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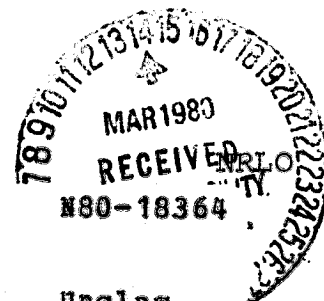
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AWARDS ABSTRACT

## FREQUENCY-SCANNING PARTICLE
## SIZE SPECTROMETER

The invention relates to apparatus and method for remotely reconstructing the effective spectrum of sizes of scattering particulates of unknown chemical composition in equivalent spheres of lower radius value approximately one micrometer and unbounded upper radius value. Conventional direct sampling methods, where particles are thermally precipitated, impacted or otherwise mechanically collected, present several problems, such as: disturbing of sample, low sampling rate, discontinuous sampling, collection efficiency problems, long sampling time and painstaking analysis.

FIG. 1 illustrates the apparatus as might be used in a laboratory, and FIGS. 2, 3 and 4 show the effects of viewing angle $\theta_s$, spectral range $\theta_{min}$ to $\theta_{max}$ and resolution $\Delta\sigma$. The technique is to measure, at intervals $\Delta\sigma$, the intensity of light, $I_o$, from a natural or artificial source $I_0$ as it is scanned in frequency ($\sigma=1/\lambda$) using a chopper 12 and a multiple-filter detector 13. At each frequency interval, a measurement is also made of the intensity of light, $I(\sigma)$ passing through a scattering medium in a cell 11 (or freely suspended in air or a liquid, such as a blood plasma) using a multiple filter detector 14 having a fixed field of view at a scattering angle $\theta_s$. Controls represented by dotted lines 15 and 16 synchronize the filters 13 and 14 in the scanning steps. A ratio $I_s=I(\sigma)/I_o$ is determined at each step by some computing means 17. Particle size distribution $n(r)$ is then computed by means 18 for display from the following equation:

$$n(r) = -\frac{\ell^3}{2\pi r^2} \int_0^\infty J_1(y) Y_1(y) y \frac{d}{d\sigma}(\sigma I_\sigma) d\sigma, \quad y=\ell r\sigma, \quad \theta=\theta_s$$

where $J_1$ is a Bessel function of first kind and order unity, $Y_1$ is a Bessel function of second kind and order unity, $\ell=2\pi\sin\theta,\theta$

Io, from a natural or artificial source Io as it is scanned in frequency ($\sigma=1/\lambda$) using a chopper 12 and a multiple-filter detector 13. At each frequency interval, a measurement is also made of the intensity of light, $I(\sigma)$ passing through a scattering medium in a cell 11 (or freely suspended in air or a liquid, such as a blood plasma) using a multiple filter detector 14 having a fixed field of view at a scattering angle $\theta_s$. Controls represented by dotted lines 15 and 16 synchronize the filters 13 and 14 in the scanning steps. A ratio $I_s=I(\sigma)/I_0$ is determined at each step by some computing means 17. Particle size distribution $n(r)$ is then computed by means 18 for display from the following equation:

$$n(r) = -\frac{\ell^3}{2\pi r^2} \int_0^\infty J_1(y)Y_1(y)y\frac{d}{d\sigma}(\sigma I_\sigma)d\sigma, \quad y=\ell r\sigma, \quad \theta=\theta_s$$

where $J_1$ is a Bessel function of first kind and order unity, $Y_1$ is a Bessel function of second kind and order unity, $\ell=2\pi\sin\theta$, $\theta$ is the fixed viewing angle at which scattered light is measured, $r$ is particle radius, and $\sigma$ is the reciprocal of wavelength. In the case of $j$ particle species embedded in $k$ gas species, the former equation remains valid provided only $I_\sigma$ is changed to the following expression:

