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FINAL REPORT TO
NASA JOHNSON SPACE CENTER
CONTRACT NAS9-15171

ANALYTICAL AND
COMPUTATIONAL
MATHEMATICS, INC.
FINAL REPORT TO NASA JOHNSON SPACE CENTER

CONTRACT NAS9-15171

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1.0 INTRODUCTION

The work done by ACM under Contract NAS9-15171 covered a wide variety of tasks. The categories of work included:

- Development of new mathematical and algorithmical techniques for solution of problems in satellite dynamics.
- Development of new solutions to satellite orbit motion.
- Dynamical analysis of Shuttle on-orbit operations.
- Development and analysis of computer software routines for use in Shuttle mission planning.
- Formulation of mathematical models of atmospheric density.

Due to the variety of the tasks and the several modifications to the contract, a separate report has been written for each task. These reports are listed in the references. The purpose of this Final Report is to describe the objectives and scope of each task, and to give a summary of the significant results of each task. Therefore, this report will serve as an overview and summary of the work done under Contract NAS9-15171. In case more detailed information is required, please refer to the individual reports. Copies of each report are available from the Technical Monitors or the JSC Technical Library.
2.0 ANALYTICAL SOLUTION OF ARTIFICIAL SATELLITE MOTION WITH DRAG

Orbit computation methods can usually be classified as:

Numerical - The calculations are carried out in a step-by-step manner. High precision is possible but computer runtime can be excessive.

Analytical - The calculations are carried out in one step, regardless of the prediction interval. Therefore, these methods have extremely fast computation times.

The fast execution times of analytical satellites theories make them very attractive as mission analysis and planning tools. But difficult problems existed in the analytical methods:

1) The solutions were expressed by extremely complex formulas which required much more computer storage than the numerical methods.

2) The accuracy of the analytical methods was restricted by the simplicity of the model or the solution technique.

3) Unlike numerical methods, the analytical theories were generally difficult to extend. For instance, numerical methods may use a geopotential model of arbitrary order or degree, whereas the analytical methods were limited to a fixed order and degree. The numerical methods can easily include new or more accurate density models but this was impossible in analytical methods.

4) Analytical theories suffered because the different perturbations had never been unified under one non-singular formulation.

These problems were the motivation behind developing a new satellite theory. The resulting theory provides a concise and efficient algorithm which has been implemented into
a working, modular computer software tool. The development of the theory and corresponding software are described in the following sections.

2.1 Perturbations due to Atmospheric Drag

The objective of this task was to arrive at a fully analytical theory for the motion of an artificial satellite perturbed by the $J_2$ term of the zonal geopotential expansion and by a drag force which is tangential to the orbit and proportional to the square of the velocity magnitude. The task was executed in two stages:

1) Development of the drag differential equations in a regular set of two body elements and in a form suitable for solution by quadrature (reference 1).

2) Development of a realistic density model suitable for application in the theory developed in stage 1 (reference 7).

The second stage is discussed in more detail in Section 4.2 of this report and so this section will restrict its discussion to the first stage.

The drag theory was built on top of the previously developed $J_2$ theory in the PSG elements. Since the density effects only the magnitude, not the direction, of the drag force, the transformation of the drag forces may be carried through without specifying the density function. A canonical treatment of this transformation of the drag effects results in a tractable set of differential equations. To allow the analytical solution of these equations, an expansion is made in powers of the eccentricity. To avoid errors, these expansions were created in an automatic manner by a minicomputer program specially designed for this task. The result is a theory of relatively concise form, programmed in FORTRAN and executable in the interactive mode on the UNIVAC 1110.

Numerical studies were performed comparing the analytical
solution to a precision numerical solution. In the first step, both analytical and numerical solutions assumed the density to be a constant. The results showed the analytical constant density solution to be accurate to within 1% of the numerical solution for Shuttle type orbits. In the second step, the analytical theory with the realistic density model was compared to numerical solutions obtained by using extremely accurate and complex drag models. Even in these rigorous tests, the analytical solution showed errors of no more than 2%.

2.2 Perturbations due to an Arbitrary Number of Zonal Terms

It was the purpose of this task to derive a "complete" first order solution to the motion of a satellite about a rotationally symmetric earth. No restriction was made on the order of the geopotential expansion, and the solution was developed entirely in non singular elements. Recursive expressions are used so that a concise formulation is maintained.

