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MINIMUM FUEL CONTROL OF A VEHICLE WITH A CONTINUOUSLY VARIABLE TRANSMISSION

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SUMMARY

The research described here was concerned with designing a control system for a vehicle with a heat engine and a continuously variable transmission. The objectives of control were to minimize fuel consumption and to achieve satisfactory dynamic response of vehicle variables as the vehicle was driven over a standard driving cycle. This is the first time that a control system design and evaluation has been attempted for this overall vehicle system. Even though the vehicle system was highly nonlinear, attention was restricted to linear control algorithms which could be easily understood and implemented on-board using a microcomputer. The effectiveness of these controllers in producing good dynamic behavior of the vehicle as well as minimum fuel consumption was demonstrated by simulation. Simulation results also revealed that the vehicle could exhibit unexpected dynamic behavior which must be taken into account in any control system design.
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1.0 INTRODUCTION

An important current area of research involves the design and development of vehicles and vehicle components which will reduce the nation's unduly high dependence on imported petroleum. The Continuously Variable Transmission (CVT), whose ratio may take on any value within a certain range, is one component which may be used to ensure that the vehicle's engine is operated efficiently with respect to fuel consumption. The research described here was directed toward investigating the control problems associated with controlling the throttle and transmission ratio of a vehicle containing a CVT so that acceptable stable dynamic responses for all important vehicle variables are obtained while minimizing fuel consumption.

The vehicle under consideration is a 1,500 Kg conventional sedan with a six cylinder engine and a continuously variable transmission. The system is inherently nonlinear because the torque and speed relationships include the transmission ratio in a multiplicative form, the relationships among engine variables are nonlinear, and the vehicle aerodynamic drag and rolling resistance are functions of the square of the velocity. The presence of these nonlinearities significantly complicates the control system analysis and design. The work described here involves development of simplified models for the components of the system, the design of control systems to achieve the desired objectives and analysis of the closed-loop performance using digital simulation.
1.1 Previous Work

Several researchers have investigated ways to minimize energy consumption or maximize efficiency in a vehicle propulsion system [1, 2, 3, 4, 6, 7, 8, 9]. Some of this work considered energy savings for the combination of a power plant and CVT [2, 4, 6] with little regard for overall control considerations, and some work focused on the design of control systems for this configuration when augmented by a flywheel [5, 7, 8]. In fact, there is little previous work which was directed toward the design of control systems for configurations which include a CVT but not a flywheel [4, 8, 9], and none of this work considered the complete vehicle system including drive train and road losses with evaluation of the control systems for a standard driving cycle.

1.2 Study Objectives

The objective of this research was to investigate control problems associated with the control of a vehicle containing a heat engine and a continuously variable transmission. The objective was to design control systems which would operate the vehicle so that (i) the heat engine is operated at the minimum energy consumption point for any particular demanded torque and speed, and (ii) the overall system is operated with minimum energy consumption for a standard driving cycle.

It is important to note that this investigation, for the first time, had the objective of considering the overall problem of controlling a vehicle with CVT while the vehicle is subject to a driving regime prescribed by a standard driving cycle; all
of the major elements of vehicle dynamics were included so that the control of the entire vehicle system was examined.

An important aspect of the objectives for this work was a determination to take an approach which would lead to easily implementable controllers. Some considerations leading to this approach are:

1. It is not possible to derive control algorithms for this system without undue simplifications because of its high degree of system nonlinearity. It is also not desirable to derive such controls because, in general, they would be in a form which would be difficult to implement.

2. Any derivation and calculation of optimal controls would necessarily be tied to a particular driving cycle, and the controls would be open loop. The results desired here (although to be evaluated with respect to a particular driving cycle) were not to be dependent upon any particular cycle.

3. It was desirable to devise control algorithms for this system which would be in a relatively simple, feedback form so that they could be implemented easily in a small, inexpensive, onboard microcomputer.

As a result of taking this approach, it was decided to use a control approach which was directed toward designing linear
control loops (or algorithms) which use signals obtainable from vehicle sensors. As a result of this decision, more specific control objectives were defined. These objectives were to determine the appropriate types of linear controllers for three control loops which control the engine speed, throttle, and CVT ratio, and to optimize the parameters of these controllers.

Section 2 deals with a description of the vehicle and development of its models while Section 3 describes the details of the approach used to design the control system. An overview of the simulation is given in Section 4, with simulation results discussed in Section 5. Conclusions and future work are discussed in Section 6.
2.0 VEHICLE DESCRIPTION

The vehicle used in this study is a conventional sedan with a six cylinder engine. However, the transmission employed is a continuously variable transmission (CVT). In the subsections below, we outline the methods used to model the vehicle and the drive train components, and we present the equations which describe the dynamic behavior of the overall system. A more detailed description of these models and a detailed derivation of the system state equations are given in Appendix A.

2.1 Vehicle Modeling

The propulsion system of the vehicle consists of an internal combustion or heat engine (HE) coupled to a continuously variable transmission; the CVT, in turn, delivers power to a differential which connects the drive shaft to the rear axle. The overall arrangement is shown in Figure 2.1. The method of modeling each component in the drive train is discussed in the paragraphs below.

![Figure 2.1 Drive Train Configuration](image)
Heat Engine (HE) Model: The HE is modeled as a rotating inertia with an applied torque. The applied engine torque is the output of a first order low pass system whose input is a torque determined from an engine map. For a given engine speed and throttle setting, the engine map determines a steady state engine torque. This torque in turn is the input to the first order system whose output is the engine torque actually developed. The first order system (with a time constant of 1.0 second) approximates the dynamics of the throttle linkages and engine combustion characteristics (a step change in throttle does not produce a step change in developed engine torque). See Figure 2.2.

![Figure 2.2 Heat Engine Configuration](image)

Continuously Variable Transmission: The CVT is modeled as a ratio (which is defined to be the ratio of drive shaft speed to engine speed, and this is allowed to vary continuously from zero to infinity), an inertia and a fixed efficiency as
shown in Figure 2.3. The inertia is defined to be the equivalent CVT inertia as seen on the drive shaft side of the transmission. It was also assumed that there are second order dynamic effects associated with changing the ratio, i.e. if there is a step change in the variable which controlled the ratio, the actual ratio will respond with a second order response. This is also shown in Figure 2.3. Finally, we note that since the CVT ratio can be set to zero, no clutch is required between the HE and CVT.

Differential: The differential is modeled in exactly the same way as the CVT except that the ratio is fixed. The ratio is defined as the ratio of axle speed to drive shaft speed.

Vehicle Body: The model of the vehicle body and wheels takes into account the weight of the vehicle and payload, aerodynamic drag, rolling resistance and grade.

A detailed description of all the above models and how they are used to derive the differential equations which describe the overall vehicle dynamics is given in Appendix A. Appendix B contains the actual parameter values employed when simulating the system.

2.2 System Differential Equations

As described in Appendix A, there are four states which characterize the dynamic behavior of the overall vehicle system:

\[ x_1 = \text{Engine speed.} \]

\[ x_2 = \text{Developed engine torque.} \]
$x_3 = \text{CVT ratio}$.

$x_4 = \text{Rate of change of CVT ratio} (= \dot{x}_3)$.

Since there is essentially no slippage between the engine and the rear wheels, the speed of the drive shaft and rear axle, as well as the vehicle velocity, can be computed from the engine speed, $x_1$. Also, since there is assumed to be a first order dynamic between a change in throttle setting and the corresponding change in developed engine torque, the latter, $x_2$, is also a state. Finally, since the CVT model includes a second order...
response of ratio to a change in the variable which controls the ratio, $x_3$ and $x_4$ are required states from the CVT model.

The four state equations which describe the vehicle dynamics are derived in Appendix A and are given as

$$\dot{x}_1 = \left[ x_2 - M_T x_3 (\phi_1 + \phi_2 + R_A R_W x_1 x_4) \right] / \left( J_T + M_T R_A R_W x_3^2 \right)$$

$$\dot{x}_2 = -\left[ x_2 - \phi_3 (x_1, u_1) \right] / \tau_L$$

$$\dot{x}_3 = x_4$$

$$\dot{x}_4 = C_1 x_4 + C_2 x_3 + C_3 u_2$$

where

$$\phi_1 (x_1, x_3) = R_A R_W \left[ D(x_1, x_3) + R(x_1, x_3) \right] / M_T K_A K_T$$

$$\phi_2 = R_A (T_B + R_W W \sin \theta) / M_T K_A K_T$$

$$M_T = (J_T / R_A R_W) + (R_A J_A / K_T R_W) + (R_A R_W M_V / K_A K_T)$$

$$M_V = (W/g) + J_W R_W^2$$

and where $u_1$ is throttle setting, $\phi_3 (x_1, u_1)$ is the steady state engine torque determined from the engine map (a function of throttle setting and engine speed), $\tau_L$ is the time constant of the throttle linkage/engine dynamic response, $W$ is the vehicle
weight, $g$ is the acceleration of gravity, $D$ and $R$ are the aerodynamic drag and rolling resistance forces, respectively (both functions of $x_1$), $\beta$ is the grade angle, $R_W$ is the wheel radius, $T_B$ is the braking torque, $J_E$, $J_W$, $J_T$ and $J_A$ are the rotating inertias of the engine, all four wheels, the CVT and the differential, respectively, $K_A$ and $K_T$ are the efficiencies of the differential and the CVT, respectively, $R_A$ is the differential ratio, $C_1$, $C_2$ and $C_3$ are constants used to characterize the second order dynamic response of the ratio changing mechanism, and $u_2$ is the variable used to produce a change in the ratio (this variable will be generated by a ratio controller which is discussed in the next section). The vehicle velocity, $v$, can be computed from the above states by

$$v = R_A R_W x_1 x_3$$

(2.6)

Figure 2.4  Block Diagram of Vehicle System
We note that two of the above state equations are highly nonlinear ((2.2) and (2.3)), thus complicating the control system design. A block diagram of the overall vehicle system showing the states and inputs is shown in Figure 2.4. The control inputs, $u_1$ and $u_2$, will be generated by the vehicle control system. Having described the characteristics of the system to be controlled, we now turn to a discussion of the design of the control system.
3.0 CONTROL SYSTEM DESIGN

The purpose of this section is to present the overall control philosophy for the vehicle system described in Section 2.0 and Appendix A, and to discuss the details of the control system designed to achieve the objectives which follow from this philosophy.

3.1 Control Objectives and Approach

The overall control objective is to manipulate throttle setting and CVT ratio changing input so that the vehicle achieves minimum fuel consumption while being driven over a standard driving cycle. An examination of a typical engine map shows that for each throttle setting there is an engine speed which achieves minimum fuel consumption for that throttle setting. In particular, a Minimum Fuel Curve can be developed from such a map which plots minimum fuel consumption engine speed against throttle setting. Such a curve (which is the one actually used in this study) is shown in Figure 3.1.

The existence of a minimum fuel consumption engine speed for each throttle setting suggests a specific control approach to achieve minimum fuel consumption: manipulate the throttle so that the vehicle follows the velocity requirements of the driving cycle, and, for each throttle setting, manipulate the CVT ratio so that the engine runs at a minimum fuel consumption speed for that throttle setting. The primary objective of
Figure 3.1 Minimum Fuel Curve
this study was to explore the feasibility of controlling the vehicle system in this manner. A block diagram of the control approach is shown in Figure 3.2.

3.2. Control System Design

In designing a control system to accomplish the task described above, an emphasis was placed on using simple, standard controllers which could be easily implemented. The use of linear control design methods for the design of these controllers was ruled out because of the highly nonlinear nature of the vehicle dynamics (see equations (2.2), (2.3), (2.6)). An additional nonlinearity is introduced by the minimum fuel curve which determines the engine speed set point for each throttle.
setting (see Figures 3.1 and 3.2). This curve is a nonlinear function of throttle setting, thus introducing a significant nonlinearity in the vehicle velocity control loop.

An additional important factor in the design of the controllers is that they should use only easily measured system variables in a feedback configuration. For a given driving cycle, it is conceivable that using optimal control theory, open-loop trajectories for throttle setting and the ratio changing input could be generated to achieve minimum fuel consumption. However, they would not be practical to implement because of inaccuracies in the vehicle models used to generate them, and because in practice a vehicle would not be driven over the specific driving cycle they were designed for. Thus, some form of feedback control is required in an actual vehicle; hence the use of feedback control in this study.

The control system employs two primary control loops: one to control vehicle velocity by manipulating throttle, and the other to control engine speed by manipulating CVT ratio. This is shown in Figure 3.3. It is assumed that the operator of the vehicle generates a signal (by manipulating a pedal or some other device) which represents the desired vehicle velocity. This signal is the set point to the velocity control loop as shown in Figure 3.3. Based on the velocity error, the velocity controller generates a throttle setting and a braking torque to make the vehicle velocity equal the set point (idle throttle during braking and zero braking torque when throttle is above idle).
Figure 3.3 Vehicle Control System - Initial Configuration
For the given throttle setting, $u_1$, the minimum fuel curve generates an engine speed set point (for minimum fuel consumption) which is enforced by the engine speed controller manipulating the CVT ratio.