$$I_\sigma \rightarrow G_\sigma = \frac{1}{j}\left[4\cos\theta \ I_\sigma - \frac{3}{2}\sum_k\left[\frac{2 - \rho_k \cos2\theta}{2 + \rho_k}\right]\right]$$
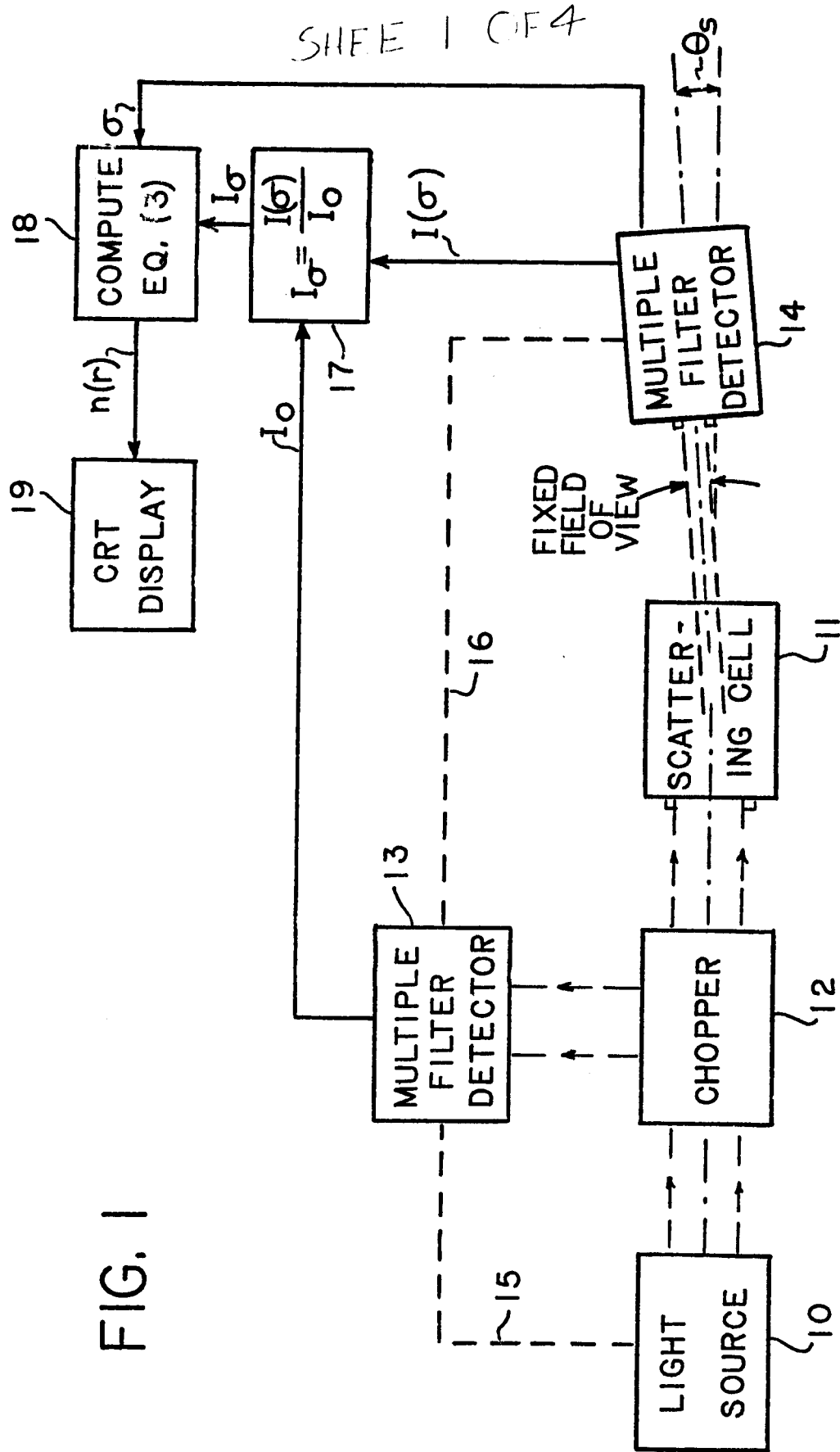
where $\rho_k$ is a depolarization factor of the $k^{th}$ gas defined as the ratio of scattered intensities in directions parallel and perpendicular to the plane of scattering for an incident beam of natural light. The preferred scattering angle $\theta_s$ is 150 min, but may be within the range of 100 to 200 min. The frequency intervals $\Delta\sigma$ should be smaller than 0.2 inverse micrometers ($\mu m^{-1}$) over a range of approximately $0.20\mu m^{-1}$ to $4.0\mu m^{-1}$.

The novelty resides in determining particle size distribution independently of refractive indices of particles, including the accurate location of the mode radius of particles forming a homogeneous cloud or medium between the light source and the detector, using remote and passive instrumentation. Even the light source may be regarded as passive since it may be natural light. This determination is provided without constraining the size distribution to any analytical model. Use of such models would necessarily bias the distribution.

# FIG. 1

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EFFECT OF VIEWING ANGLE

$0.2 \leq \sigma \leq 4.0 \ \mu m^{-1}$
$\Delta \sigma = 0.061 \ \mu m^{-1}$

n (true)

$\theta_s = 150$ min

$\theta_s = 50$ min

$\theta_s = 350$ min

SIZE DISTRIBUTION, n(r)

PARTICLE RADIUS, r($\mu$m)

FIG. 2

EFFECT OF SPECTRAL RANGE

$\theta = 150$ min

$n$ (true)

$0.198 \leq \sigma \leq 4.070 \ \mu m^{-1}$
$\Delta\sigma = 0.061 \ \mu m^{-1}$

$0.286 \leq \sigma \leq 1.190 \ \mu m^{-1}$
$\Delta\sigma = 0.056 \ \mu^{-1}$

$1.06 \leq \sigma \leq 10.0 \ \mu m^{-1}$
$\Delta\sigma = 0.5 \ \mu m^{-1}$

$0.031 \leq \sigma \leq 0.235 \ \mu m^{-1}$
$\Delta\sigma = 0.003 \ \mu m^{-1}$

SIZE DISTRIBUTION, $n(r)$

PARTICLE RADIUS, $r(\mu m)$

FIG. 3

EFFECT OF SPECTRAL RESOLUTION

$\theta = 150$ min

$0.198 \leqslant \sigma \leqslant 4.070 \ \mu m^{-1}$

n (true)

$\Delta\sigma = 0.061 \ \mu m^{-1}$

$\Delta\sigma = 0.774 \ \mu m^{-1}$

$\Delta\sigma = 0.140 \ \mu m^{-1}$

PARTICLE RADIUS, r($\mu m$)