The method of solution was to apply the Von Zeipel algorithm to a recursive formulation of the zonal geopotential. This is done by defining the zonal potential in the canonical and regular PS\( \Phi \) elements. Considerable simplications can be realized with this choice of elements. By including the true anomaly as an canonical element, the hamiltonian for a finite number of zonal harmonics becomes a finite fourier expansion in the canonical elements. Also, the second order integration of the mean motion is not necessary because the new formulation uses a mean motion related to the total energy. The detailed development of this theory is given in reference 2.

The result is a simple formulation which has been implemented in FORTRAN and executable on the UNIVAC 1110.

Numerical studies were conducted to determine the accuracy of the solution. In the studies, the analytical solution was compared to a precision numerical solution. Both numerical
and analytical solutions modeled the 18th order geopotential expansion. For Shuttle-type orbits, the differences between analytical and numerical solutions were on the order of a few meters after 500 revolutions.

2.3 An Analytical Satellite Orbit Prediction Program (ASOP)

The analytical formulations that are discussed in Sections 2.1, 2.2 and 4.2 of this report as well as certain formulations that were developed under a previous contract, are being converted into an operational computer program. This program represents a new state-of-the-art for orbit prediction computer software. ASOP is able to compute near-earth orbits to within an accuracy of a few meters. Recursive equations are used instead of complicated formulas so that the execution time of ASOP is on the order of a few milliseconds. At present these calculations only include the perturbations due to $J_2$. However, the perturbations due to atmospheric drag and all the Earth's geopotential terms are currently being incorporated into the existing ASOP program.

The current version of ASOP is now available to the general user of the UNIVAC 1110-EXEC 8 system at NASA/JSC Houston in two forms:

1. A stand-alone program that can be used interactively to obtain immediate results for a specific problem.
2. A user-subroutine package that can be incorporated into other software systems.

Both versions were designed to be small and execute quickly.

ASOP has been extensively documented (reference 3). Any additions to the program will be documented as revisions to reference 3.
Often in orbit determination or navigation algorithms one must predict how small deviations from some nominal orbit will in time cause the actual orbital path to deviate from the nominal path. If the initial deviation is small, then a linear approximation may be used to determine the deviation at any given time. The linear approximation, a truncated Taylor series expansion, requires the first partial derivatives of the coordinates defining the position and velocity at a given time, with respect to the coordinates defining the position and velocity at the initial time. This matrix of partial derivatives is commonly called the state transition matrix \( \Phi \).

\( \Phi \) may be determined by numerical integration. But when one considers the fact that the transition matrix is usually used in some iterative manner, the computational costs required by the numerical integration of the matrix differential equation becomes prohibitive.

The alternative, of course, is to determine the transition matrix by some analytical technique. Several analytical methods have determined expressions for the transition matrix under the assumption that the satellite moves along a two-body orbit, all perturbations being neglected. But this assumption may result in non-negligible errors if the perturbations are large.

For artificial satellites orbiting near the earth, the \( J_2 \) oblateness potential contributes a strong perturbation which may not be neglected for accurate satellite orbit prediction. Significant advantages are offered by a \( J_2 \) satellite theory developed from a new set of canonical elements proposed by Scheifele. The elements are in an extended phase.
space in that eight (instead of six) variables describe the state. They also have as their independent variable, a quantity related to the true anomaly instead of time. The set is similar to the Poincare elements and are therefore named the Poincare-Similar (PS) elements. The PS elements are non-singular for bounded orbits.

Because of the simplicity and accuracy of the canonical analytical solution based on PS elements, it becomes a logical choice on which to base a new analytical state transition matrix. Therefore the intention of this task was to derive a completely analytical singularity free form of the state transition matrix for orbits perturbed by an oblate spheroid.

The result is a concise, accurate and algorithmically simple state transition matrix and its inverse which includes the short period and secular effects of the zonal harmonic. The algorithm has been implemented in a working program executable in interactive mode on the UNIVAC 1110. From numerical studies it was found that the improvement over the conic matrix ranges from 2 to 4 digits better accuracy. Complete documentation on the work of this task is given in reference 4.
For accurate orbit computations for satellites perturbed by atmospheric drag, a rather complex density model must be employed. The Jacchia density model includes several variations of the atmosphere character which are related directly or indirectly to the density. In the most recent Jacchia model, the exospheric temperature $T_{\infty}$, is modeled by variations due to:

1. Averaged and daily variations in the solar flux ($F_{10.7}$).
2. Averaged and 3 hourly variations in the geomagnetic index ($a_p$).
3. Variations of the angle between satellite and atmospheric bulge (diurnal effect).

