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TOLERANCE REQUIREMENTS TO PREVENT FLUID LEAKAGE IN THE CRUCIBLE/PLUNGER MEA EXPERIMENT MPS 770030

By Thomas J. Rathz
Space Science Laboratory

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George C. Marshall Space Flight Center
Marshall Space Flight Center, Alabama
**Title and Subtitle:** Tolerance Requirements to Prevent Fluid Leakage in the Crucible/Plunger MEA Experiment MPS 770030

**Author(s):** Thomas J. Rathz

**Performing Organization:** George C. Marshall Space Flight Center
Marshall Space Flight Center, Alabama 35812

**Sponsoring Agency:** National Aeronautics and Space Administration
Washington, D.C. 20546

**Abstract:**

The work described was motivated by the unexpected leakage of molten Al-In out of the crucible of a proposed MEA materials processing in space experiment. The molten metals use a spring-loaded plunger to eliminate most free surfaces. The critical criteria necessary to initiate flow and the rate of fluid flow into the crucible/plunger annulus is calculated. Experimental in situ X-radiographs are interpreted according to the calculations. Also presented is a short note on possible effects of capillary flow if wetting occurs between crucible/plunger and liquids.

**Keywords:**

- Isothermal solidification
- Materials Experiment Assembly (MEA)
- Fluid leakage
- Materials Processing in Space Experiments

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</tr>
<tr>
<td>( v )</td>
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<td></td>
</tr>
<tr>
<td>( \rho )</td>
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<td></td>
</tr>
<tr>
<td>( t )</td>
<td>Time</td>
<td></td>
</tr>
<tr>
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<td>Coefficient of kinematic viscosity</td>
<td></td>
</tr>
<tr>
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TECHNICAL MEMORANDUM

TOLERANCE REQUIREMENTS TO PREVENT FLUID LEAKAGE IN THE CRUCIBLE/PLUNGER MEA EXPERIMENT MPS 770030

INTRODUCTION

The Materials Experiment Assembly (MEA) is an assembly of various materials processing furnaces capable of providing experimenters with the opportunity to perform materials science and fluid dynamics investigations for an extended period of time in the low-g environment of the Space Shuttle [1]. The first MEA flight is presently scheduled for the seventh Shuttle voyage. Among the set of experiments to be flown on MEA-1 will be the processing of the Al-In immiscible system. This experiment was originally flown on two separate Space Processing Application Rocket (SPAR) flights in an attempt to form a highly uniform dispersion of one phase within the other [2]. However, because of incomplete sample homogenization and possibly unexpected separation mechanics, a uniform dispersion in the solid state was not achieved. One of the particular processing modes that will be attempted on MEA with this same alloy system and is the concern of this report is the isothermal solidification of two sample compositions: Al-90 wt. pct. and 40 wt. pct. In.

The configuration to be used for the Al-90 w/o In and Al-40 w/o In cartridges is shown in Figure 1. Figure 1 is the Al-90 w/o In drawing while the Al-40 w/o In cartridge is different only in the interchanging of the alumina crucible/plunger with SiC-coated graphite components. The purpose of this change is to allow the majority phase liquid of each sample composition to preferentially wet the crucible/plunger and thus reduce the surface energy driven separation process. To further reduce surface tension driven separation, a spring-loaded plunger will contact the liquid metals and eliminate most of the free surface that would exist otherwise. Thus in a low-gravity environment the major separation processes such as Stoke's sedimentation, gravity-driven convection, and any free-surface Marangoni convection should be drastically reduced.

Because there existed a problem with reaching the requested 970°C soak temperature in the MEA furnace, some concern was expressed over attaining an initially homogeneous liquid at a new soak temperature of 860°C for the same soak time. Therefore, an Al-90 w/o In cartridge was processed at Marshall Space Flight Center having in situ X-radiography performed with the intent of learning the extent of sample homogenization taking place at the new soak temperature. However, as the sample materials became molten it was apparent from the X-rays that severe leakage of this liquid had occurred in the annular region between the plunger and the crucible. The plunger cavity region had almost become completely filled with the sample liquid. This leakage raised the questions of how much fluid flow would occur during different periods of time and temperatures as factors such as the plunger/crucible gap and spring force are varied. Such an analysis, as presented in this report, was deemed necessary for cartridge design and to prevent possible adverse effects on the scientific objectives.
Figure 1. Cartridge configuration for Al-90 w/o In liquid immiscible experiment to be flown in MEA-1's isothermal furnace.
The cartridge configuration shown in Figure 1 for this experiment had problems of molten sample leaking between the plunger and crucible. To present a more realistic view of the crucible/plunger/sample configuration, Figure 2 was drawn showing the dimensional variables that will occur in the calculations. Although Figure 2 is a simplification of Figure 1, none of the geometrical parameters that will enter into the calculations have been eliminated. The objective is to calculate mass flow rates for various gap sizes, \( a \), which forms the annular region, for various total (spring) forces, \( F \), and for various temperatures, \( T \). The diameter of the crucible, \( D_c \), will be held constant while the plunger diameter, \( D_p \), is determined by the chosen gap size.

