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Study of Rolling Element Dynamic Interactions
with Separators and Raceway Paths

Roller to Separator Contact Forces
and
Cage to Shaft Speed Ratios
in
Roller Bearings

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I. Abstract

Cage to roller force measurements, cage to shaft forces, and cage to shaft speed ratios are reported for 115 and 118mm bore roller bearings operating at speeds of 4,000, 8,000, and 12,000 rpm under loads ranging from 360 to 6670 N (80 to 1500 lb).
II Introduction

Current developments in jet engine technology are placing more stringent demands on gas turbine design. There is a constantly increasing requirement for engines to develop greater thrust outputs. In addition to this increased loading the need to raise the thrust/weight ratio of engines and to improve the fuel consumption has led to higher rotor speeds and operating temperatures, lighter components and correspondingly increased structural flexibility. In anticipation of tomorrow's requirements, further advanced knowledge of engine component technology must be obtained.(1)*

In the case of rolling contact bearings there is a need for a better understanding of cage and rolling element dynamics, particularly in ultra-high speed applications.(2,3,4,5)

Recently developed, advanced bearing theories have resulted in computerized optimization of rolling element bearing designs and in some cases accurate prediction of bearing performance. These developments and advances by no means substitute for testing of rolling element bearings which for many years was the basis for bearing development. To the contrary, the need for more refined data gathering methods has become obvious. Tests are needed to verify the theories which form the foundation of these computer programs. Also, performance tests and studies will always be needed to refine bearing designs for critical applications.

The interaction between the rolling elements of a bearing with the raceways and separators is particularly difficult to measure due

*Numbers in parentheses designate references at end of report.
to the rapidity of their motion. The kinematic behavior and the resulting forces acting on a rolling element/separatior/raceway assembly could in the past be measured only by tests where the operating conditions were drastically simplified.

III Separator Study Machine

An optical bearing test rig has been constructed to operate the bearing and make photographic records of the rolling elements and separator behavior. Figure 1a shows an overall view of the machine as it is presently installed in the Dynamics Laboratory of the Engineering Building at California State University, Northridge. The machine was originally assembled by Industrial Tectonics, Inc., Compton, Calif., and has been used in industrial bearing research, and in a ball motion study reported in (6), and in a ball to cage force study (7).

The bearing test rig is basically a shaft supported by a pair of preloaded ball bearings at one end and the test bearing at the other end. One face of the test bearing is exposed to allow free view of the rollers and the separator. Radial load is applied to the test bearing by a hydraulic actuator through a cable loop over the bearing housing. The shaft is driven by a 75 hp hydraulic motor through a geared belt drive, giving speeds infinitely variable from 100 to 15,000 rpm. Figure 1b is a schematic of the shaft assembly.

Lubricating oil for under race cooling and test bearing lubrication is supplied through a series of orifices from the rear of the test bearing.

Due to the high tangential velocities present when a bearing is rotated at shaft speeds up to 12,000 rpm, conventional photograph techniques are inadequate. The difficulty lies in obtaining photo-
graphs having sufficient resolution for analysis when very short exposures are required to freeze the motion of the bearing elements.

This problem has been overcome by eliminating the gross rotational motion using a derotation prism. The resulting image thus presents the differential motion between the separator and the rolling element, enabling observation and photographs to be made of an individual separator pocket.

Derotation is accomplished by synchronizing the rotation of a Pechan prism at half-speed with the rotation of the roller separator, thus causing the apparent image rotation and the true separator rotation to coincide. This results in the derotated image of the area of interest being imaged on the film plane of a camera. Light rays from the illuminated bearing are collected through the front window of the instrument. This window is optically coated to reject ultraviolet energy produced by ultraviolet lamps, serving the circuit for the prism speed control.

From the window, the rays travel through collimator lenses and the Pechan prism before they travel through the exit lenses. Their path is then deflected by mirrors which fold the image in different directions. Figure 1c shows light paths through the scanner.

