Aerodynamic Effect of Combustor Inlet-Air Pressure on Fuel Jet Atomization

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AERODYNAMIC EFFECT OF COMBUSTOR INLET-AIR PRESSURE ON FUEL JETATOMIZATION

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Abstract

Mean drop diameters were measured with a recently developed scanning radiometer in a study of the atomization of liquid jets injected cross stream in high velocity and high pressure airflows. At constant inlet-air pressure, reciprocual mean drop diameter, \( D_{\text{mm}} \), was correlated with airflow mass velocity, \( \rho_a V_a \), to give the relationship \( D_{\text{mm}} \propto (\rho_a V_a)^{1.2} \) for a \( \rho_a V_a \) range of 10 to 177 \( \text{g/cm}^2\text{-sec} \) at 293 K. Over a combustor inlet-air pressure range of 1 to 21 atmospheres, the ratio of orifice to mean drop diameter, \( D_0/D_{\text{mm}} \), was correlated with the product of Weber and Reynolds number, \( \text{WeRe} \), and with the molecular-scale momentum-transfer ratio of gravitational to inertial forces, \( g/\rho V_r^2 \), as follows: \( D_0/D_{\text{mm}} = 1.4 \text{ (WeRe)}^{0.4} (g/\rho V_r^2)^{0.15} \) for values of \( \text{WeRe} \times 10^6 \), where \( \text{WeRe} = \rho_o D_0^2 \gamma V_r^2 \), \( \sigma \) and \( V_r \) are airstream density and velocity, respectively, \( \sigma \) and \( \gamma \) are liquid surface tension and kinetic viscosity, respectively, \( g \) is the acceleration due to gravity, 980 \( \text{cm/sec}^2 \), \( l \) is mean free molecular path, 6.11x10^{-6} \( \text{cm} \) for air at atmospheric pressure, and \( \bar{c} \) is root-mean-square molecular velocity, 4.85x10^{-4} \( \text{cm/sec} \) for air at 273 K.

Nomenclature

- \( \bar{c} \) root-mean-square molecular velocity, \( \text{cm/sec} \)
- \( b_{g,w} \) molecular diffusivity, \( g/(\text{cm})(\text{sec}) \)
- \( D \) diameter, \( \text{cm} \)
- \( D_{32} \) Sauter mean diameter, \( \mu n D^3/\pi n^2, \text{cm} \)
- \( g \) acceleration due to gravity, 980 \( \text{cm/sec}^2 \)
- \( I \) mean free molecular path, \( \text{cm} \)
- \( M \) molecular weight
- \( \text{Nu} \) Nusselt number for heat transfer, \( hD/k \)
- \( n \) number of molecules per unit volume
- \( P \) static pressure, \( \text{atm} \)
- \( R \) universal gas constant, 8.31x10^7 \( \text{ergs/(K)(mole)} \)
- \( \text{Re} \) Reynolds number based on orifice diameter, \( D_0 V_r/\gamma \)
- \( \text{Sc} \) Schmidt number based on mass diffusivity, \( u/b_{g,w} \)
- \( V \) velocity, \( \text{cm/sec} \)
- \( \text{We} \) Weber number based on orifice diameter, \( \rho_o D_0^2 \sigma/\gamma \)
- \( \gamma \) kinematic viscosity, \( \text{cm}^2/\text{sec} \)
- \( \sigma \) surface tension, dynes/cm
- \( \rho \) density, \( g/cm^3 \)
- \( u \) absolute viscosity, \( g/cm\text{-sec} \)

Subscripts:

- \( a \) airstream
- \( g \) gas molecule
- \( l \) liquid
- \( m \) mean
- \( o \) orifice
- \( r \) relative
- \( v \) vapor

Introduction

An experimental investigation was conducted to determine the effect of combustor inlet airflow static pressure on mean drop diameters obtained by atomization of water jets injected cross stream from simple orifices into axial flow airstreams. An improved scanning radiometer was developed at NASA Lewis Research Center and used to obtain mean drop diameter data for sprays. Such data are needed to supplement previous theoretical and experimental studies of liquid atomization in order to extend our knowledge to aerodynamic breakup of fuels in both high pressure and high velocity airflows.

