Aerodynamic Design of Electric and Hybrid Vehicles: A Guidebook

D. W. Kurtz

September 30, 1980

Prepared for
U.S. Department of Energy
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PREFACE

The Electric and Hybrid Vehicle (EHV) Research, Development and Demonstration Act of 1976, Public Law 94-413, later amended by Public Law 95-238, established the governmental EHV policy and the current Department of Energy EHV Program. The EHV System Research and Development Project, one element of this Program, is being conducted by the Jet Propulsion Laboratory (JPL) of the California Institute of Technology through an agreement with the National Aeronautics and Space Administration. An objective of the Program is to develop the technologies required by the EHV industry to successfully produce vehicles with widespread acceptance. One of those technologies requiring development is vehicle aerodynamics. This guidebook presents the tools, strategies and procedures involved in the design of aerodynamically efficient vehicles. The methodology is intended to be useful to designers possessing little or no aerodynamic training.
ABSTRACT

A typical present-day subcompact EHV, operating on an SAE J227a D driving cycle, consumes up to 35% of its road energy requirement overcoming aerodynamic resistance. The application of an integrated system design approach, where drag reduction is an important design parameter, can increase the cycle range by more than 15%. This guidebook highlights a logic strategy for including aerodynamic drag reduction in the design of electric and hybrid vehicles to the degree appropriate to the mission requirements. Backup information and procedures are included in order to implement the strategy. Elements of the procedure are based on extensive wind tunnel tests involving generic subscale models and full-scale prototype EHV's. The user need not have any previous aerodynamic background. By necessity, the procedure utilizes many generic approximations and assumptions resulting in various levels of uncertainty. Dealing with these uncertainties, however, is a key feature of the strategy.
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SECTION I
INTRODUCTION

As an automobile moves along a road surface, the resulting displacement of air gives rise to various forces and moments. Depending upon the mission, or driving cycle, the aerodynamic drag experienced by a typical electric or hybrid vehicle (EHV) may consume a significant portion of the energy supplied by the propulsion system. Since the SAE J227a D cycle has been suggested as being representative of an electric passenger vehicle mission, it is proper to consider the impact of aerodynamic design upon the total road energy requirement for that cycle. Figure 1-1 shows the cycle energy split as a function of drag area, $C_{D}A_{1}$, for a typical subcompact EHV weighing 1350 kg (3000 lb) and having a rolling resistance coefficient of 1.2% of the vehicle weight (rolling losses include those due to tires, bearings, gears, brakes, etc.). Current subcompact-class vehicles have drag areas of about 0.9 m$^2$ (9.7 ft$^2$) which means that the aerodynamic component may be responsible for about 35% of the total road energy consumed over this cycle. Because of progress recently demonstrated by the automotive industry, it is reasonable to expect that, with vigorous design efforts, a drag area of 0.55 m$^2$ (5.9 ft$^2$) may be achievable. The benefit of such a 40% reduction in the $C_{D}A$ related to an electric vehicle (EV) is shown, in Figure 1-2, to be nearly a 20% improvement in range. To achieve a similar benefit via reductions in the other components would require about a 50% reduction in the rolling resistance coefficient to 0.6% (a rather unrealistic value) or a 22% reduction in vehicle weight (the removal of an additional 300 kg from an already lightweight vehicle would be very difficult). These examples, although simplified, tend to demonstrate the potential benefits from, and justification for pursuing aerodynamic resistance reduction.

Efficient aerodynamic design is an elusive accomplishment. Automotive aerodynamics is presently at the stage aircraft aerodynamics was 50 years ago. It is, however, a fundamentally different problem since a road vehicle is a bluff body, having many local areas of flow separation, and operates in the presence of the ground. Recognizing the need and potential benefits to be derived from a clearer understanding, the SAE recently commissioned the development of an automotive aerodynamic research plan (Reference 1-1).

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1 The drag coefficient, $C_{D}$, is nondimensional and is defined as

$$C_{D} = \text{Drag Force}/(1/2 \times \text{Air Density} \times \text{Velocity}^2 \times \text{Frontal area})$$

The frontal area, $A$, is the vehicle's projected area including tires, and suspension members but excluding appendages such as mirrors, roof racks, antennas, etc. The velocity is the relative speed between the air and the vehicle.
Figure 1-1. Road Energy Component Split Over the SAE J227a Schedule D Driving Cycle

Figure 1-2. Projected Vehicle Range Over the SAE J227a Schedule D Driving Cycle as a Function of Various Parameters
This plan calls for the expenditure of 25 million dollars over a five year period in order to bring the state-of-the-art of automotive aerodynamics into line with other engineering disciplines. The sheer size and commitment indicated by such an undertaking gives one some perspective into the difficulties and uncertainties inherent in automotive aerodynamic design today.

This aerodynamic design guidebook utilizes a logic strategy for designing aerodynamically-appropriate electric and hybrid vehicles with current aerodynamic understanding. Its intended user is the vehicle designer and builder who has little or no aerodynamic background. By necessity, the procedure utilizes many generic approximations and assumptions resulting in various levels of uncertainty. Dealing with these uncertainties, however, is a key feature of the strategy.
SECTION II
APPROACH

The approach is to develop an aerodynamic design sequence composed of logical path elements which provide a strategy and guide through progressively more refined levels of design. The process of developing this logic path exposed many technological gaps and information voids inherent in various path elements. In the course of this endeavor, studies and test programs were undertaken in order to alleviate the uncertainties and to provide the necessary tools and procedures required to implement the strategy.

A limited aerodynamic data base was developed by wind tunnel testing 20 electric, hybrid and subcompact vehicles (Reference 2-1). These results were used to extend, develop and refine drag prediction techniques; to develop generalized relationships between drag and yaw angle (the angle between the relative wind and the longitudinal axis of the car); and to quantify the uncertainty in subscale-to-full-scale wind tunnel test correlations.

Because of battery packaging requirements, EHV's may be subject to somewhat different constraints than conventional internal combustion (IC) engine vehicles. For instance, owing to the use of a central battery tunnel, a small vehicle may be unusually wide or long. A series of subscale tests was therefore performed to determine if aspect ratio and fineness ratio were important aerodynamic parameters.

Since any road vehicle rarely operates in a zero-wind environment, an analysis of the driving cycle-dependent effects of ambient winds on vehicle drag was performed. This is a necessary extension to aerodynamic drag evaluations and should be included in vehicle computer and dynamometer simulations.

Finally, it was necessary to evaluate simplified general aerodynamic design principles in order to determine the confidence levels resulting from their application.

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1 Aspect ratio (AR) is defined as body height divided by width, and fineness ratio (FR) as length divided by effective diameter (of equivalent area circle).
SECTION III

AERODYNAMIC DESIGN LOGIC PATH

The logic sequence incorporates path elements which terminate at one of three levels of design. These design levels are progressively more refined and are successively characterized by a higher probability of yielding a low drag design. This logic path, then, defines the procedural elements required for the design of an aerodynamically efficient EHV. Technical backup information is supplied in the various appendixes in order to facilitate applying the procedures.

The strategy which governs the use of these procedures originates in the development of a design acceptability criterion. Consider the design logic path beginning in Figure 3-1. Note that the initial steps are the definition of the mission use or cycle requirements, and the resulting determination of the aerodynamic acceptability criterion. This is the heart, the driver, of the entire process. It is imperative that one carefully characterize the mission performance objectives for which the vehicle is being designed at the outset. Once this is established, a thorough trade-off analysis must be made in order to determine the relative sensitivities of the various physical parameters. The result of such a procedure is analogous to that presented in Figure 1-2. There, the mission performance objective was to maximize range over the SAE J277 Schedule D driving cycle and the resulting sensitivity analysis was

Figure 3-1. Aerodynamic Design Logic Path, Level I
performed (using a simple vehicle computer simulation) around a postulated baseline vehicle. It should be emphasized that these sensitivity relationships are a strong function of the mission requirements.

For instance, if one were designing a postal vehicle or milk delivery truck whose mission is characterized by numerous starts and stops and virtually no constant or high speed cruising, the energy efficiency (or range) would be almost independent of the aerodynamic drag. On the other hand, if a high-speed commuter vehicle characterized by relatively few stops is being designed, the range is a very strong function of the aerodynamic drag. After these parametric sensitivities have been determined for the design mission, a target value and tolerance limit for the vehicle's aerodynamic drag may be established. This becomes the "acceptability criterion" against which various designs will be evaluated throughout the remainder of the procedure.

A. LEVEL I DESIGN

The first level of design (Figure 3-1) focuses primarily on the gross and superficial design processes characteristic of a designer's sketchbook. This may be called a subjective design analysis and is an essential beginning to any design process. First, the packaging layout and vehicle envelope must be determined. For IC engine vehicle design, this is influenced primarily by the passengers, payload and drivetrain volume requirements. For electric vehicles, the significant additional volume required for the traction batteries could impact the normal body proportions to such a degree that any first order aerodynamic influence needs to be addressed. That is, with the use of a central battery tunnel, a small car may be unusually wide; or with batteries located beneath seats (or under the floorboard), the vehicle may be unusually tall. The aerodynamic consequence is such that the specific effects of aspect ratio and fineness ratio can be identified and should be considered. Subscale tests were conducted on a family of automotive shapes in order to quantify their influence on drag. The generic trends and relationships appear in Appendix A. After iterating this trade-off within the bounds of the design theme and utility requirements, the next path element may be addressed. This is characterized as a general review and understanding of the sources of automotive drag and some of the basic principles involved in efficient aerodynamic design. A brief treatise on the subject appears in Appendix B.

With the packaging envelope and general aerodynamic guidelines in hand, the first body design sketches can begin to evolve. As a styling theme is developed and refined, the final sketches are reviewed and, after several iterations, proposed design drawings are

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1 The sensitivity analysis can be done for other performance objectives as well (e.g., acceleration, gradeability, etc.).
selected. The aerodynamic acceptability criterion, determined in the first steps, is now applied. Note that no quantitative aerodynamic analysis has been performed to this point; therefore, there is considerable uncertainty as to the value of the drag coefficient represented by this design. The probability of it being an exceptionally low-drag design is quite small. If, however, the sensitivity analysis performed earlier indicated a weak dependence of the performance objective (e.g., range) on the drag level, the large uncertainty may be perfectly acceptable. That is, there would be no justification for refining the aerodynamic design any further, and the Level I design would yield a vehicle having "appropriate aerodynamic design" commensurate to its mission. If, on the other hand, the sensitivity analysis had indicated a stronger dependence on drag level and the resulting acceptability criterion had required that the drag coefficient be no greater than, say 0.5, then Level I Design, with its characteristically large uncertainty, would be unacceptable. If such were the case, continuation to the next level of design would then be required.

B. LEVEL II DESIGN

The second level of design (Figure 3-2) can be described as an empirical design analysis utilizing procedures and practices which are generically effective. The final sketches resulting from the Level I design procedures become a baseline or strawman design for the Level II analysis.

![Aerodynamic Design Logic Path, Level II](image)

Figure 3-2. Aerodynamic Design Logic Path, Level II
Drag prediction for automotive shapes is generally unreliable in an absolute sense; its real value lies in the possibility of highlighting various drag producing elements. These drag prediction procedures (Appendix C) are a drag buildup approach (References 3-1, 3-2, and 3-3). That is, the vehicle is divided up into about a dozen regions and the drag contribution from each region is then determined by examining the local shape characteristics. By noting the relative magnitude of various drag elements, those regions deserving of more attention are identified. Any necessary modifications can be factored in and reevaluated in an iterative manner.

A general principle associated with low-drag vehicle design is the desirability of maintaining attached flow. Regions of separated flow give rise to pressure drag increments. Even if it remains locally attached, each time the flow bends in order to follow a body contour, it gives up a portion of its kinetic energy. Because of the resulting momentum loss, the successful negotiation of subsequent contours becomes less probable and the onset of separation at some other marginal point on the vehicle is more likely to occur. For these reasons, it has been postulated (References 3-4 and 3-5) that the drag produced by a vehicle moving through a fluid may be reduced by minimizing the body contour gradients. A possible corollary to that premise is that the rate of change of vehicle cross-sectional area with longitudinal station is representative of the integral of all the local body contours. Adopting that premise, the "area distribution" procedure (Appendix D) is applied to the streamlining a plot of cross-sectional area versus longitudinal station at about 10-cm intervals. Those regions where the area is rapidly changing are candidates for subtle modification. Certain unavoidable lumps and bumps occur in the neighborhood of the tires and wheelhouses, but some smoothing may be possible in the transition regions.