The exospheric temperature is then related to the density by the solution of the diffuse equilibrium equation for the different constituents of the atmosphere and the desired altitude. Other variations are then computed directly as changes in the density; they include:

1. Changes due to semi annual effect.
2. Changes due to seasonal-latitudinal effect.

The causes for these variations are not exactly known but may be modeled by fitting empirical data.

Although the model is quite accurate, it requires a great deal of computation time and storage. The inefficiency of the model cannot be reconciled by simply neglecting some of the effects and other models such as the 1962 standard are grossly inaccurate for altitudes above 90km. In addition, the complexity of the Jacchia model renders it useless for analytical satellite theory applications.

The goal of this task was therefore to develop new density models which are efficient for applications in numerical methods or which may be applied in satellite theories. The manner in
which these goals were met are described in detail in references 5, 6 and 7. A brief overview is given in the following sections.

4.1 Application to Numerical Orbit Computation Methods

In an effort to avert the computational costs, two density models have been independently developed to simulate the Jacchia model without the costs of an inefficient algorithm. The first model, referred to as Babb-Mueller (B-M), has been developed in Mueller (reference 5) and numerical studies showed it to be an efficient yet accurate model. The B-M model assumes the density can be modeled by rather simple expressions but the parameters of the model are unknown. These expressions can be easily inverted i.e. given the density at a few points the parameters can be determined. Thus the B-M model can be "calibrated" to fit the Jacchia model, by evaluating the Jacchia model at a few specific points. The model parameters found by calibration are implicit functions of the slowly varying characters of the atmosphere and can be considered constants over a limited period of about a month.

The second model, named Jacchia-Lineberry (J-L), is of a similar nature as the B-M model. It also assumes rather simple expressions for the density whose parameters have been determined by a least square fit with the Jacchia model. Unlike the B-M model, the J-L model's parameters are indeed constants and thus no maintenance is required to update the parameters. But the J-L model does have an overhead in that a considerable number of parameters are required for the complete model. In any case, both models show large computer cost savings over the complex Jacchia model.

In this task the algorithm for the B-M model was documented in reference 6. Also in that reference, the complete development of the J-L model was given. Several versions of the J-L
model were developed and implemented in a computer package on the UNIVAC 1110. A user's guide is given in reference 6, including software documentation. In addition, numerical studies showed the J-L model to be very accurate for altitudes below 500km. Run times showed the J-L model to be 3 to 9 times faster than the Jacchia model depending on which version was used.

4.2 Application to Analytical Satellite Theories

In the past, the computation of the drag perturbations by analytical methods has not been feasible because of their inability to model the "real world" density.

In developing a density model for the analytical theory, one is severely restricted by the fact that the model must be in the form of a fourier series in the true longitude. As is the case in most analytical theories, the perturbation must be written in a fourier series to facilitate the solution of the differential equations of motion. Usually, the solution is obtained by quadrature.

Several density models have been developed to predict accurately the density at any point in space and time. Examples are the Jacchia model and the USSR model. But both models are extremely complicated and too unwieldly for analytical satellite theories. In the analytical theory of Brouwer and Hori, the density was assumed to be an exponential function of the position radius of the satellite. The exponential must then be expanded in a Poisson series so the quadrature can be performed. This model has several difficulties. It first has a problem with convergence, which Brouwer points out. Secondly, it is simply a poor model for describing the dynamic atmosphere. The density is extremely effected by such factors as the level of solar activity and whether it is summer or winter, day or night. Thus the model in Brouwer, Hori theory is simply inadequate.
Recently an extremely simple density model (referred to here as B-M) has been developed to match the Jacchia model to a high degree of accuracy (reference 5). The variations in the density due to changes in the height and changes in the relationship of the vehicle and sun position (diurnal effect) are included explicitly. Long period variations such as the changes in the average solar activity and semi-annual variations are included implicitly in the coefficients of the model. The value of the coefficients are determined by a procedure called "calibration". The simple formulation allows the model to be inverted, i.e. given the density at different points in space (as determined from Jacchia) one can compute the coefficients of the B-M model. Since the coefficients are implicit functions of long period effects, they can be considered constants over a limited period of about a month.