One light trace travels to a beam splitter where approximately 15% of the light is reflected to the eyepiece optics to provide an image observable to the operator. The balance of light enters the aperture of the pulse camera.

Alignment and positioning of the optical elements ensure that the eyepiece observes the same image quality and format as that which the film sees.

Another image is folded and demagnified in the transfer lens assembly before it enters a high speed camera when one is used.

A derotated image of the luminous painted segment of the test bearing separator is optically folded out and directed toward an
image splitting mirror surface wedge which proportions the light entering two photomultiplier tube photocathodes. The electronic signals from these tubes are used by the tracking system to control the prism speed.

A tracking system holds the image of a selected point at the test bearing separator in the field of view. It will accommodate a variation of up to 10% of a fixed ratio of separator-to-shaft speed without loss of the ability to lock onto the proper position within one revolution of the bearing retainer.

It is necessary to sense the tracking error in angular position of the derotation prism to provide an input for the servo system. This error signal is provided in the form of the difference in output of the two multiplier phototubes.

A sector on the bearing retainer is coated with fluorescent paint and illuminated with ultraviolet light. An image of the sector of arc is formed in a plane containing the apex of a mirror surface wedge. The light striking the two surfaces of the wedge is reflected and illuminates the photocathode of the photomultiplier tubes. Rotation of the prism results in a displacement of the image and a consequent increase in the output of one tube and decrease in the output of the other.

Electronic filtering is provided to discriminate between the steady signal due to the ultraviolet excitation of the phosphor and any intermittent excitation due to strobe lamps to reduce any interaction between the level of light striking the phosphor and the error signal produced by the photomultipliers.

Four Chadwick-Helmuth Strobex lamps are flashed at the 16-frame-per-second camera rate to illuminate the separator and to stop the images of the protractors on the inner and outer races of the bearing so that angular position information is recorded on the photographs.
Four mercury vapor spot lamps with ultraviolet filters illuminate the flourescent patch for the tracking system.

The camera used was a Neyhart Enterprises model G-4. The camera film magazine accepts 100 or 200 foot reels of 35mm film. The camera has a data box, the image of which is projected onto each film frame.

IV. Test Bearings

Three bearings were used in the roller to separator contact force investigation. They were mainshaft roller bearings representative of those used in aircraft gas turbine engines. Two of the bearings were 118mm bore, part number FWA 5110041, with cylindrical outer raceways. The third was 115mm bore, part number FWA 501511B with an out-of-round outer raceway. Dimensions and other characteristics of these bearings are given in Table 1.

V. Separator Force Transducer

A roller contact force transducer was constructed on the bearing separator by introducing a cantilever beam between two of the bearing rollers. The cantilever beam replaced a rigid separating element so that cantilever beam deflection would give an indication of the roller contact force. A hole was drilled through one of the side rails of the separator to hold the fixed end of the cantilever beam. A notch to frame the deflected end of the cantilever was cut in the other side rail opposite the hole. Various beam cross-sections were used depending on contact forces and deflections encountered. A plastic rubbing block was cemented to the center portion of the beam to make up the normal roller spacing dimension of the rigid separator element replaced by the roller force indicating beam.
duplicate modification was installed at 180° to the first to maintain separator balance.

With the shaft end test bearing operating at a speed and load condition to be investigated, the derotation prism was synchronized with the separator to produce a stationary image of the deflecting end of the cantilever beam as the roller and separator repeatedly moved through loaded and unloaded regions of the bearing. The 16 frame per second 35 mm instrumentation camera photographed the motions of the cantilever beam deflections relative to the notch in the separator. As roller contact forces may be expected to be a repetitive event from revolution to revolution the relatively slow framing rate can be extended to a very high effective framing rate by taking a large number of photographs over many revolutions of the bearing. This gives frames covering 0 to 360° to the applied load. The angle to the applied load was indicated by the position of the cantilever beam relative to a fixed protractor on the bearing outer race. Radial loads were applied vertically at the 360° (0) degree mark on the protractor.