![Figure 2](image)

Figure 2. Cross sectional view of a simplified drawing of Figure 1 showing fluid flow into annular gap region.

The general Navier-Stokes equation for viscous incompressible flow which describes molten metals very well is given as

\[
\frac{D\hat{V}}{D\tau} = \frac{\hat{V}V}{\tau} + \nabla \cdot V\hat{V} = \hat{X} - \frac{\Delta P}{\rho} + \nu \nabla^2 \hat{V}
\]  

(1)
where:

\[\rho = \text{fluid density}\]
\[\mathbf{v} = \text{velocity vector}\]
\[t = \text{time}\]
\[\nu = \text{coefficient of kinematic viscosity}\]
\[P = \text{pressure}\]
\[\mathbf{X} = \text{body force per unit mass}\]

Since this formidable equation cannot be solved analytically, it must be reduced to a form that can be dealt with. To do this requires an analysis of the magnitude of each term in equation (1) using appropriate assumptions, constraints, or boundary conditions.

The most obvious assumption to be made for the configuration shown in Figure 2 is to assume that steady state flow has been attained in the annular region. This results in

\[\frac{\partial \mathbf{v}}{\partial t} = 0 \quad (2)\]

If cylindrical coordinates are chosen because of the problem's geometry, then another set of constraints that will be used are the following:

\[v_r = v_\theta = 0 \quad (3a)\]
\[P = P(z) \quad (3b)\]

Application of equations (3a) and (3b) to the following continuity equation

\[\frac{\partial v_r}{\partial r} + \frac{1}{r} \frac{\partial (rv_\theta)}{\partial \theta} + \frac{\partial v_z}{\partial z} = -\frac{\rho v_r}{r} \quad (4)\]

results in the further restraint that

\[\frac{\partial v_z}{\partial z} = 0 \quad .\]
That is, the only flow that will occur is a constant flow in the $z$-direction and the velocity of this flow will depend only upon its radial position within the annulus (Fig. 3). Also, the pressure will depend only on the $z$-direction. Equation (3a) implies that

$$\frac{\partial v_r}{(\partial \theta, \partial r, \partial z)} = \frac{\partial v_\theta}{(\partial \theta, \partial r, \partial z)} = 0$$

and equation (3b) implies that

$$\frac{\partial v_z}{(\partial \theta, \partial z)} = 0 .$$

Equation (1) now becomes in cylindrical coordinates:

$$\frac{Dv_r}{Dt} - \frac{v_\theta^2}{r} = X_r - \frac{1}{\rho r} \frac{\partial P}{\partial r} + \nu \left( \frac{\partial^2 v_r}{r^2} - \frac{2}{r^2} \cdot \frac{\partial v_\theta}{\partial \theta} \right)$$

$$\frac{Dv_\theta}{Dt} + \frac{v_r v_\theta}{r} = X_\theta - \frac{1}{\rho r} \frac{\partial P}{\partial \theta} + \nu \left( \frac{\partial^2 v_\theta}{r^2} - \frac{2}{r^2} \cdot \frac{\partial v_r}{\partial \theta} - \frac{v_\theta}{r} \right)$$

$$\frac{Dv_z}{Dt} = X_z - \frac{1}{\rho} \frac{\partial P}{\partial z} + \nu \nabla^2 v_z$$

where by definition:

$$\frac{D}{Dt} = v_r \frac{\partial}{\partial r} + v_\theta \frac{\partial}{\partial \theta} + v_z \frac{\partial}{\partial z} + \frac{\partial}{\partial t}$$

$$\nabla^2 = \frac{1}{r} \frac{\partial}{\partial r} \left( r \frac{\partial}{\partial r} \right) + \frac{1}{r^2} \frac{\partial^2}{\partial \theta^2} + \frac{\partial^2}{\partial z^2} .$$