SIZE DISTRIBUTION, n(r)
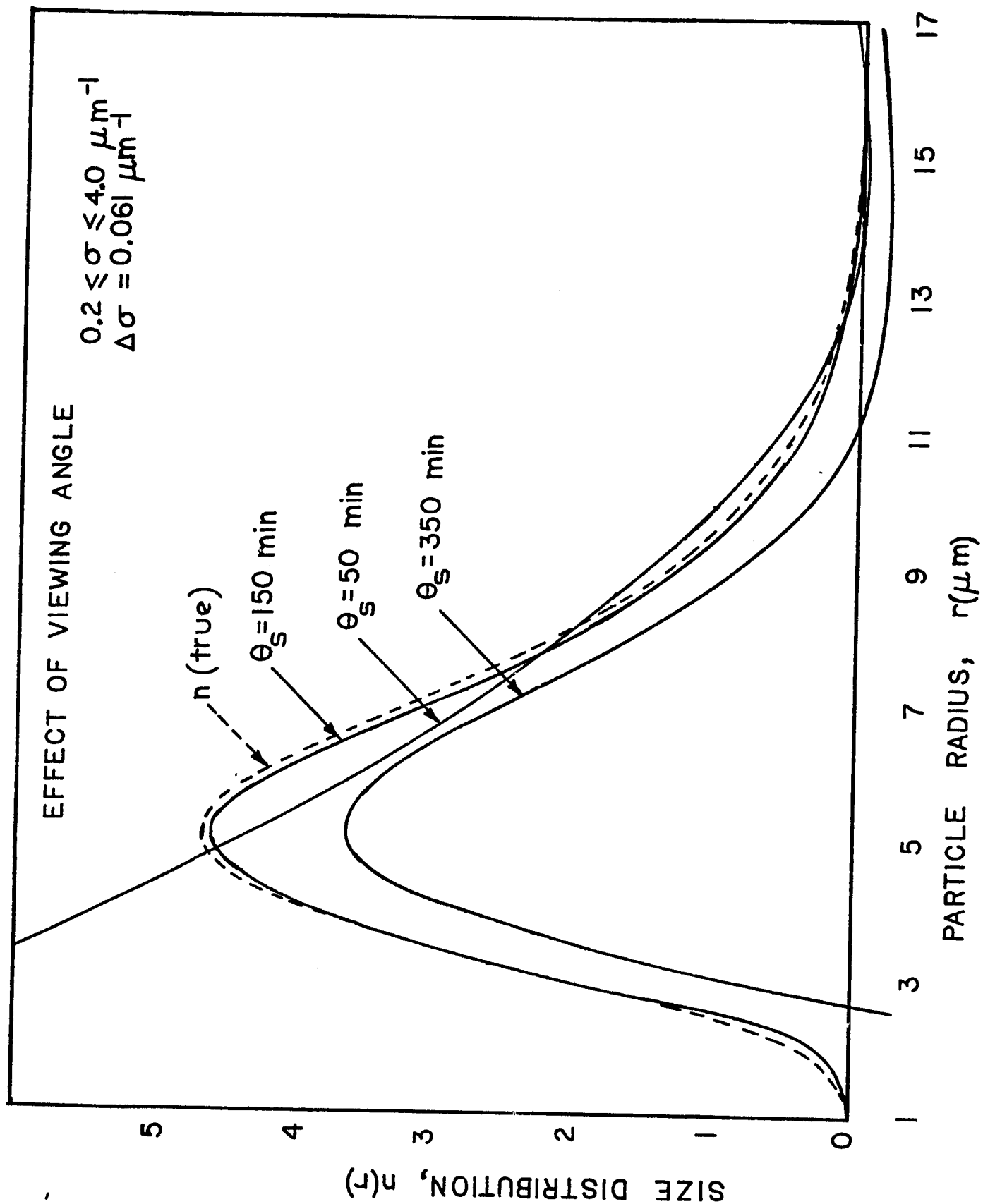