ABSOLUTE PHOTOIONIZATION CROSS SECTIONS OF ATOMIC OXYGEN

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ABSTRACT

The absolute values of the photoionization cross sections of atomic oxygen have been measured from the ionization threshold to 120 Å. An autoionizing resonance belonging to the 2s2p^4(^3P)3p(3d0, 3s0, 3p0) transition has been observed at 479.43 Å and another line at 389.97 Å. The experimental data is in excellent agreement with rigorous close-coupling calculations that include electron correlations in both the initial and final states.

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INTRODUCTION

In recent years progress has been made in the theoretical understanding of photoionization of closed-shell atoms. In general, electron correlation effects have been found to be very important. Efforts are now underway to extend this understanding to open shell atoms. However, there is a serious lack of experimental data dealing with open shell atoms to provide adequate data for comparison to theory. This is understandable because of the problem of producing these atoms. In the present work we have chosen to study atomic oxygen because it can be produced in reasonable numbers in a simple microwave discharge and because of its importance to upper atmosphere research.

The first measurement of the absolute photoionization cross section of atomic oxygen was made by Cairns and Samson in 1964. Two subsequent measurements were made by Comes et al. and by Kohl et al. These measurements were made at a few discrete wavelengths from threshold to about 450Å. However, there is quite a variation between the different measurements, reaching a factor of two near threshold.

Huffman et al. and Dehmer et al. have studied the autoionizing structure of atomic oxygen from threshold to 650Å but do not present absolute cross sections. The photoelectron spectra of atomic oxygen has been studied by Samson and Petrosky showing the presence of excited molecular oxygen in the products of a microwave discharge in O₂.

On the theoretical side, numerous calculations have been made since the earliest calculations by Bates and Seaton in 1949. Again, a large variation in absolute cross sections exists, ranging from a factor of 50% in the 500-600 Å region to a factor of two near threshold.
The main aim of the present work was to measure the relative cross sections of atomic oxygen as accurately as possible and over a large wavelength range (120-900 Å). Then to make an absolute measurement at one or two wavelengths allowing the relative values to be placed on an absolute basis. The 584Å He I and 304 Å He II lines were chosen for the absolute measurement.

EXPERIMENTAL

Atomic oxygen was produced in a microwave discharge by flowing a mixture (in the ratio 1:4) of O₂ and He at ~ 0.2 Torr through a pyrex tube coated internally with boric acid. The discharged products were constrained to flow past a small orifice leading to the ion chamber of a mass spectrometer (see Fig. 1). A 60 L/s rotary pump maintained a fast flow of the mixture to minimize wall recombination of the oxygen atoms.

The literature describes many materials used for coating flow tubes. These include phosphoric acid, teflon, hydrofluoric, boric acid, etc. However, we obtained best results with the boric acid treatment. The flow tube was first cleaned with a detergent and rinsed. When dry, a boiling saturated solution of boric acid was poured into the flow tube, coating all of the interior surface, then poured out. The tube was subsequently heated at 200°C in an oven for about 4-6 hours.

The products of a microwave discharge in O₂ are ground state O(3P) atoms and excited state O₂(1Δ) molecules in addition to the residual ground state molecules. The gas pressure used and the geometry of the flow tube insure sufficient collisions to de-excite most species and thermalize the
products. In an identical arrangement used to study the photoelectron spectra of $O_2$ and $O$ at 584\AA{} we found the integrated signal from $O_2(^1\Sigma)$ to be ~ 1\% of $O_2(^3\Sigma)$.\textsuperscript{7} Other authors quote values of 3 to 10\%.\textsuperscript{23-25} We make use of this information in the derivation, in the Appendix, of $\sigma(o)$ the photoionization cross section of atomic oxygen.

A photoionization-magnetic mass spectrometer with a mass resolution of about 1 in 65 was used to identify the ions produced in the ion chamber. Details of this instrument have been described previously.\textsuperscript{26,27} It was estimated that about 20-30\% of $O_2$ was dissociated as indicated by the decrease in the intensity of the $O_2^+$ signal from the mass spectrometer when the microwave generator was switched on.