Since a vehicle rarely operates in a zero-wind environment, the instantaneous drag coefficient is a function of the local relative yaw angle. Therefore, knowledge of the drag versus yaw characteristic is required. A general equation describing this relationship as a function of generic vehicle shape parameters (developed from References 2-1 and 3-6) is presented in Appendix E. The effective drag experienced by a vehicle can be evaluated by figuratively driving the vehicle over a prescribed velocity-time schedule in the presence of a time-variant wind which is statistically probable from any direction (Reference 3-2). The resultant combination of the vehicle velocity and wind vector distribution yields an instantaneous yaw angle with respect to the vehicle. With the vehicle's drag-yaw characteristic known, the resultant drag may be determined at each instant. Therefore, the energy required to overcome aerodynamic resistance can be calculated by integrating the instantaneous aerodynamic power required over the cycle. It is then possible to determine what constant drag coefficient would have been necessary in order to yield the same result. The ratio of this new effective coefficient, $c_D$, to the original zero-yaw drag coefficient $c_D^0$ is...
(C_D_o) is the wind weighting factor, F. A simplified procedure for calculating F is presented in Appendix F.

Relative to the result of Level I Design, the uncertainty band associated with this Level II effective drag coefficient prediction is considerably narrowed. One should expect that, at the conclusion of the Level II analysis, the drag prediction uncertainty band will be of the order of ±15%. That result is again evaluated according to the previously-developed acceptability criterion. If the design requirements are satisfactorily met, then the Level II Design represents an "appropriate aerodynamic design" and the process is complete. If either a lower drag value or less uncertainty is demanded by the acceptability criterion, Level II design is inadequate, and one must continue on to a further level of design refinement.

C. LEVEL III DESIGN

The third and most-refined level of design is an experimental process relying heavily on insight and experience. Persons having some knowledge of experimental automotive aerodynamic techniques should be involved (e.g., a consultant) or little can be gained by this process. In addition, a relatively large financial commitment must be undertaken in order to proceed. Up to this point, no procurements have been required, no hardware has been created and the total effort expended has been a few man-months. Building models and performing developmental wind tunnel tests may increase these aerodynamic design related costs by a factor of 10 or more. If that level of expenditure is warranted, Level III Design should be initiated (Figure 3-3).

Utilizing the results of the Level II design process, a subscale wind tunnel model is constructed. Since the objective of these tests is to fine tune the design, a model with the capability of incorporating subtle changes is required. A special clay surface laid on a rigid substructure has proved to be the most practical approach. The model scale and support details are functions of the specific wind tunnel being used. Quarter to three-eighths scale have been the most popular. It is highly recommended that the level of model detail and scale fidelity be guided by an automotive aerodynamicist and the construction be performed by professional model builders with specific wind tunnel experience. Improperly-constructed models can yield misleading results, or even worse, disintegrate due to the airloads experienced in a wind tunnel.

In order to minimize controversial wind tunnel wall corrections, the model scale should be chosen such that the model cross-sectional area be no more than 5% of the tunnel cross-sectional area (above the ground plane).
BUILD MODEL

TO SUCCESSFULLY PROCEED REQUIRES SOME EXPERIENCE IN AUTOMOTIVE AERODYNAMICS

WIND TUNNEL TESTS

DRAG PREDICTION AND UNCERTAINTY

ACCEPTABLE?

LEVEL III DESIGN

MODEL TUNING

MAJOR MODEL CHANGE REQUIRED?

Figure 3-3. Aerodynamic Design Logic Path, Level III

A minimum of 15 to 20 wind tunnel occupancy hours will be required for testing of the preliminary model in original and slightly-modified forms (sometimes called, "aerodynamic tuning"). This is in addition to initial shakedown runs to check out the model construction, verify that the data acquisition and tunnel systems are operating properly and to quantify the effects of Reynolds Number (sensitivity of aerodynamic coefficients to air speed). Usually, the effect is small and a convenient tunnel air speed\(^1\) can be adopted for the most of the test. If a real-time data reduction system is provided, the model drag coefficient can be continuously monitored. Tests should be performed at yaw angles up to about 40 degrees in order to develop the information necessary for the wind weighting analysis (Appendix F). Applying factors to account for subscale to full-scale correlations,\(^2\) a drag prediction and associated uncertainty may be determined. The acceptability criterion is applied as described earlier.

If the criterion were immediately satisfied at this point, the design process could be concluded. However, the expense and effort committed to model testing plus the ever present uncertainty band (due largely to unavoidable body panel surface misalignments in the

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\(^1\) The speed should be high enough to get good resolution on the loads being measured (a function of the balance system).

\(^2\) This is a function of the model level of detail and the particular subscale wind tunnel and data reduction procedures. Calibration models are currently being tested in all the major subscale and full-scale tunnels in the country (and abroad).
production vehicle) warrants some further testing. For instance, since stabilized flow attachment is an attribute of low drag designs, a means of observing local surface flow behavior is desirable.

- Several methods exist and each has advantages and disadvantages. Attaching rows of soft, flexible yarn tufts is simple, inexpensive, easy to photograph and effectively highlights flow instabilities; it does, however, modify the surface detail by its very presence and can consequently affect the absolute level of the data. An alternative is the use of ink drops (or other visible fluids) which, when placed on the surface spread out and indicate the path of the streamlines on the vehicle surface with very little flow interference; the disadvantages of the technique are its transient nature, gravity effects as the droplet spreads along the body side and the mess. Seeding the airflow with smoke or particulates is another approach. This usually has many tunnel operation considerations which may prove unsatisfactory. Often, the ink drop approach is preferred on clay models since tuft attachment may be difficult. Flow separation and instabilities are easily identified. With a combination of engineering judgment and artistic style, the clay surface is iteratively altered in order to develop a smooth, stable flow pattern. It is extremely important to document each alteration with pictures, measurements and templates, as it is often necessary to return to an intermediate configuration before continued progress can be made. Front underbody air dams (chin spoilers) and rear deck spoilers (lips) can often provide beneficial results if properly designed and located (References 3-8 and 3-9). A good candidate device should be effective through a reasonable range of yaw angles. Drag data should be continuously monitored in order to help guide the process. If, after repeated attempts, large areas of flow separation still exist, major model contour or shape modifications may be necessary. If the flow is everywhere stabilized and the rear separation point is such that the wake size is minimized, further significant drag reduction is unlikely. Pressure taps may be installed in the surface of the model in order to optimally locate the inlets and exits for interior ventilation. If high-mass flow ram air is required for motor or engine (hybrid) cooling, it would be wise to construct a model with properly scaled internal flow path ducts. Not only is there a drag component associated with the internal flow losses, but the condition may significantly alter the flow over the outer surface of the vehicle as well.

Little more can be accomplished in model scale. Owing to local Reynolds number, scale fidelity and flow conditions, the absolute drag levels measured in test are rarely substantiated in full-scale tests on the prototype or production vehicle; full-scale test results are often 10 to 20% greater (Reference 3-10), thus contributing to a rather large uncertainty even at this point. Experience and correlations from previous subscale and full-scale tests in the same

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1Because model installation and setup is not a trivial matter, tunnel test time is usually contracted for a 6-8 hr minimum.
facilities can reduce the uncertainty to about +5%. As an ultimate step, aerodynamic tuning on a full-scale replica may be considered. The expense involved in building a single-purpose wind tunnel model may not be warranted; however, a full-scale mock-up or male buck might be suitably altered for test purposes. To make that step worthwhile, special attention should be paid to the underbody and internal flow details.

D. CONCLUDING REMARKS

This process should not be considered to be a mindless formula for success. Rather, it is a framework upon which the design development is built. The procedures are highly dependent upon many subjective determinations which rely heavily upon common sense and experience. There may be many alternative solutions to the same set of design requirements.

The objective behind the creation of the design guide is to encourage EHV designers to address aerodynamic drag as an important design parameter; and once goals are targeted, to systematically evolve a design which is aerodynamically matched to the anticipated mission while minimizing unnecessary effort.

1Unlike high-speed sports and competition vehicles which rely heavily on aerodynamic forces for such things as traction and stability, the conventional road vehicle is primarily concerned with the drag component. This is not the say that the other five aerodynamic components are not of interest, but unless unusual operational conditions are anticipated, low drag optimization is usually pursued without compromise.
SECTION IV
REFERENCES


SECTION V

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Road Testing
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APPENDIX A

EFFECTS OF ASPECT RATIO AND FINENESS RATIO ON
THE AERODYNAMIC CHARACTERISTICS OF AUTOMOBILE SHAPES

Because of their special battery packaging requirements, electric vehicles may not be subject to the same design constraints as conventional IC engine vehicles. For instance, owing to the use of a central battery tunnel, a small vehicle may be unusually wide or long. A series of tests was therefore performed in the CALCIT 10 foot wind tunnel (Caltech) to determine if aspect ratio or fineness ratio\(^1\) was an important aerodynamic parameter, and further, whether one can generalize the effect of either or both in combination for simplified automobile shapes.

These tests were exploratory in nature and intended to determine what, if any, trends would appear. The initial tests involved both a sharp-edged and a round-edged basic model (Figures A-1 and A-2), in order to quantify the effect of local flow separation on the observed aerodynamic trends.

The parameters varied were height, length, width, and ground clearance; Figure A-3 illustrates the model construction technique. Three variations were available for each of the four parameters. Figure A-4 illustrates the drag trends demonstrated by highly separated (sharp-edged model) and highly attached (round-edged model) flow situations at low to moderate fineness ratios. As one might expect, for very short vehicles, the drag is reduced with increasing fineness ratio. This is probably due to a reduction in the form drag component (see Appendix D, Part D) at the expense of a small increase in surface friction drag. Owing to local separation points, the drag gradient is not as large for the sharp-edged model as for the round-edged, but the trend is not significantly different. Subsequent tests involved only the round-edged model.

The effects of ground clearance were found to be significant with these smooth-underbody models (see Figure A-5). This also presents a problem in data presentation since the manner by which the ground clearance is nondimensionalized can distort the effects of aspect and fineness ratios. For instance, if the ground clearance is nondimensionalized by body width and the aspect ratio is varied by changes in body width \((g/W)\) ground clearance changes with aspect ratio and dominates the whole effect. Similarly, ground clearance nondimensionalized by body length \((g/L)\) will dominate the effects of changes in fineness ratio. For these reasons, two ground clearance parameters, \(g/L\) \(g/W\), are used when evaluating the effects of aspect and fineness ratios, respectively.

\(^1\)Aspect ratio (AR) is defined as body height (not including ground clearance) divided by width, and fineness ratio (FR) as length divided by effective diameter (of equivalent area circle).
Figure A-1. Basic Sharp-Edged Model Mounted in GALCIT Wind Tunnel

Figure A-2. Basic Round-Edged Model Mounted in GALCIT Wind Tunnel
Figure A-3. Some of the 56 Pieces Used to Alter Aspect and Fineness Ratios

Figure A-4. Drag Coefficient vs. Fineness Ratio for Sharp-Edged and Round-Edged Automobile Shapes (g/W = 0.15, Ground Clearance = 15% of Body Width)
The effect of aspect ratio on drag is shown in Figure A-6 at two levels of ground clearance representative of present day automobiles (g/W = 5%) and vans (g/W = 8%). In both cases, the drag usually increases with aspect ratio (short and wide has some advantages over tall and narrow), being more pronounced at the highest fineness ratio (longest vehicle). For high-ground-clearance vehicles, there seems to be a weak aspect ratio effect up to about AR = 0.8; beyond that point, the drag increases significantly.