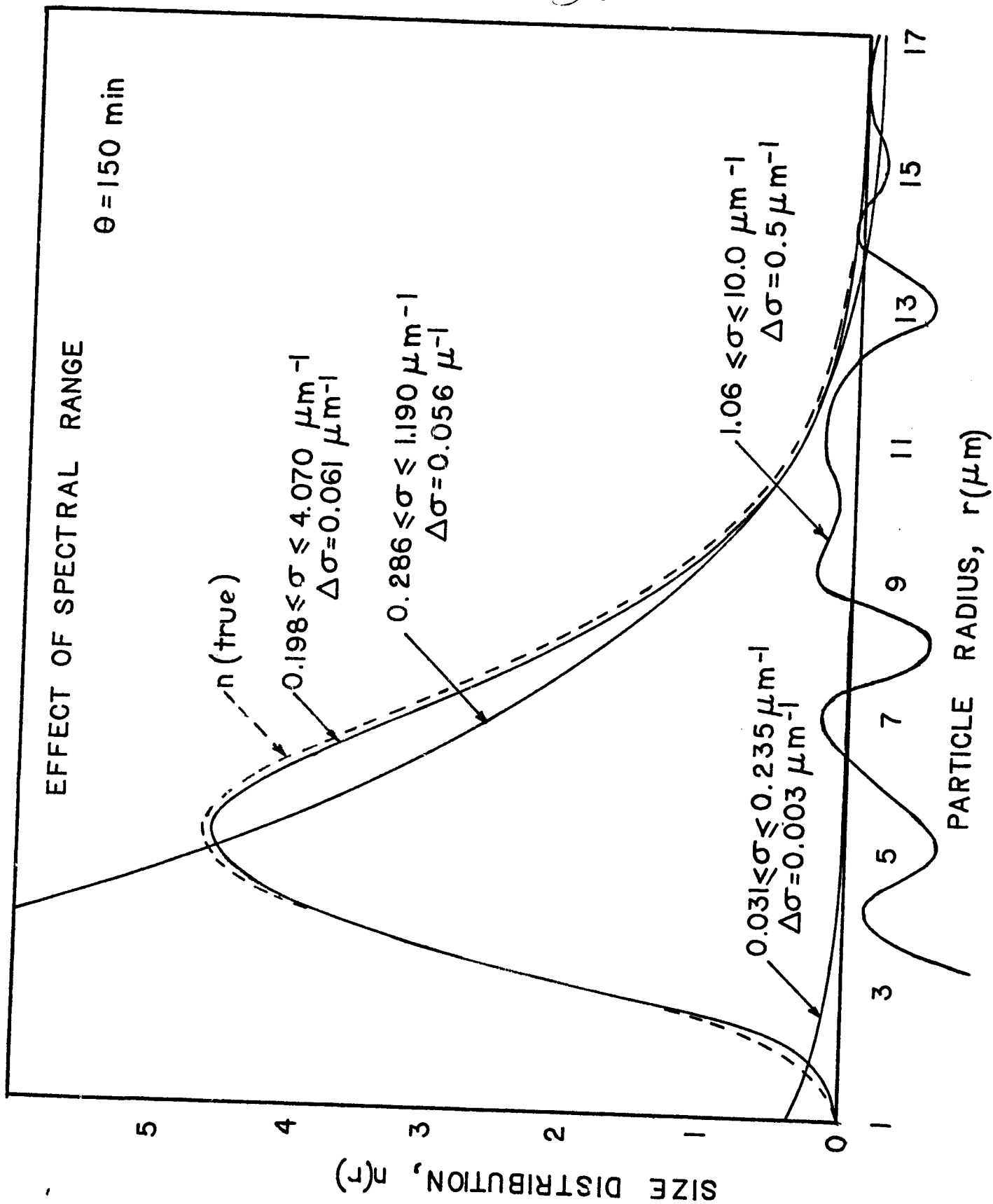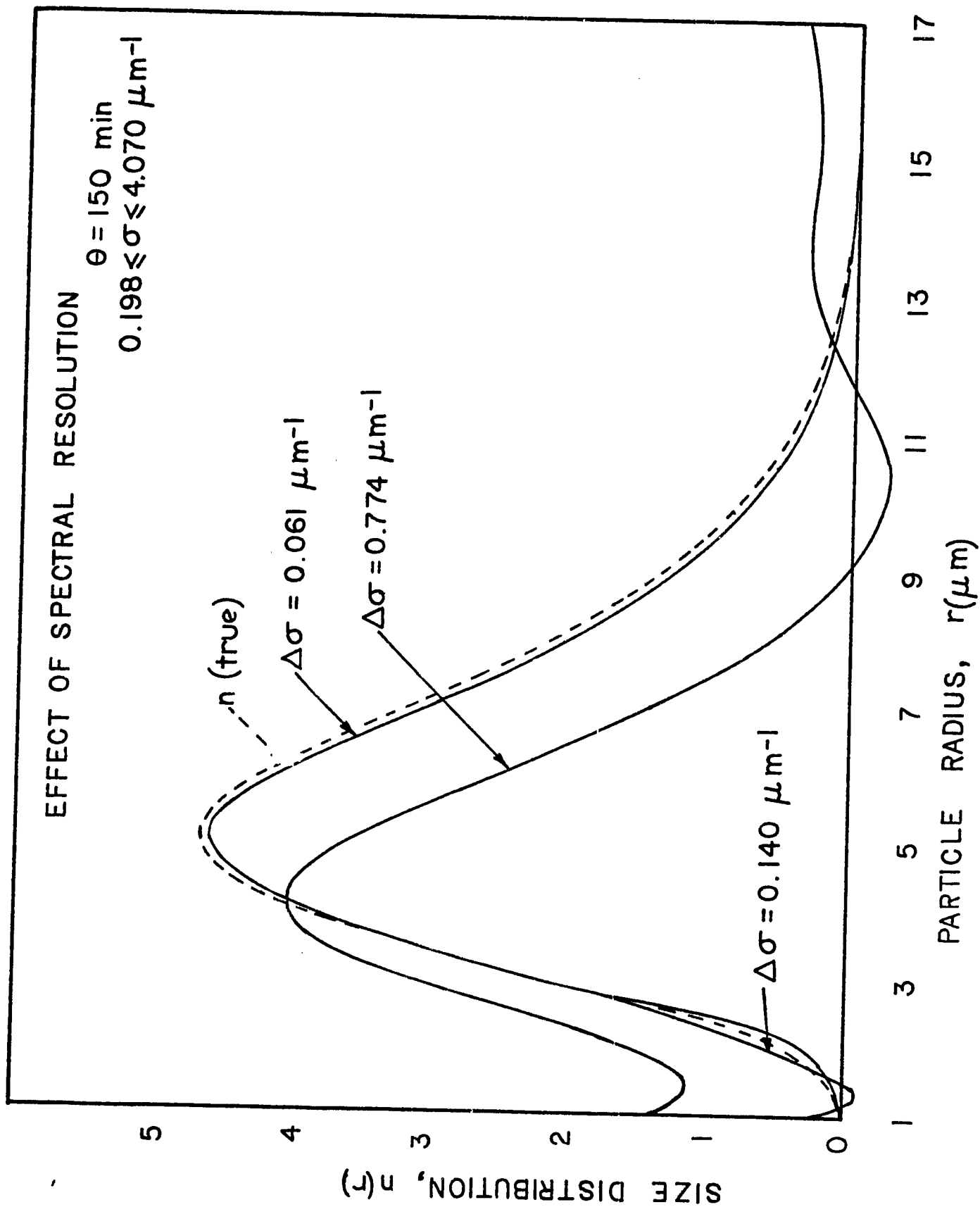
FIG. 4