Even this extremely simple model cannot be applied in the analytical drag theory because it cannot be written in the form of a fourier series. However the technique of the B-M model does give important insight and direction to follow.

In all the models discussed, the representations of the density are considered to be global. In other words, given any position in the atmosphere one can determine its density. The approach taken in this task was to develop a model which expresses the density along a particular orbit. The coefficients in the model are calibrated with the Jacchia model in a manner similar to the B-M model. But in this case, the coefficients in the model are not only implicit functions of the long period variations in the atmosphere but also the orbital elements which describe the orbit. The result is a density model which can be written in a fourier series and easily implemented into the drag theory. Since the orbital elements are perturbed by \( J_2 \) and drag, the coefficients in the model must be updated periodically or corrected in some manner to
reflect the changes. Since the perturbations are small, the updating would be infrequent. Details of the development can be found in reference 7.

The new density model has several distinct advantages. It has a rather subtle yet extremely important advantage in that the model is a power expansion in \( \zeta_1 \); i.e., the basic expansion used in Scheifele's development of the differential equations.

Another advantage of the new density model is its ability to simulate any density model. In this task the Jacchia model was chosen for the simulations, but any other model could have been used. If more accurate density models are developed, they may also be chosen for simulation and thus the analytical drag theory can reflect the accuracy of the newly developed models.

Finally, it is concluded that the analytical satellite theory need not be limited by a simplified drag model. With the approaches developed in this report, it is feasible to make the accuracy of the analytical theory competitive with precision numerical methods, while retaining a concise formulation and quickness of execution.
5.0 ORBITAL MOTION OF THE SOLAR POWER SATELLITE

It has been proposed to put a series of large satellites into geosynchronous orbit for the purpose of collecting solar energy and redirecting it toward the earth via microwave radiation. Preliminary studies are being carried out at JSC on the feasibility of these Solar Power Satellites (SPS).

The large area of the collecting surface (approximately 144 square kilometers) means that solar radiation pressure will cause significant perturbations on the SPS orbit. In fact solar pressure will be as important as gravitational perturbations. The purpose of this task was to determine the effects of solar radiation pressure on the SPS orbit. It was shown that the eccentricity of the orbit can get rather large (.08) even when it is initially zero. This is the primary difference between the SPS orbit and other geosynchronous satellite orbits.

The SPS configuration being considered here is described in a study report by the Johnson Space Center. However, the results in this study are applicable to any geosynchronous satellite that resembles a flat surface that continually faces the sun. The main purpose of this study was to investigate the orbital evolution of the SPS over its expected thirty year lifetime. An additional goal was to describe the motion with analytical formulas. These formulas could then be used as a basis for developing an orbit control theory that will minimize station keeping costs.

The perturbing forces acting on the satellite were studied in detail. To a first approximation, three types of forces can be considered separately since they have different effects on the orbit.

1. Longitude dependent tesseral terms in the earth's geopotential cause a slow drift of the satellite's mean longitude.
(2) Sun and moon gravity cause a rotation of the orbital plane.

(3) Solar radiation pressure will cause an increase in the orbital eccentricity.

The following is a summary of the main results of the study. The detailed reports are given in references 8 and 9.

(1) An analytical solution was developed, giving the motion of orbital eccentricity and line of apsides as a function of time. This solution has a concise formulation and is accurate to within a few percent.

(2) It was shown that the eccentricity of the sun's orbit about the earth causes a linear increase in the eccentricity of the SPS orbit.

(3) The eccentricity and inclination of the SPS orbit can be controlled by choosing certain nonzero values of eccentricity and inclination.

(4) Graphical data on the orbital elements was put into appropriate form for use in mission planning or feasibility studies.

(5) Explicit equations were developed for the daily motion in longitude and latitude. It was shown that, for small eccentricities and inclinations, the ground track will be an ellipse centered on the equator and mean longitude.
6.0 A REFINED NUMERICAL METHOD FOR CALCULATIONS OF SATELLITE ORBITS

Solutions to ordinary differential equations are usually obtained through the application of either analytical or numerical solution methods. Each approach has its own set of advantages and disadvantages. A particular method is usually chosen according to how it may satisfy foreseen applications.

