Systems Showing Common and Unique Equipments for Vehicles, Signposts, and Base Stations

Class I, II, and III techniques may use any of the various vehicle polling techniques. Polling does not apply to the Class IV monitored signposts. The consideration of which polling method is to be used may depend heavily on whether or not equipments requiring digital communication have already been installed.

2. Technical and cost parameters. Virtually every technical performance and cost estimate parameter of a particular vehicle location technique is system-dependent. The AVM system accuracy, the numbers of fixed sites, the message lengths, the data rates, the base station computing, the information displays, software, and RF channel requirements are all functions of the particular application. Some functional elements and performance factors can be determined to a limited extent, such as the cost and coverage radius of the various signposts, RF beacons and traffic presence sensors in Classes II, III, and IV; and also the cost and minimum message requirements of the vehicle sensors and data processors in Class I.

In order that cost estimates could be made for the various AVM techniques, extremely simplified block diagrams of the unique functional elements associated primarily with the vehicle location process were developed. That is, only the vehicle sensor and AVM fixed sites associated with the particular technique were considered. These cost figures accompany each of the descriptions and considerations of the method in the following section.

B. AVM COST CONSIDERATIONS

In addition to the costs associated with the vehicular and fixed site functional elements required for the basic location process, there are the costs of yearly maintenance and vehicular radio additions or modifications for transmitting and receiving AVM signals. Estimates of the vehicular costs (as of 1974) for each class of AVM are presented in Table 2. In this table, the radio cost and the radio modification columns represent optional choices. That is, the radio modification cost is not applicable where a separate radio for AVM signals is selected.

The costs for fixed sites equipment, installation, operational maintenance, data link, and mileage charges per mile per month are summarized in Table 3 for Classes II, III, and IV.

Table 2. Vehicle Equipment Costs* for All AVM Classes and Systems

TECHNIQUE	COSTS PER VEHICLE IN \$					
	SENSOP	PROC.	RADIO	PAD.MOD	INST	O-HI
CLASS I						
KEYBOARD	45	40	1200	50	35	15
STYLUS MAP	2465	35	1200	50	35	25
2-ACCELEROMETERS	400	1000	1200	200	100	100
LASER VELOCINTP	500	1000	1200	200	135	150
ULTRASONIC WELD	270	200	1200	200	100	150
COMPASS ODOMETER	265	1000	1200	200	20	40
COMPASS LASER WEL	655	1000	1200	200	150	30
COMPASS U-SONIC WEL	385	1000	1200	200	100	30
OMEGA	2500	0	1200	200	80	75
LOPAN	2600	0	1200	200	80	75
DECCA	950	0	1200	200	60	75
AM-STATIONS	230	0	1200	200	50	60
DIFF. OMEGA	2300	0	1200	200	30	75
DIFF. LOPAN	2600	0	1200	200	30	75
DIFF. AM-STA.	315	0	1200	150	50	60
RELAY OMEGA	375	0	1200	150	80	100
RELAY LOPAN	425	0	1200	150	30	100
CLASS II						
BUPIED RES. LOOPS	90	0	1200	50	40	15
REFLECTING SIGNS	430	0	1200	50	130	20
REFLECTING ROAD	75	0	1200	50	60	15
VIS-BAND POST	120	0	1200	50	40	10
HF. WAF POST	105	0	1200	50	40	10
LF POST	100	0	1200	50	40	15
LIGHT I-P POST	95	0	1200	50	70	25
BUPIED MAGNETS	50	0	1200	50	40	0
ULTRASONIC POST	85	0	1200	50	35	25
TRAFFIC SENSOR	95	0	1200	50	40	10
CLASS III						
NAR-BAND FM PHASE	60	0	1200	165	40	25
MID-BAND FM PHASE	2875	0	0	30	90	25
PULSE T-O-APPRIAL	2575	0	0	0	150	25
NOISE CORRELATION	785	0	0	0	100	25
DIRECTION FINDER	35	0	0	0	15	0
CLASS IIII						
TRAFFIC LOOPS	80	0	0	0	65	10
WAYSIDE RADIO	75	0	0	0	40	10
PHOTO I-P DETECT	115	0	0	0	70	15
ULTRASONIC DETECT	125	0	0	0	65	15

* Costs as of 1974.

Table 3. Fixed Site Costs* for Class II, III, and IV AVM Systems

TECHNIQUE	FIXED COST PER SITE (OP UNIT) IN \$				
	EQUIP	INST	O-M	DATA LINE	LINE FEET
CLASS I					
KEYBOARD	0	0	0	0	0
STYLUS MAP	0	0	0	0	0
2-ACCELEROMETERS	0	0	0	0	0
LASER VELOCITY	0	0	0	0	0
ULTRASONIC WELD	0	0	0	0	0
COMPASS ODOMETER	0	0	0	0	0
COMPASS LASER WEL	0	0	0	0	0
COMPASS U-SONIC WEL	0	0	0	0	0
OMEGA	0	0	0	0	0
LOPAN	0	0	0	0	0
DECCA	0	0	0	0	0
AN-STATIONS	0	0	0	0	0
DIFF. OMEGA	0	0	0	0	0
DIFF. LOPAN	0	0	0	0	0
DIFF. AN-STA.	0	0	0	0	0
RELAY OMEGA	0	0	0	0	0
RELAY LOPAN	0	0	0	0	0
CLASS II					
BURIED RES. LOOPS	10	17	0	0	0
REFLECTING SIGNS	55	30	0	0	0
REFLECTING ROAD	5	30	25	0	0
V-SAND POST	230	45	15	0	0
HF. VHF POST	150	45	15	0	0
LF POST	125	45	15	0	0
LIGHT I-R POST	100	55	25	0	0
BURIED MAGNETS	2	4	0	0	0
ULTRASONIC POST	35	35	10	0	0
TRAFFIC SENSOR	95	40	0	0	0
CLASS III					
NAR-BAND FM PHASE	4500	500	500	25	5
MID-BAND FM PHASE	9500	1500	500	2070	0
PULSE T-O-APPRIAL	12000	2500	500	2000	0
NOISE CORRELATION	7500	1500	500	2000	0
DIRECTION FINDER	26000	1500	1200	25	5
CLASS IIII					
TRAFFIC LOOPS	165	113	10	13	4
WAYSIDE RADIO	160	113	25	13	4
PHOTO I-R DETECT	170	113	25	13	4
ULTRASONIC DETECT	180	113	25	13	4

* Costs as of 1974.

Additional costs associated with each AVM technique when configured as a system are the base station costs and the vehicle polling system costs, given in Table 4. The base station is assumed to include the vehicle location computer, the peripherals, the dispatcher displays, software, and yearly operational maintenance.

1. Vehicle cost parameters. Vehicle costing for an AVM system is a straightforward multiplicative process of determining the total cost to equip all vehicles in the fleet with the appropriate AVM sensor, data processor, vehicle polling equipment, and radio modification; motorcycles are not considered. If a separate radio link is deemed necessary for AVM purposes, then this additional cost must be added.

If the vehicle fleet has already been equipped with digital message entry devices (DiMED), keyboards, hard-copy printers, gas-plasma or cathode-ray displays, then some of the functional elements required for an AVM system have been established. Prior installation of digital message equipment was not considered in the costing of vehicular equipment.

2. Fixed site costs. Site costs unique to AVM systems are considered only in Classes II, III and IV. In determining the system costs, the number of installed units must first be determined. The design algorithms for fixed sites are dependent on the density distributions of intersections, road segments, and lanes, and on the area to be covered.

Most of the Class II AVM techniques that rely on radio ID signals are configured and costed on the basis of one autonomous signpost per intersection. The exception is the HF signpost which is configured on the basis of one unit for each four intersections because of the greater coverage radius. The reflective pattern signs techniques require two installations for each road segment because of the geometry constraints between vehicle and sign, whereas the traffic presence sensors require one installation for each road segment because of the nature of the normal installation. Buried loops and magnets require an installation per lane in each road segment. In addition, each installation is actually a multiple installation; i. e., there must be sufficient loops or magnets to provide adequate coding for each road segment. The cost estimates for fixed sites were based on an average of 2.4 lanes for each road segment, i. e., about 1 four-lane road for each 6 two-lane roads.

Table 4. Base Station Costs* for All AVM Classes and Systems

BASECOST									
AVL BASE STATION COSTS IN THOUSANDS OF \$									
TECHNIQUE	SML	COMPUTER			O-N	DISP	SOFTWARE		
		MED	LGE	INST			SML	MED	LGE
CLASS I									
KEYBOARD	30	40	60	10	100	3	10	20	30
STYLUS MAP	30	40	60	10	100	3	10	20	30
Z-ACCELEROMETERS	40	60	80	10	100	3	25	25	50
LASER VELOCINTP	40	60	80	10	100	3	25	35	50
ULTRASONIC VELO	40	60	80	10	100	3	25	35	50
COMPASS ODOMETER	40	60	80	10	100	3	25	35	50
COMPASS LASER VEL	40	60	80	10	100	3	25	35	50
COMPASS U-SONIC VEL	40	60	80	10	100	3	25	35	40
OMEGA	30	50	70	10	100	3	20	30	40
LOPAN	30	50	70	10	100	3	20	30	40
DECCA	30	50	70	10	100	3	20	30	40
AM-STATIONS	30	50	70	10	100	3	20	30	40
DIFF. OMEGA	30	50	70	10	100	3	20	30	40
DIFF. LOPAN	30	50	70	13	100	3	20	30	40
DIFF. AM-STA.	30	50	70	10	100	3	20	30	40
DELAY OMEGA	30	50	70	10	100	3	20	30	40
DELAY LOPAN	30	50	70	10	100	3	20	30	40
CLASS II									
BUPIED PLS. LOOPS	30	40	60	10	100	3	10	20	30
REFLECTING SIGNS	30	40	60	10	100	3	10	20	30
REFLECTING ROAD	30	40	60	10	100	3	10	20	30
V-BAND POST	30	40	60	10	100	3	10	20	30
HF, VHF POST	30	40	60	10	100	3	10	20	30
LF POST	30	40	60	10	100	3	10	20	30
LIGHT I-P POST	30	40	60	13	100	3	10	20	30
BUPIED MAGNETS	30	40	60	10	100	3	10	20	30
ULTRASONIC POST	30	40	60	10	100	3	10	20	30
TRAFFIC SENSOR	30	40	60	10	100	3	10	20	30
CLASS III									
NAR-BAND FM PHASE	33	80	137	8	100	3	20	40	60
MID-BAND FM PHASE	40	70	70	10	200	3	25	50	100
PULSE T-O-APPRIAL	100	250	250	10	175	3	35	70	100
NOISE CORRELATION	100	250	250	10	175	3	35	70	100
DIRECTION FINDER	15	30	60	10	150	3	15	30	60
CLASS IV									
TRAFFIC LOOPS	30	40	60	10	100	3	10	20	30
WAYSIDE RADIO	30	40	60	10	100	3	10	20	30
PHOTO I-P DETECT	30	40	60	10	100	3	10	20	30
ULTRASONIC DETECT	30	40	60	10	100	3	10	20	30

*Costs as of 1974.

The number of loops at each lane segment was that sufficient to provide a unique base-2 code for each road segment. The number of magnets used is half this value since spaces can be used to provide approximately half the coding bits (magnet for "one", space for "zero").

Since the Class III synchronized RF sites are more sparsely distributed, their numbers are estimated on the basis of urban area for the selected phase and pulse time-of-arrival techniques. The radius of coverage for narrow-band and pulse systems, based on prior tests and experiments, is set at 5 km (3 miles). In addition, the requirement that, wherever possible, four or more antennas should cover the given area is imposed. This procedure provides data for least-squares computation as opposed to the analytic "flat earth" solution of vehicle location. The wide-band antenna coverage radius is set at 11 km (7 miles), based on prior tests. Design algorithms were established from the rectangular model cities data as follows:

$$\text{Number of narrow-band and pulse sites} = 6 + \frac{\text{area in km}^2}{10}$$

$$\text{Number of wide-band sites} = 4 + \frac{\text{area in km}^2}{40}$$

The number of fixed sites in the southern California UGAC cities was determined from geometrical gridlined overlays superposed on outline maps of the cities. The outline and site locations for the cities are depicted in figures that accompany Part 2 of this Report. A minimum number of fixed sites for noise correlation and direction finding was established, recognizing that this number is probably insufficient for all but the smallest cities.

Class IV monitored signposts were configured and costed on the same basis as the equivalent Class II devices. Telephone line rental is, however, included in the site costs where applicable as the line should be considered an equipment cost as opposed to an operation cost.

3. Base station costs. Base station equipment costs were estimated on the basis of both urban area coverage and fleet size. The station's computer costs were estimated on the basis of area, and the software costs were based on fleet size. This separation of cost elements is only partially defensible. It is assumed that a minicomputer is usually used to support the AVM function with varying amounts of bulk storage (disc) to accommodate the city map for output display.

Exceptions are in the Class III time-of-arrival (TOA) methods, where larger machines are assumed. The pulse and noise-correlation techniques also require a larger computer with more speed and versatility than can be provided by a minicomputer because of the inherent capability of servicing many more vehicles per unit time and the need to accommodate a large number of inputs in real time. The software estimate based on fleet size is also difficult to justify totally. Much reliance was placed on prior work estimates and on the judgments of systems analysts.

Three estimates each of base station computer and software costs were made based on model city parameters for small, medium and large cities. For the UGAC cities, the costs were determined based on the urban areas and the total fleet size, excluding motorcycles, using linear interpolation.

Display equipment costs are included in the base station costs on the basis of the actual number of dispatchers in the case of UGAC cities. For the model cities, the costs are estimated on the basis of 1 display console for each 50 vehicles or less.

4. Installation costs. Equipment installation costs were obtained by multiplying the cost per unit vehicle and the cost per fixed site installation by the appropriate number of units. Together with the base station installation cost, they make up the tabulated total cost. A constant cost value is assumed for the base station, which is a rounded average value of prior estimates made in conjunction with AVM demonstration tests.

5. Operation and maintenance costs. The estimates of O - M costs for equipment installed in vehicles, at fixed sites, and the base station are based on experience values for both mobile and fixed equipments. In the base station, the principal cost element is for operation and maintenance personnel. Three persons (one per shift) were assumed in all AVM techniques to provide software support or equipment service. Although this assumption may not be justifiable, it was believed that AVM is a comparatively new technology which will probably interface with computer-aided dispatching and digital message systems and that additional service personnel would be required for a substantial time period after the initial installation.

V. VEHICLE POLLING AND LOCATION PERFORMANCE

Four classes of vehicle polling are considered for AVM Systems:

(1) Synchronous, (2) Commanded or random access, (3) Synchronous with Command capability, and (4) Volunteer or contention. All four techniques are generally applicable to Class I and II AVM Systems. Synchronous polling and synchronous with command are used mainly in Class III Systems. For the Class IV monitored signpost systems, which use land lines, polling by radio is not applicable in the context used in this description.

All polling techniques are suitable for half-duplex (base station and vehicle on the same frequency), but when the base station relays all vehicle transmissions or when each vehicle monitors all other vehicles, then the Volunteer technique can only be used on full-duplex (base and vehicle on different frequencies).

1. Synchronous polling. In this technique, each vehicle transmits location data at a preselected time within the fleet polling sequence. Equipment on the vehicle keeps track of the start of the sequence and internally determines when its time to respond occurs. The cost of the vehicle polling equipment installed (as of 1974) is about \$270.

2. Synchronous with command capability. This polling technique allows the base station to modify the position of each vehicle in the polling sequence. The cost of the vehicle equipment installed is about \$365.

3. Commanded or random access polling. In this technique, the base station sends a request to each vehicle whenever location data is required. This technique is the most flexible but requires more use of available RF time.

4. Volunteer polling. This contention method requires that each vehicle determine whether the channel is "clear" before transmitting. The cost of vehicle equipment installed is about \$170.

These vehicle polling techniques were evaluated with both a simple one-time radio message transmission and with redundant transmissions where every message is sent twice. The digital message rate is set at 1500 bps. Where equivalent RF channels are assumed, a channel spacing of 25 kHz is used. Message lengths are about 20 bits, or occupy about 15 millisecond transmission time. Delays due to equipment turn-on times reduce the achievable polling rate.

**PART ONE:
AVM COST BENEFIT
INFORMATION BASE**

G.R. Hansen

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PART ONE. AVM COST BENEFIT INFORMATION BASE

I. PERFORMANCE AND COSTS OF PROVED AVM TECHNIQUES

Costs and performance parameters of 36 operational or proved techniques used for automatic vehicle monitoring (AVM) are described and illustrated in this section. Schemes that are primarily intended for vehicle identification, such as those used in rail freight or extensions of point-of-sale methods are not included. In this Report, the vehicle monitoring techniques are categorized into five broad classes, based on system element types and functions: Class O Manual Monitoring, with no augmentation of location information; Class I AVM, with no additions to the urban environment, Class II AVM, using densely distributed autonomous signposts, Class III AVM, using sparsely distributed special transmitting/receiving fixed RF sites, and Class IV AVM, using densely distributed monitored signposts. Estimated special equipment and installation costs are as of 1974.

A. Class O Manual Monitoring. No AVM

This is the baseline vehicle location technique against which other systems should be compared. A manual monitoring system consists of a dispatcher, an existing real-time communication system, and a fleet of vehicles. The dispatcher's knowledge of vehicle locations depends upon voice communications with the officers in the vehicles. Even in the manual vehicle monitoring class, there are several options that affect both performance and costs. The dispatcher can, for example, rely strictly upon his knowledge of each vehicle's designated location or patrol area and its subsequent assignments. Alternatively, he can use some of his RF resources (channels and air time) to interrogate and obtain actual vehicle locations vocally.

A relatively wide range of options is available to the dispatcher for use with Class O non-automated vehicle monitoring. The simplest visual location aid is just a map on which the assigned beat areas are permanently marked, the dispatcher relying on his memory to locate the vehicles on the map. Numbered magnets or lights may be used which may be updated manually to augment his memory. Elaborate electro-optical display devices are available, which indicate each vehicle's last known location, status, and anticipated destination, all driven by manual input.

The dollar cost of a purely manual vehicle management system is almost bound to be competitive, but the use of RF resources could be prohibitive, and the attainable dispatching performance is also an open question. With an AVM system, the closest available vehicle can quickly be dispatched in response to a service request. Analyses indicate that response times are reduced and fleet efficiency is increased by up to 7%, permitting a reduction in fleet size and in operating costs.

B. Class I AVM. No Modification to Urban Environment

1. Officer update. Vehicle location data may be encoded automatically by means of manually operated devices installed in the vehicle, such as keyboards or stylus maps.

a. Keyboard entry. This manual data input technique for providing automatic vehicle location data at the base requires the officer to enter some code or identifying numerical sequence on a digital keyboard (Fig. 1-1). The keyboard can be either the device being used for sending digital messages or a separate unit. The location code can relate to a particular street segment and/or intersection and would probably be four or five digits in length. The vehicle location code is transmitted to the base station either by "Touch-Tone" or some other digital modulation techniques. Volunteer or random-access vehicle polling is most suitable for this technique. The AVM system accuracy is dependent on the code used; that is, either (1) the nearest intersection if only streets or intersections have codes, (2) a particular block on a street if each segment is coded, or (3) the location in a block if street segment is followed by address digits of closest property parcel. The automatic computational requirement is a table look-up function to translate the code to a geographical location. While this AVM technique is low in cost, particularly if a digital message entry device (DIMED) is already installed, it is extremely slow and requires much memorization on the part of the patrolling officers. If the car is out of the normal beat, either a map or street guide would have to be used by the officer for reference to determine the code.

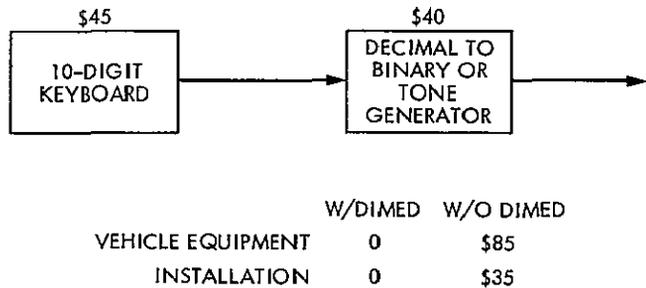


Fig. 1-1. Class I AVM Officer Update Option, Using Keyboard Entry

b. Stylus map. This officer update technique is a manual method whereby the patrolling officer indicates his vehicle's location by pressing the appropriate spot on a special map (Fig. 1-2) with a stylus. The map-and-holder combination encodes the spot where the pressure is applied, and the digital code is sent to the base station. The location polling process can be either in response to a request or volunteered

as part of a transmission from the vehicle. Location accuracy is dependent on the scale of the map and on the holder encoding technique. For example, a 20 x 25 cm (8 x 10 in.) portion of a 7.5-minute U. S. Geological Survey topographic map (scale 1 24000) would cover an area of 6 x 4.8 km (3.6 x 3 mi). If this information were encoded by 5 binary bits (1 in 32) on each axis for a 10-bit location code, then the location could be achieved within a rectangle of about 190 x 150 meters (600 x 500 ft). By increasing the encoding to 12 bits or using a map with half the scale, the size of the vehicle's location rectangle could be decreased by one-half in each dimension. Maps of other beats would probably be required by each officer together with some means of identifying when these maps were in use. The base station computation requirement is a table look-up function to translate the code to a geographical location.

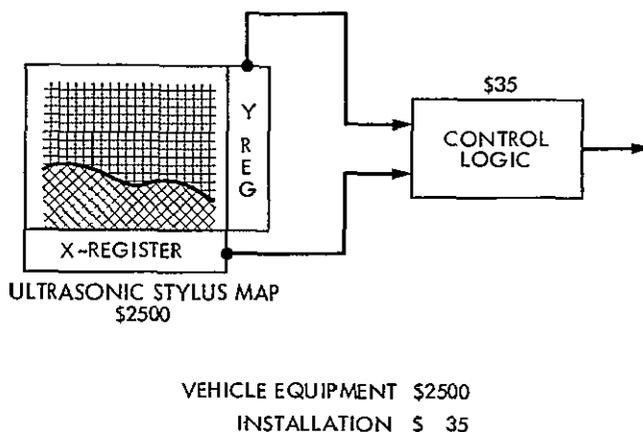


Fig. 1-2. Class I AVM Officer Update Option, Using Stylus Map

2. Kinematic sensors. Changes in vehicle location may be sensed either by accelerometers, velocimeters, or odometers.

a. Two accelerometers. Dead reckoning, which can measure the change in location of a vehicle, can be mechanized with two accelerometers (Fig. 1-3). These devices would measure the rate of change of velocity of the vehicle in the horizontal plane of the vehicle in both the fore-and-aft and sideways directions. The outputs of the two accelerometers can be used to compute velocities attained as well as changes in direction and distance during a selected time interval. The computations can be performed on-board the vehicle and the results transmitted to the base station, or the outputs of the accelerometers can be encoded and transmitted directly to the base station.

A U-turn made at a speed of 10 m/sec (23 mph) in a 4-lane street about 18 m (60 feet) wide is about the limit of vehicle turning performance. This turn would result in about a 0.8-g indication of lateral motion for just over 3 seconds. If the accelerations are sampled and transmitted every 0.03 second, then the 16 data bits each time would lead to a data rate of 4800 bits/sec. Based on personal rapid transit studies, the "comfort"

zone of vehicle operation is in the less than 0.2-g range. If most accelerations experienced by the vehicle are maintained in this 0.2-g region, then a 1% full-scale error during a low-g maneuver causes these normal measurements to be in error by 4% or more.

b. Orthogonal laser velocimeters. This kinematic sensor technique is based on prior work by G. Stavits (Ref. 1), which used a laser velocimeter (Fig. 1-4) and compass (Fig. 1-5). In this scheme, the laser would be used to measure not only the forward velocity of the vehicle, but also that velocity component which occurs during turns and is at a right angle to the fore-and-aft motion. All portions of the vehicle which are not located on the turning axis experience some side velocity during a turn. The sign and magnitude of this velocity component is a function of the distance from and location with respect to the turning axis. If both forward and side velocities are measured at the same point remote from the turning radius, then the velocities at this point provide a means to keep track of the vehicle motion. The operation of the laser velocimeter is based on the speckle pattern observed in the reflection of coherent laser light from a surface that moves relative to the source. The speckles tend to move in the opposite direction to the relative motion between the laser source and the reflecting surface. By passing the reflected laser light through a diffraction grating and then to a photodetector, a signal can be derived with a frequency that is a direct measure of the velocity of the reflecting surface. The velocity measured is that at right angles to the rulings on the grating. Two photo detectors and two gratings with the rulings at right angles provide the means to measure the two components of motion of a single laser spot. Investigators in the cited work (Ref. 1) indicate that a laser velocimeter's dynamic range is of the order of 2500:1 and that the maximum and minimum measurable velocities are primarily a function of the rulings on the grating. For example, a vehicle velocity range of 50 m/sec to 2 cm/sec (115 mph to 0.05 mph) could be accommodated, and turning rates of 0.01 radian/sec (0.6 °/s) could be detected. Maximum data bit rates of about 5000/sec for speed and 100/sec for turning may require in-vehicle computation.

c. Ultrasonic velocimeters. The use of ultrasonic waves for intrusion detectors, motion sensors, and distance measuring is well established. The doppler frequency shift of a reflected sound wave from the road surface can form the basis of a velocimeter (Fig. 1-6). An ultrasonic wave directed at an angle at the road surface will reflect a doppler-shifted frequency proportional to the cosine of the angle of incidence times the surface velocity. For example, if a 33-kHz frequency is chosen which has a wave length of about 1 cm directed at a 45-degree angle to the road surface and traveling at 50 m/sec (115 mph) will yield a doppler shift of about 10%. If a dynamic range of 2000:1 can be achieved, a minimum velocity of 2.5 cm/sec (0.05 mph) can be detected. If the velocimeters are mounted on each side of the vehicle and the differential velocities are measured to the same 2.5 cm/sec, then minimal directional changes of 12 mrad (about 0.7 deg) can be detected. This precision is on the order of that achieved with the differential odometer, described later.

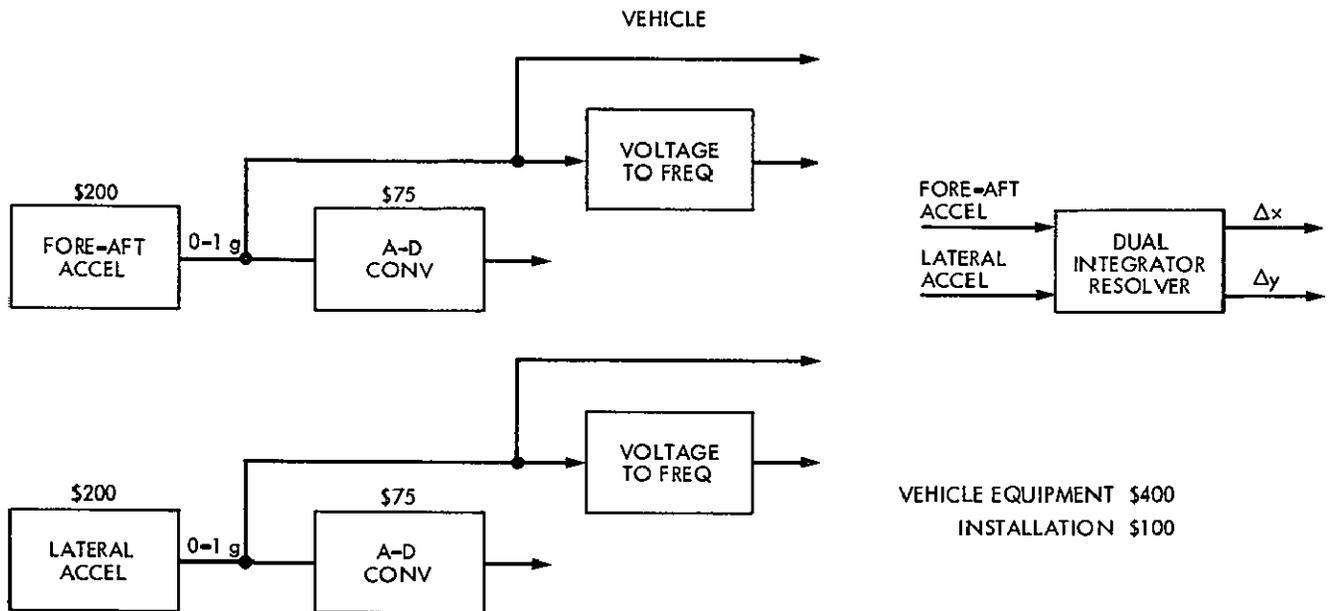


Fig. 1-3. Class I AVM Kinematic Sensor Using Two Accelerometers

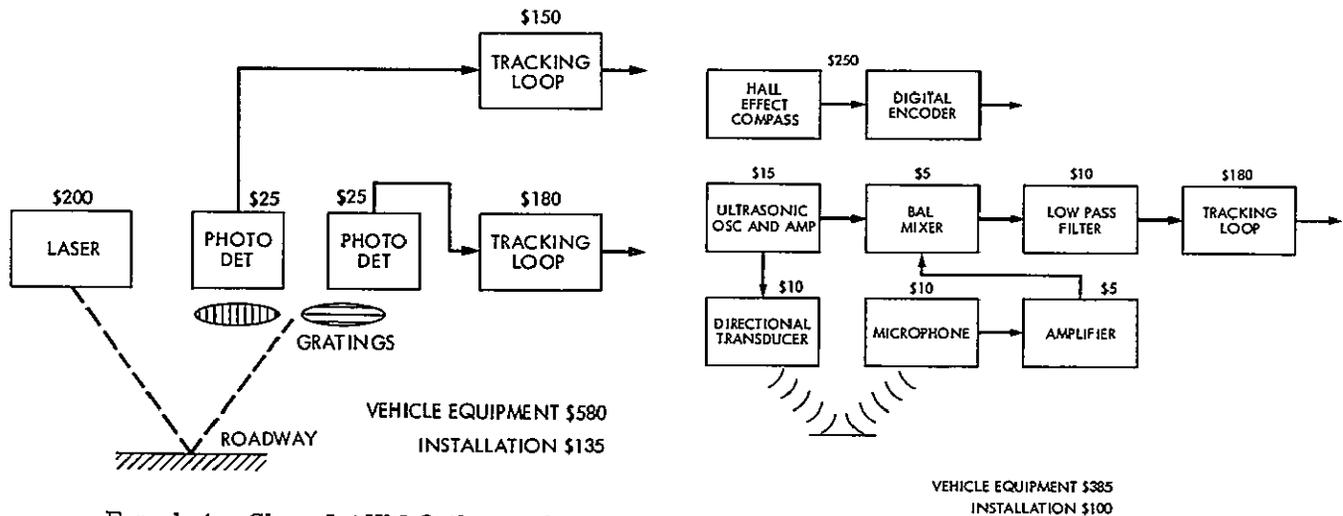


Fig. 1-4. Class I AVM Orthogonal Laser Velocimeter

Fig. 1-6. Class I AVM Magnetic Compass with Ultrasonic Velocimeter

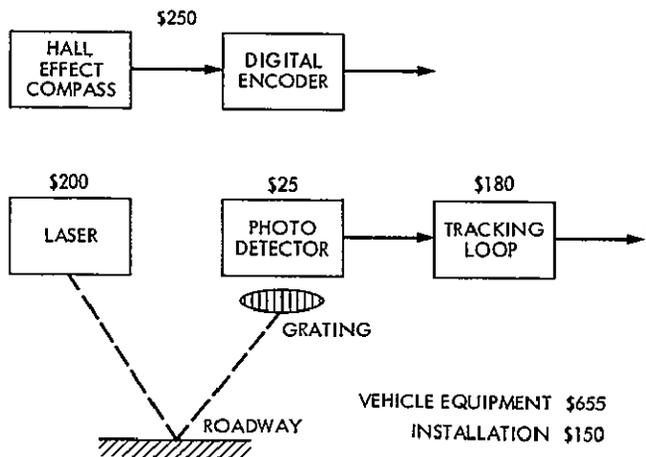


Fig. 1-5. Class I AVM Magnetic Compass with Laser Velocimeter

d. Odometer-Compass. Dead reckoning with compass and odometer (Fig. 1-7) has been tested, built and furnished to several armed forces (U. S., Canada, Britain) as a means of keeping track of military vehicles in off-road situations. The systems have all achieved some measure of success, and all have included on-board computation to indicate position in northings and eastings (Y- and X-coordinates). Accuracies within 0.6 to 2% of the distance travelled have been demonstrated. Error sources are the inaccuracies in the odometer measurement and compass heading. The odometer is affected by tread wear and wheel slip maneuvering. Compass heading is influenced by local anomalies, and proposed filtering techniques have included measuring the steering gear angle, vertical component of the field, and limiting direction change as a function of vehicle speed. At present, gyro compasses are not suited for vehicular applications.

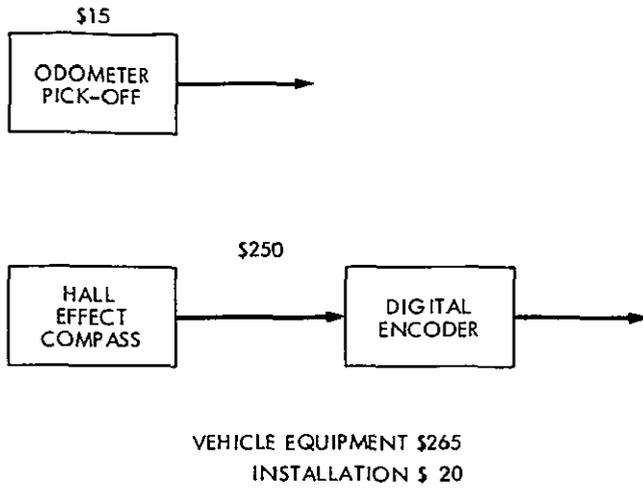


Fig. 1-7. Class I AVM Magnetic Compass with Odometer

3. Wide-area navigation. The three principal wide-area navigation schemes use synchronized radiolocation beacons. They are hyperbolic techniques which operate in three different modes: OMEGA, LORAN, and DECCA.

a. OMEGA. This navigation scheme (Fig. 1-8) uses very low frequency (10-13 kHz) time-multiplexed RF signals. The relative phase of the

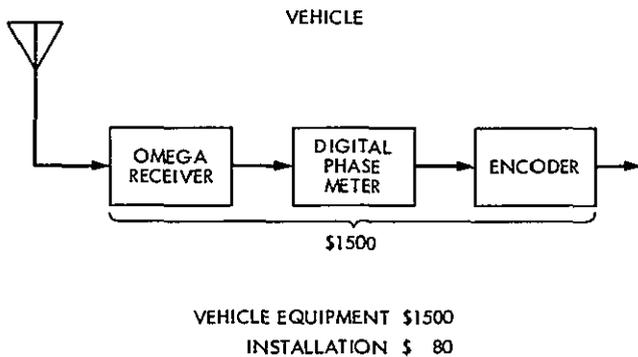


Fig. 1-8. Class I AVM Normal and Differential OMEGA Navigation

signals, transmitted on the same frequency in sequence from several sites, defines a set of lines of position (LOP). At the intersection point of the LOPs is the receive location. There are ambiguities in position since the phase patterns repeat every 15 km-or so. Differential OMEGA is a technique for reducing the effects of local anomalies. A fixed receiver at a precisely known location is used to remove these anomalies over a 15 to 30 km radius through continuous monitoring of the received signals.

b. Relay OMEGA. In this technique (Fig. 1-9), the vehicle rebroadcasts the raw OMEGA signals on another frequency to the base station. The base station then measures the phase differences and computes the LOPs. This is a time-consuming operation as each vehicle would have to transmit the entire OMEGA sequence lasting several seconds.

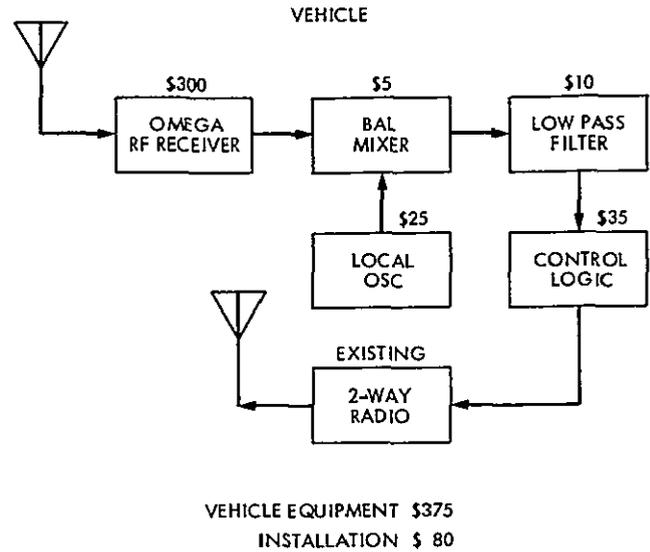


Fig. 1-9. Class I AVM Relay OMEGA Navigation System

c. LORAN. This technique (Fig. 1-10) uses combined pulse and phase time-multiplexed RF signals for determining LOPs. Pulsed signals from three or more stations are transmitted 10 to

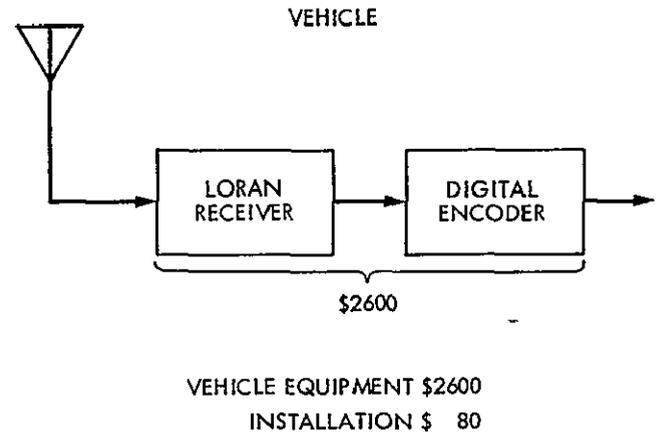


Fig. 1-10. Class I AVM Normal and Differential LORAN Navigation

33 times a second in coded groups. The receiver measures the time of arrival difference from given pairs of signals to determine the LOP. No ambiguity exists, and each LOP is unique geographically. Differential LORAN also uses fixed site receivers to remove local propagation anomalies.

d. Relay LORAN. In this system (Fig. 1-11), the received signals are retransmitted to a base station for time differencing. Some bandwidth compression is required and is used in a technique called LOCATES in order to retransmit the 90 to 110 kHz LORAN over voice communication channels. The 20-kHz bandwidth signals are reduced to 3 to 7 kHz for retransmission. The higher repetition rates of LORAN make relaying more feasible than in OMEGA.

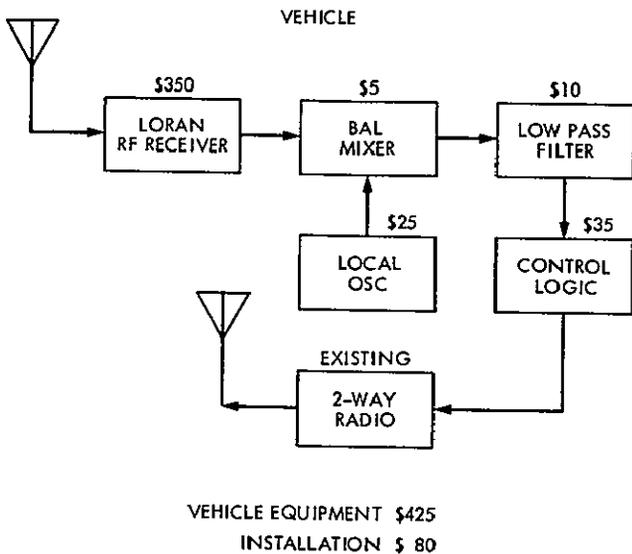


Fig. 1-11. Class I AVM Relay LORAN Navigation System

e. DECCA. The DECCA system (Fig. 1-12) is a continuous-wave phase-difference technique in which each transmitter operates on a different, but harmonically related, signal to other transmitters. The location is determined by simultaneous reception and comparison of the phase of the signals. Since the LOPs determined by the phase measurements are not unique, special signals are transmitted frequently to enable the determination of the correct one.

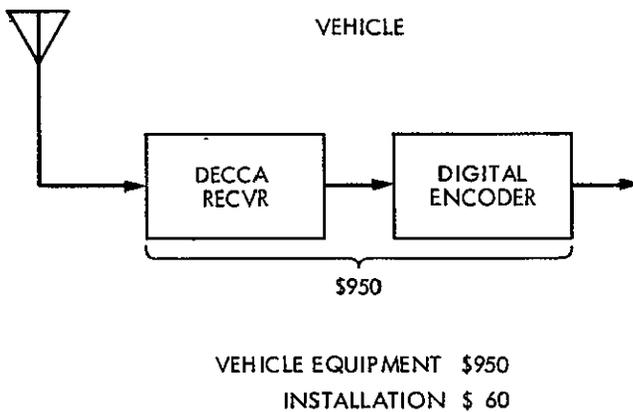
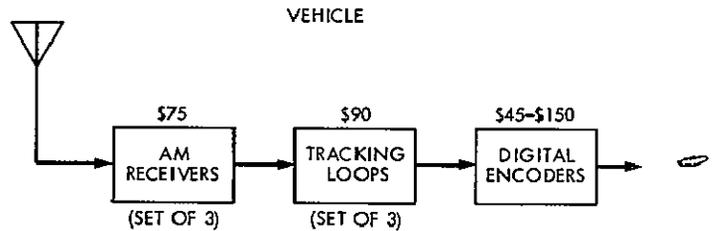


Fig. 1-12. Class I AVM DECCA Navigation System

f. AM Broadcasting stations as radiolocation beacons. Carrier signal frequencies, being transmitted from three commercial broadcasting stations located around a city's perimeter, can each be separately received and multiplied by relatively low-cost in-vehicle equipment to synthesize a new common frequency. These three identical frequencies can be made relatively phase coherent. Virtual hyperbolic patterns of navigational LOPs are generated by the signals received

from each pair of AM stations. These LOPs can serve as the basis for a reliable AVM system (Fig. 1-13). A vehicle's starting position is first noted and recorded at the central command base. When the vehicle moves, the phase differences produced in the three signal frequencies are measured on-board, and the number of times that the phase pattern is repeated can be counted on-board. This digital information is then sent to the base where a minicomputer converts it to the vehicle's new geographical location. In Part Four of this report, this AVM system is described in detail.



	NORMAL	DIFFERENTIAL
VEHICLE EQUIPMENT	\$200	\$315
INSTALLATION	\$ 50	

Fig. 1-13. Class I AVM AM Broadcasting Station Navigation Systems

C. Class II AVM: Autonomous Signposts Throughout Urban Area

All autonomous signpost location techniques rely on the vehicle coming near or passing over an instrumented geographical location. The instrument, located at an intersection or road segment, is usually a continuously radiating device sending out a uniquely coded message, either radio, light, IR, ultrasound, or magnetic. The vehicle is equipped with a suitable receptor to receive and store the message for subsequent retransmission to the base station and in this way inform the base as to the last instrumented location passed.

1. Radio frequency signposts. Most of the techniques use RF signals as the medium for the short-range link from wayside or roadway signpost to vehicle. These signals, which may range from low frequencies (190 kHz) through VHF to X-band (10 GHz), require the equipment shown in Figs. 1-14, 1-15, 1-16. Elevated locations for the signposts are usually selected to achieve a larger coverage area, freedom from blocking by large vehicles, and to lessen the probability of vandalism. Vehicle location accuracies of the Class II AVM systems are a function of the radius of influence and density of the signposts, and similarly the message repetition rate from the post must increase as the radius of influence decreases to ensure complete message reception by a fast moving vehicle.

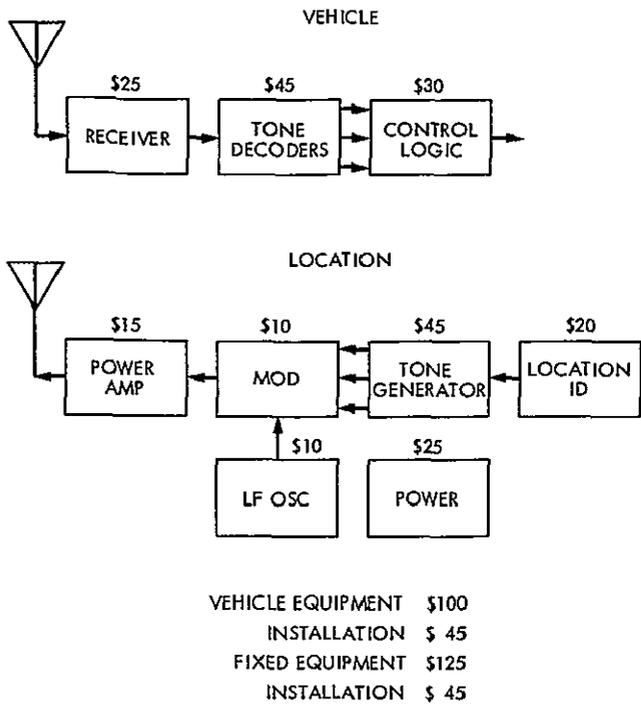


Fig. 1-14. Class II AVM Low-Frequency Wayside Radio Signposts

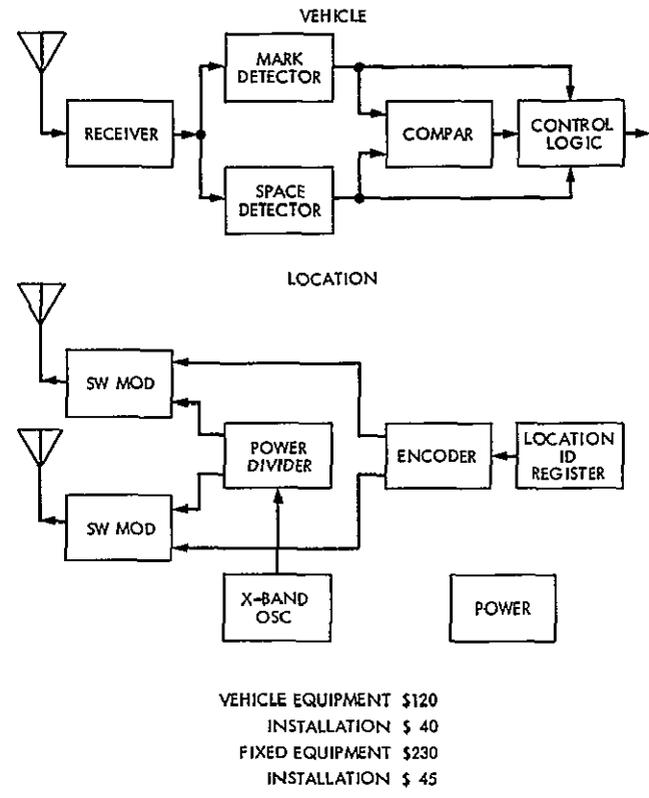


Fig. 1-16. Class II AVM X-Band Wayside Radio Signposts

Since active electronic signposts require some primary power source, difficulties may be encountered in general applications if reliance is placed on either street lighting circuits or traffic signals. In some applications, alternate power sources will be necessary. Options other than utility power are long-lived batteries, solar, and radioisotope sources.

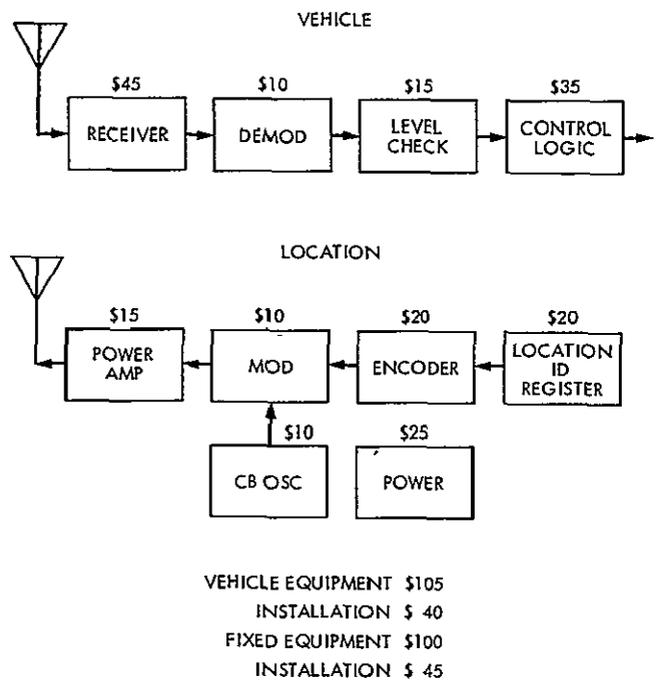
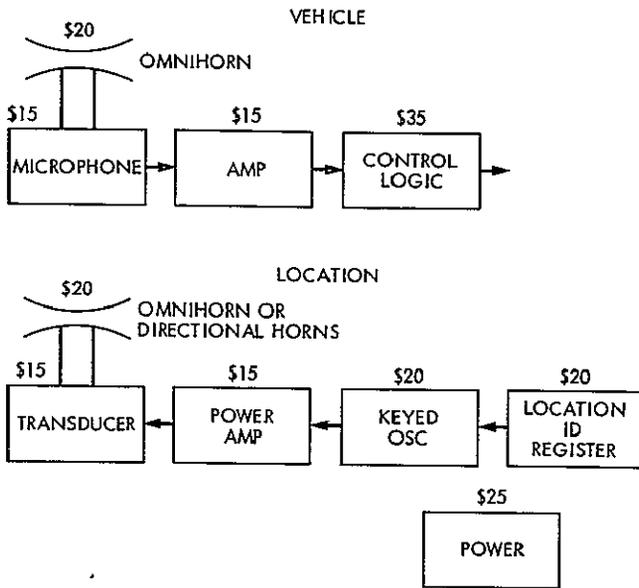


Fig. 1-15. Class II AVM Citizen Band or VHF Wayside Radio Signposts

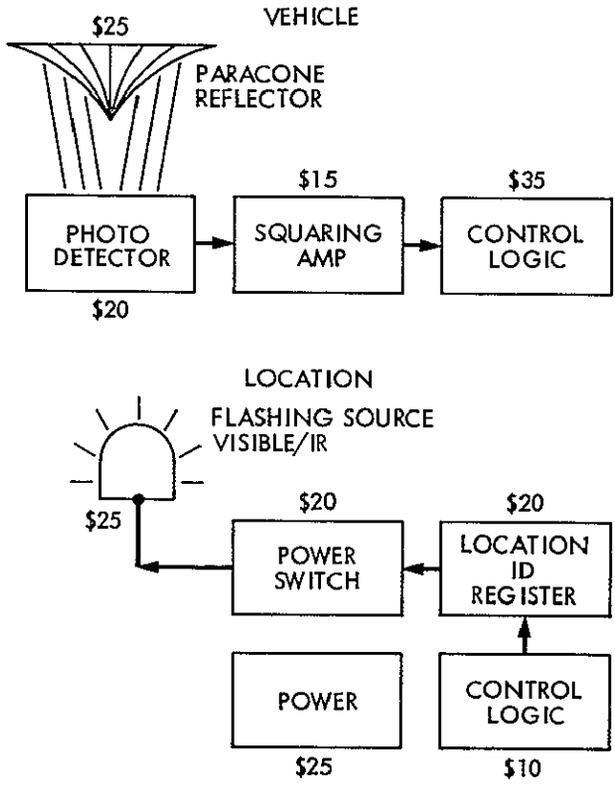
2. Ultrasonic and photo or IR signposts. Ultrasonic and light radiation are possible practical approaches to the message link to avoid further RF congestion and interference to other services. The ultrasonic waves (Fig. 1-17) are similar in length to X-Band RF (less than 1 cm), and "horn" antennas can be designed for focusing sound to a desired coverage area. The flashing light approach (Fig. 1-18), either visible or infrared, is also a practical short-range information transfer method. Both of these techniques are, however, somewhat hindered by weather conditions, particularly fog, rain, and wind.

3. Buried active antennas. The buried antenna approach using existing traffic-presence sensor loops as electronic signposts (Fig. 1-19) is currently being tested in San Francisco and New York as a toll authority billing technique for equipped buses. In these systems, the antenna (buried loop) interrogates continually and receives responses from instrumented buses so that the buses may be billed for toll fees without having to stop. The use of traffic sensor loops as antennas is a practical implementation for electronic signposts and has an added advantage in that weather-proof enclosures and power are available in the traffic signal controller.



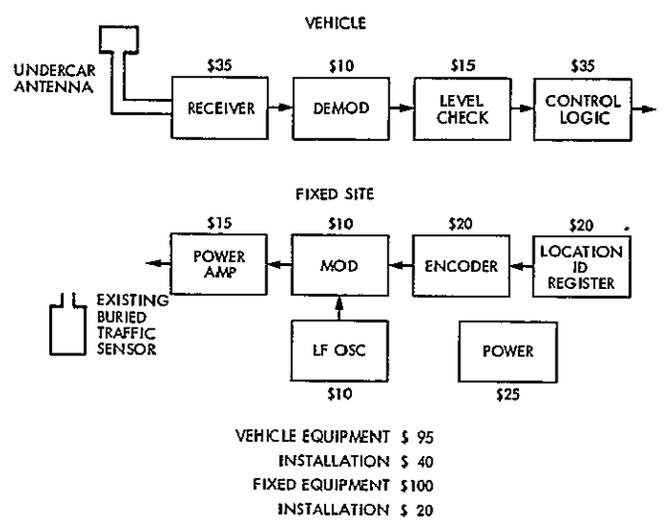
VEHICLE EQUIPMENT \$ 85
 INSTALLATION \$ 85
 FIXED EQUIPMENT \$115
 INSTALLATION \$ 45

Fig. 1-17. Class II AVM Autonomous Ultrasonic Signposts



VEHICLE EQUIPMENT \$ 95
 INSTALLATION \$ 75
 FIXED EQUIPMENT \$100
 INSTALLATION \$ 55

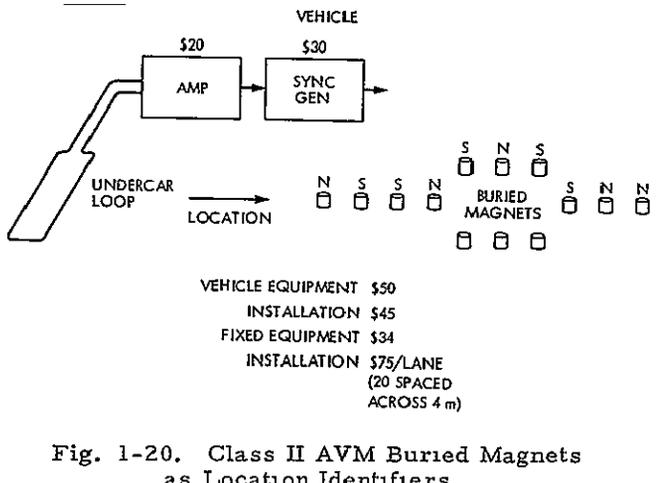
Fig. 1-18. Class II AVM Flashing Visible or IR Light Signposts



VEHICLE EQUIPMENT \$ 95
 INSTALLATION \$ 40
 FIXED EQUIPMENT \$100
 INSTALLATION \$ 20

Fig. 1-19. Class II AVM Active Buried Antenna Traffic Sensors

4. Buried magnet autonomous location identifiers. Buried permanent magnets are used to provide a means of passive proximity location identification (Fig. 1-20). In this concept, rows of permanent magnets are installed along vehicle lanes to provide a means of inducing a voltage in a sensing coil mounted on the vehicle. The magnets could be either placed in drilled holes in the pavement or propelled into the surface by using an explosive-actuated concrete fastener tool. Magnets in the rows have either N or S poles up to provide binary identification of the location. The sense coil in a forward moving vehicle would detect signals of different polarities depending on the vehicle direction across the magnetic field. Reasonably strong magnets must be used, both to be detected in the presence of the earth's field, which is about 0.5 gauss, and to withstand added spacing that could be created by street resurfacing.