There are two possible ways of envisioning how the engine speed controller can change the CVT ratio. First, the output of the controller could be $u_2$, the variable which drives the ratio changing mechanism. Alternatively, the output of the engine speed controller could be a ratio set point which drives a ratio control loop; the ratio controller compares actual ratio to desired ratio and generates the input, $u_2$, to the ratio actuator (see Figure 3.3). This alternative allows the ratio controller to be selected to speed up, if necessary, a sluggish ratio changing mechanism. This second approach was the approach adopted in the present study.

The overall control system thus consists of three control loops: a velocity loop, an engine speed loop and a ratio loop. In addition, simulation runs showed that an improvement in control could be obtained by placing two low pass filters in the system; one to smooth out throttle changes and the other to smooth out changes in desired engine speed. The next three subsections describe the design of the controllers for each of the three control loops and the placement and design of the two low pass filters.
3.3 Vehicle Velocity Controller Design

The job of the vehicle velocity controller is to manipulate the throttle and brakes so that the vehicle velocity equals the velocity set point (driving cycle velocity). The input to the controller is the velocity error and, in keeping with the design objective of using simple, standard controllers, the controller is assumed to be a proportional plus integral (PI) controller. This is a natural choice because it represents how an actual operator would manipulate the throttle in response to a velocity error. In particular, an operator would depress the throttle in proportion to the velocity error; as the vehicle came up to speed and the error decreased, the operator would back off on the throttle, hence the need for the proportional term. An integral term is also needed to keep the throttle depressed at the value necessary to achieve zero steady state velocity error; without the integral term the throttle would approach idle position as the velocity error approached zero and a nonzero steady state velocity error would result.

Since the controller contains an integral term, and the actuator it is driving can limit (throttle has an upper limit of 100%), it is necessary to incorporate an antiwindup feature in the controller. The antiwindup feature essentially inhibits additional corrections to the throttle if the throttle is at its limit, and prevents the integrator in the PI controller from saturating or "winding up". The details of this feature are discussed in Appendix D.
Finally, later simulation runs revealed that rapid changes in the throttle at start-up (more rapid than an actual driver could produce) could cause instability in the vehicle velocity. It was found that smoothing of the throttle controller output reduces this possibility; hence a first order low pass filter was added at the output of the throttle controller.

A block diagram of the throttle controller is shown in Figure 3.4. The PI control algorithm, the antiwindup logic and the filter generate what might be considered a pedal position, $P$. A pedal position of $K_1$ (see blocks labeled throttle and brake limiter in Figure 3.4) corresponds to idle throttle. If the pedal is below $K_1$ the throttle limiter sets the throttle at idle position and the brake limiter generates a braking torque proportional to pedal position. For a pedal position between $K_1$ and 100 the braking torque is zero and the throttle equals the pedal position. For a pedal position above 100, the throttle is limited to 100%. The braking torque and throttle position are inputs to the vehicle dynamic simulation and the throttle setting $u_1$ is also an input to the minimum fuel curve (see Figure 3.3). This curve generates a set point for the engine speed control loop such that the engine runs at its minimum fuel consumption speed for the particular throttle setting.

Referring to Figure 3.4, the transfer function for the PI algorithm can be expressed as (ignoring the effects of the antiwindup logic).

$$\frac{M(s)}{V_s(s)} = \frac{K_{VP}s + K_V}{s}$$

(3.1)
Figure 3.4 Velocity Controller
where $K_{VP}$ and $K_{VI}$ are the proportional and integral gains, respectively. If we define the controller state as ($x_5$ is used in conjunction with the engine speed controller)

$$x_6 = m - K_{VP}(v_D - v)$$

(3.2)

Then using (2.6) the controller state and output equations can be expressed as

$$\dot{x}_6 = K_{VI}(v_D - R_A R_W x_1 x_3)$$

(3.3)

and

$$m = x_6 + K_{VP}(v_D - R_A R_W x_1 x_3)$$

(3.4)

The transfer function of the throttle filter can be written as

$$\frac{P(s)}{M(s)} = \frac{1}{\tau_T s + 1}$$

(3.5)

where $\tau_T$ is the filter time constant. If we define the filter state as

$$x_7 = P$$

(3.6)

then using (3.4) and (3.5) the filter state equation is

$$\dot{x}_7 = \frac{1}{\tau_T} (x_6 - x_7) + \frac{K_{VP}}{\tau_T}(v_D - R_A R_W x_1 x_3)$$

(3.7)

Equations (3.3), (3.6) and (3.7) describe the overall dynamic behavior of the throttle controller. It is important to note, however, that these equations only apply to the case where the actuator is not at a limit and the antiwindup logic has no effect on the controller output.
3.4 Engine Speed Controller Design

The job of the engine speed controller is to change the CVT ratio so that for a given throttle setting, the engine runs at its minimum fuel consumption speed. This is shown in Figure 3.5. The control algorithm was chosen to be a PI algorithm (the integral term is used to produce zero steady state error to a constant desired engine speed) with an antiwindup feature (the ratio has a lower limit of zero and the controller contains an integral term. See Section 3.2 and Appendix D). As discussed in Section 3.1, the output of the engine speed controller is a ratio set point $R_D$, which is implemented by the ratio control loop.

Simulation studies showed that the nonlinearity of the minimum fuel curve could produce instabilities in the control system. In particular, the curve (Figure 3.1) changes to a steep slope (large gain) for throttle settings above 45%; it was found that when the throttle made the transition from the low to high gain portions of the curve, the vehicle velocity could begin to oscillate. This instability was due, in part, to a rapid change in the engine speed set point. To slow down this rapid change, a low pass filter was placed immediately after the minimum fuel curve as shown in Figure 3.5. With the addition of this filter, the engine speed controller does not control to exactly the minimum fuel engine speed. However, it is unrealistic to expect the engine speed controller to follow rapid variations in desired engine speed; what is desirable is to track more gradual changes in optimum engine speed. Hence, the control loop controls to $\omega_A$ rather than $\omega_D$. 
Figure 3.5 Engine Speed Controller

The transfer function for the PI algorithm can be expressed as (ignoring the effects of the antiwindup logic)

\[
\frac{R_D(s)}{\omega_A(s) - x_1(s)} = \frac{K_{EP}s + K_{EI}}{s} \tag{3.8}
\]

where \(K_{EP}\) and \(K_{EI}\) are the proportional and integral gains, respectively. If we define the controller state as

\[
x_5 = R_D - K_{EP}(\omega_D - x_1) \tag{3.9}
\]

then the controller state and output equations can be expressed as

\[
\dot{x}_5 = K_{EI}(\omega_A - x_1) \tag{3.10}
\]

and

\[
R_D = x_5 + K_{EP}(\omega_A - x_1) \tag{3.11}
\]
The actual output $R_D$ is then modified by the antiwindup logic to produce the final desired ratio. The low pass filter transfer function is given as

$$\frac{\omega_A(s)}{\omega_D(s)} = \frac{1}{\tau_E s + 1} \quad (3.12)$$

where $\tau_E$ is the filter time constant and $\omega_D$ is the minimum fuel engine speed corresponding to the current throttle setting. If we define the filter state as

$$x_8 = \omega_A \quad (3.13)$$

then from (3.12)

$$\dot{x}_8 = -\frac{1}{\tau_E} x_8 + \frac{1}{\tau_E} \omega_D(u_1) \quad (3.14)$$

where the dependence of $\omega_D$ on $u_1$ is shown explicitly. Using (3.13) in (3.10) and (3.11) we have

$$\dot{x}_5 = K_{EI}(x_8 - x_1) \quad (3.15)$$

$$R_D = x_5 + K_{EP}(x_8 - x_1) \quad (3.16)$$

The state and output equations for the engine speed controller are thus given by (3.14), (3.15) and (3.16).

### 3.5 Ratio Control Loop

The ratio control loop is shown in Figure 3.6. In designing the ratio controller it is important to note that it is not necessary for the actual ratio, $x_3$, to equal the desired ratio,
$R_D$, in steady state. The ratio is being changed so that the engine speed equals the engine speed set point; the actual, final value of ratio which achieves this is unimportant. Hence the ratio controller need not contain an integral term for zero steady state error. This controller is therefore chosen to be a proportional controller only. Thus, from Figure 3.6,

$$u_2 = K_{RP}(R_D - x_3) \quad (3.17)$$

where $K_{RP}$ is the proportional gain of the ratio controller.

Using (3.16) in (3.17) we have

$$u_2 = K_{RP} \left[ x_5 + K_{EP}(x_8 - x_1) - x_3 \right] \quad (3.18)$$
The second order dynamics relating $x_3$ and $u_1$ are given by (2.4) and (2.5).

The value of $K_{RP}$ can be chosen to speed up the second order response of the ratio changing mechanism. In fact, this is the only reason for using a ratio control loop rather than having the engine speed controller generate $u_2$ and directly drive the ratio changing mechanism. It is important to note, however, that with a proportional ratio controller there is a second order system between the output of the engine speed controller and $x_3$, independent of whether the engine speed controller generates a set point for a ratio loop or generates the actuator input $u_2$ directly.

### 3.6 Summary of Closed-Loop State Equations

Since the closed loop-system state equations are spread throughout Section 2.0 and this section, it is useful to summarize them here for easy reference. First, the closed-loop system states are defined as

\[
\begin{align*}
x_1 &= \text{engine speed.} \\
x_2 &= \text{developed engine torque} \\
x_3 &= \text{CVT ratio.} \\
x_4 &= \dot{x}_3 \\
x_5, x_8 &= \text{states characterizing throttle controller.} \\
x_6, x_7 &= \text{states characterizing engine speed controller.}
\end{align*}
\]

The states $x_5$ through $x_8$ are not easily associated with physical variables because both controllers contain numerator dynamics.
The state equations are listed below using the equation number from previous sections.

\[
\begin{align*}
\dot{x}_1 &= \frac{x_2 - M_T x_3 (\phi_1(x_1, x_3) + \phi_2 + R_A R_W x_1 x_4)}{J_E + M_T R_A R_W x_3^2} \quad (2.2) \\
\dot{x}_2 &= -\frac{[x_2 - \phi_3(x_1, u_1)]}{\tau_L} \quad (2.3) \\
\dot{x}_3 &= x_4 \quad (2.4) \\
\dot{x}_4 &= C_2 x_3 + C_1 x_4 + C_3 u_2 \quad (2.5) \\
\dot{x}_5 &= K_E (x_8 - x_1) \quad (3.15) \\
\dot{x}_6 &= K_V (v_D - R_A R_W x_1 x_3) \quad (3.3) \\
\dot{x}_7 &= \frac{1}{\tau_T} (x_6 - x_7) + \frac{K_V P}{\tau_T} (v_D - R_A R_W x_1 x_3) \quad (3.7) \\
\dot{x}_8 &= \frac{1}{\tau_E} [-x_8 + \omega_D(u_1)] \quad (3.14)
\end{align*}
\]

where \(v_D\) is the driving cycle velocity, \(\omega_D(u_1)\) is the minimum fuel engine speed as a function of throttle setting (minimum fuel curve), \(u_1\) is the throttle input, \(u_2\) is the ratio actuator input, \(\phi_3\) is the steady state torque from the engine map, \(\phi_1\) reflects the effects of road load losses on engine
speed and $\phi_2$ reflects the effects of braking torque and grade on engine speed. The rest of the entries in the above equations are constants. Reference should be made to the appropriate prior section (determined by the equation number) for more details. The control inputs $u_1$ and $u_2$ are generated from the states by

$$
\begin{align*}
    u_1 &= \begin{cases} 
    100, & x_7 \geq 100 \\
    x_7, & K_1 \leq x_7 < 100 \\
    K_1, & x_7 < K_1
    \end{cases}
\end{align*}
$$

and

$$
    u_2 = K_{RP} \left[ x_5 + K_{EP}(x_8-x_1) - x_3 \right] \tag{3.18}
$$

Here, $K_1$ represents idle throttle (see Figure 3.4).

Having described the control approach and the details of the control system, we conclude this section with a brief discussion of how the control system might be implemented in an actual vehicle.

### 3.7 Control System Implementation

The control system is envisioned as being implemented with an on-board microcomputer-based system. The control algorithms discussed in the previous subsections are easily programmed on such a system, and the measurements required for control are all easily generated from standard sensors.

A block diagram of the control system showing the operator, control computer and vehicle is given in Figure 3.7. To
implement the control algorithms, the control computer requires measurements of vehicle velocity, engine speed and ratio. If the ratio is not measurable directly from the CVT, it can be calculated from engine speed and vehicle velocity (see Equation (2.6)). The control algorithms implemented by the computer are discrete time versions of equations (3.3), (3.7), (3.14), (3.15) and (3.18) (See Section 4.1 for the sampling time) which are given at the end of Section 3.6. These algorithms are easily implemented and do not require the use of component maps and interpolation.