VI. Force Transducer Calibration

The force transducing cantilever beam was assembled into the separator with epoxy resin with the plastic spacing element also epoxied in place. The separator was held in a small vise and loaded with a wire hook positioned over the plastic rub block. A small weight pan and weights were used to load the cantilever beam. Cantilever deflections were photographed. Figure 2 shows a representative force-deflection relation.

VII. Experimental Procedure

The lubricating oil used throughout the tests was a 5-centistoke neopentylpolyol (tetra) ester. This is a type II oil which conforms
to specification MIL-L-23699. Test bearing inlet oil was heated and controlled to 485° K (1500°F).

The Separator Study Machine bearing rig was started with a load applied and brought up to speed, the desired load condition applied, the prism synchronized with the separator and 100 to 200 photographs taken. Film used was Kodak 2475 Recording Film. It was cut into lengths fitting stainless steel reels and developed in a small tank with HC 110 developer, dilution A, for 30 minutes at laboratory room temperature. This seemed to give images of adequate contrast, with background fog just beginning to be noticeable on fresh film.

**VIII. Data Analysis**

After chemical processing of the film was completed the film was respliced and read with a Benson-Lehner model N-2 film reader capable of indicating 4 digits with the least digit representing 0.005 mm (0.0002 in.) in the film image. The film images, however, varied in density and sharpness from frame to frame due to variation in Xenon flash intensity, duration, and jitter in flash initiation among the four Xenon flash tubes.

Readings were taken by aligning a cross-hair onto the lowest edge of the notch for R1, the bottom of the beam end for R2, the top of the beam end for R3, and the top of the notch for R4. A computer program was used to calculate differences R2-R1, R3-R1, R4-R1, R3-R2, R4-R3, and R4-R2. From R4-R1 and R3-R2 a consistency check was available to pull out or correct obviously defective readings as the notch dimension and beam height should always be of constant value. After subtraction of undeflected (zero) readings, the differences give indications of the beam deflection in that film frame.
The computer program also calculated average values of notch size for the photo set and normalized the deflection indications on the average notch size to compensate for image size variation with focus setting. It then scaled the deflections to the lineal measured notch dimension. The deflection indications were then multiplied by the spring constant determined in the force transducer calibration, and are listed and plotted by a Calcomp plotter.

It was possible to determine cage to shaft speed ratio with some accuracy over 10 successive photographs of multiple shaft revolutions from the following considerations.

As stated previously, the derotating prism is synchronized to rotate at half the separator speed thus producing a stationary image of the separator to be photographed. Protractors which are mounted on the stationary outer race and on the rotating inner race are visible in the photographs. Four Xenon flash tubes with a flash duration of 50 microseconds permit clear instantaneous photographs of the stationary separator and stop the motion of the protractor images. Typically 100 to 200 photographs were taken at a cine frame rate of 16 per second for each case investigated.

In these photographs the angle turned through by the separator (cage) can be determined from the difference in angle on the stationary outer race protractor between two consecutive frames. Thus,

\[ 2 \Delta \theta = \Delta \theta_p = \frac{\Delta \theta_c}{\cos W} \Delta t \]  \hspace{1cm} (1)

where:

- \( \Delta \theta_p \) = true prism angle turned through
- \( \Delta \theta_c \) = true cage angle turned through
- \( \Delta \theta_0 \) = angle difference \( +360^\circ \times \) number of revolutions between photographs
\[ \frac{W_C}{W_s} = \text{separator to shaft speed ratio in the operating bearing} \]
\[ W_s = \text{shaft speed} \]
\[ \Delta t = \text{time between photographs} \]