The light source was a spark discharge lamp that produced a rich spectrum of intense lines extending down to about 100\AA{}.\textsuperscript{28} The radiation was dispersed by a 2.2 m grazing incidence monochromator.

Our method for measuring the photoionization cross section of atomic oxygen was similar to that used by Comes et al.\textsuperscript{3} but differs in some important details. The measurement procedure was as follows:

The incident radiation was free to pass through the ion chamber of the mass spectrometer and subsequently monitored by a windowless photo-diode. The ions produced were mass-analyzed and detected with a Johnson type electron multiplier. To eliminate any effects caused by light source intensity variations each ion current was measured simultaneously with the photo-diode current. Because $O^+$ ions were also produced from dissociative photoionization of $O_2$ it was necessary to measure the ion currents $O^+$ and $O_2^+$ with the microwave discharge off and on. An analysis of the ionization process leads to the
following equation for the absolute photoionization cross section of atomic oxygen $\sigma(0)$, see Appendix, Eq. (A14),

$$\sigma(0) = \left[\frac{1}{2}(1 - \alpha)\right]\left(\frac{\Gamma_2 T_2}{\Gamma_1 T_1}\right) \left[\left(\frac{S_1'}{S_1}\right) - \frac{S_1}{S_2}\right] \sigma_\Sigma .$$

Subscripts 1 and 2 refer to atomic and molecular properties, respectively, and primes indicate measurements made with the microwave on. Thus, $\Gamma_1$ and $\Gamma_2$ represent the secondary electron emission probability for $O^+$ and $O_2^+$ ions, respectively, impinging on the first dynode of the electron multiplier. $S_1'$ and $S_1$ represent the $O^+$ ion signals with the microwave generator on and off, respectively. $S_2$ represents the $O_2^+$ ion signal with no microwave discharge. $T_1$ and $T_2$ refer to the transmission of $O^+$ and $O_2^+$ ions through the mass spectrometer, respectively. $\sigma_\Sigma$ is the dissociative photoionization cross section for producing $O_2^+$ ions from neutral $O_2$ ground state molecules (microwave off). These cross sections have been tabulated by Samson et al.\textsuperscript{26} The constant $\alpha$ represents the ratio of the $O_2$ number density with discharge on and off. That is, $\alpha = n'(O_2)/n_\Sigma$, where $n'(O_2) = n_\Sigma + n_\Xi$, which is the sum of the number densities of the $O_2$ molecules in their $^3\Sigma$ and $^1\Delta$ states with the discharge on. $n_\Sigma$ is the number density of $O_2(3\Sigma)$ with discharge off. An approximate value for $\alpha$ can be determined by the derivation given in the Appendix, namely,

$$\alpha = \frac{S_2'}{S_2} .$$
The ratio $S_2'/S_2$ was measured at numerous wavelengths within the ionization continuum and was found to be constant within $\pm 1.5\%$. Typical values were 0.7 to 0.8 depending upon the condition of the boric acid coating. However, when we selected wavelengths that coincided with autoionizing transitions in the $O_2$ spectrum we found some variation in the ratio. The maximum variation was 10\%. From the Appendix we see that the ratio $S_2'/S_2$ is weakly dependent on the ratio of the ionization cross sections of $O_2(^1\Delta)$ and $O_2(^3\Sigma)$. If this ratio shows large variations with wavelength, as is likely in autoionizing regions, we can expect the variation observed above.

The relative atomic photoionization cross section can be obtained from Eq. (1) as shown in the Appendix. The term $(S_2'/\sigma_2)$ is proportional to the absolute intensity $I_o$ of the radiation, which in turn is proportional to $(i_{ph}/\eta)$, where $i_{ph}$ is the photodiode current and $\eta$ is the photoelectric efficiency of the cathode. From this we obtain the relation given by Eq. (A18) in the Appendix, namely,

$$\sigma(0) \propto (n/i_{ph})(S_1' - \alpha S_1) \ .$$

(3)

Our procedure was to measure the relative cross section over the entire wavelength region by use of Eq. (3). It was important to keep the gas pressure constant during the measurements. This was achieved by use of a Baratron capacitance manometer with a servo-controlled leak valve. After accurate relative cross sections were made they were placed on an absolute basis by determining $\sigma(0)$ from Eq. (1) at 304 and 584Å.