![Computer Implemented Control System](Image)

**Figure 3.7** Computer Implemented Control System
It is assumed that the operator manipulates some sort of device (e.g. a pedal) to indicate desired velocity. Based on this demand, the control computer generates a throttle setting and a signal to change the ratio so that the desired velocity is achieved and the engine is running most efficiently. The computer also displays vehicle velocity to the operator. The brake pedal is assumed to be under the control of the operator. However, it is conceivable that the control computer could also generate braking actions to make the vehicle achieve a desired velocity. In fact, this approach was adopted in this study (see Figure 3.5). Having described the control system and the vehicle dynamics in this and the previous section, respectively, we now turn to a description of how the overall system was simulated in order to tune the controllers and study the dynamic behavior of the overall closed-loop system.
4.0 SYSTEM SIMULATION

The performance of the closed-loop system was evaluated using a digital computer simulation of the vehicle dynamics and the control algorithms. The vehicle was made to follow a specific velocity vs. time profile or driving cycle (SAE J227a, schedule D (modified)) as shown in Figure 4.1. The driving cycle velocity provided the command input to the throttle controller. In effect, the simulation solved the eight state equations describing the vehicle and controller dynamics for given initial conditions and the given driving cycle. The equations actually solved are given in Section 3.6; equations (2.2) through (2.5) describe the vehicle dynamics, while equations (3.3), (3.7), (3.14), (3.15) and (3.18) describe the controller dynamics and outputs. The simulation results are trajectories of vehicle and controller states and outputs (as the vehicle traverses the driving cycle) as well as vehicle energy consumption.

In the actual simulation, two different time scales were used for integrating the vehicle and controller state equations. The controller state equations were approximated with discrete time equivalents with a basic sampling period or time step size of 0.1 seconds. Hence the control inputs to the vehicle dynamics were updated every 0.1 seconds and held constant between updates. This was felt to be quite acceptable because it simulated what an on-board computer would actually do; the computer would generate piecewise constant controls updated
Figure 4.1 Driving Cycle SAE J227a, Schedule D (modified)

Vehicle Desired Velocity (km/h)

Time (s)
only at sampling instances. On the other hand, the vehicle state equations were integrated using a variable step size Runge-Kutta integration scheme which produced an average step size which was orders of magnitude smaller than 0.1 second. This, of course, makes sense since the vehicle is a continuous system and not piecewise constant as are the controller outputs.

The simulation program was organized into several Fortran subroutines whose primary purposes are listed in Table 4.1. Subroutines PHI3, PHI4 and PHI6 use steady-state engine characteristics, in the form of table or "maps", and interpolate as necessary to yield the desired results. A detailed listing of the simulation program is given in Appendix C.
<table>
<thead>
<tr>
<th>Subroutine</th>
<th>Purpose</th>
</tr>
</thead>
<tbody>
<tr>
<td>MAIN</td>
<td>Inputs data, coordinates simulation of system for driving cycle, computes control inputs, outputs results.</td>
</tr>
<tr>
<td>NIN</td>
<td>Numerically integrates state equations using 4th order Runge-Kutta method.</td>
</tr>
<tr>
<td>RHS</td>
<td>Computes right hand side of state equations for NIN.</td>
</tr>
<tr>
<td>PHI1</td>
<td>Computes drag and rolling resistance.</td>
</tr>
<tr>
<td>PHI2</td>
<td>Computes braking torque and effect of grade angle on vehicle.</td>
</tr>
<tr>
<td>PHI3</td>
<td>Computes steady state engine torque for given throttle and engine speed.</td>
</tr>
<tr>
<td>PHI4</td>
<td>Computes most fuel-efficient steady state engine speed for given throttle position.</td>
</tr>
<tr>
<td>PHI5</td>
<td>Limits the CVT ratio within pre-defined bounds.</td>
</tr>
<tr>
<td>PHI6</td>
<td>Computes steady state fuel rate for given engine speed and throttle.</td>
</tr>
<tr>
<td>VSP</td>
<td>Calculates driving cycle velocity for any time.</td>
</tr>
</tbody>
</table>

Table 4.1 Simulation Program Subroutines
5.0 SIMULATION RESULTS

The overall objective of the simulation was to study the feasibility of the control approach described in the preceding sections. In particular, the simulation revealed the degree to which the controllers described in Section 3.0 can control the propulsion system, the ease or difficulty of tuning the controllers, and the nature of the resulting dynamic behavior of the vehicle. We consider these results in the subsections below.

5.1 Controller Tuning

The controllers were tuned so that the vehicle satisfactorily followed the specific driving cycle shown in Figure 4.1. The driving cycle consisted of an acceleration phase followed by a cruise phase and, finally, a braking phase. Two different (but constant) decelerations were assumed for the braking phase. The driving cycle served as a velocity command input to the propulsion control system.

Three controllers required tuning: the vehicle velocity or throttle controller, the engine speed controller and the ratio controller. In addition, the time constants of the two smoothing filters (one after the minimum fuel curve and one after the velocity PI controller) had to be selected. Specifically, it was necessary to select values for the proportional and integral gains, $K_{VP}$ and $K_{VI}$, respectively, of the throttle controller, the proportional and integral gains, $K_{EP}$ and $K_{EI}$, respectively,
of the engine speed controller, the proportional gain, $K_{RP}$, of the ratio controller, and the two filter time constants, $\tau_E$ and $\tau_T$.

Since the ratio control loop (see Figure 3.6) consists of the proportional control of a known, second order system, the gain, $K_{RP}$, was determined analytically; the particular value was chosen so that the ratio loop responded as a critically damped second order system to a step change in the ratio set point. Furthermore, it was found from repeated runs of the simulation that a time constant of 1.0 seconds for both filters provided adequate smoothing.

Generally speaking, an iterative process was used to select the gains for the throttle and engine speed PI controllers. The throttle controller was first tuned to obtain as close a match as possible between driving cycle velocity and vehicle actual velocity ("close" was measured by a combination of velocity mean square error and visual examination of the velocity profile). Then the engine speed controller was adjusted to obtain as close a match as possible between actual and desired engine speed ("close" measured by mean square error). Each time any of the four gains was changed, a resimulation of the complete driving cycle was required to evaluate the effects of the gain change. The process was repeated until no significant overall improvement in either the velocity error or engine speed error was obtained; although time consuming, the procedure did converge to a set of gain values which gave
reasonably good dynamic response of the vehicle. The specific values for the controller gains are given in Appendix B. An example of responses which are representative of the best responses are given in Figures 5.1 through 5.4. These are discussed in detail in the next subsection.

5.2 Closed Loop Dynamic Response of the Vehicle

The dynamic responses of interest for the closed loop system are those of vehicle velocity, CVT ratio, engine speed and throttle setting.

Figures 5.1 through 5.4 show examples of the best responses obtained. In interpreting these curves, it should be remembered that for a given vehicle velocity, an increase in ratio is required to produce a decrease in engine speed. The basic response of the vehicle is summarized as follows: Initially the vehicle is at rest with an idle throttle, an idle engine speed and a zero ratio. As the driving cycle starts, the velocity error causes the throttle to increase. This in turn causes both the engine speed and its set point (via the minimum fuel curve) to increase. The engine speed is actually above the set point, so the ratio increases to bring this speed down. At about 45% throttle there is a rapid increase in engine speed set point (due to the nonlinear minimum fuel curve) which causes the ratio to drop to bring up the engine speed. This type of dynamical behavior continues (with the ratio slowly increasing again as the engine speed overshoots the set point) until the cruise part of the driving cycle is reached. At this point the
Figure 5.1  Vehicle Velocity

Figure 5.2  Engine Speed
Figure 5.3 CVT Ratio

Figure 5.4 Throttle
velocity error rapidly decreases causing the throttle to drop off sharply. This, in turn, causes a rapid drop in desired engine speed via the minimum fuel curve to bring the engine speed down the ratio therefore increases to about 2.3. When the cruise period is complete, it is necessary to apply various amounts of braking torque to make the vehicle follow the driving cycle from cruise down to a stopped condition. During this time, the throttle is constant at idle position and the engine speed makes small excursions below the idle speed desired. Finally, the vehicle comes to a stop as a result of sufficient braking torque and the ratio approaching zero.

The responses demonstrate that the control system is capable of making the vehicle follow the driving cycle velocity profile while at the same time keeping the engine at the minimum fuel consumption engine speed; Figure 5.2 shows that there is very little error between desired and actual engine speed. Although the vehicle's actual velocity is quite close to the driving cycle velocity, there is some error during the acceleration phase and at the start of the cruise phase. To a large extent, this is due to the classical tradeoff in control system design between tracking error and transient response. If the velocity controller gain is increased so that the vehicle tracks the velocity ramp in the acceleration phase more closely, the transient response will be made more oscillatory and there will be a larger overshoot when the cruise phase is reached. In addition, as discussed later, increasing this gain to reduce
the tracking error can also introduce instabilities when the vehicle first begins to accelerate.

In tuning the controllers to produce the above responses a number of observations were made concerning the sensitivity of the responses to controller gain values, and instabilities and unexpected dynamic behavior of the closed loop system. These observations are given below.

With regard to controller tuning, it was found that the responses of the vehicle variables were rather sensitive to choices for the controller gain values. This was due in large part to the nonlinearities of the vehicle and, particularly, the nonlinear minimum fuel curve. Examination of Figure 3.1 shows that the minimum fuel engine speed is a highly nonlinear function of throttle setting; examination of Figure 3.3 reveals that this nonlinearity acts as a nonlinear gain in the loop which is controlling engine speed by manipulating the ratio. The presence of a nonlinear gain makes it particularly difficult to come up with one set of controller gains which will give good transient response over a wide range of vehicle operation. If the controller gains are selected to give good transient response for throttle settings below 45% (the low gain region on the curve), then during acceleration when the throttle moves into the region above 45% (high gain region) the loop gain goes up markedly and the response will tend to be oscillatory. In fact, complete instability of all four
variables during the acceleration phase of the drive cycle was often observed in the process of tuning the controllers. The final method used to deal with this nonlinear gain was a worst case approach: choose controller gains so that good performance was achieved in the high gain region of the minimum fuel curve; the closed-loop system would then be a little sluggish in the low gain region of the curve, but it would not produce oscillations in ratio, throttle and vehicle velocity.

Two other approaches to deal with this nonlinear gain which were considered but ultimately discarded are outlined below. First, with reference to Figure 3.3, a nonlinear gain was introduced at the output of the throttle controller; the output of this nonlinear gain was the throttle setting, \( u_1 \). The new nonlinearity was chosen to exactly compensate for the minimum fuel curve nonlinearity; in effect the gain in the engine speed control loop was made to be linear and the nonlinearity of the minimum fuel curve was shifted to the vehicle velocity control loop. It was felt that the performance of this latter loop might be less sensitive to the presence of a nonlinear gain. However, this did not turn out to be the case and the approach was abandoned. The second approach was similar to the first: the gains of the velocity PI controller were made to depend on the throttle position. In effect, the gains were decreased if the system was operating on the high gain portion of the minimum fuel curve. This approach exhibited instabilities as the system was passing from one gain region to the next, and so was also abandoned.
As mentioned above, an approach which gives satisfactory results is to tune the controller for the worst case where the system is operating on the steep part of the minimum fuel curve. Alternatively, consideration should be given to using an approximate, linear minimum fuel curve. It is not practical to control the engine speed to exactly the minimum fuel consumption engine speed for each throttle setting; the throttle is continually changing and there is always lag in the engine speed control loop. It would appear that the use of an approximate, linear minimum fuel curve will lead to both good fuel consumption characteristics and good dynamic response of the vehicle.

We now discuss the actual dynamic responses observed for the vehicle velocity, engine speed, ratio and throttle setting; instabilities and unusual dynamic responses observed during the simulation runs are discussed. We begin this discussion by first noting that the control loop on vehicle velocity and the one on engine speed are highly interacting. Throttle is used to control velocity, while ratio is used to control engine speed. This can be viewed as a two input/two output system as shown in Figure 5.5. The strong interaction between the loops comes about because a change in throttle (with ratio constant) will cause a change in both vehicle velocity and engine speed; similarly, a change in ratio (with throttle constant) will produce a change in both velocity and engine speed. Furthermore, the throttle setting (control input for
the top loop Figure 5.5) determines the set point for the bottom loop. Hence a change in throttle forces a change in ratio. This strong and unusual type of interaction (the set point of one loop determined from the control input to another loop) makes this system very difficult to control.

Figure 5.5 Two Input/Output Model of Control System

A typical instability in all four variables observed during the simulation runs was at start-up when the vehicle first begins to traverse the driving cycle (see Figure 5.5). The sequence of events is as follows. The desired velocity increases above zero, causing the throttle setting to increase above idle throttle. The vehicle will not move, however,
until the ratio comes off zero. This will begin to occur in
this instance because as the throttle setting increases, the
desired engine speed also increases; this produces an engine
speed error which causes the ratio to increase from zero.
The instability begins to show up if either or both of the pro-
portional gains of the controllers are too large. In this
case, as the desired velocity initially increases there is a
large throttle increase for the essentially unloaded engine
(ratio is still close to zero). This causes the engine speed
to increase rapidly and become much larger than the desired
minimum fuel engine speed set point corresponding to the throt-
tle setting. This large engine speed error, in turn, causes
a large increase in the ratio in an attempt to bring the engine
speed down. The increased ratio and large throttle setting
cause the vehicle to accelerate rapidly, resulting in a vehicle
velocity which is much greater than the desired velocity cor-
responding to the driving cycle. Also, the engine speed has
now dropped below the set point due to the load placed on the
engine. At this point the sequence of events is reversed: to
counteract the large velocity error the throttle is set back
to almost idle; the desired engine speed corresponding to this
lower throttle is still above the actual engine speed, hence
the ratio drops to almost zero. This causes the vehicle to
come to a standstill, causing the throttle in turn to once
again increase by a large amount. The cycle is then repeated.
The gains which cause the above instability are not unreasonable. For example, the instability was initially observed while attempting to tune the controllers by increasing the proportional gains so that the vehicle would more closely follow the ramp of desired velocity during the acceleration phase of the driving cycle. The start-up instability described above was the determining factor in how large the proportional gains could be made; keeping the gains low to avoid the instability produced a noticeable velocity error during the acceleration phase of the driving cycle (see Figure 5.1). This error could not be reduced by increasing the integral gain of the velocity controller because such an increase would produce too much velocity overshoot when the cruise phase of the driving cycle was reached (again, see Figure 5.1). The integral gain finally selected represented a tradeoff between velocity error during the acceleration phase and velocity overshoot when the cruise phase is reached.