# S P E C I F I C A T I O N

TO ALL WHOM IT MAY CONCERN:


BE IT KNOWN THAT ALAIN L. FYMAT, a citizen of

Morocco, residing at 1080 South El Molino Avenue, Pasadena,

California 91106, in the County of Los Angeles, State of

California, has invented a new and useful


## FREQUENCY-SCANNING PARTICLE
## SIZE SPECTROMETER


of which the following is a specification:

## ABSTRACT OF THE DISCLOSURE


A particle size spectrometer having a fixed field of
view within the forward light scattering cone at an angle $\theta_s$
between approximately 100 and 200 minutes of arc (preferably at
150 minutes), a spectral range extending approximately from 0.2
to 4.0 inverse micrometers ($\mu m^{-1}$), and a spectral resolution
between about 0.1 and 0.2 $\mu m^{-1}$ (preferably toward the lower end
of this range of spectral resolution), is employed to determine
the distribution of particle sizes, independently of the chemical
composition of the particles, from measurements of incident light,
$I_o$, at each frequency, $\sigma$ ($=1/\lambda$), and scattered light, $I(\sigma)$,
according to the equation:

$$n(r) = -\frac{\ell^3}{2\pi r^2} \int_0^\infty J_1(y)Y_1(y)y\frac{d}{d\sigma}(\sigma I_\sigma)d\sigma, \quad y=\ell r\sigma,$$

where $\ell = 2\pi\sin\theta$, $\theta$ being the fixed viewing angle $\theta_s$ at which
scattered light is measured, r is particle size, $\sigma$ is the
reciprocal of wavelength, $J_1$ is a Bessel function of first

kind and order unity, $Y_1$ is a Bessel function of second kind and order unity. The quantity, $I_C$, is the ratio of scattered light to incident light at each frequency interval. The apparatus is a passive remote sensor that can be used in laboratories, field stations, flying aircrafts and airships, and on board an orbiting satellite.

## ORIGIN OF THE INVENTION

The invention described herein was made in the performance of work under a NASA contract and is subject to the provisions of Section 305 of the National Aeronautics and Space Act of 1958, Public Law 85-568 (72 Stat. 435; 42 USC 2457).

## BACKGROUND OF THE INVENTION

This invention relates to a method and apparatus for determining the distribution of particle sizes of a scattering medium of unknown chemical composition. The medium may consist of a composite mixture of arbitrary numbers of chemically different particles embedded in various gases.

There is a continuing need to determine the size distribution of any arbitrary number of particle species which may present a distribution in their refractive indices, and which may be embedded in a scattering medium of unknown chemical composition, for such industrial purposes as environmental pollution monitoring and control, chemical analyses, aeronautical engineering and rocket engineering as well as for such other purposes as meteorological research, geophysical research, and biomedical analyses. The composite mixture of

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particles and gases may be contained in an experimental chamber,
suspended freely in the air, or suspended in fluids such as
medical plasmas, or in any other similar situation where parti-
culate sizes must be determined without disturbing the sample.

5      Conventional direct sampling methods where particles
are thermally precipitated, impacted or otherwise mechanically
collected, as well as _in situ_ imaging methods, present several
problems. Some of these problems are: disturbing of sample,
low sampling rate, discontinuous sampling, collection efficiency
10   problems, long sampling time and painstaking analyses.
Additionally, they cannot be used as remote sensors for real-
time operation.

       To avoid these problems of direct sampling, and at
the same time provide a remote sensing capability, methods
15   have been developed which exploit the forward light scattering
properties of particles at frequencies within the range 0.198 to
4.070 inverse micrometers ($\mu m^{-1}$) or within any larger range
extending down to $0.02\mu m^{-1}$ and up to $9.27\mu m^{-1}$. Incident light,
$I_o$, possessing a spectrum of frequencies in the ranges above
20   specified, is characterized only by its wavenumber, $\sigma_i$, the
reciprocal of the wavelength, $\lambda_i$. Its direction of propagation,
$\theta_i$, is the direction of reference, $\theta_i = 0$. The subscript, i,
here stands for "incidence." Particles are characterized by
their nature and micro-structure, respectively represented by
25   a refractive index, m, a complex number, and a size distribution,
n (r), representing a partial concentration per unit volume and
per unit increment of the radius r. Only n (r) is independent

of the wavenumber. The various particles, assumed to be spherical in shape, may also present a distribution in m itself. Gases will be similarly characterized by their number density, i.e. number of atoms or molecules per unit volume, refractive

5 index and geometrical shape. Scattered light, on the other hand, is characterized by its wavenumber, $\sigma_s$, and direction, $\theta_s$, of propagation. Here the subscript, s, stands for "scattering." The direction, $\theta_s$, is thus the scattering angle with reference to the incident light direction $\theta_i$.

10 For a given incident light, i.e., for a situation where $\sigma_i$ and $\theta_i$ are given, and for a given assembly of scatterers, i.e., for an assembly of particles of given refractive indices, $m(\sigma_s)$, and size distribution, n (r), Mie's theory of scattering by a conducting sphere enables us to

15 determine the scattered light for any arbitrary $\sigma_s$ and $\theta_s$. Conversely if the incident light is known for any $\sigma_i$ and $\theta_i$ to be prescribed, and the scattered light is measured for various $\sigma_s$ and $\theta_s$ to be also prescribed, we should be able in principle to infer the properties of the particles, that is their size

20 distribution, and refractive index values at the various $\sigma_s$. In other words, Mie's theory enables us to compute the output, $I_s$, in all its detailed variations if we know the input, $I_o$, and the properties of the particles $m(\sigma_s)$ and n(r). However, what is of interest is a determination of the scatterers

25 from a knowledge of the input, $I_o$, and the output, $I_s$. But from an inversion of Mie's theory it would be possible to determine only the combined relation between the refractive indices, $m(\sigma_s)$, and size distribution, n(r), and not the size distribution separately.