The protractors are engraved with angle increasing in the direction of shaft rotation. The shaft turns through a greater angle than does the separator; consequently, the cage photographs centered on the transducer in the cage show the inner race angles decreasing. The true angle that the shaft has turned through in the \( \frac{1}{16} \) second between successive frames may be determined from the protractor angles photographed by

\[
\Delta \theta_i = \Delta \theta_o - \Delta \theta_s \cdot \left( \frac{W_c}{W_s} \right) \Delta t - W_s \Delta t
\]

where:

\[ \Delta \theta_s = \text{angle difference on inner race protractor between photographs} \]
\[ = (\theta_{s_{i+1}} - \theta_{s_i}) \text{ with } i \text{ being the frame number} \]

\[ \Delta \theta_i = \text{true angle turned through by the shaft in time } \Delta t \]

From equation 2, then \( \Delta \theta_{st} = \Delta \theta_o - \Delta \theta_s \), and \( \frac{W_C}{W_s} \Delta t = \Delta \theta_o \),

\[ W_s \Delta t = \Delta \theta_{st} \text{ so:} \]

\[
\frac{W_C}{W_s} = \frac{\Delta \theta_o}{\Delta \theta_o - \Delta \theta_s}
\]

where \( \Delta \theta_s \) is a negative number.
Care must be taken in calculating angle differences $\Delta \theta_o$ and $\Delta \theta_s$ between photographs and in using equation (3). Multiple revolutions of shaft and separator occur without this being apparent in the photographs. At 16 frames per second with an appropriate epicyclic speed for $W_c/W_s$, the ranges of angle differences given in Table 3 may be anticipated.

To obtain the true angle of rotation of the cage between successive frames, it is necessary to:

1. Subtract the angle read from the reference point of the separator in the photograph from that read in the i-1 frame.
2. Determine the number of full rotations between frames using Table 4.
3. Add the number of full rotations to the difference found in step 1.
4. Critically examine the value calculated if the test speed is close to a speed at which a different number of revolutions might be possible or if speeds much different from epicyclic light occur.

These considerations led to the cage/shaft speed ratios that appear on the cage force figure captions and in the cage/shaft speed ratio versus load figures.

**IX Results and Discussion**

This investigation was undertaken to experimentally evaluate roller to cage contact forces. It was subsequently noted that information on cage to inner race land contact force, and cage to shaft speed ratios was also available in the data obtained.
A. Roller to Cage Contact Forces

The principal results of this investigation are the roller to cage contact forces shown in Figures 3-5. These figures show the roller force on the cage as a function of roller location in the bearing. **Roller location is measured clockwise from the centerline of the radial load at 0° (360°).** Table 2 summarizes the data obtained.

Different spring constants were necessary as the investigation progressed and as larger forces were encountered. The investigation began with a spring constant of 22.8 N/mm (130 lb/in). These transducers appeared to function adequately in the 501511B bearing with the out-of-round outer raceway, and were initially installed in the 541043D-1 bearing with the 0.18 mm (0.007 in) clearance. Failures in bending fatigue occurred in beams with 22.8 N/mm (130 lb/in) and 29.3 N/mm (160 lb/in) spring constants.

Transducers of spring constant 75.9 N/mm (45 lb/in) were fabricated and used in the 541043D bearings to obtain the data of Figures 3a-i and 4a-i.

Positive forces in the figures are those exerted by rollers tending to accelerate the cage. Negative forces are those exerted by rollers tending to retard or decelerate the cage. In general stiffer cantilever beam deflecting elements indicate greater forces, with more scatter in the film readings.

The force indicated by a cantilever deflection is created by a roller advancing into the cantilever located on the cage. A roller's advance relative to the cage, which moves with average roller speed, is determined by roller kinematics such as roller location on the raceway path, deflections, etc. The motion of the roller relative to the average roller...
will deflect the cantilever until the roller begins to recede from
the cantilever due to roller kinematics, provided limiting traction
forces are not exceeded. Thus the cantilever is deflected as much as
necessary to accommodate the roller advance relative to the cage. For
a given roller advance, the stiffer cantilever's deflection indicates
larger force. The stiffer cantilever deflecting elements will also
have smaller deflections. Errors in measuring the stiffer cantilevers' deflections will produce larger variations in the force measure-
ments. All of the variation in the figures may not be due to
errors in cantilever deflection, however. It is possible that there
is some variation in the rollers' motion as they traverse various por-
tions of raceway surfaces with possible cage motions of oscillation,
rocking and impacting on rollers and inner race land surfaces.