A second, and quite dramatic, instability occurred during either the acceleration or cruise phase of the driving cycle. As with the start-up instability described above, this instability is a consequence of the pronounced interactions in the system, i.e. throttle changes and ratio changes each have a strong effect on both vehicle velocity and engine speed. If the controllers are not tuned properly, this interaction can cause the vehicle to actually speed up as that throttle is decreased during either the acceleration or cruise phase of the driving cycle. Responses of the system variables showing this
instability are given in Figures 5.6 through 5.8. It must be remembered in examining these responses that they represent the case of improperly tuned controllers; they are included only because of the interacting instability they reveal.

Between about 15 seconds and 30 seconds the throttle is decreasing dramatically, yet the vehicle velocity continues to increase. Similarly, from 40 seconds to about 50 seconds the throttle increases while the vehicle velocity decreases. This phenomenon is due to the strong effect that both ratio and throttle have on vehicle velocity; the behavior from 15 to 30 seconds is explained as follows (the behavior from 40 to 50 seconds is explained by just the opposite reasoning). As the throttle is decreased to slow down the vehicle, the desired engine speed also decreases; this causes the ratio to increase in an attempt to bring the engine speed down. However, increasing the ratio also speeds up the vehicle, resulting in a further decrease in the throttle. If the ratio change has a greater effect on the vehicle velocity than the throttle change (which can occur in certain operating regions) then the above sequence of events will cause the vehicle to speed up as the throttle is decreased.

This type of behavior would, of course, be unacceptable to a human driver; less throttle means the vehicle must, within a short time, slow down, not speed up. In effect, what is occurring above is that the vehicle is being driven by the ratio, i.e. the ratio rather than the throttle is having the dominant
Figure 5.6 Vehicle Velocity for Improperly Tuned Controllers
Figure 5.7 Ratio for Improperly Tuned Controllers

Figure 5.8 Throttle for Improperly Tuned Controllers
effect on vehicle velocity and it is being manipulated in a way to maintain the vehicle velocity at the driving cycle set point velocity. The problem is avoided by proper tuning of both controllers.

5.3 Conclusions

The experience gained from numerous simulations and from working with the controllers has led to a number of conclusions regarding the feasibility of the control philosophy and approach described in the preceding pages of this report. To reiterate, the control philosophy is to minimize fuel consumption by manipulating throttle to achieve vehicle desired velocity and by manipulating ratio so that, for each throttle setting, the engine is operated at its minimum fuel consumption point. The simulation results demonstrate that it is feasible to control a vehicle in such a manner, and it is possible to do it with relatively simple controllers (PI controllers with anti-windup logic) which use easily measured system variables (CVT ratio, engine speed and vehicle velocity). Furthermore, there would be no difficulty in implementing the control system with an on-board microcomputer.

The simulation results also demonstrate that the vehicle nonlinearities and the minimum fuel curve nonlinearity can cause instabilities in vehicle operation both at start up and during the acceleration and cruise phases of the driving cycle. These instabilities can be avoided by proper tuning of the
controllers. To simplify the job of tuning the controllers, and to minimize the possibility of producing an instability, consideration should be given to replacing the nonlinear minimum fuel curve with a straight line approximation, i.e. minimum fuel engine speed should be approximated by a linear function of throttle setting.
6.0 CONCLUSIONS AND FUTURE WORK

This project has demonstrated, for the first time, that it is possible to achieve satisfactory, stable control of all significant dynamic variables of a heat engine-CVT vehicle propulsion system by designing linear control loops for control of engine speed, throttle position and CVT ratio. The system simulation has illustrated the difficulty of controlling this nonlinear system which exhibits strong interaction between the input variables (CVT ratio and throttle) and output variables (engine speed and vehicle speed).

The feasibility of controlling the propulsion system so that the vehicle followed the modified SAE driving cycle was demonstrated by the simulation. Satisfactory dynamic responses of the variables were accompanied by a low average deviation of the engine speed from its desired, low fuel consumption value.

The control algorithms developed were in a simple, linear form which could easily be implemented on-board a vehicle using a microcomputer.

Future work could be concerned with adding a flywheel for energy storage to the system as investigated to date, and then to investigate the resultant control problems. Before such an investigation could be started, it would be necessary to define decision rules or strategies for using two sources of on-board energy, the engine and the flywheel. Thus, a prime candidate for near term future work is an investigation of power flow strategies for a vehicle with two (or more) on-board power
sources. This should be followed by investigations into implementing these strategies using control systems.
7.0 REFERENCES


APPENDIX A

VEHICLE MODEL

Section 2.0 of the report presents an overview of the methods used to model the vehicle and the resulting state equations which describe the vehicle dynamics. This Appendix is devoted to a detailed presentation of this material. In developing the vehicle model, the following variables will be used (Appendix B contains a complete list of all variables and parameters used in the vehicle model):

\[ D = \text{vehicle drag force.} \]
\[ J_{EQ} = \text{equivalent load inertia as seen by the CVT.} \]
\[ R = \text{vehicle rolling resistance force.} \]
\[ R_T = \text{CVT ratio.} \]
\[ T_A = \text{torque required at rear axle.} \]
\[ T_B = \text{braking torque.} \]
\[ T_E = \text{actual torque developed by the engine.} \]
\[ T_L = \text{equivalent load torque as seen by the CVT.} \]
\[ T_m = \text{steady state engine torque.} \]
\[ T_1 = \text{load torque seen by the engine.} \]
\[ u_1 = \text{throttle setting.} \]
\[ u_2 = \text{ratio actuator input.} \]
\[ v = \text{vehicle velocity} \]
\[ v_w = \text{wind velocity} \]
\[ x_1 = \text{vehicle first state}(= \omega_E). \]
\[ x_2 = \text{vehicle second state}(= T_E). \]
\[ x_3 = \text{vehicle third state}(= R_T). \]
\[ x_4 = \text{vehicle fourth state}(= R_T). \]
$\beta$ = grade angle.

$\omega_E$ = engine speed.

$\omega_D$ = drive shaft speed.

The drive train of the vehicle is shown in Figure A1 and consists of a heat engine (HE), a continuously variable transmission (CVT), and a differential to transmit power from the drive shaft to the rear axle and wheels. Before deriving the equations which govern the overall dynamics of the vehicle, we first present the methods used to model each of the individual components.

Figure A1  **Drive Train Configurations**

**Heat Engine**: The heat engine model is shown in Figure A2 and consists of a steady state engine map (which determines a steady state engine torque, $T_m$, for a given throttle setting, $u_1$, and engine speed, $\omega_E$), a first order lag which models the throttle linkage and engine combustion dynamics (see Section 2.1 under heat engine model), and a rotating inertia.
Continuously Variable Transmission: The CVT is modeled as shown in Figure A3 and consists of an inertia $J_T$, an efficiency $K_T$ and a ratio, $R_T$, which is allowed to vary continuously from zero to infinity. The inertia is defined to be the equivalent CVT inertia as seen on the drive shaft side of the CVT. It is also assumed that there are second order dynamic effects associated with changing the ratio, i.e. if there is a step change in the variable, $u_2$, which controls the ratio, then the actual ratio will respond with a second order response.

Figure A3 CVT Model
**Differential:** The differential is modeled in exactly the same way as the CVT, except that the ratio is fixed; hence there is a differential inertia, $J_A$ (defined to be the inertia of the differential as seen on the axle side of the differential), an efficiency, $K_A$, and a ratio, $R_A$ (defined to be the ratio of axle speed to drive shaft speed).

**Vehicle Body:** The vehicle body is assumed to consist of a mass to be accelerated (up or down a grade, as necessary) which is subject to aerodynamic drag and rolling resistance forces and braking torque.

In deriving the equations which describe the dynamic behavior of the drive train and vehicle body, we combine all of the inertias downstream of the CVT with the CVT inertia to form an equivalent load inertia; we also develop an expression for an equivalent CVT load torque which includes the combined effects of the aerodynamic drag and rolling resistance forces, the braking torque and the force necessary to accelerate the vehicle mass. The overall model is shown in Figure A4. In addition, as mentioned earlier, the CVT ratio, $R_T$, has a second order dynamic response to a change in the ratio actuator input, $u_2$, as shown in Figure A3. Finally, the engine model includes a first order lag between the engine map and the developed engine torque, $T_E$, to simulate the dynamics of the throttle linkage and engine combustion. This is shown in Figure A2.
Figure A4  Overall Model of Drive Train

From Figure A4 we can write

\[ J_E \dot{\omega}_E = T_E - T_1 \]  \hspace{1cm} (A1)

\[ J_{EQ} \dot{\omega}_D = \left( \frac{T_1}{R_T} \right) - T_L \]  \hspace{1cm} (A2)

and

\[ \omega_D = R_T \omega_E \]  \hspace{1cm} (A3)

where \( J_E \) is the engine inertia. Differentiating (A3) and noting that the ratio is time varying, we get

\[ \dot{\omega}_D = R_T \dot{\omega}_E + R_T \dot{\omega}_E \]  \hspace{1cm} (A4)

Using (A4) in (A2) and solving for \( T_1 \) yields

\[ T_1 = R_T J_{EQ} (R_T \dot{\omega}_E + R_T \dot{\omega}_E) + R_T T_L \]  \hspace{1cm} (A5)

Then using (A5) in (A1) we can write

\[ J_E \ddot{\omega}_E = T_E - R_T J_{EQ} (R_T \dot{\omega}_E + R_T \dot{\omega}_E) - R_T T_L \]

or
It is now necessary to develop expressions for $J_{EQ}$ and $T_L$ to substitute into (A6). First consider $J_{EQ}$. This inertia consists of the sum of the CVT inertia, $J_T$, plus the differential inertia reflected through the differential ratio and taking into account the CVT efficiency (see Figure A3; note that $J_T$ is upstream of $K_T$ and that the equivalent inertia $J_{EQ}$ is being computed at the position of $J_T$), and the combined axle and wheel inertias, $J_W$, reflected through the differential ratio and taking into account the efficiencies of both the differential and the CVT. Following standard procedures for reflecting inertias, we can write

$$J_{EQ} = R_T + \left(\frac{R_A^2}{K_T}\right)J_A + \left(\frac{R_A^2}{K_T}\right)J_A + \left(\frac{R_A^2}{K_A K_T}\right)J_W$$

(A7)

Next, we derive an expression for the equivalent load torque, $T_L$, as seen by the CVT. The forces acting on the vehicle are given as

Drag Force = $D = \frac{1}{2}(\rho / g)C_D A (v + v_W)^2 \text{sgn}(v + v_W)$

(A8)

Rolling Resistance Force = $R = \mu W (1 + 1.4 \times 10^{-3}v + 1.2 \times 10^{-5}v^2)$

(A9)

Acceleration Force = $(W/g)v$

(A10)

Grade Force = $W \sin \theta$

(A11)

Multiplying the sum of these forces by the wheel radius, and adding the braking torque to the result, we obtain the torque.
\( T_A \), required at the axle necessary to provide the vehicle with acceleration \( \dot{v} \):

\[
T_A = R_W[D + R + W\sin\beta + (W/g)\dot{v}] + T_B \tag{A12}
\]

Reflecting this torque through the differential efficiency and ratio, and through the CVT efficiency, we obtain

\[
T_L = T_A \left( \frac{R_A}{K_A K_T} \right) \tag{A13}
\]

Finally, we note that

\[
v = R_A R_W R_T \omega_E \tag{A14}
\]

and

\[
\dot{v} = R_A R_W (R_T \omega_E + R_T \dot{\omega}_E) \tag{A15}
\]

We are now in a position to derive the first (of four) state equations which govern the vehicle dynamics. Substituting (A14) and (A15) into (A12), and that result into (A13), we can express \( T_L \) as a function of \( \omega_E \) and \( \dot{\omega}_E \) rather than \( v \) and \( \dot{v} \). Then substituting that result for \( T_L \) along with (0) into (A6), and using the notation \( x_1 = \omega_E \), \( x_2 = T_E \), \( x_3 = R_T \) and \( x_4 = \dot{R}_T \), we get

\[
\dot{x}_1 = (x_2 - M_T x_3) (\phi_1 + \phi_2 + R_A R_W x_1 x_4)/(J_E = M_T R_A R_W x_3^2) \tag{A16}
\]

where

\[
\phi_1 = R_A R_W(D+R)/M_T K_A K_T \tag{A17}
\]

\[
\phi_2 = R_A (T_B + k_W W\sin\beta)/M_T K_A K_T \tag{A18}
\]
\[ M_T = \left( \frac{J_T}{R_A R_W} \right) + \left( R_A J_A K_T R_W \right) + \left( R_A R_W M_V K_T K_A \right) \]  \hspace{1cm} (A19)

\[ M_V = \left( \frac{W}{g} \right) + \left( \frac{J_W}{R_W^2} \right) \] \hspace{1cm} (A20)

The above state equation describes the response of engine speed, \( x_1 \) to changes in developed engine torque, \( x_2 \), CVT ratio, \( x_3 \) and \( x_4 \), grade angle, \( \beta \), braking torque, \( T_B \), and wind velocity, \( v_W \). Given engine speed, vehicle speed can be determined from (A14).