Applying equations (2), (3a), and (3b) to equations (4) and (5) results in

$$v_z \frac{\partial v_z}{\partial z} = X_z - \frac{1}{\rho} \frac{\partial P}{\partial z} + \nabla^2 v_z$$

5
for the Navier-Stokes equation. Using the continuity constraint from equation (4) finally gives

\[ 0 = X_z - \frac{1}{\rho} \frac{dP}{dz} + \rho \frac{\partial^2 v_z}{\partial z^2} . \]  

(8)

Since the only body force of concern to this problem is gravity and due to its orientation in Figure 2 we can thus reduce the dimensionality of equation (8) to two independent terms:

\[ 0 = A + \mu \left( \frac{\partial^2 v_z}{\partial r^2} + \frac{1}{r} \frac{\partial v_z}{\partial r} \right) \]  

(9a)

where

\[ A = \rho X_z(z) - \frac{dP(z)}{dz} \]  

(9b)

is independent of \( r \) and \( \mu \) is the coefficient of viscosity. If we now solve (9a) by applying the following boundary conditions

\[ v_z = 0 \quad \text{at} \quad r = r_1, \quad \text{and} \quad r = r_2 \]  

(10)

we obtain the velocity of fluid flow within an annulus between two coaxial cylinders.
\[ v_z(r) = \left( \frac{1}{4\mu} A \right) \left[ \left( r_2^2 - r_1^2 \right) + \frac{(n_2^2 - 1)r_1^2}{\ln(n)} \ln \left( \frac{r}{r_1} \right) \right] \]  \hspace{1cm} \text{original page is of poor quality} \]

where \( n = \frac{r_2}{r_1} \).

The quantity of most usefulness to examine is the mass flow rate which can be found from

\[ \dot{m} = \rho \int_0^{2\pi} \int_{r=r_1}^{r=nr_1} v_z r \, dr \, d\theta \]  \hspace{1cm} (12)

\[ = \frac{nr_1^4 \rho A}{8\mu} \left[ (n^4 - 1) - \frac{(n_2^2 - 1)^2}{\ln(n)} \right] \]  \hspace{1cm} (13)

Note that \( \dot{m} \) is proportional to \( F \) through \( dP/dz \) in \( A \), where \( F \) is the force on the piston. A big assumption in the derivation of \( \dot{m} \) is the neglect of the effects the moving plunger will have on the boundary conditions of equation (10). This effect can be included in the boundary conditions but, as is shown below, this is small enough to be neglected. By conservation of volume flux, the relationship between the fluid height \( h \) and the downward distance \( \Delta z \) moved by the piston as shown in Figure 2 is given by

\[ \frac{h}{\Delta z} = \frac{(D_c - 2a)^2}{4a(D_c - a)} \]  \hspace{1cm} (14)

which results in a range of values \( 20 \leq \frac{h}{\Delta z} \leq 518 \) for \( 0.005 \text{ in.} \leq a \leq 0.0002 \text{ in.} \). Thus for the entire range of annular gap values, the plunger motion can indeed be neglected.

Since the magnitude of \( \dot{m} \) in equation (13) depends upon \( \dot{m} \), the relative size of each term in \( A \) need be examined. The only body force to consider is that of the constant gravitational acceleration such that \( X(z) = g \). Now the pressure gradient \( dP/dz \) is that pressure acting through a chosen distance, or height, of 1 cm due to the resultant forces of the spring and the masses of the retainer and plunger acting over the plunger-face area. These forces are summarized in Table 1 and when the spring force is compared to the maximum body force, the latter can be considered negligible for dynamic flows. However, this body force due to the plunger/retainer masses in 1-g amounts to approximately 10 percent of the spring force. This 10 percent additional force does not appear to be much until the static forces in Figure 4 are examined in the next paragraph.
**Table 1. Component Forces Acting on Plunger**

<table>
<thead>
<tr>
<th></th>
<th>$\rho$ (g/cc)</th>
<th>Volume (cc)</th>
<th>1-g (dynes)</th>
<th>0-g</th>
</tr>
</thead>
<tbody>
<tr>
<td>Alumina Plunger</td>
<td>3.96</td>
<td>1.298</td>
<td>5047</td>
<td>-</td>
</tr>
<tr>
<td>Graphite Plunger</td>
<td>1.85</td>
<td>1.298</td>
<td>2353</td>
<td>-</td>
</tr>
<tr>
<td>Spring Retainer (304 S.S.)</td>
<td>8.044</td>
<td>0.59</td>
<td>4655</td>
<td>-</td>
</tr>
<tr>
<td>Quartz Spring</td>
<td>-</td>
<td>-</td>
<td>$1.1 \times 10^5$</td>
<td>$1.1 \times 10^5$</td>
</tr>
</tbody>
</table>