VEHICLE EQUIPMENT \$50
 INSTALLATION \$45
 FIXED EQUIPMENT \$34
 INSTALLATION \$75/LANE
 (20 SPACED
 ACROSS 4m)

Fig. 1-20. Class II AVM Buried Magnets as Location Identifiers

5. Reflective paint patterns on signposts and roadways. Other passive techniques require that the vehicle continually interrogate the area travelled either by low-frequency RF or light radiation. In the case of the reflective wayside sign (Fig. 1-21) or pattern on the road (Fig. 1-22), the vehicle must be in a fairly precise position to

receive a response — less in the case of the road pattern than the wayside sign.

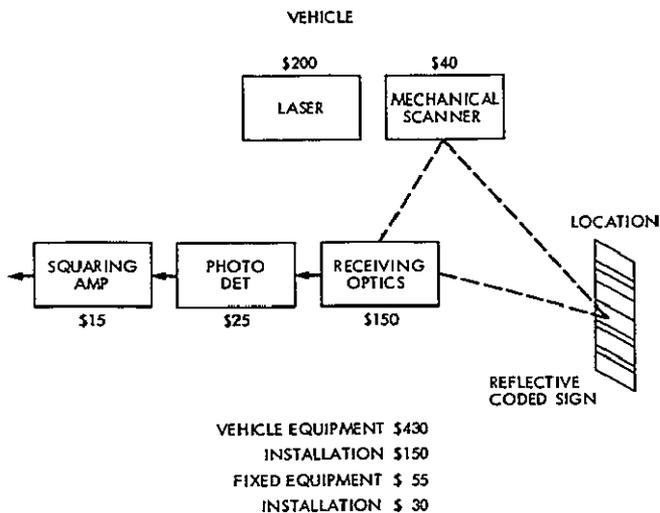


Fig. 1-21. Class II AVM Sensor of Reflective Patterns on Signposts

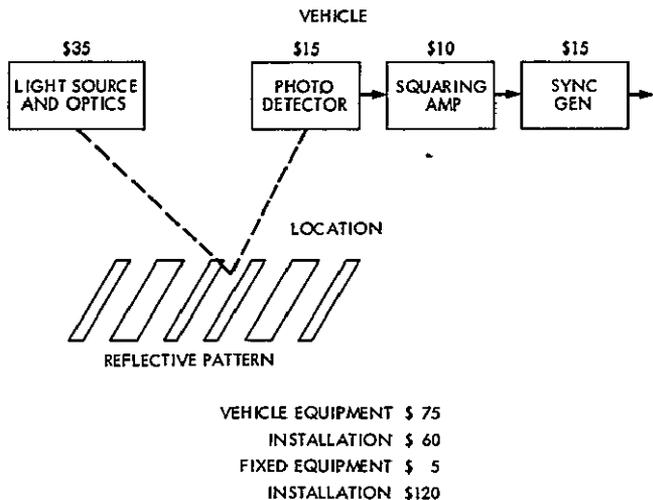


Fig. 1-22. Class II AVM Sensor of Reflective Patterns on Roadway

6. Passive buried loops. The passive buried loop (Fig. 1-23) requires that the vehicle, equipped with under-car antennas, pass over and excite the loops to obtain a response. Results of a detailed analysis of the buried loop coupling are included in Part Four of this report.

D. Class III AVM. Sparsely Distributed Special RF Sites

This class of AVM systems encompasses those vehicle location techniques of the trilateration rho-rho (range-range) and triangulation theta-theta (angle-angle) types with sparsely distributed RF sites primarily intended for medium or small urban area coverage, 7 km (4 mi) to 11 km (7 mi) radius.

1. Trilateration Systems. Included in the rho-rho systems are trilateration techniques which measure the time-of-arrival (TOA) of a signal emanating from a vehicle at several fixed receiving sites. Each pair of time differences

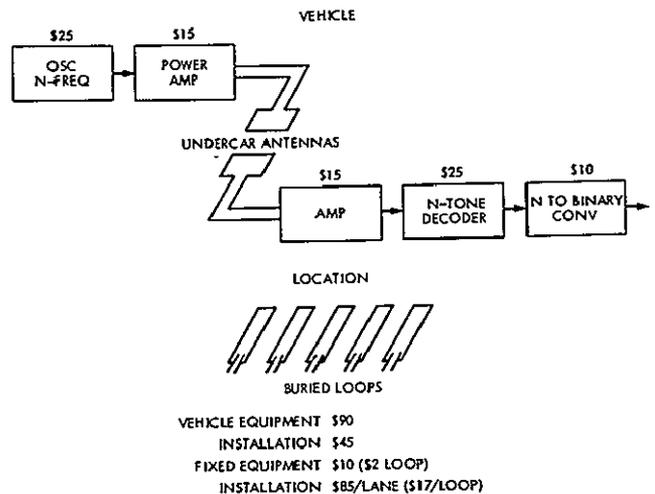


Fig. 1-23 Class II AVM Sensor of Passive Buried Resonant Loops

forms a hyperbolic line-of-position (LOP). The intersection of these LOPs establishes the position of the vehicle. This information may be sent to the base station from the site by leased telephone lines or by microwave transmissions.

Hyperbolic trilateration methods tested have used either a pulsed (or keyed) carrier from the vehicle or an audio-tone frequency modulating a carrier. The pulse systems measure the TOA of the signal and establish the range differences directly. The tone trilateration systems measure the relative phase of the audio tone at the receiving sites, and the phase difference measurement then determines the range difference.

The tested tone phase TOA trilateration methods used 2.7 kHz and approximately 18 kHz frequencies whose phase patterns repeat at 111 km and 16 km, respectively. These AVM systems have been termed narrow-band (Fig. 1-24) and wide-band (Fig. 1-25) since the first can be accommodated in a narrow-band FM voice channel (25 kHz) while the second requires eight times the bandwidth or four adjacent channels (100 kHz). In comparison, the pulse TOA method (Fig. 1-26) utilizes up to 10 MHz of bandwidth to preserve the leading edge of the pulse.

Another wide-band trilateration method is based on interferometer techniques. As currently envisaged, each vehicle would transmit a carrier signal modulated with either white or P-N sequence noise (Fig. 1-27). These signals would again be received at the several sites, and by correlation computation the time differences of arrival would be established. Since only the signals from one vehicle would show substantial correlation, it would be possible but not necessary to have all vehicles broadcasting the noise modulated signals simultaneously. The effects of multipath on trilateration techniques have been analyzed and modeled by George Turin (Ref. 5).

2. Triangulation Systems. The direction finding methods proposed would measure the azimuth angle of the vehicle signal at several fixed sites (Fig. 1-28). The intersection of the extension of these bearing angles would be the position of the vehicle. Multipath in this method would probably cause uncertainty in the angle of arrival of the vehicle signal leading to

approximately the same accuracy limitations as those for trilateration. Of the Class III AVM systems delineated, the direction finding and narrow-band phase TOA would allow the use of the normal vehicle transceiver. The pulse, wide-band phase, and noise modulation TOA methods would require an additional AVM transmitter.

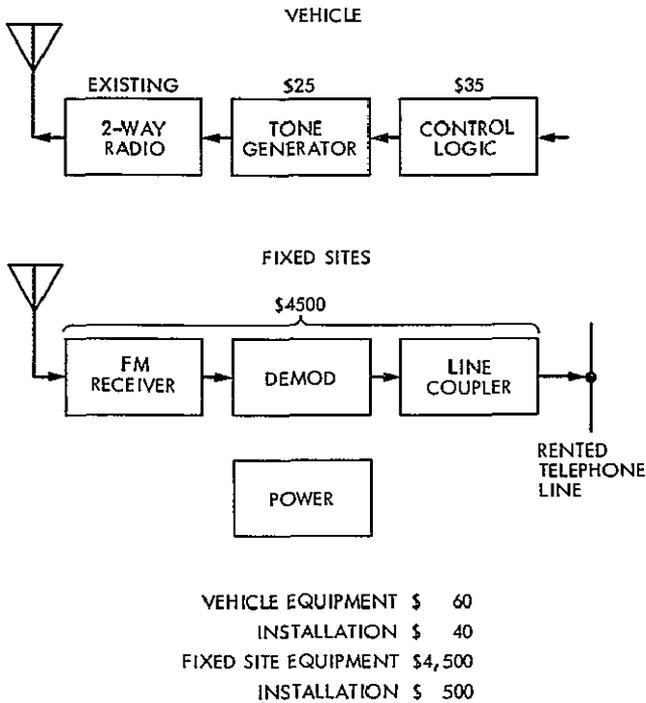


Fig. 1-24. Class III AVM Narrow-Band FM Phase TOA Trilateration

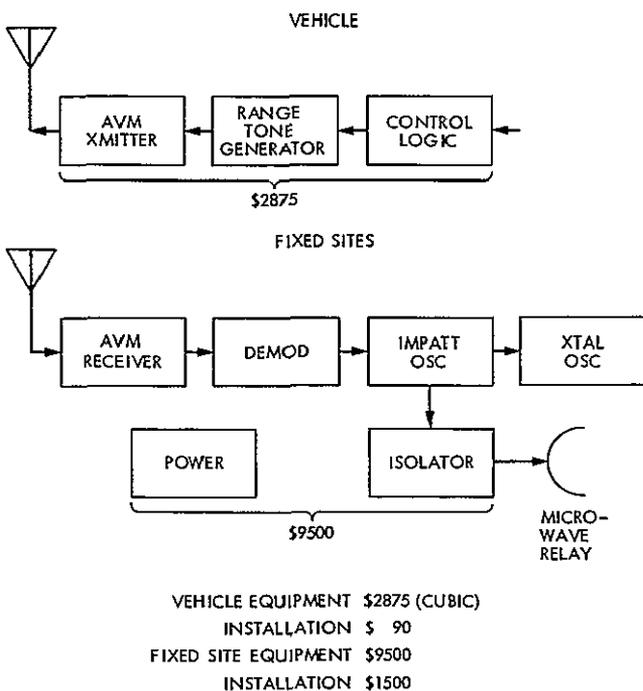


Fig. 1-25. Class III AVM Wide-Band FM Phase TOA Trilateration

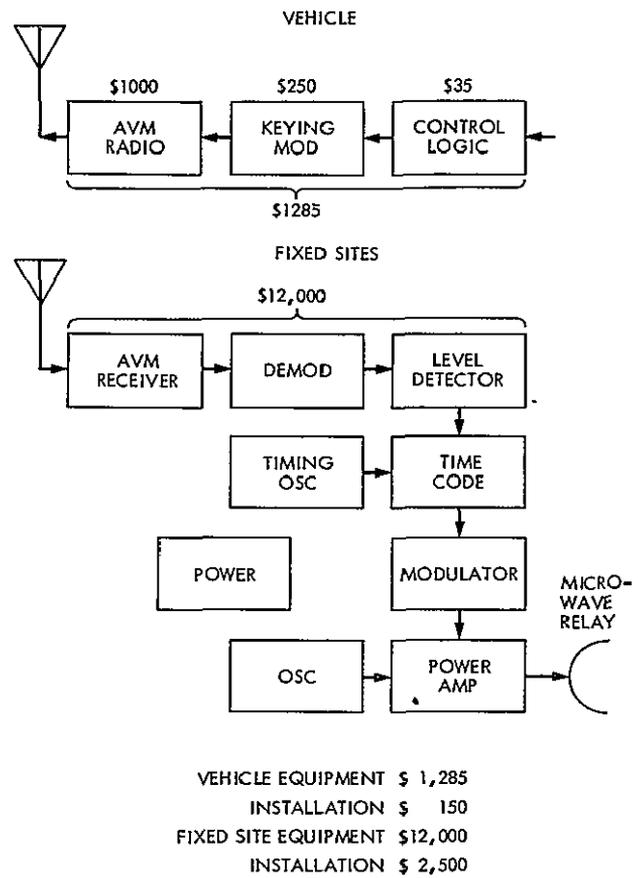


Fig. 1-26. Class III AVM Pulse TOA Fixed Site Trilateration

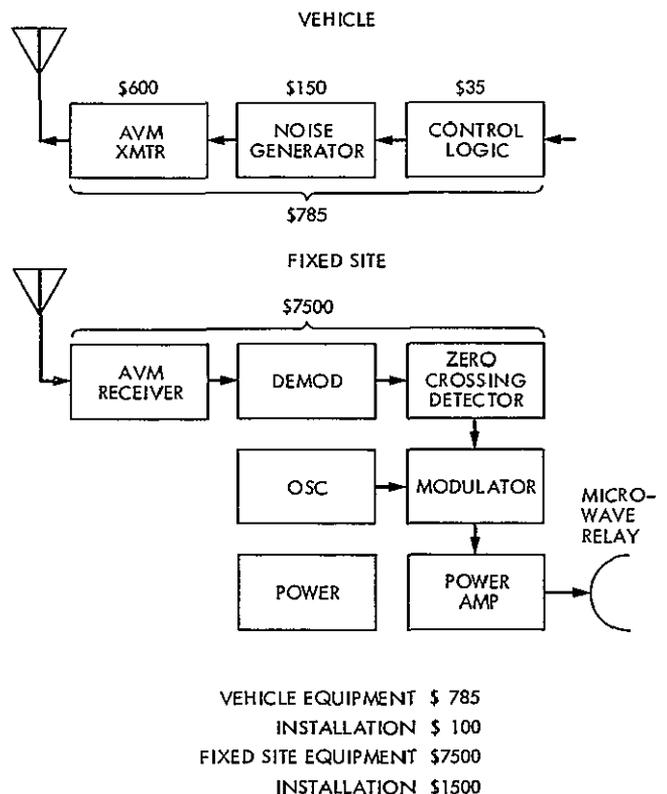


Fig. 1-27. Class III AVM Noise Correlation TOA Trilateration

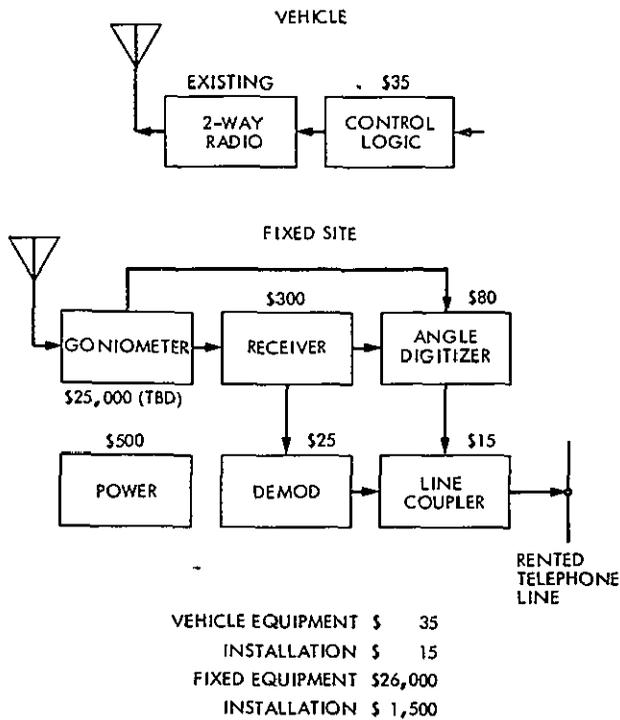


Fig. 1-28. Class III AVM Direction Finding from Special RF Sites

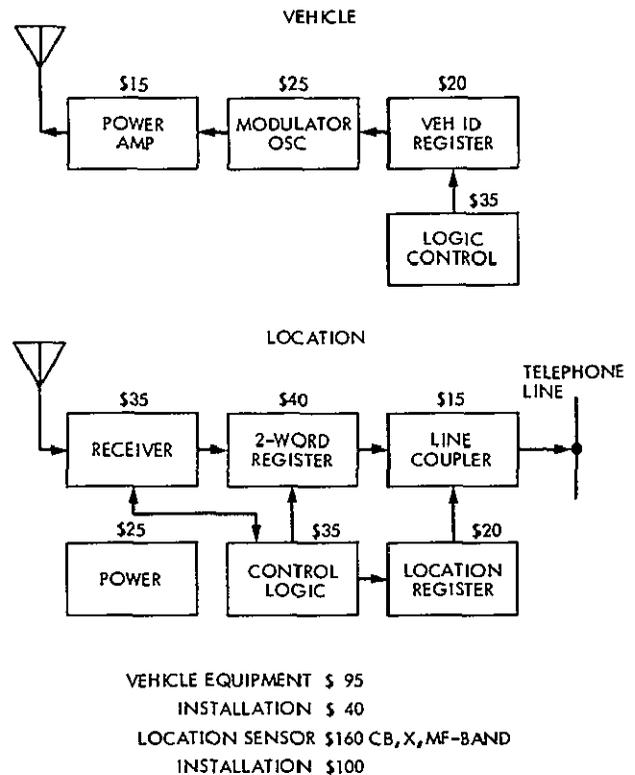


Fig. 1-29. Class IV AVM Monitored Wayside Radio Receivers

E. Class IV AVM, Monitored Signposts Throughout Urban Area

This class of AVM techniques is an inversion of the Class II autonomous wayside or buried signposts and removes the data collection link responsibility from the vehicle. In Class IV AVM, a vehicle-to-signpost link (Fig. 1-29) is maintained, but the information flow is the vehicle's identity to the monitored signpost. The data link to the base station or central collection point is based either on telephone lines rented from the local utility or on call-box lines for police and fire use. Since individual lines from each signpost are usually not considered economically practical, it is usually proposed to group the signposts on "party lines". The "party line" approach requires that each signpost not only transmit the vehicle ID data received but also identify itself to the central collection point at the base station. The telephone line is an additional complication to the Class IV installation, and a prime power connection is still required.

A technique of using the buried loop-sensors, which actuate traffic signals, as receiving antennas (Fig. 1-30) can be used in the monitored Class IV as in the autonomous Class II signpost method. This is an especially attractive approach if the signals are centrally controlled because dedicated communication lines are usually already installed. Ultrasonic as well as photo/IR detectors could also be used on monitored signposts (Figs. 1-31, 1-32).

In Class IV, the vehicle polling function is replaced either by line-finding, as is used in normal telephone service, or by a continual scanning of the lines to find an "off hook" indication that a signpost on one of the party lines has information to forward.

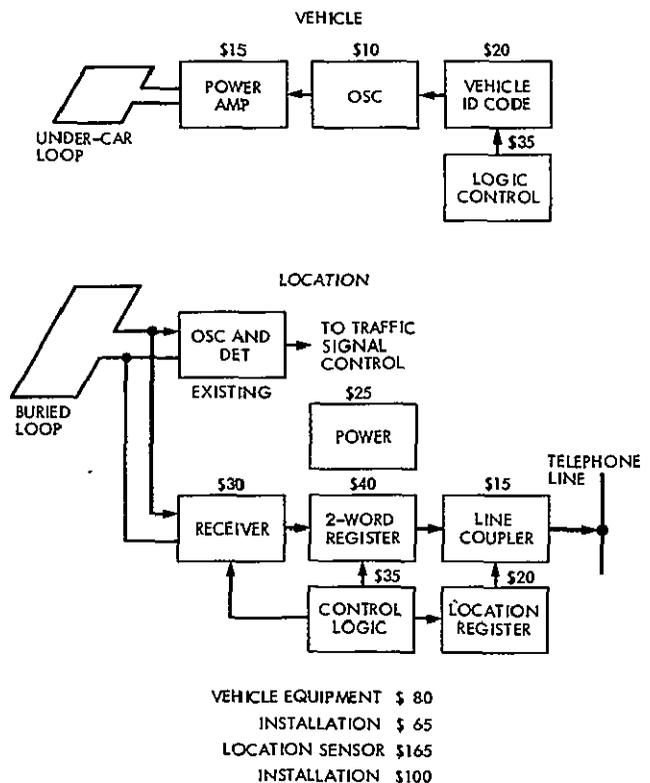


Fig. 1-30. Class IV AVM Monitored Traffic Presence Sensors

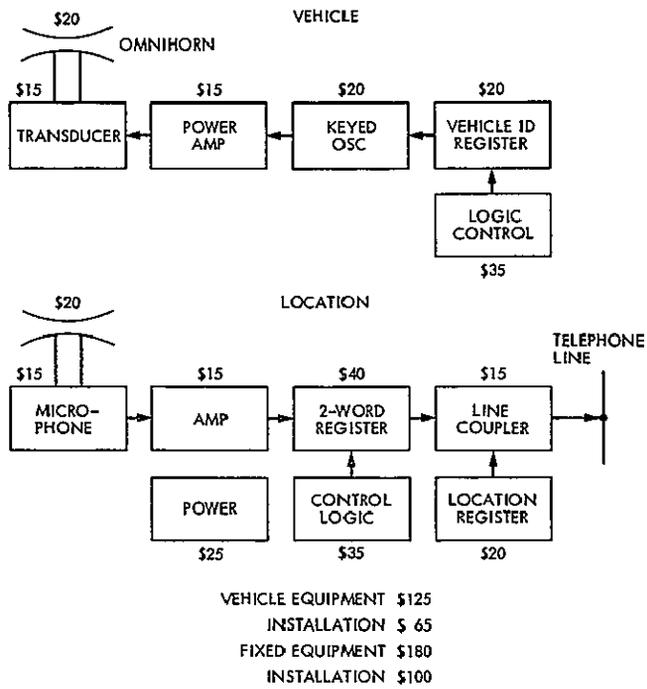


Fig. 1-31. Class IV AVM Monitored Ultrasonic Wave Receptors

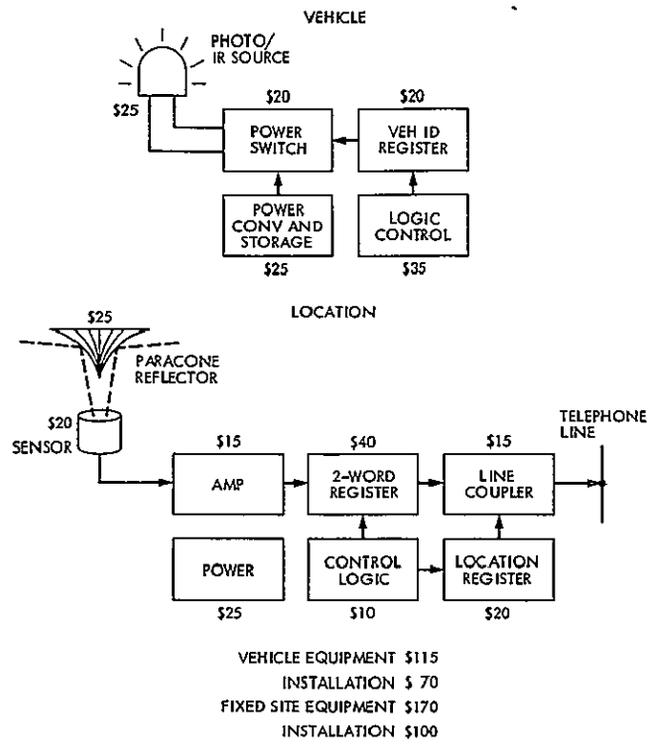


Fig. 1-32. Class IV AVM Monitored Photo or IR Detectors

II. VEHICLE POLLING AND LOCATION PERFORMANCE

A. Vehicle Polling Techniques and Costs

Four general classes of vehicle polling are considered for AVM Systems: (1) Synchronous, (2) Commanded or random access, (3) Synchronous with command capability, and (4) Volunteer or contention. All four techniques are generally applicable to Class I and II AVM systems. Synchronous polling and synchronous with command are used mainly in Class III AVM systems with sparsely distributed special signposts. Volunteer polling is usually considered only for low-density Class II autonomous signpost systems. For the Class IV monitored signpost systems which use land-lines, vehicle polling by radio is not applicable in the context used here.

All of the polling techniques are suitable for half-duplex (base station and vehicle on the same frequency), but when the base station relays all vehicle transmissions or when each vehicle monitors all other vehicles, then volunteer polling can only be used on full-duplex (base and vehicle on different frequencies).

In Class I and II AVM systems where the currently installed 2-way radio is to be used for AVM purposes, speed-up modifications are required. These changes to antenna switching, transmitter stabilization time, and squelch delay are necessary to reduce the substantial guard time required between transmissions from vehicles adjacent in the polling sequence or to reduce the transition time interval from receive to transmit in Commanded or random access polling.

A modification of the Volunteer polling method only allows location data to be transmitted as a precursor or brief interruption of voice transmissions, but this technique has limited application. Interrupted speech as a technique in other polling methods relies on very short transmit on-off-on sequences for a vehicle currently using voice when another vehicle responds with data.

1. Synchronous polling. In this technique, each vehicle transmits location data at a pre-selected time within the polling sequence. The equipment on the vehicle keeps track of the start of the polling sequence and internally determines when the appropriate time to respond occurs. The functional elements of Synchronous polling are shown in Fig. 1-33. The fact that the start of the polling sequence must be periodically transmitted to each vehicle for correction purposes leads to the capability of the base station to modify the time when the vehicles are to respond in the polling epoch.

2. Synchronous with command capability. This technique allows the base station to modify the position of each vehicle in the polling sequence. The additional functional elements for the command option are shown in Fig. 1-34 connected by dashed lines to the elements required for synchronous polling.

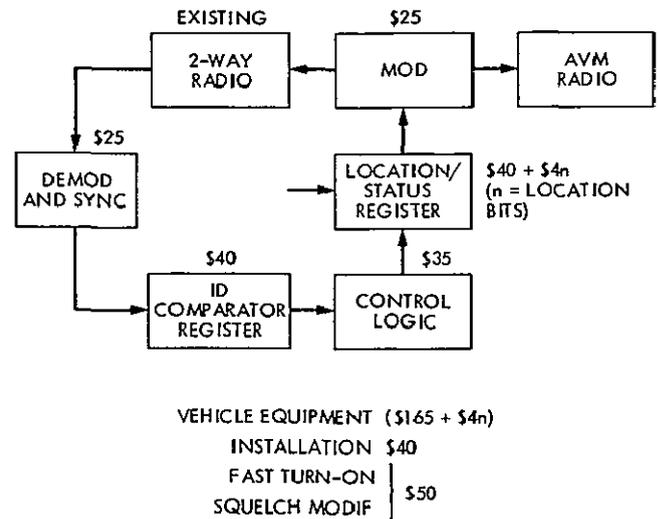


Fig. 1-33. Vehicle Synchronized Polling for AVM Classes I, II, III

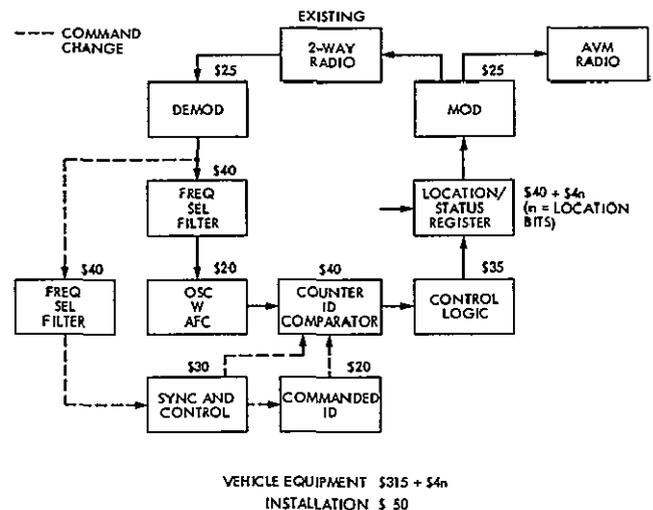


Fig. 1-34. Vehicle Commanded Polling for AVM Classes I, II, III.

3. Commanded or random access polling. Commanded polling requires that the base station send a request to each vehicle whenever location data is required. This random access technique is the most flexible but requires substantially more use of available RF time than the synchronous method or the synchronous with command capability. The elements required for the commanded polling method are shown in Fig. 1-34.

4. Volunteer polling. This contention method of sending location data requires that each vehicle determine if the channel is "clear" before transmitting. A mechanization is shown in Fig. 1-35. Some technique of providing a random delay in each vehicle after determining that the channel is clear and before transmitting is usually necessary

to preclude certain vehicles from dominating the channel.

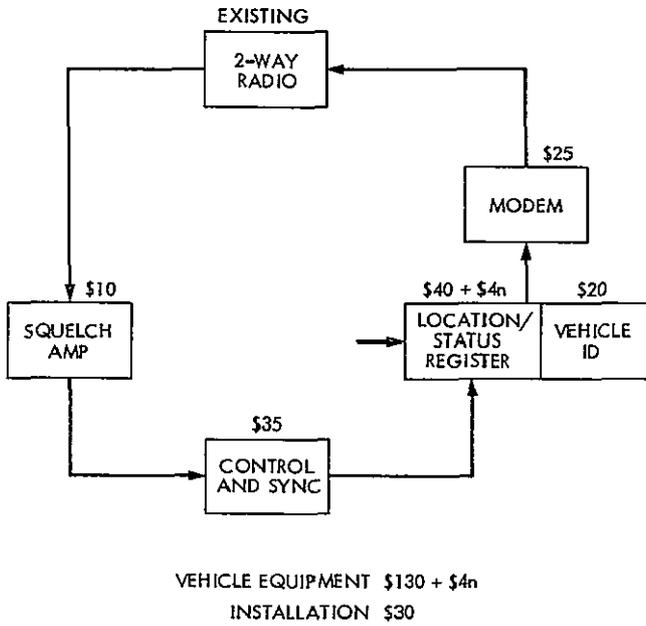


Fig. 1-35. Vehicle Volunteer Polling for AVM Class II Systems

B. Vehicle Polling and RF Link Evaluations

The three vehicle polling techniques: Synchronous (SYN), Volunteer (VOL), and Random (RAND) or commanded were evaluated with both a simple one-time radio message transmission and with redundant transmission, where every message is sent twice. In all cases, the digital message rate is set at 1500 bps. Where equivalent RF channels are assumed, a channel spacing of 25 kHz is used.

Any delays in the polling processes will tend to reduce the number of vehicles which can be accommodated by an RF channel. Therefore all of the delays are lumped into one parameter called turn-on time. Thirty two of the Class I, II and III AVM techniques were evaluated in both the simple and redundant modes of the three polling methods. The range of turn-on times examined was from 0 to 0.3 second, in five steps. This range is sufficient to estimate the performance of full-duplex radios with separate antenna circuits relative to half-duplex with electro-mechanical antenna transfer relays. Tables 1-1 through 1-5 are compilations of the vehicles polled per second per RF channel. Each table includes a theoretical maximum entry which is the 1500 bps rate divided by the number of bits in the location message. Included under Class II techniques are small and large entries as the location message length is a function of the number of instrumented intersections, therefore data are provided for both small and large urban areas. Since the Class III techniques in general are not amenable to volunteer (VOL) polling methods, no VOL calculations were made for this class. Also, with the exception of direction finding and narrow-band phase location, transponder type radio equipment is required which does not have the same order of delays.

Table 1-1. Vehicles Polled/Second/RF Channel For 0 Sec Turn-On

TECHNIQUE	THEO MAX	CAPS PER SECOND PER RF CHANNEL WITH DIFFERENT POLLING		
		SYN	VOL	RAND
CLASS I				
KEYBOARD	137	137	72	72
STYLUS MAP	84	84	54	54
2-ACCELEROMETERS	108	108	63	63
LASEP VELOCINTP	44	44	58	58
ULTRASONIC VELO	108	108	63	63
COMPASS/ODOMETER	108	108	63	63
COMPASS/LASEP VEL	108	108	63	63
COMPASS/U-SONIC VEL	108	108	63	63
OECCA	56	56	41	41
LORAN	47	47	36	36
DECCA	50	50	38	38
AM-STATIONS	125	125	69	69
DIFF OECCA	56	56	41	41
DIFF LORAN	47	47	36	36
DIFF AM-STA	50	50	42	42
RELAY OECCA	1	1	1	1
RELAY LORAN	3	3	3	3

TECHNIQUE	THEO MAX	CAPS PER SECOND PER RF CHANNEL WITH DIFFERENT POLLING		
		SYN	VOL	RAND
CLASS II				
BURIED RES LOOPS	150	150	108	108
REFLECTING SIGNS	150	150	108	108
REFLECTING ROAD	150	150	108	108
X-BAND POST	167	167	116	116
HF, VHF POST	215	215	137	137
LF POST	167	167	116	116
LIGHT/I-P POST	167	167	116	116
BURIED MAGNETS	150	150	108	108
ULTRASONIC POST	167	167	116	116
TRAFFIC SENSOR	150	150	108	108

TECHNIQUE	MIN RF CHANNELS	CAPS PER SECOND		
		SYN	VOL	RAND
CLASS III				
NAR-BAND FM PHASE	1	67	47	47
MID-BAND FM PHASE	4	400	110	110
PULSE T-O-ARRIVAL	400	10000	10000	10000
NOISE CORRELATION	200	1000	1000	1000
DIRECTION FINDER	1	5	5	5

Table 1-2. Vehicles Polled/Second/RF Channel For 0.01-Sec Turn-On

TECHNIQUE	THEO MAX	CAPS PER SECOND PER RF CHANNEL WITH DIFFERENT POLLING		
		SYN	VOL	RAND
CLASS I				
KEYBOARD	137	137	72	72
STYLUS MAP	84	84	54	54
2-ACCELEROMETERS	108	108	63	63
LASER VELOCINTP	44	44	58	58
ULTRASONIC VELO	108	108	63	63
COMPASS/ODOMETER	108	108	63	63
COMPASS/LASEP VEL	108	108	63	63
COMPASS/U-SONIC VEL	108	108	63	63
OECCA	56	56	41	41
LORAN	47	47	36	36
DECCA	50	50	38	38
AM-STATIONS	125	125	69	69
DIFF OECCA	56	56	41	41
DIFF LORAN	47	47	36	36
DIFF AM-STA	50	50	42	42
RELAY OECCA	1	1	1	1
RELAY LORAN	3	3	3	3

TECHNIQUE	THEO MAX	CAPS PER SECOND PER RF CHANNEL WITH DIFFERENT POLLING		
		SYN	VOL	RAND
CLASS II				
BURIED RES LOOPS	150	150	108	108
REFLECTING SIGNS	150	150	108	108
REFLECTING ROAD	150	150	108	108
X-BAND POST	167	167	116	116
HF, VHF POST	215	215	137	137
LF POST	167	167	116	116
LIGHT/I-P POST	167	167	116	116
BURIED MAGNETS	150	150	108	108
ULTRASONIC POST	167	167	116	116
TRAFFIC SENSOR	150	150	108	108

TECHNIQUE	MIN RF CHANNELS	CAPS PER SECOND		
		SYN	VOL	RAND
CLASS III				
NAR-BAND FM PHASE	1	40	32	32
MID-BAND FM PHASE	4	30	50	50
PULSE T-O-ARRIVAL	400	10000	10000	10000
NOISE CORRELATION	200	1000	1000	1000
DIRECTION FINDER	1	5	5	5

Table 1-3. Vehicles Polled/Second/RF Channel For 0.03-Sec Turn-On

TECHNIQUE	CARS PER SECOND			CHANNEL WITH DIFFERENT POLLING		
	THEO MAX	SYN SH/LG	RAID SH/LG	SYN SH/LG	RAID SH/LG	RAID SH/LG
CLASS I						
VEHBOARD	137	17	13	17	13	13
STYLUS MAP	34	2	13	19	17	17
ACCELEROMETERS	100	10	14	21	17	17
LASER VELOCIMTR	24	10	15	20	16	17
ULTRASONIC VELO	100	10	14	21	17	17
COMPASS/ODOMETEP	100	10	14	21	17	17
COMPASS/LASER VEL	100	10	14	21	17	17
COMPASS/UL-SONIC VEL	100	10	14	21	17	17
ONEGA	56	21	12	16	13	13
LOPAH	47	20	12	16	13	13
DECCA	50	20	12	16	13	13
HI-STATIONS	125	27	14	22	17	17
DIFF ONEGA	56	21	12	16	13	13
DIFF LOPAH	47	20	12	16	13	13
DIFF HI-STA	56	22	12	16	13	13
RELAY ONEGA	1	1	1	1	1	1
RELAY LOPAH	3	3	3	2	2	2

Table 1-5. Vehicles Polled/Second/RF Channel For 0.3 Sec Turn-On

TECHNIQUE	CARS PER SECOND			CHANNEL WITH DIFFERENT POLLING		
	THEO MAX	SYN SH/LG	RAID SH/LG	SYN SH/LG	RAID SH/LG	RAID SH/LG
CLASS I						
VEHBOARD	137	17	13	17	13	13
STYLUS MAP	34	2	13	19	17	17
ACCELEROMETERS	100	10	14	21	17	17
LASER VELOCIMTR	24	10	15	20	16	17
ULTRASONIC VELO	100	10	14	21	17	17
COMPASS/ODOMETEP	100	10	14	21	17	17
COMPASS/LASER VEL	100	10	14	21	17	17
COMPASS/UL-SONIC VEL	100	10	14	21	17	17
ONEGA	56	21	12	16	13	13
LOPAH	47	20	12	16	13	13
DECCA	50	20	12	16	13	13
HI-STATIONS	125	27	14	22	17	17
DIFF ONEGA	56	21	12	16	13	13
DIFF LOPAH	47	20	12	16	13	13
DIFF HI-STA	56	22	12	16	13	13
RELAY ONEGA	1	1	1	1	1	1
RELAY LOPAH	3	3	3	2	2	2

TECHNIQUE	CARS PER SECOND			CHANNEL WITH DIFFERENT POLLING		
	THEO MAX	SYN SH/LG	RAID SH/LG	SYN SH/LG	RAID SH/LG	RAID SH/LG
CLASS II						
BURIED RES LOOPS	150	28	26	24	21	21
REFLECTING SIGNS	150	28	26	24	21	21
REFLECTING ROAD	150	28	26	24	21	21
W-BAND POST	167	28	26	24	21	21
HF, VHF POST	215	24	27	26	23	23
LF POST	167	28	26	24	21	21
LIGHT/I-R POST	167	28	26	24	21	21
BURIED MAGNETS	150	28	26	24	21	21
ULTRASONIC POST	167	28	26	24	21	21
TRAFFIC SENSOR	150	28	26	24	21	21

TECHNIQUE	CARS PER SECOND			CHANNEL WITH DIFFERENT POLLING		
	THEO MAX	SYN SH/LG	RAID SH/LG	SYN SH/LG	RAID SH/LG	RAID SH/LG
CLASS II						
BURIED RES LOOPS	150	28	26	24	21	21
REFLECTING SIGNS	150	28	26	24	21	21
REFLECTING ROAD	150	28	26	24	21	21
W-BAND POST	167	28	26	24	21	21
HF, VHF POST	215	24	27	26	23	23
LF POST	167	28	26	24	21	21
LIGHT/I-R POST	167	28	26	24	21	21
BURIED MAGNETS	150	28	26	24	21	21
ULTRASONIC POST	167	28	26	24	21	21
TRAFFIC SENSOR	150	28	26	24	21	21

TECHNIQUE	CARS PER SECOND			REDUNDANT	
	MIN CHANNELS	SYN SH/LG	RAID SH/LG	SYN SH/LG	RAID SH/LG
CLASS III					
NAP-BAND FM PHASE	1	23	20	17	17
W-BAND FM PHASE	4	31	26	29	29
PULSE T-O-ARRIVAL	400	10000	10000	10000	10000
NOISE CORRELATION	200	1000	1000	1000	1000
DIRECTION FINDER	1	5	5	3	3

TECHNIQUE	CARS PER SECOND			REDUNDANT	
	MIN CHANNELS	SYN SH/LG	RAID SH/LG	SYN SH/LG	RAID SH/LG
CLASS III					
NAP-BAND FM PHASE	1	23	20	17	17
W-BAND FM PHASE	4	31	26	29	29
PULSE T-O-ARRIVAL	400	10000	10000	10000	10000
NOISE CORRELATION	200	1000	1000	1000	1000
DIRECTION FINDER	1	5	5	3	3

Table 1-4. Vehicles Polled/Second/RF Channel For 0.1-Sec Turn-On

TECHNIQUE	CARS PER SECOND			CHANNEL WITH DIFFERENT POLLING		
	THEO MAX	SYN SH/LG	RAID SH/LG	SYN SH/LG	RAID SH/LG	RAID SH/LG
CLASS I						
VEHBOARD	137	17	13	17	13	13
STYLUS MAP	34	2	13	19	17	17
ACCELEROMETERS	100	10	14	21	17	17
LASER VELOCIMTR	24	10	15	20	16	17
ULTRASONIC VELO	100	10	14	21	17	17
COMPASS/ODOMETEP	100	10	14	21	17	17
COMPASS/LASER VEL	100	10	14	21	17	17
COMPASS/UL-SONIC VEL	100	10	14	21	17	17
ONEGA	56	21	12	16	13	13
LOPAH	47	20	12	16	13	13
DECCA	50	20	12	16	13	13
HI-STATIONS	125	27	14	22	17	17
DIFF ONEGA	56	21	12	16	13	13
DIFF LOPAH	47	20	12	16	13	13
DIFF HI-STA	56	22	12	16	13	13
RELAY ONEGA	1	1	1	1	1	1
RELAY LOPAH	3	3	3	2	2	2

Message lengths of most vehicle polling techniques are about 20 bits or occupy about 15 milliseconds or less of transmission time at the selected bit rate. Turn-on times of this order will therefore reduce the achievable polling rate to less than half the theoretical value. Turn-on times quickly dominate the polling rates at values above 0.03 second.

Class IV AVM systems, with monitored signposts, do not require radio polling. The vehicle polling function is replaced either by line finding, as is used in "normal" telephone service, or by a continual scanning of "party lines" to find an "off-hook" indication on one of the party lines that one of a group of signposts has some information to forward regarding the ID of a fleet vehicle that is passing its vicinity.

C. Location Performance Parameters

Several technical performance parameters of individual vehicle location techniques, including accuracy, quantity of location data, and fix time, affect both the design and expected performance of complete AVM systems. Accuracy of the location information is the parameter which usually elicits the most interest. This ultimate achievable accuracy for a given technique is, however, almost always degraded when the technique is configured into an AVM system. The reduction in location accuracy is caused by the vehicle's motion, the delay in vehicle-to-base transmission, the computer processing time to relate the vehicle data received to a physical location, and

the delay in displaying the location on a map or other computer output device. In dead-reckoning systems, the location error is cumulative, and the accuracy is proportioned to a percentage of the distance travelled (% dist).

The amount of location data which must be sent to or from the vehicle is another parameter that affects performance. Not only is it a function of the location technique, but also of the number of vehicles in the system, the area of the urban coverage, the density of streets or intersections in the area, and the dimensions of the urban area in each direction. The quantity of location data, together with the polling technique used and the availability of RF channels, determines the delays in receiving vehicle data at the base, which in turn affects the AVM system accuracy.

Another parameter is the "fix" time required for the vehicle to receive or generate whatever raw data is required for the new location to be determined elsewhere, which is primarily technique dependent. Similarly the interval between successive messages from the vehicle is also technique dependent. That is, no new location information will be forthcoming until a definite time period or travelled distance has elapsed or has been accumulated.

A tabular compilation of four location performance characteristics has been developed from several sources such as test data, prototype demonstrations, and performance estimates by both system developers and other evaluators. In Table 1-6, the performance values for the location accuracy or radius, the amount of location data, and the fix time parameters are listed for the four AVM classes and 36 systems. An explanation of each parameter follows:

1. Accuracy. This tabular entry represents either the estimated or test-result accuracy of vehicle location for Class I and Class III AVM systems. Since the accuracy cannot always be stated as a single value, a range of values is given in some cases. In the case of Class II and IV signpost systems, the term accuracy is inappropriate, and the term radius is used.

2. Radius. In Class II, III, and IV AVM systems, this radius figure represents the estimated coverage of the individual signpost or the special purpose fixed site.

3. Fix time. This value is the time in seconds required for the vehicle to receive or generate new location data. In Class I AVM systems, the fix time is determined by the updating rate of the vehicle sensors or the repetition rate of the navigational aid. In Class II or IV systems, the fix time is a comparative number only and represents the time interval required such that a vehicle near the signpost will receive at least two location messages while moving at a speed of 50 m/sec (113 mph). In Class III systems, the fix time represents only the time of transmission of a location signal from the vehicle to the special RF site.

4. Location data. This tabulated number represents the minimum quantity of raw data required to locate an individual vehicle. In Class I AVM dead-reckoning methods, the location data figure is the combined number of bits required to represent a change in vehicle position to the indicated accuracy. In Class I navigational aids, the figure is either the number of bits required to indicate the time or phase differences of the received signals or the actual RF bandwidth (BW) required in the relay systems. In Class II or IV AVM systems, the location data value is the number of bits required to uniquely identify each signpost or each vehicle, respectively. The Class III location data is the RF bandwidth required for the tone, pulse, or noise location signal.

III. URBAN CHARACTERISTICS THAT AFFECT AVM COSTS

A. City Model Parameters For AVM System Design

In order to develop a basis for AVM System cost comparisons, it was necessary to establish baseline system design parameters applicable to each technique. To make these designs somewhat realistic, three model cities were developed, based on the populations and physical parameters of the seven representative UGAC cities in Southern California. Characteristics of the small, medium, and large model city are given in Table 1-7. The justification or rationalization for the model city parameters and the other factors considered in the system design are as follows:

1. City Shape. One characteristic of the model cities that is difficult to justify is shape. In this Report, the assumption is made that the cities are rectangular with a 2-to-1 aspect ratio. The development of most cities either along a river, railway, or coastal harbor usually results in one dimension being significantly greater than the other. The choice of a rectangle is believed to be more realistic than the square or circular city sometimes chosen.

2. Urban area. The areas chosen for the three city models are 10, 100, and 1000 km² (4, 40, and 400 mi²), which compare with Montclair and Monterey Park as the smallest cities, Anaheim, Pasadena, and Long Beach as the medium cities, and Los Angeles and San Diego as the large cities. (See Part Two of this Report, p. 2-1.)

3. Population. The populations of the model cities are based on population densities in the actual cities, which average 3000 people per square kilometer (7800/mi²).

4. Vehicle fleet size. Two classifications of vehicles are assumed for each city. These are the patrolling vehicles and the total number of instrumented vehicles. An assumption is made that one-half the fleet is patrolling while the remainder is involved in investigation.

Table 1-6. Location Performance Parameters for All AVM Classes and Systems

Technique	Accuracy or Radius	Value used, (m)	Location Data, bits or BW	Fix Time, sec
CLASS I AVM				
	Accuracy			
Keyboard update	10-100 m	(33)	6-20 bits	2-5 s
Stylus map update	30 m	(30)	14-20	3
2-Accelerometers	2% dist	(34)	14	0.3
Laser velocimtr	0.5% dist	(13)	16	0.3
Ultrasonic velo	3% dist	(40)	14	0.3
Compass/odometer	1% dist	(20)	14	0.3
Compass/laser vel	0.6% dist	(15)	14	0.3
Cmpss/u-sonic vel	0.8% dist	(17)	14	0.3
OMEGA navigation	1600 m	(1600)	27	3-10
LORAN navigation	0.4 m/km	(160)	32	0.06-.2
DECCA navigation	0.5 m/km	(200)	30	0
AM-Stations nav	150-250 m	(200)	12	0-3
Diff OMEGA nav	160 m	(160)	27	3-10
Diff LORAN nav	120-400 m	(400)	32	0.06-.2
Diff AM-Stations	150-250 m	(250)	21-32	0-3
Relay OMEGA nav	200-600 m	(500)	3 kHz BW	3-10
Relay LORAN nav	800 m	(800)	10 kHz BW	0.06-.2
CLASS II AVM				
	Radius m			
Buried res loops	10	—	10-18 bits	1-2 s
Reflecting signs	10	—	10-18	1-2
Reflecting road	3	—	10-18	1-2
X-Band signposts	12-100	—	9-17	1-2
HF, VHF signpost	15-100	—	7-15	2-5
LF Signposts	100	—	9-17	1-2
Light/IR post	30	—	9-17	1-2
Buried magnets	10	—	10-18	1-2
Ultrasonic post	20	—	9-17	1-2
Traffic sensor	10	—	10-18	1-2
CLASS III AVM				
	Accuracy			
Nar-band FM phase	800-1300 m	(1000)	3 kHz BW	0.015 s
Wid-band FM phase	1000-1500	(1200)	15-40 kHz	0.01
Pulse T-O-Arrival	100 m	(100)	10 MHz	0.0001
Noise correlation	100 m	(100)	5-10 MHz	0.001
Direction finder	3% dist	(700)	3 kHz	0.2-1
CLASS IV AVM				
	Radius, m			
Traffic loops	10	—	N/A	1-2 s
Wayside radio	100	—	N/A	1-2
Photo/IR detect	30	—	N/A	1-2
Ultrasonic detect	20	—	N/A	1-2

Table 1-7. Model City Parameters That Affect AVM Costs

Parameter	Small	Medium	Large
Area, km ²	10	100	1000
Dimensions, km	2.2 × 4.5	7.1 × 14.2	22.3 × 44.7
Vehicles, patrol/total	5/10	50/100	500/1000
Intersections*	350	3500	35000
Road segments × lanes	1600	16800	168000
Road distance, km	125	1245	12450
Telephone lines, km	83	828	8275
Population	30,000	300,000	3,000,000

*Based on 25/75% ratio of 50/30 blocks/km² in the urban area.

5. Intersections. The number of intersections in each city is based on two business area street densities. They are based on actual measurements of randomly selected areas of the UGAC cities, and the values assumed are 30/km² for 75% of the area and 50/km² for 25% of the area.

6. Road distance. For the purposes of the models, the blocks are assumed to have the same aspect ratio as the city, namely 2:1, and to be in a regular array. An average of 2.4 lanes for each road segment was assumed, based on UGAC city averages.

7. Telephone line distance. Class IV AVM systems require land line monitoring; and for the purposes of comparison, an equal division of sensors is assumed of up to a maximum of 100 sensors for each phone "party" line. These party lines are assumed to parallel the long streets so that the total mileage of lines is about two-thirds of the total road distance.

8. Building distribution and topography. A uniform low-rise building distribution is assumed for location accuracy comparison purposes. The topography of the model cities is assumed to be essentially flat without "blind" radio areas or special areas that might unduly affect any particular technique.

9. Radio. The only information sent from the vehicle in this comparison is that required for location, either as a binary message or equivalent RF bandwidth for the Class I, II, and III systems. Radio modifications are also assumed to enable automatic message transmission. Additionally, transmitter turn-on stabilization time, squelch delay, and antenna transfer are assumed constant at several values.

10. Model city AVM cost and performance summaries. Tables 1-8 through 1-16 summarize the AVM system costs in each of three model cities, small, medium, and large, for each of thirty six location techniques and for three polling methods.

a. Small city summary. The costs of all AVM techniques in the small city model are dominated by the operation-and-maintenance (O-M) cost with the result that there is a great similarity in total costs regardless of the vehicle location technique. The Class II and IV system costs are higher because the signposts and the associated costs are relatively greater than the vehicle costs (see Tables 1-8, 1-9, 1-10).

b. Medium city summary. The costs of AVM Class I in the medium city model show an increase which is almost all due to vehicular equipment. The Class II costs increase by a greater factor due again to signposts. The site costs of the buried resonant loops are substantially higher than those of any other Class II technique because of installation costs. The more sparsely distributed RF posts, either HF or VHF, do not impact the total cost to the extent of the techniques which use a post at each intersection. In the Class III techniques that require pulse or wideband equipment, the vehicular equipment accounts for about one-third the total cost.

In Class IV techniques, the telephone line rental which is included in the site cost is the primary cost factor (see Tables 1-11, 1-12, 1-13).

c. Large city summary. The AVM costs in the large model city show the same trend with Class II techniques (save for two exceptions) costing some 2 to 4 times the Class I techniques and about twice the cost of Class III systems. The Class II techniques systems costs are reducible by less dense placement of posts (see Tables 1-14, 1-15, 1-16).

The method of vehicle polling has only a slight impact on AVM system costs in any of the techniques in any of the model cities. Applications of the AVM cost analysis to actual cities in Southern California are presented in Part Two of this Report (p. 2-1).

B. Small Model City AVM Cost Summary Tables

Table-1-8. Small Model City Parameters Used in AVM Cost Analysis

AREA IS 4 SQUARE MILES.

EAST WEST DISTANCE IS 1.4 MILES.

NORTH SOUTH DISTANCE IS 2.3 MILES.

TOTAL ROAD MILEAGE IS 77 MILES.

THE NUMBER OF INTERSECTIONS IS 350.

THE ESTIMATED NUMBER OF ROAD SEGMENTS IS 700.

THERE ARE 10 CARS IN THE FLEET

AND THERE ARE 0 MOTORCYCLES.

THE NUMBER OF VEHICLES ON EACH SHIFT IS:

FIRST SHIFT MAX. 5

FIRST SHIFT MIN. 5

SECOND SHIFT MAX. 5

SECOND SHIFT MIN. 5

THIRD SHIFT MAX. 5

THIRD SHIFT MIN. 5

THE CITY WOULD REQUIRE 4 WIDE-BAND OR

PULSE T-O-A ANTENNA SITES AND 6 NARROW

BAND ANTENNA SITES WITH 7 AND 3 MILE COVERAGE RADIUS.