The effect of fineness ratio (Figure A-7) is a little more confusing in that the trends with constant aspect ratios are not as internally consistent. Note also, that the two ground clearances representing "automotive (g/W = 10%) and van-like (g/W = 20%)" are nondimensionalized by body width for the reasons explained earlier. In general, the trend is consistent with Figure A-4 which covered the very low fineness-ratio end of the spectrum. However, as the fineness ratio is increased, significant drag reduction ceases and the drag actually begins to increase beyond a fineness ratio of 2.7 at the higher ground clearance. This may indeed be the result of a rapid buildup of the surface friction drag component (see Appendix B, Part B), which may be magnified in the underbody region at high ground clearances.
Figure A-6. Drag vs. Aspect Ratio at Two Ground Clearances

Figure A-7. Drag vs. Fineness Ratio at Two Ground Clearances
In summary, these results indicate that there are aspect and fineness ratio effects on vehicle drag that warrant consideration during initial design stages when packaging requirements are being developed.
APPENDIX B

FOUNDATIONS OF AERO_DYNAMIC DESIGN

The purpose of this section is to familiarize the EHV design engineer with certain basic concepts related to automotive aerodynamics. First, the historical development of the automobile, from an aerodynamic perspective, is briefly reviewed. Next, the generally accepted "sources of drag" are identified, ranked by importance and described by example. Finally, a limited aerodynamic data base, developed by wind tunnel testing 20 electric, hybrid and subcompact vehicles, is presented in order to orient the design engineer with the state of the art.

A. HISTORICAL DEVELOPMENT

Although many of the principles involved in low-drag designs have long been known, the drag coefficient of the average production car in the early 1920s was about 0.8. By 1940 it had dropped to about 0.6 and by 1960 to about 0.5 (see Figure B-1). Further improvement has come slowly, especially in this country, and the average drag coefficient of domestic automobiles actually increased slightly (to about 0.55) in recent years with the trend toward more formal styling with less rounding of edges. Most recently, however, the pressures brought by federally mandated fuel economy requirements have sparked renewed interest in reducing aerodynamic losses. In Europe, the current average production car drag coefficient is somewhat lower, about 0.46. Drag coefficients as low as 0.15 were reported as early as 1922 by W. Klempner (Reference B-1) on an elongated tear-drop automobile model. A. Morelli in 1976 (Reference 3-5) developed (in full-scale mock-up) a body shape encompassing reasonable four-passenger compartment and engine cooling airflow with a drag coefficient of 0.172. Daimler-Benz recently unveiled the new experimental Mercedes C-111/3, a turbodiesel which set several speed records and is reported to have a drag coefficient of 0.195 (Reference 6-2). Perhaps the lowest recorded drag coefficient for a real ground vehicle is 0.12 for the Goldenrod, which holds the land speed record for wheel-driven vehicles (Reference B-3). It appears, then, that there exists a rather large gap between the drag level of today's automobile and what is theoretically possible as demonstrated by some of these very specialized vehicles. Obviously, there are many practical constraints on production automobiles which compromise efforts to achieve low drag levels. However, the hope of eventually cutting present-day production car drag levels nearly in half may not be completely unrealistic.
9. SOURCES OF DRAG

The actual mechanisms of automotive drag production are not at all well understood. Automotive aerodynamics is characterized by ground interference and large areas of separated and vortex flow. Unlike aircraft aerodynamics, it is largely unresponsive to classical analytical treatment. It has therefore become a rather empirical science, relying heavily on development through wind tunnel test techniques. Reference B-4 and others break down the sources of drag into five basic categories: (1) form drag, (2) interference drag, (3) internal flow drag, (4) surface friction drag, and (5) induced drag. A simple schematic depicting their relative importance for an IC engine car is presented in Figure B-2.

Figure B-2. Distribution of IC Engine Vehicle Aerodynamic Drag (Reference B-4)
Form drag (sometimes called profile drag) is a function of the basic body shape. Bodies which minimize the positive pressure on the nose and the negative pressure on the tail will exhibit lower form drag. For example, a flat plate positioned normal to the flow would represent a worst case, whereas a streamlined teardrop shape would be characteristic of minimum form drag.

Interference drag develops as the flow over the many exterior appendages of a vehicle body interacts with the flow over the basic shape or the flow due to the constraining influence of the ground. Various component projections such as a hood ornament, windshield wipers, radio antenna, external mirrors, door handles, luggage rack, rain gutters, and underbody protuberances all contribute to the interference drag component. For example (Reference B-4), an external mirror in a free airstream may have a drag force of 4 newtons. In close proximity to the vehicle body where the local airflow is accelerated by 25-30%, the drag on the mirror may be 6.4 newtons—a 60% increase! Since an external mirror usually has a large flat aft end, it spreads a turbulent wake behind it which disturbs the basic flow on the side of the vehicle, adding a further drag increment. Projecting elements usually cause less interference on high-drag body shapes than on low-drag bodies. Since a high-drag body is usually characterized by extensive regions of separated flow, many of these elements are hidden in the already disturbed flow pattern. Conversely, the low drag of an efficient body is the result of a high degree of flow attachment. That condition is usually tenuous and any projection from the surface may cause separation. The underbody projections are some of the prime offenders as the installation of a smooth belly pan has demonstrated many times (Reference 3-8). In the case of electric vehicles the traditional arguments against using a smooth belly pan—such as ease of maintenance, safety (oil drippings, etc.), and engine cooling restrictions—may not apply.

Internal flow drag arises because air is required to move through the vehicle as well as around it. A conventional water-cooled IC engine requires a substantial amount of radiator airflow. Typically, the flow path is highly inefficient as local stagnation areas develop in the engine compartment and the exit path is filled with struts, hoses, brackets, and suspension elements. Here again, an electric vehicle may have an inherent advantage since its cooling requirement may be an order of magnitude less. However, ventilation of the passenger compartment is an important comfort and noise consideration, and care must be taken to design and locate the inlets and exits properly. The conventional approach is to place a flush inlet in a relatively high pressure region (usually at the base of the windshield) and either place exits in a low pressure region around the rear window or rely on normal body leaks. Unless a scoop is placed out in the flow (in which case there is an interference drag component), the drag increment due to normal occupant ventilation requirements is negligible.
Surface friction drag results from the boundary layer which is formed as air moves along a surface. Owing to viscous friction forces, the velocity gradient normal to the surface gives rise to a shear layer. The surface finish or small imperfections, and the size of the area exposed to the flow, determine the level of this drag component. Production car finishes (surface grain size of 0.2 to 0.5 mils) are well below the critical level where additional smoothness would reduce the local friction. A smooth, continuous surface keeps skin friction low. As the flow moves rearward along a body it continually loses energy and separation is more likely to occur in critical areas. Window frames, gaps, mismatched parts, and normal skin friction all contribute to cause a buildup of the boundary layer, leading to separation, more turbulence and increased drag.

Induced drag arises from the formation of longitudinal trailing vortices generated by the pressure differential between the vehicle's underbody and roof. The energy required to generate and support this vortex field is related to the energy consumed by induced drag. Often termed "lift-induced" drag or drag due to lift, there is now real doubt that any simple relationship between lift and induced drag exists (Reference 3-4). It can normally be minimized by careful attention to design detail on the rear portions of the vehicle, but this usually requires an experimental approach.

C. AERODYNAMIC DATA BASE

Very little reliable aerodynamic data on conventional automobiles and virtually none on special electric or hybrid vehicles is available in the public domain. The automobile manufacturers, both foreign and domestic, have generated a great deal of aerodynamic information for IC engine vehicles but it remains largely proprietary. Most of the available data is from subscale wind tunnel tests of questionable or unknown origin. Here lies a basic problem with random wind tunnel data: it is usually not reliable nor directly comparable to other test results. Owing to such factors as scale, level of detail (internal flow paths, undercarriage, etc.) flow conditions, and data reduction procedures, the absolute values of the coefficients are of limited value. The difference in measured drag between a "reasonably detailed" scale model and the full-sized production vehicle is often 20% or greater. The same automobile tested in two different wind tunnels may yield drag results which differ by 10%. The various tunnel wall corrections alone can modify the drag by 10%. To maximize its usefulness, a data base must be generated at the same model scale, in the same wind tunnel under the same conditions, and be handled using identical data reduction procedures. The relative effects represented by the data base should then be sufficiently reliable for design use. Correlations with road test results can help to establish a confidence level for the absolute values.

With this background in mind, it was determined that the development of an EHV aerodynamic data base should be initiated by performing full-scale tests in the Lockheed-Georgia Low-Speed Wind
A Request for Quotation (RFQ) was prepared and sent to 25 owners or developers of electric or hybrid vehicles asking for the use of a vehicle for aerodynamic characterization testing during a specific time period. Nine bids were received before the RFQ closing date. Among the selection criteria used were:

1. Availability.
2. Compatibility with wind tunnel balance system.
3. Aerodynamic interest.
4. Loan and transportation fees.

Four vehicles were selected by this process. In addition, three electric vehicles were loaned by the NASA Lewis Research Center. One was loaned by South Coast Technology and three were available at JPL. To supplement the group, several conventional IC subcompacts were borrowed from local dealerships and individuals. In three cases, a facsimile of an IC engine/EHV conversion was substituted.

These vehicles are described in Table B-1 and shown in Figure B-3. Forty-eight vehicle configurations were investigated in the course of the testing to quantify the effects of such things as open windows, attitude changes (due to loading) and pop-up headlights (References 2-1 and 3-10 contain more detailed information on this as well as other aerodynamic force and moment components). The zero-yaw drag coefficients of all 20 vehicles in their "standard" configurations, their frontal areas and drag-area products are also included in Figure B-3. When the yaw characteristics are considered (effects of ambient winds), the relative values change slightly (Reference 2-1). See Appendix F.

The vehicles were mounted on the external balance by means of a four-point support system. No attachment was required; the wheels merely rested on the four pads with the parking brakes locked. The friction between the tires and the pads was normally sufficient to maintain model position. In certain cases, chocks were placed behind the tires. Because of the extremely short wheelbases of some of these electric vehicles, it was necessary to use pad extensions. These raised the position of the vehicle in the tunnel by approximately 3 centimeters. To quantify the effect of this position change, tests were made using spacers with a few of the vehicles that were capable of using the unmodified pads. Elevating a vehicle in this manner appeared to increase the measured drag by 1-2% over the entire yaw range.

All tests were performed at 88 kph and the yaw angle (ψ) was varied through ±40 degrees. Runs were also made on all vehicles with the two front windows open. Some tests of IC engine cars were run with radiators both open and blocked.
D. OBSERVATIONS

It is difficult to make universal statements about the data since, in automotive aerodynamics, broad generalizations usually prove to be unreliable. There are many subtle details characteristic of each vehicle which affect the local flow conditions and hence, the forces and moments. To state that vehicles of a particular class all exhibit predictable aerodynamic traits is risky at best. Nevertheless, certain features characteristic of this data base will be highlighted in what follows. In addition, a simplified procedure for accurately determining the effects of statistically varying ambient winds on a vehicle's drag is presented (and applied to this data base) in Appendix F.

Drag

It is interesting to note that the selected vehicles represent a range of zero-yaw drag coefficients from 0.308 to 0.583. Further, the highest value (least aerodynamically efficient) of the group was the Kaylor open roadster followed closely by the boxy Otis van; however, the HEVAN drag coefficient was nearly 15% less at 0.497 despite its boxy lines. Another interesting result was that the Horizon's drag coefficient was over 18% lower than the Chevette's even though they are very similar in shape.

General Electric's ETV-1 and Centennial have drag valves significantly lower than the rest of the group—a probable result of the importance of aerodynamics in the design theme and subscale wind tunnel testing.