When using Eq. (1) the assumption was made that the transmission factors $T_2$ and $T_1$ were equal because both $O_2^+$ and $O^+$ ions were formed with
thermal energies and were extracted from the mass spectrometer ion chamber with equal energies. To avoid mass discrimination within the ion chamber a repeller plate inside the ion chamber produced a field of approximately 100 V/cm to drive the ions out into the accelerating field of the mass spectrometer where they received an additional 800V of energy before entering the mass analyzer.

In the development of Eq. (1) in the Appendix the value of the ratio $T_1^D/T_1$ is important. This is the ratio of the transmission of energetic atomic oxygen ions produced in the dissociative ionization process to the transmission of thermal energy oxygen ions produced in the microwave discharge. The transmission of ions in any mass spectrometer with narrow entrance and exit slits, as in the present instrument, will be small for ions originally created with excess kinetic energy as in the process of dissociative ionization. This ratio can be determined as follows: By measuring the number of ions/photons transmitted the relative apparent dissociative ionization cross section can be measured. This quantity is normalized to the true dissociative ionization cross section, $26 \sigma^D_{\Sigma_g}$, at threshold where the ion energy is close to zero and the transmission is essentially $T_1$. The ratio of this normalized curve to the true value of $\sigma^D_{\Sigma_g}$ yields $T_1^D/T_1$. The individual curves are shown in Fig. 2. It can be seen that the ratio varies from 0.2 and 1.0 between 120 and 650Å.

The steps in the solid line near threshold for the absolute curve represent the vibrational space of the $B^2\Sigma_g^-$ state of $O_2$. The heights of the steps are proportional to the transition probabilities. Transitions into this state are followed by predissociation producing the observed $O^+$ ions.

The value of the relative response of the electron multiplier ($\Gamma_2/\Gamma_1$) to $O^+_2$ and $O^+$ ions was measured and found to be 1.08 when the ions impinged with energies ~ 3.9 kV.
RESULTS AND DISCUSSION

The measured absolute photoionization cross sections of atomic oxygen are tabulated in Table I and are shown in Fig. 3 along with the previous experimental results. The results by Cairns and Samson\cite{2} were influenced by autoionizing structure in atomic oxygen\cite{5,6} and possibly by structure in the excited \( O_2(1\Delta) \) molecular species. Thus, we have selected from their results only the data points that appear to be free from the effects of structure, and we have shown all their data points in the non-structured region below 665Å. The latter data are in very good agreement with our present results. The data of Kohl et al.\cite{4} fall between our earlier results and the present ones and average about 10% higher than the present data. This agreement is significant because of the diverse nature of the three experiments. The results of Comes et al.\cite{3} are consistently 30 to 50% lower over most of the wavelength range from threshold to 450Å. Moreover, their equation for obtaining \( \sigma(0) \) appears to be missing a factor of 2 in the denominator when compared to our Eq. (1) expressing the same relation. This would further reduce their values relative to the present results.

The experimental data clearly show the contribution to the cross section for producing \( O^+ \) ions in their \( 4s^0, 2p^0, \) and \( 2p^0 \) states. Care was taken to avoid measurements that coincided with the autoionizing structure preceding the \( 2p^0 \) and \( 2p^0 \) thresholds (tabulated by Huffman et al.\cite{5} and Dehmer et al.\cite{6}). However, at wavelengths shorter than the \( 2p^0 \) threshold data were taken at all possible wavelengths because the position of structure is unknown in this region. There is clear evidence of an autoionizing line at approximately 479.4Å, presumably belonging to a Rydberg series leading to the
level. Less evident is possible structure at 390 Å. These were chance coincidences with our discrete emission lines. A continuum source of radiation will be used to explore this region in more detail.

The random rms errors of the measured quantities cause an uncertainty in the relative cross section curve, Eq. (3). The absolute value of \( \sigma(0) \) obtained from Eq. (1) has an estimated random rms error of \( \pm 9\% \). However, the scatter among the data points is much less than the quoted errors as can be seen from Fig. 3.