Analytical methods require extensive development of mathematical formulas. Once they have been obtained, the formulas can be used to study certain global properties of the solution. Also, the analytical formulas can be used in computing machines to provide extremely rapid numerical calculations.

There is relatively little apriori mathematical development of numerical methods. They allow extremely accurate numerical calculations of the solution and are usually not difficult to program on the computer. However, the solution must be developed step-by-step, which can take large amounts of computer time. Also, very little qualitative or global information on the solution is available.

For some applications, it may be advantageous to develop new specialized methods that combine features of both the analytical and the numerical methods. This is the suggested approach for those applications that require repetitive solutions of the differential equations, but for which no analytical solutions are available. Therefore, the advantage in speed of an analytical solution might be partially realized by using a limited application of an analytical method. Numerical step-by-step calculations still need to be done, but usually in a more efficient manner.

This task concerns a new approach for the solution of artificial satellite trajectory problems. The basic idea is to apply an analytical solution method (the Method of Averages)
to an appropriate formulation of the orbital mechanics equations of motion (the KS-element differential equations). The result is a set of transformed equations of motion that are more amenable to numerical solution.

An important problem that is found when attempting the numerical solution of the satellite differential equations, is that the maximum size of the numerical integration steps is limited by the high frequency (short period) tesseral terms contained in the geopotential. This problem appears even with the KS formulation. Even though their amplitudes are small and may be considered negligible for many applications, the short period terms cause the following practical problems:

(i) Since the tesseral terms depend on time, the orbital frequency based on the total energy is no longer constant. If small steps are not taken to "track" the high frequency oscillations, large down range errors can result.

(ii) If the tesseral terms were simply neglected in the numerical integration, larger steps could be taken but unacceptable intrack errors would result.

(iii) Evaluation of all tesseral terms in the numerical integration force model consumes a major part of the computation time.

An approach to solving the three above problems is developed in this task. Basically, the idea is to carry out a numerical integration without the tesseral terms. In order to avoid the second of the above problems, the KS elements are initialized with a mean frequency (total energy). The mean values are obtained via a specialized application of the Method of Averages. Since the force model contains only zonal geopotential terms plus, possibly, atmospheric drag and external bodies, computer run time and stability problems associated with the tesseral terms are avoided.

A Modified Method of Averages was developed and applied
to the KS differential equations. This theory was then used to develop an Averaging Initialization Algorithm. Tests show that this algorithm can decrease the computation time required for predicting near earth orbits. For prediction intervals of one or more days, the computation time will be reduced by a factor of three to four. The method is particularly suited to iterative applications where accurate in-orbit satellite position information is required.

Documentation of theoretical developments and numerical experiments is given in reference 10. The computer subroutine package for the initialization algorithm has been implemented in the KSFAST program and is documented in reference 13.
7.0 A COMPARATIVE STUDY OF THE UNIFIED SYSTEM FOR
ORBIT COMPUTATION AND THE FLIGHT DESIGN SYSTEM

The high flight rate anticipated for the Shuttle Trans-
portation System (STS) era beginning in the 1980's is caus-
ing a review of the mission design and analysis computer soft-
ware structures. The rather individual case-by-case planning
procedures and software products which were used for earlier
missions are no longer adequate when considering the projected
budgets for the STS operations. Standardized planning tools
are absolutely necessary in the environment of shuttle flight
design since many tasks are repetitive. Also, profit must be
taken from the experience gained with earlier missions and from
the advances made in the areas of flight design techniques
and computer hardware and software standards.

In this study, two recent software systems were described
and compared. One is the Flight Design System (FDS), cur-
rently being developed at MPAD of NASA/JSC†. The other
is the Unified System for Orbit Computation (USOC), cur-
rently operational at MAD of ESA/ESOC++. The complete
report on the results of this study is given in reference 11.

The FDS software consists of a set of functional and
utility processors, components of the data base structure and
the executive logic. It is designed as an efficient production
tool for flight design and analysis tasks, to be accomplished
for the support of operational shuttle missions and orbital
flight tests. It also includes an interface with a system for
automated generation of flight planning documents.

† Mission Planning and Analysis Division of NASA/Johnson
Space Center, Houston, Texas.