Loads of 360, 670, 1330, and 4450 N (50, 150, 300, and 1000 lb)
were applied to the 501511 B bearing without indication of skidding.
When these same loads were applied to the 541043 D-1 bearing the cage
to shaft speed ratios were 0.396, 0.409, 0.436, and 0.453 at 4,000 rpm
as compared to the 0.4562 epicyclic speed ratio. Loads of 6670, 4450,
and 2220 N (1500, 1000, and 500 lb) were used in the rest of the in-
vestigation to reduce the likelihood of skidding damage to the test
bearings.

Figures 3 and 4 show the magnitude and distribution of roller to cage
forces in the 0.18 mm (0.0073 in) and 0.21 mm (0.0083 in) clearance bearings as
indicated by a 79.5 N/mm (454 lb/in) spring constant transducer. The
0.18 mm clearance bearing seems to experience a rather narrow but well
defined force peak of 40 N (9 lb) in lightly loaded high speed cases which
is not apparent in the 0.21 mm clearance bearing data, though other
general characteristics of the two bearings are similar in that positive and negative forces of 25 N (5 lb) are not uncommon at 8,000 and 12,000 rpm speeds.

Figure 5 seems to indicate that the cage of the out-of-round outer race bearing experiences forces of 5 to 10 N (1 to 2 lb) that are more nearly constant throughout the bearing. These data were obtained with a 22.8 N/mm (130 lb/in) transducer. Testing with this bearing was terminated after severe fretting was discovered. This was apparently due to centrifugal force loosening the fit between the bearing, sleeve spacer, and shaft of the test rig. The sleeve for the 118 mm bearings was manufactured to provide a 0.025 mm (0.001 in) interference at the shaft diameter after the sleeve was assembled in the bearing bore, and has seemed to function adequately.

E. Cage to Inner Face Land Contact Force

From the data of Figures 3, 4, and 5 it was possible to derive the force between the cage and its guiding contact with the inner race land. This force was obtained by taking horizontal and vertical components of each force point as plotted in Figures 3, 4, and 5. Adding vertical and horizontal forces in a 12.9 degree sector, and dividing by the number of forces in the sector gave the average force one of the 26 rollers would exert on the cage. The sum of the 26 roller forces should equal the resultant force that the inner race must exert on the cage. The angular location of the resultant force was obtained by taking the arc tangent of the ratio of horizontal to vertical force components. Figure 6 summarizes the magnitude and direction of the cage to inner race land force due to ball contact forces for various speeds and loads. It should be noted that this calculation did not include the weight of the cage (1.63 and 2.24 N (0.37 and 0.50 lb) for the 118 and 115 mm bearings).
C. Cage to Shaft Speed Ratios

Figure 7 shows the cage to shaft speed ratios calculated by the method described in Section VIII, Data Analysis. The epicyclic cage speed for the 115 mm may be calculated from the data in Table 1 to be 0.4565 and that for the 118 mm bearing to be 0.4562. Figure 7 and Table 2 seem to indicate that the out-of-round outer raceway bearing had little tendency to skid, (0.2% cage slip) even at very low loads, while the cylindrical outer raceway bearings did skid appreciably at very low loads, and had a maximum value of cage to shaft speed ratio of 0.4539 (0.5% cage slip) for the larger clearance bearing at a 6670 N (1500 lb) load, the maximum used, at the 4,000 rpm speed.