Table 1-9. Small Model City
AVM Cost Summary

SMALL MODEL CITY CLASS I	TECHNIQUE	CARS	THOUSANDS OF \$				TOTALS			
			SITES	BASE	INST	O-H	UOL	SVNC	RANDOM	
KEYBOARD	2	0	44	11	101	153	156	156		
STYLUS MAP	26	0	44	11	101	182	181	181		
2-ACCELEROMETERS	16	0	68	11	101	198	200	200		
LASEP VELOCIMTR	18	0	69	12	102	202	204	203		
ULTRASONIC VELO	13	0	69	11	102	196	198	198		
COMPASS/ODMETER	15	0	69	11	101	196	194	193		
COMPASS/LASEP VEL	19	0	69	12	101	202	204	203		
CHPSS-U-SONIC VEL	16	0	69	11	101	194	191	190		
ONEGA	27	0	54	11	101	195	197	197		
LOPAN	28	0	54	11	101	196	198	198		
DECCA	12	0	54	11	101	174	172	171		
AM-STATIONS	4	0	54	11	101	171	173	173		
DIFF ONEGA	27	0	54	11	101	195	197	197		
DIFF LOPAN	28	0	54	11	101	196	198	198		
DIFF AM-STA	5	0	54	11	101	172	174	175		
RELAY ONEGA	6	0	54	11	101	173	172	172		
RELAY LOPAN	6	0	54	11	101	174	172	176		
CLASS II										
BURIED PES LOOPS	4	168	44	297	101	612	610	610		
REFLECTING SIGNS	5	77	44	54	100	269	270	267		
REFLECTING ROAD	2	81	44	61	143	259	260	257		
W-SOLID POST	2	91	44	27	106	260	261	258		
HF, UHF POST	2	91	44	15	102	172	173	171		
LF POST	2	91	44	27	106	223	224	221		
LIGHT/I-R POST	2	35	44	30	100	322	322	320		
BURIED MAGNETS	1	17	44	45	100	303	303	306		
ULTRASONIC POST	2	67	44	71	108	265	265	263		
TRAFFIC SENSOR	2	67	44	59	101	253	253	251		
CLASS III										
NAR-BAND FM PHASE	3	29	57	12	104	203	205	205		
MID-BAND FM PHASE	30	47	69	17	203	364	367	367		
PULSE T-O-ARRIVAL	26	84	139	27	179	454	456	457		
NOISE CORRELATION	8	29	139	16	177	370	371	371		
DIRECTION FINDER	1	79	34	15	154	282	281	281		
CLASS IV										
TRAFFIC LOOPS	1	204	44	106	109	462	462	460		
INSIDE RADIO	1	170	44	70	118	422	422	424		
PHOTO-I-R DETECT	1	2	44	51	109	309	309	303		
ULTRASONIC DETECT	2	103	44	51	109	307	307	307		

C. Medium Model City AVM Cost Summary Tables

Table 1-11. Medium Model City Parameters
Used in AVM Cost Analysis

AREA IS 40 SQUARE MILES.
 EAST WEST DISTANCE IS 4.41 MILES.
 NORTH SOUTH DISTANCE IS 6.62 MILES.
 TOTAL ROAD MILEAGE IS 774 MILES.
 THE NUMBER OF INTERSECTIONS IS 3500.
 THE ESTIMATED NUMBER OF ROAD SEGMENTS IS 7000.
 THERE ARE 100 CARS IN THE FLEET
 AND THERE ARE 0 MOTORCYCLES.
 THE NUMBER OF VEHICLES ON EACH SHIFT IS:

FIRST SHIFT MAX. 50

FIRST SHIFT MIN. 50

SECOND SHIFT MAX. 50

SECOND SHIFT MIN. 50

THIRD SHIFT MAX. 50

THIRD SHIFT MIN. 50

THE CITY WOULD REQUIRE 5 WIDE-BAND OF
 PULSE T-O-A ANTENNA SITES AND 10 NARROW

BAND ANTENNA SITES WITH 7 AND 5 MILE COVERAGE RADII.

Table 1-12. Medium Model City AVM Cost Summary

MEDIUM MODEL CITY, CLASS I	TECHNIQUE	CAPS	THOUSANDS OF \$				TOTALS			
			SITES	BASE	INST	O-H	UOL	SVNC	RANDOM	
KEYBOARD	1	0	67	11	102	152	152	156	136	
STYLUS MAP	255	0	67	11	100	184	184	181	136	
2-ACCELEROMETERS	160	0	92	20	110	302	302	302	136	
LASEP VELOCIMTR	173	0	102	24	115	355	355	350	136	
ULTRASONIC VELO	127	0	102	20	113	300	300	305	136	
COMPASS/ODMETER	147	0	102	12	104	291	291	295	136	
COMPASS/LASEP VEL	186	0	102	25	100	429	429	425	136	
CHPSS-U-SONIC VEL	159	0	102	20	109	366	366	368	136	
ONEGA	270	0	67	18	108	499	525	519	136	
LOPAN	200	0	67	10	100	504	525	531	136	
DECCA	115	0	67	16	100	342	368	363	136	
AM-STATIONS	40	0	67	15	106	264	283	279	136	
DIFF ONEGA	270	0	67	18	108	499	518	519	136	
DIFF LOPAN	200	0	67	10	100	509	523	531	136	
DIFF AM-STA	47	0	67	15	102	271	290	290	136	
RELAY ONEGA	53	0	67	18	110	284	288	293	136	
RELAY LOPAN	53	0	67	18	110	289	273	313	136	
CLASS II										
BURIED PES LOOPS	14	2124	67	3728	102	6110	6120	6094	136	
REFLECTING SIGNS	48	770	67	445	172	1516	1528	1502	136	
REFLECTING ROAD	19	84	67	320	322	1221	1231	1205	136	
W-SOLID POST	17	895	67	172	154	1230	1240	1214	136	
HF, UHF POST	16	83	67	54	115	356	366	368	136	
LF POST	15	438	67	172	154	862	871	846	136	
LIGHT/I-R POST	15	350	67	210	190	848	857	832	136	
BURIED MAGNETS	10	219	67	452	100	864	873	847	136	
ULTRASONIC POST	14	595	67	614	173	1478	1487	1462	136	
TRAFFIC SENSOR	15	665	67	294	101	1158	1167	1142	136	
CLASS III										
NAR-BAND FM PHASE	23	48	127	17	108	322	347	349	136	
MID-BAND FM PHASE	241	50	127	27	205	707	732	735	136	
PULSE T-O-ARRIVAL	258	140	327	50	183	957	982	985	136	
NOISE CORRELATION	79	29	327	25	179	654	663	665	136	
DIRECTION FINDER	4	79	67	16	154	331	319	319	136	
CLASS IV										
TRAFFIC LOOPS	8	3193	67	966	105	4404	4424	4424	136	
INSIDE RADIO	8	2766	67	805	276	3921	3921	3921	136	
PHOTO-I-R DETECT	12	1740	67	413	109	2420	2420	2420	136	
ULTRASONIC DETECT	13	1775	67	412	109	2455	2455	2455	136	

Table 1-10. Small City
Vehicle Polling

WALK TIME IN SECONDS TO POLL AND HIGH UNITS DEPLOYED

CLASS I TECHNIQUE	TOTAL FLEET	SAMPLE INFL						
		SVNC	INST	PRIO	SVNC	INST	PRIO	PRIO
KEYBOARD	170	0.54	0.55	1.06	0.57	0.60	0.60	1.13
STYLUS MAP	112	0.56	0.57	1.04	0.57	0.57	0.57	1.17
2-ACCELEROMETERS	109	0.55	0.56	1.17	0.57	0.57	0.57	1.10
LASEP VELOCIMTR	111	0.55	0.57	1.06	0.57	0.57	0.57	1.10
ULTRASONIC VELO	104	0.55	0.57	1.05	0.57	0.57	0.57	1.10
COMPASS/ODMETER	109	0.55	0.56	1.07	0.57	0.57	0.57	1.10
COMPASS-LASEP VEL	104	0.55	0.56	1.07	0.57	0.57	0.57	1.10
CHPSS-U-SONIC VEL	104	0.55	0.56	1.07	0.57	0.57	0.57	1.10
ONEGA	112	0.54	0.60	1.12	0.56	0.71	0.71	1.13
LOPAN	101	0.54	0.60	1.11	0.56	0.71	0.71	1.13
DECCA	120	0.54	0.61	1.13	0.57	0.71	0.71	1.13
AM-STATIONS	103	0.54	0.55	1.07	0.56	0.61	0.61	1.13
DIFF ONEGA	113	0.54	0.60	1.12	0.56	0.71	0.71	1.13
DIFF LOPAN	121	0.54	0.62	1.12	0.57	0.71	0.71	1.13
DIFF AM-STA	117	0.54	0.60	1.11	0.56	0.70	0.70	1.13
RELAY ONEGA	101	50.50	50.51	51.03	100.50	100.53	101.05	101.05
RELAY LOPAN	433	50.50	50.51	51.03	100.50	100.53	101.05	101.05
CLASS II								
BURIED PES LOOPS	107	0.53	0.55	1.06	0.57	0.57	0.57	1.11
REFLECTING SIGNS	107	0.53	0.55	1.06	0.57	0.57	0.57	1.11
REFLECTING ROAD	107	0.53	0.55	1.06	0.57	0.57	0.57	1.11
W-SOLID POST	106	0.53	0.54	1.06	0.57	0.57	0.57	1.11
HF, UHF POST	105	0.53	0.54	1.05	0.55	0.57	0.57	1.10
LF POST	106	0.53	0.54	1.05	0.55	0.57	0.57	1.10
LIGHT/I-R POST	106	0.53	0.54	1.05	0.55	0.57	0.57	1.10
BURIED MAGNETS	107	0.53	0.55	1.06	0.57	0.57	0.57	1.11
ULTRASONIC POST	106	0.53	0.54	1.05	0.55	0.57	0.57	1.11
TRAFFIC SENSOR	106	0.53	0.54	1.05	0.55	0.57	0.57	1.11

Table 1-13. Medium City Vehicle Polling

CLASS I TECHNIQUE KEYBOARD	TOTAL FLEET	CYCLE TIME IN SECONDS TO POLL (MAX AND MIN UNITS DEPLOYED)					
		SYNC UOL	SINGLE UOL	PAID UOL	SYNCH UOL	REQUIREMENT UOL	PAID UOL
STYLUS MAP	11 20	5 37 5 37	5 08 5 08	10 83 10 83	5 73 5 73	6 28 6 28	11 67 11 67
2-ACCELEROMETERS	10 93	5 60 5 60	5 33 5 33	11 07 11 07	5 20 5 20	6 07 6 07	12 13 12 13
LASER VELOCIMETER	11 07	5 50 5 50	5 47 5 47	10 93 10 93	5 07 5 07	6 33 6 33	12 08 12 08
ULTRASONIC VELO	10 93	5 47 5 47	5 70 5 70	10 93 10 93	5 93 5 93	6 40 6 40	11 87 11 87
COMPASS/ODOMETER	10 93	5 47 5 47	5 70 5 70	10 93 10 93	5 93 5 93	6 40 6 40	11 87 11 87
COMPASS/LASER VEL	10 93	5 47 5 47	5 70 5 70	10 93 10 93	5 93 5 93	6 40 6 40	11 87 11 87
COMPASS/U-SONIC VEL	10 93	5 47 5 47	5 70 5 70	10 93 10 93	5 93 5 93	6 40 6 40	11 87 11 87
OMEGA	11 84	5 47 5 47	5 13 5 13	11 37 11 37	5 20 5 20	7 27 7 27	12 73 12 73
LORAN	12 13	5 07 5 07	5 13 5 13	11 37 11 37	7 13 7 13	7 27 7 27	13 87 13 87
DECCA	12 00	5 00 5 00	5 23 5 23	11 47 11 47	7 00 7 00	7 47 7 47	12 93 12 93
AM-STATIONS	14 80	5 40 5 40	5 08 5 08	10 87 10 87	5 80 5 80	6 27 6 27	11 73 11 73
DIFF OMEGA	11 30	5 40 5 40	5 13 5 13	11 37 11 37	5 20 5 20	7 27 7 27	12 73 12 73
DIFF LORAN	12 13	5 07 5 07	5 23 5 23	11 53 11 53	7 13 7 13	7 60 7 60	13 73 13 73
DIFF AM-STA	11 73	5 87 5 87	5 18 5 18	11 33 11 33	5 73 5 73	7 20 7 20	12 67 12 67
RELAY OMEGA	1010 00	5 07 5 07	5 18 5 18	11 33 11 33	5 73 5 73	7 20 7 20	12 67 12 67
RELAY LORAN	43 33	21 67 21 67	21 40 21 40	27 13 27 13	38 33 38 33	44 27 44 27	11 87 11 87
CLASS II BURIED RES LOOPS	10 87	5 43 5 43	5 07 5 07	10 40 10 40	5 87 5 87	6 33 6 33	11 80 11 80
REFLECTING SIGNS	14 87	5 43 5 43	5 07 5 07	10 40 10 40	5 87 5 87	6 33 6 33	11 80 11 80
REFLECTING ROAD	10 87	5 43 5 43	5 07 5 07	10 40 10 40	5 87 5 87	6 33 6 33	11 80 11 80
A-BAND POST	10 40	5 40 5 40	5 03 5 03	10 37 10 37	5 80 5 80	6 27 6 27	11 73 11 73
HF VHF POST	10 67	5 33 5 33	5 37 5 37	10 80 10 80	5 67 5 67	6 13 6 13	11 60 11 60
LF POST	10 30	5 40 5 40	5 03 5 03	10 37 10 37	5 80 5 80	6 27 6 27	11 73 11 73
LIGHT I-P POST	10 30	5 40 5 40	5 03 5 03	10 37 10 37	5 80 5 80	6 27 6 27	11 73 11 73
BURIED MAGNETS	10 30	5 40 5 40	5 03 5 03	10 37 10 37	5 80 5 80	6 27 6 27	11 73 11 73
ULTRASONIC POST	10 30	5 40 5 40	5 03 5 03	10 37 10 37	5 80 5 80	6 27 6 27	11 73 11 73
TRAFFIC SENSOR	10 80	5 40 5 40	5 03 5 03	10 37 10 37	5 80 5 80	6 27 6 27	11 73 11 73

Table 1-14. Large Model City Parameters Used in AVM Cost Analysis (Cont'd)

THE CITY WOULD REQUIRE 29 WIDE-BAND OR PULSE T-O-A ANTENNA SITES AND 106 NARROW BAND ANTENNA SITES WITH 7 AND 3 MILE COVERAGE RADII.

Table 1-15. Large Model City AVM Cost Summary

LARGE MODEL CITY CLASS I TECHNIQUE	CAPS	THOUSANDS OF \$					TOTALS	
		SITES	BASE	INST	O-M	UOL	SYNCH	RANDOM
KEYBOARD	135	0	121	45	115	576	416	416
STYLUS MAP	2530	0	121	45	125	3041	2841	2841
2-ACCELEROMETERS	1680	0	161	118	208	2231	2428	2378
LASER VELOCIMETER	1780	0	161	145	250	2456	2693	2643
ULTRASONIC VELO	1270	0	161	118	250	1951	2148	2098
COMPASS/ODOMETER	1450	0	161	34	140	1956	2196	1093
COMPASS/LASER VEL	1855	0	161	160	190	2526	2766	2663
COMPASS/U-SONIC VEL	1585	0	151	110	190	2196	2436	2333
OMEGA	2700	0	141	90	175	3266	3531	3469
LORAN	2500	0	141	90	175	3266	3631	3599
DECCA	1150	0	141	70	175	1696	1961	1911
AM-STATIONS	400	0	141	60	160	921	1111	1064
DIFF OMEGA	2700	0	141	90	175	3266	3456	3469
DIFF LORAN	2300	0	141	98	175	3266	3556	3539
DIFF AM-STA	465	0	141	60	160	980	1170	1270
RELAY OMEGA	525	0	141	98	280	1116	956	1356
RELAY LORAN	575	0	141	98	280	1166	1006	1406
CLASS II								
BURIED RES LOOPS	140	28560	121	48687	115	27793	27793	27543
REFLECTING SIGNS	480	7700	121	4360	620	13641	13736	13441
REFLECTING ROAD	125	8-8	121	5110	4315	10671	10766	10511
X-BAND POST	170	3050	121	1625	635	10761	10856	10681
HF VHF POST	155	575	121	444	242	196	2091	1636
LF POST	150	4375	121	1630	640	7076	7171	6916
LIGHT-I-R POST	145	3500	121	2010	1080	6936	7031	6776
BURIED MAGNETS	160	2556	121	5767	199	9184	9199	8944
ULTRASONIC POST	145	9490	121	6845	825	13236	13331	13076
TRAFFIC SENSOR	145	6650	121	2850	116	10936	10131	9876
CLASS III								
NAR-BAND FM PHASE	225	499	228	101	178	1231	1481	1506
HID-BAND FM PHASE	2905	336	282	144	240	3826	4086	4161
PULSE T-O-RADIAL	2975	1484	382	425	253	5119	5369	5394
DIRECTION CORRELATION	785	29	382	115	282	1672	1762	1787
PHOTO-I-R FINDER	35	80	151	30	154	569	449	449
CLASS IV								
TRAFFIC LOOPS	80	68763	121	9567	950	74481	79481	79481
WAYSIDE RADIO	75	61233	121	7960	1860	71249	71249	71249
PHOTO-I-R DETECT	115	41148	121	4035	990	46401	46401	46401
ULTRASONIC DETECT	125	41498	121	4038	990	46756	46756	46756

D. Large Model City AVM Cost Summary Tables

Table 1-14. Large Model City Parameters Used in AVM Cost Analysis

AREA IS 400 SQUARE MILES.
 EAST WEST DISTANCE IS 13.9 MILES.
 NORTH SOUTH DISTANCE IS 27.3 MILES.
 TOTAL ROAD MILEAGE IS 7736 MILES.
 THE NUMBER OF INTERSECTIONS IS 35000.
 THE ESTIMATED NUMBER OF ROAD SEGMENTS IS 70000.
 THERE ARE 1000 CARS IN THE FLEET
 AND THERE ARE 0 MOTORCYCLES.
 THE NUMBER OF VEHICLES ON EACH SHIFT IS:
 FIRST SHIFT MAX. 500
 FIRST SHIFT MIN. 500
 SECOND SHIFT MAX. 500
 SECOND SHIFT MIN. 500
 THIRD SHIFT MAX. 500
 THIRD SHIFT MIN. 500

Table 1-16. Large City Vehicle Polling

CLASS I TECHNIQUE KEYBOARD	TOTAL FLEET	CYCLE TIME IN SECONDS TO POLL (MAX AND MIN UNITS DEPLOYED)					
		SYNC UOL	SINGLE UOL	PAID UOL	SYNCH UOL	REQUIREMENT UOL	PAID UOL
STYLUS MAP	112 00	5 37 5 37	5 08 5 08	10 83 10 83	5 73 5 73	6 28 6 28	11 67 11 67
2-ACCELEROMETERS	109 30	5 60 5 60	5 33 5 33	11 07 11 07	5 20 5 20	6 07 6 07	12 13 12 13
LASER VELOCIMETER	110 67	5 50 5 50	5 47 5 47	10 93 10 93	5 07 5 07	6 33 6 33	12 08 12 08
ULTRASONIC VELO	104 33	5 47 5 47	5 70 5 70	10 93 10 93	5 93 5 93	6 40 6 40	11 87 11 87
COMPASS/ODOMETER	109 33	5 47 5 47	5 70 5 70	10 93 10 93	5 93 5 93	6 40 6 40	11 87 11 87
COMPASS/LASER VEL	109 33	5 47 5 47	5 70 5 70	10 93 10 93	5 93 5 93	6 40 6 40	11 87 11 87
COMPASS/U-SONIC VEL	109 33	5 47 5 47	5 70 5 70	10 93 10 93	5 93 5 93	6 40 6 40	11 87 11 87
OMEGA	110 00	5 47 5 47	5 13 5 13	11 37 11 37	5 20 5 20	7 27 7 27	12 73 12 73
LORAN	121 33	5 07 5 07	5 13 5 13	11 37 11 37	7 13 7 13	7 27 7 27	13 87 13 87
DECCA	120 00	5 00 5 00	5 23 5 23	11 47 11 47	7 00 7 00	7 47 7 47	12 93 12 93
AM-STATIONS	106 00	5 40 5 40	5 08 5 08	10 87 10 87	5 80 5 80	6 27 6 27	11 73 11 73
DIFF OMEGA	110 00	5 40 5 40	5 13 5 13	11 37 11 37	5 20 5 20	7 27 7 27	12 73 12 73
DIFF LORAN	121 33	5 07 5 07	5 23 5 23	11 53 11 53	7 13 7 13	7 60 7 60	13 73 13 73
DIFF AM-STA	117 33	5 87 5 87	5 18 5 18	11 33 11 33	5 73 5 73	7 20 7 20	12 67 12 67
RELAY OMEGA	10100 00	5 07 5 07	5 18 5 18	11 33 11 33	5 73 5 73	7 20 7 20	12 67 12 67
RELAY LORAN	433 33	21 67 21 67	21 40 21 40	27 13 27 13	38 33 38 33	44 27 44 27	11 87 11 87
CLASS II							
BURIED RES LOOPS	111 33	5 43 5 43	5 07 5 07	10 40 10 40	5 87 5 87	6 33 6 33	11 80 11 80
REFLECTING SIGNS	111 33	5 43 5 43	5 07 5 07	10 40 10 40	5 87 5 87	6 33 6 33	11 80 11 80
REFLECTING ROAD	111 33	5 43 5 43	5 07 5 07	10 40 10 40	5 87 5 87	6 33 6 33	11 80 11 80
A-BAND POST	110 67	5 40 5 40	5 03 5 03	10 37 10 37	5 80 5 80	6 27 6 27	11 73 11 73
HF VHF POST	109 33	5 33 5 33	5 37 5 37	10 80 10 80	5 67 5 67	6 13 6 13	11 60 11 60
LF POST	110 67	5 40 5 40	5 03 5 03	10 37 10 37	5 80 5 80	6 27 6 27	11 73 11 73
LIGHT I-R POST	110 67	5 40 5 40	5 03 5 03	10 37 10 37	5 80 5 80	6 27 6 27	11 73 11 73
BURIED MAGNETS	111 33	5 40 5 40	5 03 5 03	10 37 10 37	5 80 5 80	6 27 6 27	11 73 11 73
ULTRASONIC POST	110 67	5 40 5 40	5 03 5 03	10 37 10 37	5 80 5 80	6 27 6 27	11 73 11 73
TRAFFIC SENSOR	110 67	5 40 5 40	5 03 5 03	10 37 10 37	5 80 5 80	6 27 6 27	11 73 11 73

IV. AVM SYSTEM ACCURACIES AND COST BENEFITS

A. System Parameters That Affect AVM Costs

The prediction of the expected accuracies of AVM systems is essentially a probabilistic problem. Actually there are two distinct problems, one a precursor to the other, depending on the class of AVM system. Classes I and III are loosely referred to as "random route" systems because the techniques have the capability of vehicle location anywhere within their surveillance areas. Classes II and IV are called "fixed route" systems because the location capability exists only in the vicinities of signposts that are distributed along the wayside or on the roadway at intersections within the covered area. Besides the inherent range of uncertainty in the location measurements provided by individual AVM techniques, Classes I and III are subject to another location error, which is the shift in the moving vehicle's position during the interval between the instant of polling and the display of location data at the base. On the other hand, Class II and IV techniques provide location information only at the time when the vehicle passes within the sensing radius of a wayside or buried signpost. This information is the best available until the time that the vehicle enters the sensing radius of another signpost. A measure of this uncertainty in location is required to determine the "inherent" accuracy of the signpost AVM techniques. This is particularly true when the signposts are less than maximally dense; that is, when the signposts are placed two or more intersections apart.

It is intuitively reasoned that if the signpost sensors in Classes II and IV are placed at each intersection, then the location of any vehicle can be found to plus-or-minus one block. It also follows that if the sensors are placed in a diamond pattern at every other block in each direction, then the accuracy is plus-or-minus two blocks. This reasoning is valid only if every passage through instrumented intersections by all vehicles is known. If the polling technique or RF channel loading is such that this data frequency cannot be assured, then the achievable accuracy is not as well known. A tutorial treatment of the less dense signpost placement by Markov, or random-walk, processes is included in Part Three of this Report. The analysis technique leads to a prediction of the mean and variance of the distance traveled by a vehicle starting at an unsensed intersection before it passes a sensed intersection. The results of this technique for various signpost densities are as follows:

Ratio (Sensed/Unsensed)	Mean	Variance
1/1	1	1
3/8	1.778	1.778
3/9	2	2

The second approach to the system accuracy prediction considers not only the inherent error in the vehicle location technique but also the additional inaccuracies introduced by the delays in

successive pollings of the vehicles and by the computation of location when the vehicles in the fleet are moving at various speeds. In Part Three of this Report, the analysis, the method of solution, and the tabular results are presented.

The technique for predicting the location accuracy was used to generate the family of curves in Fig. 1-36. These contours of system accuracy correlate the independent variables of the polling interval and the standard deviation of the inherent error. The accuracy contour yields the 95% confidence interval for vehicle fleets that move with an exponential velocity distribution such that more than half the vehicles are moving at speeds less than 15 mph (6.67 m/s). It can be seen from the curves that either the polling interval or the inherent error can quickly dominate the achievable system accuracy if either is very large. The curves are shown for the system accuracy interval of 100 to 1000 meters (0.1 to 0.6 mile). The curves for less than 100 and greater than 1000 meters are repetitions of those shown and can be derived with subtraction or addition of a unit constant on both axes (equivalent to division or multiplication of the interval or deviation by a factor of 10).

B. Estimated Cost Savings Based on Urban Parameters

1. System accuracy estimation. The accuracy to be expected from any given AVM system in a locality is estimated by a step-by-step process. First, from the data provided for the particular city, the maximum and minimum number of vehicles deployed is obtained. Next, the number of bits in the location message required from each vehicle for each technique is determined. The time required to poll the deployed vehicles with a 0.1-sec radio turn-on time is then computed for the redundant mode of the random polling process. This value yields very conservative (or pessimistic) polling intervals for the two values of vehicles deployed. These intervals together with the value obtained from the table of technique accuracies provide the entries to the graph of system accuracies. These curves are prestored in the computer program. A rather simple linear interpolation program yields a maximum and minimum estimation of the 95% confidence level of system accuracy for the maximum and minimum vehicle deployments. The location accuracies used are usually greater than the standard deviation value.

2. Vehicles saved estimation. Based on the prior work of Larson (Ref. 2), Knickel (Ref. 3), and Doering (Ref. 4), a quantitative measure of efficiency increase in responding to calls for service should be determinable from the accuracy of the AVM system. One of the approaches to this problem is to compare a situation where, in response to a call for service, the dispatcher always sends the vehicle responsible for a beat to that where the location of the vehicles is known and the "closest" vehicle is dispatched to the scene.

The efficiency comparison is made either in the excess time required or the excess distance travelled by the beat vehicles relative to the closest located vehicles. The conclusions of this approach are generally that a vehicle location accuracy of about 1/5 the beat-side dimension is

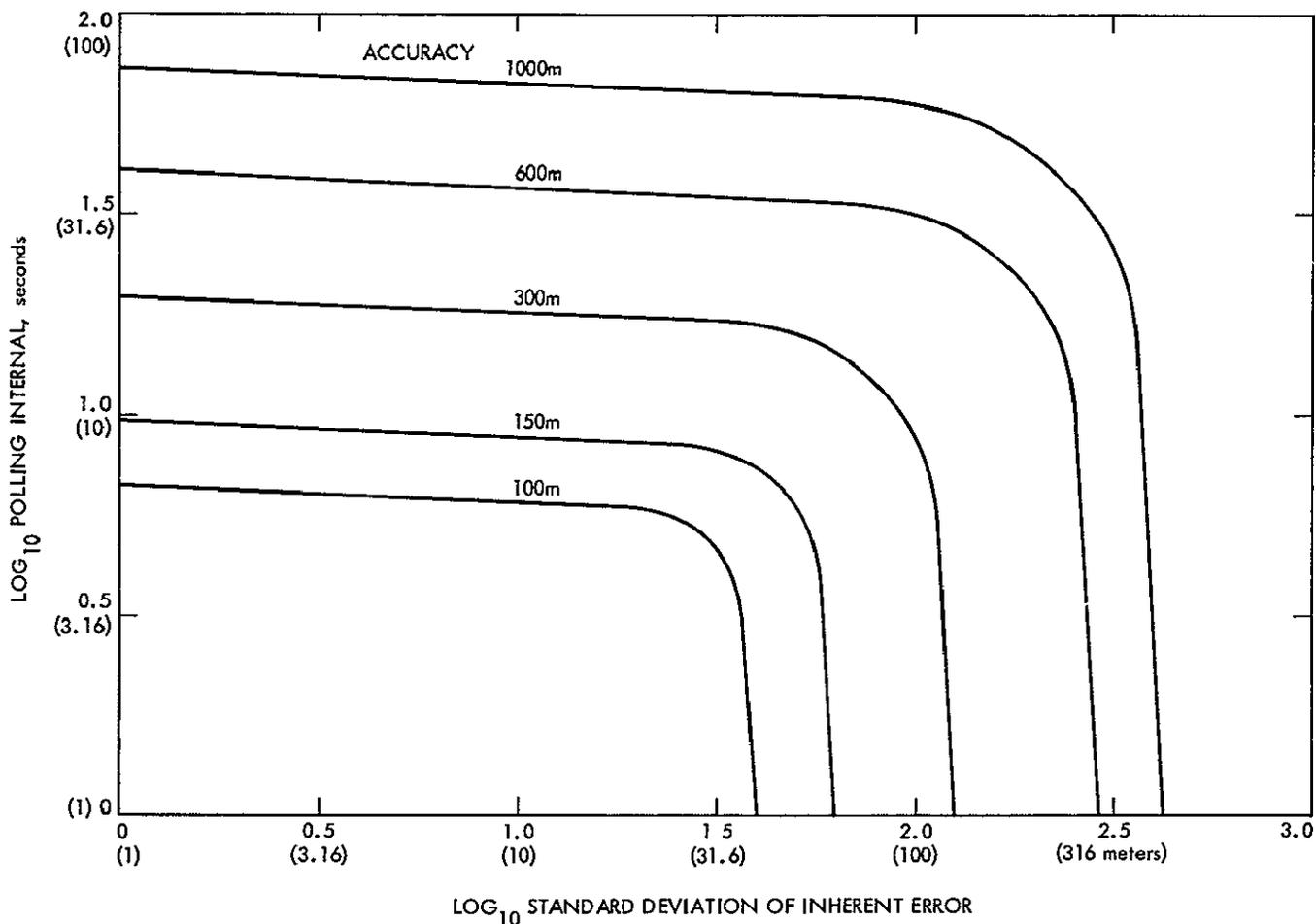


Fig. 1-36. Vehicle Polling Intervals vs 95% AVM System Accuracy

sufficient. Additionally the service improvement is found to be about 7% for the locator system dispatches versus the "center of mass" or beat vehicle dispatches.

The more recent study of Doering (Ref. 4), however, compares response time performance in a situation with differing absolute accuracy values of the AVM system and a given fleet size with the number of vehicles required to provide the same response time with no AVM. Doering's study indicated that, in the area studied (the city of Orlando, Florida), 34 vehicles in the AVM fleet where the accuracy is 240 meters (800 ft) would provide a response time which would require 35.8 vehicles in a non-AVM fleet. Extrapolation of the curves presented by Doering indicates that 8 to 10% fewer vehicles in an AVM system fleet with perfect (0 feet) accuracy can provide the same response performance as the larger number of vehicles in a non-AVM fleet. Extrapolation in the direction of less accurately known location, indicates that there is little improvement in response time with location accuracies of 450 meters (1500 ft) or more. It may be coincidental that this value is about 0.3 km (0.2 mile), which is 1/5 the average beat side dimension in the Orlando simulation studies. A plot of the increase required in a non-AVM vehicle fleet to equal AVM vehicles response time performance versus accuracy shows a linearly decreasing value as the AVM accuracy decreases.

For the purposes of this study, a 7% increase in efficiency is assumed for a perfect AVM system, with the percentage decreasing linearly to zero at an AVM accuracy of 0.2 times the average beat side length. The average beat is calculated by dividing the area by the number of vehicles deployed.

For maximum and minimum deployments, the efficiency increase assumption yields different values for the same AVM technique accuracy. In cases where the minimum deployment is substantially lower than the maximum, the apparent beat size may be increased to the point where an AVM technique which yields no efficiency increase with maximum deployment may display a marked improvement in response. Additionally, the minimum deployment decreases the polling time interval which provides an additional improvement in system accuracy.

The calculation of cars saved is based on a reasonable reciprocity assumption that fewer cars with AVM can yield the same performance as that obtained now with a given fleet size. The number of cars saved is determined by multiplying the percentage efficiency value, obtained from the beat dimension and system accuracy, by the number of vehicles deployed. Savings of less than one vehicle are allowed by the calculation. As stated before, the factors tending to increase efficiency are such that, in some cases, the number of cars

saved with minimum deployment exceeds that for maximum deployment with a given technique.

3. Estimated 5-year cost saving. The 5-year saving calculation, presented in Tables 1-17 through 1-20 is an attempt to place a dollar value on the efficiency increase which might in turn indicate possible choices of candidate AVM systems. The calculation assumes that each car saved is worth \$150,000 annually, which is primarily salaries and overhead (as of 1974). This is an average value for a 1-man car based on 5 salaries and 100% overhead. The saving for small, medium, and large cities is a straightforward multiplication of the maximum of the cars saved times the annual value of the car minus the O-M costs of the AVM technique. The value

obtained is then multiplied by 5 years for the total saving.

The 5-year saving is positive only if the value of the car saving exceeds the annual O-M cost. The calculation is performed for a given technique only if a car saving is indicated, and the result is presented regardless of sign. No calculation is performed if no car saving is indicated.

A simple summation of savings rather than a present worth of an annuity calculation is justified on the basis that it is less speculative and might be more nearly correct if salaries rise at a percentage rate which exceeds the rate of return that can be realized on 5-year municipal investments. The 5-year saving estimation is presented solely for AVM system comparison purposes.

Table 1-17. Small Model City Cost Benefits from AVM System Usage

SMALL MODEL CITY											
CLASS I	TECHNIQUE	ULTIMATE ACCURACY	VEHICLES SAVED	ACCURACY	VEHICLES SAVED						
KEYBOARD	33	0	36	3	2	1	2	2	2	2	2
STYLUS MAP	31	0	75	3	2	2	2	2	2	2	2
2-ACCELFONETIPS	24	0	34	2	2	2	2	2	2	2	2
LASEP VELOCINTP	13	0	34	3	3	3	3	3	3	3	3
ULTRASONIC VELD	10	0	171	16	2	2	2	2	2	2	2
COMPASS-ODOMETEP	20	0	44	4	2	2	2	2	2	2	2
COMPASS-LHSEF VEL	15	0	70	3	2	2	2	2	2	2	2
CIPCS-U-SOINIC VEL	17	0	43	3	2	2	2	2	2	2	2
ONEGA	1600	0	2632	263	0	0	0	0	0	0	0
LORAH	160	0	270	27	0	0	0	0	0	0	0
DECCA	200	0	44	4	0	0	0	0	0	0	0
AI-STATIOLC	200	0	44	4	0	0	0	0	0	0	0
DIFF ONEGA	160	0	270	27	0	0	0	0	0	0	0
DIFF LORAH	160	0	270	27	0	0	0	0	0	0	0
DIFF AI-STA	200	0	44	4	0	0	0	0	0	0	0
RELA. ONEGA	1600	0	2632	263	0	0	0	0	0	0	0
RELA. LORAH	160	0	270	27	0	0	0	0	0	0	0
CLASS II											
BURIED FCS LOOPS	10	0	27	2	2	2	2	2	2	2	2
REFLECTING SIGNS	10	0	1	1	1	1	1	1	1	1	1
REFLECTING FORD	3	0	13	1	1	1	1	1	1	1	1
U-SHED POST	12	0	22	2	2	2	2	2	2	2	2
HF, UHF POST	15	0	38	3	3	3	3	3	3	3	3
LF POST	150	0	21	2	2	2	2	2	2	2	2
LIGHT-I-P POST	30	0	75	7	7	7	7	7	7	7	7
BURIED MAGNETS	1	0	17	1	1	1	1	1	1	1	1
ULTRASONIC POST	20	0	44	4	4	4	4	4	4	4	4
TRAFFIC SENSOP	10	0	27	2	2	2	2	2	2	2	2
CLASS III											
MAP-BAND FM PHASE	1000	0	2632	263	0	0	0	0	0	0	0
NID-BAND FM PHASE	1200	0	2709	270	0	0	0	0	0	0	0
PULSE T-O-APPIVAL	100	0	166	16	1	1	1	1	1	1	1
NOISE CORRELATION	100	0	165	16	1	1	1	1	1	1	1
DIRECTION FINDER	700	0	1715	171	0	0	0	0	0	0	0
CLASS IV											
TRAFFIC LOOPS	10	0	26	2	2	2	2	2	2	2	2
WYSIDE RADIO	100	0	234	23	2	2	2	2	2	2	2
PHOTO-I-P DETECT	30	0	72	7	7	7	7	7	7	7	7
ULTRASONIC DETECT	20	0	48	4	4	4	4	4	4	4	4

Table 1-18. Medium Model City Cost Benefits from AVM System Usage

MEDIUM MODEL CITY											
CLASS I	TECHNIQUE	ULTIMATE ACCURACY	VEHICLES SAVED	ACCURACY	VEHICLES SAVED						
KEYBOARD	33	0	136	13	1	1	1	1	1	1	1
STYLUS MAP	31	0	293	29	3	3	3	3	3	3	3
2-ACCELFONETIPS	24	0	203	20	2	2	2	2	2	2	2
LASEP VELOCINTP	13	0	193	19	1	1	1	1	1	1	1
ULTRASONIC VELD	10	0	204	20	2	2	2	2	2	2	2
COMPASS-ODOMETEP	20	0	199	19	1	1	1	1	1	1	1
COMPASS-LHSEF VEL	15	0	198	19	1	1	1	1	1	1	1
CIPCS-U-SOINIC VEL	17	0	199	19	1	1	1	1	1	1	1
ONEGA	1500	0	2677	267	0	0	0	0	0	0	0
LORAH	160	0	408	40	0	0	0	0	0	0	0
DECCA	200	0	492	49	0	0	0	0	0	0	0
AI-STATIOLC	200	0	490	49	0	0	0	0	0	0	0
DIFF ONEGA	1600	0	2688	268	0	0	0	0	0	0	0
DIFF LORAH	160	0	408	40	0	0	0	0	0	0	0
DIFF AI-STA	200	0	492	49	0	0	0	0	0	0	0
RELA. ONEGA	1500	0	2677	267	0	0	0	0	0	0	0
RELA. LORAH	160	0	408	40	0	0	0	0	0	0	0
CLASS II											
BURIED FCS LOOPS	10	0	194	19	1	1	1	1	1	1	1
REFLECTING SIGNS	10	0	14	1	1	1	1	1	1	1	1
REFLECTING FORD	3	0	187	18	1	1	1	1	1	1	1
U-SHED POST	12	0	194	19	1	1	1	1	1	1	1
HF, UHF POST	15	0	193	19	1	1	1	1	1	1	1
LF POST	150	0	270	27	2	2	2	2	2	2	2
LIGHT-I-P POST	30	0	200	20	2	2	2	2	2	2	2
BURIED MAGNETS	1	0	184	18	1	1	1	1	1	1	1
ULTRASONIC POST	20	0	197	19	1	1	1	1	1	1	1
TRAFFIC SENSOP	10	0	193	19	1	1	1	1	1	1	1
CLASS III											
MAP-BAND FM PHASE	1000	0	2687	268	0	0	0	0	0	0	0
NID-BAND FM PHASE	1200	0	2763	276	0	0	0	0	0	0	0
PULSE T-O-APPIVAL	100	0	185	18	1	1	1	1	1	1	1
NOISE CORRELATION	100	0	207	20	2	2	2	2	2	2	2
DIRECTION FINDER	700	0	1918	191	0	0	0	0	0	0	0
CLASS IV											
TRAFFIC LOOPS	10	0	23	2	2	2	2	2	2	2	2
WYSIDE RADIO	100	0	209	20	2	2	2	2	2	2	2
PHOTO-I-P DETECT	30	0	61	6	6	6	6	6	6	6	6
ULTRASONIC DETECT	20	0	43	4	4	4	4	4	4	4	4

Table 1-19. Large Model City Cost Benefits from AVM Systems Using One RF Channel

LARGE MODEL CITY											
CLASS I	TECHNIQUE	ULTIMATE ACCURACY	VEHICLES SAVED	ACCURACY	VEHICLES SAVED						
KEYBOARD	33	0	203	20	2	2	2	2	2	2	2
STYLUS MAP	31	0	2132	213	2	2	2	2	2	2	2
2-ACCELFONETIPS	24	0	2095	209	2	2	2	2	2	2	2
LASEP VELOCINTP	13	0	2053	205	2	2	2	2	2	2	2
ULTRASONIC VELD	10	0	2106	210	2	2	2	2	2	2	2
COMPASS-ODOMETEP	20	0	2062	206	2	2	2	2	2	2	2
COMPASS-LHSEF VEL	15	0	2044	204	2	2	2	2	2	2	2
CIPCS-U-SOINIC VEL	17	0	2052	205	2	2	2	2	2	2	2
ONEGA	1600	0	2652	265	0	0	0	0	0	0	0
LORAH	160	0	211	21	0	0	0	0	0	0	0
DECCA	200	0	2403	240	0	0	0	0	0	0	0
AI-STATIOLC	200	0	2126	212	0	0	0	0	0	0	0
DIFF ONEGA	1600	0	2651	265	0	0	0	0	0	0	0
DIFF LORAH	160	0	212	21	0	0	0	0	0	0	0
DIFF AI-STA	200	0	2371	237	0	0	0	0	0	0	0
RELA. ONEGA	1600	0	2655	265	0	0	0	0	0	0	0
RELA. LORAH	160	0	212	21	0	0	0	0	0	0	0
CLASS II											
BURIED FCS LOOPS	10	0	2053	205	0	0	0	0	0	0	0
REFLECTING SIGNS	10	0	1430	143	0	0	0	0	0	0	0
REFLECTING FORD	3	0	1930	193	0	0	0	0	0	0	0
U-SHED POST	12	0	2053	205	0	0	0	0	0	0	0
HF, UHF POST	15	0	2044	204	0	0	0	0	0	0	0
LF POST	150	0	2123	212	0	0	0	0	0	0	0
LIGHT-I-P POST	30	0	2119	211	0	0	0	0	0	0	0
BURIED MAGNETS	1	0	1947	194	0	0	0	0	0	0	0
ULTRASONIC POST	20	0	2055	205	0	0	0	0	0	0	0
TRAFFIC SENSOP	10	0	2042	204	0	0	0	0	0	0	0
CLASS III											
MAP-BAND FM PHASE	1000	0	2616	261	0	0	0	0	0	0	0
NID-BAND FM PHASE	1200	0	2644	264	0	0	0	0	0	0	0
PULSE T-O-APPIVAL	100	0	207	20	1	1	1	1	1	1	1
NOISE CORRELATION	100	0	232	23	2	2	2	2	2	2	2
DIRECTION FINDER	700	0	2182	218	0	0	0	0	0	0	0
CLASS IV											
TRAFFIC LOOPS	10	0	21	2	2	2	2	2	2	2	2
WYSIDE RADIO	100	0	187	18							

V. COMPUTER PROGRAMS FOR ANALYSES OF AVM NEEDS

The cost estimates for the AVM techniques are in almost all cases precisely that — estimates as of 1974. They have the additional shortcoming that large-scale production is assumed, which accounts for the generally low system cost amounts. Therefore, additional studies are necessary to refine these estimates in view of the rapidly changing technology and costs.

Although the cost estimation procedure for AVM systems in model cities is a valid technique, it does not take into account the individual differences of real cities. That is, the system engineering aspect where the vagaries of a particular city and operational methodology are considered has not been included. The AVM system cost estimation and particularly the performance estimation and resultant estimated savings are essentially averaging processes. Since each city differs in details from each other city, and the AVM system cost, performance, and impact depend on these differences, final selection of an AVM system will require an individual analysis such as those presented in Part Two.

An individualized analysis for a particular city requires the two following steps: (1) Synthesis of AVM systems corresponding to each of the desired concepts as they would be configured for the physical, political, and cost environment of that city, and (2) evaluation of the effects of each of those systems. The process of synthesizing a particular AVM system is a straightforward but tedious task, requiring detailed technical knowledge that may not be readily available in real cities. It can be made easily available, however, by the development of an AVM system synthesis computer program, as is described later. The expected effects can then be assessed by using the resultant systems in a system simulation computer program, which is described in more detail in Section B. Since these two programs were planned to be developed in Phase One of this AVM Systems Study project, they do not yet exist.

A. AVM System Synthesis Computer Program

The synthesis program will be based on design algorithms, equations, cost estimates, and the AVM data base developed in Phase Zero of this Study. These program components include antenna siting algorithms for time-of-arrival systems, message length equations for different location technique and polling combinations, accuracy estimation equations for various reporting intervals or signpost densities, and life-cost equations. A preliminary concept of the basic elements of the AVM system synthesis computer program is shown in Figure 1-37. A concept of the operations sequence in using the synthesis program is presented in Table 1-21. Salient features of the synthesis program are listed in the following subsections.

1. City and fleet data for AVM System Synthesis Program. The synthesis program will first summarize the data provided from the input file. The purpose of this step is to provide the user with an opportunity to review the input before actually running the synthesis program. Table 1-22 lists some of the parameters that will be included in the data input summary.

Table 1-21. Operating Sequence of AVM System Synthesis Computer Program

<p><u>Step 1.</u> The user will supply the values of those parameters that describe his particular city. Some of the data may be fairly extensive, for example, geocoding data or DIME file type information which describes the city street/block system in detail. For information of this type a computer-readable data file will be used. An auxiliary program, separate from the AVM system synthesis program, will be developed to facilitate the interactive development of the data file.</p> <p><u>Step 2.</u> The synthesis program will read the data file and determine the AVM system configurations suited to the city. If any data is missing or incomplete, the program will indicate which systems cannot be evaluated and provide an opportunity to modify the data file.</p> <p><u>Step 3.</u> The program will present basic comparison data for each system configuration option.</p> <p><u>Step 4.</u> After selecting the viable configuration options, the program will shift to a "trade-off" or compromise mode in which the user can access further detail and investigate the options available within a particular choice of system concept.</p>

Table 1-22. City and Fleet Input Data for AVM System Synthesis Program

<p>City name AAAAAAAAAAAAAAAAAAAAAAAAAA Area monitored. XX.X sq miles Maximum X and Y dimensions: XX.XX mi. by XX.XX miles Street length: XXX.X miles Number of intersections: NNNN Number of road segments: NNNN Number of vehicles instrumented: NNNN Average number of vehicles each shift: NN, NN, NN Number of beats per shift: NN, NN, NN Shift hours: HH-HH, HH-HH, HH-HH Number of dispatcher consoles: N Utilization factor by shift: FF%, FF%, FF% (This is the fraction of time available to respond to calls for service). Average call for service time by shift: HH, HH, HH RF channel utilization factor: P%, P%, P% RF channel assigned: N Planned: N LORAN coverage in area?: Y-N; DECCA?: Y-N AM stations in area K--, W--, K--, W--</p>

2. AVM Configuration options for AVM System Synthesis. Each of the AVM options identified by the selection process will be described briefly in narrative form. Each will be tagged with an identity code for later use. Then for each of the applicable options, the following gross data will be presented for comparison:

a. Cost estimates. Total system cost, "present value. "\$XX XXX XXX (These figures

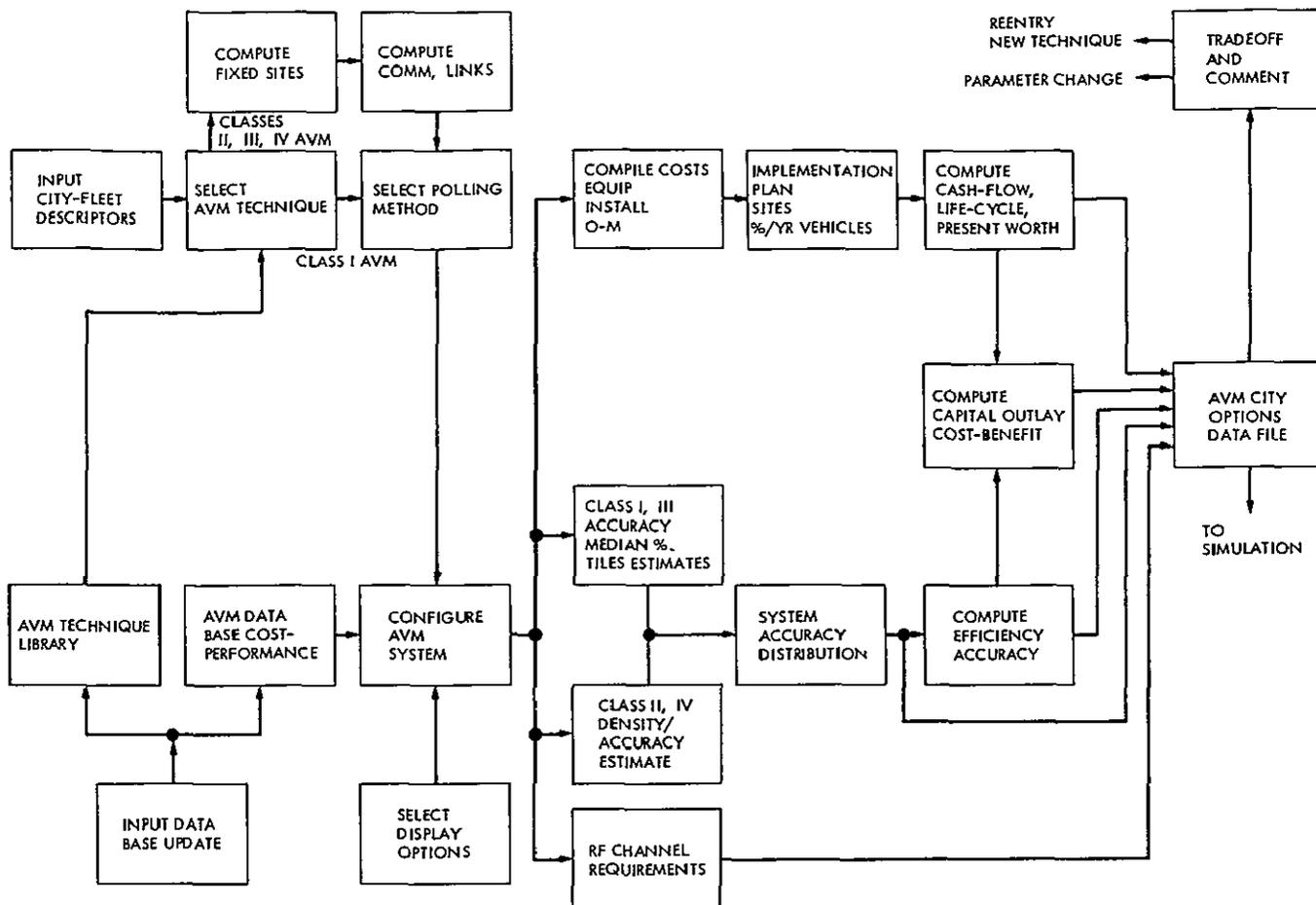


Figure 1-37. Concept for AVM System Synthesis Computer Program

will be for comparison purposes only. A breakdown follows:)

One-time costs	\$XX XXX XXX
(development, conversion, facilities)	
Installation costs	\$XX XXX XXX
Recurring costs	\$XXX XXX per year
(operations, maintenance, training)	
Replacement	\$XXX XXX per year
(equivalent annual payment at 10% year)	
Upgrading costs	
Display consoles	\$XXX XXX plus \$XX XXX per year (each)
Fixed sites	\$XXX XXX plus \$XX XXX per year (each)
Signposts	\$ XXX plus \$ XXX per year (each)
Vehicle equipment	\$ X XXX plus \$ XXX per year (each)
Telephone mileage	\$XXX XXX plus \$XXX XXX per year (each)

b. Resource utilization estimate.

Radio channels required: XX.X

Microwave or dedicated telephone lines needed: XXX

Computer memory estimate: XXX XXX bytes

c. Performance estimates.

Median location accuracy: XX ft (effective polling rate = XX vehicles/second)

Fraction of fleet with error

less than ___ft: XX%

less than ___ft: XX%

less than ___ft: XX%

d. Comments. Design features and other relevant considerations will be noted. Typical comments that might apply to specific systems are as follows:

"Vehicle status is monitored".

"Field unit alarm capability is present".

"Polling procedures are inflexible".

"Shared usage by several agencies would be difficult to implement".

"Effect of weather on performance expected to be small".

"Fleet locations easily monitored by public".

"Each 90 vehicles monitored requires an additional radio channel".

"Sensors may require protection from vandalism".

e. Trade-off potential. This portion of the output will identify significant trade-off possibilities and the potential outcome that could result from those trade-offs. The trade-off relationships will be accessible during Step 4 (Table 1-21) of the program. Typical trade-offs that might be possible for all or some of the systems are these:

Location accuracy vs number of radio channels (via the polling option and rate).

Computing at the command center vs computing on-board the vehicles. (This affects the costs and accuracy vs radio spectrum trade-off.)

Display characteristics vs cost. (These trade-offs may be independent of the other descriptors of the system.)

Location accuracy vs cost (via the spatial density of signposts, the number of fixed sites, etc).

f. Cost benefit estimate. A preliminary estimate of efficiency increase with AVM will also be an output. The cost benefit estimate will be derived from the estimated increase in efficiency and data such as that listed below:

Patrolman average salary:
\$XX, XXX per year
Patrolmen required for each vehicle: N
Support personnel for each vehicle: N.N
Overhead on salaries: PP%
Replacement cost of vehicle: \$X, XXX
Maintenance cost of vehicle:
\$X, XXX per year

*Based on the size of the fleet and these parameters, a cost benefit (deficit) first estimate will be provided such as:

Number of vehicles saved by shift: X, X, X
Vehicle cost saving equivalent: \$XXX, XXX
AVM capital investment equivalent,
10 yr: \$XXX, XXX
5 yr: \$XXX, XXX

The information provided by the AVM system synthesis program will not in itself provide sufficient justification for selection but will be a very important first step that eliminates obvious non-competitive techniques and allows for more detailed consideration of the viable techniques.