++ Mission Analysis Division of the European Space Agency/
European Space Operations Centre, Darmstadt, Germany.
USOC has been used for the planning, analysis, and design of spacecraft missions, both earth orbital and interplanetary. It makes use of an automated approach to the generation of problem-specific application programs from a library of functional modules. A module selector program interfaces with the user and selects the necessary modules for a particular application. The USOC design expressly facilitates quick modifications by the analyst.

The FDS is a production-oriented software product, mainly designed to satisfy flight design needs of the class of shuttle missions which are considered as standard missions or deviations of such. It is not intended to satisfy the total analysis needs of MPAD. One of the goals of this study was to evaluate the approach of USOC for the planning and design of unique shuttle flight phases.

The two software systems were compared on the basis of the following considerations:

- Scope of applications
- Software system structures
- Hardware/software requirements to host computer system
- Software flexibility
- System transportability
- Unique features of each system

Although there exists some overlapping of the scope of applications of USOC and FDS, the structures of these two systems are very different, according to their different basic requirements. Their requirements are in fact, incompatible. While the FDS is designed to meet the requirements of a standardized production tool, USOC is designed for rapid generation of particular application programs. The main emphasis of USOC is put on the adaptability to new types of missions.

A software system having a USOC-like structure, adapted
to the specific needs of MPAD, would be appropriate to support planning tasks in the area of unique STS missions. There appears to be a need for such an additional system within MPAD.
8.0 ANALYTICAL FORMULATION OF SELECTED ACTIVITIES OF THE REMOTE MANIPULATOR SYSTEM

The Remote Manipulator System (RMS) will be used by NASA for Shuttle on-orbit payload (P/L) deployment and retrieval. Large simulation software is being used by several organizations to support the development of the RMS. However, for certain analyses such as evaluation of optimum RMS maneuvers, interactions with attitude and orbit control of the shuttle, etc., much simpler and faster mathematical models are needed. In addition, analytical closed form solutions will allow an estimation of operational limits of the system. These limits are not easily detectable with the big simulation programs that require considerable computing time. Finally, the transparency and redundancy of a simplified mathematical model are further advantages to be expected.

The purpose of this task was to develop new methods of analysis for the Shuttle Orbiter based RMS. The methods are based on simplified kinematical models. The motions of the simplified mathematical model are described either by explicit analytical formulas or by concise numerical algorithms.

The purposes of the new methods are to:

- Provide insight into the coupled motion of the Orbiter - RMS - Payload system.
- Provide fast answers to typical problems in the design and analysis of Shuttle missions requiring the RMS.
- Provide qualitative and quantitative results on the motion to be used as a check on numerical simulation software.
- Isolate and analyze those RMS operations that are most critical from the point of view of mission success or RMS design limits.
- Investigate further extensions of the mathematical model in order to take account of arm flexibility, drive motor characteristics and RMS control laws.

The equations of motion for a general treatment of the coupled motion of Orbiter and P/L were derived. It was shown that P/L capture and P/L deployment are governed by the same equations. Also, all phases of coupled motion are described by the same general equation of motion.

In order to demonstrate the applicability and efficiency of the derived equations, some example problems are given. The corresponding equations were simplified to the extent of these special cases. Explicit analytical solutions are presented for the most interesting RMS phases of operation. These are the following:

- P/L capture,
- P/L stowage into cargo bay and its removal from the cargo bay,
- P/L deployment.

The analytical formulations were used to study problems in mission planning and on-orbit operations. Recommendations are given on maximum capture velocity of payloads, optimum capture philosophy, payload stowage and deployment techniques, and hardware modifications. A detailed report on the study is given in reference 12.
9.0 MAINTENANCE AND MODIFICATION
OF THE KSFAST PROGRAM

Since the initial release of the KSFAST program, a few minor problems have been detected, recommendations for improvements have been made and new theories for the KS elements have been developed and proven. Therefore, the KSFAST program has been modified to incorporate some of these improvements and to correct deficiencies.

There have been three basic areas of modification:

a) Changing some of the numerical constants to the more generally accepted values.

b) Changing the input/output units from Earth radii and minutes to Kilometers, seconds and days.

c) Incorporation of the mean element theory for approximating some of the Earth's geopotential terms.

The first two modifications were done to make the KSFAST program more acceptable by the using public. The third involved a considerable programming effort to implement, but resulted in significant savings in program execution time. (For a complete description of the mean element theory, see reference 10).

A revised version of the KSFAST program documentation (reference 13) has been published, including all recent modifications.
REFERENCES