Previous studies have shown that the force or mass velocity of an airstream is a very important factor in determining the fineness of atomization of fuel in a combustor primary-zone. As a result, the effect of airstream mass velocity on fuel atomization is receiving considerable attention in advanced combustor research investigations. Also, earlier studies have shown that high combustion efficiencies can be attained and exhaust emissions reduced by controlling the aerodynamic force of the airstream, in the breakup of liquid fuel jets, instead of relying on hydrodynamic pressure drop of the fuel to do the work as is the case in the use of pressure atomizing fuel nozzles. The high combustion efficiency and reduction in pollutants was attributed to improved fuel atomization. This conclusion was substantiated in a later study, in which it was found that nitrogen oxide emissions in the exhaust gases of swirl can combustor modules varied directly with the square of the mean drop diameter of the fuel spray.

The present trend of advanced combustor research toward higher primary-zone inlet air pressures and temperatures has stimulated the need to know the effect of airstream pressure on fuel atomization and combustion. Although there are very little data available that show this effect, expressions have been derived which relate Weber and Reynolds numbers to the mean drop diameter of fuel sprays and predict the effect of airstream pressure on mean drop size.
Different expressions have been derived depending on whether atomization occurs in the capillary-wave or acceleration-wave regimes. In Ref. 4 it was found, when transition from capillary to acceleration or aerodynamic wave breakup occurs the effect of the product of the Weber and Reynolds number on mean drop size increases considerably. As a result, a marked change in the effect of airstream pressure on mean drop size is also predicted. Such a correlation is quite useful in the design of fuel injectors for combustor applications since fuel nozzles can be calibrated with water and mean drop diameters can then be calculated for the desired fuel, such as Jet-A, with the aid of such correlations.

In the present investigation, relationships involving the product of Weber and Reynolds number investigated for the condition \( \text{WeRe} > 10^6 \). The acceleration or aerodynamic wave breakup regime was chosen for investigation since high velocity airstreams are required in simulating fuel atomization in turbine combustors at idle, take-off and cruise operating conditions. Thus, water jets were injected from an airfoil type of spray bar cross stream or normal to the airflow and mean drop diameters of the sprays were measured with an improved scanning radiometer recently developed at NASA Lewis Research Center. Combustor inlet-air static pressure was varied from 1 to 21 atmospheres over a range of airflow rates per unit area of 10 to 177 g/(cm\(^2\)) (sec), at 293 K. Spray bar orifice diameters were varied from 0.033 to 0.132 cm and liquid flowrates from 27 to 68 liters per hr. Mean drop diameter data were then correlated with the product of Weber and Reynolds number and the pressure sensitive molecular scale dimensionless group \( g/\Omega^2 \). The resulting empirical relationships for liquid-jet breakup were compared with those obtained from a previous experimental study of cross stream injection of radial jets in high velocity airflow.  

### Apparatus and Procedure

The test section is shown in Fig. 1 with two 5.1-cm-diam windows passing laser light beam through the spray of droplets produced in the high velocity and high pressure airflow. The closed-duct high pressure test facility in which the test section was mounted is shown in Fig. 2. Airflow was drawn from the laboratory supply system, at ambient temperature (293 K) and exhausted into the altitude exhaust system to obtain drop size data at low airstream pressure and into the atmosphere for high pressure airflow test conditions. The airflow control valve was opened until the desired airflow rate per unit area was obtained. The bellmouth test section shown in Fig. 3 has a total length of 0.152 m, an inside diameter of 0.076 m and is mounted inside of a duct that is 2.1 m in length with an inside diameter of 0.152 m.

Multiple jets of water were injected at the duct center line and directed cross stream with the fuel spray bar shown in Fig. 3. Water flow-rate was controlled, by gradually opening and regulating the valve, over a range of 27 to 68 liters per hr. One of the fuel spray bars is shown in detail in Fig. 4. Three different spray bars were investigated to obtain drop size data over an orifice diameter range of 0.033 to 0.130 cm. The first spray bar had twelve 0.033-cm-diam orifices, the second had four 0.102-cm-diam orifices and the final configuration had three 0.130-cm-diam orifices, respectively. Thus, at a liquid flowrate of 22.7 liters per hr. liquid/jet velocities were 614, 194, and 158 cm/sec, respectively, for the three spray bars.