B. AVM System Simulation Computer Program

Much work has already been done by others in regard to AVM simulation (see Bibliography). The intent of this study effort is to utilize as much of that work as possible.

There is one aspect of the prior work where it is believed that improvement is needed. This is in the area of AVM system accuracy estimation. Prior AVM simulation work has investigated the overall command and control function to determine the effect of AVM system accuracy on "wrong dispatches" and the average distance travelled as a result of these "wrong dispatches." A "wrong dispatch" results when the closest available vehicle is not the one directed to respond to the call for service. This incorrect action results from not knowing precisely the vehicle locations, and thus the entire system performance is degraded owing to unnecessary distance travelled and time consumed in responding to calls for service.

In these prior simulations of the command and control functions, the investigators assigned values such as a 95 percentile value of a radial error of X feet to the AVM system accuracy. It has been assumed that this error distribution is normal and constant with time. The computer simulation programs determine the exact location of each vehicle from a mobility routine or driver scenario. Then, in order to test the system response to a call for service, each of the exact locations is corrupted in some random fashion with either X and Y or with an angle and range to the exact location. The apparent location is then used by the dispatching routine in the search for the vehicle closest to the call for service. The foregoing mode of simulation effectively assumes a constant value for the AVM system accuracy which may be misleading for all but those techniques that use very short intervals between vehicle location determinations. Short interval interrogation of location is not a requisite mode of operation in many AVM techniques and is impractical or inappropriate in others.

A more realistic approach to AVM accuracy simulation is to model the actual vehicle location process, including the expected or appropriate polling technique and taking into consideration the time lapse from the last location determination, the motion of the vehicles, and the resultant effect on closest car determination. In this mode of simulation, the vehicle mobility or driver location routine can be altered by a time-varying location uncertainty, if that is appropriate for the particular AVM system concept. The exact nature of this uncertainty or modification to the exact location may also be a function of other factors in addition to time. These factors may be vehicle speed, physical location at time of interrogation, distance travelled since last location, or distance travelled since last signpost proximity update. These factors will be explicitly considered by the AVM simulation program.

An accurate measure of the reduction in response time requires that a reasonably accurate geocoded definition of the coverage area be a part of the simulation program. Simulations that sum the absolute values of the differences in X- and Y-distances from the vehicle position

to the location of the call for assistance give a correct solution only for idealized rectangular cities. Geocoded descriptions of the coverage area will allow an accurate measure of distance in each instance, since the optimum travel routes can be used in the simulation.

The advantage of using the more accurate AVM simulation models is that a more realistic appraisal of the expected increase in efficiency can be determined. In addition, the possible variations in system configuration that affect performance parameters of the entire system can be investigated with the assurance that the influence of the variation has been considered.

Other technical performance parameters that will be considered in the simulation program include the data links involved in the vehicle location process and the effects of errors in reception; the effects of entry of new vehicles into the coverage area, and the re-establishment of the position of "lost" vehicles in relative location techniques. In addition, the actual location algorithm for each technique can be exercised with the expected input data. The preliminary concept of the main components of the AVM system simulation program are shown in Fig. 1-38. As already indicated, the intent is to develop this program around prior work insofar as possible.

Heretofore, simulation has been used almost exclusively in regard to reducing response time. The proposed simulation program will allow the investigation of other aspects of vehicle location. The utility of post data analysis can be evaluated, and the effects of an officer-needs-assistance incident can be assessed, both for the impact on subsequent calls for service and on the response time improvement to the officer in trouble.

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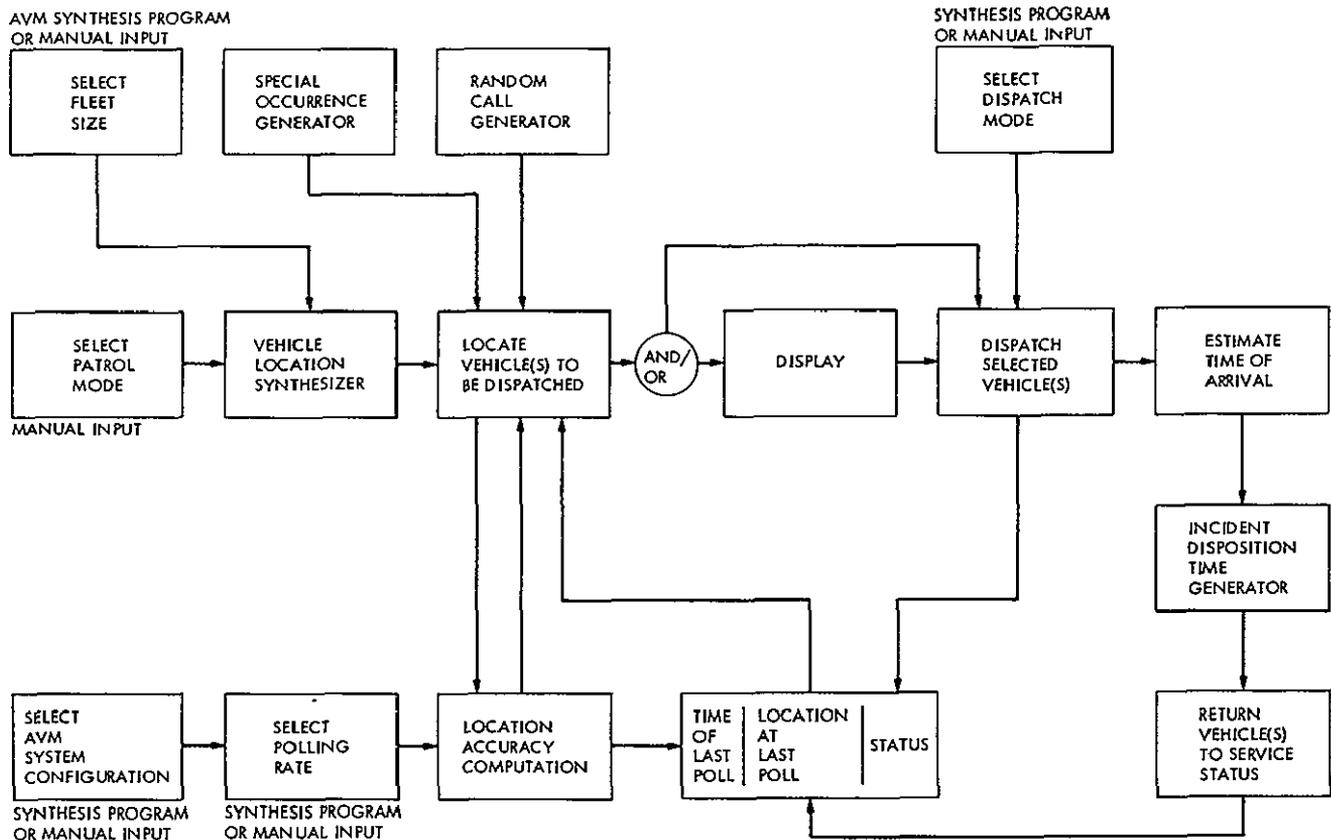


Figure 1-38. Concept for AVM System Simulation Computer Program

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**PART TWO:
AVM DATA FOR USER
GROUP ADVISORY
COMMITTEE CITIES**

G.R. Hansen

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PART TWO. AVM DATA FOR USER GROUP ADVISORY COMMITTEE CITIES

I. COST BENEFITS OF AVM SYSTEMS FOR SEVEN CITIES

A. Rationale for Selection of UGAC Cities

In order that a more realistic appraisal of the costs and expected performance of AVM Systems could be estimated, police department representatives from several cities were invited to participate in a User Group Advisory Committee (UGAC) devoted to studying AVM technologies. A set of nine criteria was established for selecting typical Southern California cities for the UGAC study. Some criteria are obvious and were established for time and economic considerations, while others were arrived at by heuristic processes. In this listing, the future tense is used because the criteria were established before city selection began. A brief rationale is presented with each criterion, to wit:

- (1) City Size. Cities in three categories, (a) less than 20 sq miles, (b) between 20 and 100 sq miles, and (c) greater than 100 sq miles, will be solicited to determine the impact on urban areas to be covered by AVM Systems.
- (2) Geography/Topography. Essentially flat as well as hilly areas in the communities are desirable to ascertain the effects on AVM methods as well as the communication data links.
- (3) Population Density/Land Use. These criteria are closely allied, and agricultural areas, industrial centers, and suburban as well as high-rise residential areas should be a part of the cities. This criterion will eliminate those cities formed to be wholly agricultural or industrial areas for tax purposes.
- (4) Building Sizes. The inclusion of high-rise dense metropolitan, low-rise business (less than 6-10 stories), mixed business and residential, and suburban areas is desirable to match and extend prior AVM work and to include the effects of these structure distributions on the communication links.
- (5) Population. Cities with populations of (a) more than 1,000,000, (b) between 200,000 and 1,000,000, and (c) less than 200,000 will be solicited. These numbers are arbitrary and are not firm, but the population somewhat determines the size of the municipal government. It is felt that this criterion is desirable as differing governing bodies will require AVM information to different degrees. Additionally, the participants in the user group will probably have different authority within their city governments as a function of population. It is believed, that those from smaller cities may be closer to the policy making level than those from major cities.
- (6) Willingness to Cooperate. This is an obvious but important criterion and is

difficult to assess beforehand. It is essential because the participants will be required to furnish data about their city as well as being regular in meeting attendance.

- (7) Pursuing or Contemplating AVM. This criterion is necessary to assure some active interest in the study effort.
- (8) Close to JPL. Economic considerations require this criterion since expense monies are not available in the grant for the participants. Additionally, regular frequent meetings are required and extensive travel time would be an additional expense to the participating city.
- (9) Must Have Public Safety Department. This is an obvious and perhaps trivial requirement, but is necessary to eliminate those cities that contract for police services with another government agency. These cities would probably fail Criterion (7) as well. This criterion is a natural outgrowth of the principal thrust of the proposed work which will focus on public safety vehicle location.

None of the foregoing criteria were intended to preclude participation by governmental bodies other than cities, such as counties. By criterion (8), only Los Angeles and possibly, San Bernardino, Ventura and Riverside counties could have been considered.

Seven cities were selected which met the majority of the criteria. Small cities were Montclair and Monterey Park. Medium cities selected were Pasadena, Long Beach, and Anaheim. The large cities were San Diego and Los Angeles.

Senior police officers from each of these cities participated in the UGAC and provided information concerning police operations and plans as well as statistical data for the individual cities.

B. Parameters Used in AVM Cost Analyses

Each UGAC city had different modes of operation and requirements regarding the implementation of AVM systems. For example, some police departments operate on a three-shift basis, while others use the ten-four plan where the officers work four 10-hour days in sequence. In responding to calls for service, some police departments use only patrolling vehicles while others dispatch the plain colored (i. e., pastels) in response to citizen calls. The inclusion of motorcycles, either two- or three-wheelers, in the AVM system was planned by some cities, but not by others. In the main, however, there is sufficient commonality of parameters to allow for automation of the AVM cost and performance estimation procedures.

1. Number of vehicles in the fleet. The total number of vehicles to be instrumented is the basis for the car cost estimates. Motorcycles were not included because a satisfactory digital message capability for motorcycles does not yet

exist. Vehicles, which in general do not respond to calls for service were also not included. The maximum and minimum number of vehicles by shift was determined and normalized to a three-shift operation. This parameter is necessary to determine vehicle polling intervals.

2. City area, street mileage, number of intersections and road segments. This information was provided by the representatives for the UGAC cities. The beat area is an important parameter which is used in the AVM system accuracy estimation, but no standard or common method of determining this parameter could be found. In some cities, the beats are correlated with the crime reporting technique. In others, the beats are periodically readjusted as determined by the average number of vehicles deployed on particular shifts. The beat size parameter is an independent variable in predicting the response-time improvement that should accrue with a given location accuracy value. For the purposes of this study, the beat size was placed at the values resulting from dividing the city area by the number of vehicles deployed. This average value assumption cannot be wholly justified when, for example, beats vary from 6 blocks to 49 square miles in size as they do in San Diego.

3. Number of signposts or fixed sites required. The fixed site enumeration parameter in Class II and IV AVM systems was determined from the data supplied concerning the number of intersections or road segments. Where the technique was dependent on the number of lanes in the segment, the average value of 2.4 lanes per street segment was assumed as in the model cities. For the Class III AVM techniques, the placement and/or the number of widely distributed fixed sites required was determined by an algorithm which was only a function of the area in the model city estimations. The boundaries and shape of the UGAC cities seemed to dictate a more realistic approach. Boundary outline maps of each city were prepared, and the most optimum placement of a grid representing the spacings for narrow-band and wide-band antennas was determined. The minimum number of sites that would be necessary was thereby determined. The assumptions made were that there were no "difficult" RF areas that would require additional coverage, and that a fixed site could be placed where needed regardless of zoning, existing structure, or geographical restrictions.

4. Costing procedure for AVM Systems in UGAC cities. The costing of the various AVM system configurations for the UGAC cities was accomplished through the use of the APL computer programming language (see Part Three). The costs of vehicle equipment, fixed sites, base equipments, and polling elements were stored in the table form by technique and cost category (e.g., equipment, installation, operation and maintenance). This assemblage forms the cost data base. The various parameters for each UGAC city are also stored in a prescribed manner as follows:

- (1) Urban area in square miles.
- (2) East to West extent in miles.
- (3) North to South extent in miles.

- (4) Road mileage.
- (5) Number of intersections.
- (6) Number of road segments.
- (7) Number of vehicles in AVM fleet.
- (8) Number of motorcycles.
- (9) Maximum number vehicles deployed in first shift.
- (10) Minimum number of vehicles deployed in first shift.
- (11) Maximum number of vehicles deployed in second shift.
- (12) Minimum number of vehicles deployed in second shift.
- (13) Maximum number of vehicles deployed in third shift.
- (14) Minimum number of vehicles deployed in third shift.
- (15) Number of dispatcher consoles.
- (16) Number of small coverage (or narrow band) Class III AVM sites.
- (17) Number of wide coverage (wide-band) Class III AVM sites.

The cost estimates (as of 1974) are compiled into the cost categories after multiplying by the appropriate parameter. The program is very simple, being really a programmed desk calculator with automatic input. The rationale for programming was to avoid a repetitious procedure of calculating fine cost categories and obtaining three totals for each of 36 AVM techniques in the seven UGAC and three model cities and to simplify future cost estimations.

C. Descriptions and Summary Analyses of UGAC Cities

In Sections II through VIII, outline maps of each UGAC city are presented along with detailed listing of each city's physical parameters, AVM cost summaries, vehicle polling cycle times, and estimates of the AVM system accuracies and 5-year cost savings. The seven selected cities were Anaheim, Long Beach, Montclair, Monterey Park, Pasadena, San Diego, and Los Angeles. Thirty-six techniques in the four AVM classes were investigated for each city. Each of the seven cities was treated as an entity, with the exception of Los Angeles which was evaluated for each of its four geographical bureaus. Additionally, because of the large number of vehicles deployed in the cities of San Diego and the four Los Angeles bureaus, the system accuracies were determined for shorter cycle times or polling intervals. That is, more than one RF channel (half-duplex) was allowed for these areas.

In this Section, the summary analyses for each UGAC city are based solely on a comparison of the estimated 5-year saving and the estimated costs (as of 1974) of particular AVM systems.

The 5-year saving is predicted on only one factor of AVM performance, namely response time improvement. There are many other aspects of AVM systems which should enter into the decision process. Many of the thirty-six listed techniques which appear viable have never been developed or tested in typical urban environments. Therefore, only the developed and/or tested concepts will be discussed in the following summary descriptions. Complete tabulations are given in Sects. II to VIII.

1. Anaheim, CA. This city might be characterized as a break-even city with response time improvement such that cost savings just equal AVM costs, but only for the dead-reckoning techniques in Class I. Anaheim is slightly smaller than the medium model city (see Part One, Sect. III) in both area and fleet size, and the cost summary indicates Class I system costs for the dead-reckoning techniques of about \$280,000. The 5-year saving is about \$300,000 for a magnetic-compass/odometer system with a system accuracy of 50 to 75 meters.

The Class II AVM systems which indicate some car saving are the wide-spaced signposts and buried magnets. The accuracies achievable are roughly 250 meters and 50 to 75 meters, respectively. The cost of the Class II wide-spaced signposts is about twice the saving, while the buried magnets may cost four times the 5-year saving.

The most accurate Class III and all Class IV systems resulted in car saving, but the cost saving was negative. (See Sect. II.)

2. Long Beach, CA. The same AVM techniques as in Anaheim are viable in this city, but because the city is slightly larger in area with a substantially bigger vehicle fleet, the costs are about \$50,000 more for the Class I dead-reckoning techniques. The 5-year savings are lower, about \$160,000, because the maximum deployment considered is less than in Anaheim.

There is a large difference between Anaheim and Long Beach in the Class II AVM systems as Long Beach has almost four times the road mileage and almost twice the number of intersections. Long Beach is unique in having a large number of named dedicated alleys in the central area which results in an intersection density of 144/km² (400 per square mile). This factor causes the Class II and Class IV techniques to have a greater number of installations than are really required. Wide-spaced signposts and buried magnets indicate car savings, but the 5-year figure is well below the systems cost. If the high central density were reduced to a more reasonable value, the disparity between cost and saving would lessen to the point where the saving would be half the cost.

The pulse TOA Class III technique and all the Class IV systems indicated car savings, but cost savings were negative. (See Sect. III.)

3. Montclair, CA. In this city, the dead-reckoning techniques of Class I AVM and most of the techniques in the other classes indicate car savings primarily because system accuracies are very high. This is a direct result of a very short polling cycle time. The 5-year savings for all systems that indicate a saving are negative and exceed a "loss" of \$200,000. The car savings are

in the order of 5% of the deployed vehicles (4 to 7), that is, 0.2 to 0.4 cars.

Despite the fact that Montclair has a wide-spaced signpost AVM system installed and operational for over a year, this analysis indicates that the cost is substantially greater than the saving. The reason this analysis is faulty in this case is that Montclair does not have either a computer in the system nor the operation and maintenance (O-M) personnel indicated as required for all systems.

The system accuracy indicated for the wide-spaced Class II signposts is about 250 meters, which is quite close to that achieved in Montclair. The installed system has an accuracy of 0.2 km (1/8 mile) with slightly fewer signposts. The system costs are quite similar for the technique if the O-M category is omitted (\$60K versus \$71K). (See Sect. IV.)

4. Monterey Park, CA. Car savings are indicated for all classes of AVM in this city. Again as in the other small city, or small model, the cost saving is near zero or negative. This city, because of the great difference between maximum and minimum deployment and short polling cycle shows a greater car saving when fewer vehicles are deployed. If the O-M costs were greatly reduced, the 5-year saving would exceed the costs. (See Sect. V.)

5. Pasadena, CA. This city is roughly half-way between the small and medium models. Again a car saving is shown in all AVM classes with negative 5-year cost savings. Again, the short polling cycle causes little degradation of achievable accuracy. The O-M costs are the principal element mitigating against a positive saving, and the value for cars saved is less than a whole car. (See Sect. VI.)

6. San Diego, CA. In this city, virtually every AVM technique indicates a positive 5-year saving.—The Class I dead-reckoning techniques system costs are exceeded by the estimated savings, and the Class III costs are close to the savings. This result occurs despite the poor system accuracies caused by relatively long polling cycles. There is a substantial car savings because the averaging of beat areas leads to results in which apparent response time improvements with very inaccurate techniques occur. More than half the area of San Diego is covered by five northern beats which causes the average beat to be 40% larger in side dimension than the average beat that would result if these five beats and the area involved were not considered. The reduction in beat dimension would cause a decrease in apparent response time improvement.

In an attempt to reduce cycle time effects, the system accuracy and cost savings calculation were also performed for three RF channels for AVM. The cost savings under these conditions for Class I systems were doubled. The savings for Class II were uniformly increased by about \$1.8 million to the point where the cost of the buried magnet system was equalled, as were the costs of the Class III pulse TOA system, by the cost saving. (See Sect. VII.)

7. Los Angeles, CA. Los Angeles was analyzed separately for each of the four bureaus

(Central, South, West, Valley), which range in area from 130 to 500 km² (50 to 200 square miles). Again as in the medium model city, all of the bureaus show a 5-year saving for most of the AVM techniques. All bureaus operate about the same number of cars, so the effect of beat size on the response time efficiency increase is greater for the larger bureaus. In overall cost savings, the Valley bureau shows the greatest saving, followed in order by the West, Central, and South Bureaus.

The AVM system accuracy and 5-year saving calculations were performed for 2 and 3 RF channels for the AVM systems for each of the bureaus. As expected, the accuracy improved to about one-half and one-third that of the one RF channel case. The 5-year saving with 3 channels showed an increase when changing from 2 to 3 RF channels that was almost twice that obtained in changing from 1 to 2 RF channels. The increase in accuracy leads to increased car savings, thereby reducing the effect of the constant O-M expenses (See Sect. VIII.)

II. Anaheim, CA, City AVM Cost Benefit Analysis Tables

Table 2-1. Anaheim, CA, City AVM Physical Parameters

CITY IS 55.5 SQUARE MILES.
 GREATEST DISTANCE IS 15.3 MILES.
 NORTH SOUTH DISTANCE IS 8 MILES
 TOTAL ROAD MILEAGE IS 456 MILES.
 THE NUMBER OF INTERSECTIONS IS 4500.
 THE ESTIMATED NUMBER OF ROAD SEGMENTS IS 4500
 THERE ARE 56 CARS IN THE FLEET.
 AND THERE ARE 0 MOTORCYCLES.
 THE NUMBER OF VEHICLES ON EACH SHIFT IS:
 FIRST SHIFT MAX. 14
 FIRST SHIFT MIN. 14
 SECOND SHIFT MAX. 12
 SECOND SHIFT MIN. 12
 THIRD SHIFT MAX. 19
 THIRD SHIFT MIN. 19
 THE NUMBER OF DISPATCHERS IS 1
 THE CITY WOULD REQUIRE 6 WIDE-BAND OR
 PULSE ANTENNA SITES AND 16 NARROW BAND
 FM ANTENNA SITES FOR 7 AND 1 MILE RADIUS COVERAGE.

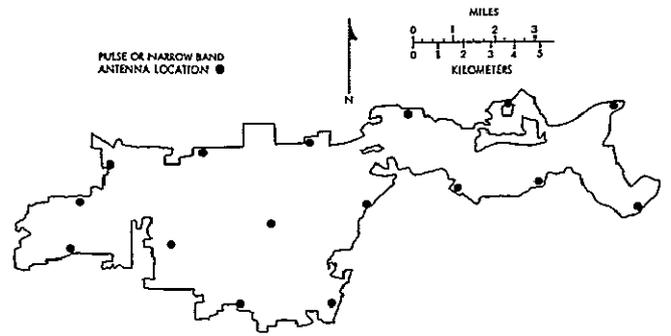


Figure 2-1. Anaheim, CA, AVM Pulse or Narrow-Band Antenna Locations

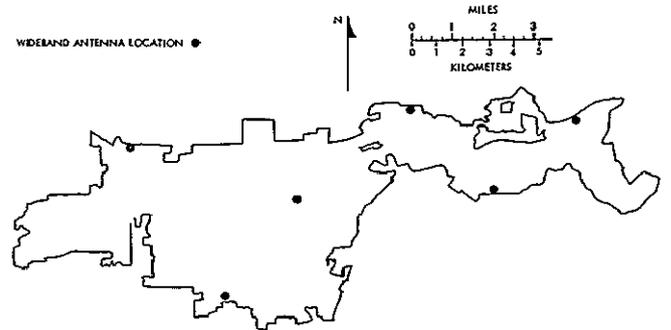


Figure 2-2. Anaheim, CA, AVM Wide-Band Antenna Locations

Table 2-2. Anaheim, CA, AVM Systems Cost Analyses

ANAHEIM CLASS I	TECHNIQUE	LAPS	THOUSANDS OF \$					TOTALS	
			CITEC	BASE	INST	O-M	UTIL	OMIC	PRODM
	KEYBOARD	5	0	54	12	101	1.2	176	176
	ST. LUS MAP	92	0	54	12	101	269	269	269
	2-ACCELEROMETERS	50	0	80	14	104	261	268	268
	LARGE VELOCITY	65	0	90	15	106	281	289	289
	ULTRASONIC VEH	40	0	90	14	106	261	268	268
	COMPASS/ODOMETER	53	0	90	11	102	261	270	270
	COMPASS/LASER VEL	67	0	90	16	104	282	290	290
	COMPASS/ULTRASONIC VEL	58	0	90	14	104	274	279	279
	OMEGA	78	0	75	13	103	274	304	304
	LUPHAI	101	0	75	13	103	298	307	306
	DECCA	72	0	75	13	103	255	247	245
	HI-STATIONS	15	0	75	12	102	210	216	215
	DIFF OMEGA	48	0	75	12	102	244	301	301
	DIFF LUPHAI	111	0	75	13	103	293	304	306
	DIFF HI-STA	17	0	75	12	102	212	219	222
	PELAY OMEGA	14	0	75	13	104	211	211	225
	PELAY LUPHAI	21	0	75	13	104	218	213	227
	CLASS II								
	BUPTED PES LOOPS	6	3226	59	5496	101	3392	3395	346
	REFLECTING SIGNS	18	1456	59	592	197	1927	1930	1921
	REFLECTING ROAD	5	116	59	704	677	1565	1568	1559
	VEHICLE POST	7	1104	59	228	173	1575	1579	1569
	HE MAP POST	6	120	59	66	114	375	378	369
	LF POST	6	600	54	228	173	1071	1074	1065
	LIGHT/1-P POST	6	460	54	277	221	1048	1051	1042
	BUPTED MAGNETS	4	220	54	657	100	1148	1152	1142
	ULTRASONIC POST	5	816	59	830	197	1912	1915	1906
	TRAFFIC SENSOR	6	912	54	396	101	1478	1482	1473
	CLASS III								
	WIDE-BAND FM PHASE	9	76	103	18	109	313	322	323
	NARROW-BAND FM PHASE	105	70	110	23	204	511	520	521
	PULSE T-0-MAPRIUM	93	224	257	56	194	313	322	323
	NOISE CORRELATION	29	29	257	14	178	516	519	520
	DIRECTION FINDER	2	74	57	16	154	310	306	306
	CLASS IV								
	TRAFFIC LOOPS	3	2343	54	1015	216	4535	4535	4535
	WAYSIDE RADIO	3	2476	54	1047	241	3974	3974	3974
	PHOTO-I-P DETECT	5	1455	59	555	221	2293	2293	2293
	ULTRASONIC DETECT	5	1503	59	555	221	2342	2342	2342

Table 2-3. Anaheim, CA, AVM Polling Cycle
Min/Max Times

CYCLE TIME IN SECONDS TO POLL MAX AND MIN UNITS DEPLOYED

CLASS I TECHNIQUE	TOTAL FLEET	SIMPLE			REDUNDANT		
		SYNC VOL	RAND VOL	SYNC VOL	RAND VOL	RAND VOL	
KEYBOARD	3 86	2 04	2 12	4 09	2 18	2 33	3 38
STYLUS MAP	4 03	1 29	1 34	2 53	1 38	1 47	4 56
2-ACCELEROMETERS	3 94	2 13	2 20	4 12	2 36	2 51	4 58
LHSEP VELOCINTR	3 94	1 31	1 39	2 64	1 49	1 58	4 58
LHSEP VELOCINTR	3 98	2 08	2 15	4 13	2 25	2 41	4 43
ULTRASONIC VELO	3 94	1 31	1 36	2 61	1 42	1 52	4 51
COMPASS/ODMETER	3 94	2 08	2 15	4 13	2 25	2 41	4 43
COMPASS/LASER VEL	3 94	1 31	1 36	2 61	1 42	1 52	4 51
COMPASS/U-SONIC VEL	3 94	2 08	2 15	4 13	2 25	2 41	4 43
OMEGA	4 25	1 31	1 36	2 61	1 42	1 52	4 51
LORAN	4 37	1 42	1 46	2 71	1 53	1 73	3 02
DECCA	4 32	2 23	2 30	4 33	2 66	2 81	3 10
HI-STATIONS	3 89	1 44	1 49	2 74	1 58	1 78	3 07
DIFF OMEGA	4 25	2 05	2 13	4 10	2 20	2 36	4 70
DIFF LORAN	4 37	1 42	1 46	2 71	1 53	1 73	3 02
DIFF HI-STA	4 22	1 42	1 46	2 71	1 53	1 73	3 02
RELAY OMEGA	303 60	191 90	191 98	193 95	381 90	382 05	384 10
RELAY LORAN	15 60	121 20	121 25	122 50	241 20	241 30	242 59
CLASS II							
DUPIED RES LOOPS	3 94	2 08	2 15	4 13	2 25	2 41	4 43
REFLECTING SIGNS	3 94	1 31	1 36	2 61	1 42	1 52	4 51
REFLECTING ROAD	3 94	2 08	2 15	4 13	2 25	2 41	4 43
A-BAND POST	3 91	1 31	1 36	2 61	1 42	1 52	4 51
HF, UHF POST	3 86	2 04	2 12	4 09	2 18	2 33	3 38
LF POST	3 91	1 30	1 35	2 60	1 41	1 50	4 43
LIGHT/I-P POST	3 91	2 06	2 14	4 12	2 23	2 38	4 43
BURIED MAGNETS	3 94	1 30	1 35	2 60	1 41	1 50	4 43
ULTRASONIC POST	3 91	2 06	2 14	4 12	2 23	2 38	4 43
TRAFFIC SENSOR	3 91	1 30	1 35	2 60	1 41	1 50	4 43

III. Long Beach, CA, City AVM Cost
Benefit Analysis Tables

Table 2-5. Long Beach, CA, City AVM
Physical Parameters

AREA IS 50.2 SQUARE MILES.
 EAST WEST DISTANCE IS 10 MILES.
 NORTH SOUTH DISTANCE IS 9.6 MILES.
 TOTAL ROAD MILEAGE IS 2000 MILES.
 THE NUMBER OF INTERSECTIONS IS 5000.
 THE ESTIMATED NUMBER OF ROAD SEGMENTS IS 10000.
 THERE ARE 61 CARS IN THE FLEET.
 AND THERE ARE 51 MOTORCYCLES.
 THE NUMBER OF VEHICLES ON EACH SHIFT IS:
 FIRST SHIFT MAY BE
 FIRST SHIFT MIN. 16
 SECOND SHIFT MAY BE
 SECOND SHIFT MIN. 16
 THIRD SHIFT MAY BE
 THIRD SHIFT MIN. 16
 THE NUMBER OF DISPATCHERS IS 2
 THE CITY WOULD REQUIRE 7 WIDE-BAND OR
 PULSE ANTENNA SITES AND 21 NARROW BAND
 ANTENNA SITES FOR 7 AND 3 MILE RADIUS COVERAGE

REPRODUCIBILITY OF THE ORIGINAL PAGE IS POOR

Table 2-4. Anaheim, CA, AVM Accuracies
and Cost Benefits

ANAHEIM CLASS I TECHNIQUE	SYSTEM ACCURACIES ULTIMATE ACCURACY	THEO VEHICLES		SYSTEM ACCURACY		ESTIMATED \$1000 VEHICLES SAVED		SAVINGS ESTIMATED 5-YEAR PERIOD
		SAVED	MIN	MIN	MAX	MIN	MAX	
KEYBOARD	30	1	4	4	7	1	1	145
STYLUS MAP	30	1	83	38	7	1	1	230
2-ACCELEROMETERS	34	1	73	95	7	1	1	230
LHSEP VELOCINTR	10	1	73	49	7	1	1	135
ULTRASONIC VELO	41	1	108	105	6	1	1	200
COMPASS/ODMETER	20	1	74	51	7	1	1	215
COMPASS/LASER VEL	15	1	74	49	7	1	1	205
COMPASS/U-SONIC VEL	17	1	74	49	7	1	1	205
OMEGA	1000	0	3914	3040	0	0	0	0
LORAN	100	1	392	381	0	0	1	305
DECCA	200	1	472	463	0	0	0	340
HI-STATIONS	200	1	470	461	0	0	0	340
DIFF OMEGA	160	1	391	384	0	0	1	305
DIFF LORAN	100	0	1081	105	0	0	0	0
DIFF HI-STA	150	1	563	55	0	0	0	0
RELAY OMEGA	500	0	6307	4115	0	0	0	0
RELAY LORAN	500	0	2215	2100	0	0	0	0
CLASS II								
DUPIED RES LOOPS	10	1	73	43	7	1	1	120
REFLECTING SIGNS	10	1	73	43	7	1	1	120
REFLECTING ROAD	3	1	71	43	7	1	1	110
A-BAND POST	12	1	73	43	7	1	1	120
HF, UHF POST	15	1	73	43	7	1	1	120
LF POST	100	1	258	252	4	0	0	440
LIGHT/I-P POST	30	1	52	30	7	1	1	135
BURIED MAGNETS	4	1	71	47	7	1	1	125
ULTRASONIC POST	20	1	74	51	7	1	1	160
TRAFFIC SENSOR	10	1	73	43	7	1	1	120
CLASS III								
WIDE-BAND FM PHASE	1000	0	238	232	0	0	0	0
WIDE-BAND FM PHASE	1200	0	2954	2889	0	0	0	0
PULSE T-O-MPHIAL	100	1	177	173	0	0	0	330
NOISE COPPELITION	100	1	146	14	0	0	0	305
DIRECTION FINDING	700	0	1830	1730	0	0	0	0
CLASS IV								
TRAFFIC LOOPS	10	1	25	25	0	0	1	130
NARROW BAND RADIO	100	1	214	22	0	0	0	1250
PHOTO-I-R DETECT	30	1	65	62	0	0	1	230
ULTRASONIC DETECT	20	1	45	43	0	0	1	330

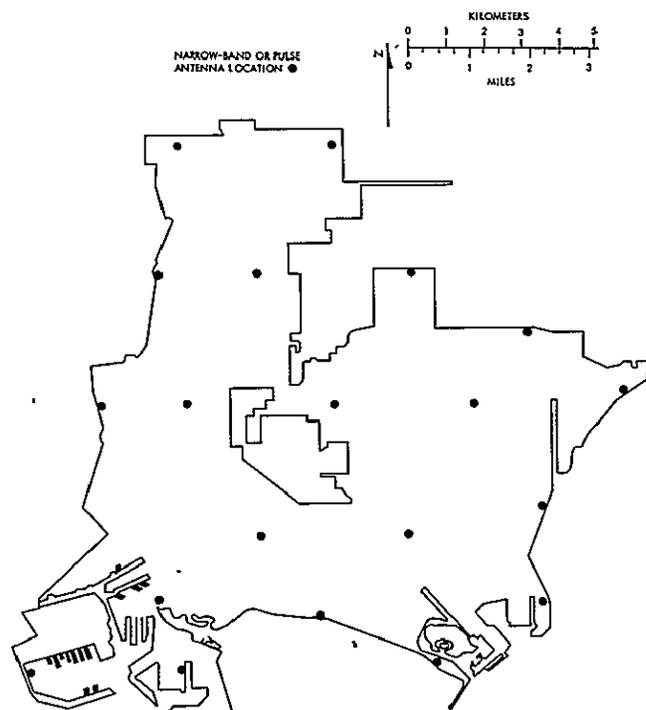


Figure 2-3. Long Beach, CA, AVM Pulse or
Narrow-Band Antenna Locations

WIDE-BAND ANTENNA LOCATION ●

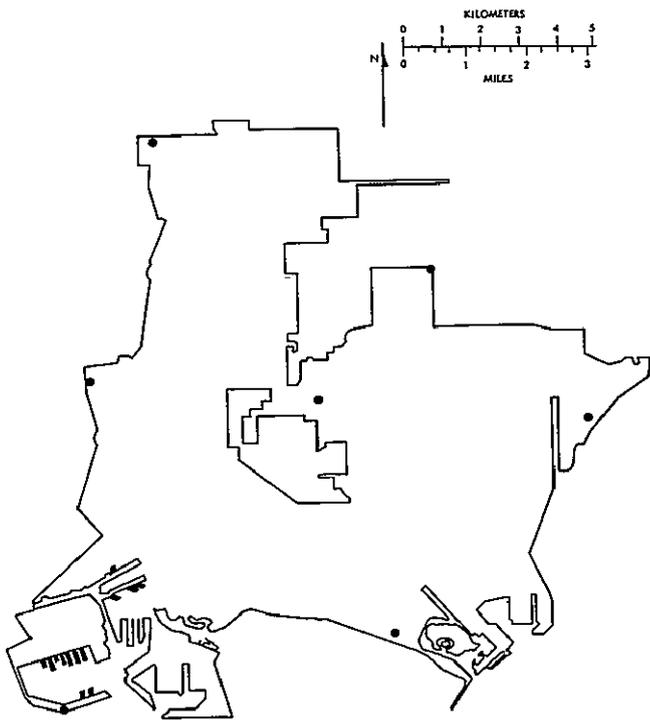


Figure 2-4. Long Beach, CA, AVM Wide-Band Antenna Locations

Table 2-7. Long Beach, CA, AVM Polling Cycle Min/Max Times

CLASS I TECHNIQUE	TOTAL FLEET	CYCLE TIME IN SECONDS TO POLL MAX AND MIN UNITS DEPLOYED							
		SYNC	SIMPLE VOL	REAR	SYNC	REDUNDANT VOL	REAR	REAR	
KEYBOARD	12 02	1 72	1 79	3 47	1 83	1 98	3 73	3 73	
STYLUS MAP	12 54	1 79	1 87	3 54	1 98	2 13	3 88	3 88	
2-ACCELEROMETERS	12 25	1 75	1 82	3 50	1 90	2 05	3 80	3 80	
LASER VELOCITP	12-40	1 77	1 85	3 52	1 94	2 09	3 84	3 84	
ULTRASONIC VELO	12-25	1 75	1 82	3 50	1 90	2 05	3 80	3 80	
COMPASS/ODOMETER	12-25	1 75	1 82	3 50	1 90	2 05	3 80	3 80	
COMPASS-LASER VEL	12-25	1 75	1 82	3 50	1 90	2 05	3 80	3 80	
COMPASS/U-SONIC VEL	12-25	1 75	1 82	3 50	1 90	2 05	3 80	3 80	
OMEGA	13 22	1 89	1 96	3 64	2 18	2 33	4 07	4 07	
LORAN	13 59	1 94	2 02	3 69	2 28	2 43	4 18	4 18	
DECCA	13 44	1 92	1 99	3 67	2 24	2 39	4 14	4 14	
ANT-STATIONS	12 10	1 73	1 80	3 48	1 86	2 01	3 75	3 75	
DIFF OMEGA	13 22	1 89	1 96	3 64	2 18	2 33	4 07	4 07	
DIFF LORAN	13 59	1 94	2 02	3 69	2 28	2 43	4 18	4 18	
DIFF ANT-STA	13 14	1 88	1 95	3 63	2 16	2 30	4 05	4 05	
RELAY OMEGA	1131-20	161 60	161 60	163 35	321 60	321 75	323 50	323 50	
RELAY LORAN	48 53	6 93	7 01	8 68	12 27	12 42	14 17	14 17	
CLASS II									
BURIED RES LOOPS	12 25	1 75	1 82	3 50	1 90	2 05	3 80	3 80	
REFLECTING SIGNS	12 25	1 75	1 82	3 50	1 90	2 05	3 80	3 80	
REFLECTING ROAD	12 25	1 75	1 82	3 50	1 90	2 05	3 80	3 80	
X-BAND POST	12 17	1 74	1 81	3 49	1 88	2 03	3 78	3 78	
HF, UHF POST	12 02	1 72	1 79	3 47	1 83	1 98	3 73	3 73	
LF POST	12 17	1 74	1 81	3 49	1 88	2 03	3 78	3 78	
LIGHT/I-R POST	12 17	1 74	1 81	3 49	1 88	2 03	3 78	3 78	
BURIED MAGNETS	12 25	1 75	1 82	3 50	1 90	2 05	3 80	3 80	
ULTRASONIC POST	12 17	1 74	1 81	3 49	1 88	2 03	3 78	3 78	
TRAFFIC SENSOR	12 17	1 74	1 81	3 49	1 88	2 03	3 78	3 78	

Table 2-6. Long Beach, CA, AVM Systems Cost Analyses

LONG BEACH CLASS I	TECHNIQUE	CAPS	THOUSANDS OF \$		TOTAL									
			SITES	BASE	INST	OH	VOL	SYNC	PARADIM	CLASS I	ULTIMATE	VEHICLES	SAVED	ESTIMATED
	KEYBOARD	3	0	66	13	101	148	188	102	102	102	102	102	102
	STYLUS MAP	150	0	66	13	102	148	188	102	102	102	102	102	
	2-ACCELEROMETERS	90	0	90	17	107	140	182	107	107	107	107	107	
	LASER VELOCITP	109	0	99	19	110	143	185	110	110	110	110	110	
	ULTRASONIC VELO	78	0	99	17	110	142	184	110	110	110	110	110	
	COMPASS/ODOMETER	90	0	99	12	100	132	174	100	100	100	100	100	
	COMPASS/LASER VEL	114	0	99	20	106	138	180	106	106	106	106	106	
	COMPASS/U-SONIC VEL	97	0	99	17	106	138	180	106	106	106	106	106	
	OMEGA	165	0	34	15	105	137	179	105	105	105	105	105	
	LORAN	171	0	34	15	105	137	179	105	105	105	105	105	
	DECCA	71	0	34	14	105	136	178	105	105	105	105	105	
	ANT-STATIONS	25	0	34	14	105	136	178	105	105	105	105	105	
	DIFF OMEGA	165	0	34	15	105	137	179	105	105	105	105	105	
	DIFF LORAN	171	0	34	15	105	137	179	105	105	105	105	105	
	DIFF ANT-STA	29	0	34	14	105	136	178	105	105	105	105	105	
	RELAY OMEGA	32	0	34	15	107	140	182	107	107	107	107	107	
	RELAY LORAN	36	0	34	15	107	140	182	107	107	107	107	107	
	CLASS II													
	BURIED RES LOOPS	9	0	66	13	101	148	188	102	102	102	102	102	
	REFLECTING SIGNS	10	0	66	13	101	148	188	102	102	102	102	102	
	REFLECTING ROAD	8	0	66	13	101	148	188	102	102	102	102	102	
	X-BAND POST	11	0	66	13	101	148	188	102	102	102	102	102	
	HF, UHF POST	10	0	66	13	101	148	188	102	102	102	102	102	
	LF POST	10	0	66	13	101	148	188	102	102	102	102	102	
	LIGHT/I-R POST	10	0	66	13	101	148	188	102	102	102	102	102	
	BURIED MAGNETS	7	0	66	13	101	148	188	102	102	102	102	102	
	ULTRASONIC POST	9	0	66	13	101	148	188	102	102	102	102	102	
	TRAFFIC SENSOR	9	0	66	13	101	148	188	102	102	102	102	102	
	CLASS III													
	NAR-BAND FM PHASE	14	0	119	21	113	145	187	113	113	113	113	113	
	MID-BAND FM PHASE	178	0	126	26	206	266	332	206	206	206	206	206	
	PULSE T-O-APRIUAL	153	0	298	72	108	140	182	108	108	108	108	108	
	NOISE SUPPELATION	48	0	299	21	174	224	284	174	174	174	174	174	
	DIRECTION FINDER	3	0	67	16	154	204	264	154	154	154	154	154	
	CLASS IV													
	TRAFFIC LOOPS	5	0	66	13	101	148	188	102	102	102	102	102	
	NAYSIDE PHDIO	5	0	66	13	101	148	188	102	102	102	102	102	
	PHOTO-I-P DETECT	3	0	66	13	101	148	188	102	102	102	102	102	
	ULTRASONIC DETECT	3	0	66	13	101	148	188	102	102	102	102	102	

Table 2-8. Long Beach, CA, AVM Accuracies and Cost Benefits

LONG BEACH	CLASS I TECHNIQUE	ULTIMATE ACCURAC	3-STEP ACCURACIES (4) VEHICLES AND ESTIMATED \$1000 SAVINGS				ESTIMATED 5-YEAR SAVING	
			VEHICLES SAVED	MIN ACCURAC	MIN SAVING	MIN SAVING		
	KEYBOARD	33	1	43	93	0 4	0 4	170
	STYLUS MAP	30	1	42	92	0 4	0 4	165
	2-ACCELEROMETERS	24	1	47	97	0 4	0 4	140
	LASER VELOCITP	13	1	65	65	0 9	0 9	120
	ULTRASONIC VELO	48	1	107	107	0 9	0 9	120
	COMPASS/ODOMETER	20	1	65	65	0 9	0 9	160
	COMPASS/LASER VEL	15	1	64	64	0 9	0 9	145
	COMPASS/U-SONIC VEL	17	1	64	64	0 9	0 9	145
	OMEGA	1500	0	3880	3380	0 0	0 0	0
	LORAN	160	0	309	309	0 3	0 3	100
	DECCA	200	0	469	469	0 1	0 1	100
	ANT-STATIONS	200	0	469	469	0 1	0 1	100
	DIFF OMEGA	160	0	309	309	0 3	0 3	100
	DIFF LORAN	400	0	1073	1073	0 0	0 0	0
	DIFF ANT-STA	250	0	565	565	0 0	0 0	0
	RELAY OMEGA	300	0	534	534	0 0	0 0	0
	RELAY LORAN	300	0	534	534	0 0	0 0	0
	CLASS II							
	BURIED RES LOOPS	10	1	64	64	0 4	0 4	170
	REFLECTING SIGNS	10	1	64	64	0 4	0 4	165
	REFLECTING ROAD	8	1	62	62	0 4	0 4	140
	X-BAND POST	12	1	64	64	0 4	0 4	120
	HF, UHF POST	15	1	63	63	0 4	0 4	120
	LF POST	10	1	64	64	0 4	0 4	120
	LIGHT/I-R POST	10	1	64	64	0 4	0 4	120
	BURIED MAGNETS	7	1	62	62	0 4	0 4	120
	ULTRASONIC POST	9	1	64	64	0 4	0 4	120
	TRAFFIC SENSOR	9	1	64	64	0 4	0 4	120
	CLASS III							
	NAR-BAND FM PHASE	1000	0	2467	2467	0 0	0 0	0
	MID-BAND FM PHASE	1200	0	2430	2430	0 0	0 0	0
	PULSE T-O-APRIUAL	100	0	175	175	0 7	0 7	115
	NOISE SUPPELATION	100	0	176	176	0 7	0 7	115
	DIRECTION FINDER	700	0	1815	1815	0 0	0 0	0
	CLASS IV							
	TRAFFIC LOOPS	10	1	25	25	1 0	1 0	115
	NAYSIDE PHDIO	100	1	221	221	0 0	0 0	1305
	PHOTO-I-P DETECT	30	1	64	64	0 4	0 4	120
	ULTRASONIC DETECT	20	1	45	45	1 0	1 0	115

IV. Montclair, CA, City AVM Cost Benefit Analysis Tables

Table 2-9. Montclair, CA, City AVM Physical Parameters

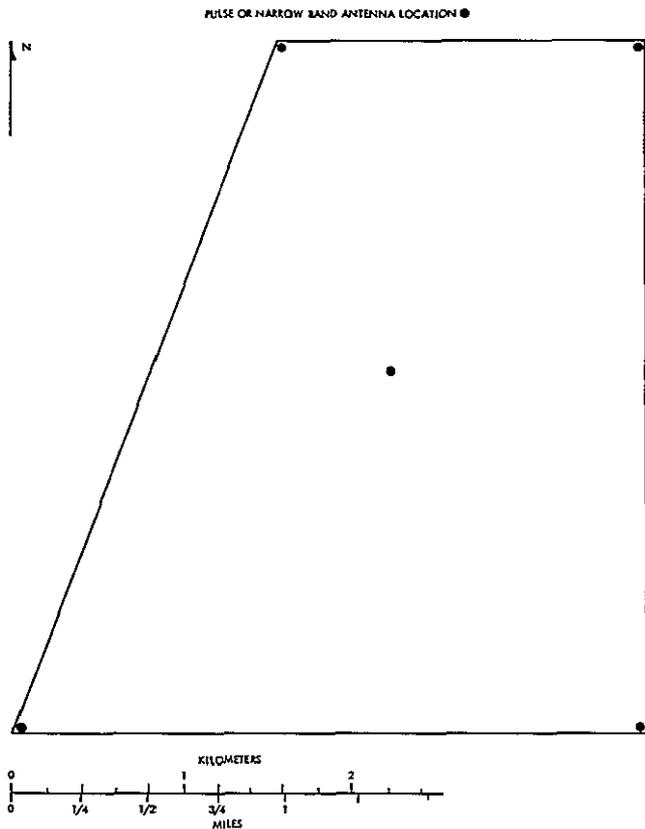


Figure 2-5. Montclair, CA, AVM Pulse or Narrow-Band Antenna Locations

AREA IS 5.2 SQUARE MILES.
 EAST WEST DISTANCE IS 2.3 MILES.
 NORTH SOUTH DISTANCE IS 2.5 MILES.
 TOTAL ROAD MILEAGE IS 67 MILES.
 THE NUMBER OF INTERSECTIONS IS 333.
 THE ESTIMATED NUMBER OF ROAD SEGMENTS IS 506.
 THERE ARE 10 CARS IN THE FLEET.
 AND THERE ARE 0 MOTORCYCLES.
 THE NUMBER OF VEHICLES ON EACH SHIFT IS:
 FIRST SHIFT MAX. 5
 FIRST SHIFT MIN. 4
 SECOND SHIFT MAX. 5
 SECOND SHIFT MIN. 4
 THIRD SHIFT MAX. 7
 THIRD SHIFT MIN. 7
 THE NUMBER OF DISPATCHERS IS 1

THE CITY WOULD REQUIRE 5 WIDE-BAND OR PULSE ANTENNA SITES AND 5 NARROW BAND FM ANTENNA SITES FOR 7 AND 3 MILE RADIUS COVERAGE.

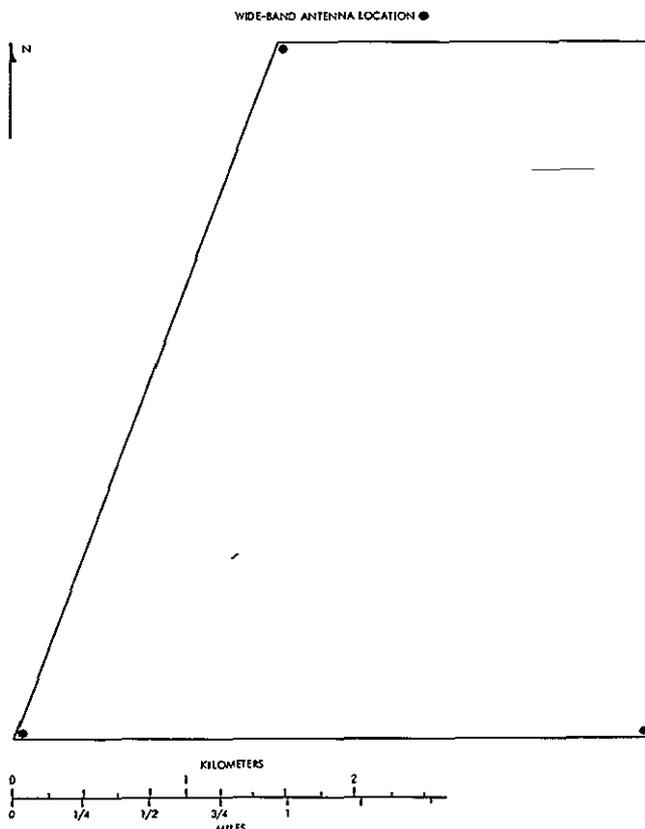


Figure 2-6. Montclair, CA, AVM Wide-Band Antenna Locations

Table 2-10. Montclair, CA, AVM Systems Cost Analyses

MONTCLAIR CLASS I	TECHNIQUE	CARS	THOUSANDS OF \$			TOTALS			
			SITES	EASE	INST	O-H	W/L	S.HC	PAIDON
	VE/BOARD	2	0	40	11	101	159	157	157
	STYLUS MAP	20	0	45	11	101	133	182	132
	2-ACCELEROMETERS	10	0	68	11	101	190	200	200
	LASEP VELOCIMET	10	0	70	12	102	209	205	204
	ULTRASONIC VELU	10	0	70	11	102	197	199	199
	CUMPHSC/ODOMETER	15	0	70	11	101	197	199	199
	CUMPHSC/LASER VEL	15	0	70	12	101	200	205	204
	CUMPHSC/U-SONIC VEL	15	0	70	11	101	200	202	201
	OMEGA	27	0	55	11	101	196	198	198
	LOFAN	28	0	55	11	101	197	199	199
	DECCA	12	0	55	11	101	190	183	182
	RF-STATIONS	7	0	55	11	101	172	174	174
	DIFF. OMEGA	27	0	55	11	101	196	198	198
	DIFF. LOFAN	23	0	55	11	101	197	199	199
	DIFF. RF-STA	5	0	55	11	101	173	175	176
	PELA, OMEGA	7	0	55	11	101	174	173	177
	PELA, LOFAN	6	0	55	11	101	175	174	177
	CLASS II								
	BUDED ACS LOOPS	2	110	45	147	101	454	455	453
	REFLECTING SIGNS	5	56	45	42	106	255	256	253
	REFLECTING ROAD	2	7	45	48	131	232	203	230
	X-BAND POST	2	78	45	26	106	257	256	256
	HF, UHF POST	2	9	45	15	102	170	174	171
	LF POST	2	43	45	26	106	222	223	220
	LIGHT/I-P POST	2	34	45	30	103	220	221	219
	BUDED MAGNETS	1	11	45	33	100	191	132	190
	ULTRASONIC POST	2	44	45	54	106	251	252	247
	TRAFFIC SENSOR	2	49	45	31	101	227	229	226
	CLASS III								
	NAR-BAND FM PHASE	3	24	54	11	103	199	201	202
	MID-BAND FM PHASE	30	35	72	15	202	303	350	350
	PULSE T-O-RAPPHUL	28	70	143	24	174	441	443	444
	NOISE CORRELATION	3	29	143	16	177	374	375	375
	DIRECTION FINDER	1	79	35	15	154	284	282	282
	CLASS IV								
	TRAFFIC LOOPS	1	229	45	103	109	485	485	485
	WAYSIDE RADIO	1	155	45	68	113	381	381	381
	PHOTO-I-R DETECT	2	117	45	49	109	320	320	320
	ULTRASONIC DETECT	2	100	45	49	109	324	324	324

Table 2-11. Montclair, CA, AVM Polling Cycle Min/Max Times

CLASS I TECHNIQUE	TOTAL FLEET	CYCLE TIME IN SECONDS TO POLL MAX AND MIN UNITS DEPLOYED					
		SYNC	SIMPLE VOL	RAND	RECURRENT SYNC	RECURRENT VOL	RECURRENT RAND
KEYBOARD	1 07	0 75	0 77	1 49	0 80	0 84	1 58
STYLUS MAP	1 12	0 43	0 44	0 85	0 46	0 48	0 90
2-ACCELEROMETERS	1 09	0 45	0 46	0 87	0 50	0 52	1 04
LASER VELOCIMTR	1 11	0 77	0 78	1 50	0 83	0 87	1 61
ULTRASONIC VELO	1 09	0 44	0 45	0 86	0 48	0 50	0 92
COMPASS/ODOMETER	1 09	0 77	0 78	1 50	0 83	0 87	1 61
COMPASS/LASER VEL	1 09	0 44	0 45	0 86	0 48	0 50	0 92
COMPASS/U-SONIC VEL	1 09	0 77	0 78	1 50	0 83	0 87	1 61
ONEGA	1 18	0 83	0 85	1 56	0 45	0 48	1 73
LORAN	1 21	0 47	0 48	0 89	0 54	0 57	0 99
DECCA	1 20	0 84	0 86	1 58	0 48	0 51	1 75
AM-STATIONS	1 03	0 48	0 49	0 90	0 56	0 59	1 00
DIFF- ONEGA	1 18	0 43	0 44	0 85	0 46	0 48	0 91
DIFF- LORAN	1 21	0 83	0 85	1 56	0 45	0 48	1 73
DIFF AM-STA	1 17	0 47	0 48	0 89	0 54	0 57	0 99
RELAY ONEGA	101 00	78-70	70-72	71-44	140-70	140-74	141-48
RELAY LORAN	4 33	3 03	3 05	3 77	5 37	5 40	6 14
CLASS II							
BURIED RES. LOOPS	1 06	0 74	0 76	1 48	0 78	0 82	1 56
REFLECTING SIGNS	1 06	0 42	0 43	0 85	0 45	0 47	0 89
REFLECTING ROAD	1 06	0 74	0 76	1 48	0 78	0 82	1 56
X-BAND POST	1 06	0 42	0 43	0 85	0 45	0 47	0 89
HF, UHF POST	1 05	0 74	0 76	1 48	0 78	0 82	1 56
LF POST	1 06	0 42	0 43	0 85	0 45	0 47	0 89
LIGHT/1-R POST	1 06	0 74	0 76	1 48	0 78	0 82	1 56
BURIED MAGNETS	1 06	0 42	0 43	0 85	0 45	0 47	0 89
ULTRASONIC POST	1 06	0 74	0 76	1 48	0 78	0 82	1 56
TRAFFIC SENSOR	1 06	0 42	0 43	0 85	0 45	0 47	0 89

V. Monterey Park, CA, City Cost Benefit Analysis Tables

Table 2-13. Monterey Park, CA, City AVM Physical Parameters

AREA IS 7.3 SQUARE MILES.
 EAST WEST DISTANCE IS 4.6 MILES.
 NORTH SOUTH DISTANCE IS 3 MILES.
 TOTAL ROAD MILEAGE IS 101 MILES.
 THE NUMBER OF INTERSECTIONS IS 596.
 THE ESTIMATED NUMBER OF ROAD SEGMENTS IS 226.
 THERE ARE 15 CARS IN THE FLEET.
 AND THERE ARE 0 MOTORCYCLES.
 THE NUMBER OF VEHICLES ON EACH SHIFT IS:
 FIRST SHIFT MAX. 14
 FIRST SHIFT MIN. 4
 SECOND SHIFT MAX. 14
 SECOND SHIFT MIN. 4
 THIRD SHIFT MAX. 14
 THIRD SHIFT MIN. 4

THE NUMBER OF DISPATCHES IS 1

THE CITY WOULD REQUIRE 3 WIDE-BAND OF PULSE ANTENNA SITES AND 5 NARROW BAND FM ANTENNA SITES FOR 7 AND 3 MILE RADIUS COVERAGE.