X Summary of Results

Roller to cage contact forces were evaluated experimentally. The maximum roller-cage force observed was 43 N (9.5 lb) and occurred at light load and high speed. Resultant cage to shaft forces were calculated from roller to cage contact forces. The maximum cage-shaft force was 60 N (13.6 lb) and also occurred at light load and high speed. The out-of-round outer raceway was effective in preventing skidding even at very light loads. Skidding was observed, however, in the cylindrical outer race bearings.
References


FIG. 1b Schematic of Shaft Assembly
Figure 1c
Light Paths Through The Scanner
PWA 54:043 D ROLLER BEARING
4.78X0.84 MM CROSS SECTION
0.5 MM VERTICAL POSITION BEAM
SEPT. 4, 1977

FIG. 2 Sample Force Transducer Calibration
FIG. 3m

FORCE (POUNDS)

-5.00 -4.00 -3.00 -2.00 -1.00 0.00 1.00 2.00 3.00 4.00 5.00

FORCE (NEWTONS)

-25.00 -20.00 -15.00 -10.00 -5.00 0.00 5.00 10.00 15.00 20.00 25.00

PMA 54043 D ROLLER BEARING
4450 N (1000 LB) LOAD
4051 RPM 08/15/77-3
0.4527 CAGE SHAFT SPEED RATIO

70090119NYPAN7

09/14/77
FIG. 39

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FORCE (POUNDS)

-5.00 -4.00 -3.00 -2.00 -1.00 0.00 1.00 2.00 3.00 4.00 5.00

FORCE (NEWTONS)

-25.00 -20.00 -15.00 -10.00 -5.00 0.00 5.00 10.00 15.00 20.00 25.00

PWA 541043 D ROLLER BEARING

8870 N (1500 LB) LOAD

4056 RPM 08/25/77-4

0.454 CASE/SHAFT SPEED RATIO
FIG. 4a

FORCE (POUNDS)

-5.00 -4.00 -3.00 -2.00 -1.00 0.00 1.00 2.00 3.00 4.00 5.00

FORCE (NEWTONS)

-25.00 -20.00 -15.00 -10.00 -5.00 0.00 5.00 10.00 15.00 20.00 25.00

PMA 541043 D-2
4016 RPM (500 LB) LOAD
0.4523 CAGE/SHAFT SPEED RATIO

2220 N (500 LB) LOAD
0.4523 CAGE/SHAFT SPEED RATIO
FIG. 5a

FORCE (POUNDS)

-5.00  -4.00  -3.00  -2.00  -1.00  0.00  1.00  2.00  3.00  4.00  5.00

-25.00 -20.00 -15.00 -10.00 -5.00  0.00  5.00  10.00 15.00 20.00 25.00

PMA 5011538 ROLLER BEARING
4000 RPM 07/17/77-4
0.454 CASE/SHAFT SPEED RATIO

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FIG. 5e

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0.4801 CASE/SHAFT SPEED RATIO
7034 RPM 07/05/77-5
260 N (50 LB) LOAD
PWA 501519 ROLLER BEARING
FIG. 5

PMA 50151B ROLLER BEARING
870 N (150 LB) LOAD
7928 RPM 07/05/77-1
0.458\% CAGE/SHAFT SPEED RATIO

FORCE (POUNDS)

-5.00 -4.00 -3.00 -2.00 -1.00 0.00 1.00 2.00 3.00 4.00 5.00

FORCE (NEWTONS)

-25.00 -20.00 -15.00 -10.00 -5.00 0.00 5.00 10.00 15.00 20.00 25.00
FIG. 5j

670 M (150 LB) RADIAL LOAD
0.4500 CASE/SHAFT SPEED RATIO
FIG. 5k

PWA 501118 ROLLER BEARING
1350 N (300 LB) LOAD
0.4560 CAGE/SHAFT SPEED RATIO
FIG. 6a PWA 541043D-1
- 2220 N (500 lbs) Load
- 4450 N (1000 lbs) Load
- 6670 N (1500 lbs) Load

FIG. 6b PWA 541043D-2
- 2220 N (500 lbs) Load
- 4450 N (1000 lbs) Load
- 6670 N (1500 lbs) Load