Figure 4. Interfacial pressure at the region of coexistence between the liquid alloy and external vapor as a function of the annular gap parameter for various liquid vapor surface tensions.
To initiate fluid flow, a static pressure larger than the interfacial pressures of Figure 4 is needed to form the meniscus since we have assumed no wetting of the container by the fluids. Curves 1 and 2 are for values of the liquid surface tension spanning the set of values for the pure components [and thereby the (Al-In)-mixtures] for the range of temperatures used during the MEA experiments. Curve 3 shows the applied spring pressure: if curve 3 lies above curves 1 or 2, then flow could ensue. As can be seen, the 10 percent additional static force of the retainer/plunger masses in 1-g will be a critical factor. Also, since flow has been observed in ground based experiments performed with cartridges as designed in Figure 1, then either the spring force or the annular gap was larger than expected, or the additional mass forces caused the problem. Since the latter is a 1-g effect, this paper concentrated on the effects of the possible variations in the spring force on the flow rate, \( \dot{m} \), in zero-gravity as a function of annular gap.

The following calculations of \( \dot{m} \) used the thermophysical data of Table 2 and the following assumptions:

- The pressure gradient producing flow was only due to the spring force (nominally \( 10^5 \) dyne) acting over a 1-cm distance; and most importantly, this force was big enough to overcome the liquid disjoining pressure detailed in Figure 4.
- The crucible inside diameter was 1.054 cm.
- The plunger was concentric with the crucible and thus eliminated any possible frictional forces between crucible/plunger.
- No wetting of the crucible/plunger by the liquid phases took place which would have allowed capillary flow (see appendix).
- The annular gap opens into a larger area into which the fluid flowed so that the interfacial pressure was not a factor in the dynamic flow up the 1-cm height.
- Hydrostatic body forces were negligible.
- Distance traveled and motional effects of plunger were negligible compared to height or speed of liquid flow rate.

The results of the calculations are shown in Figures 5 through 7. Figure 5 shows the relative size of the mass flow rate for the various liquid metals at a temperature of 1000°C and spring force of \( 10^5 \) dyne. Even though the density and viscosity of equation (13) each have their own separate temperature dependence, it is the kinematic viscosity \( (\nu/\rho) \) which causes several of the curves in Figure 5 to nearly overlay one another. As expected, however, the higher viscosity of Al causes a slower rate of loss. The curves fall well within a factor of 5 of each other at any particular gap value.

Figures 6a through 6d show the temperature dependence of the mass flow rate of the (Al, In) liquids of interest for a spring force of \( 10^5 \) dyne. As expected, the flow rate increases with temperature for a particular material due to the decreasing exponential temperature dependence of the viscosity as opposed to the decreasing linear dependence of the density in the models used. Approximately 40 percent difference exists in flow rates for a temperature difference of 300°C for a particular material. Because In has a lower melting temperature than the other Al or Al-In
### Table 2. Calculated Thermophysical Properties for (In, Al) Liquids

<table>
<thead>
<tr>
<th>Temperature (C)</th>
<th>Al-40 w/o In</th>
<th>Al-90 w/o In</th>
<th>Pure In</th>
<th>Pure Al</th>
</tr>
</thead>
<tbody>
<tr>
<td>200</td>
<td>-</td>
<td>-</td>
<td>556</td>
<td>6.99</td>
</tr>
<tr>
<td>600</td>
<td>-</td>
<td>-</td>
<td>520</td>
<td>6.72</td>
</tr>
<tr>
<td>700</td>
<td>763 3.19 0.0141</td>
<td>592 5.64 0.01</td>
<td>511</td>
<td>6.65</td>
</tr>
<tr>
<td>1000</td>
<td>638 3.05 0.0068</td>
<td>537 5.46 0.006</td>
<td>484</td>
<td>6.45</td>
</tr>
<tr>
<td>Ref.</td>
<td>4b 4 4</td>
<td>4b 4 4</td>
<td>3 5 5 5</td>
<td>3 5 5 5</td>
</tr>
</tbody>
</table>