Table 2-12. Montclair, CA, AVM Accuracies and Cost Benefits

CLASS I TECHNIQUE	SYSTEM ACCURACY	THEO VEHICLES SAVED	SYSTEM ACCURACY	MIN	MAX	ESTIMATED VEHICLES SAVED	\$1000 SAVINGS	ESTIMATED 5-YEAR SAVINGS
KEYBOARD	33	0	28	24	0 2	0 2	0 2	200
STYLUS MAP	30	0	77	4	0 2	0 2	0 2	200
2-ACCELEROMETERS	34	0	91	33	0 2	0 2	0 2	200
LASER VELOCIMTR	13	0	25	3+	0 2	0 2	0 2	200
ULTRASONIC VELO	40	0	103	100	0 2	0 2	0 2	200
COMPASS/ODOMETER	20	0	50	48	0 2	0 2	0 2	200
COMPASS/LASER VEL	15	0	39	30	0 2	0 2	0 2	200
COMPASS/U-SONIC VEL	17	0	43	42	0 2	0 2	0 2	200
ONEGA	1500	0	3751	3664	0 0	0 0	0 0	0
LORAN	160	0	375	367	0 0	0 0	0 0	0
DECCA	200	0	452	442	0 0	0 0	0 0	0
AM-STATIONS	200	0	375	366	0 0	0 0	0 0	0
DIFF- ONEGA	150	0	450	440	0 0	0 0	0 0	0
DIFF- LORAN	400	0	983	945	0 0	0 0	0 0	0
DIFF- AM-STA	250	0	545	532	0 0	0 0	0 0	0
RELAY ONEGA	500	0	2446	2342	0 0	0 0	0 0	0
RELAY LORAN	300	0	2110	2053	0 0	0 0	0 0	0
CLASS II								
BURIED RES. LOOPS	10	0	27	27	0 2	0 2	0 2	200
REFLECTING SIGNS	10	0	27	27	0 2	0 2	0 2	200
REFLECTING ROAD	3	0	27	15	0 2	0 2	0 2	200
X-BAND POST	12	0	32	32	0 2	0 2	0 2	200
HF, UHF POST	15	0	34	33	0 2	0 2	0 2	200
LF POST	100	0	245	239	0 2	0 2	0 2	200
LIGHT/1-R POST	30	0	77	7+	0 2	0 2	0 2	200
BURIED MAGNETS	0	0	27	15	0 2	0 2	0 2	200
ULTRASONIC POST	20	0	50	40	0 2	0 2	0 2	200
TRAFFIC SENSOR	10	0	27	27	0 2	0 2	0 2	200
CLASS III								
WIDE-BAND FM PHASE	1000	0	2370	2306	0 0	0 0	0 0	0
NARROW-BAND FM PHASE	1200	0	2914	2739	0 0	0 0	0 0	0
PULSE T-O-APPROVAL	100	0	164	16+	0 1	0 1	0 1	215
NOISE SUPPRESSION	100	0	103	103	0 1	0 1	0 1	210
DIRECTION FINDER	700	0	1743	1647	0 0	0 0	0 0	0
CLASS IV								
TRAFFIC LOOPS	10	0	26	26	0 2	0 2	0 2	200
WIDE-BAND RADIO	100	0	230	23	0 2	0 2	0 2	200
PHOTO-EYE DETECT	30	0	70	70	0 2	0 2	0 2	200
ULTRASONIC DETECT	20	0	47	43	0 2	0 2	0 2	200

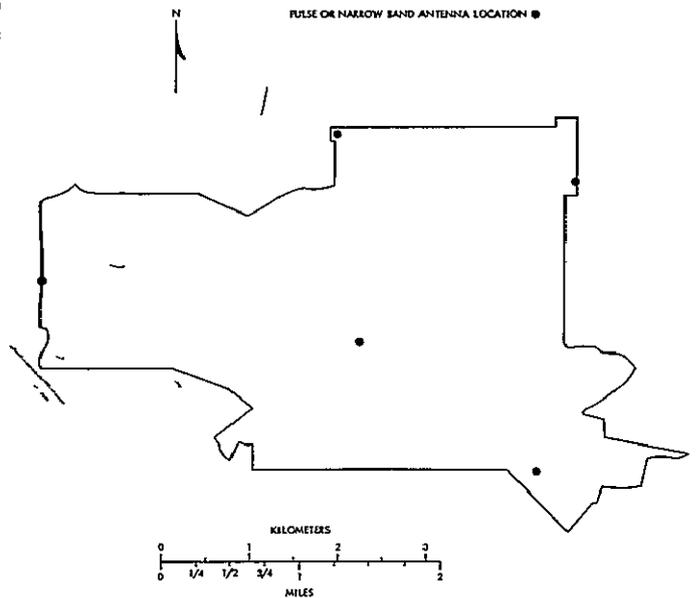


Figure 2-7. Monterey Park, CA, AVM Pulse or Narrow-Band Antennas

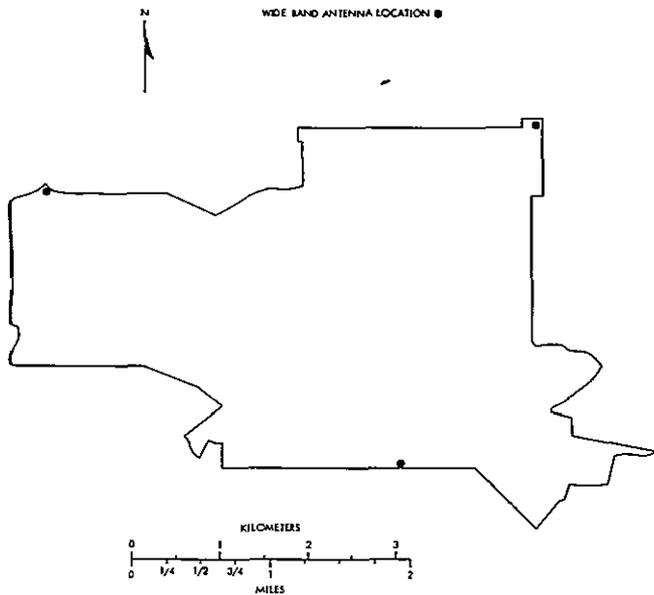


Figure 2-8. Monterey Park, CA, AVM Wide-Band Antenna Locations

Table 2-15. Monterey Park, CA, AVM Polling Cycle Min/Max Times

CLASS I TECHNIQUE	TOTAL FLEET	CYCLE TIME IN SECONDS TO POLL MAX AND MIN UNITS DEPLOYED							
		S/MC	UOL	PAND	SYNC	REDUNDANT	NOI	RAND	
KEYBOARD	1 01	1 50	1 54	2 98	1 01	1 01	1 01	1 01	
STYLUS MAP	1 68	0 43	0 44	0 35	0 46	0 43	0 43	0 43	
2-ACCELEROMETERS	1 64	1 53	1 57	3 01	1 06	1 74	0 21	0 21	
LASER VELOCINTP	1 66	0 44	0 45	0 36	0 48	0 50	0 22	0 22	
ULTRASONIC VELO	1 64	1 53	1 57	3 01	1 06	1 74	0 21	0 21	
COMPASS/ODOMETER	1 64	1 53	1 57	3 01	1 06	1 74	0 21	0 21	
COMPASS/LASEP VEL	1 64	1 33	1 57	3 01	1 06	1 74	0 21	0 21	
COMPASS-U-SONIC VEL	1 64	1 53	1 57	3 01	1 06	1 74	0 21	0 21	
OMEGA	1 77	1 05	1 09	3 13	1 06	1 98	3 45	3 45	
LORAN	1 82	1 70	1 74	3 17	2 00	2 07	3 55	3 55	
DECCA	1 80	1 08	1 72	3 16	1 96	2 03	3 51	3 51	
RM-STATIONS	1 62	1 51	1 55	2 99	1 02	1 70	3 17	3 17	
DIFF OMEGA	1 77	1 05	1 09	3 13	1 06	1 98	3 45	3 45	
DIFF LORAN	1 82	1 70	1 74	3 17	2 00	2 07	3 55	3 55	
DIFF. RM-STR	1 76	1 66	1 68	3 12	1 89	1 96	3 44	3 44	
RELAY OMEGA	151.50	141 40	141 44	142 88	281 40	281 47	282 95	282 95	
RELAY LORAN	6 50	6 07	6 10	7 54	10 73	10 81	12 28	12 28	
CLASS II									
BURIED RES LOOPS	1 00	1 49	1 53	2 97	1 59	1 66	3 14	3 14	
REFLECTING SIGNS	1 00	1 49	1 53	2 97	1 59	1 66	3 14	3 14	
REFLECTING ROAD	1 00	1 49	1 53	2 97	1 59	1 66	3 14	3 14	
X-BAND POST	1 60	1 49	1 53	2 97	1 59	1 66	3 14	3 14	
HF, VHF POST	1 58	1 47	1 51	2 95	1 55	1 62	3 18	3 18	
LF POST	1 60	1 49	1 53	2 97	1 59	1 66	3 14	3 14	
LIGHT/I-R POST	1 60	1 49	1 53	2 97	1 59	1 66	3 14	3 14	
BURIED MAGNETS	1 60	1 49	1 53	2 97	1 59	1 66	3 14	3 14	
ULTRASONIC POST	1 60	1 49	1 53	2 97	1 59	1 66	3 14	3 14	
TRAFFIC SENSOR	1 60	1 49	1 53	2 97	1 59	1 66	3 14	3 14	

Table 2-14. Monterey Park, CA, AVM Systems Cost Analyses

MONTEPE, PMP	THOUSANDS OF \$		TOTALS	
CLASS I	SITES	BASE	INST	0-N
TECHNIQUE	CHPS			
KEYBOARD	3	48	11	131
STYLUS MAP	39	43	11	191
2-ACCELEROMETERS	4	72	12	102
LASEP VELOCINTP	7	75	13	103
ULTRASONIC VELO	20	75	12	103
COMPASS/ODOMETER	22	75	11	101
COMPASS/LASEP VEL	28	75	13	102
COMPASS-U-SONIC VEL	24	75	12	102
OMEGA	11	60	12	102
LORAN	12	60	12	102
DECCA	10	60	11	102
RM-STATIONS	11	60	11	101
DIFF OMEGA	11	60	12	102
DIFF. LORAN	12	60	12	102
DIFF. RM-STR	11	60	11	101
RELAY OMEGA	6	60	12	102
RELAY LORAN	6	60	12	102
CLASS II				
BURIED RES LOOPS	3	149	3-8	101
REFLECTING SIGNS	3	149	3-8	101
REFLECTING ROAD	3	149	3-8	101
X-BAND POST	3	149	3-8	101
HF, VHF POST	3	149	3-8	101
LF POST	3	149	3-8	101
LIGHT/I-R POST	3	149	3-8	101
BURIED MAGNETS	3	149	3-8	101
ULTRASONIC POST	3	149	3-8	101
TRAFFIC SENSOR	3	149	3-8	101
CLASS III				
MAP-BAND FM PHASE	14	24	71	100
MID-BAND FM PHASE	14	30	01	100
PULSE T-O-RAPPIAL	39	70	175	170
VOICE CORRELATION	10	29	175	177
DIRECTION FINDER	1	79	41	154
CLASS IV				
TRAFFIC LOOPS	370	48	172	115
IN-SIDE RADIO	234	48	104	121
PHOTON-I-P DETECT	137	48	79	116
ULTRASONIC DETECT	133	48	79	116

Table 2-16. Monterey Park, CA, AVM Accuracies and Cost Benefits

MONTEPE, PMP	CLASS I	ULTIMATE ACCURACY	VEHICLES SAVED	VEHICLES AND SYSTEM OCCUPANCY	ESTIMATED SAVINGS	ESTIMATED SAVING
TECHNIQUE						
KEYBOARD	33	90	1	0 2	0 5	15 1
STYLUS MAP	30	81	1	0 0	0 0	1 5
2-ACCELEROMETERS	14	96	1	0 2	0 5	10 5
LASEP VELOCINTP	10	96	1	0 2	0 5	10 5
ULTRASONIC VELO	10	106	1	0 2	0 5	10 5
COMPASS/ODOMETER	20	96	1	0 2	0 5	20 5
COMPASS/LASEP VEL	15	96	1	0 2	0 5	15 5
COMPASS-U-SONIC VEL	17	96	1	0 2	0 5	17 5
OMEGA	1500	36-1	0	0 0	0 0	0 0
LORAN	100	33	0	0 0	0 0	0 0
DECCA	200	36	0	0 0	0 0	0 0
RM-STATIONS	230	36	0	0 0	0 0	0 0
DIFF OMEGA	100	36	0	0 0	0 0	0 0
DIFF LORAN	100	36	0	0 0	0 0	0 0
DIFF. RM-STR	250	36	0	0 0	0 0	0 0
RELAY OMEGA	500	36	0	0 0	0 0	0 0
RELAY LORAN	500	36	0	0 0	0 0	0 0
CLASS II						
BURIED RES LOOPS	10	50	1	0 2	0 7	10 7
REFLECTING SIGNS	10	50	1	0 2	0 7	10 7
REFLECTING ROAD	3	50	1	0 2	0 7	3 7
X-BAND POST	12	50	1	0 2	0 7	12 7
HF, VHF POST	15	50	1	0 2	0 7	15 7
LF POST	100	50	1	0 2	0 7	100 7
LIGHT/I-R POST	30	50	1	0 2	0 7	30 7
BURIED MAGNETS	1	50	1	0 2	0 7	1 7
ULTRASONIC POST	20	50	1	0 2	0 7	20 7
TRAFFIC SENSOR	10	50	1	0 2	0 7	10 7
CLASS III						
MAP-BAND FM PHASE	1000	2451	236	0 0	0 0	0 0
MID-BAND FM PHASE	1200	2311	239	0 0	0 0	0 0
PULSE T-O-RAPPIAL	100	174	164	0 1	0 2	7 4
VOICE CORRELATION	100	174	163	0 1	0 1	7 4
DIRECTION FINDER	700	1803	1697	0 0	0 0	0 0
CLASS IV						
TRAFFIC LOOPS	100	25	26	0 2	0 3	25 3
IN-SIDE RADIO	100	223	237	0 1	0 0	230 0
PHOTON-I-P DETECT	30	67	73	0 2	0 6	100 6
ULTRASONIC DETECT	20	67	73	0 2	0 7	100 7

VI. Pasadena, CA, City AVI Cost Benefit
Analysis Tables

Table 2-17. Pasadena, CA, City AVI Physical Parameters

AREA IS 63 SQUARE MILES.
 EAST WEST DISTANCE IS 6 MILES.
 NORTH SOUTH DISTANCE IS 5 MILES.
 TOTAL ROAD MILEAGE IS 350 MILES.
 THE NUMBER OF INTERSECTIONS IS 1260.
 THE ESTIMATED NUMBER OF ROAD SEGMENTS IS 2720.
 THERE ARE 35 CARS IN THE FLEET.
 AND THERE ARE 0 MOTORCYCLES.
 THE NUMBER OF VEHICLES ON EACH SHIFT IS:
 FIRST SHIFT MAX. 10
 FIRST SHIFT MIN. 10
 SECOND SHIFT MAX. 10
 SECOND SHIFT MIN. 10
 THIRD SHIFT MAX. 10
 THIRD SHIFT MIN. 10
 THE NUMBER OF DISPATCHES IS 1
 THE CITY WOULD REQUIRE 3 WIDE-BAND OR
 PULSE ANTENNA SITES AND 7 NARROW BAND
 FM ANTENNA SITES FOR 7 AND 2 MILE RADIUS COVERAGE.

Table 2-18. Pasadena, CA, AVI Systems Cost Analyses

PASADENA CLASS I	THOUSANDS OF \$				TOTAL			
TECHNIQUE	CHPS	SITES	BASE	INST	O-II	MUL	SYN	RAIDON
VEYSUNFD	0	0	57	12	101	120	170	170
ST/LUS MAP	40	0	57	12	101	120	200	200
2-MICROPHONETERS	56	0	70	10	100	200	200	200
LASEF VELOCIMTR	60	0	87	15	106	275	282	281
ULTRASONIC VELO	45	0	87	10	106	256	260	261
COMPASS/ODOMETER	52	0	87	11	102	256	265	261
COMPASS/LACEP VEL	65	0	37	16	104	276	235	281
COMPASS/ULTRASONIC VEL	56	0	37	14	104	265	270	270
ORIGA	55	0	70	13	103	288	297	295
LORAN	90	0	70	10	103	292	301	299
DECCA	41	0	70	13	103	290	292	291
NAVIGATIONS	14	0	42	10	103	305	213	211
DIFF ORIGA	45	0	70	10	103	288	295	295
DIFF LORAN	98	0	70	10	103	292	290	290
DIFF AN-SYS	17	0	70	10	100	260	215	210
RELA ORIGA	13	0	70	10	100	210	207	201
RELA LORAN	21	0	70	10	104	215	204	200
CLASS II								
BUPIED RES LOOPS	5	107	57	180	101	203	306	307
REFLECTING SIGNS	17	10	57	20	100	205	200	200
REFLECTING ROAD	5	5	57	20	100	210	210	210
7-3RD POST	0	100	37	20	100	210	210	210
HF, IHF POST	0	0	57	20	100	210	210	210
LF FUJ	0	200	37	20	100	210	210	210
LIGHT-T-R POST	0	180	57	115	100	210	210	210
BUPIED MAGNETS	0	100	57	20	100	210	210	210
ULTRASONIC POST	5	317	57	300	100	210	210	210
TRAFFIC SENCOP	0	354	57	100	100	210	210	210
CLASS III								
WIDE-BAND FM PHASE	0	33	90	13	100	207	205	200
NARROW-BAND FM PHASE	102	35	105	10	100	400	471	470
PULSE T-O-ARRIVAL	91	98	240	23	100	600	657	650
NOISE CORRELATION	20	29	200	18	100	500	500	500
DIRECTION FINDER	2	79	0	10	100	300	300	300
CLASS IV								
TRAFFIC LOOPS	3	1037	57	517	100	200	200	200
WIDE-BAND RADIO	0	100	57	20	100	200	200	200
PHOTO-T-R DETECT	0	200	57	20	100	200	200	200
ULTRASONIC DETECT	5	413	57	200	100	200	200	200

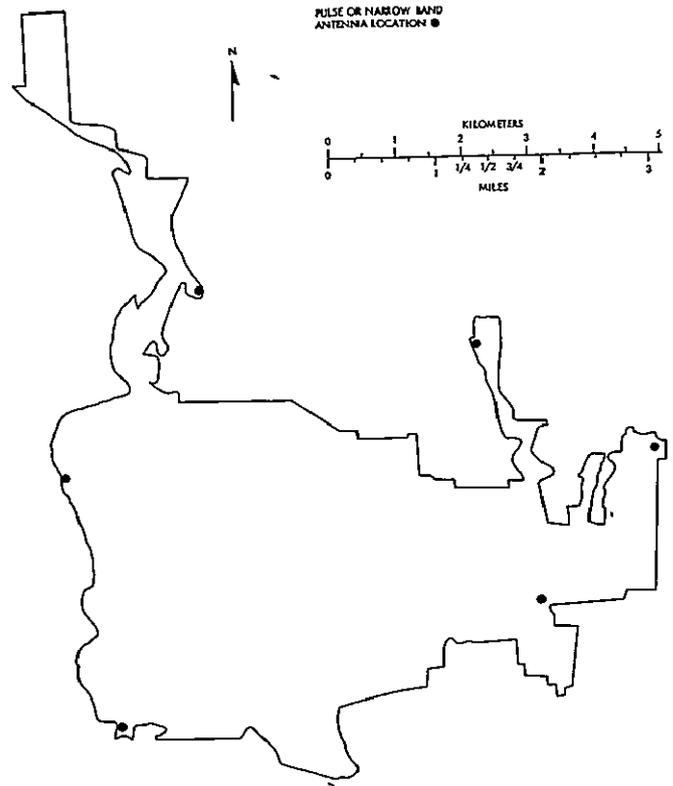


Figure 2-9. Pasadena, CA, AVI Pulse or Narrow-Band Antenna Locations

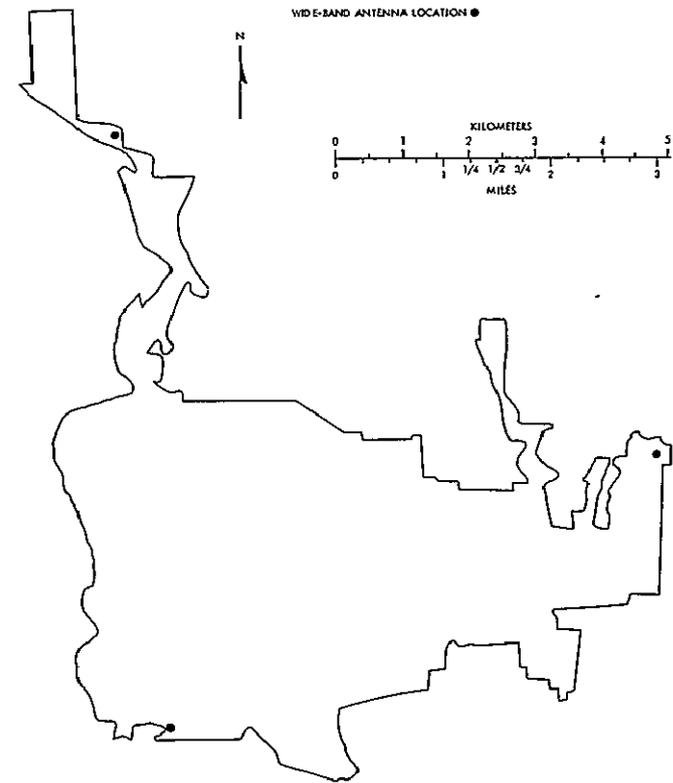


Figure 2-10. Pasadena, CA, AVI Wide-Band Antenna Locations

Table 2-19. Pasadena, CA, AVM Polling Cycle Min/Max Times

VII. San Diego, CA, City AVM Cost Benefit Analysis Tables

CYCLE TIME IN SECONDS TO POLL MAX AND MIN UNITS DEPLOYED

CLASS I TECHNIQUE	TOTAL FLEET	SIMPLE			REDUNDANT		
		SYNC	UOL	RAND	SYNC	UOL	RAND
KEYBOARD	3 76	1 07	1 11	2 15	1 15	1 23	2 31
STYLUS MAP	3 92	1 12	1 16	2 20	1 24	1 32	2 40
2-ACCELEROMETERS	3 83	1 09	1 13	2 17	1 17	1 27	2 35
LASER VELOCIMTR	3 87	1 11	1 15	2 19	1 21	1 29	2 37
ULTRASONIC WELD	3 83	1 09	1 13	2 17	1 19	1 27	2 35
COMPASS/ODOMETEP	3 83	1 09	1 13	2 17	1 19	1 27	2 35
COMPASS/LASER VEL	3 83	1 09	1 13	2 17	1 19	1 27	2 35
COMPASS-U-SONIC VEL	3 83	1 09	1 13	2 17	1 19	1 27	2 35
OMEGA	4 13	1 18	1 22	2 26	1 30	1 41	2 52
LORAN	4 25	1 21	1 25	2 29	1 43	1 51	2 59
DECCA	4 25	1 21	1 25	2 29	1 43	1 51	2 59
RF-STATIONS	3 78	1 08	1 12	2 16	1 16	1 24	2 32
DIFF OMEGA	4 13	1 18	1 22	2 26	1 36	1 44	2 52
DIFF LORAN	4 25	1 21	1 25	2 29	1 43	1 51	2 59
DIFF RF-STA	4 11	1 17	1 21	2 25	1 32	1 41	2 51
RELAY OMEGA	353 50	101 00	101 04	102 08	201 00	201 06	202 16
RELAY LORAN	15 17	4 33	4 37	5 41	7 67	7 73	8 83
CLASS II							
BURIED RES LOOPS	3 78	1 08	1 12	2 16	1 16	1 24	2 32
REFLECTING SIGNS	3 73	1 08	1 12	2 16	1 16	1 24	2 32
REFLECTING ROAD	3 78	1 08	1 12	2 16	1 16	1 24	2 32
X-BAND POST	3 76	1 07	1 11	2 15	1 15	1 23	2 31
HF, VHF POST	3 71	1 06	1 10	2 14	1 12	1 20	2 28
LF POST	3 76	1 07	1 11	2 15	1 15	1 23	2 31
LIGHT/I-R POST	3 76	1 07	1 11	2 15	1 15	1 23	2 31
BURIED MAGNETS	3 78	1 08	1 12	2 16	1 16	1 24	2 32
ULTRASONIC POST	3 76	1 07	1 11	2 15	1 15	1 23	2 31
TRAFFIC SENSOR	3 76	1 07	1 11	2 15	1 15	1 23	2 31

Table 2-21. San Diego, CA, City AVM Physical Parameters

AREA IS 331 SQUARE MILES.
 EAST WEST DISTANCE IS 23.6 MILES.
 NORTH SOUTH DISTANCE IS 41.2 MILES.
 TOTAL ROAD MILEAGE IS 1945 MILES.
 THE NUMBER OF INTERSECTIONS IS 13700.
 THE ESTIMATED NUMBER OF ROAD SEGMENTS IS 27400.
 THERE ARE 300 CARS IN THE FLEET
 AND THERE ARE 52 MOTORCYCLES.
 THE NUMBER OF VEHICLES ON EACH SHIFT IS.
 FIRST SHIFT MAX. 66
 FIRST SHIFT MIN. 66
 SECOND SHIFT MAX. 95
 SECOND SHIFT MIN. 95
 THIRD SHIFT MAX. 60
 THIRD SHIFT MIN. 60

Table 2-20. Pasadena, CA, AVM Accuracies and Cost Benefits

PASADENA	SYSTEM ACCURACIES (%)		VEHICLES AND SYSTEM ACCURAC.		ESTIMATED \$1000 SAVINGS		ESTIMATED 5-YEAR SAVING
	ULTIMATE ACCURACY	THEO. VEHICLES	HA	MIN	HA	MIN	
TECHNIQUE							
KEYBOARD	33	1	90	90	0 5	0 5	-130
STYLUS MAP	50	1	74	74	0 5	0 5	-130
2-ACCELEROMETERS	37	1	44	44	0 5	0 5	-75
LASER VELOCIMTR	13	1	41	41	0 5	0 5	-155
ULTRASONIC WELD	40	1	10	10	0 5	0 5	-16
COMPASS/ODOMETEP	29	1	54	54	0 5	0 5	-70
COMPASS/LASER VEL	17	1	40	40	0 5	0 5	-70
COMPASS-U-SONIC VEL	17	1	40	40	0 5	0 5	-70
OMEGA	1600	0	3310	3310	0 0	0 0	0
LORAN	160	0	381	381	0 1	0 1	-40
DECCA	200	0	460	460	0 0	0 0	0
RF-STATIONS	200	0	450	450	0 0	0 0	0
DIFF OMEGA	130	0	331	331	0 1	0 1	-40
DIFF LORAN	400	0	1050	1050	0 0	0 0	0
DIFF RF-STA	250	0	550	550	0 0	0 0	0
RELAY OMEGA	500	0	3460	3460	0 0	0 0	0
RELAY LORAN	600	0	2147	2147	0 0	0 0	0
CLASS II							
BURIED RES LOOPS	10	1	40	40	0 5	0 5	-75
REFLECTING SIGNS	10	1	40	40	0 5	0 5	-75
REFLECTING ROAD	3	1	39	39	0 5	0 5	-117
X-BAND POST	12	1	40	40	0 5	0 5	-145
HF, VHF POST	15	1	40	40	0 5	0 5	-30
LF POST	100	1	250	250	0 3	0 3	-420
LIGHT/I-R POST	30	1	79	79	0 5	0 5	-305
BURIED MAGNETS	7	1	37	37	0 5	0 5	-31
ULTRASONIC POST	20	1	50	50	0 5	0 5	-145
TRAFFIC SENSOR	10	1	40	40	0 5	0 5	-55
CLASS III							
HF-BAND FBI PHASE	1000	0	2411	2411	0 0	0 0	0
HF-BAND FBI PHASE	1200	0	2364	2364	0 0	0 0	0
PULSE T-O-A ARRIVAL	100	1	172	172	0 7	0 7	-500
NOISE CORRELATION	100	1	192	192	0 7	0 7	-500
DIRECTION FINDER	700	0	1774	1774	0 0	0 0	0
CLASS IV							
TRAFFIC LOOPS	10	1	25	25	0 5	0 5	-275
WAYSIDE RADIO	100	1	220	220	0 3	0 3	-45
PHOTO-I-R DETECT	30	1	60	60	0 5	0 5	-200
ULTRASONIC DETECT	20	1	46	46	0 5	0 5	-220

THE CITY SHOULD REQUIRE 23 WIDE-BAND OR
 PULSE T-O-A ANTENNA SITES AND 85 NARROW
 BAND ANTENNA SITES WITH 7 AND 3 MILE COVERAGE RADII.

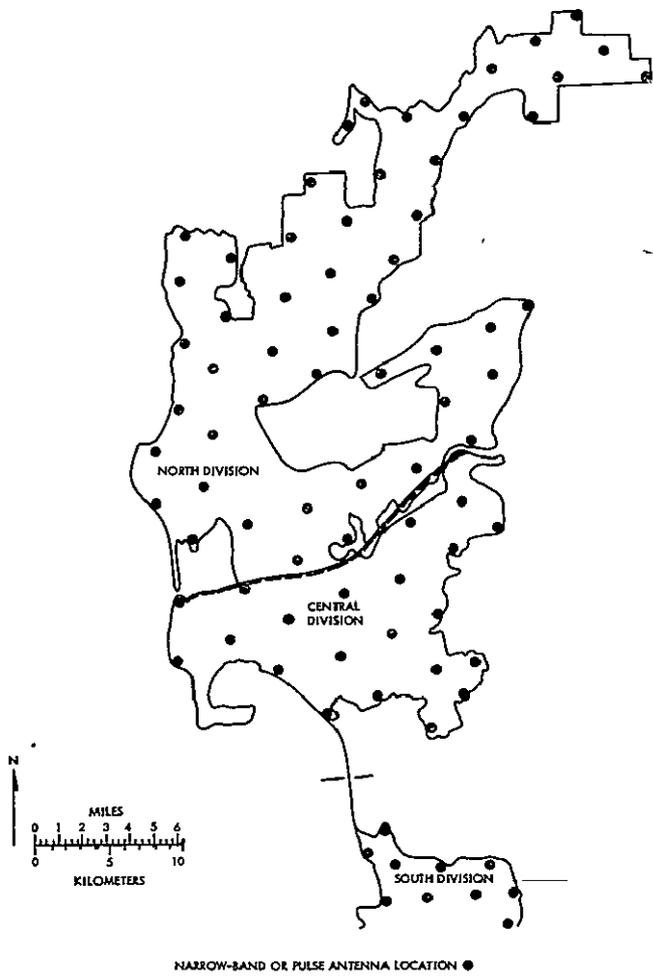


Figure 2-11. San Diego, CA, AVM Pulse or Narrow-Band Antenna Locations

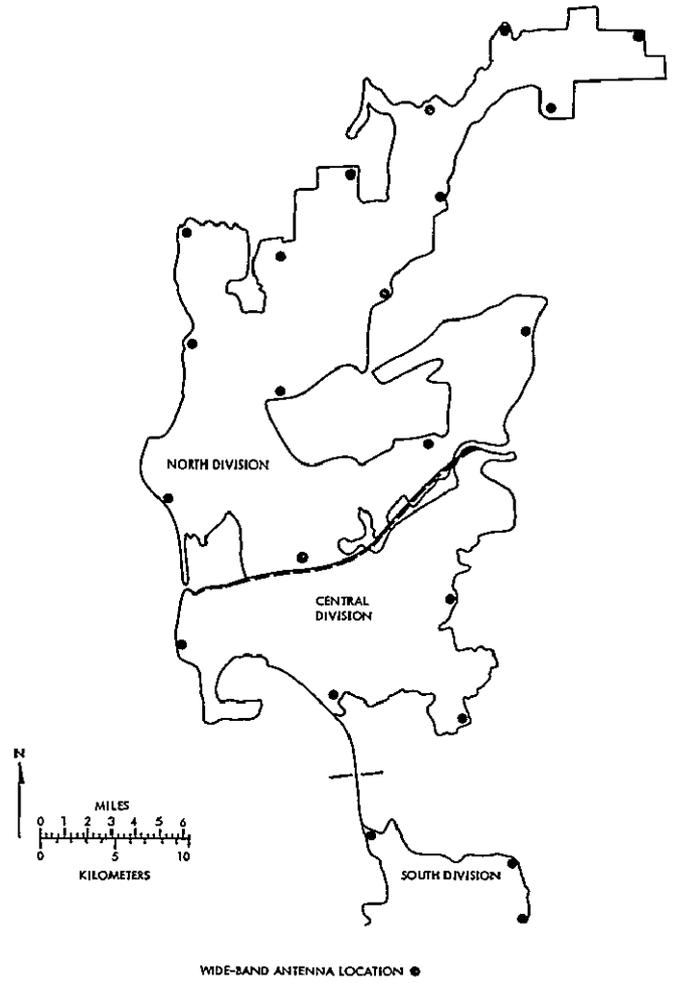


Figure 2-12. San Diego, CA, AVM Wide-Band Antenna Locations

Table 2-22. San Diego, CA, AVM Systems Cost Analyses

SAN DIEGO CLASS I	TECHNIQUE	THOUSANDS OF \$				TOTALS			
		CHPG	SITES	BASE	INST	O-H	UUL	SYNC	RANDOM
1EYBOARD	+1	0	09	21	165	503	255	255	
STYLUS MAP	765	0	09	21	108	1050	982	302	
2-ACCELEPHOMETERS	480	0	120	40	130	826	986	871	
LASEP VELOCINTP	534	0	126	51	145	406	950	755	
ULTRASONIC VELO	381	0	120	40	145	7-2	302	787	
COMPASS/ODOMETER	+40	0	128	16	112	7-4	316	735	
COMPASS/LASER VEL	557	0	123	55	127	915	487	456	
COMPASS-U-SONIC VEL	+76	0	119	40	127	810	282	351	
ONEGA	810	0	103	34	123	1107	1203	1185	
LOPAM	3-5	0	109	37	123	1157	1233	1221	
DECCA	120	0	109	29	123	653	722	717	
ARI-STATIONS	810	0	109	25	110	7-20	477	463	
DIFF ONEGA	840	0	109	34	123	1107	1101	1185	
DIFF LOPAM	140	0	109	25	118	4-40	4-97	527	
DIFF ARI-STA	152	0	109	34	150	7-7	4-31	551	
RELAY ONEGA	173	0	109	37	100	4-4	4-46	566	
RELAY LOPAM									
CLASS II									
DUPLED RES LOOPS	+2	985	09	16793	185	26240	26969	26832	
REFLECTING SIGNS	1-4	3014	89	1699	380	5974	5400	5366	
REFLECTING ROAD	33	229	09	2001	1749	4253	4282	4286	
X-BAND POST	51	3151	89	639	389	4206	4315	4333	
HF VHF POST	47	343	89	177	155	357	355	314	
LF POST	+5	1713	89	640	318	2645	2873	2737	
LIGHT/I-P POST	44	1370	89	726	510	2707	3315	3709	
DUPLED MAGNETS	00	487	89	1997	188	3650	3274	3202	
ULTRASONIC POST	+1	2329	89	2365	282	5550	5381	5205	
TRAFFIC SENSOR	+4	2603	09	1110	183	4005	4033	3357	
CLASS III									
NAR-BAND FM PHASE	15	400	176	60	150	506	931	309	
MID-BAND FM PHASE	072	267	176	72	219	1605	1683	1667	
PULSE T-O-APPRIVAL	773	1190	357	268	225	2812	2837	2895	
NOISE CORRELATION	236	29	357	45	134	888	925	732	
DIRECTION FINDER	11	80	112	19	154	411	375	375	
CLASS IV									
TRAFFIC LOOPS	04	15550	09	3745	432	13840	14440	14840	
MARSIDE RADIO	23	13573	89	3119	778	17611	17611	17611	
PHOTO-I-R DETECT	25	8767	89	1538	447	10917	10917	10917	
ULTRASONIC DETECT	33	2904	89	1578	447	11055	11055	11055	

Table 2-24. San Diego, CA, AVM Accuracies and Cost Benefits with One Radio Channel

SAN DIEGO	CLASS I	TECHNIQUE	SYSTEM ACCURACY	VEHICLES		ESTIMATED \$1000 SAVINGS	SAVINGS ESTIMATED 5-YEAR
				THEO	SAVED		
1EYBOARD	33	0	382	2-5	2-8	2-4	1-75
STYLUS MAP	50	0	4-5	253	2-7	2-0	1-35
2-ACCELEPHOMETERS	34	0	388	2-9	2-8	2-3	1-51
LASEP VELOCINTP	13	7	381	2-4	2-0	2-0	1-75
ULTRASONIC VELO	40	0	340	2-5	2-8	2-0	1-75
COMPASS/ODOMETER	20	0	322	2-3	2-8	2-0	1-75
COMPASS/LASER VEL	15	0	378	2-3	2-8	2-4	1-75
COMPASS-U-SONIC VEL	17	6	308	2-4	2-3	2-4	1-75
ONEGA	1000	0	412	0-0	0-0	0-0	0
LOPAM	100	5	413	1-9	1-7	1-7	310
DECCA	200	1	506	4-6	1-4	1-0	405
ARI-STATIONS	200	4	503	4-4	1-4	1-0	400
DIFF ONEGA	100	5	413	4-1	1-4	2-0	305
DIFF LOPAM	400	4	1167	11-2	0-0	0-0	0
DIFF ARI-STA	250	4	617	5-9	0-0	0-0	10
RELAY ONEGA	500	1	3300	28-6	0-0	0-0	0
RELAY LOPAM	300	3	2143	23-3	0-0	0-0	0
CLASS II							
DUPLED RES LOOPS	10	7	277	2-1	2-3	2-4	155
REFLECTING SIGNS	10	7	277	2-1	2-3	2-4	150
REFLECTING ROAD	3	7	122	2-3	2-9	2-6	2570
X-BAND POST	12	7	277	2-1	2-8	2-4	585
HF VHF POST	15	6	375	2-40	2-0	2-4	1265
LF POST	150	6	480	37-2	3-6	2-2	410
LIGHT/I-P POST	44	6	307	2-43	2-3	2-2	106
DUPLED MAGNETS	4	6	367	3-35	2-8	2-5	1600
ULTRASONIC POST	20	7	382	2-5	2-8	2-5	140
TRAFFIC SENSOR	10	7	375	2-40	2-8	2-5	1535
CLASS III							
NAR-BAND FM PHASE	1000	0	2690	2530	0-0	0-0	0
MID-BAND FM PHASE	1200	0	3167	3106	0-0	0-0	0
PULSE T-O-APPRIVAL	100	0	191	187	3-1	1-5	2250
NOISE CORRELATION	100	0	214	209	3-0	1-5	2250
DIRECTION FINDER	700	0	1974	1455	0-0	0-0	0
CLASS IV							
TRAFFIC LOOPS	10	7	20	23	4-0	1-0	2565
MARSIDE RADIO	100	0	203	207	3-0	1-5	2250
PHOTO-I-R DETECT	20	0	59	60	3-8	1-9	1190
ULTRASONIC DETECT	20	0	42	43	3-3	1-1	2340

Table 2-23. San Diego, CA, AVM Polling Cycle Min/Max Times

CYCLE TIME IN SECONDS TO PULL MAX AND MIN UNITS DEPLOYED

CLASS I	TECHNIQUE	TOTAL FLEET	SYNC UUL	SIMPLE UUL	PAND	RECUMBANT	FRAND
1EYBOARD	07 78	10 30	10 77	20 84	10 89	12 03	22 67
STYLUS MAP	09 42	10 64	11 21	21 28	11 78	12 92	23 06
2-ACCELEPHOMETERS	33 49	10 34	10 66	21 03	11 27	12 41	23 05
LASEP VELOCINTP	33 49	10 34	10 66	21 03	11 27	12 41	23 05
ULTRASONIC VELO	33 49	10 34	10 66	21 03	11 27	12 41	23 05
COMPASS/ODOMETER	33 49	10 34	10 66	21 03	11 27	12 41	23 05
COMPASS/LASER VEL	33 49	10 34	10 66	21 03	11 27	12 41	23 05
COMPASS-U-SONIC VEL	33 49	10 34	10 66	21 03	11 27	12 41	23 05
ONEGA	+1 54	11 21	11 78	21 05	12 92	14 06	24 70
LOPAM	42 71	11 53	12 10	22 17	13 55	14 69	25 33
DECCA	+2 24	11 40	11 57	22 04	13 30	14 44	25 08
ARI-STATIONS	33 02	10 26	10 83	20 98	11 02	12 16	22 30
DIFF ONEGA	+1 54	11 21	11 78	21 05	12 92	14 06	24 70
DIFF LOPAM	+2 71	11 53	12 10	22 17	13 55	14 69	25 33
DIFF ARI-STA	+1 38	11 15	11 72	21 79	12 79	13 93	24 57
RELAY ONEGA	3555 20	959 50	968 87	976 14	1909 58	1910 64	1921 28
RELAY LOPAM	152 53	606 06	612 72	612 72	1206 00	1206 72	1213 44
CLASS II							
DUPLED RES LOOPS	33 72	10 45	11 02	21 09	11 40	12 54	23 18
REFLECTING SIGNS	33 72	10 45	11 02	21 09	11 40	12 54	23 18
REFLECTING ROAD	33 72	10 45	11 02	21 09	11 40	12 54	23 18
X-BAND POST	33 49	10 39	10 96	21 03	11 27	12 41	23 05
HF VHF POST	33 02	10 26	10 83	20 90	11 02	12 16	22 30
LF POST	33 49	10 39	10 96	21 03	11 27	12 41	23 05
LIGHT/I-P POST	33 49	10 39	10 96	21 03	11 27	12 41	23 05
DUPLED MAGNETS	33 72	10 45	11 02	21 09	11 40	12 54	23 18
ULTRASONIC POST	33 49	10 39	10 96	21 03	11 27	12 41	23 05
TRAFFIC SENSOR	33 49	10 39	10 96	21 03	11 27	12 41	23 05

Table 2-25. San Diego, CA, AVM Accuracies and Cost Benefits with Two Radio Channels

SAN DIEGO	CLASS I	TECHNIQUE	SYSTEM ACCURACY	VEHICLES		ESTIMATED \$1000 SAVINGS	SAVINGS ESTIMATED 5-YEAR
				THEO	SAVED		
1EYBOARD	33	0	123	45	3-6	5-2	3375
STYLUS MAP	30	0	103	42	3-7	5-1	3285
2-ACCELEPHOMETERS	34	0	108	44	3-7	5-2	3290
LASEP VELOCINTP	13	7	120	60	3-7	5-2	1173
ULTRASONIC VELO	40	6	131	108	3-5	5-1	3100
COMPASS/ODOMETER	20	6	120	80	3-7	5-2	3300
COMPASS/LASER VEL	15	6	127	74	3-7	5-2	3285
COMPASS-U-SONIC VEL	17	6	128	74	3-7	5-2	3285
ONEGA	1000	0	404	3928	0-0	0-0	0
LOPAM	100	5	481	393	2-8	2-4	1025
DECCA	200	4	483	474	1-5	1-3	510
ARI-STATIONS	200	4	481	472	1-5	1-3	505
DIFF ONEGA	100	5	480	393	2-8	2-2	1025
DIFF LOPAM	400	2	1109	1105	0-0	0-0	0
DIFF ARI-STA	250	4	581	570	1-0	0-2	160
RELAY ONEGA	500	1	1994	6592	0-0	0-0	0
RELAY LOPAM	300	0	2272	2221	0-0	0-0	0
CLASS II							
DUPLED RES LOOPS	10	7	126	74	3-7	5-2	3375
REFLECTING SIGNS	10	7	126	74	3-7	5-2	3300
REFLECTING ROAD	3	7	122	76	3-7	5-2	3370
X-BAND POST	12	7	126	78	3-7	5-2	3355
HF VHF POST	15	6	150	25	3-7	5-2	1125
LF POST	150	6	130	31	3-7	5-2	1150
LIGHT/I-P POST	44	6	123	77	3-7	5-2	400
DUPLED MAGNETS	4	6	128	80	3-7	5-2	1146
ULTRASONIC POST	20	7	126	78	3-7	5-2	3305
TRAFFIC SENSOR	10	7	126	78	3-7	5-2	3305
CLASS III							
NAR-BAND FM PHASE	1000	0	2550	2494	0-0	0-0	0
MID-BAND FM PHASE	1200	0	3024	2962	0-0	0-0	0
PULSE T-O-APPRIVAL	100	0	191	167	3-1	1-5	2250
NOISE CORRELATION	100	0	214	209	3-0	1-5	2250
DIRECTION FINDER	700	0	1876	1025	0-0	0-0	0
CLASS IV							
TRAFFIC LOOPS	10	7	20	23	4-0	1-0	2565
MARSIDE RADIO	100	0	203	207	3-0	1-5	2250
PHOTO-I-R DETECT	20	0	59	60	3-8	1-9	1190
ULTRASONIC DETECT	20	0	42	43	3-3	1-1	2340

REPRODUCIBILITY OF THE ORIGINAL PAGE IS POOR

VIII. Los Angeles, CA, City AVM Cost Benefit Analysis Tables

Table 2-28. Los Angeles, CA, Central Bureau AVM Polling Cycle Times

Table 2-26. Los Angeles, CA, Central Bureau AVM Physical Parameters

AREA IS 57.5 SQUARE MILES.
 EAST WEST DISTANCE IS 9 MILES.
 NORTH SOUTH DISTANCE IS 13 MILES.
 TOTAL ROAD MILEAGE IS 1152 MILES.
 THE NUMBER OF INTERSECTIONS IS 9570.
 ONE ESTIMATED NUMBER OF ROAD SEGMENTS IS 13140.
 THERE ARE 157 CARS IN THE FLEET.
 AND THERE ARE 0 MOTORCYCLES.
 THE NUMBER OF VEHICLES ON EACH SHIFT IS:
 FIRST SHIFT MAX. 60
 FIRST SHIFT MIN. 50
 SECOND SHIFT MAX. 90
 SECOND SHIFT MIN. 30
 THIRD SHIFT MAX. 100
 THIRD SHIFT MIN. 30
 THE NUMBER OF DISPATCHERS IS 2
 THE CITY WOULD REQUIRE 2 WIDE-BAND OF
 FULSE ANTENNA SITES AND 14 NARROW BAND
 FM ANTENNA SITES FOR 7 AND 3 MILE RADIUS COVERAGE.