It has been discovered that the Fraunhofer theory of
angular diffraction of light of fixed single frequency at an
aperture in a plane screen can be extended to a range of multiple
frequencies. Under these conditions, the light scattered by a
5      particle is essentially independent of the refractive index,
$m(\sigma_s)$, and depends only on its size as though the particle
were an aperture in a screen of the same radius. It has also
been discovered that, working within the restricted domain
of applicability of the theory thus extended ($\theta_s$ between 100 and
10      200 minutes of arc, approximately, preferably $\theta_s = 150$ minutes;
and $0.2\mu m^{-1} \leq \sigma_s \leq 4.0\mu m^{-1}$, approximately), it is possible to
determine size distribution, n (r), independently of refractive
indices $m(\sigma_s)$, i.e., to determine size distribution of particles
of radius larger than approximately one micrometer ($\mu m$) without
15      knowing anything of their refractive indices, from known incident
light, $I_o$, and measured scattered light, $I_s$.

If the assembly of scatterers under study consists of
particles of j different species and k different gases, the
identical determination of n (r) can still be made provided only
20      j, k, and the so-called depolarization factor of each gas (this
is defined as the ratio of scattered intensities in directions
parallel and perpendicular to the plane of scattering for an
incident beam of natural light), $\rho_k$, are known.

## SUMMARY OF THE INVENTION

25      In accordance with the present invention, a natural
or artificial light source is passed through a volume of
scattering particles the size distribution of which is to be
determined. The intensity of light scattered by the particles,

at a fixed angle between approximately 100 and 200 minutes of arc from the direction of incident light, preferably 150 minutes of arc, is recorded as a function of frequency, $I(\sigma)$. Records

5 are made across the approximate frequency interval $0.20\mu m^{-1}$ to $4.0\mu m^{-1}$, at frequency steps smaller than about $0.2\mu m^{-1}$. Simultaneously, the intensity of the incident light at each frequency, $I_o$, is recorded. The ratio $I_\sigma$ of scattered light, $I(\sigma)$, to incident light, $I_o$, is then obtained. In order to determine the size distribution, $n(r)$, from the ratio $I_\sigma$, the

10 following equation has been derived and investigated with regard to its correctness, the uniqueness of the solution obtained from it, and the stability of this solution with regard to inherent experimental and analytical noises :

$$n(r) = - \frac{\ell^3}{2\pi r^2} \int_0^\infty J_1(y)Y_1(y)y\frac{d}{d\sigma}(\sigma I_\sigma)d\sigma, \quad y=\ell r\sigma,$$

15 where $J_1$ is a Bessel function of first kind and order unity, $Y_1$ is a Bessel function of second kind and order unity, $\ell = 2\pi\sin\theta$, $\theta$ being the fixed viewing angle at which scattered light is measured, $r$ is particle radius, and $\sigma$ is the reciprocal of wavelength. In the case of $j$ particle species embedded in $k$

20 gas species, the former equation remains valid provided only $I_\sigma$ is changed to the following expression:

$$I_\sigma \rightarrow G_c = \frac{1}{j}\left[4\cos\theta \, I_\sigma - \frac{3}{2}\sum_k \frac{2-\rho_k\cos2\theta}{2+\rho_k}\right],$$

where $\rho_k$ is a so-called depolarization factor of the $k^{th}$ gas defined as the ratio of scattered intensities in directions

25 parallel and perpendicular to the plane of scattering for an incident beam of natural light.

The novel features of the invention are set forth with particularity in the appended claims. The invention will best be understood from the following description when read in conjunction with the accompanying drawings.

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## BRIEF DESCRIPTION OF THE DRAWINGS

The FIG. 1 illustrates schematically an example of apparatus for the method of the present invention, where the method steps operating on measured quantities are represented by functional blocks.

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FIG. 2 is a graph showing the effect of viewing angle, $\theta_s$, on determining particle size distribution from light scattered by the particles according to the present invention.

FIG. 3 is a graph showing the effect of spectral

15
range $\theta_{min}$ to $\theta_{max}$, in scanning the frequency of light incident on particles for determining particle size distribution.

FIG. 4 is a graph showing the effect of spectral resolution, $\Delta\sigma$, in the process of determining particle size

20
distribution according to the present invention.

## DESCRIPTION OF THE PREFERRED EMBODIMENTS

Referring to FIG. 1, a natural or artificial light source 10 is directed to a cell 11 filled with a medium of unknown chemical composition through a chopper 12 which

5 cyclically deflects the incident light, $I_o$, to a reference multiple-filter detector 13 for the purpose of measuring the incident light intensity as the light source is scanned in frequency. The filter of the detector is preferably changed as the light source is scanned in order that the reference

10 measurement $I_o$ be accurate for each frequency of incident light. An object multiple-filter detector 14 is likewise controlled to detect scattered light at the different prescribed frequencies as the source is scanned. That is represented by dotted lines 15 and 16 for synchronized control

15 of the detector and light source. The reference and object multiple-filter detectors can be detector arrays in which each detector element is slaved to a specific frequency.

The object detector 14 is designed to have a fixed field of view at a fixed angle $\theta_s$ of less than 6° within the

20 forward scattering cone of the cell 11. For best results, the scattering angle $\theta_s$ is made about 150 minutes of arc, but it may be any angle between 100 and 200 minutes of arc, approximately. It is also designed to have a spectral resolution, i.e., a frequency step, $\Delta\sigma$, as coarse as $0.2\mu m^{-1}$ or as fine as

25 $0.1\mu m^{-1}$, and to operate within the approximate spectral frequency limits of $\sigma_{min} = 0.2\mu m^{-1}$ and $\sigma_{max} = 4.0\mu m^{-1}$.