**Units:**
- \( \gamma \) = surface tension (ergs/cm²);
- \( \rho \) = density (g/cc);
- \( \eta \) = viscosity (dyne-s/cm²)

**A.**
- \( \gamma_{Al} = 2.385 \times 10^{-4} (T - 660.1) (2.8 \times 10^{-4}) \)
- \( \gamma_{In} = 7.023 \times (T - 156.6) (6.8 \times 10^{-4}) \)

**B.**
- \( \eta_{Al} = 0.001492 \exp [16.5 \times 10^3 / 8.3144(T')] \)
- \( \eta_{In} = 0.00302 \exp [0.65 \times 10^3 / 8.3144(T')] \)

**Footnotes:**
- T' = temperature (K), T = temperature (C)
- Calculations based on Guggenheim model.
Figure 5. Calculated mass loss rate versus annular gap for several Al-In compositions at 1000°C and $10^5$ dynes of spring force.

(a) Pure Al
(b) Al-40 w/o In
(c) Al-90 w/o In
(d) Pure In

Figure 6. Calculated mass loss rate versus annular gap at various temperature and at $10^5$ dynes of spring force for (a) pure Al, (b) Al-40 w/o In, (c) Al-90 w/o In, and (d) pure In.
alloys, three curves are illustrated in Figure 6d. The pure Al and In figures are presented because of the possibility of having In fluid flow into the annular gap (Fig. 1) before the Al melts and mixes; or, the possibility exists of having the molten Al segregate to the top of the sample and thereby having the Al flow into the gap.

To illustrate the effects of various spring forces, Figure 7 presents the Al-90 w/o In material at 1000°C for spring forces of $10^4$, $10^5$, and $10^6$ dynes. Again, as expected from equation (13), an order of magnitude variation in the spring force causes an equal order of magnitude change in the flow rate.

Some general comments about the entire set of graphs should be made concerning the magnitude of the mass flow rate. At the most conservative values of flow rate (approximately 0.1 g/sec for Al at 700°C and $F_s = 10^4$ dynes) and for a typical Al 90 w/o In cartridge annular gap value of $5.08 \times 10^{-3}$ cm (2 mils), the entire volume of metal would be squeezed out of the crucible in less than 100 sec. A second comment concerns the sensitivity of the mass flow rate (MFR) to the gap size. A $2.54 \times 10^{-3}$ cm (1 mil) change in the gap can increase the MFR by almost an order of
magnitude; however, at smaller gap values this is no longer true. At these smaller values, the slope is such that any small uncertainties in the gap value (which will most likely occur in crucible/plunger machining processes) will produce large uncertainties in the MFR, although the overall magnitude of the MFRs will still be quite low. This latter effect is particularly expected for the Al-40 w/o In cartridges whose annular gap is supposed to be about $1.27 \times 10^{-3}$ cm (0.5 mils).

OBSERVED FLOWS

As stated in the introduction, MEA ground based experiments were performed in which in situ X-radiographs were taken at critical temperatures during the processing of both Al-40 w/o and 90 w/o In samples. From these radiographs can be seen several of the effects discussed in the previous section. Figure 8a shows the processing of cartridge P-4 (Al-90 w/o In: alumina crucible/plunger) at the monotectic temperature of 640°C during heat-up; although nonuniform, flow has begun. The "bubbles" are of In and are forming in the plunger cavity region. Thus the critical vapor-liquid surface tension discussed in Figure 4 has been exceeded so that flow can commence. As seen in Figure 8a, the density inversion of the Al and In layers will cause some Al to be forced into the gap and up into the plunger cavity. As evidenced in Figure 8b at $T = 820^\circ$C, the Al-rich and In-rich phases in the plunger cavity are now beginning to separate upon cooling from a soak time/temperature of 8 hr/860°C.

**Figure 8.** Radiograph of cartridge P-4, Al 90 w/o In, with in furnace while (a) heating up to 640°C: localize flow through annular gap and into plunger cavity; sample density stratification beginning; (b) cooling down to 820°C where Al-In separation seen in plunger cavity.
There were several interesting phenomena observed in these radiographs. One surprise was the non-uniformity of the flow up the sides which suggest that there existed possible machining flaws in the plunger that provided non-uniform flow channels. The biggest surprise was the lack of steady flow of the entire volume of fluid out of the crucible. Since the spring constant and spring force were given as $8.8 \times 10^4$ dyne/cm and $1.1 \times 10^5$ dynes respectively, the expected travel distance allowable for the plunger would thus be 1.25 cm which is about the full depth of the crucible. Since this entire fluid drain was not observed, speculations such as plunger/crucible skewness, or vapor deposition and locking at the upper crucible/plunger junction, or other mechanisms can only be postulated to have stopped the plunger from advancing further.