We measured the absolute value of \( \sigma(0) \) at 584 Å and 304 Å by use of Eq. (1) and obtained cross sections of 13.7 Mb and 7.8 Mb, respectively. The ratio of these two absolute values is 1.76, whereas the ratios of the relative values obtained by using Eq. (3) gives 1.72. The good agreement of these two ratios is encouraging because they are independent measurements. In Eq. (3) we must use the cross section of Ne to determine \( n \), whereas Eq. (1) requires the dissociative ionization cross sections for producing \( O_2^+ \) from \( O_2 \).²⁹

Our present technique should provide accurate relative photoionization cross sections of atomic oxygen. To check that our normalization of the data at 304 and 584 Å to provide absolute cross sections is reasonable we first consider the assumption that the atomic cross section should be approximately equal to one-half the total absorption cross section of molecular oxygen for high energy photons. Figure 4 shows this comparison between \( \sigma(0) \) and \( \frac{1}{2} \sigma(O_2) \) from 500-120 Å. Over most of the range \( \frac{1}{2} \sigma(O_2) \) is within \( \pm 10\% \) of the atomic cross section, and there appears to be a convergence between the two curves as they approach 120 Å (103 eV). Of course, there is no reason that the two curves should precisely coincide in this wavelength region. Ejection of valence shell electrons from the molecules are still important and this can
move molecular oscillator strengths from one spectral region to another. In fact, the bump in the \( \frac{1}{2}\sigma(\text{O}_2) \) curve around 300Å is caused by an increase in dissociative ionization of \( \text{O}_2 \) (see ref. 26), which presumably has stolen oscillator strength from the longer wavelength region. However, we might expect the two curves to agree at higher photon energies, particularly when inner-shell electrons are involved (e.g. K-shell electrons). The work by Henke and co-workers certainly supports this premise.\(^{30}\)

A more accurate check on the accuracy of the absolute data is to measure the total oscillator strength for the absorption process. According to the Thomas-Reiche-Kuhn sum rule the total oscillator strength \( f(\text{total}) \) should equal the number of electrons in an atom or molecule.\(^{31}\)

\[
\text{Thus, } f(\text{total}) = \sum_s f_s + 113 \int_0^\text{EIP} \frac{\sigma_a(\lambda)}{\lambda^2} \, d\lambda, \tag{4}
\]

where the first term is the oscillator strength for the discrete spectrum and the second term applies to the ionization continuum. \( \sigma_a \) is the total absorption cross section at wavelength \( \lambda \). For an atom the absorption and ionization cross sections are identical at wavelengths shorter than the ionization threshold. Thus, we evaluated the continuum oscillator strength from the ionization threshold, 910Å, down to 120Å using the present data and from 120Å to 0Å from the compilation by Henke et al.\(^{30}\) The results were 4.58 and 2.58, respectively, yielding a total continuum \( f \)-value of 7.16. The problem now is to determine the contribution from discrete lines. \( f \)-values of several discrete lines, including autoionizing transitions, have been
measured by many groups. A critical compilation of the data has been given by Wiese et al. We have selected all the allowed absorption transitions from these compilations along with the data reported by Dehmer et al. and obtain $E_f = 0.71$. This gives a total oscillator strength of 7.87, which is only 1.6% less than the required value of 8. Of course, there will be a small contribution from the remaining discrete transitions still to be analyzed.

Although the uncertainty of the line oscillator strengths, quoted by Wiese et al., are 25 to 50% this only alters the final total oscillator strength by a few percent. Thus, the above analysis of the total oscillator strength provides a self consistent check on the accuracy of the present data.

Figure 5 compares our experimental results (solid circles) with the theoretical calculations of Starace et al., Taylor and Burke, and with Pradhan. The data of Starace et al. (solid line) were derived by use of Herman-Skillman (HS) wave functions. These calculations do not include any electron correlation effects. The agreement with the experimental data is extraordinary! There is precise agreement in shape and magnitude with experiment from 120 to 500 Å and less than 10% deviation from 500 Å to the $2p^0$ threshold at 731.8 Å.