After water and airflow rates were set, mean drop diameter data were obtained with the scanning radiometer mounted 25.4 cm downstream of the fuel tube supporting the spray bar. The scanning radiometer optical system shown in Fig. 5 consisted of a 1-milliwatt helium-neon laser, a 0.003-cm-diam aperture, a 7.5-cm-diam collimating lens, a 10-cm-diam converging lens, a 5-cm-diam collecting lens, a scanning disk with a 0.5 by 2.5 cm slot, a timing light, and a photo-multiplier detector. A more complete description of the improved scanning radiometer, the mean drop diameter range of 10 to 500 \( \mu \)m, and the method of determining mean particle size are discussed in Refs. 5 and 6.

### Experimental Results

To obtain a better understanding of liquid jet atomization theory and thereby advance fuel injection technology for jet engine applications, the aerodynamic-wave breakup of liquid jets in high pressure and high velocity airflow was investigated in a simulated gas turbine combustor primary-zone. Mean drop diameter data were obtained for water jets atomized under simulated high pressure combustor inlet airflow conditions. The atomization of a liquid jet in an axial-flow airstream is depicted in Fig. 6 as a process of forming ligaments from the crests of waves formed on the surface of a liquid jet. The ligaments are then atomized into drops. Short wave-length disturbances near the tip of the injector produced relatively small droplets whereas long wave-length disturbances farther out in the airstream produced relatively large drops.

### Airstream Mass Velocity Effect on Mean Drop Size

Mean drop diameter data were determined for the breakup of water jets injected cross stream in axial airflows. As a measure of fineness of atomization or spray specific surface area, the reciprocal mean drop diameter, \( D_m^{-1} \), was determined with the scanning radiometer and plotted against mass velocity, \( D_m \), as shown in Fig. 7. The reciprocal of the mean drop diameter, \( D_m^{-1} \), was used since it is useful in characterizing a spray in terms of the surface area per unit volume of the spray and can be defined as:

\[
D_m^{-1} - D_{32}^{-1} = \frac{\pi D_3^2}{\pi D_3^2} = D_23
\]

where \( D_3 \) is a single drop having the same ratio of surface area to volume as that of the entire spray.
was found that heat transfer coefficients for valid over an airstream static pressure range of \( \text{gl/cm}^2 \), was needed in the correlation to make it Schmidt numbers, \( \text{ReSc} \). Also it was found that a new pressure sensitive dimensionless group, \( \text{Nu} \), was required to produce the same mean drop size at an inlet-air pressure of only 2 atmospheres.

**Airstream Pressure Effect on Mean Drop Size**

In a previous study described in Ref. 7, it was found that the mean drop size of sprays produced by cross stream injection of a number of different liquids into airstreams could be correlated with the product of the Weber number and the Reynolds number, \( \text{WeRe} \), as follows:

\[
\frac{D_0}{D_m} = 0.20 (\text{WeRe})^{0.25} \quad \text{for } \text{WeRe} < 10^6 \quad (2)
\]

for the case of capillary-wave breakup of liquid jets. However more recently it was shown in Ref. 4 that, at high values of airstream mass velocity, aerodynamic-wave breakup occurs and the expression becomes:

\[
\frac{D_0}{D_m} = 0.027 (\text{WeRe})^{0.4} \quad \text{for } \text{WeRe} > 10^6 \quad (3)
\]

and the transition from capillary-wave to aerodynamic-wave breakup occurs at \( \text{WeRe} = 10^6 \) as shown in Fig. 8 which is taken from Ref. 4.