FIG. 6c PWA 501511B
- 360 N (80 lbs) Load
- 670 N (150 lbs) Load
- 1330 N (300 lbs) Load
- 4450 N (1000 lbs) Load
FIG. 6d PWA 541043D-1
- ○ 2220 N (500 lbs) Load
- □ 4450 N (1000 lbs) Load
- △ 6670 N (1500 lbs) Load

FIG. 6e PWA 541043D-2
- ○ 2220 N (500 lbs) Load
- □ 4450 N (1000 lbs) Load
- △ 6670 N (1500 lbs) Load

FIG. 6f PWA 501511B
- ○ 360 N (80 lbs) Load
- □ 670 N (150 lbs) Load
- △ 1330 N (300 lbs) Load
- ◇ 4450 N (1000 lbs) Load

FIGS. 6d-f Resultant Cage Force Location Versus Shaft Speed
FIG. 7a Cage to Shaft Speed Ratios

- 4000 RPM 09/07/77-5 09/07/77-3 09/07/77-4
- 8000 RPM 09/07/77-8 09/07/77-6 09/07/77-7
- 12000 RPM 09/21/77-1 09/21/77-2 09/16/77-3

PWA 541043 D-1 0.18 MM (.0073 IN) CLEARANCE

FIG. 7b Cage to Shaft Speed Ratios

- 4000 RPM 09/30/77-5 09/30/77-4 09/30/77-3
- 8000 RPM 09/30/77-8 09/30/77-7 09/30/77-6
- 12000 RPM 10/05/77-4 10/05/77-3 10/05/77-2

PWA 541043 D-2 0.21 MM (.0083 IN) CLEARANCE
0000 RPM 7/1/77-8 7/1/77-7 7/1/77-6 7/1/77-5
8000 RPM 7/5/77-5 7/5/77-4 7/5/77-3 7/5/77-2
12000 RPM 7/12/77-2 7/12/77-3 7/12/77-4
PWA 501511 B OUT-OF-ROUND OUTER RACE

FIG. 7c Cage to Shaft Speed Ratios
Table 1
Test Bearing Specifications

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<th>PWA 501511 B</th>
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<td>inches</td>
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<td>Inner Race</td>
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<td>Bore Dia.</td>
<td>118</td>
<td>4.6457</td>
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<td>Raceway Dia.</td>
<td>131.66</td>
<td>5.1834</td>
</tr>
<tr>
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<td>137.47</td>
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*Bearing Serial Number A2284 has clearance .18 mm (.0073 in), is designated PWA 541043 D-1 in figures.
Bearing Serial Number A2279 has clearance .21 mm (.0083 in), is designated PWA 541043 D-2 in figures.
Clearance is outer race inner diameter minus 2 roller dia. minus inner race outer diameter.

**PWA 501511 B has out-of-round outer raceway.
<table>
<thead>
<tr>
<th>Fig.</th>
<th>Beam</th>
<th>Speed</th>
<th>Load</th>
<th>Resultant Cage Force</th>
<th>Cage/Shaft</th>
<th>Cage Slip</th>
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Beam A has K = 79.5 N/mm (65 lb/in)
Beam B has K = 29.3 N/mm (160 lb/in)
Beam C has K = 22.6 N/mm (130 lb/in)

**Table 2**

**Summary of Test Conditions and Data**

<table>
<thead>
<tr>
<th>Fig.</th>
<th>Beam</th>
<th>Speed</th>
<th>Load</th>
<th>Resultant Cage Force Magnitude</th>
<th>Cage/Shaft Speed Ratio</th>
<th>Cage Slip</th>
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**Beam A has K = 79.5 N/mm (65 lb/in)**
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**Beam C has K = 22.6 N/mm (130 lb/in)**

Original Page is of Poor Quality
Table 3
Calculated Number of Shaft Revolutions Between Photographs
For Bearings with Epicyclic Speed Ratio of 0.456

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<th>$\Delta \theta_{\text{rev}}$</th>
<th>$W_s = (\Delta \theta)_{16} x 60$</th>
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