In contrast, the calculations of Taylor and Burke (dashed line) used the more rigorous R-matrix method. They point out that all channels associated with the main final states along with all channels of the initial state (viewed as a bound state of the electron-plus-ion system) were included in their cross section calculation. Thus, in addition, they were able to calculate the positions and shapes of many autoionizing lines. Their results (dipole length)
are nearly identical to the HS calculations from the $2p^0$ threshold to shorter wavelengths. Their agreement with experiment from threshold to 400Å is even better including their prediction of the $2s2p^4(^4P)3p(^3D^0, ^3S^0, ^3P^0)$ autoionizing lines. They predict, in agreement with experiment, the slow rise in cross section nearly 20Å away from the peak shown in Fig. 5 by the dashed line. They also predict the peak position of the resonance lines to occur at 479.3Å, 477.6Å, and 475.6Å. The position of the observed resonance can be estimated only from the partial coincidence with the resonance of an emission line from our light source at 479.43Å. Taylor and Burkes' results near the $^4S^0$ threshold are shown in the dipole length (short dashes) and dipole velocity (long dashes) approximations. At threshold their cross sections are 4.1 and 3.4 Mb, respectively.

The calculations by Pradhan$^{19}$ (crosses) and earlier by Pradhan and Saraph$^{18}$ also used the close-coupling approximation with correlations in both the initial and final states. However, there are slight differences in the number and types of channels included in their calculations compared to those of Taylor and Burke. Again the agreement with the present data is excellent. They have calculated the positions of many autoionizing resonances. We reproduce their cross sections before and after the $3p(^3D^0, ^3S^0, ^3P^0)$ resonance to show the agreement with Taylor and Burke and with experiment.

The good agreement between the HS and close-coupling calculations with the experimental results suggests that correlation effects are not too important in calculating the total photoionization cross sections of atomic
oxygen, except near thresholds and in predicting the shape and positions of autoionizing structure. However, good calculations that only partially take into account correlations show poorer agreement with the present data, at least from threshold down to about 450Å. Towards shorter wavelengths most of the calculations agree with experiment.

The one remaining discrepancy between theory and experiment is the shape and magnitude of the cross section between the $^2\Pi_0^+$ threshold and the first resonance line. It is possible that there is still some correlation lacking that might explain this peak in the cross section.

ACKNOWLEDGEMENTS

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REFERENCES


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FIGURE CAPTIONS

1. Diagram of pyrex flow tube and microwave cavity for the production of atomic oxygen.

2. Dissociative photoionization cross sections for the production of $O^+$ ions from $O_2(O_2^D)$. curve (a): Absolute values. curve (b): Relative values influenced by instrumental discrimination against energetic ions. Data normalized at threshold to absolute value where the kinetic energy of the fragment ions is essentially zero. The ratio of the two curves is equal to the transmission $T_{1D}$ of the energetic $O^+$ ions through the mass spectrometer.

3. Absolute photoionization cross sections of atomic oxygen as a function of wavelength. • Present data; o Cairns and Samson (ref. 2); △ Kohl et al. (ref. 4); □ Comes et al. (ref. 3).

4. Comparison of direct photoionization of atomic oxygen, $\sigma(0)$, with one half the molecular cross section $\frac{1}{2}\sigma(O_2)$, as a function of wavelength.

5. Comparison of the absolute photoionization cross section of atomic oxygen with theoretical results. • present experimental data; x close coupling calculations by Pradhan (ref. 19); Solid line (excluding resonances), Herman-Skillman calculations by Starace et al. (ref. 16); Short and long dashed lines, dipole velocity and length approximations, respectively, in the close-coupling calculations by Taylor and Burke (ref. 17).
Determinations of $\sigma(0)$

When atomic oxygen is produced by a microwave discharge in $O_2$ the products of the discharge are primarily $O(^3P)$, $O_2(^3\Sigma)$, and $O_2(a^1\Delta)$. Each of these species can be ionized in the spectral region of interest. In addition, both the $^3\Sigma$ ground state and the $^1\Delta$ excited state of $O_2$ produce atomic ions through the process of dissociative photoionization. The following analysis to determine the direct photoionization cross section of atomic oxygen $\sigma(0)$ takes into account the presence of these products.

From the Lambert-Beer Law the number of ions of a given species that are produced per second is given by,

$$N = I_0 e^{-nl}$$

where $I_0$ is the incident number of photons/s, $\sigma$ is the photoionization cross section for producing a specific ion, $n$ is the number density of the neutral gas, and $l$ is the path length from which the ions are collected. The above expression is true for $nl \ll 1$.