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Although a cell is indicated, the scattering particles
forming a homogeneous cloud or medium between the light source
and the detector may be contained in a laboratory chamber,
suspended freely in the air, contained in fluids such as plasmas

5      and blood, emitted from any type of industrial or engine
nozzle, or in any other similar situation where particulate
sizes must be determined without disturbing the sample in any
manner.  Also, although a variable light source is indicated,
radiance from particles that exhibit significant thermal emission

10     e.g., radiance from atmospheric particles which emerges from
the atmosphere, can also be used.  On the other hand, a light
source may be employed that emits all of the frequencies to be
scanned.  In the latter case, the control for frequency scanning
may be effected at only the detectors 13 and 14, while in the

15     former case it is effected only at detector 14.

If the foregoing restrictions on the fixed angle,
$\theta_s$, spectral frequency range, $\sigma_{min}$ to $\sigma_{max}$, and spectral resolu-
tion, $\Delta\sigma$, of the reference and object detectors are observed,
the measurements of scattered light $I(\sigma)$ can provide the complete

20     spectrum of particulate sizes, i.e., particle size distribution,
$n(r)$, in radii of equivalent spheres, from approximately 1μm
to any arbitrarily larger value, including the accurate location
of the mode radius (corresponding to the largest concentration
of particles).  The technique will now be described.  Consider

25     an incident beam of radiation of wavenumber, $\sigma = 1/\lambda$, ($\lambda$=wave-
length), and intensity, $I_o$, illuminating a single particle of
radius, r.  The singly-scattered light intensity, $I(\sigma)$, at
angle, $\theta$, in units of $I_o$, is expressed by the formula:

$$I_\sigma \equiv \frac{I(\sigma)}{I_o} \approx \left[ \frac{r\, J_1\,(kr\,\sin\,\theta)}{\sin\,\theta} \right]^2, \quad \theta = \theta s, \qquad (1)$$

where $k = 2\pi\sigma$ and $J_1$ is a Bessel function of first kind and order unity. For a distribution of sizes, $n(r)$, the generalization of this expression will provide the total scattered light

5    intensity :

$$I_\sigma = \frac{1}{\sin^2\theta} \int_0^\infty n(r)\, r^2\, J_1^2(x)dr, \quad x = kr\,\sin\,\theta. \qquad (2)$$

It may be noted that equations (1) and (2) depend only on r. In order to determine $n(r)$ from measurements of $I_\sigma$, it is necessary to invert this equation. The analytical inverse of

10    equation (2) is obtained in the form:

$$n(r) = - \frac{\ell^3}{2\pi r^2} \int_0^\infty J_1(y)Y_1(y)y \frac{d}{d\sigma} (\sigma I_\sigma)\, d\sigma, \quad y = \ell r\sigma, \qquad (3)$$

where $\ell = 2\pi\,\sin\,\theta$ and $Y_1$ is a Bessel function of second kind and order unity.

If the scattering medium being illuminated consists

15    of j different species of particles embedded in k different species of gases, equations (2) and (3) remain valid provided only we replace in these equations the quantity $I_\sigma$ by the following quantity:

$$I_\sigma \rightarrow G_\sigma = \frac{1}{j} \left[ 4\cos\,\theta\, I_\sigma - \frac{3}{2} \sum_k \frac{2 - \rho_k\,\cos\,2\theta}{2 + \rho_k} \right], \qquad (4)$$

20    where $\rho_k$ is the depolarization factor of the $k^{th}$ gas.

It must be stressed that Equation (3) utilizing either $I_\sigma$ or $G_\sigma$ is a closed form expression for $n(r)$ which makes no assumption on any analytical form by which this function may be modeled. It is exactly true for the function $I_\sigma$ defined by

5    Equation (2) or the function $G_\sigma$ defined by Equation (4). It may be noted, however, that $\sigma$ will not vary over an infinite range as indicated by Equation (3).

For example, if it is wished to use this instrument as a remote sensor on board a planetary orbiter, $\sigma$ has a

10    lower bound which will vary according to the brightness temperature of the planetary atmosphere of interest. This value of $\sigma$ is that at which the planetary radiation dominates the visible solar radiation reflected by the planet. This is because the thermal radiation from the planet surface and atmosphere system,

15    which is emitted due to the temperature of this surface and atmosphere, is not the absolute zero. Thus, on Earth, this cut-off value is approximately $0.37\mu m^{-1}$. However, although the integration indicated in Equation (3) cannot be carried out completely, and it is conceivable that in some extreme cases

20    the distribution $n(r)$ may either not be reproduced exactly or not at all, it has been discovered that an object detector designed to operate within the limits set forth hereinbefore will permit the integration to be carried out to provide the detailed spectrum of sizes (particle size distribution) in

25    equivalent spheres of the scattering particles. These limits provide a unique method which has been submitted to detailed scrutiny as to stability with regard to both inherent experimental and analytical noises.