Windows Open/Closed

Because of their current limited energy capacity, electric vehicles will not immediately be able to afford the luxury of an active air conditioning system; it is therefore reasonable to expect that they will be operated in a windows-open configuration over a significant portion of their lifetime. As previously discussed, open windows adversely affect the slope and ultimate magnitude of the drag-yaw curves. Curiously, open windows may or may not increase the drag at zero-yaw angle. In fact, four vehicles (Honda Civic Sedan and Wagon, HEVAN, and the Chevrolet Corvette) actually had a lower zero-yaw drag with their front windows open than when closed (almost 4% lower on the Civic wagon). This situation was previously observed while performing precision coast-down testing on a 1975 Chevrolet Impala (Reference 3-8). Although they reported this result, the authors were uncomfortable with it, and desired further investigation. The present data seems to confirm that the circumstance can and does occur. However, it should be noted that a vehicle operates at some angle of yaw (wind-induced) over most of its

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1The relative drag levels of the cars tested in the Lockheed-Georgia wind tunnel must not be taken as typical of all their manufacturer's products.
lifetime; therefore, the effect of open window operation is a net increase in the vehicle's drag of approximately 3 to 5% (depending upon the driving cycle and wind speed - see Appendix F).

Ground Clearance

There is a natural boundary layer (velocity gradient) growth along the wind tunnel floor resulting in a thickness of about 15 cm (6 in.) at the test section midpoint for the Lockheed-Georgia wind tunnel. Since several of the short wheel base vehicles had to be mounted on raised/cantilevered plates (approximately 3 cm above the floor), a brief check was made to quantify the effect. The Chevette had a wheelbase length which made it possible to mount it either on the flush balance pads or on the cantilevered plates. Tests were performed in both positions with all other parameters unchanged. The effect of raising the vehicle was to increase the drag by from 1% to 2% over the entire yaw range. Certainly, one would expect there to be some increase since the vehicle is moving further out into the undisturbed freestream flow. It is believed that the effect observed with the Chevette is probably typical for the other vehicles tested on the cantilevered plates. It should be noted, however, that the data presented for these vehicles have not been corrected for this effect. The vehicles are: (1) Honda Civic Sedan, (2) Honda Civic Wagon, (3) Ford Fiesta (here the mounting procedure resulted in only a 1 1/2 cm elevation and the effect is expected to be less than 1%), (4) CDA Town Car, (5) Sebring-Vanguard Citicar, and (6) the Zagato Elcar.

Radiator Airflow

It has long been recognized that, for conventional automobiles, radiator airflow is a major source of aerodynamic drag. A great deal of effort has gone into developing designs which accomplish the engine cooling task while minimizing the detrimental aerodynamic effects (References B-3, B-6 and B-7). An all-electric vehicle, however, does not have a motor cooling requirement of similar magnitude and therefore should possess an inherent advantage in this respect. In an effort to quantify the benefit, two vehicles (the Chevette and the Corvette) were tested with their radiators both open to airflow and blocked. The blocking was accomplished by simply covering the grille, and other radiator inlet areas, with flexible sheet plastic held firmly in place with duct tape; all related body contours remained undisturbed. The Chevette with an open radiator exhibited about 7-8% higher drag than when the radiator was blocked. This increment was approximately constant across the yaw range, but the asymmetry was exaggerated with the open radiator. The Corvette had a 6 1/2% drag increase when open compared to blocked; this comparison, however, was made at zero yaw only. It is anticipated that the radiator drag increment might be different for each vehicle, and had time permitted, this would have been investigated. In summary, however, if an IC engine vehicle were converted to electric power and the radiator airflow were eliminated, one could expect a drag benefit of from 5 to 10%.
Table B-1. Data Base Vehicles

<table>
<thead>
<tr>
<th>Figure</th>
<th>Vehicle</th>
<th>Type</th>
</tr>
</thead>
<tbody>
<tr>
<td>a</td>
<td>General Electric Co.: ETV-1</td>
<td>4-passenger electric commuter</td>
</tr>
<tr>
<td>b</td>
<td>Garrett AiResearch Co.: ETV-1</td>
<td>4-passenger electric commuter</td>
</tr>
<tr>
<td>c</td>
<td>General Electric Co.: Centennial Electric</td>
<td>4-passenger electric commuter</td>
</tr>
<tr>
<td>d</td>
<td>Copper Development Association: Town Car</td>
<td>2-passenger electric commuter</td>
</tr>
<tr>
<td>e</td>
<td>South Coast Technology: Electric Rabbit</td>
<td>2-passenger electric commuter</td>
</tr>
<tr>
<td>f</td>
<td>Sebring-Vanguard: Citicar</td>
<td>2-passenger electric commuter</td>
</tr>
<tr>
<td>g</td>
<td>Zagato: Elcar</td>
<td>2-passenger electric commuter</td>
</tr>
<tr>
<td>h</td>
<td>Jet Industries: Electra Van 600</td>
<td>Electric delivery van</td>
</tr>
<tr>
<td>i</td>
<td>Otis Elevator Co.: Otis P-500A Van</td>
<td>Electric delivery van</td>
</tr>
<tr>
<td>j</td>
<td>Kaylor Energy Products: Kaylor GT</td>
<td>2-passenger hybrid-electric open roadster</td>
</tr>
<tr>
<td>k</td>
<td>Energy Research and Development Corp.: HEVAN (Hybrid Electric Van)</td>
<td>Hybrid-electric delivery van</td>
</tr>
<tr>
<td>l</td>
<td>American Motors Corp.: 1978 Pacer Station Wagon</td>
<td>Internal combustion engine</td>
</tr>
<tr>
<td>m</td>
<td>American Motors Corp.: 1978 Pacer Sedan</td>
<td>Internal combustion engine</td>
</tr>
<tr>
<td>n</td>
<td>General Motors Corp.: 1967 Chevrolet Corvette</td>
<td>Internal combustion engine</td>
</tr>
<tr>
<td>o</td>
<td>General Motors Corp.: 1973 Oldsmobile Delta 88</td>
<td>Internal combustion engine</td>
</tr>
<tr>
<td>p</td>
<td>General Motors Corp.: 1978 Chevrolet Chevette 4-door</td>
<td>Internal combustion engine</td>
</tr>
<tr>
<td>q</td>
<td>Chrysler Corp.: 1978 Plymouth Horizon 4-door</td>
<td>Internal combustion engine</td>
</tr>
<tr>
<td>r</td>
<td>Honda Motors: 1978 Civic Sedan</td>
<td>Internal combustion engine</td>
</tr>
<tr>
<td>s</td>
<td>Honda Motors: 1978 Civic Wagon</td>
<td>Internal combustion engine</td>
</tr>
<tr>
<td>t</td>
<td>Ford Motor Co.: 1978 Fiesta</td>
<td>Internal combustion engine</td>
</tr>
</tbody>
</table>

**Table Notes**

1. This production IC engine Pacer Wagon represented a reasonable facsimile of the Electric Vehicle Associates "Change of Pace" converted electric Pacer Wagon.

2. This production IC engine Corvette represented a reasonable facsimile of the Cutler-Hammer Electric '67 Corvette of Santini. The front grille was blocked in order to eliminate the radiator losses, which are not present in the electric version.

3. This production IC engine Delta 88 was a reasonable facsimile of the proposed National Motors Hybrid-Electric Gemini II. Here the radiator was not blocked since the hybrid vehicle would retain its V-6 engine and cooling system.
<table>
<thead>
<tr>
<th></th>
<th>CD₀</th>
<th>A, m²</th>
<th>CD₀A, m²</th>
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</thead>
<tbody>
<tr>
<td><strong>GE ETV-1</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>CD₀</td>
<td>0.308</td>
<td>1.840</td>
<td>0.567</td>
</tr>
<tr>
<td><strong>Garrett ETV-2</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>CD₀</td>
<td>0.395</td>
<td>2.028</td>
<td>0.801</td>
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Figure B-3. Vehicles Tested in the Lockheed-Georgia Low-Speed Wind Tunnel
<table>
<thead>
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<th>A, m²</th>
<th>CD₀A, m²</th>
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</thead>
<tbody>
<tr>
<td>0.337</td>
<td>1.851</td>
<td>0.624</td>
</tr>
</tbody>
</table>

**CDA Town Car**

<table>
<thead>
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<th>CD₀</th>
<th>A, m²</th>
<th>CD₀A, m²</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.367</td>
<td>1.754</td>
<td>0.644</td>
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*Figure B-3. Vehicles Tested in the Lockheed-Georgia Low-Speed Wind Tunnel (Continuation 1)*
Sebring-Vanguard Citicar

<table>
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<tr>
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<th>$C_{D_0}A, m^2$</th>
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</thead>
<tbody>
<tr>
<td>0.541</td>
<td>1.700</td>
<td>0.920</td>
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Figure B-3. Vehicles Tested in the Lockheed-Georgia Low-Speed Wind Tunnel (Continuation 2)
Zagato Elcar

<table>
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<tbody>
<tr>
<td>0.490</td>
<td>1.838</td>
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Jet 600 Van

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<th>$C_D A$, m²</th>
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<tbody>
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<td>0.539</td>
<td>1.942</td>
<td>1.029</td>
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</table>

Figure B-3. Vehicles Tested in the Lockheed-Georgia Low-Speed Wind Tunnel (Continuation 3)
Figure B-3. Vehicles Tested in the Lockheed-Georgia Low-Speed Wind Tunnel (Continuation 4)
### Energy R&D HEVAN

<table>
<thead>
<tr>
<th>$C_{D_0}$</th>
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</thead>
<tbody>
<tr>
<td>0.497</td>
<td>3.283</td>
<td>1.632</td>
</tr>
</tbody>
</table>

### AMC Pacer Wagon

<table>
<thead>
<tr>
<th>$C_{D_0}$</th>
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<th>$C_{D_0}A$, m²</th>
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<tbody>
<tr>
<td>0.406</td>
<td>2.225</td>
<td>0.903</td>
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</table>

Figure B-3. Vehicles Tested in the Lockheed-Georgia Low-Speed Wind Tunnel (Continuation 5)
Figure B-3. Vehicles Tested in the Lockheed-Georgia Low-Speed Wind Tunnel (Continuation 6)
Oldsmobile Delta 88 Sedan

<table>
<thead>
<tr>
<th>$C_D_0$</th>
<th>$A$, $m^2$</th>
<th>$C_D_0A$, $m^2$</th>
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<tbody>
<tr>
<td>0.558</td>
<td>2.077</td>
<td>1.159</td>
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Chevrolet Chevette

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<thead>
<tr>
<th>$C_D_0$</th>
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<th>$C_D_0A$, $m^2$</th>
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<tbody>
<tr>
<td>0.502</td>
<td>1.765</td>
<td>0.886</td>
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</table>

Figure B-3. Vehicles Tested in the Lockheed-Georgia Low-Speed Wind Tunnel (Continuation 7)
Figure 8-1. Vehicles Tested in the Lockheed-Georgia Low-Speed Wind Tunnel (Continuation 8)

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<th>Car</th>
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<th>$A$ (m²)</th>
<th>$C_d A$ (m²)</th>
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<tbody>
<tr>
<td>Honda Civic Sedan</td>
<td>0.411</td>
<td>1.906</td>
<td>0.783</td>
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</table>

<table>
<thead>
<tr>
<th>Car</th>
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<th>$A$ (m²)</th>
<th>$C_d A$ (m²)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Honda Civic Sedan</td>
<td>0.503</td>
<td>1.630</td>
<td>0.820</td>
</tr>
</tbody>
</table>
### Honda Civic Wagon

<table>
<thead>
<tr>
<th>$C_D^0$</th>
<th>$A$, $m^2$</th>
<th>$C_D^0A$, $m^2$</th>
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</thead>
<tbody>
<tr>
<td>0.514</td>
<td>1.685</td>
<td>0.866</td>
</tr>
</tbody>
</table>

### Ford Fiesta

<table>
<thead>
<tr>
<th>$C_D^0$</th>
<th>$A$, $m^2$</th>
<th>$C_D^0A$, $m^2$</th>
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</thead>
<tbody>
<tr>
<td>0.468</td>
<td>1.747</td>
<td>0.818</td>
</tr>
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</table>

*Figure B-3. Vehicles Tested in the Lockheed-Georgia Low-Speed Wind Tunnel (Continuation 9)*
APPENDIX C
A REVIEW OF GENERAL AERODYNAMIC DRAG
PREDICTION PROCEDURES, APPLICATION, AND UTILITY

A. DRAG ESTIMATION METHODS

Several aerodynamicists have attempted to make generalizations or to predict a vehicle's drag based on various shape characteristics (References 3-1, 3-2, and C-1). The usual method is to assemble a large data base and develop correlations. Perhaps the best known effort is that of R.G.S. White (Reference 3-1) of Britain's Motor Industry Research Association (MIRA). Wind tunnel tests of 141 different vehicles were utilized. Each vehicle was divided into six basic zones, three of which were further subdivided. Numbers were assigned to features in each zone or subzone in an attempt to rate their obstructive effects on the airflow around the vehicle.