In another Al-90 w/o In experiment, the sample (P-3) was run for 9.5 hr at 970°C. The greater amount of plunger bearing surface near the sample provided a slight variation in this experiment. However, as shown in Figure 9, the radiograph taken after processing indicates that partial flow again occurred but only along one side and not into the cavity. This provides indications that plunger/crucible skewness existed which could only provide flow along one side until the plunger is immobilized and flow is stopped. Skewness can stop flow by presenting a channel on one side of the plunger which is too narrow for surface tension to be overcome (Fig. 4). This critical width will be encountered at varying heights when the plunger is skewed with respect to the crucible. Even a reprocessing of this same cartridge at 970°C for 1 hr in a figure 1-inverted position failed to cause any changes in the fluid profile of Figure 9. This inverted processing lends credence to the negligible effect of gravity compared to the spring force on the fluid flow in the annular gap.

![Figure 9. Radiograph of cartridge P-3, Al-90 w/o In at room temperature after processing at 970°C for 9.5 hr. Non-uniform flow along one side of plunger.](image-url)

Finally there were two Al-40 w/o In cartridges which were processed. In situ X-radiographs taken of one cartridge (S-2) processed at 880°C for 3.5 hr and X-radiographs taken of another (S-3) after processing at 960°C for 9 hr showed no evidence of fluid flow (Fig. 10). This could be expected from the smaller annular
gap of less than $2.54 \times 10^{-3}$ cm (1 mil) and the implications thereby provided from Figure 4. Even though the Al was invisible because of the X-ray intensity used, any flow of the Al-In mixture would have been readily seen. One side comment must be made concerning the somewhat dispersed appearance of the Al-In solid seen in Figure 10. Some separation is seen in Figure 10 but not as complete as that seen in the room temperature radiographs of samples P-4 and P-3 (Fig. 9) or in any previous Al-In ground base (1 g) experiments which have always been performed with very large free surfaces available, i.e., non-plunger configuration [2]. This effect will be further investigated and reported later.

**SUMMARY**

From the calculations performed for the cartridge configuration of Figure 1, the onset of fluid flow can be determined from various experimental parameters. The overall critical criteria is the data presented in Figure 4 in which the spring force must initially overcome the disjoining pressure of the liquid-vapor interface at the gap before flow can transpire. The maximum gap allowable beyond which flow occurs is presented in the following tabulation as a function of the applied spring force. Thus, it is crucial that the spring force be well known at all temperatures and the critical annular gap size be appropriately chosen. A prudent choice would be as small a gap as manufacturally possible so that if the critical gap is met, then flow will be as minimal as possible. However, the potential exists for attaining a critical frictional force between the greater crucible and plunger contact surface area as the gap size is reduced which may entirely inhibit plunger motion. This can be determined by laboratory test.

The variances in the sample's thermophysical properties and the spring force do not produce as great a change in the computed mass flow rates as compared to the variances in the annular gap value. This result is exemplified in the observed flows.
Critical Maximum Annular Gap

<table>
<thead>
<tr>
<th>Force (d × 10^{-5})</th>
<th>(cm × 10^3)</th>
<th>(mils)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.5</td>
<td>15.9</td>
<td>6.3</td>
</tr>
<tr>
<td>1.0</td>
<td>8.2</td>
<td>3.2</td>
</tr>
<tr>
<td>1.5</td>
<td>5.5</td>
<td>2.2</td>
</tr>
<tr>
<td>2.0</td>
<td>4.2</td>
<td>1.6</td>
</tr>
<tr>
<td>2.5</td>
<td>3.3</td>
<td>1.3</td>
</tr>
<tr>
<td>3.0</td>
<td>2.8</td>
<td>1.1</td>
</tr>
</tbody>
</table>

As seen in the Al-90 w/o In cartridges, fluid flow is fairly prevalent but not continuous nor uniform. This suggests a halting of the plunger motion by a possible skewness with the crucible. The Al-40 w/o In showed no signs of flow which suggest that the smaller gap value for these cartridges presents a surface tension barrier to flow, as suggested by Figure 4.