CYCLE TIME IN SECONDS TO POLL MAX AND MIN UNITS DEPLOYED

CLASS I TECHNIQUE	TOTAL FLEET	SYNCHRONOUS		ASYNCHRONOUS		REDUNDANT	
		MAX	MIN	MAX	MIN	MAX	MIN
KEYBOARD	16 85	10 73	11 27	21 80	11 47	12 53	23 80
STYLUS MAP	17 58	5 37	5 63	10 90	5 73	6 27	11 80
2-ACCELEROMETERS	17 17	11 20	11 73	22 27	12 40	13 47	24 33
LASER VELOCIMTR	17 38	5 60	5 87	11 13	6 20	6 73	12 27
ULTRASONIC VELO	17 17	5 47	5 73	11 00	5 93	6 47	12 00
COMPASS/ODOMETER	17 17	11 07	11 60	22 13	12 13	13 20	24 27
COMPASS-LASER VEL	17 17	5 53	5 80	11 07	6 07	6 80	12 13
CHPASS-U-SONIC VEL	17 17	18 93	11 47	22 00	11 87	12 93	24 00
OMEGA	18 53	5 47	5 73	11 00	5 93	6 47	12 00
LORAN	19 05	10 93	11 47	22 00	11 87	12 93	24 00
DECCA	18 84	5 47	5 73	11 00	5 93	6 47	12 00
AM-STATIONS	16 96	10 93	11 47	22 00	11 87	12 93	24 00
DIFF OMEGA	18 53	11 80	12 33	22 87	13 60	14 67	25 73
DIFF LORAN	19 05	5 90	6 17	11 43	6 80	7 33	12 97
DIFF AM-STA	18 42	12 13	12 67	23 20	14 27	15 33	26 40
RELAY OMEGA	1585 70	6 07	6 33	11 00	7 13	7 67	13 20
RELAY LORAN	68 03	11 73	12 27	22 80	13 47	14 53	25 60
CLASS II		5 67	6 13	11 40	6 73	7 27	12 30
BURIED RES LOOPS	17 27	1818 00	1818 53	1021 07	2018 00	2011 07	2022 13
REFLECTING SIGNS	17 27	43 33	43 87	54 40	76 67	77 73	88 80
REFLECTING ROAD	17 27	21 67	21 93	27 20	38 33	38 87	44 40
X-BAND POST	17 17	11 00	11 53	22 07	12 00	13 07	24 13
HF, VHF POST	16 96	5 58	5 77	11 03	6 00	6 53	12 07
LF POST	17 17	11 00	11 53	22 07	12 00	13 07	24 13
LIGHT/I-R POST	17 17	5 50	5 77	11 03	6 00	6 53	12 07
BURIED MAGNETS	17 27	10 93	11 47	22 00	11 87	12 93	24 00
ULTRASONIC POST	17 17	5 47	5 73	11 00	5 93	6 47	12 00
TRAFFIC SENSOR	17 17	10 93	11 47	22 00	11 87	12 93	24 00

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Table 2-27. Los Angeles, CA, Central Bureau AVM Systems Cost Analyses

Table 2-29. Los Angeles, CA, Central Bureau AVM Accuracies and Cost Benefits with One Radio Channel

LA-CENTRAL BUREAU CLASS I	THOUSANDS OF \$				TOTALS			
	CARS	SITES	BASE	INST	O-M	UOL	SYNC	RANDOM
KEYBOARD	22	0	72	16	103	237	212	212
STYLUS MAP	401	0	72	16	184	617	592	592
2-ACCELEROMETERS	232	0	100	26	116	313	549	541
LASER VELOCIMTR	280	0	100	32	124	368	599	591
ULTRASONIC VELO	230	0	100	26	124	482	519	505
COMPASS/ODOMETER	231	0	100	14	107	483	521	509
COMPASS-LASER VEL	232	0	100	34	115	573	610	594
CHPASS-U-SONIC VEL	249	0	100	26	115	520	553	542
OMEGA	424	0	92	23	112	670	717	708
LORAN	440	0	92	23	112	692	733	727
DECCA	181	0	92	20	112	429	471	463
AM-STATIONS	63	0	92	18	110	389	338	330
DIFF OMEGA	424	0	92	23	112	676	706	706
DIFF LORAN	440	0	92	23	112	692	721	727
DIFF AM-STA	74	0	92	18	110	318	348	363
RELAY OMEGA	63	0	92	23	112	338	313	376
RELAY LORAN	91	0	92	23	116	346	321	384
CLASS II								
BURIED RES. LOOPS	22	6891	72	11731	103	18843	18858	18914
REFLECTING SIGNS	76	2186	72	1182	295	3755	3770	3730
REFLECTING ROAD	28	230	72	1398	1251	2995	3010	2970
X-BAND POST	27	2202	72	447	246	3817	2032	2992
HF, VHF POST	25	240	72	124	138	623	638	597
LF POST	24	1197	72	448	246	2011	2026	1966
LIGHT/I-R POST	23	957	72	549	344	1969	1984	1944
BURIED MAGNETS	16	690	72	1396	100	2298	2312	2272
ULTRASONIC POST	22	1627	72	1651	296	3691	3706	3666
TRAFFIC SENSOR	23	1819	72	782	102	2822	2837	2797
CLASS III								
NAR-BAND FM PHASE	36	66	142	22	111	376	415	419
WIDE-BAND FM PHASE	457	24	135	28	205	847	888	890
PULSE T-O-ARRIVAL	405	190	332	69	186	1187	1326	1230
NOISE CORRELATION	124	29	332	31	181	720	734	738
DIRECTION FINDER	6	79	78	17	154	352	333	333
CLASS IV								
TRAFFIC LOOPS	13	9890	72	2616	332	12922	12922	12922
WAYSIDE RADIO	12	8608	72	2189	581	11451	11451	11451
PHOTO-I-R DETECT	19	5497	72	1103	342	7031	7031	7031
ULTRASONIC DETECT	20	5592	72	1102	342	7127	7127	7127

LA-CENTRAL BUREAU	SYSTEM ACCURACIES (%)				VEHICLES AND ESTIMATED \$1000 SAVINGS			
	ULTIMATE ACCURACY	THEO SAUED	SYSTEM ACCURACY	VEHICLES SAUED	MAX	MIN	ESTIMATED SAVINGS	5-YEAR SAVING
KEYBOARD	33	6	346	201	1 4	0 0	0	535
STYLUS MAP	30	6	410	201	1 4	0 0	0	-55
2-ACCELEROMETERS	34	6	403	205	1 4	0 0	0	470
LASER VELOCIMTR	13	6	296	201	1 4	0 0	0	-39
ULTRASONIC VELO	40	6	405	206	1 4	0 0	0	-30
COMPASS/ODOMETER	20	6	397	202	1 4	0 0	0	515
COMPASS-LASER VEL	15	7	394	200	1 4	0 0	0	-75
CHPASS-U-SONIC VEL	17	7	395	201	1 4	0 0	0	-75
OMEGA	1000	0	4199	2079	0 0	0 0	0	0
LORAN	100	2	468	408	0 0	0 0	0	0
DECCA	200	1	506	492	0 0	0 0	0	0
AM-STATIONS	200	1	504	490	0 0	0 0	0	0
DIFF OMEGA	100	2	449	408	0 0	0 0	0	0
DIFF LORAN	400	0	1169	1132	0 0	0 0	0	0
DIFF AM-STA	250	1	616	592	0 0	0 0	0	0
RELAY OMEGA	500	0	34669	17461	0 0	0 0	0	0
RELAY LORAN	300	0	2148	2022	0 0	0 0	0	0
CLASS II								
BURIED RES LOOPS	10	7	391	199	1 4	0 0	0	535
REFLECTING SIGNS	10	7	391	199	1 4	0 0	0	-25
REFLECTING ROAD	3	7	378	192	1 5	0 0	0	-510
X-BAND POST	12	7	391	199	1 4	0 0	0	-130
HF, VHF POST	15	7	390	198	1 4	0 0	0	-60
LF POST	100	7	415	201	1 4	0 0	0	-705
LIGHT/I-R POST	30	6	401	204	1 4	0 0	0	-670
BURIED MAGNETS	4	7	381	192	1 5	0 0	0	625
ULTRASONIC POST	10	6	397	202	1 4	0 0	0	430
TRAFFIC SENSOR	10	7	389	198	1 4	0 0	0	540
CLASS III								
NAR-BAND FM PHASE	1000	0	2646	2607	0 0	0 0	0	0
WIDE-BAND FM PHASE	1000	0	3173	3093	0 0	0 0	0	0
PULSE T-O-ARRIVAL	100	4	192	105	1 6	1 4	0	270
NOISE CORRELATION	100	4	215	207	1 3	0 8	0	70
DIRECTION FINDER	700	0	1984	1916	0 0	0 0	0	0
CLASS IV								
TRAFFIC LOOPS	10	7	23	23	2 2	6 3	0	3065
WAYSIDE RADIO	100	4	202	209	1 3	1 1	0	-1930
PHOTO-I-R DETECT	30	6	59	61	2 8	5 3	0	2265
ULTRASONIC DETECT	20	6	42	43	3 0	5 7	0	2565

Table 2-30. Los Angeles, CA, Central Bureau AVM Accuracies and Cost Benefits with Two Radio Channels

LA-CENTRAL BUREAU										
CLASS I TECHNIQUE	ULTIMATE ACCURACY	THEO VEHICLES SAVED	SYSTEM ACCURACY			ESTIMATED 5-YEAR SAVINGS	\$1000 SAVINGS	VEHICLES SAVED	MIN	MAX
			MAX	MIN	MAX					
KEYBOARD	33	6	201	35	2.5	1.2	1360			
STYLUS MAP	30	6	209	103	2.4	1.0	1250			
2-ACCELEROMETERS	34	10	205	101	2.4	1.1	1220			
LASER VELOCITY	13	0	101	95	2.3	1.2	1035			
ULTRASONIC VELD	+8	0	205	109	2.3	1.0	1195			
COMPASS/ODIOMETER	20	0	202	96	2.5	1.2	1340			
COMPASS-LASER VEL	15	7	200	95	2.5	1.2	1300			
CHPSS/U-SONIC VEL	17	7	201	95	2.5	1.2	1300			
OMEGA	1600	0	+079	3963	0.0	0.0	0			
LORAN	160	2	+08	397	0.0	0.0	0			
DECCA	200	1	+92	473	0.0	0.0	0			
AM-STATIONS	200	1	+90	476	0.0	0.0	0			
DIFF OMEGA	160	2	+08	396	0.0	0.0	0			
DIFF LORAN	+80	0	1132	1096	0.0	0.0	0			
DIFF AM-STA	250	1	532	575	0.0	0.0	0			
RELAY OMEGA	500	0	17461	7973	0.0	0.0	0			
RELAY LORAN	+80	0	2322	2245	0.0	0.0	0			
CLASS II										
BURIED PES LOOPS	10	7	199	94	2.5	1.3	1300			
REFLECTING SIGNS	10	7	199	94	2.5	1.3	+400			
REFLECTING ROAD	3	7	192	92	2.5	1.5	-380			
X-BAND POST	12	7	199	94	2.5	1.3	645			
HF, VHF POST	15	7	198	94	2.5	1.3	1155			
LF POST	100	4	271	262	0.3	0.0	600			
LIGHT/I-R POST	30	0	204	101	2.4	1.1	0			
BURIED MAGNETS	4	7	193	92	2.5	1.4	1375			
ULTRASONIC POST	20	0	202	96	2.5	1.2	395			
TRAFFIC SENSOR	10	7	198	94	2.5	1.3	1305			
CLASS III										
NAR-BAND FH PHASE	1000	0	2507	2521	0.0	0.0	0			
WID-BAND FH PHASE	1200	0	3082	2994	0.0	0.0	0			
PULSE T-O-ARRIVAL	100	4	192	185	1.6	1.4	270			
NOISE CORRELATION	100	4	215	207	1.3	0.0	70			
DIRECTION FINDER	700	0	1918	1855	0.0	0.0	0			
CLASS IV										
TRAFFIC LOOPS	10	7	23	23	3.2	6.3	3005			
WAYSIDE RADIO	100	4	202	209	1.3	1.1	1930			
PHOTO-I-R DETECT	30	6	59	61	2.8	5.3	2265			
ULTRASONIC DETECT	20	6	+2	43	3.0	5.7	2565			

Table 2-31. Los Angeles, CA, Central Bureau AVM Accuracies and Cost Benefits with Three Radio Channels

LA-CENTRAL BUREAU											
CLASS I TECHNIQUE	ULTIMATE ACCURACY	THEO VEHICLES SAVED	SYSTEM ACCURACY			ESTIMATED 5-YEAR SAVINGS	\$1000 SAVINGS	VEHICLES SAVED	MIN	MAX	ESTIMATED 5-YEAR SAVINGS
			MAX	MIN	MAX						
KEYBOARD	33	6	134	93	2.5	3.1	1810				
STYLUS MAP	30	6	139	92	2.6	3.0	1720				
2-ACCELEROMETERS	34	6	136	97	2.5	3.1	1670				
LASER VELOCITY	13	7	137	107	2.4	3.0	1750				
ULTRASONIC VELD	+8	6	137	107	2.4	3.0	1620				
COMPASS/ODIOMETER	20	6	134	68	2.2	3.1	1790				
COMPASS-LASER VEL	15	7	133	67	2.8	3.1	1750				
CHPSS/U-SONIC VEL	17	7	133	67	2.8	3.1	1750				
OMEGA	1600	0	4011	3896	0.0	0.0	0				
LORAN	160	2	401	390	0.0	0.0	0				
DECCA	200	1	+94	+70	0.0	0.0	0				
AM-STATIONS	200	1	+82	+68	0.0	0.0	0				
DIFF OMEGA	160	2	401	390	0.0	0.0	0				
DIFF LORAN	400	0	1111	1076	0.0	0.0	0				
DIFF AM-STA	250	1	582	566	0.0	0.0	0				
RELAY OMEGA	500	0	11529	566	0.0	0.0	0				
RELAY LORAN	+80	0	2277	2202	0.0	0.0	0				
CLASS II											
BURIED PES LOOPS	10	7	132	67	2.3	3.2	1.05				
REFLECTING SIGNS	10	7	132	67	2.3	3.2	125				
REFLECTING ROAD	3	7	127	65	2.3	3.3	-3700				
X-BAND POST	12	7	132	67	2.3	3.2	1170				
HF, VHF POST	15	7	131	67	2.3	3.2	1710				
LF POST	100	4	265	257	0.3	0.0	630				
LIGHT/I-R POST	30	6	130	82	2.6	3.1	605				
BURIED MAGNETS	4	7	128	65	2.3	3.3	1975				
ULTRASONIC POST	20	0	134	68	2.3	3.1	345				
TRAFFIC SENSOR	10	7	131	68	2.3	3.2	1.30				
CLASS III											
NAR-BAND FH PHASE	1000	0	2556	2472	0.0	0.0	0				
WID-BAND FH PHASE	1200	0	3031	2935	0.0	0.0	0				
PULSE T-O-ARRIVAL	100	4	192	185	1.6	1.4	270				
NOISE CORRELATION	100	4	215	207	1.3	0.8	70				
DIRECTION FINDER	700	0	1881	1818	0.0	0.0	0				
CLASS IV											
TRAFFIC LOOPS	10	7	23	23	3.2	6.3	3005				
WAYSIDE RADIO	100	4	202	209	1.3	1.1	1930				
PHOTO-I-R DETECT	30	6	59	61	2.8	5.3	2265				
ULTRASONIC DETECT	20	6	42	43	3.0	5.7	2565				

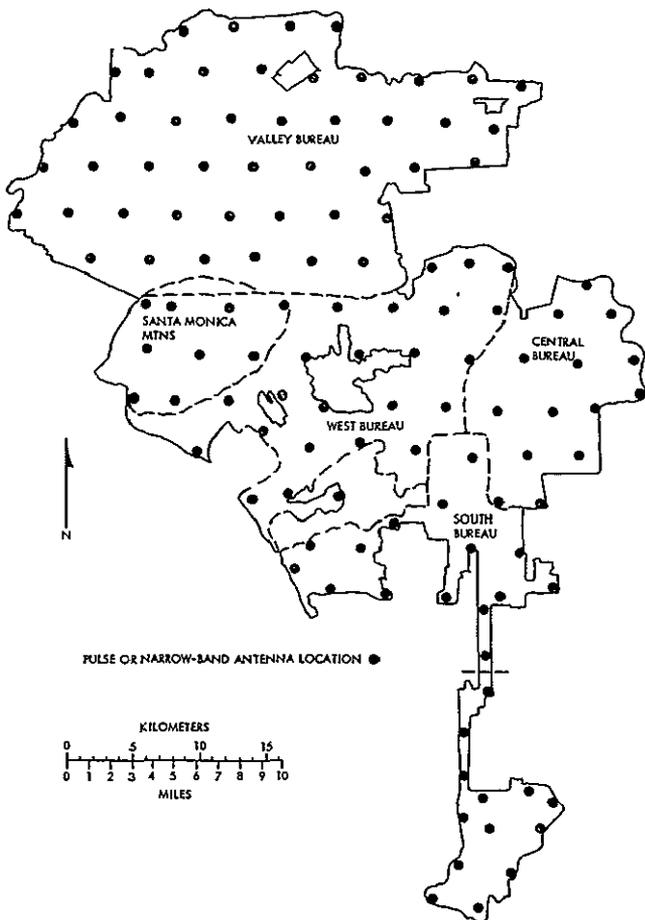


Figure 2-13. Los Angeles, CA, AVM Pulse or Narrow-Band Antennas

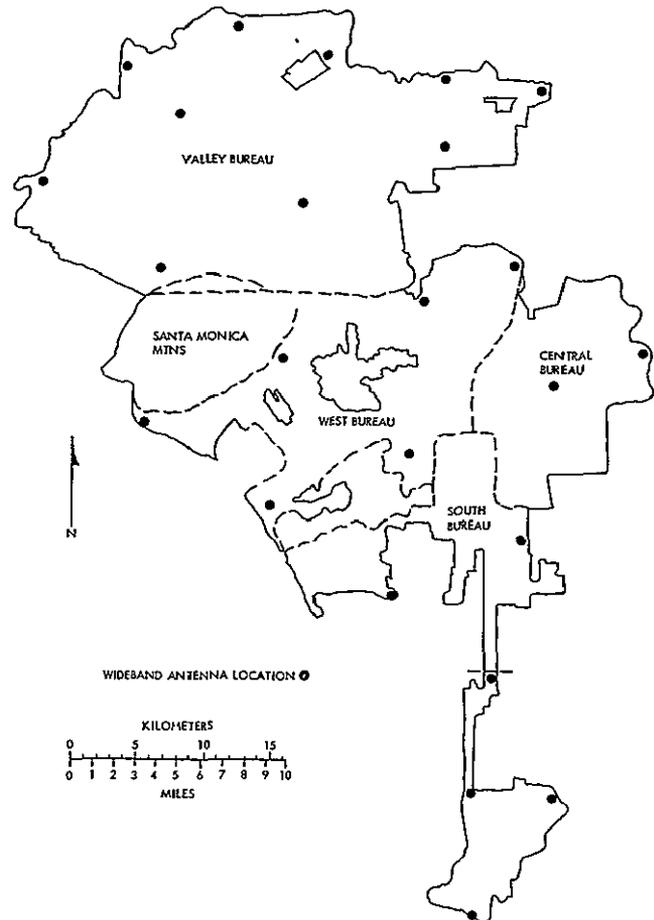


Figure 2-14. Los Angeles, CA, AVM Wide-Band Antenna Locations

Table 2-32. Los Angeles, South Bureau
AVM Physical Parameters

AREA IS 55.2 SQUARE MILES.
EAST WEST DISTANCE IS 9 MILES.
NORTH SOUTH DISTANCE IS 23 MILES.
TOTAL ROAD MILEAGE IS 973 MILES.
THE NUMBER OF INTERSECTIONS IS 6090.
THE ESTIMATED NUMBER OF ROAD SEGMENTS IS 12100.
THERE ARE 165 CARS IN THE FLEET.
AND THERE ARE 0 MOTORCYCLES.
THE NUMBER OF VEHICLES ON EACH SHIFT IS:
FIRST SHIFT MAX. 63
FIRST SHIFT MIN. 53
SECOND SHIFT MAX. 94
SECOND SHIFT MIN. 34
THIRD SHIFT MAX. 104
THIRD SHIFT MIN. 94
THE NUMBER OF DISPATCHERS IS 2
THE CITY WOULD REQUIRE 5 WIDE-BAND OR
PULSE ANTENNA SITES AND 23 NARROW BAND
FM ANTENNA SITES FOR 7 AND 3 MILE RADIUS COVERAGE.

Table 2-33. Los Angeles, South Bureau
AVM Systems Cost Analyses

LA-SOUTH BUREAU CLASS I	TECHNIQUE	THOUSANDS OF \$				TOTAL
		SITES	BASE	INST	O-M	
KEYBOARD	23	0	73	16	103	214
STYLUS MAP	421	0	73	10	105	614
2-ACCELEROMETERS	264	0	100	27	127	504
LASER VELOCINTR	294	0	100	33	133	507
ULTRASONIC VELO	210	0	109	27	126	529
COMPASS/ODOMETER	242	0	109	14	107	498
COMPASS/LASER VEL	307	0	109	35	115	592
COMPASS/U-SONIC VEL	262	0	107	27	115	507
OMEGA	452	0	93	24	113	701
LORAN	190	0	93	24	113	701
DECCA	446	0	93	24	113	701
FM-STATIONS	66	0	93	24	113	701
DIFF- OMEGA	446	0	93	24	113	701
DIFF- LORAN	452	0	93	24	113	701
DIFF- FM-STA	77	0	93	19	110	325
RELAY OMEGA	97	0	93	24	117	340
RELAY LORAN	95	0	93	24	117	328
CLASS II						
BURIED RES LOOPS	24	4093	73	6975	103	11293
REFLECTING SIGNS	80	1340	73	760	226	2510
REFLECTING ROAD	21	147	73	897	834	1997
X-BAND POST	29	1401	73	291	193	2012
HF, VHF POST	26	153	73	86	125	487
LF POST	25	762	73	232	134	1371
LIGHT/I-R POST	24	509	73	253	237	1347
BURIED MAGNETS	17	410	73	246	180	1462
ULTRASONIC POST	23	1034	73	1060	226	2443
TRAFFIC SENSOR	24	1158	73	504	102	1886
CLASS III						
NAR-BAND FM PHASE	56	109	143	27	116	431
WID-BAND FM PHASE	480	58	134	33	207	911
PULSE T-O-ARRIVAL	425	322	331	93	191	1361
NOISE CORRELATION	130	29	331	31	181	720
DIRECTION FINDER	6	79	78	17	154	353
CLASS IV						
TRAFFIC LOOPS	14	4823	73	1673	240	6829
WAYSIDE RADIO	13	4135	73	1393	407	6019
PHOTO-I-R DETECT	19	2548	73	710	253	3605
ULTRASONIC DETECT	21	2609	73	709	255	3667

Table 2-34. Los Angeles, South Bureau
AVM Polling Cycle Times

CLASS I TECHNIQUE	TOTAL FLEET	CYCLE TIME IN SECONDS TO POLL MAX AND MIN UNITS DEPLOYED					
		SYNC	SINGLE VOL	RAND	SYNC	REDUNDANT VOL	RAND
KEYBOARD	17-71	11-16	11-72	22-67	11-93	13-84	24-54
STYLUS MAP	18-48	5-69	5-97	11-55	6-88	6-64	12-51
2-ACCELEROMETERS	18-04	11-65	12-20	23-16	12-90	14-01	25-31
LASER VELOCINTR	18-26	5-94	6-22	11-80	6-57	7-14	13-00
ULTRASONIC VELO	18-04	11-37	11-93	22-88	12-34	13-45	24-96
COMPASS/ODOMETER	18-04	5-79	6-08	11-66	6-29	6-85	12-72
COMPASS/LASER VEL	18-04	11-37	11-93	22-88	12-34	13-45	24-96
COMPASS/U-SONIC VEL	18-04	5-79	6-08	11-66	6-29	6-85	12-72
OMEGA	19-47	12-27	12-83	23-78	14-14	15-25	26-76
LORAN	20-02	6-25	6-54	12-12	7-21	7-77	13-64
DECCA	19-80	12-62	13-17	24-13	14-04	15-95	27-46
FM-STATIONS	17-82	6-43	6-71	12-30	7-56	8-13	13-99
DIFF OMEGA	19-47	12-27	12-83	23-78	14-14	15-25	26-76
DIFF LORAN	20-02	6-25	6-54	12-12	7-21	7-77	13-64
DIFF- FM-STA	19-36	6-43	6-71	12-30	7-56	8-13	13-99
RELAY OMEGA	1606-50	6-22	6-50	12-08	7-14	7-70	13-57
RELAY LORAN	71-50	535-30	535-58	541-17	1065-30	1065-87	1071-73
CLASS II							
BURIED RES LOOPS	18-04	11-37	11-93	22-88	12-34	13-45	24-96
REFLECTING SIGNS	18-04	5-79	6-08	11-66	6-29	6-85	12-72
REFLECTING ROAD	18-04	11-37	11-93	22-88	12-34	13-45	24-96
X-BAND POST	17-93	5-79	6-08	11-66	6-29	6-85	12-72
HF, VHF POST	17-71	11-16	11-72	22-67	11-93	13-04	24-54
LF POST	17-93	5-69	5-97	11-55	6-08	6-64	12-51
LIGHT/I-R POST	17-93	11-30	11-86	22-81	12-20	13-31	24-82
BURIED MAGNETS	18-04	5-79	6-08	11-66	6-29	6-85	12-72
ULTRASONIC POST	17-93	11-30	11-86	22-81	12-20	13-31	24-82
TRAFFIC SENSOR	17-93	5-79	6-08	11-66	6-29	6-85	12-72

Table 2-35. Los Angeles, South Bureau
AVM Accuracies and Cost Benefits
with One Radio Channel

LA-SOUTH BUREAU	SYSTEM ACCURACIES (M), VEHICLES AND ESTIMATED \$1000 SAVINGS									
	CLASS I TECHNIQUE	ULTIMATE ACCURACY	VEHICLES SAVED	SYSTEM ACCURACY	VEHICLES SAVED	ESTIMATED SAVINGS	5-YEAR			
KEYBOARD	33	0	+11	213	1-2	0-0	305			
STYLUS MAP	30	6	425	201	1-2	0-0	375			
2-ACCELEROMETERS	34	6	418	217	1-2	0-0	315			
LASER VELOCINTR	10	7	411	213	1-2	0-0	175			
ULTRASONIC VELO	40	6	420	210	1-2	0-0	275			
COMPASS/ODOMETER	20	7	412	214	1-2	0-0	365			
COMPASS/LASER VEL	15	7	409	212	1-3	0-0	400			
COMPASS/U-SONIC VEL	17	7	410	213	1-3	0-0	400			
OMEGA	1600	0	4206	2089	0-0	0-0	0			
LORAN	150	2	470	469	0-0	0-0	0			
DECCA	200	1	507	493	0-0	0-0	0			
FM-STATIONS	200	1	505	491	0-0	0-0	0			
DIFF OMEGA	160	2	466	409	0-0	0-0	0			
DIFF LORAN	400	0	1171	1135	0-0	0-0	0			
DIFF- FM-STA	250	1	618	594	0-0	0-0	0			
RELAY OMEGA	200	0	35972	12512	0-0	0-0	0			
RELAY LORAN	300	0	2152	2329	0-0	0-0	0			
CLASS II										
BURIED RES LOOPS	10	-	-04	209	1-0	0-0	400			
REFLECTING SIGNS	10	7	404	203	1-0	0-0	155			
REFLECTING ROAD	3	7	390	202	1-4	0-0	-3120			
X-BAND POST	11	-	404	209	1-5	0-0	10			
HF, VHF POST	13	7	402	200	1-3	0-0	350			
LF POST	100	7	429	271	0-0	0-0	520			
LIGHT/I-R POST	30	6	415	215	1-0	0-0	305			
BURIED MAGNETS	4	7	394	204	1-4	0-0	500			
ULTRASONIC POST	20	7	410	213	1-3	0-0	155			
TRAFFIC SENSOR	10	7	402	204	1-0	0-0	405			
CLASS III										
NAR-BAND FM PHASE	1000	0	2702	2615	0-0	0-0	0			
WID-BAND FM PHASE	1200	0	3179	3090	0-0	0-0	0			
PULSE T-O-ARRIVAL	100	4	192	180	1-0	1-3	2-5			
NOISE CORRELATION	100	4	215	208	1-0	0-6	0			
DIRECTION FINDER	700	0	1987	1923	0-0	0-0	0			
CLASS IV										
TRAFFIC LOOPS	10	7	23	23	3-4	6-5	30-35			
WAYSIDE RADIO	100	4	202	209	1-0	1-0	-1060			
PHOTO-I-R DETECT	30	6	39	41	0-0	5-4	-275			
ULTRASONIC DETECT	20	7	42	43	3-2	5-4	-150			

Table 2-36. Los Angeles, South Bureau
AVM Accuracies and Cost Benefits
with Two Radio Channels

CLASS I TECHNIQUE	ULTIMATE ACCURACY	THEO VEHICLES SAVED		SYSTEM ACCURACY		ESTIMATED \$1000 VEHICLES SAVED		SAVINGS ESTIMATED 5-YEAR SAVING
		MAX	MIN	MAX	MIN	MAX	MIN	
KEYBOARD	33	6	209	185	2 5	0 7	1360	
STYLUS MAP	30	6	217	189	2 4	0 5	1275	
2-ACCELEROMETERS	34	6	213	187	2 4	0 6	1215	
LASER VELOCIMTR	13	7	209	185	2 5	0 7	1250	
ULTRASONIC VELO	40	6	214	188	2 4	0 6	1175	
COMPASS/ODOMETER	20	7	210	186	2 5	0 7	1300	
COMPASS/LASER VEL	15	7	208	185	2 5	0 8	1300	
CHPASS/U-SONIC VEL	17	7	209	185	2 5	0 7	1300	
OMEGA	1600	0	406	397	0 0	0 0	0	
LORAN	160	2	489	398	0 0	0 0	0	
DECCA	200	1	493	479	0 0	0 0	0	
RAI-STATIONS	200	1	491	477	0 0	0 0	0	
DIFF. OMEGA	160	2	409	397	0 0	0 0	0	
DIFF. LORAN	400	0	1134	1099	0 0	0 0	0	
DIFF. RAI-STA	250	1	593	577	0 0	0 0	0	
RELAY OMEGA	500	0	18162	8380	0 0	0 0	0	
RELAY LORAN	800	0	2327	2252	0 0	0 0	0	
CLASS II								
BURIED RES LOOPS	10	7	205	183	2 5	0 4	1360	
REFLECTING SIGNS	10	7	205	183	2 5	0 4	745	
REFLECTING ROAD	3	7	198	76	2 6	0 9	2220	
X-BAND POST	12	7	205	183	2 5	0 3	310	
HF, UHF POST	15	7	205	183	2 5	0 3	1250	
LF POST	100	4	271	262	0 7	0 0	445	
LIGHT/I-R POST	30	6	211	186	2 5	0 7	590	
BURIED MAGNETS	4	7	200	180	2 5	1 0	1375	
ULTRASONIC POST	20	7	209	185	2 5	0 8	745	
TRAFFIC SENSOR	10	7	204	183	2 5	0 4	1365	
CLASS III								
NAR-BAND FM PHASE	1000	0	2512	2528	0 0	0 0	0	
MID-BAND FM PHASE	1200	0	3088	3082	0 0	0 0	0	
PULSE T-O-ARRIVAL	100	4	192	186	1 6	1 3	245	
NOISE CORRELATION	100	4	215	208	1 3	0 6	70	
DIRECTION FINDER	700	0	1922	1860	0 0	0 0	0	
CLASS IV								
TRAFFIC LOOPS	10	7	23	23	3 4	6 5	3635	
WAYSIDE RADIO	100	4	202	209	1 3	1 0	1000	
PHOTO-I-R DETECT	30	6	59	61	3 0	5 4	2775	
ULTRASONIC DETECT	20	7	42	43	3 2	5 9	2150	

Table 2-37. Los Angeles, South Bureau
AVM Accuracies and Cost Benefits
with Three Radio Channels

CLASS I TECHNIQUE	ULTIMATE ACCURACY	THEO VEHICLES SAVED		SYSTEM ACCURACY		ESTIMATED \$1000 VEHICLES SAVED		SAVINGS ESTIMATED 5-YEAR SAVING
		MAX	MIN	MAX	MIN	MAX	MIN	
KEYBOARD	33	6	139	126	2 7	2 7	1600	
STYLUS MAP	30	6	144	82	2 7	2 7	1500	
2-ACCELEROMETERS	34	6	142	98	2 6	2 8	1515	
LASER VELOCIMTR	13	7	139	71	2 9	2 9	1550	
ULTRASONIC VELO	40	6	142	107	2 4	2 8	1475	
COMPASS/ODOMETER	20	7	139	71	2 9	2 9	1600	
COMPASS/LASER VEL	15	7	138	71	2 9	2 9	1600	
CHPASS/U-SONIC VEL	17	7	139	71	2 9	2 9	1600	
OMEGA	1600	0	4017	3906	0 0	0 0	0	
LORAN	160	2	402	391	0 0	0 0	0	
DECCA	200	1	484	471	0 0	0 0	0	
RAI-STATIONS	200	1	482	469	0 0	0 0	0	
DIFF. OMEGA	160	2	492	391	0 0	0 0	0	
DIFF. LORAN	400	0	1113	1079	0 0	0 0	0	
DIFF. RAI-STA	250	1	583	567	0 0	0 0	0	
RELAY OMEGA	500	0	12067	5922	0 0	0 0	0	
RELAY LORAN	800	0	2281	2208	0 0	0 0	0	
CLASS II								
BURIED RES LOOPS	10	7	136	70	2 9	3 0	1735	
REFLECTING SIGNS	10	7	136	70	2 9	3 0	1120	
REFLECTING ROAD	3	7	131	68	2 9	3 2	1771	
X-BAND POST	12	7	136	70	2 9	3 0	1205	
HF, UHF POST	15	7	136	70	2 9	3 0	1625	
LF POST	100	4	266	257	0 3	0 0	370	
LIGHT/I-R POST	30	6	140	82	2 7	2 9	890	
BURIED MAGNETS	4	7	133	68	2 9	2 1	1525	
ULTRASONIC POST	20	7	139	71	2 9	2 9	1605	
TRAFFIC SENSOR	10	7	136	70	2 9	3 0	1740	
CLASS III								
NAR-BAND FM PHASE	1000	0	2561	2474	0 0	0 0	0	
MID-BAND FM PHASE	1200	0	3026	2944	0 0	0 0	0	
PULSE T-O-ARRIVAL	100	4	192	186	1 6	1 3	245	
NOISE CORRELATION	100	4	215	208	1 3	0 6	71	
DIRECTION FINDER	700	0	1884	1824	0 0	0 0	0	
CLASS IV								
TRAFFIC LOOPS	10	7	23	23	3 4	6 5	3635	
WAYSIDE RADIO	100	4	202	209	1 3	1 0	1000	
PHOTO-I-R DETECT	30	6	59	61	3 0	5 4	2775	
ULTRASONIC DETECT	20	7	42	43	3 2	5 9	2150	

Table 2-38. Los Angeles, West Bureau
AVM Physical Parameters

HFEA IS 153.9 SQUARE MILES.
 EAST WEST DISTANCE IS 19 MILES.
 NORTH SOUTH DISTANCE IS 18 MILES.
 TOTAL ROAD MILEAGE IS 1677 MILES.
 THE NUMBER OF INTERSECTIONS IS 3400.
 THE ESTIMATED NUMBER OF ROAD SEGMENTS IS 16500.
 THERE ARE 193 CARS IN THE FLEET.
 AND THERE ARE 0 MOTORCYCLES.
 THE NUMBER OF VEHICLES ON EACH SHIFT IS:
 FIRST SHIFT MAX. 59
 FIRST SHIFT MIN. 33
 SECOND SHIFT MAX. 105
 SECOND SHIFT MIN. 94
 THIRD SHIFT MAX. 117
 THIRD SHIFT MIN. 95
 THE NUMBER OF DISPATCHES IS 2
 THE CITY WOULD REQUIRE 7 WIDE-BAND OF
 PULSE ANTENNA SITES AND 44 NARROW BAND
 FM ANTENNA SITES FOR 7 AND 2 MILE RADIUS COVERAGE.

Table 2-39. Los Angeles, West Bureau
AVM Systems Cost Analyses

CLASS I TECHNIQUE	LA-WEST BUREAU					TOTALS		
	CARS	SITES	BASE	INST	O-M	UOL	SYNC	RANDOM
KEYBOARD	25	0	78	17	103	252	222	222
STYLUS MAP	467	0	78	17	105	635	666	666
2-ACCELEROMETERS	293	0	116	29	119	590	616	607
LASER VELOCIMTR	325	0	116	35	120	634	679	661
ULTRASONIC VELO	233	0	116	29	128	534	570	561
COMPASS/ODOMETER	269	0	116	14	108	535	579	550
COMPASS/LASER VEL	340	0	116	38	117	639	683	664
CHPASS/U-SONIC VEL	291	0	110	29	117	575	619	600
OMEGA	495	0	98	25	114	768	809	797
LORAN	513	0	98	25	114	779	827	819
DECCA	211	0	98	21	114	470	521	512
RAI-STATIONS	74	0	98	20	111	331	366	357
DIFF. OMEGA	495	0	98	25	114	760	795	797
DIFF. LORAN	513	0	98	25	114	779	813	819
DIFF. RAI-STA	86	0	98	25	111	343	378	396
RELAY OMEGA	97	0	98	25	119	367	338	411
RELAY LORAN	106	0	98	25	119	376	347	420
CLASS II								
BURIED RES LOOPS	26	6768	78	11524	103	18528	18545	18499
REFLECTING SIGNS	88	2068	78	1166	292	3721	3738	3691
REFLECTING ROAD	23	226	78	1375	1231	2962	2979	2932
X-BAND POST	32	2162	78	441	243	2984	3081	2955
HF, UHF POST	29	235	78	124	138	631	649	602
LF POST	28	1175	78	442	244	1995	2013	1966
LIGHT/I-R POST	27	940	78	541	340	1955	1972	1925
BURIED MAGNETS	19	677	78	1372	100	2275	2292	2245
ULTRASONIC POST	25	1598	78	1624	293	3647	3664	3617
TRAFFIC SENSOR	27	1786	78	770	102	2791	2809	2762
CLASS III								
NAR-BAND FM PHASE	42	208	152	38	127	565	610	615
MID-BAND FM PHASE	532	81	154	37	209	1012	1060	1062
PULSE T-O-ARRIVAL	472	616	343	148	202	1780	1825	1830
NOISE CORRELATION	144	29	343	33	182	759	775	780
DIRECTION FINDER	7	80	91	18	154	370	348	348
CLASS IV								
TRAFFIC LOOPS	15	15470	78	2572	323	18462	18462	18462
WAYSIDE RADIO	14	13709	78	2142	572	16514	16514	16514
PHOTO-I-R DETECT	22	9114	78	1686	338	10636	10636	10636
ULTRASONIC DETECT	23	9208	78	1685	338	10731	10731	10731

Table 2-44. Los Angeles, Valley Bureau
AVM Physical Parameters

AREA IS 215.3 SQUARE MILES.
EAST WEST DISTANCE IS 23 MILES.
NORTH SOUTH DISTANCE IS 13.5 MILES.
TOTAL ROAD MILEAGE IS 2661 MILES.
THE NUMBER OF INTERSECTIONS IS 15000
THE ESTIMATED NUMBER OF ROAD SEGMENTS IS 30000;
THERE ARE 193 CARS IN THE FLEET.
AND THERE ARE 0 MOTORCYCLES.
THE NUMBER OF VEHICLES ON EACH SHIFT IS:
FIRST SHIFT MAX. 72
FIRST SHIFT MIN. 61
SECOND SHIFT MAX. 102
SECOND SHIFT MIN. 36
THIRD SHIFT MAX. 121
THIRD SHIFT MIN. 26
THE NUMBER OF DISPATCHES IS 2
THE CITY WOULD REQUIRE 10 WIDE-BAND OR
PULSE ANTENNA SITES AND 45 NARROW BAND
FM ANTENNA SITES FOR 7 AND 3 MILE RADIUS COVERAGE.

Table 2-46. Los Angeles, Valley Bureau
AVM Polling Cycle Times

CLASS I TECHNIQUE KEYBOARD	TOTAL FLEET	CIRCLE TIME IN SECONDS TO POLL MAX AND MIN UNITS DEPLOYED				REDUCED	
		SYNC	SIMPLE VUL	RAND	SYNC	VUL	RAID
KEYBOARD	20 29	12 34	13 03	26 38	13 08	15 17	28 56
STYLUS MAP	21 17	6 05	6 07	13 30	7 00	7 05	14 40
2-ACCELEROMETERS	20 66	13 23	13 08	26 02	14 36	15 05	29 04
LASEP VELOCIMTR	20 92	6 07	7 00	13 42	7 24	7 29	14 00
ULTRASONIC VELO	20 66	13 23	13 08	26 02	14 36	15 05	29 04
COMPASS/ODOMETER	20 66	6 07	7 00	13 42	7 24	7 29	14 00
COMPASS/LASER VEL	20 66	10 23	13 08	26 02	14 36	15 05	29 04
COMPASS-U-SONIC VEL	20 66	6 07	7 00	13 42	7 24	7 29	14 00
OMEGA	22 30	14 28	14 33	28 07	17 26	18 55	31 04
LORAN	22 93	14 28	14 33	28 07	17 26	18 55	31 04
DECCA	22 68	14 28	14 33	28 07	17 26	18 55	31 04
HI-STATIONS	20 41	13 07	13 71	26 46	14 04	15 32	28 72
DIFF OMEGA	22 00	14 28	14 33	28 07	17 26	18 55	31 04
DIFF LORAN	22 93	14 28	14 33	28 07	17 26	18 55	31 04
DIFF HI-STA	22 18	14 28	14 33	28 07	17 26	18 55	31 04
RELAY OMEGA	1988 90	1222 18	1222 75	2432 34	2432 10	2435 39	2446 78
RELAY LORAN	41 90	52 43	53 08	62 85	1226 10	1226 75	1232 50
CLASS II SURVED PES LOOPS	20 74	13 31	13 06	26 70	14 52	15 81	29 21
REFLECTING SIGNS	20 74	13 31	13 06	26 70	14 52	15 81	29 21
REFLECTING ROAD	20 74	13 31	13 06	26 70	14 52	15 81	29 21
N-BAND POST	20 66	13 23	13 08	26 02	14 36	15 05	29 04
HF, VHF POST	20 41	13 07	13 71	26 46	14 04	15 32	28 72
LF POST	20 66	6 07	7 00	13 42	7 24	7 29	14 00
LIGHT-I-R POST	20 66	13 23	13 08	26 02	14 36	15 05	29 04
BURIED MAGNETS	20 79	13 21	13 46	26 70	14 52	15 81	29 21
ULTRASONIC POST	20 66	13 23	13 08	26 02	14 36	15 05	29 04
TRAFFIC SENSOR	20 66	13 23	13 08	26 02	14 36	15 05	29 04

Table 2-45. Los Angeles, Valley Bureau
AVM Systems Cost Analyses

CLASS I TECHNIQUE	THOUSANDS OF \$				TOTALS			
	UNITS	SITES	BASE	INST	0-1	VOL	SYNC	PANDEM
KEYBOARD	20	0	0	17	103	286	425	245
STYLUS MAP	21	0	0	17	103	286	425	245
2-ACCELEROMETERS	20	0	116	24	11	597	63	625
LASEP VELOCIMTR	20	0	114	36	129	150	37	673
ULTRASONIC VELO	20	0	119	29	124	347	54	575
COMPASS/ODOMETER	20	0	119	1	103	53	53	574
COMPASS/LASEP VEL	20	0	119	34	110	606	701	622
COMPASS-U-SONIC VEL	20	0	111	29	112	597	33	613
OMEGA	22	0	100	26	115	700	319	619
LORAN	22	0	100	26	115	700	319	619
DECCA	22	0	100	22	115	40	52	429
HI-STATIONS	20	0	100	20	112	337	373	34
DIFF OMEGA	22	0	100	26	115	700	319	619
DIFF LORAN	22	0	100	26	115	700	319	619
DIFF HI-STA	22	0	100	20	112	337	373	34
RELAY OMEGA	1988	0	100	26	115	37	34	429
RELAY LORAN	41	0	100	26	115	33	33	429
CLASS II SURVED PES LOOPS	27	10300	80	18379	105	4419	24436	4368
REFLECTING SIGNS	27	3300	80	18379	105	4419	24436	4368
REFLECTING ROAD	27	3300	80	18379	105	4419	24436	4368
N-BAND POST	20	650	80	930	327	112	490	452
HF, VHF POST	20	375	80	107	154	673	37	29
LF POST	20	1875	80	694	328	3053	3005	0
LIGHT-I-R POST	20	1500	80	850	480	297	2945	2937
BURIED MAGNETS	19	1080	80	2174	100	3488	3506	3458
ULTRASONIC POST	20	2550	80	2577	405	5667	5625	5627
TRAFFIC SENSOR	20	2850	80	1218	102	4308	4026	4277
CLASS III NAR-BAND FM PHASE	43	212	157	59	128	577	624	629
WIDE-BAND FM PHASE	550	116	164	43	210	1081	1120	1133
PULSE T-0-ARRIVAL	43	630	349	151	203	1819	1866	1871
NOISE CORRELATION	149	29	349	3	182	771	738	793
DIRECTION FINDER	7	0	40	18	154	378	393	355
CLASS IV TRAFFIC LOOPS	16	20633	0	4091	462	25281	25281	25281
WAYSIDE RADIO	15	18176	0	3408	852	22529	22529	22529
PHOTO-I-R DETECT	22	11928	0	1719	478	14225	14225	14225
ULTRASONIC DETECT	24	12078	0	1718	478	14376	14376	14376

Table 2-47. Los Angeles, Valley Bureau
AVM Accuracies and Cost Benefits
with One Radio Channel

CLASS I TECHNIQUE	ULTIMATE ACCURACY	VEHICLES SAVED	SYSTEM ACCURACY		ESTIMATED \$1000 CHANGES	
			MAX	MIN	MIN	5-YEAR ESTIMATED
KEYBOARD	03	3	474	246	2 5	0 0
STYLUS MAP	00	8	490	255	2 4	0 0
2-ACCELEROMETERS	34	8	482	250	2 5	0 0
LASEP VELOCIMTR	10	8	474	246	2 5	0 0
ULTRASONIC VELO	40	8	454	251	2 4	0 0
COMPASS/ODOMETER	20	8	475	246	2 5	0 0
COMPASS/LASEP VEL	15	8	471	244	2 5	0 0
COMPASS-U-SONIC VEL	17	8	473	245	2 5	0 0
OMEGA	1600	0	4200	413	0 0	0 0
LORAN	150	0	551	412	1 3	0 0
DECCA	260	0	549	406	0 7	0 0
HI-STATIONS	300	5	508	494	0 7	0 0
DIFF OMEGA	160	5	538	411	1 3	0 0
DIFF LORAN	400	1	1179	1142	0 0	0 0
DIFF HI-STA	250	7	624	597	0 0	0 0
RELAY OMEGA	500	1	1473	2107	0 0	0 0
RELAY LORAN	800	0	2163	2045	0 0	0 0
CLASS II SURVED PES LOOPS	10	6	468	243	2 5	0 0
REFLECTING SIGNS	10	8	468	243	2 5	0 0
REFLECTING ROAD	10	8	452	234	2 5	0 0
N-BAND POST	17	8	468	243	2 5	0 0
HF, VHF POST	15	3	457	241	2 5	0 0
LF POST	100	6	497	237	2 5	0 0
LIGHT-I-R POST	0	8	430	249	2 5	0 0
BURIED MAGNETS	20	8	456	236	2 5	0 0
ULTRASONIC POST	20	8	475	246	2 5	0 0
TRAFFIC SENSOR	10	8	460	241	2 5	0 0
CLASS III NAR-BAND FM PHASE	1000	0	2722	2632	0 0	0 0
WIDE-BAND FM PHASE	1200	0	3194	3108	0 0	0 0
PULSE T-0-ARRIVAL	100	6	144	187	2 4	4 0
NOISE CORRELATION	100	0	217	204	2 7	1 1
DIRECTION FINDER	700	0	2002	1997	0 0	0 0
CLASS IV TRAFFIC LOOPS	10	3	22	23	4 1	5 0
WAYSIDE RADIO	100	0	200	207	2 8	4 5
PHOTO-I-R DETECT	30	0	56	60	3 0	7 0
ULTRASONIC DETECT	20	0	42	43	0 4	7 0

Table 2-48. Los Angeles, Valley Bureau
AVM Accuracies and Cost Benefits
with Two Radio Channels

CLASS I	SYSTEM ACCURACIES (%)		VEHICLES AND THEO		SYSTEM ACCURACY		VEHICLES SAVED		ESTIMATED \$1000 SAVINGS	
	ULTIMATE ACCURACY	VEHICLES SAVED	MAX	MIN	MAX	MIN	ESTIMATED 5-YEAR SAVINGS	MIN	MAX	MIN
KEYBOARD	33	8	244	122	344	34	2135	34	34	34
STYLUS MAP	30	8	253	126	33	34	2025	33	34	34
2-ACCELEROMETERS	34	8	248	124	33	35	2038	33	35	35
LASER VELOCIMTR	13	8	244	122	34	34	2455	34	34	34
ULTRASONIC VELO	40	8	249	125	33	35	1938	33	35	35
COMPASS/ODOMETER	20	3	244	122	34	34	2140	34	34	34
COMPASS/LASER VEL	15	3	242	121	34	34	2110	34	34	34
COMPASS-U-SONIC VEL	17	3	243	121	34	34	2110	34	34	34
OMEGA	1500	U	-112	344	0	0	U	0	0	0
LOPRAH	100	U	412	42	14	0	475	14	0	0
DECCA	200	U	496	42	0	0	25	0	0	0
AH-STATIONS	200	U	494	42	0	0	48	0	0	0
DIFF OMEGA	160	U	411	40	14	0	475	14	0	0
DIFF LOPRAH	400	U	1142	110	0	0	0	0	0	0
DIFF AH-STA	250	U	597	50	0	0	475	0	0	0
RELAY OMEGA	500	U	21141	1051	0	0	U	0	0	0
RELAY LOPRAH	300	U	2344	2267	0	0	0	0	0	0
CLASS II										
SUPIED FES LOOPS	10	8	241	120	34	37	2240	34	37	37
REFLECTING SIGNS	10	8	241	120	34	37	755	34	37	37
REFLECTING FORD	3	8	232	116	34	38	665	34	38	38
A-BAND POST	12	8	241	120	34	37	1148	34	37	37
H-F WAF POST	15	8	239	128	34	37	1900	34	37	37
LF POST	100	U	273	26	24	38	610	24	38	38
LIGHT/I-R POST	30	3	247	124	33	35	225	33	35	35
SUPIED MAGNETS	4	8	254	117	34	38	2350	34	38	38
ULTRASONIC POST	20	3	244	122	34	36	675	34	36	36
TRAFFIC SENSOR	10	8	239	119	34	37	2265	34	37	37
CLASS III										
NAP-BAND FM PHASE	1000	0	2631	2545	0	0	0	0	0	0
MID-BAND FM PHASE	1200	0	3107	3020	0	0	0	0	0	0
PULSE T-O-APPRVAL	100	U	194	187	29	34	2435	29	34	34
NOISE CORRELATION	100	U	217	209	27	41	2165	27	41	41
DIRECTION FINDER	700	0	1936	1870	0	0	U	0	0	0
CLASS IV										
TRAFFIC LOOPS	10	8	22	23	41	38	3640	41	38	38
WAYSIDE RADIO	100	6	260	207	28	45	205	28	45	45
PHOTO-I-R DETECT	30	8	59	40	38	48	3025	38	48	48
ULTRASONIC DETECT	20	8	42	43	39	46	3310	39	46	46

Table 2-49. Los Angeles, Valley Bureau
AVM Accuracies and Cost Benefits
with Three Radio Channels

CLASS I	SYSTEM ACCURACIES (%)		VEHICLES AND THEO		SYSTEM ACCURACY		VEHICLES SAVED		ESTIMATED \$1000 SAVINGS	
	ULTIMATE ACCURACY	VEHICLES SAVED	MAX	MIN	MAX	MIN	ESTIMATED 5-YEAR SAVINGS	MIN	MAX	MIN
KEYBOARD	33	8	162	45	34	52	2135	45	34	52
STYLUS MAP	30	8	168	33	34	51	2025	33	34	51
2-ACCELEROMETERS	34	8	165	34	35	52	2038	34	35	52
LASER VELOCIMTR	13	8	162	30	34	52	2455	30	34	52
ULTRASONIC VELO	40	8	166	108	35	51	1938	108	35	51
COMPASS/ODOMETER	20	3	163	30	34	52	2140	30	34	52
COMPASS/LASER VEL	15	3	161	30	34	52	2110	30	34	52
COMPASS-U-SONIC VEL	17	3	162	30	34	52	2110	30	34	52
OMEGA	1500	U	-403	3929	0	0	U	0	0	0
LOPRAH	100	U	403	343	14	0	475	14	0	0
DECCA	200	U	488	174	0	0	25	0	0	0
AH-STATIONS	200	U	402	42	0	0	48	0	0	0
DIFF OMEGA	160	U	404	393	14	0	475	14	0	0
DIFF LOPRAH	400	U	1121	1086	0	0	0	0	0	0
DIFF AH-STA	250	U	587	570	0	0	475	0	0	0
RELAY OMEGA	500	U	14046	6635	0	0	U	0	0	0
RELAY LOPRAH	300	U	2238	2223	0	0	U	0	0	0
CLASS II										
SUPIED FES LOOPS	10	8	160	79	37	50	2400	79	37	50
REFLECTING SIGNS	10	8	160	79	37	50	755	79	37	50
REFLECTING FORD	3	8	154	77	37	50	665	77	37	50
A-BAND POST	12	8	160	79	37	50	1148	79	37	50
H-F WAF POST	15	8	159	79	37	50	1900	79	37	50
LF POST	100	U	268	259	24	38	610	24	38	38
LIGHT/I-R POST	30	3	165	81	34	51	225	81	34	51
SUPIED MAGNETS	4	8	156	77	37	50	2350	77	37	50
ULTRASONIC POST	20	3	163	30	34	52	675	30	34	52
TRAFFIC SENSOR	10	8	159	79	37	50	2265	79	37	50
CLASS III										
NAP-BAND FM PHASE	1000	0	2580	2496	0	0	0	0	0	0
MID-BAND FM PHASE	1200	0	3055	2964	0	0	0	0	0	0
PULSE T-O-APPRVAL	100	U	194	187	29	34	2435	29	34	34
NOISE CORRELATION	100	U	217	209	27	41	2165	27	41	41
DIRECTION FINDER	700	0	1898	1836	0	0	U	0	0	0
CLASS IV										
TRAFFIC LOOPS	10	8	22	23	41	38	3640	41	38	38
WAYSIDE RADIO	100	6	260	207	28	45	205	28	45	45
PHOTO-I-R DETECT	30	8	59	40	38	48	3025	38	48	48
ULTRASONIC DETECT	20	8	42	43	39	46	3310	39	46	46

PART THREE:
ANALYTICAL TECHNIQUES
FOR ESTIMATING AVM
SYSTEM ACCURACY

J.E. Fielding
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Joseph E. Fielding

I. VEHICLE LOCATION ACCURACY FOR CLASS I AND III SYSTEMS

In this Section, an algorithm is described which can be used to determine the system accuracy of Class I and III automatic vehicle monitoring (AVM) systems as a function of the appropriate system parameters. Some of the resultant cumulative probability density functions (cdfy) are also presented, which can be interpreted as the fraction of the fleet for which the error is less than or equal to y. The flow chart shown in Fig. 3-1 is a brief outline of the vehicle location accuracy program, while Fig. 3-2 expands on the methodology of the computation of the cumulative density function.

A. Parameters for AVM System Accuracy Analysis

The inherent error, ϵ_0 , is defined to be the distance between the vehicle's actual location and the location determined by the AVM system at the

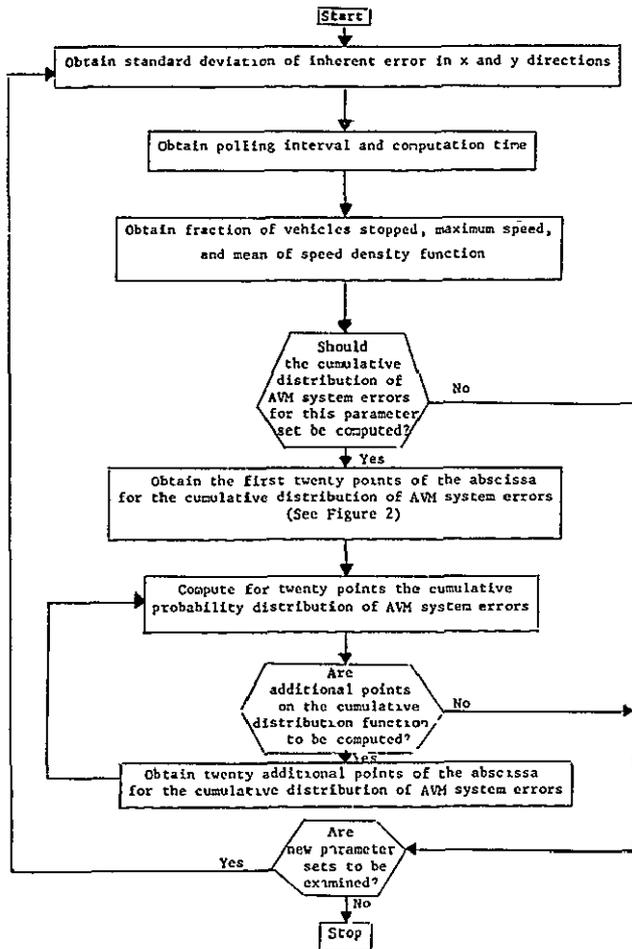


Fig. 3-1. Main AVM Accuracy Analysis Program

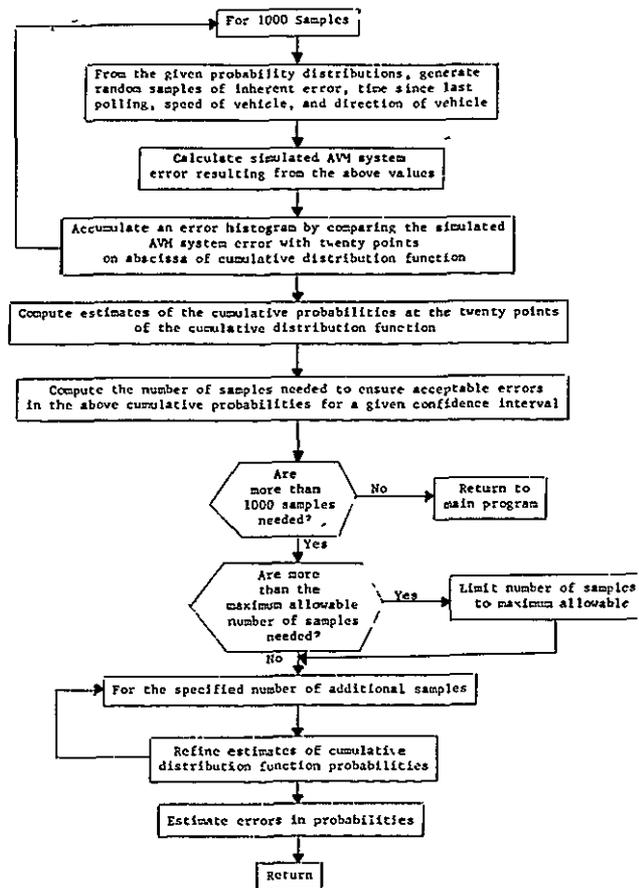


Fig. 3-2. Computation of Cumulative Distribution Function

instant of polling. Inherent error is assumed to be consistent with a Rayleigh distribution, i. e.,

$$\Phi(\epsilon_0) = \frac{\epsilon_0}{\sigma^2} e^{-1/2\left(\frac{\epsilon_0}{\sigma}\right)^2}$$

As time passes, the vehicle's location changes by a distance of $(s \cdot t)$ and a direction θ . (See Fig. 3-3.) The random variable θ is assumed to be uniformly distributed. Its probability density function is denoted by $p(\theta)$, and is equal to $1/(2\pi)$ between $-\pi$ and π .