After the ions have passed through a mass spectrometer, of transmission $T$, and are detected by an electron multiplier the output signal $S$ is given by

$$S = (I_0 e^{-nl}) G T e,$$

where $G$ is the multiplier gain, $T$ is the efficiency for secondary electron emission for a specific ion, and $e$ is the electronic charge.

Applying Eq. (A2) to the detection of $0^+$ and $O_2^+$ ions under the conditions with the microwave generator switched OFF and ON (primed quantities) and letting the constant $C = l Ge$ we obtain the following equations,
Microwave OFF

\[ \begin{align*}
0_2^+: & \quad S_2 = (I_0 C)(T_2 T_2)\sigma_L n_L. \\
0^+: & \quad S_1 = (I_0 C)(T_1 T_1)\sigma_D n_L.
\end{align*} \tag{A3} \tag{A4} \]

Microwave ON

\[ \begin{align*}
0_2^+: & \quad S'_2 = (I_0 C)(T_2 T_2)(\sigma'_L n_L + \sigma'_D n_\Delta). \\
0^+: & \quad S'_1 = (I_0 C)T_1^D T_1^D n_L + T_1^D n_\Delta + T_1 n(0)n'(0)].
\end{align*} \tag{A5} \tag{A6} \]

The subscripts 1 and 2 refer to atomic and molecular properties, respectively, and the superscript D refers to dissociative ionization processes. For example, \( T_1^D \) represents the transmission through the mass spectrometer of the energetic atomic ions produced by dissociative photoionization and \( \sigma_L^D \) represents the dissociative ionization cross section for producing \( 0^+ \) from \( O_2 \) in the ground \( 3^\Sigma \) state. The subscript \( \Delta \) refers to \( O_2 \) in the excited \( \text{a}^1\Delta \) state and \( n_L, n_\Delta \) represents the number densities of \( O_2 \) in their \( \Sigma \) and \( \Delta \) states, respectively, when the microwave generator is on.

The total number density of molecular oxygen with the microwave off is \( n_L \) (only ground state molecules present). With the microwave on some of the molecules are lost in producing atoms and some are excited into the \( ^1\Delta \) state. Thus, the new number density of molecules is given by,

\[ n'(O_2) = n'_L + n'_\Delta. \tag{A7} \]

The lost molecules are then represented by the quantity \([n_L - n'(O_2)]\).
The number density $n'(0)$ of the atomic oxygen produced by the microwave discharge and appearing in the ion chamber must be twice the number of $O_2$ molecules that disappear in the ion chamber when the discharge is on. This will be true provided that any atoms formed in the flow tube and lost by wall recombinations or any other mechanism reform into $O_2$. To check the validity of this assumption the mass spectrum was scanned with and without the microwave discharge to search for new products, for example, $O_3$. However, no additional products were observed. Thus,

$$n'(0) = 2[n_{\Sigma} - n'(0_2)] \quad (A8)$$

The following defined quantities help to simplify the above equations, namely,

$$\alpha = n'(0_2)/n_{\Sigma} \quad (A9)$$

$$2(1-\alpha) = n'(0)/n_{\Sigma} \quad (A10)$$

$$\beta = n'_\Delta / n'(0_2) \quad (A11)$$

First, eliminate $I_0C$ from Eq. (A6) by use of Eq. (A3) and solve for $\sigma(0)$, obtaining,

$$\sigma(0) = (S_1'/S_2')(T_2' T_2'/T_1')(n_{\Sigma}/n'(0))\sigma_{\Sigma} - T_1^D(n'/n'(0))\sigma_{\Delta}^D - T_1^D(n_{\Sigma}/n'(0))\sigma_{\Sigma}^D \quad (A12)$$
Factor out the quantity \( \left( \frac{n_2}{n_1'}(0) \right) \) and eliminate all number densities by use of Eqs. (A9), (A10), and (A11). Then Eq. (A12) becomes,

\[
\sigma(0) = \left[ \frac{1}{2}(1-\alpha) \right] \left( S'_1/S_2 \right) \left( R_2 T_2/R_1 T_1 \right) \sigma_\Sigma - \left( T_1^D/T_1 \right) \alpha \beta (\sigma_D^D-\sigma_D^\Sigma)-(T_1^D/T_1) \alpha \sigma_\Sigma^D. \tag{A13}
\]