The second state equation describes the response of developed engine torque to changes in engine speed and throttle setting (Characterizes throttle linkage and engine combustion dynamics, as well as engine steady-state torque-speed characteristics). Referring to Figure A5 we can write

\[ x_2 = - \left[ x_2 - \phi_3(x_1, u_1) \right]/\tau_L \]  \hspace{1cm} (A21)

where \( u_1 \) is throttle setting and \( \phi_3(x_1, u_1) \) is the torque from the steady state engine map.

The third and fourth state equations describe the second order dynamic response of the ratio, \( x_3 = R_T \), to changes in the ratio actuator input, \( u_2 \). In particular,

\[ x_3 = x_4 \] \hspace{1cm} (A22)

\[ x_4 = C_1 x_4 + C_2 x_3 + C_3 u_2 \] \hspace{1cm} (A23)

where \( C_1, C_2 \) and \( C_3 \) are constants which determine the actuator gain and second order dynamics.

Equations (A16), (A21), (A22) and (A23) are the vehicle state equations used in the study.
## APPENDIX B: PARAMETER VALUES

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>frontal area of vehicle</td>
<td>2.00 m²</td>
</tr>
<tr>
<td>C_D</td>
<td>vehicle drag coefficient</td>
<td>0.45</td>
</tr>
<tr>
<td>C_1</td>
<td>constant describing actuator dynamics</td>
<td>-12.0 s⁻¹</td>
</tr>
<tr>
<td>C_2</td>
<td>constant describing actuator dynamics</td>
<td>-12.0 (s²)⁻¹</td>
</tr>
<tr>
<td>C_3</td>
<td>ratio actuator gain constant</td>
<td>20.0 (v-s²)⁻¹</td>
</tr>
<tr>
<td>g</td>
<td>gravity constant</td>
<td>9.807 m/s²</td>
</tr>
<tr>
<td>J_A</td>
<td>inertia of differential (as seen on axle side of differential)</td>
<td>0.02 m²-kg</td>
</tr>
<tr>
<td>J_E</td>
<td>engine inertia</td>
<td>0.113 m²-kg</td>
</tr>
<tr>
<td>J_T</td>
<td>CVT (drive shaft side of CVT)</td>
<td>0.60 m²-kg</td>
</tr>
<tr>
<td>J_W</td>
<td>combined inertia of all four wheels</td>
<td>7.052 m²-kg</td>
</tr>
<tr>
<td>K_A</td>
<td>efficiency of differential</td>
<td>0.96</td>
</tr>
<tr>
<td>K_EI</td>
<td>integral gain, engine speed controller</td>
<td>0.09 rad⁻¹</td>
</tr>
<tr>
<td>K_EP</td>
<td>proportional gain, engine speed controller</td>
<td>0.018 s/rad</td>
</tr>
<tr>
<td>K_RP</td>
<td>ratio proportional controller gain</td>
<td>2.6 v</td>
</tr>
<tr>
<td>K_T</td>
<td>efficiency of transmission</td>
<td>0.9</td>
</tr>
<tr>
<td>K_VI</td>
<td>integral gain, velocity controller</td>
<td>1.8 m⁻¹</td>
</tr>
<tr>
<td>K_VP</td>
<td>proportional gain, velocity controller</td>
<td>20.4 s/m</td>
</tr>
<tr>
<td>R_A</td>
<td>differential ratio (ratio of axle speed to drive shaft speed)</td>
<td>0.362</td>
</tr>
<tr>
<td>R_W</td>
<td>vehicle wheel radius</td>
<td>0.295 m</td>
</tr>
<tr>
<td>W</td>
<td>vehicle total weight</td>
<td>15,124 n</td>
</tr>
<tr>
<td>β</td>
<td>grade angle</td>
<td>0.0</td>
</tr>
<tr>
<td>μ</td>
<td>coefficient of rolling friction</td>
<td>0.0154 n/kg</td>
</tr>
<tr>
<td>ρ</td>
<td>air weight density</td>
<td>12.02 n/m³</td>
</tr>
<tr>
<td>τ_E</td>
<td>engine speed filter time constant</td>
<td>1.0 s</td>
</tr>
<tr>
<td>τ_T</td>
<td>throttle filter time constant</td>
<td>1.0 s</td>
</tr>
<tr>
<td>τ_L</td>
<td>Time constant: linkage dynamics</td>
<td>0.5 s</td>
</tr>
</tbody>
</table>
APPENDIX C: LISTING OF SIMULATION PROGRAM

```
0001 FTN4,L
0002 PROGRAM HCVT(3,100)
0003 C *****************************************************************
0004 C ********** HEAT ENGINE/CVT SYSTEM SIMULATION *****************
0005 C ****************************************************************
0006 C*****************************************************************************
0007 C*****************************************************************************
0008 C*****************************************************************************
0009 C*****************************************************************************
0010 C*****************************************************************************
0011 C*****************************************************************************
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0046 C*****************************************************************************
0047 C*****************************************************************************
0048 C*****************************************************************************
0049 C*****************************************************************************
0050 C*****************************************************************************
0051 C*****************************************************************************
0052 C*****************************************************************************
0053 C*****************************************************************************
0054 C*****************************************************************************
0055 C*****************************************************************************
A=VEH. FRONTAL AREA,(M**2).
BP=XMISSION DAMPING FACTOR.
CD=VEH. DRAG COEFF.
DCP=DRIVING CYCLE PERIOD,(S).
ENGMAP(I,J)=ENG. TORQUE WHEN ENG. SPEED IS ENGSP(I) AND PEDAL IS PEDPCT(J), (N-M).
EW=ENG. SPEED ERROR,(R/S).
FUELFUEL CONSUMP. RATE FOR GIVEN ENG. SPEED AND PEDAL,(LBS/HR).
G=GRAVITY CONST.,(N/S**2).
INPRN=NO. OF SIMUL. STEPS BETWEEN RESULTS PRINTS.
JPR=COUNTER USED TO DETERMINE IF PRINT/OUT SHOULD OCCUR.
KA=EFF. OF REAR AXLE DIFF.'L.
KCEI,KCEP=INTEGRAL AND PROP. GAINS, ENG. SPD. CONTROLLER.
KP=SPR. CONST. OF XMISSION RATIO MOVABLE PULLEY.
KR=XMISSION PULLEY: RATIO/DISPLACEMENT GAIN.
LL=L+1.
MP=MASS OF XMISSION PULLEY.
MT=COMPOSITE EXPRESSION USED IN VDOT EQN.,(KG-M).
MWF,MWR=COMBINED MASS OF FRONT AND REAR WHEELS,(KG).
N=n+1.
NMP=N-1.
NPPRMAX=NO. OF OUTPUT LINES PRINTED PER PAGE.
OMAGAE=ENG. SPEED,(RAD/SEC).
OMP=VALUE OF ENG. SPD. SET PT. USED FOR PRINTING.
PEDL=VALUE OF PDL. USED IN RHS PEDPOS(I)=VALUE OF PDL. CORR. TO I, USED IN ENGINE MAP.
PHI1=FCN WHICH COMPUTES EFFECTS OF DRAG AND ROLLING RESISTANCE.
PHI2=FCN WHICH COMPUTES ENG TORQUE FOR KRK. TORQUE AND GRADE.
PHI3=COMPUTES ENG SPED SET PT. FOR
GIVEN ENG SPD AND PEDAL.

MIN FUEL CONSUMPTION.

PL=THROTTLE SETTING.
RA=REAR AXLE RATIO.
RHS=COMPUTES RIGHT HAND SIDE OF STATE EQNS.
RM1=REAL VALUE OF NM1.
RSPMAX=MAX ALLOW VALUE OF RSP.
RSP_PROP=CONTRIB TO RSP FROM PROP PART OF RSP PI CONTROLLER.
RTMIN=MIN VALUE OF RATIO.
SIMPER=SIMULATION LENGTH,(SECS).
TAUL=TIME CONST OF ENG. TORQ,(S)
TBF,TBR=BRAKING TORQUES,FRONT AND REAR WHEELS,(N-M)
TBF,TBR=COMPUTES BRAKING Torque.
VDC(I)=DR CYCLE VEL PROFILE,M/S
VDC(I)=PRESENT VALUES OF STATES USED BY NIN.

****************************** *************#**************%c*

**************************** *******************************

IWRTE=CHANGES DATA OUTPUT, =0 NRUN=NO. OF RUNS OF SIMULATION
IWRTE=CHANGES DATA OUTPUT, =0 NRUN=NO. OF RUNS OF SIMULATION

PHI=COMPUTES FUEL CONSUMP.
PHI6=COMPUTES FUEL CONSUMP.
R=ROLLING RESISTANCE,(N).
RHO=AIR WT. DENSITY,(KG/M**3)
RL=REAL VALUE OF L
RL=REAL VALUE OF L
RLM=LIMITED VALUE OF RATIO.
RLM=LIMITED VALUE OF RATIO.

***********************************************************
***********************************************************

ADDITIONAL SYSTEM VARIABLES
ADDITIONAL SYSTEM VARIABLES

***********************************************************
***********************************************************

DECLARE COMMONS, DIMENSIONS, REALS, EXTERNALS.
DECLARE COMMONS, DIMENSIONS, REALS, EXTERNALS.

COMMON LL,PEDL,VW(501),VDC(2001),TBF,TBR,BETA(501),C(91),JE,TAUL,K
COMMON LL,PEDL,VW(501),VDC(2001),TBF,TBR,BETA(501),C(91),JE,TAUL,K
0112 101),DCP,TBMAX,KCEI,KCEP,KPDP,RSP,RNM1
0113 COMMON/CC/PIDLE,VVEL
0114 COMMON/DD/PD
0115 REAL JE,KA,KCR,KP,KR,KT,MP,MU,MV,KG,KPDI,KCEI,KCEP,KPDP
0116 COMMON/AA/I
0117 COMMON/BB/ENGMAP(19,iO),ENGSP(i9),PEDPCT(10),FURATE(i9,i0),PEDPOS(
0118 121),OPTSP(21),RTMIN,RTMAX
0119 DIMENSION Y(iS)
0120 REAL JA,JT,JWF,JWR,MWF,MWR
0121 C EXTERNAL USED TO DENOTE SUBROUTINE NAME SPECIFIED IN A SUBROUTINE
0122 C