The first computational step of forming the ratio
indicated by Equation (2) is represented by a functional block
17, and the second computational step indicated by Equation
(3) is represented by a functional block 18. The ratio can

5      be formed using analog circuits, or upon converting the detector
signals to digital form, by digital techniques. In either case,
the result of the first computational step is preferably obtained
in digital form for storage and subsequent retrieval for solu-
tion of Equation (3). The values of this ratio at the

10     several prescribed frequencies are then inserted in Equation
(3) which is subsequently solved for various values of r larger
than approximately 1μm. For example, for $r = r_1$, the equation
yields $n_1 = n(r=r_1)$; for $r = r_2$, the solution yields $n_2 = n(r=r_2)$
and so forth. The set of values $n_1$, $n_2$, ... is the desired

15     particle distribution n(r). A general purpose computer
can be used for solving Equation (3). The computer can be
used on a time-sharing basis or a special-purpose computer
could be slaved to the apparatus. The output from such a
computer is converted to an electrical signal which is then

20     displayed visually on a cathode ray tube (CRT) display 19.
Thus, a real-time visualization of the size distribution is
provided, such as for the purpose of monitoring the changes in
particle sizes that may take place as is the case, for example,
with environmental particulate pollution.

25     The effect of viewing angle, $\theta_s$, can be appreciated
from the graph of FIG. 2 which shows a true plot of particle
size distribution by a bell-shaped curved labeled "n(true)"
for comparison with particle size distribution curves determined

at viewing angles of 50 minutes, 150 minutes and 350 minutes. The distribution curve labeled "$\theta_s$ = 150 min" is found to be very close to the true distribution curve. Consequently, it is concluded that a viewing angle of about 150 min is optimum.

5　At viewing angles between approximately 100 min and 200 min, the results are still very good, although small negative tails develop close to these two values below 1.5μm radius; but beyond that range there is not only further degradation of the results from the true curve, but totally incorrect results over

10　much of the range of particle sizes. For example, at a viewing angle as small as 50 rin, the results indicate a <u>negative</u> distribution between 14 and 17μm radius, and although it seems to follow the true distribution curve as particle radius decreases, it becomes clear at below 8μm radius that the distri-

15　bution curve is totally in error (meaningless) since size distribution increases, apparently without limit, as the particle radius decreases. Deviation from the optimum viewing angle in the other direction will not produce such absurd results, as shown by the distribution curve labeled "$\theta_s$ = 350 min". But

20　still the results have so departed from the true distribution as to not be useful except perhaps in locating the peak position. Note the <u>negative</u> distribution above 11μm and below 2.7μm radius. The true distribution cannot, of course, go below zero. This demonstrates the limited range of viewing

25　angles that can be effectively used in this technique.

The effect of spectral range can be appreciated from the graph of FIG. 3. In the range of about 0.2 to 4.0μm$^{-1}$, the result is very nearly identical to the true distribution curve as shown by a curve labeled "0.198 $\leq$ σ $\leq$ 4.070μm$^{-1}$."

This result remains substantially the same if the starting value of 0.198 were to be lowered down to $0.02\mu m^{-1}$. At the lower part of the range, namely at 0.198 to $2.860\mu m^{-1}$, the form of the distribution curve remains about the same but becomes _negative_

5 at less than 2µm radius. Increasing the upper end of the range to approximately $9.00\mu m^{-1}$ produces about the same results, but the distribution curve becomes more _negative_ at less than 2µm radius. Working in a subinterval of the lower part of the optimum range, namely in the range from 0.44 to $2.86\mu m^{-1}$, the

10 result is about the same as working at just the lower part of that optimum range, except that the distribution is found to be negative below 3µm radius and above 12µm radius, with decrease of approximately 18% in the peak. Operating at only a narrow central part of the optimum spectral range, namely

15 between about 0.3 to $1.2\mu m^{-1}$ produces the absurd result indicated by the curve labeled "$0.286 \leq \sigma \leq 1.190\mu m^{-1}$." Operating below the optimum range, such as in a range from 0.03 to $0.2\mu m^{-1}$ also produces an absurd result, as shown by the curve labeled "$0.031 \leq \sigma \leq 0.235\mu m^{-1}$." Lastly, extending

20 the optimum range, for example from 1.0 to $10.0\mu m^{-1}$ also produces the absurd result shown by the curve labeled "$1.0 \leq \sigma \leq 10.0\mu m^{-1}$."

The effect of spectral resolution is illustrated in FIG. 4. Again the curve labeled n(true) is the theoretical or true particle distribution. The optimum is shown to be a

25 spectral resolution of about $0.06\mu m^{-1}$, as shown by the curve labeled "$\Delta\sigma = 0.061\mu m^{-1}$". However, spectral resolution is less critical than spectral range or viewing angle. A smaller resolution would have no deleterious effect on the result.

A larger resolution can be tolerated to about three times the optimum. There, at the resolution of $0.18\mu m^{-1}$, the results begin to degrade, and at about $0.80\mu m^{-1}$, the results become absurd as shown by the curve labeled

5  "$\Delta\sigma = 0.774\mu m^{-1}$."

The necessary spectral range with the optimum spectral resolution may be achieved by scanning frequency at the detector using a detector-array in which each detector is slaved to a specific frequency, as noted hereinbefore. Alter-

10  natively, one or more voltage variable photodetectors are used, and frequency scanning is achieved by varying the bias voltage to the detectors. For most laboratory applications, there will be a specific light source, either variable in frequency or containing all frequencies of interest. In the latter case,

15  scanning the frequencies in the desired range could be accomplishe by the use of filters. Such an arrangement would also be used outside the laboratory from a ground-based station such as for determining the size distribution of particles in the Earth's atmosphere, where light from the sun is filtered for scanning

20  the frequency of light passed through a volume of scattering particles. In the case of an orbiting satellite, on the other han it is the thermal emission from the atmosphere-surface system that would be filtered.

Although particular embodiments of the invention

25  have been described and illustrated herein, it is recognized that modifications and equivalents may readily occur to those skilled in the art and consequently it is intended that the claims be interpreted to cover such modifications and equiva-lents.