The speed of the vehicle is represented by the symbol s and is assumed to be described by the following distribution

$$f(s) = \begin{cases} FO \cdot \delta & s=0 \\ \lambda e^{-\lambda s} & 0 < s < M \\ 0 & \text{otherwise} \end{cases}$$

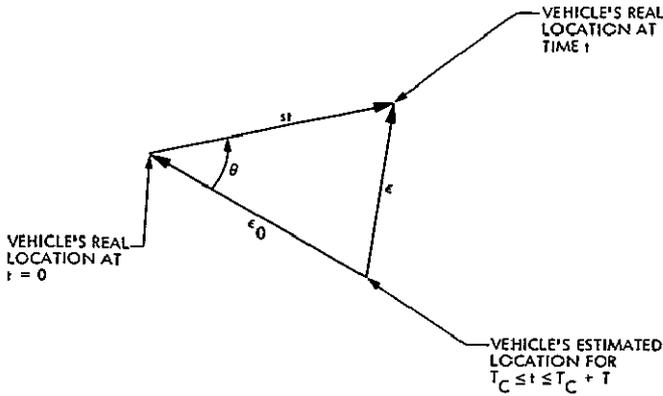


Fig. 3-3. Error in Knowledge of Vehicle's Location

There is a discrete probability FO, associated with zero speed. Between speeds zero 0 and maximum M, the speed is distributed exponentially. The parameter λ is set such that the fraction of vehicles stopped, FO, plus the fraction whose speed falls between 0 and maximum speed M sums to 0.99.

The last of the AVM system parameters is time. After the location of the vehicle is determined, there is a delay before the information becomes available. This delay is referred to as computation time, T_C . Thus, if the symbol T denotes the polling interval, the probability density function $g(t)$ is a uniform distribution over the time interval T_C through $T_C + T$.

B. Derivation of Accuracy Analysis Algorithm

Probability distribution functions have been defined for ϵ_0 , θ , s, and t, and from Fig 3-3 the actual error in the knowledge of the vehicle's location, ϵ , is:

$$\epsilon = \sqrt{\epsilon_0^2 + s^2 t^2 - 2\epsilon_0 st \cos \theta}$$

The distribution of errors is given by:

$$cdfy = \text{Prob}(\epsilon \leq y) = \iiint\iiint_R \Phi(\epsilon_0) g(t) \cdot$$

$$f(s) p(\theta) d\theta ds dt d\epsilon_0,$$

where R is the region such that $\epsilon \leq y$. Due to the complexity of R, it is not practical to evaluate this integral analytically or by numerical quadrature. Therefore a Monte Carlo integration of cdfy is used.

The Monte Carlo integration generates values for the four random variables, ϵ_0 , s, t, θ and uses these variables to calculate ϵ by the above formula. By checking whether $\epsilon \leq y_1$ for $i=1, \dots, 20$, when the y_i 's are a pre-specified array of points on the abscissa, it is possible, if enough trials are run, to determine an accurate estimate of the cumulative distribution function.

The methodology used to generate the random variables ϵ_0 , s, t and θ involves generating four uniform variates on $[0, 1]$ r_1, r_2, r_3, r_4 . Inverting the cumulative density functions leads to the expressions needed to calculate the desired variables:

$$\epsilon_0 = \sigma \sqrt{-2 \ln r_1}$$

$$t = T_C + r_2 T$$

$$s = \begin{cases} 0 & 0 \leq r_3 \leq FO \\ \frac{\ln(1-r_3)}{-\lambda} & FO < r_3 \leq 1 \end{cases}$$

$$\theta = \pi(2r_4 - 1)$$

Of prime concern in the Monte Carlo integration is the number of trials needed to ensure an acceptable estimate of the probabilities that $\epsilon \leq y_1$. If p_1 denotes the real value of cdfy for a particular y_1 , then the process becomes a long sequence of Bernoulli trials with p_1 equal to the probability of success (i.e., that $\epsilon \leq y_1$). Since the number of trials will be "large", the Bernoulli distribution can be well approximated by the Gaussian distribution with mean, $\mu = p$ Standard deviation,

$$\sigma = \sqrt{n p(1-p)/n}$$

where n = number of trials, and p_i has been replaced by p for simplicity.

Since the distribution of the number of trials for which ϵ exceeds any particular value of y is approximately gaussian, we can require the probability (of the event that the absolute error in the distribution function, cdfy, is less than some specified maximum value, E) to be at least C, the so-called "confidence level". That is, a fraction C of the distribution must be contained within the interval $p - k\sigma$ thru $p + k\sigma$ (Fig. 3-4). Thus, a value of C determines a value for k. In addition,

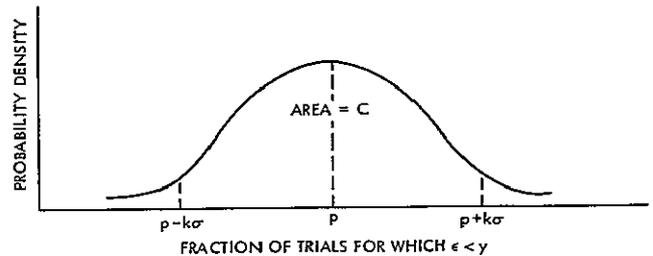


Fig. 3-4. Probability Density vs Fraction of Trials

to ensure an acceptable absolute error, E, it is required that the interval $k\sigma$ be less than or equal to E:

$$k\sigma \leq E.$$

Substituting the expression for the standard deviation σ into this last equation gives

$$k\sqrt{np(1-p)/n} \leq E$$

which may be rewritten

$$n \geq k^2 p(1-p)/E^2$$

This value for n represents the minimum number of trials needed to ensure an absolute error of less than E with confidence C. A larger value of k implies that a larger fraction of the gaussian distribution will be contained within the interval $p \pm k\sigma$, thus leading to a higher confidence C. However, a larger k requires an increased number of trials in order to satisfy the error criteria.

The accuracy algorithm specifies the maximum allowable error E, and the required confidence interval C. The program proceeds to run 1000 trials, and p_1 is then estimated as

$$(\text{number of times } \epsilon \leq y_1) / 1000 \text{ for } i=1, \dots, 20.$$

These approximate values of p_1 are used to calculate the required number of trials, n, needed to ensure (with confidence C) that none of the error terms will be greater than the maximum allowable error E. If n is found to be less than 1000, no more runs are required and the calculation of (y_1, cdfy) is complete. However, if n is greater than 1000, additional trials are needed.

In order to prevent an excessive number of runs, in terms of computer time, a constant NMAX is introduced which serves as the maximum allowable number of trials. Thus, if it is determined that more than 1000 runs are needed, the algorithm will process additional trials until the error terms are sufficiently small or until the maximum allowable number of trials is reached, whichever comes first. In the case where the number of trials reaches NMAX, the resulting errors using the improved estimates of the p_1 's are calculated. In the actual execution of the program, the number of trials is almost always extended to NMAX with resulting errors on the order of 0.005.

The accuracy program is interactive, the user being free to set the system parameters of variance in inherent error, polling interval, computation time, fraction of vehicles stopped, and the "maximum" vehicle speed. The program then computes the mean of the exponential speed distribution such that 99% of the probability is included between speeds 0 and maximum speed M. The program also specifies the 20 values to be used along the abscissa of the cumulative distribution function of AVM system errors. These values are determined as a

function of the variance of the inherent error as one can assume that the variance of system errors is somewhat correlated with this parameter. The intent is to cover the full range from 0.0 to 1.0 of the cumulative distribution function. As a safeguard against failure of full coverages, the program allows the user to calculate the cumulative distribution function for 20 additional values of y where the user specifies the initial point and the interval between points. This option for additional points can be repeated as many times as the user desires. After the cumulative distribution function is computed, the user may reset the system parameters, and the process of determining a new cumulative distribution function is repeated.

C. Results of AVM System Accuracy Analysis

The algorithm described in the previous section was exercised by running 42 cases, each one with a unique set of the input parameters, where

SIGMA	= Standard deviation of inherent error in x and y directions
T	= Polling interval
TC	= Computation time
M	= Maximum speed
FO	= Fraction stopped

Originally, all combinations of the following parameter values were to be run,

SIGMA (meters)	T (seconds)	TC (seconds)	M (meters/sec)	FO
0	2	0.01	40	0
100	10	0.1	60	
1000	60			
	120			
	300			

which would have required 60 cases. However, after the first 14 runs, it became evident that the AVM system error was stable for computation times in the range 0.01 to 0.1 second.

A value for the standard deviation of the inherent error of zero serves as a boundary condition for inherent accuracy of AVM hardware systems. Estimates of system error using SIGMA equal to zero represents the accuracy to be expected if one invests in extremely accurate hardware systems in terms of pinpointing location, assuming there is no motion. At first glance, a maximum speed of 60 meters/second (134 miles/hr) might seem a little high, however, the speed of the vehicles of the fleet is assumed to be distributed exponentially. Thus, a very small fraction of the fleet is traveling near maximum speeds; one-half of the fleet is traveling at a speed of less than (maximum speed/6) or 22.3 miles/hr. The fraction of cars stopped is set at 0 because the algorithm is designed to specifically test system accuracy assuming moving vehicles. Later, if individual users need results that reflect their mode of operation, they can supply a non-zero value for this parameter. The effects

of changes in the above variables on AVM system accuracy follows.

No modeling effort is necessary to determine whether system accuracy will improve or deteriorate given the direction of change of any input variable. As the variance in the inherent error, the polling interval, the computation time, and the maximum speed increase, system accuracy deteriorates. However, the designer requires a more detailed knowledge of the interaction between these system parameters and AVM system accuracy. He is faced with an accuracy constraint such as 80% of the vehicles must be located to within 150 meters. In order to satisfy this constraint, he must be aware of the combinations of system parameters that can meet his requirements. The above analysis provides this information. What it does not provide is information for the designers' next step, which is to determine the proper balance with respect to inherent accuracy, polling interval, and computation time so as to minimize cost as well as satisfy accuracy constraints.

The best accuracy results are obtained when SIGMA is set equal to zero. With SIGMA zero and polling interval equal to 2 seconds, 80% of the fleet is located to within 20 meters and this is not strongly dependent on maximum speed or computation time. As the polling interval is increased to 10 seconds, 80% of the fleet is located to within 65 meters at maximum speed of 40 meters/second and to within 105 meters at 60 meters/second. Thus, as polling interval increases, accuracy becomes more dependent on maximum speed. Again, the accuracy is not dependent on computation time. Table 3-1 presents similar results for the remainder of the cases with SIGMA equal to zero. The above trends continue, that is, as the polling interval increases, the 80% distance grows,

Table 3-1. Vehicle Location Accuracy at 80% Level for SIGMA = 0 Meters

T (sec)	TC (sec)	M (meters/sec)	Accuracy (meters)
2	.01	40	15
2	.01	60	20
2	.1	40	15
2	.1	60	22
10	.01	40	65
10	.01	60	105
10	.1	40	70
10	.1	60	105
60	.01	40	420
60	.01	60	620
60	.1	40	420
60	1	60	620
120	.01	40	820
120	.01	60	1350
300	.01	40	2100
300	.01	60	3080

Table 3-2. Vehicle Location Accuracy at 80% Level for SIGMA = 100 Meters

T (sec)	TC (sec)	M (meters/sec)	Accuracy (meters)
2	.01	40	180
2	.01	60	183
2	.1	40	180
2	.1	60	183
10	.01	40	195
10	.01	60	212
60	.01	40	448
60	.01	60	650
120	.01	40	850
120	.01	60	1250
300	.01	40	2100
300	.01	60	3160

the dependence on maximum speed increases, and accuracy is not dependent on computation time.

Table 3-2 presents similar data for the case SIGMA equals 100 meters. With a polling interval of 2 seconds, 80% of the vehicles in the fleet are located to within 180 meters. The trends evident in the SIGMA equal zero cases can also be seen in Table 3-2. One major difference is that, in this case, the change in accuracy as polling interval increases from 2 to 10 seconds is rather insignificant. Thus, if the system hardware has a standard deviation for inherent accuracy in the x and y direction of 100 meters, then little would be gained by specifying a polling interval shorter than 10 seconds. In comparing the results of Table 3-1 and Table 3-2, it is apparent that the accuracy of a SIGMA = zero system is not significantly better than a SIGMA = 100 meters system when the polling interval is greater than 60 seconds. Thus, if a sophisticated hardware system in terms of inherent error is installed, it requires a short polling interval to realize significant benefits.

The most striking difference between the cases with inherent error equal to 0 and 100 meters and the case with inherent error equal to 1000 meters (Table 3-3) is that the interval between the minimum and maximum accuracies is much more compact in the 100 meter case. In general, one can conclude that as the resolution in inherent error deteriorates, the system is less dependent on the remaining parameters. The accuracy figure in Table 3-3 for polling intervals of 2, 10, 60 and 120 seconds are significantly higher than the corresponding values in Tables 3-1 and 3-2, while the accuracy at a polling interval of 300 seconds is of the same order over all three Tables.

These results presenting accuracy estimates for AVM system errors can serve as a tool to be used in AVM system design.

Table 3-3. Vehicle Location Accuracy at 80% Level for SIGMA = 1000 Meters

T (sec)	TC (sec)	M (meters/sec)	Accuracy (meters)
2	.01	40	1790
2	.01	60	1790
2	.1	40	1790
2	.1	60	1790
10	.01	40	1795
10	.01	60	1810
60	.01	40	1880
60	.01	60	1950
120	.01	40	2210
120	.01	60	2500
300	.01	40	2985
300	.01	60	3500
300	.1	40	2780
300	.1	60	3650

II. MARKOV CHAIN MODEL OF VEHICLE LOCATION BY MEANS OF PROXIMITY SENSORS FOR CLASS II AND IV SYSTEMS

Marvin Perlman

One approach to automatically locating specified vehicles in an urban area involves the employment of proximity sensors. The proximity sensors (which may be active or passive) are distributed throughout a given area. Once installed, the position of a sensor is fixed. A vehicle, properly equipped, will interact with a sensor when the distance between the vehicle and the sensor is within prescribed limits. Interaction results in communicating the identity of the vehicle and the location of the sensor to a central system. Not considered in this analysis are the proximity sensor's characteristics, the required equipment for the vehicle, or the means of communicating to the central system. This analysis presents a Markov chain model of the interaction of fixed proximity sensors with moving vehicles whose locations are to be monitored.

A. Classifications of Finite Markov Chains

1. Concepts and definitions. A stochastic process is any sequence of experiments amenable to probabilistic analysis. A stochastic process is said to be finite if the set of possible outcomes is finite. An independent process is a finite stochastic process where knowledge of the outcome of any preceding experiment in no way affects the prediction of the outcome of the present experiment.

A finite Markov chain process is a finite stochastic process where knowledge of the outcome of the immediate past experiment does affect the prediction of the outcome of the present experiment. Furthermore, the dependence of the outcome of each experiment on the outcome of the immediately preceding experiment only is the same at each stage of successive experiments. A finite Markov chain is characterized by a finite set of states $\{s_1, s_2, \dots, s_n\}$. The state of a Markov chain is the outcome of the last experiment. Thus a Markov chain is in one and only one state at a given time and advances from one state to another (or remains in the same state) in accordance with a priori transition probabilities. The transition probability p_{ij} is the probability that the (Markov chain) process will move from state s_i to s_j , and p_{ij} depends only on s_i . Associated with every ordered pair of states is a known transition probability. An $n \times n$ transition probability matrix P contains as entries the transition probabilities corresponding to each of the respective n^2 ordered pairs of states as follows:

$$P = \begin{matrix} & \begin{matrix} s_1 & s_2 & \dots & s_n \end{matrix} \\ \begin{matrix} s_1 \\ s_2 \\ \cdot \\ \cdot \\ \cdot \\ s_n \end{matrix} & \begin{bmatrix} p_{11} & p_{12} & \dots & p_{1n} \\ p_{21} & p_{22} & \dots & p_{2n} \\ \cdot & \cdot & \dots & \cdot \\ \cdot & \cdot & \dots & \cdot \\ \cdot & \cdot & \dots & \cdot \\ p_{n1} & p_{n2} & \dots & p_{nn} \end{bmatrix} \end{matrix}$$

Each row in P comprises a probability event space such that

$$P_{ij} \geq 0 \quad \text{for all } i, j$$

and

$$\sum_{j=1}^n p_{ij} = 1 \quad \text{for every } i$$

The transition probability matrix P and an initial (starting state completely describe a finite Markov chain process.

2. Regular Markov chains. A Markov chain is defined to be regular if and only if after n steps (i. e., experiments) for some n , it is possible for the process to be in any state regardless of the starting state. The entry $p_{ij}^{(n)}$ in P^n (the n th power of the transition matrix) is the probability that the process is in state s_j after n steps given that it started in state s_i . A regular Markov chain has a regular transition matrix P such that P^n contains only positive entries (i. e., $p_{ij}^{(n)} > 0$ for all i, j). P may be tested for regularity by noting whether or not the entries in $P^2, (P^2)^2, (P^4)^2, \dots$ are positive assuming P has one or more 0 entry.

Example 1. Given the following (probability) matrix

$$P = \begin{matrix} & \begin{matrix} s_1 & s_2 & s_3 & s_4 \end{matrix} \\ \begin{matrix} s_1 \\ s_2 \\ s_3 \\ s_4 \end{matrix} & \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0.5 & 0.25 & 0 & 0.25 \\ 0 & 0 & 0.5 & 0.5 \end{bmatrix} \end{matrix}$$

Successive squaring of P, P^2, P^4, \dots quickly results in large powers of P . When testing for regularity, the actual values of the entries need not be determined. Denoting each positive entry by x and each zero entry 0 gives

$$P = \begin{bmatrix} 0 & x & 0 & 0 \\ 0 & 0 & x & 0 \\ x & x & 0 & x \\ 0 & 0 & x & x \end{bmatrix}$$

P^2 , P^4 and P^8 are, respectively

$$\begin{bmatrix} 0 & 0 & x & 0 \\ x & x & 0 & x \\ 0 & x & x & x \\ x & x & x & x \end{bmatrix}, \quad \begin{bmatrix} 0 & x & x & x \\ x & x & x & x \\ x & x & x & x \\ x & x & x & x \end{bmatrix} \quad \text{and} \quad \begin{bmatrix} x & x & x & x \\ x & x & x & x \\ x & x & x & x \\ x & x & x & x \end{bmatrix}$$

Thus P is a regular transition matrix.

3. Ergodic Markov chains. A Markov chain is defined to be ergodic if and only if it is possible for the process to go from every state to every other state. Clearly a regular Markov chain is always ergodic. However, an ergodic Markov chain is not necessarily regular. That is, for every n , P^n contains some 0 entries. However, P^n for different values of n , will contain zeros in different locations. As n increases, the positions of the zeros change cyclically. In this case, the chain is termed a cyclic Markov chain. Thus an ergodic Markov chain is either cyclic or regular but not both.

Example 2. Given the following transition matrix

$$P = \begin{matrix} & \begin{matrix} s_1 & s_2 & s_3 & s_4 \end{matrix} \\ \begin{matrix} s_1 \\ s_2 \\ s_3 \\ s_4 \end{matrix} & \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0.25 & 0 & 0.75 & 0 \\ 0 & 0.25 & 0 & 0.75 \\ 0 & 0 & 1 & 0 \end{bmatrix} \end{matrix}$$

or

$$P = \begin{bmatrix} 0 & x & 0 & 0 \\ x & 0 & x & 0 \\ 0 & x & 0 & x \\ 0 & 0 & x & 0 \end{bmatrix}$$

where x denotes a positive entry. For even $n > 0$,

$$P^n = \begin{bmatrix} x & 0 & x & 0 \\ 0 & x & 0 & x \\ x & 0 & x & 0 \\ 0 & x & 0 & x \end{bmatrix}$$

For odd $n > 1$,

$$P^n = \begin{bmatrix} 0 & x & 0 & x \\ x & 0 & x & 0 \\ 0 & x & 0 & x \\ x & 0 & x & 0 \end{bmatrix}$$

Starting in an odd-numbered state (s_1 or s_3), the process is in an even-numbered state (s_2 or s_4) after an odd number of steps, and in an odd-numbered state after an even number of steps.

P in Example 2 is an ergodic transition matrix which is nonregular. The process characterized by P is a cyclic (ergodic) chain.

4. Absorbing Markov chains. An absorbing state in a Markov chain is one which cannot be left once entered. An absorbing Markov chain is a Markov chain that has at least one absorbing state, and from every nonabsorbing state it is possible to move to an absorbing state (in one or more steps). The nonabsorbing states (of an absorbing chain) are known as transient states. The transition matrix P of an absorbing chain has entries $P_{ii} = 1$ for each s_i that is absorbing.

Example 3. The following transition matrix characterizes an absorbing chain

$$P = \begin{matrix} & \begin{matrix} s_1 & s_2 & s_3 & s_4 & s_5 \end{matrix} \\ \begin{matrix} s_1 \\ s_2 \\ s_3 \\ s_4 \\ s_5 \end{matrix} & \begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 0.5 & 0 & 0.5 & 0 & 0 \\ 0 & 0.5 & 0 & 0.5 & 0 \\ 0 & 0 & 0.5 & 0 & 0.5 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix} \end{matrix}$$

States s_1 and s_5 are absorbing; whereas, states s_2 , s_3 and s_4 are transient states.

5. Classification of states. The states of any given Markov chain can be partitioned into equivalence classes. An equivalence class comprises either an ergodic set of states or a transient set of states. Once the process enters an ergodic set, it remains in the set. Once the process leaves a transient set, it never reenters the set.

If a chain has two or more ergodic sets of states but no transient sets, the chain in effect is a composite of two or more unrelated chains. Each of the unrelated chains consists of a single ergodic set and may be treated separately. Without any

loss in generality, every ergodic chain (regular and cyclic) consists of a single ergodic set.

An absorbing state is an ergodic set consisting of one and only one state. Such an ergodic set is referred to as a unit set. Thus an absorbing chain has one or more unit sets and one or more transient sets.

Every state of a given set whether it is ergodic or transient can "communicate" with every other state in the set. The process, however, moves toward the ergodic sets when the chain contains transient as well as ergodic sets.

B. Properties of Absorbing Markov Chains

1. Canonical Form of P and Pⁿ. The transition matrix P of an absorbing chain can always be arranged to have the following canonical form (by relabeling states)

$$P = \begin{bmatrix} I & O \\ R & Q \end{bmatrix}$$

The submatrix I is an $l \times l$ identity matrix whose entries are the transition probabilities for every ordered pair of absorbing states (s_i, s_j) where

$$P_{ij} = \begin{cases} 0 & \text{if } i \neq j \\ 1 & \text{if } i = j \end{cases}$$

The submatrix Q is an $m \times m$ matrix whose entries are the transition probabilities for every ordered pair of transient states. The submatrix R is an $m \times l$ matrix whose entries are the transition probabilities for every ordered pair of states (s_i, s_j) where s_i is a transient state and s_j is an absorbing state. The submatrix O is an $l \times m$ matrix whose entries are zeros corresponding to the zero transition probabilities of moving from any absorbing state to any transient state. Powers of P have the canonical form

$$P^n = \begin{bmatrix} I & O \\ M & Q^n \end{bmatrix}$$

where

$$M = [I + Q + Q^2 + \dots + Q^{n-1}]R$$

Note that the expression for M is a matrix equation.

Theorem 1. In any finite Markov chain, regardless of the initial (starting) state, the probability that the process is in ergodic state after n steps approaches 1 as n approaches infinity. (A proof of Theorem 1 appears in Ref. 1.)

A Corollary to Theorem 1 is that are real numbers b and c where $b > 0$ and $0 < c < 1$ such that

$$P_{ij}^{(n)} \leq bc^n$$

for any ordered pair of transient states (s_i, s_j). This gives the rate at which $P_{ij}^{(n)}$ approaches 0.

Every entry in Q^n in the canonical form of P^n of an absorbing chain approaches 0 as n increases without limit.

2. Fundamental matrix. The fundamental matrix of an absorbing chain is defined as

$$N = [I - Q]^{-1} \quad (1)$$

Note that

$$\frac{I}{I - Q} - \frac{Q^n}{I - Q} = I + Q + Q^2 + \dots + Q^{n-1}$$

and since $Q \neq I$ and $\lim_{n \rightarrow \infty} Q^n = 0$

$$[I - Q]^{-1} = \lim_{n \rightarrow \infty} [I + Q + Q^2 + \dots + Q^{n-1}]$$

the inverse of $I - Q$ (i. e., N) always exists.

The submatrix M in P^n as n approaches infinity may be expressed as

$$M = [I - Q]^{-1} R = NR \quad (2)$$

The fundamental matrix N has the following probabilistic interpretation.

Let $u_{ij}^{(k)} = 1$ if the process starts in transient state s_i and is in transient state s_j after k moves. Otherwise $u_{ij}^{(k)} = 0$. Let $t_{ij}^{(n)}$ denote the number of times the process is in transient state s_j starting and during n moves given that it started in transient state s_i . Thus

$$t_{ij}^{(n)} = u_{ij}^{(0)} + u_{ij}^{(1)} + \dots + u_{ij}^{(n)}$$

The probability that the process is in transient state s_j after the kth move is

$$p(u_{ij}^{(k)} = 1) = q_{ij}^{(k)}$$

given that s_i is transient and the starting state. The mean of $u_{ij}^{(k)}$ is

$$m(u_{ij}^{(k)}) = 1 \cdot q_{ij}^{(k)} + 0 \cdot (1 - q_{ij}^{(k)}) = q_{ij}^{(k)}$$

The mean of $t_{ij}^{(n)}$ is

$$m(t_{ij}^{(n)}) = q_{ij}^{(0)} + q_{ij}^{(1)} + \dots + q_{ij}^{(n)}$$

the i, jth entry of

$$Q^{(0)} + Q^{(1)} + \dots + Q^{(n)}$$

where $Q^{(0)} = I$.

Then

$$n_{ij} = \lim_{n \rightarrow \infty} m(t_{ij}^{(n)})$$

is the i, j th entry of the fundamental matrix expressed in (1). The value of n_{ij} is the mean number of times the chain is in transient state s_j given that it started in transient state s_i and continues until the process is absorbed (i.e., reaches an absorbing state).

3. Statistics on the number of times the process is in a transient state. Let v_i denote the number of steps (including the original position) before absorption, given the starting state is s_i . If s_i is in an absorbing state, then $v_i = 0$. Given that the absorbing chain contains a transient set denoted by T , and s_i is a transient state if and only if $s_i \in T$ (i.e., s_i "is a member of" T). Then

$$m(v_i) = \sum_{s_j \in T} n_{ij} \quad (3)$$

which is the i th row sum of the fundamental matrix N . Each row sum of N appears in the $m \times 1$ column vector

$$\alpha = NC \quad (4)$$

where C is a $m \times 1$ column vector whose entries are all 1's.

The variance of the function v_i is

$$\text{var}(v_i) = m(v_i^2) - (m(v_i))^2$$

where

$$m(v_i^2) = \sum_{s_j \notin T} p_{ij} \cdot 1 + \sum_{s_j \in T} p_{ij} m[(v_i + 1)^2]$$

(Note that the original position is necessarily included in the expression for $m(v_i^2)$.)

Continuing,

$$m(v_i^2) = \sum_{s_j \notin T} p_{ij} + \sum_{s_j \in T} p_{ij} m(v_i^2 + 2v_i) + p_{ij}$$

$$= \sum_{s_j \in T} p_{ij} [m(v_i^2) + 2m(v_i)] + 1$$

$$\{m(v_i^2)\} = \left\{ \sum_{s_j \in T} p_{ij} [m(v_i^2) + 2m(v_i)] + 1 \right\}$$

The braces denote a column vector where each entry corresponds to a different value of i .

Therefore,

$$\{m(v_i^2)\} = Q \{m(v_i^2)\} + 2Q\alpha + C$$

$$[I - Q] \{m(v_i^2)\} = 2Q\alpha + C$$

$$\{m(v_i^2)\} = [I - Q]^{-1} [2Q\alpha + C]$$

$$= 2NQ\alpha + NC$$

$$= 2NQ\alpha + \alpha$$

Since

$$N = \frac{I}{I - Q}$$

$$N - NQ = I \quad \text{and} \quad NQ = N - I$$

and

$$\{m(v_i^2)\} = 2[N - I]\alpha + \alpha$$

$$= [2N - I]\alpha$$

Finally, the variance of v_i for each i expressed as entries in $m \times 1$ column vector is

$$\begin{aligned} \{\text{var}(v_i)\} &= \{m(v_i^2) - (m(v_i))^2\} \\ &= [2N - I]\alpha - \alpha_{sq} \end{aligned}$$

where α_{sq} results from squaring each entry $m(v_i)$ in α shown in (4).

Example 4. A particle moves a unit distance along a straight line. Given that it is in s_i , it moves to s_{i+1} , one unit to the right, with probability 0.5, or to state s_{i-1} , one unit to the left, with probability 0.5. Two states are introduced, one at each end of the line, to serve as barriers. These are absorbing states such that the process is absorbed if it reaches either absorbing state. Assume there are five states where s_1 and s_5 are absorbing, and $s_2, s_3,$ and s_4 are transient. The probability matrix appears in Example 3. Reordering the rows and columns gives the following canonical form:

$$P = \begin{array}{c} \begin{array}{ccccc} & s_1 & s_5 & s_2 & s_3 & s_4 \\ \begin{array}{c} s_1 \\ s_5 \\ s_2 \\ s_3 \\ s_4 \end{array} & \begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0.5 & 0 & 0 & 0.5 & 0 \\ 0 & 0 & 0.5 & 0 & 0.5 \\ 0 & 0.5 & 0 & 0.5 & 0 \end{bmatrix} \end{array} \end{array}$$

The fundamental matrix is

$$N = [I - Q]^{-1} = \begin{matrix} & \begin{matrix} s_2 & s_3 & s_4 \end{matrix} \\ \begin{matrix} s_2 \\ s_3 \\ s_4 \end{matrix} & \begin{bmatrix} 1.5 & 1 & 0.5 \\ 1 & 2 & 1 \\ 0.5 & 1 & 1.5 \end{bmatrix} \end{matrix}$$

Thus, for example, if the process starts in state s_2 , the mean number of time it is in state s_2 , s_3 and s_4 is 1.5, 1 and 0.5, respectively.

Furthermore,

$$\lim_{n \rightarrow \infty} P^n = \begin{bmatrix} I & 0 \\ NR & 0 \end{bmatrix}$$

since

$$\lim_{n \rightarrow \infty} Q^n = 0$$

and

$$\lim_{n \rightarrow \infty} M = NR$$

as shown in (1) and (2).

In example 4

$$R = \begin{matrix} & \begin{matrix} s_1 & s_5 \end{matrix} \\ \begin{matrix} s_2 \\ s_3 \\ s_4 \end{matrix} & \begin{bmatrix} 0.5 & 0 \\ 0 & 0 \\ 0 & 0.5 \end{bmatrix} \end{matrix}$$

and

$$NR = \begin{matrix} & \begin{matrix} s_1 & s_5 \end{matrix} \\ \begin{matrix} s_2 \\ s_3 \\ s_4 \end{matrix} & \begin{bmatrix} 0.75 & 0.25 \\ 0.5 & 0.5 \\ 0.25 & 0.75 \end{bmatrix} \end{matrix}$$

Hence, for example, if the process starts in state s_2 , it will be absorbed in state s_1 with probability 0.75 or in state s_5 with probability 0.25. The row sums of NR are necessarily 1 in accordance with Theorem 1. The mean number of steps before absorption including the original position for each transient starting state appears in α as shown in (4).

$$\alpha = NC = \begin{matrix} s_2 \\ s_3 \\ s_4 \end{matrix} \begin{bmatrix} 3 \\ 4 \\ 3 \end{bmatrix}$$

The mean number of steps before absorption is 3 if the process starts in s_2 or s_4 ; whereas, it is 4 if the process starts in s_3 .

The variance of the number of steps (including the original position) before absorption for each starting state appears in the column vector

$$[2N - I]\alpha - \alpha_{sq}$$

from expression (5). In example (4)

$$2N - I = \begin{bmatrix} 2 & 2 & 1 \\ 2 & 3 & 2 \\ 1 & 2 & 2 \end{bmatrix}, \quad \alpha = \begin{bmatrix} 3 \\ 4 \\ 3 \end{bmatrix} \quad \text{and} \quad \alpha_{sq} = \begin{bmatrix} 9 \\ 16 \\ 9 \end{bmatrix}$$

Thus

$$[2N - I]\alpha - \alpha_{sq} = \begin{matrix} s_2 \\ s_3 \\ s_4 \end{matrix} \begin{bmatrix} 8 \\ 8 \\ 8 \end{bmatrix}$$

The mean number of steps before absorption is greatest for starting at s_3 . However, the variance is the same for each starting transient state. (Note that when the variances are quite large compared to the corresponding entries in α_{sq} , it indicates that the means are unreliable estimates for that particular chain.)

C. Model of Absorbing Markov Chain for Class II and IV Systems

Consider a portion of an area to be monitored as shown in Fig. 3-5. Subareas are 5 x 5 square blocks, and each subarea has an identical sensor layout. A (monitored) vehicle entering a sensed intersection corresponds to an absorbing state. This is to be interpreted as updated information as to the vehicle's location. When the process is in an absorbing state, the location of the monitored vehicle is known (to within the detection radius of the sensor). A vehicle entering an unsensed intersection corresponds to a transient state. The absorbing Markov chain models a sequence of experiments for locating a vehicle to within prescribed limits of accuracy.

Given that a vehicle starts at any given intersection (sensed or unsensed), what is the mean and variance of the number of blocks the vehicle moves until being sensed? Once the vehicle is sensed, a new experiment begins. Thus, between sensings, an uncertainty exists as to the vehicle's location. This is reflected in the magnitude of the mean and variance of the number of blocks the vehicle moves between sensings.

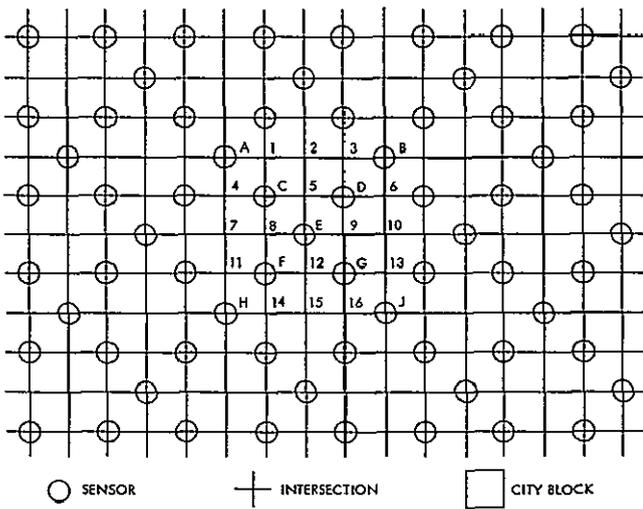


Fig. 3-5. Urban Distribution Pattern for Monitored Proximity Sensors

The number of sensors, their layout, and transition probabilities between orthogonally adjacent intersections is required a priori information. Uniformity of deployment of sensors assumes unbiased routes. Random movement of the vehicle corresponds to unbiased routing through the sensed area. Thus the direction of travel of a vehicle from an intersection will be in any one of four possible directions with equal probability.

If one were to incorporate a different transition probability for each of the four possible directions, the number of states in the Markov chain model would increase fourfold. Each state would be associated with a pair of labels. The intersection entered would be designated by one label and the direction from which it was entered by the other. Such a transition matrix would be meaningful if the transition probabilities were accurately known. That is, the probability that a vehicle upon leaving a particular intersection will go straight, make a left turn, a right turn or a U-turn is a priori information. Without this information, equiprobable direction of travel (to any of the four adjacent intersections) is assumed. The resulting statistical accuracy establishes achievable bounds on the system's accuracy.

Returning to Fig. 3-5, only the subarea with labeled intersections need be considered. Boundary intersections (of the subarea) act as reflecting boundaries in the Markov chain model. A vehicle in intersection 1 corresponds to the process being in transient state 1. The transition probability from state 1 to the intersection due North is 0.25. Since that intersection has the same relative location in its subarea as does intersection F in the subarea under discussion, an upward move (due North) is equivalent to a reflection to intersection F. Identical sensor layouts for all subareas is clearly required. This permits the use of a small transition matrix (25 x 25 in Fig. 3-5) for a Markov chain model of an entire area where fringe effects are neglected. Intersections labeled with characters are sensed and are associated with absorbing states. Unsensed intersections are labeled with numbers and are associated with transient states. The reflection properties of transient boundary intersections are apparent in the

submatrices Q and R in Figs. 3-6 and 3-7, respectively. (Note that states s_1 and s_4 are reflecting boundaries in Example 2.)

The matrix N and column vectors $\alpha = NC$ and $[2N - I]\alpha - \alpha_{sq}$ were computed on an IBM 360/65. The components of α and α_{sq} rounded to 3 decimal places are:

1	1.667	2.778
2	2.667	7.111
3	1.667	2.778
4	1.667	2.778
5	1.667	2.778
6	1.667	2.778
7	2.667	7.111
8	1.667	2.778
9	1.667	2.778
10	2.667	7.111
11	1.667	2.778
12	1.667	2.778
13	1.667	2.778
14	1.667	2.778
15	2.667	7.111
16	1.667	2.778

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
1	0	.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0
2	.25	0	.25	0	.25	0	0	0	0	0	0	.25	0	0	0	0
3	0	.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0
4	0	0	0	0	0	0	.25	0	0	0	0	0	0	0	0	0
5	0	.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0
6	0	0	0	0	0	0	0	0	0	0	.25	0	0	0	0	0
7	0	0	0	.25	0	0	0	.25	.25	0	.25	0	0	0	0	0
8	0	0	0	0	0	0	.25	0	0	0	0	0	0	0	0	0
9	0	0	0	0	0	0	0	0	0	.25	0	0	0	0	0	0
10	0	0	0	0	0	.25	0	.25	.25	0	0	0	.25	0	0	0
11	0	0	0	0	0	0	.25	0	0	0	0	0	0	0	0	0
12	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	.25
13	0	0	0	0	0	0	0	0	0	.25	0	0	0	0	0	0
14	0	0	0	0	0	0	0	0	0	0	0	0	0	0	.25	0
15	0	0	0	0	.25	0	0	0	0	0	0	.25	0	.25	0	.25
16	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	.25

Fig. 3-6. Submatrix Q of Absorbing Chain Model for Monitored Subarea in Fig. 3-5

2-2

	A	B	C	D	E	F	G	H	J
1	.25	0	.25	0	0	.25	0	0	0
2	0	0	0	0	0	0	0	0	0
3	0	.25	0	.25	0	0	.25	0	0
4	.25	0	.25	.25	0	0	0	0	0
5	0	0	.25	.25	.25	0	0	0	0
6	0	.25	.25	.25	0	0	0	0	0
7	0	0	0	0	0	0	0	0	0
8	0	0	.25	0	.25	.25	0	0	0
9	0	0	0	.25	.25	0	.25	0	0
10	0	0	0	0	0	0	0	0	0
11	0	0	0	0	0	.25	.25	.25	0
12	0	0	0	0	.25	.25	.25	0	0
13	0	0	0	0	0	.25	.25	0	.25
14	0	0	.25	0	0	.25	0	.25	0
15	0	0	0	0	0	0	0	0	0
16	0	0	0	.25	0	0	.25	0	.25

Fig. 3-7. Submatrix R of Absorbing Chain Model for Monitored Subarea in Fig. 3-5

Thus, starting in a transient state or an unsensed intersection, the mean number of blocks a vehicle moves before being sensed is 1.667 or 2.667. The variance of the number of moves for each starting state (1 through 16) is 1.778 which are the entries of

$$[2N - I]\alpha - \alpha_{sq}$$

Since 1.778 is a fraction of 2.778 and 7.111 (the distinct entries of α_{sq}), the means given in α are reliable estimates for the layout in Fig. 3-5.

Note that the probability of being sensed cannot be computed. The probability of being sensed by a sensor in the same relative location as say B (Northeast corner of a subarea) can be determined from NR. See Example 4.

The ratio of sensed intersections to the total number of intersections in a monitored area is of interest. In Fig. 3-5, 4 sensors are each sharing 4 subareas. These are sensors at intersections A, B, H and J. Thus the total number of sensors per subarea for 5 (interior) + 4 (each shared by 4 subareas)/4 or 6. The total number of intersections per subarea is 9 (interior) + 4 (each shared by 4 subareas)/4 + 12 (each shared by 2 subareas)/2 or 16. Thus the ratio of sensed intersections to total intersections is 3/8.

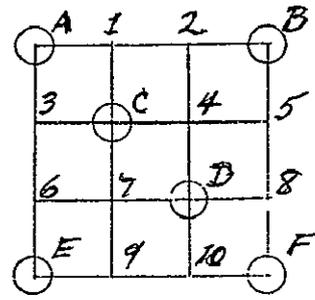


Fig. 3-8. Monitored Subarea with Sensor Density of 3/9

Consider a monitored area with identical subareas as shown in Fig. 3-8 where the ratio of sensed intersections to total intersections is 3/9. Its associated submatrices Q and R appear in Figs. 3-9 and 3-10, respectively. For completeness the fundamental matrix $N = [I - Q]^{-1}$ corresponding to Fig. 3-8 appears in Fig. 3-11. The entries are rounded off to 3 decimal places.

The mean and variance of the number of blocks a vehicle moves before detection starting from each of the unsensed intersections is 2 and 2, respectively.

	1	2	3	4	5	6	7	8	9	10
1	0	.25	0	0	0	0	.25	0	0	0
2	.25	0	0	.25	0	0	0	0	0	0
3	0	0	0	.25	0	.25	0	0	0	0
4	0	.25	0	0	.25	0	0	0	0	0
5	0	0	0	.25	0	0	0	.25	0	0
6	0	0	.25	0	0	0	.25	0	0	0
7	0	0	0	0	0	.25	0	0	.25	0
8	0	0	0	0	.25	0	.25	0	0	0
9	0	0	0	0	0	0	.25	0	0	.25
10	0	0	0	.25	0	0	0	0	.25	0

Fig. 3-9. Submatrix Q of Absorbing Chain Model for Monitored Subarea in Fig. 3-8

	A	B	C	D	E	F
1	.25	0	.25	0	0	0
2	0	.25	0	.25	0	0
3	.25	0	.25	0	0	0
4	0	0	.25	.25	0	0
5	0	.25	.25	0	0	0
6	0	0	0	.25	.25	0
7	0	0	.25	.25	0	0
8	0	0	0	.25	0	.25
9	0	0	.25	0	.25	0
10	0	0	0	.25	0	.25

Fig. 3-10. Submatrix R of Absorbing Chain Model for Monitored Subarea in Fig. 3-8

	1	2	3	4	5	6	7	8	9	10
1	1 073	0 29	0 021	0 089	0 024	0 083	0 311	0 006	0 083	0 021
2	0 287	1 15	0 006	0 311	0 083	0 024	0 089	0 021	0 024	0 006
3	0 021	0 083	1 073	0 311	0 083	0 29	0 089	0 021	0 024	0 006
4	0 077	0 308	0 003	1 156	0 308	0 012	0 044	0 077	0 012	0 003
5	0 021	0 083	0 006	0 311	1 15	0 024	0 089	0 287	0 024	0 006
6	0 006	0 024	0 287	0 089	0 024	1 15	0 311	0 006	0 083	0 021
7	0 003	0 012	0 077	0 044	0 012	0 308	1 156	0 003	0 308	0 077
8	0 006	0 024	0 021	0 089	0 29	0 083	0 311	1 073	0 083	0 021
9	0 006	0 024	0 021	0 089	0 024	0 083	0 311	0 006	1 15	0 287
10	0 021	0 083	0 006	0 311	0 083	0 024	0 089	0 021	0 29	1 073

FIG 7 The Fundamental Matrix N Corresponding to Fig 4

Fig. 3-11. Fundamental Matrix N Corresponding to Fig. 3-8

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**PART FOUR:
AM BROADCAST AND BURIED
LOOP FEASIBILITY ANALYSES
FOR AVM USE**

**G.R. Hansen
L.J. Zottarelli**

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G. R. Hansen

I. VEHICLE LOCATION BY MEANS OF AM BROADCASTING STATION CARRIER SIGNALS*

Carrier signals of commercial AM broadcasting stations can be used as the source of vehicle location information.[†] As in well-known navigation systems, the signals radiating from pairs of stations will form an hyperbolic grid or coordinate system, and vehicles which are equipped with phase-lock receivers and phase repetition counters can keep track of the location of the vehicle in this hyperbolic coordinate grid. This information is then periodically transmitted to a central command base where the transformation from hyperbolic to geographic coordinates is performed, and the actual location of the vehicle is determined and displayed.

A. Introduction

Most vehicle location and navigation systems require dedicated transmitter-receiving equipment combinations and frequency allocations for the location function. A particular advantage of the AM broadcast phase-difference monitoring system is that commercial station signals (0.53 to 1.60 MHz) are used to furnish the vehicle location information. Therefore, neither dedicated transmitters nor special frequency allocations are required.

Carrier signals from three AM stations located near the urban perimeter are used to form a coordinate system of hyperbolas of constant phase difference between the signals from pairs of stations (Fig. 4-1). Therefore, this vehicle location technique shares many of the characteristics of other hyperbolic navigation methods such as OMEGA, LORAN, and particularly DECCA. In this location method, however, the transmission frequencies from the AM stations need not be synchronized, in contrast to the established navigation systems. It is more akin to the differential versions of the foregoing systems. In the differential versions, mobile location equipment is utilized at fixed geographical sites for the purpose of improving the location accuracy of vehicles in the neighborhood by determining the signal phase or delay variance at the known site from that predicted, and this variance is used to correct the location data received by the vehicle.

The AM broadcast vehicle location technique relies on a frequency transformation method whereby the several frequencies of three AM broadcasting stations are separately normalized to a common frequency, and the relative phases of these common frequencies are compared to provide hyperbolic lines of position. An exact integral relationship between the carrier frequencies of the AM stations is not required, although harmonically related frequencies would result in a stationary "virtual hyperbolic pattern" and would somewhat simplify the location process.

Vehicular equipment consists of at least three phase-locked loop receivers to extract the carrier

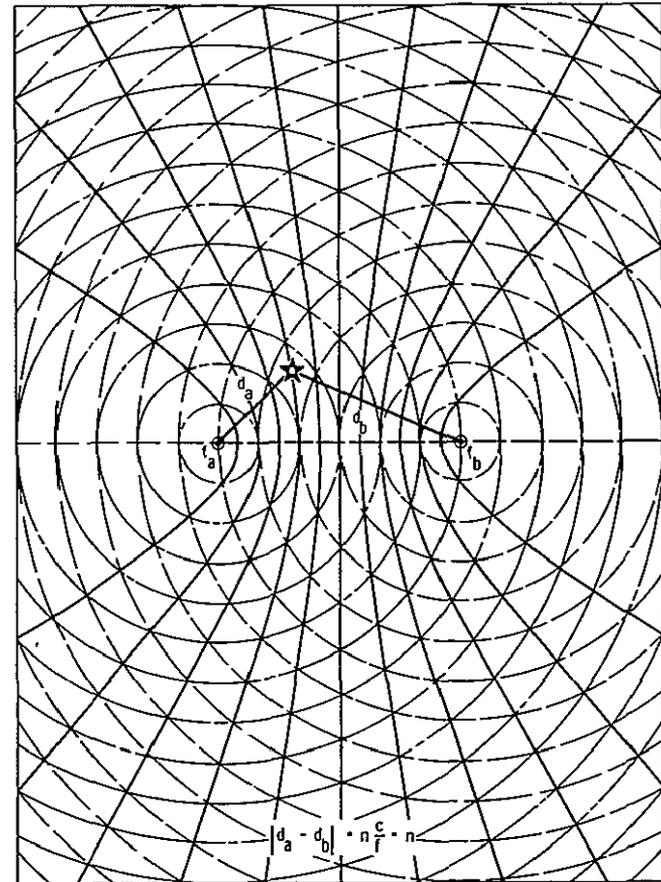


Fig. 4-1. Zero Degree Phase Difference Hyperbolic Contours Produced by Pair of Synchronized RF Signals

frequencies and also a second set of three phase-locked loop frequency multipliers to generate the common frequency. Phase comparators and digital counters are used to keep track of the vehicle location within the "virtual hyperbolic pattern." The hyperbolic coordinates are stored for subsequent transmission to a central command and control base.

Central equipment required consists of a limited arithmetic processor or table look-up computer which is needed to relate the hyperbolic pattern coordinate information to an actual geographical location

B. Hyperbolic Location Principles

If two separated and synchronized sources of radiation transmit signals in an isotropic medium, a receiver positioned midway between them, or on the locus of points which is equidistant from each transmitter, will detect no difference in the time-of-arrival or the phase of the signals from the separate sources. The locus is the perpendicular bisector of the connective between the two sources. (See Fig. 4-1.)

* U.S. Patent 3,889,264.

If the receiver is at one side or the other of the bisector, the signal from the nearer transmitter will arrive at some finite amount of time before the signal from the farther source. If the signals are continuously transmitted, the phase of the nearer will lead the phase of the farther. Another locus of constant time or phase difference can be generated by maintaining the same difference in distance from the receiver to each transmitter. The curves for constant time or phase difference will be confocal hyperbolas that are symmetric around the bisector (see Fig. 4-1).

A line-of-position (LOP) can be determined relative to a pair of RF transmitters by noting the time difference in the arrival of the signals, which corresponds to one of the hyperbolas. There will be ambiguity as to which branch of the hyperbola represents the true LOP. If the signals are continuous wave and only the phase differences are determined, the degree of LOP ambiguity increases many-fold since the phase pattern is repeated whenever the cumulative distance change to the two transmitters equals one wavelength. The resolution of the ambiguity is described later.

If the two stations are transmitting on slightly different frequencies, the relative phase between the carriers will change cyclically at a rate determined by the difference in frequency. This rate will be the same anywhere that the two signals can be received. If the locus of lines of constant phase difference are now considered, they again comprise a family of confocal hyperbolas, but instead of being stationary, they will sweep through the area covered by the two stations (Fig. 4-2). The hyperbolas, as a function of time, will tend to

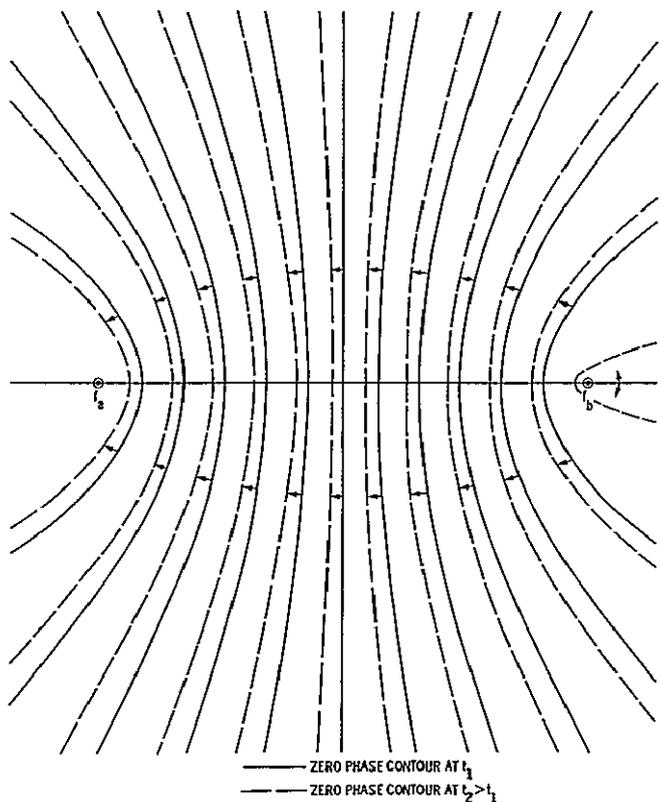


Fig. 4-2. Apparent Motion of Hyperbolas Due to Slight Difference in Two Signal Frequencies

form acutely around the station radiating the higher frequency and then move toward the lower frequency station; straightening as they reach the midpoint, then curving around the lower frequency station and then vanishing on the extension of the line joining the stations. A receiver capable of counting the passage of hyperbolas representing a particular phase difference will accumulate the same count in the same time interval regardless of the location within the service area of the two stations.

If the constant-phase difference counting receiver is positioned in a stationary hyperbolic field, no counts will be accumulated as long as the receiver's location is fixed. If the receiver is moved in such a manner as to cause the difference in the distances to the two stations to change by one wavelength, then one count will be accumulated. Similarly, in a moving field, a one-unit difference in counts will be accumulated by a stationary receiver as compared to a receiver that is moved by a wavelength distance difference.