0123 C FORMAT STATEMENTS.
0124 400 FORMAT(BF10.4)
0125 401 FORMAT(F10.4,5I5)
0126 402 FORMAT(F10.4,4I5)
0127 403 FORMAT(F10.4,3I5)
0128 500 FORMAT(IH1,3H SIMULATION OF HEAT ENGINE/CVT SYSTEM)
0129 501 FORMAT(IH0,3X,2HA=,F8.4,2X,3HP=,F8.4,2X,3HC=,F8.4,2X,2HM=,F8.4,2X
0130 1X,3HA=,F8.4,2X,3JJ=,F8.4,2X,3HT=,F8.4,2X,6HPIDLE=,F8.4)
0131 502 FORMAT(IH0,1X,4HJWF=,F8.4,1X,4HJWR=,F8.4,1X,5HKCEI=,F8.4,1X,
0132 5HKCEP 1=,F8.4,1X,4HKCR=,F8.4,2X,SHKPDI-,F8.4,2X,SHKPDP=,F8.4)
0133 503 FORMAT(IH0,2X,3HKR=,F8.4,2X,3HMP=,F8.4,2X,3HRW=,F8.4
0134 1,3X,2HW=,F12.4,2X,4HDCP=,F8.4,2X,3HKG=,F8.4,2X,3HKP=,F8.4)
0135 504 FORMAT(IH0,6X,3HNU=,F8.4,5X,4HRHO=,F8.4,3X,5HTAUL=,F8.6,3X,
0136 6HTBMAX
0137 1=F8.4)
0138 505 FORMAT(IH0,16H WIND VELOCITY = ,F8.4,5X,14H GRADE ANGLE = ,F6.2)
0139 506 FORMAT(IH0,16HEFFICIENCIES ARE,10X,24HR 24H REAR AXLE/DIFFERENTIAL= ,F7.
0140 14,5X,14HTRANSMISSION= ,F7.4)
0141 507 FORMAT(IH0,17H INTERVAL HAS ,16,9H SEGMENTS)
0142 508 FORMAT(IH0,3H INITIAL CONDITIONS FOR SIMULATION)
0143 509 FORMAT(IH0,17HVERROR,2X,4HPEDL,3X,2HRT,4X,3HRSP)
0144 510 FORMAT(SWALP=,F8.4,iX,SXALPa,FB.4)
0145 511 FORMAT(IH0,20HRMS VELOCITY ERROR =,F8.3,5X,26HAVERAGE FUEL CONSUMPTION
0146 1ITION =,F8.3,5X,24HRMS ENGINE SPEED ERROR =,F8.3)
0147 512 FORMAT(IH0,17HVERROR,2X,4HPEDL,3X,2HRT,4X,3HRSP)
0148 1ITION =,F8.3,5X,24HRMS ENGINE SPEED ERROR =,F8.3)
0149 513 FORMAT(IH0,17HVERROR,2X,4HPEDL,3X,2HRT,4X,3HRSP)
0150 1ITION =,F8.3,5X,24HRMS ENGINE SPEED ERROR =,F8.3)
0151 514 FORMAT(IH0,17HVERROR,2X,4HPEDL,3X,2HRT,4X,3HRSP)
0152 1ITION =,F8.3,5X,24HRMS ENGINE SPEED ERROR =,F8.3)
0153 515 FORMAT(IH0,17HVERROR,2X,4HPEDL,3X,2HRT,4X,3HRSP)
0154 1ITION =,F8.3,5X,24HRMS ENGINE SPEED ERROR =,F8.3)
0155 516 FORMAT(IH0,17HVERROR,2X,4HPEDL,3X,2HRT,4X,3HRSP)
0156 1ITION =,F8.3,5X,24HRMS ENGINE SPEED ERROR =,F8.3)
0157 517 FORMAT(IH0,17HVERROR,2X,4HPEDL,3X,2HRT,4X,3HRSP)
0158 1ITION =,F8.3,5X,24HRMS ENGINE SPEED ERROR =,F8.3)
0159 518 FORMAT(IH0,17HVERROR,2X,4HPEDL,3X,2HRT,4X,3HRSP)
0159 1ITION =,F8.3,5X,24HRMS ENGINE SPEED ERROR =,F8.3)
0160 519 FORMAT(IH0,17HVERROR,2X,4HPEDL,3X,2HRT,4X,3HRSP)
0160 1ITION =,F8.3,5X,24HRMS ENGINE SPEED ERROR =,F8.3)
0161 520 FORMAT(IH0,17HVERROR,2X,4HPEDL,3X,2HRT,4X,3HRSP)
0161 1ITION =,F8.3,5X,24HRMS ENGINE SPEED ERROR =,F8.3)
0162 521 FORMAT(IH0,17HVERROR,2X,4HPEDL,3X,2HRT,4X,3HRSP)
0162 1ITION =,F8.3,5X,24HRMS ENGINE SPEED ERROR =,F8.3)
0163 RFAD SYSTEM INPUTS.
0164 C READING IN PARAMETER VALUES
0165 READ(5,400) A,BP,CD,G,JA,JT,PIDLE
READ(S,400) KR,MP,RA,RW,W,DCP,KG,KP
READ(S,400) MU,RHO,TAUL,TBMAX
READ(S,400) KA,KT,RTMIN,RTMAX
READ(S,400) DELT,N,INPRIN,MET,IWRTE,NRUN
READ(S,400) VWIND,BETA(1)
DO 5 I=2,501
   BETA(I)=BETA(1)
   VW(I)=VWIND
   READ INITIAL STATES.
READ(S,400) X3,X4
   X3I=X3
   X4I=X4
   INITIALIZE VEHICLE VELOCITY.
   VVEL=0.0
   READ SPEEDS ON ENGINE MAP.
   READ(S,400) (ENGSP(I),I=1,8)
   READ(S,400) (ENGSP(I),I=9,16)
   READ(S,400) (ENGSP(I),I=17,19)
   CONVERT ENGINE SPEEDS TO RAD/SECS.
   DO 11 I=1,19
      ENGSP(I)=ENGSP(I)*0.10472
   READ PEDAL PERCENTS ON ENGINE MAP.
   READ(S,400) PEDPCT(1),I=1,10)
   READ ENGINE MAP TORQUES CORRESPONDING TO ENGSP(I) AND PEDPCT(J).
   DO 12 I=1,19
      READ(S,400) (ENGMAP(I,J),J=1,10)
   CONVERT ENGINE TORQUE TO N-M.
   DO 13 I=1,19
      DO 13 J=1,10
         ENGMAP(I,J)=ENGMAP(I,J)*1.35575
   READ PEDAL PERCENTS ON MIN FUEL CURVE.
   READ(S,400) (PEDPOS(I),I=1,16)
   READ(S,400) (PEDPOS(I),I=17,21)
   READ ENGINE SPEED VALUES ON MIN FUEL CURVE.
   READ(S,400) (OPTSP(I),I=1,8)
   READ(S,400) (OPTSP(I),I=9,16)
   READ(S,400) (OPTSP(I),I=17,21)
   CONVERT SPEED VALUES TO RAD/SEC.
   DO 131 I=1,21
      OPTSP(I)=OPTSP(I)*0.10472
   READ IN FUEL CONSUMPTION RATES.
   DO 14 I=1,19
      READ(S,410) (FURATE(I,J),J=1,10)
   SET UP SAE DRIVING CYCLE.
   NM1=N-I
   RNM1=NM1
   DO 20 I=1,N
      J=I-1
      RJ=J
   COMPUTE TIME AT EACH STEP IN SIMULATION.
   TIMARR(I)=RJ*DCP/RNM1
   T=TIMARR(I)
FIND DRIVING CYCLE VEL. AT EACH STEP IN SIMUL. AND STORE IN VDC(I)

IF(T.GT.14.0) GO TO 15

VDC(I)=1.43679*T

GO TO 20

IF(T.GT.64.0) GO TO 16

VDC(I)=20.115

GO TO 20

IF(T.GT.74.0) GO TO 17

VDC(I)=20.115-0.447*(T-64.0)

GO TO 20

IF(T.GT.83.0) GO TO 18

VDC(I)=15.645-1.738*(T-74.0)

GO TO 20

IF(T.GT.108.0) GO TO 19

VDC(I)=0.0

GO TO 20

T=T-108.0

GO TO 141

CONTINUE

OVERALL LOOP TO RUN SIMULATION TWICE.

DO 60 JRUN=1,NRUN

SET STATES EQUAL TO INITIAL STATES FOR RUN.

X3=X3I

X4=X4I

VVEL=0.0

READ IN CONTROLLER GAINS FOR THIS RUN.

READ(5,400) JWF,JWR,KCEI,KCEP,KCR,KPDI,KPDP

READ(5,400) WALP,XALP,PALP

PRINTING INPUT PARAMETERS

WRITE(6,500)

WRITE(6,501) A,BP,CD,G,JA,JE,JT,PIDLE

WRITE(6,503) KR,MP,RA,RW,W,DCP,KG,KP

WRITE(6,504) MU,RHO,TAUL,T$MAX

WRITE(6,506) KA,KT

WRITE(6,507) RTMIN,RTMAX

WRITE(6,505) VWIND,BETA(1)

L=N-I

RL=L

PRINT TIME INTERVAL OF SIMULATION.

SIMPER=RL*DELT

WRITE(6,510) SIMPER

WRITE(6,511) L

WRITE(6,502) JWF,JWR,KCEI,KCEP,KCR,KPDI,KPDP

WRITE(6,531) WALP,XALP

COMPUTE INITIAL VALUE OF ENGINE SPEED.

Xi=PHI4(PIDLE)

W.OLD=X1

WNEW=X1

XiLD=Xi

XiNW=X1

COMPUTE INITIAL VALUE OF DEVELOPED ENGINE TORQUE.

X2=PHI3(PIDLE,Xi)

COMPUTE INITIAL VALUE OF RATIO SET POINT.
0276  
0277  
0278  C COMPUTE INITIAL DRAG AND ROLLING RESISTANCE.
0279  D = 0.5 * (RHO / G) * CD * A * ((VVEL + VW(1)) ** 2)
0280  IF((VW(1) + VVEL) < 0.0) D = -D
0281  R = MU * W * (I.0 + 1.4E-3 * VVEL + 1.2E-5 * VVEL * VVEL)
0282  C INITIALIZE PEDAL CONTROLLER INTEGRATOR.
0283  X6 = PIDLE
0284  WRITE(6,520)
0285  WRITE(6,521) X1, X2, X3, X4, X5, X6
0286  C INITIAL SIMULATION TIME.
0287  T = 0.0
0288  C COMPUTE PEDAL CONTROLLER OUTPUT.
0289  VSPR = VSP(T)
0290  VERR = VSPR - VVEL
0291  PL = X6 + KPDP * VERR
0292  POLD = PL
0293  PNEW = PL
0294  PD = PL
0295  IF(PL.LT.PIDLE) PL = PIDLE
0296  C COMPUTE THROTTLE POSITION (OUTPUT OF GAIN EQUALIZER).
0297  ZIDLE = PIDLE + 0.001
0298  GO TO 24
0299  IF(PL.GT.63.29) GO TO 21

0300  IF(PL.GT.12.43) GO TO 22
0301  IF(PL.GT.ZIDLE) GO TO 29
0302  GO TO 24
0303  21 PL = 1.087 * PL - 8.7
0304  GO TO 24
0305  22 PL = 0.295 * PL + 41.33
0306  GO TO 24
0307  29 PL = PL
0308  24 CONTINUE
0309  C LIMIT THROTTLE POSITION.
0310  1F(PL.GT.100.0) PL = 100.0
0311  C COMPUTE INITIAL ENGINE SPEED SET POINT.
0312  OMEGSP = WNEW
0313  C COMPUTE INITIAL RATIO SET POINT.
0314  RSP = X5
0315  RSPOLD = RSP
0316  C COMPUTE RATIO SET POINT LIMITS.
0317  RSPMAX = RTMAX * ((KP + KCR * KR * KG) / (KCR * KR * KG))
0318  RSPMIN = RTMIN * ((KP + KCR * KR * KG) / (KCR * KR * KG))
0319  C COMPUTE INITIAL OUTPUT OF RATIO CONTROLLER, ENGINE SPEED SET POINT
0320  C USED FOR PRINTING, ENGINE SPEED AND RATIO ERRORS, INTERNAL
0321  C ENGINE TORQUE, FUEL CONSUMPTION.
0322  U = KCR * (RSP - PH15(X3))
0323  OMFR = PH14(PL)
0324  EW = OMFR - X1
0325  ER = RSP - X3
0326  TM = PH13(PL, X1)
FUEL=PHI6(X1,PL)
MV=V/G+(JWR+JWF)/(RW*RW)
MT=JT/(RA*RW)+(RA*JA)/(KT*RW)+(RA*RW*MV)/(KA*KT)
C COMPUTE INITIAL BRAKING TORQUE.
TBR=0.0
TBF=0.0
IF(PD.LT.PIDLE) TBR=-(PD-PIDLE)*TBMAX
C COMPUTE NO. OF ITERATIONS IN COMPUTER SIMULATION.
NL=N-1
C SET UP VECTOR OF CURRENT VALUES OF STATES FOR NUMERICAL INTEGR.
Y(1)=X1
Y(2)=X2
Y(3)=X3
Y(4)=X4
C INITIAL OLD STATES OF CONTROLLER INTEGRATORS.
XSOLD=X5
X6OLD=X6
C DETERMINE NO. OF OUTPUTS TO BE PRINTED (FULL OR REDUCED) AND PRINT APPROPRIATE HEADING.
IF(WRITE.EQ.0) GO TO 32
WRITE(6,S41)
GO TO 34
32 WRITE(6,S30)
34 CONTINUE
C SET UP NO. OF LINES OF OUTPUT PRINTED PER PAGE.
JPR=0
NPRMAX=60*INPRIN
NPR=0
C COMPUTE VALUES OF VARIABLES USED FOR PRINTING.
TIME=0.0
X1P=X1
X2P=X2
TBRP=TBR
VVELP=VVEL
C PRINT FIRST LINE OF OUTPUT. IF MET=1, RESULTS ARE IN METRIC.
WRITE(6,333)
333 FORMAT(4H****)
IF(MET.EQ.0) X1P=X1*9.5493
IF(MET.EQ.0) OMPR=OMPR*9.5493
IF(MET.EQ.0) EW=EW*9.5493
IF(MET.EQ.0) X2P=X2*0.73746
IF(MET.EQ.0) TM=TM*0.73746
IF(MET.EQ.0) VVELP=VVEL*2.23714
IF(MET.EQ.0) TBRP=TBR*0.73746
IF(MET.EQ.0) VSPR=VSPR*2.23714
IF(MET.EQ.0) VERR=VERR*2.23714
IF(WRITE.EQ.0) GO TO 36