**Aerodynamic-wave breakup is the regime of primary concern in this study, that is, \( \text{WeRe} > 10^6 \) as given in Eq. (3). This is demonstrated in Fig. 9 where experimental values of \( \frac{D_0}{D_m} \) are plotted against calculated values of \( \text{WeRe} \). The slope of each plot shows good agreement with the exponent 0.4 as given in Eq. (3) for aerodynamic-wave breakup of liquid jets.**

**Airstream Pressure Effect on Mean Drop Size**

In a previous study described in Ref. 8, it was found that heat transfer coefficients for vaporizing drops and Nusselt number, \( \text{Nu} \) could be correlated with the product of the Reynolds and Schmidt numbers, \( \text{ReSc} \). Also it was found that a new pressure sensitive dimensionless group, \( \text{gl/cm}^2 \), was needed in the correlation to make it valid over an airstream static pressure range of 0.59 to 1.97 atmospheres. Thus, the following semiempirical expression was derived:

\[
\frac{D_0}{D_m} = f (\text{WeRe}, \text{gl/cm}^2) \quad (4)
\]

where \( \text{Nu} = hD/k, \text{Re} = uD/\nu \) and \( \text{Sc} = \nu/\alpha \). In the formation of a spray of drops, it could also be assumed that the reciprocal mean drop diameter might be a function of the molecular scale momentum-transfer ratio of gravitational to inertial forces, \( \text{gl/cm}^2 \), as follows:

\[
\frac{D_0}{D_m} = f (\text{WeRe}, \text{gl/cm}^2) \quad (5)
\]

**Summary of Results**

Empirical correlations of reciprocal mean drop diameter with airstream mass velocity were derived for aerodynamic-wave breakup of liquid jets injected cross stream in high-pressure high-velocity airflow. This expression shows that the effect of combustor inlet-air pressure, \( P_a \), on reciprocal mean drop diameter, \( D_m \), can be written as, \( D_m^{-1} = -0.025 \), since \( (\text{gl/cm}^2) \) is plotted against the dimensionless group \( \text{gl/cm}^2 \) as shown in Fig. 10. From the slope of this plot, it is evident that \( D_0/D_m = \text{gl/cm}^2 \). Thus by plotting \( D_0/D_m \) against \( (\text{WeRe})^{0.4} \cdot (\text{gl/cm}^2) \), as shown in Fig. 11, the following expression is obtained:

\[
\frac{D_0}{D_m} = 1.4 (\text{WeRe})^{0.4} (\text{gl/cm}^2) \quad (6)
\]

for aerodynamic breakup of liquid jets injected cross stream in high-pressure high-velocity airflow. This expression shows that the effect of combustor inlet-air pressure, \( P_a \), on reciprocal mean drop diameter, \( D_m \), can be written as, \( D_m^{-1} = -0.025 \), since \( (\text{gl/cm}^2) \) is plotted against the dimensionless group \( \text{gl/cm}^2 \) as shown in Fig. 10. From the slope of this plot, it is evident that \( D_0/D_m = \text{gl/cm}^2 \). Thus by plotting \( D_0/D_m \) against \( (\text{WeRe})^{0.4} \cdot (\text{gl/cm}^2) \), as shown in Fig. 11, the following expression is obtained:

\[
\frac{D_0}{D_m} = 1.4 (\text{WeRe})^{0.4} (\text{gl/cm}^2) \quad (6)
\]

To test the validity of this assumption, \( D_0/D_m = \text{gl/cm}^2 \) is plotted against the dimensionless group \( \text{gl/cm}^2 \) as shown in Fig. 10. From the slope of this plot, it is evident that \( D_0/D_m = \text{gl/cm}^2 \). Thus by plotting \( D_0/D_m \) against \( (\text{WeRe})^{0.4} \cdot (\text{gl/cm}^2) \), as shown in Fig. 11, the following expression is obtained:

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\[
\frac{D_0}{D_m} = 1.4 (\text{WeRe})^{0.4} (\text{gl/cm}^2) \quad (6)
\]
diameter, \( \frac{D_0}{D_m} \), was correlated with the product of Weber and Reynolds number, \( \text{WeRe} \), and with the pressure sensitive dimensionless group, \( \frac{g_l}{c^2} \), as follows:

\[
\frac{D_0}{D_m} = 1.4 \left( \text{WeRe} \right)^{0.4} \left( \frac{g_l}{c^2} \right)^{0.15}
\]

where \( \frac{g_l}{c^2} = 2.55 \times 10^{-12} \) for airstreams at atmospheric pressure.