Since the publication of this paper, the experimental cartridges will have already been redesigned to insure that a maximum gap value of 1.2 × 10^{-3} cm (0.5 mil) is used for both Al-In compositions. It is hoped that no leakage into the gap occurs because any leakage will cause an unknown amount of shift in the initial composition of the alloy and thus have detrimental effects on the relative volume percentages of each immiscible phase. With relative composition unknown, modeling any observed separation that occurs will be rendered difficult or impossible. The inhibition of fluid flow beyond the plunger cavity by reducing the annular gap will also provide some margin of safety for the flight furnace by not having Al-In react through the stainless steel cartridge; but, any flow will still be deleterious to scientific analysis.
APPENDIX

In a report by Potard [6], SiC is wetted by aluminum ($\theta_{Al} < 90$) preferentially over that of indium; also, the monotectic composition wets the SiC. However, Löhberg, et al. [7] claim that neither the Al nor In wets alumina ($\theta_{Al}, \theta_{In} > 90$). Since one phase (Al) is reported to wet the crucible, and since there exist the possibility of attaining a critical temperature at which any of the other phases may wet the crucibles [8], it was decided to analyze the capillary flow that would occur in the annular gap assuming the entire Al-In composition range wets the crucibles. The following analysis is based on the simple discussion of Bourgeouis [9].

The flow equation in the annular gap region for capillary flow and no forced flow is

$$v = \frac{\rho g r_2^2 \phi}{\eta h} (h_o - h)$$  \hspace{1cm} (A-1)

where

$$\phi = \frac{1 - n^4}{1 - n^2} + \frac{1 - n^2}{\ln(n)}$$  \hspace{1cm} (A-2)

$$h_o = \frac{2 \gamma \cos \theta}{\rho g r_2 (1 - n)}$$  \hspace{1cm} (A-3)

and $v$, $\eta$, $\rho$, $g$, $n$, $r_2$, and $\theta$ are as previously defined; also, $h =$ axial position in annulus. The quantity $h_o$ is the equilibrium height of capillary rise counter-balanced by the pressure gradient established by gravity, $g$. Therefore, the position $h$, which is to be the reference point from which $v$ is computed, must be less than $h_o$; this forms a constraint in the computations. For this report's purpose the previously used 1 cm maximum height was chosen for $h$. The mass flow rate for this problem was simply taken as

$$\dot{m} = rv A$$  \hspace{1cm} (A-4)

where $A$ is cross sectional area of annular region.

Using the same thermophysical data of Table 2 as used for the previous non-wetting flow rate calculations, the following analysis is presented. The variables to alter are the $g$-level, the wetting angle, the material's thermophysical data, and the annular gap value.
Figure 11 presents the mass flow rate (MFR) for the various materials at 1000°C, wetting angle of 75 deg, and at 1-g of gravity for various annular gap values. The various material properties give MFRs within 50 percent of each other at any particular gap value. Note that the MFRs are about the same order of magnitude and functionally equivalent to the MFRs of Figure 5; this is as expected since the only major difference between the flows described by equation (A-4) versus (13) is the type of force causing the flow. Also noticeable is the MFR's dependency on the wetting angle as shown in Figure 12. Note the dramatic reduction in MFR as the limit of wetability is approached, i.e., as \( \theta \to 90 \) deg.

Finally, the effect of temperature and gravity can both be seen in Figure 13. For a particular set of conditions, the MFR will vary by about 50 percent for a temperature change of 300 deg. The MFR for a \( 10^{-4} \) g-level diverges as the annular gap increases so that there is no constant value for the amount of change that occurs. For this problem, the g level makes very little contribution to the MFR until \( g \approx 1 \) g.

![Graph](image-url)
Figure 12. Capillary flow rates versus wetting angle for a particular gap size, temperature, g-level, and material.

Figure 13. Capillary flow rates versus annular gap for two temperatures and two g-levels.
REFERENCES


APPROVAL

TOLERANCE REQUIREMENTS TO PREVENT FLUID LEAKAGE IN THE CRUCIBLE/PLUNGER MEA EXPERIMENT MPS 770030

By Thomas J. Raths

The information in this report has been reviewed for technical content. Review of any information concerning Department of Defense or nuclear energy activities or programs has been made by the MSFC Security Classification Officer. This report, in its entirety, has been determined to be unclassified.

A. J. DESSLER
Director, Space Science Laboratory