WRITE(6,S42) TIME,X1P,OMPR,EW,X2P,PL,TBRP,VVELP,VSPR,VERR,PD,X3,RS
GO TO 37
36 WRITE(6,532) TIME,X1P,OMPR,EW,X2P,PL,TBRP,VVELP,VSPR,VERR,PD,U,
X3,RSP,ER,FUEL,X5,X6
37 CONTINUE
C INITIALIZE VELOCITY SUM OF SQUARES AND AVER. FUEL CONSUMPTION.
VSQ=0.0
0382  FUAV=0.0
0383  ENGER=0.0
0384  *****************************************
0385  *****************************************
0386  BEGIN SIMULATION.
0387  DO 50 L=1,NL
0388  NPR=NPR+1
0389  JPR=JPR+1
0390  LL=LL+1
0391  NV=4
0392  PEDL=PL
0393  PERFORM NUMERICAL INTEGRATION OF STATE EQNS. OVER CURRENT TIME INT
0394  CALL NIN(RHS,NV,T,DELT,Y)
0395  INCREMENT TIME.
0396  RL=L
0397  TIME=RL*DELT
0398  UPDATE STATES WITH RESULTS FROM NUMERICAL INTEGRATION.
0399  X1=Y(1)
0400  X2=Y(2)
0401  IF(Y(3).GT.RTMAX) Y(3)=RTMAX
0402  IF(Y(3).LT.RTMIN) Y(3)=RTMIN
0403  X3=Y(3)
0404  COMPUTE NEW VEHICLE VELOCITY.
0405  RLIM=PHIS(X3)
0406  VVEL=RA*RW.*RLIM*X1
0407  CALCULATE CURRENT VALUES OF SYSTEM VARIABLES.
0408  VSPR=VSP(T)
0409  OMEGSP=WNEW
0410  U=KCR*(RSP-RLIM)
0411  OMPR=WNEW
0412  EW=WNEW-X1
0413  ER=RSP-RLIM
0414  TM=PHI3(PL,X1)
0415  D=0.5*(RH/G)*CD*X*((VVEL+VW(1))**2)
0416  IF((VW(1)+VVEL).LT.0.0) D=-D
0417  R=MURW*(1.0+1.4E-3*VVEL+1.2E-S*VVEL*VVEL)
0418  FUFL=PHI6(X1,PL)
0419  TBR=0.0
0420  IF(PD.LT.PIDLE) TBR=-(PD-PIDLE)*TBMAX
0421  IS IT TIME TO PRINT AN OUTPUT?
0422  IF(JPR.LT.INPRIN) GO TO 40
0423  IF YES, COMPUTE PRINT VALUES, CONVERT UNITS IF REQUESTED, AND PRNT
0424  X1P=X1
0425  X2P=X2
0426  TBRP=TBR
0427  VVELP=VVEL
0428  VROR=VSPR-VVEL
0429  IF(MET.EQ.0) X1P=X1*9.5493
0430  IF(MET.EQ.0) OMPR=OMPR*9.5493
0431  IF(MET.EQ.0) EW=EW*9.5493
0432  IF(MET.EQ.0) X2P=X2*0.73746
0433  IF(MET.EQ.0) TM=TM*0.73746
0434  IF(MET.EQ.0) VVELP=VVEL*2.23714
0435  IF(MET.EQ.0) TBRP=TBR*0.73746
0436  IF(MET.EQ.0) VSPR=VSPR*2.23714
IF(MET.EQ.0) VROK=VRUR*2.23714
IF(IWRTE.EQ.0) GO TO 38
WRITE(6,542) TIME,XIP,OMPR,EW,X2P,PL,TBRP,VVELP,VSPR,VROR,PD,RLIM,
IRSP
GO TO 39
WRITE(6,543) TIME,XIP,OMPR,EW,X2P,PL,TBRP,VVELP,VSPR,VROR,PD,RLIM,
IRSP
GO TO 39
CONTINUE
JPR=0
CONTINUE
PRINT PAGE HEADING IF APPROPRIATE.
IF(IWRTE.EQ.0) GO TO 41
IF(NPR.EQ.NPRMAX) WRITE(6,541)
GO TO 42
IF(NPR.EQ.NPRMAX) WRITE(6,530)
CONTINUE
IF(NPR.EQ.NPRMAX) NPR=0

VEL. ERROR IS BASED ON AN AVER OF PRESENT AND FUTURE VEL SET PTS.
VERR=((VSP(T+DELT)+VSP(T))/2.0)-VVEL

COMPUTE INTEGRAL, PROP. AND TOTAL OUTPUT OF PI CONTROLLER.
X6NEW=X6OLD+KPID*VERR*DELT
PEDPRP=KPD*VERR
PL=X6NEW+PEDPRP

ADJUST OUTPUT WITH ANTI-WIND/UP LOGIC.
IF(PL.LE.100.0) GO TO 25
IF(PEDPRP.GE.100.0) GO TO 23
X6NEW=100.0-PEDPRP
GO TO 25
X6NEW=X6OLD
PEDPRP=100.0-X6NEW
GO TO 25
CONTINUE

FILTER PEDAL VARIATIONS.
PLNEW=PLAP*PLOLD+(1.-PALP)*PL
PL=PLNEW
PLOLD=PLNEW
PD=PL
IF(PL.LT.PIDLE) PL=PIDLE
X6OLD=X6NEW
X6=X6NEW

COMPUTE THROTTLE POSITION USING GAIN EQUALIZER.
GO TO 28
IF(PL.GT.63.29) GO TO 26
IF(PL.GT.12.43) GO TO 27
IF(PL.GT.PIDLE) GO TO 31
GO TO 26
PL=f.087*PL-8.7
GO TO 28
PL=0.2.95*PL+41.33
GO TO 28

PL-PL

CONTINUE

C **********^c************************************************^C******
C COMPUTE OUTPUT OF ENGINE SPEED CONTROLLER.

C SAVE CURRENT RATIO SET POINT.

RSPOLD=RSP

C COMPUTE INTEGRAL, PROP. AND TOTAL OUTPUT OF PI CONTROLLER.

C USE NEG. OF ERROR SINCE RATIO AND ERROR VARY INVERSELY.

FILTER ENGINE SPEED SET POINT AND ENGINE SPEED.

WNEW=WALP*WOLD+(1.-WALP)*PHI4(PL)

WOLD=WNEW

X1NW=XALP*X1LD+(1.-XALP)*X1

X1LD=X1NW

XSNEW=XSOLD-KCEI*(WNEW-X1NW)*DELT

RSPROP=-KCEP*(WNEW-X1NW)

RSP=XSNEW+RSPROP

ADJUST OUTPUT WITH ANTI-WIND/UP LOGIC.

IF(RSP.GE.RSPMAX) GO TO 30

IF(RSP.GT.RSPMIN) GO TO 35

DIFF=XSNEW-XSOLD

IF(DIFF.GT.0.0) GO TO 35

XSNEW=XSOLD

RSP=RSPMIN

GO TO 55

IF(RSPROP.GE.RSPMAX) GO TO 33

XSNEW=RSPMAX-RSPROP

GO TO 35

CONTINUE

RSP=XSNEW+RSPROP

GO TO 53

INHIBIT RATIO SET POINT CHANGE IF IT MAKES

VEHICLE VELOCITY ERROR WORSE.

IF(VERR) 51,52,52

IF(RSP-RSPOLD) 53,54,54

IF(RSP-RSPOLD) 54,53,53

RSP=RSPOLD

XSNEW=XSOLD

CONTINUE

XSOLD=XSNEW

X5=X5NEW

VSQ=VSQ+VERR*VERR*DELT

ENGREG=ENGREG+EW*EW*DELT

FUAV=FUAV+FUEL*DELT

VR RMS=SQRT(VSQ/SIMPER)

ENGREG=SQRT(ENGREG/SIMPER)

WRITE(6,533) VR RMS,FUAV,ENGREG

STOP

END
SUBROUTINE NINT(GR,N,X,DX,Y)

*** #******** #**** #**##*###**##**##*###***##****#*****##########*#*#######^c########*^c**

DIMENSION S(15),YP(15),YI(15),E(15),Z(15),XK(15,3),YMAX(15),YO(15)

1,P0(15),Y(15),P(15)

DXMAX=DX
DXMIN=1.0E-4
ERRMIN=0.000005

XF=X+DX
IF(DXMAX.EQ.DXMIN) GO TO 300
X0=X
IF(X)10,10,30
HT=XF
DO 20 I=1,N
20 YMAX(I)=ABS(Y(I))

30 H=HT
X=X0
H=X0+AMIN(H,DXMAX,DX)-X0
DO 50 I=1,N
50 Y0(I)=Y(I)
CALL GR(Y,P,X,X0)
DO 60 I=1,N
60 PO(I)=P(I)
Y(I)=YO(I)+0.5*H*PO(I)
X=X0+0.5*H
CALL GR(Y,P,X,X0)
DO 80 I=1,N
80 S(I)=2.0*P(I)+PO(I)
Y(I)=YO(I)+0.25*H*P(I)
CALL GR(Y,P,X,X0)
DO 100 I=1,N
100 YP(I)=Y0(I)+H*(P(I)+S(I))/6.0
110 X=X0+0.25*H
DO 120 I=1,N
120 Y(I)=Y0(I)+0.25*H*PO(I)
CALL GR(Y,P,X,X0)
DO 130 I=1,N
130 S(I)=2.0*P(I)+PO(I)
Y(I)=YO(I)+0.25*H*P(I)
CALL GR(Y,P,X,X0)
DO 140 I=1,N
140 Y(I)=Y0(I)+0.25*H*P(I)
X = X0 + 0.5*H
CALL GR(Y,P,X,X0)
DO 150 I=1,N
Y(I) = Y0(I) + 0.5*H*(P(I) + 5(I))/6.0
150 Y(I) = Y1(I)
CALL GR(Y,P,X,X0)
DO 160 I=1,N
S(I) = P(I)
160 Y(I) = Y1(I) + 0.25*H*P(I)
X = X0 + 0.75*H
CALL GR(Y,P,X,X0)
DO 170 I=1,N
S(I) = 2.0*P(I) + 5(I)
170 Y(I) = Y1(I) + 0.25*H*P(I)
CALL GR(Y,P,X,X0)
DO 180 I=1,N
S(I) = 2.0*P(I) + 5(I)
180 Y(I) = Y1(I) + 0.5*H*P(I)
X = X0 + H
CALL GR(Y,P,X,X0)
R = 0.0
DO 190 I=1,N
Y(I) = Y1(I) + 0.5*H*(P(I) + 5(I))/6.0
E(I) = (Y(I) - YP(I))/15.0
Z(I) = AMAX1(YMAX(I), ABS(Y(I)))
IF(Z(I) .EQ. 0.0) GO TO 190
R = AMAX1(R, ABS(E(I))/Z(I))
IF(ERRMIN = R) I85, 190, 190
IF(H .LT. DXMIN) I85, 190, 190
CONTINUE
DO 200 I=1,N
Y(I) = Y(I) + E(I)
YMAX(I) = Z(I)
200 X0 = X0 + H
IF(XF = X0) 210, 210, 220
210 RETURN
IF(R = ERRMIN) 230, 230, 240
H = H + H
230 H = DMAX / FLOAT(KF)
IF(XF .LT. X0 - H) 250, 250, 40
240 H = DMIN / H
250 K = 0
DO 260 K = 1, N
260 Y0(I) = Y1(I)
CALL GR(Y,P,X,X0)
X = X0 + 0.5*H
DO 270 J = 1, 2
270 Y(I) = Y(I) + E(I)
0653      DO 320 I=1,N
0654      XK(I,J)=H*P(I)
0655     320   Y(I)=YO(I)+0.5*KK(I,J)
0656     330   CALL GR(Y,P,X,X0)
0657     330   X=X+0.5*H
0658     340   Y(I)=Y0(I)+XK(I,3)
0659     340   CALL GR(Y,P,X,X0)
0660     350   Y(I)=YO(I)+(XK(I,1)+2.*(XK(I,2)+XK(I,3)))*H*P(I))/6.0
0661     350   IF(K.LT.KF) GO TO 305
0662     350   X=KF
0663     350   RETURN
0664     360   END

FTN4 COMPILER: HP92060-16092 REV. 2026 (800423)

** NO WARNINGS ** NO ERRORS ** PROGRAM = 01725 COMMON = 00000
SUBROUTINE RHS(X,XDOT,T,T0)
C *******************************************************
C THIS SUBROUTINE EVALUATES THE RIGHT HAND SIDE OF THE STATE EQNS.
C IT IS CALLED FROM NIN.
C X=CURRENT VALUES OF STATES.
C XDOT=CURRENT VALUES OF DERIVATIVES OF STATES (SUBROUTINE OUTPUT).
C T=CURRENT TIME.
C TO=APPEARENTLY NOT USED IN SUBROUTINE.
C *******************************************************
COMMON LL,PEDL,VW(501),VDC(2001),TFB,TBF,BETA(501),C(91),JE,TAUL,K
COMMON 101,DCP,TBMAX,KCEI,KCEP,KPDP,RSP,RNM1
COMMON CC/PIDLE,VVEL
COMMON DD/PD
COMMON/HB/ENGMAP(19,i0),ENGSP(i9),PEDPCT(i0),FURATE(19,i0),PEDPOS(i2)
DIMENSION X(15),XDOT(15)
RLIM=PHIS(X(3))
VVEL=RA*RW*RLIM*X(1)
PDAL=PEDL
IF(PDAL.GT.100.0) PDAL=100.0
IF(PDAL.LT.PIDLE) PDAL=PIDLE
C COMPUTE BRAKING TORQUE.
THR=0.0
IF(PD.LT.PIDLE) THR=-(PD-PIDLE)*TBMAX
TBF=THR
XDOT(1)=(X(2)-MT*RLIM*(PHI1(VVEL,VW(1))+PHI2(TBF,TBF,BETA(1)))RA
XDOT(2)=-(X(2)-PHI3(PDAL,X(i)))/TAUL
XDOT(3)=X(4)
XDOT(4)=-(HP*X(4)+KP*RLIM-KR*KG*KCR*(RSP-RLIM))/MP
RETURN
END
REAL FUNCTION PHI1(VEL,VELW)

0707 C THIS FUNCTION HAS A VALUE WHICH CONTAINS THE EFFECTS OF DRAG AND
0708 C ROLLING RESISTANCE ON THE VEHICLE. IT APPEARS IN THE X3DOT EQN.
0709 C AND IS CALLED BY RHS.
0710 C VEL = VEHICLE VELOCITY.
0711 C VELW=WIND VELOCITY.
0712 C

0713 COMMON LL,PEDL,VW(501),VDC(2001),TBF,TBR,BETA(S01),C(91),JE,TAIL,K
0715 DCP,TBMAX,KCE1,KCEP,KPDP,RSP,RNM1
0716 COMMON/CC/PIDLE,VVEL
0717 COMMON/AA/I

0719 C COMPUTE DRAG FORCE.
0720 DEE=0.5*(RHO/G)*CD*A*((VEL+VELW)**2)
0721 IF((VEL+VELW).LT.0.0) DEE=-DEE

0722 C COMPUTE ROLLING RESISTANCE.