Although no measurement of \( \sigma_D^D \) has ever been made it is reasonable to estimate that it is of the same order of magnitude as \( \sigma_D^\Sigma \), and each is \( \ll \sigma_\Sigma^\Sigma \). Thus, \( (\sigma_D^D-\sigma_D^\Sigma)/\sigma_\Sigma^\Sigma \) will range from 0 to \( \ll 1 \). From Fig. 2 we see that \( (T_1^D/T_1) \) ranges from 0.23 to 1. We estimate \( \beta \) to be \( \sim 0.01 \) to 0.05. \( \alpha \) was typically 0.7 to 0.8. So, to a good approximation we can set the middle term to zero.

Rearranging Eq. (A13) and eliminating terms in \( (\sigma_D^D/\sigma_\Sigma^\Sigma) \) by use of Eqs. (A3) and (A6) we obtain a usable expression for the Absolute Cross Section, namely,

\[
\sigma(0) = \left[ \frac{1}{2}(1-\alpha) \right] \left( S'_1/S_2 \right) \left( R_2 T_2/R_1 T_1 \right) \left[ (S'_1 - S_1')/S_2 \right] \sigma_\Sigma. \tag{A14}
\]

The relative cross section can be obtained from Eq. (A14) by noting that \( (S_2/\sigma_\Sigma) \) is proportional to the absolute intensity \( I_0 \) of the incident radiation, see Eq. (A3). Further, from the definition of the photon detector efficiency \( \eta \), namely,

\[
\eta = \left( \frac{i_{ph}}{e} \right)/I_0 \tag{A15}
\]

where \( i_{ph} \) is the detector signal in amperes and \( e \) is the electronic charge, we see that

\[
I_0 \propto i_{ph}/\eta. \tag{A16}
\]
Substituting into Eq. (A14) we obtain the Relative Cross Section, namely,

\[ \sigma(0) \approx (n/\text{i}_{\text{ph}})(S'_1 - \alpha S_1) \]  \hspace{1cm} (A17)

Only the relative value of the detector efficiency \( n_r \) is required in Eq. (A17) and this can be found as a function of wavelength in a separate and independent experiment. When neon gas is used in the mass spectrometer we obtain the relation,

\[ \text{i}_{\text{ph}}/n_r \propto I_0 \propto S(\text{Ne}^+)/\sigma(\text{Ne}) \]  \hspace{1cm} (A18)

where \( \sigma(\text{Ne}) \) is the known cross section of Ne and \( S(\text{Ne}^+) \) is the output signal of the electron multiplier that measures the Ne\(^+\) ion current.\(^{29}\) The value of \( \alpha \) can be found in terms of measurable quantities by use of Eqs. (A3) and (A5) and from the definitions of \( \alpha \) and \( \beta \). Solving for \( S'_2/S_2 \) we obtain,

\[ S'_2/S_2 = \alpha[1 + \beta(\sigma_{\Delta} - \sigma_{\Sigma}/\sigma_{\Sigma})] \]  \hspace{1cm} (A19)

The quantity \( \beta \) is the fraction of the molecules that are in the excited \( ^1\Delta \) state. Typically, \( \beta \) lies between 0.01 and 0.1.\(^{23-25}\) Further, the cross section of most diatomic molecules in the ionization continuum are similar, with the fractional differences varying between zero and \( \pm 30\% \) between 120 and 700\(\text{Å} \). For the iso-electronic molecules CO and N\(_2\) the variation lies between 0 and 16\%.\(^{31}\) Thus, we would not expect the cross sections of such similar molecules as \( \text{O}_2(3\Sigma) \) and \( \text{O}_2(1\Delta) \) to show a larger deviation. Consequently, we take

\[ \alpha = S'_2/S_2 \]  \hspace{1cm} (A20)

This should introduce less than 1\% error in \( \alpha \). However, this assumption is not valid where autoionizing structure is present.