Rating values were assigned to each of the nine categories depending upon the vehicle's shape in those zones. The predicted drag coefficient was then determined from the following empirical equation:

$$C_D = 0.16 + 0.0095 \times \text{Drag Rating}$$

where the Drag Rating is simply the summation of the nine individual category ratings.

By way of verification, drag estimates for 20 vehicles (mainly European) were made by White using this procedure, and were then compared to measured values. The average scatter was about 7%. It should be pointed out that the drag of these vehicles was not particularly low, and that White's procedure would not necessarily reflect the subtleties inherent in drag-optimized vehicles. Another cautionary note is that measured MIRA drag values are substantially lower than similar measurements made in domestic wind tunnels. The real value of this effort is the relative ordering of the aerodynamic design consequences of several shape parameters.

A second, and less rigorous "drag rating" approach to drag estimates is presented in Reference C-1 (Cornish). Ten regions are defined and a rating of from 1 to 3 is assigned. On this basis, the most streamlined vehicle would have a rating (R) of 30 and the worst, a rating of 10. The resulting drag coefficient is then calculated from

$$C_D = 0.62 - 0.01R$$

This procedure is rather crude but simple and its accuracy is far less than the 7% reported for White's method.
Both of the two previous procedures are based upon shape correlation curves which are linear with the drag rating and are limited to conventional passenger vehicle configurations. A third estimation procedure, developed for the EPA (Pershing - Reference 3-2), is a "drag buildup" method based on quantitative geometric characteristics applicable to a large range of generic body shapes. The total vehicle drag coefficient is defined as the sum of the coefficients of 11 discrete parts.

\[ C_D^{tot} = \sum_{i=1}^{11} C_D^i \]

Although this procedure requires more quantitative knowledge of the body shape being evaluated, it has the potential of addressing the more subtle details.

Excerpts from these three references follow; sufficient detail is included to allow their application. In addition, some generalizations are set forth concerning the drag increments characteristic of various components and devices.

B. DRAG ESTIMATION PROCEDURES

1. Drag Coefficient Estimation (R.G.S. White - Reference 3-1)

White divides a vehicle into six zones and three subzones for a total of nine categories. These are listed in Table C-1. A rating number is then assigned to the particular vehicle characteristic in each of the nine categories (see Table C-2). These nine intermediate ratings are summed to yield the "drag rating." The resulting drag coefficient is calculated from

\[ C_D = 0.16 + (0.0095)(\text{Drag Rating}) \]

<table>
<thead>
<tr>
<th>Zone</th>
<th>Subzone</th>
<th>Category</th>
</tr>
</thead>
<tbody>
<tr>
<td>Front</td>
<td>(a) Outline plan</td>
<td>1</td>
</tr>
<tr>
<td></td>
<td>(b) Elevation</td>
<td>2</td>
</tr>
<tr>
<td>Windshield/Roof Junction</td>
<td>(a) Cowl and fender cross section</td>
<td>3</td>
</tr>
<tr>
<td></td>
<td>(b) Windshield plan</td>
<td>4</td>
</tr>
<tr>
<td>Roof</td>
<td>(a) Windshield peak</td>
<td>5</td>
</tr>
<tr>
<td></td>
<td>(b) Roof plan</td>
<td>6</td>
</tr>
<tr>
<td>Rear Roof/Trunk</td>
<td></td>
<td>7</td>
</tr>
<tr>
<td>Lower Rear-End</td>
<td></td>
<td>8</td>
</tr>
<tr>
<td>Underbody</td>
<td></td>
<td>9</td>
</tr>
</tbody>
</table>
### Table C-2. Drag Rating System

<table>
<thead>
<tr>
<th>Category 1. Front End Plan Outline</th>
<th>Rating</th>
</tr>
</thead>
<tbody>
<tr>
<td>Approximately semicircular</td>
<td>1</td>
</tr>
<tr>
<td>Well-rounded outer quarters</td>
<td>2</td>
</tr>
<tr>
<td>Rounded corners without protuberances</td>
<td>3</td>
</tr>
<tr>
<td>Rounded corners with protuberances (a)</td>
<td>4</td>
</tr>
<tr>
<td>Squared tapering-in corners</td>
<td>5</td>
</tr>
<tr>
<td>Squared constant-width front</td>
<td>6</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Category 2. Elevation(b)</th>
<th>Rating</th>
</tr>
</thead>
<tbody>
<tr>
<td>Low rounded front, sloping up</td>
<td>1</td>
</tr>
<tr>
<td>High tapered rounded hood</td>
<td></td>
</tr>
<tr>
<td>Low squared front, sloping up</td>
<td>2</td>
</tr>
<tr>
<td>High tapered squared hood</td>
<td></td>
</tr>
<tr>
<td>Medium height rounded front, sloping up</td>
<td>3</td>
</tr>
<tr>
<td>Medium height squared front, sloping up</td>
<td>4</td>
</tr>
<tr>
<td>High rounded front, with horizontal hood</td>
<td></td>
</tr>
<tr>
<td>High squared front, with horizontal hood</td>
<td>5</td>
</tr>
</tbody>
</table>

1 Adapted from Reference 3-1.
Table C-2. Drag Rating System (Continuation 1)

<table>
<thead>
<tr>
<th>Category 3. Cowl and Fender Cross-Section</th>
<th>Rating</th>
</tr>
</thead>
<tbody>
<tr>
<td>Windshield/Roof Junction</td>
<td></td>
</tr>
<tr>
<td>Flush hood and fenders, well-rounded body sides</td>
<td>1</td>
</tr>
<tr>
<td>High cowl, low fenders</td>
<td>2</td>
</tr>
<tr>
<td>Hood flush with rounded-top fenders</td>
<td>3</td>
</tr>
<tr>
<td>High cowl, with rounded-top fenders</td>
<td>4</td>
</tr>
<tr>
<td>Hood flush with squared-edged fenders</td>
<td>5</td>
</tr>
<tr>
<td>Depressed hood, with high squared-edged fenders</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Category 4. Windshield Plant(c)</th>
<th>Rating</th>
</tr>
</thead>
<tbody>
<tr>
<td>Full-wrap-around (approximately semicircular)</td>
<td>1</td>
</tr>
<tr>
<td>Wrapped-around ends</td>
<td>2</td>
</tr>
<tr>
<td>Bowed</td>
<td>3</td>
</tr>
<tr>
<td>Flat</td>
<td>4</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Category 5. Windshield Peak</th>
<th>Rating</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rounded</td>
<td>1</td>
</tr>
<tr>
<td>Squared (including flanges or gutters)</td>
<td>2</td>
</tr>
<tr>
<td>Forward-projecting peak</td>
<td>3</td>
</tr>
<tr>
<td>Category 6. Roof Plan</td>
<td>Rating</td>
</tr>
<tr>
<td>-----------------------</td>
<td>--------</td>
</tr>
<tr>
<td>Well- or medium-tapered to rear</td>
<td><img src="1" alt="Image" /></td>
</tr>
<tr>
<td>Tapering to front and rear (max. width at BC post) or approximately constant width</td>
<td><img src="2" alt="Image" /></td>
</tr>
<tr>
<td>Tapering to front (max. width at rear)</td>
<td><img src="3" alt="Image" /></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Category 7. Rear Roof/Trunk(d)</th>
<th>Rating</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fastback (roof line continuous to tail)</td>
<td><img src="1" alt="Image" /></td>
</tr>
<tr>
<td>Semi-fastback (with discontinuity in line to tail)</td>
<td><img src="2" alt="Image" /></td>
</tr>
<tr>
<td>Squared roof with trunk rear edge squared</td>
<td><img src="3" alt="Image" /></td>
</tr>
<tr>
<td>Rounded roof with rounded trunk</td>
<td><img src="4" alt="Image" /></td>
</tr>
<tr>
<td>Squared roof with short or no trunk</td>
<td><img src="5" alt="Image" /></td>
</tr>
<tr>
<td>Rounded roof with short or no trunk</td>
<td><img src="5" alt="Image" /></td>
</tr>
</tbody>
</table>
Table C-2. Drag Rating System (Continuation 3)

<table>
<thead>
<tr>
<th>Category 8. Lower Rear End</th>
<th>Rating</th>
</tr>
</thead>
<tbody>
<tr>
<td>Well- or medium-tapered to rear</td>
<td>1</td>
</tr>
<tr>
<td>Small taper to rear or constant width</td>
<td>2</td>
</tr>
<tr>
<td>Outward taper (or flared-out fins)</td>
<td>3</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Category 9. Underbody(s)</th>
<th>Rating</th>
</tr>
</thead>
<tbody>
<tr>
<td>Integral, flush floor, little projecting mechanism</td>
<td>1</td>
</tr>
<tr>
<td>Intermediate</td>
<td>2</td>
</tr>
<tr>
<td>Integral, projecting structure</td>
<td>3</td>
</tr>
<tr>
<td>Intermediate</td>
<td>4</td>
</tr>
<tr>
<td>Deep chassis</td>
<td>5</td>
</tr>
</tbody>
</table>

(a) Fender mirrors. Include in protuberances if at the fender leading end. Otherwise add 1.

(b) Add: 3 for separate fenders; 4 for open front to fenders (above bumper level); 2 for raised built-in headlamps; 4 for small separate headlamps; 7 for large separate headlamps.

(c) Add: 1 for upright windshield; 1 for prominent flanges or rain gutters.

(d) Add: 3 for high fins or sharp longitudinal edges to trunk; 2 for separate fenders. Note: In all the ratings in this column, the trunk is assumed to be rounded laterally.

(e) Intermediate ratings applied from vehicle examination.

NOTE: Throughout table, the word "taper" or "tapered" refers to the plan view.
2. Drag Coefficient Estimation (J. J. Cornish - Reference C-1)

Cornish divides a vehicle into 10 zones and assigns a sub-rating of from 1 to 3 to each of them (see Table C-3). The total rating, \( R \), is the sum of these 10 sub-ratings. Two windshield zone items (numbers 4 and 5) refer to the elevation and plan views, respectively. The resulting drag coefficient is calculated from

\[ C_D = 0.62 - 0.01R \]

**Table C-3. Aerodynamic Rating**

<table>
<thead>
<tr>
<th>No.</th>
<th>Item</th>
<th>1</th>
<th>2</th>
<th>3</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Grill</td>
<td>Blunt; square</td>
<td>Fairly sloped</td>
<td>Well sloped</td>
</tr>
<tr>
<td>2</td>
<td>Lights</td>
<td>Open; exposed</td>
<td>Partially inset</td>
<td>Well faired</td>
</tr>
<tr>
<td>3</td>
<td>Hood</td>
<td>Flat</td>
<td>Fairly sloped</td>
<td>Convex, sloped</td>
</tr>
<tr>
<td>4</td>
<td>Windshield</td>
<td>Steep</td>
<td>Fairly sloped</td>
<td>Well sloped</td>
</tr>
<tr>
<td>5</td>
<td>Windshield</td>
<td>Flat</td>
<td>Fairly curved</td>
<td>Well curved</td>
</tr>
<tr>
<td>6</td>
<td>Roof top</td>
<td>Open</td>
<td>Fairly sloped</td>
<td>Convex, sloped</td>
</tr>
<tr>
<td>7</td>
<td>Rear Window</td>
<td>Notched</td>
<td>Fairly sloped</td>
<td>Fastback type</td>
</tr>
<tr>
<td>8</td>
<td>Trunk</td>
<td>Cut off square</td>
<td>Fairly sloped</td>
<td>Fastback type</td>
</tr>
<tr>
<td>9</td>
<td>Wheels</td>
<td>Exposed</td>
<td>Partially closed</td>
<td>Well concealed</td>
</tr>
<tr>
<td>10</td>
<td>Underside</td>
<td>Exposed</td>
<td>Partial pan</td>
<td>Full pan</td>
</tr>
</tbody>
</table>
3. Drag Coefficient Estimation (B. Pershing - Reference 3-2)

This procedure is much more complicated but much less subjective than the previous two. The relevant vehicle dimensions and areas are illustrated in Figures C-1 and C-2. The total drag coefficient is defined as the summation of eleven component coefficients:

\[
C_{D_{\text{tot}}} = \sum_{i=1}^{11} C_{D_i}
\]

The details of the determination of the ith components follow (reproduced directly from Reference 3-2). An assessment of this procedure is given in Reference 3-3.