0723 RR=MU*W*(1.0+(1.4E-3)*VEL+(1.2E-5)*VEL*VEL)
0724 PHI1=(RA*RW*(DEE+RR))/(MT*KA*KT)
0725 RETURN
0726 END
REAL FUNCTION PHI2(RBT, FBT, ANGLE)

C THIS FUNCTION HAS A VALUE WHICH CONTAINS THE EFFECTS OF BRAKING
TORQUE AND GRADE ON THE VEHICLE. IT APPEARS IN THE X3DOT EQN.,
AND IS CALLED BY RHS.

C RBT=REAR BRAKING TORQUE (BOTH WHEELS).
C FBT=FRONT BRAKING TORQUE (BOTH WHEELS).
C ANGLE-GRAGE ANGLE.

COMMON LL, PEDL, VW(SO1), VDC(2001), TBF, TBR, BETA(SO1), C(91), JE, Taul, K
101), DCP, TBMAX, KCEI, KCEP, KPDP, RSP, RNM1
COMMON/CC/PIDLE, VVEL
COMMON/AA/I

PHI2=RA*(RBT+FBT+RW*W*SIN(ANGLE))/(MT*KA*KT)
RETURN
END
REAL FUNCTION PHI3(PEDAL, ESPEED)

THIS FUNCTION EQUALS THE STEADY STATE ENGINE TORQUE DEVELOPED FOR A GIVEN ENGINE SPEED AND PEDAL POSITION. IT IS CALLED BY RHS AND NIN.

PEDAL = PEDAL POSITION.
ESPEED = ENGINE SPEED.

COMMON/CC/PIDLE, VVEL
COMMON/BB/FNGMAP(i9,10), ENGSP(i9), PEDPCT(i0), FURATE(19,i0), PEDPOS(121), OPTSP(20,RTMIN,RTMAX)
FORMAT(140, 26MPHI3 ARGUMENT OUT OF RANGE,SX, 2F10.4)

SAVE VALUE OF PEDAL
PLL=PEDAL
LIMIT THE PEDAL.
IF(PEDAL.GT. 100.0) PEDAL=100.0
IF(PEDAL.LT. PIDLE) PEDAL=PIDLE

FIND THE INDICES OF THE VALUES IN THE ENG. SPEED ARRAY WHICH BRACKET THE ACTUAL ENGINE SPEED.
IMIN=1
DO 5 I=1,i9
IF(ESPEED.GE.ENGSP(I)) IMIN=I
IF(ESPEED.LE.ENGSP(I)) GO TO 7
CONTINUE
IMAX=IMIN+i
IF(IMAX.GE. i9) IMAX=i9
IF(IMAX.EQ.IMIN) IMIN=IMIN-i

FIND THE INDICES OF THE VALUES IN THE PEDAL PERCENT ARRAY WHICH BRACKET THE ACTUAL PEDAL POSITION.
JMIN=I
DO 15 J=1,10
IF(PEDAL.GE.PEDPCT(J)) JMIN=J
IF(PEDAL.LE.PEDPCT(J)) GO TO 17
CONTINUE
JMAX=JMIN+i
IF(JMAX.GE.i0) JMAX=i0
IF(JMAX.EQ.JMIN) JMIN=JMIN-i

INTERPOLATE TO FIND THE TORQUES CORRESPONDING TO THE BRACKETING VALUES OF PEDAL AND THE ACTUAL ENGINE SPEED.
TLOWP=((ESPEED-ENGSP(IMIN))*ENGMAP(IMAX,JMIN)+(ENGSP(IMAX)-ESPEED)*ENGMAP(IMIN,JMIN))/(ENGSP(IMAX)-ENGSP(IMIN))
THIGHP=((ESPEED-ENGSP(IMIN))*ENGMAP(IMAX,JMAX)+(ENGSP(IMAX)-ESPEED)*ENGMAP(IMIN,JMAX))/(ENGSP(IMAX)-ENGSP(IMIN))

INTERPOLATE BETWEEN THE ABOVE TORQUES TO FIND THE TORQUE CORRESPONDING TO THE ACTUAL PEDAL POSITION.
PHI3=((PEDAL-PEDPCT(JMIN))*THIGHP+(PEDPCT(JMAX)-PEDAL)*TLOWP)/(PEDPCT(JMAX)-PEDPCT(JMIN))

RESTORE VALUE OF PEDAL
PEI)AL=PLL
RETURN

END
REAL FUNCTION PHI4(PEDAL)

THIS FUNCTION COMPUTES THE ENGINE SPEED SET POINT FOR MIN FUEL
CONSUMPTION FOR A GIVEN PEDAL POSITION. IT IS CALLED BY MAIN.

COMMON/CC/PIDLE,VVEL
COMMON/AB/ENGMAP(19,10),ENGSP(19),PEDPCT(10),FURATE(19,10),PEDPOS(121),OPTSP(21),RTMIN,RTMAX

LIMIT THE PEDAL.
PEDLL=PEDAL
IF(PEDAL.LT.PIDLE) PEDLL=PIDLE
IMIN=1
DO 5 I=1,21
IF(PEDLL.GE.PEDPOS(I)) IMIN=I
IF(PEDLL.LE.PEDPOS(I)) GO TO 7
CONTINUE
IMAX=IMIN+1
IF(IMAX.GE.21) IMAX=21
IF(IMAX.EQ.IMIN) IMIN=IMIN-1
INTERPOLATE TO FIND THE ENGINE SPEED SET PT. CORRESPONDING TO THE
ACTUAL PEDAL.
PHI4=((PEDLL-PEDPOS(IMIN))*OPTSP(IMAX)+(PEDPOS(IMAX)-PEDLL)*OPTSP(IMIN))/((PEDPOS(IMAX)-PEDPOS(IMIN))
RETURN
END
REAL FUNCTION PHIS(RHAT)

THIS FUNCTION LIMITS THE TRANSMISSION RATIO. IT IS CALLED BY MAIN AND RHS.

RHAT=UNLIMITED RATIO VALUE.

COMMON/BB/ENGMAP(15,10),ENGSP(19),PEDPCT(10),FURATE(19,10),PEDPOS(121),OPTSP(21),RTMIN,RTMAX

PHIS=RHAT

IF(RTMIN.GT.RHAT) PHIS=RTMIN

IF(PHIS.GT.RTMAX) PHIS=RTMAX

RETURN

END
REAL FUNCTION PHI6(ESPEED, PEDAL)

**THIS FUNCTION EQUALS THE FUEL CONSUMPTION RATE FOR A GIVEN ENGINE SPEED AND PEDAL POSITION. IT IS CALLED BY MAIN.**

ESPEED=ENGINE SPEED.
PEDAL=PEDAL POSITION.

**COMMON/CC/PIDLE, VVEL.**

COMMON/BB/ENGMAP(19,10), ENGSP(19), PEDPCT(10), FURATE(19,10), PEDPOS(121), OPTSP(21), RTMIN, RTMAX

PEDLL=PEDAL

LIMIT PEDAL.

IF(PEDAL.LT.PIDLE) PEDLL=PIDLE

FIND THE INDICES OF THE VALUES IN THE ENGINE SPEED ARRAY WHICH BRACKET THE ACTUAL ENGINE SPEED.

IMIN=1

DO $ I=1,19
IF(ESPEED.GE.ENGSP(I)) IMIN=I
GO TO 7

CONTINUE

IMAX=IMIN+1
IF(IMAX.GE.19) IMAX=19
IF(IMAX.EQ.IMIN) IMIN=IMIN-1

FIND THE INDICES OF THE VALUES IN THE PEDAL PERCENT ARRAY WHICH BRACKET THE ACTUAL PEDAL PERCENT.

JMIN=1

DO $ J=1,10
IF(PEDLL.GE.PEDPCT(J)) JMIN=J
GO TO 17

CONTINUE

JMAX=JMIN+1
IF(JMAX.GE.10) JMAX=10
IF(JMAX.EQ.JMIN) JMIN=JMIN-1

INTERPOLATE TO FIND THE FUEL RATE CORRESPONDING TO THE BRACKETING VALUES OF ENGINE SPEED AND THE ACTUAL ENGINE SPEED.

FLWRP=((ESPEED-ENGSP(IMIN))*FURATE(IMIN,JMIN)+(ENGSP(IMAX)-ESPEED)*FURATE(IMAX,JMIN))/(ENGSP(IMAX)-ENGSP(IMIN))

FHWHP=((ESPEED-ENGSP(IMIN))*FURATE(IMAX,JMIN)+(ENGSP(IMAX)-ESPEED)*FURATE(IMAX,JMIN))/(ENGSP(IMAX)-ENGSP(IMIN))

INTERPOLATE TO FIND THE FUEL RATE CORRESPONDING TO THE ACTUAL PEDAL POSITION.

PHI6=((PEDLL-PEDPCT(JMIN))*FHWHP+(PEDPCT(JMAX)-PEDLL)*FLWRP)/(PEDPCT(JMAX)-PEDPCT(JMIN))

RETURN

END
REAL FUNCTION VSP(TIME)

THIS FUNCTION EQUALS THE DRIVING CYCLE VELOCITY CORRESPONDING TO A GIVEN TIME. IT IS CALLED BY MAIN.

TIME=CURRENT TIME. VDC(I)=ARRAY OF DRIVING CYCLE VELOCITIES.


COMMON/CC/PIDLE, VVEL

REAL JE, KA, KCR, KP, KR, KT, MP, MU, MT, MV, KG, KPDI, KCEI, KCEP, KPDP

COMMON/CC/PIDLE, VVEL

I = IFIX(TIME*RNM1/DCP)+1

J = I + 1

TM1N = TIMARR(I)

TMAX = TIMARR(J)

INTERPOLATE TO FIND VELOCITY CORRESPONDING TO CURRENT TIME.

VSP = ((TIME - TM1N) * VDC(J) + (TMAX - TIME) * VDC(I)) / (TMAX - TM1N)

RETURN

END
APPENDIX D: ANTI WINDUP ALGORITHM

Whenever a controller contains an integral term and the actuator it is driving can limit (in one or both directions), there is the possibility that the integrator will "wind-up". In particular, if the actuator is driven to a limit and the error is not zero, the integrator will continue to increase its output even though no further reduction in the error is possible. If this continues for long enough, the integrator saturates or "winds-up". If the error then changes sign (e.g. the set point is changed) the actuator will not immediately respond to decrease the error because the saturated integrator is keeping it at its limit. This type of windup can cause instability and precautions must be taken to prevent it.

A common approach, and the one adopted here, is to prevent the integral term from further integration if the actuator is at a limit and the error is such that it would tend to windup the integrator. Since the controllers used in this work also contain proportional terms, additional logic is added to account for the interaction of these two parts of the control algorithm. Finally, because there are slight differences between the throttle and engine speed controller logics, a separate flow chart for each is included.
Compute new integral and proportional parts of engine speed controller output based on current engine speed error. Sum these two parts to get new ratio set point.

Is ratio set point such that it would cause actual ratio to reach or exceed its upper limit?

no

Is ratio set point such that it would cause actual ratio to reach or go below its lower limit?

no

Set integral part of ratio set point to a value which will produce a ratio set point which will put actual ratio at its max value.

yes

Will just the proportional part of the ratio set point cause the actual ratio to reach or exceed its upper limit?

no

Set ratio set point value which will put actual ratio at lower limit.

yes

Reset integral part of ratio set point to old value (no change in integral part).

no

Is the change in the integrator portion of the ratio set point such that it will tend to bring the actual ratio off the limit?

no

Reset integral part of ratio set point to old value.

yes

Recompute ratio set point.

EXIT

Figure D1 Engine Speed Controller Anti-Windup Logic
Compute new integral and proportional parts of throttle controller output based on current velocity error.

Compute new pedal position (sum of above terms)

Is pedal greater than 100%?

yes

Is proportional part of pedal greater than 100%?

no

Set integral portion to a value which will produce a pedal of 100%.

yes

Reset throttle controller integrator to old value.

Set proportional part to a value which will produce a pedal of 100%.

Compute new pedal position.

EXIT