The AVM system based on AM broadcast signals is discrete as opposed to continuous location systems in that the intersections of hyperbolas form a grid which can be transformed into specific urban area locations corresponding to these intersections. Interpolation between grid lines is not used. Therefore it is somewhat like a proximity system with the hyperbolic intersections taking the place of physical devices or signposts located at intersections or at fixed points. Continuous systems provide somewhat uniform coverage of the service area and allow any geographical locations within this area to be determined to some limiting precision dictated by the technique. The grid described by the intersection of the hyperbolas allows the actual geographical location of the vehicle to be somewhere within the hyperbolic triangle described by the coordinates of a particular triad vertex. The dimensions of this triangle are a function of the distance to the foci of the two families of hyperbolas and also of the wavelength of the common frequency. In most continuous AVM systems, the precision diminishes with the distance from the fiducial points. In the AM Broadcast hyperbolic AVM system, the location precision can be adjusted in the principal service area by the choice of the common frequency.

Established navigation systems such as OMEGA, LORAN, and DECCA refer to the areas between adjacent hyperbolas of constant phase as lanes. These navigation lanes vary in width from 1.5 to 15 km, depending on the frequency used in the system, and the principal goal of these methods is to maintain a vehicle's location precisely within a selected lane. In contrast, the AM broadcast vehicle location method utilizes much narrower (e.g., 0.15 km) lanes and keeps track only of the ID number of the hyperbola of constant phase difference that the vehicle has crossed and in which direction the hyperbola was traversed. Therefore, the location precision is a function of the lane width and will vary with the distance from the AM station pair. This system is intended for use in metropolitan areas and adjacent suburbs of rather limited size compared to the much larger service areas of navigation systems. Since AM transmitting sites are usually located near the outskirts of the area they serve, the divergence of the hyperbolas and the consequent loss in location precision can be held to reasonable values.

In many prior studies and developments concerned with emergency vehicle location problems (see Bibliography), a general goal has been to provide a location capability to one city block, or roughly 0.16 km (0.1 mile). Lane widths of this size can be generated with a frequency of 1 MHz.

In order to generate a hyperbolic coordinate system from AM station signals, these signals must be transformed to a common frequency which is phase coherent to the AM carrier. To be useful without restraints requires that this common frequency be a multiple of the highest common divisor of the available AM carriers. The common frequency should therefore be a multiple of 10 kHz.

The individual AM carrier signals are received by the vehicle receivers, and these signals in turn are each used to separately synthesize the common frequency. The common frequencies are therefore phase-coherent with the original AM carriers and effectively change the radiation from each of the AM stations to the common frequency. A virtual hyperbolic pattern is generated from each pair of AM stations received; and if the AM signals were phase coherent, the pattern will be stationary in space. It is then only necessary to measure the phase differences and count the number of times the phase pattern has repeated as the vehicle travels in order to determine a new location from a known starting point. Three pairs of signals (three station) are sufficient to remove any ambiguity in the determination of the new location from the old location (Fig. 4-3). Since the

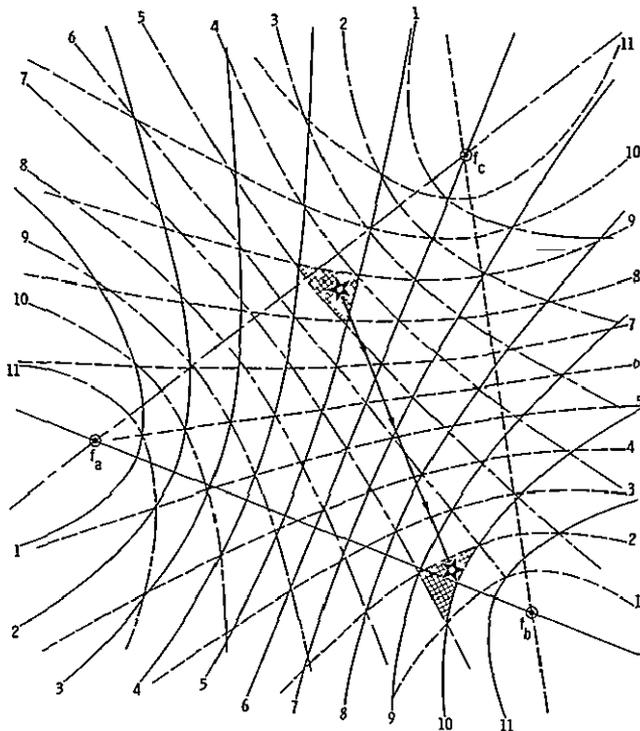


Fig. 4-3. Change in Receiver Location from Hyperbolic Area 5-9-5 to 10-2-7

spacing of the hyperbolic patterns is a function of the distance from the station pair, the relationship between the phase pattern counts and actual distances traveled would have to be computed. In this AVM system, the computational ability need not be

placed in each vehicle. The computation of locations is reserved for the central command base where the location information is desired.

It is immaterial whether the hyperbolic grid pattern is fixed or moving as far as the location process is concerned. If fixed, then only the counts accumulated by moving receivers are necessary to determine the new positions from the old. If the grid is moving, then the difference in counts between the moving receivers and a stationary receiver is all that is required. Besides the magnitude of the counts, it is also necessary to know the "direction" of passage of the hyperbola of constant phase difference. The hyperbolas always move from the higher frequency source toward the lower frequency. If the hyperbolas are stationary, the vehicle's movement toward one source will tend to increase the apparent frequency from that source while decreasing the frequency of the other. Therefore an assignment can be made as to which direction is to be called a positive count and which a negative count.

C. Vehicle Equipment Requirements

A block diagram of one of the receivers to be installed in the vehicles is shown in Fig. 4-4.

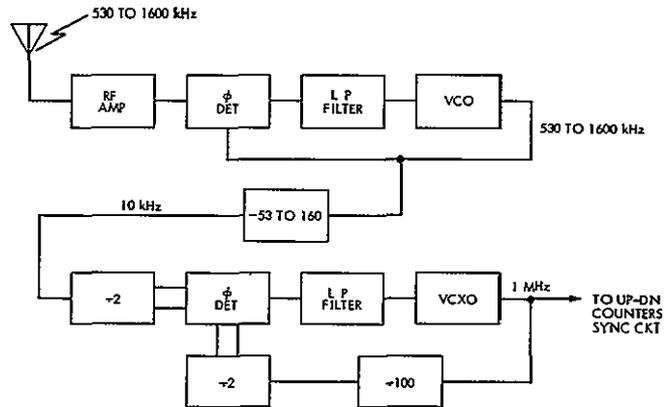


Fig. 4-4. Phase-Locked Loop AM Receiver on Vehicle for Hyperbolic AVM Technique

Three of these receivers are required for each vehicle. A conventional RF amplifier is used to provide selectivity and gain of the desired AM signal applied to the phase detector of the phase-lock loop (PLL). The voltage-controlled oscillator frequency in the PLL is adjusted to run at the same frequency as the AM station carrier. The oscillator output is divided by a variable modulus counter (-53 to 160) so as to produce an output frequency of 10 kHz. The 10 kHz signal is applied to a flip-flop which provides a square-wave of 5 kHz used as the reference input to the phase detector of the frequency multiplying PLL. A 1 MHz voltage-controlled crystal oscillator is phase-locked to the 5 kHz reference by dividing the oscillator frequency by 200 to produce a second 5 kHz signal which is compared to the reference. Therefore, the 1 MHz signal is phase-locked to the AM carrier frequency so that the phase relationship between the 1 MHz and the carrier is repeated at least every 53 to 160 cycles of the AM carrier.

Three such receivers, each tuned to a different AM station, will produce three separate 1 MHz

signals, each phase-coherent with the appropriate AM carrier.

The problem then remains to determine the ID number and direction of the hyperbola that is either traversing or being traversed by the vehicle. As stated previously, the measurement of the frequency difference and the determination of which is the greater frequency are required. The technique selected to determine the frequency difference and also to yield information as to which is the higher or lower frequency is to use an up-down counter in which one frequency provides incrementing pulses and the other decrementing pulses. The state of the counter should then indicate the integrated frequency difference between the two frequencies which is the algebraic sum of the hyperbola of constant phase difference traversed.

The up-down counter must respond to every incrementing and decrementing pulse because any pulse missed will displace the measured location by one unit in the hyperbolic grid. In order to prevent the uncertainty in the up-down counter which could be caused by the simultaneous arrival of up and down pulses, resynchronization of the 1 MHz pulses was required. A synchronizing frequency at least four times the frequency to be counted is required to assure that no pulse is lost or split. The logic for resynchronizing to 4.192 MHz is shown in Fig. 4-5. The logic discards both incrementing and decrementing pulses which are inputs to the same up-down counter and arrive in the same synchronizing interval.

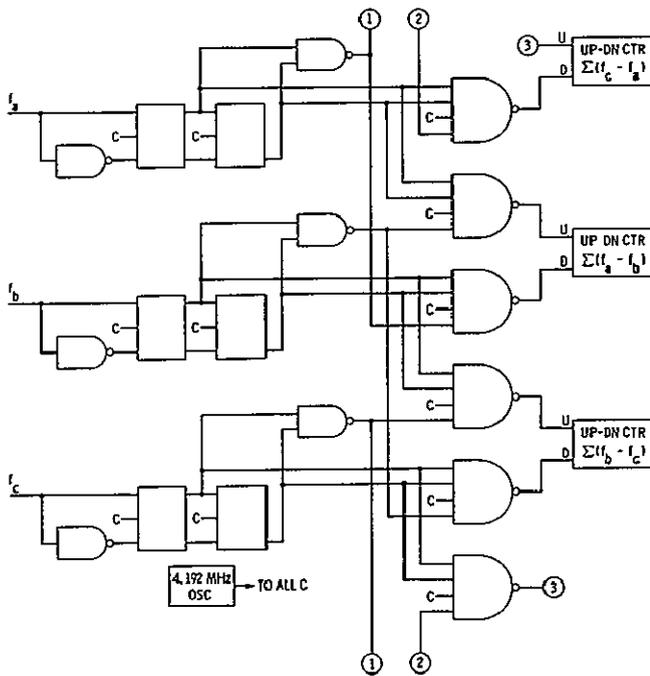


Fig. 4-5. Up-Down Counters Sync Logic for Hyperbolic AVM Technique

Each of the three counters in the receiver maintains a count which is the integrated algebraic sum of the apparent frequency difference between a pair of AM stations each nominally radiating at the common frequency. Part of this frequency difference is due to the AM stations not being phase coherent

(i. e., not exactly on the assigned frequency) and part is due to vehicular motion.

D. Vehicle Location Method

If three AM stations, A, B, and C, are monitored (Fig. 4-3) and the transformation of the carriers yields three common frequencies f_a , f_b , and f_c , then the three counters in the vehicles will accumulate counts N in a time t in accordance with:

$$N_a = (f_a - f_b)t + V_{ab} (f)t \times F(x, y) - C$$

$$N_b = (f_b - f_c)t + V_{bc} (f)t \times G(x, y) - C$$

$$N_c = (f_c - f_a)t + V_{ca} (f)t \times H(x, y) - C$$

$$C = 3 \times 10^9 \text{ m/sec}$$

where f is the common frequency, V is the vehicle velocity component parallel to the baseline of the station pair, and F, G, and H are general equations of the second degree (describing the three families of hyperbolas) in terms of X and Y which are the geographical location of the vehicle in an arbitrary orthogonal coordinate system. This system of equations does not yield an explicit analytic solution for the location in terms of X and Y. It does indicate the separability of the counts due to slight differences in the common frequency and the counts caused by vehicle motion. Counting is negligibly influenced by the difference in frequency of f_a , f_b , or f_c .

At the base, the location process is initialized by first receiving the actual geographical location (in X and Y) of the vehicle and the initial content of the three counters (called N_{a1} , N_{b1} , and N_{c1} , respectively). The coordinates in X and Y and the counter states are stored. The counter states of the stationary receiver are also stored at the same instant. An explicit calculation is then made using the X-Y location and the coordinates of the AM stations which yield the location of the vehicle in terms of the parametric families of the hyperbolas. Each hyperbola in each family is numbered, and the results of this calculation give the location in three integers which represent the nearest hyperbola of each family.

Subsequent locations are determined by receiving the current state of the three counters from the vehicle. First, the initial state of the vehicle counters is subtracted from the current state, and second, the change in the state of the stationary receiver counters (from the initializing time to the current time) is determined and subtracted to yield the change in each of the hyperbolic coordinates caused by vehicle motion. The new X-Y coordinates of the vehicle location are then calculated with an iterative least-squares algorithm. The algorithm uses the old X-Y location and develops the required changes in X and Y so that the calculated new position will have the same hyperbolic coordinates as those determined for the vehicle from the current counter states. This method was chosen over an analytic technique as it yields a "most likely" solution in less time than an analytic method which has the additional disadvantage of having several pairs of coordinates as solutions.

Only two of the three available hyperbolic coordinates are necessary in all of the calculations

as the third coordinate is not independent. The third coordinate does provide a check in that the sum of the hyperbolic coordinates should be a constant plus or minus one. Additionally, for locations near the vertex (the one AM station common to each hyperbolic family), the algorithm may become divergent and another set of coordinates should be used.

E. Accuracy Analysis

All AM broadcast stations in the United States operate on assigned carrier frequencies which are multiples of 10 kHz in the frequency region between 530 and 1600 kHz. The FCC requires that the actual carrier frequency be within 20 Hz of the assigned frequency. If all the AM stations within a given geographical area were exactly on the assigned frequency, the relationship between any two stations could be expressed as:

$$(1) f_1/f_2 = (n + p)/n, \text{ where } n \text{ and } p \text{ are} \\ \text{both integers.}$$

The carriers could be said to be phase-coherent in that the phase relationships between the two carriers are repeated every $n + p$ cycles for one carrier and every n cycles for the other. If this condition is maintained, it is then possible to synthesize another frequency, which is also a multiple of 10 kHz which is phase-coherent to each of the carriers within the area.

The 10 kHz can be multiplied to another frequency, say 1 MHz, which will be phased coherent with the original carrier. Since the FCC allows a frequency tolerance of 20 Hz, the synthesized 1 MHz signal will have a tolerance of:

$$(2) \pm X \text{ Hz} = \pm 20 \text{ Hz} (10^6 \text{ Hz})/f \text{ Hz, where} \\ f \text{ is the AM carrier frequency.}$$

Therefore X can vary between 39 and 12 Hz, depending upon the frequency of the AM broadcasting carrier. It is therefore possible that a pair of AM stations could cause a beat frequency between the two "normalized" carriers approaching 80 Hz. The impact of the frequency difference is principally upon the equipment design, the sampling rate for location purposes, and the amount of information that must be transmitted from the vehicle. These effects will be discussed later.

A secondary effect of the AM carrier being off frequency and thereby causing the 1 MHz to be slightly off is that the location process will be reduced in precision. A wavelength of the actual frequency will be slightly shorter or longer than expected by up to 39 parts per million. This error would be on the order of 1 meter on the baseline connecting a station pair with a separation of 30 km and up to 2 meters some 60 km away from either station and therefore negligible.

F. System Data Requirements and Polling Intervals

System considerations determine how much information is needed from each vehicle and how often it should be sent. Prior work in automatic vehicle monitoring has usually emphasized the fixed-rate polling method of interrogating vehicles

to determine locations. If the polling method allows any or all vehicles to travel at maximum speed and still be located to the ultimate precision, the information flow is maximized from each vehicle. If an average speed is assumed for the fleet of vehicles, then high-speed vehicles will not be located to the precision available, and parked or slowly moving vehicles will be transmitting much redundant data. Volunteer methods wherein the vehicle initiates a data transmission whenever a significant change in location has occurred require means to avoid contention and must also send additional data to identify which vehicle is transmitting. An adaptive polling technique whereby high-speed vehicles are interrogated at much shorter intervals and where average and slowly moving or parked vehicles are infrequently sampled is quite easily mechanized. The simplest polling technique requires that the central control transmit incrementing pulses (tones, or tone bursts) to all vehicles which count and accumulate these incremental signals. When the number of signals received matches the number assigned to the vehicle, a data transmission is initiated from the vehicle. The inclusion of a respond or do-not-respond pulse, tone, or burst with the incrementing signal will tell the vehicle whether data is required or not. Conversely, a vehicle which had been immobile could request inclusion in the next polling sequence by responding with an appropriate signal regardless of the command not to send data.

The amount that the AM carriers are off frequency together with the sampling intervals of the vehicles determines the number of bits required to be sent to the central command for location purposes. The length of each of the up-down counters is therefore determined by this number of bits. As stated before, two low-end of the band AM stations could cause an 80 Hz beat frequency in the synthesized 1 MHz signals which would cause a total count of about 288,000 per hour to be accumulated. A vehicle cruising at 30 km/hr along the baseline of a station pair would accumulate a count of 200 per hour due in a stationary pattern. A recent Department of Transportation requirement for vehicle monitoring required that 25% of the vehicle fleet be located each 15 sec and the remainder located each minute. The total counts for each station pair under these requirements would be 1200 for 15 sec and about 5000 for the minute interval. To accommodate this requirement, the length of the up-down counters would have to be 13 bits each. Some 40 to 50 bits per interrogation would have to be transmitted from each vehicle if a preamble, parity checks, or error detection information was added to the basic 39 bits of location data. Assuming the higher number over a voice channel from the vehicle which could conservatively accommodate 1200 bit/sec, then 24 vehicles could be interrogated and located each second. Again using the DOT requirement, 820 vehicles could be located each minute, with 205 of the vehicles being located each 15 seconds, or four times each minute for a total of 1435 locations each minute (1440 maximum). It should be realized that these are theoretical maximum numbers and neglect the practical realities of turn-on stabilization time of mobile transmitters and also assumes another channel for interrogation purposes.

The amount of data required from each vehicle could be reduced by about two-thirds if the AM

stations being utilized for location maintained phase coherency. A stationary location pattern would be generated, and the up-down counter lengths could be reduced substantially as only counts due to vehicle motion would be accumulated. Only a relatively small amount of equipment would be necessary at each AM station to maintain the carriers coherent to one another. This could be done by either a common synchronizing signal or with each station referencing the carrier frequency to the other two carriers by counting and phase-locked loop techniques. In either case, the control range of the added equipment must not allow the carrier to be pulled outside of the 20 cycle FCC tolerance limit.

Some operational difficulties that might occur with this type of vehicle location system could be caused by momentary outages of one of the AM carriers, or transmitter switchover when power is increased or reduced. In some smaller metropolitan areas it may be difficult to find three "24-hr" broadcast stations with appropriate geometry, and different configurations may have to be used for day and night operation.

G. Computer Simulation Programs

Two computer programs, a location simulator called LOCATE (Table 4-1), and a vehicle count

Table 4-1. Vehicle Location Simulator Program, LOCATE

```

LOCATE[0]V
V LOCATE
[1] XS=4*YS,XS[1]
[2] YS=4*YS,Y[1]
[3] D=300
[4] X=Z1[1]
[5] Y=Z1[2]
[6] RP=L-1
[7] D=((X-XS)*2)+(Y-Y[1])*2)+0 5
[8] D=D D[1]
[9] C<-300
[10] RE A[L]=((X-XS[L])*D[L])-((X-XS[1])*D[1])
[11] DC=(0 (CTR[1]-LAP[1]),(LA [3]-CTR[3]))*300
[12] B[L]=((Y-Y[1])*D[L])+D[L]-((Y-Y[1])*D[1])
[13] C[LL]=D[L]-B[1]-Q[L]+C[1]
[14] RE=1(30i-L+1)
[15] DFJ=((+A*2)*(+B*2))-((+A*2))*2
[16] AX-(((+A*2)*(+B*2))-((+7*CK)*(+A*2)))+DFJ
[17] DY-(((+A*2)*(+B*2))-((+7*CK)*(+A*2)))+DFJ
[18] X=X-AX
[19] Y=Y-DY
[20] RP=1((|AX|>10)V(|DY|>10))
[21] OLD=X,Y
[22] 'REI' X AND Y ARE 'OLD
[23] 'AX AND DY ARE ' (X-X), (Y-Y)

```

generator called FIG (Table 4-2) were written to test the location method. A SETAUP program (Table 4-3) was also written which stores the locations of the AM stations in the arbitrary coordinate system and determines the lengths of the baselines connecting the stations.

In order to make the simulation more realistic, three AM stations in the Los Angeles, CA, metropolitan area were chosen: KFI (640 kHz) located in the Buena Park-La Mirada area southwest of the Los Angeles Civic Center; KNX (1070 kHz) in Torrance which is south and slightly west of the Civic Center; and KMPC (710 kHz) with transmitter in North Hollywood which is northwest of the Civic Center. The baseline distances are: KFI-KNX 31 km, KNX-KMPC 35 km; and KMPC-KFI 51 km.

Table 4-2. Vehicle Hyperbolic Lane Count Generator Program, FIG

```

VFIG[0]V
V OLD FIG Z2
[1] XS=Z1-Y*-DC-DD-CTR-CNT-W-Q+300
[2] X=Z1[1]-OLD[1]
[3] Y=Z1[2]-OLD[2]
[4] X=X-X2,X3
[5] Y=Y-Y2,Y3
[6] DC-(((X-XS)*2)+(Y-Y[1])*2)+0 5
[7] HD=(DC[1]-DC[1]),(DC[3]-DC[2]),(DC[1]-DC[3])
[8] HD=HD+300
[9] IAH=C+300
[10] CTR=(M+IAI+0 5)
[11] 'OLD COUNTER WAS ' CTR
[12] X=X-Z2[1]
[13] Y=Y-Z2[2]
[14] DD-(((X-XS)*2)+(Y-Y[1])*2)+0 5
[15] HH=(DD[2]-DD[1]),(DD[3]-DD[2]) (DD[1]-DD[3])
[16] 'H=HH+300
[17] CRT=(M+IAH+0 5)
[18] 'NEW COUNTER IS ' CRT
[19] W=CTR-CTR
[20] 'CHANGE WAS ' W
[21] Q=(0,(W[1]) (-W[3]))*300

```

Table 4-3. AM Broadcast Station Locations and Baseline Lengths Program, SETAUP

```

VSETAUP[0]V
V SETAUP
[1] C=Z-P-A-R+300
[2] 'SET X AND Y FOR EACH OF THREE AM STATIONS IN METERS '
[3] C=0
[4] X1=C[1]
[5] X2=C[3]
[6] X3=C[5]
[7] Y1=C[2]
[8] Y2=C[4]
[9] Y3=C[6]
[10] A-((X2-X1)*2),((X3+X2)*2),((X1+X3)*2)
[11] B-((Y2-Y1)*2),((Y3+Y2)*2),((Y1+Y3)*2)
[12] F=(X2-X1),(Y3-Y2),(X1-X3)
[13] P=(Y2-Y1),(Y3-Y2),(Y1-Y3)
[14] L=1
[15] RE G[L]=((B[L])*2)+(F[L]*2)+0 5

```

An arbitrary origin for the coordinate system was located some 8 km (5 miles) in the Pacific west of the Palos Verdes peninsula such that most of the area of interest for location purposes would be in the first quadrant of the X-Y system. The origin is at 118°30'W and 33°45'N.

The location (LOCATE) program and the vehicle count generator (FIG) program were written in APL computer language. The vehicle count generator requires two input variables. These are the initial and terminal values in meters of the X-Y coordinates representing each change of position of the vehicle. The hyperbolic coordinates of each location are calculated and the integral difference determined. The difference represents the counts that would be accumulated by a vehicle in traveling from the initial to the terminal location of each leg of travel. The count difference and the initial location are the inputs to the LOCATE routine which determines the new location. The new location is determined by a reiterative technique whereby the deltas of X and Y which would satisfy

the change in counts of the hyperbolic coordinates are calculated and added to the initial location.

H. Conclusions

A vehicle location method for use in metropolitan areas is available, which uses the carrier signal information from three currently operating AM broadcasting stations located near the urban perimeters. Two advantages of the method are that (1)

dedicated transmitters for location purposes are not required and that (2) the phase-lock-loop counting receivers installed in the vehicles are inexpensive. The mathematical technique for vehicle location is relatively simple and requires only that the initial location be known. While the technique is not explicit, location can be determined with adequate accuracy to the precision implied by the geometric configurations of the AM stations used and the frequency of the synthesized signal used for phase comparison.

II. VEHICLE LOCATION BY MEANS OF BURIED LOOPS*

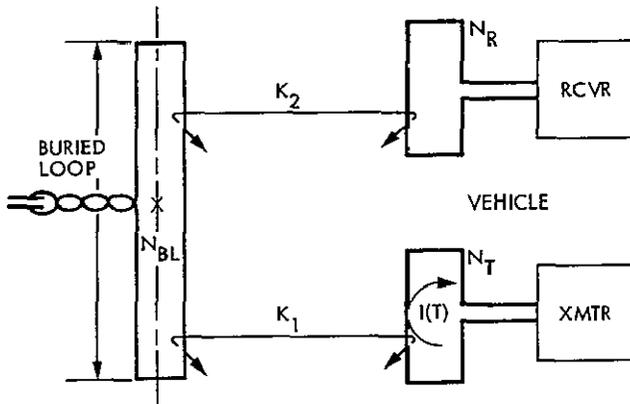
Lawrence J. Zottarelli

With the exception of the cut-to-fit development method, the evaluation of the buried loop* AVM system requires as a basis some mathematically analytic relations. Since such relations do not seem readily available in the open literature, an analytic approach was developed to determine the effects of loop spacings, dimensions, and height above roadway on RF signal detection and on identification of the vehicle's location.

A. Relationships of Three-Loop Vehicle Location System

The approach is to find the mutual inductance of the vehicle's transmitter and receiver loops through the intermediary of the passive buried loop. A typical three-loop configuration is shown in Fig. 4-6. The assumptions are:

1. The XMTR and RCVR are sufficiently remote from each other so that direct mutual inductance is of secondary importance.
2. The buried loop is tuned with a capacitor to the vehicle transmitter frequency, and the buried loop resistance is directly proportional to the number of turns.
3. The loops are in an isotropic medium.



$I(T)$ = XMTR CURRENT
 K_1 = XMTR/BL COUPLING
 K_2 = RCVR/BL COUPLING
 N_R = RCVR TURNS
 N_T = XMTR TURNS
 N_{BL} = BURIED LOOP TURNS
 R_{BL} = BL RESISTANCE

Fig. 4-6. Configuration of Vehicle's Transmitting and Receiving Loops Relative to Buried Loop

1. Analytic Relations of Loop Mutual Inductances

- (1) The magnetic flux lines Φ coupling the buried loop (BL) due to the XMTR current $I(T)$ at point P is

$$\Phi_{BL} = K_1 \cdot N_T \cdot I(T)$$

where

$$I(T) = I_P \sin(\omega t), \quad K_1 = \text{XMTR/BL}$$

coupling, and $N_T = \text{XMTR turns}$.

- (2) The voltage E coupled to the buried loop with width W is

$$E_{BL}(T) = N_{BL} \frac{d\Phi_{BL}}{dt} = W \cdot K_1 \cdot N_T \cdot N_{BL} \cdot I_P \cdot \cos(\omega t)$$

- (3) The current in the buried loop (which is at resonance), with resistance R, is

$$I_{BL}(T) = \frac{E_{BL}(T)}{R_{BL}} = \frac{[K_1 \cdot N_T \cdot N_{BL} \cdot W \cdot I_P \cdot \cos(\omega t)]}{R_{BL}}$$

- (4) The flux lines coupling K_2 the RCVR due to the buried loop is

$$\Phi_{RCVR}(T) = K_2 \cdot N_{BL} \cdot I_{BL}(T)$$

substituting

$$\Phi_{RCVR}(T) = \frac{[-K_1 \cdot K_2 \cdot N_T \cdot (N_{BL})^2 \cdot W \cdot I_P \cdot \cos(\omega t)]}{R_{BL}}$$

- (5) The voltage at the RCVR due to the buried loop is

$$E_{RCVR} = N_R \frac{d\Phi_{RCVR}}{dt} = \frac{[-K_1 \cdot K_2 \cdot N_T \cdot N_{BL} \cdot N_R \cdot (W I_P)^2 \cdot \sin(\omega t)]}{R_{LOOP}}$$

allowing now the resistance per turn (R/turn)

$$R_{loop} = (R/\text{turn}) \cdot N_{BL}$$

$$QED \cdot E_{RCVR} = \frac{[-K_1 \cdot K_2 \cdot N_T \cdot N_{BL} \cdot N_R \cdot (W I_P)^2 \cdot \sin(\omega t)]}{(R/\text{turn})}$$

* U. S. Patent 3, 772, 691, "Automatic Vehicle Location System."

2. Comments. The reasoning involved in deriving the relationship permit the geometrical and electrical aspects of the solution to be separable and simply multiplicative. If E_{RCVR} is to be of the form MdI/dt then:

$$M_{\text{equivalent}} \text{ becomes } [K_1 \cdot K_2 \cdot N_T \cdot N_R \cdot N_{BL} \cdot (WIP)] / (R/\text{turn})$$

and $I(t)$ becomes $IP \cos(\omega t)$

B. Magnetic Field Generated by Rectangular Loop of Wire

1. Development of Flux Density Equations. It is desired to find the flux intensity B at a point $P(x, y, z)$ generated by the rectangular loop of wire, with the X-axis direction across the lane width and the Y-axis in the direction of roadway travel.

Given:

- (1) A rectangular loop of wire of length L and width W , with the lane width equal to the buried loops length.
- (2) The loop is in a free-space plane (of x, y, z rectangular coordinates) having equations $z = 0$.
- (3) The loop has a DC current of I .
- (4) The coordinate space has its origin at $(0, 0, 0)$, which is the center of the loop wire.
- (5) The linkage or mutual inductance of two parallel planar loops (not necessarily coplanar) lying in x, y -plane uses only the z -component of flux density.

Method:

- (1) Decompose the loop into four linear segments
- (2) Apply the Biot Savart law from each segment to the point of interest

$$|B_p| = \left(\frac{\mu}{4\pi}\right) \cdot \left(\frac{I}{a}\right) \cdot (\cos\gamma - \cos\alpha)$$

- (3) Decompose the flux density into its vector components, and sum the components.

The complete mathematical analysis is presented in Ref. 1.

C. Computer Programs for Calculating Mutual Inductance

Two programs are used to generate the mutual inductance of rectangular wire loops. The programs **LOOPS** and **CARCUP** are written in the Stanford Artificial Intelligence Language, "SAIL," which is an extended ALGOL 60.

1. "LOOPS" and "CARCUP" Programs.

The "LOOPS" program is used to find (1) the XMTR/RCVR direct mutual coupling, (2) the self inductance of a loop, and (3) the direct coupling

between the Buried Loop and the XMTR or between the Buried Loop and the RCVR or between two Buried Loops. The "CARCUP" program is used to find the mutual coupling between the XMTR and the RCVR via the Buried Loop, the inner workings of the two programs are similar, the program "CARCUP" is, in effect, the program "LOOPS" run twice. Both of the programs have Input/Output in common.

a. LOOPS Program. This program (Table 4-4) asks the user: (1) if he wants more detailed information, (2) to specify "how many steps," or data points, (3) where is the starting point of the pickup loop and what size is the loop (in terms of XMIN, XMAX, YMIN, YMAX) and how high above the buried loop (in terms of Z), (4) to specify the aspect ratio of the buried loop, K.

The LOOPS program calculates and prints out the mutual inductance for the number of data points specified. Each successive data point represents the mutual inductance of the buried loop and pickup loop moving along the positive Y-direction (along the roadway lane) by 1/10 of its length (i.e., $(YMAX-YMIN)/10$). The mutual inductance is in relative units. To find the answer in henrys, multiply the answer by half the lane width (in meters), by 10^{-7} , by the number of turns of the buried loop, and by the number of turns of the pickup loop.

b. CARCUP Program. This program (Table 4-5) asks the user: (1) if he wants more detailed information, (2) to specify "how many steps," or data point, (3) where is the starting point of the XMTR loop, and what is its size and how high above the buried loop (in terms of XTMIN, XTMAX, YTMIN, YTMAX, ZT); also where is the starting point of the RCVR loop and

Table 4-4. **LOOPS Program for Mutual Inductance of Buried/Pickup Loops, and Sample Run**

```
.TYPE LOOPS SAI
00100 BEGIN "LOOPS"
00150 INTERNAL INTEGER EXIT ,FOPEP.1
00200 INTEGER I,J,S,EPK,
00300 DEFINE RF="153.12"
00400 REAL X,MIN,MAX,Z,MIN,MAX,END,AR,AR,AR,C,D,E,HA,BA,CC,DD,F,
00500 G,H,K,L,M,N,G,P,P,T,Q,R,Z,C,YES,INC,
00550 STRING ST,
00600 OUTSTR("DO YOU WANT NOTES (TYPE IN EITHER YES OR NO FOLLOWED BY
CAP LET) ");
00700
00800 IF INCHL="YES" THEN OUTSTR("
00900 THE PURPOSE OF THIS PROGRAM IS TO CALCULATE THE FREE SPACE
01000 RELATIVE COUPLING BETWEEN TWO FLAT BUT NOT COPLANAR RECTANGULAR
01100 LOOPS OF WIRE (THE SIDES OF WHICH ARE PARALLEL TO THE COORDINATE
01200 AXES OF REFERENCE) IT IS TO BE APPLIED IN AUTOMOTIVE VEHICLE
01300 LOCATION HENCE THE TEMP OF THE FOLLOWING INTRODUCTION.
01400 THE LANE WIDTH IS THE X DIMENSION THE LANE LENGTH IS
01500 THE Y DIMENSION, THE VERTICAL DISTANCE BETWEEN LOOPS IS THE
01600 Z DIMENSION THE CENTER OF THE BURIED LOOP IS AT COORDINATES
01700 0,0,0 THE WIDTH OF THE BURIED LOOP IS THE LANE WIDTH
01800 K IS THE ASPECT RATIO OF THE BURIED LOOP (WIDTH DIVIDED BY
LENGTH)
01900 (MIN,XMAX),MIN,YMAX DETERMINE THE SIDES AND LOCATION OF THE
02000 PICKUP LOOP
02100 ALL INPUT DIMENSIONS ARE TO BE NORMALIZED TO HALF THE LANE
02200 WIDTH.
02400 HOW MANY STEPS REFERS TO MOVING THE PICKUP LOOP ALONG
02500 THE LANE LENGTH (GENERALLY AWAY FROM ABOVE THE BURIED LOOP) BY
02600 1/10 OF THE PICKUP LOOP LENGTH AND THEN CALCULATING ITS
02700 NORMALIZED Z DIRECTED COUPLING FROM THE BURIED LOOP.
02800 THE PRINTOUT IS THE CALCULATED FLUX IN RELATIVE FLUX UNITS
02900 AND OF SUCCESSIVE STEPPING.
03000 TO FIND THE ACTUAL FLUX IN VOLT SECONDS, MULTIPLY THE DATA
03100 BY THE FOLLOWING FACTOR:
03200 (I)*(LANE WIDTH/2)*(10<-7)
03300 WHERE I IS THE BURIED LOOP CURRENT IN AMPS
03400 WHERE THE LANE WIDTH IS IN METERS *RF;
03500 OUTSTR("HOW MANY STEPS ");
03600 Q<(10<REALSCAN(<ST>+INCHL),ERF)); OUTSTR(RF);
03700 BEGIN
03700 REAL ARRAY V(10);
03800 OUTSTR("XMIN="),XMIN+REALSCAN(<ST>+INCHL),ERF; OUTSTR(RF);
03900 OUTSTR("XMAX="),XMAX+REALSCAN(<ST>+INCHL),ERF; OUTSTR(RF);
04000 OUTSTR("YMIN="),YMIN+REALSCAN(<ST>+INCHL),ERF; OUTSTR(RF);
04100 OUTSTR("YMAX="),YMAX+REALSCAN(<ST>+INCHL),ERF; OUTSTR(RF);
04200 X<XMIN+XMAX>+YMAX-XMIN>/10;
```

Table 4-4. (Continued)

```

04300 Y+YMIN YA+(YMAX-YMIN)/10;
04400 YEND=YMIN+YA*0
04500 T=0;Z=1;D=0;
04600 OUTSTR("Z=");Z=REALSCAN(ST+INCHWL);ERK); OUTSTR(PF);
04700 E+Z;J=1;I=1;
04800 OUTSTR("Y=");Y=REALSCAN(ST+INCHWL);EPK); OUTSTR(PF);
04900 EXIT +0;FORER +0
04950 BEGIN
05000 PROCEDURE FIZ;
05100 BEGIN
05200 A+(Y+1);B+(Y-1);
05300 C+(Y+K);D+(Y-K);
05400 AA=(A+1)+E;CC=(Y+Y)+2;
05500 BB=(A-1)+2;DD=(Y-K)+2;
05600 F=(E+DD+AA)*(5);G=(E+CC+AA)*(5);
05700 H=(E+DD+BB)*(5);N=(E+CC+BB)*(5);
05800 P=(A/(E+AA))*(B/F+C/G);
05900 R=(B/(E+BB))*(D/H+C/N);
06000 L=(C/(E+CC))*(D/H+A/G);
06100 M=(D/(E+DD))*(C/B/H+A/F);
06200 BZ=(P+R+L+M)+A+YA;
06300 END;
06400
06500 PROCEDURE FLUXCUP;
06600 BEGIN
06700 SETFORMAT(13;3);
06800 WHILE Y GEQ YMIN AND Y LEQ (YEND-(9999)+YA) DO
06900 BEGIN
07000 WHILE X GEQ XMIN AND X LEQ (XMAX-(9999)+XA) DO
07100 BEGIN
07200 BIZ; T=T+BZ;V=X+XA
07300 VCS;T=X+XMIN;Y=Y+YA;S=S+1;T+0
07400 END;
07500 WHILE J LEQ (S-10) DO
07600 BEGIN
07700 WHILE (J+10)>I DO
07800 BEGIN
07900 D=D+V(I);I+I+1
08000 END;
08100 OUTSTR(CVEC(I))
08200 D=0;J+J+1; IF (I MOD 5) = 0 THEN OUTSTR(PF);I+J
08300 END;
08400 END;
08500 FLUXCUP;
08550 END;END;
08600 END "LOOPS"

```

PULL LOOPS _AV

DO YOU WANT NOTES (TYPE IN EITHER YES OR NO FOLLOWED BY CAR PET) YES

THE PURPOSE OF THIS PROGRAM IS TO CALCULATE THE FREE SPACE RELATIVE COUPLING BETWEEN TWO FLAT BUT NON-COPLANAR RECTANGULAR LOOPS OF WIRE (THE SIDES OF WHICH ARE PARALLEL TO THE COORDINATE AXES OF REFERENCE) IT IS TO BE APPLIED IN AUTOMOTIVE VEHICLE LOCATION HENCE THE TEND OF THE FOLLOWING INTRODUCTION. THE LANE WIDTH IS THE X DIMENSION OF THE LANE LENGTH IS THE Y DIMENSION THE VERTICAL DISTANCE BETWEEN LOOPS IS THE Z DIMENSION. THE CENTER OF THE BURIED LOOP IS AT COORDINATES 0,0,0 THE WIDTH OF THE BURIED LOOP IS THE LANE WIDTH K IS THE ASPECT RATIO OF THE BURIED LOOP (WIDTH DIVIDED BY LENGTH) XMIN,XMAX,YMIN,MYN DETERMINE THE SIDES AND LOCATION OF THE PICKUP LOOP ALL INPUT DIMENSIONS ARE TO BE NORMALIZED TO HALF THE LANE WIDTH HOW MANY STEPS REFERS TO MOVING THE PICKUP LOOP ALONG THE LANE LENGTH (GENERALLY FROM ABOVE THE BURIED LOOP) BY 1/10 OF THE PICKUP LOOP LENGTH AND THEN CALCULATING ITS NORMALIZED Z DIRECTION COUPLING FROM THE BURIED LOOP THE PRINTOUT IS THE CALCULATED FLUX IN RELATIVE FLUX UNITS AND OF SUCCESSIVE STEPPINGS TO FIND THE ACTUAL FLUX IN VOLT SECONDS (MULTIPLY THE DATA BY THE FOLLOWING FACTOR (1)*((LANE WIDTH/2)^2)*((10*(K-7))) WHERE 1 IS THE BURIED LOOP CURRENT IN AMPS WHERE THE LANE WIDTH IS IN METERS HOW MANY STEPS 100

```

YMIN=-1
XMAX=1 000
YMIN=-0001 00
XMAX=1
Z=0
K=1

```

.34392	.10009	10299	10299	.10299
10299	10299	10299	10299	10299
.10299	-.53091	-.30191	-.19391	-.13591
-.10091	-.770	-.607	-.489	-.401
-.334	-.281	-.227	-.185	-.178
-.155	-.136	-.120	-.107	-.9509-1
-.2519-1	-.7659-1	-.919-1	-.8269-1	-.5699-1
-.3199-1	-.4739-1	-.4359-1	-.4009-1	-.3699-1
-.2419-1	-.3159-1	-.2929-1	-.2729-1	-.2529-1
-.2099-1	-.2209-1	-.2069-1	-.1939-1	-.1819-1
-.1709-1	-.1609-1	-.1519-1	-.1429-1	-.1349-1
-.1279-1	-.1209-1	-.1149-1	-.1099-1	-.1029-1
-.7909-2	-.6409-2	-.5779-2	-.5359-2	-.4969-2
-.7599-2	-.7249-2	-.6929-2	-.6619-2	-.6329-2
-.6059-2	-.5799-2	-.5559-2	-.5329-2	-.5119-2
-.4909-2	-.4719-2	-.4529-2	-.4359-2	-.4199-2
-.4039-2	-.3889-2	-.3749-2	-.3609-2	-.3479-2
-.3359-2	-.3239-2	-.3129-2	-.3019-2	-.2919-2
-.2829-2	-.2729-2	-.2639-2	-.2559-2	-.2479-2
-.2399-2	-.2309-2	-.2249-2	-.2179-2	-.2119-2
-.2059-2	END OF CHIL EXECUTION			

Table 4-5. CARCUP Program for Mutual Inductance of XMTR/RCVR Loops, and Sample Run

```

TYPE CARCUP SAI
09100 BEGIN "CARCUP"
09200 INTERHAL INTEGER EXIT ;FORER.;
09300 INTEGER I,J;Z;S;ERK1
09400 DEFINE AF=1/5E/12"
09500 REAL Y,YMIN;XTRAX;Y;YMIN;YTHA;YEND;A;YA;A;B;C;D;E;AA;BB;CC;D;
D;F;
09600 G;H;K;L;M;N;O;P;R;T;BC;JES;ND;XMIN;XMAX;YMIN;YRMAX;ZT;ZP;
09700 REAL XMIN;YMIN;XMAX;
09800 STRING ST;
09900 OUTSTR("DO YOU WANT NOTES (TYPE IN EITHER YES OR NO THEN CHR PET
")");
10100 IF INHAL="YES" THEN OUTSTR("TO FIND THE ACTUAL OUTPUT VOLTS, M
MULTIPLY THE DATA BY THE FOLLOWING
01103 -(NT+H*LN(S)*((10*(K-7)))+(LANE WIDTH/2)^2)+2*(U+2)+(IP+2)*SI
N(UT)");R
10200 WHERE
10300 NT = NUMBER OF TURNS ON THE TRANSMITTER LOOP
10400 NBL = NUMBER OF TURNS ON THE BURIED LOOP
10500 NP = NUMBER OF TURNS ON THE RECEIVER LOOP
10600 LANE WIDTH IS IN METERS
10700 W = 2*PI*F
10800 F = TRANSMITTER FREQUENCY (HERTZ)
10900 IP = THE PEAK TRANSMITTER CURRENT
10200 SIN(WT) = HOW MUCH WANT
10100 R = THE PER TURN RESISTANCE OF THE BURIED LOOP
10200 / = DIVIDE, * = MULTIPLY, † = TO THE POWER OF
"RAF");
02400 OUTSTR("HOW MANY STEPS ");
02500 O=10+(REALSCAN(ST+INCHWL);EPK)); OUTSTR(PF);
BEGIN
02600 FEEL ARFA/VE1 Q;PEHL ARPH;WCI Q(0-9)J
02800
02900 OUTSTR("XMIN=");XMIN=REALSCAN(ST+INCHWL);EPK); OUTSTR(PF);
03000 OUTSTR("XMAX=");XMAX=REALSCAN(ST+INCHWL);EPK); OUTSTR(PF);
03100 OUTSTR("YMIN=");YMIN=REALSCAN(ST+INCHWL);EPK); OUTSTR(PF);
03200 OUTSTR("YMAX=");YMAX=REALSCAN(ST+INCHWL);EPK); OUTSTR(PF);
03300 OUTSTR("Z=");Z=REALSCAN(ST+INCHWL);EPK); OUTSTR(PF);
03400 OUTSTR("YMIN=");YMIN=REALSCAN(ST+INCHWL);EPK); OUTSTR(PF);
03500 OUTSTR("YMAX=");YMAX=REALSCAN(ST+INCHWL);EPK); OUTSTR(PF);
03600 OUTSTR("YMIN=");YMIN=REALSCAN(ST+INCHWL);EPK); OUTSTR(PF);
03700 OUTSTR("YMAX=");YMAX=REALSCAN(ST+INCHWL);EPK); OUTSTR(PF);
03800 OUTSTR("ZP=");ZP=REALSCAN(ST+INCHWL);EPK); OUTSTR(PF);
03900 OUTSTR("K=");K=REALSCAN(ST+INCHWL);EPK); OUTSTR(PF);
04000 EXIT +0;FORER +0;
04100 BEGIN
04200 PROCEDURE FIZ;
04300 BEGIN
04400 A+(Y+1);B+(Y-1);
04500 C+(Y+K);D+(Y-K);
04600 AA=(A+1)+E;CC=(Y+Y)+2;
04700 BB=(A-1)+2;DD=(Y-K)+2;
04800 F=(E+DD+AA)*(5);G=(E+CC+AA)*(5);
04900 H=(E+DD+BB)*(5);N=(E+CC+BB)*(5);
05000 P=(A/(E+AA))*(B/F+C/G);
05100 R=(B/(E+BB))*(D/H+C/N);
05200 L=(C/(E+CC))*(D/H+A/G);
05300 M=(D/(E+DD))*(C/B/H+A/F);
05400 BZ=(P+R+L+M)+A+YA;
05500 END;
05600
05700 PROCEDURE FLUXCUP;
05800 BEGIN
05900 WHILE Y GEQ YMIN AND Y LEQ (YEND-(9999)+YA) DO
06000 BEGIN
06100 WHILE X GEQ XMIN AND X LEQ (XMAX-(9999)+XA) DO
06200 BEGIN
06300 BIZ; T=T+BZ;V=X+XA
06400 VCS;T=X+XMIN;Y=Y+YA;S=S+1;T+0
06500 END;
06600 WHILE J LEQ (S-10) DO
06700 BEGIN
06800 WHILE (J+10)>I DO
06900 BEGIN
07000 D=D+V(I);I+I+1
07100 END;
07200 UC I=10;WCI=10;D;
07300 D=0;J+J+1;I+J;
07400
07500 END;
07600 END;
07700 Z+1;WHILE Z LEQ (0-9) DO
07800 BEGIN
07900 UCZ;I+1;
08000 Z+Z+1
08100 END;
08200 T+0;S-1;D=0
08300 A+YMIN;YA=C*(XMAX-YMIN)/10;YTHA=(A+(YMAX-YMIN))/10;
08400 YEND=YTHA+YA+C*(YMIN-YTHA);XMIN=XTHA;XMAX=XTHA;
08500 E=Z+2;J+1;I+1;
08600 FLUXCUP;
08700 T+0;S+1;D=0;
08800 X=XMIN;AA=(XMAX-YMIN)/10;YRMIN=YEND-YRMIN+YA+0;
08900 YA=YRMIN-YMIN/10;YMIN=YMIN-YMIN+YMIN;XMAX=XRMAX;
09000 E+Z+2;J+1;I+1;
09100 FLUXCUP;
09200 SETFORMAT(13;3);I+1;
09300 WHILE I LEQ (0-9) DO
09400 BEGIN
09500 OUTSTR(CVEC(I))
09600 IF (I MOD 5)=0 THEN OUTSTR(PF);
09700 I+I+1
09800 END;
10000 END;END;
10100 END "CARCUP"

```

Table 4-5. (Continued)

```
.RUN CARCUP.SAV
DO YOU WANT NOTES (TYPE IN EITHER YES OR NO THEN CAR PET) YES
TO FIND THE ACTUAL OUTPUT VOLTS, MULTIPLY THE DATA BY THE FOLLOWING
-(NT*NL*NR*(((10+(-7))*(LANE WIDTH/2)+2)+2)*CW+2)*(IF+2)*$IN(WT) R
WHERE
NT = NUMBER OF TURNS ON THE TRANSMITTER LOOP
NL = NUMBER OF TURNS ON THE BURIED LOOP
NR = NUMBER OF TURNS ON THE RECEIVER LOOP
LANE WIDTH IS IN METERS
U = 24914F
F = TRANSMITTER FREQUENCY (HERTZ)
IP = THE PEAK TRANSMITTER CURRENT
SIN(WT) = YOU KNOW WHAT
R = THE PER TURN RESISTANCE OF THE BURIED LOOP
/ = DIVIDE, * = MULTIPLY, + = TO THE POWER OF

HOW MANY STEPS 30
XMIN=-.45
XMAX=.55
YMIN=-.05
YMAX=.05
ZT=.1
XRMIN=-.55
XRMAX=-.45
YRMIN=-.05
YRMAX=.05
ZR=.1
K= 4
1199-1      1199-1      1209-1      -1209-1      1209-1
1219-1      1229-1      1239-1      -1239-1      1249-1
1289-1      1309-1      1329-1      -1349-1      1379-1
-1409-1     1439-1      1479-1      -1509-1      -1549-1
-1599-1     -1639-1     1699-1      -1729-1      -1779-1
1819-1     1859-1     1889-1      -1919-1      -1919-1
1899-1 END OF SAIL EXECUTION
```

what is its size and how high above the buried loop (in terms of XRMIN, XRMAX, YRMIN, YRMAX, ZR), (4) to specify the aspect ratio of the buried loop, K.

The CARCUP program calculates and prints out the mutual inductance for the number of data points specified. Each successive data point represents the mutual inductance of the XMTR/RCVR through the buried loop by moving along the positive Y-direction (along the roadway lane) by 1/10 of the XMTR length. The results are in units of relative mutual inductance and to get real answers, answer "yes" when the program asks if you want more detailed information.

2. Method of computing. The inputs to the program (XMAX, YMIN, etc.) describe the area swept out by the motion of the pickup loop(s). The program calculates the mutual inductance between the entire buried loop and portions of the swept-out area using elements of area 1/10 the pickup loop width by 1/10 the pickup loop length.

$$\Delta X = (XMAX - XMIN) / 10$$

$$\Delta Y = (YMAX - YMIN) / 10$$

The swept-out area is divided into portions having dimensions ΔY by $(XMAX - XMIN)$. There are $(10 + \text{"how many steps"})$ portions. The mutual inductances are calculated and stored for those portions.

Summing the values of 10 successive portions yields the mutual inductance of the buried loop to one particular position of the pickup loop.

The CARCUP program sums the corresponding 10 successive portions of both XMTR and RCVR and multiplies them together to get the overall mutual inductances. There are two main subroutine procedures used to calculate the mutual inductances, BIZ and FLUXCUP. With respect to the

BIZ subroutine, the flux density is calculated for that corner of the area XA by YA which is closest to the point (XMIN, YMIN). With respect to the FLUXCUP subroutine, FLUXCUP in the LOOPS program differs from FLUXCUP in the CARCUP program, the difference being in form only for the purpose of minimizing data handling.

D. Optimum Relative Configuration of Three-Loop AVM System

1. Buried loop interaction with adjacent coplanar loops. The results seem to favor loops having aspect ratios of ≥ 1 . However, the practical aspect of packing the buried loops as densely as possible is a primary consideration. At any rate, if K is greater than 0.025, a center-to-center spacing of the buried loops of greater than $4 \times K$ (i. e., 2 times the loop width along the lane) results in a coupling of less than 5% of the same loops superimposed.

2. XMTR and RCVR direct coupling. If it is presumed that the XMTR and RCVR loops "ought to be the same," then the results seem to favor loops having aspect ratios ≥ 1 . That is, the loops should be rectangular and have their "small ends" pointed toward one another. The XMTR and RCVR on the vehicle are small compared to the buried loop. The choice of their aspect ratios has a limit to avoid extending beyond the buried loop.

At any height, sensors having more turns on smaller loops are as effective as ones with large loops having fewer turns. At any height the coupling varies with later position, being highest near 0.8 from center to end of the buried loop. The variation between these limits is about 10%.

If a sensor loop is placed lower than the optimum height, it results in overcoupling and relatively high noise signal, thus also reducing buried loop packing density. This is most pronounced for buried loop aspect ratios much greater than pickup loop size. XMTR and RCVR coils of differing shapes will function and may permit three-loop systems whereby the smallest moving coil may be made the optimal for signal to "noise" ratio.

3. Expected real-life signal levels. The following configurations and conditions are assumed: (1) Roadway with lane width $2l = 3$ meters, (2) buried loops with aspect ratio $K = 0.1$ and separated by $4 \times k \times l$, (3) pickup loops (XMTR and RCVR) having sides $P = 0.1l$, height $Z = 0.1l$, and separated by l . (4) All loops have 10 turns each of #27 wire and resistivity of 1.36 ohm/meter. (5) The transmitter is producing 100 kHz at 1 amp peak. (6) Self-inductance of buried loop 495 microhenrys. (7) Mutual inductance of two buried loops 20.25 microhenrys. (8) XMTR/RCVR self-inductance 7.87 microhenrys each. (9) Direct mutual inductance of XMTR and RCVR 0.0045 microhenry. (10) Three-loop system maximum mutual inductance 1.24 microhenrys. (11) Voltage signals produced by XMTR/RCVR direct coupling 2.8 mV cos wt. (12) Voltage signals produced by three-loop system -0.78 mV sin wt.

4. Comments. The direct coupling of the transmitter and receiver produces a voltage at the receiver of constant peak amplitude, having the transmitter frequency and shifted in phase by

+90 degrees. The three-loop system response envelope is a function of the vehicle speed. The output frequency is shifted 180 degrees with respect to the input current frequency.

REFERENCE

1. Zottarelli, L. J., "Burried Loops," JPL Interoffice Memo addressed to G. R. Hansen, 1974.