**Front End Drag Coefficient, \( C_{D_1} \)**

\[
C_{D_1} = 0.707 \left( \frac{A_F}{A_R} \right) \left[ 1.0 - 2.79 \left( \frac{R}{E} \right)_u + 0.82 \left( \frac{R}{E} \right)_l - 5.21 \left( \frac{R}{E} \right)_v \right]
- 29.5 \left( \frac{R}{E} \right)_u \left( \frac{R}{E} \right)_l \left[ 1.0 - 2.25 \left( \frac{R}{E} \right)_v \right]
\]

where

- \( A_R \) = total vehicle projected frontal area, \( m^2 \) (\( ft^2 \))
- \( A_F \) = front end projected area, \( m^2 \) (\( ft^2 \))
- \( R \) = edge radius, \( m \) (\( ft \))
- \( E \) = running length of the edge radius, \( m \) (\( ft \))

and the subscripts u, l, and v refer to the upper, lower, and vertical edges of the front end, respectively. The \( \left( \frac{R}{E} \right)_i \) are to be taken as 0.105 when the estimated values exceed this magnitude.

**Windshield Drag Coefficient, \( C_{D_2} \)**

\[
C_{D_2} = 0.707 \left( \frac{A_W}{A_R} \right) \left[ 1.0 - 2.79 \left( \frac{R}{E} \right)_u \cos \beta - 5.21 \left( \frac{R}{E} \right)_v \right] \cos^2 \gamma
\]

where

- \( A_W \) = projected area of windshield, \( m^2 \) (\( ft^2 \))
- \( \gamma \) = slope of the windshield measured from the vertical, deg
- \( \beta = 2\gamma \)
Figure C-1. Vehicle Dimensions (Reference 3-2)

Figure C-2. Hatchback-Notchback Drag Coefficient Ratio
and the subscripts \( u' \) and \( v' \) refer to the roof-windshield intersection and the windshield posts, respectively. The value of \( \cos \gamma \) is to be taken as zero for \( \gamma \) larger than 45 degrees and the \( (R/E)_i \) are to be taken as 0.105 for estimated values exceeding this magnitude.

**Front Hood Drag Coefficient, \( C_{D3} \)**

\[
C_{D3} = 0.707 \left( \frac{A_h - A_p}{L_h} \right)^2 \frac{1}{A_R}
\]

where

\[
A_h = \text{projected area of body below the hood-windshield intersection, } m^2 \text{ (ft}^2\text{)}
\]

\[
L_h = \text{length of hood in the elevation or side view, } m \text{ (ft)}
\]

and the quantity \( (A_h - A_p) \) is to be taken as zero if it is negative.

**Rear Vertical Edge Drag Coefficient, \( C_{D4} \)**

\[
C_{D4} = -0.19 \left( \frac{R_v}{W} \right) \left( \frac{E_b}{H} \right) \quad \text{for} \quad \left( \frac{R_v}{W} \right) \leq 0.105
\]

\[
= -0.02 \left( \frac{E_b}{H} \right) \quad \text{for} \quad \left( \frac{R_v}{W} \right) > 0.105
\]

where

\[
R_v = \text{radius of rear vertical edges, } m \text{ (ft)}
\]

\[
W = \text{vehicle width, } m \text{ (ft)}
\]

\[
E_b = \text{length of rear vertical edge radius, } m \text{ (ft)}
\]

\[
H = \text{vehicle height, } m \text{ (ft)}
\]

**Base Region Drag Coefficient, \( C_{D5} \)**

\[
C_{D5} = 0.15 \left[ \left( \frac{A_B}{A_R} \right) + \left( \frac{C_{D_H}}{C_{D_B}} \right) \left( \frac{A_H}{A_R} \right) \right]
\]

where

\[
A_B = \text{projected area of flat portion of base region}
\]

\[
A_H = \text{projected area of upper rear or hatch portion of base region measured from the upper rear roof break (or for smoothly curved rooflines, that point where the rooftop slope is 15 degrees) to the top of the flat base, } m^2 \text{ (ft}^2\text{)}
\]

\[
C_{D_B} = \text{drag coefficient of the flat base}
\]
$C_{D_H}$ = drag coefficient of the upper rear or hatch portion of the base region

and the ratio $(C_D/C_{D_H})$ is shown in Figure C-2 as a function of $\phi$, the angle of the line from the upper rear roof break to the top of the flat base as measured from the horizontal.

**Underbody Drag Coefficient, $C_{D_6}$**

$$C_{D_6} = 0.025 \left(0.5 - \frac{x}{L}\right) \left(\frac{A_p}{A_R}\right) \quad \text{for } 0 \leq \frac{x}{L} \leq 0.5$$

$$= 0 \quad \text{for } \frac{x}{L} > 0.5$$

where

$x$ = smoothed forward length of the underbody, m (ft)
$L$ = vehicle length, m (ft)
$A_p$ = projected plan area of the vehicle, m$^2$ (ft$^2$)

**Wheel and Wheel Well Drag Coefficient, $C_{D_7}$**

$C_{D_7} = 0.14$

**Rear Wheel Well Fairing Drag Coefficient, $C_{D_8}$**

$C_{D_8} = -0.01$

**Protuberance Drag Coefficient, $C_{D_9}$**

$$C_{D_9} = \frac{1.1}{A_R} \sum A_{p_j}$$

where

$A_{p_j}$ = projected area of $j$th protuberance, m$^2$ (ft$^2$)

**Bullet Mirror Drag Coefficient, $C_{D_{10}}$**

$$C_{D_{10}} = 0.4 \frac{A_M}{A_R}$$

where

$A_M$ = projected area of mirror with bullet fairing, m$^2$ (ft$^2$)
Cooling Drag Coefficient, \( C_{D11} \)

\[
C_{D11} = 1.8 \left( \frac{A_T}{A_R} \right) \left( \frac{u_T}{u} \right) \left[ 1.0 - 0.75 \left( \frac{u_T}{u} \right) \right]
\]

where

- \( A_T \) = radiator area, \( m^2 \) (\( ft^2 \))
- \( u_T \) = exit velocity of cooling air from radiator
- \( \left( \frac{u_T}{u} \right) = 0.233 \left[ 1.0 - k \left( \frac{u}{100} \right)^2 \right] \)

and

\[
k = 1.14C \ (m/sec)^{-2} \quad \text{[or 0.299 (mph)^{-2}]}\]

4. Drag Increment Generalizations

General rule-of-thumb values have been given to many interference components and drag reduction devices. These are helpful only in the broadest sense; that is, most effects are a function of the specific application. For instance, a front air dam (or chin spoiler) might significantly reduce the drag for one vehicle but increase it for another. Similarly, some low-drag device may be detrimental at a yaw angle. Such dramatic results, however, are generally reserved for special cases. If one limits the application to an "average, conventional sedan," perhaps the generalizations in Table C-4 can provide some guidelines. The increments should not be considered as purely additive; this is particularly obvious in the case of an underpan and air dam.
### Table C-4. Drag Increment Generalizations

<table>
<thead>
<tr>
<th>Component or Configuration</th>
<th>$C_D$ (%)</th>
<th>Reference(s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Full length underpan</td>
<td>-5 to -15</td>
<td>3-8, 3-10, C-2, C-3</td>
</tr>
<tr>
<td>Front &quot;chin&quot; spoiler (air dam)</td>
<td>-6 to -9</td>
<td>3-8, 3-9, C-4</td>
</tr>
<tr>
<td>Rear deck spoiled (lip)</td>
<td>-5 to -9</td>
<td>3-8, 3-9, C-3, C-4</td>
</tr>
<tr>
<td>Flush windshield and side glass (no raingutters)</td>
<td>-3 to -7</td>
<td>3-10, C-5</td>
</tr>
<tr>
<td>Wheel discs and rear fender skirts</td>
<td>0 to -2</td>
<td>3-10, C-4</td>
</tr>
<tr>
<td>Sideview mirror(s)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Conventional A - pillar, stalk mount</td>
<td>+1 to +4</td>
<td>3-10, B-4, C-5</td>
</tr>
<tr>
<td>A - pillar, integral mount</td>
<td>+1 to +2</td>
<td>3-10</td>
</tr>
<tr>
<td>Fender mount (two)</td>
<td>+6</td>
<td>3-10</td>
</tr>
<tr>
<td>Headlights</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Pop-up</td>
<td>+3 to +6</td>
<td>3-10, C-6</td>
</tr>
<tr>
<td>Pocket</td>
<td>+3 to +6</td>
<td>3-10</td>
</tr>
<tr>
<td>Open front windows</td>
<td>0 to +3</td>
<td>3-8, C-2, C-6</td>
</tr>
<tr>
<td>Body side rubstrip</td>
<td>+1</td>
<td>3-10</td>
</tr>
<tr>
<td>Road trim package$^1$</td>
<td>+2 to +8</td>
<td>3-10, B-4,</td>
</tr>
</tbody>
</table>

---

$^1$ Consists of conventional mirror, windshield wipers, door handles, license plate, body gaps.
APPENDIX D

APPLICATION OF AREA-DISTRIBUTION SMOOTHING PROCEDURES TO AUTOMOTIVE AERODYNAMIC DESIGN

Basic Principles

Since early times, man has recognized that certain shapes found in nature move more efficiently through air and water. The hulls of even primitive ships were often modeled after the well-known tear drop-shaped body exhibited by many fish and birds. It was therefore only logical that early attempts to streamline automotive shapes were approached in a similar manner. These often took the form of a "torpedo on wheels" or the superposition of several "half drop" shapes. However, these potentially low drag designs were often severely compromised by many unfaired appendages such as wheels, lights, suspension members, open cockpits and the like.

The basic principle demonstrated by low drag bodies found in nature, however, can still find application in road vehicles. A "streamlined" body has low drag by virtue of well attached flow (no boundary layer separation) and the resultant minimum size wake. This boundary layer (flow immediately adjacent to the body surface), will remain attached as the flow negotiates its way along a smooth body so long as its momentum is sufficient to overcome any adverse pressure gradient. Momentum loss, however, is a function of the body surface contour gradients in the direction of flow. A well streamlined body has only moderate contour gradients whereas a modern automobile is characterized by many steep gradients. A representative contour parameter suggested by Hucho in Reference 3-4 is the line integral of the rate of change of curvature along the body surface. For simplicity, Hucho considers only the integral along the body centerline but it is recognized, that it should be applied over the entire body surface. Although theoretically possible, this would require a tremendous effort.

The present principle suggests a simple, if imperfect, compromise. The distribution of cross-sectional area as a function of longitudinal station along the body may be an approximation, representative of an integrated body contour parameter. The area distribution principle may be stated thusly:

"Gradual area variations along a body length are characteristic of a streamlined design."

It is pointed out that this may be a necessary, if not sufficient, attribute. Clearly, one could conceive of a shape satisfying the smooth area distribution criteria with cavities opposite sharp lumps and bumps canceling their effect. In order to minimize that particular anomaly, a corollary is added to the principle:

"The body camber-line should be as smooth as possible."
Here the camber-line is defined as the locus of points connecting the centroids of the cross-sectional area slices. Although the emphasis is different¹ these simplified principles are in general agreement with Reference 3-5.

Procedure

The application of the area distribution and camber-line principles represents an attempt to provide an intermediate alternative to costly developmental wind tunnel testing. Although the procedure relies heavily on perceptive decisions, it does produce an analytical/graphical evaluation process which iteratively guides one to a more streamlined design.