**Appendix**

**Calculation of Molecular-Scale Momentum-Transfer Group, \( \frac{g_l}{c^2} \)**

The mean free molecular path \( l \) may be expressed as:

\[
l = \frac{1}{\sqrt{2}} \frac{n D^2}{\pi^2} = 6.11 \times 10^{-6} \text{ cm}
\]

since the number of molecules per unit volume \( n \) is \( 2.7 \times 10^{19} \) at a temperature of 0° C and a pressure of one atmosphere and the diameter of an air molecule, \( D_0 \), is \( 3.7 \times 10^{-8} \text{ cm} \).

The root-mean-square molecular velocity \( \bar{c} \) may be expressed as \( \bar{c} = (3RT/M)^{0.5} \) which yields:

\[
\bar{c}^2 = \frac{3}{29} \left( \frac{8.31 \times 10^7}{273} \right) = 2.35 \times 10^9 \text{ (cm/sec)}^2
\]

Since \( g \) is 980 cm per sec per sec:

\[
\frac{g_l}{c^2} = \frac{1980 \left( 6.11 \times 10^{-6} \right)}{(2.35 \times 10^9)} = 2.55 \times 10^{-12}
\]

**References**

Figure 1. - Apparatus and auxiliary equipment.
Figure 3. - High pressure test section.

Figure 4. - Schematic diagram of multiple-orifice spray bar. (Dimensions are in centimeters.)
Figure 5. - Scanning radiometer optical path.
Figure 6. - Schematic of a liquid jet breaking up into ligaments and drops.
Figure 7. - Variation of reciprocal mean drop diameter, $D_m^{-1}$, with airstream mass velocity, $\rho_a V_a$. 

(a) Orifice diameter, 0.1016 cm. 
(b) Orifice diameter, 0.132 cm. 
(c) Orifice diameter, 0.033 cm.
Figure 8. Relation between orifice to mean diameter ratio and Weber-Reynolds number.
Figure 9. - Variation of mean drop diameter, $D_m$, with product of Weber and Reynolds number.
Figure 10. - Correlation of mean drop diameter, $D_m$, with dimensionless group $gl/c^2$. 

(a) Orifice diameter, 0.1016 cm. 
(b) Orifice diameter, 0.033 cm. 
(c) Orifice diameter, 0.132 cm.
Figure 11. - Correlation of mean drop diameter, $D_m$, with dimensionless groups $gl/c^2$ and WeRe.

(a) Orifice diameter, 0.1016 cm.
Figure 11. - Continued.

(b) Orifice diameter, 0.132 cm.
Figure 11. - Concluded.

(c) Orifice diameter, 0.033 cm.
**1. Title and Subtitle**
Aerodynamic Effect of Combustor Inlet-Air Pressure on Fuel Jet Atomization

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**16. Abstract**
Mean drop diameters were measured with a recently developed scanning radiometer in a study of the atomization of liquid jets injected cross stream in high velocity and high pressure airflows. At constant inlet-air pressure, reciprocal mean drop diameter, $D_m^{-1}$, was correlated with airflow mass velocity, $\rho_a V_a$, to give the relationship $D_m^{-1} \sim (\rho_a V_a)^{1.2}$ for a $\rho_a V_a$ range of 10 to 177 g/cm$^2$-sec at 293 K. Over a combustor inlet-air pressure range of 1 to 21 atmospheres, the ratio of orifice to mean drop diameter, $D_o/D_m$, was correlated with the product of Weber and Reynolds number, $WeRe$, and with the molecular-scale momentum-transfer ratio of gravitational to inertial forces, $g\ell/c^2$, as follows:

$$
D_o/D_m = 1.4 \left(\frac{WeRe}{10^6}\right)^{0.4} \left(\frac{g\ell/c^2}{0.15}\right)
$$

for values of $WeRe > 10^6$, where $WeRe = \rho_a D_o^2 V_r^3 / \sigma \gamma$, $\rho_a$ and $V_r$ are airstream density and velocity, respectively, $\sigma$ and $\gamma$ are liquid surface tension and kinetic viscosity, respectively, $g$ is the acceleration due to gravity, 980 cm/sec$^2$, $\ell$ is mean free molecular path, 6.11x10$^{-6}$ cm for air at atmospheric pressure, and $c$ is root-mean-square molecular velocity, 4.85x10$^4$ cm/sec for air at 273 K.