Before the process can be implemented it is necessary to have rather detailed three-view loft drawings or station templates of the candidate body. Section views may then be created at about 5 to 10 cm intervals (full-scale) along the longitudinal axis (more frequently where the area is perceived to be changing rapidly and fewer where the area change is less dramatic). A planimeter (or other means) may then be used to measure the area of each cross section. The areas, thus determined, are then plotted as a function of station position. Figure D-1 is a schematic example of the procedure and the result. The diagram created in this manner is called the body "area distribution." Those regions where the area is changing rapidly are candidates for modification. However, in order to help guide these modifications, the corresponding body camber-line should be developed. As indicated earlier, this is merely a plot of the section area centroids versus station position. An easy way of determining the centroid of a section area is to first cut the shape out of a piece of stiff paper or cardboard. Next, suspend it from a pin near the perimeter at some arbitrary point (such that it's free to rotate) and draw a vertical line through the pin hole. Rotate the shape about 90° and repeat. If the material is homogeneous, the intersection of the two lines will be the centroid. Obviously, the point should lie midway between the sides of each section or the design is not laterally symmetrical. The vertical displacement from some reference such as the ground varies from section to section. These measurements when plotted versus section position, produce the body camber-line. (This result is also depicted in Figure D-1.) With the added constraint that the camber-line be as smooth as possible, the sections requiring area modifications are reexamined. If it appears that some area needs to be added at a few stations (in order to smooth the hood/windshield interface, for example) and the camber-line is low in that region, then the area should be added near the upper surfaces. If the camber-line could be smoothed by lowering it in that region,

¹Morelli, in developing his "Body Shape of Minimum Drag" (Reference 3-5), begins by defining a specialized camber-line and bases the body shape upon it.
Figure D-1. Schematic Showing Area Distribution Procedure
the area should be added below the centroid. It is generally admirable to make this area addition around the rocker panel rather than under the body. The technique is iterative, and the area distribution and camber-line curves should be checked following each complete modification. Quite clearly, this procedure cannot be mindlessly applied, but rather requires a blend of artistic style and sensible judgement. Certain individuals may be able to accomplish much the same result by "integrating with their eye" but in any event, this technique provides a methodology to measure the designer's intuition.

Examples

The General Electric ETV-1 represents an exceptionally well integrated low-drag \( C_D = 0.3 \) vehicle body (Figure D-2a). It was designed by Chrysler using subscale developmental wind tunnel test techniques on a series of clay models (Reference B-5). Nevertheless, it is interesting to examine its area distribution in order to test the area distribution principle. That is, does this low-drag vehicle exhibit the gradual area variation typical of naturally streamlined bodies? Figure D-2b shows that the ETV-1 area distribution is fairly smooth. However, without some basis for comparison it is difficult to assess whether a particular area curve is exceptional or whether there is room for improvement. An example of a low drag design, near the extreme practical limit for an automotive shape, was developed using the area distribution technique described earlier and verified in subsequent wind tunnel tests (Figure D-3a). The styling theme is clearly reminiscent of the "Body Shape of Minimum Drag" developed by Morelli (Reference 3-5). The area distribution resulting from this very streamlined, low-drag design is shown in Figure D-3b. Obviously, the gradient is smooth since the design was refined using that technique. Both the ETV-1 and this design (Mays-B) are drag-optimized shapes for their respective design themes. It should be pointed out, however, that the former was developed through costly wind tunnel developmental testing (equivalent to a Level III Design) and the latter using the area gradient principle (equivalent to a Level II Design).

A third example is the Garrett AiResearch ETV-2 electric vehicle (Figure D-4a) which employed neither of these processes during design. In fact, this vehicle is representative of a Level I Design. As shown in Figure D-4b, the area distribution of the Garrett vehicle

---

1 This work was performed under subcontract to the Art Center College of Design in Pasadena as a student project by J.C. Mays (Reference D-1). This outstanding design was found to have a \( C_D = 0.2 \) from clay model wind tunnel tests. Further alterations in the tunnel paid no drag dividends; it had indeed been drag optimized on paper. (Since the model lacked a certain level of detail, which would be present on an actual vehicle, it is estimated that a prototype version might have a drag coefficient around 0.25.)
Figure D-2a. General Electric ETV-1

Figure D-2b. Area Distribution and Camber-Line for the General Electric ETV-1
Figure D-3a. Mays Aero Car (Model)

Figure D-3b. Area Distribution and Camber-Line for the Mays Aero Car
Figure D-4a. Garrett AiResearch ETV-2

Figure D-4b. Area Distribution and Camber-Line for the Garrett AiResearch ETV-2
is significantly rougher than either of the other two vehicle shapes. This is consistent with full-scale wind tunnel test results which found the Garrett drag coefficient to be about 0.4 (significantly greater than either of the other two example vehicles).

These few examples by no means provide conclusive proof of the area distribution principle but there is sufficient evidence of its value to include it as a part of the design strategy.
APPENDIX E

ESTIMATING DRAG CHARACTERISTICS IN YAW FOR AUTOMOBILE SHAPES

Since a road vehicle operates in the presence of ambient winds which are rarely aligned with its longitudinal axis, some knowledge of the relationship between drag and yaw angle is necessary. The first and most significant effort to quantify and generalize these characteristics for automotive shapes was performed by Barth of the Stuttgart Technical College (Reference E-1) two decades ago. Limited to side force and yawing moment coefficients, his results were derived from wind tunnel tests of four basic shapes and four groups of small automobile models totaling 28 specimens in all. He showed that variations with yaw angle were generally linear (up to 25°) and that differences in body form and features affected only the slope of the variation. The body features upon which Barth based his correlations were aspect ratio and fineness ratio.

Ten years later, recognizing the need to generalize yaw effects for all the aerodynamic coefficients (particularly drag), Bowman of Ford Motor Company compiled wind tunnel data on 3/8-scale models of 21 automobile body forms (Reference 3-6). Suggesting that the range of aspect ratios for prevailing American sedans was not sufficiently large enough to provide a suitable correlation parameter, he looked for non-geometric relationships. Specifically, he determined that the drag-yaw characteristic had a typical maximum of about 30° and the amplitude was a function of the drag coefficient at zero yaw. Bowman’s general equation was of the form:

\[ C_D = C_D_0 + K_1(1 - \cos \psi) \]  

(E-1)

where \( K_1 \) is a function of \( C_D_0 \) (the zero-yaw drag coefficient) and a few general shape descriptions; \( \psi \) is the yaw angle in degrees.

In an effort to correlate the model and full-scale wind tunnel data developed during the present program, it was determined that Bowman’s representation was entirely inadequate to represent the range of vehicles investigated. Since extensive model tests had been performed on the effects of aspect and fineness ratios for automotive shapes (see Appendix A), these data were examined for yaw characteristic correlations. Using a formulation format similar to Bowman’s, the following equation was derived:

\[ \frac{C_D}{C_D_0} = 1 + K(1 - \cos \psi) \]  

(E-2)

where \( K \) is not a function of \( C_D_0 \) but a function of aspect ratio (AR) and fineness ratio (FR). That is,

\[ K = (0.15AR - 0.03)FR - 0.513AR + 0.336 \]  

(E-3)

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where AR is the ratio of body height (not including ground clearance) to body width, and FR is the ratio of body length to the diameter of a circle equivalent to the body frontal area.

The fit to the experimental data is quite good, as is shown in the following table:

<table>
<thead>
<tr>
<th>AR</th>
<th>FR</th>
<th>K measured</th>
<th>K Eq. E-3</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.58</td>
<td>2.2</td>
<td>0.16</td>
<td>0.16</td>
</tr>
<tr>
<td></td>
<td>2.7</td>
<td>0.19</td>
<td>0.19</td>
</tr>
<tr>
<td></td>
<td>3.2</td>
<td>0.22</td>
<td>0.22</td>
</tr>
<tr>
<td>0.70</td>
<td>2.2</td>
<td>0.13</td>
<td>0.14</td>
</tr>
<tr>
<td></td>
<td>2.7</td>
<td>0.18</td>
<td>0.18</td>
</tr>
<tr>
<td></td>
<td>3.2</td>
<td>0.22</td>
<td>0.22</td>
</tr>
<tr>
<td>0.77</td>
<td>2.2</td>
<td>0.14</td>
<td>0.13</td>
</tr>
<tr>
<td></td>
<td>2.7</td>
<td>0.19</td>
<td>0.17</td>
</tr>
<tr>
<td></td>
<td>3.2</td>
<td>0.22</td>
<td>0.21</td>
</tr>
<tr>
<td>0.88</td>
<td>2.2</td>
<td>0.10</td>
<td>0.11</td>
</tr>
<tr>
<td></td>
<td>2.7</td>
<td>0.14</td>
<td>0.16</td>
</tr>
<tr>
<td></td>
<td>3.2</td>
<td>0.16</td>
<td>0.21</td>
</tr>
</tbody>
</table>

Encouraged by this clear correlation, Equation E-3 was applied and compared to the results of the full scale prototype wind tunnel tests (Reference 2-1). Because the simple AR and FR parameters did not adequately describe the details of each vehicle shape, the correlation was not nearly as good. However, for design purposes, this equation should suffice for typical hatchback or fastback subcompact vehicles. A few modifying comments are necessary, however, for vehicles with specifically distinctive characteristics.
In summary, the variation of drag with yaw angle can, to a first approximation, be described by the following function and associated comments:

\[ \frac{C_D}{C_{D_0}} = 1 + K (1 - \cos 6\psi) \]  \hspace{1cm} (E-2)

where

\[ K = (0.15AR - 0.03)FR - 0.513AR + 0.336 \]  \hspace{1cm} (E-3)

- Not valid for fineness ratios less than 1.5.
- Reduce \( K \) by up to 50\% for extremely low nose and sloping hoodlines.
- Increase \( K \) by up to 10\% for harsh, angular design with corner radii less than 10 cm.
- Increase \( K \) by up to 15\% for notch back designs.

Note that a maximum is reached at \( \psi = 30^\circ \) such that,

\[ \frac{C_{D_{\text{max}}}}{C_{D_0}} = 1 + 2K \]  \hspace{1cm} (E-4)

This parameter is useful in predicting the effects of ambient winds in Appendix F.
APPENDIX F

DETERMINATION OF DRAG WIND-WEIGHTING FACTORS
FOR VEHICLES OPERATING IN AMBIENT WINDS

As a vehicle moves along a roadway, it normally operates in a windy environment. Since the wind vector is usually not aligned with the highway, the vehicle is effectively yawed with respect to the flow. Therefore, range predictions that utilize the zero-yaw drag values will inaccurately characterize the aerodynamic contribution and yield optimistic results.

A procedure to accurately determine the effects of ambient winds on vehicle drag has recently been developed (Reference 3-7). The approach is to figuratively (in a computer simulation) drive a vehicle over a prescribed velocity-time schedule in the presence of a wind which varies statistically in speed (a speed probability function designated by some annual mean wind speed) and comes with equal probability from any direction. The resultant combination of the vehicle and wind velocity vectors yields an instantaneous yaw angle with respect to the vehicle. If the vehicle's drag-yaw characteristic is known or assumed, the resultant drag may be determined at each instant. Therefore, the energy required to overcome aerodynamic resistance is calculated by integrating the instantaneous aerodynamic power required over the entire cycle. It is then possible to determine the constant drag coefficient that would have been necessary in order to yield the same result. The ratio of this new effective coefficient, $C_{D_{eff}}$, to the original zero-yaw drag coefficient, $C_D$, is the wind weighting factor, $F$. $F$ is thus a multiplier to correct the zero-yaw drag coefficient for the effects of ambient winds.

This rigorous procedure was used to generate $F$-factors for a large range of vehicle characteristics, wind conditions, and driving cycles. Analysis of these results yielded many fortuitous relationships leading to simplifying assumptions which are accurate to within about 3%.

The wind-weighting factor, $F$, was found to be a simple exponential function of the dominant parameter, $C_{D_{max}}/C_{D_{o}}$; the yaw angle where $C_{D_{max}}$ occurs ($\Psi = 30^\circ \pm 5^\circ$) is of second order significance and is neglected. For design purposes, the parameter $C_{D_{max}}/C_{D_{o}}$ may be estimated by a special case of the yaw characteristic equation presented in Appendix E (Equation E-4). $F$ is then only a function of yaw angle, the annual mean wind speed and the particular driving cycle or constant speed. The resulting equations for $F$ are given in Tables F-1 and F-2 in metric and English units, respectively.
### Table F-1. Wind-Weighting Factor Equations - Metric Units

<table>
<thead>
<tr>
<th>Equation</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$W = \text{annual mean wind speed in km/hr (12 km/hr mean average in U.S.)}$</td>
<td></td>
</tr>
<tr>
<td>$V = \text{vehicle speed in km/hr}$</td>
<td></td>
</tr>
</tbody>
</table>

**EPA CYCLES**

**URBAN:**

$$F = (1.22 \times 10^{-4}w^2 + 1.61 \times 10^{-2}w)(c_{D_{\text{max}}}/c_{D_0}) + 2.89 \times 10^{-4}w^2 - 1.47 \times 10^{-2}w + 1.0$$

**HIGHWAY:**

$$F = (1.94 \times 10^{-4}w^2 + 5.61 \times 10^{-3}w)(c_{D_{\text{max}}}/c_{D_0}) + 2.86 \times 10^{-5}w^2 - 5.32 \times 10^{-3}w + 1.0$$

**COMBINED: (55% - 45% split):**

$$F = (1.72 \times 10^{-4}w^2 + 1.11 \times 10^{-2}w)(c_{D_{\text{max}}}/c_{D_0}) + 1.40 \times 10^{-4}w^2 - 1.11 \times 10^{-2}w + 1.0$$

**SAE ELECTRIC CYCLES (J227a)**

**B:**

$$F = (9.41 \times 10^{-5}w^2 + 3.76 \times 10^{-2}w)(c_{D_{\text{max}}}/c_{D_0}) + 5.97 \times 10^{-4}w^2 - 2.83 \times 10^{-2}w + 1.0$$

**C:**

$$F = (1.18 \times 10^{-4}w^2 + 2.22 \times 10^{-2}w)(c_{D_{\text{max}}}/c_{D_0}) + 3.61 \times 10^{-4}w^2 - 1.94 \times 10^{-2}w + 1.0$$

**D:**

$$F = (1.81 \times 10^{-4}w^2 + 1.25 \times 10^{-2}w)(c_{D_{\text{max}}}/c_{D_0}) + 1.44 \times 10^{-4}w^2 - 1.33 \times 10^{-2}w + 1.0$$

**CONSTANT SPEED**

$$F = \left[0.98 \ (W/V)^2 + 0.63 \ (W/V)\right] \times (c_{D_{\text{max}}}/c_{D_0}) - 0.40 \ (W/V) + 1.0$$

**Constraints:**

- For $(W/V) < 0.09$ \( F = 1.0 \)
- For $(W/V) > 1.0$ \( (W/V) = 1.0 \)

---

1These constraints may be necessary if this equation is applied to the quasi-steady instantaneous vehicle speeds in a computer simulation (i.e., the function goes to infinity at $V = 0$). In a physical sense, however, the equation is entirely proper without these boundary conditions.
Table F-2. Wind-Weighting Factor Equation - English Units

$W$ = annual mean wind speed in mph (7.5 mph mean average in U.S.)
$V$ = vehicle speed in mph

**EPA CYCLES**

**URBAN:**

\[
F = (3.16 \times 10^{-4}w^2 + 2.59 \times 10^{-2}w)(C_{D_{max}}/C_{D_o}) + 7.49 \times 10^{-4}w^2 - 2.37 \times 10^{-2}w + 1.0
\]

**HIGHWAY:**

\[
F = (5.02 \times 10^{-4}w^2 + 9.04 \times 10^{-3}w)(C_{D_{max}}/C_{D_o}) + 7.41 \times 10^{-5}w^2 - 8.56 \times 10^{-3}w + 1.0
\]

**COMBINED: (55% - 45% split):**

B: \[F = (4.47 \times 10^{-4}w^2 + 1.78 \times 10^{-2}w)(C_{D_{max}}/C_{D_o}) + 3.62 \times 10^{-3}w^2 - 1.79 \times 10^{-2}w + 1.0\]

**SAE ELECTRIC CYCLES (J227a)**

B: \[F = (2.44 \times 10^{-4}w^2 + 6.06 \times 10^{-2}w)(C_{D_{max}}/C_{D_o}) + 1.55 \times 10^{-3}w^2 - 4.56 \times 10^{-2}w + 1.0\]

C: \[F = (3.07 \times 10^{-4}w^2 + 3.57 \times 10^{-2}w)(C_{D_{max}}/C_{D_o}) + 9.37 \times 10^{-4}w^2 - 3.12 \times 10^{-2}w + 1.0\]

D: \[F = (4.68 \times 10^{-4}w^2 + 2.01 \times 10^{-2}w)(C_{D_{max}}/C_{D_o}) + 3.73 \times 10^{-4}w^2 - 2.14 \times 10^{-2}w + 1.0\]

**CONSTANT SPEED**

\[
F = \left[0.98(w/V)^2 + 0.63(w/V)\right]x(C_{D_{max}}/C_{D_o}) - 0.40(w/V) + 1.0
\]

Constraints:

For \(w/V \leq 0.09\) \(F = 1.0\)

For \(w/V > 1.0\) \(w/V = 1.0\)
In order to further simplify the application, Figures F-1 and F-2 are presented. These are graphical representations from Table F-1 with the annual mean wind speed fixed at 12 km/hr (7.5 mph); this is the average condition across the country.

Therefore, in the course of the design process, after the zero-yaw drag coefficient, $C_{D_0}$, has been estimated, the effective wind weighted coefficient $C_{D_{eff}}$ may be determined by

1. Calculating the $C_{D_{max}}/C_{D_0}$ ratio from Equation E-4.
2. Determining $F$, for the design cycle, from Figure F-1 or F-2.
3. Calculating, $C_{D_{eff}} = F \times C_{D_0}$.

An example to demonstrate just how important the wind weighting analysis might be in making drag estimations is presented in Table F-3. Using the vehicles in the EHV Aerodynamic Data Base (Appendix B, Part C), the effective wind weighted drag coefficient, $C_{D_{eff}}$, was determined (for operation over a J227a D cycle). In this case the $C_{n_{max}}/C_{D_0}$ ratio was precisely known for each vehicle from wind tunnel test data at yaw angles up to $40^\circ$. Therefore, the wind weighting factor, $F$, could be directly determined for each vehicle from Figure F-1 (for an annual mean wind speed of 12 km/hr). The effective drag coefficient, $C_{D_{eff}}$, is, as before, the product of $F$ and $C_{D_0}$.

As can be seen, the wind-weighting factor, $F$, averaged about 1.08 (an 8% correction), ranging from 5 1/2% to almost 12%. Had this analysis been performed for a "B" cycle, the correction would be as high as 42%. (The wind vector is more of a factor at lower vehicle speeds; however, the aerodynamic component is smaller portion of the total energy requirements.)

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\[ ^1 \text{It should be noted that this is not a constant average speed, but rather a statistical average. For instance, an annual mean wind speed of 12 km/hr has winds of up to 50 km/hr occurring about 3% of the time and winds less than 12 km/hr occurring about 70% of the time.} \]
Figure F-1. Wind-Weighting Factors for Various Driving Cycles

Figure F-2. Ambient Wind Drag Factor as a Function of Various Constant Speeds
Table F-3. Effective Wind-Weighted Drag of Test Vehicles Performing J227a D Cycles in the Presence of a 1.2 kph Annual Mean Wind Speed Equally Probable From Any Direction (Windows Closed)\(^1\)

<table>
<thead>
<tr>
<th>Vehicle</th>
<th>CD (_0)</th>
<th>CD (_{\text{max}})/CD (_0)</th>
<th>F</th>
<th>CD (_\text{eff})</th>
<th>CD (_\text{eff}), m(^2)</th>
</tr>
</thead>
<tbody>
<tr>
<td>GE ETV-1</td>
<td>0.308</td>
<td>1.27</td>
<td>1.084</td>
<td>0.333</td>
<td>0.614</td>
</tr>
<tr>
<td>Garrett ETV-2</td>
<td>0.395</td>
<td>1.50</td>
<td>1.124</td>
<td>0.444</td>
<td>0.990</td>
</tr>
<tr>
<td>GE Centennial</td>
<td>0.337</td>
<td>1.12</td>
<td>1.058</td>
<td>0.357</td>
<td>0.660</td>
</tr>
<tr>
<td>CDA Town Car</td>
<td>0.367</td>
<td>1.16</td>
<td>1.065</td>
<td>0.391</td>
<td>0.686</td>
</tr>
<tr>
<td>SCT Rabbit</td>
<td>0.459</td>
<td>1.26</td>
<td>1.082</td>
<td>0.496</td>
<td>0.903</td>
</tr>
<tr>
<td>Sebring-Vanguard Citicar</td>
<td>0.541</td>
<td>1.20</td>
<td>1.072</td>
<td>0.580</td>
<td>0.986</td>
</tr>
<tr>
<td>Zagato Elcar</td>
<td>0.490</td>
<td>1.37</td>
<td>1.102</td>
<td>0.540</td>
<td>0.992</td>
</tr>
<tr>
<td>Jet 600 Van</td>
<td>0.530</td>
<td>1.40</td>
<td>1.107</td>
<td>0.586</td>
<td>1.138</td>
</tr>
<tr>
<td>Otis Van</td>
<td>0.581</td>
<td>1.30</td>
<td>1.090</td>
<td>0.633</td>
<td>1.641</td>
</tr>
<tr>
<td>Kaylor GT</td>
<td>0.583</td>
<td>(2)</td>
<td>-----</td>
<td>-----</td>
<td>-----</td>
</tr>
<tr>
<td>Energy R&amp;D HEVAN</td>
<td>0.497</td>
<td>(2)</td>
<td>-----</td>
<td>-----</td>
<td>-----</td>
</tr>
<tr>
<td>AMC Pacer Wagon</td>
<td>0.406</td>
<td>1.27</td>
<td>1.085</td>
<td>0.441</td>
<td>0.980</td>
</tr>
<tr>
<td>AMC Pacer Sedan</td>
<td>0.450</td>
<td>1.24</td>
<td>1.079</td>
<td>0.486</td>
<td>1.079</td>
</tr>
<tr>
<td>Chevrolet Corvette</td>
<td>0.490</td>
<td>1.10</td>
<td>1.055</td>
<td>0.517</td>
<td>0.995</td>
</tr>
<tr>
<td>Oldsmobile Delta 88 Sedan</td>
<td>0.558</td>
<td>1.46</td>
<td>1.118</td>
<td>0.624</td>
<td>1.296</td>
</tr>
<tr>
<td>Chevrolet Chevette</td>
<td>0.502</td>
<td>1.14</td>
<td>1.062</td>
<td>0.533</td>
<td>0.941</td>
</tr>
<tr>
<td>Plymouth Horizon</td>
<td>0.411</td>
<td>1.32</td>
<td>1.093</td>
<td>0.449</td>
<td>0.880</td>
</tr>
<tr>
<td>Honda Civic Sedan</td>
<td>0.503</td>
<td>1.28</td>
<td>1.086</td>
<td>0.566</td>
<td>0.890</td>
</tr>
<tr>
<td>Honda Civic Wagon</td>
<td>0.514</td>
<td>1.22</td>
<td>1.076</td>
<td>0.553</td>
<td>0.932</td>
</tr>
<tr>
<td>Ford Fiesta</td>
<td>0.468</td>
<td>1.22</td>
<td>1.076</td>
<td>0.504</td>
<td>0.880</td>
</tr>
</tbody>
</table>

\(^1\)With front windows open, the CD \(_{\text{max}}\)/CD \(_0\) ratio increases by an average of 16% for this group of vehicle.

\(^2\)Maximum CD was not determined since test yaw angle was limited to 20 degrees.
End of Document